

25 CHOOSING SEARCH HEURISTICS BY NON-STATIONARY REINFORCEMENT LEARNING

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Abstract: Search decisions are often made using heuristic methods because real-world applications can rarely be tackled without any heuristics. In many cases, multiple heuristics can potentially be chosen, and it is not clear a priori which would perform best. In this article, we propose a procedure that learns, during the search process, how to select promising heuristics. The learning is based on weight adaptation and can even switch between different heuristics during search. Different variants of the approach are evaluated within a constraint-programming environment.

Keywords: Non-stationary reinforcement learning, Optimization, Local search, Constraint programming.

25.1 INTRODUCTION

All kinds of search techniques include choice points at which decisions must be made between various alternatives. For example, in refinement search, an extension step from a variables' partial assignment toward a complete assignment must be chosen. In local search methods, it must be decided how a complete but suboptimal/infeasible assignment is to be changed toward an optimal/feasible assignment.

However, for large and complex real-world problems, decisions can rarely be made in an optimal way. Especially for local search techniques, this is a very critical issue because they do not normally incorporate backtracking

mechanisms. Many different metaheuristic techniques have therefore been developed to handle the complications involved when choosing a decision alternative.

Figure 25.1 shows a choice point, representing the current state (i.e., the current variable assignment) of local search, and multiple decision alternatives, representing the so-called *neighbor states* that can be reached within an iteration.

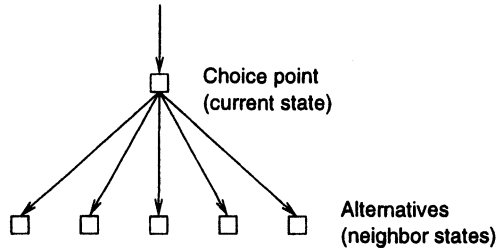


Figure 25.1 A decision point in local search.

Nearly all local search methods evaluate all neighbor states in a kind of look-ahead step to choose the most beneficial alternative. However, complex real-world problems – such as action planning including time, resources and optimization – often have utility functions whose computation requires a great deal of computing power. Analyzing large neighborhoods is mostly out of the question, and even smaller neighborhoods are difficult to check. Techniques like simulated annealing (Kirkpatrick et al., 1983) are highly suitable for these tasks because *only one neighbor is analyzed* for a choice decision (though more neighbors may be analyzed if the current neighbor appears to be unsuitable).

For the purposes of this paper, we go one step further, not analyzing any neighbor, but choosing a neighbor according to learned utility values. In addition, we do not choose a specific neighbor state but a *transformation heuristic* that will be applied to create the new state. Unlike other reinforcement learning approaches for learning which heuristics perform well, our approach allows the search to switch between different heuristics during search to adapt to specific regions of the search space.

Section 25.2 introduces the constraint-programming environment that is applied in our experiments, and details the use of heuristics. Weights and their adaptation are presented in Section 25.3. The scheme is evaluated in Section 25.4. Conclusions and related work are discussed in Section 25.5.

25.2 SEARCH DECISIONS

As an example of local search, we give a brief description of the search method applied in the **DragonBreath** engine. The underlying paradigm is presented in detail in Nareyek (2001b).

The problem is specified as a so-called constraint satisfaction problem (CSP). A CSP consists of

- a set of variables $x = \{x_1, \dots, x_n\}$
- where each variable is associated with a domain d_1, \dots, d_n
- and a set of constraints $c = \{c_1, \dots, c_m\}$ over these variables.

The domains can be symbols as well as numbers, continuous or discrete (e.g., “door”, “13”, “6.5”). Constraints are relations between variables (e.g., “ x_a is a friend of x_b ”, “ $x_a < x_b \times x_c$ ”) that restrict the possible value assignments. Constraint satisfaction is the search for a variable assignment that satisfies the given constraints. Constraint optimization requires an additional function that assigns a quality value to a solution and tries to find a solution that maximizes this value.

In our local search approach, a specific cost function is specified for every constraint (so-called *global constraints*), which returns a value that represents the constraint’s current inconsistency/optimality with respect to the connected variables. For example, a simple Sum constraint with two variables a and b to be added and an s variable for the sum could specify its costs as $\text{Sum}_{\text{costs}} = |a + b - s|$. The total costs o_{now} of a current variable assignment (which is often also called *objective function value*) is a function of all constraints’ costs, e.g., a simple addition.

In addition, a constraint has a number of heuristics to improve its cost function. For example, a heuristic for the Sum constraint could randomly choose one of the related variables and change it such that there are no more costs. Another heuristic might resolve the inconsistency by distributing the necessary change such that all variables are changed by the same (minimal) amount. The constraint must make the choice as to which heuristic to apply on its own.

On top of all constraints is a *global search control* which selects, in each iteration of local search, one of the constraints which is to perform a change, i.e., the transition to a neighbor state. Figure 25.2 shows the control flow.

The global search control possesses qualitative and quantitative information from the constraints’ cost functions to decide which constraint to choose (e.g., the constraint with the maximal costs), but a constraint itself has little guidance as to which of its heuristics to choose. This choice point — for choosing one of the constraint’s heuristics — is investigated below.

25.3 UTILITY WEIGHT

For a choice point, a *utility value* $\omega_a \geq 1$ is computed/maintained for every alternative a (an *alternative* stands for a *heuristic* here) that expresses the expected benefit of choosing this alternative.

The utility values are subject to learning schemes, which change the values based on past experiences with choosing this alternative. In many cases, an appropriate balance of the utility values will depend on the area of the search space that the search is currently in. We will therefore focus on schemes that dynamically adapt the weights *during* search and not only after a complete run.

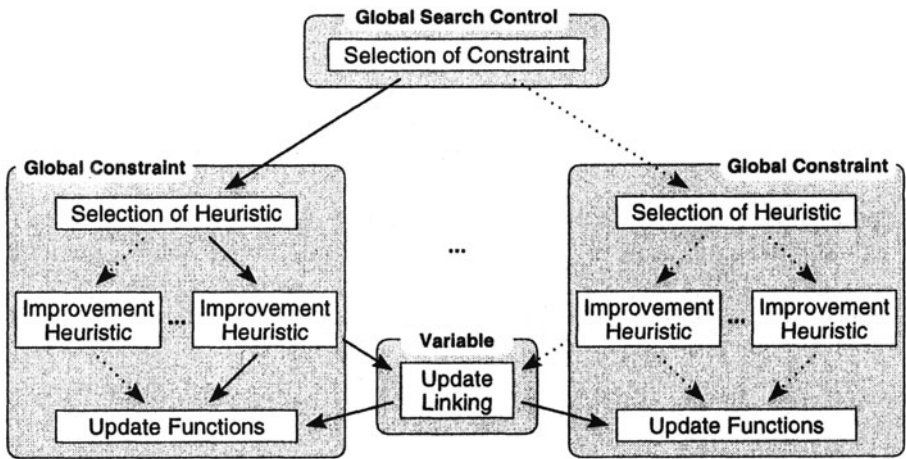


Figure 25.2 Using global constraints for local search.

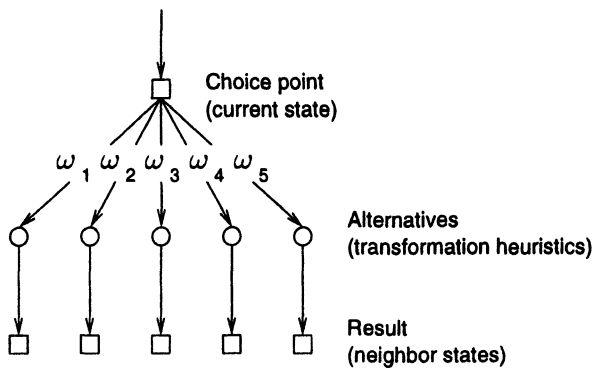


Figure 25.3 A decision point in our approach.

25.3.1 Selection function

Selection between possible alternatives is done based on the alternative's utility values. Here, we look at two simple ones. The first is a *fair random choice* (often called a *softmax* kind of selection rule), referred to below as M:0, which selects an alternative a from the choice point's alternatives \mathcal{A} with a choice probability p_a in proportion to the alternative's utility value ω_a :

$$\text{M:0} : p_a = \frac{\omega_a}{\sum_{i \in \mathcal{A}} \omega_i}$$

Another possibility is to make a random choice between the alternatives with *maximal* utility values:

$$\text{M:1} : p_a = \frac{\begin{cases} 0 & : \exists i \in \mathcal{A} : \omega_a < \omega_i \\ 1 & : \forall i \in \mathcal{A} : \omega_a \geq \omega_i \end{cases}}{\sum_{i \in \mathcal{A} \mid \forall j \in \mathcal{A} : \omega_i \geq \omega_j} 1}$$

25.3.2 Weight adaptation

All utility weights have integer domains and are initially set to 1. If the choice point is selected, the utility weight of the alternative is changed that was chosen by the choice point when it was called last time. The kind of change depends on the relation of the current cost function value o_{now} to the cost function value when the choice point was called last time o_{before} (i.e., if there is a positive or negative reinforcement). The update schemes below can be combined to give many different strategies, e.g., a simple P:1-N:1 strategy.

o_{now} better-than o_{before} :
(positive reinforcement)

P:1 (Additive adaptation): $\omega_a \leftarrow \omega_a + 1$

P:2 (Escalating additive adaptation): $\omega_a \leftarrow \omega_a + m_{promotion}$

P:3 (Multiplicative adaptation): $\omega_a \leftarrow \omega_a \times 2$

P:4 (Escalating multiplicative adaptation): $\omega_a \leftarrow \omega_a \times m_{promotion}$

P:5 (Power adaptation): $\omega_a \leftarrow \begin{cases} \omega_a \times \omega_a & : \omega_a > 1 \\ 2 & : \omega_a = 1 \end{cases}$

o_{now} worse-than-or-equal-to o_{before} :
(negative reinforcement)

N:1 (Subtractive adaptation): $\omega_a \leftarrow \omega_a - 1$

N:2 (Escalating subtractive adaptation): $\omega_a \leftarrow \omega_a - m_{demotion}$

N:3 (Divisional adaptation): $\omega_a \leftarrow \frac{\omega_a}{2}$

N: 4 (Escalating divisional adaptation): $\omega_a \leftarrow \frac{\omega_a}{m_{demotion}}$

N: 5 (Root adaptation): $\omega_a \leftarrow \sqrt{\omega_a}$

If a utility value falls below 1, it is reset to 1; if a utility value exceeds a certain max_ω , it is reset to max_ω ; if a utility value is assigned a non-integer value, it is rounded down. In the case of an escalating adaptation, each time there is a consecutive improvement/deterioration, the $m_{promotion}/m_{demotion}$ value is doubled. Otherwise, it is reset to 1 (for P: 2 and N: 2) or 2 (for P: 4 and N: 4).

25.3.3 A weight-adaptation example

For the illustration of the weight-adaptation mechanism, we follow the development of the weights of a choice point's six heuristics below. The heuristics A to F change the values of the problem definition's variables in different ways, e.g., by additions and subtractions. The chosen weight-adaptation strategy is P: 1-N: 2 with a fair random choice M: 0. The current search situation is to be

ω_A	ω_B	ω_C	ω_D	ω_E	ω_F	last choice: E	$O_{before} = 20$
1	2	1	3	3	1	$m_{demotion} = 1$	$O_{now} = 12$

and one of the heuristics is to be selected for execution.

Entering this choice point, the heuristics' weights will be updated at first. The cost function value is now better (assuming that we want to minimize here) than the last time this decision had to be made, and the last choice was heuristic E. According to strategy P: 1, the weight of heuristic E is rewarded by increasing it by one.

Next, a heuristic is to be selected for execution. The choice probability for the E option is the highest (weight value divided by the sum of all weight values; $4/12 = 33\%$), and we assume that this alternative is chosen by strategy M: 0. Heuristic E is executed.

Other changes may follow, and after some iterations, our choice point might be called again. The situation is now:

ω_A	ω_B	ω_C	ω_D	ω_E	ω_F	last choice: E	$O_{before} = 12$
1	2	1	3	4	1	$m_{demotion} = 1$	$O_{now} = 17$

The cost function value has deteriorated since the last time the choice point was entered, and — according to strategy N: 2 — the last decision's weight value ω_E is decreased by the $m_{demotion}$ value of 1. The choice probability for

heuristic E is now about 27% (3/11) and we assume that this alternative is chosen again.

After some time, our choice point is called once more:

ω_A	ω_B	ω_C	ω_D	ω_E	ω_F	last choice: E	$O_{before} = 17$
1	2	1	3	3	1	$m_{demotion} = 1$	$O_{now} = 17$

The cost function value is the same as at the last call. Stagnation is considered to be as bad as deterioration, and because this is a consecutive deterioration, the $m_{demotion}$ value is doubled. Heuristic E's weight value is therefore decreased by 2. We assume that heuristic D is chosen this time (probability of $3/9 = 33\%$) for execution.

At the next call of the choice point, the situation is:

ω_A	ω_B	ω_C	ω_D	ω_E	ω_F	last choice: D	$O_{before} = 17$
1	2	1	3	1	1	$m_{demotion} = 2$	$O_{now} = 16$

The cost function value has improved, and so, the weight value of heuristic D is increased by one, and the $m_{demotion}$ value is set back to 1.

25.3.4 Invalid alternatives

For some choice points, more than one alternative must be tested. For example, an alternative may turn out to be infeasible (i.e., the corresponding transformation is not applicable). An *applicability flag* f with a value of 0 or 1 is introduced for every alternative, indicating whether the alternative is still a valid option:

$$\omega_a \leftarrow f_a \times \omega_a$$

By the option of setting an applicability flag to 0, alternatives can often be ruled out a priori by simple feasibility tests.

However, in some cases, the infeasibility of an alternative will only become apparent during the state-transformation process of the chosen heuristic, i.e., after the choice has been made. In such a case, all changes in the current state that were made after the choice point are reversed, the corresponding applicability flag is set to 0 and the choice process is repeated. If no alternative remains applicable, the choice point's improvement fails.

If the choice point's selection is subject to the learning scheme, applicability flags are not set to 0 if an alternative fails. The failure may be caused by a bad random decision during the alternative's computations and the alternative may not be *fully* inapplicable. The learning process can handle this situation more appropriately than in a non-learning case, skipping the usual update of the utility weights and *temporarily* dividing the failed alternative's utility weight by two (though no weight may fall below one). If one of the alternatives has been successfully applied, all adaptations of the utility weights that were done for the restarts are undone.

25.4 EMPIRICAL EVALUATION

Two optimization problems — the Orc Quest problem and a modification of the Logistics Domain — are evaluated with different learning/selection schemes. The problems are only roughly described here because the actual problems are not important with respect to our following analysis. A detailed presentation of the problems can be found in Nareyek (2001a).

The Orc Quest problem's solving process involves only three constraints with six heuristics each. Each of these heuristics applies a specific set of additions and subtractions to the problem variables. There is a hierarchical cost function, demanding the minimization/maximization of specific problem variables. The learning scheme is applied to the choice points of all three constraints.

The Logistics Domain is a classical benchmark in the action-planning community. The problem investigated here is enriched so that actions have durations (more specifically, the duration minimization of Problem 6-1a is analyzed). The problem involves a large number of constraints, which are even created and deleted during the solving process. The learning scheme is applied to all constraints of the STATE RESOURCE type. This constraint type is responsible for projecting a specific state of the environment and has to ensure that all related preconditions of actions are fulfilled. Such a constraint can for example be responsible for the location of a truck, and must ensure that the truck is at the right location when a loading action is to take place. The constraint type includes five alternative heuristics, e.g., to create a new action, to temporally shift an action, and to delete an action.

25.4.1 Results

A strategy is denoted by P-N-M, $P \in \{1..5\}$ indicating the adaptation scheme that is applied in the case of an improvement, $N \in \{1..5\}$ the adaptation scheme for non-improvement, and $M \in \{0, 1\}$ if the fair random choice is applied or a maximal value is chosen.

The results for some strategies for the Orc Quest problem are shown in Figure 25.4 as the percentage of test runs (100 % = 100,000 test runs) that found the optimal solution after a specific number of iterations¹. For example, in case of strategy 1-5-1, about 98 % of the test runs found the optimal solution after 2,000 iterations while 2 % were still running. The strategies' curves are overlapping in some cases, which means that for these strategies, the strategy dominance is dependent on available computation time.

The problem from the Logistics Domain is much harder, so only the best solution (minimal duration) found after 100,000 iterations is shown in Figure 25.5 (100 % test runs = 1,000 test runs).

¹While presenting results as so-called *run-time distributions* is not widespread in the Operations Research community, it addresses a number of serious issues related to result presentation and analysis (see Hoos and Stützle (1998)).

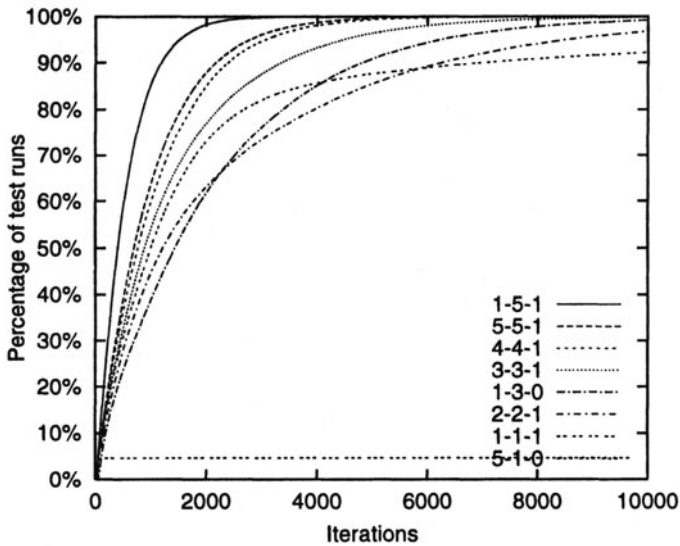


Figure 25.4 Sample strategies for the Orc Quest problem.

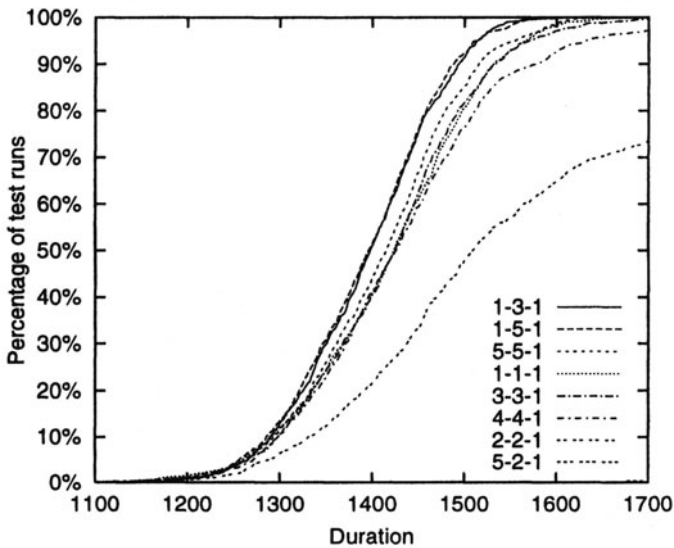


Figure 25.5 Sample strategies for the Logistics Domain.

The following figures will display more detailed results, i.e., for all possible strategy mixes. The amount of data to be shown does however not allow for a complete picture like in the graphs above. Only for specific percentages of test runs, it is shown after how many iterations this percentage of test runs found the optimum (for the Orc Quest problem — Figure 25.6), and the lowest duration that was found by this percentage of test runs after 100,000 iterations (for the Logistics Domain — Figure 25.7). This corresponds to vertical slices of the previous figures. The strategies are sorted according to which strategy resulted in the least iterations/duration for a maximal percentage of test runs (not considering the 100 % rate).

The general trend is that a low (e.g., additive/ $P:1$) rate of adaptation is good in the case of an improvement, a strong (e.g., root/ $N:5$) rate of adaptation is good in the case of deterioration, and a choice of a maximal weight is often better than a fair random choice. The explorative feature of the fair random choice may not be that important because there are very often cases of negative reinforcement that quickly change the weight situation.

Because the Orc Quest problem involves only three constraints, we can easily visualize some further properties of the search process. Figure 25.8 shows how many times a constraint's highest weight changes, i.e., how many times a weight is assigned a value above a certain percentage of the total values of the choice point's weights, and the last time this percentage threshold was reached, it was reached by another weight. Strategies that perform many changes in the configuration appear to perform better. This might be an indication of why strategies with a low rate of adaptation in the case of an improvement and a strong rate of adaptation in the case of a deterioration are likely to perform better — such strategies facilitate a reconfiguration of the weight situation.

An exception here are strategies with a very low positive reaction ($P:1$). Because of the slow growth of the weights, a smaller number of clear reconfigurations are performed. However, this simmering situation would appear to have its advantages as well.

Figure 25.9 shows how many times the highest weight is re-established, i.e., how many times a weight is assigned a value above a certain percentage of the total values of the choice point's weights, and the last time this percentage was reached, it was reached by the *same* weight. In general, one would expect strategies that re-establish old configurations to do needless work and thus, possibly perform worse. However, the figures do not show many differences here. The reason for this is probably that the better strategies perform many configuration changes in general, and, are thus also more likely to re-establish configurations more often. Even though the absolute numbers of re-established configurations are similar for all strategies, the better strategies have a much lower ratio of re-established configurations to all reconfigurations.

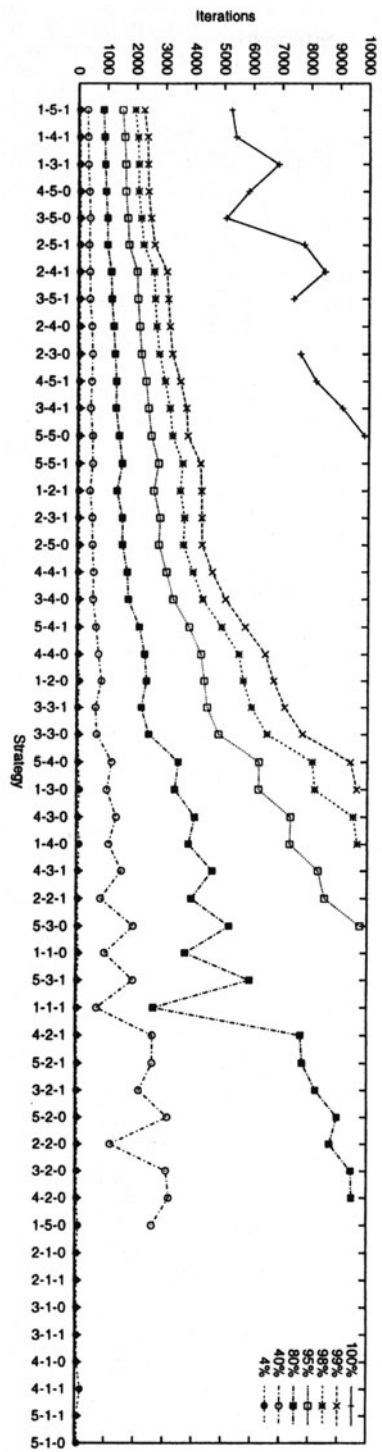


Figure 25.6 Weight-adaptation results for the Orc Quest problem.

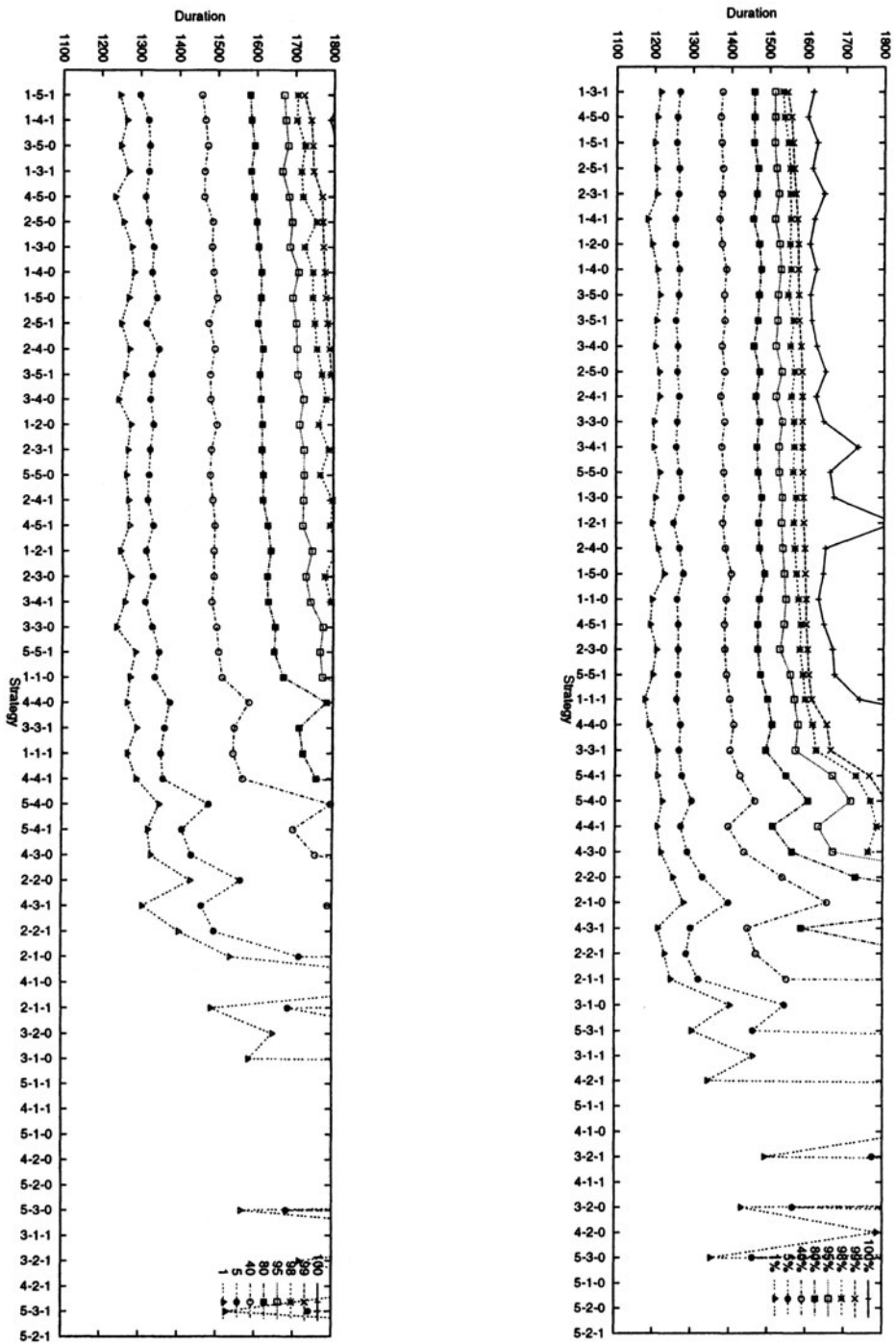


Figure 25.7 Weight-adaptation results for the Logistics Domain after 25,000 (left) and 100,000 (right) iterations.

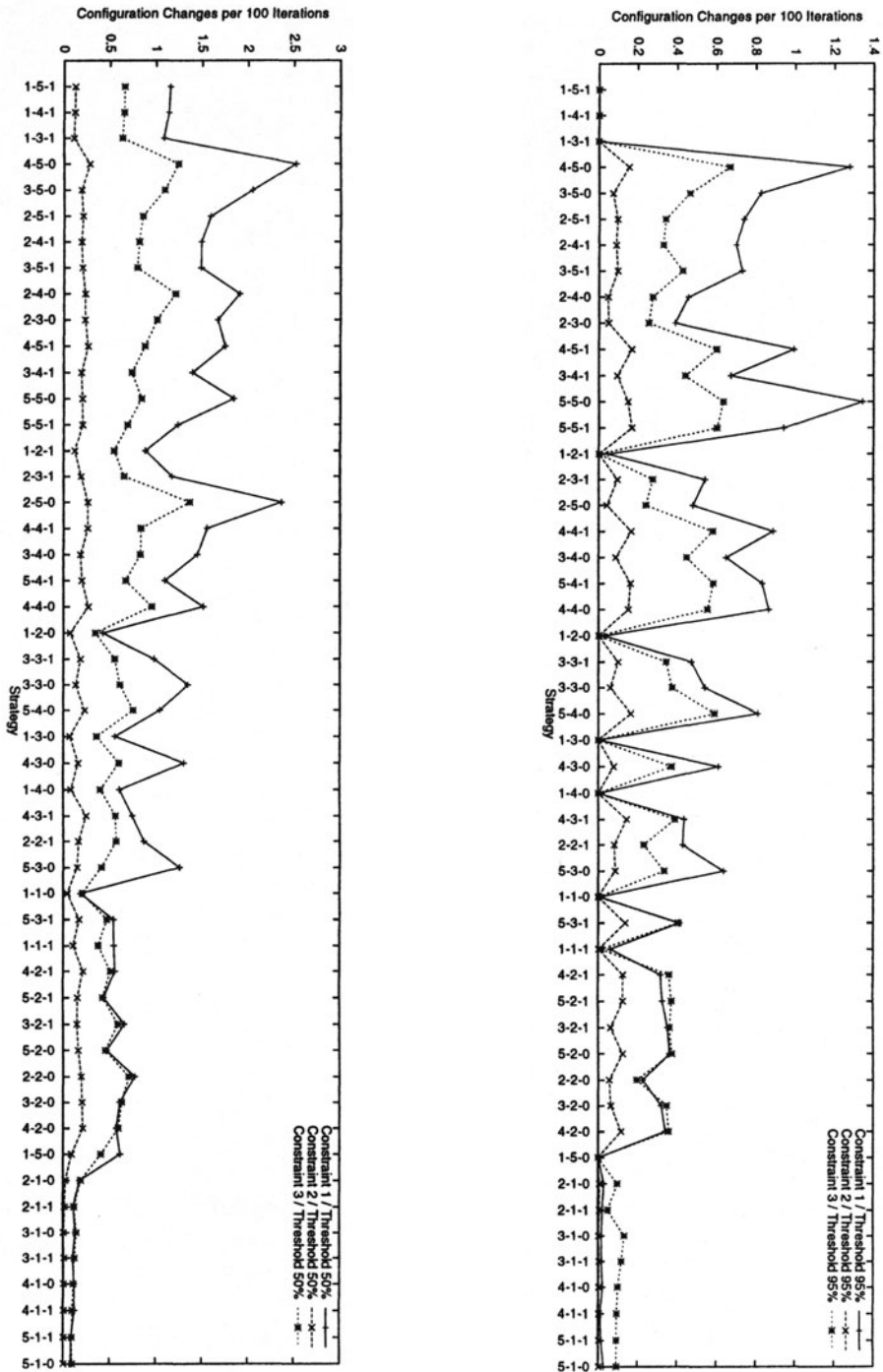


Figure 25.8 Number of configuration changes for the Orc Quest problem.

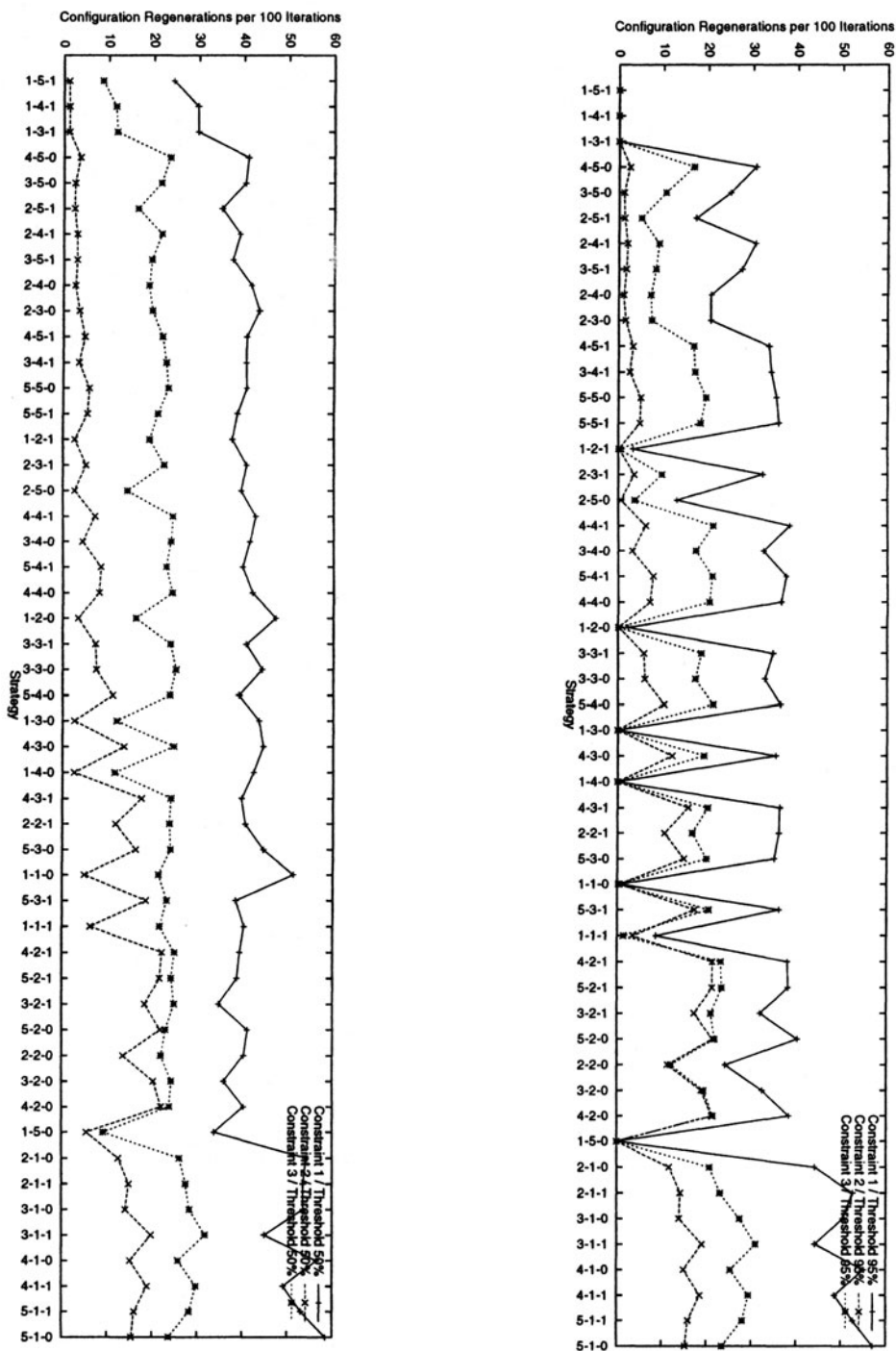


Figure 25.9 Number of configuration regenerations for the Orc Quest problem.

25.4.2 Extended experiments

Following the observed trend, we can extend our experiments by more extreme options in this direction:

P: 0 (No adaptation): $\omega_a \leftarrow \omega_a$

To enable weight increases for this option at all, in the case of a negative change, the decrease of ω_a is distributed as an increase to all $\omega_{i \neq a}$ (starting with high initial weights).

N: 6 (Total loss adaptation): $\omega_a \leftarrow 1$

Figure 25.10 shows that these options do not improve performance for the Orc Quest problem. However, as shown in Figure 25.11, strategies with an N: 6 option appear to work well for the early phase of search, i.e., for less constrained problems.

25.4.3 Stationary reinforcement learning

So far, we have looked at different methods to adapt the weights during search, assuming that different areas of the search space can be handled more efficiently using different search strategies. Although this assumption seems to be intuitively correct, it remains to be shown to be true. This section, then, compares adaptive non-stationary learning with stationary approaches.

Previous approaches adapted learning parameters *after a complete run* or *when a local minimum was reached*. Of these two options, only an adaptation after a complete run (with an upper bound of a specific number of iterations) is applicable here because we do not evaluate the whole neighborhood and cannot therefore tell if we are in a local minimum. The time taken by the learning process to find an optimal stationary weight distribution is not measured because the results may be very different for different learning techniques. Thus, the adaptive learning strategies are compared with the optimal stationary distribution.

For the Orc Quest problem, we can actually find an optimal static weight distribution such that all test runs find the optimum in about 35 iterations. With the most simple, non-stationary 1-1-0 strategy, 50% of the test runs found the optimum after 1,305 iterations, and after 405 iterations for strategy 1-5-1. Thus, an adaptive strategy would seem to perform very poorly for the simple Orc Quest problem. This is not completely true, however, given the time that would be required to learn the optimal stationary distribution. For example, using a simple static distribution such that every heuristic is chosen equally often, none of the 100,000 test runs found the optimum within 100,000 iterations. We conclude that, if the problem (or very "similar" problems) is solved very often, a stationary reinforcement learning approach will ultimately perform much better; but for a short time-frame, the non-stationary approach is probably much superior.

For the more complex Logistics Domain, our findings are different. The performance of even the most simple, non-stationary 1-1-0 strategy is sim-

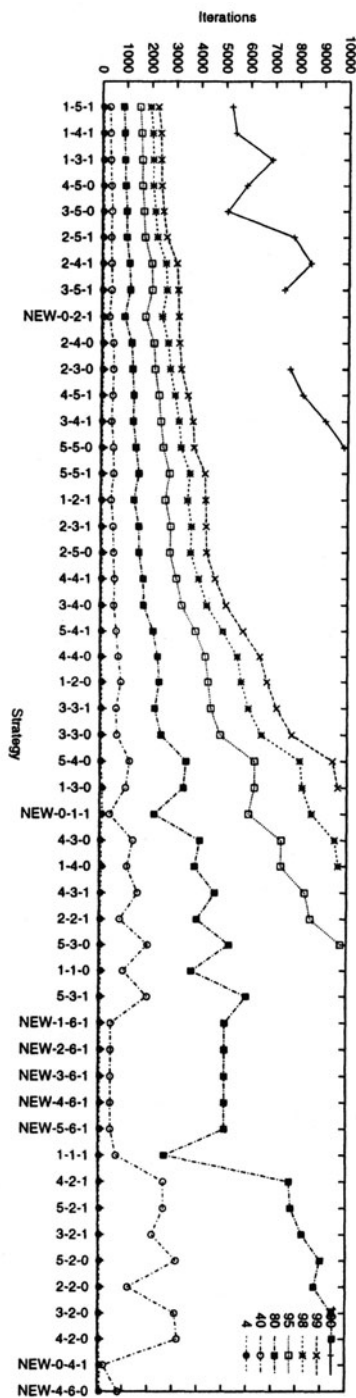


Figure 25.10 Extended weight-adaptation results for the Orc Quest problem; showing only the 50 best strategies.

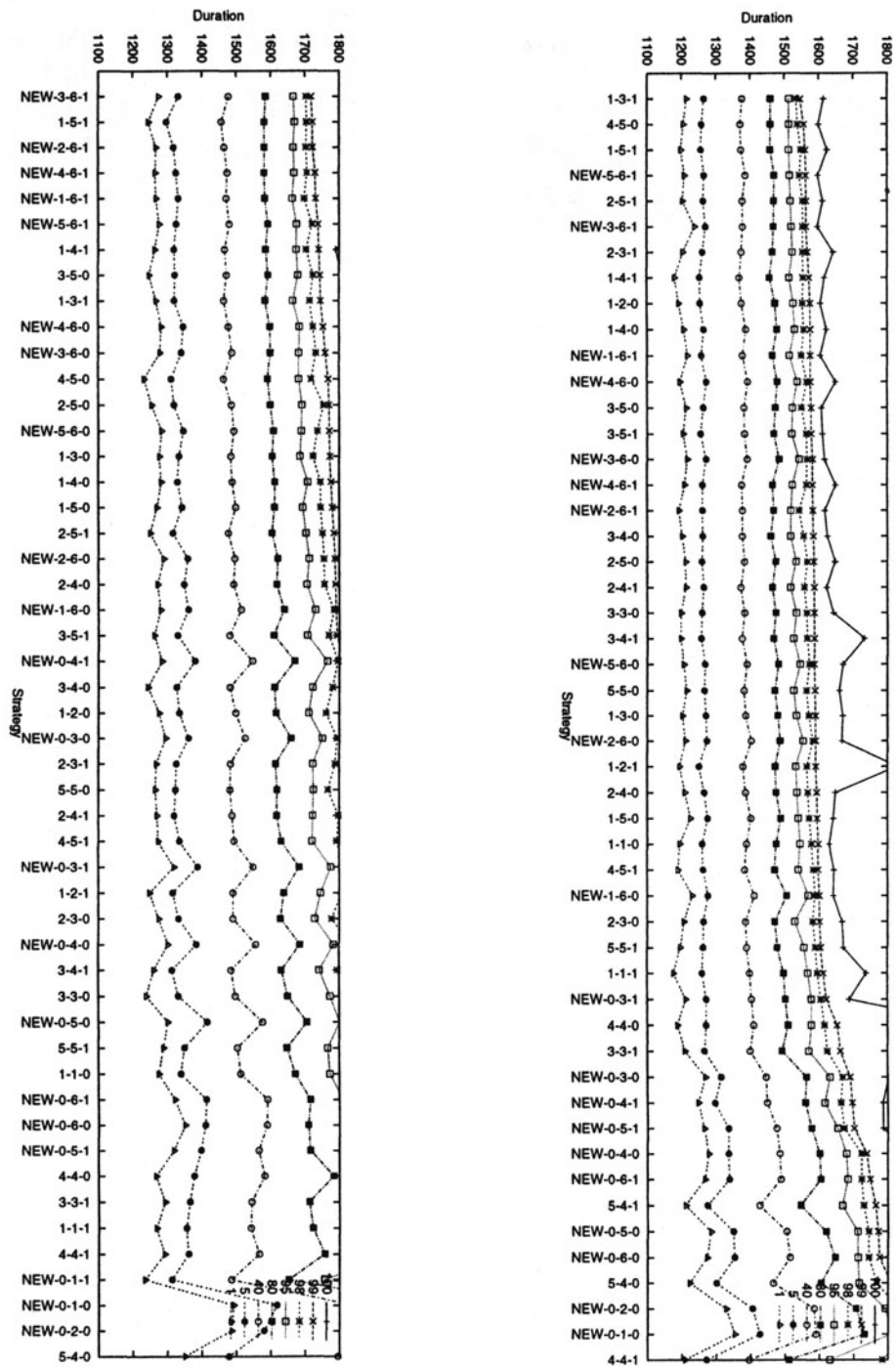


Figure 25.11 Extended weight-adaptation results for the Logistics Domain after 25,000 (left) and 100,000 (right) iterations; showing only the 50 best strategies.

ilar to that of a carefully hand-tailored static weight distribution, i.e., a static distribution does not work well even disregarding the learning time for it (see Figure 25.12). Our assumption that it is useful to switch between different heuristics during search to adapt to specific regions of the search space proves valid for this more complicated problem.

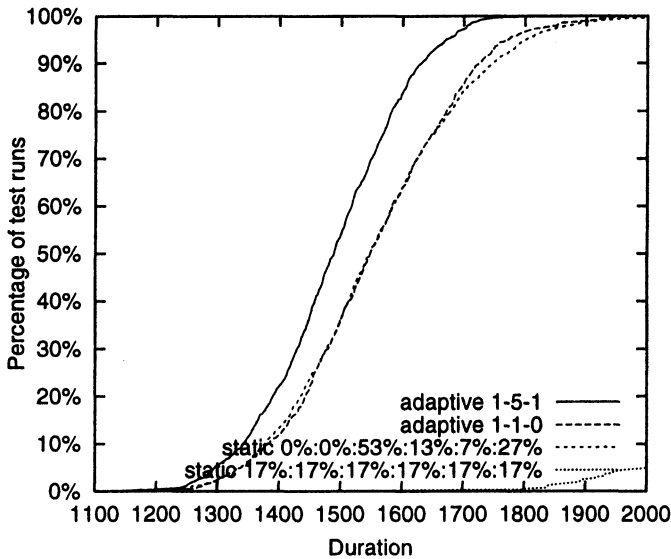


Figure 25.12 Adaptive vs. static strategies for the Logistics Domain (after 25,000 iterations), disregarding the learning time for the static distribution.

25.5 CONCLUSION

The use of a neighborhood of repair heuristics is a promising way to implement a local search — especially for complex real-world problems in which the computation of a state's cost function value is often very costly. Using the repair heuristics, domain-dependent knowledge to guide the search can easily be incorporated into the search process. The approach used here is based on Nareyek (2001b). Similar techniques were applied in Rabideau et al. (1999); Smith (1994); Zweben et al. (1994).

However, finding an appropriate strategy that guides when to apply which heuristics is not easy. This article has presented a promising approach to learn a selection strategy by modifying weights. Other approaches that make use of weights for re-structuring the neighborhood include Boyan and Moore (1997), Schuurmans and Southey (2000), and Voudouris and Tsang (1995). Unlike these approaches, we do not only change the weights when a local optimum or solution is reached. Search usually undergoes different phases (i.e., search-space regions) in which different search heuristics work best. Thus, even during search, the heuristics' configuration is constantly updated. For this pur-

pose, a less-carrot-more-stick strategy seems to be most adequate, allowing for quick configuration changes and preventing the old configuration from being re-established too quickly.

WGSAT (Frank, 1997) follows a similar strategy, even though weights are connected to problem features (i.e., SAT clauses) instead of improvement heuristics. The approach is not really comparable, but it is close to a $P:0-N:1$ strategy with an additional decay factor.

In reinforcement learning, non-stationary environments (such as the search-space region) are only rarely considered. Examples include approaches based on supervised techniques (Schmidhuber, 1990), evolutionary learning (Littman and Ackley, 1991) and model-based learning (Michaud and Matarić, 1998). Unlike these approaches, we have used a modification of standard action-value methods (Sutton and Barto, 1998), applying functional updates instead of cumulative value additions in order to influence the impact of the already learned reinforcements. This simple method enables the search to compute weight updates very quickly – which is very important for a local search environment because a single iteration should consume only very little computing power.

Adaptive weights are not restricted to local search; they can also be used for (esp. restart-based) refinement search. Examples include the pheromone trails in ant colony optimization (Dorigo et al., 1999), the use of domain-specific prioritizers (Joslin and Clements, 1999) and action costs in adaptive probing (Ruml, 2001). The results obtained in this study may be transferred to these areas, and techniques like pheromone evaporation are worth studying for neighborhoods of heuristics as well.

So far, we have not considered quantitative cost-function effects of decisions. Improvement or non-improvement was the only criterion for learning. However, “good” heuristics may not be equally good on the quantitative level and incorporating mechanisms to exploit the quantitative differences is a promising idea for future work. An interesting approach in this direction was presented at this conference by Cowling et al. (2001).

The presented techniques are integrated into the **DragonBreath**² engine, which is a free optimization engine based on constraint programming and local search. It can be obtained via:

Acknowledgments

Thanks to Michael Littman for his feedback.

²Can be obtained at <http://www.ai-center.com/projects/dragonbreath/>.

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