

Understanding Lifetimes

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Outline

Lifetimes Concepts

Phases of the NLL

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Lifetimes Concepts

Where are the lifetimes from

What is the lifetimes

Phases of the NLL

Lifetimes

```
{
  let r;                                // -----+-- 'a
  {                                     //      |
    let x = 5;                         // -+-- 'b  |
    r = &x;                           //  |      |
  }                                   // -+      |
                                     //      |
  println!("r: {}", r);               //      |
}                                     // -----+
```



?



```
{  
    let r;  
  
    {  
        let x = 5;  
  
        r = &x;  
  
    }  
  
    println!("{}", r);  
}
```

```
{  
    let r;  
  
    {  
        let x = 5;  
        r = &x  
        ^^^^^^ borrowed value does not live long enough  
    }  
    - `x` dropped here while still borrowed  
  
    println!("{}", r);  
    - borrow later used here  
}
```


Rust 2018

```
{  
    let r;  
  
    {  
        let x = 5;  
        r = &x  
        ^^^^^ borrowed value does not live long enough  
    }  
    - `x` dropped here while still borrowed  
  
    println!("{}", r);  
}
```

- borrowed value needs to live until here

Rust 2015

```
{  
  let r;  
  
  {  
    let x = 5;  
  
    r = &x;  
  
    println!("{}", r);  
  }  
}
```




```
{  
  let r;  
  
  {  
    let x = 5;  
  
    r = &x;  
  
    println!("{}", r);  
  }  
}
```

move to

Rust 2018 

```
{  
  let r;  
  {  
    let x = 5;
```

Rust 2015



```
    r = &x  
    ^^^^^^ borrowed value does not live long enough  
    println!("{}", r);
```

```
  }  
  - `x` dropped here while still borrowed
```

```
}  
- borrowed value needs to live until here
```

Where are the Lifetimes from?

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Borrow

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```
let foo = &bar;
```

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```
let foo:&'foo T = &'bar bar;
```

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let foo:&'foo T;  
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Where are the Lifetimes from?

Borrow

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let foo:&'foo T;  
  
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```

A **Borrow** will generate a **reference**,
and this reference will be tagged with **a Lifetimes**

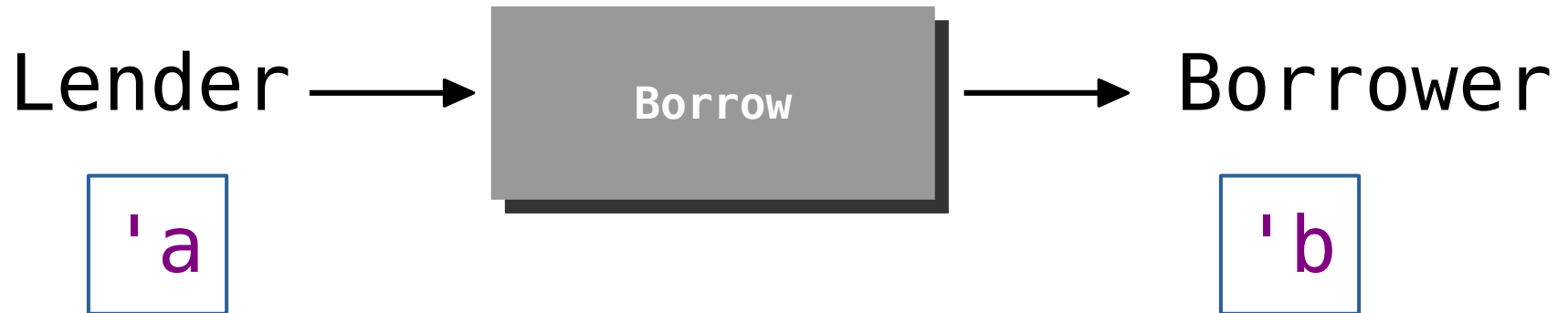
Subtyping

- **Notation** : $'a : 'b$
- **Meaning** : Lifetimes $'a$ is outlives Lifetimes $'b$

Subtyping

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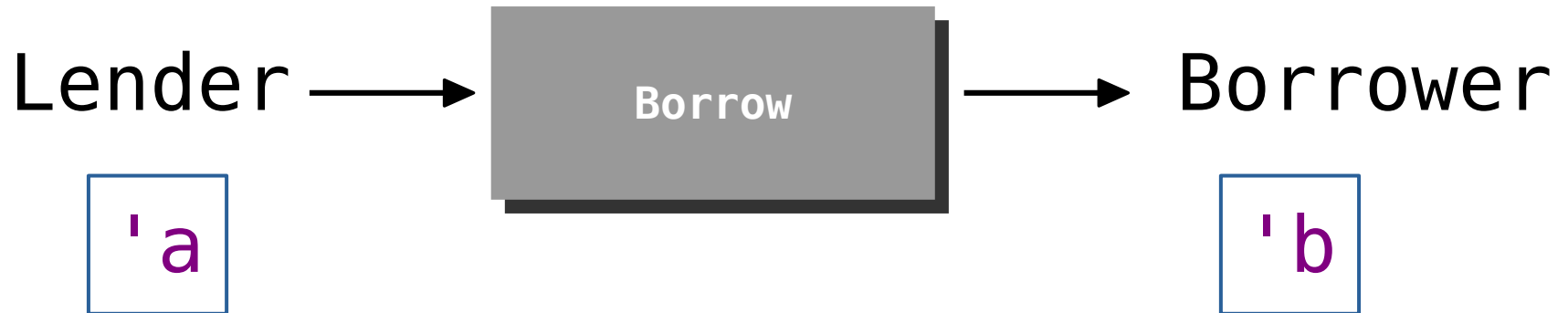
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Subtyping

- **Notation** : $'a : 'b$

- **Meaning** : Lifetimes $'a$ is outlives Lifetimes $'b$



- **Example** : `let p: $&'p$ T = $&'foo$ foo;`

Then we say: $'foo : 'p$

What is Lifetimes ?

- Definition:

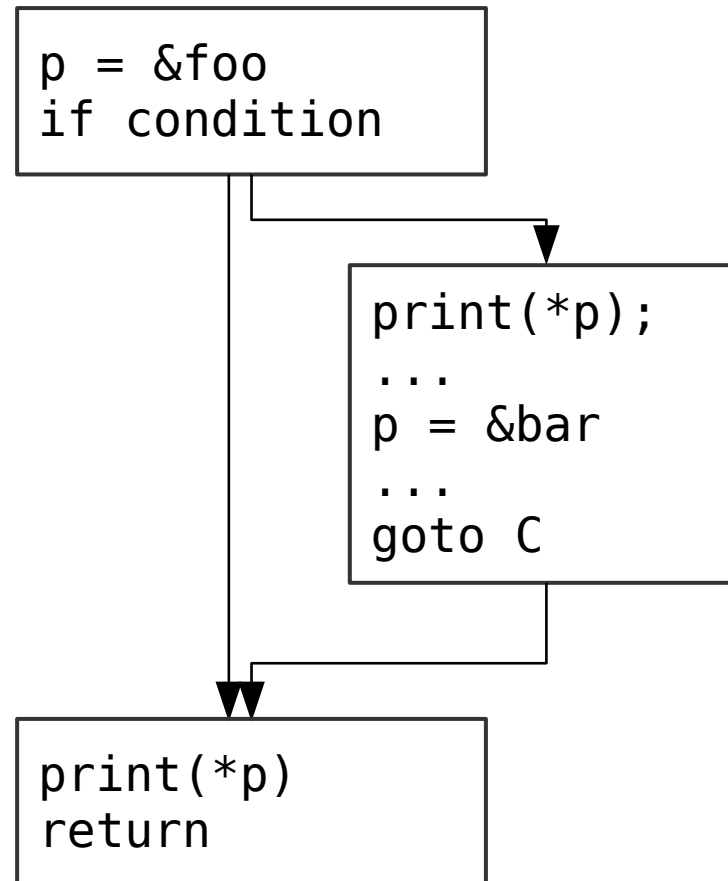
What is Lifetimes ?

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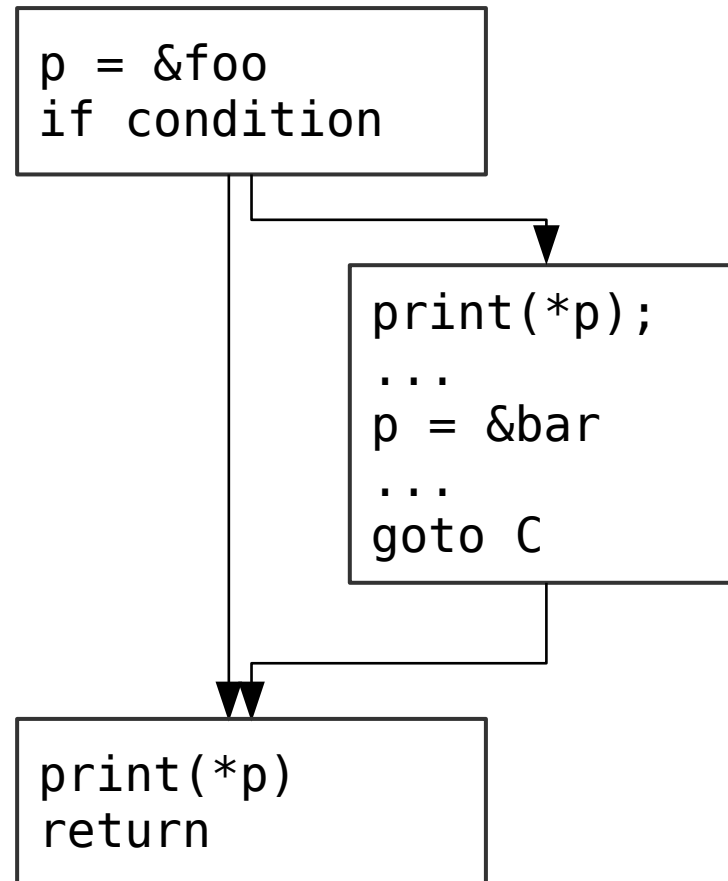
```
let foo: T = ...;  
let bar: T = ...;  
  
let mut p = &foo;  
  
if condition {  
    print(*p);  
    p = &bar;  
}  
  
print(*p);
```



What is Lifetimes ?

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```
let foo: T = ...;  
let bar: T = ...;  
  
let mut p = &'foo foo;  
  
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What is Lifetimes ?

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```
let foo: T = ...;  
let bar: T = ...;
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```
let mut p = &'foo foo;
```

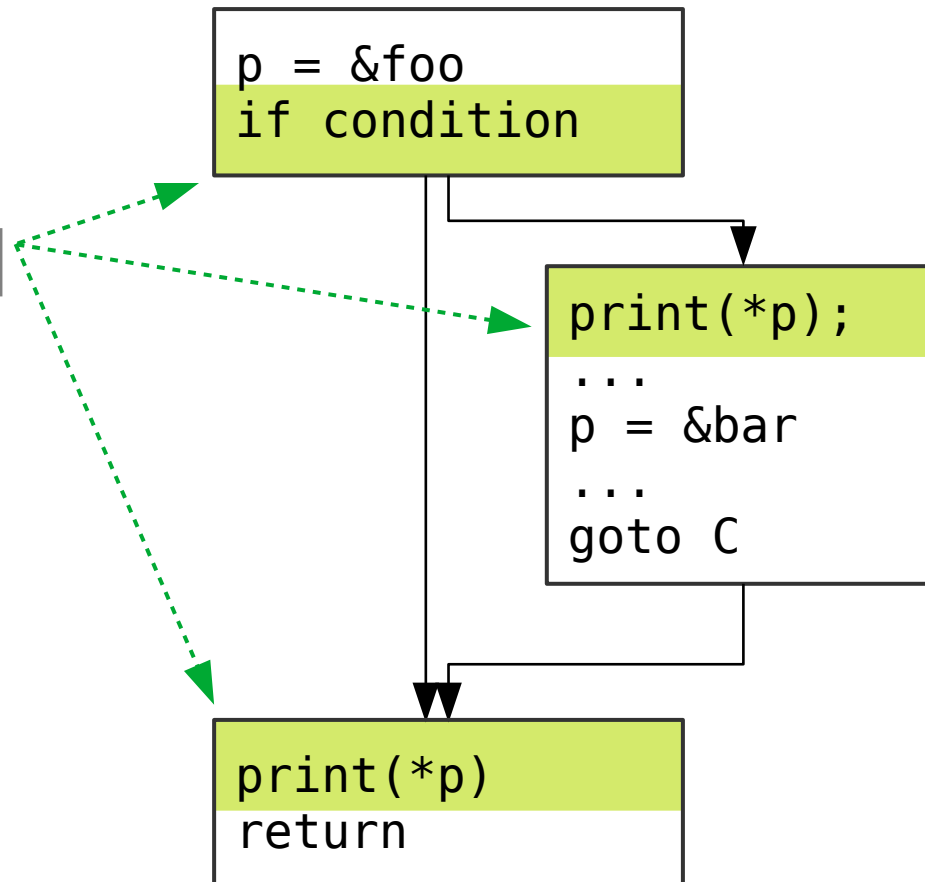
```
if condition {
```

```
    print(*p);
```

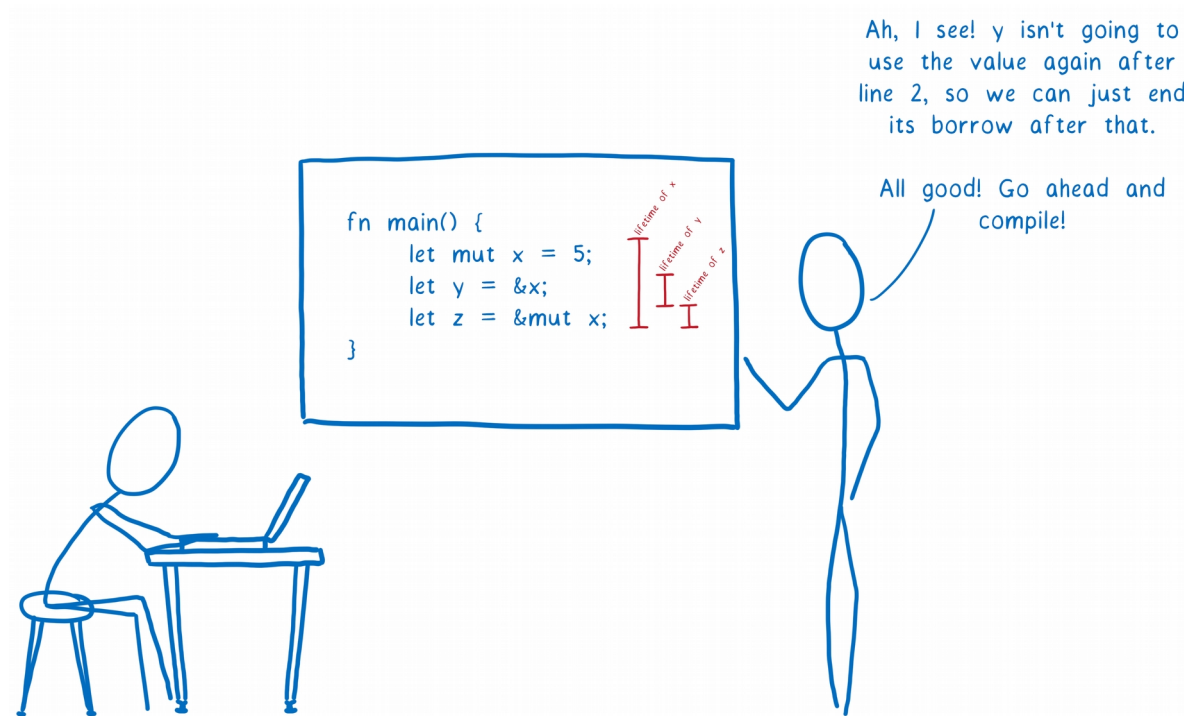
```
    p = &bar;
```

```
}
```

```
print(*p);
```



NLL



```
let mut s = "hello".to_string();  
let mut c = || s += " world";  
c();  
println!("{}", s);
```

```
let mut s = "hello".to_string();
```

```
let mut c = || s += ' world';
```

Borrow as **mut**

```
c();
```

```
println!("{}", s);
```

Borrow as **immut**

```

fn process_or_default(map: &mut HashMap<usize, String>,
                      key: usize)
{
    match map.get_mut(&key) {
        Some(value) => {
            process(value);
            return;
        }

        None => {
            map.insert(key, V::default());
        }
    }
}

```

```
fn process_or_default(map: &mut HashMap<usize, String>,
                      key: usize)
{
    match map.get_mut(key) {
        Some(value) => {
            process(value);
            return;
        }
        None => {
            map.insert(key, V::default());
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    }
}
```

Borrow as **mut**

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        }
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            map.insert(key, V::default());
        }
    }
}
```

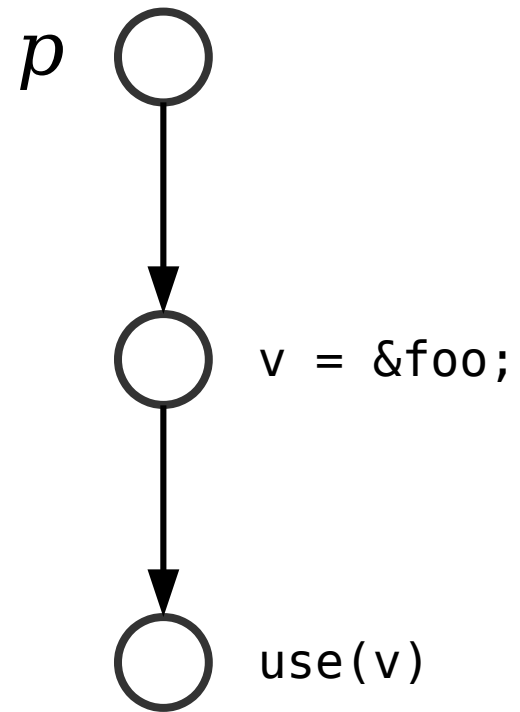
Borrow as **mut**

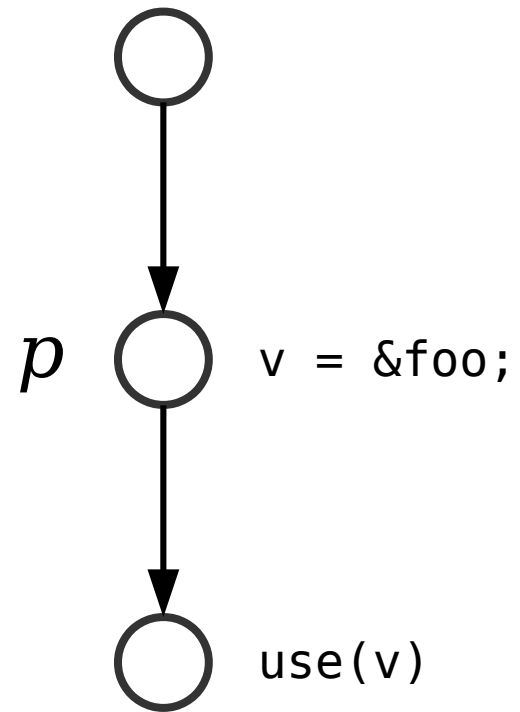
Borrow as **mut**

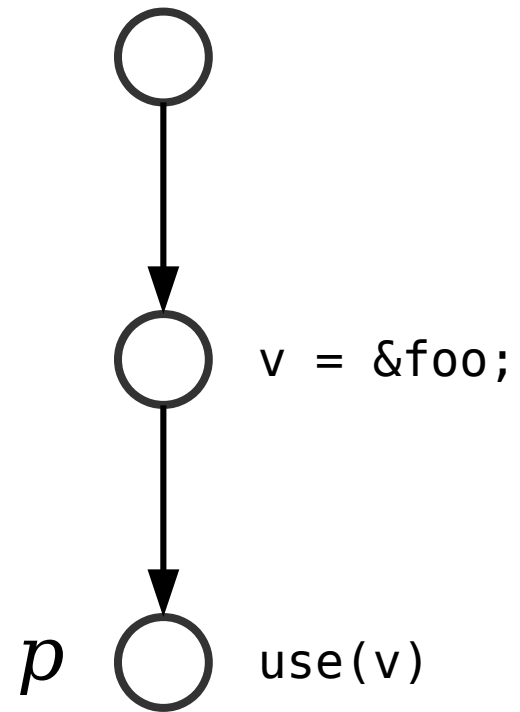
Liveness

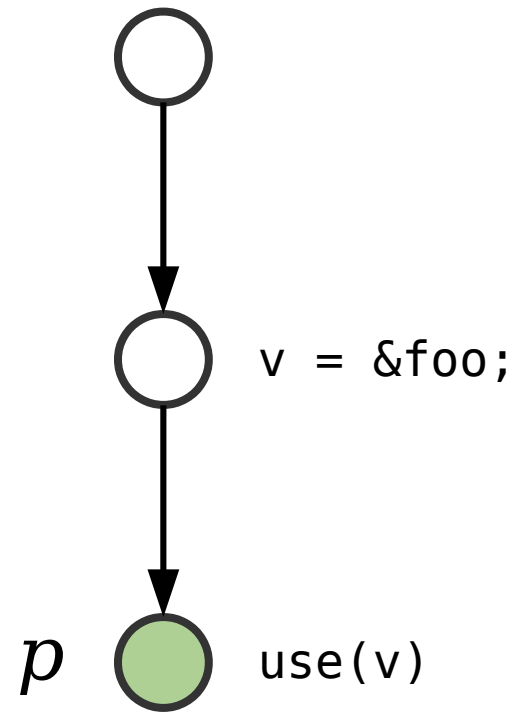
- **Meaning :**

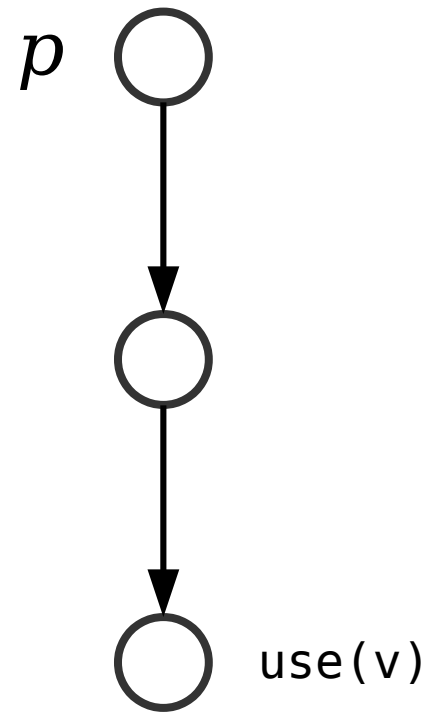
a variable v is live at point p if and only if there exists a path in CFG from p to a use of v along which v is not redefined.

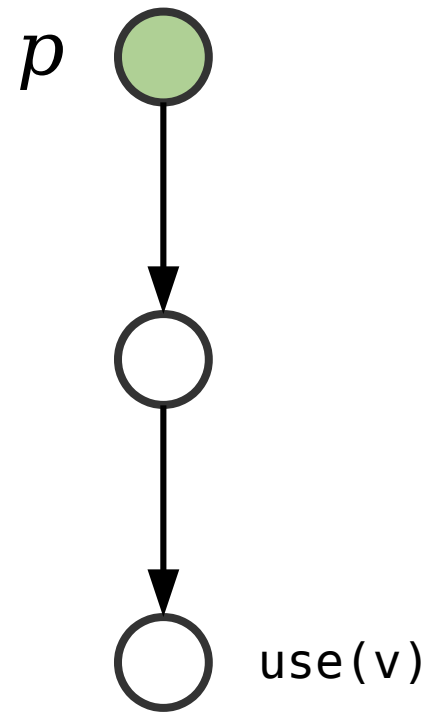


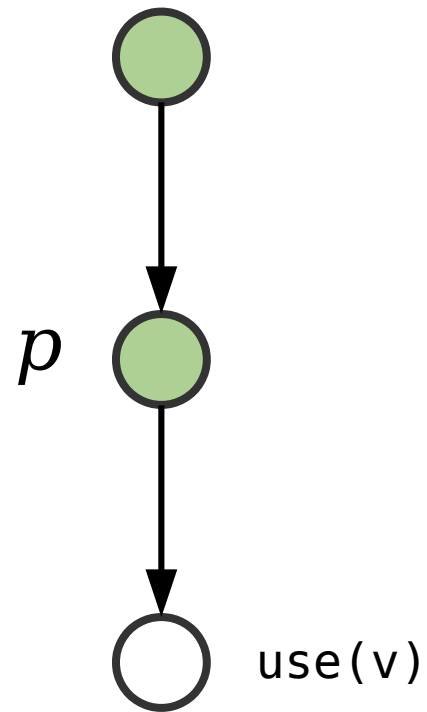


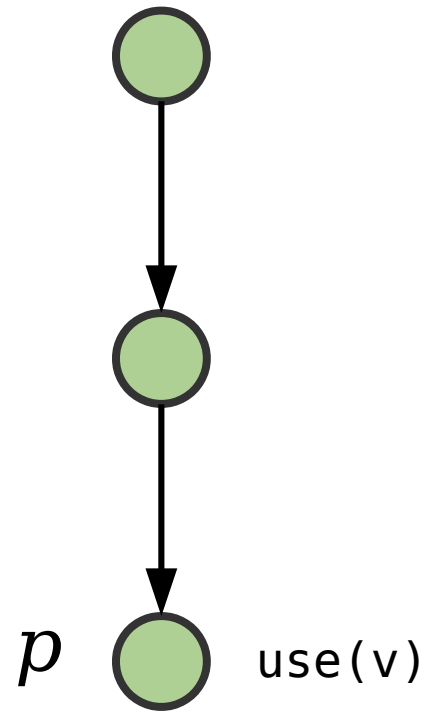








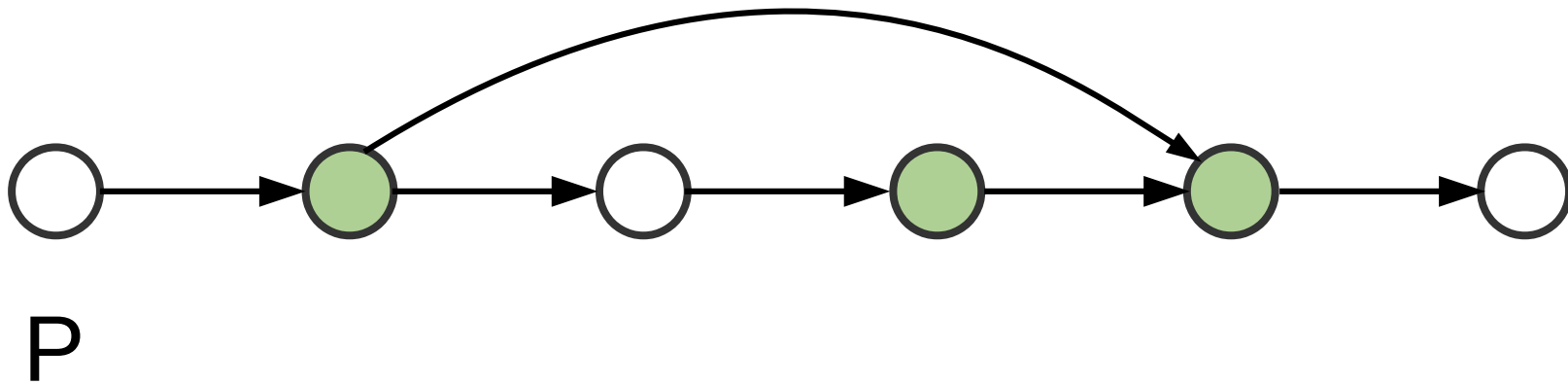
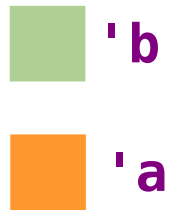




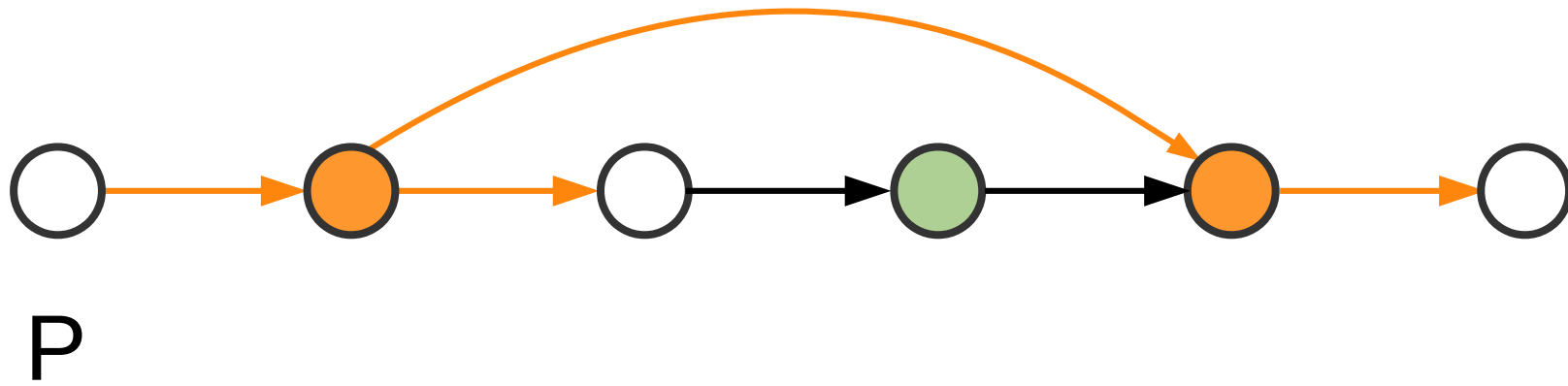
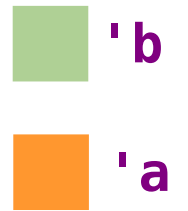
Location-aware Subtyping

- **Notation** : $('a : 'b) @ P$
- **Meaning** : Lifetimes $'a$ must include all points in $'b$
that are reachable from location P

('a : 'b) @ P



('a : 'b) @ P



Phases of NLL

1. Building Liveness and Constraints



2. Solving Constraints



3. Compute Loans in Scope



4. Check action and report Error

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Phases of NLL

('a : 'b) @ P

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Phases of NLL

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a fixed-point iteration algorithm

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Phases of NLL

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Borrow expressions ←

3. Compute **Loans** in Scope



4. Check action and report Error

Phases of NLL

1. Building Liveness and Constraints



2. Solving Constraints

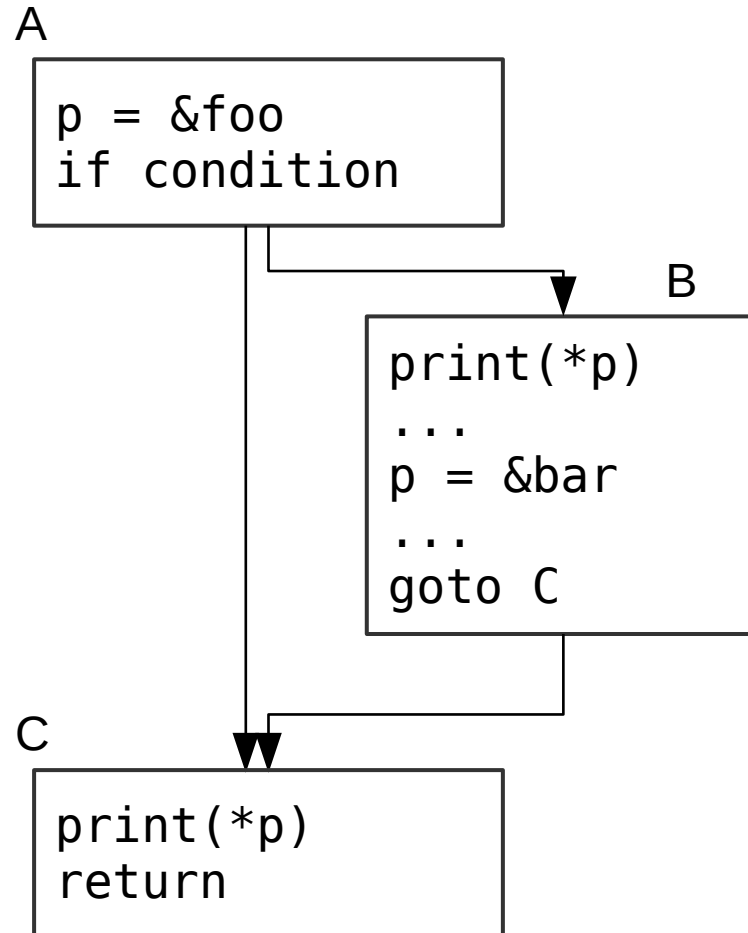


3. Compute Loans in Scope



4. Check action and report Error

Liveness

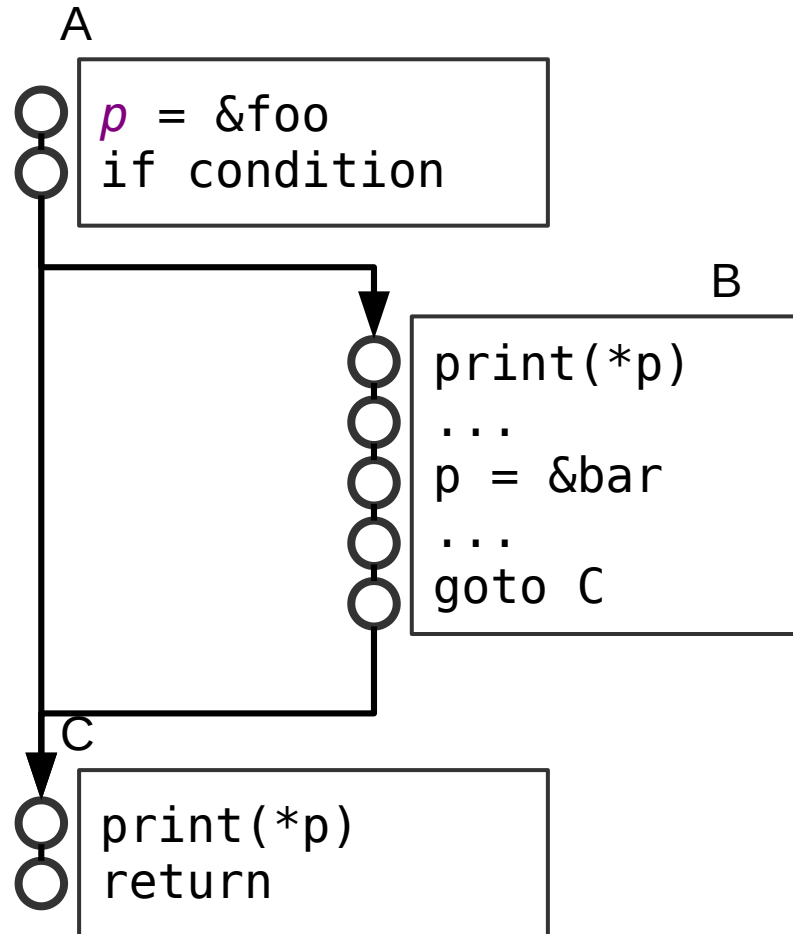


p : { }

foo : { }

bar : { }

Liveness

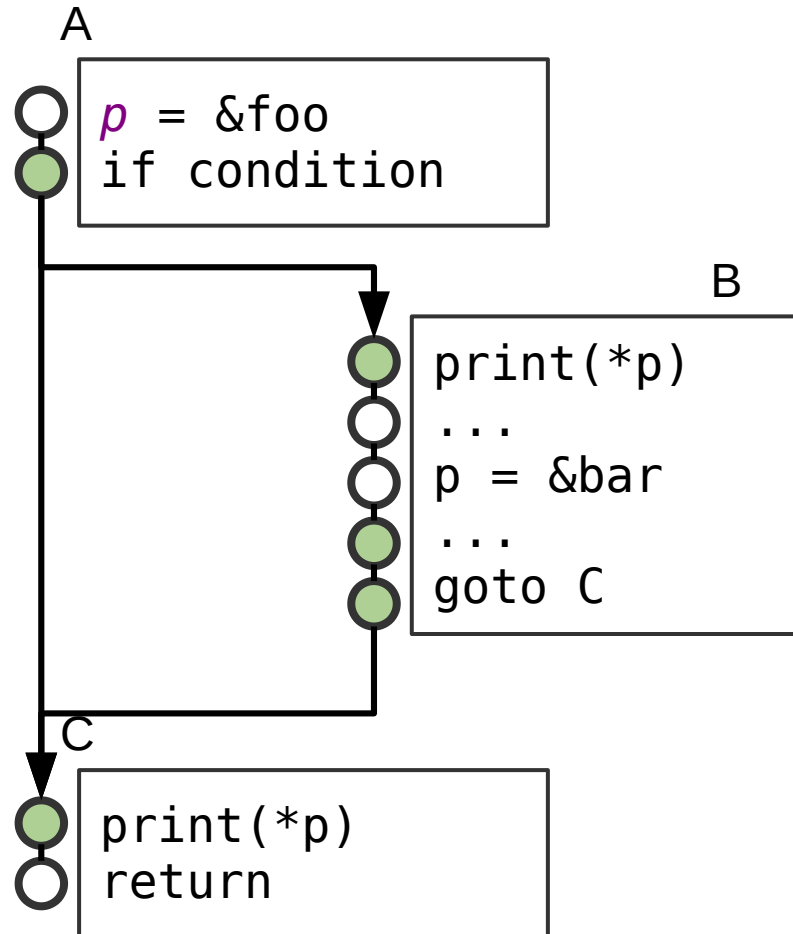


$p : \{ \}$

$\text{foo} : \{ \}$

$\text{bar} : \{ \}$

Liveness

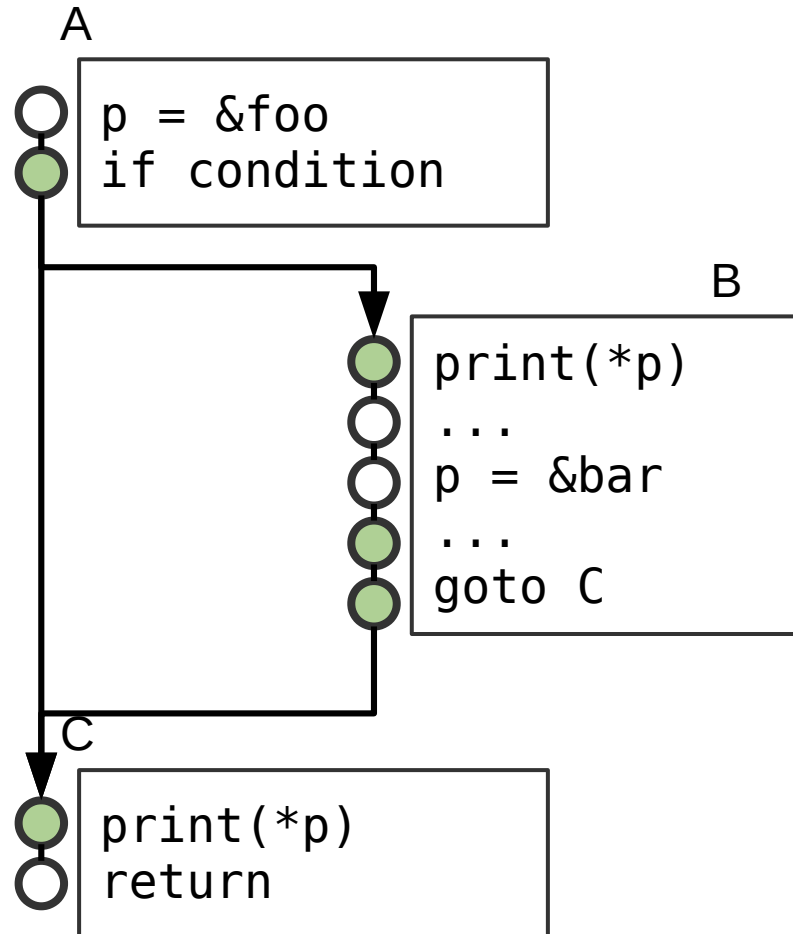


`p : { A/1, B/0, B/3, B/4, C/0 }`

`foo : { }`

`bar : { }`

Constraints

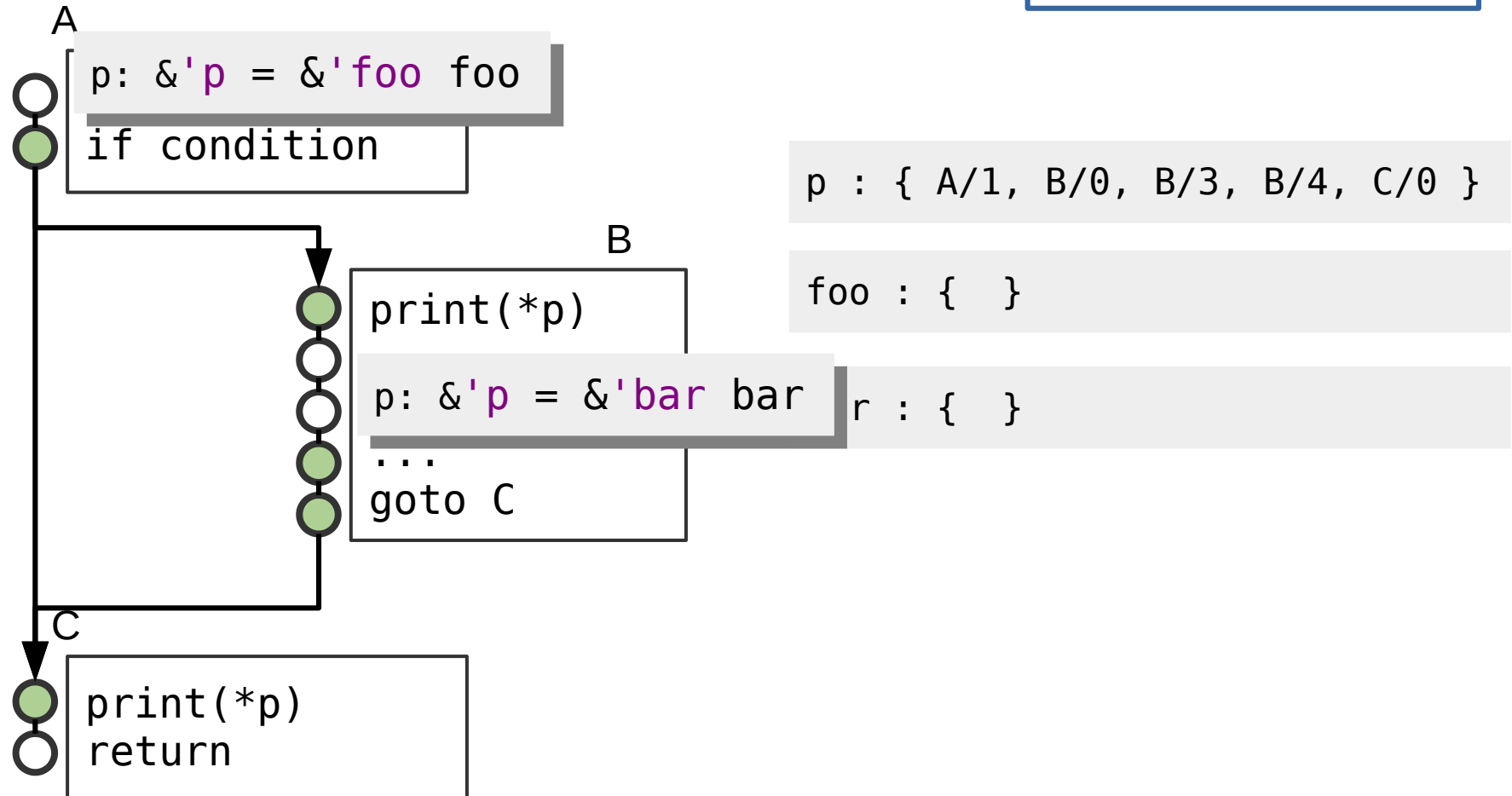


`p : { A/1, B/0, B/3, B/4, C/0 }`

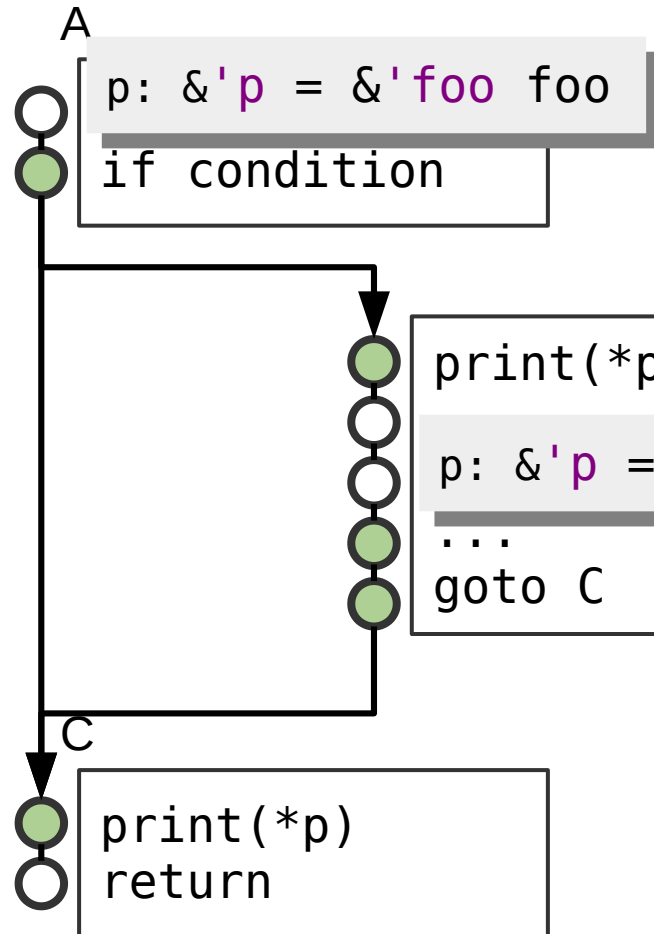
`foo : { }`

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Constraints



Constraints



`p : { A/1, B/0, B/3, B/4, C/0 }`

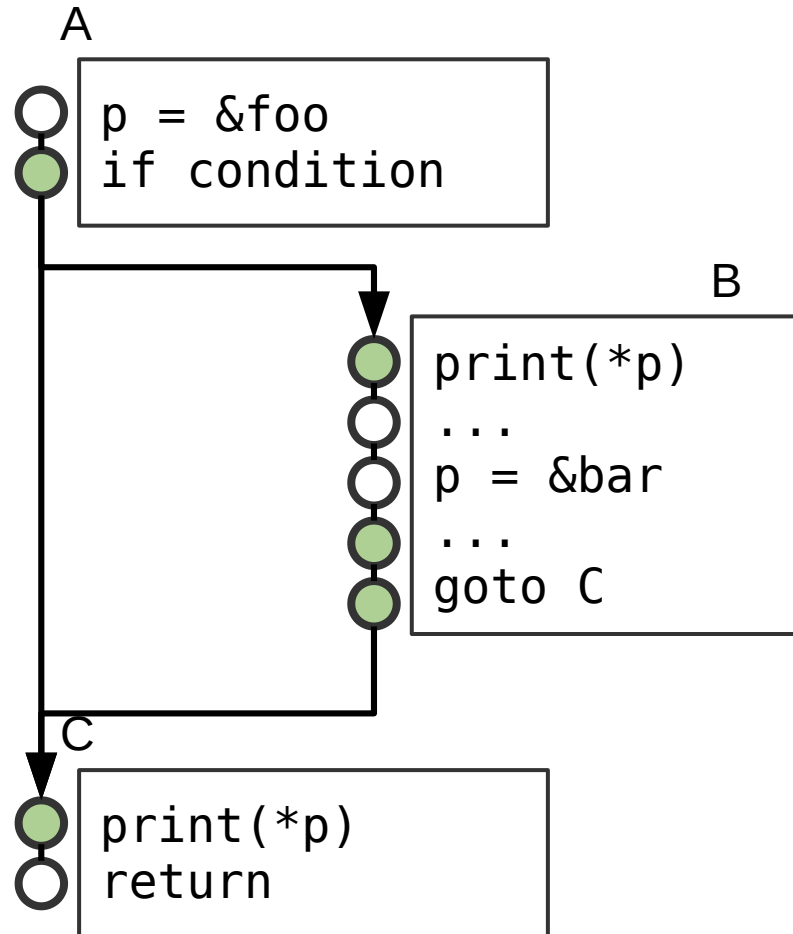
`foo : { }`

`r : { }`

1. `'foo : 'p @ A/0`

2. `'bar : 'p @ B/2`

Constraints



`p : { A/1, B/0, B/3, B/4, C/0 }`

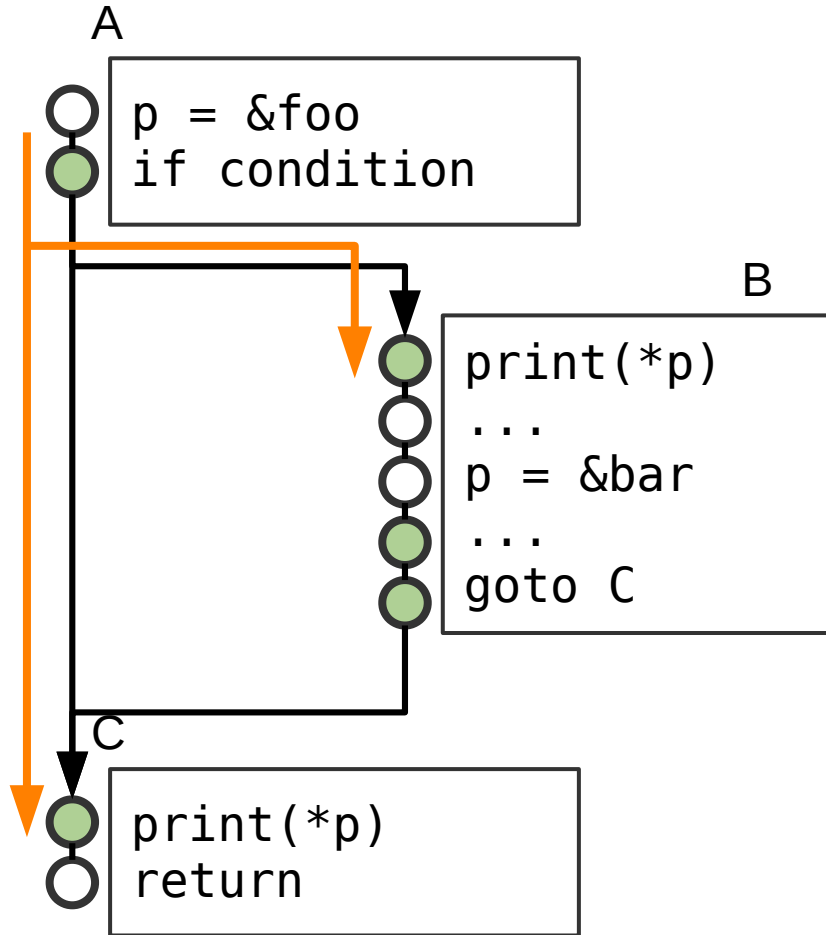
`foo : { }`

`bar : { }`

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Solving Constraints



`p : { A/1, B/0, B/3, B/4, C/0 }`

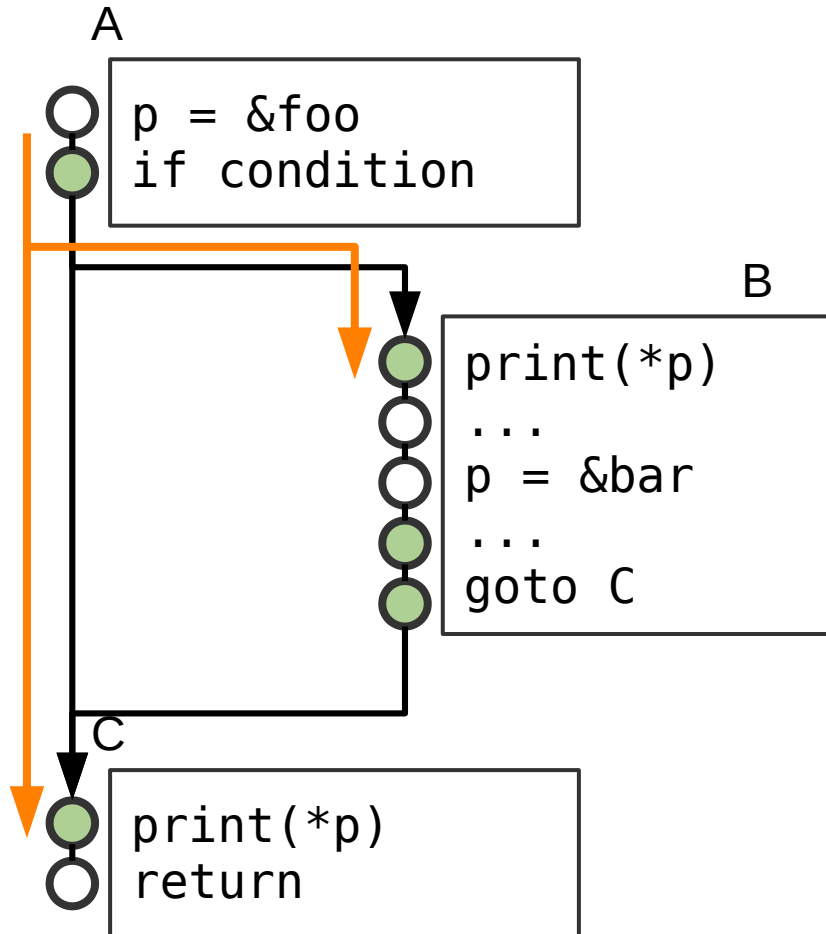
`foo : { }`

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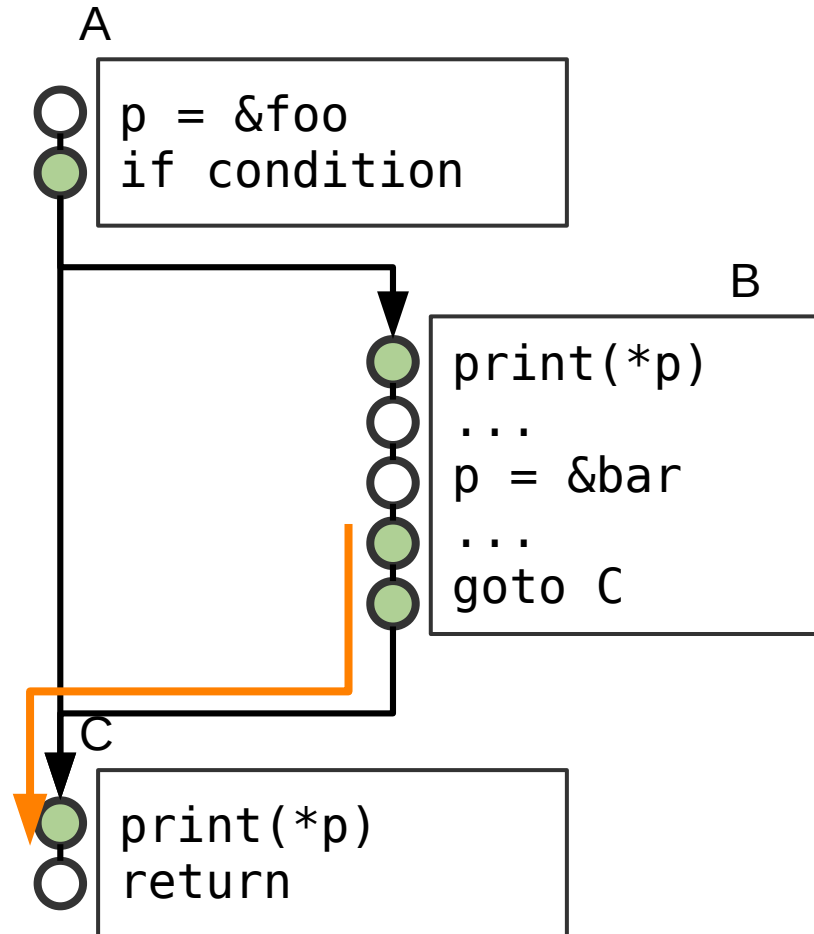
`foo : { A/1, B/0, C/0 }`

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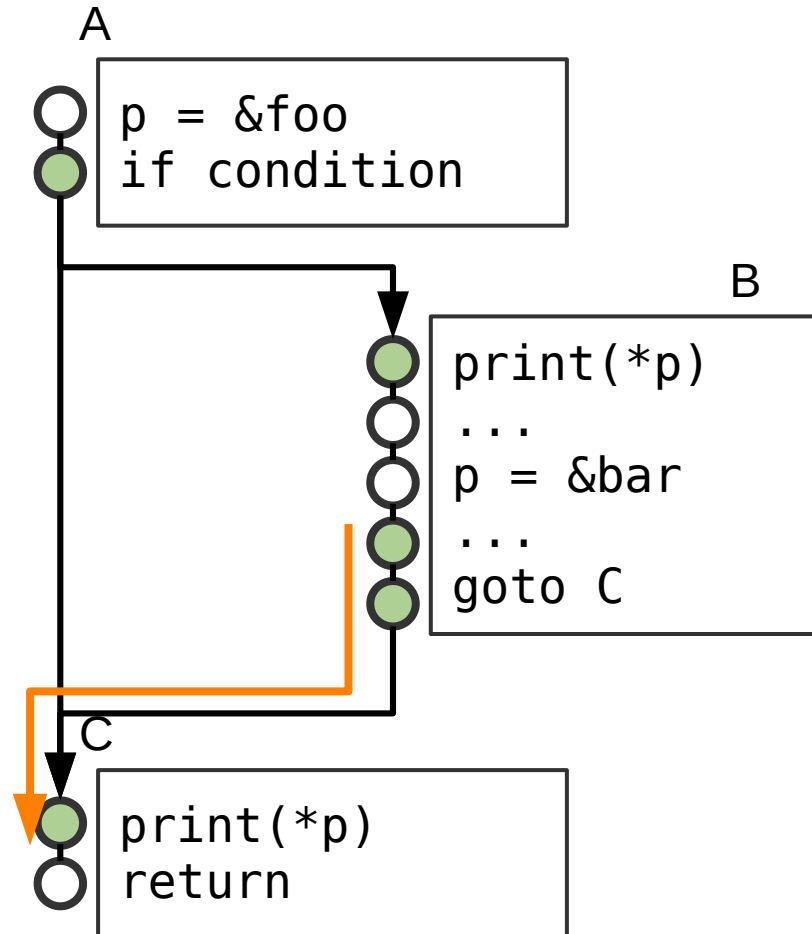
`foo : { A/1, B/0, C/0 }`

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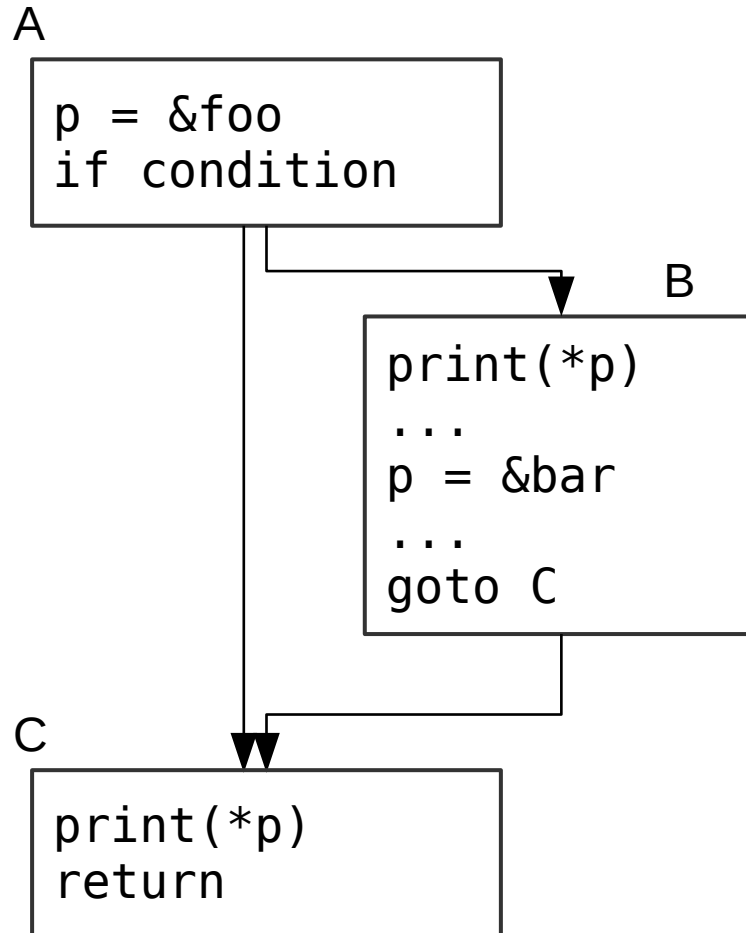
`p : { A/1, B/0, B/3, B/4, C/0 }`

`foo : { A/1, B/0, C/0 }`

`bar : { B/3, B/4, C/0 }`

1. `'foo : 'p @ A/0`

2. `'bar : 'p @ B/2`



Lifetimes:

p : { A/1, B/0, B/3, B/4, C/0 }

foo : { A/1, B/0, C/0 }

bar : { B/3, B/4, C/0 }

Compute Loans in Scope

loans: a set of borrow expressions

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a Loan:

```
A/0 p = &'foo foo;
```

Compute Loans in Scope

loans: a set of borrow expressions

a Loan:

A/0 p = &'foo foo;

```
Loan L0
{
  point:  A/4,
  path:   foo,
  kind:   shared
  region: 'foo {
           A/1, B/0, C/0
         }
}
```

Compute Loans in Scope

loans: a set of borrow expressions

Borrow checker will compute loans at each point via fixed-point dataflow computation with transfer function:

Compute Loans in Scope

loans: a set of borrow expressions

Borrow checker will compute loans at each point via **fixed-point dataflow computation** with transfer function:

-Example: Dataflow equation of Live variable analysis:

$$Live_{in}(s) = Gen(s) \cup (Live_{out}(s) \cap \overline{Kill(s)})$$

Compute Loans in Scope

loans: a set of borrow expressions

Borrow checker will compute loans at each point via fixed-point dataflow computation with **transfer function**:

Transfer function:

Kill Li @ P If $P \notin \text{Li.region}$

Gen Li @ P If Borrow expression occur @ P

Kill Li @ P If $LV \in \text{Li.path}$

```
let list: &mut List<T> = &mut a;
```

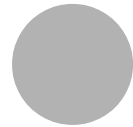
```
let v = &mut (*list).value;
```

```
list = &mut b; // assignment
```

```
use(v)
```

```
use(list)
```

```
let list: &mut List<T> = &mut a;
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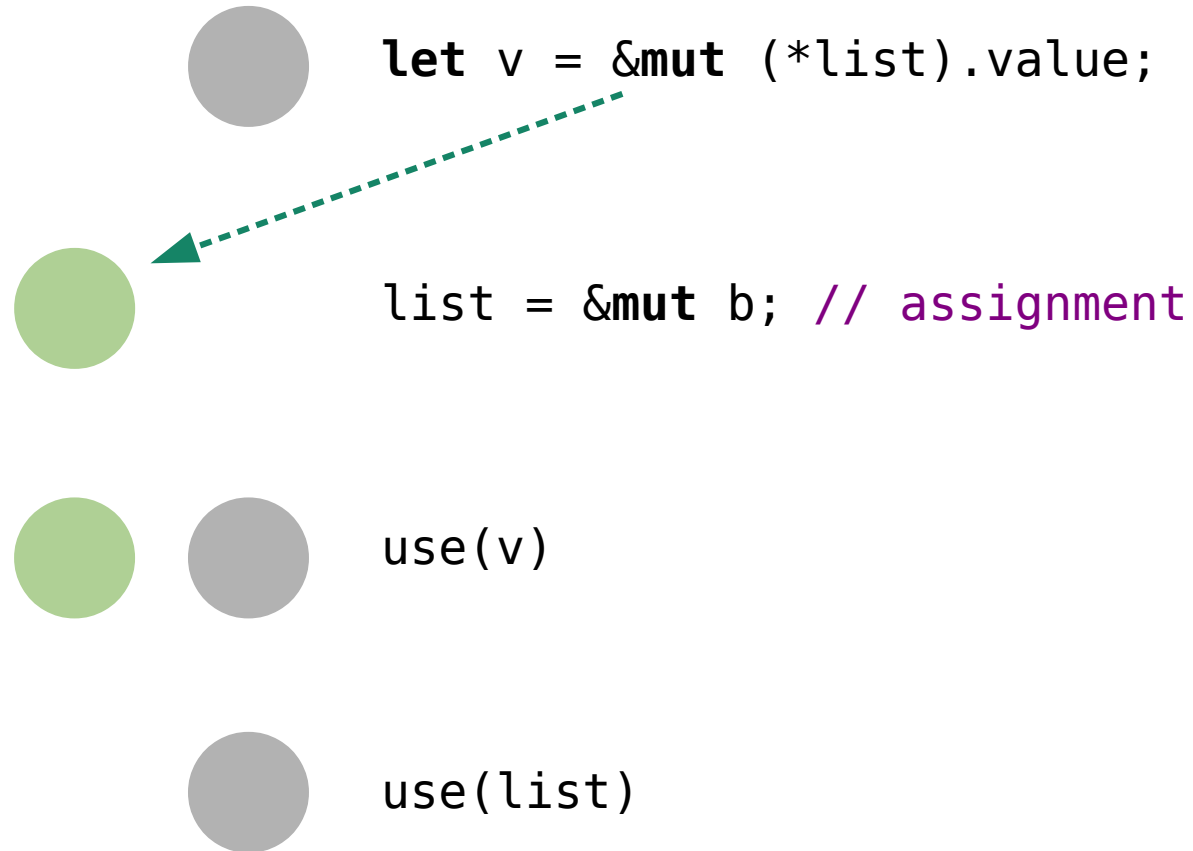


```
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```
use(list)
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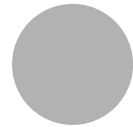


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let v = &mut (*list).value;
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gen L1



```
list = &mut b; // assignment
```

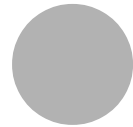


```
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```
use(list)
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```
let list: &mut List<T> = &mut a;
```



```
let v = &mut (*list).value;
```

gen	L1
-----	----



```
list = &mut b; // assignment
```

kill	L1
------	----

gen	L2
-----	----



```
use(v)
```



```
use(list)
```

```

Loan L1
{
  point:  A/1,
  path:  {
    (*list).value ,
    *list,
    list
  },
  kind:   shared
  region: 'c {
    A/2, A/3
  }
}

```

```
let list: &mut List<T> = &mut a;
```

```
let v = &mut (*list).value;
```

gen L1

```
list = &mut b; // assignment
```

kill L1

gen L2



use(v)



use(list)

```

Loan L1
{
  point:  A/1,
  path:  {
    (*list).value ,
    *list,
    list
  },
  kind:   shared
  region: 'c {
    A/2, A/3
  }
}

```

```
let list: &mut List<T> = &mut a;
```

```
let v = &mut (*list).value;
```

gen L1

```
list = &mut b; // assignment
```

kill L1

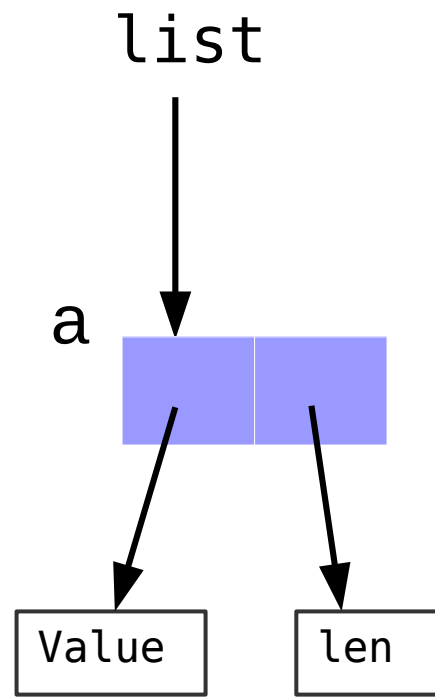
gen L2

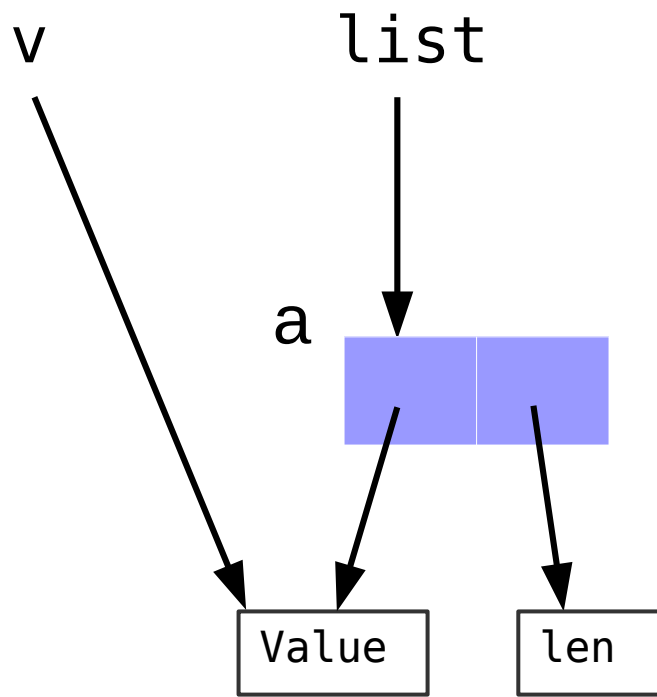


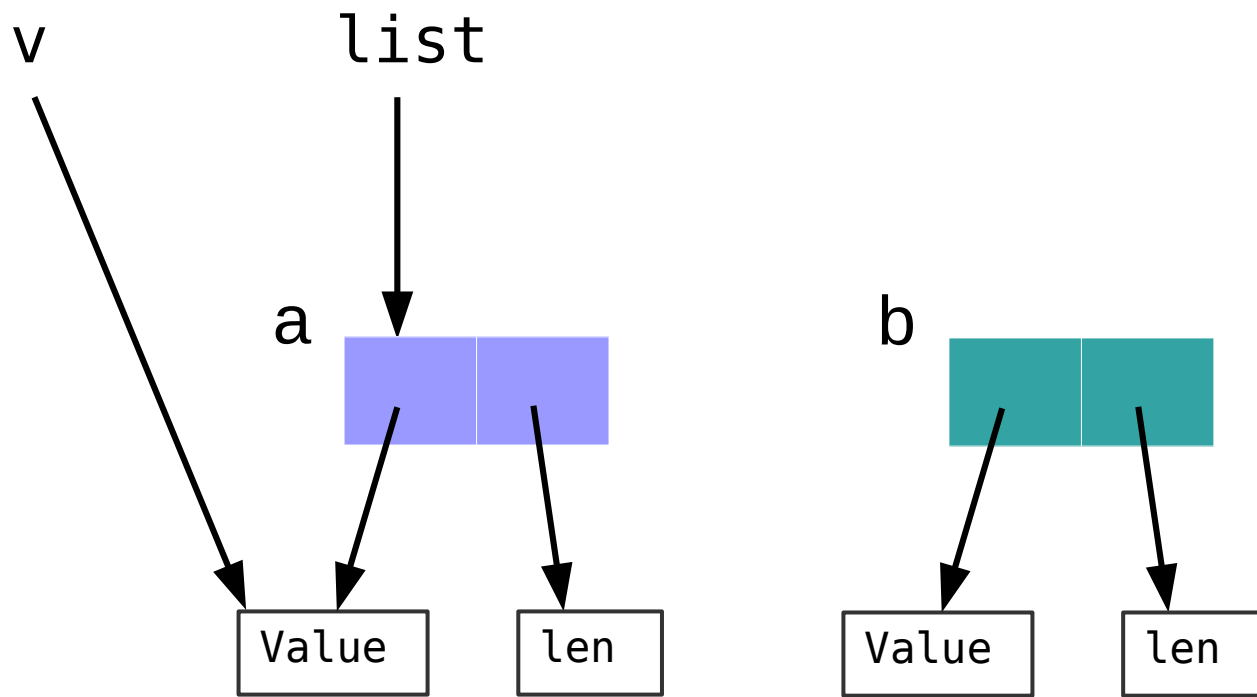
use(v)

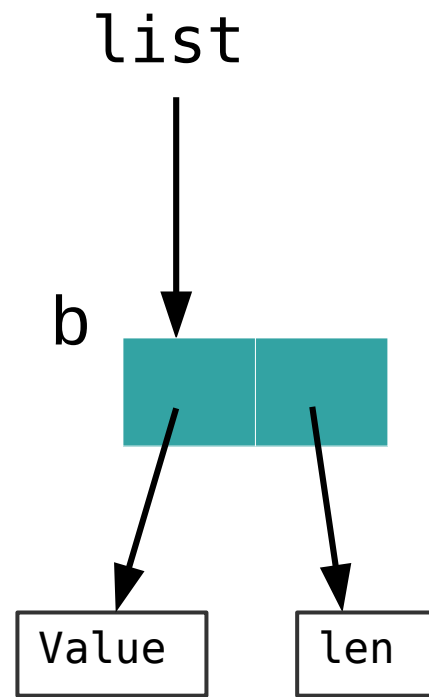
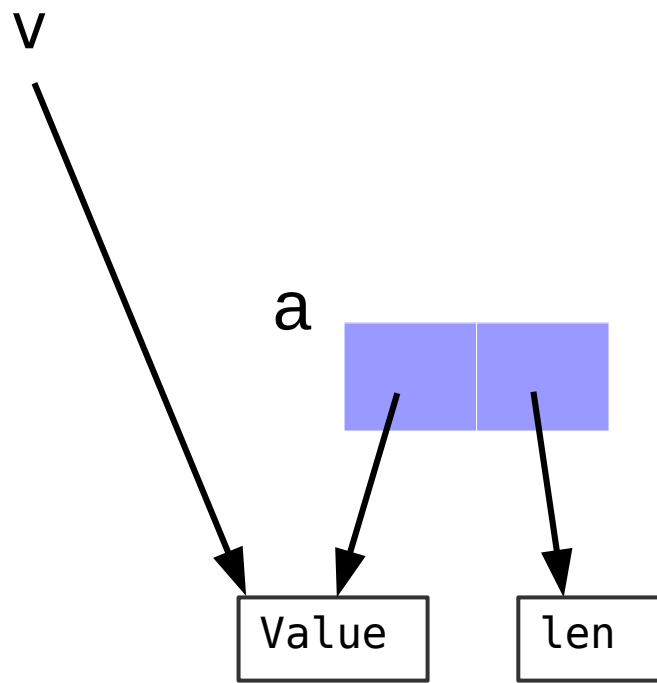


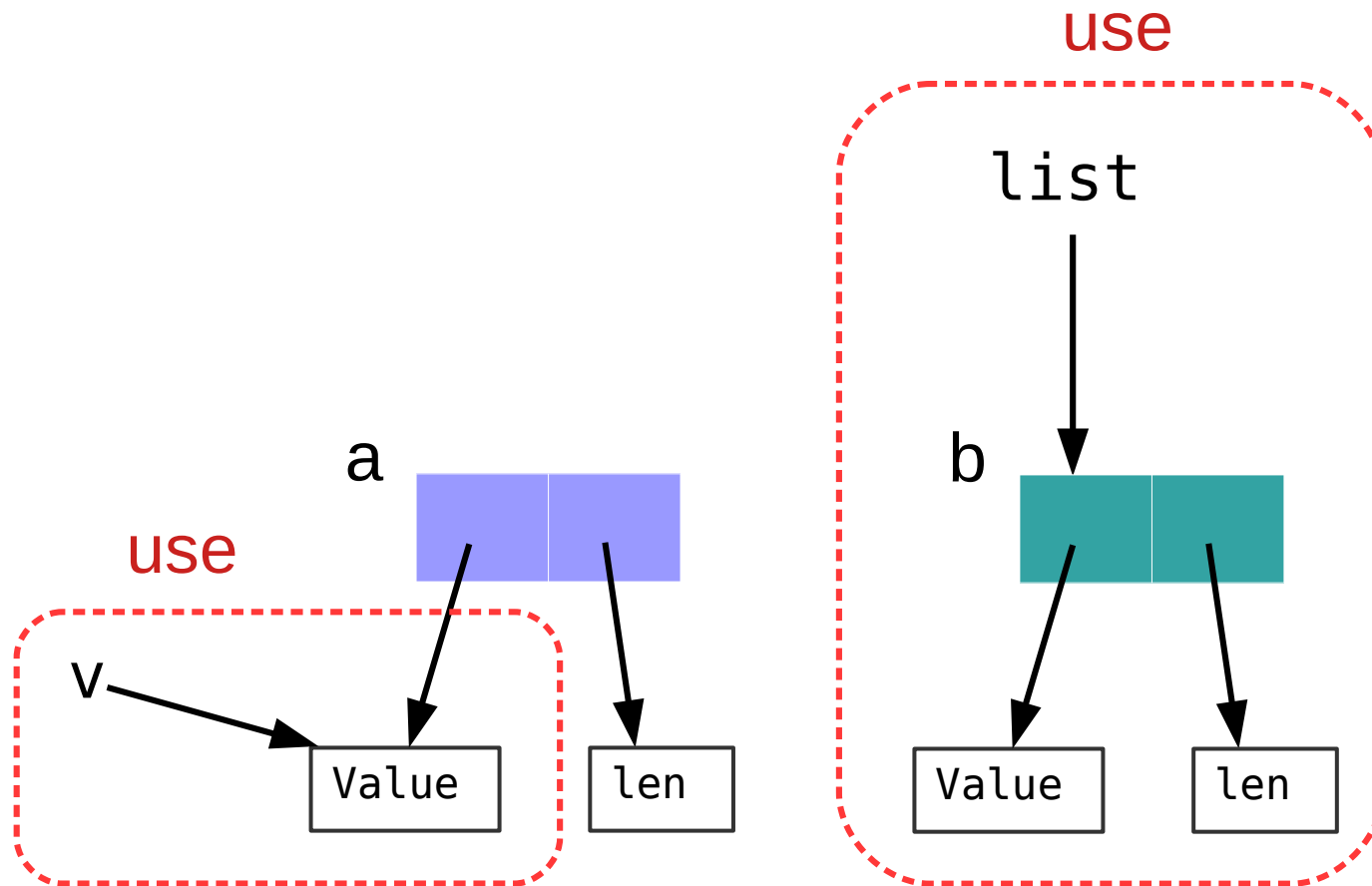
use(list)











Another Example

```

struct Thing;

impl Thing {
    fn maybe_next(&mut self) -> Option<&mut Self> {
        None
    }
}

fn main() {
    let mut temp = &mut Thing;
    loop {
        match temp.maybe_next() {

            Some(v) => { temp = v; }

            None => { }
        }
    }
}

```

```

struct Thing;

impl Thing {
    fn maybe_next(&mut self) -> Option<&mut Self> {
        None
    }
}

fn main() {
    let mut temp = &mut Thing;
    loop {
        match temp.maybe_next() {
            Some(v) => { temp = v; }
            None => { }
        }
    }
}

```

← mutable borrow starts here in previous iteration of loop


```


struct Thing;

impl Thing {
    fn maybe_next(&mut self) -> Option<&mut Self> {
        None
    }
}

fn main() {
    let mut temp = &mut Thing;
    loop {
        match temp.maybe_next()
            Some(v) => { temp = v; }

            None => { }
        }
    }
}

```



```


struct Thing;

impl Thing {
    fn maybe_next(&mut self) -> Option<&mut Self> {
        None
    }
}

fn main() {
    let mut temp = &mut Thing;
    loop {
        match temp.maybe_next()
            Some(v) => { temp = v; }

            None => { }
        }
    }
}

```



gen Loan: L0

```

struct Thing;

impl Thing {
    fn maybe_next(&mut self) -> Option<&mut Self> {
        None
    }
}

fn main() {
    let mut temp = &mut Thing;
    loop {
        match temp.maybe_next() {
            Some(v) => { temp = v; }
            None => { }
        }
    }
}

```

gen Loan: L0

```
struct Thing;
```

```
impl Thing {  
    fn maybe_next(&mut self) -> Option<&mut Self> {  
        None  
    }  
}
```

```
fn main() {  
    let mut temp = &mut Thing;  
    loop {  
        match temp.maybe_next() {  
            Some(v) => { temp = v; }  
            None => { }  
        }  
    }  
}
```

path: temp

gen Loan: L0

```
struct Thing;
```

```
impl Thing {  
    fn maybe_next(&mut self) -> Option<&mut Self> {  
        None  
    }  
}
```

```
fn main() {  
    let mut temp = &mut Thing;  
    loop {  
        match temp.maybe_next() {  
            Some(v) => { temp = v; }  
            None => { }  
        }  
    }  
}
```

path: temp

gen Loan: L0

kill L0

```
struct Thing;
```

```
impl Thing {  
    fn maybe_next(&mut self) -> Option<&mut Self> {  
        None  
    }  
}
```

```
fn main() {  
    let mut temp = &mut Thing;  
    loop {  
        match temp.maybe_next() {  
            Some(v) => { temp = v; }  
            None => { }  
        }  
    }  
}
```

path: temp

gen Loan: L0

kill L0

But L0 not be killed in None arm

```

struct Thing;

impl Thing {
    fn maybe_next(&mut self) -> Option<&mut Self> {
        None
    }
}

fn main() {
    let mut temp = &mut Thing;
    loop {
        match temp.maybe_next() {

            Some(v) => { temp = v; }

            None => { break; }
        }
    }
}

```

Future : Polonius


```

struct Thing;


impl Thing {
    fn maybe_next(&mut self) -> Option<&mut Self> {
        None
    }
}

fn main() {
    let mut temp = &mut Thing;
    loop {
        match temp.maybe_next() {

            Some(v) => { temp = v; }

            None => { }
        }
    }
}

```


 require relation is dropped

```
struct Thing;
```

```
impl Thing {  
    fn maybe_next(&mut self) -> Option<&mut Self> {  
        None  
    }  
}
```

```
fn main() {  
    let mut temp = &mut Thing;  
    loop {  
        match temp.maybe_next() {  
            Some(v) => { temp = v; }  
            None => { }  
        }  
    }  
}
```

$$\frac{R_1 \text{ live at } P \quad R_1 \text{ require } L \text{ at } P}{L \text{ live at } P}$$



require relation is dropped

```
struct Thing;
```

```
impl Thing {  
    fn maybe_next(&mut self) -> Option<&mut Self> {  
        None  
    }  
}
```

```
fn main() {  
    let mut temp = &mut Thing;  
    loop {  
        match temp.maybe_next() {  
            Some(v) => { temp = v; }  
            None => { }  
        }  
    }  
}
```

$$\frac{R_1 \text{ live at } P \quad R_1 \text{ require } L \text{ at } P}{L \text{ live at } P}$$

So, L will not live at None arm

Leetcode example N0026

Leetcode - N0026

Remove duplicated from sorted array

Input :

0, 0, 1, 1, 1, 2, 2, 3, 3, 4

Leetcode - N0026

Remove duplicated from sorted array

Input :

0, 0, 1, 1, 1, 2, 2, 3, 3, 4

Output :

0, 1, 2, 3, 4, 2, 2, 3, 3, 4

Return : 5

```
int removeDuplicates(vector<int>& nums) {  
    if (nums.empty()) return 0;  
    auto it = nums.begin();  
    int cache = *it;  
    for (auto x : nums) {  
        if (x != cache) {  
            cache = *(++it) = x;  
        }  
    }  
    return it - nums.begin() + 1;  
}
```

```
int removeDuplicates(vector<int>& nums) {
    if (nums.empty()) return 0;
    auto it = nums.begin();
    int cache = *it;
    for (auto x : nums) {
        if (x != cache) {
            cache = *(++it) = x;
        }
    }
    return it - nums.begin() + 1;
}
```

Borrow as mut


```
int removeDuplicates(vector<int>& nums) {
    if (nums.empty()) return 0;
    auto it = nums.begin();
    int cache = *it;
    for (auto x : nums) {
        if (x != cache) {
            cache = *(++it) = x;
        }
    }
    return it - nums.begin() + 1;
}
```

Borrow as **mut**

Borrow as **immut**

```
pub fn remove_duplicates(nums: &mut Vec<i32>) -> i32 {  
    if nums.is_empty() {  
        return 0;  
    }  
  
    let mut it = nums.iter_mut();  
  
    let mut cache = *(it.next().unwrap());  
  
    let mut count = 1;  
  
    for &x in nums.iter() {  
        if x != cache {  
            ...  
        }  
    }  
}
```

```
pub fn remove_duplicates(nums: &mut Vec<i32>) -> i32 {  
    if nums.is_empty() {  
        return 0;  
    }  
  
    let mut it = nums.iter_mut()  
  
    let mut cache = *(it.next().unwrap());  
  
    let mut count = 1;  
  
    for &x in nums.iter() {  
        if x != cache {  
            ...  
        }  
    }  
}
```

```
pub fn remove_duplicates(nums: &mut Vec<i32>) -> i32 {  
    if nums.is_empty() {  
        return 0;  
    }  
  
    let mut it = nums.iter_mut()  
  
    let mut cache = *(it.next().unwrap());  
  
    let mut count = 1;  
  
    for &x in nums.iter() {  
        if x != cache {  
            ...  
        }  
    }  
}
```

```
pub fn remove_duplicates(nums: &mut Vec<i32>) -> i32 {  
    if nums.is_empty() {  
        return 0;  
    }  
  
    let mut it = nums.iter_mut()  
  
    let mut cache = *(it.next().unwrap());  
  
    let mut count = 1;  
  
    for &x in nums.iter() {  
        if x != cache {
```



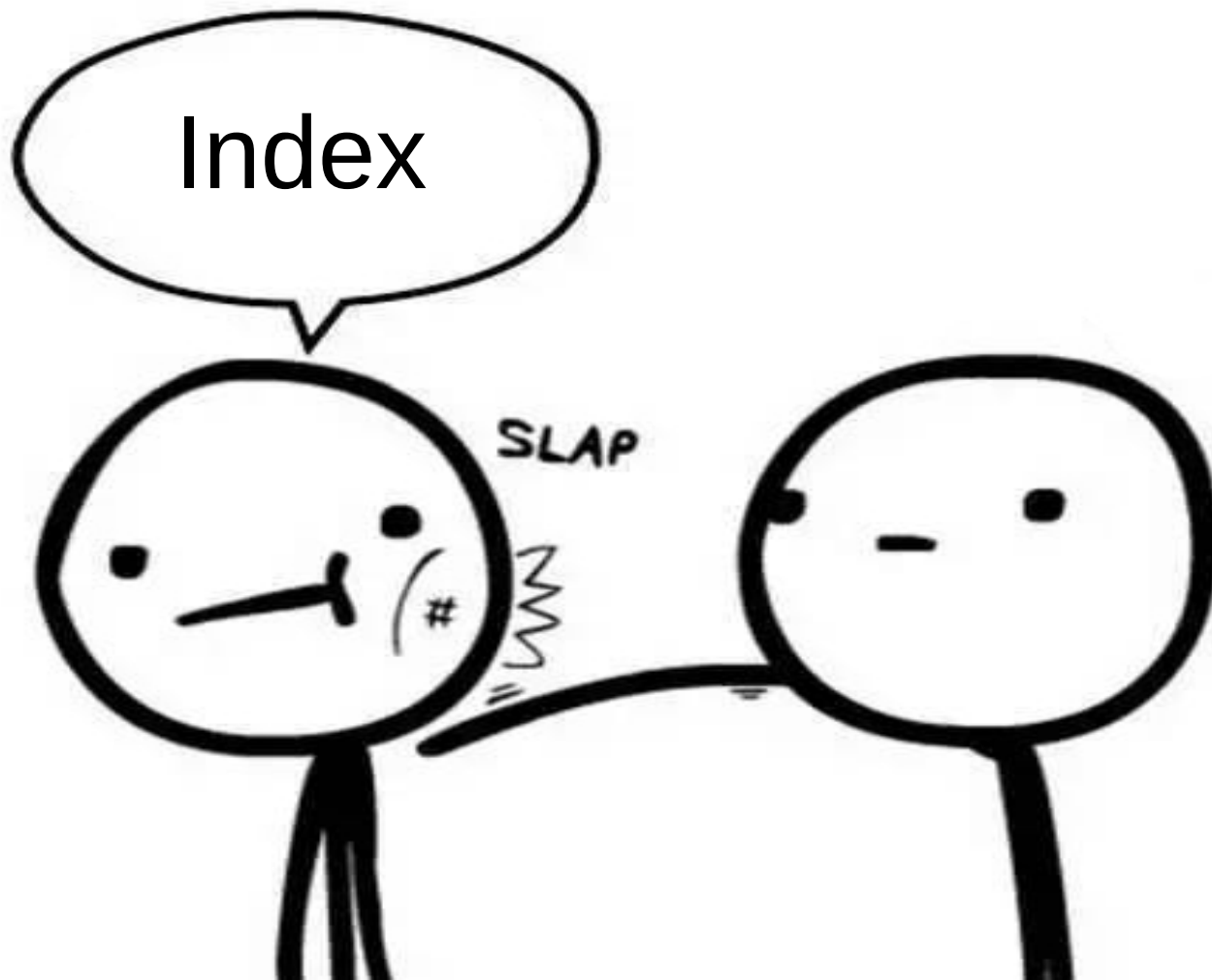
use **x** and **it** at the same time

```
pub fn remove_duplicates(nums: &mut Vec<i32>) -> i32 {  
    if nums.is_empty() {  
        return 0;  
    }  
  
    let mut count = 1;  
  
    let mut cache = nums[0];  
  
    for i in 1..nums.len() {  
        if nums[i] != cache {  
            count+=1;  
  
            nums[count] = nums[i];  
  
            cache = nums[i];  
        }  
    }  
    count  
}
```

Rust

```
pub fn remove_duplicates(nums: &mut Vec<i32>) -> i32 {  
    if nums.is_empty() {  
        return 0;  
    }  
  
    let mut count = 1;  
  
    let mut cache = nums[0];  
  
    for i in 1..nums.len() {  
        if nums[i] != cache {  
            count+=1;  
  
            nums[count] = nums[i];  
  
            cache = nums[i];  
        }  
    }  
    count  
}
```







```
if nums.is_empty() { return 0; }

let mut p = nums.as_mut_ptr();

let mut cache = unsafe { *p };

let mut count = 1;

for &x in nums.iter() {
    if x != cache {
        unsafe {
            p = p.offset(1);
            *p = x;
            cache = *p;
        }

        count += 1;
    }
}

return count;
```

```
if nums.is_empty() { return 0; }

let mut p = nums.as_mut_ptr();

let mut cache = unsafe { *p };

let mut count = 1;

for &x in nums.iter() {
    if x != cache {
        unsafe {
            p = p.offset(1);
            *p = x;
            cache = *p;
        }

        count += 1;
    }
}

return count;
```

```
if nums.is_empty() { return 0; }
```

```
let mut p = nums.as_mut_ptr();
```

```
let mut cache = unsafe { *p };
```

```
let mut count = 1;
```

```
for &x in nums.iter() {
```

```
    if x != cache {
```

```
        unsafe {
```

```
            p = p.offset(1);
```

```
            *p = x;
```

```
            cache = *p;
```

```
        }
```

```
        count += 1;
```

```
    }
```

```
}
```

```
return ((p as usize - nums.as_ptr() as usize) >> 2) as i32 + 1
```

```
fn steal<'a, 'b, T>(x: &'a mut T) -> &'b mut T {  
    let _tmp = x as *mut T;  
    unsafe { std::mem::transmute:::<*mut T, &mut T>(x) }  
}
```

```
fn steal<'a, 'b, T>(x: &'a mut T) -> &'b mut T {  
    let _tmp = x as *mut T;  
    unsafe { std::mem::transmute:::<*mut T, &mut T>(x) }  
}
```

$x: \&'a \text{ mut } T \longrightarrow _tmp: *mut T \longrightarrow _0: \&'b \text{ mut } T$

```
if nums.is_empty() { return 0; }

let mut it = steal(nums).iter_mut();

let mut cache = *(it.next().unwrap());
let mut count = 1;

for &x in nums.iter() {
    if x != cache {
        *(it.next().unwrap()) = x;

        cache = x;

        count += 1;
    }
}

return count;
```

```
if nums.is_empty() { return 0; }

let mut it = steal(nums).iter_mut();

let mut cache = *(it.next().unwrap());

nums.iter().for_each(|&e| if e != cache {
    *(it.next().unwrap()) = e;
    cache = e;
});

return (nums.len() - it.len()) as i32;
```



```
if nums.is_empty() { return 0; }

let mut it = steal(nums).iter_mut();

let mut cache = *(it.next().unwrap());

nums.iter().for_each(|&e| if e != cache {
    *(it.next().unwrap()) = e;
    cache = e;
});

return (nums.len() - it.len()) as i32;
```

*And so once again, the day is saved
thanks to... The Unsafe*

That's All

QA



github.com/rniczh