

關於生命週期的一點事兒

The relationship of Lifetimes and DataFlow

Rnic / H.-S. Zheng

Aug 17, 2019 @ COSCUP

Audience

- 讀過 Rust Book
- 想要了解編譯器怎麼看待 Lifetimes
- 對編譯器有那麼一點興趣
- ~~想要輕鬆駕馭 Rust's Lifetimes~~
- ~~想要快快樂樂寫 Rust~~

Outline

- 1. Introduction
 - Example1
 - Basic Lifetimes Concepts

- 2. Borrow Checker
 - Collaborate with Data Flow
 - Example2
 - Datafrog (a datalog engine used in Polonius)

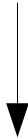
Compilation of Rust

Rust Code

```
let foo: T = Foo {};  
let bar: T = Bar {};  
  
let mut p = &foo;  
  
if cond {  
    println!("{}", *p);  
    ...  
    p = &bar;  
    ...  
}  
  
println!("{}", *p);
```

Compilation of Rust

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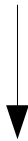


HIR

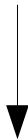
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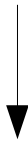
MIR



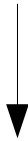
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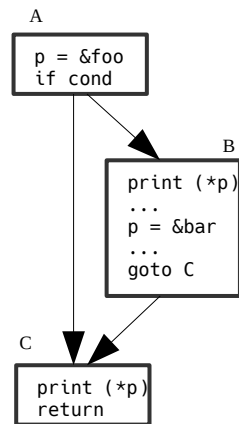
HIR



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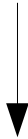
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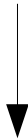
Control Flow Graph

Compilation of Rust

Rust Code



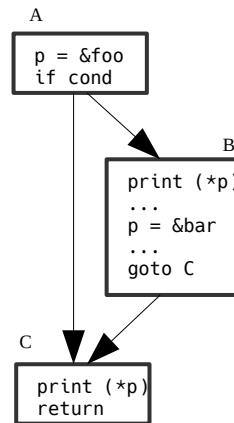
HIR



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Control Flow Graph



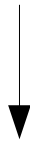
Borrow checker

Theorem: Data Flow Analysis

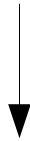
Tool: Datafrog

Compilation of Rust

Rust Code



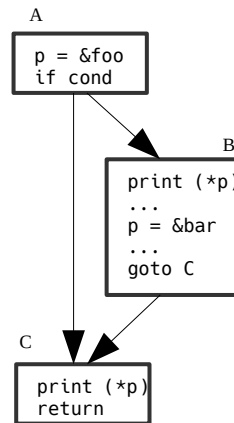
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Control Flow Graph

Documents

NLL RFC:
2094-nll

Polonius:
an-alias-based-formulation
-of-the-borrow-checker



Borrow checker

Theorem: Data Flow Analysis

Tool: Datafrog

Example

```
fn list_not(mut head: Option<Box<ListNode>>) -> Option<Box<ListNode>>
{
    let mut cur = &mut head;

    while let Some(nodeBox) = cur.as_mut() {
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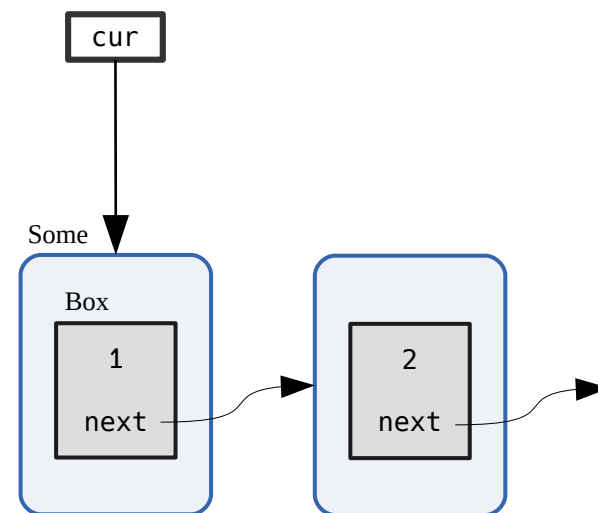
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}
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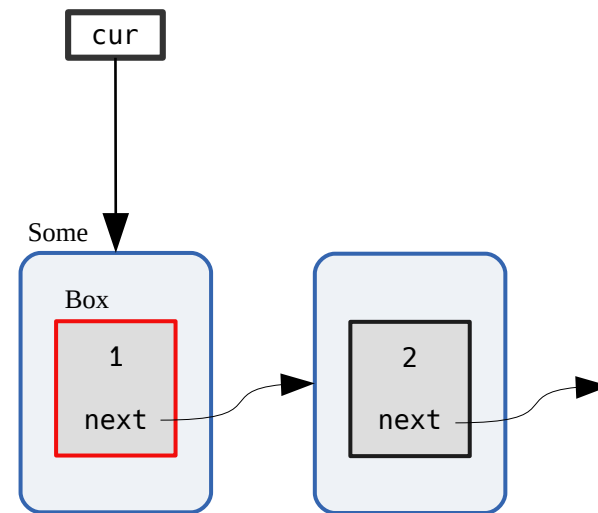


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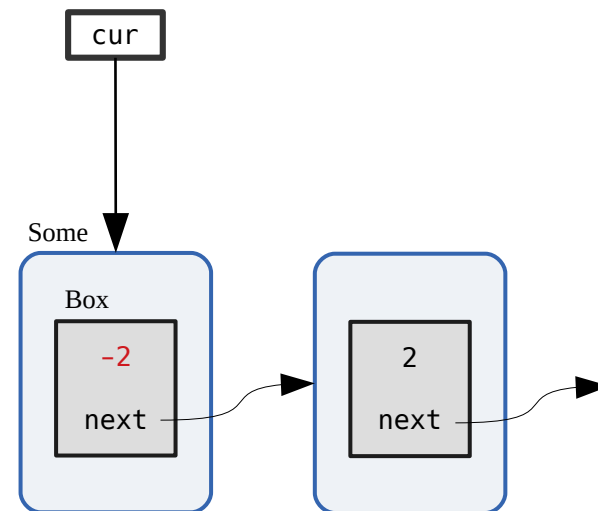


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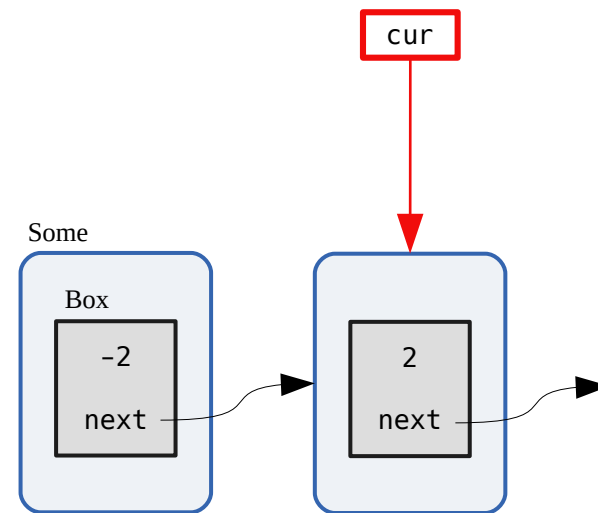
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依照使用區間判斷

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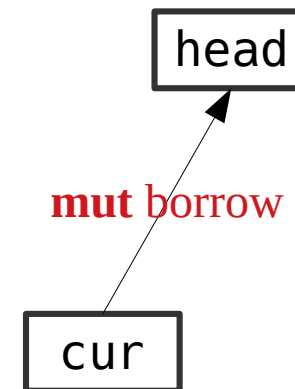
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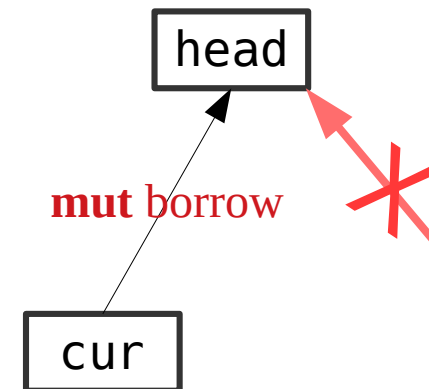
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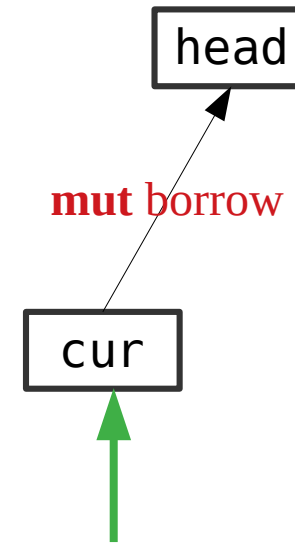
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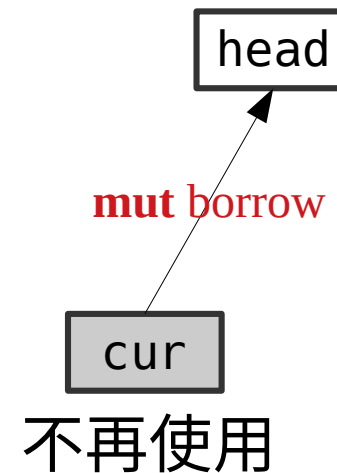


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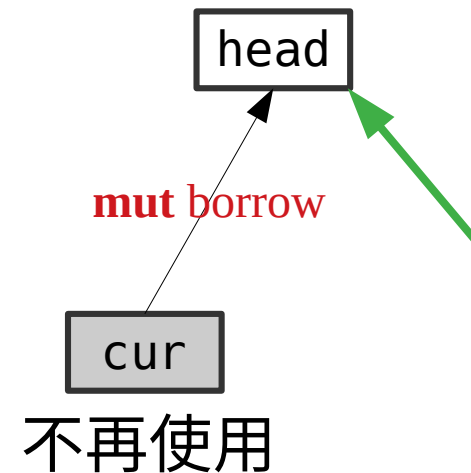
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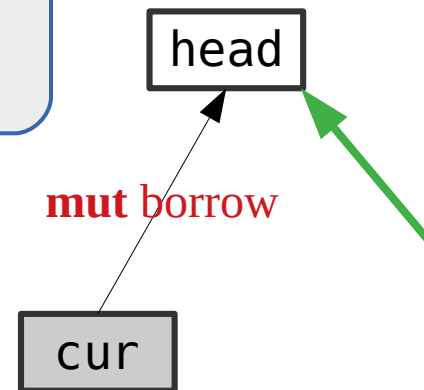
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    }
}
```

`cur` only used here

```
while let Some(nodeBox) = cur.as_mut() {
    nodeBox.val = !nodeBox.val;
    cur = &mut nodeBox.next;
}
```

head



不再使用

依照使用區間判斷

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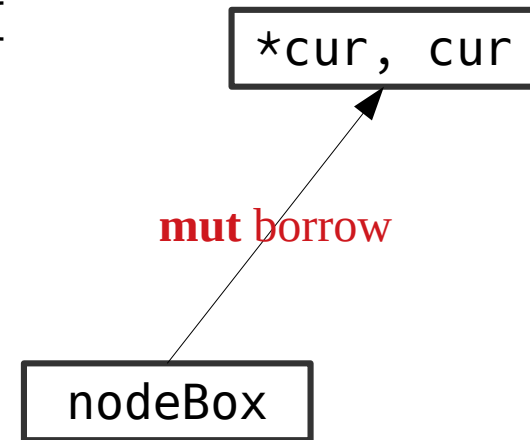
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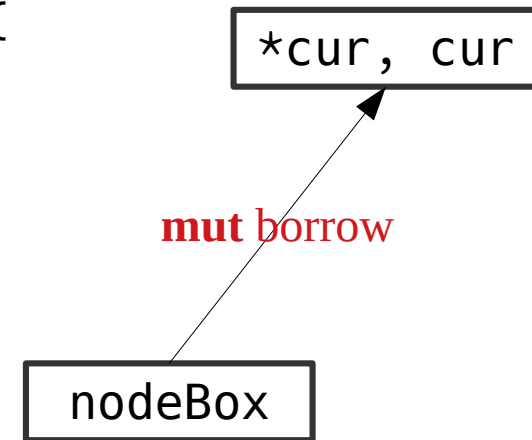


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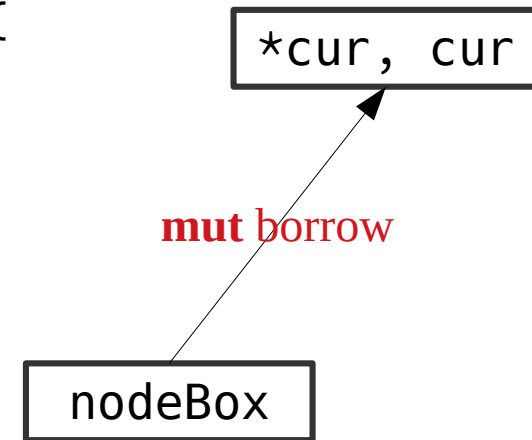


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    head
}
```



1. **nodeBox** finally used here
2. Assignment to **'cur'** killed the borrow expression

Borrow

P_0 : **let** r : $\&T$

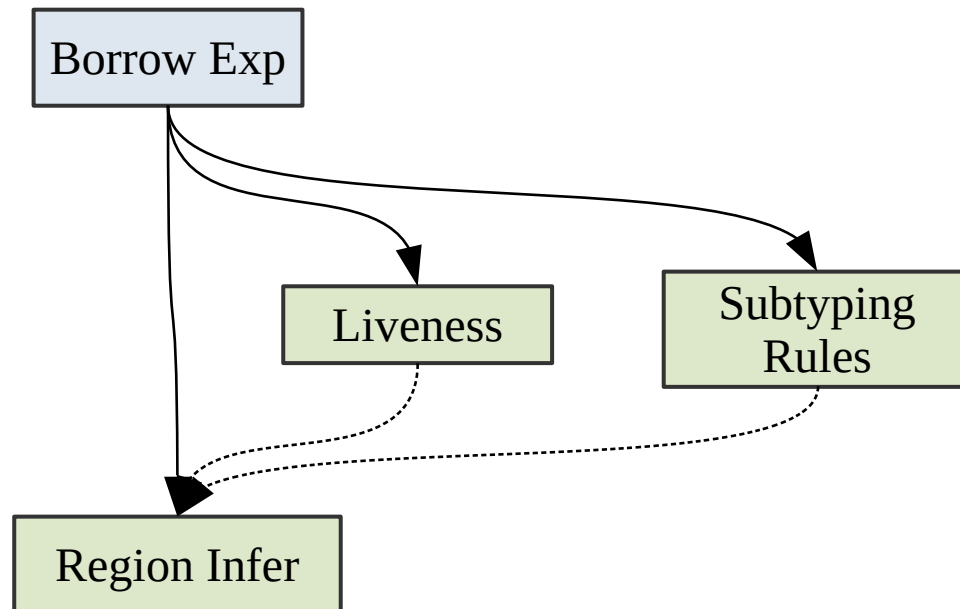
P_1 : $r = \&x$;

Borrow Exp

Borrow

P_0 : **let** r : $\&'0$ T

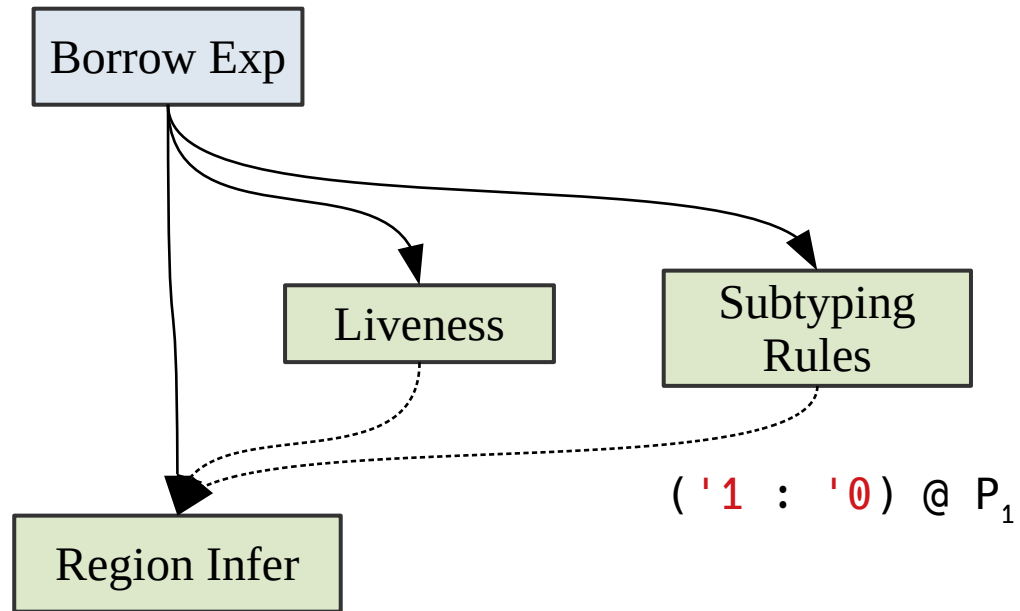
P_1 : $r = \&'1$ x ;



Borrow

P_0 : **let** r : $\&'0$ T

P_1 : $r = \&'1$ x ;



$'0$: $\{ P_1 , P_2 \dots \}$

$'1$: $\{ P_1 , \dots \}$

Borrow

Each Borrow expression will
corresponding to each Loan

```
Loan L0 {
  point: P1,
  path: x,
  kind: shared
  region: '1 {
    P1 ...
  }
}
```

$P_0 : \text{let } r : \&'0 \text{ T}$

$P_1 : r = \&'1 x;$

Borrow Exp

Liveness

Subtyping
Rules

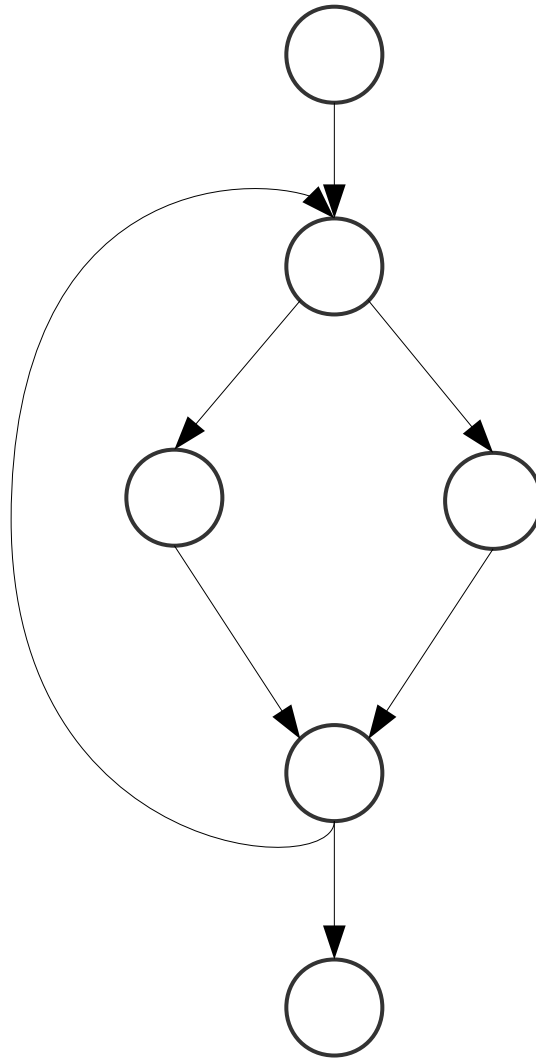
Region Infer

$('1 : '0) @ P_1$

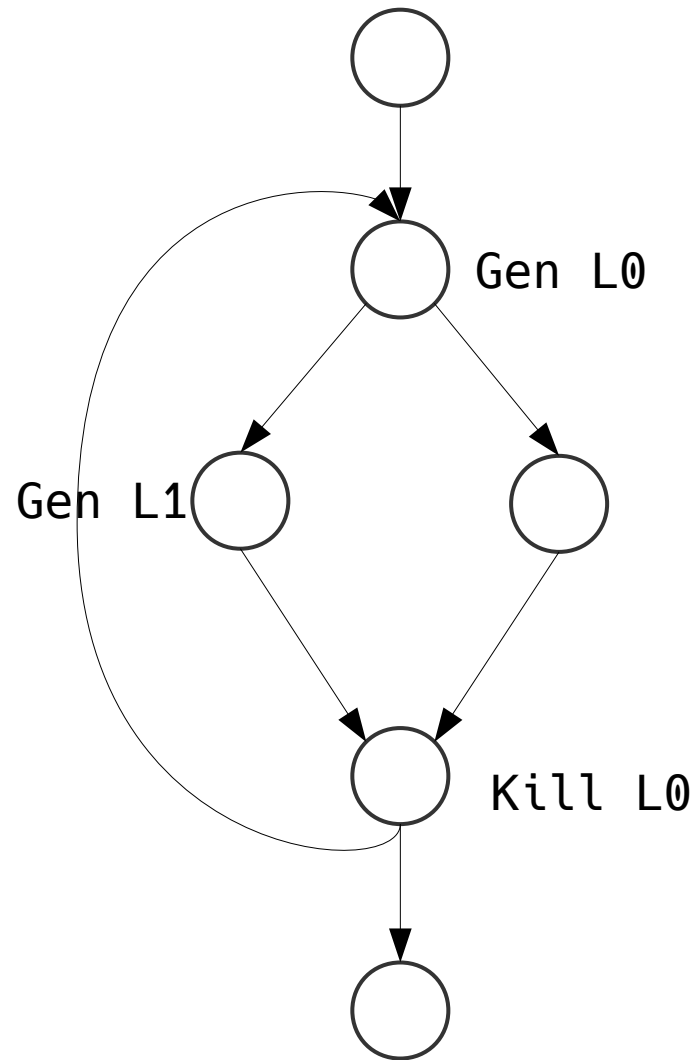
$'0 : \{ P_1 , P_2 \dots \}$

$'1 : \{ P_1 , \dots \}$

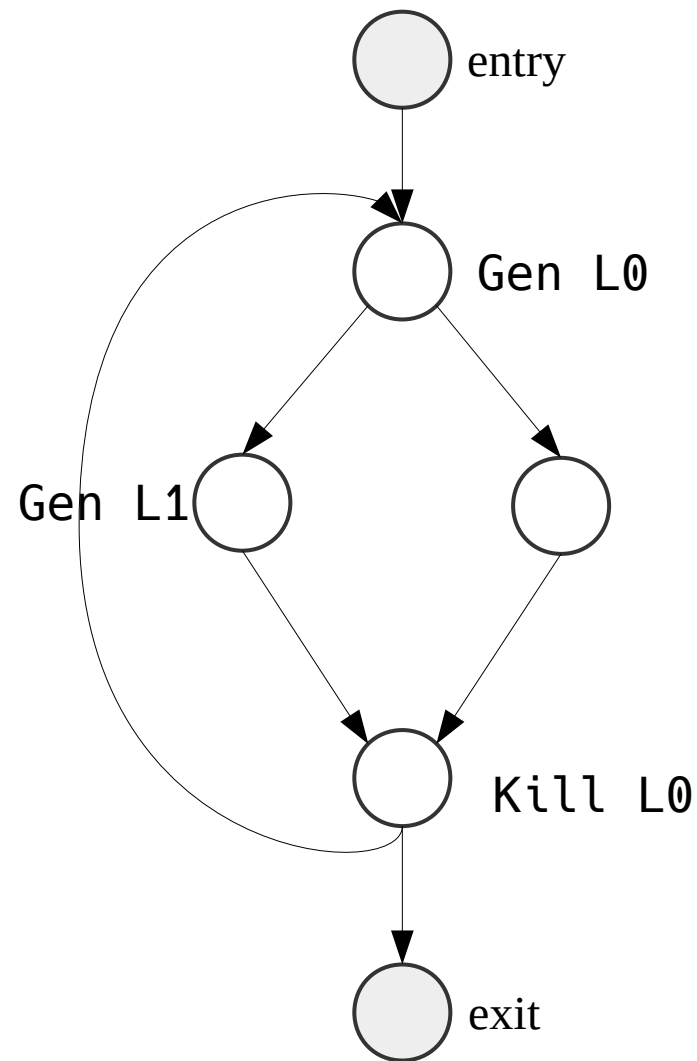
The Data Flow of the Loan



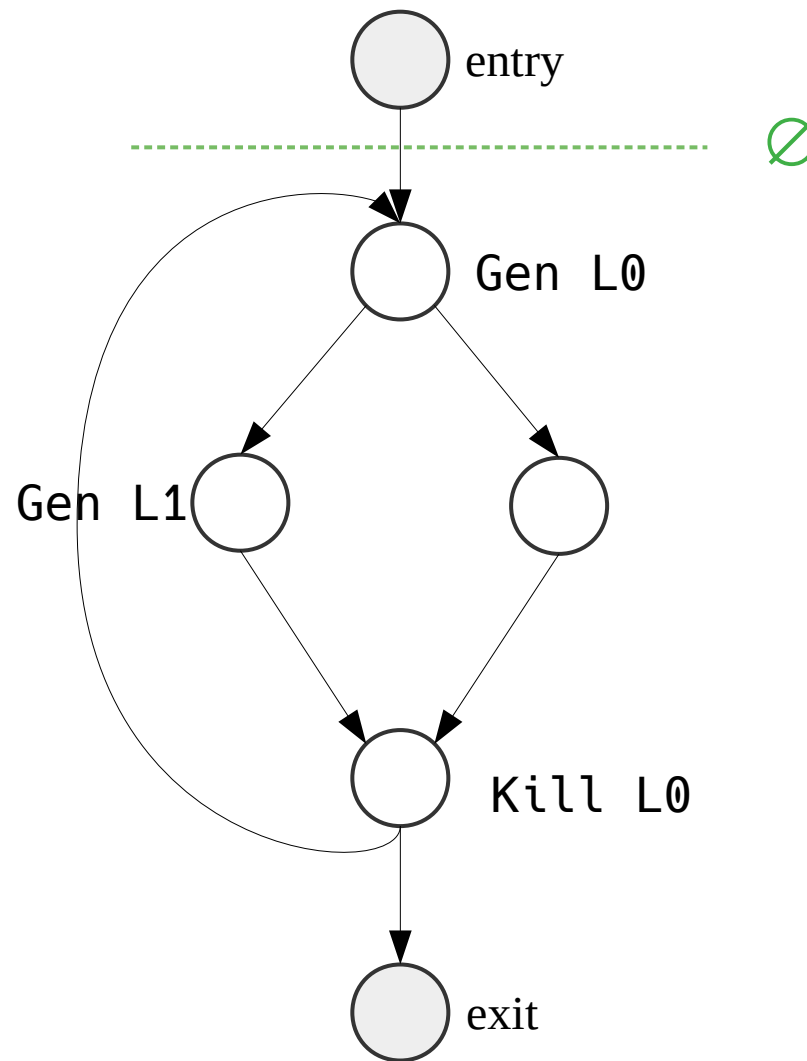
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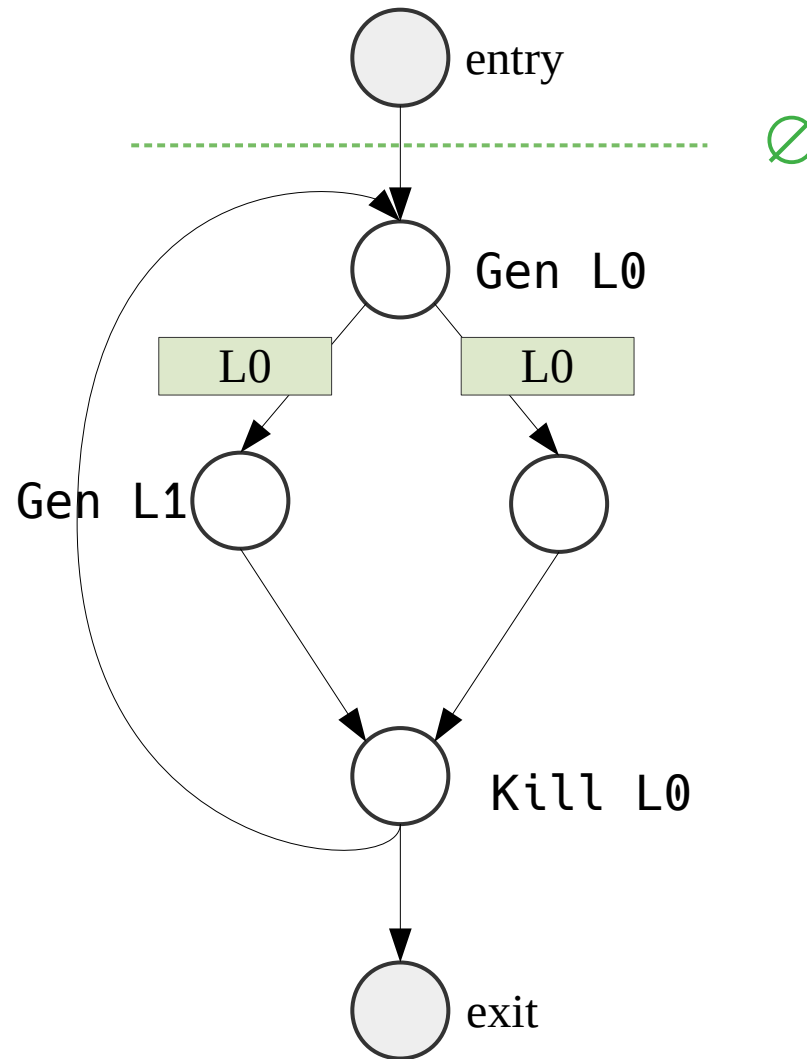
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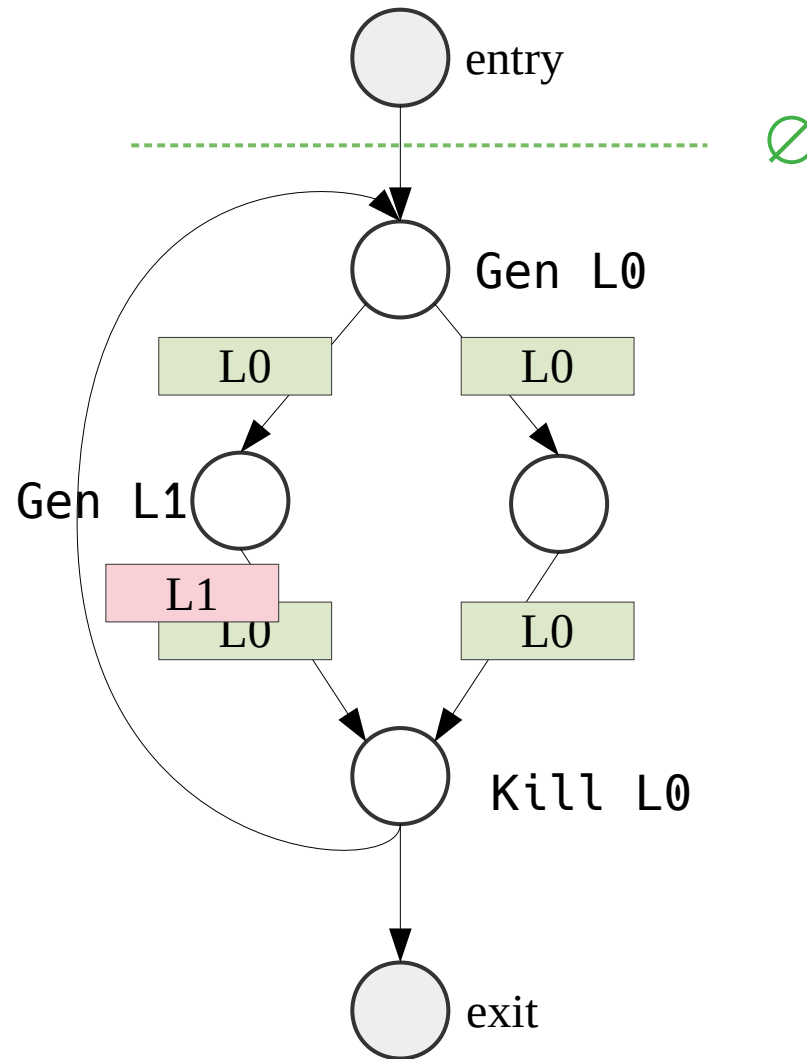
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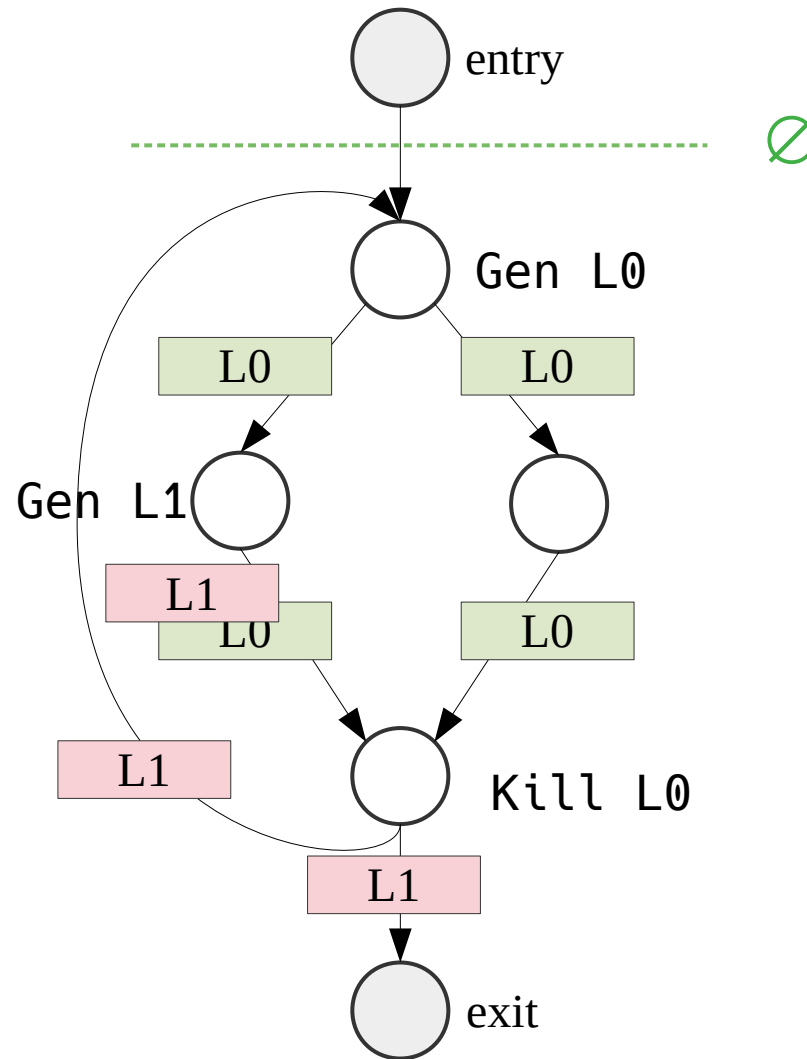
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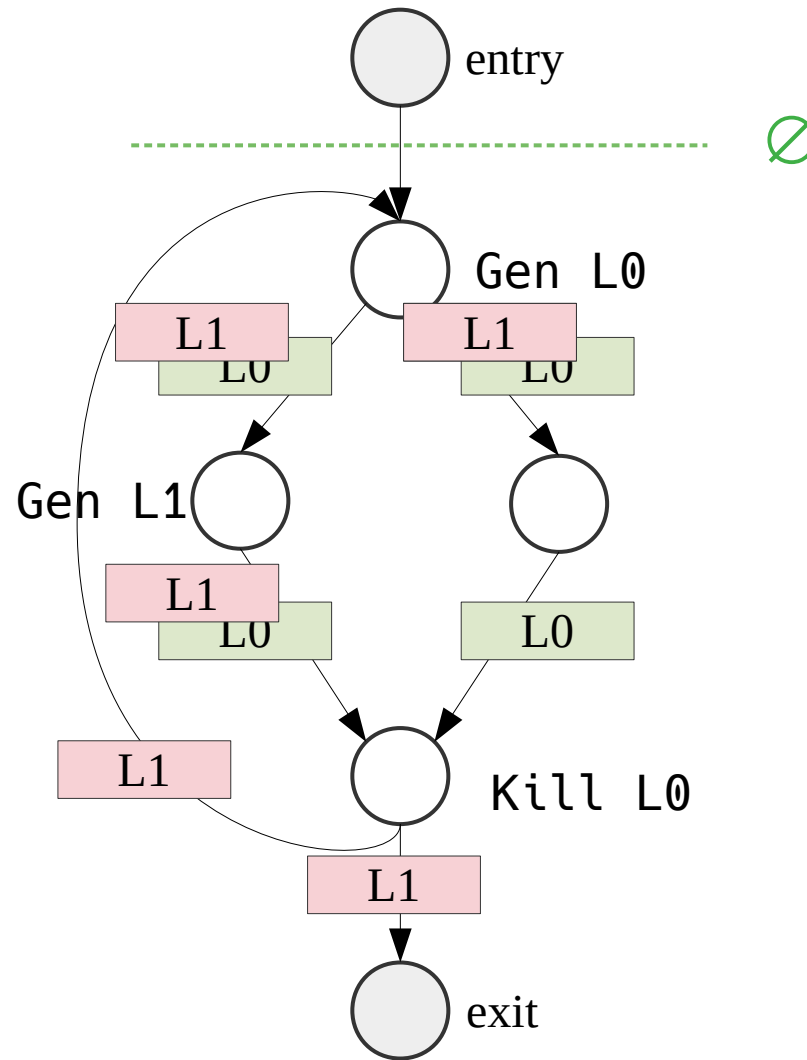
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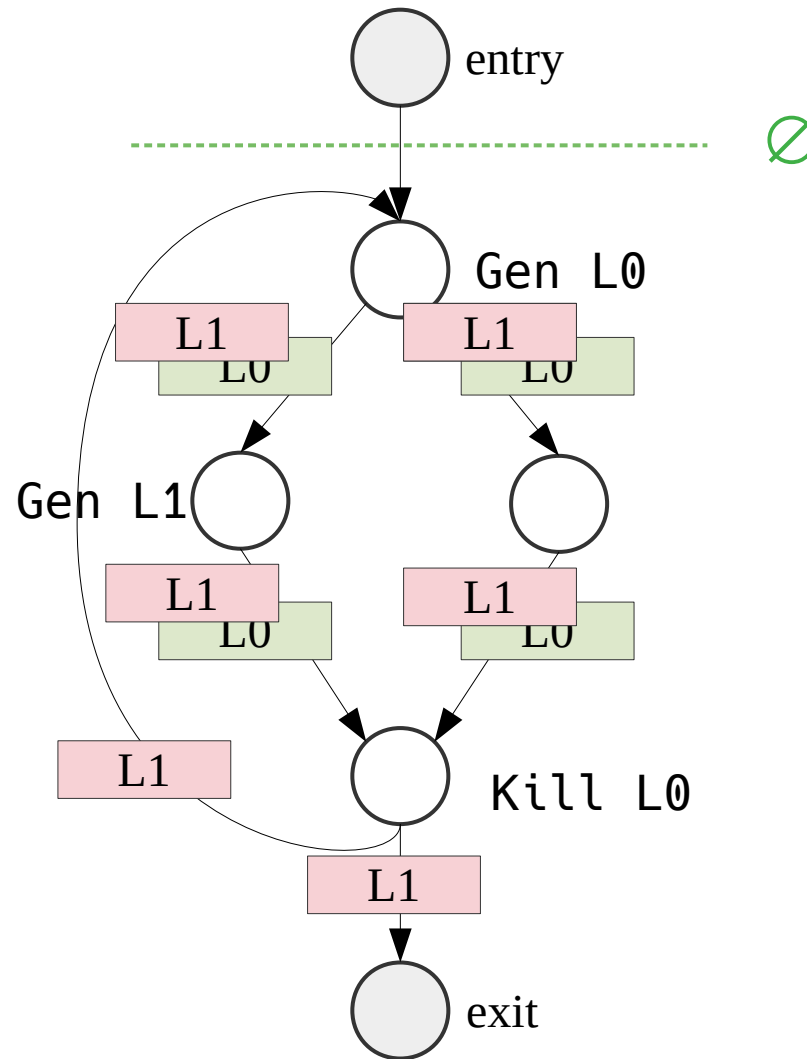
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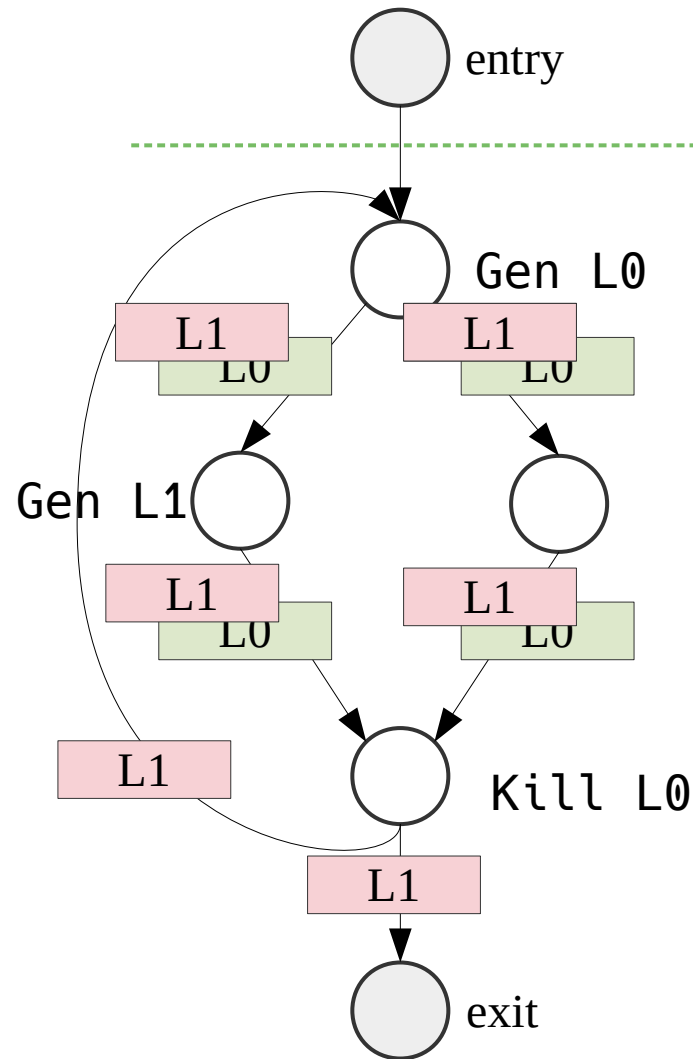


The Data Flow of the Loan



The Data Flow of the Loan

Key: which loan live at which points



When all the sets are stable, that's mean **the state is not changed anymore**, then the data flow computation is complete.

When to Gen, Kill

Gen Loan :

If it's a borrow expression, then gen a Loan

Kill Loan :

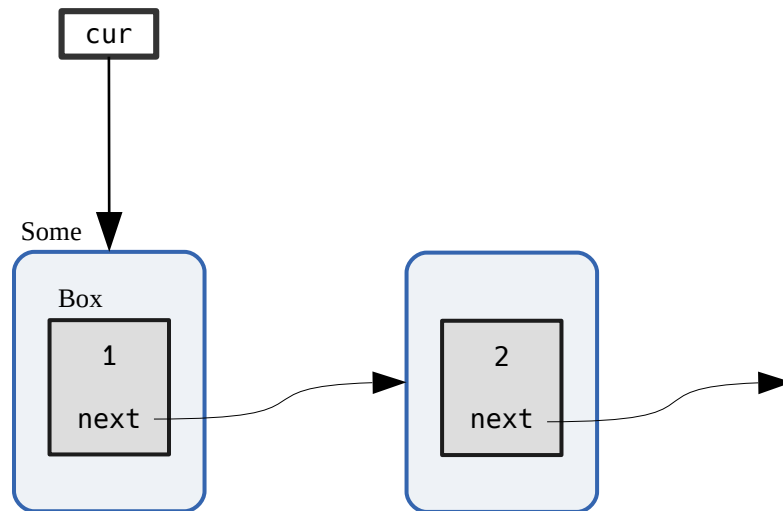
- 1) $LV = \text{Loan}_i . \text{path}$
- 2) $\text{point} \notin \text{Loan}_i . \text{region}$

Example

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fn do_something(mut head: Option<Box<ListNode>>)  
{  
    let mut cur = &mut head;  
  
    if let Some(nodeBox) = cur.as_mut() {  
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    }  
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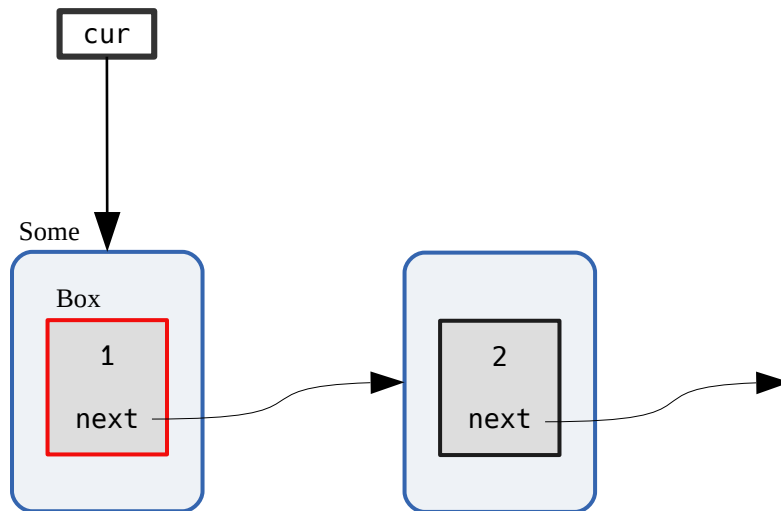
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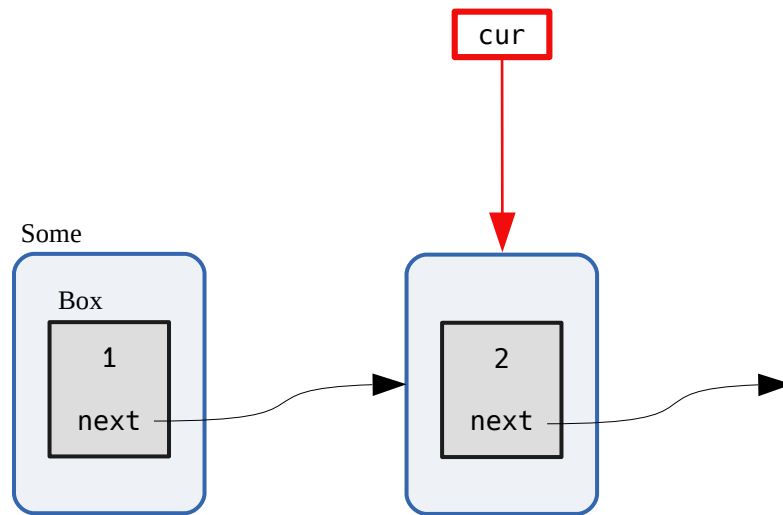
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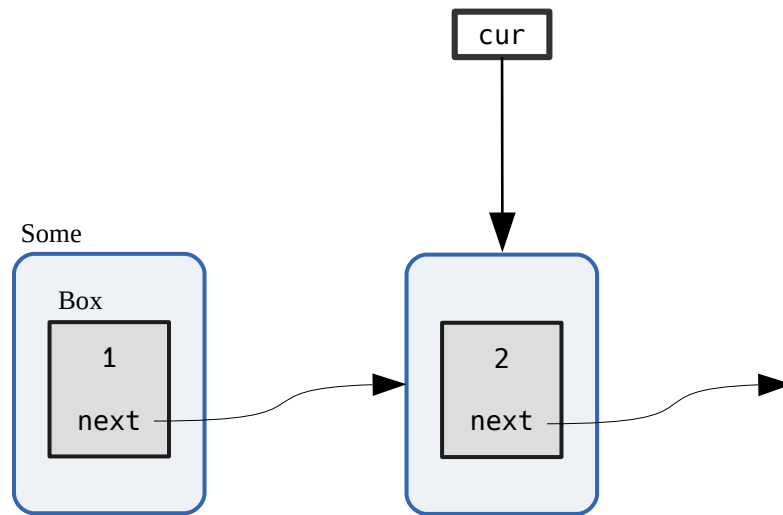
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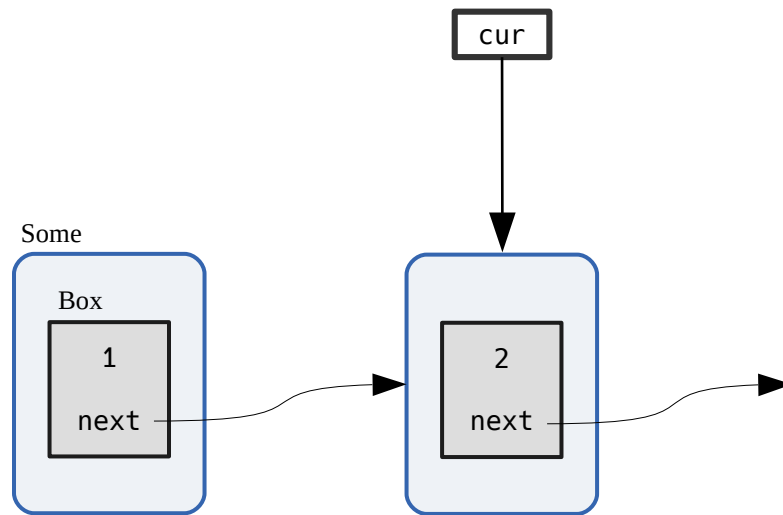
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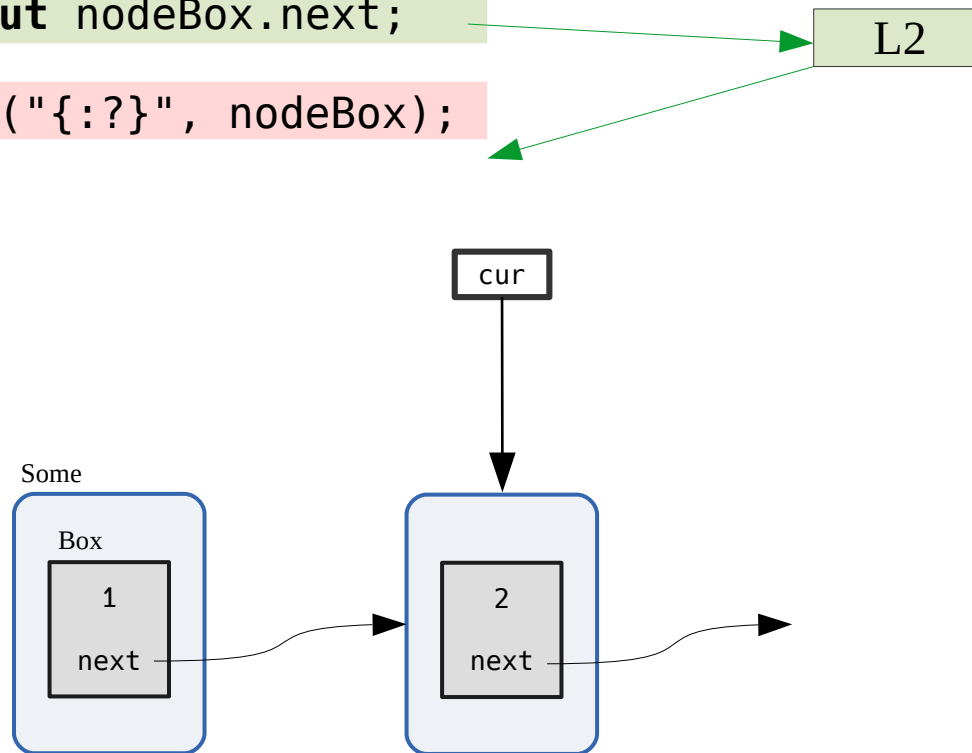
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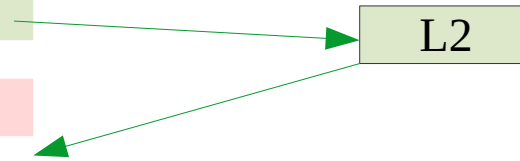
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Example

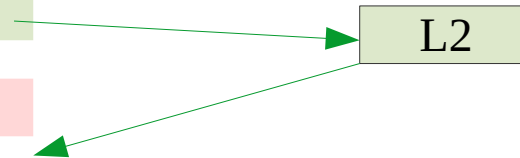
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```



Why **L2** live at this point ?

Example

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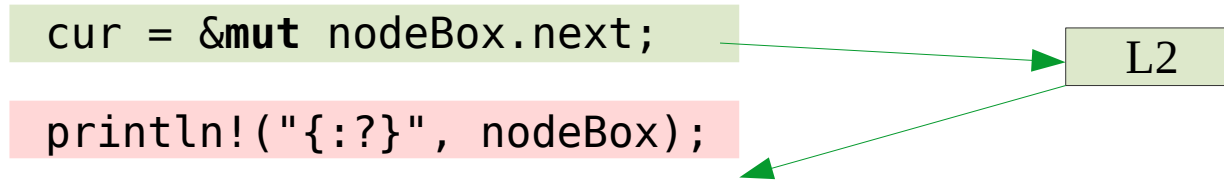


Why **`L2'** live at this point ?

1. no assignment to { nodeBox, nodeBox.next }
2. **`cur'** will be used later

Example

```
fn do_something(mut head: Option<Box<ListNode>>)  
{  
    let mut cur = &mut head;  
  
    if let Some(nodeBox) = cur.as_mut() {  
        cur = &mut nodeBox.next;  
        println!("{:?}", nodeBox);  
    }  
}
```



Why **`L2'** live at this point ?

1. no assignment to { nodeBox, nodeBox.next }
2. **`cur'** will be used later

It is rejected in the current borrow checker, but it is accepted by the Polonius borrow checker in the future.

參考題目

Leetcode : remove linked list elements

Datafrog

The tool used in Rust's new borrow checker called
Polonius

Idea

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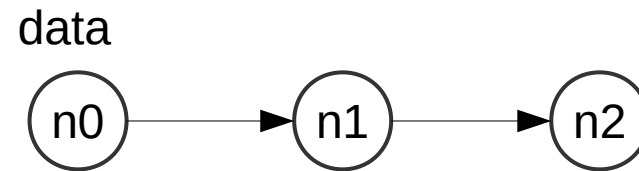
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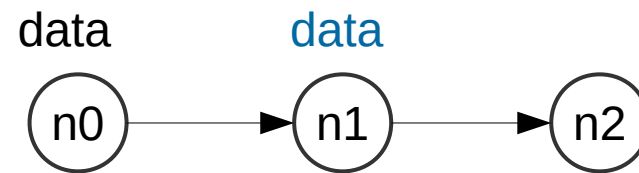
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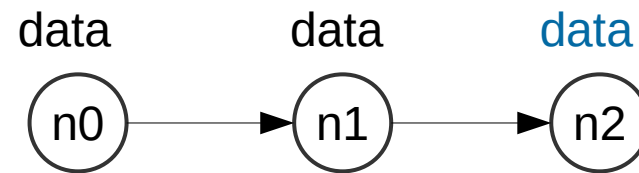
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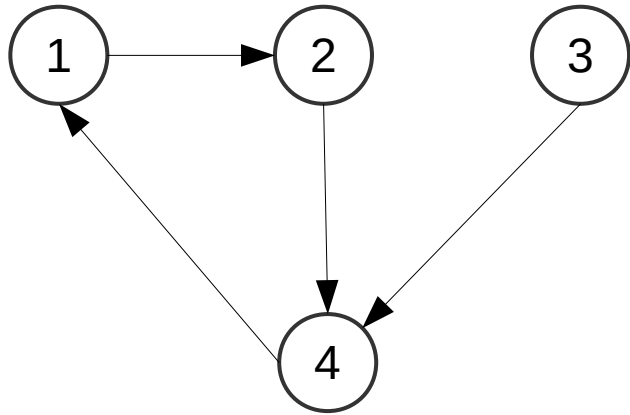
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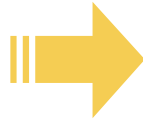
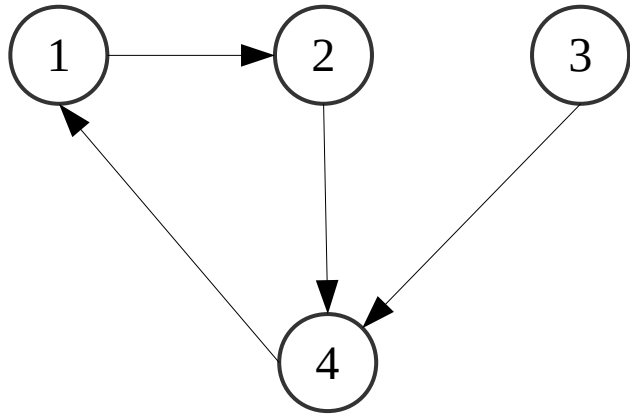
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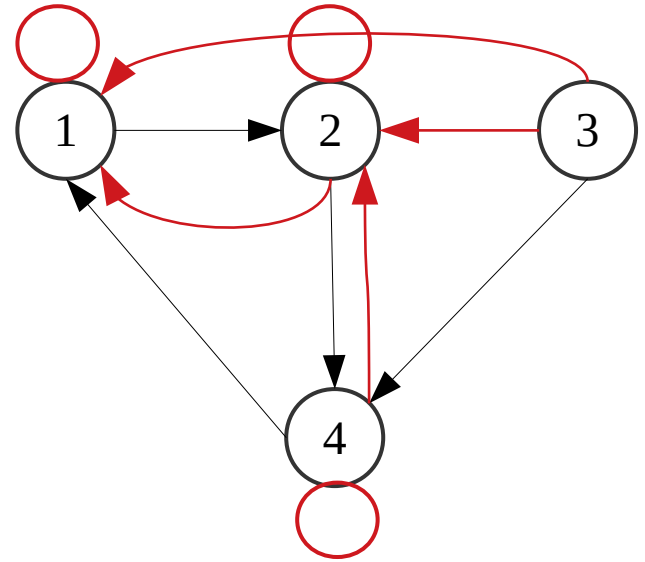
Example . Transitive Closure



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$$\frac{e(a,b) \quad e(b,c)}{e(a,c)}$$



Implementation – Initial

```
// create a iteration context
let mut iteration = Iteration::new();

// create some variables for later use
let v_edges  = iteration.variable::<(u32, u32)>("edges");
let v_redges = iteration.variable::<(u32, u32)>("reverse edges");

// load the initial variables
v_edges.insert(edges.into());

// start iteration
while iteration.changed() {

    ...

}


let result = v_edges.complete();
```

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v_edges.insert(edges.into());

// start iteration
while iteration.changed() {
     Writing Rules here
}

let result = v_edges.complete();
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Implementation – Writing Rules

```
while iteration.changed() {  
    // reverse edges for mapping  
    v_redges.from_map(&v_edges, |&(a, b)| (b, a));  
  
    // e(a,c) <- e(a,b), e(b,c)  
    v_edges.from_join(&v_redges, &v_edges, |_b, &a, &c| (a, c));  
}
```

Implementation – Writing Rules

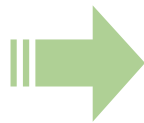
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$$\frac{e(a,b)}{e(b,c)} \frac{e(b,c)}{e(a,c)}$$



$$\frac{e(a,b)}{r(b,a)}$$

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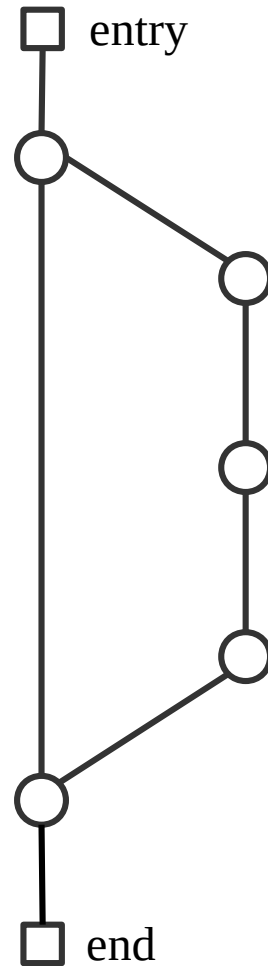
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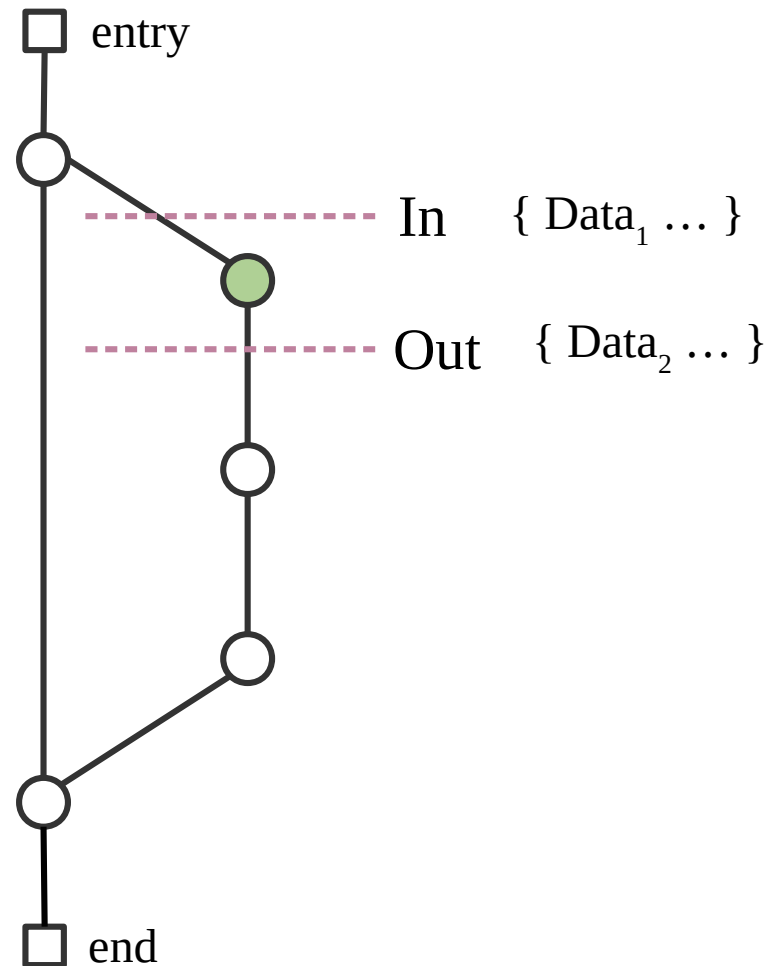
$$\frac{e(a,b)}{e(b,c)} \quad \Rightarrow \quad \frac{e(a,b)}{r(b,a)} \quad \frac{r(\textcolor{red}{b}, \textcolor{green}{a})}{e(\textcolor{red}{b}, \textcolor{blue}{c})} \quad \frac{e(a,c)}{e(a,c)}$$

QA

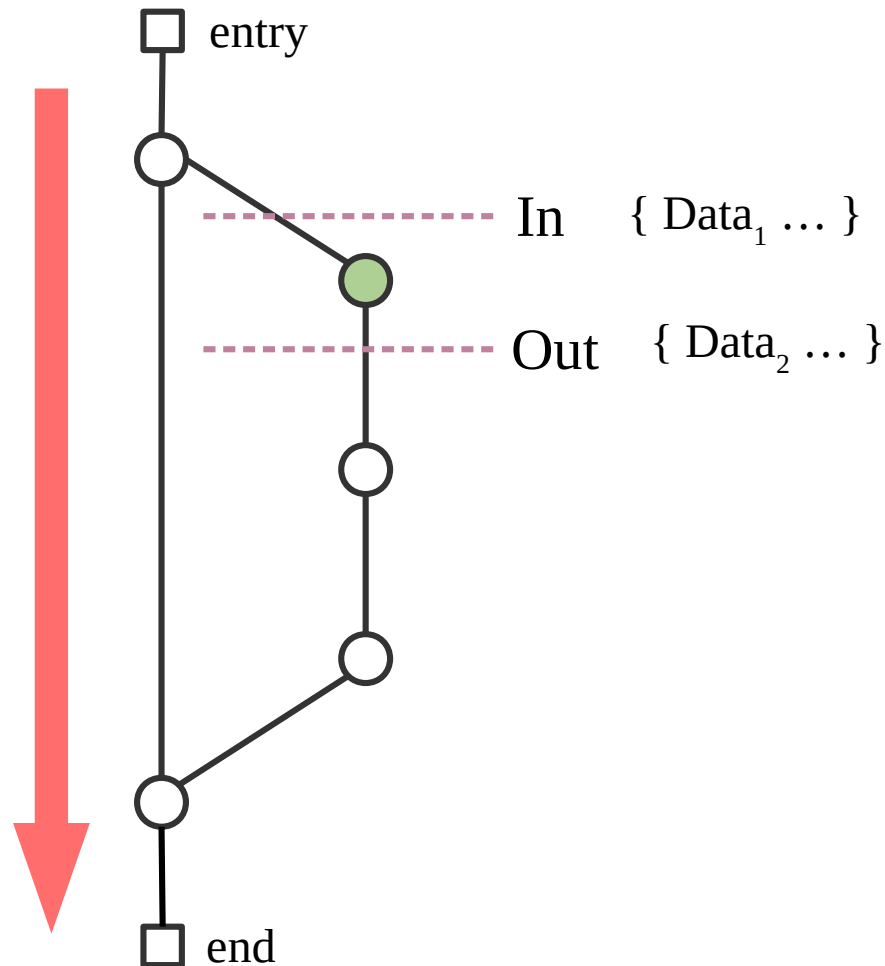
Data Flow Concepts $\langle D, V, \wedge, F \rangle$



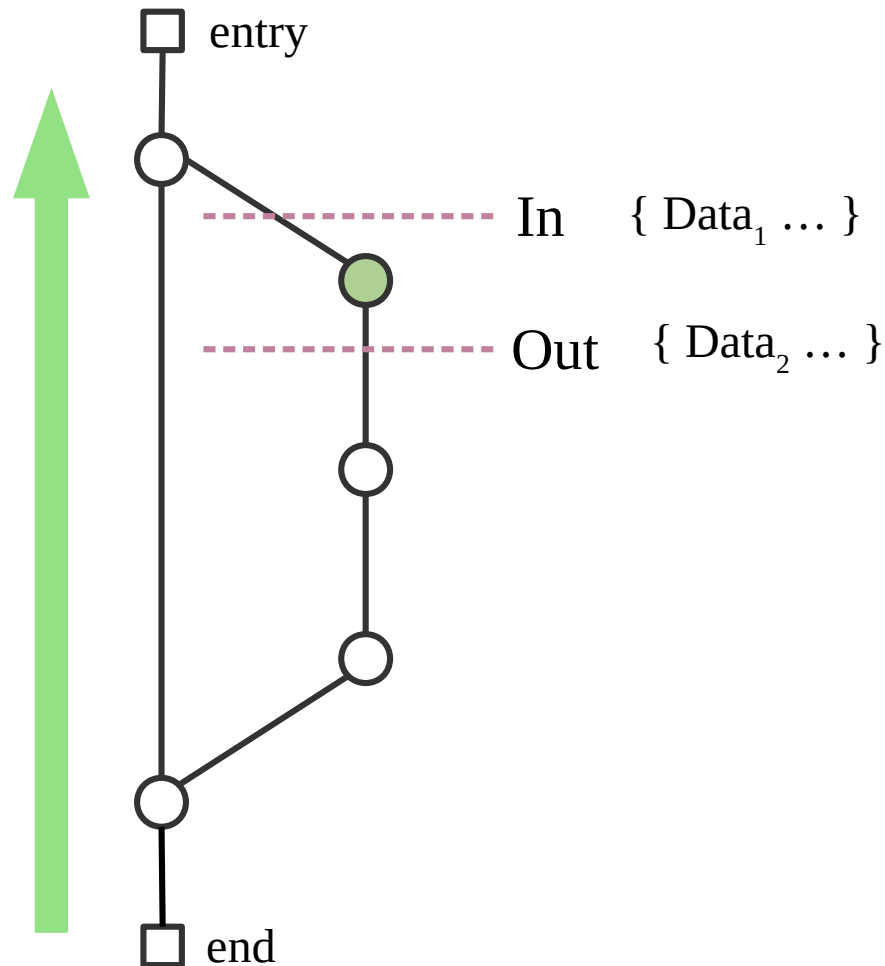
Data Flow Concepts $\langle D, \mathbf{V}, \Lambda, F \rangle$



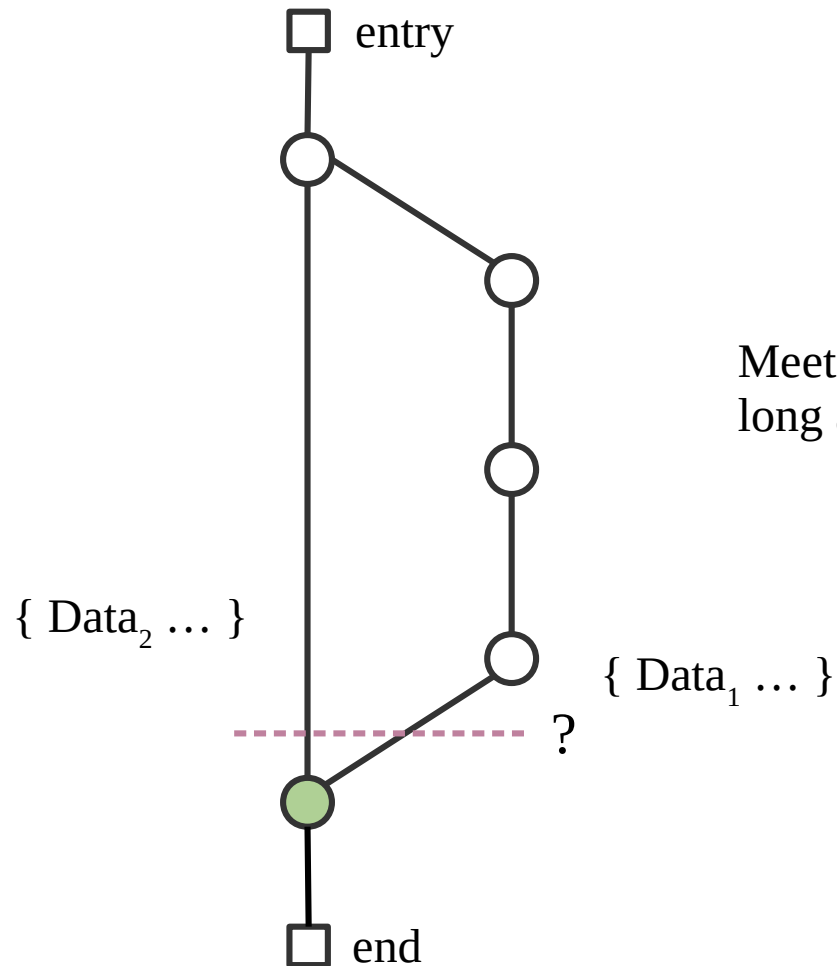
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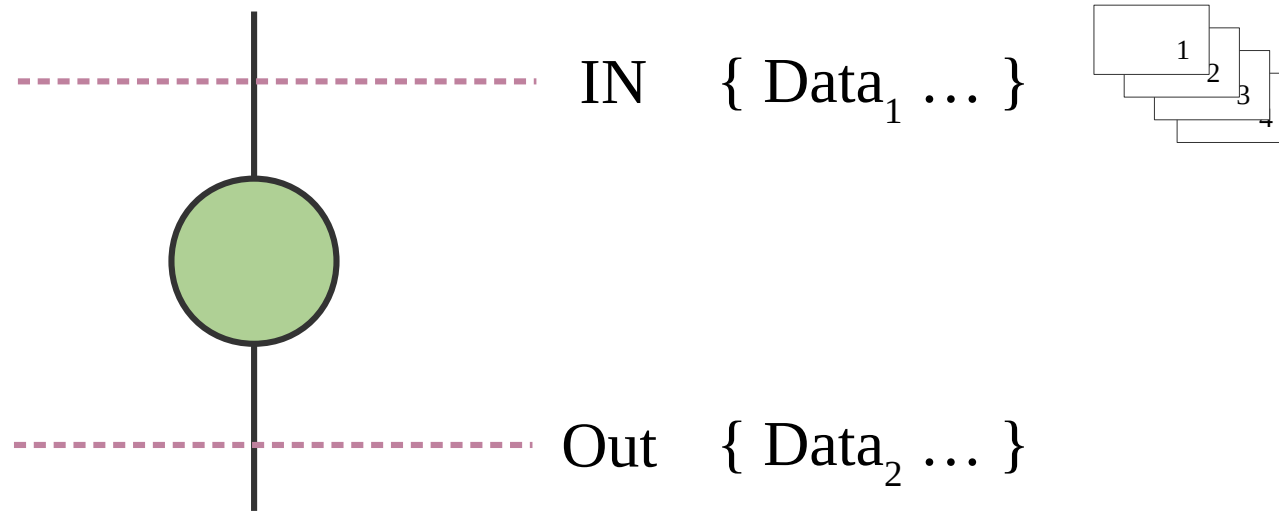


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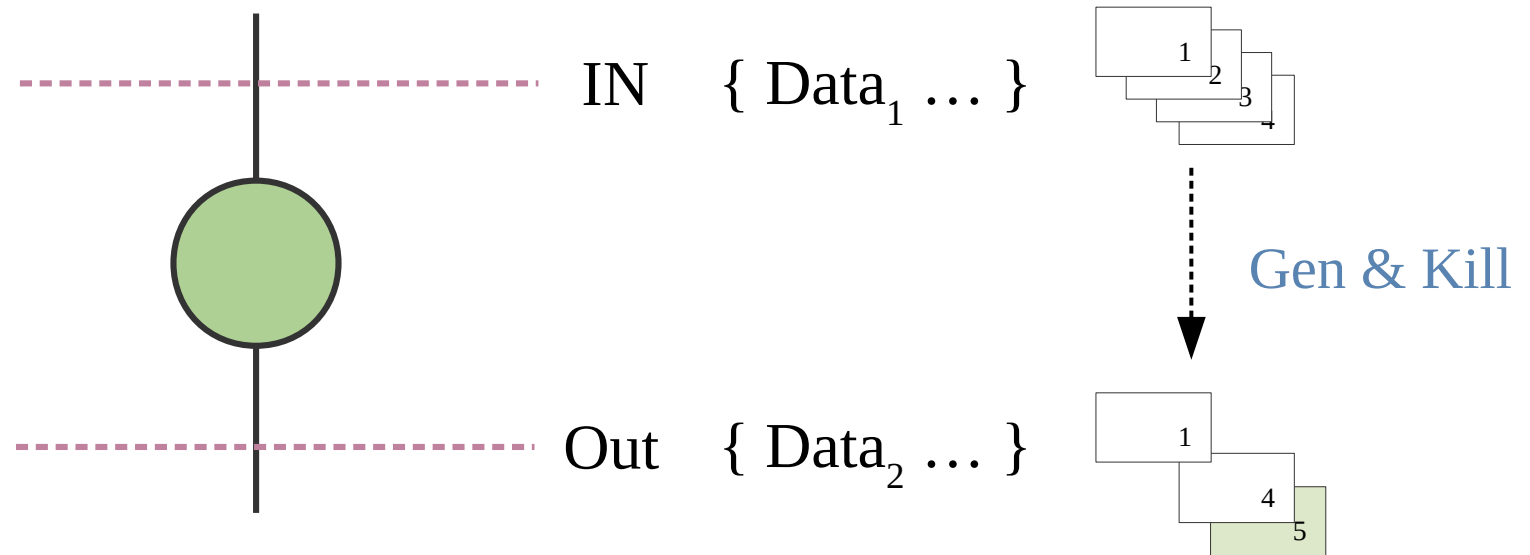


Meet operator can be union, intersection, as long as it can make $(V, \mathbf{\Lambda})$ semilattice.

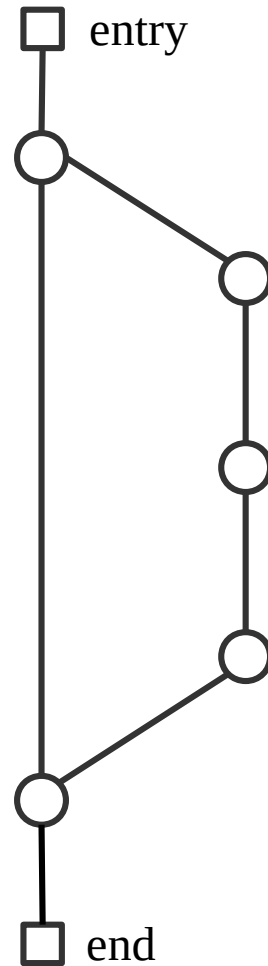
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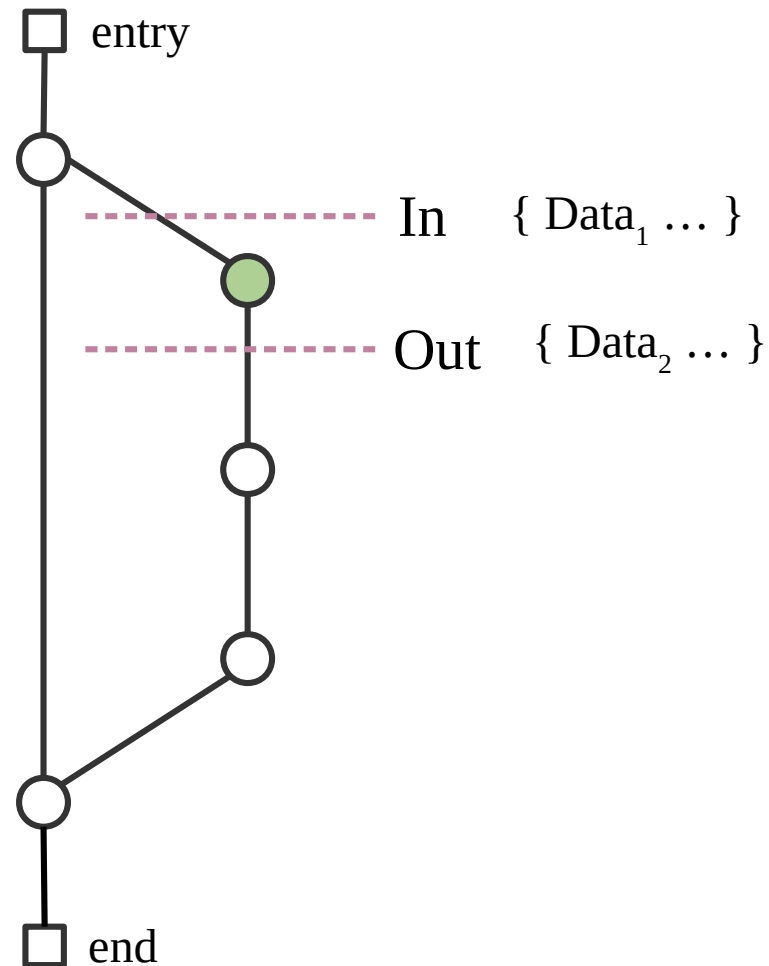
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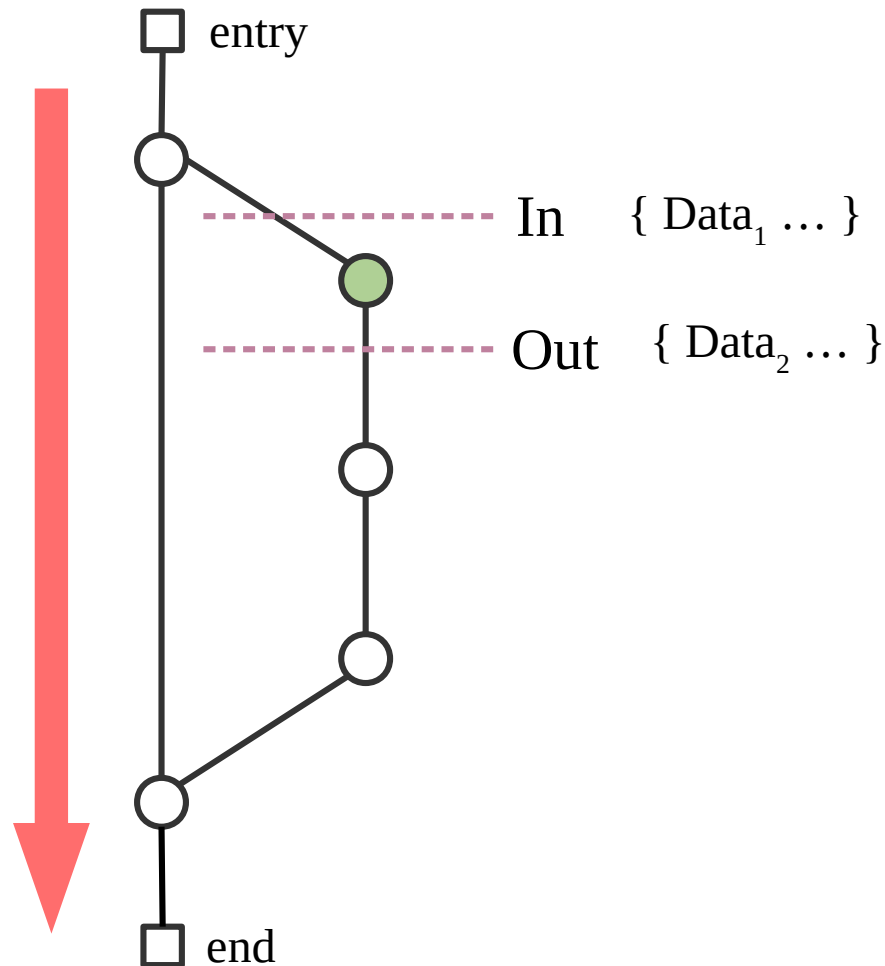
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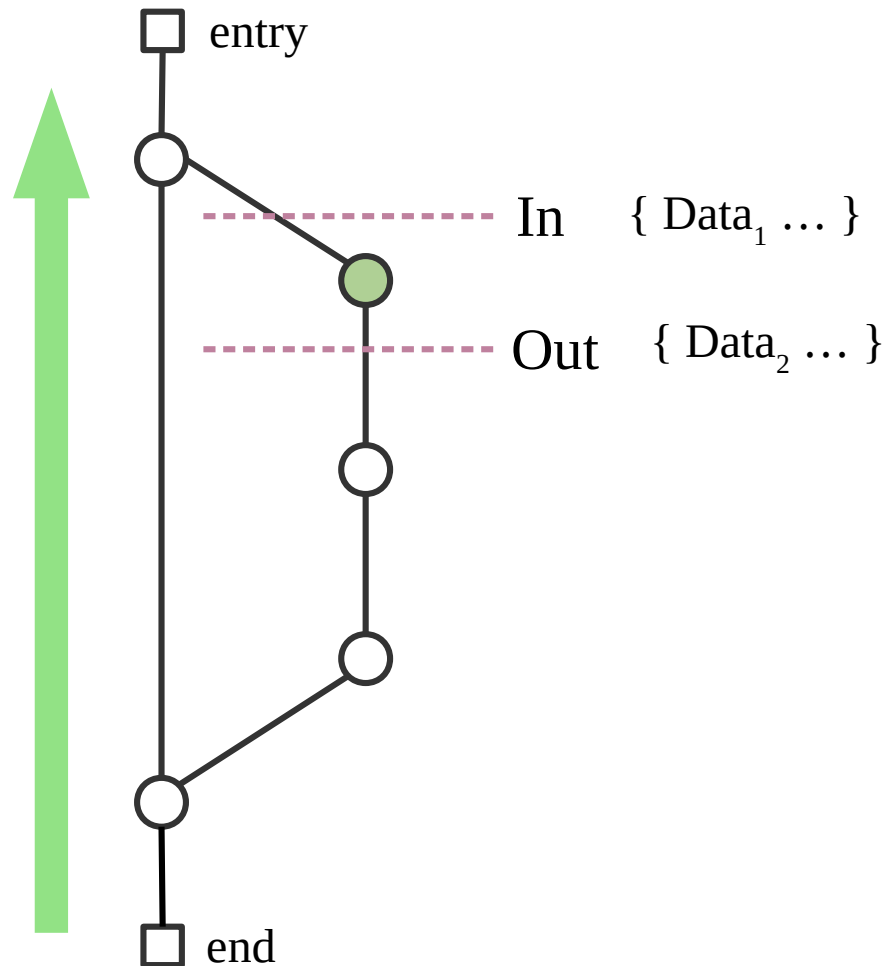
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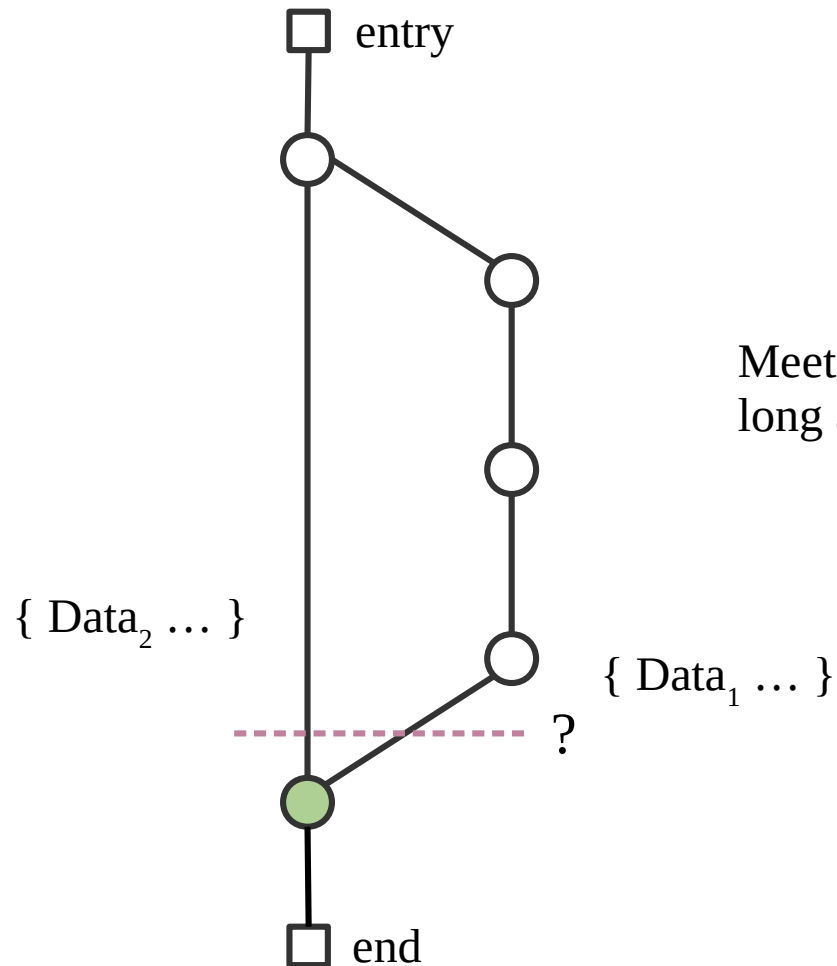
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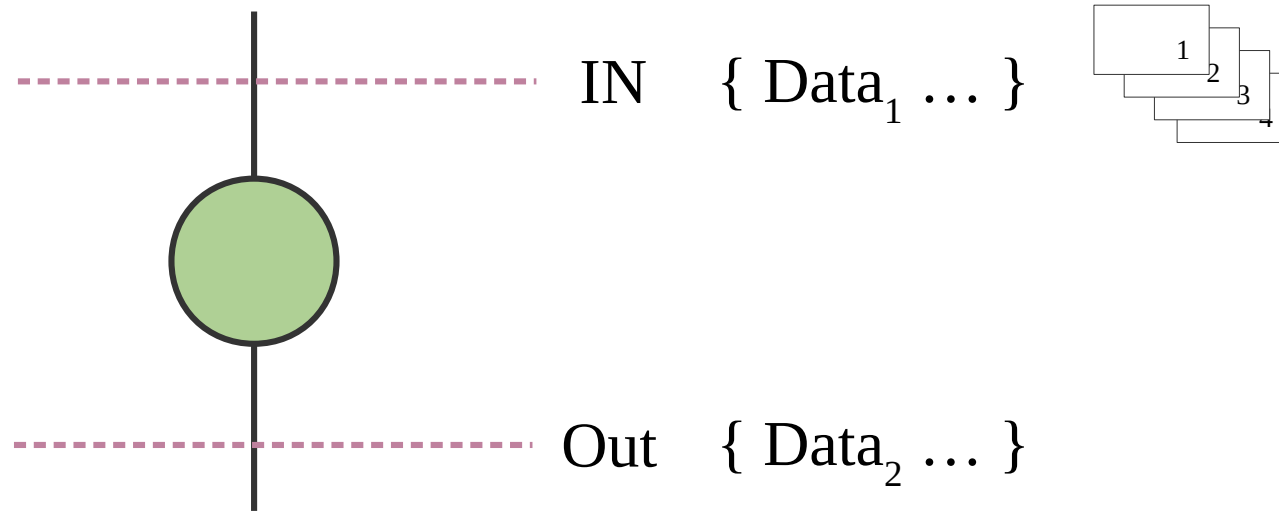


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