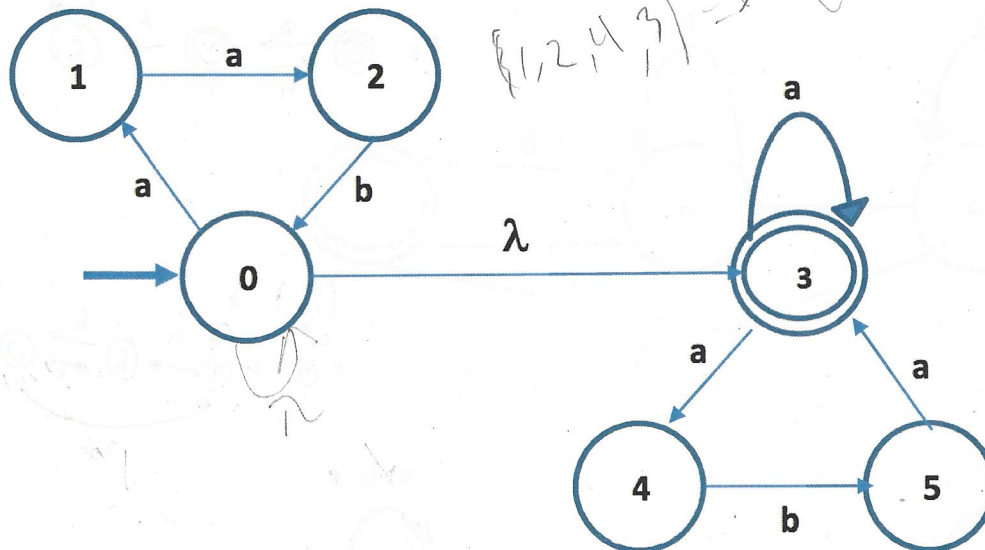


NAME Robert Martinez

792

Midterm #2

PROBLEM #1. Given the following NFA find its DFA.



#	Pts
1	1
2	6
3	26
4	0
5	6
Total	

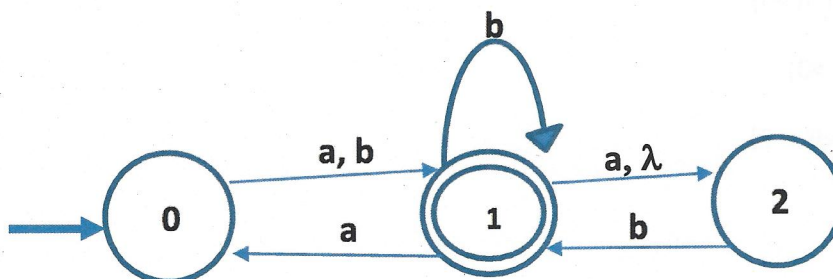
$$A = 2 - \text{dos}(0) \{0, 3\}$$

$$(A, a) = \{1, 3, 4\} = B$$

$$(A, b) = \emptyset = C$$

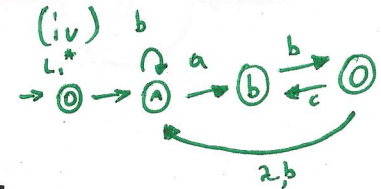
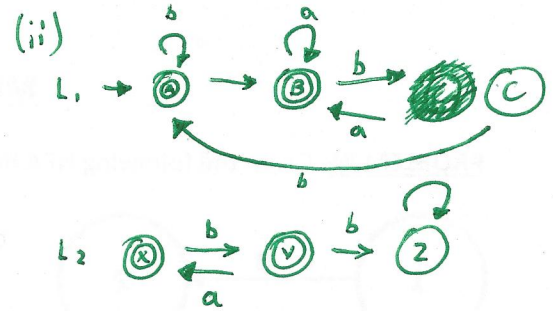
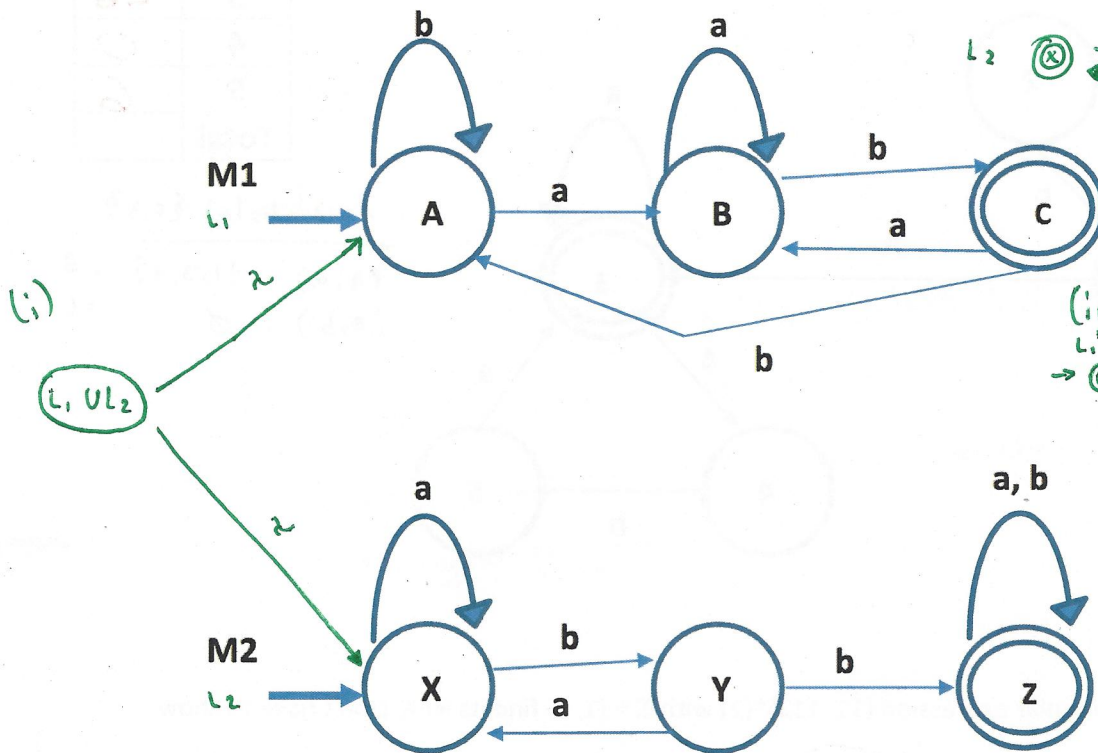
PROBLEM #2. Given the regular expression $(11, 112)^*\{2\}$ with $\Sigma = \{1, 2\}$ find its NFA. Don't have to show all the steps.

PROBLEM #3. Given $\Sigma = \{a, b\}$ and the strings: aa, abaab, baaba, aaa, bbbb. Which of these strings are accepted by the NFA given below? Prove it by doing **ALL** the corresponding delta transitions.



PROBLEM #4. Given $\Sigma = \{a, b\}$. Let M_1 and M_2 be the FAs pictured below accepting the languages L_1 and L_2 respectively. Draw FAs accepting the following languages:

- (i) $L_1 \cup L_2$ (ii) $L_1 \cap L_2$ (iii) $L_1 - L_2$ (iv) $L_1^* L_2^*$



PROBLEM #5. Given $\Sigma = \{a, b\}$. Which one of the following is a regular language? If regular, prove it by building FAs or using theorems studied in class or giving the correct argument. If not, then explain why.

- (i) $L_1 = \{w \in \{a\}^* : |w| \bmod 5 = 3\}$
- (ii) $L_2 = \{w \in \Sigma^* : w = a^n b^m, m, n > 0\}$
- (iii) $L_3 = \{w \in \Sigma^* : w = a^n b^n, n > 0\}$
- (iv) $(L_4)^c = \{w \in (a)^* : |w| \bmod 6 > 2\}$
- (v) $L_4 - L_1$
- (vi) $L_3 - L_4$

#1

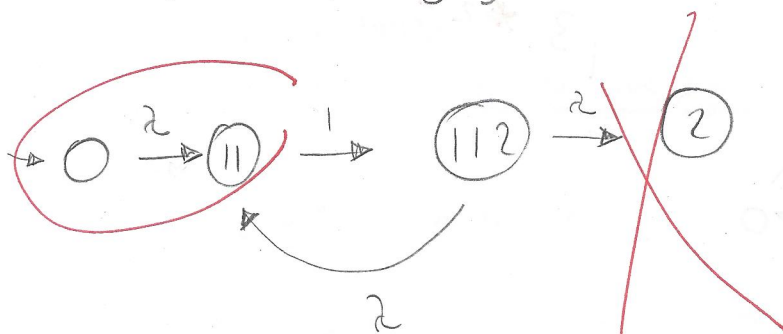
S	a	b	λ
0	1	\emptyset	<u>3</u>
1	2	\emptyset	\emptyset
2	\emptyset	\emptyset	\emptyset
<u>3</u>	<u>3,4</u>	\emptyset	\emptyset
4	\emptyset	5	\emptyset
5	<u>3</u>	\emptyset	\emptyset

 $a = \lambda\text{-closure}(0)$ 

a ↓



#2

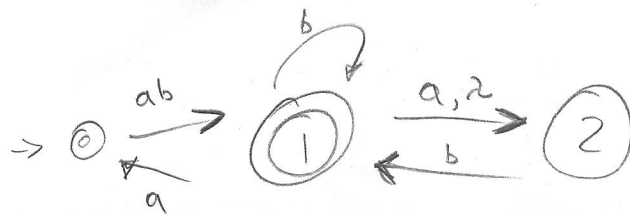
 $(11, 112)^* \{2\}$ λ jumps

$$\text{State: } 2 * 2 = 4$$

$$\lambda: 1 * 2 = 2$$

$$6$$

③



Not Accepted Final State

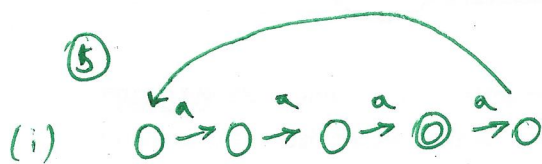
- × $\delta(0, aa) \rightarrow \delta(1, a) \rightarrow \delta(2, 2) - \text{NAFS}$
- × $\delta(0, abaab) \rightarrow \delta(1, baab) \rightarrow \delta(1, aab) \rightarrow \delta(2, ab) - \emptyset$
- × $\delta(0, baaba) \rightarrow \delta(1, aaba) \rightarrow \delta(2, aba) - \emptyset$
- × $\delta(0, aqa) \rightarrow \delta(1, aa) \rightarrow \delta(2, a) - \emptyset$
- ✓ $\delta(0, bbbb) \rightarrow \delta(1, bbb) \rightarrow \delta(1, bb) \rightarrow \delta(1, b) \rightarrow \delta(1, 2) - \text{AFS}$

Accepted Final State

④ X

$$13 * 2 = 26$$

⑤



(ii) a^n is regular

b^m is regular

Concatenation ab^m is regular

(iii) L_3 is not regular (showed in class)



(v) $L_3 - L_1$ Not regular

⑤ (i) $L_1 = \{w \in \{a\}^* : |w| \bmod 5 = 3\}$

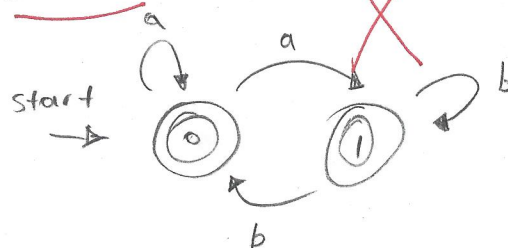
Proof: We build a DFA knowing that $\{a\}^*$ is a regular language, then regardless of any $\{a\}^*$, it will be a regular language even after its condition.

(ii) $L_2 = \{w \in \Sigma^* : w = a^n b^m, n > 0\}$

Proof: Not a regular language, because $n > 0$, therefore m could be any arbitrary number and $n > 0$ is limited, therefore since they can't have the same then it's not a regular.

(iii) $L_3 = \{w \in \Sigma^* : w = a^n b^n, n > 0\}$

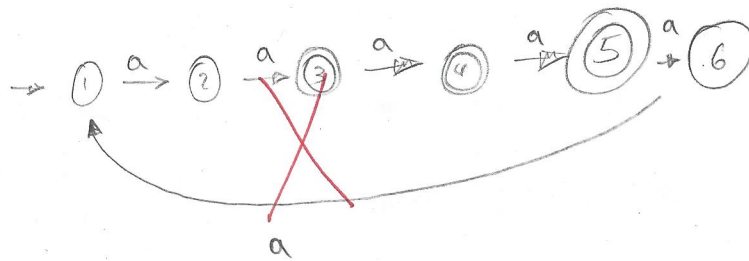
Proof: Regular Language



- Could always be regular language, as long as they have same numbers of a's & b's ($a^n b^n$)

$$(iv) (L_4)^c = \{w \in (a)^* : |w| \bmod 6 > 2\}$$

Proof:



Regular
✓ Language

2

$$(v) L_4 - L_1$$

Proof: By definition L_4 is a regular language since by regular expression definition it says. ^{Say what?} Therefore L_1 is a regular language too. Even after $L_4 - L_1$, it's still a regular language. ✓

2

$$(vi) L_3 - L_4$$

Proof: By definition L_3 is a regular language since by regular expression definition it says. Therefore L_4 is a regular language too. Even after $L_3 - L_4$, it's still a regular language.
X

Midterm #2 Corrections

Always itself or
any lambda near
there...

$$A = 2 - (\log(0)) = \{0, 3\}$$

$$(A, a) = \{1, 2, 3, 4\} = B \quad (E, a) = \{3\} = H$$

$(A, b) = \emptyset$

$$(E, b) = d = \mathbb{C}$$

$$(B, \alpha) = \{2, 3, 4\} = D$$

$$(F, a) = \{3, 4\} = F$$

$$(B, b) = \{ 5 \} = F$$

$$(F, b) = \{5\} = E$$

$$(c, a) = c$$

$$(G, a) = \{1, 3, 4\} = B$$

$$(c, b) = c \leftarrow$$

$$(6,6) = \emptyset$$

$$(p, \alpha) = \{3, 4\} = F$$

$$(14, a) : \{3, 4\} = F$$

$$(p, b) = \{0, 3, 5\} = G$$

$$(H, b) = \emptyset = C$$

	a	b
A	B	C
B	D	E
C	C	C
D	F	G
E	H	C
F	F	E
G	B	C
H	F	C

②

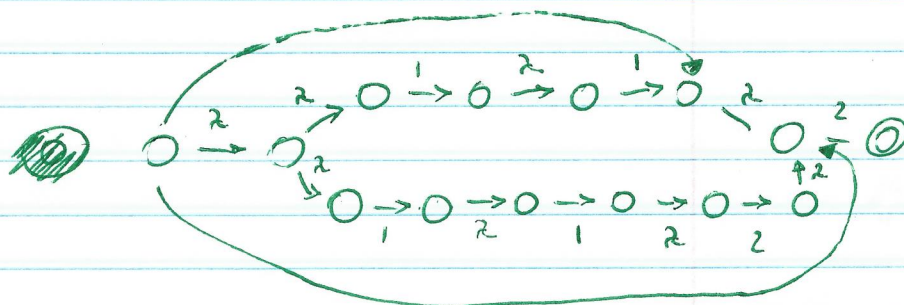
$$Z(11, 112)^* 2$$

$\odot \rightarrow \bigcirc \xrightarrow{1} \textcircled{10}$

$$\textcircled{2} \rightarrow \textcircled{0} \xrightarrow{2} \textcircled{0}$$

$$\textcircled{11} \rightarrow \textcircled{0} \xrightarrow{1} \textcircled{0} \xrightarrow{2} \textcircled{0} \xrightarrow{1} \textcircled{0}$$

(112) $\xrightarrow{4} \bigcirc \xrightarrow{1} \bigcirc \xrightarrow{2} \bigcirc \xrightarrow{1} \bigcirc \xrightarrow{2} \bigcirc \xrightarrow{2} \bigcirc$



Always itself or
any lambda move
there...

③ $\delta(0, aa) \rightarrow \delta(1, a) \rightarrow \delta(2, a) \times$

$\rightarrow \delta(2, 2) \times$

$\rightarrow \delta(0, 2) \times$

$\delta(2, aab) \times$

$\nearrow \delta(2, ab) \times$

$\delta(0, aabab) \rightarrow \delta(1, baab) \rightarrow \delta(1, aab) \rightarrow \delta(0, ab) \rightarrow \delta(1, b)$

$\rightarrow \delta(2, baab)$

\downarrow
 $\delta(1, 2)$
accept

\swarrow
 $\delta(aab) \rightarrow \delta(2, aab)$

$\searrow \delta(2, ab)$

$\downarrow \delta(1, aab)$

$\nearrow \delta(2, aab)$

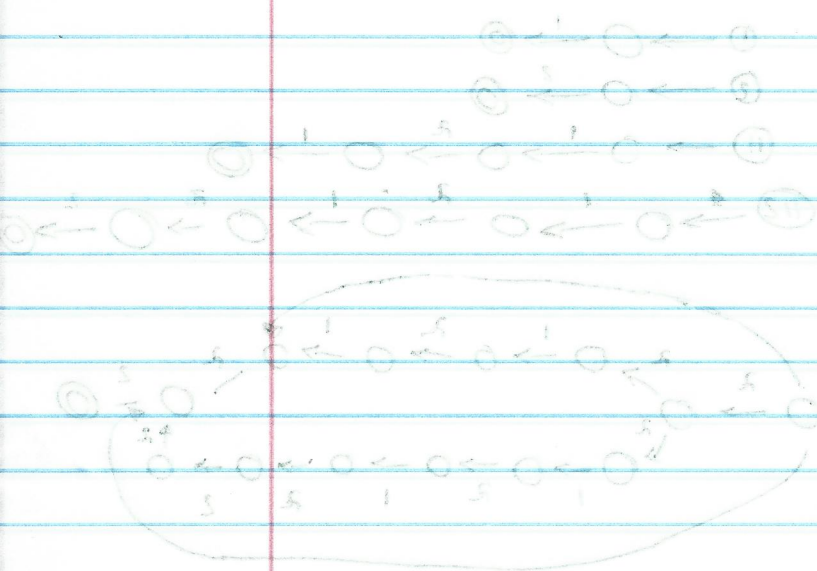
$\nearrow \delta(2, ab)$

$\searrow \delta(0, ab)$

$\searrow \delta(1, b)$

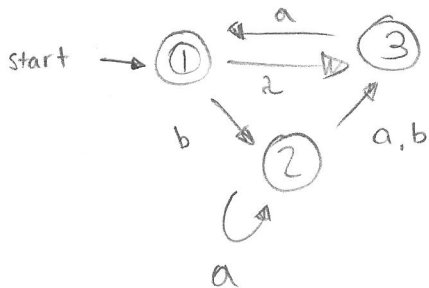
$\searrow \delta(1, 2)$

d	p	
0	a	(A)
1	a	(A)
2	a	(C)
3	b	(D)
4	a	(E)
5	b	(F)
6	a	(G)
7	b	(H)



NFA → DFA

NFA



$$A = \text{Clos}(1) = \{1, 3\}$$

$$(1,3,a) = (A,a) = \{1,3\} \quad A$$

$$(1,3,b) = (A,b) = \{2\} \quad B$$

$$(2,a) = (B,a) = \{2,3\} \quad C$$

$$(2,b) = (B,b) = \{3\} \quad D$$

$$(2,3,a) = (C,a) = \{2,3,1\} \quad E$$

$$(2,3,b) = (C,b) = \{3\} \quad D$$

$$(3,a) = (D,a) = \{1,3\} \quad A$$

$$(3,b) = (D,b) = \{\emptyset\} \quad F$$

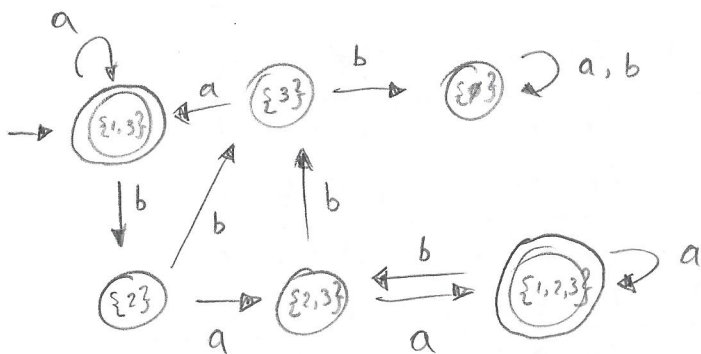
$$(1,2,3,a) = (E,a) = \{2,3,1\} \quad E$$

$$(1,2,3,b) = (E,b) = \{2,3\} \quad C$$

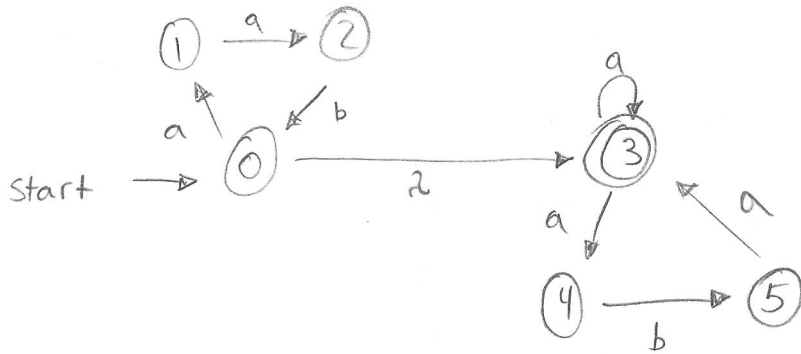
$$(\emptyset, a) = (F,a) = \{\emptyset\} \quad F$$

$$(\emptyset, b) = (F,b) = \{\emptyset\} \quad F$$

DFA	NFA	a	b
A	$\{1,3\}$	A	B
B	$\{2\}$	C	D
C	$\{2,3\}$	E	D
D	$\{3\}$	A	F
E	$\{1,2,3\}$	E	C
F	$\{\emptyset\}$	F	F



NFA → DFA (Midterm #2 Problem)



$$A = \delta^*(0) = \{0, 3\}$$

$$(0, 3, a) \quad (A, a) = \{1, 3, 4\} \quad B$$

$$(0, 3, b) \quad (A, b) = \{\emptyset\} \quad C$$

$$(1, 3, 4, a) \quad (B, a) = \{2, 3, 4\} \quad D$$

$$(1, 3, 4, b) \quad (B, b) = \{5\} \quad E$$

$$(\emptyset, a) \quad (C, a) = \{\emptyset\} \quad C$$

$$(\emptyset, b) \quad (C, b) = \{\emptyset\} \quad C$$

$$(2, 3, 4, a) \quad (D, a) = \{3, 4\} \quad F$$

$$(2, 3, 4, b) \quad (D, b) = \{0, 3, 5\} \quad G$$

$$(5, a) \quad (E, a) = \{3\} \quad H$$

$$(5, b) \quad (E, b) = \{\emptyset\} \quad C$$

$$(3, 4, a) \quad (F, a) = \{3, 4\} \quad F$$

$$(3, 4, b) \quad (F, b) = \{5\} \quad E$$

$$(0, 3, 5, a) \quad (G, a) = \{1, 3, 4\} \quad B$$

$$(0, 3, 5, b) \quad (G, b) = \{\emptyset\} \quad C$$

$$(3, a) \quad (H, a) = \{3, 4\} \quad F$$

$$(3, b) \quad (H, b) = \{\emptyset\} \quad C$$

NFA	DFA	a	b
<u>A</u>	$\{0, 3\}$	B	C
<u>B</u>	$\{1, 3, 4\}$	D	E
<u>C</u>	$\{\emptyset\}$	C	C
<u>D</u>	$\{2, 3, 4\}$	F	G
<u>E</u>	$\{5\}$	H	C
<u>F</u>	$\{3, 4\}$	F	E
<u>G</u>	$\{0, 3, 5\}$	B	C
<u>H</u>	$\{3\}$	F	C

