

CSE-103

DISCRETE MATHEMATICS

ASSIGNMENT NO : *06 (Out of the book Assignment #4)*
ASSIGNED TO : *PROF. DR. M. KAYKOBAD*

DATE OF ASSIGNED :
 30-11-2018
DATE OF SUBMISSION :
 07-12-2018

SUBMITTED BY

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STD ID : *1705070*

SECTION : *B*

LEVEL-1 TERM-2

(Out of the text assignment #3)

Problem Statement :

An old father told his son his son that he stored some gold in a forest. The son must find identical trees A and B, and a stone S. He then should walk from S to A and equal distance perpendicularly towards the other tree to find a point C. He should again come back to the stone S and do the same with respect to the other tree B to obtain a point D. Gold is just in the middle of the line joining C and D. The son could find trees but not the stone. How could he find the gold?

Answer

It is not important where is the stone, because wherever the stone is , the treasure is always in the same position. Here is my prove:

For the prove , let draw a square imaging that AB , here A and B is the point where the tree is located , is the diagonal of the square .

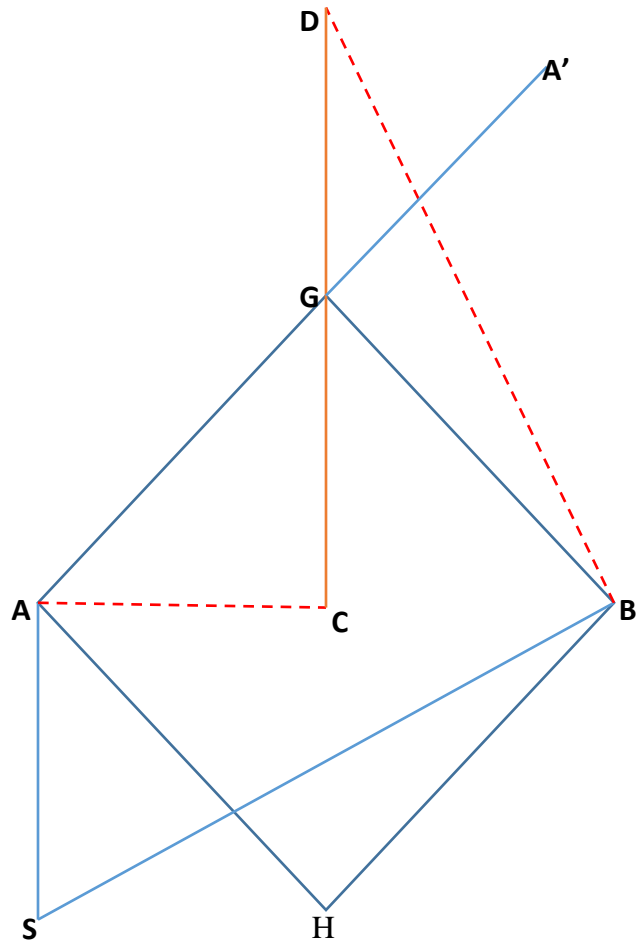
Suppose that the stone is at S . Now draw SA from S to A and SB from S to B and then AC from A to C and BD from B to D so that $AC = SA$ and $BD = SB$

Now we will prove that G is midpoint of CD , that's all . And thus G point contains treasure.

$\angle SAC = \angle GAH$ [both are 90 degrees]

Or $\angle SAH = \angle CAG$ [subtracting $\angle HAC$]

Now in triangle SAH and triangle CAG ,



$$SA = CA$$

$$HA = GA \text{ and } \angle SAH = \angle CAG$$

So they are compatible hence

$$SH = CG$$

$$\text{and } \angle AHS = \angle AGC \quad \dots\dots\dots (1)$$

$$\text{Again } \angle SBD = \angle HBG \text{ So } \angle SBH = \angle DBG \quad \dots\dots\dots [\text{subtracting } \angle SBG]$$

Then in triangle SBH and triangle DBG

$$SB = DB$$

$$HB = GB \text{ and } \angle SBH = \angle DBG$$

So they are compatible hence

$$HS = GD$$

$$\text{and } \angle SHB = \angle DGB \quad \dots\dots\dots (2)$$

$$\text{Also } \angle SHB = \angle SHA + \angle AHB$$

$$\text{Or } \angle DGB = \angle AGC + 90 \quad \dots\dots\dots [\text{from (1) and (2) }]$$

$$\text{Or } \angle DGB - 90 = \angle AGC$$

$$\text{Or } \angle DGA' = \angle AGC \quad \dots\dots\dots [A' \text{ is in extension of AG, so } \angle A'GB = 90]$$

So these two are vertical angles hence D, G, C are collinear and

$$\text{as } DG = GC \quad \dots\dots\dots [\text{from (1) and (2)}]$$

so G is the midpoint of CD. So G is the point where the treasure is located

according to the question . So the sons had no need to find the stone , if they can find the trees they can find the gold . But there is a possibility that the gold is not at the position G but it is at the position of opposite of G and from figure this point is H (it can prove using the point S at the side of G is located).

This condition is same for any position of S. (Proved)

