



Linear Search

The Search We Use Every Day

Recap: Introduction to Algorithms

- Understanding Algorithms
 - Find student with maximum grade



Recap: Introduction to Algorithms

- Understanding Algorithms
 - Find student with maximum grade
- Expressing Algorithms
 - Pseudocode



Recap: Introduction to Algorithms

- Understanding Algorithms
 - Find student with maximum grade
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 - Python Implementation



Recap: Introduction to Algorithms

- Understanding Algorithms
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 - Python Implementation
 - Functions: `find_max`



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First Video



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- Understanding Algorithms
 - Find student with maximum grade
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 - Functions: `find_max`
- `find_max`



Recap: Introduction to Algorithms

- Understanding Algorithms
 - Find student with maximum grade
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 - Functions: `find_max`
- `find_max`
 - Step count, or complexity



Recap: Introduction to Algorithms

- Understanding Algorithms
 - Find student with maximum grade
- Expressing Algorithms
 - Pseudocode
 - Python Implementation
 - Functions: `find_max`

- `find_max`
 - Step count, or complexity



Second Video



Recap of Complexity Analysis

```
1. def find_max(numbers):  
2.     max_value = numbers[0]  
3.     for number in numbers:  
4.         if number > max_value:  
5.             max_value = number  
6.     return max_value
```



Recap of Complexity Analysis

1. `def find_max(numbers):`
2. `max_value = numbers[0]`
3. `for number in numbers:`
4. `if number > max_value:`
5. `max_value = number`
6. `return max_value`



Recap of Complexity Analysis

```
1. def find_max(numbers):  
2.     max_value = numbers[0]  
3.     for number in numbers:  
4.         if number > max_value:  
5.             max_value = number  
6.     return max_value
```



Depends on input size (i.e.,
length of the list of numbers)



Recap of Complexity Analysis

1. `def find_max(numbers):`
2. `max_value = numbers[0]`
3. `for number in numbers:` **n steps**
4. `if number > max_value:`
5. `max_value = number`
6. `return max_value`



Recap of Complexity Analysis

1. `def find_max(numbers):` 1 step
2. `max_value = numbers[0]` 1 step
3. `for number in numbers:` n steps
4. `if number > max_value:`
5. `max_value = number`
6. `return max_value` 1 step



Recap of Complexity Analysis

- | | | |
|----|--|---------|
| 1. | <code>def find_max(numbers):</code> | 1 step |
| 2. | <code> max_value = numbers[0]</code> | 1 step |
| 3. | <code> for number in numbers:</code> | n steps |
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Recap of Complexity Analysis

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$$1 + 1 + n + n + n + 1 = 3n + 3 \text{ steps}$$



Recap of Complexity Analysis

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| 1. | def find_max(numbers): | 1 step |
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For a list of size **n**,
the total steps are **roughly n**
→ linear complexity

$$1 + 1 + n + n + n + 1 = 3n + 3 \text{ steps}$$



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For a list of size **n**,
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→ linear complexity

$$3n + 3 \approx O(n)$$

$$1 + 1 + n + n + n + 1 = 3n + 3 \text{ steps}$$



Recap of Complexity Analysis

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Introducing Linear Search

Algorithm FindMax

Algorithm LinearSearch



Introducing Linear Search

Algorithm FindMax

Input: A list of numbers

Algorithm LinearSearch

Input: A list of numbers, a **target**



Introducing Linear Search

Algorithm FindMax

Input: A list of numbers

Output: The maximum number in the list

Algorithm LinearSearch

Input: A list of numbers, a **target**

Output: The **position** of **target** or -1



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Algorithm FindMax

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$\text{max} \leftarrow \text{list}[0]$

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Introducing Linear Search

Algorithm FindMax

Input: A list of numbers

Output: The maximum number in the list

Begin

max \leftarrow list[0]

for each number in numbers do

if number > max then

Algorithm LinearSearch

Input: A list of numbers, a target

Output: The position of target or -1

Begin

~~max~~ \leftarrow list[0]

for each number in numbers do

if number == target then



Introducing Linear Search

Algorithm FindMax

Input: A list of numbers

Output: The maximum number in the list

Begin

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max \leftarrow number

Algorithm LinearSearch

Input: A list of numbers, a target

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Introducing Linear Search

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return -1

End



Implementing Linear Search

```
def find_max(numbers):
```

```
    max_number = numbers[0]
    for number in numbers:
        if number > max_number:
            max_number = number
    return max_number
```

```
sample_numbers = [5, 3, 9, 1, 6]
print("The maximum number is:",
      find_max(sample_numbers))
```

```
def linear_search(numbers, target):
```



Implementing Linear Search

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    for number in numbers:
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```
def linear_search(numbers, target):
```

```
    for number in numbers:
        if number == target:
            return ?
```



Implementing Linear Search

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def find_max(numbers):
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    max_number = numbers[0]
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def linear_search(numbers, target):
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sample_list = [5, 3, 9, 1, 6]
target = 1
```



Implementing Linear Search

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def find_max(numbers):
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    max_number = numbers[0]
    for number in numbers:
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sample_numbers = [5, 3, 9, 1, 6]
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```
def linear_search(numbers, target):
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```
    for number in numbers:
        if number == target:
            return ?
    return -1
```

```
sample_list = [5, 3, 9, 1, 6]
target = 1
print("The target is found at :",
      linear_search(sample_list, target))
```



Refining Implementation

```
def linear_search(numbers, target):
```

```
    for number in numbers:
```

```
        if number == target:
```

```
            return ?
```

```
    return -1
```

```
sample_list = [5, 3, 9, 1, 6]
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```
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```

```
print("The target is found at :", linear_search(sample_list, target))
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Refining Implementation

```
def linear_search(numbers, target):
```

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    for number in numbers:    for i in range(len(numbers)):
        if number == target:
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    return -1
```

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sample_list = [5, 3, 9, 1, 6]
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Refining Implementation

5	3	9	1	6
0	1	2	3	4

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def linear_search(numbers, target):
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    return -1
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    for i in range(len(numbers)):
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sample_list = [5, 3, 9, 1, 6]
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    if number == target:  
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sample_list = [5, 3, 9, 1, 6]
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print("The target is found at :", linear_search(sample_list, target))
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Refining Implementation

```
def linear_search(numbers, target):
```

```
    for i in range(len(numbers)):
```

```
        if numbers[i] == target:
```

```
            return i
```

```
    return -1 ←
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sample_list = [5, 3, 9, 1, 6]
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```
sample_list = [5, 3, 9, 1, 6]
```

```
target = 1
```

```
print("The target is found at:", linear_search(sample_list, target))
```

```
index = linear_search(sample_list, target)
```



Refining Implementation

```
def linear_search(numbers, target):  
    for i in range(len(numbers)):  
        if numbers[i] == target:  
            return i  
    return -1
```

```
sample_list = [5, 3, 9, 1, 6]  
target = 1  
index = linear_search(sample_list, target)  
if index == -1:  
    print("The target is not found!")
```



Refining Implementation

```
def linear_search(numbers, target):  
    for i in range(len(numbers)):  
        if numbers[i] == target:  
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sample_list = [5, 3, 9, 1, 6]
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target = 1
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index = linear_search(sample_list, target)
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```
if index == -1:
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    print("The target is not found!")
```

```
else:
```

```
    print("The target is found at location:", index)
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Refining Implementation

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def linear_search(numbers, target):  
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def linear_search(numbers, target):  
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    return -1
```

```
sample_list = [5, 3, 9, 1, 6]
```

```
target = int(input("Enter the number to search: "))
```

```
index = linear_search(sample_list, target)
```

```
if index == -1:
```

```
    print("The target is not found!")
```

```
else:
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    print("The target is found at location:", index)
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Complexity of Linear Search

```
def linear_search(numbers, target):
```

1 step

```
    for i in range(len(numbers)):
```

```
        if numbers[i] == target:
```

```
            return i
```

```
    return -1
```



Complexity of Linear Search

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```

1 step

n steps



Complexity of Linear Search

def linear_search(numbers, target): 1 step

 for i in range(len(numbers)): n steps

 if numbers[i] == target:

 return i

return -1

Worst Case → n steps



Complexity of Linear Search

def linear_search(numbers, target): 1 step

 for i in range(len(numbers)): n steps

 if numbers[i] == target:

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Worst Case → n steps

Best Case → 1 step



Complexity of Linear Search

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1 step
n steps
n steps



Complexity of Linear Search

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1 step
n steps
n steps
1 step



Complexity of Linear Search

def linear_search(numbers, target):	1 step
for i in range(len(numbers)):	n steps
if numbers[i] == target:	n steps
return i	1 step
return -1	1 step



Complexity of Linear Search

def linear_search(numbers, target): 1 step

 for i in range(len(numbers)): n steps

 if numbers[i] == target: n steps

 return i 1 step

return -1 1 step

$$1 + n + n + 1 + 1 = 2n + 3 \text{ steps}$$



Complexity of Linear Search

def linear_search(numbers, target): 1 step

 for i in range(len(numbers)): n steps

 if numbers[i] == target: n steps

 return i 1 step

return -1 1 step

$2n + 3 \approx O(n)$

$$1 + n + n + 1 + 1 = 2n + 3 \text{ steps}$$



Complexity of Linear Search

def linear_search(numbers, target): 1 step

 for i in range(len(numbers)): n steps

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$$1 + n + n + 1 + 1 = 2n + 3 \text{ steps}$$

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$$\cancel{2n + 3} \approx \cancel{O(n)}$$



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Worst Case: $O(n)$



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Worst Case: $O(n)$

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Complexity of Linear Search

def linear_search(numbers, target): 1 step

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$$1 + n + n + 1 + 1 = 2n + 3 \text{ steps}$$

$$2n + 3 \approx O(n)$$

$$\cancel{2n + 3} \approx O(n)$$

**Linear Search
Is a
Linear Time Algorithm**

Worst Case: $O(n)$

Best Case: $O(1)$



Summary and Next Steps

- What We Covered:



Summary and Next Steps

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 - Analyzed complexity of **find_max**



Summary and Next Steps

- What We Covered:
 - Analyzed complexity of **find_max**
 - Introduced **Big Oh** notation



Summary and Next Steps

- What We Covered:
 - Analyzed complexity of **find_max**
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 - Explored the **linear_search** algorithm in comparison to **find_max**.



Summary and Next Steps

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 - Analyzed the best case, and worst case scenarios for complexity.



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 - Analyzed complexity of **find_max**
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- Exercise:
 - Action Required: Visit our GitHub page (link in the description) to complete the exercise.



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Coming Up Next:

Topic: Binary Search—An efficient algorithm for **sorted lists**.



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 - Explored the **linear_search** algorithm in comparison to **find_max**.
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- Exercise:
 - Action Required: Visit our GitHub page (link in the description) to complete the exercise.
 - Objective: Analyze step counts in **different linear_search scenarios**.

Coming Up Next:

Topic: Binary Search—An efficient algorithm for **sorted lists**.

Highlights: Learn how Binary Search dramatically **reduces search time** by halving the search range.





Thank You for Watching!