Fully Connected Neural Networks

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Outline

Learning Goals

- Fully Connected Neural Networks
 - Single-layer Network
 - Multi-layer Network

Summary



Learning Goals

Introduce fully connected neural networks

Learn how to compute the number of parameters of your model

Learn how to use dropout to avoid model overfitting

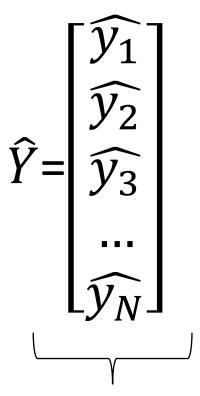


Notation

$$X = \begin{bmatrix} x_{11} & x_{12} & \dots & x_{1M} \\ x_{21} & x_{22} & \dots & x_{2M} \\ x_{31} & x_{32} & \dots & x_{3M} \\ \dots & \dots & \dots & \dots \\ x_{N1} & x_{N2} & \dots & x_{NM} \end{bmatrix}$$

$$Y = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ \dots \\ y_5 \end{bmatrix}$$

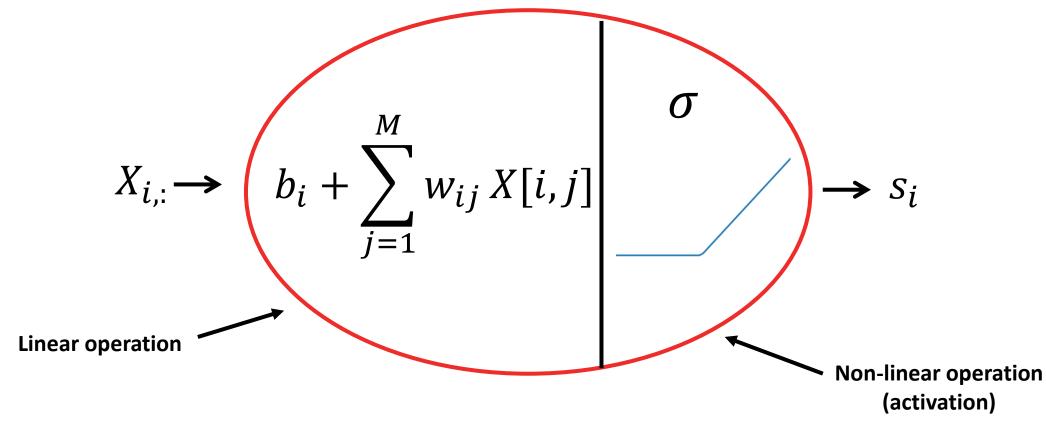
True Labels



Predicted Labels



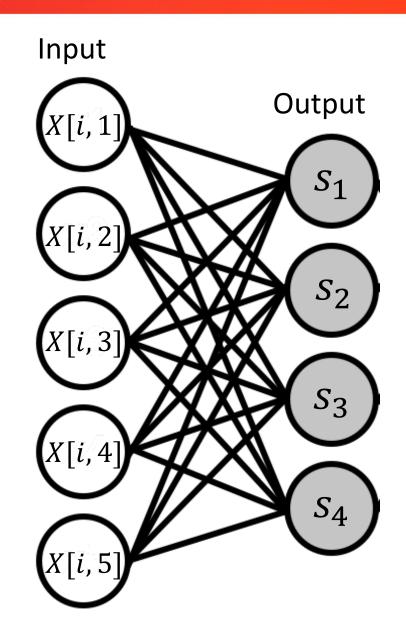
The Neuron Model



- b_i is the bias
- w_{ij} are the weights
- s_i is the output of the neuron
- σ is the activation function



Single-layer Fully Connected Neural Network



$$[S]_{C\times 1} = \sigma([W]_{C\times M}X_{i,:}^T + [B]_{C\times 1})$$
Matrix formulation

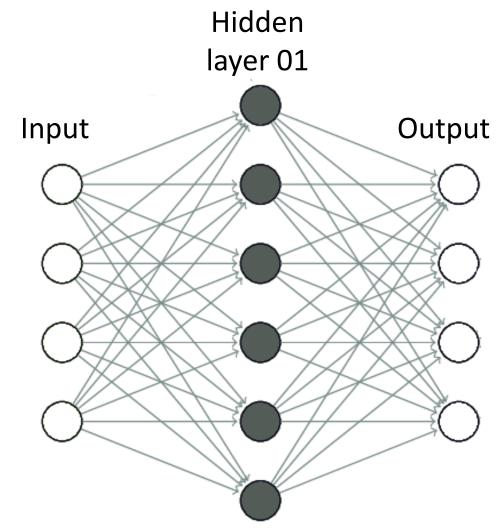
If the activation σ is the softmax function, then:

$$\hat{y} = \underset{\forall i}{\operatorname{argmax}}(s_i)$$

Number of parameters: C x
 (M+1) = 4 x 6 = 24



Multi-layer Fully Connected Neural Network



$$[S^{(1)}] = \sigma_1([W^{(1)}] X_{i,:}^T + [B^{(1)}])$$

$$[S^{(2)}] = \sigma_2([W^{(2)}] S^{(1)} + [B^{(2)}])$$

- Number of parameters:
 - First layer: $(4 + 1) \times 6 = 30$
 - Second layer: (6+1) x 4 = 28



Summary

 Fully connected neural networks alternate linear operations (matrix multiplication + bias term) and non-linear activations

 The number of parameters in each layer is given by the (number of inputs +1) x the number of outputs



Thank you!

