

# experimento 5: 4o run 3 - 16fb0897c5

## USER

A base de dados anexada no arquivo dados\_50\_50.csv possui quatro variáveis: IDENTIFICADOR, CARGO, PERCENT\_PRI E DISTANCE\_KM. A primeira variável é o código que identifica o funcionário, a segunda apresenta os códigos dos cargos, a terceira é um índice que varia de 0 a 1, sendo o 0 o melhor e, por fim, a última variável é a distância em KM entre o funcionário e o cargo que ele poderá assumir, ou seja, quanto maior a distância, pior. Gostaria que me propusesse uma metodologia para solucionar meu problema de alocação de forma a minimizar o PERCENT\_PRI ou a DISTANCE\_KM ou os dois juntos. Determine e execute o código para solucionar o problema e indique o custo total minimizado.

## BOT

To solve the problem of allocating employees to positions while minimizing **PERCENT\_PRI**, **DISTANCE\_KM**, or both together, we can model this as an **assignment problem**. The assignment problem is a type of optimization problem where we aim to assign resources (employees) to tasks (positions) in a way that minimizes the total cost.

Here's a step-by-step methodology to solve the problem:

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### ### Step 1: Understand the Problem

- **Objective**: Minimize the total cost of allocation.
  - Cost can be based on:
    1. **PERCENT\_PRI** (priority index).
    2. **DISTANCE\_KM** (distance between employee and position).
    3. A **weighted combination** of both (e.g.,  $w_1 * \text{PERCENT\_PRI} + w_2 * \text{DISTANCE\_KM}$ ).
- **Constraints**:
  - Each employee can be assigned to only one position.
  - Each position can be assigned to only one employee.

This is a classic **linear assignment problem** that can be solved using optimization techniques like the **Hungarian algorithm** or linear programming.

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### ### Step 2: Formulate the Problem

1. **Decision Variables**:
  - Let  $x[i, j]$  be a binary variable:
    - $x[i, j] = 1$  if employee  $i$  is assigned to position  $j$ .
    - $x[i, j] = 0$  otherwise.
2. **Objective Function**:
  - Minimize the total cost:
    - If minimizing **PERCENT\_PRI**:  $\text{minimize } \sum(i, j) \text{ PERCENT\_PRI}[i, j] * x[i, j]$ .
    - If minimizing **DISTANCE\_KM**:  $\text{minimize } \sum(i, j) \text{ DISTANCE\_KM}[i, j] * x[i, j]$ .
    - If minimizing both:  $\text{minimize } \sum(i, j) (w_1 * \text{PERCENT\_PRI}[i, j] + w_2 * \text{DISTANCE\_KM}[i, j]) * x[i, j]$ .
3. **Constraints**:
  - Each employee is assigned to exactly one position:  $\sum(j) x[i, j] = 1$  for all  $i$ .
  - Each position is assigned to exactly one employee:  $\sum(i) x[i, j] = 1$  for all  $j$ .

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### ### Step 3: Solve the Problem

We will use Python and the `scipy.optimize.linear_sum_assignment` function, which implements the Hungarian algorithm to solve the assignment problem efficiently.

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### ### Step 4: Implement the Solution

Below is the Python code to solve the problem:

```

```python
import pandas as pd
import numpy as np
from scipy.optimize import linear_sum_assignment

# Step 1: Load the data
file_path = "dados_50_50.csv" # Replace with the correct file path
data = pd.read_csv(file_path, sep=";")

# Step 2: Prepare the cost matrices
# Convert PERCENT_PRI and DISTANCE_KM to numeric (replace commas with dots for decimals)
data['PERCENT_PRI'] = data['PERCENT_PRI'].str.replace(',', '.').astype(float)
data['DISTANCE_KM'] = data['DISTANCE_KM'].str.replace(',', '.').astype(float)

# Pivot the data to create cost matrices
employees = data['IDENTIFICADOR'].unique()
positions = data['CARGO'].unique()

# Create cost matrices for PERCENT_PRI and DISTANCE_KM
cost_percent_pri = data.pivot(index='IDENTIFICADOR', columns='CARGO', values='PERCENT_PRI').to_numpy()
cost_distance_km = data.pivot(index='IDENTIFICADOR', columns='CARGO', values='DISTANCE_KM').to_numpy()

# Normalize the cost matrices (optional, for combined optimization)
cost_percent_pri /= cost_percent_pri.max()
cost_distance_km /= cost_distance_km.max()

# Combine the costs (weighted sum)
w1, w2 = 0.5, 0.5 # Weights for PERCENT_PRI and DISTANCE_KM
combined_cost = w1 * cost_percent_pri + w2 * cost_distance_km

# Step 3: Solve the assignment problem
row_ind, col_ind = linear_sum_assignment(combined_cost)

# Step 4: Calculate the total minimized cost
total_cost = combined_cost[row_ind, col_ind].sum()

# Step 5: Display the results
assignments = pd.DataFrame({
    "Employee": employees[row_ind],
    "Position": positions[col_ind],
    "Cost": combined_cost[row_ind, col_ind]
})

print("Optimal Assignments:")
print(assignments)
print(f"Total Minimized Cost: {total_cost}")
```

```

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### ### \*\*Step 5: Explanation of the Code\*\*

#### 1. \*\*Data Preparation\*\*:

- The data is loaded and cleaned (e.g., converting `PERCENT\_PRI` and `DISTANCE\_KM` to numeric).
- Cost matrices are created for `PERCENT\_PRI` and `DISTANCE\_KM`.

#### 2. \*\*Cost Combination\*\*:

- If both criteria are to be minimized, a weighted combination of the two matrices is created.

#### 3. \*\*Optimization\*\*:

- The `linear\_sum\_assignment` function is used to find the optimal assignment that minimizes the total cost.

#### 4. \*\*Results\*\*:

- The optimal assignments and the total minimized cost are displayed.

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### ### \*\*Step 6: Output\*\*

The output will include:

1. A table showing the optimal assignment of employees to positions and the associated cost for each assignment.
2. The total minimized cost.

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### \*\*Step 7: Next Steps\*\*

- Adjust the weights `w1` and `w2` to prioritize either **PERCENT\_PRI** or **DISTANCE\_KM**.
- Analyze the results to ensure the solution aligns with your business goals.

Let me know if you need further assistance!

Execution Result:

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Optimal Assignments:

|    | Employee | Position | Cost     |
|----|----------|----------|----------|
| 0  | 1        | 14       | 0.609065 |
| 1  | 2        | 2        | 0.658924 |
| 2  | 3        | 3        | 0.769260 |
| 3  | 4        | 5        | 0.439027 |
| 4  | 5        | 55       | 0.420782 |
| 5  | 6        | 17       | 0.931846 |
| 6  | 7        | 56       | 0.512248 |
| 7  | 8        | 6        | 0.695864 |
| 8  | 9        | 57       | 0.511853 |
| 9  | 10       | 7        | 0.962081 |
| 10 | 11       | 70       | 0.392220 |
| 11 | 12       | 9        | 0.043284 |
| 12 | 13       | 10       | 0.341080 |
| 13 | 14       | 11       | 0.907152 |
| 14 | 15       | 58       | 0.531797 |
| 15 | 16       | 59       | 0.724956 |
| 16 | 17       | 60       | 0.668815 |
| 17 | 18       | 12       | 0.832347 |
| 18 | 19       | 71       | 0.679455 |
| 19 | 20       | 18       | 0.622527 |
| 20 | 21       | 61       | 0.726129 |
| 21 | 22       | 15       | 0.715622 |
| 22 | 23       | 16       | 0.948931 |
| 23 | 24       | 20       | 0.332597 |
| 24 | 25       | 22       | 0.529328 |
| 25 | 26       | 62       | 0.042555 |
| 26 | 27       | 19       | 0.545412 |
| 27 | 28       | 25       | 0.764711 |
| 28 | 29       | 21       | 0.673072 |
| 29 | 30       | 29       | 0.532049 |
| 30 | 31       | 23       | 0.507430 |
| 31 | 32       | 63       | 0.658180 |
| 32 | 33       | 64       | 0.611315 |
| 33 | 34       | 24       | 0.522967 |
| 34 | 35       | 65       | 0.668815 |
| 35 | 36       | 73       | 0.593167 |
| 36 | 37       | 66       | 0.689401 |
| 37 | 38       | 26       | 0.313706 |
| 38 | 39       | 27       | 0.647186 |
| 39 | 40       | 67       | 0.647868 |
| 40 | 41       | 28       | 0.521633 |
| 41 | 42       | 69       | 0.348171 |
| 42 | 43       | 68       | 0.479090 |
| 43 | 44       | 8        | 0.502807 |
| 44 | 45       | 13       | 0.589484 |
| 45 | 46       | 30       | 0.789665 |
| 46 | 47       | 1        | 0.508048 |
| 47 | 48       | 72       | 0.658180 |
| 48 | 49       | 4        | 0.423548 |
| 49 | 50       | 74       | 0.562435 |

Total Minimized Cost: 29.308085556184693

