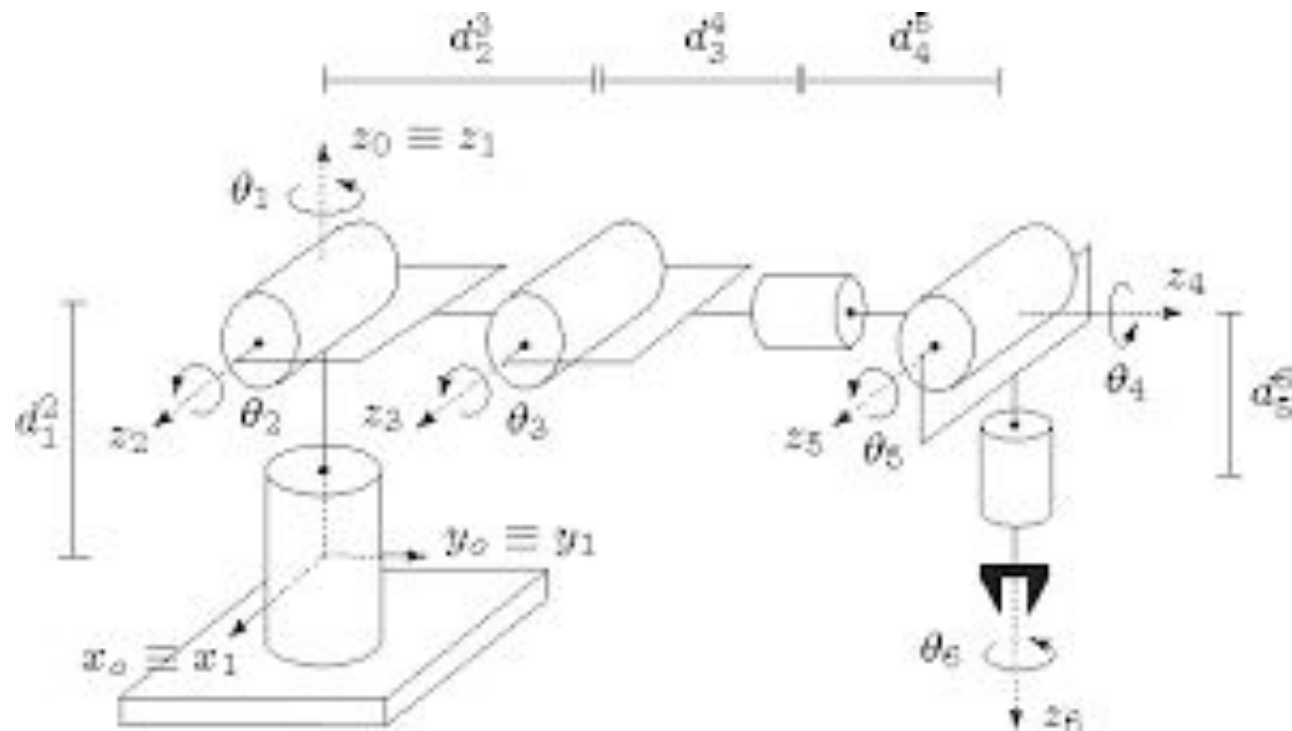
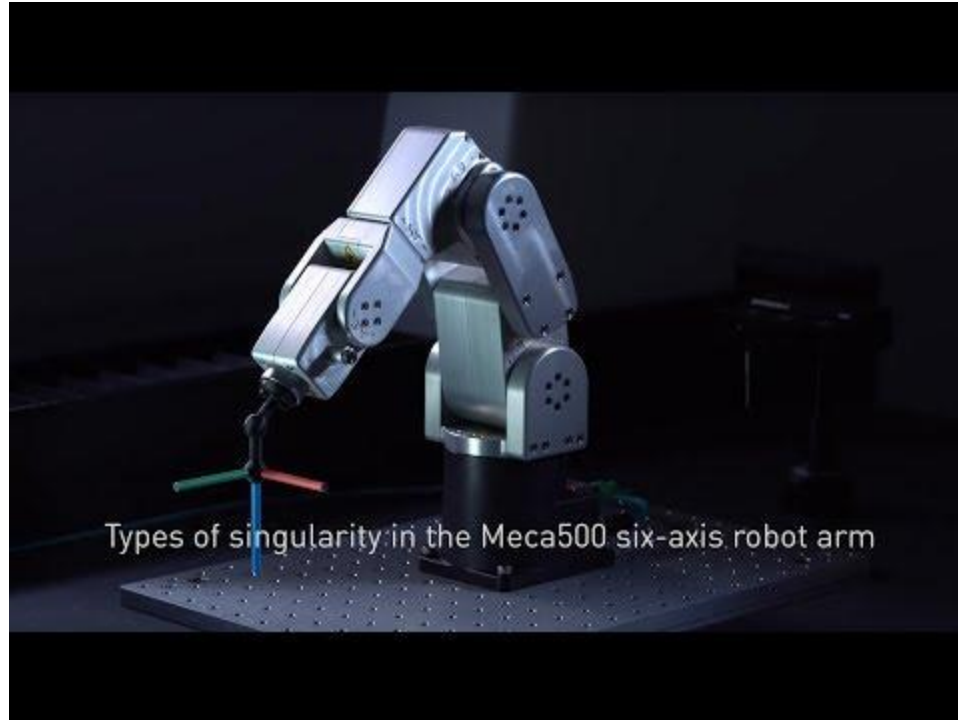


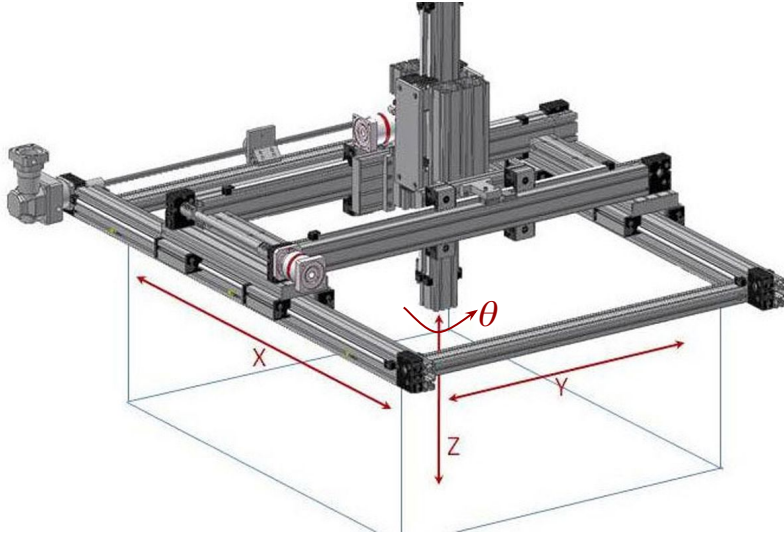
# Elbow Manipulator



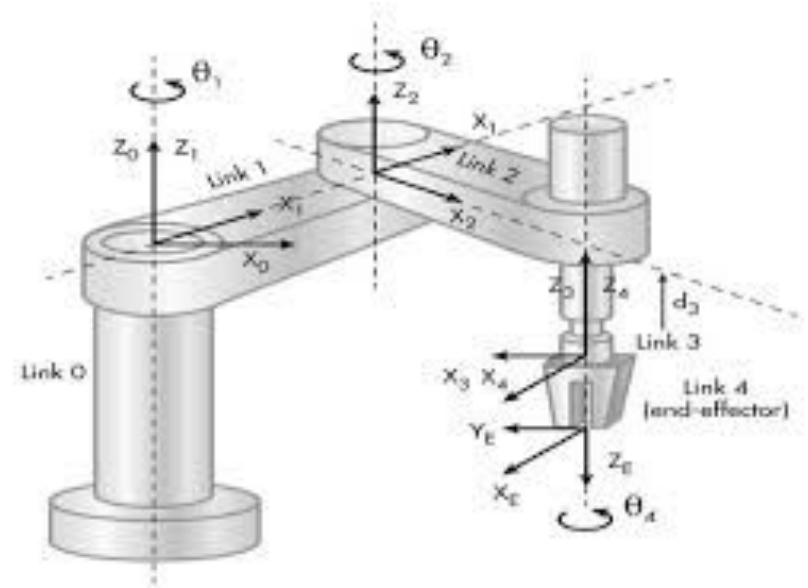
# Some common singularities



# Two robot designs for control in $x, y, z, \theta$



Cartesian



SCARA

# Invertible Matrix Theorem

The for an  $n \times n$  matrix  $A$ , the following statements are equivalent:

- $A$  is invertible
- The columns of  $A$  are linearly independent
- The reduced row echelon form of  $A$  is  $I_{n \times n}$
- The rank of  $A$  is  $n$
- The range of the rows is  $\mathbb{R}^n$
- The range of the columns is  $\mathbb{R}^n$
- $A$  doesn't have a null space (only the zero vector)
- The nullity of  $A$  is zero
- The determinant of  $A$  is nonzero