```
In [1]:
```

```
import sklearn.datasets
import numpy as np
import pandas as pd
from sklearn.model selection import train test split
from sklearn.datasets import load wine
from sklearn.datasets import load digits
from sklearn.preprocessing import MinMaxScaler
from sklearn.datasets import make blobs
import matplotlib.pyplot as plt
import mglearn as mglearn
from sklearn.preprocessing import StandardScaler
from sklearn.svm import SVC
from sklearn import linear model
from sklearn.decomposition import PCA
from numpy import linal as LA
from sklearn.neighbors import KNeighborsClassifier
from sklearn.datasets import make blobs
from sklearn.cluster import KMeans
import scipy.cluster.hierarchy as sch
from sklearn.cluster import AgglomerativeClustering
from sklearn.datasets import load iris
from sklearn.model selection import cross val predict
from sklearn.manifold import TSNE
```

In [2]:

```
#
print("Question 1")
print()
print()
print()
```

Question 1

```
In [3]:
wine = load wine()
df = pd.DataFrame(wine.data,columns=wine.feature names)
df['target'] = pd.Series(wine.target)
X train, X test, y train, y test = train test split(wine.data,
                                                  wine.target,
                                                   stratify = w
ine.target,
                                                  random state
= 42)
df.head()
print()
print(wine.target names)
['class_0' 'class_1' 'class_2']
In [4]:
wine.DESCR
Out[4]:
'Wine Data Database\n=================\n\nNotes\n
----\nData Set Characteristics:\n
                                     :Number of Ins
tances: 178 (50 in each of three classes)\n
er of Attributes: 13 numeric, predictive attributes
and the class\n
                 :Attribute Information:\n \t\t- 1
) Alcohol\n \t\t- 2) Malic acid\n \t\t- 3) Ash\n\t\t
- 4) Alcalinity of ash \n \times t = 5) Magnesium\n \times t = 6
6) Total phenols\n \t - 7) Flavanoids\n \t - 8) No
nflavanoid phenols\n \t\- 9) Proanthocyanins\n\t\-
10)Color intensity\n \times t- 11)Hue\n \times t- 12)OD280/O
D315 of diluted wines\n \t\t- 13)Proline\n
                         - class 0\n
- class:\n
- class 1\n
                          - class 2\n\t\t\n
                           mary Statistics:\n \n
===== ===== ===== ===== ====\n
                    SD\n
                            _____
Min
     Max
           Mean
====== =====\n
                                  Alcohol:
             13.0 \quad 0.8\n
                             Malic Acid:
11.0 14.8
0.74
             2.34 1.12\n
    5.80
                             Ash:
          2.36
```

 $0.27\n$

14.3\n

19.5 3.3\n

99.7

Alcalinity of Ash:

Magnesium:

Total Phenols:

1.36

10.6

3.23

30.0

70.0 162.0

0.98 2.29 $0.63\n$ 3.88 Flavanoids: 0.34 5.08 2.03 1.00\n Nonflavanoid Phenols: 0.36 $0.12\n$ 0.13 0.66 Proanthocyanins: 1.59 $0.57 \n$ Colour Intensity: 0.41 3.58 2.3\n 1.3 5.1 13.0 Hue: 1.71 0.96 $0.23\n$ OD280/OD315 of diluted 0.48 $2.61 \quad 0.71\n$ wines: 1.27 4.00 Proline: 278 315\n 1680 746 ===== ==== ===== ====\n\n :Missing Attr ibute Values: None\n :Class Distribution: class_0 (59), class 1 (71), class 2 (48)\n :Creator: R.A. :Donor: Michael Marshall (MARSHALL%PLU@i :Date: July, 1988\n\nThis is a o.arc.nasa.gov)\n copy of UCI ML Wine recognition datasets.\nhttps://a rchive.ics.uci.edu/ml/machine-learning-databases/win e/wine.data\n\nThe data is the results of a chemical analysis of wines grown in the same\nregion in Italy by three different cultivators. There are thirteen d ifferent\nmeasurements taken for different constitue nts found in the three types of\nwine.\n\nOriginal O wners: \n\nForina, M. et al, PARVUS - \nAn Extendibl e Package for Data Exploration, Classification and C orrelation. \nInstitute of Pharmaceutical and Food A nalysis and Technologies, \nVia Brigata Salerno, 1614 7 Genoa, Italy.\n\nCitation:\n\nLichman, M. (2013). UCI Machine Learning Repository\n[http://archive.ics .uci.edu/ml]. Irvine, CA: University of California,\ nSchool of Information and Computer Science. \n\nRef erences $\n----\n(1)$ \nS. Aeberhard, D. Coomans and O. de Vel, \nComparison of Classifiers in High D imensional Settings, \nTech. Rep. no. 92-02, (1992), Dept. of Computer Science and Dept. of \nMathematics and Statistics, James Cook University of North Queen sland. \n(Also submitted to Technometrics). \n\nThe data was used with many others for comparing various \nclassifiers. The classes are separable, though onl y RDA \nhas achieved 100% correct classification. \n (RDA: 100%, QDA 99.4%, LDA 98.9%, 1NN 96.1% (z-tran sformed data)) \n(All results using the leave-one-ou t technique) $\n\n(2)$ \nS. Aeberhard, D. Coomans and O. de Vel, \n"THE CLASSIFICATION PERFORMANCE OF RDA" \nTech. Rep. no. 92-01, (1992), Dept. of Computer Sc ience and Dept. of \nMathematics and Statistics, Jam es Cook University of North Queensland. \n(Also subm

```
In [5]:
print( X train.shape, X test.shape, y train.shape, y test.shape)
(133, 13) (45, 13) (133,) (45,)
In [6]:
#Scaling Data#
print("Scaling Data")
print('')
scaler = MinMaxScaler()
scaler.fit(X train)
MinMaxScaler(copy=True, feature_range=(0, 1))
X train scaled = scaler.transform(X train) # transform data
print("transformed shape: {}".format(X train scaled.shape))
                                                                #
print dataset properties before and after scaling
print('')
print("per-feature minimum before scaling:\n {}".format(X train.
min(axis=0)))
print('')
print("per-feature maximum before scaling:\n {}".format(X train.
max(axis=0)))
print('')
print("per-feature minimum after scaling:\n {}".format(X train s
caled.min(axis=0)))
print('')
print("per-feature maximum after scaling:\n {}".format(X train s
```

itted to Journal of Chemometrics). \n'

caled.max(axis=0)))

```
transformed shape: (133, 13)
per-feature minimum before scaling:
 [1.103e+01 7.400e-01 1.360e+00 1.060e+01 7.000e+01
9.800e-01 3.400e-01
 1.300e-01 4.200e-01 1.280e+00 4.800e-01 1.270e+00 2
.780e+021
per-feature maximum before scaling:
 [1.483e+01 5.800e+00 3.220e+00 3.000e+01 1.620e+02
3.880e+00 3.740e+00
 6.300e-01 3.580e+00 1.300e+01 1.710e+00 3.920e+00 1
.515e+03]
per-feature minimum after scaling:
 [0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.]
per-feature maximum after scaling:
 [1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. ]
In [7]:
X test scaled = scaler.transform(X test)
#print dataset properties before and after scaling
print("transformed shape: {}".format(X test scaled.shape))
print('')
print("per-feature minimum before scaling:\n {}".format(X test.m)
in(axis=0))
print('')
print("per-feature maximum before scaling:\n {}".format(X_test.m)
ax(axis=0))
print('')
print("per-feature minimum after scaling:\n {}".format(X test sc
aled.min(axis=0)))
print('')
print("per-feature maximum after scaling:\n {}".format(X test sc
aled.max(axis=0)))
```

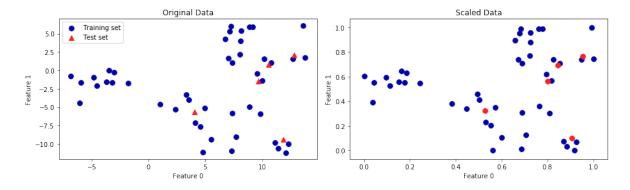
Scaling Data

```
transformed shape: (45, 13)
per-feature minimum before scaling:
 [1.156e+01 8.900e-01 1.700e+00 1.200e+01 7.800e+01
1.150e+00 4.800e-01
 1.700e-01 4.100e-01 2.150e+00 5.700e-01 1.290e+00 2
.900e+02]
per-feature maximum before scaling:
 [1.438e+01 5.650e+00 3.230e+00 2.850e+01 1.280e+02
3.520e+00 5.080e+00
 6.600e-01 2.960e+00 1.068e+01 1.450e+00 4.000e+00 1
.680e+031
per-feature minimum after scaling:
 [ 0.13947368  0.02964427  0.1827957  0.07216495  0
.08695652 0.05862069
                        -0.00316456 0.07423208 0.
  0.04117647 0.08
07317073 0.00754717
  0.009700891
per-feature maximum after scaling:
 [0.88157895 0.97035573 1.00537634 0.92268041 0.6304
3478 0.87586207
 1.39411765 1.06
                 0.80379747 0.80204778 0.78861
789 1.03018868
 1.13338723]
In [8]:
```

```
X, = make blobs(n samples = 50, centers = 5, random state = 4,
cluster std = 2)
X train, X test = train test split(X, random state = 5, test siz
e = 0.1)
```

In [9]:

```
#plot training and test sets
fig, axes = plt.subplots(1, 2, figsize=(13, 4))
axes[0].scatter(X train[:, 0], X train[:, 1], c=mglearn.cm2(0),
label="Training set", s=60)
axes[0].scatter(X test[:, 0], X test[:, 1], marker='^', c=mglear
n.cm2(1), label='Test set', s=60)
axes[0].legend(loc='upper left')
axes[0].set title("Original Data")
#scale data using MinMaxScalar
scaler = MinMaxScaler()
scaler.fit(X train)
X train scaled = scaler.transform(X train)
X test scaled = scaler.transform(X test)
#visualize the properly scaled data
axes[1].scatter(X train scaled[:, 0], X train scaled[:, 1], c=mg
learn.cm2(0), label="Training set", s=60)
axes[1].scatter(X test scaled[:, 0], X test scaled[:, 1], c=mgle
arn.cm2(1), label="Test set", s=60)
axes[1].set title("Scaled Data")
for ax in axes:
    ax.set xlabel("Feature 0")
    ax.set ylabel("Feature 1")
    fig.tight layout()
```



```
X train, X test, y train, y test = train test split(wine.data, w
ine.target, stratify = wine.target, random state=66)
svm = SVC(C=100)
svm.fit(X train, y train)
print("Test set accuracy: {:.2f}".format(svm.score(X test, y test))
t)))
print('')
print("Preprocessing using 0-1 scaling with MinMaxScaler")
scaler = MinMaxScaler()
scaler.fit(X train)
X train scaled = scaler.transform(X train)
X test scaled = scaler.transform(X test)
print('')
print("Learn an SVM on scaled training data:")
svm.fit(X train scaled, y train)
print("Scoring on scaled test set")
print("Scaled test set accuracy: {:.2f}".format(svm.score(X test
scaled, y test)))
```

Test set accuracy: 0.49

Preprocessing using 0-1 scaling with MinMaxScaler

Learn an SVM on scaled training data: Scoring on scaled test set Scaled test set accuracy: 0.96

```
In [11]:

print("Test set accuracy: {:.2f}".format(svm.score(X_test, y_test)))
print('')
print("Preprocessing using 0-1 scaling with MinMaxScaler")
scaler = StandardScaler()
scaler.fit(X_train)
X_train_scaled = scaler.transform(X_train)
X_test_scaled = scaler.transform(X_test)
print('')
svm.fit(X_train_scaled, y_train)
print("SVM test set accuracy: {:.2f}".format(svm.score(X_test_scaled, y_test)))

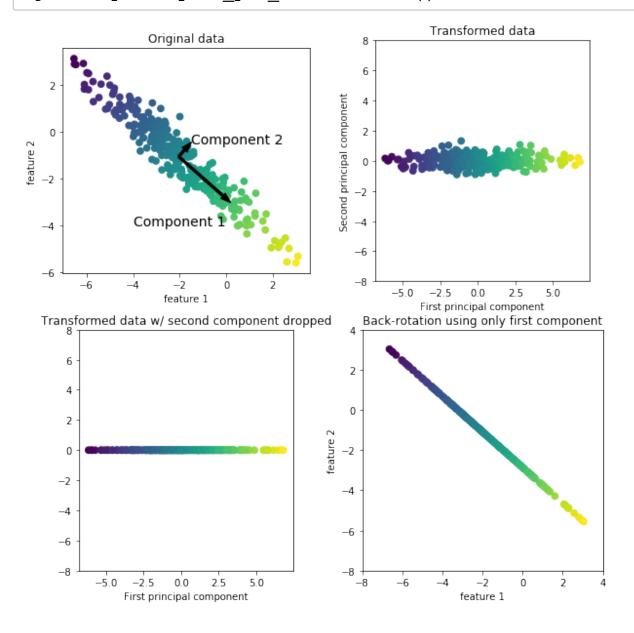
Test set accuracy: 0.40
Preprocessing using 0-1 scaling with MinMaxScaler
```

In [12]:

SVM test set accuracy: 0.98

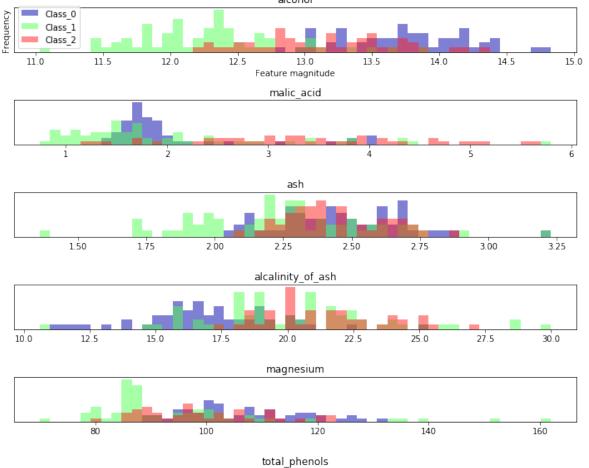
Question 2

mglearn.plots.plot_pca_illustration()



```
In [14]:
```

```
fig, axes = plt.subplots (13, 1, figsize = (10, 20))
Class 0 = wine.data[wine.target == 0]
Class 1 = wine.data [wine.target == 1]
Class 2 = wine.data [wine.target == 2]
ax = axes.ravel()
for i in range (13):
    , bins = np.histogram (wine.data[:,i], bins = 50)
    ax [i].hist(Class 0 [:,i], bins = bins, color = mglearn.cm3
(0), alpha = .5)
    ax [i].hist(Class 1 [:,i], bins = bins, color = mglearn.cm3
(2), alpha = .5)
   ax [i].hist(Class 2 [:,i], bins = bins, color = mglearn.cm3
(1), alpha = .5)
    ax [i].set title(wine.feature names [i])
    ax [i].set yticks(())
    ax [0].set xlabel( "Feature magnitude" )
    ax [0].set_ylabel( "Frequency" )
    ax [0].legend (["Class 0", "Class 1", "Class 2"], loc = "bes
t")
fig.tight layout ()
                         alcohol
```





```
In [15]:
```

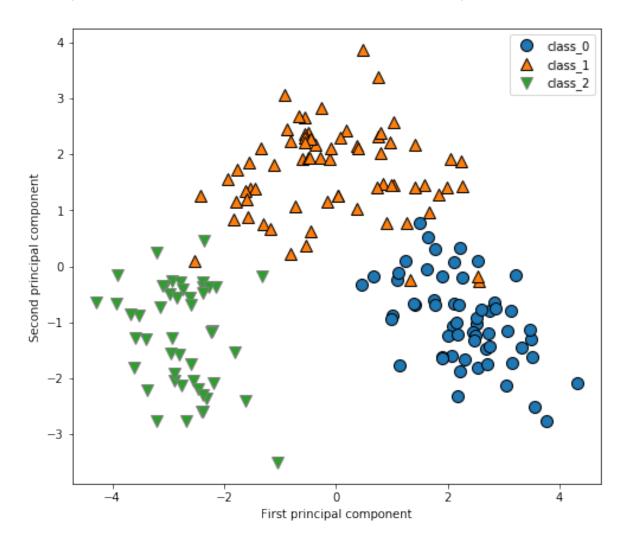
```
print("Scale Dataset")
scaler = StandardScaler()
scaler.fit(wine.data)
X scaled = scaler.transform(wine.data)
print('')
pca = PCA(n components = 4)
pca.fit(X scaled)
#transform data onto the first two principal components
X pca = pca.transform(X scaled)
print("Original shape: {}".format(str(X scaled.shape)))
print("Reduced shape: {}".format(str(X pca.shape)))
print('')
#plot first vs. second principal components
plt.figure(figsize=(8, 8))
mglearn.discrete_scatter(X_pca[:, 0], X_pca[:, 1], wine.target)
plt.legend(wine.target names, loc="best")
plt.gca().set aspect("equal")
plt.xlabel("First principal component")
plt.ylabel("Second principal component")
```

Scale Dataset

Original shape: (178, 13)
Reduced shape: (178, 4)

Out[15]:

Text(0,0.5,'Second principal component')

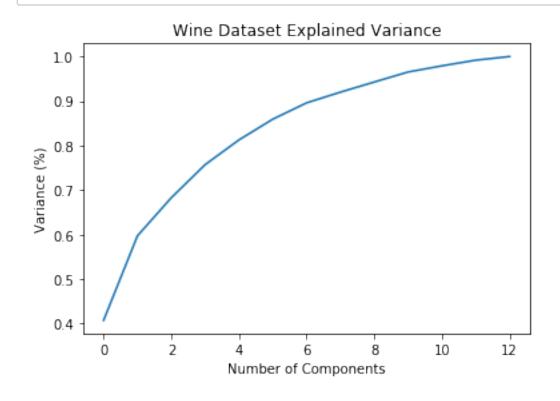


In [16]:

```
scaler = MinMaxScaler(feature_range=[0, 1])
wine_rescaled = scaler.fit_transform(X_scaled)

#Fitting the PCA algorithm with our Data
pca = PCA().fit(wine_rescaled)

#Plotting the Cumulative Summation of the Explained Variance
plt.figure()
plt.plot(np.cumsum(pca.explained_variance_ratio_))
plt.xlabel('Number of Components')
plt.ylabel('Variance (%)') #for each component
plt.title('Wine Dataset Explained Variance')
plt.show()
```

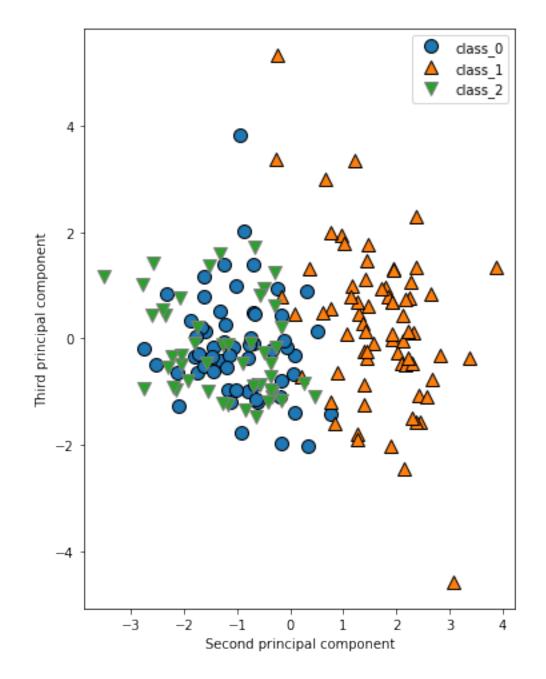


In [17]:

```
#plot second vs. third principal components
plt.figure(figsize=(8, 8))
mglearn.discrete_scatter(X_pca[:, 1], X_pca[:, 2], wine.target)
plt.legend(wine.target_names, loc="best")
plt.gca().set_aspect("equal")
plt.xlabel("Second principal component")
plt.ylabel("Third principal component")
```

Out[17]:

Text(0,0.5,'Third principal component')

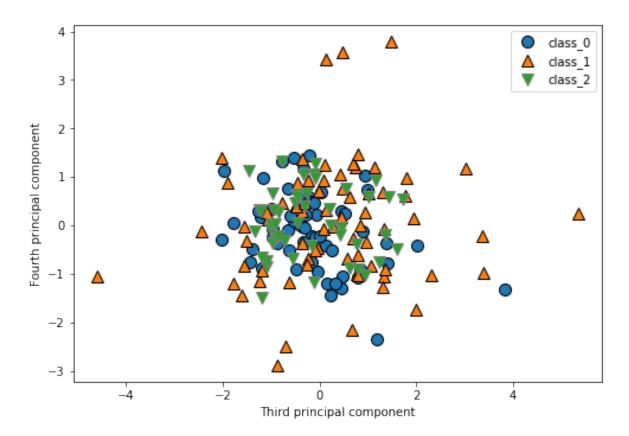


In [18]:

```
#plot secind vs. third principal components, colored by class
plt.figure(figsize=(8, 8))
mglearn.discrete_scatter(X_pca[:, 2], X_pca[:, 3], wine.target)
plt.legend(wine.target_names, loc="best")
plt.gca().set_aspect("equal")
plt.xlabel("Third principal component")
plt.ylabel("Fourth principal component")
```

Out[18]:

Text(0,0.5,'Fourth principal component')



```
In [19]:
```

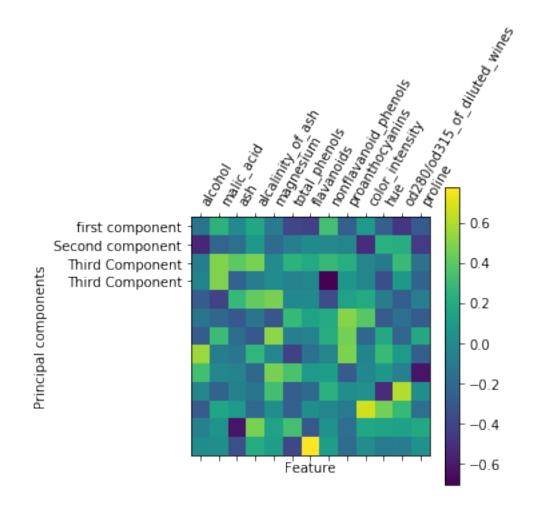
```
print("PCA component shape: {}".format(pca.components .shape))
print("PCA components:\n{}".format(pca.components ))
plt.matshow(pca.components , cmap='viridis')
plt.yticks([0, 1, 2, 3], ["first component", "Second component",
"Third Component", "Third Component"])
plt.colorbar()
plt.xticks(range(len(wine.feature names)), wine.feature names, r
otation=60, ha='left')
plt.xlabel("Feature")
plt.ylabel("Principal components")
PCA component shape: (13, 13)
PCA components:
[[-1.33367664e-01 2.48515807e-01 -7.39167565e-04
                                                    1
.77838621e-01
  -8.86572802e-02 -3.95070868e-01 -4.14589792e-01
                                                    3
.33108614e-01
  -2.52902105e-01 9.23290406e-02 -2.51137258e-01 -4
.73492101e-01
  -2.86862112e-011
 [-5.50883679e-01 -2.27390577e-01 -1.63091200e-01
.97763293e-02
  -1.88165658e-01 -7.41447292e-02 -1.00692215e-03 -9
.96036899e-03
  -3.14178847e-02 -5.19707496e-01 2.37206223e-01
                                                    2
.15562246e-01
  -4.43888361e-01]
 [-8.38483848e-02 \quad 4.92039271e-01 \quad 4.03009367e-01
                                                    4
.77242411e-01
   6.55069647e-03 2.53065140e-01 1.96105456e-01
                                                    2
.85981862e-01
   2.28342345e-01 -3.30999741e-02 -1.06588781e-01
                                                    2
.97776289e-01
  -1.51968292e-011
                  4.86032016e-01 -2.41975652e-01 -8
 [-4.03281504e-02]
.16939916e-02
   1.58801742e-02 -5.26432313e-02 -2.70332340e-02 -7
.09095281e-01
   7.65736687e-02 -2.63220354e-02 -3.52498013e-01
.20620051e-02
  -2.29792503e-011
```

```
[-2.78010089e-01 -4.12889958e-01 2.86393800e-01
.18304878e-01
       4.70898721e-01 -1.80297818e-02 2.57297682e-03 -3
.60037857e-01
       1.48665877e-01 2.00582427e-01 -7.71620754e-02 -2
.63396482e-01
    -7.65558029e-021
  [-1.37254317e-01 -2.13102785e-01 -3.00964675e-01 -1
.35609774e-01
    -3.12518646e-01 2.83604411e-01 1.47044786e-01
                                                                                                                                1
.97231755e-01
       5.03115302e-01 3.88031900e-01 -2.83041419e-01 -1
.67278047e-01
    -2.76348795e-01]
  [-2.75352205e-01 \ 3.10301653e-01 \ -1.71805330e-01 \ -2.75352205e-01 \ 3.10301653e-01 \ -2.75352205e-01 \ -2.7535205e-01 \ -2.75352056e-01 \ -2.7535205e-01 \ -2.75352056e-01 \ -2.75352005e-01 \ -2.75352005e-01 \ -2.75352005e-01 \ 
.97555954e-01
       5.20419359e-01 -6.65236704e-02 -5.06982802e-02
.14888676e-01
       4.66206579e-01 -2.12595824e-01 1.93314973e-01 -2
.24561421e-01
       1.88372489e-01]
  [5.55030622e-01 -7.69281456e-02 -1.23460354e-01]
                                                                                                                                2
.70756271e-01
    -1.99366070e-02 -4.13383802e-01 -1.56460745e-01 -3
.42321550e-02
       4.83470145e-01 -3.69237057e-02 2.95371717e-01
                                                                                                                                1
.02303314e-01
    -2.60228843e-01]
  [ 3.26686683e-01 -1.44706000e-02 -4.43615384e-02 -2
.04923518e-01
       4.71910296e-01 3.51231855e-01 8.89602892e-02
                                                                                                                                1
.22889237e-01
    -2.84054087e-01 -2.37079985e-02 6.87746576e-02 -6
.01970243e-02
    -6.24838818e-01]
  [-3.59116648e-02 -2.37072825e-01 -5.68986375e-02 -1
.32503040e-01
       3.25867728e-01 -2.63006307e-01 -1.99444858e-01
                                                                                                                                2
.36774685e-01
       1.87429817e-02 3.91434937e-02 -5.34248137e-01
                                                                                                                                6
.02193751e-01
       2.38290504e-021
  [-2.80684930e-01 1.70374648e-01 9.07566359e-02 -2
.00864181e-01
       2.72773854e-02 -2.47764000e-01
                                                                                       3.05792695e-02 -3
```

```
.25501002e-02
 -9.93148337e-02 6.69144086e-01 4.58587544e-01
.87815292e-01
 -1.69476208e-01]
[-5.61269360e-02 6.16542748e-02 -6.32537780e-01
.76650308e-01
  1.44634964e-01
                  3.33709022e-01 -2.99870770e-01
                                                    4
.73112536e-02
                 1.79211241e-01 1.57379260e-01
 -1.64956850e-01
                                                    1
.41063254e-01
  1.93164791e-01]
                   2.94277481e-02 -3.48604449e-01
                                                    2
[ 1.13596663e-02
.12755282e-01
  1.23445378e-01 -3.87627848e-01 7.75691511e-01
.18318269e-01
 -1.80607204e-01 1.62431688e-02 -9.56238231e-02 -8
.17454885e-02
  4.81186875e-02]]
```

Out[19]:

Text(0,0.5,'Principal components')

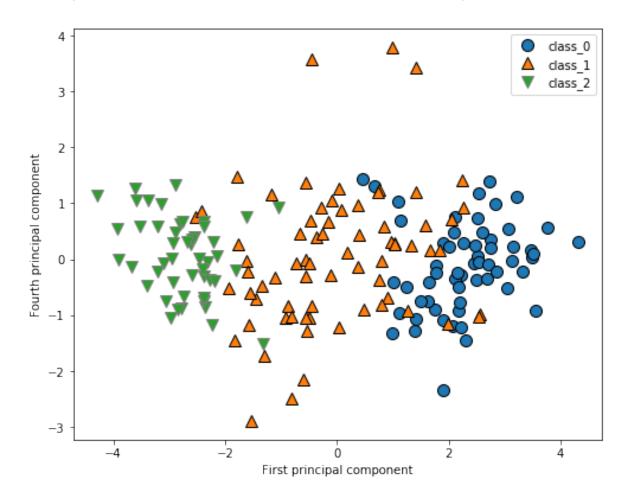


In [20]:

```
plt.figure(figsize=(8, 8))
mglearn.discrete_scatter(X_pca[:, 0], X_pca[:, 3], wine.target)
plt.legend(wine.target_names, loc="best")
plt.gca().set_aspect("equal")
plt.xlabel("First principal component")
plt.ylabel("Fourth principal component")
```

Out[20]:

Text(0,0.5,'Fourth principal component')



```
In [21]:
counts = np.bincount(wine.target)
for i, (count, name) in enumerate(zip(counts, wine.target names)
):
    print("{0:8} {1:10}".format(name, count), end=" |
    if (i+1) % 3 == 0:
        print()
class 0
                 59
                     class 1
                                         71
                                                clas
s 2
             48
In [22]:
mask = np.zeros(wine.target.shape, dtype=np.bool)
for target in np.unique(wine.target):
    mask[np.where(wine.target == target)[0][:50]] = 1
X wine = wine.data[mask]
y wine = wine.target[mask]
X_train, X_test, y_train, y_test = train_test_split(X_wine, y_wi
ne, stratify=y wine, random state=0)
knn = KNeighborsClassifier(n neighbors=1)
```

print("Test set score of 1-nn: {:.2f}".format(knn.score(X test,

Test set score of 1-nn: 0.76

knn.fit(X_train, y_train)

print()

y test)))

In [23]:

```
mglearn.plots.plot_pca_whitening()

pca = PCA(n_components=4, whiten=True, random_state=0).fit(X_train)

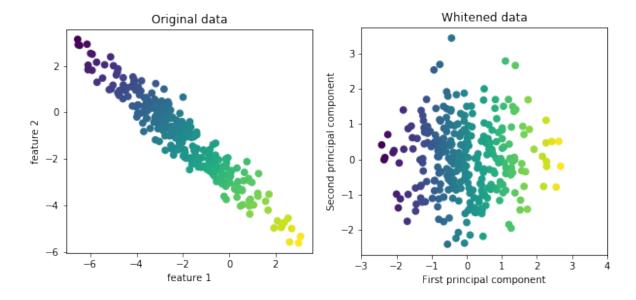
X_train_pca = pca.transform(X_train)

X_test_pca = pca.transform(X_test)

print("X_train_pca.shape: {}".format(X_train_pca.shape))

X_train_pca.shape: (1547, 100)
```

X_train_pca.shape: (111, 4)



In [24]:

```
knn = KNeighborsClassifier(n_neighbors=1)
knn.fit(X_train_pca, y_train)
print()
print("Test set score of 1-nn: {:.2f}".format(knn.score(X_test_p ca, y_test)))
```

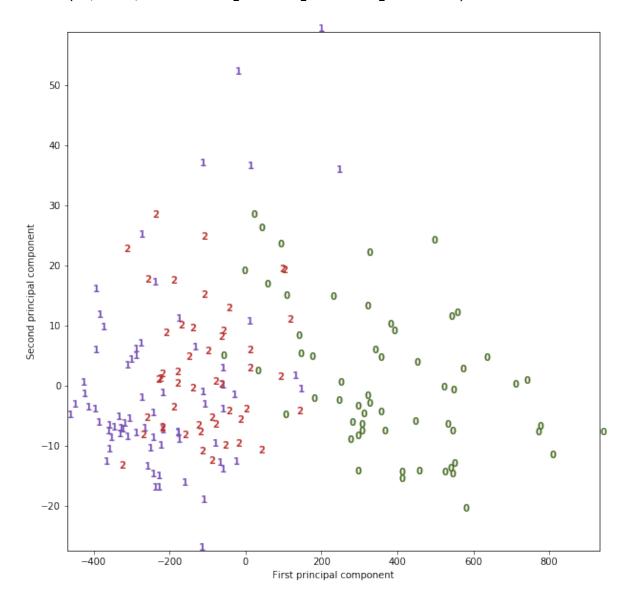
Test set score of 1-nn: 0.89

```
In [25]:
```

```
#build a PCA model
pca = PCA(n components=4)
pca.fit(wine.data)
#transform the digits data onto the first two principal componen
ts
wine pca = pca.transform(wine.data)
plt.figure(figsize=(10, 10))
plt.xlim(wine_pca[:, 0].min(), wine_pca[:, 0].max())
plt.ylim(wine pca[:, 1].min(), wine pca[:, 1].max())
colors = ["#476A24", "#7851B8", "#BD3430"]
for i in range(len(wine.data)):
    plt.text(wine pca[i, 0], wine pca[i, 1], str(wine.target[i])
, color = colors[wine.target[i]], fontdict={'weight': 'bold', 's
ize': 10})
plt.xlabel("First principal component")
plt.ylabel("Second principal component")
```

Out[25]:

Text(0,0.5,'Second principal component')



```
In [26]:
```

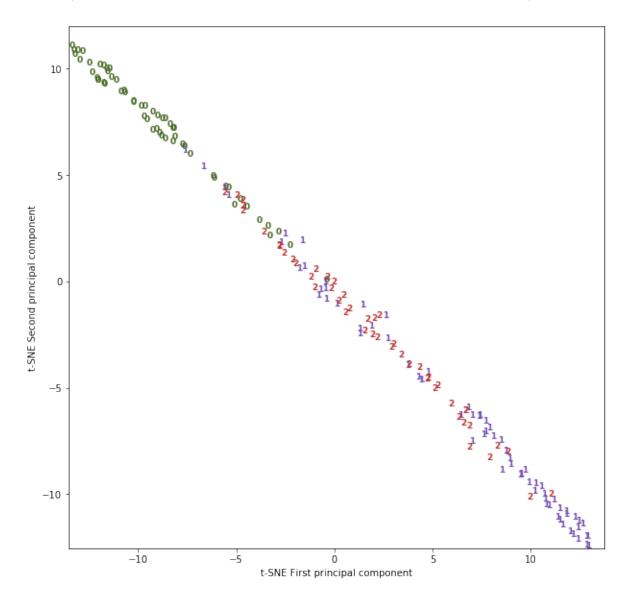
```
tsne = TSNE(random_state=42)

#use fit_transform instead of fit, as TSNE has no transform meth
od
wine_tsne = tsne.fit_transform(wine.data)
plt.figure(figsize=(10, 10))
plt.xlim(wine_tsne[:, 0].min(), wine_tsne[:, 0].max()+1)
plt.ylim(wine_tsne[:, 1].min(), wine_tsne[:, 1].max()+1)
for i in range(len(wine.data)):

    plt.text(wine_tsne[i, 0], wine_tsne[i, 1], str(wine.target[i]), color = colors[wine.target[i]], fontdict={'weight': 'bold', 'size': 9})
plt.xlabel("t-SNE First principal component")
plt.ylabel("t-SNE Second principal component")
```

Out[26]:

Text(0,0.5,'t-SNE Second principal component')



In [27]:

Question 6

```
In [28]:
```

```
data = make blobs(n samples = 300, n features = 2, centers = 3,
cluster std = 1.5, random state=20)
points = data[0]
print(data)
(array([[
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In [29]:
```

```
#Plotting data
print("Plotting data")
plt.scatter(data[0][:,0], data[0][:,1], c = data[1], cmap = 'vir
idis')
plt.xlim(-15, 15)
plt.ylim(0, 15)
```

```
(0, 15)

14
12
10
8
6
4
2
```

Ò

In [30]:

0

-15

Plotting data

Out[29]:

```
#KMeans Clustering
print("KMeans Clustering")
kmeans = KMeans(n_clusters = 3)
kmeans.fit(points) #fit
print(kmeans.cluster_centers_) #cluster locations
y_km = kmeans.fit_predict(points) #saving clusters for charts
```

Ė.

10

```
KMeans Clustering
[[ 7.84332115  6.52081551]
  [-9.45327176  3.98472662]
  [ 1.94132523  7.83718523]]
```

-5

-10

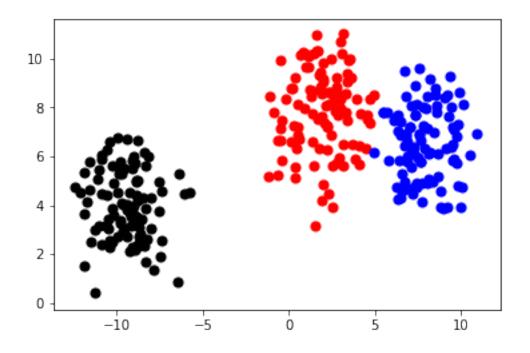
In [31]:

```
print("Plotting KMeans")
plt.scatter(points[y_km == 0,0], points[y_km == 0,1], s=50, c='r
ed')
plt.scatter(points[y_km == 1,0], points[y_km == 1,1], s=50, c='b
lack')
plt.scatter(points[y_km == 2,0], points[y_km == 2,1], s=50, c='b
lue')
```

Plotting KMeans

Out[31]:

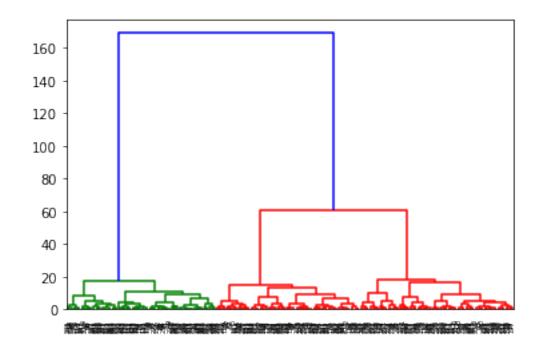
<matplotlib.collections.PathCollection at 0x1c23b2be
80>



In [32]:

```
#Hierarchical Clusering
print("Hierarchical Clusering")
dendrogram = sch.dendrogram(sch.linkage(points, method='ward'))
hc = AgglomerativeClustering(n_clusters=3, affinity = 'euclidean
', linkage = 'ward')
y_hc = hc.fit_predict(points)
```

Hierarchical Clusering



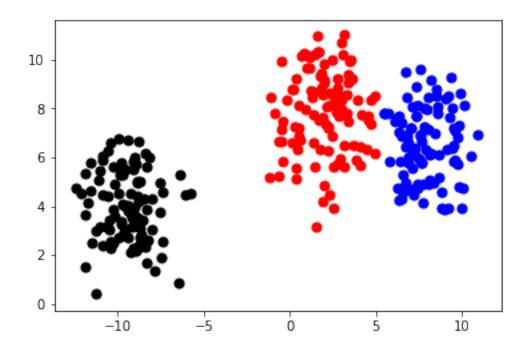
In [33]:

```
print("Plotting Hierarchical")
plt.scatter(points[y_hc ==0,0], points[y_hc == 0,1], s=50, c='re
d')
plt.scatter(points[y_hc==1,0], points[y_hc == 1,1], s=50, c='bla
ck')
plt.scatter(points[y_hc ==2,0], points[y_hc == 2,1], s=50, c='bl
ue')
```

Plotting Hierarchical

Out[33]:

<matplotlib.collections.PathCollection at 0x1c23f009
40>



In [34]:

```
#
print("Question 7")
print()
print()
print()
```

Question 7

```
In [35]:
iris = load iris()
iris.data.shape
Out[35]:
(150, 4)
In [36]:
X = iris.data[:, :2]
y = iris.target
print(X.shape)
print(y.shape)
(150, 2)
(150,)
In [37]:
plt.scatter(X[:,0], X[:,1], c = y, cmap = 'viridis')
plt.xlabel('Sepal Length', fontsize=10)
plt.ylabel('Sepal Width', fontsize=10)
Out[37]:
Text(0,0.5,'Sepal Width')
  4.5
  4.0
Sepal Width
  3.5
  3.0
```

7.0

7.5

8.0

6.5

2.5

2.0

5.0

4.5

5.5

6.0

Sepal Length

```
In [48]:
```

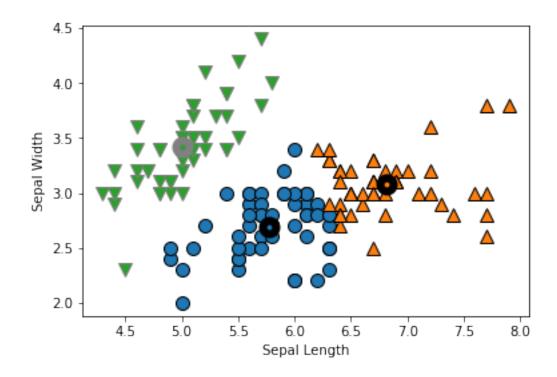
```
kmeans = KMeans(n_clusters = 3, n_jobs = 4, random_state=21)
kmeans.fit(X) #fitting data
centers = kmeans.cluster_centers_
y_km = kmeans.fit_predict(points) #saving clusters for charts
print(centers)
```

```
[[5.77358491 2.69245283]
[5.006 3.418 ]
[6.81276596 3.07446809]]
```

In [49]:

Out[49]:

Text(0,0.5,'Sepal Width')



```
In [41]:
```

```
kmeans = KMeans(n_clusters=3)
kmeans.fit(X)
print("Cluster:\n{}".format(kmeans.labels_))
print("k-Means Prediction:\n{}".format(kmeans.predict(X)))

lr = linear_model.LinearRegression()
y = iris.target

predicted = cross_val_predict(lr, iris.data, y, cv=5)

fig, ax = plt.subplots()
ax.scatter(y, predicted)
ax.plot([y.min(), y.max()], [y.min(), y.max()], ' ', lw=2)
ax.set_xlabel('Actual')
ax.set_ylabel('Predicted')
ax.set_title('Actual vs Predicted')
plt.show()
```

Cluster: 2 2 2 2 2 2 2 2 2 2 2 $0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0$ 1 0 1 1 1 1 0 1 1 1 1 1 1 0 0 1 1 1 1 0 1 0 1 0 1 1 0 0 1 1 1 1 1 0 0 1 1 1 0 1 1 1 0 1 1 1 0 1 1 0] k-Means Prediction: 2 2 2 2 2 2 2 2 2 2 2 1 0 0 0 0 0 0 0 0 0 0 1 0 1 1 1 1 0 1 1 1 1 1 0 0 1 1 1 1 0 1 0 1 0 1 1 1 0 0 1 1 1 1 1 0 0 1 1 1 0 1 1 1 0 1 1 1 0 1 1 0]

