

Consider  $n$  streams of time series describing the utilization traces of  $n$  resources, each at some (fixed) granularity. Denote the space of a time series as  $S$

Define a function  $d$ :

$$\begin{aligned} d_{a,b}: S^2 &\rightarrow [0, 1] \\ (x[a : b], y[a : b]) &\mapsto [0, 1] \end{aligned} \tag{1}$$

where  $d$  maps a portion of two time series to a real number in  $[0, 1]$  that represents the distance between the partial time series.

Additionally, we require  $d$  to satisfy the triangle inequality:

$$d(x, y) \leq d(x, z) + d(z, y) \tag{2}$$