FRQ Packet #4 - Riemann Sums

2010 AP Calculus AB FRQ (Form A) Question 2

Calculator - In Class

t (hours)	0	2	5	7	8
E(t) (hundreds of entries)	0	4	13	21	23

A zoo sponsored a one-day contest to name a new baby elephant. Zoo visitors deposited entries in a special box between noon (t = 0) and 8 P.M. (t = 8). The number of entries in the box t hours after noon is modeled by a differentiable function E for $0 \le t \le 8$. Values of E(t), in hundreds of entries, at various times t are shown in the table above.

- (a) Use the data in the table to approximate the rate, in hundreds of entries per hour, at which entries were being deposited at time t = 6. Show the computations that lead to your answer.
- (b) Use a trapezoidal sum with the four subintervals given by the table to approximate the value of $\frac{1}{8} \int_0^8 E(t) dt$. Using correct units, explain the meaning of $\frac{1}{8} \int_0^8 E(t) dt$ in terms of the number of entries.
- (c) At 8 P.M., volunteers began to process the entries. They processed the entries at a rate modeled by the function P, where $P(t) = t^3 30t^2 + 298t 976$ hundreds of entries per hour for $8 \le t \le 12$. According to the model, how many entries had not yet been processed by midnight (t = 12)?
- (d) According to the model from part (c), at what time were the entries being processed most quickly? Justify your answer.

2006 AP Calculus AB FRQ (Form A) Question 4

No Calculator - In Class

t (seconds)	0	10	20	30	40	50	60	70	80
v(t) (feet per second)	5	14	22	29	35	40	44	47	49

Rocket A has positive velocity v(t) after being launched upward from an initial height of 0 feet at time t = 0 seconds. The velocity of the rocket is recorded for selected values of t over the interval $0 \le t \le 80$ seconds, as shown in the table above.

- (a) Find the average acceleration of rocket A over the time interval 0 ≤ t ≤ 80 seconds. Indicate units of measure.
- (b) Using correct units, explain the meaning of $\int_{10}^{70} v(t) dt$ in terms of the rocket's flight. Use a midpoint Riemann sum with 3 subintervals of equal length to approximate $\int_{10}^{70} v(t) dt$.
- (c) Rocket *B* is launched upward with an acceleration of $a(t) = \frac{3}{\sqrt{t+1}}$ feet per second per second. At time t = 0 seconds, the initial height of the rocket is 0 feet, and the initial velocity is 2 feet per second. Which of the two rockets is traveling faster at time t = 80 seconds? Explain your answer.

2009 AP Calculus AB FRQ (Form B) Question 6

No Calculator - HW Not Timed

t (seconds)	0	8	20	25	32	40
v(t) (meters per second)	3	5	-10	-8	-4	7

The velocity of a particle moving along the x-axis is modeled by a differentiable function v, where the position x is measured in meters, and time t is measured in seconds. Selected values of v(t) are given in the table above. The particle is at position x = 7 meters when t = 0 seconds.

- (a) Estimate the acceleration of the particle at t = 36 seconds. Show the computations that lead to your answer. Indicate units of measure.
- (b) Using correct units, explain the meaning of $\int_{20}^{40} v(t) dt$ in the context of this problem. Use a trapezoidal sum with the three subintervals indicated by the data in the table to approximate $\int_{20}^{40} v(t) dt$.
- (c) For $0 \le t \le 40$, must the particle change direction in any of the subintervals indicated by the data in the table? If so, identify the subintervals and explain your reasoning. If not, explain why not.
- (d) Suppose that the acceleration of the particle is positive for 0 < t < 8 seconds. Explain why the position of the particle at t = 8 seconds must be greater than x = 30 meters.

2007 AP Calculus AB FRQ (Form A) Question 5

No Calculator - HW Timed 15 minutes

t (minutes)	0	2	5	7	11	12
r'(t) (feet per minute)	5.7	4.0	2.0	1.2	0.6	0.5

The volume of a spherical hot air balloon expands as the air inside the balloon is heated. The radius of the balloon, in feet, is modeled by a twice-differentiable function r of time t, where t is measured in minutes. For 0 < t < 12, the graph of r is concave down. The table above gives selected values of the rate of change, r'(t), of the radius of the balloon over the time interval $0 \le t \le 12$. The radius of the balloon is 30 feet when

- t = 5. (Note: The volume of a sphere of radius r is given by $V = \frac{4}{3}\pi r^3$.)
- (a) Estimate the radius of the balloon when t = 5.4 using the tangent line approximation at t = 5. Is your estimate greater than or less than the true value? Give a reason for your answer.
- (b) Find the rate of change of the volume of the balloon with respect to time when t = 5. Indicate units of measure.
- (c) Use a right Riemann sum with the five subintervals indicated by the data in the table to approximate $\int_0^{12} r'(t) dt$. Using correct units, explain the meaning of $\int_0^{12} r'(t) dt$ in terms of the radius of the balloon.
- (d) Is your approximation in part (c) greater than or less than $\int_0^{12} r'(t) dt$? Give a reason for your answer.

2005 AP Calculus AB FRQ (Form A) Question 3

Calculator - HW Timed 15 minutes

Distance x (cm)	0	1	5	6	8
Temperature $T(x)$ (°C)	100	93	70	62	55

A metal wire of length 8 centimeters (cm) is heated at one end. The table above gives selected values of the temperature T(x), in degrees Celsius (°C), of the wire x cm from the heated end. The function T is decreasing and twice differentiable.

- (a) Estimate T'(7). Show the work that leads to your answer. Indicate units of measure.
- (b) Write an integral expression in terms of T(x) for the average temperature of the wire. Estimate the average temperature of the wire using a trapezoidal sum with the four subintervals indicated by the data in the table. Indicate units of measure.
- (c) Find $\int_0^8 T'(x) dx$, and indicate units of measure. Explain the meaning of $\int_0^8 T'(x) dx$ in terms of the temperature of the wire.
- (d) Are the data in the table consistent with the assertion that T''(x) > 0 for every x in the interval 0 < x < 8? Explain your answer.