# A Local Weather Simulation Model and Extentions to the Transaction Model for BigPetStore

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## 1 Introduction

BigPetStore is a family of realistic example applications for the Hadoop and Spark ecosystems based on around synthetic transaction data for a fictional chain of pet stores. At the heart of BigPetStore is a data generator that implements a model for simulating customer behavior. The patterns embedded in the data as a result of the model are used as the basis for analytics examples. The incorporation of additional effects can increase the realism of the data and provide opportunities for adding more examples analyses to BigPetStore.

The data generator model aims to, where possible, incorporate effects based on *ab initio* assumptions of customer behavior. This has the advantage of making it easy to recover the resulting patterns given knowledge of the assumptions. As part of our continual effort to expand and improve the model, we want to model the effect of weather patterns on customer purchasing habits. For example, customers tend to bulk up on items before impending bad weather such as snow storms. Economic activity also tends to be reduced during cold weather. A side effect of incorporating the influence of weather in the model is the addition of regional variations in customer purchasing behavior.

Of course, to incorporate the effects of weather into the model, we first need weather data. To support simulation of arbitrary time periods, we decided to develop a simple dynamical model for generating weather data, parameterized by real, historical weather data.

## 2 Local Weather Model

#### 2.1 Data Sources and File Formats

#### NOAA QCLCD

#### 2.2 Temperature

To build a model, we need to a make assumptions governing the behavior of the model. By analyzing the existing data, we can infer patterns to inform our assumptions. For the analysis, we'll use the average daily temperatures from South Bend, IN between October, 2011 to September, 2014.

The average daily temperatures are plotted in Figure ??. The temperatures seem to be governed by multiple frequencies, in particular high-frequency components related to daily variations in temperature and low-frequency components related to seasonal variations. The frequency spectra of the autocorrelation of the temperatures is plotted in Figure ??. The frequency spectra is dominated by a low-frequency signal with a period of 363.3 days. The high-amplitude, low-frequency signals correspond to the seasonal change we observed in the raw data. The changes in temperature over time (derivative) (Figure 1e) appear to follow a normal distribution.

Based on the observed properties, we propose a model combining a first-order Fourier series with a period of 365 days for the low-frequency components and an Orstein-Uhlenbeck process for the noise.

$$T(t) = \frac{1}{2}a_0 + a_1 \sin\left(\frac{-2.0\pi t}{365}\right) + a_2 \cos\left(\frac{-2.0\pi t}{365}\right) + Z(t)$$
 (1)

$$dZ_t = \theta(\mu - Z_t)dt + \sigma dW_t \tag{2}$$

Variable	Description
T(t)	Simulated temperature
$\overline{t}$	time
$\overline{a_0}$	Fourier coefficient
$\overline{a_1}$	Fourier coefficient
$\overline{a_2}$	Fourier coefficient
$\overline{Z_t}$	Ornstein-Uhlenbeck process
$\theta$	Damping coefficient
$\mu$	long-term mean
$\sigma^2$	variance of the Wiener process
dW(t)	Weiner process

Table 1: Descriptions of variables in the model

In implementing the model, we made several decisions. We determined the values of the coefficients  $a_0$ ,  $a_1$ , and  $b_1$  from a Fourier Transform of the real data. We set the long-term mean  $\mu$  to 0 and determined the variance  $\sigma^2$  from the distribution of the derivative values of the real temperature data.

We chose to numerically integrate the Orstein-Uhlenbeck process Z(t) using the Euler-Maruyama method:

$$Z_{t+1} = -\theta Z_t \Delta t + \sigma \sqrt{\Delta t} X_{t+1}$$

$$Z_0 = 0$$
(3)
(4)

$$Z_0 = 0 (4)$$

where  $\Delta t$  is the time step (one day) and  $X_t \sim N(0, \sigma^2)$ .

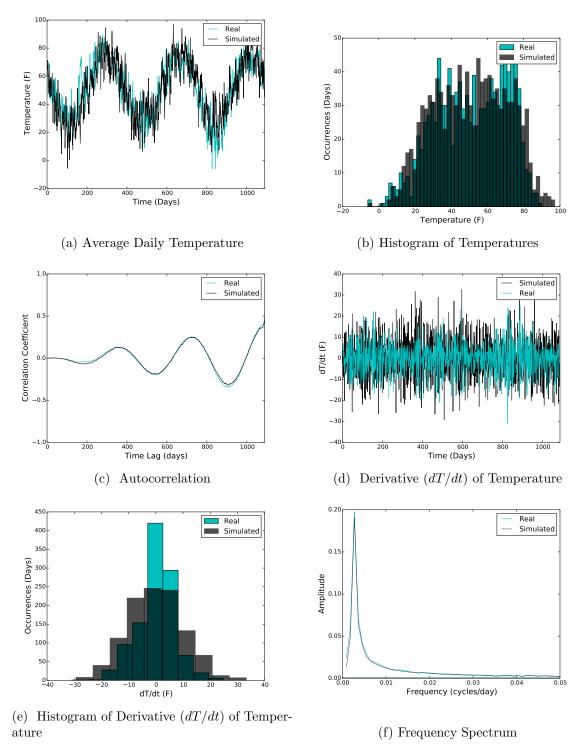


Figure 1

## 2.3 Precipitation

#### 2.3.1 Analysis of Real Data

- 1. Precipitation is not correlated in time. i.e., precipitation is independent day to day
- 2. Frequencies follow an exponential distribution
- 3. State (e.g., rain, snow) depends on temperature

## 2.3.2 Description of Model

Precipitation frequency follows an exponential distribution:

$$p(P_t|t) = \lambda \exp(-\lambda P_t) \tag{5}$$

Precipitation amounts for a given day are determined by sampling a value for  $P_t$  from  $p(P_t|t)$ . The precipitation is given as "water equivalent," meaning the amount of liquid water.

Snow-rain ratio is modeled by a logistic function r(t) of the temperature:

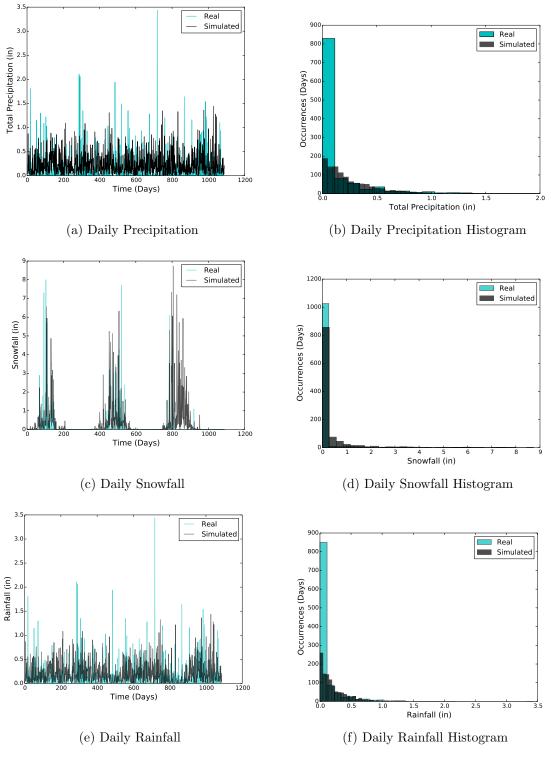
$$r(T) = \frac{1}{1 + \exp(-a(T - b))} \tag{6}$$

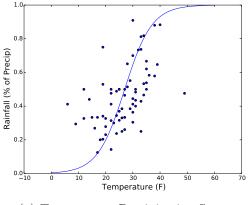
The amount of snowfall must be calculated from the precipitation  $r_t$  and percentage of snowfall r(T). Assuming that snow has a density that is 1/10 that of water, the amount of snowfall is given by:

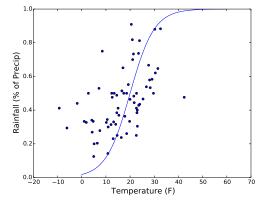
$$s(t) = 10.0 (1 - r(T_t)) P_t \tag{7}$$

## 2.3.3 Implementation of the Model

## 2.3.4 Evaluation of Model







- (a) Temperature-Precipitation Scatter
- (b) Wind Chill-Precipitation Scatter

Figure 3

## TODO autocorr, FFT, snowfall graph

## 2.4 Wind

#### 2.4.1 Analysis of Raw Data

- 1. The wind process is driven by two components: a single signal in the low-frequency regime with an amplitude > the median amplitude while the other frequencies have amplitudes near the median (FFT).
- 2. The low-frequency signal is deterministic and sinosidal (autcorrelation).
- 3. The signals for the remaining frequencies are characterized by a stochastic process (autocorrelation).
- 4. The derivative of the wind, which is dominated by the white noise, is normally (Gaussian) distributed (derivative value histogram).

#### 2.4.2 Description of Model

Based on the properties observed in Section ??, we can derive a model.

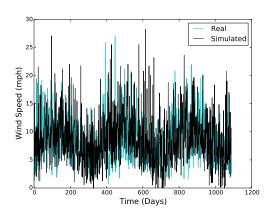
$$V(t) = \frac{1}{2}b_0 + b_1 \sin\left(\frac{-2.0\pi t}{365}\right) + b_2 \cos\left(\frac{-2.0\pi t}{365}\right) + X_t$$
 (8)

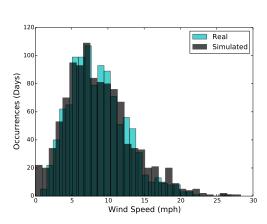
Variable	Description
$\overline{V(t)}$	Simulated wind speed
$\overline{t}$	time
$\overline{b_0}$	average wind speed
$\overline{b_1}$	Fourier coefficient
$b_2$	Fourier coefficient
$\overline{X_t}$	$X_t \sim Erlang(k, \theta)$

Table 2: Descriptions of variables in the model

## 2.4.3 Implementation of the Model

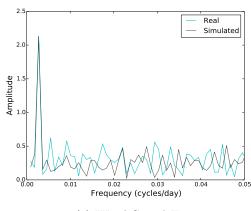
## 2.4.4 Evaluation of the Model





(a) Daily Wind Speed

(b) Daily Wind Speed Histogram



(c) Wind Speed FT

Figure 4

## 2.5 Review of Other Weather Models

## 3 Proposed Modifications to Transaction and Purchasing Models

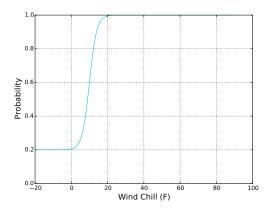
## 3.1 Determination of Weather Quality

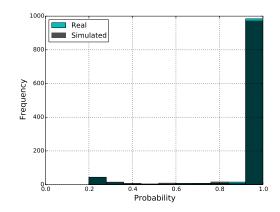
Need models to quantify "quality" of weather as a value in [0,1] where 1 indicates the best possible weather and 0 indicates the worst possible weather. Weather quality could be modeled separately for temperature, snow fall, rain fall, and wind and combined using a "min" operator.

Based on the weather quality for each day, we would need to model the probability of a customer going shopping given the weather conditions.

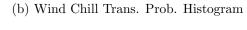
$$q_T(T) = \frac{1 - c}{1 + \exp(-a(T - b))} + c \tag{9}$$

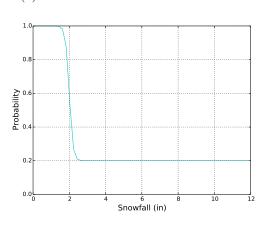
$$q_s(s) = 1 - \frac{1 - c}{1 + \exp(-a(s - b))}$$
(10)

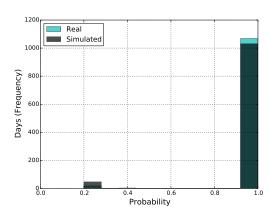




(a) Wind Chill Transaction Probabilities

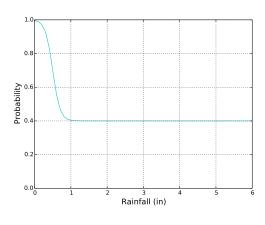


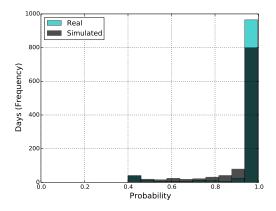




(c) Snowfall Transaction Probability

(d) Snowfall Trans. Prob. Histogram

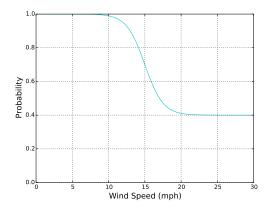


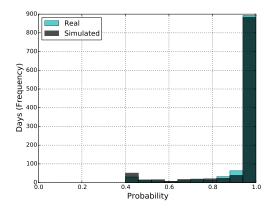


(e) Rainfall Transaction Probability

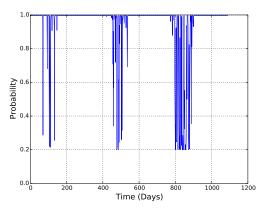
(f) Rainfall Trans. Prob. Histogram

Figure 5





- (a) Wind Speed Transaction Probability
- (b) Wind Speed Trans. Prob. Histogram



(c) Weather Trans. Prob.

Figure 6

TODO quality vs day, total precipitation, windchill

## 3.2 Transaction Model

## 3.2.1 Review of Existing Model

## 3.2.2 Proposed Changes to Model

Assumptions:

1. The probability of customers going to the store on a particular day is decreased under bad weather conditions.

$$p(\text{trans}|t_i) = \frac{p_{\text{(trans}}|t_i, \text{weather)} p_{\text{exhaustion offset}}(\text{trans}|t_i) p_{\text{arrow of time}}(\text{trans}|t_i \ge t_{i-1})}{Z}$$
(11)

## 3.2.3 Evaluation of Changes

## 3.3 Purchasing Model

## 3.3.1 Review of Existing Model

## 3.3.2 Proposed Changes to Model

## Assumptions:

1. Customers will buy larger quantities if they anticipate bad weather coming

#### Ideas:

- 1. Add additional term to category weight functions based on amount of bad weather in the next N days.
- 2. Increase preferences for larger sizes

## 3.3.3 Evaluation of Changes

## 4 Conclusion