

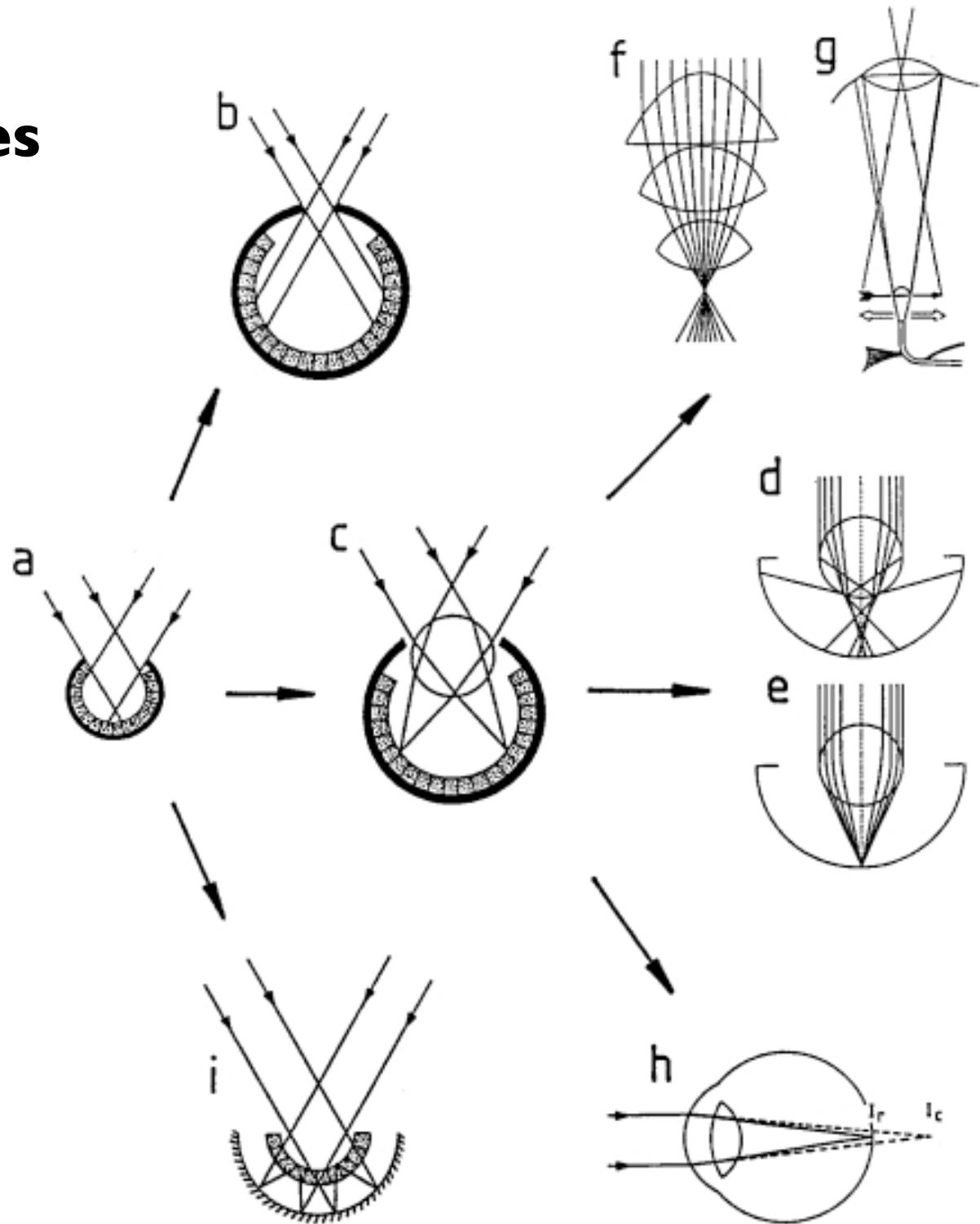


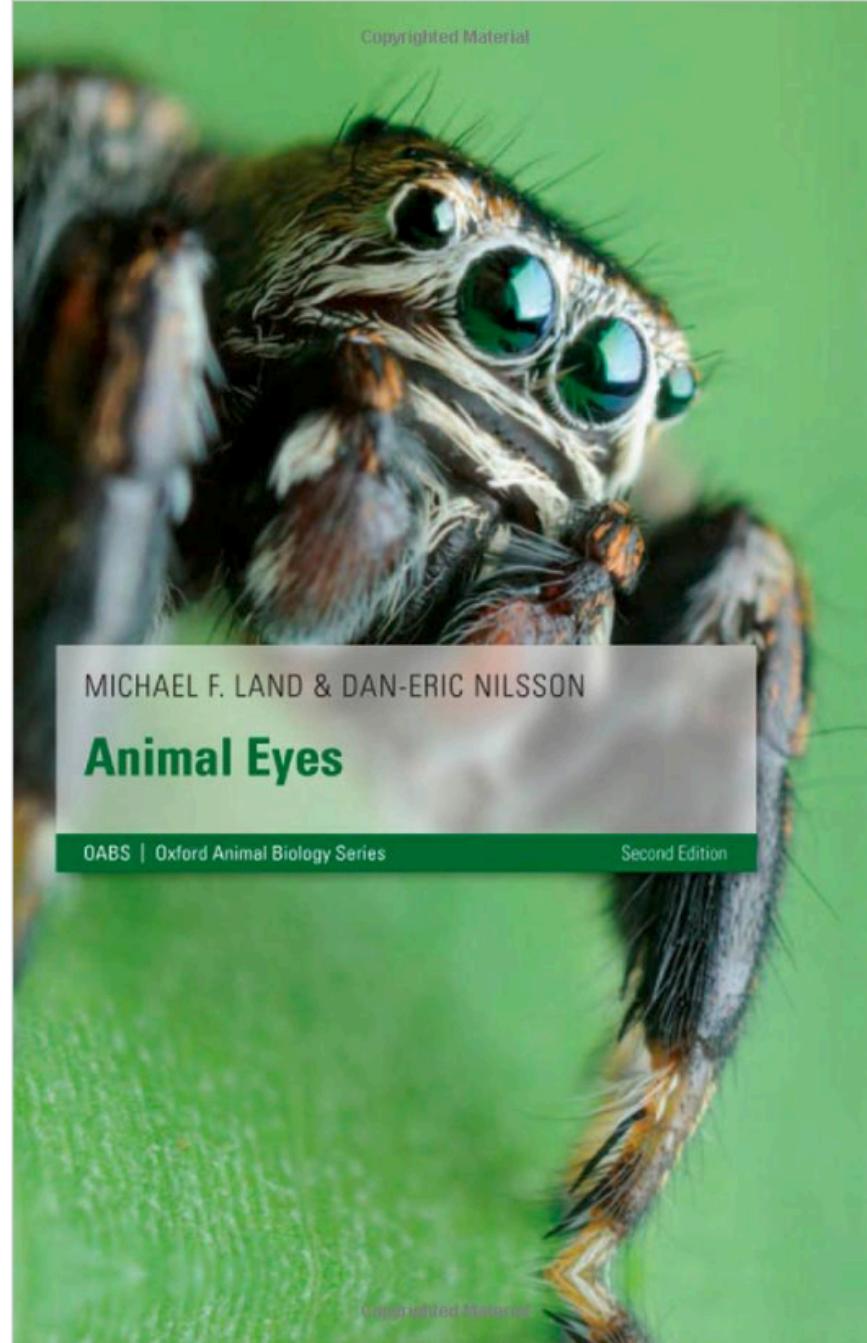
Redwood Center for Theoretical Neuroscience - April 2018

1. How did vision evolve? What is it for?
2. What constitutes an efficient code of color information?
3. How to form a stable color percept from unstable images?
4. How are color categories learned? How and where are they represented in brain?

The evolution of eyes

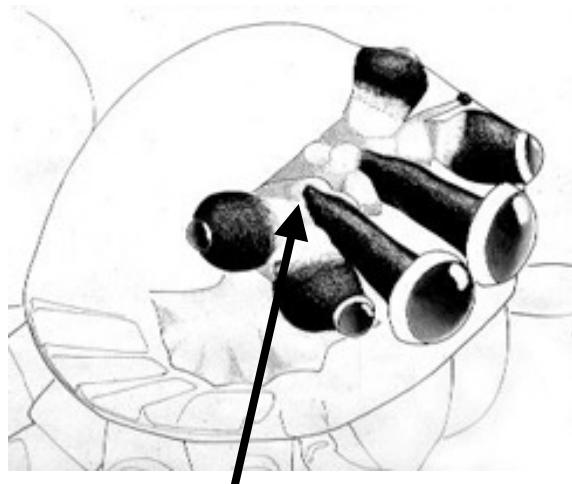
Land & Fernald (1992)





http://rctn.org/wiki/VS298:_Animal_Eyes

Vision in jumping spiders



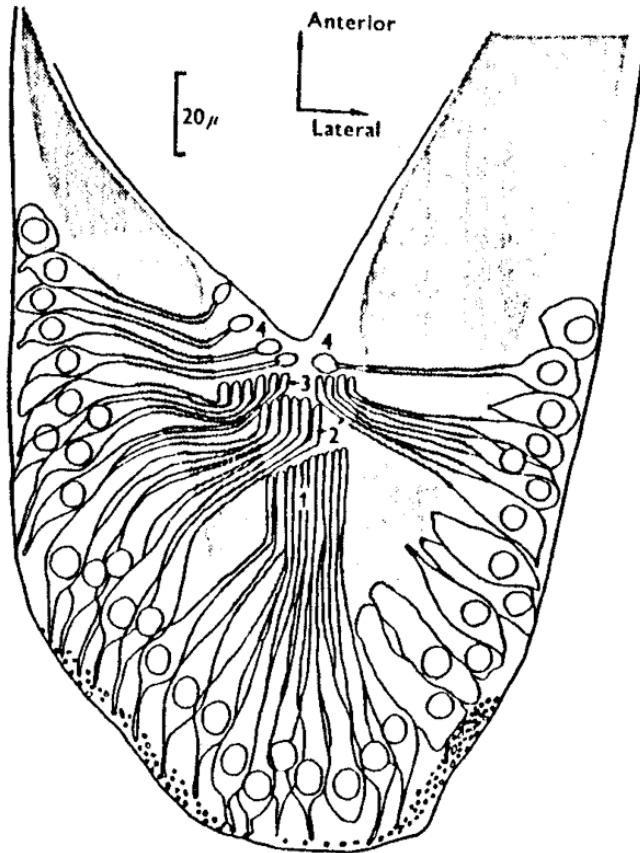
(Wayne Maddison)



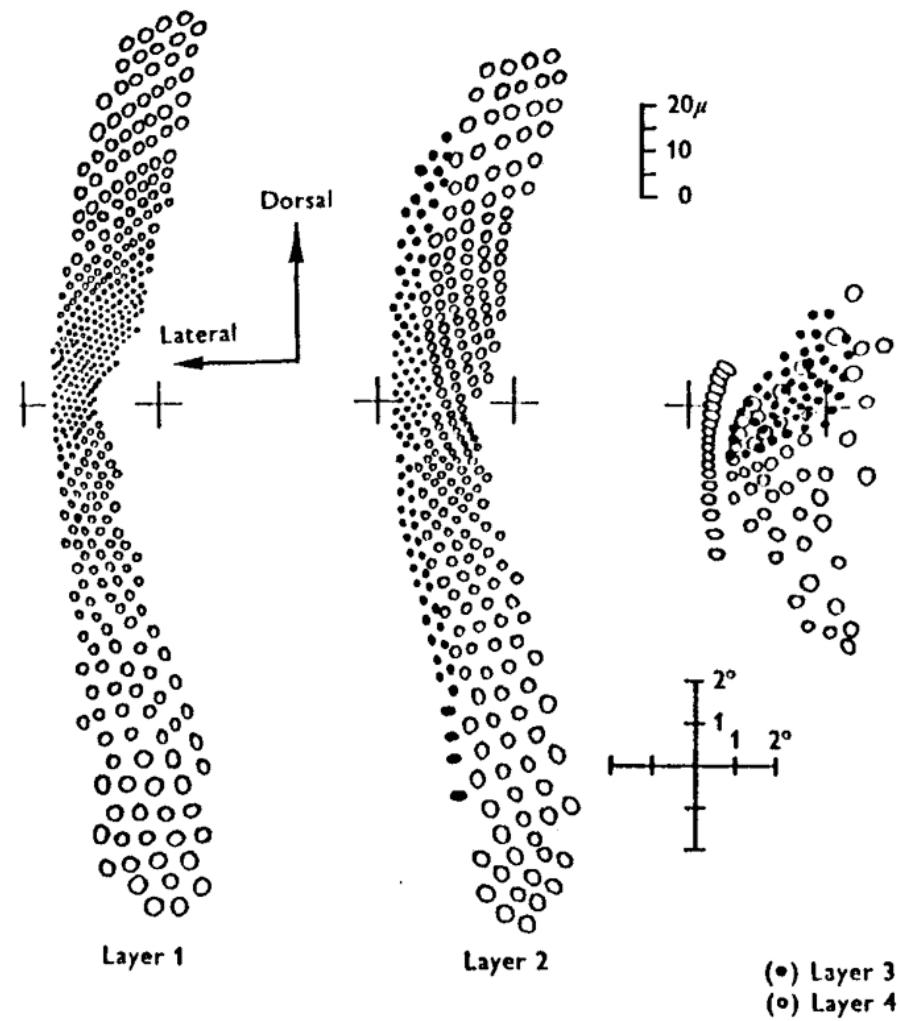
(Bair & Olshausen, 1991)

Jumping spider retina

horizontal section



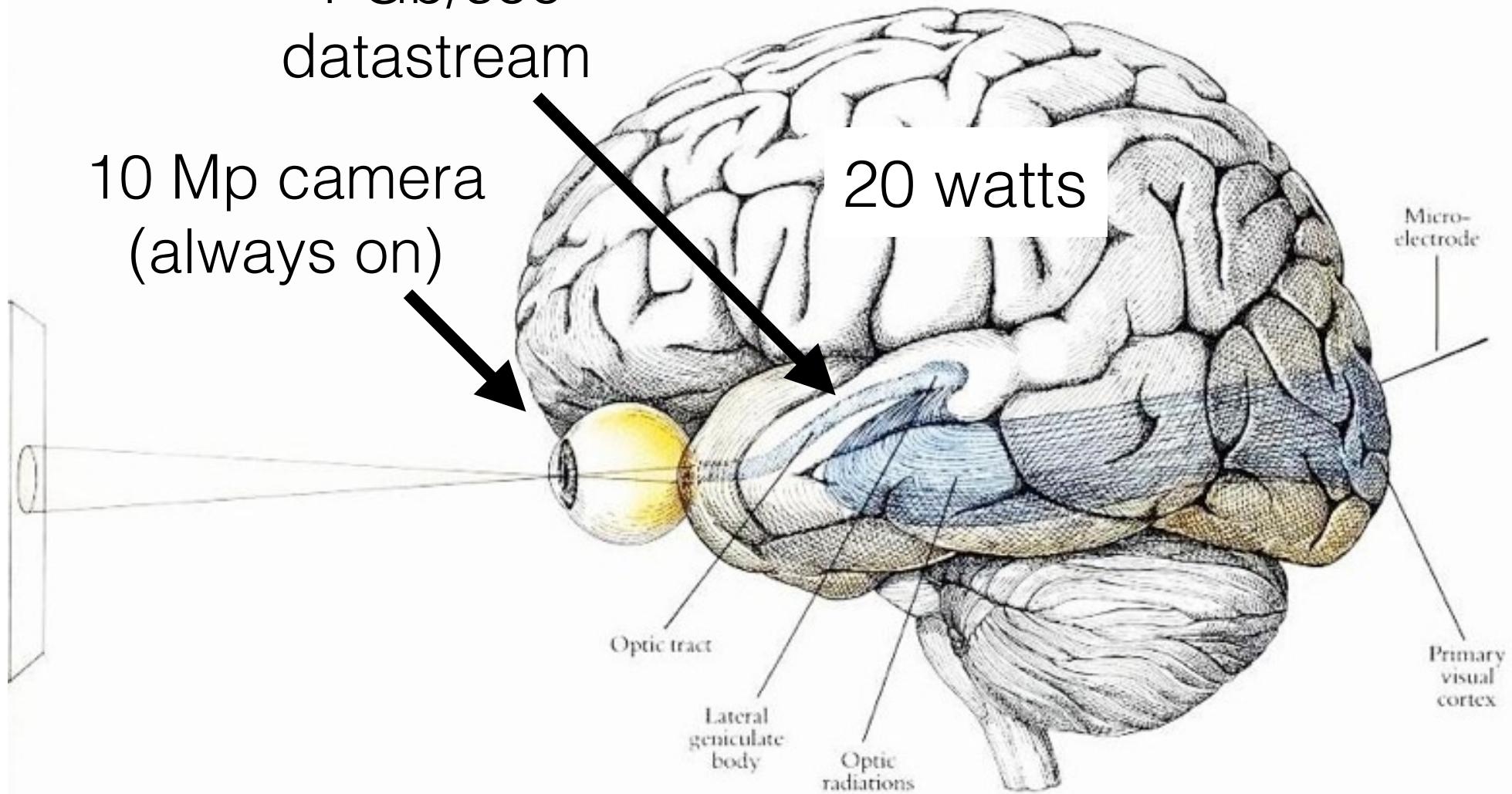
photoreceptor array

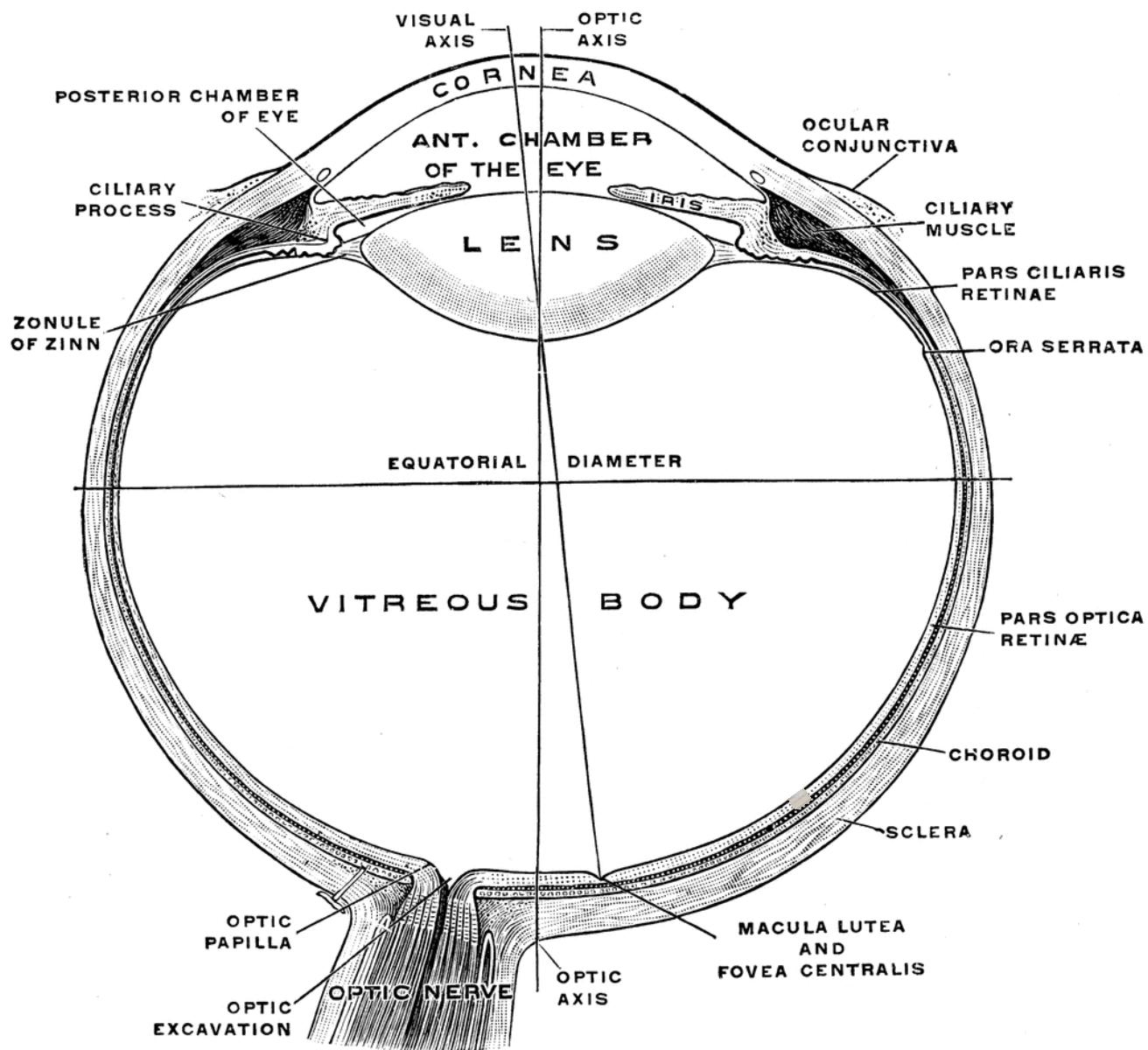


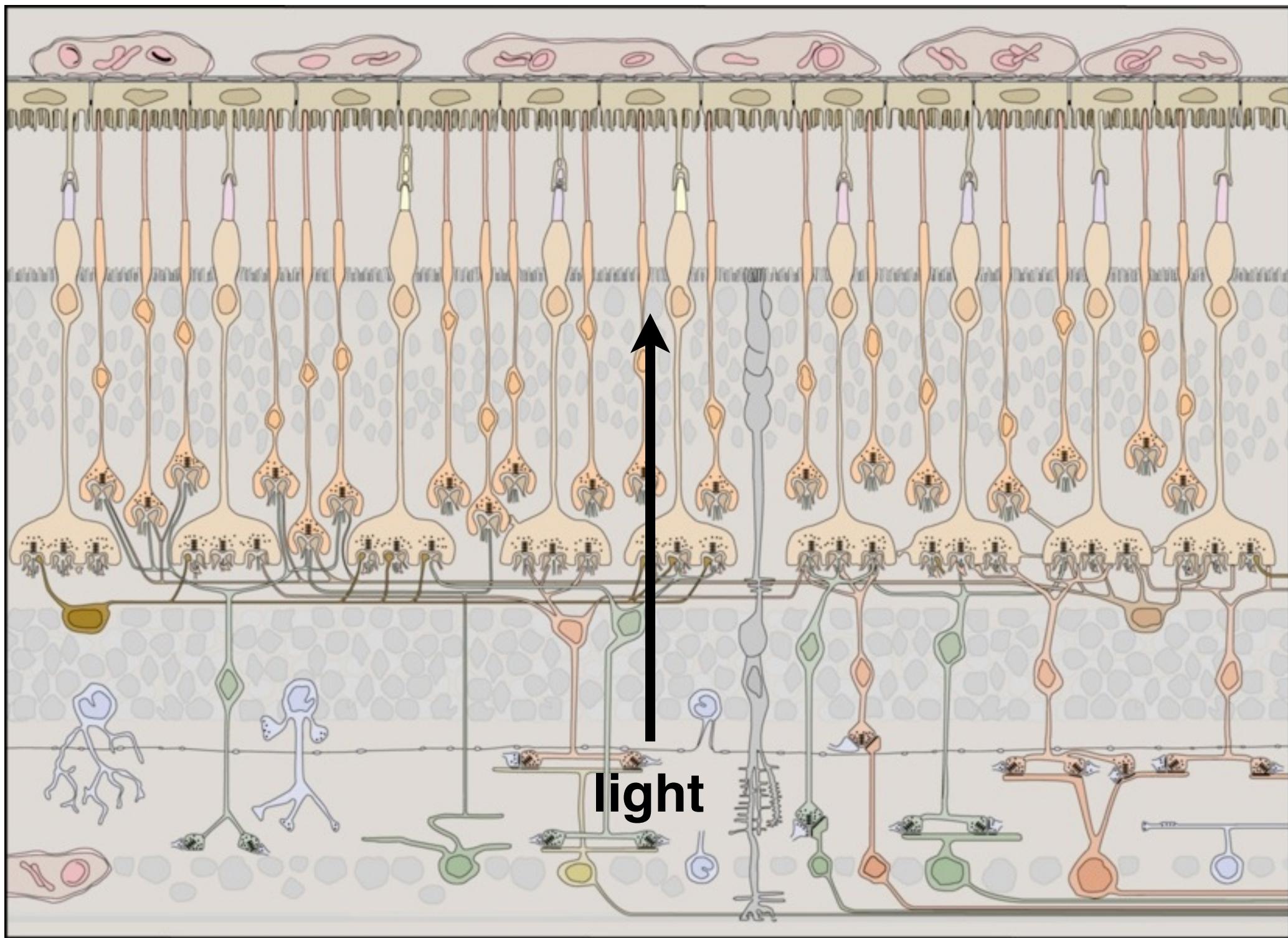
2. What constitutes an efficient code of color information?

1 Gb/sec
datastream

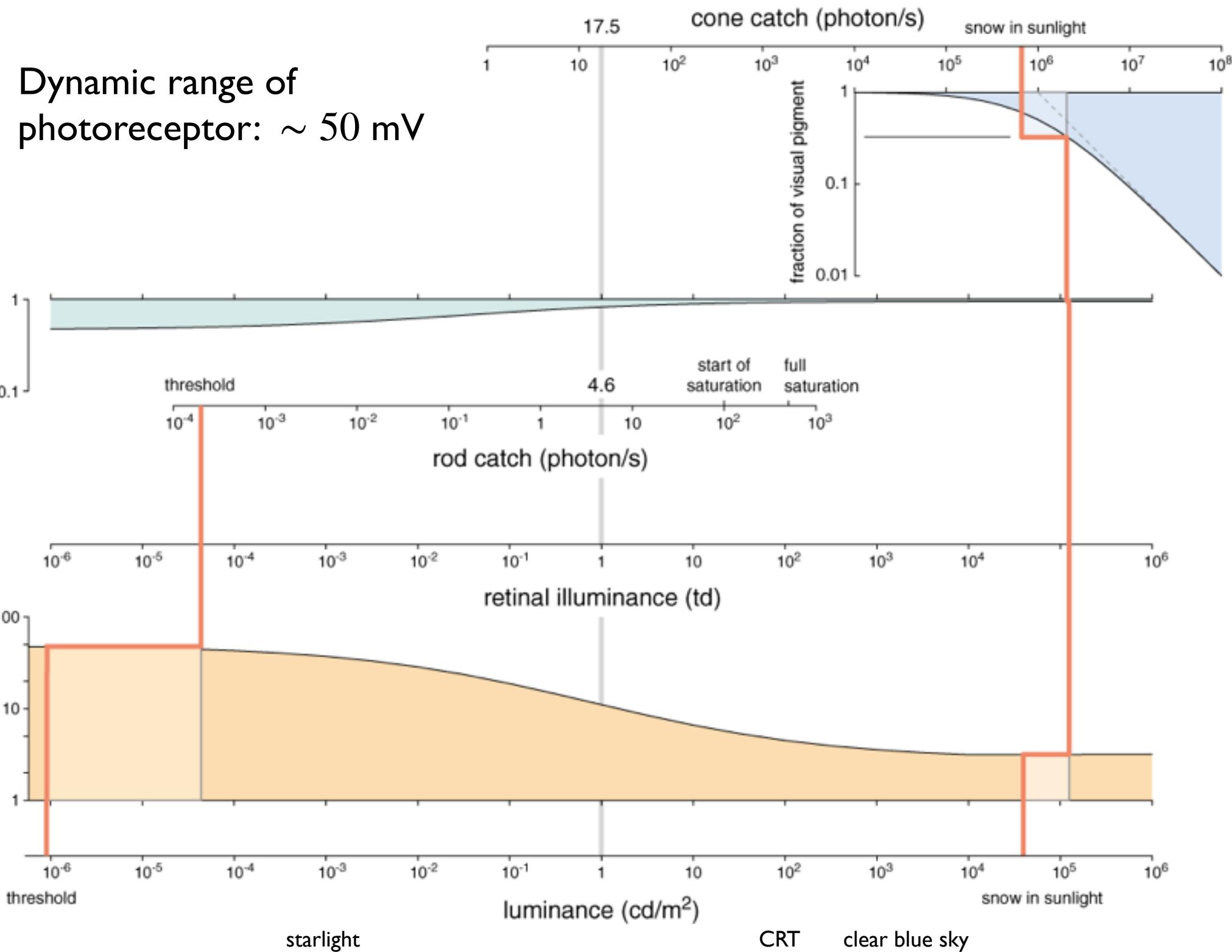
10 Mp camera
(always on)



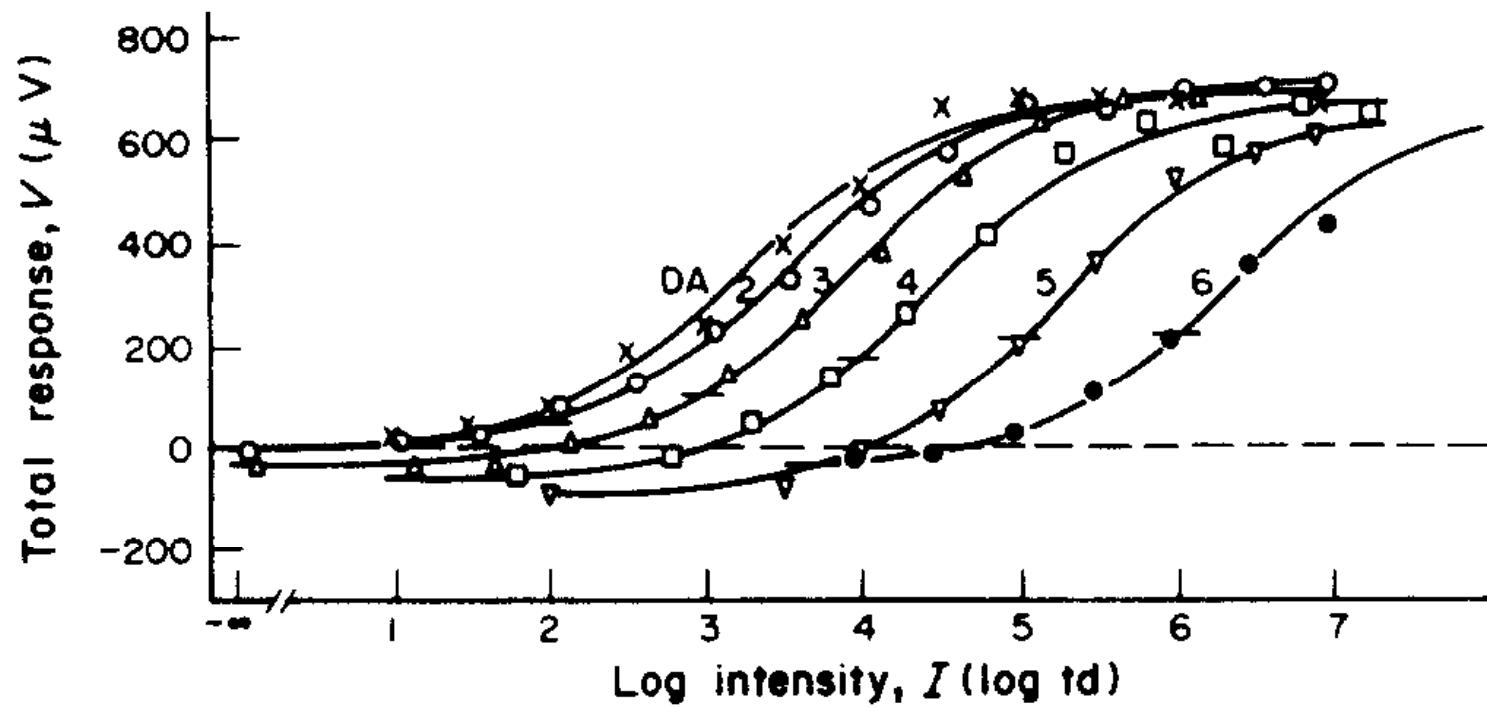




Dynamic range of photoreceptor: ~ 50 mV

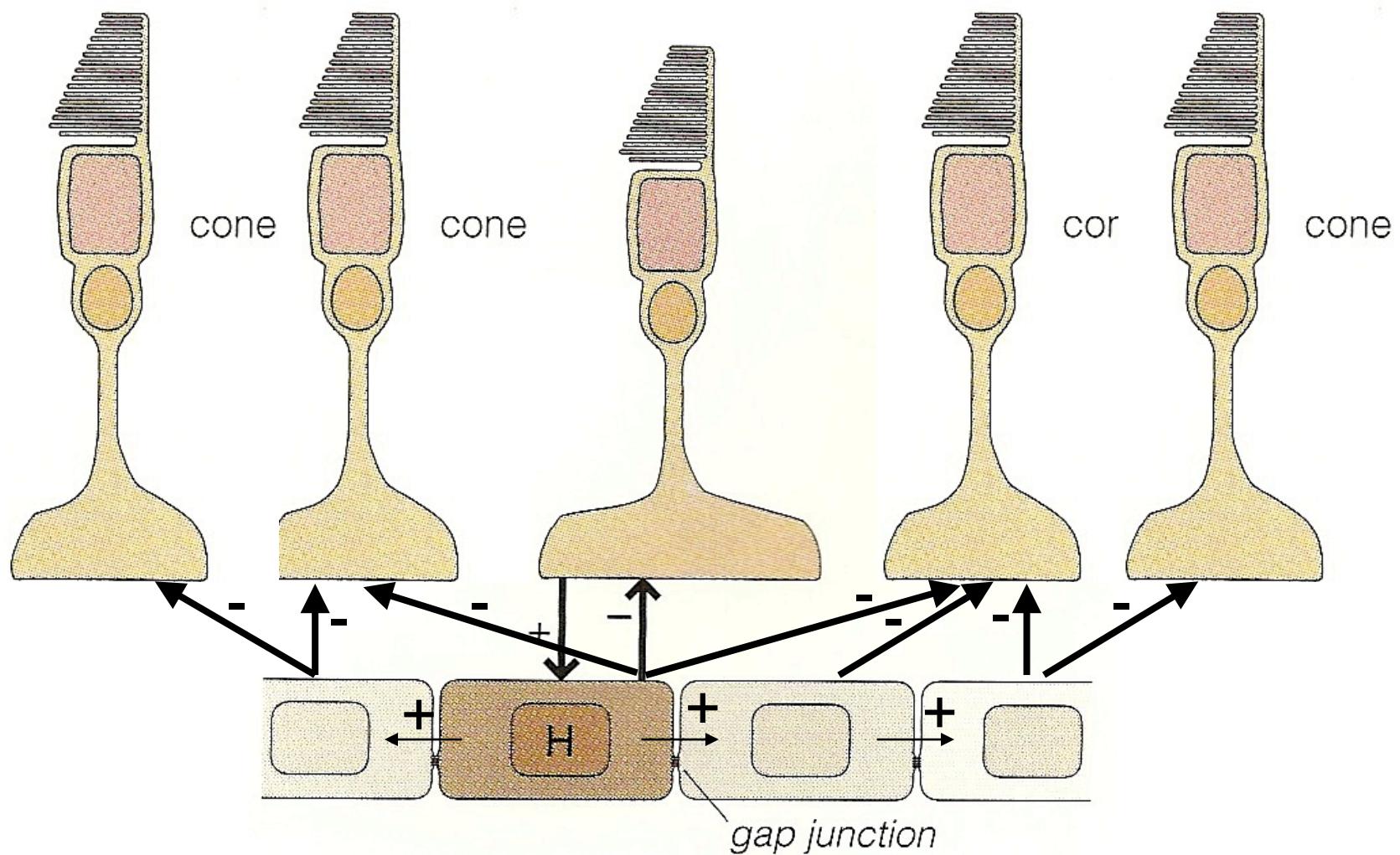


Light adaptation (primate cones)



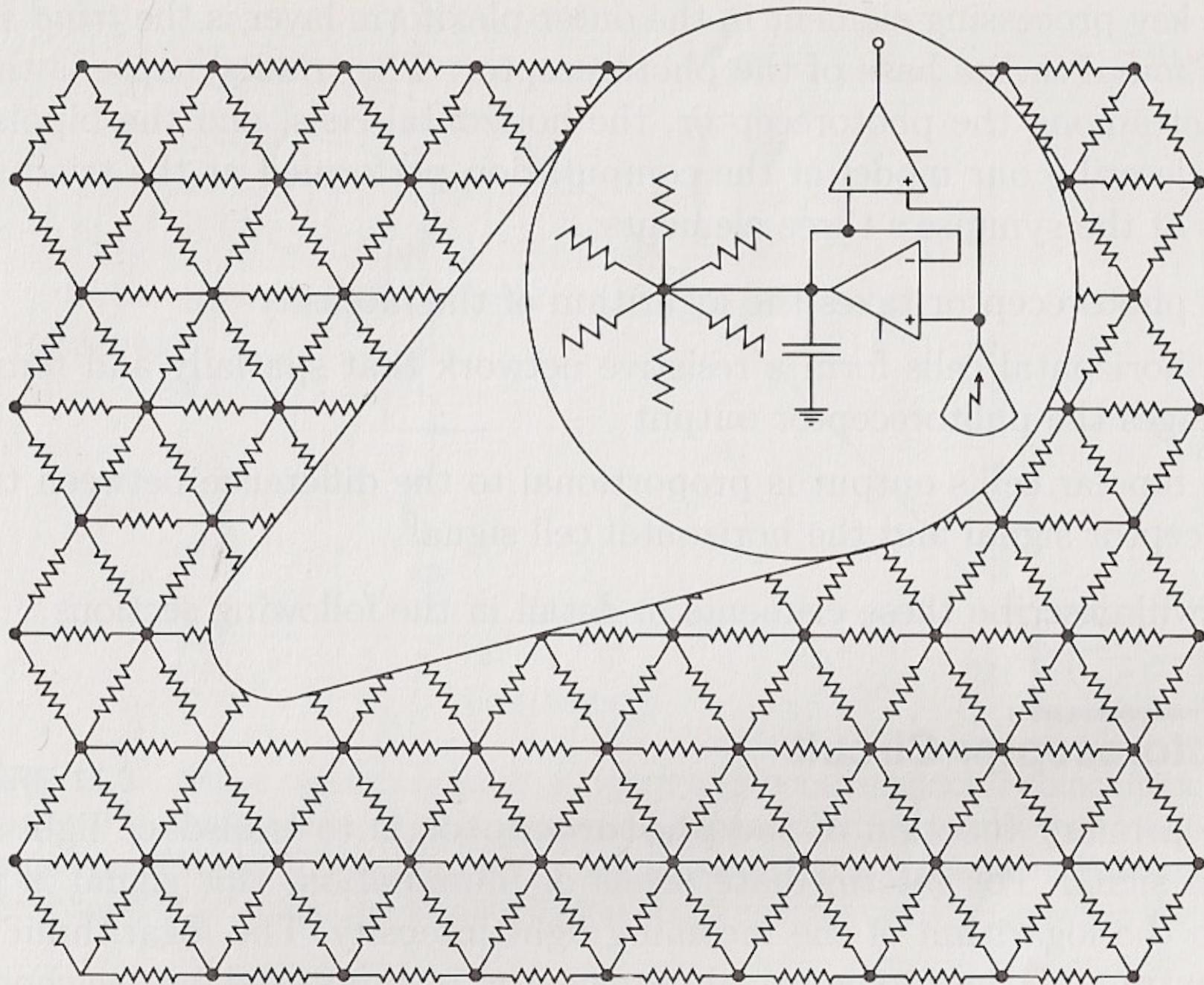
Valeton & van Norren (1983)

Hyperpolarization of horizontal cell spreads to other horizontal cells via gap junctions

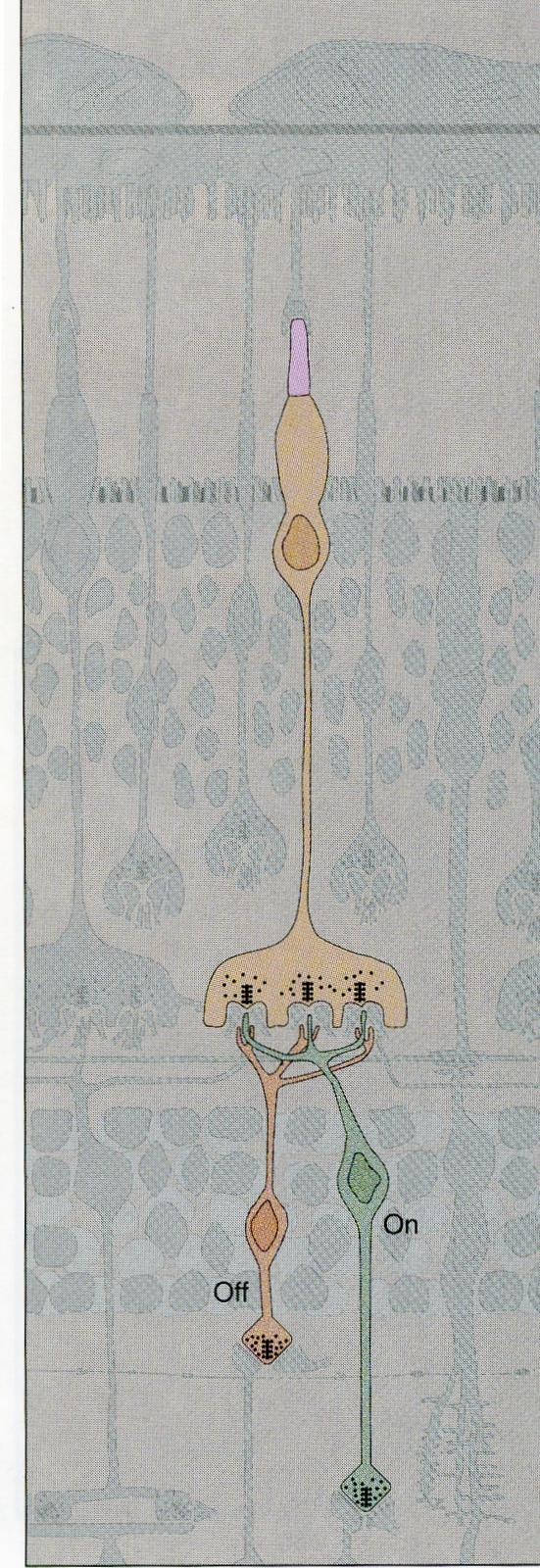


Analog VLSI retina

(Mead & Mahowald, 1989)



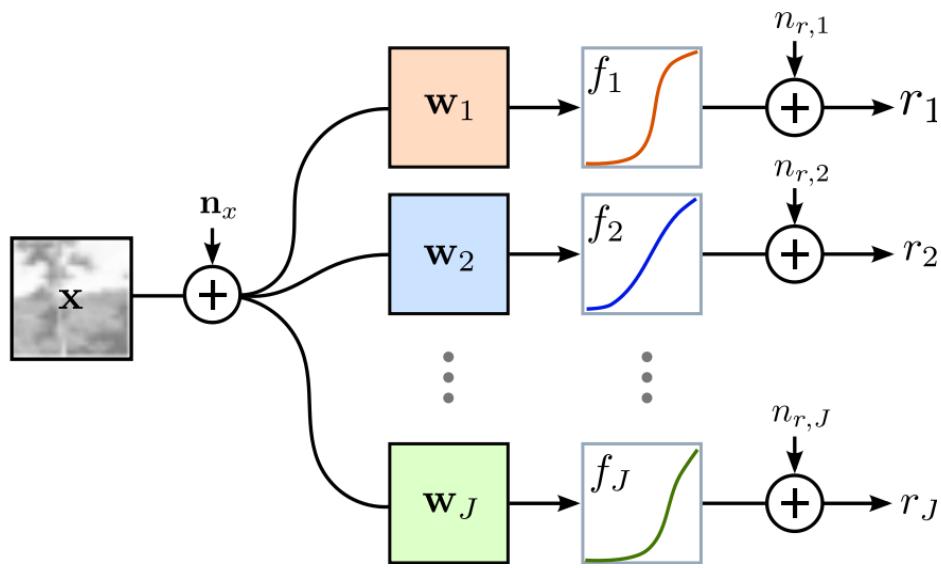
On vs. *off* cone bipolar cells



Efficient coding model of retina

(Karklin & Simoncelli 2012)

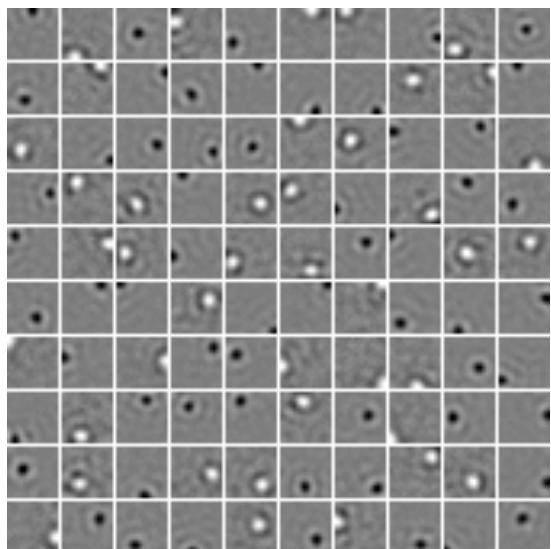
a



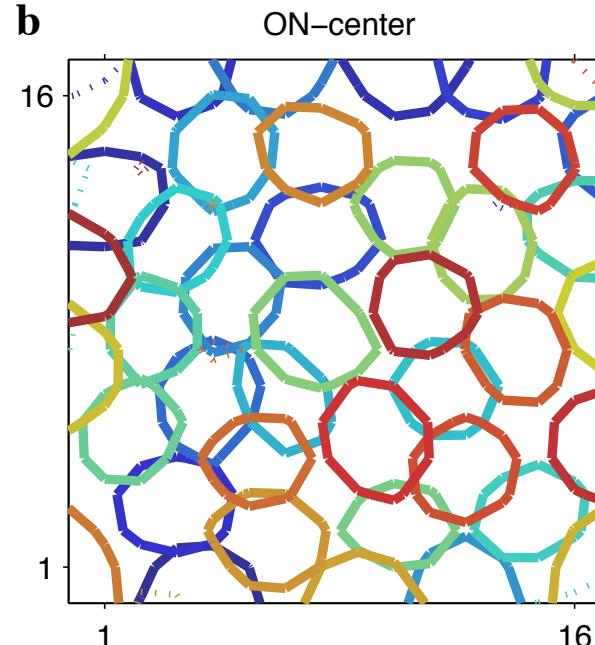
Objective function:

$$I(X; R) - \sum_j \lambda_j \langle r_j \rangle$$

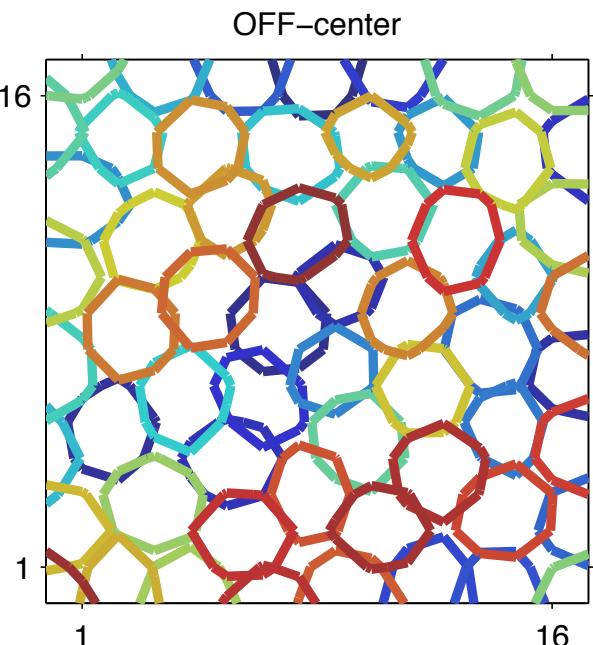
a



b



ON-center

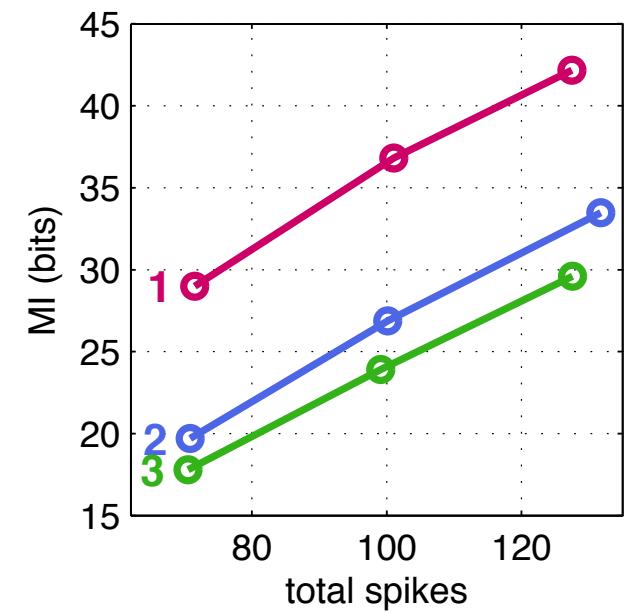
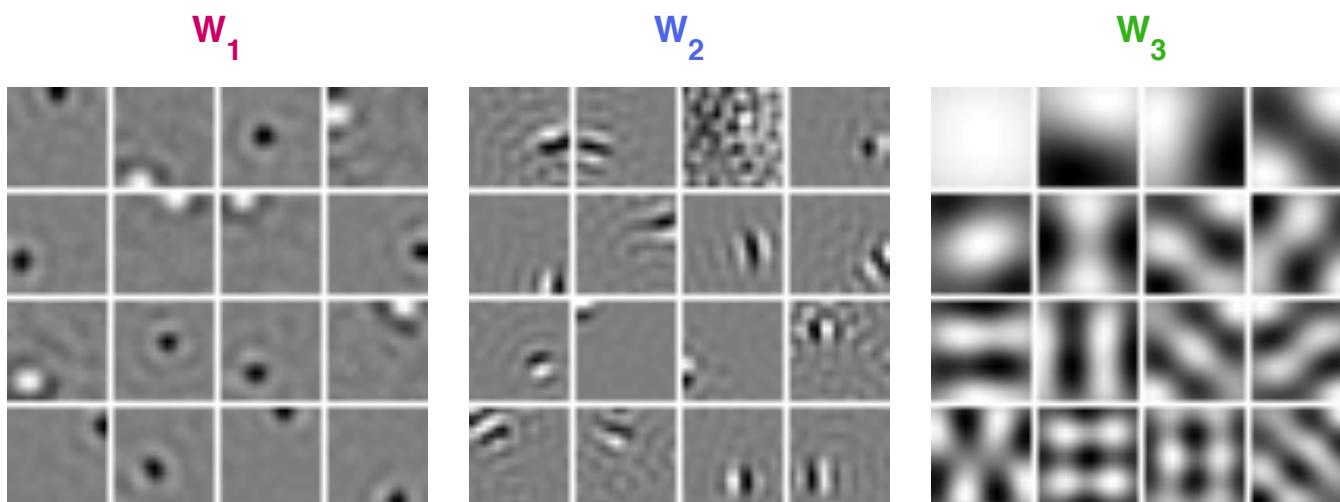


OFF-center

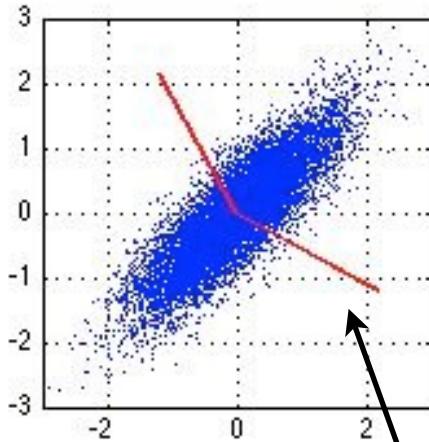
c

Efficient coding model of retina

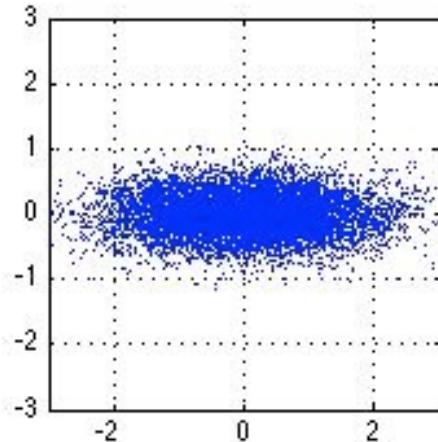
(Karklin & Simoncelli 2012)



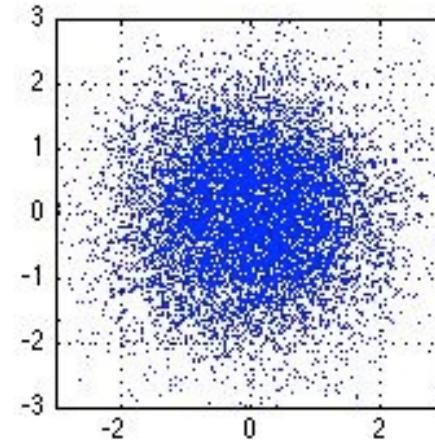
Whitening



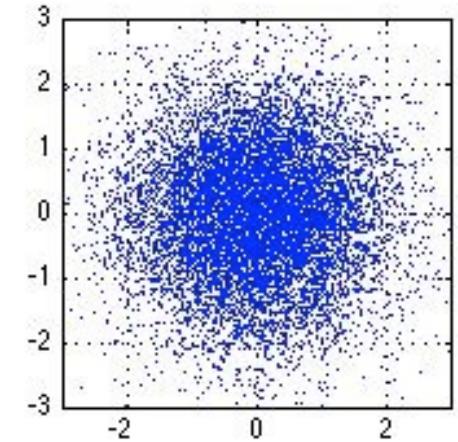
\mathbf{X}



$\mathbf{E}^T \mathbf{X}$



$\Lambda^{-\frac{1}{2}} \mathbf{E}^T \mathbf{X}$



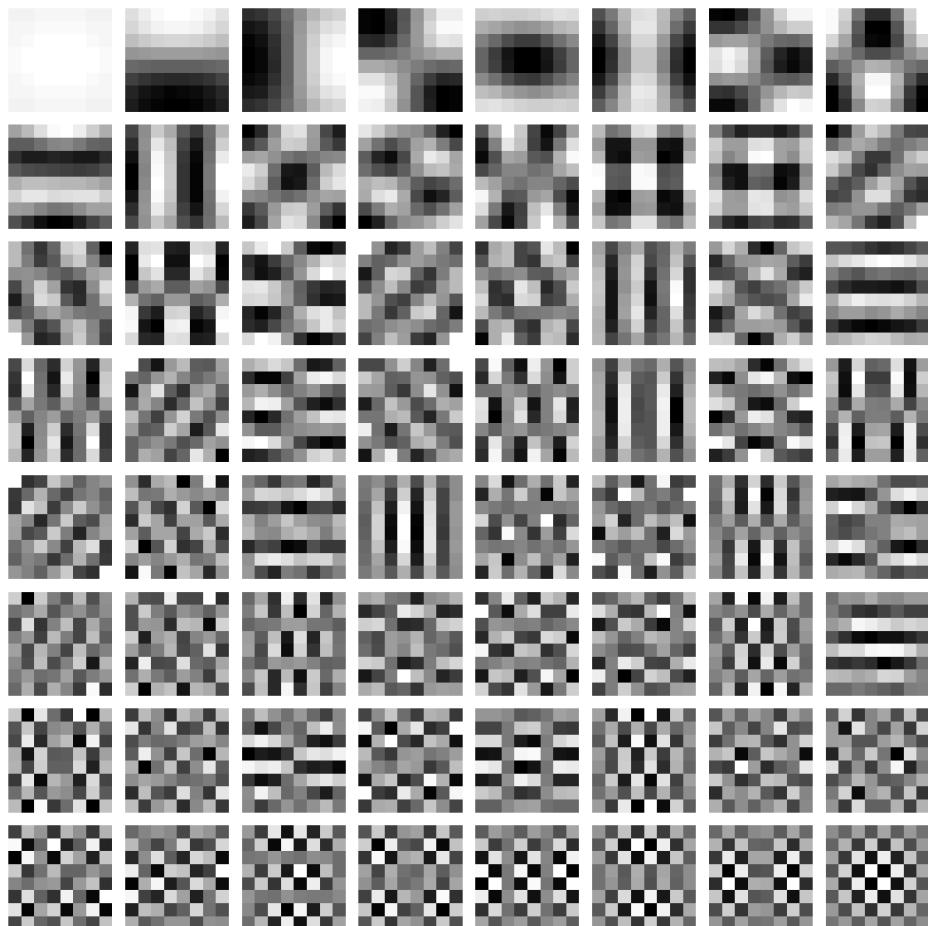
$\mathbf{E} \Lambda^{-\frac{1}{2}} \mathbf{E}^T \mathbf{X}$

$$\mathbf{Y} = \mathbf{W} \mathbf{X}$$

$$\mathbf{W} = \mathbf{E} \Lambda^{-\frac{1}{2}} \mathbf{E}^T$$

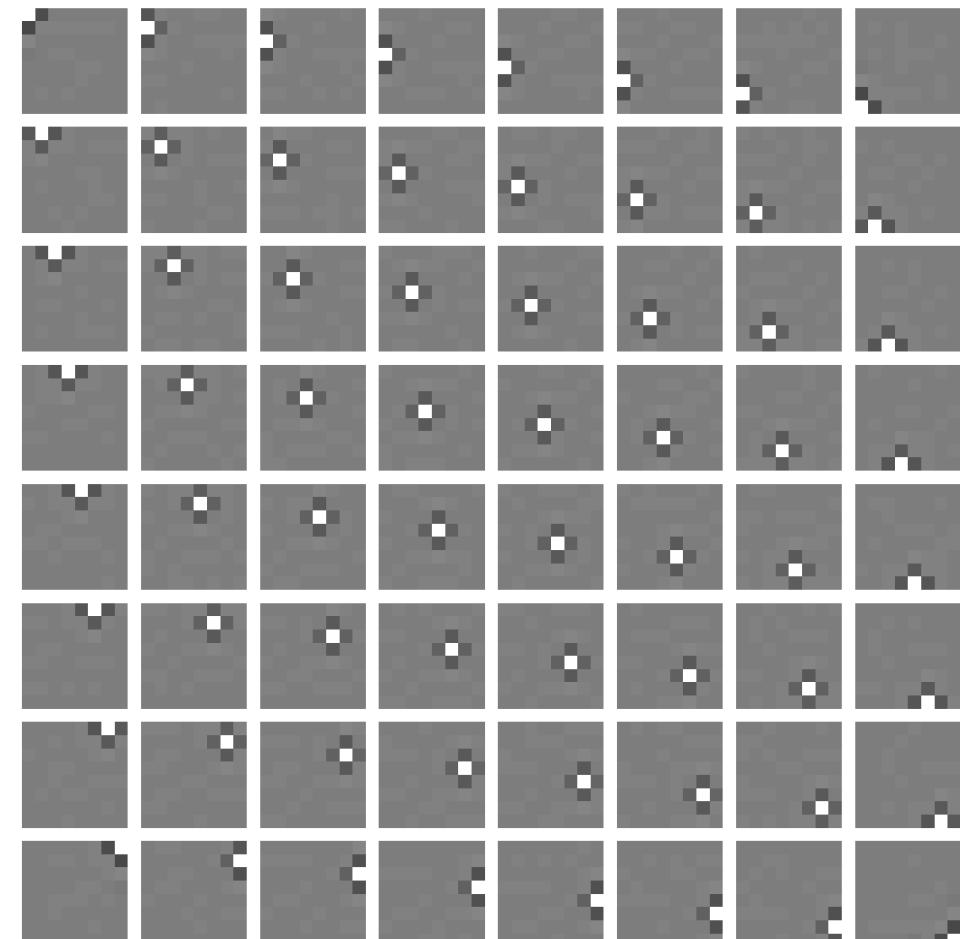
PCA

$$\mathbf{W} = \mathbf{E}^T$$



Whitening

$$\mathbf{W} = \mathbf{E}\Lambda^{-\frac{1}{2}}\mathbf{E}^T$$

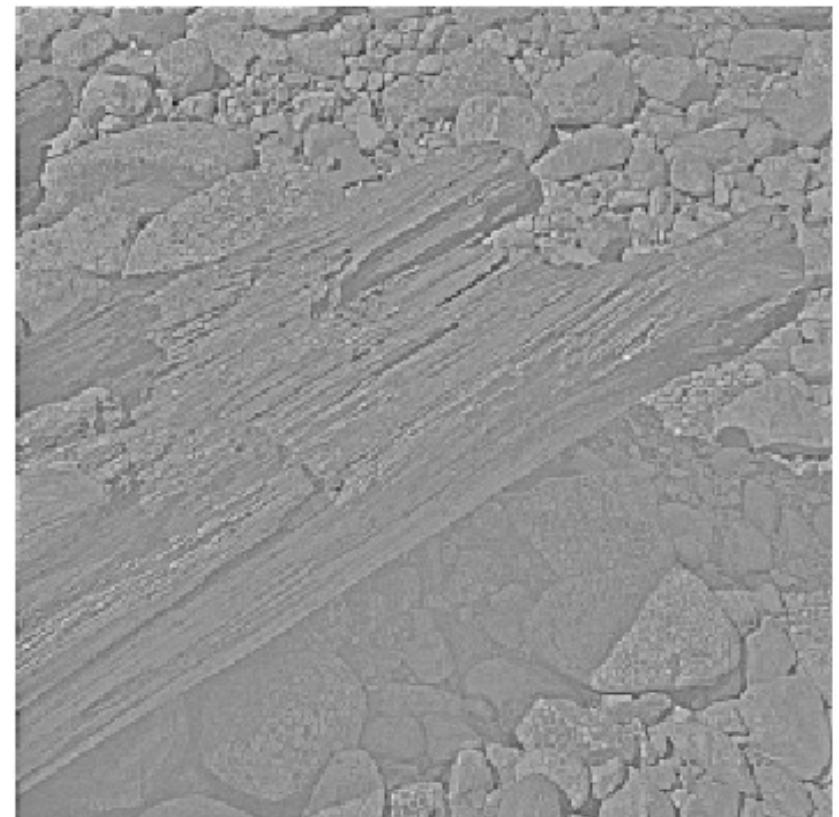


Whitening

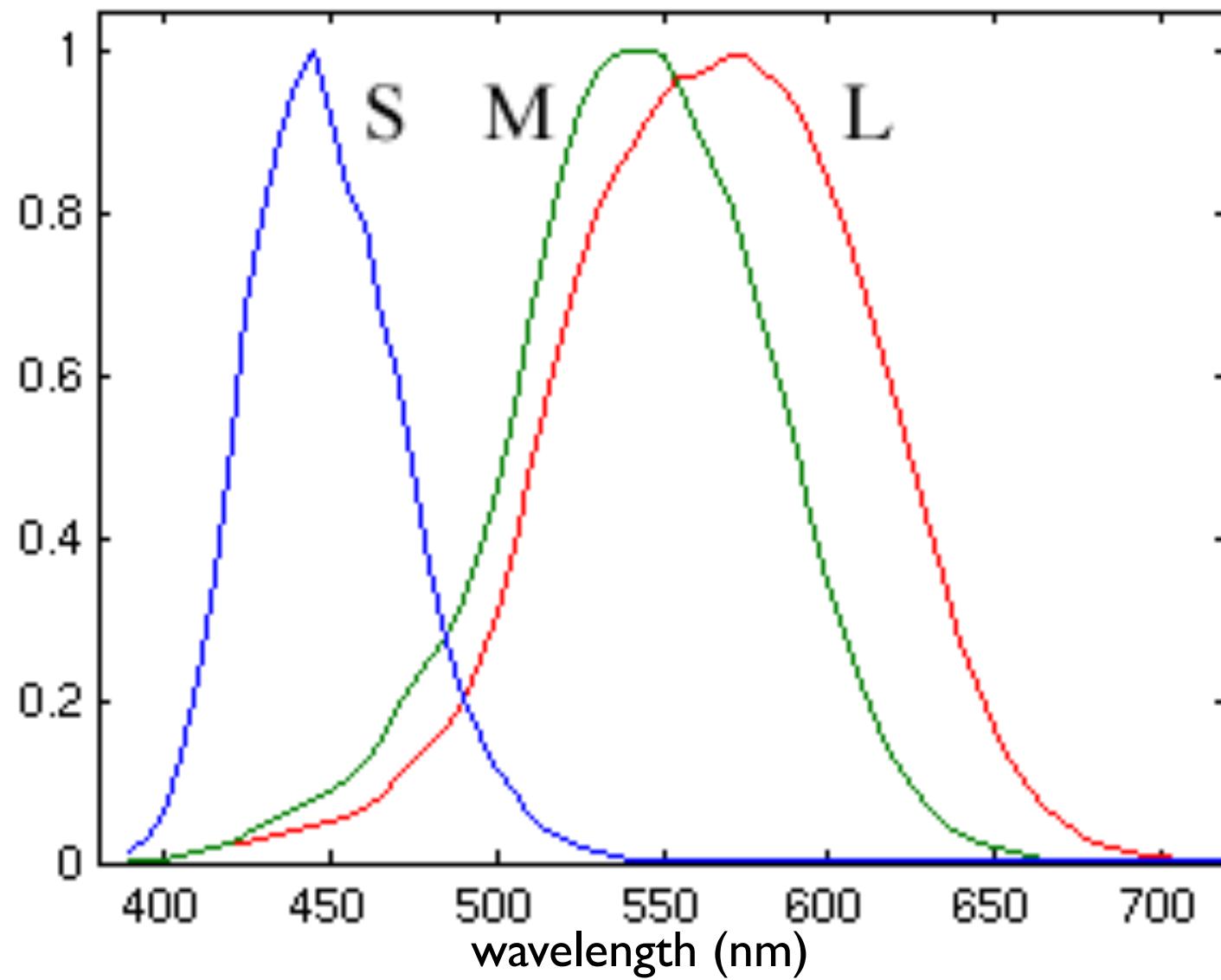
before



after

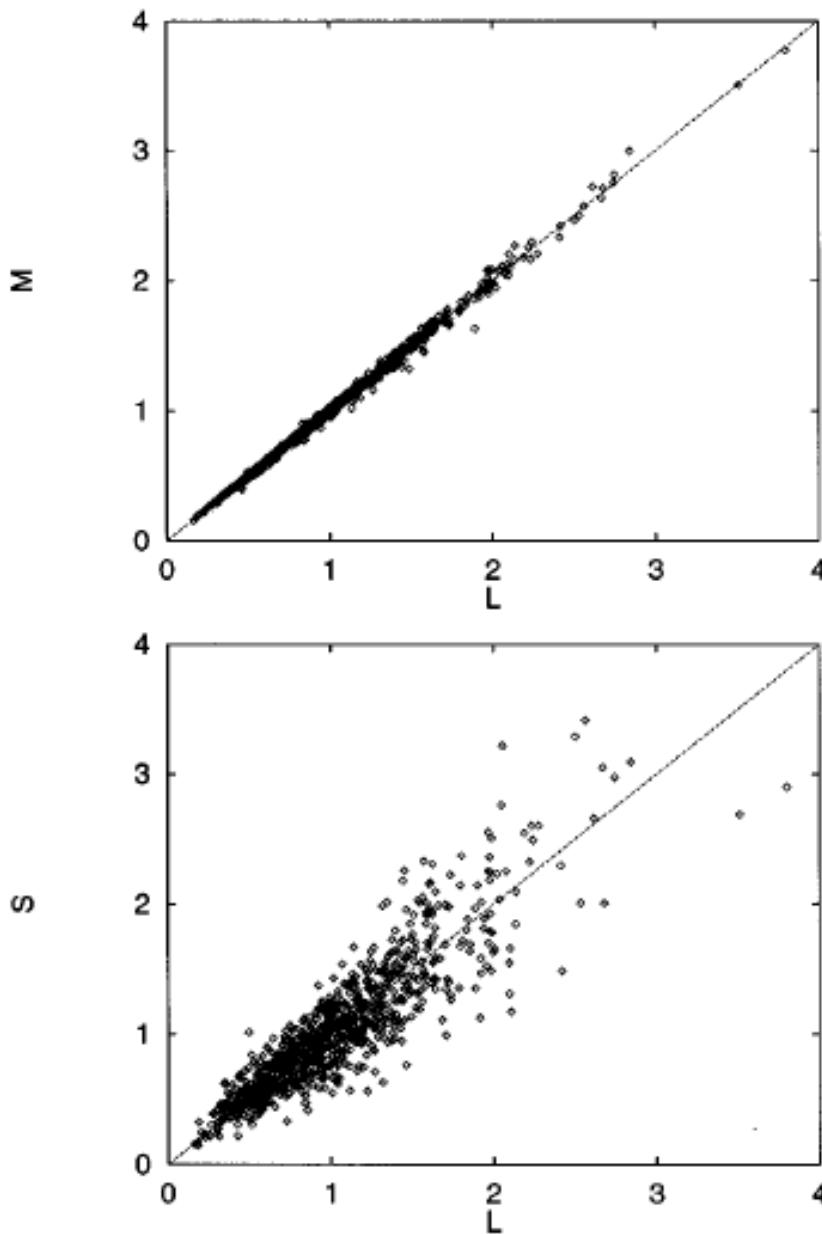


Human - cone spectral sensitivities



Joint statistics of cone responses

(Ruderman et al. 1998)



PCA of cone responses

(Ruderman et al. 1998)

$$\hat{l} = \frac{1}{\sqrt{3}} (\hat{\mathcal{L}} + \hat{\mathcal{M}} + \hat{\mathcal{S}}),$$

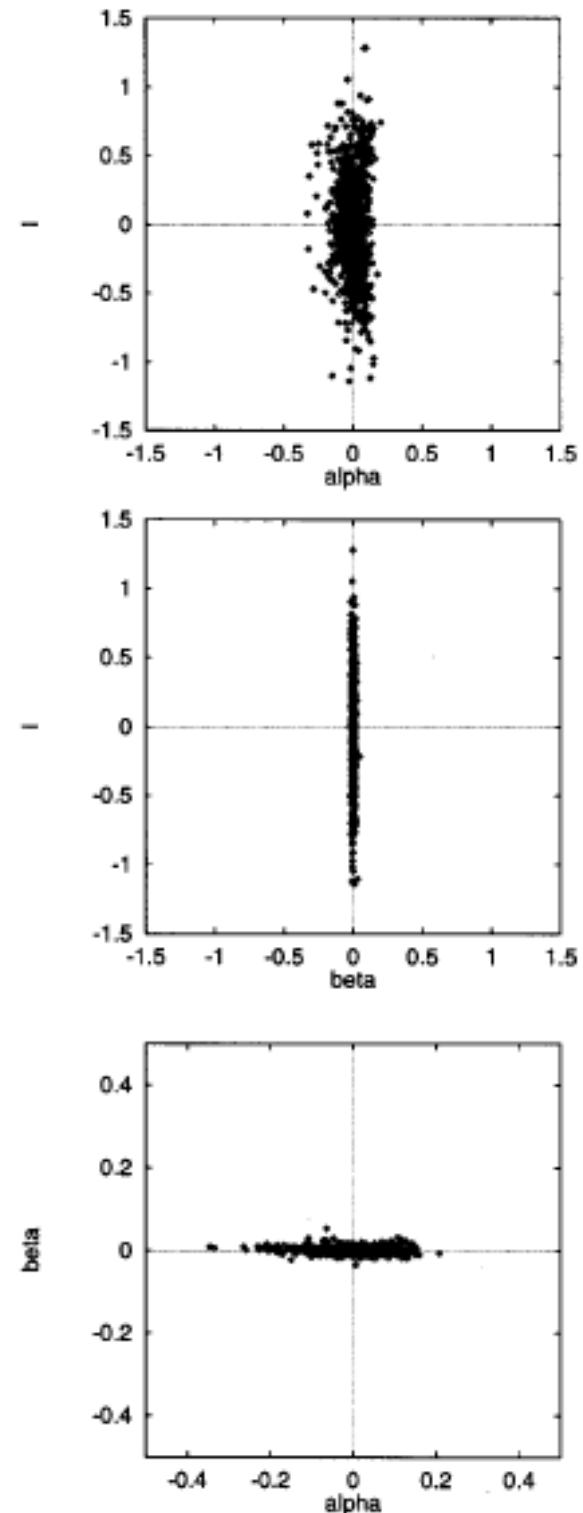
$$\hat{\alpha} = \frac{1}{\sqrt{6}} (\hat{\mathcal{L}} + \hat{\mathcal{M}} - 2\hat{\mathcal{S}}),$$

$$\hat{\beta} = \frac{1}{\sqrt{2}} (\hat{\mathcal{L}} - \hat{\mathcal{M}}),$$

where $\mathcal{L} = \log L - \langle \log L \rangle$,

$\mathcal{M} = \log M - \langle \log M \rangle$,

$\mathcal{S} = \log S - \langle \log S \rangle$.



Decomposition into luminance and color-opponent channels



l



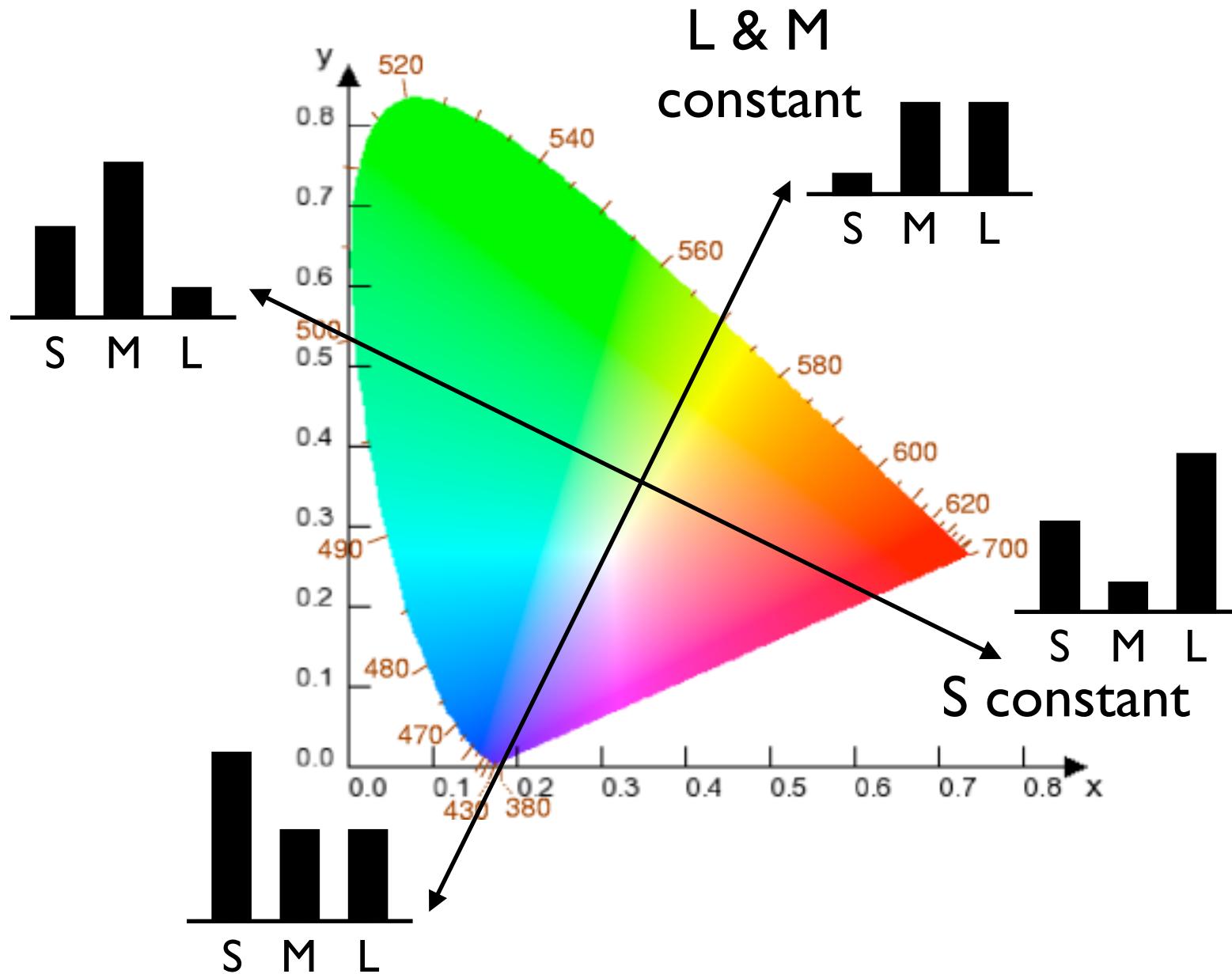
α



β

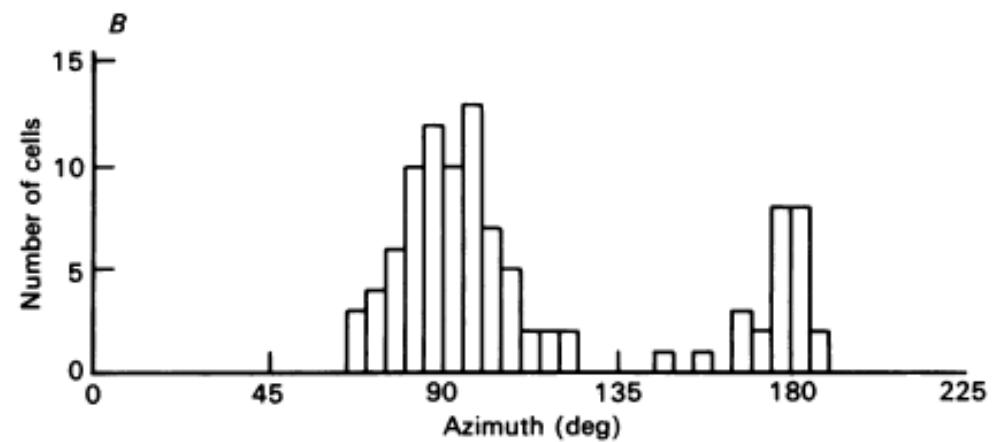
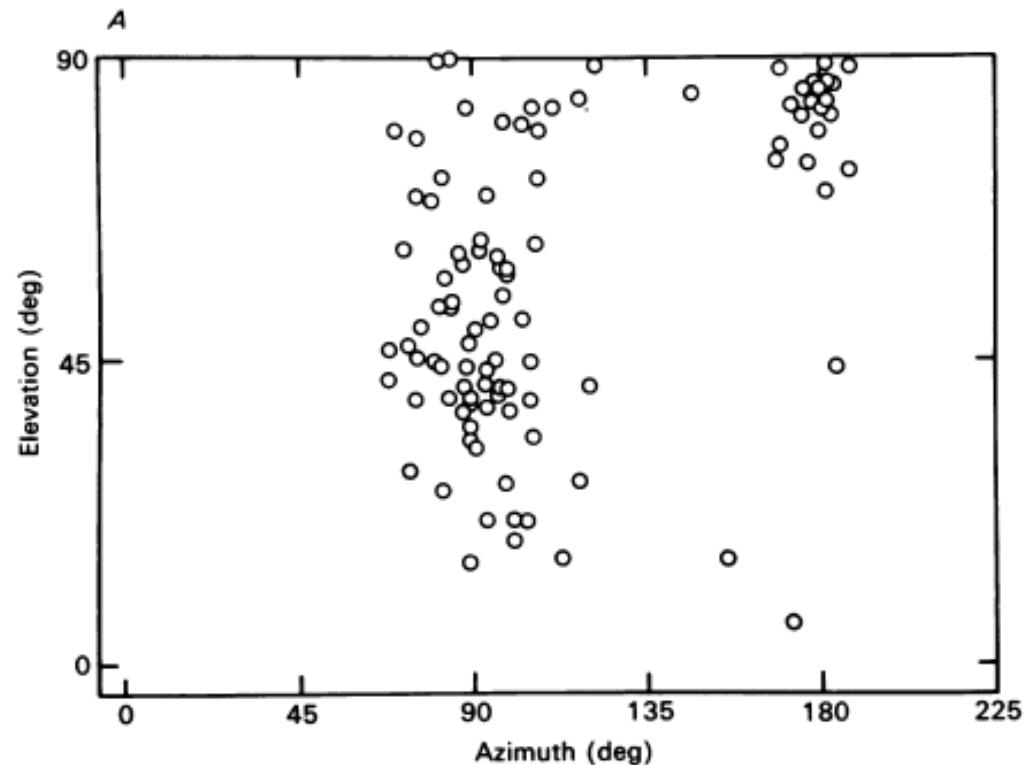
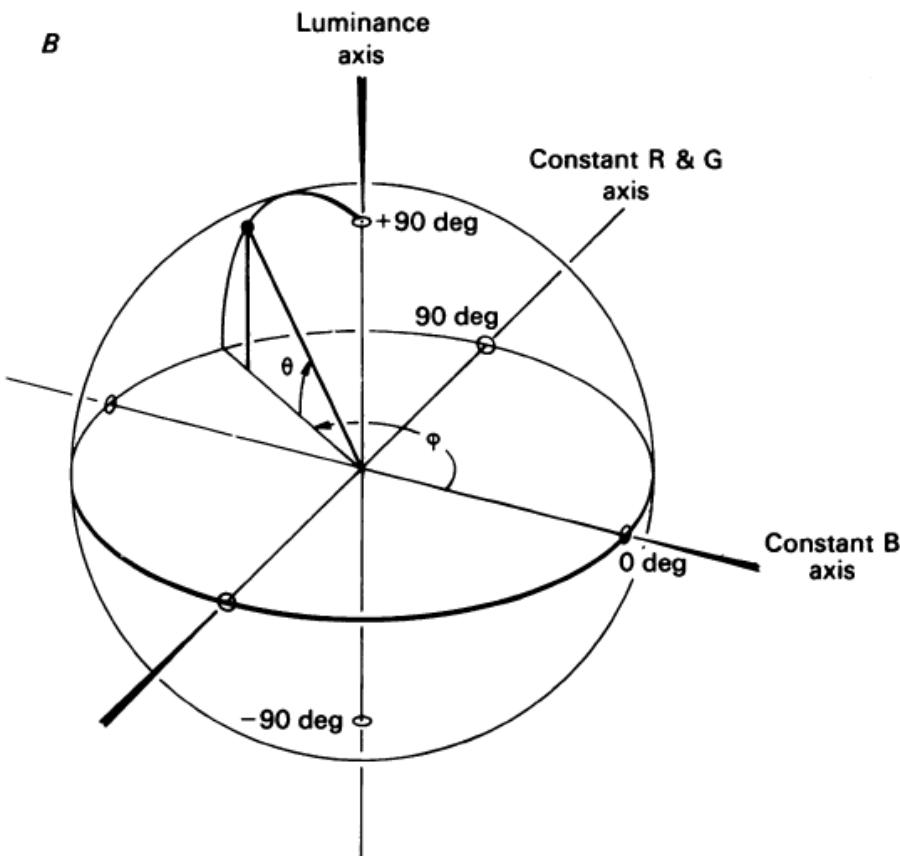


Color opponency



Color opponency in LGN

(Derrington, Krauskopf & Lennie, 1984)

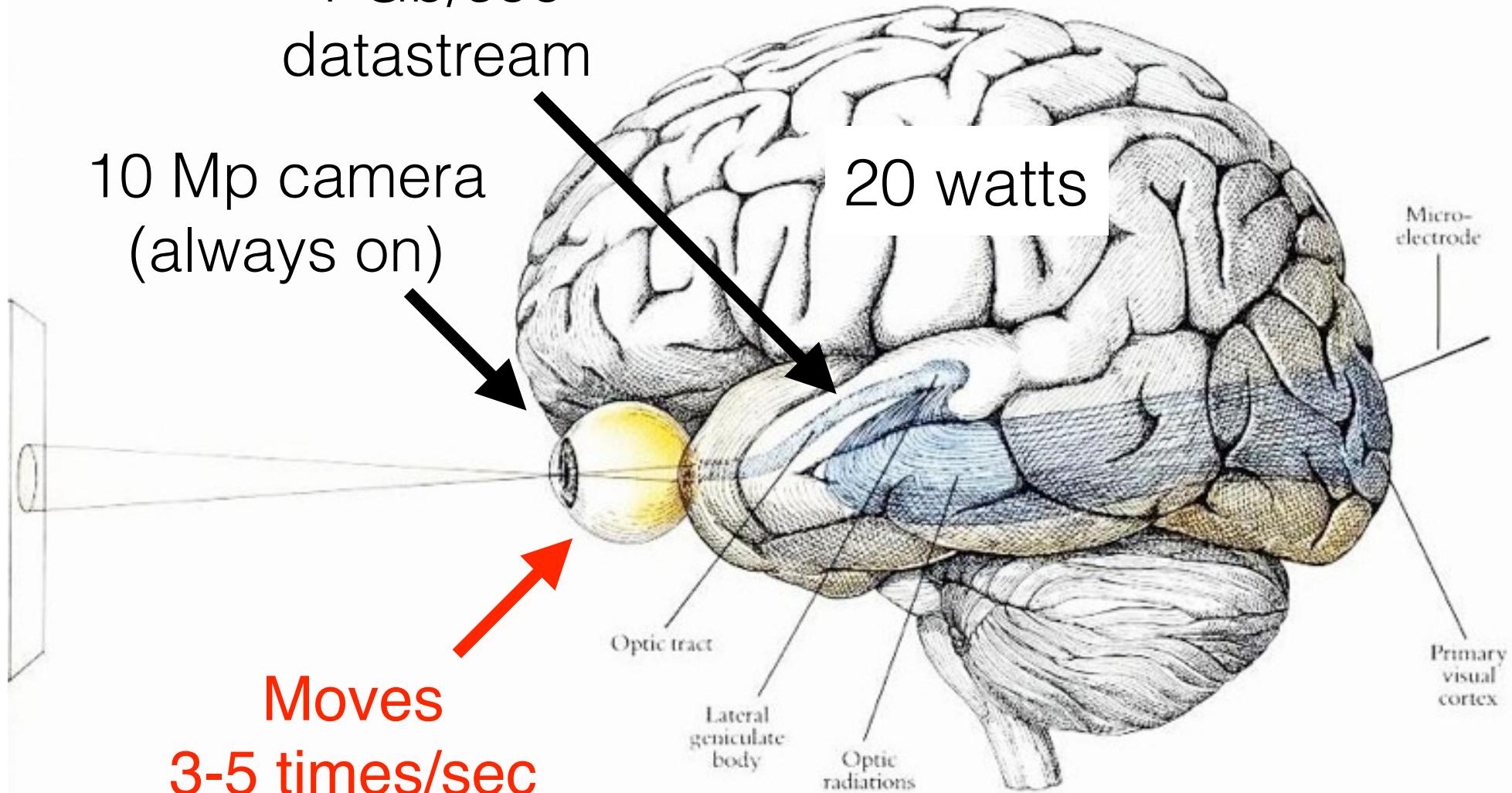


3. How to form a stable color percept from unstable images?

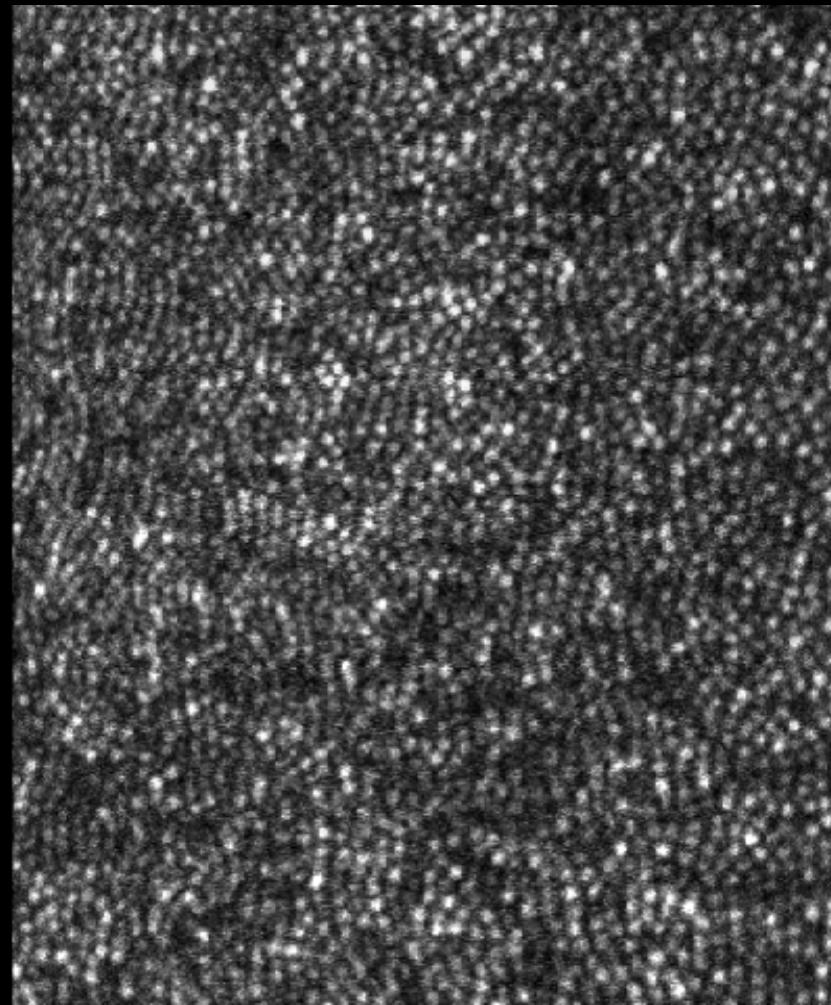
1 Gb/sec
datastream

10 Mp camera
(always on)

Moves
3-5 times/sec

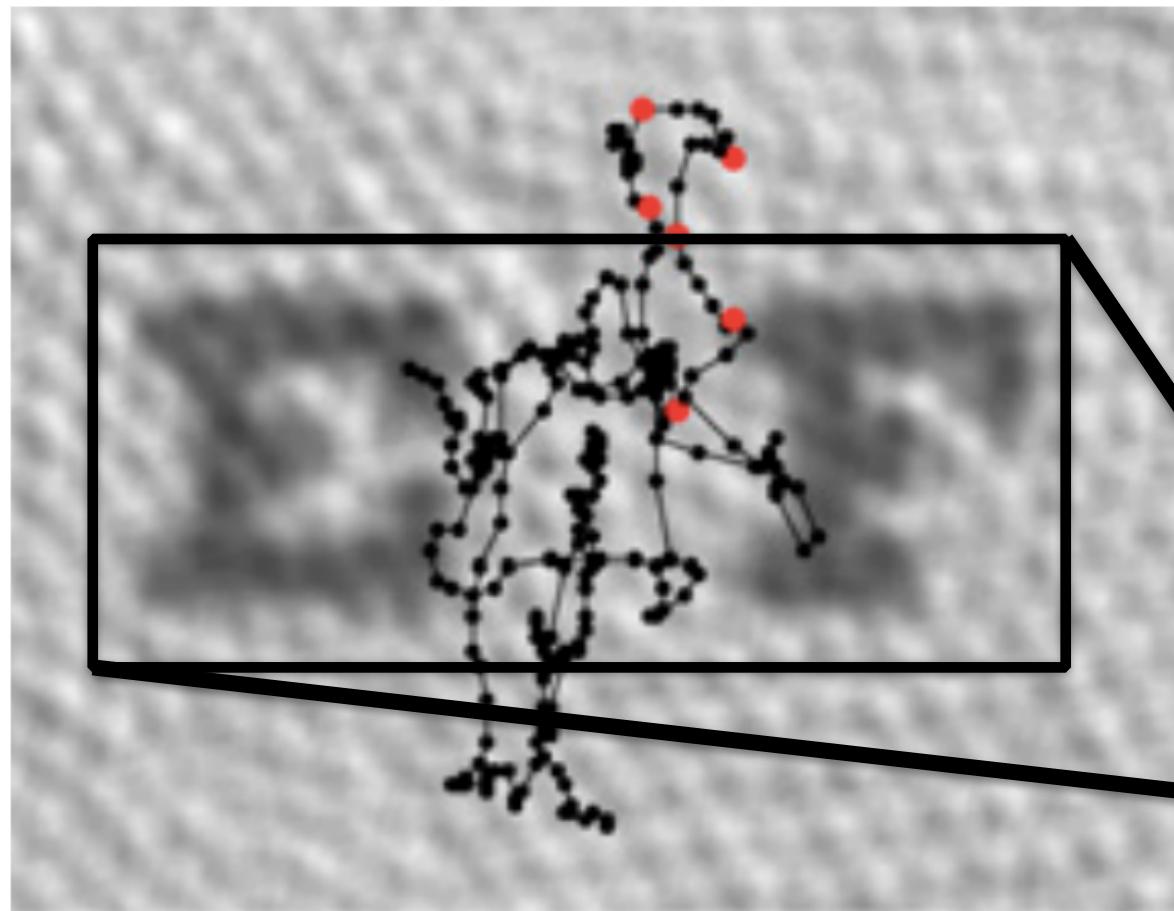


Fixational eye movements (drift)



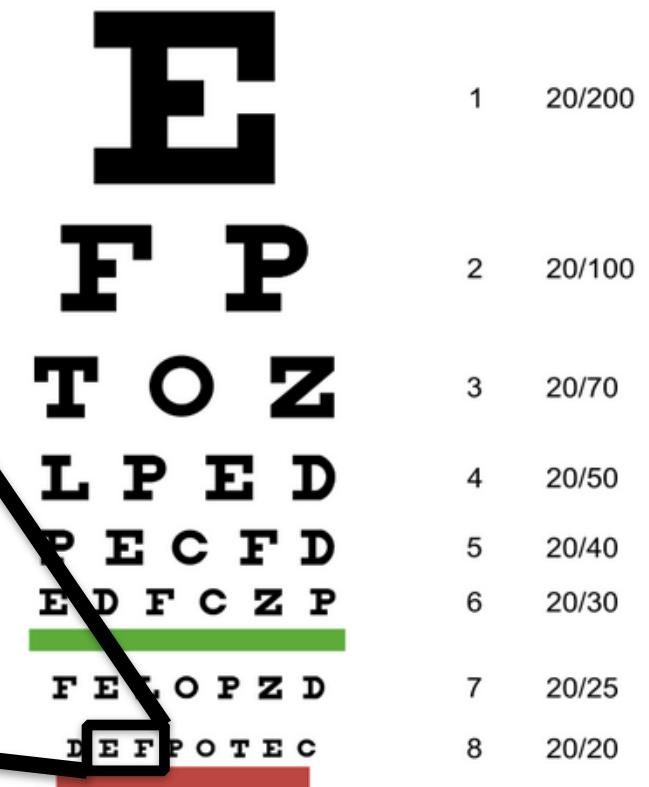
(from Austin Roorda, UC Berkeley)

Retinal image drift is large relative to cone spacing



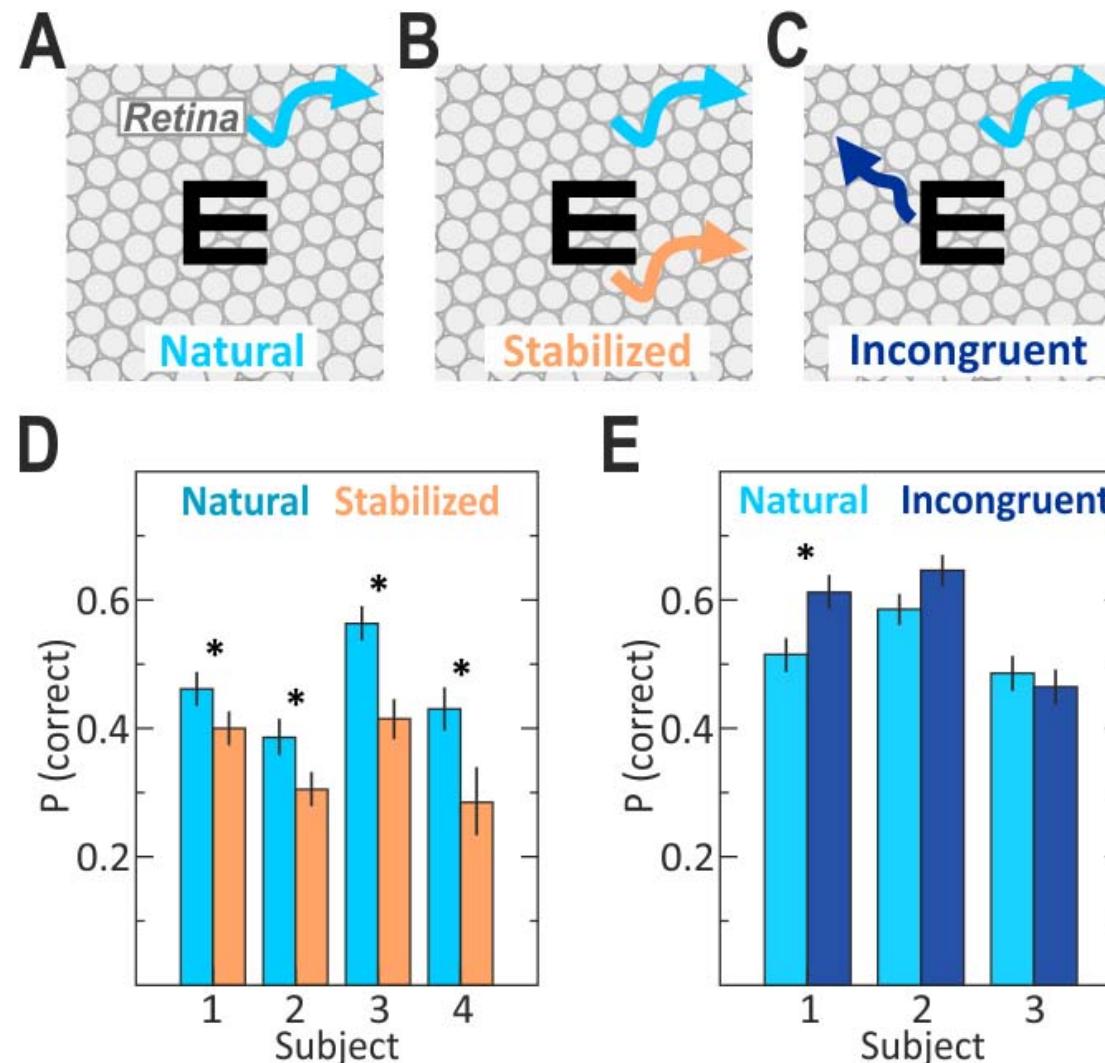
Foveal Cone Mosaic

5 arcmin



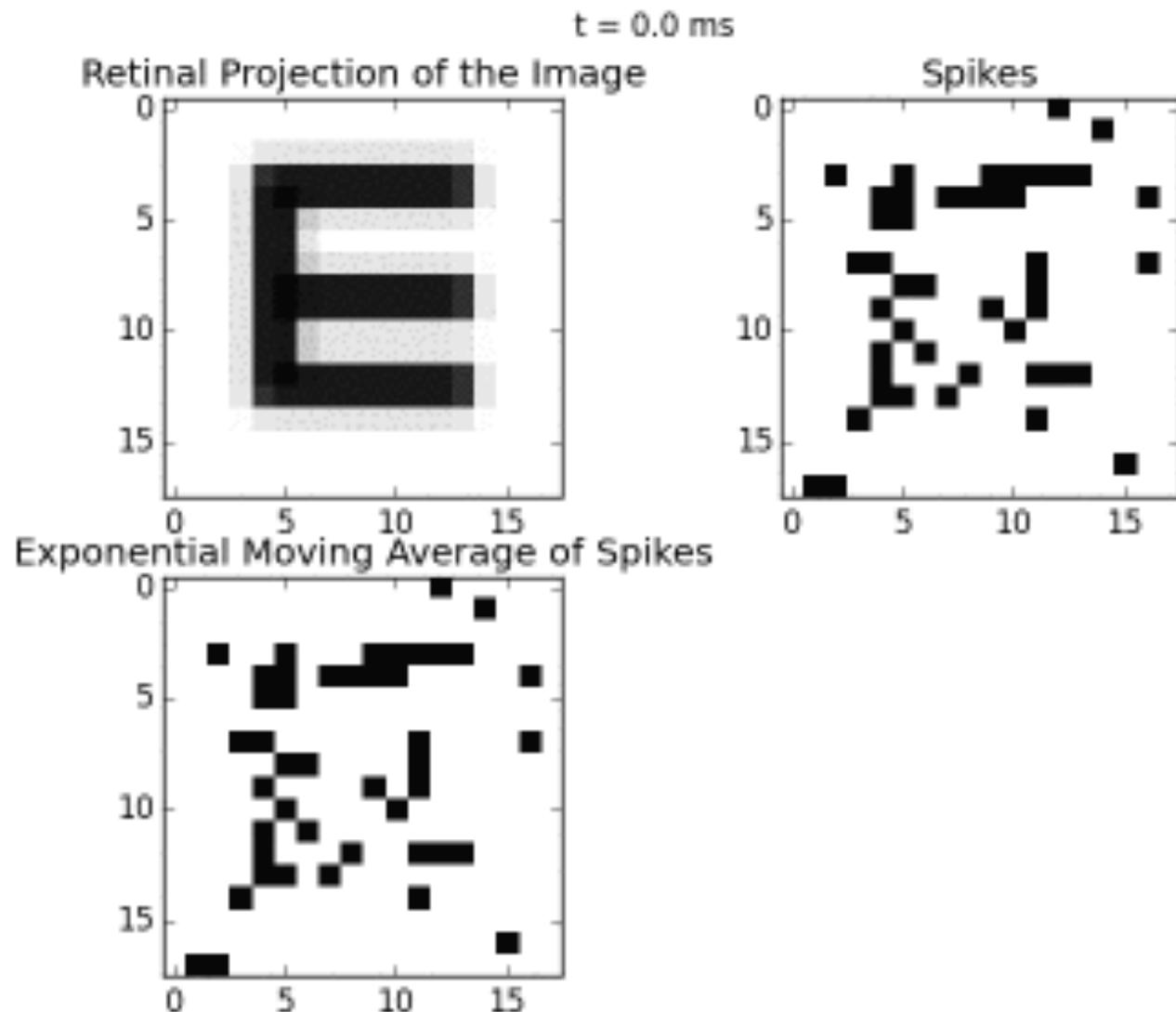
(from Burak et al., 2010)

Retinal image motion helps pattern discrimination



Ratnam, K., Domdei, N., Harmening, W. M., & Roorda, A. (2017). Benefits of retinal image motion at the limits of spatial vision. *Journal of Vision*, 17, 1–11.

Simple averaging is not sufficient



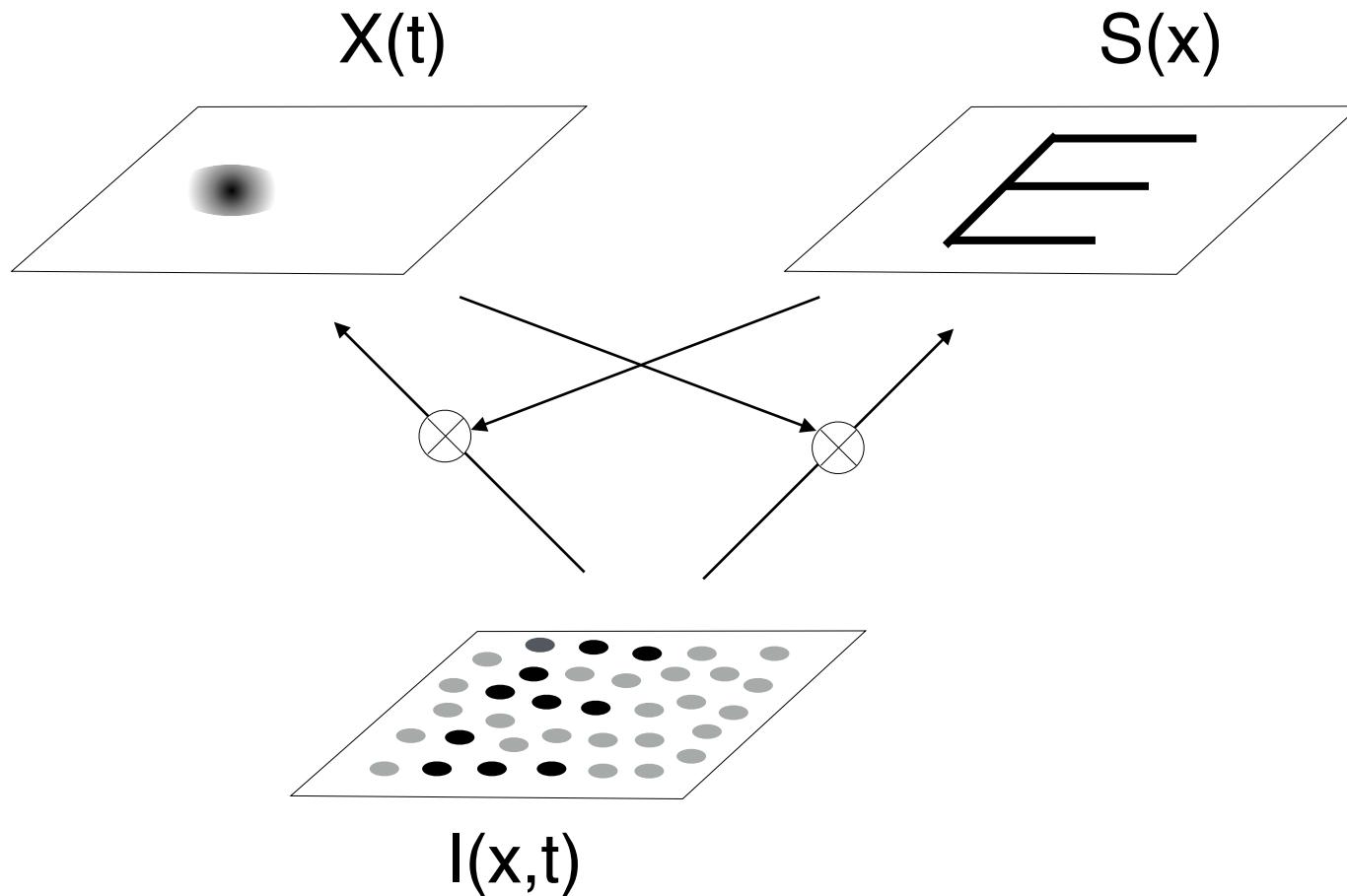
The problem

$$I(\vec{x}, t) = S(\vec{x} - \Delta\vec{x}(t)) + \epsilon(\vec{x}, t)$$

$$\hat{\Delta\vec{x}}(t) = \arg \min_{\Delta\vec{x}(t)} |I(\vec{x}, t) - S(\vec{x} - \Delta\vec{x}(t))|^2$$
$$\hat{S}(\vec{x}) = \int I(\vec{x} + \Delta\vec{x}(t)) dt$$

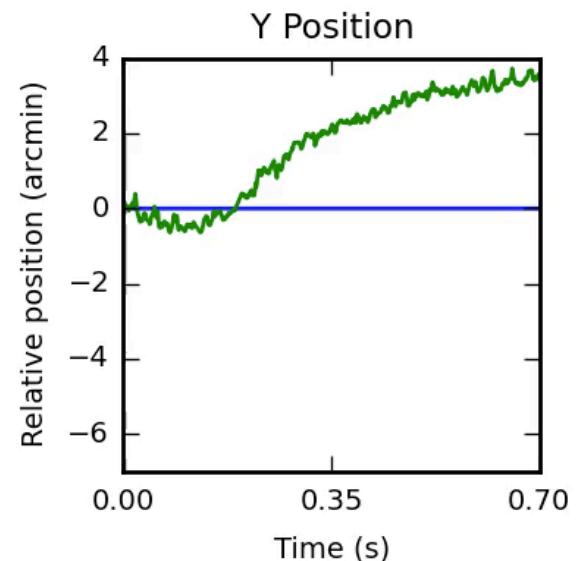
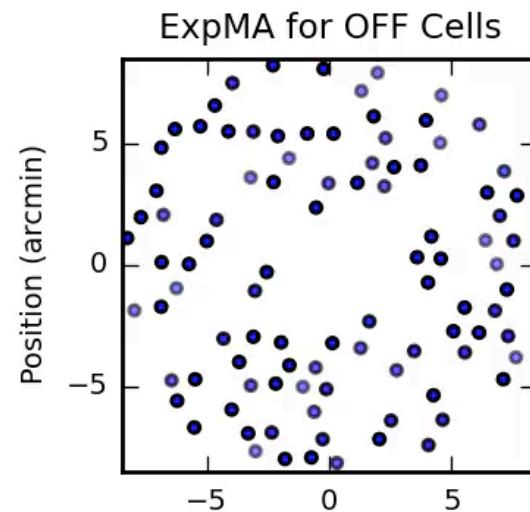
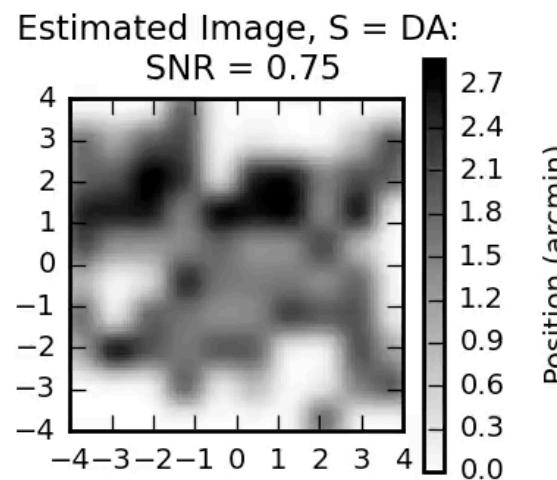
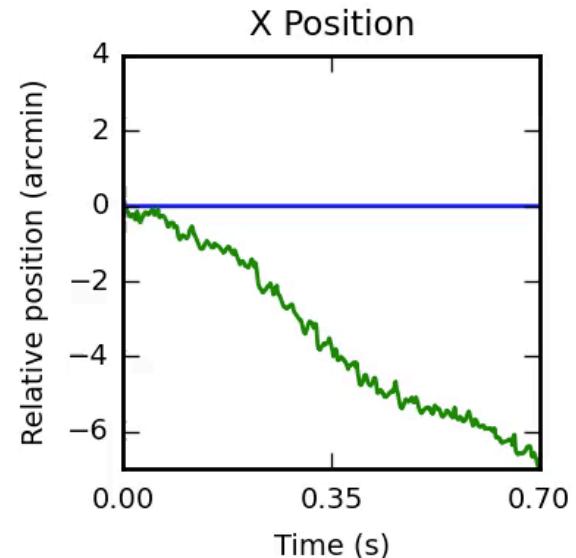
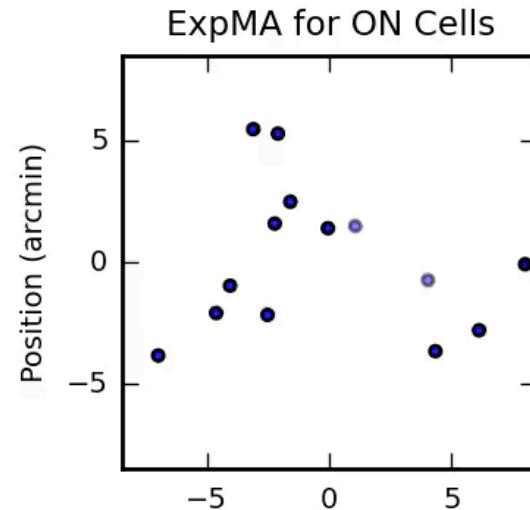
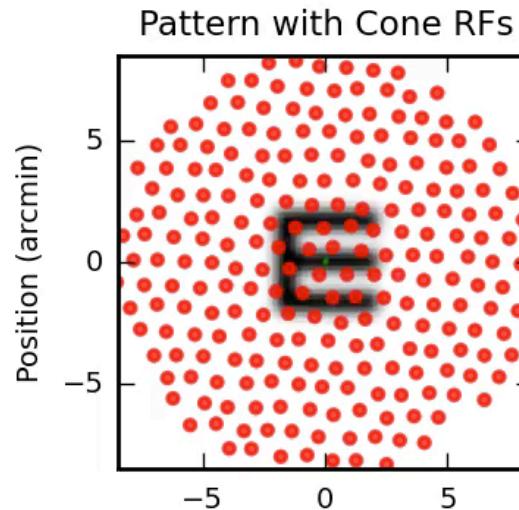
Joint estimation of pattern (S) and position (X) from retinal spike trains (R)

(Anderson, Ratnam, Roorda & Olshausen, 2020)

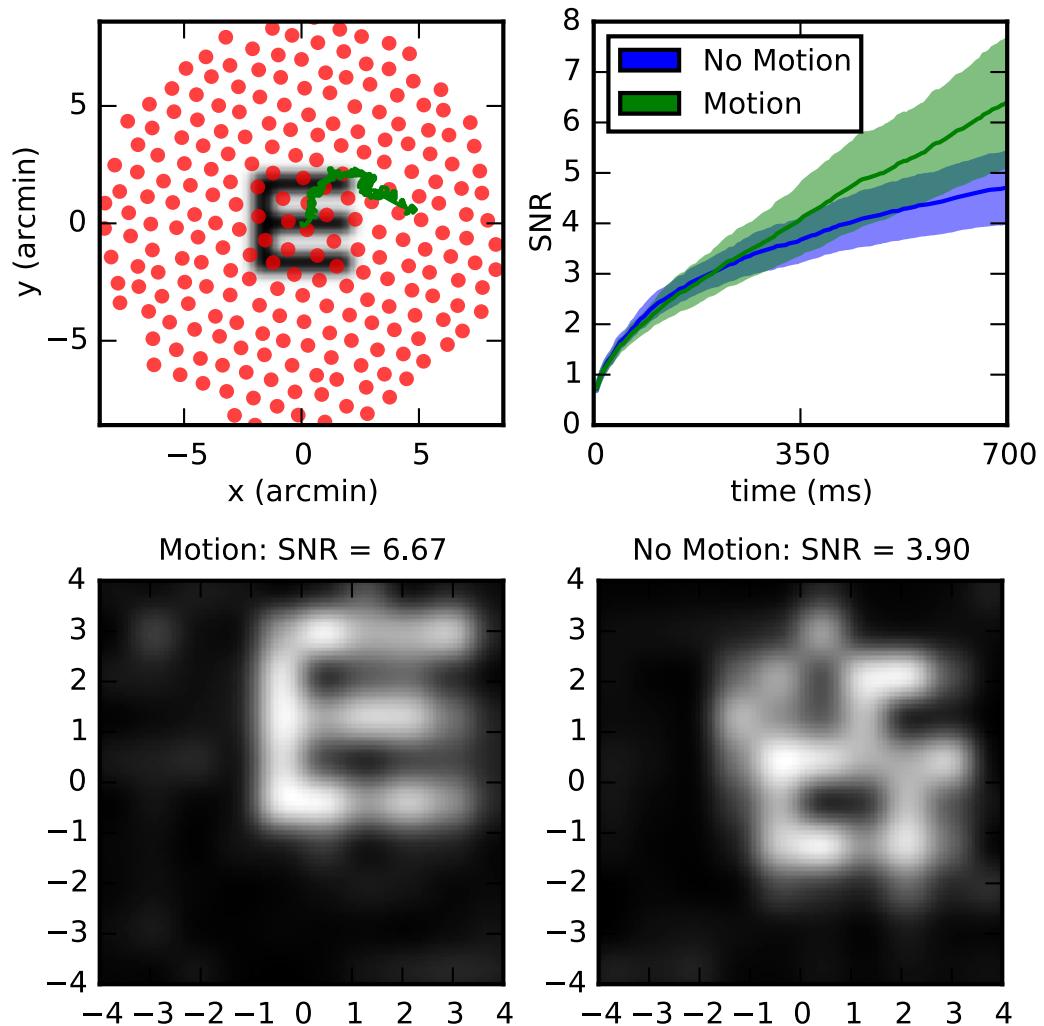


Joint estimation of pattern (S) and position (X)

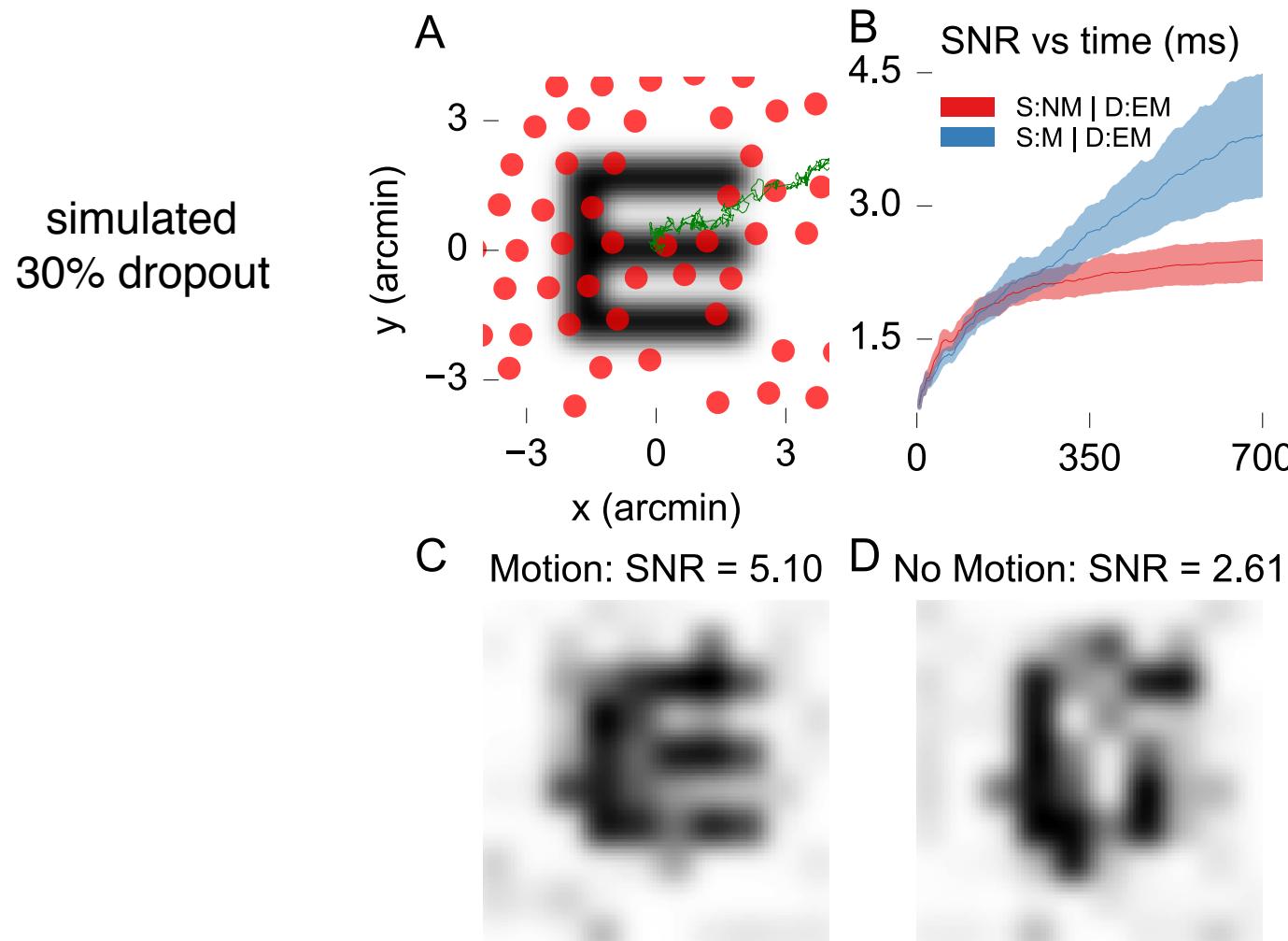
Image Projected on the Retina and Generated Spikes at $t = 005$ ms



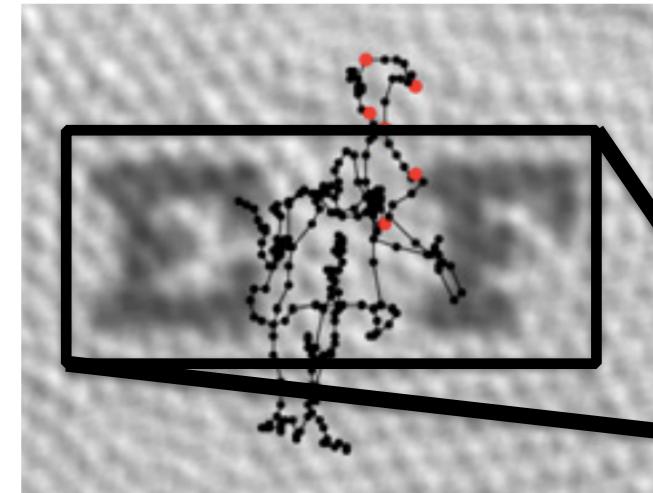
Motion helps estimation of pattern S



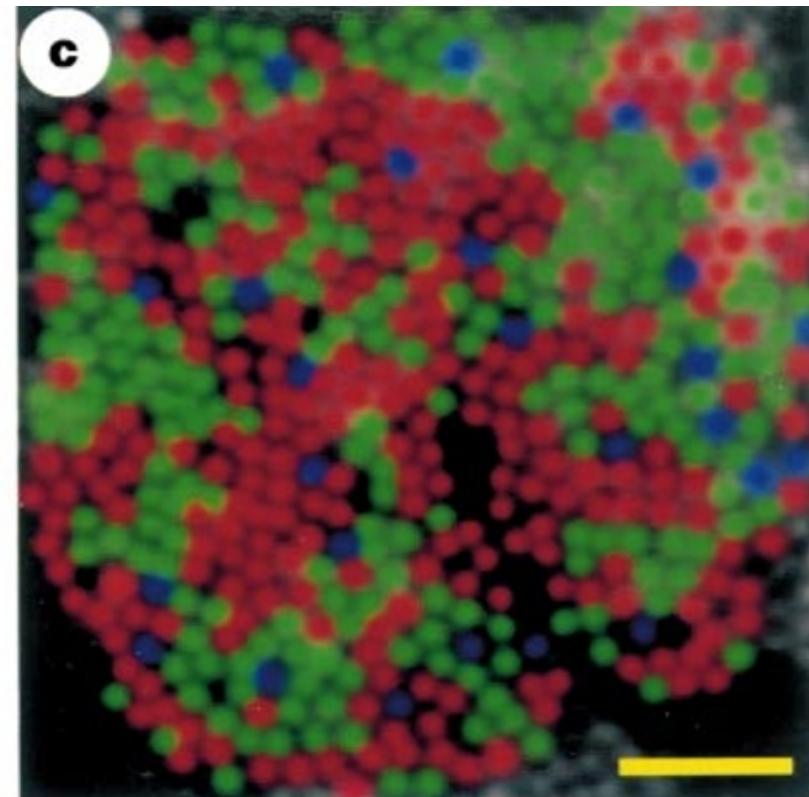
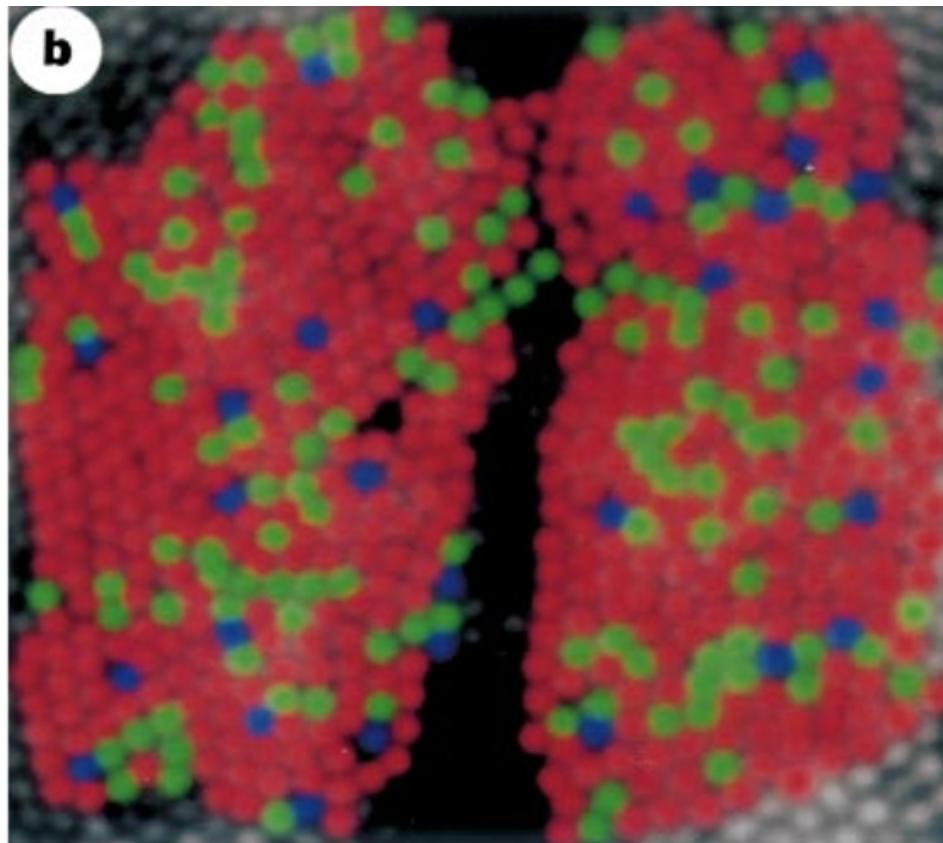
...especially under conditions of cone loss.



How to extend this to color?

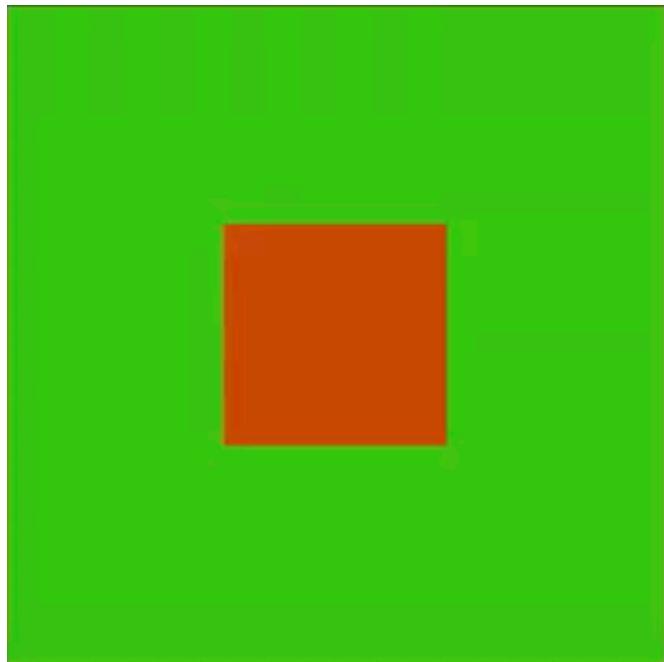


5 arcmin

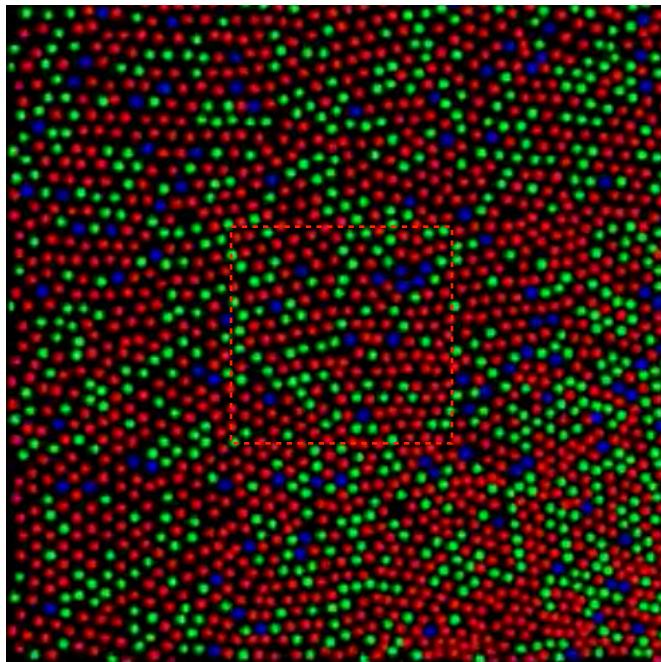


How do we perceive regular shape and uniform color from *irregular* and *non-uniform* sensory stimulation?

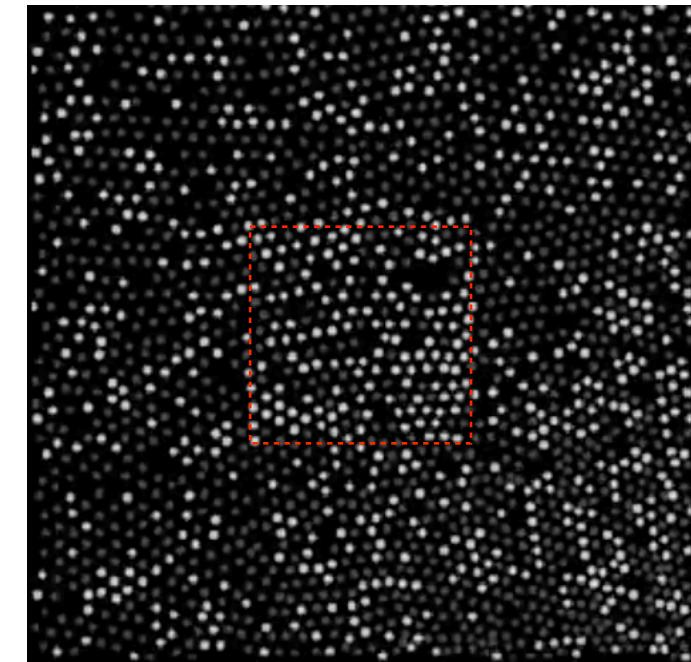
Stimulus

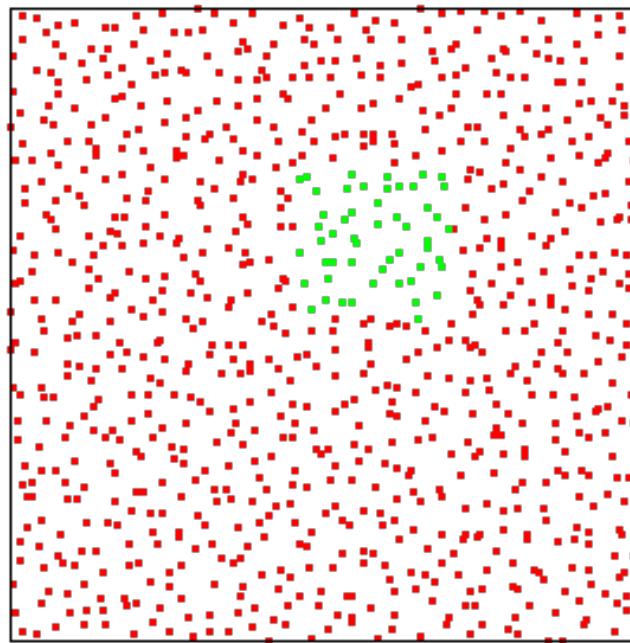


Retinal Mosaic



Cone Excitations

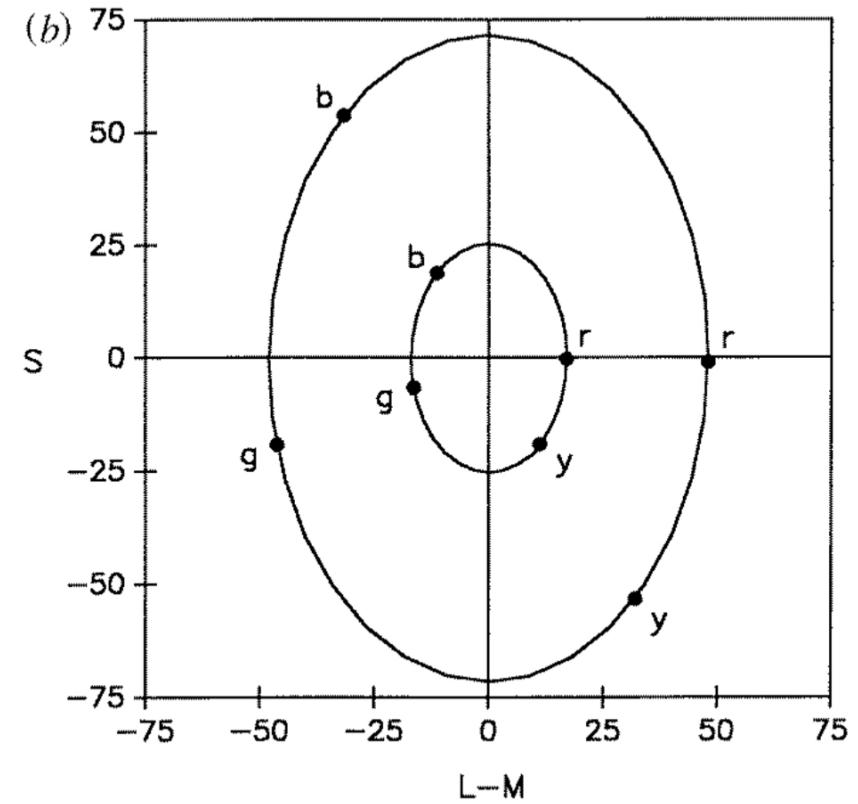
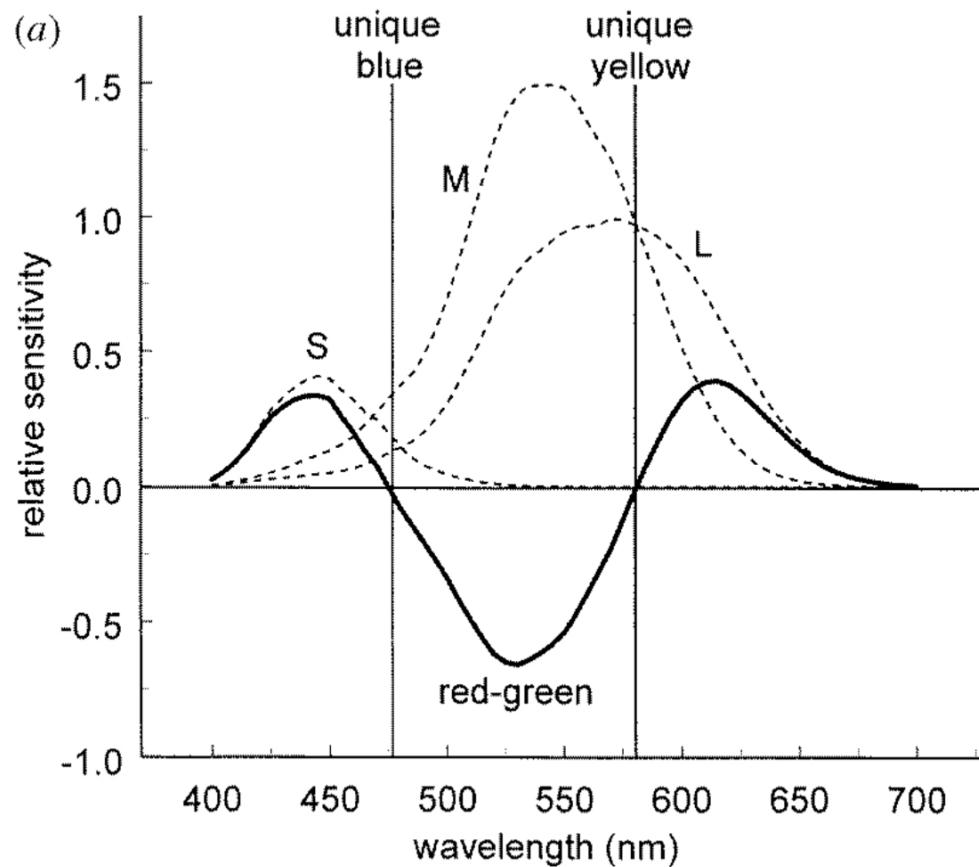




(From Hoffman, *Visual Intelligence*, 1998)

4. How are color categories learned? How and where are they represented in brain?

Unique hues do not align with color-opponent axes



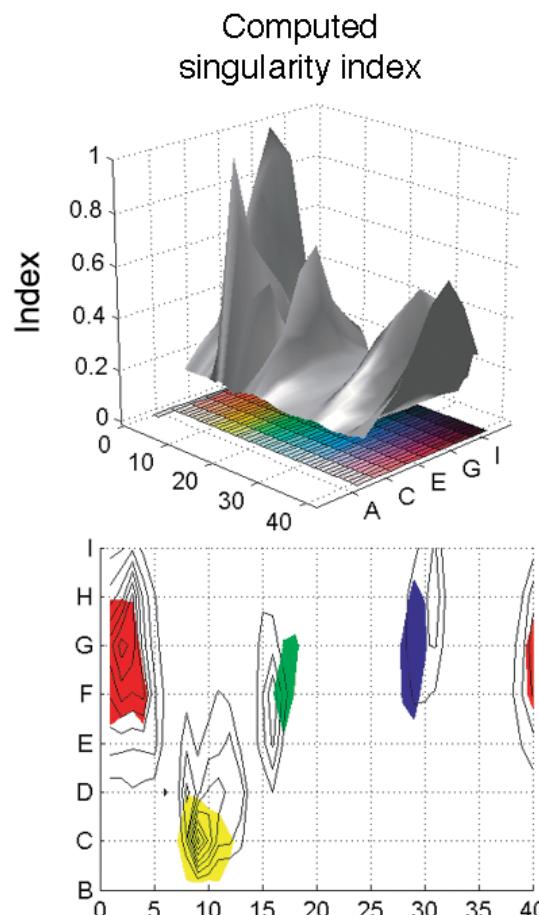
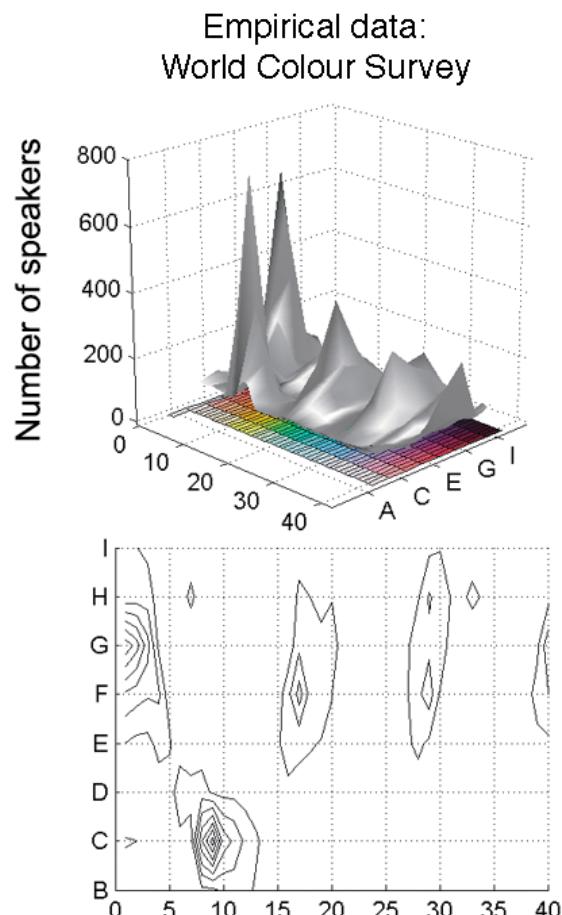
(from Webster 1996)

Color naming, unique hues, and hue cancellation predicted from singularities in reflection properties

DAVID L. PHILIPONA AND J. KEVIN O'REGAN

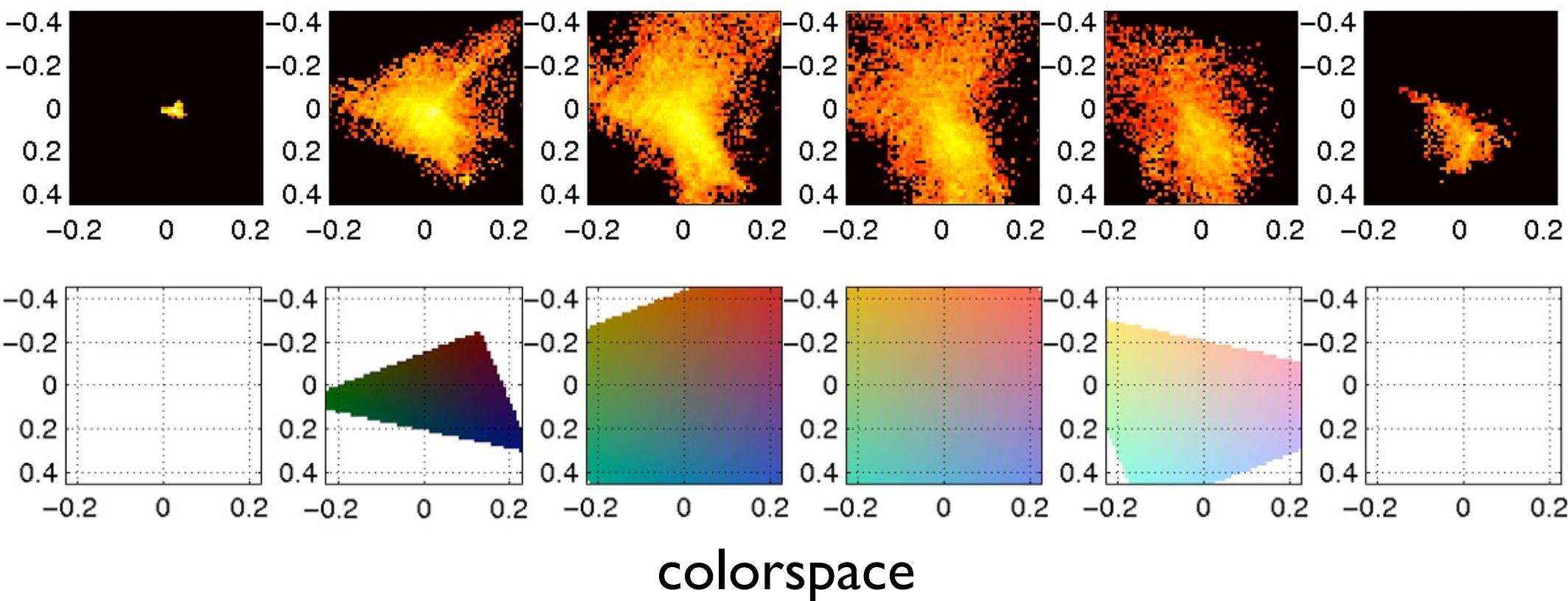
Laboratoire de Psychologie de la Perception, CNRS, Université Paris 5 René Descartes, Paris, France

(RECEIVED August 1, 2005; ACCEPTED December 29, 2005)



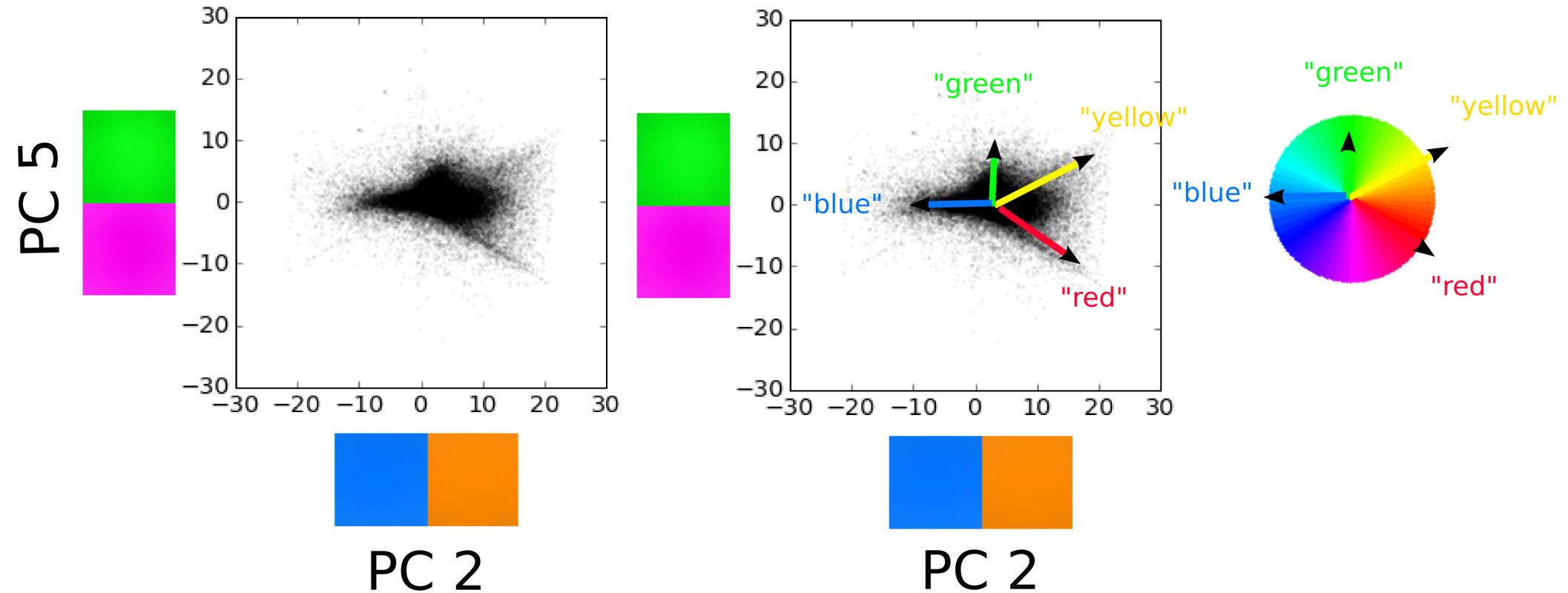
Joint statistics of color are non-Gaussian

probability distribution



Sparse coding recovers unique hues

(Paxton Frady 2016)



Wild hummingbirds discriminate nonspectral colors

Mary Caswell Stoddard^{a,b,1} , Harold N. Eyster^{b,c,2} , Benedict G. Hogan^{a,b,2} , Dylan H. Morris^a , Edward R. Soucy^d , and David W. Inouye^{b,e} 

^aDepartment of Ecology and Evolutionary Biology, Princeton University, Princeton, NJ 08544; ^bRocky Mountain Biological Laboratory, Crested Butte, CO 81224; ^cInstitute for Resources, Environment and Sustainability, University of British Columbia, Vancouver, BC V6T 1Z4, Canada; ^dCenter for Brain Science, Harvard University, Cambridge, MA 02138; and ^eDepartment of Biology, University of Maryland, College Park, MD 20742

Edited by Scott V. Edwards, Harvard University, Cambridge, MA, and approved April 28, 2020 (received for review November 5, 2019)

