

# What's the Difference between Cpk and Ppk?

<u>Cpk</u>	<u>Ppk</u>
Process <u>Capability</u> Index	Process <u>Performance</u> Index
Cp, Cpu, Cpl, Cpk	Pp, Ppu, Ppl, Ppk
Sometimes referred to as "Short term" capability	Sometimes referred to as "Long term" capability
Uses $\hat{\sigma}$ , an estimate of standard deviation R-bar / d2	Uses 's' as the standard deviation stdev.s
Considers only <u>within subgroup</u> variation	Considers <u>overall</u> variation
Does NOT account for the shifts and drifts between subgroups	Does account for the shifts and drifts between subgroups
Potential capability	"As viewed by customer" capability

### Capability Indices by Sampling Option

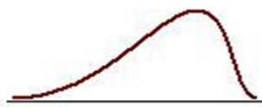
	<u>Option #1</u> Measure 100% of parts in batch	<u>Option #2</u> Measure a randomly selected sample of parts from batch	<u>Option #3</u> Measure repeated samples of parts drawn at uniform intervals across batch production
Arithmetic mean or Average	$\mu$ , pronounced /mew/, mean of the population	$\bar{x}$ , pronounced /ex-bar/, mean of the sample	$\bar{\bar{X}}$ , pronounced /ex-double bar/, grand average of the sample means
Standard Deviation (measures spread of data)	$\sigma$ , Pronounced /sig-ma/, Population standard deviation	$s$ , Sample standard deviation	$\hat{\sigma}$ , pronounced /sig-ma hat/, Estimated standard deviation
Formula for standard deviation	$\sigma = \sqrt{\frac{\sum (x_i - \mu)^2}{N}}$	$s = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}}$	$\hat{\sigma} = \bar{R} / d_2$
Where	N = Count of population	n = Count of sample	R-bar = Average of range vlaues from control chart d2 = Constant from Table of Control Chart Constants
Indices used	Pp, Ppu, Ppl, Ppk, Ppm	Pp, Ppu, Ppl, Ppk, Ppm	Cp, Cpu, Cpl, Cpk, Cpm
Formulas	$Pp = (USL - LSL) / (6 * \sigma)$	$Pp = (USL - LSL) / (6 * s)$	$Cp = (USL - LSL) / (6 * \hat{\sigma})$
	$Ppu = (USL - \mu) / (3 * \sigma)$	$Ppu = (USL - \bar{x}) / (3 * s)$	$Cpu = (USL - \bar{\bar{X}}) / (3 * \hat{\sigma})$
	$Ppl = (\mu - LSL) / (3 * \sigma)$	$Ppl = (\bar{x} - LSL) / (3 * s)$	$Cpl = (\bar{\bar{X}} - LSL) / (3 * \hat{\sigma})$
	$Ppk = [Ppu, Ppl]_{Min}$	$Ppk = [Ppu, Ppl]_{Min}$	$Cpk = [Cpu, Cpl]_{Min}$
	$Ppm = (USL - LSL) / 6 * \text{SQRT}[\sigma^2 + (\mu - T)^2]$	$Ppm = (USL - LSL) / 6 * \text{SQRT}[s^2 + (\bar{x} - T)^2]$	$Cpm = (USL - LSL) / 6 * \text{SQRT}[\hat{\sigma}^2 + (\bar{\bar{X}} - T)^2]$
Where	USL = Upper Specification Limit, LSL - Lower Specification Limit, T = Target, SQRT = Square root of		

## Capability Analysis Tools

A Capabaility level of ____ Cpk	Equates to +/- ____ sigma before the extent of the process curve meets a specification limit	At which point, the expected Defective Parts per Million (DPPM) is ____
0.50	1.5	133,610
1.00	3	2,700
1.33	4	63
1.50	4.5	6.8
1.67	5	0.57
2.00	6	0.002

### Skewness

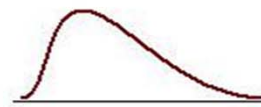
The coefficient of Skewness is a measure for the degree of symmetry in the variable distribution.



Negatively skewed distribution  
or Skewed to the left  
Skewness < 0



Normal distribution  
Symmetrical  
Skewness = 0



Positively skewed distribution  
or Skewed to the right  
Skewness > 0

### Kurtosis

The coefficient of Kurtosis is a measure for the degree of peakedness/flatness in the variable distribution.



Platykurtic distribution  
Low degree of peakedness  
Kurtosis < 0



Normal distribution  
Mesokurtic distribution  
Kurtosis = 0



Leptokurtic distribution  
High degree of peakedness  
Kurtosis > 0

Sample Size	d2 (used to estimate sigma for an x-bar control chart)
2	1.128
3	1.693
4	2.059
5	2.326
6	2.534
7	2.704
8	2.847
9	2.970
10	3.078
11	3.173
12	3.258
13	3.336

Sample Size	d2 (used to estimate sigma for an x-bar control chart)
14	3.407
15	3.472
16	3.532
17	3.588
18	3.640
19	3.689
20	3.735
21	3.778
22	3.819
23	3.858
24	3.895
25	3.931