Assignment is below at the bottom

```
Video 13.1 https://www.youtube.com/watch?v=kIGHE7Cfe1s
```

Video 13.2 https://www.youtube.com/watch?v=Rm9bJcDd1KU

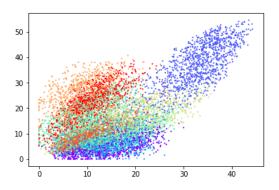
Video 13.3 https://youtu.be/6HjZk-3LsjE

```
In [3]: from keras.callbacks import TensorBoard
         from keras.layers import Input, Dense
         from keras.models import Model
         from keras.datasets import mnist
         import numpy as np
         (xtrain, ytrain), (xtest, ytest) = mnist.load_data()
         xtrain = xtrain.astype('float32') / 255.
         xtest = xtest.astype('float32') / 255.
         xtrain = xtrain.reshape((len(xtrain), np.prod(xtrain.shape[1:])))
         xtest = xtest.reshape((len(xtest), np.prod(xtest.shape[1:])))
         xtrain.shape, xtest.shape
Out[3]: ((60000, 784), (10000, 784))
In [18]: # this is the size of our encoded representations
         encoding_dim = 4 # 32 floats -> compression of factor 24.5, assuming the input is 784 floats
         # this is our input placeholder
         x = input_img = Input(shape=(784,))
         # "encoded" is the encoded representation of the input
         x = Dense(256, activation='relu')(x)
         x = Dense(128, activation='relu')(x)
         encoded = Dense(encoding_dim, activation='relu')(x)
         # "decoded" is the lossy reconstruction of the input
         x = Dense(128, activation='relu')(encoded)
         x = Dense(256, activation='relu')(x)
         decoded = Dense(784, activation='sigmoid')(x)
         # this model maps an input to its reconstruction
         autoencoder = Model(input_img, decoded)
         encoder = Model(input_img, encoded)
         # create a placeholder for an encoded (32-dimensional) input
         encoded_input = Input(shape=(encoding_dim,))
         # retrieve the last layer of the autoencoder model
         dcd1 = autoencoder.layers[-1]
         dcd2 = autoencoder.layers[-2]
         dcd3 = autoencoder.layers[-3]
         # create the decoder model
         decoder = Model(encoded_input, dcd1(dcd2(dcd3(encoded_input))))
In [19]: autoencoder.compile(optimizer='adam', loss='binary_crossentropy')
In [21]: autoencoder.fit(xtrain, xtrain,
                         batch size=256,
                         shuffle=True.
                        validation_data=(xtest, xtest))
                        #callbacks=[TensorBoard(log_dir='/tmp/autoencoder')])
         Epoch 1/5
         235/235 [===========] - 8s 20ms/step - loss: 0.2575 - val_loss: 0.1977
         Epoch 2/5
         235/235 [================== ] - 5s 20ms/step - loss: 0.1830 - val_loss: 0.1737
         Epoch 3/5
         235/235 [================== ] - 3s 13ms/step - loss: 0.1706 - val_loss: 0.1671
         Epoch 4/5
         235/235 [============] - 3s 13ms/step - loss: 0.1655 - val_loss: 0.1633
         Epoch 5/5
         235/235 [============ ] - 3s 13ms/step - loss: 0.1622 - val loss: 0.1612
Out[21]: <keras.callbacks.History at 0x1c19c99e0a0>
In [38]: encoded_imgs
```

```
Out[38]: array([[11.943697 , 9.005527 , 12.027234 , 32.89881 ],
                [23.76052 , 13.926956 , 5.6552634, 8.942506 ],
               [35.62965 , 34.729908 , 24.666973 , 41.5047 ],
               [ 5.3135986, 11.108302 , 14.398285 , 17.106884 ],
               [ 4.376413 , 19.419018 , 15.854642 , 11.992302 ],
               [ 7.41167 , 18.699078 , 30.420742 , 11.0364065]], dtype=float32)
In [52]: noise = np.random.normal(20,4, (4,4))
         noise_preds = decoder.predict(noise)
In [55]: plt.imshow(noise_preds[1].reshape(28,28))
Out[55]: <matplotlib.image.AxesImage at 0x13bf35780>
          5
         10
         15
         20
         25
                     10
                          15
                                20
In [41]: np.max(encoded_imgs)
Out[41]: 54.59457
In [32]: encoded_imgs = encoder.predict(xtest)
         decoded_imgs = decoder.predict(encoded_imgs)
         \textbf{import} \ \texttt{matplotlib.pyplot} \ \textbf{as} \ \texttt{plt}
         n = 20 # how many digits we will display
         plt.figure(figsize=(40, 4))
         for i in range(n):
            # display original
            ax = plt.subplot(2, n, i + 1)
            plt.imshow(xtest[i].reshape(28, 28))
            plt.gray()
            ax.get_xaxis().set_visible(False)
            ax.get_yaxis().set_visible(False)
            # display reconstruction
             ax = plt.subplot(2, n, i + 1 + n)
            plt.imshow(decoded_imgs[i].reshape(28, 28))
             plt.gray()
             \verb"ax.get_xaxis().set_visible(False)"
             ax.get_yaxis().set_visible(False)
         72104149590690159734
                                        19949069015973
In [33]: encoded imgs
Out[33]: array([[11.943697 , 9.005527 , 12.027234 , 32.89881 ],
               [23.76052 , 13.926956 , 5.6552634, 8.942506 ],
[35.62965 , 34.729908 , 24.666973 , 41.5047 ],
               [ 5.3135986, 11.108302 , 14.398285 , 17.106884 ],
               [ 4.376413 , 19.419018 , 15.854642 , 11.992302 ],
               [ 7.41167 , 18.699078 , 30.420742 , 11.0364065]], dtype=float32)
In [26]: %matplotlib inline
In [34]: plt.scatter(encoded_imgs[:,1], encoded_imgs[:,0], s=1, c=ytest, cmap='rainbow')
Out[34]: <matplotlib.collections.PathCollection at 0x13c081978>
```

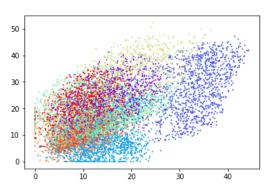
```
50
          40
          30
          20
          10
Out[35]: cmatplotlib.collections.PathCollection at 0x13b695e10>
```

```
In [35]: plt.scatter(encoded_imgs[:,1], encoded_imgs[:,3], s=1, c=ytest, cmap='rainbow')
```



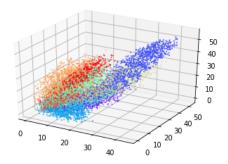
```
In [36]: plt.scatter(encoded_imgs[:,1], encoded_imgs[:,2], s=1, c=ytest, cmap='rainbow')
```

Out[36]: cmatplotlib.collections.PathCollection at 0x13b6eaf60>



```
In [37]: from mpl_toolkits.mplot3d import Axes3D
          fig = plt.figure()
ax = fig.add_subplot(111, projection='3d')
          ax.scatter(encoded_imgs[:,1], encoded_imgs[:,2], encoded_imgs[:,3], c=ytest, cmap='rainbow', s=1)
```

Out[37]: cmpl_toolkits.mplot3d.art3d.Path3DCollection at 0x13c0e7da0>



Assignment

1. change the encoding_dim through various values (range(2,18,2) and save the loss you can get. Plot the 8 pairs of dimensions vs loss on a scatter plot

```
In [23]: # dimensions list is out of order so that the second part of the assignment can be completed without recreating the model
         dimensions = [2,4,6,10,12,14,16,8]
In [7]: losses = []
         for encoding_dim in dimensions:
             print(encoding_dim)
             x = input_img = Input(shape=(784,))
             # "encoded" is the encoded representation of the input
             x = Dense(256, activation='relu')(x)
             x = Dense(128, activation='relu')(x)
             encoded = Dense(encoding_dim, activation='relu')(x)
             # "decoded" is the lossy reconstruction of the input
             x = Dense(128, activation='relu')(encoded)
             x = Dense(256, activation='relu')(x)
             decoded = Dense(784, activation='sigmoid')(x)
             # this model maps an input to its reconstruction
             autoencoder = Model(input_img, decoded)
             encoder = Model(input_img, encoded)
             # create a placeholder for an encoded (32-dimensional) input
             encoded_input = Input(shape=(encoding_dim,))
             # retrieve the last layer of the autoencoder model
             dcd1 = autoencoder.layers[-1]
             dcd2 = autoencoder.layers[-2]
             dcd3 = autoencoder.layers[-3]
             # create the decoder model
             decoder = Model(encoded_input, dcd1(dcd2(dcd3(encoded_input))))
             autoencoder.compile(optimizer='adam', loss='binary_crossentropy')
             autoencoder.fit(xtrain, xtrain,
                             epochs=20,
                             batch size=256.
                             shuffle=True,
                             validation_data=(xtest, xtest),
                             callbacks=[TensorBoard(log dir='/tmp/autoencoder')]
             loss = autoencoder.evaluate(xtest,xtest,verbose=0)
             losses.append(loss)
```

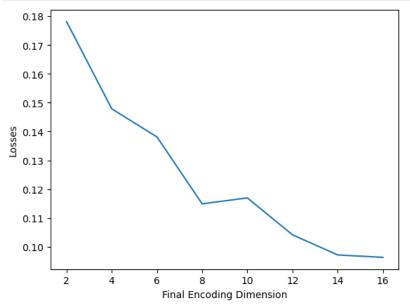
```
2
Epoch 1/20
235/235 [================= ] - 3s 11ms/step - loss: 0.2838 - val_loss: 0.2491
Epoch 2/20
Epoch 3/20
235/235 [==
     Epoch 4/20
235/235 [============ ] - 2s 9ms/step - loss: 0.2029 - val loss: 0.1987
Epoch 5/20
Epoch 6/20
235/235 [============== ] - 2s 9ms/step - loss: 0.1917 - val_loss: 0.1902
Epoch 7/20
Epoch 8/20
Epoch 9/20
Epoch 10/20
Epoch 11/20
Epoch 12/20
Epoch 13/20
235/235 [============== ] - 2s 9ms/step - loss: 0.1813 - val_loss: 0.1816
Epoch 14/20
Epoch 15/20
Epoch 16/20
Epoch 17/20
Epoch 18/20
Epoch 19/20
Epoch 20/20
Epoch 1/20
235/235 [===
      Epoch 2/20
Epoch 3/20
Epoch 4/20
235/235 [===
        =========] - 2s 8ms/step - loss: 0.1654 - val_loss: 0.1635
Epoch 5/20
Epoch 6/20
Epoch 7/20
235/235 [============ ] - 2s 10ms/step - loss: 0.1580 - val loss: 0.1574
Epoch 8/20
235/235 [============] - 2s 10ms/step - loss: 0.1564 - val_loss: 0.1564
Epoch 9/20
235/235 [=============] - 2s 10ms/step - loss: 0.1551 - val_loss: 0.1548
Epoch 10/20
235/235 [===========] - 2s 10ms/step - loss: 0.1540 - val_loss: 0.1540
Epoch 11/20
Epoch 12/20
Epoch 13/20
Epoch 14/20
235/235 [============ ] - 2s 10ms/step - loss: 0.1503 - val loss: 0.1508
Epoch 15/20
235/235 [=================== ] - 2s 11ms/step - loss: 0.1496 - val_loss: 0.1503
Epoch 16/20
235/235 [================ ] - 2s 10ms/step - loss: 0.1489 - val_loss: 0.1496
Epoch 17/20
235/235 [============] - 2s 10ms/step - loss: 0.1482 - val_loss: 0.1492
Epoch 18/20
235/235 [============ ] - 2s 10ms/step - loss: 0.1475 - val loss: 0.1485
Epoch 19/20
235/235 [=============== ] - 2s 10ms/step - loss: 0.1470 - val loss: 0.1484
Epoch 20/20
Epoch 1/20
235/235 [============= ] - 4s 11ms/step - loss: 0.2616 - val loss: 0.2074
Epoch 2/20
```

```
235/235 [============ ] - 2s 10ms/step - loss: 0.1779 - val loss: 0.1633
Epoch 3/20
235/235 [================== ] - 3s 11ms/step - loss: 0.1603 - val_loss: 0.1568
Epoch 4/20
235/235 [================ ] - 2s 10ms/step - loss: 0.1549 - val_loss: 0.1526
Epoch 5/20
235/235 [============] - 2s 10ms/step - loss: 0.1514 - val_loss: 0.1504
Epoch 6/20
235/235 [============ ] - 2s 10ms/step - loss: 0.1491 - val loss: 0.1483
Epoch 7/20
235/235 [=============] - 3s 11ms/step - loss: 0.1473 - val loss: 0.1469
Epoch 8/20
235/235 [============] - 2s 10ms/step - loss: 0.1459 - val_loss: 0.1454
Epoch 9/20
Epoch 10/20
Epoch 11/20
235/235 [===========] - 2s 10ms/step - loss: 0.1426 - val_loss: 0.1426
Epoch 12/20
235/235 [============ ] - 2s 10ms/step - loss: 0.1418 - val loss: 0.1419
Epoch 13/20
Epoch 14/20
235/235 [===========] - 2s 10ms/step - loss: 0.1403 - val_loss: 0.1408
Epoch 15/20
235/235 [=============] - 2s 10ms/step - loss: 0.1397 - val_loss: 0.1401
Epoch 16/20
235/235 [============] - 2s 10ms/step - loss: 0.1391 - val_loss: 0.1395
Epoch 17/20
235/235 [===========] - 2s 10ms/step - loss: 0.1385 - val_loss: 0.1393
Epoch 18/20
235/235 [=================== ] - 2s 10ms/step - loss: 0.1379 - val_loss: 0.1386
Epoch 19/20
235/235 [====
       Epoch 20/20
235/235 [=================== ] - 2s 10ms/step - loss: 0.1369 - val_loss: 0.1381
10
Epoch 1/20
235/235 [===========] - 3s 11ms/step - loss: 0.2491 - val_loss: 0.1786
Epoch 2/20
235/235 [============] - 2s 10ms/step - loss: 0.1611 - val_loss: 0.1497
Enoch 3/20
235/235 [====
       Epoch 4/20
Epoch 5/20
235/235 [============= ] - 2s 9ms/step - loss: 0.1365 - val loss: 0.1340
Epoch 6/20
235/235 [===
          Epoch 7/20
Epoch 8/20
Epoch 9/20
235/235 [============= - 2s 9ms/step - loss: 0.1289 - val loss: 0.1282
Epoch 10/20
235/235 [============= ] - 2s 9ms/step - loss: 0.1277 - val_loss: 0.1269
Epoch 11/20
235/235 [============== ] - 2s 9ms/step - loss: 0.1264 - val_loss: 0.1251
Epoch 12/20
Epoch 13/20
Epoch 14/20
Epoch 15/20
Epoch 16/20
Epoch 17/20
Epoch 18/20
Epoch 19/20
235/235 [============] - 2s 10ms/step - loss: 0.1170 - val_loss: 0.1173
Epoch 20/20
12
Epoch 1/20
235/235 [================== ] - 4s 11ms/step - loss: 0.2305 - val_loss: 0.1603
Enoch 2/20
235/235 [==
       Epoch 3/20
Epoch 4/20
```

```
235/235 [============= ] - 2s 10ms/step - loss: 0.1317 - val loss: 0.1283
Epoch 5/20
Epoch 6/20
235/235 [=============== ] - 3s 11ms/step - loss: 0.1221 - val_loss: 0.1186
Epoch 7/20
235/235 [============] - 2s 10ms/step - loss: 0.1181 - val_loss: 0.1159
Epoch 8/20
235/235 [============ ] - 2s 9ms/step - loss: 0.1157 - val loss: 0.1137
Epoch 9/20
Epoch 10/20
235/235 [=============] - 2s 10ms/step - loss: 0.1123 - val_loss: 0.1113
Epoch 11/20
Epoch 12/20
Epoch 13/20
235/235 [===========] - 3s 12ms/step - loss: 0.1089 - val_loss: 0.1079
Epoch 14/20
235/235 [============ ] - 2s 10ms/step - loss: 0.1080 - val loss: 0.1074
Epoch 15/20
Epoch 16/20
235/235 [===========] - 3s 11ms/step - loss: 0.1065 - val_loss: 0.1064
Epoch 17/20
235/235 [============] - 2s 11ms/step - loss: 0.1059 - val_loss: 0.1058
Epoch 18/20
235/235 [============= ] - 2s 9ms/step - loss: 0.1052 - val_loss: 0.1049
Epoch 19/20
235/235 [===========] - 2s 10ms/step - loss: 0.1047 - val_loss: 0.1047
Epoch 20/20
14
Epoch 1/20
235/235 [============] - 3s 11ms/step - loss: 0.2317 - val_loss: 0.1588
Epoch 2/20
235/235 [============= ] - 2s 10ms/step - loss: 0.1453 - val loss: 0.1346
Epoch 3/20
Epoch 4/20
235/235 [============] - 2s 10ms/step - loss: 0.1211 - val_loss: 0.1167
Epoch 5/20
235/235 [====
       Epoch 6/20
Epoch 7/20
235/235 [============ ] - 2s 10ms/step - loss: 0.1094 - val loss: 0.1076
Epoch 8/20
235/235 [===
         =========] - 2s 10ms/step - loss: 0.1074 - val_loss: 0.1054
Epoch 9/20
235/235 [================ ] - 2s 10ms/step - loss: 0.1059 - val_loss: 0.1041
Epoch 10/20
Epoch 11/20
235/235 [============ ] - 2s 10ms/step - loss: 0.1033 - val loss: 0.1020
Epoch 12/20
235/235 [============] - 3s 11ms/step - loss: 0.1023 - val_loss: 0.1014
Epoch 13/20
235/235 [=============] - 2s 10ms/step - loss: 0.1015 - val_loss: 0.1006
Epoch 14/20
Epoch 15/20
Epoch 16/20
Epoch 17/20
235/235 [============= ] - 2s 9ms/step - loss: 0.0989 - val loss: 0.0985
Epoch 18/20
Epoch 19/20
235/235 [================== ] - 2s 10ms/step - loss: 0.0980 - val_loss: 0.0976
Epoch 20/20
Epoch 1/20
Epoch 2/20
Epoch 3/20
Enoch 4/20
235/235 [==
      Epoch 5/20
Epoch 6/20
```

```
235/235 [============ ] - 2s 10ms/step - loss: 0.1104 - val loss: 0.1080
     Epoch 7/20
     235/235 [================== ] - 2s 10ms/step - loss: 0.1078 - val_loss: 0.1057
     Epoch 8/20
     235/235 [===
               Epoch 9/20
     235/235 [====
              Epoch 10/20
     235/235 [============ ] - 2s 9ms/step - loss: 0.1026 - val loss: 0.1013
     Epoch 11/20
     235/235 [================= ] - 2s 11ms/step - loss: 0.1016 - val_loss: 0.1007
     Epoch 12/20
     Epoch 13/20
     235/235 [===
                Epoch 14/20
     Epoch 15/20
     235/235 [===========] - 2s 10ms/step - loss: 0.0985 - val_loss: 0.0981
     Epoch 16/20
     235/235 [============ ] - 2s 10ms/step - loss: 0.0980 - val loss: 0.0976
     Epoch 17/20
     235/235 [====
                 Epoch 18/20
     235/235 [===========] - 2s 10ms/step - loss: 0.0971 - val_loss: 0.0966
     Enoch 19/20
     235/235 [===
               Epoch 20/20
     235/235 [============] - 2s 10ms/step - loss: 0.0961 - val_loss: 0.0963
     8
     Epoch 1/20
     235/235 [===========] - 4s 12ms/step - loss: 0.2433 - val_loss: 0.1774
     Epoch 2/20
     235/235 [====
               Epoch 3/20
     235/235 [==
                Epoch 4/20
     235/235 [============ - 2s 9ms/step - loss: 0.1333 - val loss: 0.1306
     Epoch 5/20
     Epoch 6/20
     235/235 [=========== ] - 2s 9ms/step - loss: 0.1271 - val_loss: 0.1255
     Epoch 7/20
     235/235 [==
               Epoch 8/20
     Epoch 9/20
     235/235 [============ ] - 2s 10ms/step - loss: 0.1224 - val loss: 0.1214
     Epoch 10/20
     235/235 [===
                  =========] - 2s 11ms/step - loss: 0.1212 - val_loss: 0.1206
     Epoch 11/20
     235/235 [================ ] - 2s 10ms/step - loss: 0.1203 - val_loss: 0.1195
     Epoch 12/20
     235/235 [================== ] - 3s 11ms/step - loss: 0.1195 - val_loss: 0.1187
     Epoch 13/20
     235/235 [============ ] - 2s 11ms/step - loss: 0.1186 - val loss: 0.1181
     Epoch 14/20
     235/235 [============] - 2s 10ms/step - loss: 0.1180 - val_loss: 0.1177
     Epoch 15/20
     235/235 [============= ] - 2s 10ms/step - loss: 0.1174 - val loss: 0.1171
     Epoch 16/20
     235/235 [===========] - 2s 10ms/step - loss: 0.1167 - val_loss: 0.1166
     Epoch 17/20
     Epoch 18/20
     235/235 [====
                Epoch 19/20
     Epoch 20/20
     235/235 [============ ] - 2s 10ms/step - loss: 0.1148 - val loss: 0.1149
In [8]: losses
Out[8]: [0.17809730768203735,
      0.14785830676555634,
      0.1381126046180725.
      0.11696751415729523,
      0.10415196418762207,
      0.09717812389135361,
      0.09633705019950867
      0.11490143090486526]
In [25]: import matplotlib.pyplot as plt
     %matplotlib inline
     dimensions, losses = zip(*sorted(zip(dimensions, losses)))
```

```
plt.figure()
plt.plot(dimensions,losses)
plt.xlabel('Final Encoding Dimension')
plt.ylabel('Losses')
plt.show()
```



1. **After** training an autoencoder with encoding_dim=8, apply noise (like the previous assignment) to *only* the input of the trained autoencoder (not the output). The output images should be without noise.

Print a few noisy images along with the output images to show they don't have noise.

```
In [10]: noise = xtest + np.random.normal(0, .1, size=(10000, 784))
In [11]: encoded_imgs = encoder.predict(noise)
    decoded_imgs = decoder.predict(encoded_imgs)
        import matplotlib.pyplot as plt
        n = 20 # how many digits we will display
        plt.figure(figsize=(40, 4))
        for i in range(n):
            # display original
            ax = plt.subplot(2, n, i + 1)
            plt.imshow(noise[i].reshape(28, 28))
            plt.gray()
            ax.get_xaxis().set_visible(False)
            ax.get_yaxis().set_visible(False)
            # display reconstruction
            ax = plt.subplot(2, n, i + 1 + n)
            plt.imshow(decoded_imgs[i].reshape(28, 28))
            plt.gray()
            ax.get_xaxis().set_visible(False)
            ax.get_yaxis().set_visible(False)
        plt.show()
        313/313 [======== ] - 1s 3ms/step
                                             - 1s 1ms/step
                                                        590690159
                                                  9890690159
```