

#### RADIATIVE TRANSFER IN GALAXIES

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#### **Abstract**

In this thesis, we present a novel algorithm for computing the radiation field in astrophysical simulations.



# Acknowledgements

Thank you to all that helped.

"Some sort of quote?"

Albert Einstein (1879-1955)

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# Introduction

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# **Numerical Methods**

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#### The Numerical Method

In the absence of absorbing material, the problem of radiative transfer reduces down to that of gravity. As such, the tree-algorithm for calculating gravity can be used (?).

- A tree can be used to partition space.
- Each level of the tree holds finer partitions of the volume. See figure ??
- Each node of the tree contains accumulated information about the tree below it (total mass, etc.).
- In order to calculate gravity on a particular leaf (bucket), you can interact with the moment of another cell (??).
- To decide what level of the tree to interact with, you can define an opening angle/radius,  $\theta$ . If a cell is smaller than this opening angle (the distribution of matter inside the cell is contained within a small enough angle on the sky), the entire cell can be used in the force calculation. If not, you must consider the child nodes separately. See equation ??.

- On average, the number of interactions a each particle will have is  $\log N$ , where N is the total number of particles. Thus, the force calculation for the whole simulation scales as  $N \log N$ . Note that lowering  $\theta$  shifts the number of calculations that are approximated by large cells to smaller cells, and thus if  $\theta$  is very small, the code approached scaling of order  $N^2$ .
- In the case of radiation, the math is very similar (See eq??). However, since radiation does not cancel like forces, the dipole moment does not disappear and a rougher approximation is possible (wording wrong, fix this).
- In this case, the interaction scales as  $N_{\text{sink}} \log N_{\text{source}}$ . However, assuming the full tree is still used, the tree-build still scales as  $N \log N$ .

- 3.1 Tree Data Structures
- 3.1.1 kd-Tree
- 3.2 Building a Radiation Tree
- 3.2.1 Criteria for Opening Cells
- 3.2.2 Accumulating Cell Properties
- 3.3 The Simple Case No Absorption
- 3.3.1 Exchanging Radiation
- 3.4 Adding Absorption
- 3.4.1 Making Use of the Tree
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# **Discussion**

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# **Conclusions**

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# Appendix A