

21.

$$f(x) = 3x^4 - 8x^2 + 12, \quad x_0 = -2$$

$$f(x) = f(x_0) + \frac{f'(x_0)}{1!}(x-x_0) + \frac{f''(x_0)}{2!}(x-x_0)^2 + \dots + \frac{f^{(n)}(x_0)}{n!}(x-x_0)^n + \dots$$

$$f'(x_0) = 28$$

$$f''(x_0) = 12x_0^3 - 16x_0 = -64$$

$$f'''(x_0) = 36x_0^2 - 16 = 128$$

$$f^{(iv)}(x_0) = 72x_0 = -144$$

$$f^{(v)}(x_0) = 72$$

$$f^{(vi)}(x_0) = 0.$$

$$f(x) = 28 - 64(x-2) + \frac{128}{2}(x-2)^2 - \frac{144}{6}(x-2)^3 + \frac{72}{24}(x-2)^4 =$$

$$= 28 - 64(x-2) + 64(x-2)^2 - 24(x-2)^3 + 3(x-2)^4.$$