

# Phylodynamic inference of contact network parameters through approximate Bayesian computation

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## Background

When an infectious disease spreads through a population, transmissions cannot generally occur between any two individuals at any time. Rather, the individuals must have a particular mode of contact with one another, which varies with the disease’s mode of transmission. For airborne pathogens, physical proximity may be sufficient, but for sexually transmitted diseases, either sexual or blood-to-blood contact is required. The set of links between individuals along which transmission can occur is called the contact network (Klovdahl 1985). The structure of the contact network underlying an epidemic can profoundly impact the speed and pattern of the epidemic’s expansion. Network structure can influence the prevalence trajectory (O’Dea and Wilke 2010) and epidemic threshold (Barthélemy et al. 2005), in turn affecting the estimates of quantities such as effective population size (Goodreau 2006). From a public health perspective, contact networks have been explored as tools for curtailing epidemic spread, by way of interventions targeted to well-connected nodes (Wang et al. 2015). True contact networks are a challenging type of data to collect, requiring extensive epidemiological investigation (Welch, Bansal, and Hunter 2011).

Viral sequence data, on the other hand, has become relatively inexpensive and straightforward to collect on a population level. Due to the high mutation rate of RNA viruses, epidemiological processes impact the course of viral evolution, thereby shaping the intra-host viral phylogeny (Drummond et al. 2003). The term “phylodynamics” was coined to describe this interaction, as well as the growing family of inference methods to estimate epidemiological parameters from viral phylogenies (Grenfell et al. 2004). These methods have revealed diverse properties of local viral outbreaks, from basic reproductive number (Stadler et al. 2011), to the degree of clustering (Hughes et al. 2009), to the elevated

transmission risk during acute infection (Volz et al. 2012). On the other hand, inference of structural network parameters has to date been limited. However, it has been shown that network structure has a tangible impact on phylogeny shape (Leventhal et al. 2012; Colijn and Gardy 2014; Goodreau 2006; Robinson et al. 2013), suggesting that such statistical inference might be possible (Welch, Bansal, and Hunter 2011).

Survey-based studies of sexual networks (Liljeros et al. 2001; Schneeberger et al. 2004) have found that sexual contact networks are best described by a preferential attachment model (although there has been some disagreement, see Jones and Handcock 2003). Under these models, nodes with a high number of contacts attract new connections at an elevated rate. Networks produced by preferential attachment have a power-law degree distribution, meaning that the number of nodes of degree  $k$  is proportional to  $k^{-\gamma}$  for some constant  $\gamma$ . These networks are also referred to as “scale-free”. The first contact network model incorporating preferential attachment was introduced by Barabási and Albert (1999), and is now referred to as the Barabási-Albert (BA) model. Under this model, networks are formed by iteratively adding nodes with  $m$  new edges each. These new edges are joined to existing nodes of degree  $k$  with probability proportional to  $k^\alpha$ , so that nodes of high degree tend to attract more connections (in the original paper, only  $\alpha = 1$  was investigated).

Previous work offers precedent for the possibility of statistical inference of structural network parameters. Britton and O’Neill (2002) develop a Bayesian approach to estimate the edge density in an Erdős-Rényi network (Erdős and Rényi 1960) given observed infection dates, and optionally recovery dates. Their approach was later extended by Groendyke, Welch, and Hunter (2011) and applied to a much larger data set of 188 individuals. Leigh Brown et al. (2011) found that a Waring distribution, which is produced by a different preferential attachment model, was a good fit to a phylogenetically estimated transmission network relating 60% of HIV infected men who have sex with men (MSM) in the United Kingdom. The transmission network is a subgraph of the contact network which includes only those edges which have already led to a new infection.

Standard methods of model fitting involve calculation of the likelihood of observed data under the model. In maximum likelihood estimation, a quantity proportional to the likelihood is optimized, often through a standard multi-dimensional numerical optimization procedure. Bayesian methods integrate prior information by optimizing the posterior probability instead. To avoid calculation of a normalizing constant, Bayesian inference is often performed using Markov chain Monte Carlo (MCMC), which requires the calculation of likelihood ratios. Unfortunately, it is generally difficult to explicitly calculate the likelihood of an observed transmission tree under a contact network model. To do so, it would be necessary to integrate over all possible networks, and also over all possible labellings of the internal nodes of the transmission tree. While it is not known (to us) whether such integration is tractable, a simpler alternative is offered by likelihood-free

methods, namely approximate Bayesian computation (ABC). ABC leverages the fact that, although calculating the likelihood may be impossible, generating simulated datasets according to a model is often straightforward. If our model fits the data well, the simulated data it produces should be similar to the observed data. More formally, if  $D$  is the observed data, the posterior distribution  $f(\theta \mid D)$  on model parameters  $\theta$  is replaced as the target of statistical inference by  $f(\theta \mid \rho(\hat{D}, D) < \varepsilon)$ , where  $\rho$  is a distance function,  $\hat{D}$  is a simulated dataset according to  $\theta$ , and  $\varepsilon$  is a small tolerance (Sunnåker et al. 2013). In the specific case when  $\rho$  is a kernel function, the approach is known as kernel-ABC.

Here, we apply kernel-ABC to the problem of statistical inference of contact network parameters from an estimated transmission tree, using the tree kernel developed by Poon et al. (2013). We then estimate the parameters of the BA model on a variety of simulated and real data sets. Our results show that the attachment power parameter  $\alpha$  can be inferred with reasonable accuracy, and can vary considerably between epidemics from different settings.

## Methods

We implemented a Gillespie simulation algorithm (Gillespie 1976) for simulating epidemics and transmission trees over static contact networks, in the same fashion as several previous studies (e.g. O’Dea and Wilke 2010; Robinson et al. 2013; Leventhal et al. 2012; Groendyke, Welch, and Hunter 2011; Goodreau 2006). To check that our implementation was correct, we reproduced Figure 1A of Leventhal et al. (2012) (our ??), which plots the unbalancedness of transmission trees simulated over four network models at various levels of pathogen transmissibility.

We chose to study the BA network model (Barabási and Albert 1999). In addition to  $m$  and  $\alpha$ , we investigated the parameters  $N$ , which denotes the total number of nodes in the network, and  $I$ , which is the number of infected nodes at which to stop the simulation and sample the transmission tree. Nodes in our networks followed simple susceptible-infected (SI) dynamics, meaning that they became infected at a rate proportional to their numbers of infected neighbours, and never recovered. For all analyses, the transmission trees’ branch lengths were scaled by dividing by their mean. We used the *igraph* library’s implementation of the BA model (Csardi and Nepusz 2006) to generate the graphs. The analyses were run on Westgrid (<https://www.westgrid.ca/>) and a local computer cluster.

### Kernel classifiers

We used the phylogenetic kernel developed by Poon et al. (2013) to test whether the parameters of the BA model had an effect on tree shape. The parameters were varied one at a time

over the following values:  $N = \{3000, 5000, 8000\}$ ,  $I = \{500, 1000, 2000\}$ ,  $m = \{2, 3, 4\}$ , and  $\alpha = \{0.5, 1, 1.5\}$ . The parameters not being tested were fixed at the values  $N = 5000$ ,  $I = 1000$ ,  $m = 2$ , and  $\alpha = 1$ . For each parameter set, 100 networks were generated, and a transmission tree was simulated over each (300 trees per parameter set). The 300 trees were compared pairwise with the tree kernel to form a  $300 \times 300$  kernel matrix. We constructed a kernel support vector machine (kSVM) classifier for the parameter of interest using the *kernlab* package (Karatzoglou et al. 2004), and evaluated its accuracy with 1000 two-fold cross-validations. The construction of the kernel matrices and classifiers was repeated for several combinations of the kernel meta-parameters  $\lambda$  (the “decay factor”), and  $\sigma$  (the “radial basis function variance”) (see Poon et al. 2013), and for transmission trees of sizes 100, 500, and 1000. We also tested univariate classifier based on Sackin’s index (Shao 1990) and an ordinary SVM based on the normalized lineages-through-time (nLTT) statistic (Janzen, Höhna, and Etienne 2015).

## ABC simulations

We implemented the adaptive sequential Monte-Carlo (SMC) algorithm for ABC developed by Del Moral, Doucet, and Jasra (2012). To check that our implementation was correct, we applied it to the same mixture of Gaussians used by Del Moral, Doucet, and Jasra to demonstrate their method (originally used by Sisson, Fan, and Tanaka (2007)). We were able to obtain a close approximation to the function (see ??), and attained the stopping condition used by the authors in a comparable number of steps.

We simulated three transmission trees, each with 500 tips, under every element of the Cartesian product of these parameter values:  $N = 5000$ ,  $I = \{1000, 2000\}$ ,  $m = \{2, 3, 4\}$ , and  $\alpha = \{0.0, 0.5, 1, 1.5\}$ . This produced a total of 24 parameter combinations  $\times$  three trees per combination = 72 trees total. The adaptive ABC algorithm was applied to each tree with these priors:  $m \sim \text{Uniform}(1, 5)$ ,  $\alpha \sim \text{Uniform}(0, 2)$ , and  $(N, I)$  jointly uniform on the triangular region  $\{500 \leq N \leq 15000, 500 \leq I \leq 5000, I \leq N\}$ . Following Del Moral, Doucet, and Jasra (2012) and Beaumont et al. (2009), all proposals were Gaussian, with variance equal to twice the empirical variance of the particles. The algorithm was run with 1000 particles, 5 simulated datasets per particle, and the “quality” parameter controlling the decay rate of the tolerance  $\varepsilon$  set to 0.95. We used the same stopping criterion as Del Moral, Doucet, and Jasra, namely when the MCMC acceptance rate dropped below 1.5%. Point estimates for the parameters were obtained by taking the highest point of an estimated kernel density on the final set of particles, using the *density* function with the default parameters in *R*. highest posterior density (HPD) intervals were calculated with the *HPDinterval* function from the *R* package *coda* (Plummer et al. 2006).

Two further analyses were performed to address potential sources of error. To evaluate

the effect of model misspecification in the case of heterogeneity among nodes, we generated a network where half the nodes were attached with power  $\alpha = 0.5$ , and the other half with power  $\alpha = 1.5$ . The other parameters for this network were  $N = 5000$ ,  $I = 1000$ , and  $m = 2$ . To investigate the effects of potential sampling bias, we simulated a transmission tree where the tips were sampled in a peer-driven fashion, rather than at random. That is, the probability to sample a node was twice as high if any of that node’s network peers had already been sampled. The parameters of this network were  $N = 5000$ ,  $I = 2000$ ,  $m = 2$ , and  $\alpha = 0.5$ .

## Investigation of published data

We applied our kernel-ABC method to several published HIV datasets. Because the BA model generates networks with a single connected component, we specifically searched for datasets which originated from existing clusters, either phylogenetically or geographically defined. Characteristics of the datasets we investigated are given in table 1.

| Reference              | Sequences ( $n$ ) | Location              | Risk group | Gene       |
|------------------------|-------------------|-----------------------|------------|------------|
| (Wang et al. 2015)     | 173               | Beijing, China        | MSM        | <i>pol</i> |
| (Cuevas et al. 2009)   | 287               | Basque Country, Spain | mixed      | <i>pol</i> |
| (Novitsky et al. 2013) | 180               | Mochudi, Botswana     | mixed      | <i>env</i> |
| (Novitsky et al. 2014) | 280               | Shanghai, China       | MSM        | <i>pol</i> |
| (Li et al. 2015)       | 136               | România               | IDU        | <i>pol</i> |

Table 1: Characteristics of published datasets investigated with kernel-ABC. Acronyms: MSM, men who have sex with men; IDU, injection drug users.

We downloaded all sequences associated with each study from GenBank. For the Novitsky et al. (2014) data, each sequence was aligned pairwise to the HXB2 reference sequence (Genbank accession number HIVHXB2CG) and the hypervariable regions were clipped out with BioPython version 1.66+ (Cock et al. 2009). Sequences were multiply aligned using *MUSCLE* version 3.8.31 (Edgar 2004), and alignments were manually inspected with *Seaview* version 4.4.2 (Gouy, Guindon, and Gascuel 2010). Phylogenies were constructed from the nucleotide alignments by approximate maximum likelihood using *FastTree2* version 2.1.7 with the general time-reversible (GTR) model. Transmission trees were estimated by rooting and time-scaling the phylogenies by root-to-tip regression, using a modified version of Path-O-Gen (distributed as part of BEAST (Drummond and Rambaut 2007)) as described previously (Poon 2015).

Two of the datasets (Li et al. 2015; Novitsky et al. 2014) were initially much larger than the others, containing 1265 and 1299 sequences respectively. To ensure that the analyses were comparable, we reduced these to a number of sequences similar to the smaller datasets.

For the Li et al. (2015) data, we detected a cluster of size 280 using a patristic distance cutoff of 0.02 as described previously (Poon et al. 2014). Only sequences within this cluster were carried forward. For the Novitsky et al. (2014) data, no large clusters were detected using the same cutoff, so we analysed a subtree of size 180 chosen arbitrarily.

## Results

### Kernel classifiers

Accuracy of the kSVM classifiers varied based on the parameter being tested (fig. 1). Classifiers based on two other tree statistics, the nLTT and Sackin’s index, generally exhibited worse performance than the tree kernel, although the magnitude of the disparity varied between the parameters (fig. 2 and ???). For appropriate choices of the kernel meta-parameters, the kSVM classifier for  $\alpha$  had an  $R^2$  above 0.8 for all combinations of tree size and epidemic size (fig. 2). The other classifiers’  $R^2$  averaged between 0.49 and 0.61 for the SVM based on the nLTT, and between 0.73 and 0.76 for the linear regression against Sackin’s index. The  $I$  parameter was also classified accurately by the tree kernel (??), with an average  $R^2$  of 0.93 for 500-tip trees or 0.7 for 100-tip trees. The nLTT performed almost as well on this parameter as the tree kernel, with  $R^2$  values of 0.83 for 500-tip trees or 0.55 for 100-tip trees. Sackin’s index was an extremely poor classifier for this parameter, with both  $R^2$  values below 0.08.

The  $m$  parameter was much harder to classify (??), with  $R^2$  for the kSVM varying between 0.004 and 0.36 depending on  $I$  and the tree size. The nLTT was also universally poor, with  $R^2$  below 0.02 for all scenarios. Sackin’s index fared slightly better, especially on trees with a higher number of tips, with  $R^2$  between 0 and 0.18. Finally, the accuracy of the kSVM classifier for  $N$  varied widely (??), from 0.08 to 0.82. The nLTT performed well in classifying  $N$  when the epidemic was large, improving upon the tree kernel in the scenarios with  $I = 2000$  and 100- or 500-tip transmission trees ( $R^2 = 0.31$  and 0.53), although it performed poorly when  $I$  was 500 or 1000 (average  $R^2 = 0.07$ ). Sackin’s index could not classify  $N$ , with all  $R^2$  below 0.11. Based on inspection of the cross-validation results, we chose to use the meta-parameters  $\lambda = 0.3$  and  $\sigma = 4$  in further analyses, and not to use Sackin’s index or the nLTT.

### ABC simulations

Of the four parameters,  $\alpha$  was the most accurately estimated, with a median [IQR] absolute error of 0.11 [0.05-0.18]. (fig. 3 and table 2). The accuracy of the estimates was not significantly different between values of  $m$  or  $I$  (both one-way ANOVA,  $p = 0.1$  and 0.25),

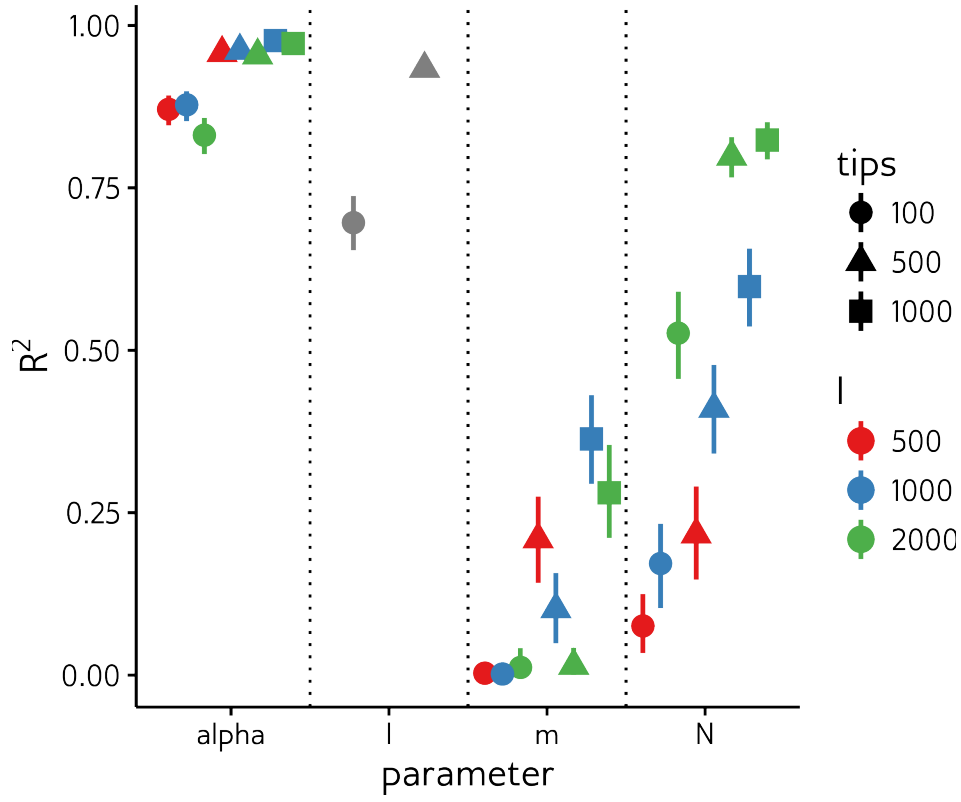


Figure 1: Cross-validation accuracy of kernel-SVM classifiers for BA model parameters, with kernel meta-parameters  $\lambda = 0.3$  and  $\sigma = 4$ . Each point was calculated based on 300 simulated transmission trees over networks with three different values of the parameter being tested. Vertical lines are empirical 95% confidence intervals based on 1000 2-fold cross-validations.

although the errors when the true value of  $\alpha$  was zero were significantly greater than the other values (Wilcoxon rank-sum test,  $p = 6.41 \times 10^{-4}$ ). The error in the estimated value of  $I$  was 305.66 [107.76-606.59]. Errors were significantly higher for  $\alpha \geq 1$  (Wilcoxon rank-sum test,  $p = 6.12 \times 10^{-4}$ ) and for  $I = 2000$  ( $p = 1.58 \times 10^{-6}$ ), but not for any values of  $m$  (one-way ANOVA,  $p = 0.33$ ). The  $m$  parameter was estimated correctly in 37 % of simulations, with an error of one in 40 % and of two or more in 22 % (the only possible  $m$  values were 1, 2, 3, 4, or 5). The true values of  $m$  and  $I$  did not significantly affect the error (one-way ANOVA,  $p = 0.5$  and  $0.68$ ). Finally, the total number of nodes  $N$  was consistently over-estimated by about a factor of two (error  $6.59 \times 10^3$  [ $4.21 \times 10^3$ - $8.28 \times 10^3$ ]). No other parameters influenced the accuracy of the  $N$  estimates (one-way ANOVA,  $p \geq 0.72$ ).

The dispersion of the ABC approximation to the posterior also varied between the parameters, with narrower HPD intervals for those with the most accurate point estimates (table 2). Figure 4 shows the distributions for for one simulation (equivalent plots for all the simulations can be found in the supplemental materials). HPD intervals around  $\alpha$  and

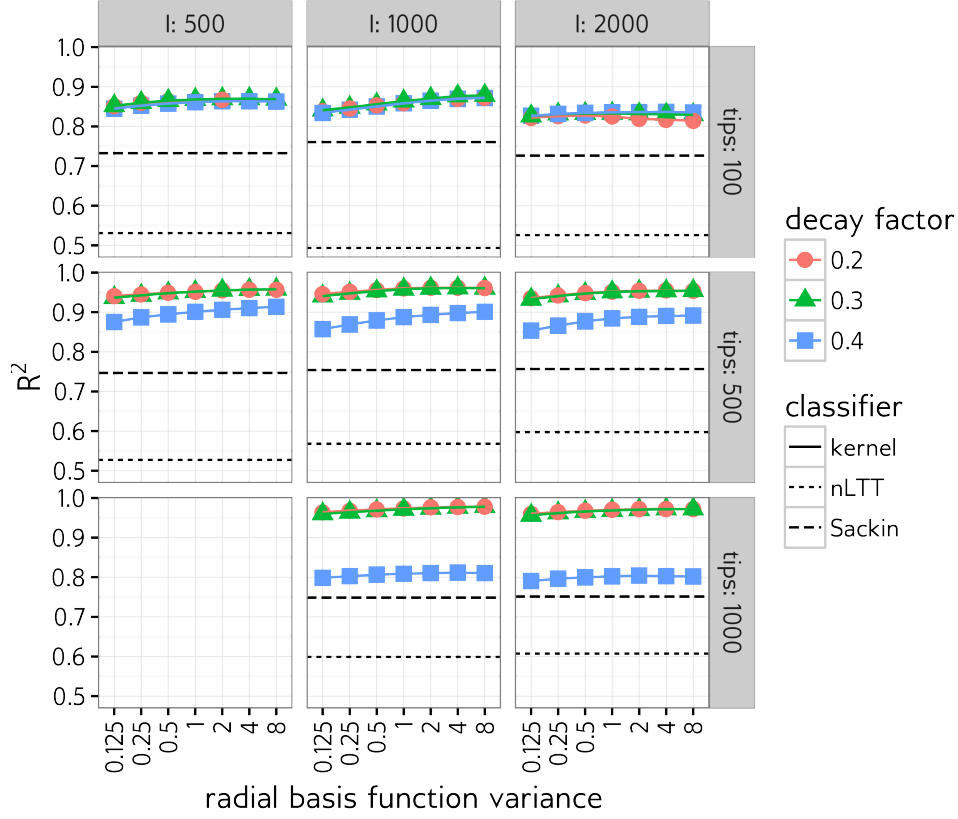


Figure 2: Cross-validation accuracy of kernel-SVM classifiers for  $\alpha$  parameter of BA network model, for various tree kernel meta-parameters and epidemic scenarios. Each point was calculated based on 300 simulated transmission trees over networks with  $\alpha = 0.5, 1.0$ , or  $1.5$ . Dotted and dashed lines indicate, respectively, performance of SVM using the nLTT statistic, and linear regression using Sackin's index. Facets are number of infected nodes before the simulation was stopped ( $I$ ) and number of tips in the sampled transmission tree.

$I$  were narrow relative to the region of nonzero prior density, whereas the intervals for  $m$  and  $N$  were more widely dispersed.

To test the effect of model misspecification, we simulated one network where the nodes exhibited heterogeneous preferential attachment power (half  $0.5$ , the other half  $1.5$ ), with  $m = 2$ ,  $N = 5000$ , and  $I = 1000$ . The maximum *a posteriori* (MAP) [95% HPD] estimates for each parameter were:  $\alpha$ ,  $1$  [ $0.85$ -  $1.12$ ];  $I$ ,  $5.23$  [ $2.05$ -  $5.85$ ];  $m$ ,  $10^4$  [ $3.06 \times 10^3$ -  $1.5 \times 10^4$ ];  $N$ ,  $1.17 \times 10^3$  [ $505.71$ -  $1.75 \times 10^3$ ].

To test the effect of sampling bias, we sampled one transmission tree in a peer-driven fashion, where the probability to sample a node was twice as high if one of its peers had already been sampled. The parameters for this experiment were  $N = 5000$ ,  $m = 2$ ,  $\alpha = 0.5$ , and  $I = 2000$ . The estimated values were  $\alpha$ ,  $0.48$  [ $0.03$ -  $0.83$ ];  $I$ ,  $3.6$  [ $2.18$ -  $5.9$ ];  $m$ ,  $1.08 \times 10^4$  [ $3.11 \times 10^3$ -  $1.48 \times 10^4$ ];  $N$ ,  $2.48 \times 10^3$  [ $1.28 \times 10^3$ -  $3.87 \times 10^3$ ].



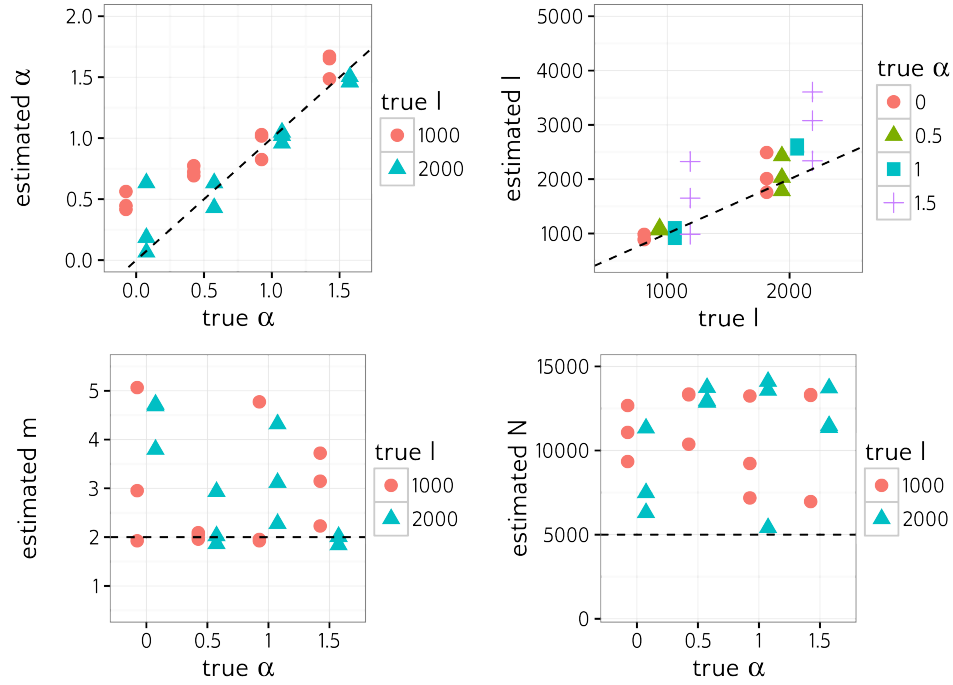


Figure 3: Point estimates of BA model parameters obtained by running kernel-ABC on simulated phylogenies. Dotted lines indicate the true values, and limits of the  $y$ -axes are the regions of uniform prior density.

## Real data

There was substantial heterogeneity among the parameter estimates for the five published HIV datasets we analysed. Two of the datasets (Niculescu et al. 2015; Wang et al. 2015) had estimated  $\alpha$  values near unity (MAP estimate [95% HPD] 1.06 [0.63-1.27] and 1 [0.41-1.16]). Another two datasets (Li et al. 2015; Cuevas et al. 2009) had lower estimated values and wider HPD intervals (0.77 [0.01-1.03] and 0.66 [0.03-0.84]). The Novitsky et al. (2014) data had an extremely low estimated  $\alpha$  and a very wide HPD interval 0.17 [0.04-1.39]). For all the datasets except Novitsky et al. (2014), estimated values of  $I$  were below 2000, with narrow HPD intervals around two of the datasets (Cuevas et al. (2009), 880.52 [290.7-1.51  $\times 10^3$ ]; Niculescu et al. (2015), 175.05 [138.74-454.51]) and wider intervals around the other two (Li et al. (2015), 1.59  $\times 10^3$  [284.01-3.81  $\times 10^3$ ]; Wang et al. (2015), 651.72 [268.94-4.24  $\times 10^3$ ]). The Novitsky et al. (2014) data was again the outlier, with a very high estimated  $I$ , and HPD interval spanning almost the entire prior region (7.55  $\times 10^3$  [228.96-8.92  $\times 10^3$ ]). Little information was gleaned about the  $m$  parameter, with the HPD interval occupying the entire prior region for all datasets. The estimates of  $N$  were similarly uninformative, with the exception that the point estimate for the Wang et al. (2015) data was smaller (5.84  $\times 10^3$ ) than the estimates for other datasets.

| Parameter | True value | Mean point estimate | Mean HPD width |
|-----------|------------|---------------------|----------------|
| $\alpha$  | 0.0        | 0.24                | 0.72           |
| $\alpha$  | 0.5        | 0.42                | 0.79           |
| $\alpha$  | 1.0        | 0.97                | 0.50           |
| $\alpha$  | 1.5        | 1.48                | 0.57           |
| $I$       | 1000       | 1155.68             | 1804.16        |
| $I$       | 2000       | 2646.07             | 2875.82        |
| $m$       | 2          | 2.92                | 3.17           |
| $m$       | 3          | 3.33                | 2.96           |
| $m$       | 4          | 3.62                | 3.12           |
| $N$       | 5000       | 10962.61            | 11969.32       |

Table 2: Average HPD interval widths for ABC model parameter estimates.

## Discussion

Contact networks can have a strong influence on epidemic progression, and are potentially useful as a public health tool. Despite this, few methods exist for investigating contact network parameters in a phylodynamic framework. Kernel-ABC is a model-agnostic method which can be used to investigate any quantity that affects tree shape. In this work, we developed a kernel-ABC-based method to infer the parameters of a contact network model. The method is general, and could be applied to any model from which contact networks can be simulated. We demonstrated the method on the BA model, which is a simple model incorporating the preferential attachment feature commonly seen in real-world networks.

By training a kernel-SVM classifier, we found that the  $\alpha$  and  $I$  parameters, representing preferential attachment power and number of infected nodes, had a strong influence on tree shape. This was reflected in the relative accuracy of the kernel-ABC estimates of these parameters. On the other hand, the  $m$  and  $N$  parameters did not produce much variation in tree shape, resulting in both poorly performing classifiers and uninformative kernel-ABC estimates. The total number of nodes  $N$  was almost always significantly overestimated. Since the prior on  $N$  and  $I$  is jointly uniform on a triangular region ( $I \leq N$ ), there is more prior mass on high  $N$  values. In retrospect, it is unreasonable to expect good estimation of  $N$ , because adding more nodes to a BA network does not change the edge density or overall shape. This can be illustrated by imagining that we add a small number of nodes to a network after the epidemic simulation has already been completed. It is possible that none of these new nodes attains a connection to any infected node. Thus, running the simulation again on the new, larger network could produce the exact same transmission tree as before.

Our investigation of published HIV datasets indicated heterogeneity in the contact network structures underlying several distinct local epidemics. Cuevas et al. (2009) studied a group of newly diagnosed individuals in the Basque Country, Spain. Although the individ-

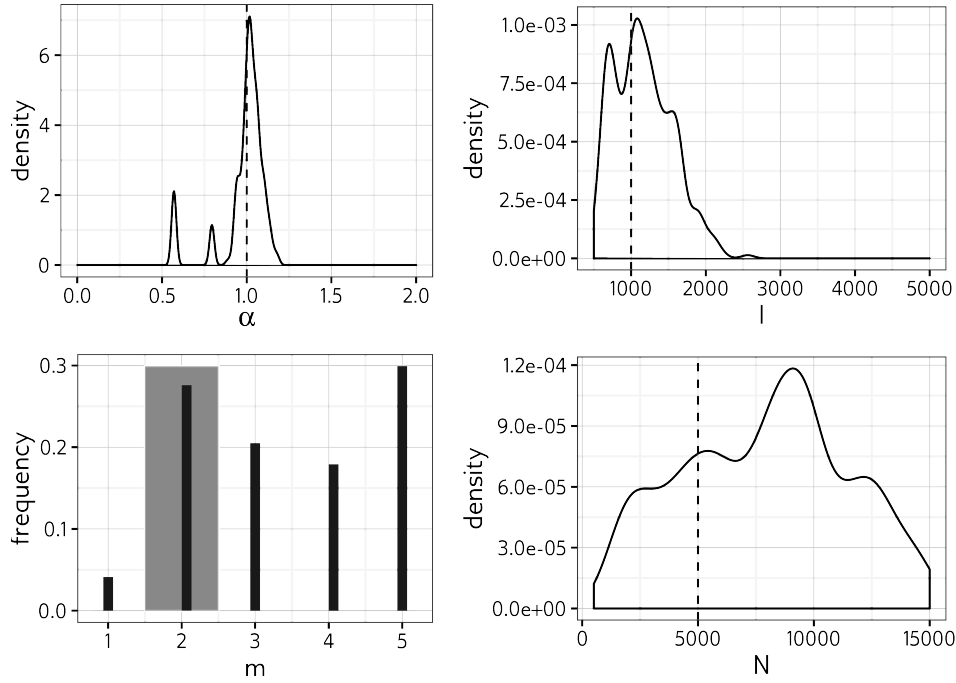


Figure 4: Marginal estimated posterior distributions obtained with ABC on a single simulated dataset. Dotted lines and shaded polygon indicate true values.

uals were of mixed risk group, and therefore unlikely to comprise a single contact network, a high proportion of them (47%) grouped into local transmission clusters, allowing for the possibility of weak preferential attachment dynamics. We estimated a relatively low attachment power for these data, which is consistent with the sampled sequences comprising many distinct sub-networks. **li2015** sampled a large number of acutely infected MSM in Shanghai, China. By using a patristic distance cutoff (Poon et al. 2014), we identified and analysed a large cluster. Surprisingly, the estimated attachment power was fairly low with a large credible interval.

Niculescu et al. (2015) studied a recent outbreak among Romanian injection drug user (IDU). The estimated attachment power for this dataset was the highest among all we considered, at slightly above one. The dataset constituted a fairly high sampling prevalence of 33% of newly diagnosed IDU infections over the study period. Wang et al. (2015) sampled acutely infected MSM in Beijing, China, and discovered a high degree of clustering which indicated that the local MSM subnetwork had been deeply sampled. In both these datasets, the estimated attachment power was close to one.

Novitsky et al. (2013) sampled approximately 44% of the HIV-infected individuals in the northern area of Mochudi, Botswana. Additional sampling in a later study (Novitsky et al. 2014) brought the genotyping coverage up to 70%. Even with such a high sampling coverage, we did not detect any large clusters using patristic distance, and therefore chose to analyze a subtree instead. The estimated attachment power was extremely low, with a very

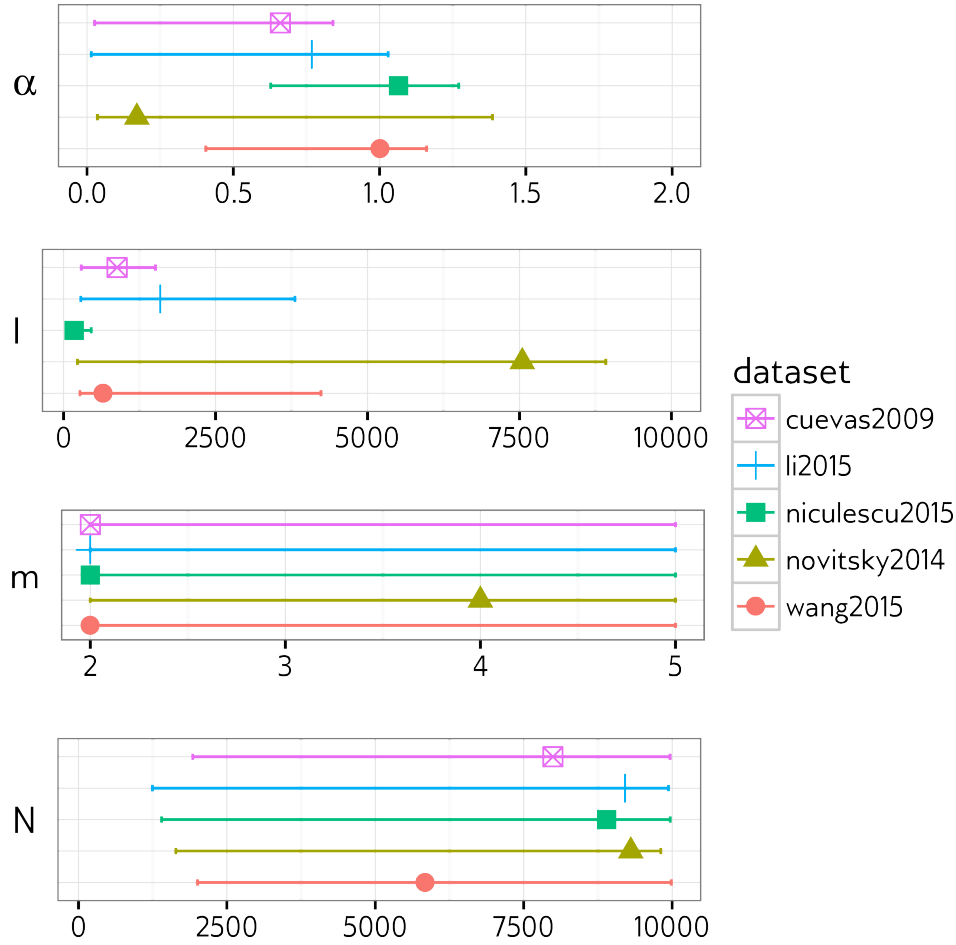


Figure 5: Point estimates and 95% HPD intervals for BA network parameters of published HIV datasets, obtained with kernel-ABC.

wide credible interval. The estimated number of infected nodes was also extremely high, much higher than the HIV-infected population of the town, with a similarly wide credible interval. Several factors may have contributed to this result. First, the authors note that the their sample was 75% female. In a primarily heterosexual risk environmet, removal of a disproportionate nmuber of males from the network could obfuscate the true network structure. Second, the town in question was in close proximity to the country’s capital, and the authors indicated that a high amount of migration takes place between the two locations. This suggests a reason for the high estimate of  $I$ : the contact network includes a much larger group based in the capital city.

When interpreting these results, we caution that the BA model is quite simple and most likely misspecified for these data. In particular, the average degree of a node in the network is equal to  $2m$ , and therefore is constrained to be a multiple of 2. Furthermore, we considered the case  $m = 1$ , where the network has no cycles, to be implausable and assigned it zero prior probability. This forces the average degree to be at least four, which may be unrealistically high for sexual networks. Additional modelling assumptions, include the

network being connected and static, the epidemic following simple SI dynamics, and the underlying behaviour of all nodes is the same. This last is particularly problematic, as we showed by simulating a network where some nodes exhibited a higher attachment power than others. The estimated attachment power was simply the average of the two values, indicating that, although we could characterize the network in aggregate, the estimated parameters could not be said to apply to any individual node. However, we note that, given the model-agnostic nature of our method, it is possible to fit a model with heterogeneous node behaviour, and indeed this may prove a fruitful avenue for future investigations.

Our method itself has of caveats, perhaps the most significant being that it takes a transmission tree as input. In reality, true transmission trees are not available and must be approximated, often by way of a viral phylogeny. Although this has been demonstrated to be a fair approximation in practice (e.g. Leitner et al. 1996), the topologies of a viral phylogeny and transmission tree can differ significantly (Ypma, Ballegooijen, and Wallinga 2013). In addition, it is computationally intensive, taking about a day when run on 20 cores in parallel with the settings we described in the methods. However, there are no other methods available to perform the types of estimation we do here, and we therefore believe our method will be useful to epidemiological researchers interested in the network structure underlying disease outbreaks.

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