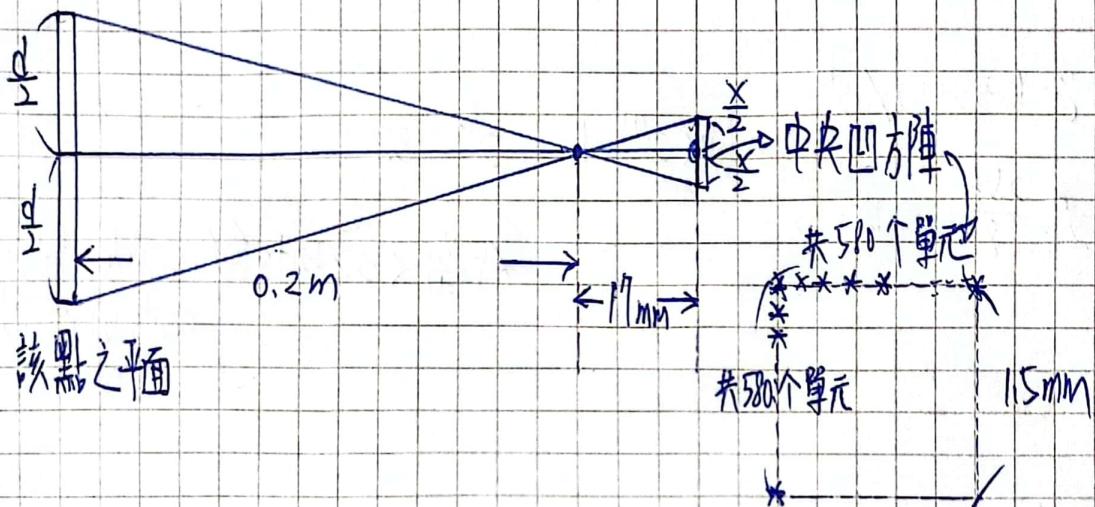


Q1:

Section 2.1 提到金屬體約 337,000 單元，若是以方陣來表示則長寬約為 580 單位

其中中央凹為  $15\text{mm} \times 15\text{mm}$  的正方形陣列



因為單元間之間隔與單元大小一致，故  $15\text{mm} = 580 \text{個單元} + 519 \text{個間隔}$

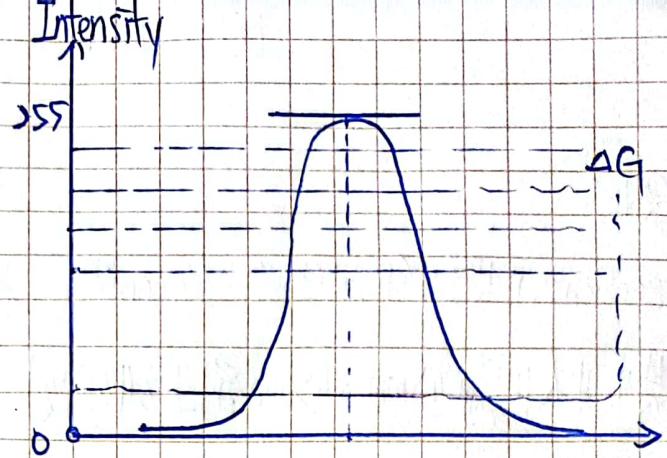
$$\text{根據相似三角形} \quad \frac{\frac{d}{2}}{0.2\text{m}} = \frac{\frac{x}{2}}{17 \times 10^{-3}\text{m}} \quad x = 15 \times 10^3 / 1159 \approx 1.3 \times 10^{-6}\text{m}$$

$$\frac{1}{2} \times 17 \times 10^{-3} = 0.2 \times \frac{1}{2} \times 1.3 \times 10^{-6}$$

$$\frac{2.6 \times 10^{-1}}{17 \times 10^{-3}} = \frac{2.6}{17} \times 10^{-5} \approx 1.53 \times 10^{-5}\text{m}$$

Q2:

$$\begin{aligned}f(x, y) &= \bar{r}(x, y) r(x, y) \\&= 255 e^{-[(x-x_0)^2 + (y-y_0)^2]} \times 1.0 \\&= 255 e^{-[(x-x_0)^2 + (y-y_0)^2]}\end{aligned}$$



$$\Delta G = 8 = (255+1)/2^m$$

$$2^m = \frac{256}{8} \Rightarrow m = 5$$

$$\times 2^m = k = 2^5 = 32$$

A: 當 < 32 bits 會有 visible false contouring 的問題。

Q3:

$$\text{width} : \text{height} = \frac{16}{9}$$

已知垂直方向有 1125 lines  $\Rightarrow$  也就是 1125 pixels  
 $\hookrightarrow \text{width} = \frac{16}{9} \times 1125 = 2000 \text{ pixels}$

單位換算：

$$\text{RGB 各 8 bits} \Rightarrow 3 \times 8 = 24 \times \text{每 field } \frac{1}{60} \text{ s 共 2 fields} \Rightarrow \frac{1}{60} \times 2 = \frac{1}{30} \text{ s}$$

$$2 \text{ hrs} = 7200 \text{ s}$$

$$\frac{2000 \times 1125 \times 24 \times 7200}{\text{pixel RGB } \frac{1}{\text{hr}} \frac{1}{30} \text{ s}} = 1.1664 \times 10^{13} \text{ bits}$$

$$A = 1.1664 \times 10^{13} \text{ bits}$$

Q4:

	$S_1$	$S_2$	
0	0 0 0 0 0	0 0 1 1 0	
1	0 0 1 0 0	0 1 0 0 1	
1	0 0 1 0 0	1 0 0 0 0	
0	0 1 1 ① 0	0 0 0 0 0	
	P		
0	0 1 1 0 0	0 1 1 1 1	

先選 p, q  
(a) 可看出  $S_1, S_2$  並非 4-connected 因為 p 的上下左右都不是 1  
故和 4-connected adjacent 違背矛盾 和右都不是 1

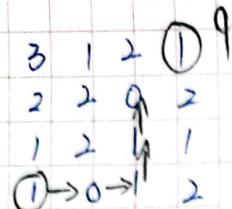
(b) 可看出  $S_1, S_2$  符合 8-connected  $\because q$  在  $N_8(p)$  這個集合。

(c) 可看出  $S_1, S_2$  符合 m-connected  $\because q$  在  $N_D(p)$  內且  $N_4(p) \cap N_4(q)$  是空的。

Q5.

Let  $V = \{0, 1\}$

5-(a)



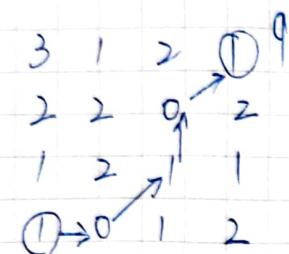
P

#1

由#1可知並非 4-adjacent 之 p 到不 3q

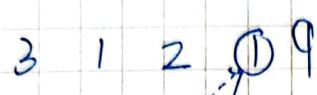
由#2 可知 8-adjacent 的 shortest path 長度為 4

由#3 可知 m-adjacent 的 shortest path 長度為 5



P

#2



2 2 0 2

1 2 1 1

① → 0 → 1 2

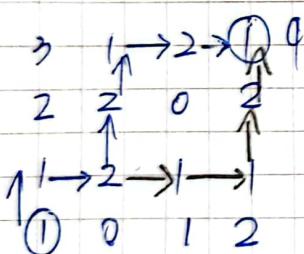
P #3

→ 這邊不能算的原因

m-adjacent 的定義  $N_4(p) \cap N_4(q) \Rightarrow \emptyset$

5-(b) Let  $V = \{1, 2\}$

由#4 可知 4-adjacent 有  $\rightarrow \rightarrow$  2 種 shortest path  
長度皆是 6

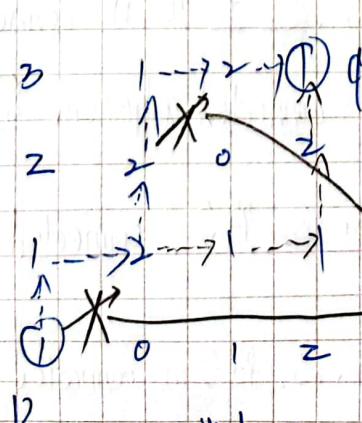
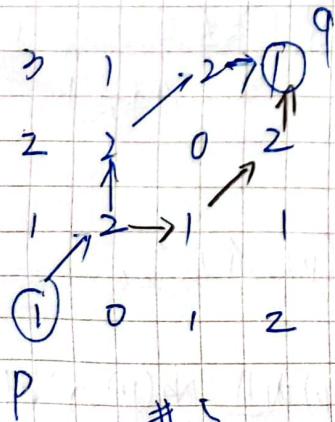


P

#4

由#5 可知 8-adjacent 有  $\rightarrow \rightarrow$  2 種 shortest path  
長度皆是 4

由#6 可知 m-adjacent 的 shortest path 為 6



$N_4(p) \cap N_4(q) \neq \emptyset$ ; 不能算

Q6:

Let  $S_1 = \{3, -5, 8\}$ ,  $S_2 = \{21, 25, 31\}$

$H(S_1) = 3$ ;  $H(S_2) = 25$

$H(aS_1 + bS_2) \Leftrightarrow a=1; b=1 \Rightarrow H(S_1 + S_2) = \text{median}\{24, 20, 39\} = 24$

$\times \because H(aS_1 + bS_2) \neq aH(S_1) + bH(S_2)$  (i.e. non-linear)

$24 \neq 3 + 25$

Q7: (1)  $r(x,y,u,v) = e^{j2\pi(ux/M + vy/N)}$

separable:  $r(x,y,u,v) = e^{-j2\pi(ux/M + vy/N)}$

$$= e^{-j2\pi(ux/M)} \times e^{-j2\pi(vy/N)}$$

$$= r_1(x,u) \times r_2(y,v) \#$$

symmetric: 'if  $r_1(x,y)$  is functionally equal to  $r_2(x,y)$

' $r_1(x,u)r_2(y,v) = r_1(x,u)r_1(y,v) \#$

(2)  $s(x,y,u,v) = \frac{1}{MN} e^{j2\pi(ux/M + vy/N)}$

separable:  $s(x,y,u,v) = \frac{1}{MN} \times e^{j2\pi(ux/M)} \times e^{j2\pi(vy/N)}$

$$= \frac{1}{MN} \times s_1(x,u) \times s_2(y,v) \#$$

symmetric: 'if  $s_1(x,y)$  is functionally equal to  $s_2(x,y)$

' $\frac{1}{MN} \times s_1(x,u)s_2(y,v) = \frac{1}{MN} s_1(x,u)s_1(y,v) \#$

Q8: Please print out the simulation code along with your results for the problems below. 8. Reducing the Number of Intensity Levels in an Image (10%)

(a) Write a computer program capable of reducing the number of intensity levels in an image from 256 to 2, in integer powers of 2. The desired number of intensity levels needs to be a variable input to your program.

```
import cv2
import numpy as np
import matplotlib.pyplot as plt

def reduce_intensity_levels(image_path, levels):
    # 讀取圖像
    image = cv2.imread(image_path, cv2.IMREAD_GRAYSCALE)
    # 計算每個強度級別的間隔
    interval = 256 // levels
    # 減少強度級別
    reduced_image = (image // interval) * interval
    # 顯示原始圖像
    plt.figure(figsize=(8, 8))
    plt.subplot(1, 2, 1)
    plt.imshow(image, cmap='gray')
    plt.title('Original Image')
    plt.axis('off')
    # 顯示處理後的圖像
    plt.subplot(1, 2, 2)
    plt.imshow(reduced_image, cmap='gray')
    plt.title('From 256 to 2')
    plt.axis('off')
# 輸入圖像的檔案路徑和所需的強度級別
image_path = "/content/Fig0221(a) (ctskull-256).tif"
desired_levels = 2

# 呼叫函式進行圖像處理
reduce_intensity_levels(image_path, desired_levels)
```

Original Image



From 256 to 2



(b) Download Fig. 2.21(a) from the course web site and duplicate the results shown in Fig. 2.21 of the book.

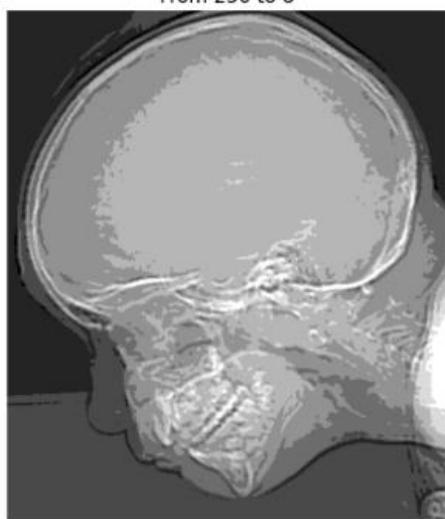
```
1 import cv2
2 import numpy as np
3 import matplotlib.pyplot as plt
4
5 def reduce_intensity_levels(image_path, levels):
6     # 讀取圖像
7     image = cv2.imread(image_path, cv2.IMREAD_GRAYSCALE)
8
9     # 計算每個強度級別的間隔
10    interval = 256 // levels
11
12    # 減少強度級別
13    reduced_image = (image // interval) * interval
14
15    return reduced_image
16
17 # 輸入圖像的檔案路徑和所需的強度級別
18 image_path = "/content/Fig0221(a) (ctskull-256).tif"
19 desired_levels = [16, 8, 4, 2]
20
21 # 呼叫函式進行圖像處理
22 fig, axs = plt.subplots(2, 2, figsize=(10, 10))
23
24 for i, levels in enumerate(desired_levels):
25     reduced_image = reduce_intensity_levels(image_path, levels)
26     row = i // 2
27     col = i % 2
28     axs[row, col].imshow(reduced_image, cmap='gray')
29     axs[row, col].set_title(f'From 256 to {levels}')
30     axs[row, col].axis('off')
31
32 plt.tight_layout()
33 plt.show()
```

☒

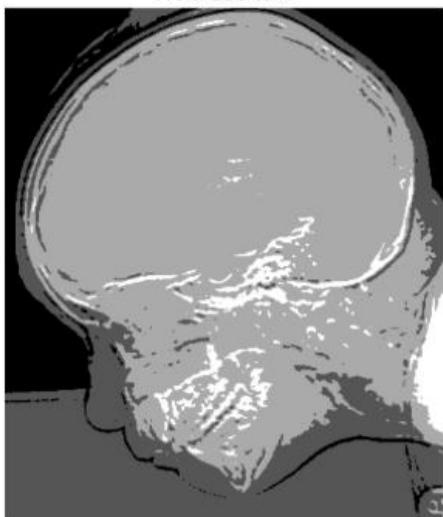
From 256 to 16



From 256 to 8



From 256 to 4

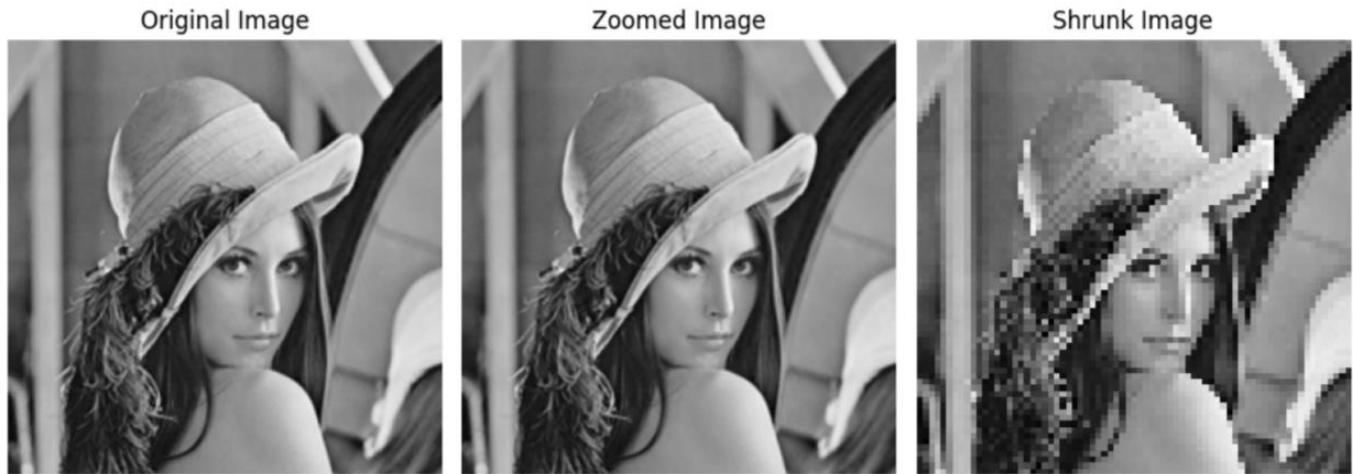


From 256 to 2



9. Zooming and Shrinking Images by Pixel Replication (10%) (a) Write a computer program capable of zooming and shrinking an image by pixel replication. Assume that the desired zoom/shrink factors are integers.

```
1 import cv2
2 from matplotlib import pyplot as plt
3
4 def zoom_image(image, zoom_factor):
5     height, width = image.shape[:2]
6     zoomed_height = height * zoom_factor
7     zoomed_width = width * zoom_factor
8
9     zoomed_image = cv2.resize(image, (zoomed_width, zoomed_height), interpolation=cv2.INTER_NEAREST)
10    return zoomed_image
11
12 def shrink_image(image, shrink_factor):
13     height, width = image.shape[:2]
14     shrunk_height = height // shrink_factor
15     shrunk_width = width // shrink_factor
16
17     shrunk_image = cv2.resize(image, (shrunk_width, shrunk_height), interpolation=cv2.INTER_NEAREST)
18    return shrunk_image
19
20 # Load the image
21 image = cv2.imread('/content/Lena.png', cv2.IMREAD_GRAYSCALE)
22
23 # Zoom the image by pixel replication
24 zoom_factor = 20 # Adjust the zoom factor as needed
25 zoomed_image = zoom_image(image, zoom_factor)
26
27 # Shrink the image by pixel replication
28 shrink_factor = 3 # Adjust the shrink factor as needed
29 shrunk_image = shrink_image(image, shrink_factor)
30
31 # Display the zoomed and shrunk images
32 plt.figure(figsize=(10, 8))
33 plt.subplot(1, 3, 1)
34 plt.title('Original Image')
35 plt.imshow(image, cmap='gray')
36 plt.axis('off')
37
38 plt.subplot(1, 3, 2)
39 plt.title('Zoomed Image')
40 plt.imshow(zoomed_image, cmap='gray')
41 plt.axis('off')
42
43 plt.subplot(1, 3, 3)
44 plt.title('Shrunk Image')
45 plt.imshow(shrunk_image, cmap='gray')
46 plt.axis('off')
47
48 plt.tight_layout()
49 plt.show()
```



(b) Download Fig. 2.20(a) from the course web site and use your program to shrink the image by a factor of 12.

```

1 import cv2
2 from matplotlib import pyplot as plt
3
4 def shrink_image(image, shrink_factor):
5     height, width = image.shape[:2]
6     shrunk_height = height // shrink_factor
7     shrunk_width = width // shrink_factor
8
9     shrunk_image = cv2.resize(image, (shrunk_width, shrunk_height), interpolation=cv2.INTER_NEAREST)
10    return shrunk_image
11
12 # Load the image
13 image = cv2.imread('/content/Fig0220(a) (chronometer 3692x2812 2pt25 inch 1250 dpi).tif', cv2.IMREAD_GRAYSCALE)
14
15 # Shrink the image by pixel replication
16 shrink_factor = 12 # Adjust the shrink factor as needed
17 shrunk_image = shrink_image(image, shrink_factor)
18
19 # Display the original and shrunk images
20 plt.figure(figsize=(10, 8))
21 plt.subplot(1, 2, 1)
22 plt.title('Original Image')
23 plt.imshow(image, cmap='gray')
24 plt.axis('off')
25
26 plt.subplot(1, 2, 2)
27 plt.title('Shrunk Image')
28 plt.imshow(shrunk_image, cmap='gray')
29 plt.axis('off')
30
31 plt.tight_layout()
32 plt.show()
33 # Save the shrunk image
34 cv2.imwrite('/content/shrunk_clock.png', shrunk_image)

```



True

(c) Use your program to zoom the image in (b) back to the resolution of the original. Explain the reasons for their differences.

A: 會有落差的原因是因為當進行縮小或放大時會在進行內插的時候丟失一些特徵值，導致有些細節被丟失，所以就算縮放回原本大小也會和原圖產生落差。

```

1 import cv2
2 from matplotlib import pyplot as plt
3
4 def zoom_image(image, zoom_factor):
5     height, width = image.shape[:2]
6     zoomed_height = height * zoom_factor
7     zoomed_width = width * zoom_factor
8
9     zoomed_image = cv2.resize(image, (zoomed_width, zoomed_height), interpolation=cv2.INTER_NEAREST)
10    return zoomed_image
11
12 # Load the image
13 image = cv2.imread('/content/shrunk_clock.png', cv2.IMREAD_GRAYSCALE)
14 origin = cv2.imread('/content/Fig0220(a) (chronometer 3692x2812 2pt25 inch 1250 dpi).tif', cv2.IMREAD_GRAYSCALE)
15 # Zoom the image by pixel replication
16 zoom_factor = 12 # Adjust the zoom factor as needed
17 zoomed_image = zoom_image(image, zoom_factor)

```

```
19 # Display the zoomed and shrunk images
20 plt.figure(figsize=(10, 8))
21 plt.subplot(1, 3, 1)
22 plt.title('Original Image')
23 plt.imshow(origin, cmap='gray')
24 plt.axis('off')
25
26 plt.subplot(1, 3, 2)
27 plt.title('After Shrunk and Zoomed Image')
28 plt.imshow(zoomed_image, cmap='gray')
29 plt.axis('off')
30
31 plt.tight_layout()
32 plt.show()
```

Original Image

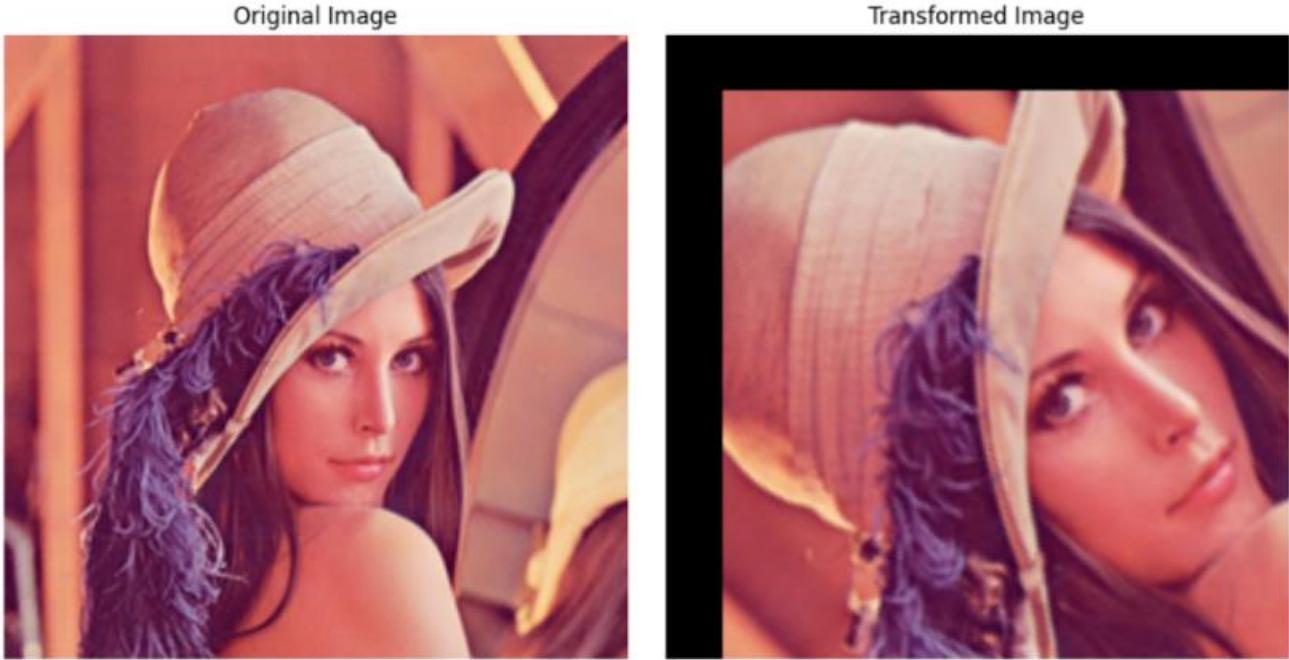


After Shrunk and Zoomed Image



10. Image Rotation, Scaling, Translation and Intensity Interpolation (10%) (a) Write a computer program capable of rotating, scaling, and translating an image by specified degree, ratio, and pixels. The rotation degree, scaling ratio, and translating pixels need to be variable inputs to your program.

```
1 import cv2
2 import numpy as np
3 import matplotlib.pyplot as plt
4
5 def transform_image(image_path, rotation_degree, scaling_ratio, translation_pixels):
6     # Read the image
7     image = cv2.imread(image_path)
8
9     # Get image dimensions
10    height, width = image.shape[:2]
11
12    # Calculate the rotation center
13    center = (width // 2, height // 2)
14
15    # Define the rotation matrix
16    rotation_matrix = cv2.getRotationMatrix2D(center, rotation_degree, scaling_ratio)
17
18    # Perform the rotation
19    rotated_image = cv2.warpAffine(image, rotation_matrix, (width, height))
20
21    # Define the translation matrix
22    translation_matrix = np.float32([[1, 0, translation_pixels[0]], [0, 1, translation_pixels[1]]])
23
24    # Perform the translation
25    translated_image = cv2.warpAffine(rotated_image, translation_matrix, (width, height))
26
27    # Display the original and transformed images
28    plt.figure(figsize=(10, 5))
29    plt.subplot(1, 2, 1)
30    plt.imshow(cv2.cvtColor(image, cv2.COLOR_BGR2RGB))
31    plt.title("Original Image")
32    plt.axis("off")
33
34    plt.subplot(1, 2, 2)
35    plt.imshow(cv2.cvtColor(translated_image, cv2.COLOR_BGR2RGB))
36    plt.title("Transformed Image")
37    plt.axis("off")
38
39    plt.tight_layout()
40    plt.show()
41
42
43 image_path = "/content/Lena.png"
44
45 # Specify the rotation degree, scaling ratio, and translation pixels
46 rotation_degree = 45
47 scaling_ratio = 1.5
48 translation_pixels = (20, 20)
49
50 # Apply the transformations to the image
51 transform_image(image_path, rotation_degree, scaling_ratio, translation_pixels)
```



(b) Download Fig. 2.36 (a) from the course web site and rotate the image  $23^{\circ}$  clockwise, scale it to  $2/3$  of original size, and shift it by 18 and 22 pixels in x and y directions, respectively. Show the results using three interpolation approaches mentioned in the textbook. Please also zoom in the results to compare the differences as shown in Figs. 2.36 (b) – (d).

```

1 import cv2
2 import numpy as np
3 import matplotlib.pyplot as plt
4
5 def transform_image(image_path, rotation_degree, scaling_ratio, translation_pixels):
6     # Read the image
7     image = cv2.imread(image_path)
8
9     # Get image dimensions
10    height, width = image.shape[:2]
11
12    # Calculate the rotation center
13    center = (width // 2, height // 2)
14
15    # Define the rotation matrix
16    rotation_matrix = cv2.getRotationMatrix2D(center, rotation_degree, scaling_ratio)
17
18    # Perform the rotation
19    rotated_image = cv2.warpAffine(image, rotation_matrix, (width, height))
20
21    # Define the translation matrix
22    translation_matrix = np.float32([[1, 0, translation_pixels[0]], [0, 1, translation_pixels[1]]])
23
24    # Perform the translation
25    translated_image = cv2.warpAffine(rotated_image, translation_matrix, (width, height))

```

```

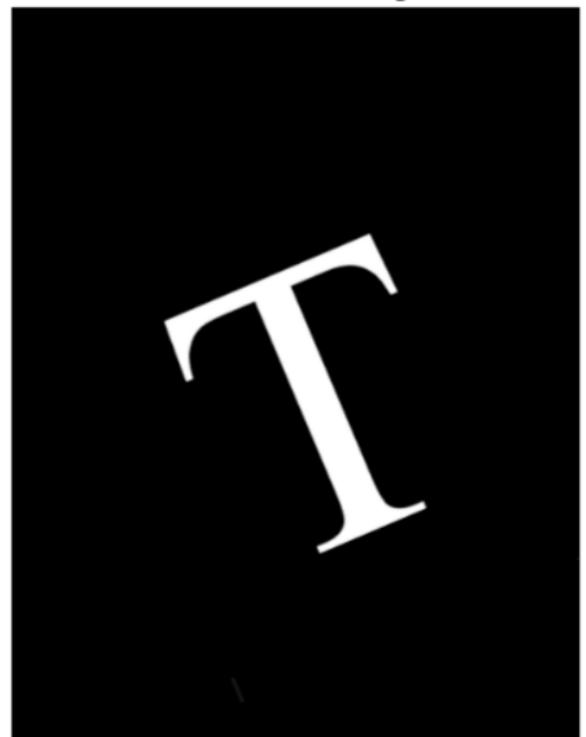
27 # Display the original and transformed images
28 plt.figure(figsize=(10, 5))
29 plt.subplot(1, 2, 1)
30 plt.imshow(cv2.cvtColor(image, cv2.COLOR_BGR2RGB))
31 plt.title("Original Image")
32 plt.axis("off")
33
34 plt.subplot(1, 2, 2)
35 plt.imshow(cv2.cvtColor(translated_image, cv2.COLOR_BGR2RGB))
36 plt.title("Transformed Image")
37 plt.axis("off")
38
39 plt.tight_layout()
40 plt.show()
41
42
43 image_path = "/content/Fig0236(a) (letter_T).tif"
44
45 # Specify the rotation degree, scaling ratio, and translation pixels
46 rotation_degree = 23
47 scaling_ratio = 2/3
48 translation_pixels = (18, 22)
49
50 # Apply the transformations to the image
51 transform_image(image_path, rotation_degree, scaling_ratio, translation_pixels)

```

Original Image



Transformed Image



下一頁使用課本介紹的三種內插法進行比較

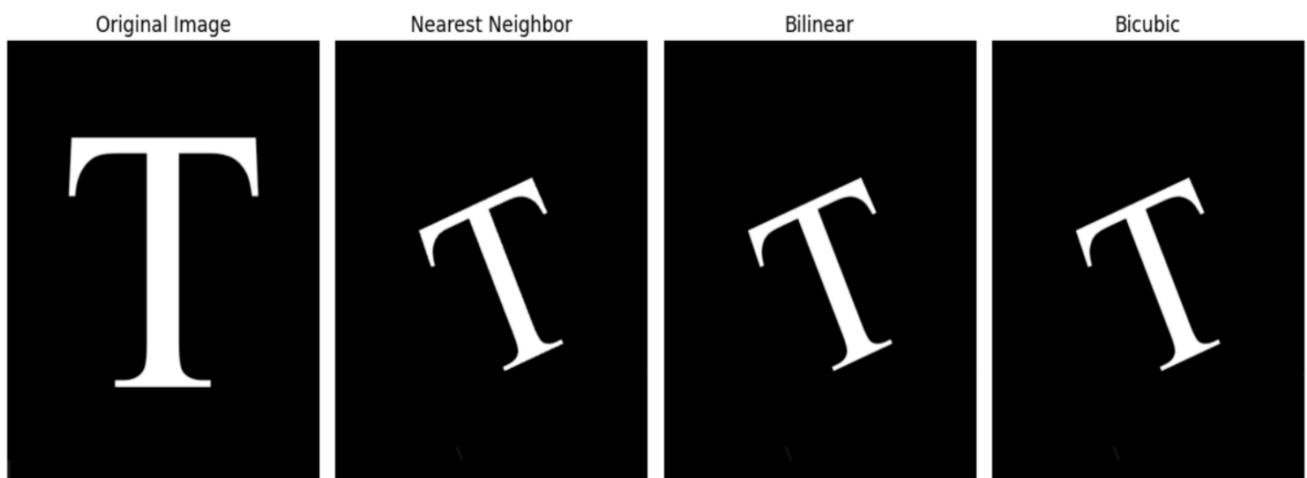
```
1 import cv2
2 import numpy as np
3 import matplotlib.pyplot as plt
4
5 def transform_image(image_path, rotation_degree, scaling_ratio, translation_pixels, interpolation):
6     # Read the image
7     image = cv2.imread(image_path)
8
9     # Get image dimensions
10    height, width = image.shape[:2]
11
12    # Calculate the rotation center
13    center = (width // 2, height // 2)
14
15    # Define the rotation matrix
16    rotation_matrix = cv2.getRotationMatrix2D(center, rotation_degree, scaling_ratio)
17
18    # Perform the rotation
19    rotated_image = cv2.warpAffine(image, rotation_matrix, (width, height), flags=interpolation)
20
21    # Define the translation matrix
22    translation_matrix = np.float32([[1, 0, translation_pixels[0]], [0, 1, translation_pixels[1]]])
23
24    # Perform the translation
25    translated_image = cv2.warpAffine(rotated_image, translation_matrix, (width, height), flags=interpolation)
26
27    return translated_image
28
```

```
29 # Specify the image file path
30 image_path = "/content/Fig0236(a)(letter_T).tif"
31
32 # Specify the rotation degree, scaling ratio, and translation pixels
33 rotation_degree = 23
34 scaling_ratio = 2/3
35 translation_pixels = (18,22)
36
37 # Apply the transformations to the image using different interpolation methods
38 nearest_neighbor_image = transform_image(image_path, rotation_degree, scaling_ratio, translation_pixels, cv2.INTER_NEAREST)
39 bilinear_image = transform_image(image_path, rotation_degree, scaling_ratio, translation_pixels, cv2.INTER_LINEAR)
40 bicubic_image = transform_image(image_path, rotation_degree, scaling_ratio, translation_pixels, cv2.INTER_CUBIC)
41
42 # Display the images
43 plt.figure(figsize=(12, 4))
```

```

37 # Apply the transformations to the image using different interpolation methods
38 nearest_neighbor_image = transform_image(image_path, rotation_degree, scaling_ratio, translation_pixels, cv2.INTER_NEAREST)
39 bilinear_image = transform_image(image_path, rotation_degree, scaling_ratio, translation_pixels, cv2.INTER_LINEAR)
40 bicubic_image = transform_image(image_path, rotation_degree, scaling_ratio, translation_pixels, cv2.INTER_CUBIC)
41
42 # Display the images
43 plt.figure(figsize=(12, 4))
44
45 plt.subplot(1, 4, 1)
46 plt.imshow(cv2.cvtColor(cv2.imread(image_path), cv2.COLOR_BGR2RGB))
47 plt.title("Original Image")
48 plt.axis(["off"])
49
50 plt.subplot(1, 4, 2)
51 plt.imshow(cv2.cvtColor(nearest_neighbor_image, cv2.COLOR_BGR2RGB))
52 plt.title("Nearest Neighbor")
53 plt.axis("off")
54
55 plt.subplot(1, 4, 3)
56 plt.imshow(cv2.cvtColor(bilinear_image, cv2.COLOR_BGR2RGB))
57 plt.title("Bilinear")
58 plt.axis("off")
59
60 plt.subplot(1, 4, 4)
61 plt.imshow(cv2.cvtColor(bicubic_image, cv2.COLOR_BGR2RGB))
62 plt.title("Bicubic")
63 plt.axis("off")
64
65 plt.tight_layout()
66 plt.show()

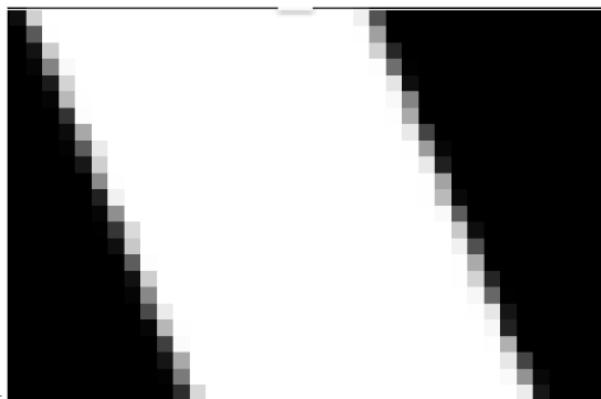
```



比較三者邊緣細節差異：

1) Nearest Neighbor:

✓ 比較三者邊緣細節



Nearest Neighbor:

2) Bilinear:



Bilinear:

3) Bicubic:



Bicubic: