# JIDT: An information-theoretic toolkit for studying the dynamics of complex systems

Outline



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The University of Sydney

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# Java Information Dynamics Toolkit (JIDT)



On google code → github (https://lizier.me/jidt/)

JIDT provides a standalone, open-source (GPL v3 licensed) implementation of information-theoretic measures of information processing in complex systems, i.e. information storage, transfer and modification.

#### JIDT includes implementations:

- Principally for transfer entropy, mutual information, their conditional variants, active information storage etc;
- For both discrete and continuous-valued data;
- Using various types of estimators (e.g. Kraskov-Stögbauer-Grassberger, linear-Gaussian, etc.).

# Java Information Dynamics Toolkit (JIDT)



JIDT is written in Java but directly usable in Matlab/Octave, Python, R, Julia, Clojure, etc.

JIDT requires almost zero installation.

#### JIDT is distributed with:

- A paper describing its design and usage;
  - J.T. Lizier, Frontiers in Robotics and AI 1:11, 2014; (arXiv:1408.3270)
- A full tutorial and exercises
- Full Javadocs;
- A suite of demonstrations, including in each of the languages listed above.

Code credits: JL, Ipek Özdemir, Pedro Martínez Mediano



# JIDT tutorial – Objectives



#### Participants will:

- Understand measures of information dynamics;
- Be able to obtain and install JIDT distribution;
- Understand and run sample scripts in their chosen environment;
- Be able to generate new code or modify sample scripts for new analysis;
- Know how and where to seek support information (wiki, Javadocs, mailing list, twitter).

Introduction

Outline

- 2 Information dynamics
  - Information theory
  - The information dynamics framework
- Stimation techniques
- Overview of JIDT
- Demos
- 6 Exercise
- Wrap-up

## Hi, I'm Joe ..



- My background.
- Why I started this information-theoretic toolkit project.



• Where are you from? Unis, other organisations?



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- Which languages/environments are you using, and how much coding experience do you have?



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- How familiar are you with information theory what measures do you know? Are you using it for analysis yet?



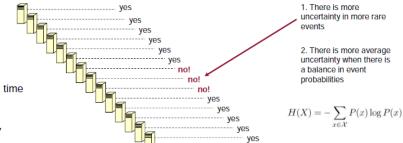
- Where are you from? Unis, other organisations?
- Which languages/environments are you using, and how much coding experience do you have?
- How familiar are you with information theory what measures do you know? Are you using it for analysis yet?
- What types of information-theoretic analysis do you have planned (perhaps with JIDT)?

## Entropy



(Shannon) entropy is a measure of uncertainty. Intuitively: if we want to know the value of a variable, there is uncertainty in what that value is before we inspect it (measured in bits).

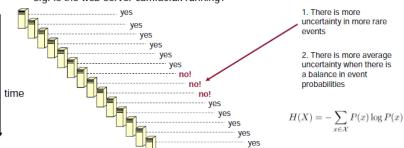
e.g. Is the web server cam.ac.uk running?



# Sample entropy calculation



• e.g. Is the web server cam.ac.uk running?



Here we have p(yes) = 11/14, p(no) = 3/14 – what is H?

x = yes   no	p(x)	$-\log_2 p(x)$	$-p(x)\log_2 p(x)$
yes	0.786	0.348	0.273
no	0.214	2.22	0.476
			H = 0.750  bits

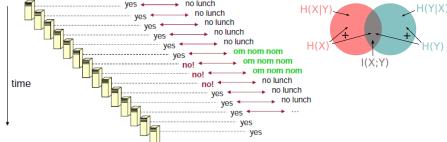
# Conditional entropy



Uncertainty in one variable X in the context of the known measurement of another variable Y.

Intuitively: how much uncertainty is there in X after we know the value of Y?

e.g. How uncertain are we about the web server is running if we know the IT guy is at lunch?



$$H(X|Y) = H(X,Y) - H(Y) = -\sum_{x \in X} \sum_{y \in Y} p(x,y) \log p(x|y)$$

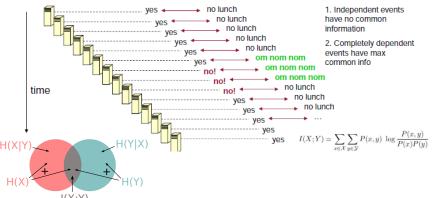
## Mutual information



Information is a measure of uncertainty reduction.

Intuitively: common information is the amount that knowing the value of one variable tells us about another.

e.g. How much common info b/w if IT guy is at lunch and the web server running?



# Information-theoretic quantities

JIDT

$$H(X) = -\sum_{x} p(x) \log_2 p(x)$$
$$= \langle -\log_2 p(x) \rangle$$

Conditional entropy

$$H(X|Y) = -\sum_{x,y} p(x,y) \log_2 p(x|y)$$

Mutual information (MI)

$$I(X; Y) = H(X) + H(Y) - H(X, Y)$$

$$= \sum_{x,y} p(x, y) \log_2 \frac{p(x|y)}{p(x)}$$

$$= \left\langle \log_2 \frac{p(x|y)}{p(x)} \right\rangle$$

$$Y: Y|X\rangle = H(X|X) + H(Y|X) + H(Y|X)$$

Conditional MI

$$I(X; Y|Z) = H(X|Z) + H(Y|Z) - H(X, Y|Z)$$
$$= \left\langle \log_2 \frac{p(x|y, z)}{p(x|z)} \right\rangle$$

#### Local measures



We can write local (or point-wise) information-theoretic measures for specific observations/configurations  $\{x, y, z\}$ :

$$h(x) = -\log_2 p(x),$$
  $i(x; y) = \log_2 \frac{p(x|y)}{p(x)}$   
 $h(x|y) = -\log_2 p(x|y),$   $i(x; y|z) = \log_2 \frac{p(x|y, z)}{p(x|z)}$ 

- We have  $H(X) = \langle h(x) \rangle$  and  $I(X; Y) = \langle i(x; y) \rangle$ , etc.
- If X, Y, Z are time-series, local values measure dynamics over time.

# What can we do with these measures in ALife/CI?



- Measure the diversity in agent strategies (Miramontes, 1995;
   Prokopenko et al., 2005).
- Measure long-range correlations as we approach a phase-transition (Ribeiro et al., 2008).
- Feature selection for machine learning (Wang et al., 2014).
- Quantify the information held in a response about a stimulus, and indeed about specific stimuli (DeWeese and Meister, 1999).
- Measure the common information in the behaviour of two agents (Sperati et al., 2008).
- Guide self-organisation using these measures (Prokopenko et al., 2006).
- . . .
- $\rightarrow$  Information theory is useful for answering specific questions about information content, shared information, and where and to what extent information about some variable is mirrored.



We talk about computation as:

- Memory
- Signalling
- Processing

#### Distributed computation is any process involving these features:

- Time evolution of cellular automata
- Information processing in the brain
- Gene regulatory networks computing cell behaviours
- Flocks computing their collective heading
- Ant colonies computing the most efficient routes to food
- The universe is computing its own future!



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- Idea: quantify computation via:
  - Information storageInformation transfer

  - Information modification

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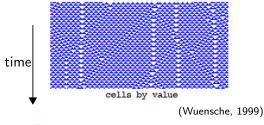
General idea: by quantifying intrinsic computation in the language it is normally described in, we can understand how nature computes and why it is complex.

## Motivating example: cellular automata





CAs: simple dynamical systems; known causal structure and rules.



#### Emergent structure:

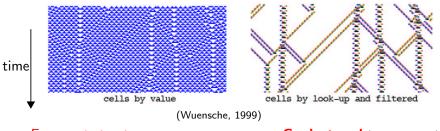
- Domain, blinkersParticles
- - Gliders, domain walls
- Collisions

## Motivating example: cellular automata





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#### **Conjectured** to represent:

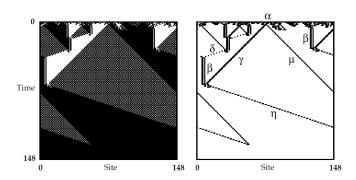
- Information storageInformation transfer
- - Information modification

It's easy to identify which components store, transfer and modify information in a PC – it's not so easy in complex systems.



## Motivating example: cellular automata





Mitchell et al. (1994, 1996) used GAs to evolve CAs to solve specific computational tasks.

In attempting the density classification task (above), the CA uses:

- ullet domains and blinkers eta to store information;
- gliders  $\gamma$ , $\eta$  to transfer information;
- glider collisions e.g.  $\gamma + \beta \rightarrow \eta$  to modify/process information.



JIDT

#### We talk about computation as:

- Memory
- Signalling
- Processing

## Information dynamics

- Information storage
- Information transfer
- Information modification

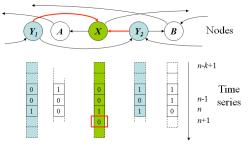
#### Key properties of the information dynamics approach:

- A focus on individual operations of computation rather than overall complexity;
- Alignment with descriptions of dynamics in specific domains;
- A focus on the local scale of info dynamics in space-time;
- Information-theoretic basis directly measures computational quantities:
  - Captures non-linearities;
  - Is applicable to, and comparable between, any type of time-series.





Key question: how is the next state of a variable in a complex system **computed**?

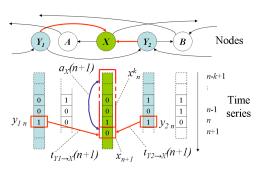


- Q: Where does the information in  $x_{n+1}$  come from, and how can we measure it?
- Q: How much was stored, how much was transferred, can we partition them or do they overlap?

Complex system as a multivariate time-series of states



Studies computation of the next state of a target variable in terms of information storage, transfer and modification: (Lizier et al., 2008, 2010, 2012)



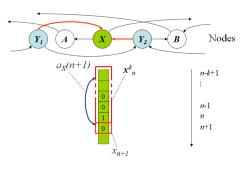
The measures examine:

- State updates of a target variable;
- Dynamics of the measures in space and time.

# Active information storage (Lizier et al., 2012)



How much information about the next observation  $X_{n+1}$  of process X can be found in its past state  $\mathbf{X}_{\mathbf{n}}^{(\mathbf{k})} = \{X_{n-k+1} \dots X_{n-1}, X_n\}$ ?



#### Active information storage:

Nodes 
$$A_X = I(X_{n+1}; \mathbf{X}_n^{(\mathbf{k})})$$

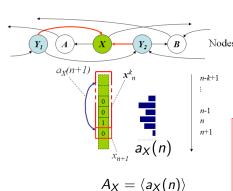
$$= \left\langle \log_2 \frac{p(x_{n+1}|\mathbf{x}_n^{(\mathbf{k})})}{p(x_{n+1})} \right\rangle$$

Average information from past state that is in use in predicting the next value.

# Active information storage (Lizier et al., 2012)



How much information about the next observation  $X_{n+1}$  of process X can be found in its past state  $\mathbf{X}_{\mathbf{n}}^{(\mathbf{k})} = \{X_{n-k+1} \dots X_{n-1}, X_n\}$ ?



#### Active information storage:

Nodes 
$$A_X = I(X_{n+1}; \mathbf{X}_n^{(k)})$$
  
=  $\left\langle \log_2 \frac{p(x_{n+1}|\mathbf{x}_n^{(k)})}{p(x_{n+1})} \right\rangle$ 

Average information from past state that is in use in predicting the next value.

#### Local active information storage:

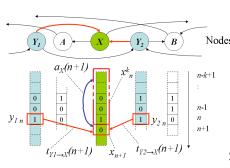
$$a_X(n) = \log_2 \frac{p(x_{n+1}|x_n^{(k)})}{p(x_{n+1})}$$

Information from a specific past state that is in use in predicting the specific next value.

### Information transfer



How much information about the state transition  $X_n^{(k)} \to X_{n+1}$  of X can be found in the past state  $Y_n^{(l)}$  of a source process Y?



Transfer entropy: (Schreiber, 2000)

$$T_{Y \to X} = I(\mathbf{Y}_{\mathbf{n}}^{(1)}; X_{n+1} | \mathbf{X}_{\mathbf{n}}^{(k)})$$
$$= \left\langle \log_2 \frac{\rho(x_{n+1} | \mathbf{x}_{\mathbf{n}}^{(k)}, \mathbf{y}_{\mathbf{n}}^{(l)}))}{\rho(x_{n+1} | \mathbf{x}_{\mathbf{n}}^{(k)})} \right\rangle$$

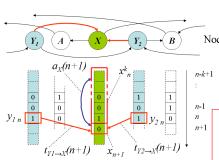
Average info from source that helps predict next value in context of past.

Storage and transfer are complementary:  $H_X = A_X + T_{Y \to X} + \text{higher order terms}$ 

## Information transfer



How much information about the state transition  $\mathbf{X}_{\mathbf{n}}^{(\mathbf{k})} \to X_{n+1}$  of X can be found in the past state  $\mathbf{Y}_{\mathbf{n}}^{(\mathbf{l})}$  of a source process Y?



Transfer entropy: (Schreiber, 2000)

$$T_{Y \to X} = I(\mathbf{Y}_{\mathbf{n}}^{(1)}; X_{n+1} \mid \mathbf{X}_{\mathbf{n}}^{(k)})$$
$$= \left\langle \log_2 \frac{p(x_{n+1} \mid \mathbf{x}_{\mathbf{n}}^{(k)}, \mathbf{y}_{\mathbf{n}}^{(l)}))}{p(x_{n+1} \mid \mathbf{x}_{\mathbf{n}}^{(k)})} \right\rangle$$

Average info from source that helps predict next value in context of past.

**Local** transfer entropy: (Lizier et al., 2008)  $t_{Y \to X}(n) = \log_2 \frac{p(x_{n+1}|\mathbf{x}_n^{(k)}, \mathbf{y}_n^{(l)}))}{p(x_{n+1}|\mathbf{x}_n^{(k)}))}$ 

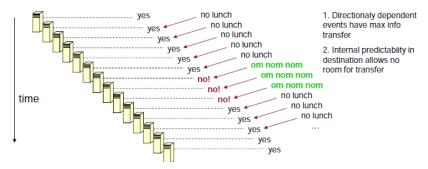
Information from a specific observation about the specific next value.

## Information transfer



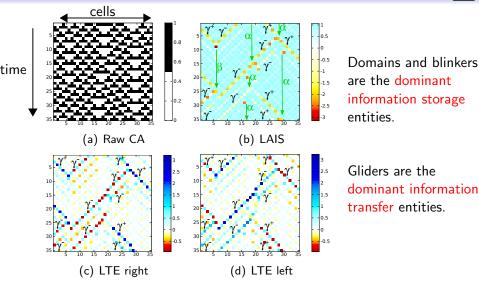
Transfer entropy measures directed coupling between time-series. Intuitively: the amount of information that a source variable tells us about a destination, in the context of the destination's current state.

e.g. How much does knowing the IT guy is at lunch tell us about the web server running, given its previous state?



# Information dynamics in CAs

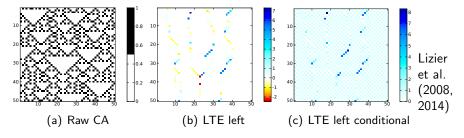




# Other transfer entropy characteristics



TE can be made conditional  $T_{Y \to X|Z} = I(\mathbf{Y}_{\mathbf{n}}^{(\mathbf{l})}; X_{n+1} \mid \mathbf{X}_{\mathbf{n}}^{(\mathbf{k})}, \mathbf{Z}_{\mathbf{n}}^{(\mathbf{m})})$  or multivariate  $T_{Y \to X|Z} = I(\{\mathbf{Y}_{\mathbf{n}}^{(\mathbf{l})}, \mathbf{Z}_{\mathbf{n}}^{(\mathbf{m})}\}; X_{n+1} \mid \mathbf{X}_{\mathbf{n}}^{(\mathbf{k})})$  (Lizier et al., 2008, 2010, 2011)



Computed over delay u as  $T_{Y \to X|Z} = I(\mathbf{Y}_{\mathbf{n}-\mathbf{u}+\mathbf{1}}^{(\mathbf{l})}; X_{n+1} \mid \mathbf{X}_{\mathbf{n}}^{(\mathbf{k})})$  (Wibral et al., 2013).

## Discrete: plug-in estimator



For discrete variables x and y, to compute H(X, Y)

- **1** estimate:  $p(x,y) = \frac{\text{count}(X=x,Y=y)}{N}$ , where N is our sample size;
- ② plug-in each estimated PDF to H(X, Y) to get  $\hat{H}(X, Y)$

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Bias: expected offset of estimated value from a finite sample set from the true underlying value of the measure. There are several available bias correction techniques.

Variance: variance in estimated values of the measure (from a finite sample set) around the expected value.

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A simple way to handle continuous variables is to discretise or bin them.

## Continuous variables → Differential entropy



#### Differential entropy:

$$H_D(X) = -\int_{S_X} f(x) \log f(x) dx$$

for PDF f(x), where  $S_X$  is the set where f(x) > 0.

Evaluate all measures as sums and differences of  $H_D(X)$  terms.

The properties of  $H_D(X)$  are slightly odd ... however, the properties of  $I_D(X;Y)$  are the same as for discrete variables.

JIDT includes 3 estimation methods for differential entropy based MIs (and conditional MIs)  $\dots$ 

### Gaussian model



If a multivariate  $\mathbf{X}$  (of d dimensions) is Gaussian distributed (Cover and Thomas, 1991):

$$H(\mathbf{X}) = rac{1}{2} \ln \left[ (2\pi e)^d \mid \Omega_{\mathbf{X}} \mid 
ight]$$

(in *nats*) where  $\mid \Omega_{\mathbf{X}} \mid$  is the determinant of the  $d \times d$  covariance matrix  $\Omega_{\mathbf{X}} = \overline{\mathbf{X}} \overline{\mathbf{X}}^T$ .

Any measure is computed as sums and differences of these joint entropies.

Pros: fast  $(O(Nd^2))$ , parameter free Cons: subject to the linear-model assumption

### Kernel estimation



Estimate PDFs with a *kernel function*  $\Theta$ , measuring "similarity" between pairs of samples  $\{x_n, y_n\}$  and  $\{x_{n'}, y_{n'}\}$  using a resolution or *kernel width* r.

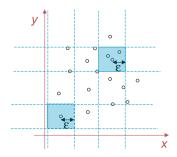
E.g.: 
$$\hat{p}_r(x_n, y_n) = \frac{1}{N} \sum_{n'=1}^N \Theta\left( \left| \left( \begin{array}{c} x_n - x_{n'} \\ y_n - y_{n'} \end{array} \right) \right| - r \right).$$

By default  $\Theta$  is the step kernel  $(\Theta(x > 0) = 0, \ \Theta(x \le 0) = 1)$ , and the norm  $|\cdot|$  is the maximum distance.

Pros: model-free (captures non-linearities)
Cons: sensitive to r, is biased, less time-efficient (though can be reduced to  $O(N \log N)$ ).

# Estimating p(x, y), p(x) and p(y)



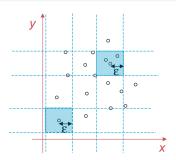


#### Kernel estimation

- Fixed width  $r = \epsilon$
- MI: "How does knowing x within r help me predict y within r?"

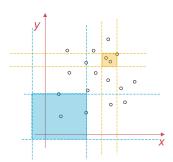
# Estimating p(x, y), p(x) and p(y)





#### Kernel estimation

- Fixed width  $r = \epsilon$
- MI: "How does knowing x within r help me predict y within r?"



Kraskov (KSG) technique (Kraskov et al., 2004)

- Dynamic width *r* and bias correction
- MI: "How does knowing x within the K neasrest neighbours in the joint space help me predict y?"

# KSG estimators (Kraskov et al., 2004)



Improve on box-kernel estimation with lower bias via:

- Harnessing Kozachenko-Leonenko entropy estimators;
- Using nearest-neighbour counting, with a fixed number K of neighbours in the full joint space.

# KSG estimators (Kraskov et al., 2004)



Improve on box-kernel estimation with lower bias via:

- Harnessing Kozachenko-Leonenko entropy estimators;
- Using nearest-neighbour counting, with a fixed number K of neighbours in the full joint space.

There are two algorithms; algorithm 1 gives:

$$I^{(1)}(X;Y) = \psi(K) - \langle \psi(n_x+1) + \psi(n_y+1) \rangle + \psi(N),$$

(in *nats*) where  $\psi$  denotes the digamma function. Extensions to conditional MI are available (Frenzel and Pompe, 2007; Gomez-Herrero et al., 2010; Wibral et al., 2014).

Pros: model-free, bias corrected, best of breed in terms of data efficiency and accuracy, and is effectively parameter free (w.r.t K).

Cons: less time-efficient (though fast nearest neighbour searching reduces this to  $O(KN \log N)$ ).

### Why JIDT?



JIDT is unique in the combination of features it provides:

- Large array of measures, including all conditional/multivariate forms of the transfer entropy, and complementary measures such as active information storage.
- Wide variety of estimator types and applicability to both discrete and continuous data

### Measure-estimator combinations



#### As of V1.2 distribution:

Measure		Discrete		Cont	inuous estimators	
Name	Notation	estimator	Gaussian	Box-Kernel	Kraskov et al.(KSG)	Permutation
Entropy	H(X)	<b>√</b>	<b>√</b>	✓	*	
Entropy rate	$H_{\mu X}$	<b>√</b>	Use tu	o multivariate e	entropy calculators	
Mutual information (MI)	I(X;Y)	<b>√</b>	<b>√</b>	✓	✓	
Conditional MI	$I(X; Y \mid Z)$	<b>√</b>	<b>√</b>		✓	
Multi-information	1(X)	<b>√</b>		√"	√"	
Transfer entropy (TE)	$T_{Y \to X}$	<b>√</b>	<b>√</b>	✓	✓	√"
Conditional TE	$T_{Y \to X Z}$	<b>✓</b>	√ u		√"	
Active information storage	$A_X$	<b>√</b>	√ u	√"	√"	
Predictive information	EX	<b>✓</b>	√ u	√ u	√"	
Separable information	S <sub>X</sub>	<b>✓</b>				

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- Wide variety of estimator types and applicability to both discrete and continuous data
- Local measurement for all estimators;
- Statistical significance calculations for MI, TE;
- No dependencies on other installations (except Java);
- Lots of demos and information on website/wiki:
  - https://code.google.com/p/information-dynamics-toolkit/

## Why implement in Java?



The Java implementation of JIDT gives us several fundamental features:

- Platform agnostic, requiring only a JVM;
- Object-oriented code, with a hierachical design to interfaces for each measure, allowing dynamic swapping of estimators for the same measure;
- JIDT can be directly called from Matlab/Octave, Python, R, Julia, Clojure, etc, adding efficiency for higher level code;
- Automatic generation of Javadocs.

### Installation



- Oownload the latest full distribution by following the Download link at https://lizier.me/jidt/ (links to google code or github after JIDT moves there ...)
- ② Unzip it to your prefered location for the distribution
- To be able to use it, you will need the infodynamics.jar on your classpath.

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That's it!

### Installation – caveats



- You'll need a JRE installed (Version  $\geq 6$ )
  - Should come automatically with Matlab/Octave/Python-JPype installation
- You need ant if you want to rebuild the project using build.xml
- You need junit if you want to run the unit tests
- Additional preparation may be required to use JIDT in GNU Octave or Python ...

# Check that your environment works



#### Java:

• Run demos/java/example1TeBinaryData.sh or .bat

### Matlab/Octave:

- For Octave version < 3.8, first follow steps on the wiki, including installing octave-java from octave-forge.
- Q Run demos/octave/example1TeBinaryData.m

#### Python:

- Install jPype to connect Python to Java (or jpype1-py3 for Python 3)
- Q Run demos/python/example1TeBinaryData.py

In case of issues, see the wiki pages on Non-Java environments or the Instructor.

### Contents of distribution



- license-gplv3.txt GNU GPL v3 license;
- infodynamics.jar library file;
- Documentation
- Source code in java/source folder
- Unit tests in java/unittests folder
- build.xml ant build script
- Demonstrations of the code in demos folder.

### Documentation



#### Included in the distribution:

- readme.txt;
- InfoDynamicsToolkit.pdf a pre-print of the publication introducing JIDT;
- tutorial folder a full tutorial presentation and sample exercise (also via JIDT wiki)
- javadocs folder documents the methods and various options for each estimator class;
- PDFs describing each demo in the demos folder;

#### Also see:

- The wiki pages on the JIDT website
- Our email discussion list jidt-discuss on Google groups.

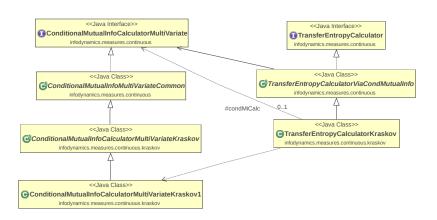
### Source code structure



Source code at java/source is organised into the following Java packages (mapping directly to subdirectories):

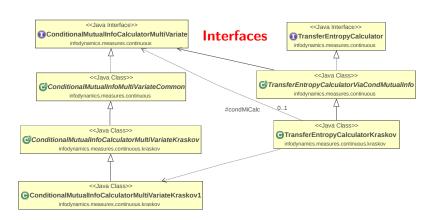
- infodynamics.measures
  - infodynamics.measures.discrete for discrete data;
  - infodynamics.measures.continuous for continuous data
    - top level: Java interfaces for each measure, then
    - a set of sub-packages (gaussian, kernel, kozachenko, kraskov and symbolic) containing implementations of such estimators for these interfaces.
  - infodynamics.measures.mixed experimental discrete-to-continuous MI calculators
- infodynamics.utils utility functions
- infodynamics.networkinference higher-level algorithms





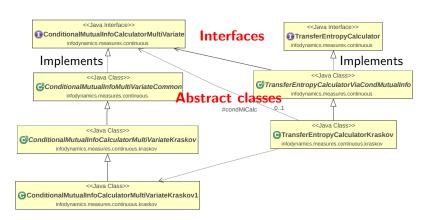
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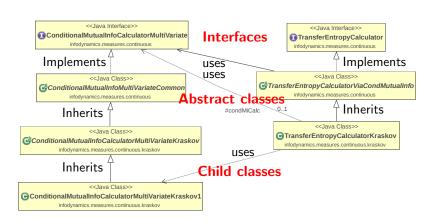
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▶ Return to JIDT contents

### Demos



JIDT is ditributed with the following demos:

- Auto-analyser GUI (code generator)
- Simple Java Demos
  - Mirrored in Matlab/Octave, Python, R, Julia, Clojure.
- Recreation of Schreiber's original transfer entropy examples;
- Information dynamics in Cellular Automata;
- Detecting interaction lags;
- Interregional coupling;
- Behaviour of null/surrogate distributions;

All have documentation (PDF and wiki pages) provided to help run them.



### A GUI application to:

- Make simple MI and TE calculations for you;
- Create code for you.

While this auto-analysis is only provided for MI and TE, note that the general coding paradigm for all calculators is the same. Scripts to start the apps are in the demos/AutoAnalyser folder:

- runTEAutoAnalyser.sh (and .bat) for TE, and
- runMIAutoAnalyser.sh (and .bat) for MI.

Run: runTEAutoAnalyser.sh (or .bat)



### Computing TE and MI could not be easier

Calculation parameters	Generated code
Calculator Type: Discrete	Java Python Matlab
Data file: Opnomics/demos/data/2coupledBinaryColsUseC21st Select Valid data file with 1000 rows and 2 columns Source column: Destination column:	Awaiting new parameter selection (press compute)
Property name Property value L base 2	JIDT
Compute	



### Computing TE and MI could not be easier

🚫 🖨 🗊 JIDT Transfer Entropy Auto-Analyser	
Calculation parameters	Generated code
Calculator Type: Discrete	Java Python Matlab
Data file: Dynamics/demos/data/2coupledBinaryColsUseK2.txt	Awaiting new parameter selection (press compute)
Select Valid data file with 1000 rows and 2 columns	Lar Cilla alla Cill
Source column:	Just follow the GUI:
Destination column: 1	
Property name Property value	Select estimator
k_HISTORY 1 base 2	Select data file
-	
	Identify source/target
	columns in data
	501a5 dasa
	Fill out properties (use
	tool tip for descriptions)
	Olick "Compute"
	Click Collipute
Compute	



### Clicking "compute" then gives you:

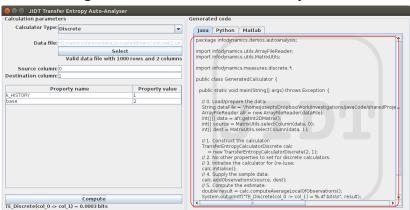
The resulting TE and MI

Calculation parameters		Generated code		
Calculator Type: Discrete	~	Java Python Matlab		
	2coupledBinaryColsUseK2.txt lelect 1000 rows and 2 columns	package infodynamics.demos.autoanalysis; import infodynamics.utils.ArrayFileReader; import infodynamics.utils.MatrixUtils; import infodynamics.measures.discrete.*;		
Property name	Property value	public class GeneratedCalculator {  public static void main(String[] args) throws Exception {		
k_HISTORY base	2	// 0. Loadjorepare the data:   String data: lie - 'fromelgesephDrophov/Work/Investigations/JavaCode/sharedProje   ArrayFileReader afr - new ArrayFileReader(dataFile);   Int		
		TransferEntropic alculator Discrete calc  = new TransferEntropic Aculator Discrete (2, 1);  // 2. No other properties to set for discrete calculators.  // 3. Initials the calculator for (re-use: calc.initialse();  // 4. Supply the amount of calculators.  // 5. Compute the estimate double results — calc. compute Average Local Of Observations();  // 5. Compute the estimate:		



### Clicking "compute" then gives you:

- The resulting TE and MI, and
- 2 Code to generate this calculation in Java, Python and Matlab



# Auto Analyser GUI (code generator) – discrete



Let's generate a sample TE calculation on discrete data:

- Select Discrete estimator
- Select the data file 2coupledBinaryColsUseK2.txt from the default directory in the Select popup.
  - Note: the GUI checks validity of the file
  - Valid file format is described when you hover on Data file
- Leave source and destination columns, and properties, for now
- Olick Compute

Did everyone get the result 0.0003 bits?

# Auto Analyser GUI (code generator) – discrete



Let's generate a sample TE calculation on discrete data:

- Select Discrete estimator
- Select the data file 2coupledBinaryColsUseK2.txt from the default directory in the Select popup.
  - Note: the GUI checks validity of the file
  - Valid file format is described when you hover on Data file
- Leave source and destination columns, and properties, for now
- Click Compute

Did everyone get the result 0.0003 bits? What if you change the property k\_HISTORY to 2? Hover on the property names to see the description for them

### Auto Analyser GUI – discrete – code analysis



Let's examine the code that was generated.

#### Either:

- Olick on the panel for the language you want to work in, OR
- Open the file that was automatically generated for you:
  - demos/java/infodynamics/demos/autoanalysis/-GeneratedCalculator.java OR
  - @ demos/AutoAnalyser/GeneratedCalculator.m OR
  - demos/AutoAnalyser/GeneratedCalculator.py

### Auto Analyser GUI – discrete – code analysis



Observe how the classpath is pointed to infodynamics.jar:

- Java: java command line in demos/AutoAnalyser/runAutoGenerated.sh/.bat (or in IDE);
- Matlab/Octave: javaaddpath() statement;
- Python: startJVM() statement.

### Auto Analyser GUI – discrete – code analysis



Observe how the classpath is pointed to infodynamics.jar:

- Java: java command line in demos/AutoAnalyser/runAutoGenerated.sh/.bat (or in IDE);
- Matlab/Octave: javaaddpath() statement;
- Python: startJVM() statement.

Note: Discrete data (source and dest) represented as int[] arrays:

- with values in the range 0... base 1, where e.g. base=2 for binary.
- for time-series measures, the array is indexed by time.
- for multivariate time-series, we use int[][] arrays, indexed first by time then variable number.



- Construct the calculator, providing parameters
  - Always check Javadocs for which parameters are required.
  - ② Here the parameters are the number of possible discrete symbols per sample (2, binary), and history length for TE (k = 1).
  - **3** Constructor syntax is different for Matlab/Octave/Python.



- Initialise the calculator prior to:
  - use, or
  - e-use (e.g. looping back from line 5 back to line 3 to examine different data).
  - 3 This clears PDFs ready for new samples.



- Supply the data to the calculator to construct PDFs:
  - addObservations() may be called multiple times;
  - Convert arrays into Java format:
    - From Matlab/Octave using our octaveToJavaIntArray(array), etc., scripts.
    - From Python using JArray(JInt, numDims)(array) for conversion or use numpy arrays directly, etc.

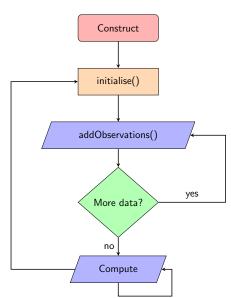


#### Compute the measure:

- Value is always returned in bits for discrete calculators.
- Result here approaches 0 bits for k = 1 (as written above), or 1 bit for k = 2, as destination is an XOR between the (random) source and it's own value from 2 time steps in the past.
- Other computations include:
  - ① computeLocalOfPreviousObservations() for local values
  - computeSignificance() to compute p-values of measures of predictability (see Appendix A5 of paper for description).

## Discrete Data – Usage Paradigm





# Auto Analyser GUI (code generator) – continuous



Next we generate a sample TE calculation on continuous data:

- Select Kraskov (KSG) estimator
- Select the data file 2coupledRandomCols-1.txt from the default directory in the Select popup.
- Leave source and destination columns
- Set the property k\_HISTORY to 2
  - You can hover on the properties to see their meaning and valid values
- Click Compute

## Auto Analyser GUI (code generator) - continuous



Next we generate a sample TE calculation on continuous data:

- Select Kraskov (KSG) estimator
- Select the data file 2coupledRandomCols-1.txt from the default directory in the Select popup.
- Leave source and destination columns
- Set the property k\_HISTORY to 2
  - You can hover on the properties to see their meaning and valid values
- Click Compute

Did everyone get the result 0.2906 nats?

### Auto Analyser GUI – discrete – code analysis



Let's examine the code that was generated.

Can you notice anything different to the discrete case?

## Auto Analyser GUI – discrete – code analysis



Let's examine the code that was generated.

Can you notice anything different to the discrete case?

Note: Continuous data (source and dest) represented as double[] arrays:

- for time-series measures, the array is indexed by time.
- of for multivariate time-series, we use double[][] arrays, indexed first by time then variable number.



```
// double[] source and dest defined and loaded earlier
TransferEntropyCalculator calc = new TransferEntropyCalculatorKraskov();
calc.setProperty(TransferEntropyCalculator.K_PROP_NAME, "2");
calc.initialise();
calc.setObservations(source, dest);
double result = calc.computeAverageLocalOfObservations();
```

- Construct the calculator, possibly providing parameters
  - Always check Javadocs for which parameters are required.
  - For continuous calculators, parameters may always be provided later (see next slide) to allow dynamic instantiation.
  - **3** Constructor syntax is different for Matlab/Octave/Python.



```
// double[] source and dest defined and loaded earlier
TransferEntropyCalculator calc = new TransferEntropyCalculatorKraskov();
calc.setProperty(TransferEntropyCalculator.K_PROP_NAME, "2");
calc.initialise();
calc.setUbservations(source, dest);
double result = calc.computeAverageLocalOfObservations();
```

- Set properties for the calculator (new method for continuous):
  - Formally: Check the Javadocs for available properties for each calculator;
    - In Auto Analyser GUI, you can hover on each parameter to read about it.
  - **2** E.g. here we set the embedding (history) length k=2 for the TE calculation.
  - Property names and values are always key-value pairs of String objects;
  - Only guaranteed to hold after the next intialise() call.
  - Properties can easily be extracted and set from a file (see Simple Demo 6).





```
// double[] source and dest defined and loaded earlier
TransferEntropyCalculator calc = new TransferEntropyCalculatorKraskov();
calc.setProperty(TransferEntropyCalculator.K_PROP_NAME, "2");
calc.initialise();
calc.setObservations(source, dest);
double result = calc.computeAverageLocalOfObservations();
```

- Initialise the calculator prior to:
  - use or re-use, as for Discrete.
  - This clears PDFs ready for new samples, and finalises any new property settings.
  - There may be several overloaded forms taking different properties in directly. E.g. for TE, calc.initialise(1) sets history length k = 1. We could also call calc.initialise(k, tau\_k, 1, 1\_tau, delay) to specify embedding dimensions and source-target delay. Check Javadocs for options here.



```
// double[] source and dest defined and loaded earlier
TransferEntropyCalculator calc = new TransferEntropyCalculatorKraskov();
calc.setProperty(TransferEntropyCalculator.K_PROP_NAME, "2");
calc.initialise();
calc.setObservations(source, dest);
double result = calc.computeAverageLocalOfObservations();
```

- Supply the data to the calculator to construct PDFs:
  - setObservations() may be called once, OR
  - call addObservations() multiple times, in between startAddObservations() and finaliseAddObservations() calls.
  - 3 Convert arrays into Java format:
    - From Matlab/Octave using our octaveToJavaDoubleArray(array), etc., scripts.
    - From Python using JArray(JDouble, numDims)(array) for conversion or use numpy arrays directly, etc.

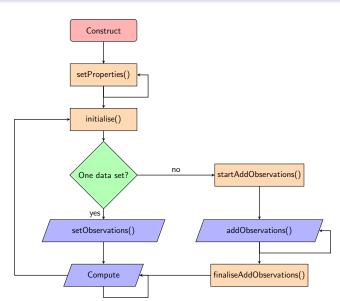


```
// double[] source and dest defined and loaded earlier
TransferEntropyCalculator calc = new TransferEntropyCalculatorKraskov();
calc.setProperty(TransferEntropyCalculator.K_PROP_NAME, "2");
calc.initialise();
calc.setUbservations(source, dest);
double result = calc.computeAverageLocalOfObservations();
```

- Compute the measure:
  - Value may be in *bits* (kernel) OR in *nats* (KSG, Gaussian) calculators.
  - Result here is 0.2906 nats since destination is correlated with the (random) source.
  - Other computations include:
    - ① computeLocalOfPreviousObservations() for local values
    - computeSignificance() to compute p-values of measures of predictability (see Appendix A5 of paper for description).

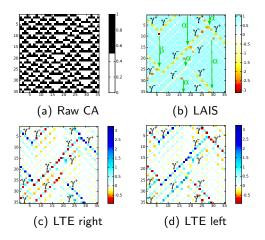
## Continuous Data – Usage Paradigm





## Many other demos – e.g. local dynamics in CAs





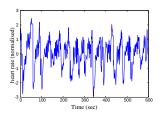
See PDF documentation for demos/octave/CellularAutomata/ to recreate, e.g. run GsoChapterDemo2013.m.

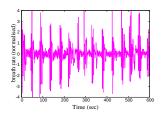




Let's consider the common information between heart rate & breath rate measurements (data from Rigney et al. (1993) in demos/data/SFI-heartRate\_breathVol\_bloodOx.txt).

#### Open the data file to take a look:





Heart rate

Breath rate



- Task on demos/data/SFI-heartRate\_breathVol\_bloodOx.txt:
  - Compute Mutual Information between the heart and breath rate time-series data in that example (samples 2350 to 3550, inclusive),
  - Using a Kraskov (KSG) estimator, algorithm 2, with 4 nearest neighbours.
- 4 How to approach it?



- Task on demos/data/SFI-heartRate\_breathVol\_bloodOx.txt:
  - Compute Mutual Information between the heart and breath rate time-series data in that example (samples 2350 to 3550, inclusive),
  - Using a Kraskov (KSG) estimator, algorithm 2, with 4 nearest neighbours.
- Mow to approach it?
  - Easy way: use the MI Auto Analyser GUI to generate code, then you can alter which samples it is using.



- ② Task on demos/data/SFI-heartRate\_breathVol\_blood0x.txt:
  - Compute Mutual Information between the heart and breath rate time-series data in that example (samples 2350 to 3550, inclusive),
  - Using a Kraskov (KSG) estimator, algorithm 2, with 4 nearest neighbours.
- How to approach it?
  - Easy way: use the MI Auto Analyser GUI to generate code, then you can alter which samples it is using.
  - More challenging: Start from KSG TE demo on this data set, in your preferred environment, and modify it to compute MI:
    - demos/java/infodynamics/java/schreiberTransferEntropyExamples/-HeartBreathRateKraskovRunner.java
    - demos/octave/SchreiberTransferEntropyExamples/runHeartBreathRateKraskov.m
    - demos/python/SchreiberTransferEntropyExamples/runHeartBreathRateKraskov.py
    - 4 Hint 1: A KSG MI calculator is used in Simple Demo 6.
    - **6** Hint 2: Remember the usage paradigm on slide **62**.

Introduction Information dynamics Estimators Overview of JIDT Demos Exercise Wrap-up

#### Exercise

Outline



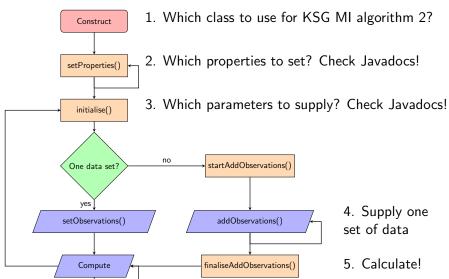
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    - demos/java/infodynamics/java/schreiberTransferEntropyExamples/-HeartBreathRateKraskovRunner.java
    - @ demos/octave/SchreiberTransferEntropyExamples/runHeartBreathRateKraskov.m
    - demos/python/SchreiberTransferEntropyExamples/runHeartBreathRateKraskov.py
    - Mint 1: A KSG MI calculator is used in Simple Demo 6.
    - **6** Hint 2: Remember the usage paradigm on slide **62**.

Answer: **0.134**  $\pm$  **0.002 nats**; if you use all data: 0.0994  $\pm$  0.0005.



## Exercise – Remember the usage paradigm!





### Exercise – sample answer



```
import infodynamics.measures.continuous.kraskov.
     MutualInfoCalculatorMultiVariateKraskov2;
3 // New KSG MI (algorithm 2) calculator:
  miCalc = new
     MutualInfoCalculatorMultiVariateKraskov2();
  miCalc.initialise(1,1); // univariate
     calculation
  miCalc.setProperty("k", "4"); // 4 nearest
     neighbours
  miCalc.setObservations(heart, chestVol);
  double miHeartToBreath = miCalc.
     computeAverageLocalOfObservations();
```

#### **Debrief**



How did you find the exercise?

Was it difficult? Which parts?

Did you know where to find the information you needed?

Any questions arising from the exercise?

## Exercise – Challenge task 1



Extend to compute MI(heart;breath), for a variety of **lags** between the two time-series. E.g., investigate lags of [0, 1, ..., 14, 15].

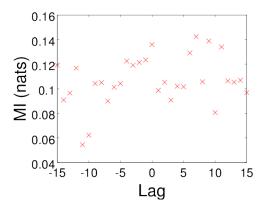
#### **HINT**: You could either:

- shift the time-series with respect to eachother to affect the lag, or
- (cleaner) check out the available properties for this MI calculator in the Auto Analyser GUI or the Javadocs.
   (Challenge: what to do if you want to use negative lags, i.e. a positive lag from breath to heart, with this property?)

## Exercise – Challenge task 1



Extend to compute MI(heart; breath), for a variety of lags between the two time-series. E.g., investigate lags of [0, 1, ..., 14, 15].



What would you interpret from the results? Can you think of some logical further investigations here?





What I wanted you to take away today:

- Understand measures of information dynamics;
- Be able to obtain and install JIDT distribution;
- Be able to use the GUI Auto Analyser;
- Understand the code it generates in your chosen environment;
- Be able to modify sample scripts for new analysis;
- Know how and where to seek support information (wiki, Javadocs, mailing list, twitter).



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Did we get there?



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Did we get there?
Did you get what you came here for?



What I wanted you to take away today:

- Understand measures of information dynamics;
- Be able to obtain and install JIDT distribution;
- Be able to use the GUI Auto Analyser;
- Understand the code it generates in your chosen environment;
- Be able to modify sample scripts for new analysis;
- Know how and where to seek support information (wiki, Javadocs, mailing list, twitter).

Did we get there?
Did you get what you came here for?
Any other questions?

## Final messages

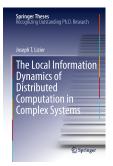


We're seeking PhD students for our Complex Systems group at University of Sydney – talk to me if interested

## Final messages



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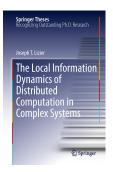


"The local information dynamics of distributed computation in complex systems", J. T. Lizier, Springer, Berlin (2013).

## Final messages

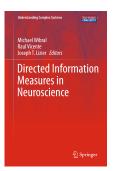


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"The local information dynamics of distributed computation in complex systems", J. T. Lizier, Springer, Berlin (2013).

"Directed information measures in neuroscience", edited by M. Wibral, R. Vicente and J. T. Lizier, Springer, Berlin (2014).



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