

The U-net Model

A Fully Convolutional Neural Network Model

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Outline

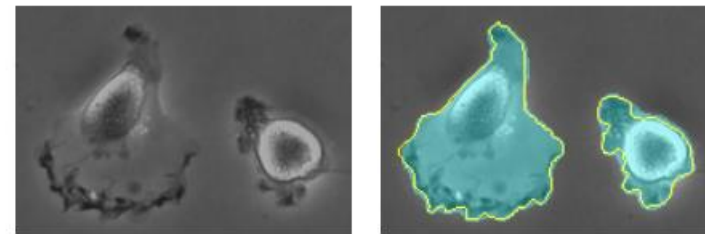
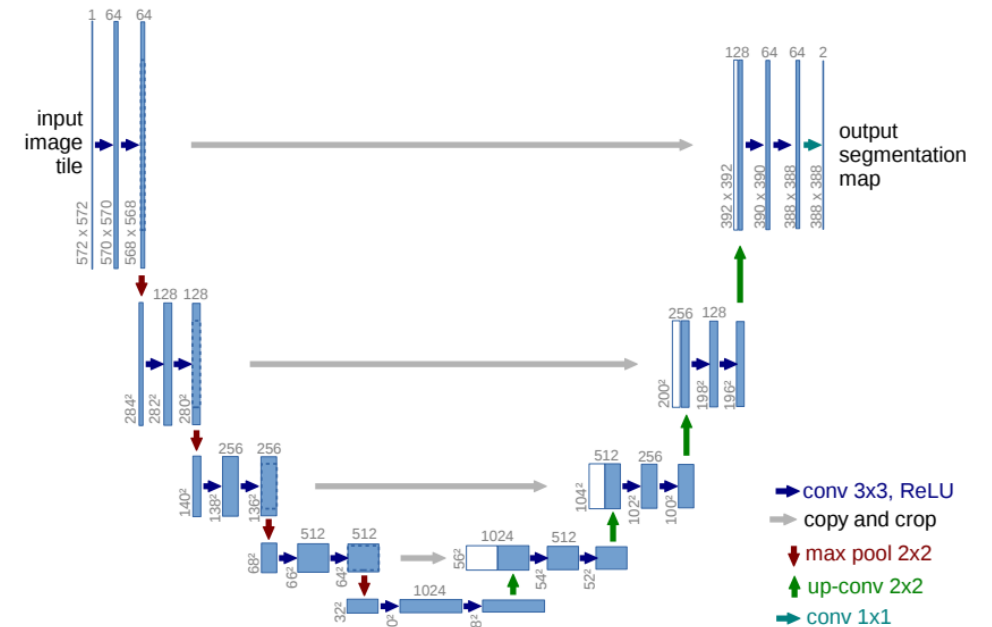
- Learning Goals
- The U-net Model
- Summary

Learning Goals

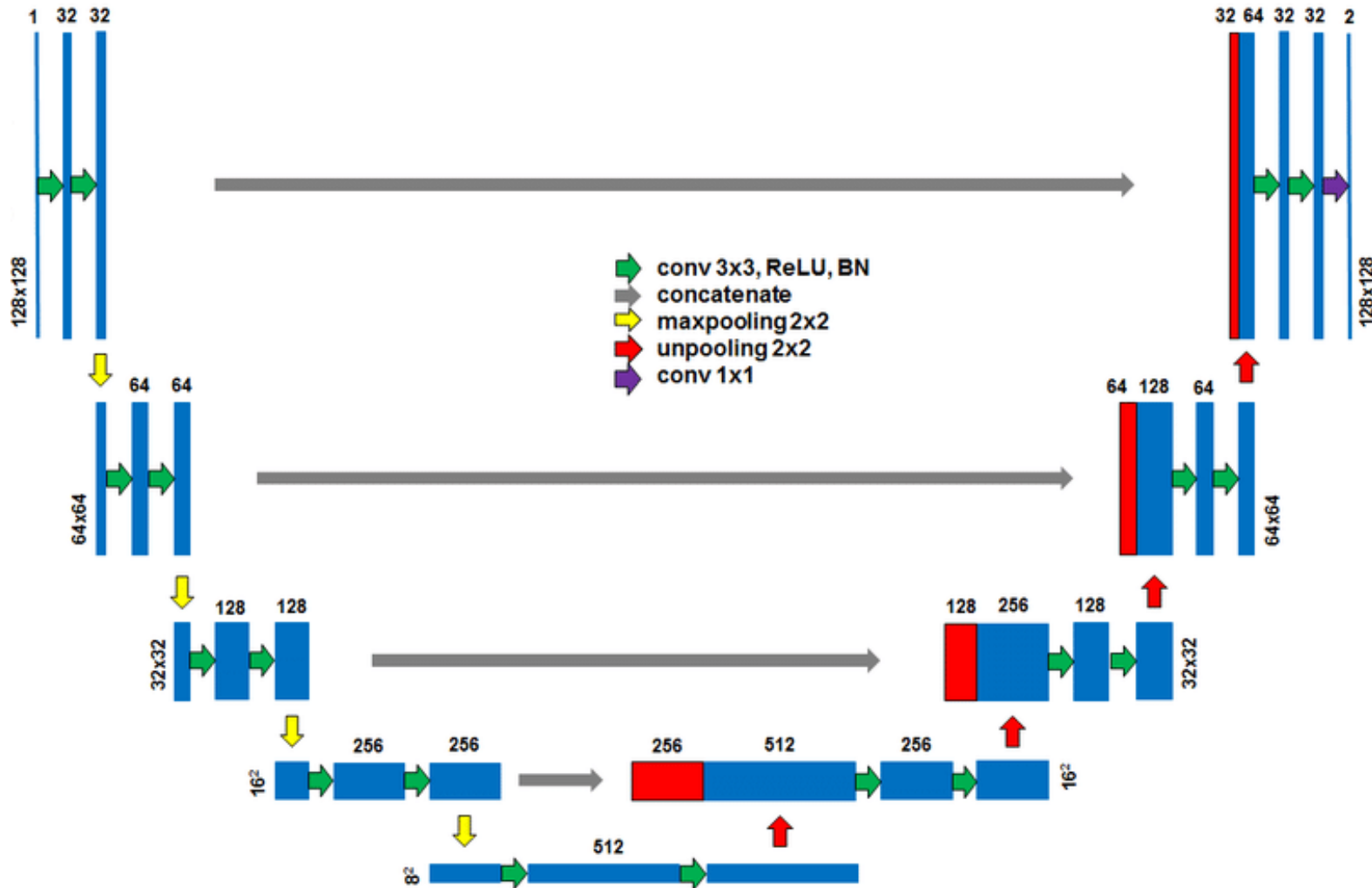
- Understand the U-net architecture and its building blocks
- Discuss potential applications of the U-net model

The U-net Model

- The U-net is a fully convolutional neural network (i.e., no fully connected layers)
- Initially proposed for biomedical image segmentation problems
- It maps an input of size N into an output also of size N (if the convolutions are padded)



The U-net Model



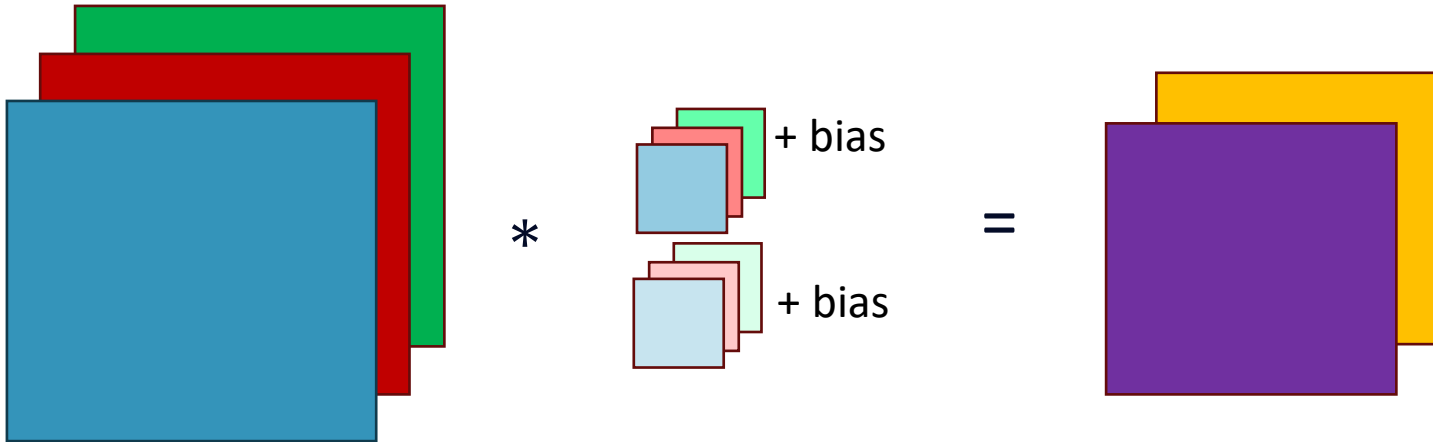
Number of parameters

For one layer:

params =

weights + biases =

[input maps x filter size x output maps] + output maps



Number of parameters

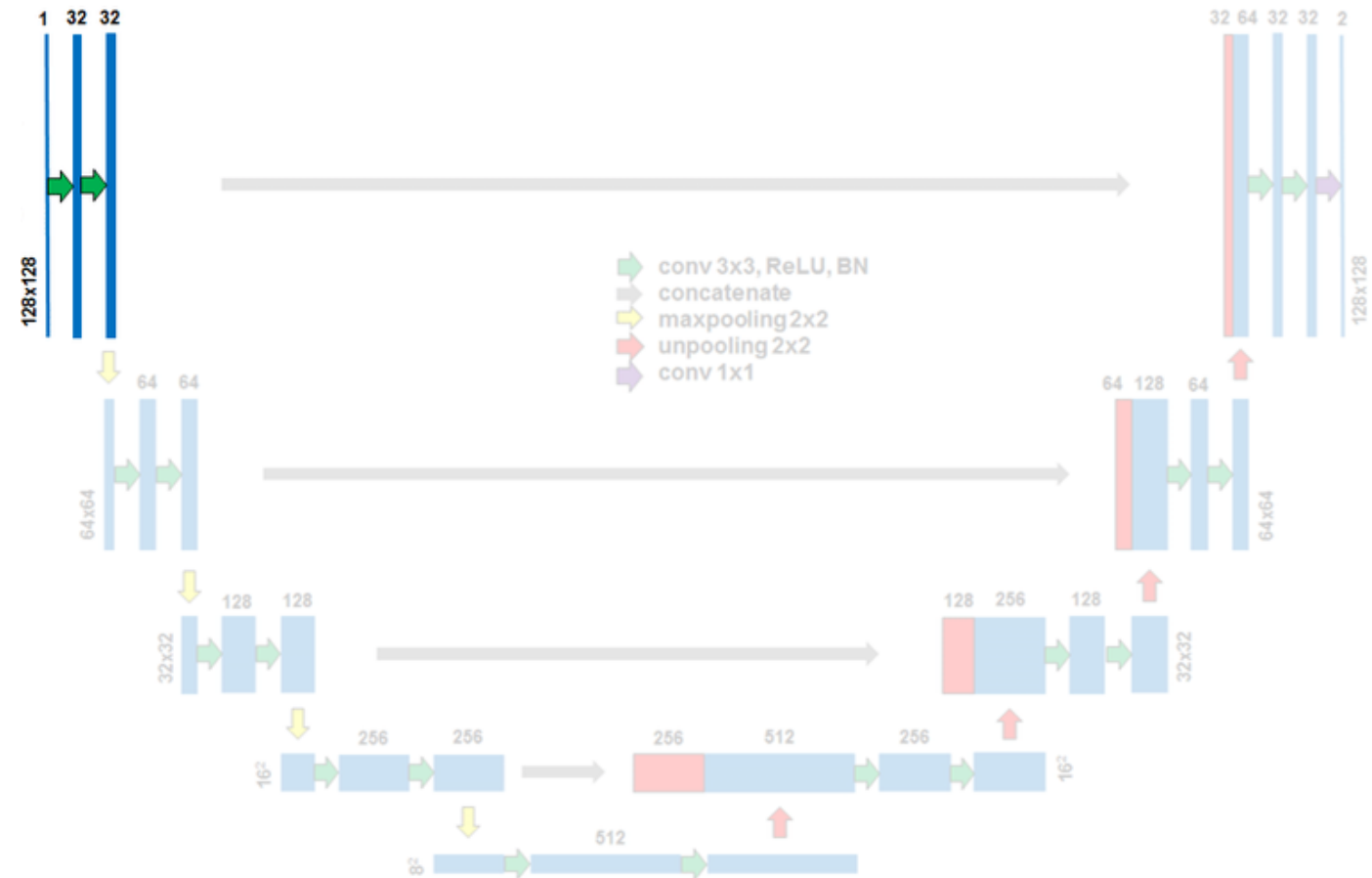
Layer 1 params:

$$1 \times (3 \times 3) \times 32 + 32 = 320$$

Layer 2 params:

$$32 \times (3 \times 3) \times 32 + 32 = 9248$$

Total: 9568



Number of parameters

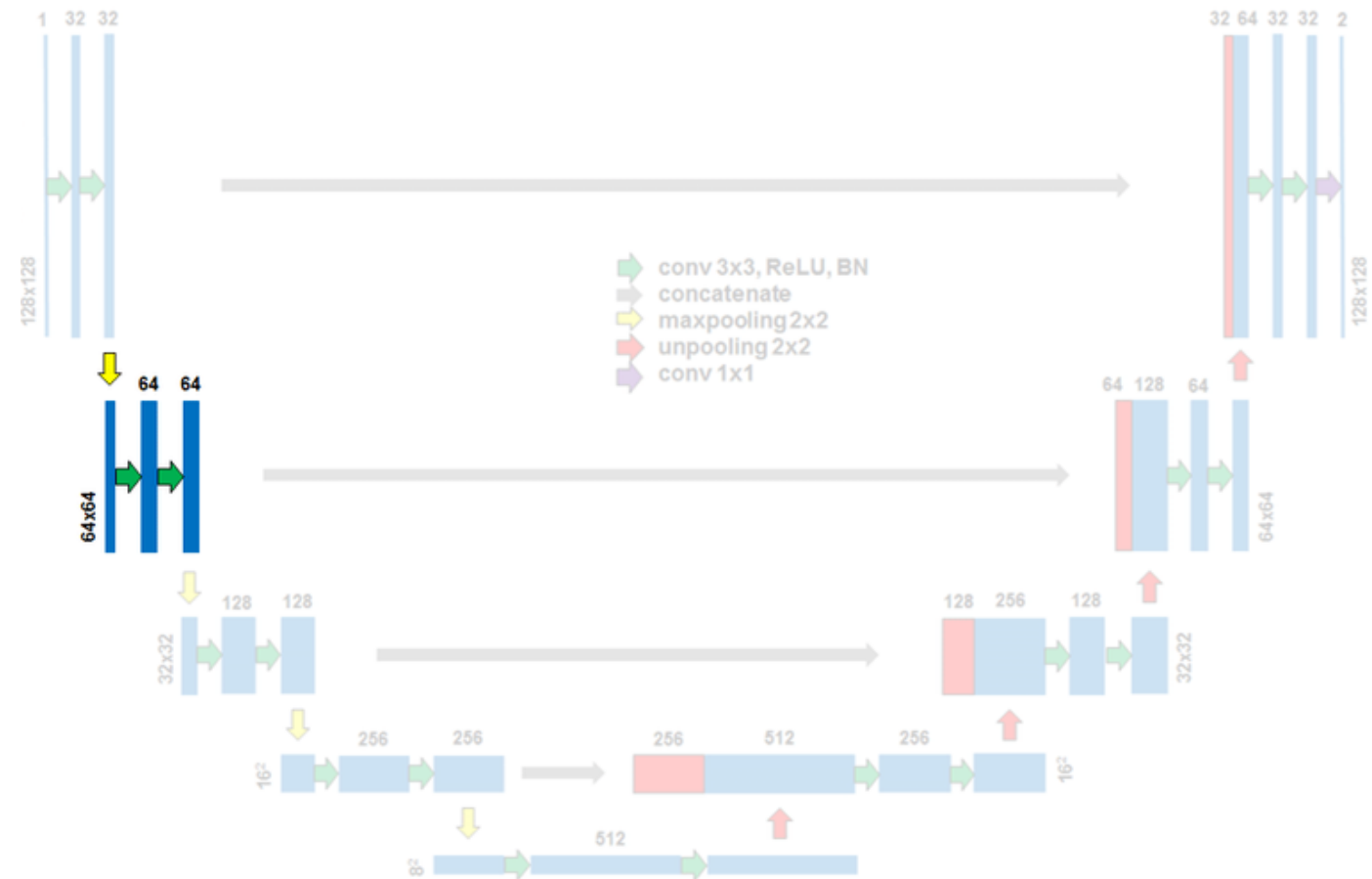
Layer 1 params:

$$32 \times (3 \times 3) \times 64 + 64 = 18,496$$

Layer 2 params:

$$64 \times (3 \times 3) \times 64 + 64 = 36,928$$

Total: 55,424



Number of parameters

Layer 1 params:

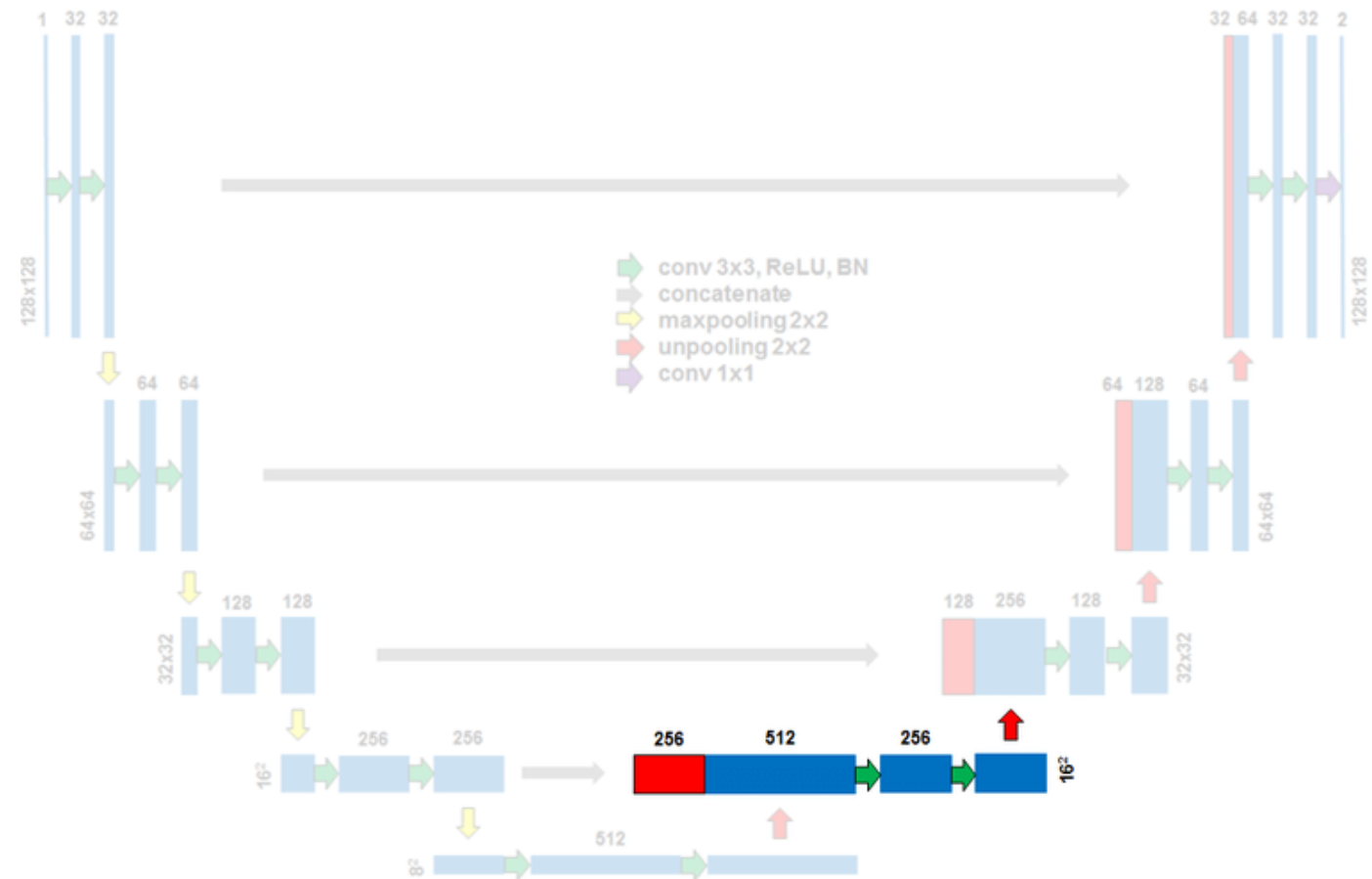
$$768 \times (3 \times 3) \times 256 + 256 = 1,769,728$$

Layer 2 params:

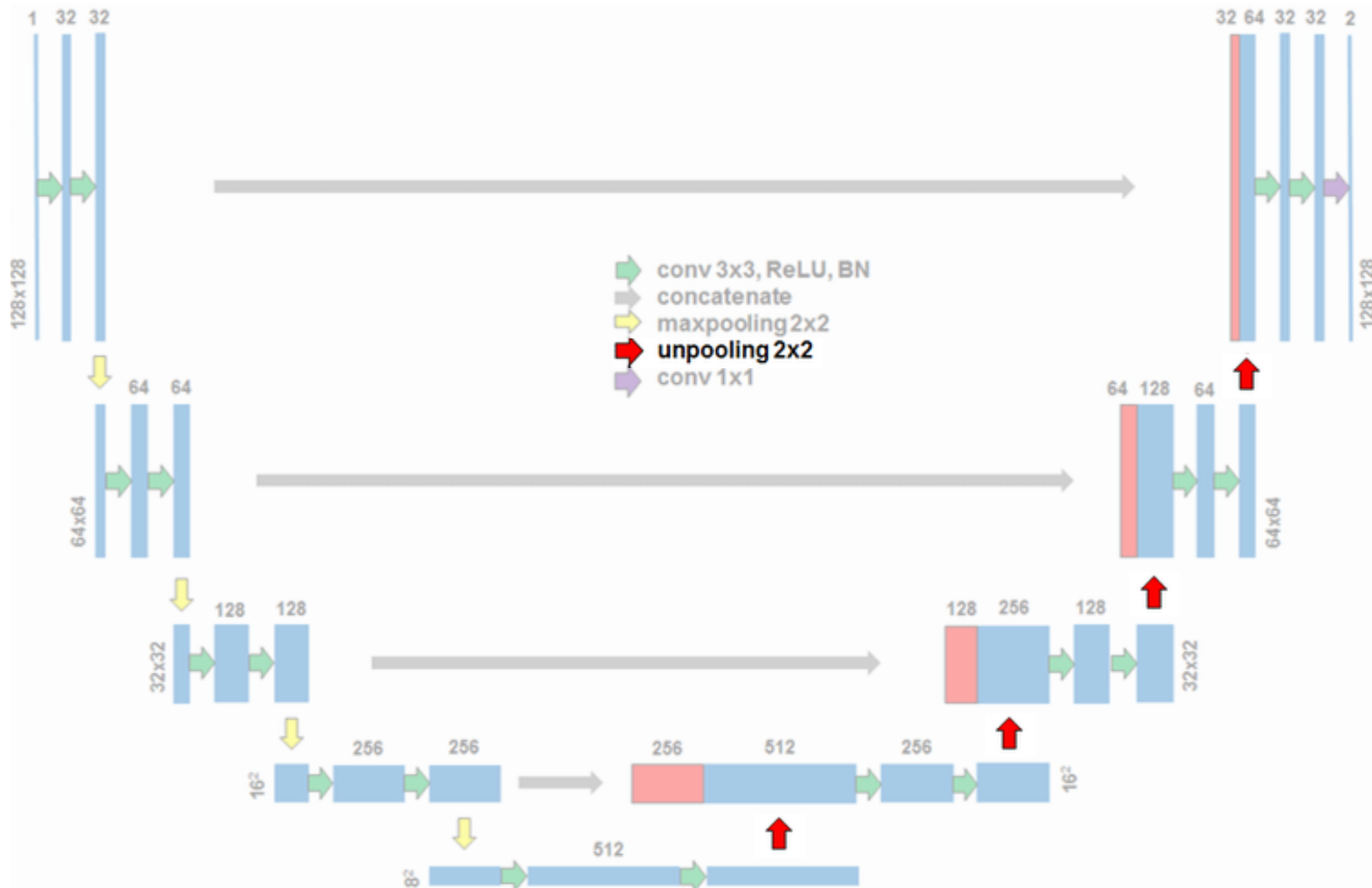
$$256 \times (3 \times 3) \times 256 + 256 = 590,080$$

Total: 2,359,808

Grand total: ~7.8 million

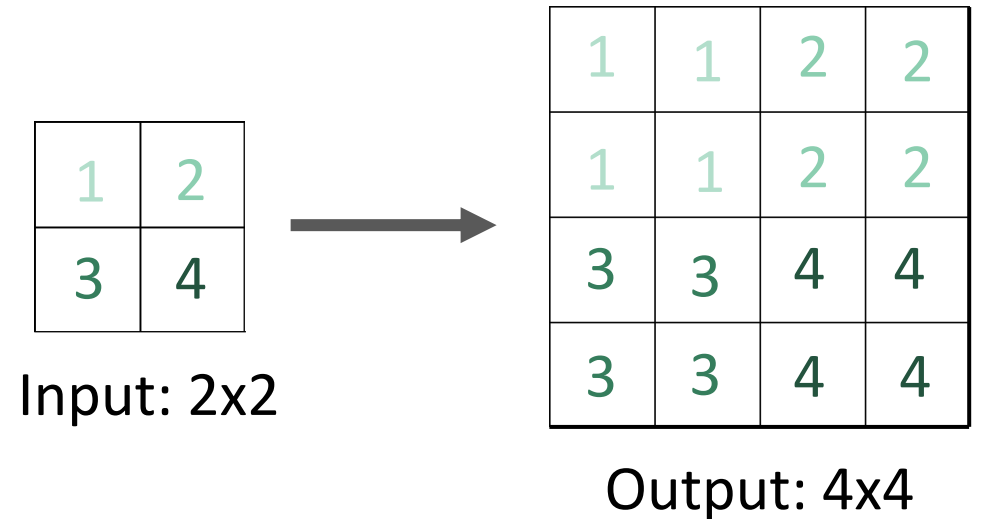


Upsampling

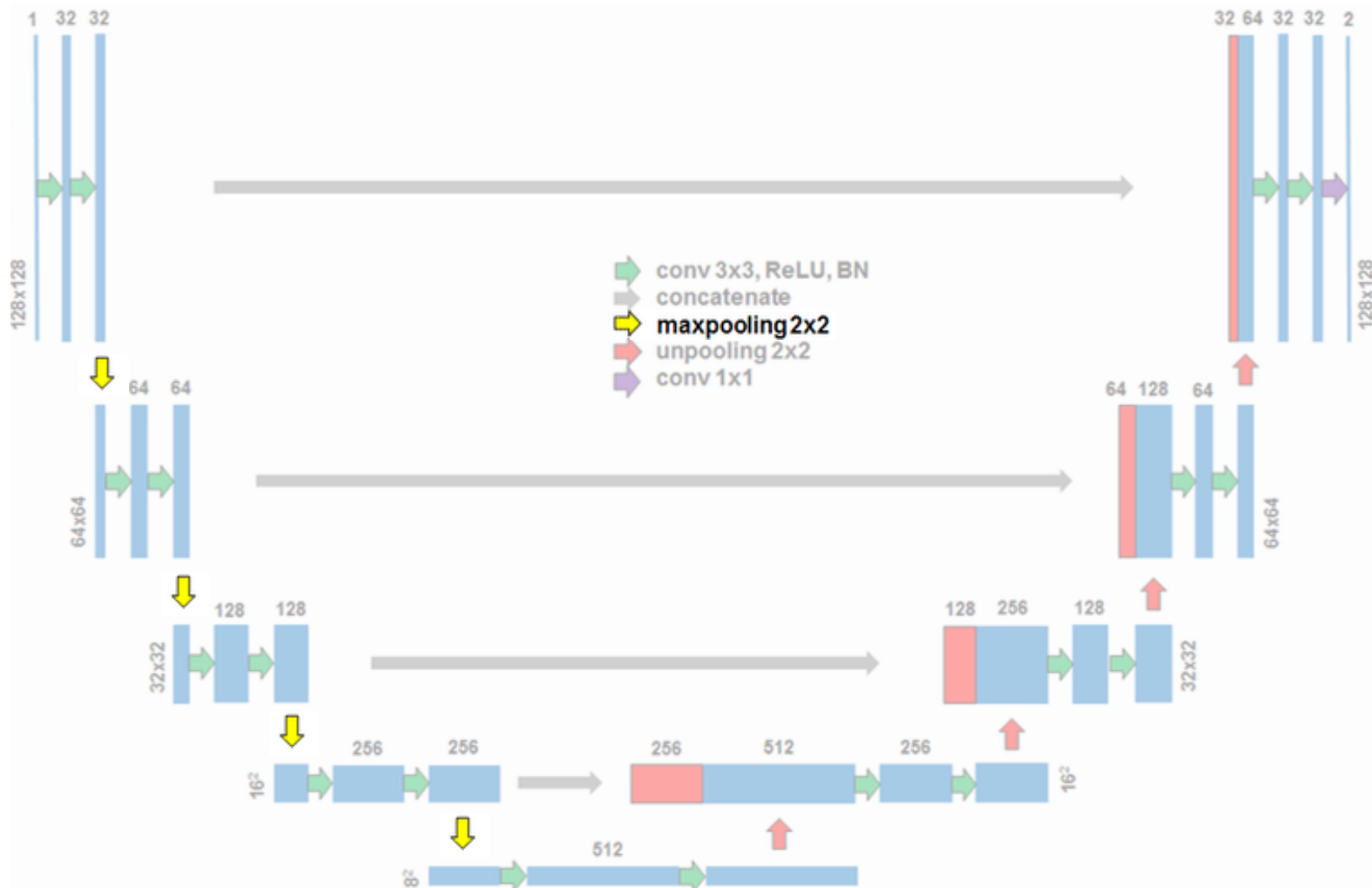


Upsampling

- Opposite effect of max-pooling
- Many ways to do it
 - Transpose convolution
 - Nearest neighbor interpolation
 - Linear interpolation
 - ...

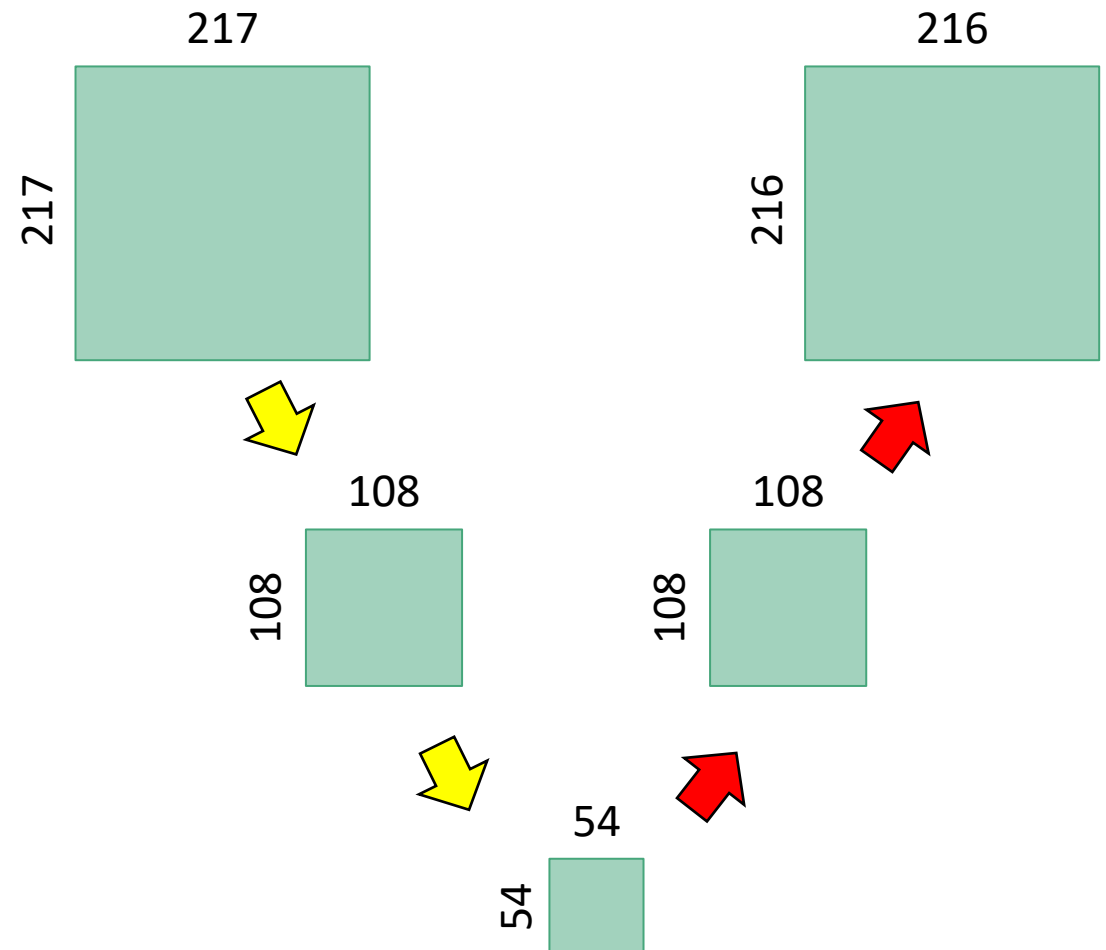


Max pooling



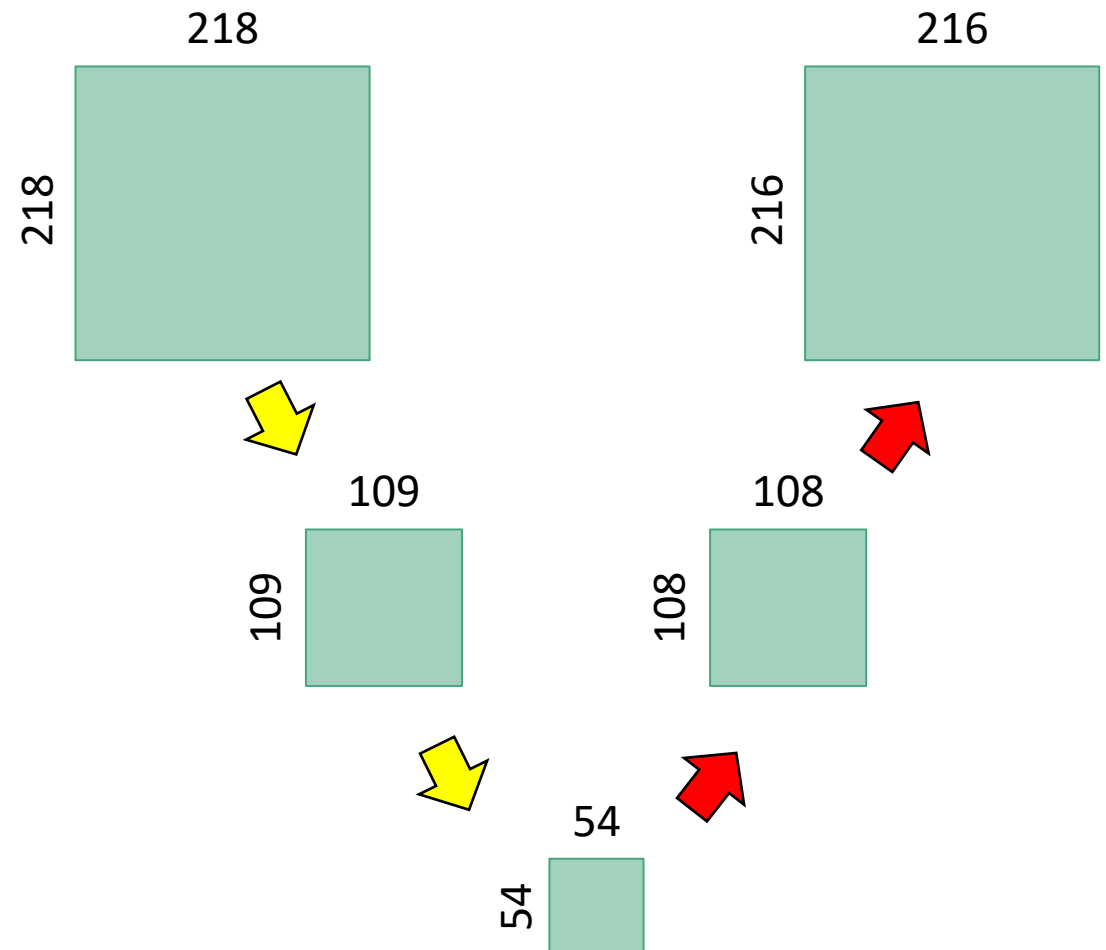
Maxpooling

- U-net uses 2D max pooling
- What happens when we have
 - Odd image dimensions?

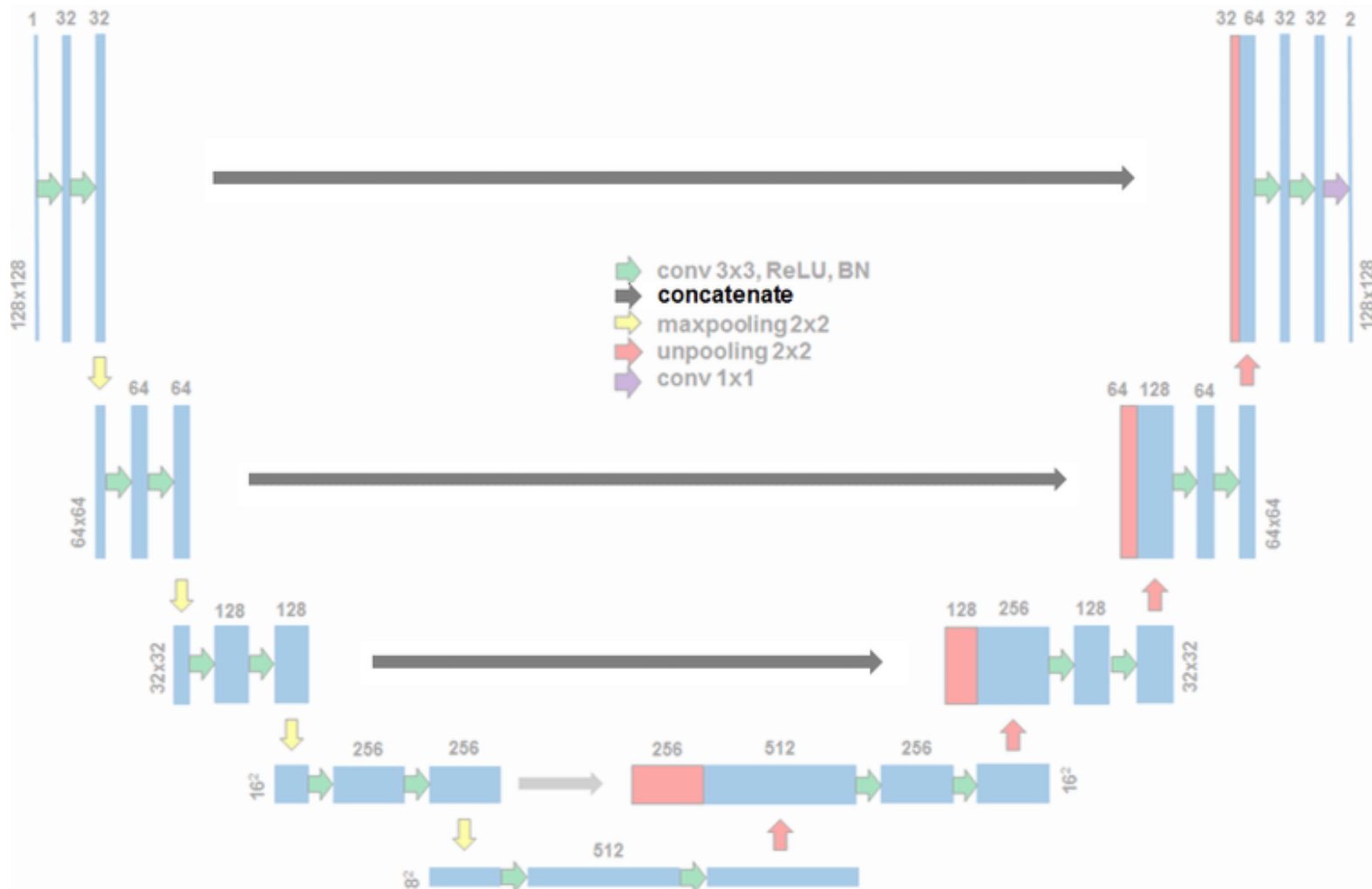


Maxpooling

- U-net uses 2D max pooling
- What happens when we have
 - Odd image dimensions?
 - Other even image dimensions?
- Solution: pad input to nearest dimension divisible by 2 # max pool layers

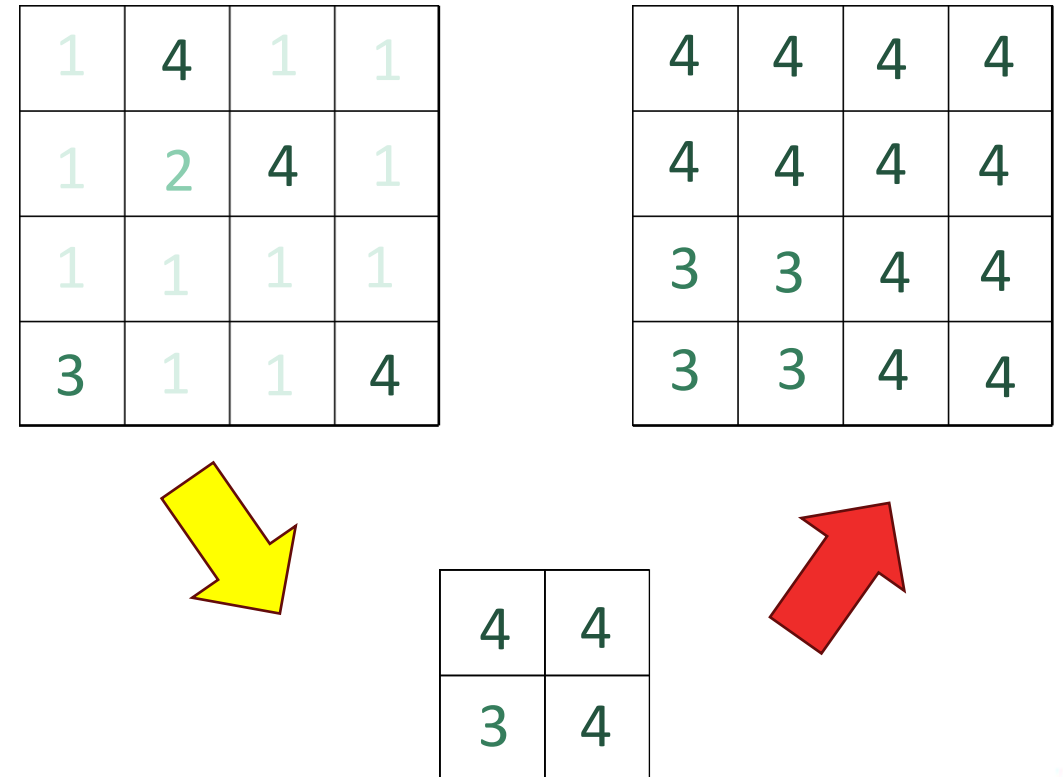


Skip connections

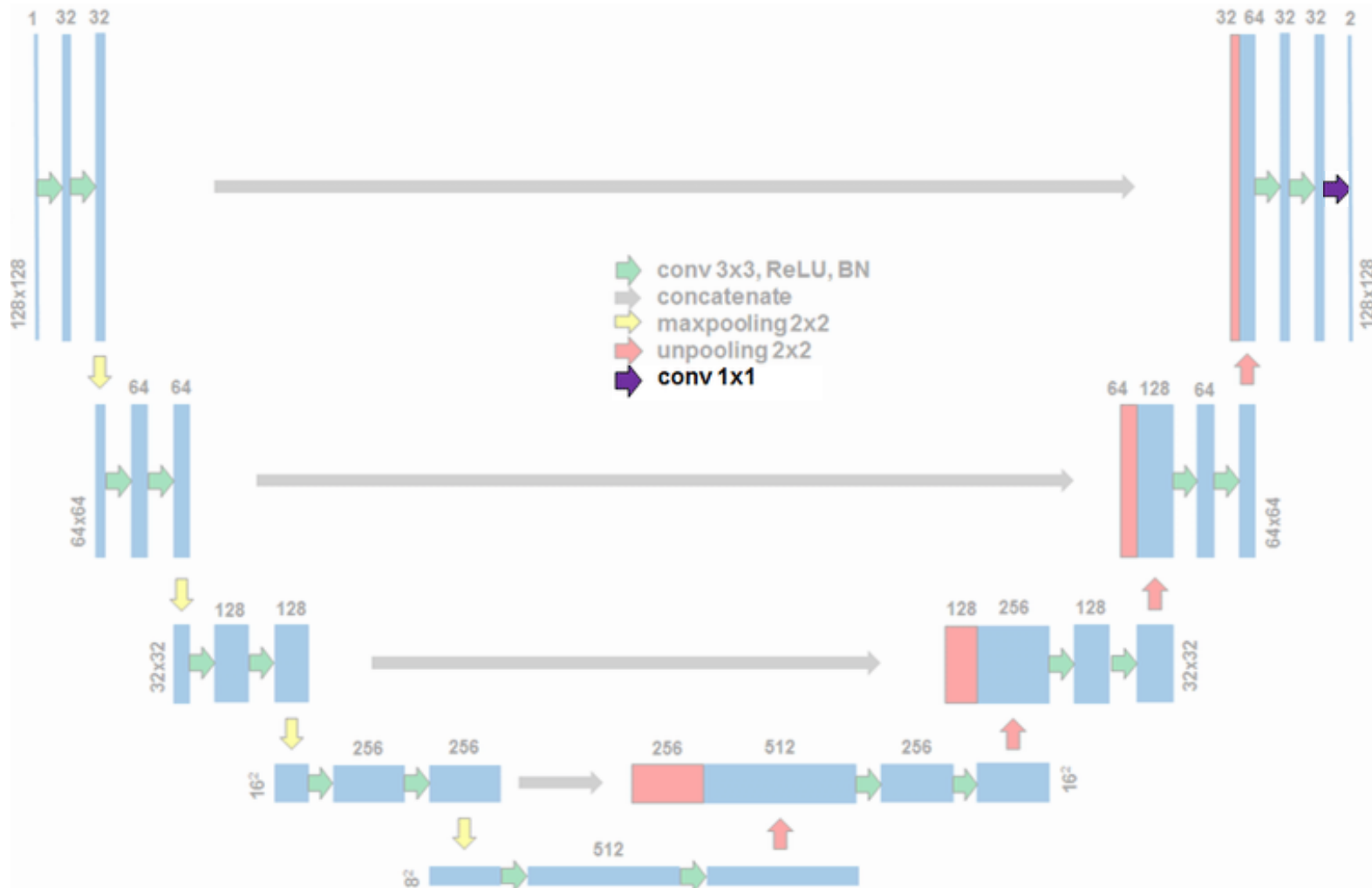


Skip connections

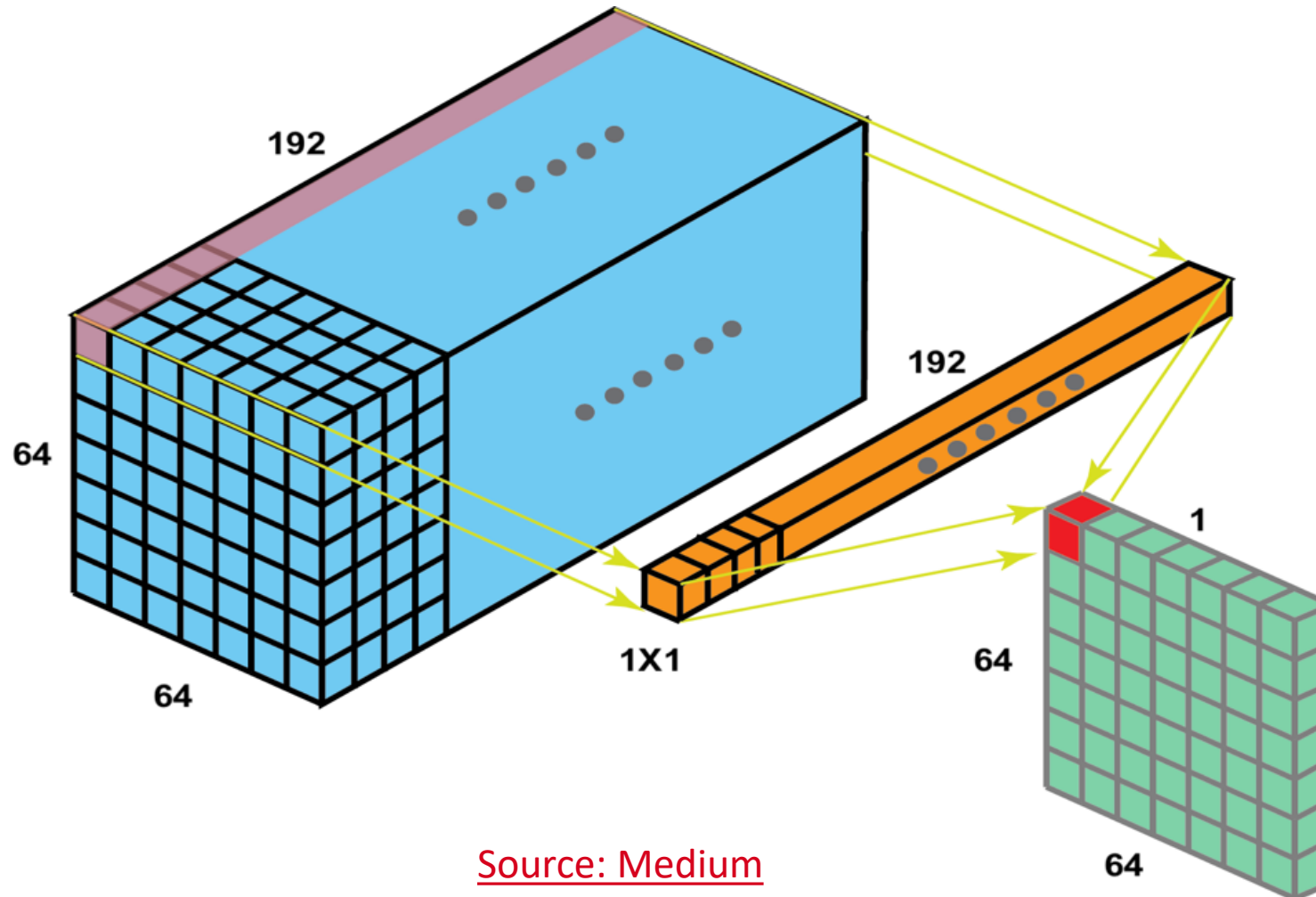
- Propagate multi-scale information
- Improved spatial information



1x1 Convolution

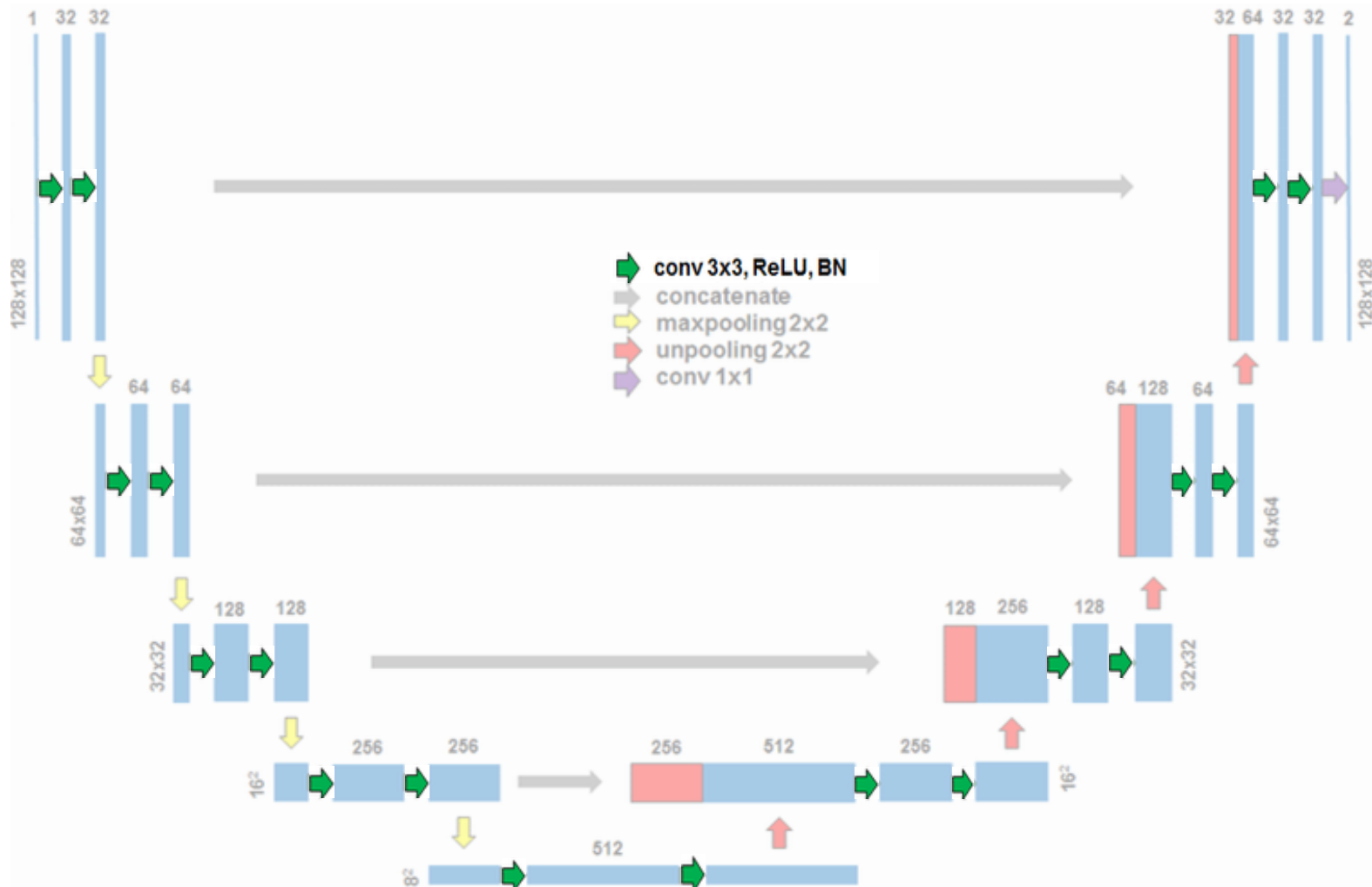


1x1 Convolution



Source: Medium

Batch normalization



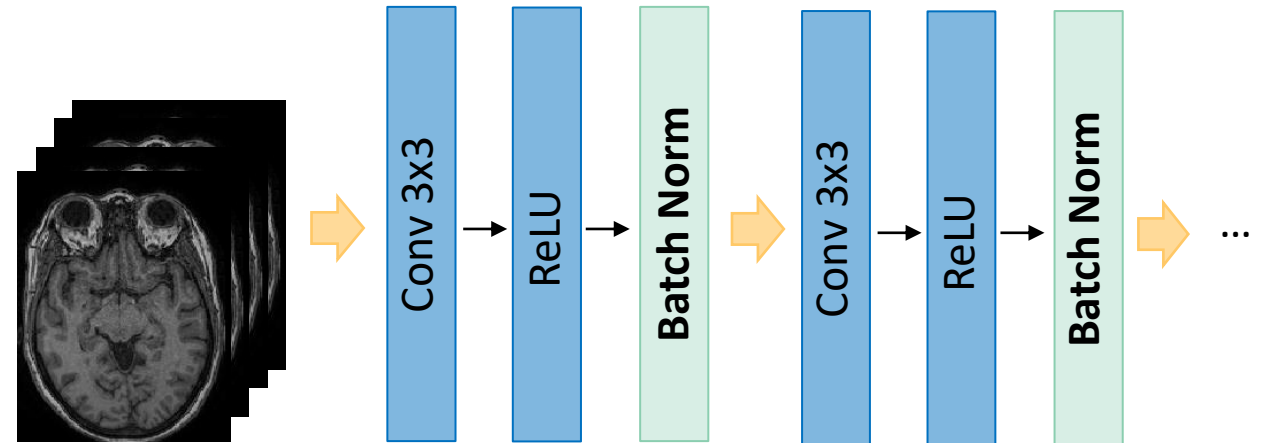
Batch normalization

- Normalizes your batch of data in between layers

$$y = \frac{x - E[x]}{\sqrt{\text{Var}[x] + \epsilon}} * \gamma + \beta$$

Diagram illustrating the Batch Normalization formula:

- $E[x]$ (Expected value of x) is labeled as "Computed parameters".
- γ and β are labeled as "Learnable parameters".



Batch normalization

- Each feature/feature map is normalized!
- During training, running mean and variance computed for use during inference

$$E[x]_{run} = \alpha E[x]_{run} + (1 - \alpha) E[x]$$

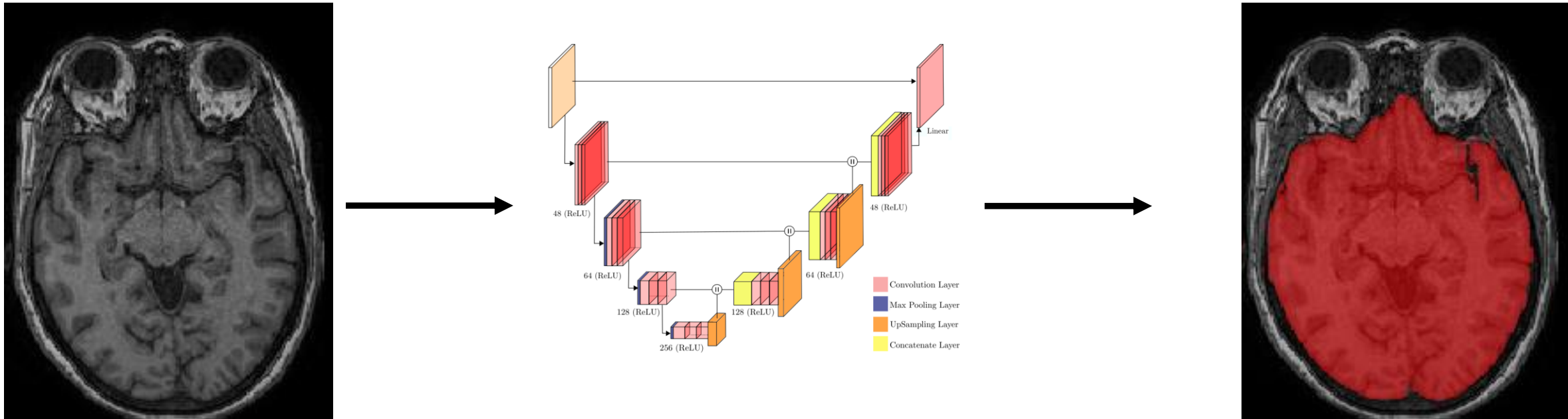
$$Var[x]_{run} = \alpha Var[x]_{run} + (1 - \alpha) Var[x]$$

Momentum

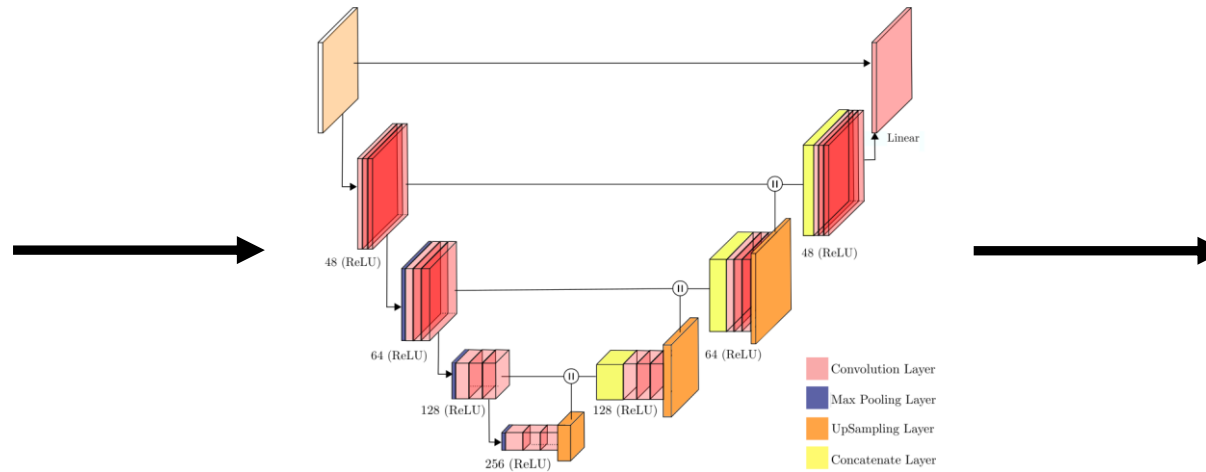


U-net - Segmentation

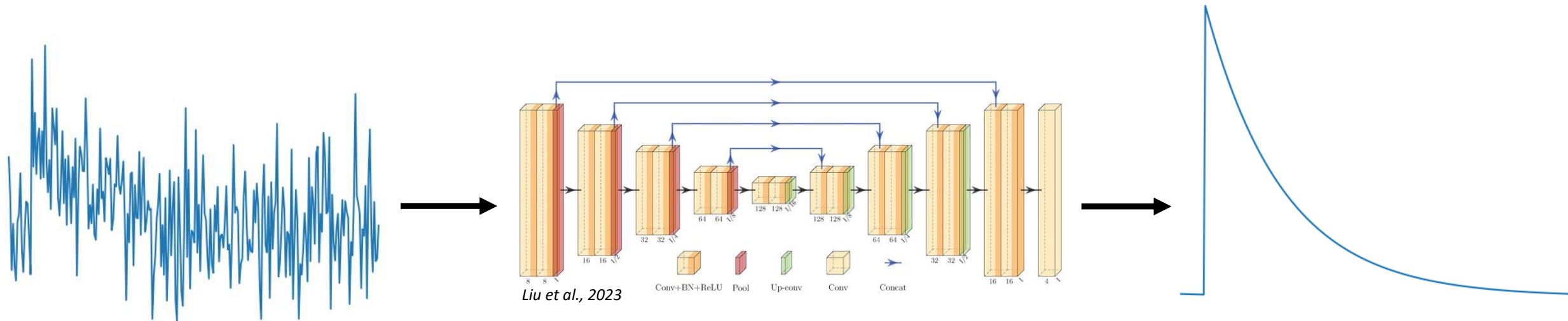
Segmentation = pixel-wise or voxel-wise segmentation



U-net – 2D Regression



U-net – 1D Regression



Metrics

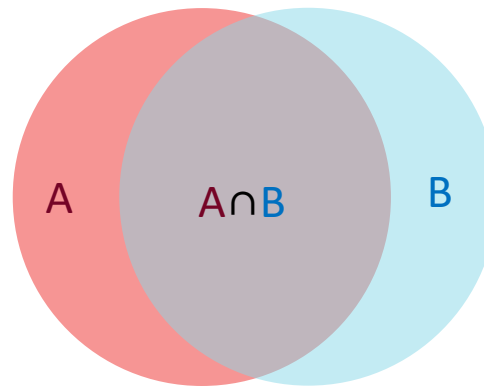
- For regression:

- Mean squared error
- Mean absolute error
- ...

y			-	\hat{y}		
3	4	4		3	3	1
2	3	4		2	3	3
1	2	3		2	2	3

- For segmentation:

- Dice coefficient
- Jaccard coefficient
- ...



Summary

- The U-net is a very powerful deep learning model that maps inputs to outputs of the same size
- The model works across different scales of the input signal/image
- It is a fully convolutional model that is independent of the input size

Thank you!

