

Data Structures/Tradeoffs

Data Structures

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It is important to fully understand the problem you need to solve before choosing a data structure because each structure is optimized for a particular job. Hash tables, for example, favor fast lookup times over memory usage while arrays are compact and inflexible. Other structures, such as stacks, are optimized to enforce rigid rules on how data is added, removed and accessed throughout the program execution. A good understanding of data structures is fundamental because it gives us the tools for thinking about a program's behavior in a structured way.

[TODO:]

Use asymptotic behaviour to decide, most importantly seeing how the structure will be used: an infrequent operation does not need to be fast if it means everything else will be much faster

[TODO:]

Can use a table like this one to compare the asymptotic behaviour of every structure for every operation on it.

Sequences (aka lists):

	Array	Dynamic Array	Array Deque	Singly Linked List	Double Linked List
Push (Front)	-	$O(n)$	$O(1)$	$O(1)$	$O(1)$
Pop (Front)	-	$O(n)$	$O(1)$	$O(1)$	$O(1)$
Push (Back)	-	$O(1)$	$O(1)$	$O(n)$, maybe $O(1)^*$	$O(1)$
Pop (Back)	-	$O(1)$	$O(1)$	$O(n)$	$O(1)$
Insert before (given iterator)	-	$O(n)$	$O(n)$	$O(n)$	$O(1)$
Delete (given iterator)	-	$O(n)$	$O(n)$	$O(n)$	$O(1)$
Insert after (given iterator)	-	$O(n)$	$O(n)$	$O(1)$	$O(1)$
Delete after (given iterator)	-	$O(n)$	$O(n)$	$O(1)$	$O(1)$
Get nth element (random access)	$O(1)$	$O(1)$	$O(1)$	$O(n)$	$O(n)$
Good for implementing stacks	no	yes (back is top)	yes	yes (front is top)	yes
Good for implementing queues	no	no	yes	maybe*	yes
C++ STL	<code>std::array</code>	<code>std::vector</code>	<code>std::deque</code>	<code>std::forward_list</code>	<code>std::list</code>
Java Collections	<code>java.util.Array</code>	<code>java.util.ArrayList</code>	<code>java.util.ArrayDeque</code>	-	<code>java.util.LinkedList</code>

singly-linked lists can push to the back in $O(1)$ with the modification that you keep a pointer to the last node

Associative containers (sets, associative arrays):

	Sorted Array	Sorted Linked List	Self-balancing Binary Search Tree	Hash Table
Find key	$O(\log n)$	$O(n)$	$O(\log n)$	$O(1)$ average $O(n)$ worst
Insert element	$O(n)$	$O(n)$	$O(\log n)$	$O(1)$ average $O(n)$ worst
Erase key	$O(n)$	$O(n)$	$O(\log n)$	$O(1)$ average $O(n)$ worst
Erase element (given iterator)	$O(n)$	$O(1)$	$O(1)$	$O(1)$
Can traverse in sorted order?	yes	yes	yes	no
Needs	comparison function	comparison function	comparison function	hash function
C++ STL	-	-	<code>std::set</code> <code>std::map</code> <code>std::multiset</code> <code>std::multimap</code>	<code>_gnu_cxx::hash_set</code> <code>_gnu_cxx::hash_map</code> <code>_gnu_cxx::hash_multiset</code> <code>_gnu_cxx::hash_multimap</code>
Java Collections	-	-	<code>java.util.TreeSet</code> <code>java.util.TreeMap</code>	<code>java.util.HashSet</code> <code>java.util.HashMap</code>

- Please correct any errors

Various Types of Trees

	Binary Search	AVL Tree	Binary Heap (min)	Binomial Queue (min)
Insert element	$O(\log n)$	$O(\log n)$	$O(\log n)$	$O(1)$ (on average)
Erase element	$O(\log n)$	$O(\log n)$	unavailable	unavailable
Delete min element	$O(\log n)$	$O(\log n)$	$O(\log n)$	$O(\log n)$
Find min element	$O(\log n)$	$O(\log n)$	$O(1)$	$O(\log n)$ (can be $O(1)$ if ptr to smallest)
Increase key	unavailable	unavailable	$O(\log n)$	$O(\log n)$
Decrease key	unavailable	unavailable	$O(\log n)$	$O(\log n)$
Find	$O(\log n)$	$O(\log n)$	unavailable	unavailable
Delete element	$O(\log n)$	$O(\log n)$	unavailable	unavailable
Create	$O(1)$	$O(1)$	$O(1)$	$O(1)$
find kth smallest	$O(\log n)$	$O(\log n)$	$O((k-1)*\log n)$	$O(k*\log n)$

Hash table:

	Hash table (hash map)
Set Value	$\Omega(1)$, $O(n)$
Get Value	$\Omega(1)$, $O(n)$
Remove	$\Omega(1)$, $O(n)$

[TODO:]
Can also add a table that specifies the best structure for some specific need
e.g. For queues, double linked. For stacks, single linked. For sets, hash tables. etc...

[TODO:]
Could also contain table with space complexity information (there is a significant cost
in using hash tables or lists implemented via arrays, for example).

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