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93103



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SCHOLARSHIP EXEMPLAR



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Tick this box if you
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Scholarship 2021 Physics

Time allowed: Three hours
Total score: 32

Check that the National Student Number (NSN) on your admission slip is the same as the number at the top of this page.

You should answer ALL the questions in this booklet.

For all ‘describe’ or ‘explain’ questions, the answers should be written or drawn clearly with all logic fully explained.

For all numerical answers, full working must be shown and the answer must be rounded to the correct number of significant figures and given with the correct SI unit.

Formulae you may find useful are given on page 3.

If you need more room for any answer, use the extra space provided at the back of this booklet.

Check that this booklet has pages 2–20 in the correct order and that none of these pages is blank.

YOU MUST HAND THIS BOOKLET TO THE SUPERVISOR AT THE END OF THE EXAMINATION.

Question	Score
ONE	
TWO	
THREE	
FOUR	
TOTAL	

ASSESSOR'S USE ONLY

QUESTION ONE: NEUTRONS

Planck's constant	$= 6.63 \times 10^{-34} \text{ J s}$
Neutron mass	$= 1.67 \times 10^{-27} \text{ kg}$
Charge of an electron	$= -1.60 \times 10^{-19} \text{ C}$
Acceleration due to gravity	$= 9.81 \text{ m s}^{-2}$

A research nuclear reactor is designed to produce a beam of neutrons. The neutrons are produced by the fission of uranium, with one of several possible reactions being described by the following equation:



The neutrons released in these reactions have a wide range of energies, but can be slowed down by passing them through material of similar nuclear mass, to form a beam of "slow neutrons".

- (a) Use the concept of binding energy to explain why fission reactions occur.

Binding energy is the energy required to separate the atom into its nucleons. The nucleons are held by strong force. However, the big atoms are less affected by this strong force and try to be stable by fission. As the fission results the atom into daughter atoms with stronger binding energy, the energy that was used to hold the atom together is released during fission. Therefore, the fission reactions occur with release of energy.

- (b) Particles such as neutrons also behave as if they have a wavelength, given by $\lambda = \frac{h}{p}$, where h is Planck's constant and p is the momentum of the particle.

Show that the wavelength of a slow neutron with a kinetic energy of 0.0400 eV is $1.43 \times 10^{-10} \text{ m}$.

$$p = mv, \quad E_k = \frac{1}{2}mv^2, \quad v = \sqrt{\frac{2E_k}{m}}$$

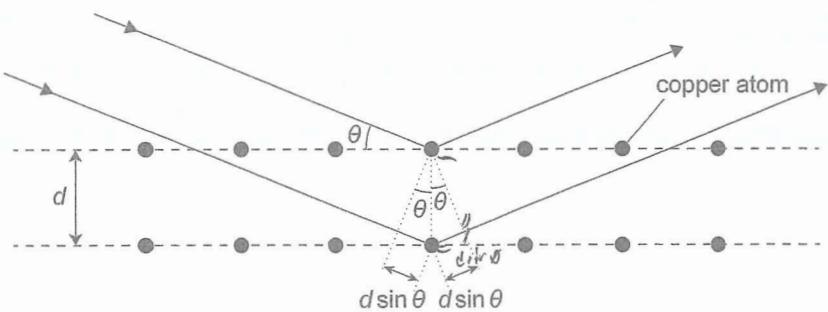
$$\therefore p = m \times \sqrt{\frac{2E_k}{m}} = \sqrt{2mE_k} \quad \text{as} \quad \frac{m}{m} = 1$$

$$\therefore \lambda = \frac{h}{\sqrt{2mE_k}}, \quad \lambda = \frac{6.63 \times 10^{-34}}{(2 \times 1.67 \times 10^{-27} \times 0.0400 \times 1.60 \times 10^{-19})^{\frac{1}{2}}}$$

$$= 1.43400 \times 10^{-10}$$

$$= 1.43 \times 10^{-10} \text{ (3sf) m}$$

- (c) Neutrons of energy 0.0400 eV can diffract from planes of atoms in crystalline copper, of spacing $d = 2.20 \times 10^{-10} \text{ m}$, as shown below.



By first considering the path difference for neutrons scattered from adjacent planes, show that a diffraction peak will be observed at angle $\theta = 19.0^\circ$.

the diffraction of neutrons will form the interference pattern and the peak will be observed when path difference between them is whole number or ~~half~~ number and a half.

$$\therefore \frac{\lambda}{2} = d \sin \theta, \quad \lambda = 1.47 \times 10^{-10} \text{ m}, \quad d = 2.20 \times 10^{-10} \text{ m}$$

$$\frac{\lambda}{2} = d \sin \theta, \quad \frac{1.47 \times 10^{-10}}{2.20 \times 10^{-10}} = \sin \theta$$

$$\sin \theta = 0.325$$

$$\theta = \sin^{-1}(0.325) = 18.965^\circ, \quad 19.0^\circ (\text{int})$$

- (d) Neutrons have mass, but zero charge. A neutron with kinetic energy of 0.0400 eV is initially travelling horizontally.

- (i) Calculate the vertical deflection of the neutron due to gravity as it travels a horizontal distance of $1.00 \times 10^2 \text{ m}$.

$$E_k = 0.0400 \times 1.60 \times 10^{-19} = 6.4 \times 10^{-21} \text{ J}, \quad E_k = \frac{1}{2}mv^2 = 6.4 \times 10^{-21}$$

$$100 / 2768.5 = 0.036 \text{ sec}, \quad V_f = V_i + at, \quad V_{f_{ver}} = 0.354 \text{ m/s} \quad v^2 = 7664670.67$$

$$v_f^2 = V_i^2 + 2ad, \quad 0.354^2 = 0 + 2(9.8)d, \quad d = 6.40 \times 10^{-3} \text{ m} \quad v = 7664670.67 \text{ m/s}$$

$$\tan \theta = \frac{6.40 \times 10^{-3}}{100}, \quad \theta = 3.666 \times 10^{-3}, \quad 3.67 \times 10^{-3}^\circ \text{ (if deflected degrees)}$$

- (ii) Explain whether or not a uniform electric field can be used to compensate for the effect of gravity on the neutron.

NO we can not use electric field. As neutron ~~is~~ does not have charge, it will not be affected by energy change due to travelling distance in field. Only proton and electron will have a change in energy and ~~be~~ are able to compensate the effect.

QUESTION TWO: STRINGS AND SPRINGS



A typical guitar has six strings. Two of these strings are tuned to the notes "A" and "D". When tuned correctly, the "A" string has a fundamental frequency of 110.0 Hz, and the 4th harmonic of the "A" string has the same frequency as the 3rd harmonic of the "D" string.

- (a) (i) Explain how the principle of beats can be used to determine if the "D" string is at the correct frequency, if it is known that the "A" string already has the correct fundamental frequency of 110.0 Hz.

The Beat is created when the sound waves that has slightly different frequency interfere each other, and creates repetition of beat variation of beaten. Therefore, if the frequency of D is slightly different, the beat will produced.

~~Thus, we can find correct frequency when the beat is not produced as the frequencies are identically 110.0 Hz.~~ (extra paper) (continued)

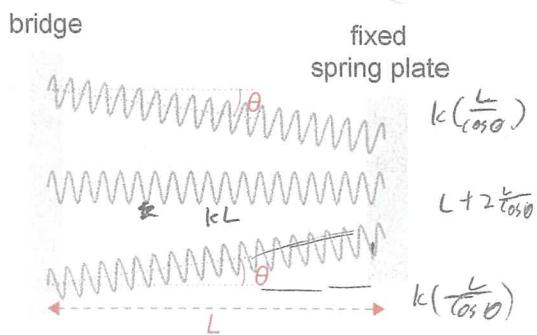
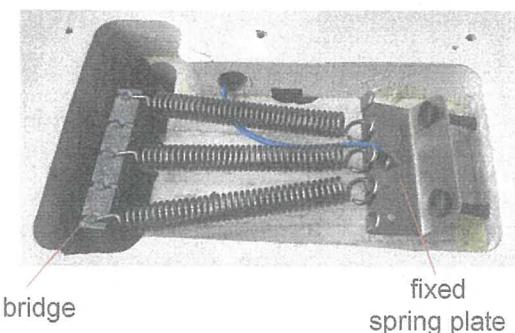
- (ii) Calculate the fundamental frequency of the "D" string when it is correctly tuned.

As the "D" is same frequency with 4th harmonic of "A" its frequency will be $4 \times 110.0 = 440.0 \text{ Hz}$.

The fundamental frequency of "D" will be $\frac{4}{3}$ of 3rd harmonic

$$\therefore \frac{440.0}{3} = 146.67 \text{ Hz}, 146.7 \text{ Hz (4st)}$$

Some guitars use a set of three identical springs to apply tension to the strings. The three springs all have spring constant, k , and an unstretched length, L_0 . They are then stretched and connected between the bottom side of a pivoted metal plate called the bridge and a fixed spring plate, as shown.



- (b) Show that the net force, F , applied to the bridge by the three stretched springs is given by:

$$F = k(3L - L_0(1 + 2 \cos \theta))$$

$$F = kx, \therefore F_{\text{total}} = k(3L - L_0) \quad (\text{for middle spring})$$

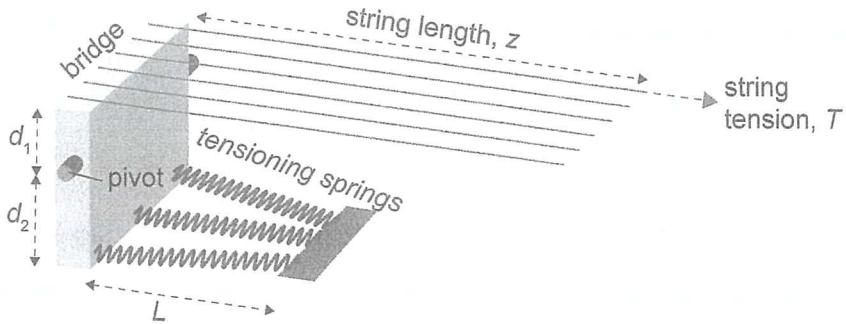
$$\text{for top spring, } x = \frac{L - L_0}{\cos \theta} \quad F_t = k\left(\frac{L}{\cos \theta} - L_0\right)$$

However, the pull's force from spring is horizontal component

$$\therefore F_{\text{horizontal}} = k\left(\frac{L}{\cos \theta} - L_0\right) \cos \theta = k(L - L_0 \cos \theta)$$

$$\therefore F_{\text{total}} = k(L - L_0) + 2k(L - L_0 \cos \theta) = k(L - L_0 + 2L - 2L_0 \cos \theta) \\ = k(3L - L_0(1 + 2 \cos \theta))$$

The bridge is where the strings connect to the body of the guitar. Some guitars have a “floating bridge” design, where the springs are attached to the bottom and the strings to the top of the pivoted bridge, as shown below.



The speed of a transverse wave in a string is given by: $v = \sqrt{\frac{T}{\mu}}$,

where T is the tension in the string, and μ is the linear density of the string.

- (c) Assuming that all strings have equal tension, T , and length, z , show that the fundamental frequency of a string is given by:

$$f_f = \sqrt{\frac{kd_2(3L - L_0(1 + 2\cos\theta))}{24\mu d_1 z^2}}$$

$$\frac{d_2}{d_1} \frac{d_2}{6c_1}$$

$$v = f\lambda, \quad f = \frac{v}{\lambda}, \quad \lambda = 2z, \quad \therefore f\lambda = \sqrt{\frac{T}{\mu}}$$

$$f = \frac{1}{2z} \times \sqrt{\frac{T}{\mu}} = \sqrt{\frac{T}{4z^2\mu}}$$

To fit the string sprbg $\frac{d_2}{d_1} \frac{d_1}{\mu}$ sprgs, the line will be equal in magnitude
 $\therefore T_{spr} d_2 = d_1 T_{str} \times 6$, $6T_{str} = \frac{d_2}{d_1} T_{spr}$. as $T_{spr} = k(3L - L_0(1 + 2\cos\theta))$

$$T_{str} = \frac{d_2}{6d_1} k(3L - L_0(1 + 2\cos\theta))$$

$$\therefore f = \sqrt{\frac{T_{str}}{4z^2\mu}} = \sqrt{\frac{\frac{d_2}{6d_1} k(3L - L_0(1 + 2\cos\theta))}{4z^2\mu}} = \sqrt{\frac{kd_2(3L - L_0(1 + 2\cos\theta))}{24z^2\mu d_1}}$$

//

- (d) If the “D” string on a guitar with a floating bridge screws, explain how the fundamental frequency of the “A” string will be affected, and state the new fundamental frequency of the “A” string.

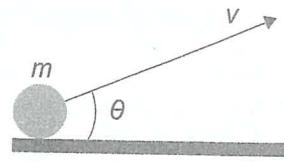
Assume that the string length, z , is constant.

As the D strg is screws, the bridge is oscillating with the frequency of 146.67 Hz If the “D” string is screws, the tension that is provided to the strg “A” will be increased as provided tension from sprng is constant and there are less number of strings. As the $v = \sqrt{\frac{T}{\mu}}$, the velocity of wave through strg A will be increased. Since $v = f\lambda$, the frequency of waves wave through strg A will also be increased. As there are now only 4 strgs, the tension will be increased by $\frac{5}{4}$ times.

QUESTION THREE: ABOUT A BALL

$$2\sin\theta\cos\theta = \sin 2\theta$$

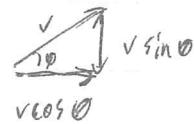
A ball with mass, m , is launched at a speed, v , at an angle, θ , to the horizontal, as shown. The projectile lands at the same height that it was launched from.



- (a) The horizontal distance travelled, d , is maximum when $\theta = 45^\circ$.

By considering components of the velocity, v , show that the maximum horizontal distance travelled, d , is given by: $d = \frac{v^2}{g}$.

Assume that drag is negligible for this part of the question.



$$\text{horizontal} \quad V_f = V_i + at, \quad V_i \sin \theta = -V_i \sin \theta + gt \quad t = \frac{2V_i \sin \theta}{g}$$

$$d = vt, \quad V_i = v \cos \theta$$

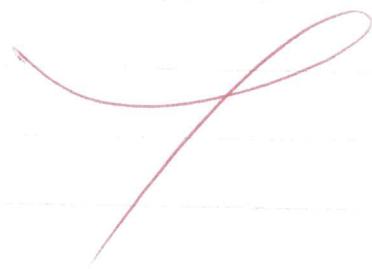
$$d = \frac{v \cos \theta (2V_i \sin \theta)}{g}$$

$$= \frac{2 \cos \theta \sin \theta v^2}{g}$$

$$= \frac{\sin 2\theta \cdot v^2}{g}$$

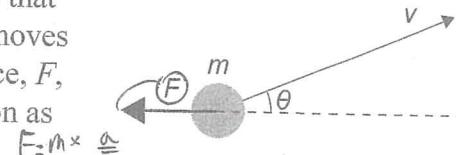
$$= \frac{v^2}{g}$$

$$= 1$$



$$\begin{aligned} 2\sin \theta \cos \theta &= \sin 2\theta, \\ \sin 2(45^\circ) &= 1 \end{aligned}$$

A more accurate model of the situation includes a drag force, F , that acts on the ball. This force changes the motion of the ball as it moves through the air. A simple assumption would be that the drag force, F , is constant in magnitude, and acts only in the horizontal direction as the ball moves through the air, as shown.



- (b) Show that in the case of a constant, horizontal drag force, F , the horizontal distance travelled, d , by a ball launched at speed, v , at an angle, θ , to the horizontal, is given by the expression:

$$d = \frac{v^2}{g} \left(\sin 2\theta - \frac{2F}{mg} \sin^2 \theta \right)$$

As F_{drag} is horizontal, the time will be constant, $t = \frac{2V_i \sin \theta}{g}$

$$\begin{aligned} V_f &= V_i + at, \quad V_f = 0, \quad V_i = v \cos \theta, \quad a \leftarrow F_{\text{drag}} = \frac{F}{m}, \quad a_{\text{drag}} = -\frac{F}{m}, \quad \text{negative as opposite direction} \\ 0 &= v \cos \theta - \frac{2F}{m} t \quad V_f = v \cos \theta - \frac{F}{m} \cdot \frac{2V_i \sin \theta}{g} = v \cos \theta - \frac{F}{m} \cdot \frac{2v \sin \theta}{g} \\ \frac{v \cos^2 \theta}{2F} m &= d \quad V_f^2 = V_i^2 + 2ad \quad \therefore d = \frac{2v^2 \sin \theta \cos \theta}{g} + \frac{v^2 \sin^2 \theta}{g} \\ \left(v \cos \theta + \frac{2F \sin \theta}{mg} \right)^2 &= v^2 \cos^2 \theta + \frac{2F}{m} d, \quad \therefore d = \frac{2v^2 \sin \theta \cos \theta}{g} + \frac{v^2 \sin^2 \theta}{g} \\ \frac{v^2 \cos^2 \theta}{m g^2} + \frac{4v^2 F^2 \sin^2 \theta}{m^2 g^2} - \frac{4vF \sin \theta \cos \theta}{mg} &= v^2 \cos^2 \theta + \frac{2F}{m} d, \quad \therefore d = \frac{2v^2 \sin \theta \cos \theta}{g} + \frac{v^2 \sin^2 \theta}{g} \\ \frac{4v^2 F^2 \sin^2 \theta}{m^2 g^2} + \frac{4vF \sin^2 \theta}{mg} &= \frac{2F}{m} d \end{aligned}$$

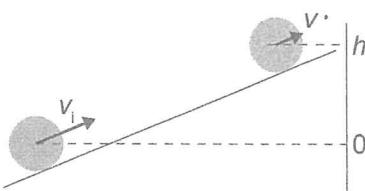
- (c) Discuss the validity of the assumptions about the drag force in part (b).

Describe more realistic assumptions about the drag force, and explain how these would affect the horizontal distance travelled by the ball.

The drag force also affects the vertical when the ball as the ball also has fall rising/falling motion. The drag force will be generated from air resistance between the ball and the ball. As the drag force acts in the opposite direction of applied force (acceleration), the ball will not have less time in the air due to decreasing of vertical acceleration from drag force. This causes the ball to travel shorter horizontal distance while it is in the air.

- (d) After receiving an initial push, the solid ball begins rolling up a slope, as shown on the right.

The ball has mass m , radius R , and moment of inertia $I = \frac{2}{5}mR^2$.



When it is at height = 0, the centre of mass of the ball has velocity v_i . When it has reached height = h , the centre of mass of the ball has velocity v .

- (i) Assuming that drag is negligible in this situation, show that the velocity of the centre of mass of the ball, v , when it has reached height, h , is given by:

$$\underline{\underline{m s^{-1}}} \quad 2\pi R v / v = T$$

$$v = \sqrt{v_i^2 - \frac{10gh}{7}}$$

$$E_{\text{kin, final}} + E_{\text{kin, rot}} + E_{\text{pot, gravitational potential energy}} = E_{\text{kin, initial}} + E_{\text{rot}}$$

$$\cancel{\frac{1}{2} I w^2} + \frac{1}{2} m v^2 + mgh = \frac{1}{2} m v_i^2 + \cancel{\frac{1}{2} I w^2}, \quad w = \frac{2\pi}{T}, \quad \text{as } \frac{v = m s^{-1}}{2\pi R / v} = \frac{1}{T} \text{ and } \cancel{w^2} = 2\pi v$$

$$\cancel{\frac{1}{2} I w^2} + mgh = \frac{1}{2} m v_i^2 + \cancel{\frac{1}{2} I w^2}, \quad \text{cancel } m$$

$$\frac{1}{2} v^2 + \frac{1}{2} v^2 + mgh = \frac{1}{2} v_i^2 + \frac{1}{2} I w^2$$

$$\frac{7}{10} v^2 + mgh = \frac{7}{10} v_i^2$$

$$\frac{7}{10} v^2 = \frac{7}{10} v_i^2 - mgh$$

$$v^2 = v_i^2 - \frac{10gh}{7}$$

$$\therefore v = \sqrt{v_i^2 - \frac{10gh}{7}}$$

- (ii) Give an expression for the maximum height reached by the ball as it rolls up the ramp.

when it is at maximum, $E_{\text{potential}} = \text{initial } E_k + \text{initial } E_{\text{rot}}$

$$mgh = \frac{1}{2} m v_i^2 + \cancel{\frac{1}{2} I w^2}$$

$$gh = \frac{7}{10} m v_i^2$$

$$h = \frac{7 m v_i^2}{10 g}$$

QUESTION FOUR: DC CIRCUITS

A parallel circuit is connected to a 1.10×10^2 V DC supply and a switch, as shown.

One branch of the circuit has a $22.4\ \Omega$ resistor, R_1 , and an uncharged capacitor, C , in series. The other branch has only a $27.5\ \Omega$ resistor, R_2 .

- (a) Sketch clearly labelled lines/curves on the axes on the right to show how the voltage across each component, R_1 , R_2 , and the capacitor, C , will change when the switch is closed at $t = 0$ s.

Explain why the voltage across each component changes in this way.

As the circuit is parallel, the voltage across three components will be same with 110V at $t = 0$.

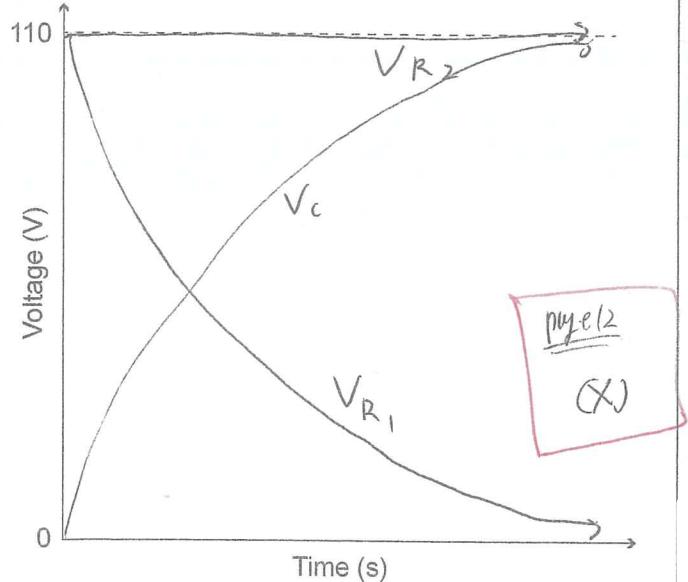
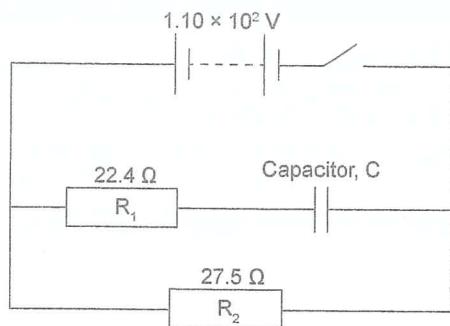
However, the voltage across R_1 and capacitor will be decreased as the charge is being stored on

the plate of capacitor and repel the already existing charges. the time constant that voltage decreased by its 63% value will be, $T = RC$. ~~22.4~~ then ~~it will be~~ the voltage across the R_1 and capacitor will be zero ~~or the~~ after ≈ 5 the constant is passed. The voltage across the R_2 will be constantly 110V ~~as~~ because the current across the R_2 will change as the ~~total resistance of circuit alternates~~ change as ~~1~~ due to ~~1~~ the change the ~~current~~ current across the R_1 is changed. The capacitor will be charged so voltage across it will be increased.

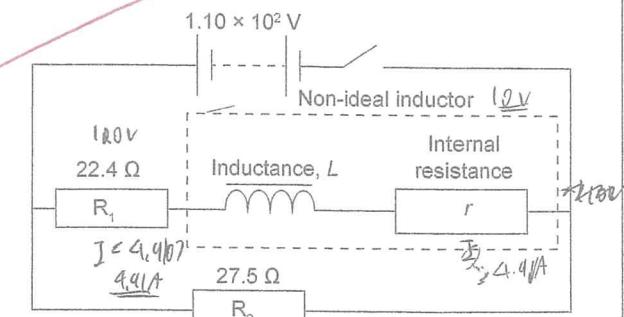
The capacitor is removed from the circuit and replaced with a non-ideal inductor.

The non-ideal inductor has both inductance, L , and internal resistance, r .

At $t = 0$ s, the switch is closed. The voltage across each component, R_1 , R_2 , and L , is measured for 3.00 s, and plotted on the graph on the facing page.



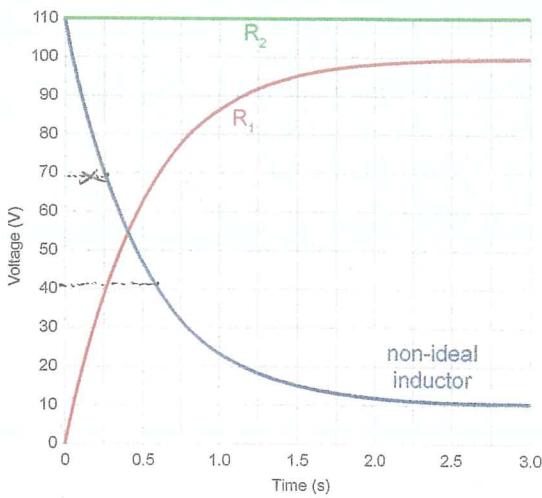
If you need to redraw your response, use the axes on page 12.



- (b) Using physics principles, explain why each of the three lines on the graph has the shape it does.

When the ~~control~~ switch is closed, there is the inductor is induced by the changing of current. As the change of current was maximum at $t=0$, the induced voltage is maximum according to Faraday's law ($E = L \frac{dI}{dt}$)

This makes the potential difference across path that contains R_1 and inductor be zero, so initially, the voltage across R_1 becomes 0. However, as the time flow, the ~~the rate of change of current will decrease and reach to steady current gradually. As the voltage induced on inductor is decreased, the voltage across the R_1 increase gradually. The R_2 will receive same voltage as the circuit is parallel.~~



- (c) Use information from the graph to estimate the time at which the current through R_1 and the current through R_2 are equal.

The time when ~~R_1 and R_2 be be equal~~ is the time when voltage ~~is~~ induced on inductor become zero. The inductor is considered to be zero induced to ~~zero~~ fully and have 0V after 5T. ~~As~~ the control T is the time taken to be reduced by 63% of its voltage value. $\therefore T$ for this inductor is approximately, $\frac{0.60}{0.27} = 2.25$ sec $\therefore 5 \times 0.60 = 3.0$ sec

- (d) Using information from the graph, calculate the value of the inductance, L , and internal resistance, r , of the non-ideal inductor.

$$T_{\text{inductor}} = \frac{L}{R}, \quad R = R_1 + r$$

$$\therefore T = L(R_1 + r), \quad T = \text{about } 0.60$$

$$L = 0.60(R_1 + r), \quad R_1 = 22.4 \Omega$$

$$L = 0.60(22.4 + r)$$

$\therefore 110V$ is induced to non-ideal inductor, terminal voltage = 100V.

From Ohm's law, $110 = 22.4$ From graph, voltage ~~induced~~ across $R_1 = 100V$

$\therefore V_{\text{across } r} = 10V$, as ~~the~~ r and R_1 is in same path, $I_{R_1} = I_L$

$$I_{R_1} = 4.464, \quad 4.46 A (7st) \quad \frac{100}{22.4}$$

$$10 = 4.46 \times r, \quad r = 2.24 \Omega$$

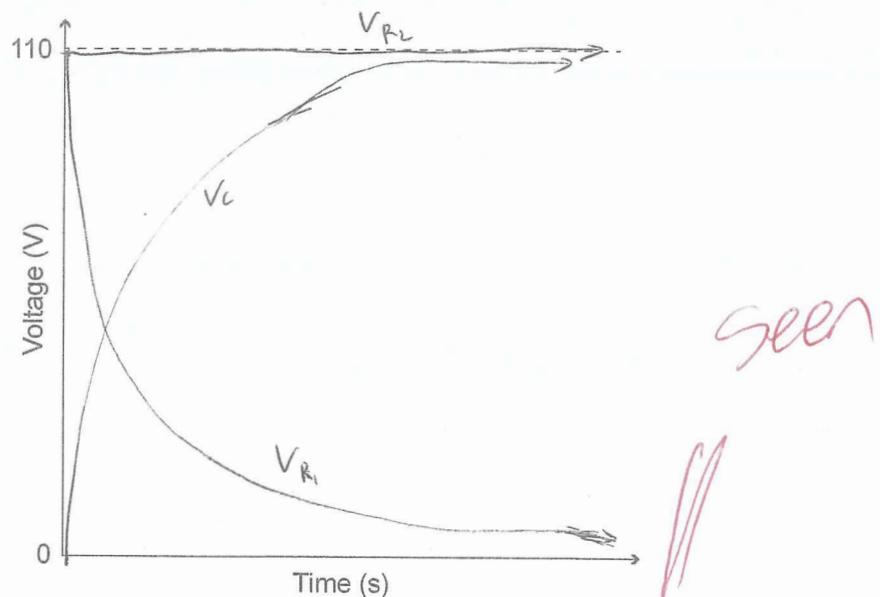
$$L = 0.60(22.4 + 2.24)$$

$$= 0.60(24.64)$$

$$= 14.784, \quad 14.8 M (3st)$$

SPARE DIAGRAM

If you need to redraw your response to Question Four (a), use the diagram below. Make sure it is clear which answer you want marked.



Extra space if required.
Write the question number(s) if applicable.

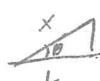
A2 (a)(i)

Thus we can check If the string D is tuned correctly or not by checking the frequency of beat produced when fluctuating two strings together. If the string D is tuned correctly, the ~~3rd~~ fundamental ~~harmonic~~ harmonic of string D will produce $\frac{4}{3}$ of fundamental frequency of "A". As frequency of ~~string~~ beat = $|f_1 - f_2|$, the beat frequency of $\frac{4}{3}f_1 - f_1 = \frac{1}{3}f_1$ will be heard. *(A)*

or As the fundamental frequency f_0 of "D" is $\frac{4}{3}$ of fundamental frequency of "A", we can make the tension of string A ~~increase~~ be increased to "A" has $\frac{4}{3}$ times of its own frequency. So this will ~~not~~ ^{not} create the beat as their frequency will be same and just enhance each other. *(A)*

$$\Delta L \quad L_0 \quad L \quad 2L_0 \cos \theta$$

$$(2L_0 \cos \theta - L_0)$$



$$\cos \theta = \frac{x}{L}$$

$$\text{KE } x = L - L_0$$

$$x = \frac{L}{\cos \theta} \text{ stretched} = \frac{L}{\cos \theta}, \text{ so}$$

$$L = \frac{L}{\cos \theta} - L_0$$

$$k \left(\frac{L}{\cos \theta} - L_0 \right) + k(L - L_0)$$

$$k \left(\frac{L}{\cos \theta} - 2L_0 + L \right)$$

$$L = x \cos \theta \\ (x = \frac{L}{\cos \theta})$$

$$k \left(\frac{L}{\cos \theta} - L_0 \right) \times \cos \theta$$

$$2k(L - L_0 \cos \theta)$$

Extra space if required.
 Write the question number(s) if applicable.

Q2 (d)

from $v = \sqrt{\frac{T}{\mu}}$, as T increased by $\frac{5}{4}$
 v increased by $\sqrt{\frac{5}{4}} = \frac{\sqrt{5}}{2}$

Given since $v = f\lambda$, as λ is constant, f will be increased by $\frac{\sqrt{5}}{2}$ and.

∴ The new fundamental frequency will be $(110 \times \frac{\sqrt{5}}{2})$

$$= 122.55 \text{ Hz}$$

$$= 122.98,$$

$$123.0 \text{ Hz (4sf)}$$

Scholarship exemplar 2021

Subject:		Physics	NZS standard:	93103	Total score:	21
Q	Score	Annotation				
1	6	Scholarship level understanding of binding energy shown. Indifferent grasp of interference phenomena resulting in a grade just below outstanding				
2	7	Outstanding understanding of force components as well as torque, equilibrium and the frequency relationship with tension. Only marred by a small mathematical error in the last part.				
3	5	Demonstrates scholarship level of understanding of dynamics calculations. Inferior layout and incomplete explanations prevented an outstanding performance.				
4	3	Only a rudimentary grasp of the operation of capacitors and inductors has been demonstrated. This is below scholarship level.				