

$$16. \begin{cases} x = \frac{1+\ln t}{t^2} \\ y = \frac{3+2\ln t}{t} \end{cases} \quad t_0 = \frac{1}{e}$$

$$y'_x = \frac{y'_t}{x'_t} = \frac{\left(\frac{3+2\ln t}{t}\right)'}{\left(\frac{1+\ln t}{t^2}\right)'} = t \quad ; \quad x\left(\frac{1}{e}\right) = 0 \quad ; \quad y\left(\frac{1}{e}\right) = e$$

$$y'_x(0) = \frac{1}{e}$$

$$y - y(x_0) = y'_x(x_0)(x - x_0)$$

$$y - e = \frac{1}{e}(x - 0)$$

$$y = \frac{x}{e} + e \quad \text{— график касательной}$$

$$y - y(x_0) = -\frac{1}{y'_x(x_0)}(x - x_0)$$

$$y - e = -e(x - 0)$$

$$y = -ex + e \quad \text{— график нормали}$$

$$y''_{xx} = \frac{(y''_x)'}{x'_t} = \frac{t'}{\left(\frac{1+\ln t}{t^2}\right)'} = \frac{1}{-\frac{2\ln t + 1}{t^3}} = -\frac{t^3}{2\ln t + 1} = -\frac{\frac{1}{e^3}}{-2+1} = \underline{\underline{\frac{1}{e^3}}}$$