DATA 605 : Final Exam - Problem2

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Problem 2 - Digit Recognizer

Digit Recognizer is one of the basic and first problem that a budding Machine Learning engineer should try their hands on. It is a simple problem where the challenge is to recognize hand-written digits.

1. Go to Kaggle.com and build an account if you do not already have one. It is free.

Answer:	An existing	account	used to	access	Kaggle.com	

2. Go to https://www.kaggle.com/c/digit-recognizer/overview, accept the rules of the competition, and download the data. You will not be required to submit work to Kaggle, but you do need the data.

Answer:			

3. Using the training.csv file, plot representations of the first 10 images to understand the data format. Go ahead and divide all pixels by 255 to produce values between 0 and 1. (This is equivalent to min-max scaling.)

```
train <- read.csv("train.csv")
test <- read.csv("test.csv")
# Total Rows of training dataset
nrow(train) # Dataset has 4200 records</pre>
```

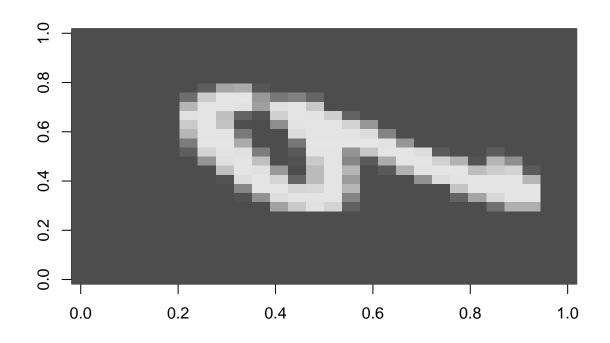
Answer:

[1] 42000

```
# Total columns of training dataset
ncol(train)
```

[1] 785

```
# Total Rows of training dataset
nrow(test) # Dataset has 4200 records
## [1] 28000
# Total columns of training dataset
ncol(test)
## [1] 784
# Print top records from train dataset
head(train[1:10])
    label pixel0 pixel1 pixel2 pixel3 pixel4 pixel5 pixel6 pixel7 pixel8
##
## 1
                 0 0
                              0
      1 0
                                     0
                                           0
                                                 0
                                                       0
## 2
      0
            0
                   0
                        0
                               0
                                                 0
                                                       0
## 3
      1
            0
                   0
                        0
                               0
                                           0
                                                 0
                                                       0
                                     0
                                          0
## 4
       4
            0
                   0
                         0
                               0
                                     0
                                                 0
                                                       0
## 5
                   0
                               0
                                                       0
                                                             0
      0
            0
                         0
                                     0
                                          0
                                                0
## 6
      0
                         0
                              0
                                                 0
                                                       0
summary(train[train$label==1, 408])
##
     Min. 1st Qu. Median
                         Mean 3rd Qu.
                                       Max.
##
      0.0 253.0
                 253.0
                        246.5
                              254.0
                                      255.0
summary(train[train$label==0, 408])
##
     Min. 1st Qu. Median Mean 3rd Qu.
                                       Max.
    0.000 0.000 0.000 4.517 0.000 255.000
##
m<-matrix(unlist(train[12,-1]), nrow=28, byrow = T)</pre>
image(m, col = grey.colors(255))
```



```
flip <- function(matrix){
    apply(matrix, 2, rev)
}

digit<-function(x){
    m<-matrix(unlist(x), nrow=28, byrow=T)
    m<-t(apply(m, 2, rev))
    image(m, col=grey.colors(255))
}

par(mfrow=c(3,4))

for(i in 1:10){
    digit(train[i, -1])
}

# divide all pixels by 255 to produce values between 0 and 1.

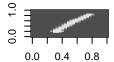
train_255 <- train/255.0
test_255 <- test/255.0
head(train_255[1:10])</pre>
```

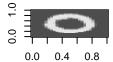
```
label pixel0 pixel1 pixel2 pixel3 pixel4 pixel5 pixel6 pixel7 pixel8
##
## 1 0.003921569
                      0
                             0
                                    0
                                           0
                                                   0
                                                          0
                                                                 0
                                                                        0
## 2 0.000000000
                      0
                             0
                                    0
                                           0
                                                   0
                                                          0
                                                                 0
```

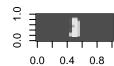
```
## 3 0.003921569
## 4 0.015686275
                         0
                                 0
                                         0
                                                 0
                                                          0
                                                                  0
                                                                          0
                                                                                  0
                                                                                          0
                                                          0
## 5 0.000000000
                         0
                                 0
                                         0
                                                 0
                                                                  0
                                                                          0
                                                                                  0
                                                                                          0
## 6 0.000000000
                         0
                                 0
                                         0
                                                 0
                                                          0
                                                                  0
                                                                          0
                                                                                  0
                                                                                          0
```

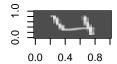
```
# In dataset-remove the first column of label. Create a new data set for this operation apply Min-Max n
normalize <- function(x, na.rm = TRUE) {
    return((x- min(x)) /(max(x)-min(x)))
}

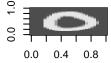
train_b <- train %>% select( 2:ncol(.) )
train_b<- as.data.frame(lapply(train_b[,-1], normalize))
par(mfrow=c(3,4))</pre>
```

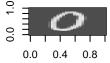


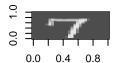


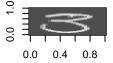


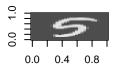


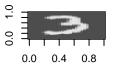












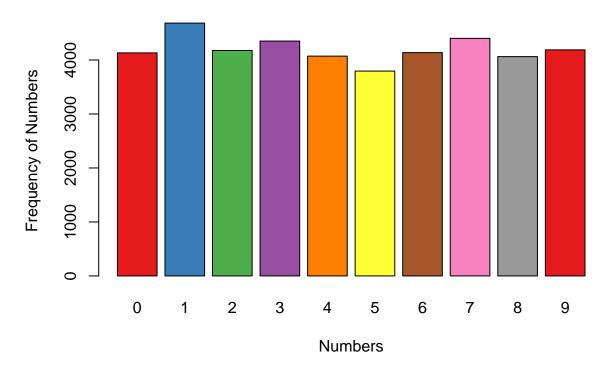
```
#Removing Missing values from training(train) dataframe train[is.na(train)] <- 0
```

4. What is the frequency distribution of the numbers in the dataset?

Answer: Frequency Distribution: A frequency distribution is a representation, either in a graphical or tabular format, that displays the number of observations within a given interval or categories. It is also called the Frequency Distribution table. Given this dataset, frequency distribution table shows occurrence

of various labels in training dataset. To investigate the balance of the data for each label, function will plot all of them along with their name. A plot for the same is below

Total Number of Digits (Training dataset)

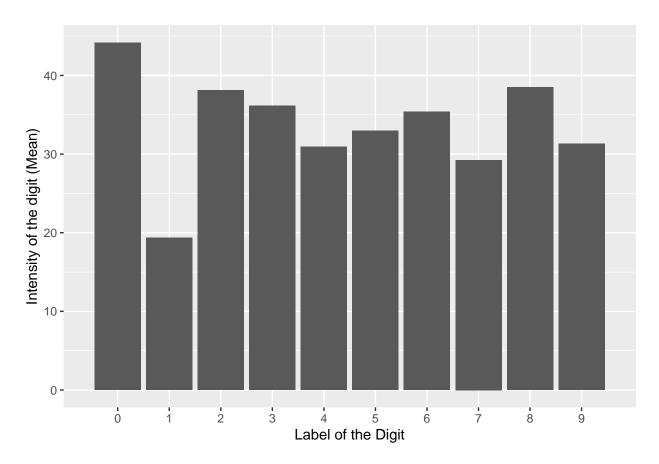


5. For each number, provide the mean pixel intensity. What does this tell you?

Answer: To find mean pixel intensity of all of the pixels, we can reshape the dataframe. The output is actually a series, indexed by the original index as well as the pixel label:

```
# Lets calculate mean of each row in training data set to find pixel intensity of all of the pixels
train$intensity <- apply(train[,-1], 1, mean)
intensity_by_label <- aggregate (train$intensity, FUN = mean, by = list(train$label))</pre>
```

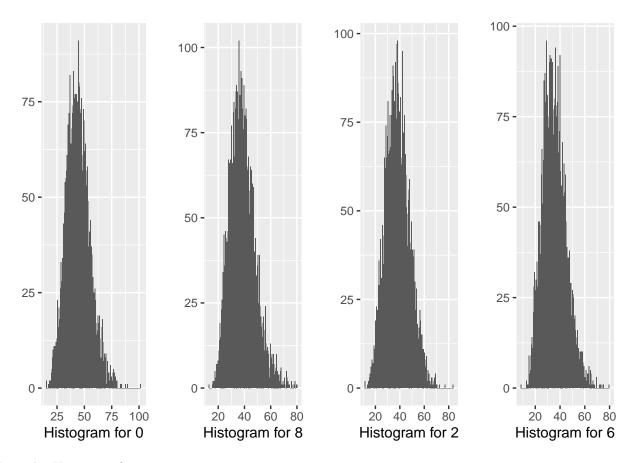
```
# Now lets plot intensity_by_label
ggplot(data=intensity_by_label, aes(x=Group.1, y = x)) +
    geom_bar(stat="identity")+scale_x_discrete(limits=0:9) + xlab("Label of the Digit") +
    ylab("Intensity of the digit (Mean)")
```



We see that pixel values have different intensity across the dataset. 0, 8, 2, 6 are with higher mean pixel intensity where as 1, 4, 7, and with low mean pixel intensity. If we want to bin the intensity values into statistical quantiles, we can do that. Overall digit "0" is the most intense and "1" is the less intense.

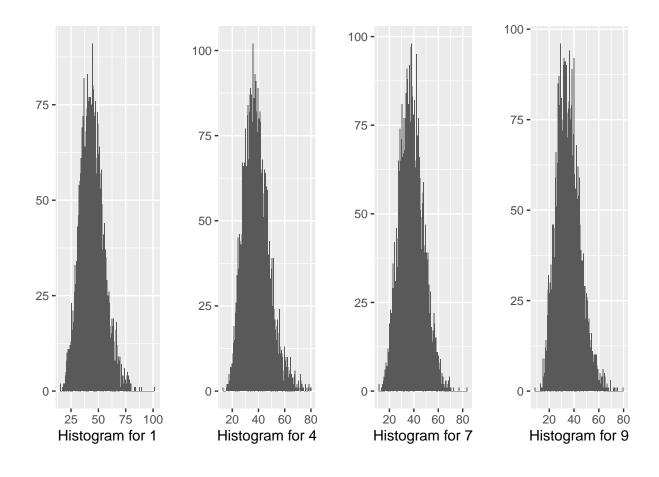
Lets plot Histogram for 0, 8, 2, 6

```
grid.arrange(qplot(subset(train, label ==0)$intensity, binwidth = .5, xlab = "Histogram for 0"), qplot(subset(train, label ==8)$intensity, binwidth = .5, xlab = "Histogram for 8"), qplot(subset(train, label ==2)$intensity, binwidth = .5, xlab = "Histogram for 2"), qplot(subset(train, label ==6)$intensity, binwidth = .5, xlab = "Histogram for 6"),ncol = 4)
```



Lets plot Histogram for 1, 4, 7, 9

```
grid.arrange(qplot(subset(train, label ==0)$intensity, binwidth = .5, xlab = "Histogram for 1"),
qplot(subset(train, label ==8)$intensity, binwidth = .5, xlab = "Histogram for 4"),
qplot(subset(train, label ==2)$intensity, binwidth = .5, xlab = "Histogram for 7"),
qplot(subset(train, label ==6)$intensity, binwidth = .5, xlab = "Histogram for 9"),ncol = 4)
```

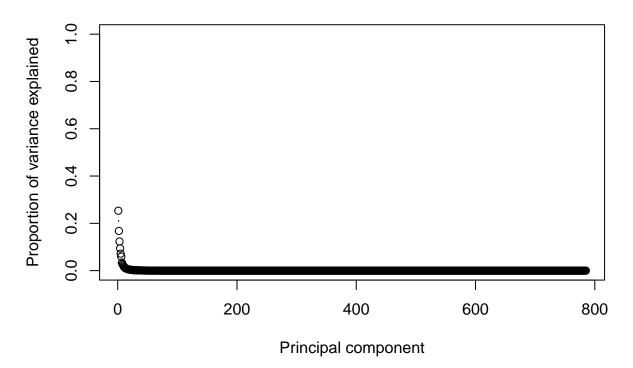


6. Reduce the data by using principal components that account for 95% of the variance. How many components did you generate? Use PCA to generate all possible components (100% of the variance). How many components are possible? Why?

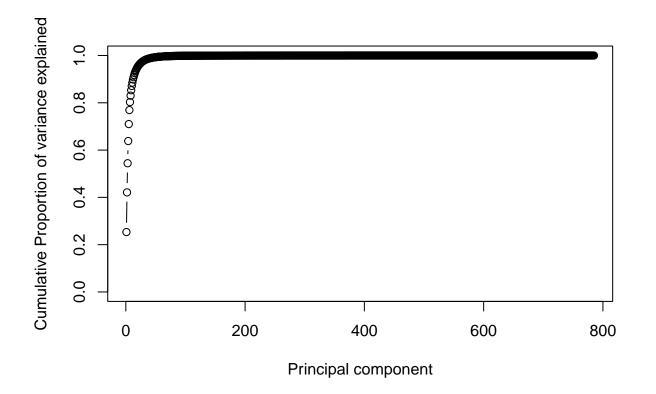
```
pcaCharts <- function(x) {
    x.var <- x$sdev ^ 2
    x.pvar <- x.var/sum(x.var)
    par(mfrow=c(1,1))
    plot(x.pvar,xlab="Principal component", ylab="Proportion of variance explained", ylim=c(0,1), type=
    plot(cumsum(x.pvar),xlab="Principal component", ylab="Cumulative Proportion of variance explained",
    screeplot(x,type="l")
    par(mfrow=c(1,1))
}

#Reducing data using PCA
train_norm<-as.matrix(train[,-1])/255
train_norm_cov <- cov(train_norm)
pca <- prcomp(train_norm_cov)

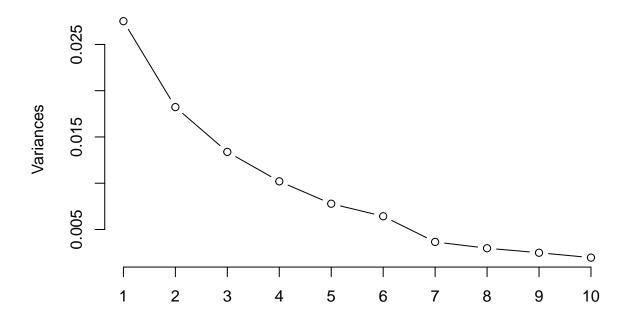
pcaCharts(pca)</pre>
```



Answer:







```
# Calculate the variance explained by each principal component
variance_explained<-as.data.frame(pca$sdev^2/sum(pca$sdev^2))
variance_explained<-cbind(1:785, cumsum(variance_explained))
colnames(variance_explained)<-c("Number", "Variance")
variance_explained<-as.data.frame(variance_explained)
head(variance_explained,100)</pre>
```

##		Number	Variance
##	1	1	0.2533019
##	2	2	0.4211143
##	3	3	0.5443375
##	4	4	0.6382797
##	5	5	0.7099622
##	6	6	0.7691849
##	7	7	0.8028326
##	8	8	0.8302254
##	9	9	0.8531247
##	10	10	0.8711668
##	11	11	0.8853364
##	12	12	0.8986528
##	13	13	0.9080900
##	14	14	0.9174678
##	15	15	0.9256073
##	16	16	0.9328088
##	17	17	0.9384871
##	18	18	0.9438281

```
## 19
           19 0.9483989
## 20
           20 0.9527310
## 21
           21 0.9564960
## 22
           22 0.9598711
## 23
           23 0.9629199
## 24
           24 0.9656478
## 25
           25 0.9682119
           26 0.9705036
## 26
## 27
           27 0.9726586
## 28
           28 0.9746368
## 29
           29 0.9764279
## 30
           30 0.9779677
##
  31
           31 0.9793804
## 32
           32 0.9807166
## 33
           33 0.9818930
## 34
           34 0.9830205
## 35
           35 0.9840633
##
  36
           36 0.9850209
## 37
           37 0.9858696
## 38
           38 0.9866471
## 39
           39 0.9873878
## 40
           40 0.9880989
## 41
           41 0.9887694
## 42
           42 0.9894178
## 43
           43 0.9899900
## 44
           44 0.9905075
## 45
           45 0.9909903
## 46
           46 0.9914504
## 47
           47 0.9918771
## 48
           48 0.9922717
## 49
           49 0.9926425
## 50
           50 0.9929780
## 51
           51 0.9933007
## 52
           52 0.9936134
## 53
           53 0.9938955
## 54
           54 0.9941623
## 55
           55 0.9944194
## 56
           56 0.9946575
## 57
           57 0.9948887
## 58
           58 0.9951032
## 59
           59 0.9953134
## 60
           60 0.9955119
## 61
           61 0.9956998
## 62
           62 0.9958863
## 63
           63 0.9960555
## 64
           64 0.9962159
## 65
           65 0.9963657
## 66
           66 0.9965039
## 67
           67 0.9966386
## 68
           68 0.9967638
## 69
           69 0.9968865
## 70
           70 0.9970029
## 71
           71 0.9971165
## 72
           72 0.9972235
```

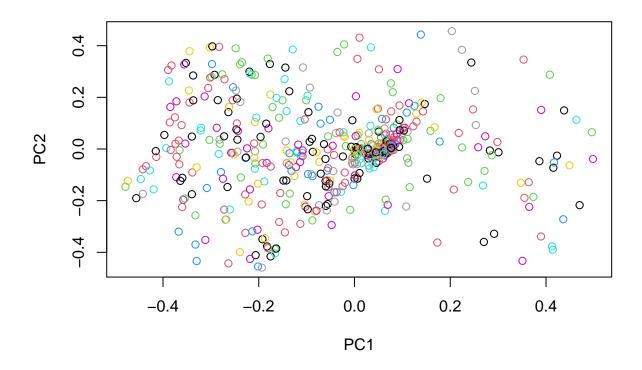
```
## 73
           73 0.9973257
## 74
           74 0.9974232
           75 0.9975134
##
  75
##
  76
           76 0.9976006
##
  77
           77 0.9976845
  78
           78 0.9977623
##
  79
           79 0.9978322
##
## 80
           80 0.9978985
## 81
           81 0.9979637
## 82
           82 0.9980280
##
  83
           83 0.9980911
  84
           84 0.9981509
##
##
  85
           85 0.9982082
  86
##
           86 0.9982642
## 87
           87 0.9983192
## 88
           88 0.9983697
## 89
           89 0.9984186
##
  90
           90 0.9984655
## 91
           91 0.9985092
## 92
           92 0.9985516
## 93
           93 0.9985929
## 94
           94 0.9986328
## 95
           95 0.9986710
## 96
           96 0.9987087
## 97
           97 0.9987440
## 98
           98 0.9987787
## 99
           99 0.9988124
## 100
          100 0.9988451
```

There are around 20 components generated at 95% of variance

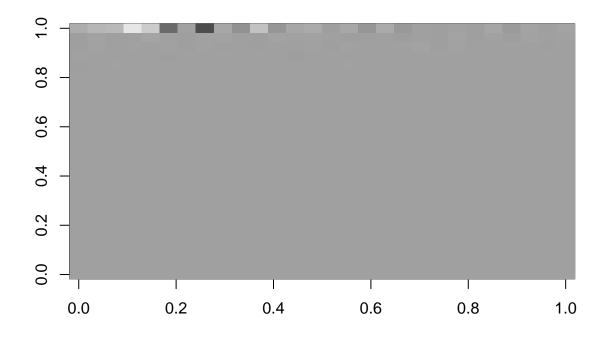
7. Plot the first 10 images generated by PCA. They will appear to be noise. Why?

Answer: Because PCs of higher eigenvalues to show more generic features. The specialized features are also being added for more PCs. So removing removing some PCs with lower eigenvalues actually acting as some sort of regularization and your model is only learning the more general features. If you take all of them the 100% of the data-variations will be restored like the original dimensions.

```
labelClasses <- factor(train$label)
plot(main="",pca$x, col = labelClasses)</pre>
```



```
for(i in 1:10){
  digit(pca$x[i, -1])
}
```



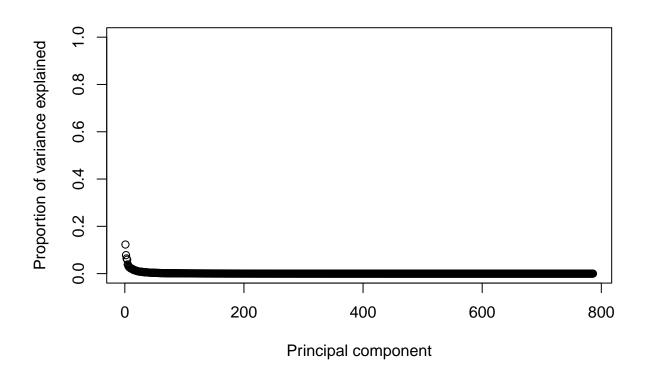
8. Now, select only those images that have labels that are 8's. Re-run PCA that accounts for all of the variance (100%). Plot the first 10 images. What do you see?

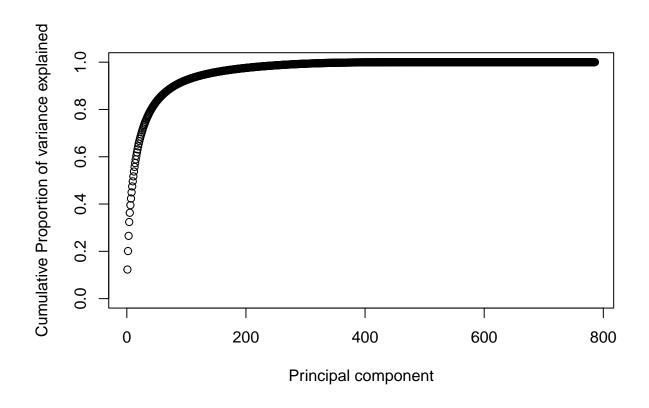
```
train_sub_8<-subset(train, label ==8)
nrow(train_sub_8)</pre>
```

Answer:

[1] 4063

```
pca <- prcomp(train_sub_8)
pcaCharts(pca)</pre>
```







```
Agriances

Agriculture of the state of the s
```

```
par(mfrow=c(3,4))
for(i in 1:10){
  digit(train_sub_8[i, -1])
}
```



In above images, different type of 8 letters seems to be visible. ***

9. An incorrect approach to predicting the images would be to build a linear regression model with y as the digit values and X as the pixel matrix. Instead, we can build a multinomial model that classifies the digits. Build a multinomial model on the entirety of the training set. Then provide its classification accuracy (percent correctly identified) as well as a matrix of observed versus forecast values (confusion matrix). This matrix will be a 10×10 , and correct classifications will

be on the diagonal.

NOTE: Please note models used below for this problem are running on small dataset extracted from train.csv file. Normal laptop doesn't return with the result even after many hours of continuous processing.

Answer: To build a multinomial model on the entirety of the training, I started with training dataset by splitting dataset further into to train and test where 70% data used for training the model and 30% dataset for testing it. Approach is run multinom function which will than return multinomModel than use multinomModel in predict function for probable results. Running this model produced around 93% accuracy.

Lines below for this model are commented, this model for 42K records takes around 4 days of time to return the results.

```
train <- read.csv("train_1.csv")

train[is.na(train)] <- 0
sample_size = round(nrow(train)*.70) # setting what is 70%</pre>
```

```
index <- sample(seq_len(nrow(train)), size = sample_size)

train <- train[index, ]

test <- train[-index, ]

#Build Multinomial Model

#multinomModel <- multinom(label ~., family = "multinomial", data = train, MaxNWts =100000, maxit=10);

#summary (multinomModel) # model summary

#predicted_scores <- predict (multinomModel, test, "probs") # predict on multinomModel data

#predicted_class <- predict (multinomModel, test) # model summary

#Confusion Matrix and Misclassification Error

#table(predicted_class, test$label)

#mean(as.character(predicted_class) != as.character(test$label))</pre>
```

A classification accuracy of 93.3% from multinom model is probably too high. We should try other ML approaches as well for this problem.

*** Gradient boosted trees model for multinomial ***: Gradient boosting is a machine learning technique used in regression and classification tasks, among others. It gives a prediction model in the form of an ensemble of weak prediction models, which are typically decision trees. Gradient boosted trees also run directly on the multiclass labels. The model performs much better if I increase the interaction depth slightly. Increasing it past 2-3 is beneficial in large models, but rarely useful with smaller cases like this. I could also play with the learning rate, but won't fiddle with that here for now.

```
# Model fitting
Xtrain <- as.matrix(train)
Xtest <- as.matrix(test)
ytrain <- train[,1]
ytest <- test[,1]
gbm_result <- gbm.fit(Xtrain, factor(ytrain), distribution="multinomial", n.trees=500, interaction.dep</pre>
```

##	Iter	TrainDeviance	ValidDeviance	${\tt StepSize}$	Improve
##	1	2.3026	nan	0.0010	0.0161
##	2	2.2939	nan	0.0010	0.0147
##	3	2.2860	nan	0.0010	0.0161
##	4	2.2774	nan	0.0010	0.0120
##	5	2.2704	nan	0.0010	0.0126
##	6	2.2633	nan	0.0010	0.0141
##	7	2.2557	nan	0.0010	0.0131
##	8	2.2487	nan	0.0010	0.0142
##	9	2.2411	nan	0.0010	0.0139
##	10	2.2336	nan	0.0010	0.0134
##	20	2.1644	nan	0.0010	0.0117
##	40	2.0321	nan	0.0010	0.0100
##	60	1.9249	nan	0.0010	0.0077
##	80	1.8270	nan	0.0010	0.0076
##	100	1.7395	nan	0.0010	0.0088
##	120	1.6551	nan	0.0010	0.0079
##	140	1.5792	nan	0.0010	0.0065
##	160	1.5100	nan	0.0010	0.0058
##	180	1.4455	nan	0.0010	0.0073

```
##
      200
                  1.3852
                                                0.0010
                                                           0.0057
                                       nan
##
      220
                  1.3283
                                                0.0010
                                                          0.0059
                                       nan
##
      240
                  1.2753
                                       nan
                                                0.0010
                                                           0.0041
      260
##
                  1.2263
                                                0.0010
                                                          0.0042
                                       nan
##
      280
                  1.1778
                                       nan
                                                0.0010
                                                           0.0053
##
      300
                                                0.0010
                                                          0.0044
                  1.1306
                                       nan
##
                                                0.0010
                                                          0.0035
      320
                  1.0856
                                       nan
##
      340
                  1.0442
                                       nan
                                                0.0010
                                                          0.0037
##
      360
                  1.0028
                                                0.0010
                                                          0.0027
                                       nan
      380
##
                  0.9643
                                       nan
                                                0.0010
                                                          0.0033
##
      400
                  0.9281
                                                0.0010
                                                          0.0032
                                       nan
##
      420
                                                0.0010
                                                           0.0034
                  0.8923
                                       nan
##
      440
                  0.8576
                                                0.0010
                                                          0.0038
                                       nan
##
      460
                  0.8252
                                       nan
                                                0.0010
                                                          0.0027
##
      480
                  0.7931
                                                0.0010
                                                           0.0030
                                       nan
##
      500
                  0.7620
                                                0.0010
                                                           0.0026
                                       nan
```

```
#summary(gbm_result)
gbm_prediction <- apply(predict(gbm_result, Xtest, n.trees=gbm_result$n.trees),1,which.max) - 1L
# Prediction
gbm_prediction</pre>
```

```
## [1] 4 3 1 7 0 1 1 1 0 6 0 9 0 3 9 1 3 0 3 9 9 2 5 6 4 0 4 5 7 8 8 2 6 0 2 5 4 1
## [38] 9 2 9 9 2 4 2 1 0 5 9 7 7 4 0 7 8 4 7 2 4 4 6 2 9 5 6 5 0 7 2 5 3 3 8 5 3
## [75] 1 2 0 4 4 1 3 8 2 0 9 7 2 2 1 6 2 8 1 0 6 8 8 5 1 0 7 7 3 2 8 4 9 4 5 5
## [112] 9 5 2 5 1 1 0 4 6 0 7 3 5 5 7 4 5 1 9 1 9 9 3 2 5 4 4 0 4 6 2 4 6 1 9 5 2
## [149] 6 5 9 6 6 0 1 5 6 7 2 3 9 7 3 9 0 7 2 6 1 2 1 1 5 3 5 6 3 8 4 1 9 5 2 2 5
## [186] 4 3 3 1 2 0 3 6 2 5 5 1 3 4 3 9 0 7 1 7 9 3 4 8 7 0 8 1 1 8 1 7 0 6 9 6 9
## [223] 8 6 7 4 5 5 4 8 9 6 0 0 8 9 2 6 7 0 8 9 0 7 7 9 0 5 2 3 1 3 4 5 0 0 9 9 9 3 2
## [260] 1 2 1 7 4 1 6 5 0 0 8 9 2 6 7 0 8 9 0 7 7 9 0 5 2 3 1 3 4 5 0 0 9 9 9 3 2
## [277] 1 7 4 2 9 1 4 6 7 6 6 4 9 5 5 0 3 2 9 8 7 4 9 6 3 2 0 2 5 1 7 2 8 8 4 1 8
## [334] 7 6 3 7 0 8 4 3 6 4 2 9 4 0 7 2 5 1 8 2 4 4 9 6 9 8 0 8 1 5 0 9 0 8 2 3 7
## [371] 2 9 9 1 0 0 4 6 1 8 8 2 7 5 5 8 8 8 4 7 4 8 0 7 8 8 9 7 5 6 5 5 1 3
```

Lets try Ridge regression for prediction and confusion, I'll directly use the multinomial loss function and let the R function do cross validation this time.

```
library(glmnet)
outLm <- cv.glmnet(Xtrain, ytrain, alpha=0, nfolds=3,
                    family="multinomial")
outLm
##
## Call: cv.glmnet(x = Xtrain, y = ytrain, nfolds = 3, alpha = 0, family = "multinomial")
##
## Measure: Multinomial Deviance
##
##
       Lambda Index Measure
                                  SE Nonzero
## min 0.01624
                 100 0.8403 0.02915
                                         629
## 1se 0.03753
                  91 0.8666 0.03246
                                         629
```

```
##
         8
              8
                  8
##
   175
        652
            970
                  71
         5
                  3
##
     5
#Mis-classification rates by class
tapply(predLm != ytest, ytest, mean)
##
          0
                              2
                                        3
                                                            5
                                                                     6
##
          7
                    8
## 0.02500000 0.00000000 0.02083333
# Confusion Metric
table(predLm,ytest)
##
        ytest
##
  predLm
         0
               2
            1
                  3
##
       0 42
##
       1
         0
         0
                    0
                       0
                          0
##
                  0
                                  0
##
       3
                       0
                          0
         0
                  0
                       0
                          0
##
##
       5
         0
            0
                    0
                      42
                          0
               0
##
       6
         0
            0
               0
                  0
                    0
                       0
                                  0
##
       7
         0
            0
               0
                 0
                    0
                       0
                          0
                           39
                                  1
```

We might think that a lot 2's, 6's and 9's are being mis-classified as one another (they do look similar in some ways). Looking at the confusion matrices we see that this is not quite the case.

0 47

8 0 0 0

0 0 0 0 0 0

##

##

0 0

0 0