Centro de Estatística Aplicada

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Junho de 2021

Sumário

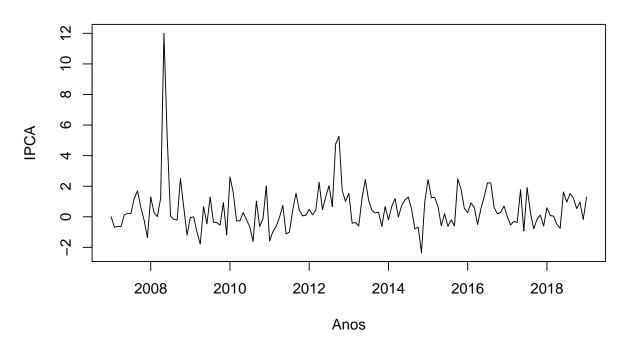
Análise Descritiva	2
Funções de Autocorrelações	10
Análise Correlação Cruzada	16
Regressão LASSO	22
Regressão classifica no contexto de Séries Temporais	25

 $^{^{1}}$ Número USP: 9795810 2 Número USP: 9299208 3 Número USP: 9790502

Análise Descritiva

```
\#setwd("C:\\Near \\Acount \\Near \\Near \\Acount \\Near \Near \\Near \
#data = read_xlsx("IPCA_DADOS_AGRUPADOS.xlsx", sheet = 1)
setwd("C:\\Users\\Rodrigo Araujo\\Documents\\IME-USP\\CEA 1\\dados")
data = read_xlsx("IPCA_DADOS_AGRUPADOS.xlsx", sheet = 1)
data$Data <- as.Date(data$Data)</pre>
head(data)
## # A tibble: 6 x 24
         Data
                              Arroz 'Avicultura de ~ 'Avicultura de ~ Banana Batata
##
                                                                                            <dbl> <dbl> <dbl>
         <date>
                              <dbl>
                                                             <dbl>
## 1 2007-01-01 0.01
                                                             0.295
                                                                                              3.43 -2.86
                                                                                                                     0.75
## 2 2007-02-01 -0.68
                                                             1.71
                                                                                              2.82 -1.62 -3.83
## 3 2007-03-01 -0.635
                                                             2.26
                                                                                            10.1
                                                                                                           1.05
                                                                                                                     7.61
## 4 2007-04-01 -0.635
                                                            -0.56
                                                                                             1.31 -2.65 36.4
## 5 2007-05-01 0.13
                                                            -0.13
                                                                                            -1.11 -1.46 11.6
## 6 2007-06-01 0.230
                                                             0.27
                                                                                              4.93 -1.07 -5.17
## # ... with 18 more variables: Bovinocultura <dbl>, 'Cacau e produtos' <dbl>,
         Café <dbl>, Cebola <dbl>, 'Complexo soja' <dbl>, 'Complexo
            sucroalc.' <dbl>, Feijão <dbl>, Frutas <dbl>, Hortícolas <dbl>,
            Indefinido <dbl>, 'Laranja e citros' <dbl>, Lácteos <dbl>, Mandioca <dbl>,
## #
            Milho <dbl>, Pescado <dbl>, Suinocultura <dbl>, Tomate <dbl>, Trigo <dbl>
zt2 <- ts(data[,2], frequency = 12, start = 2007, end = 2019)
zt3 <- ts(data[,3], frequency = 12, start = 2007, end = 2019)
zt4 <- ts(data[,4], frequency = 12, start = 2007, end = 2019)
zt5 <- ts(data[,5], frequency = 12, start = 2007, end = 2019)
zt6 <- ts(data[,6], frequency = 12, start = 2007, end = 2019)
zt7 <- ts(data[,7], frequency = 12, start = 2007, end = 2019)
zt8 <- ts(data[,8], frequency = 12, start = 2007, end = 2019)
zt9 <- ts(data[,9], frequency = 12, start = 2007, end = 2019)
zt10 \leftarrow ts(data[,10], frequency = 12, start = 2007, end = 2019)
zt11 <- ts(data[,11], frequency = 12, start = 2007, end = 2019)
zt12 <- ts(data[,12], frequency = 12, start = 2007, end = 2019)
zt13 <- ts(data[,13], frequency = 12, start = 2007, end = 2019)
zt14 <- ts(data[,14], frequency = 12, start = 2007, end = 2019)
zt15 <- ts(data[,15], frequency = 12, start = 2007, end = 2019)
zt16 <- ts(data[,16], frequency = 12, start = 2007, end = 2019)
zt17 <- ts(data[,17], frequency = 12, start = 2007, end = 2019)
zt18 <- ts(data[,18], frequency = 12, start = 2007, end = 2019)
zt19 <- ts(data[,19], frequency = 12, start = 2007, end = 2019)
zt20 <- ts(data[,20], frequency = 12, start = 2007, end = 2019)
zt21 \leftarrow ts(data[,21], frequency = 12, start = 2007, end = 2019)
zt22 <- ts(data[,22], frequency = 12, start = 2007, end = 2019)
zt23 <- ts(data[,23], frequency = 12, start = 2007, end = 2019)
zt24 <- ts(data[,24], frequency = 12, start = 2007, end = 2019)
```

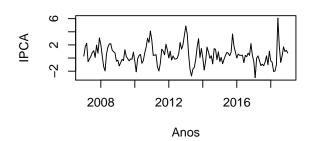
Série Temporal do Arroz

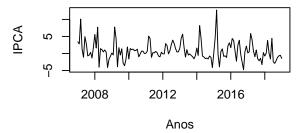


```
par(mfrow = c(2, 2))
plot(zt3,main="Série Temporal de Avicultura de Corte", xlab= "Anos", ylab="IPCA")
plot(zt4,main="Série Temporal de Avicultura de Postura", xlab= "Anos", ylab="IPCA")
plot(zt5,main="Série Temporal da Banana", xlab= "Anos", ylab="IPCA")
plot(zt6,main="Série Temporal da Batata", xlab= "Anos", ylab="IPCA")
```

Série Temporal de Avicultura de Corte

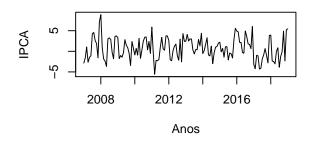
Série Temporal de Avicultura de Postura

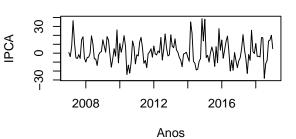




Série Temporal da Banana

Série Temporal da Batata





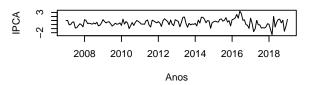
```
par(mfrow = c(3, 2))

plot(zt7,main="Série Temporal da Bovinocultura", xlab= "Anos", ylab="IPCA")
plot(zt8,main="Série Temporal do Cacau e Produtos", xlab= "Anos", ylab="IPCA")
plot(zt9,main="Série Temporal do Café", xlab= "Anos", ylab="IPCA")
plot(zt10,main="Série Temporal da Cebola", xlab= "Anos", ylab="IPCA")
plot(zt11,main="Série Temporal do Complexo Soja", xlab= "Anos", ylab="IPCA")
plot(zt12,main="Série Temporal do Complexo Sucroalc.", xlab= "Anos", ylab="IPCA")
```

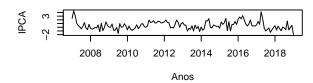
Série Temporal da Bovinocultura

2008 2010 2012 2014 2016 2018 Anos

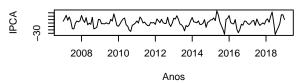
Série Temporal do Cacau e Produtos



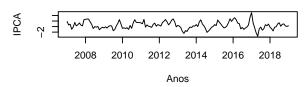
Série Temporal do Café



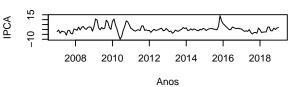
Série Temporal da Cebola



Série Temporal do Complexo Soja



Série Temporal do Complexo Sucroalc.



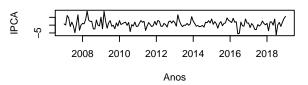
```
par(mfrow = c(3, 2))

plot(zt13,main="Série Temporal do Feijão", xlab= "Anos", ylab="IPCA")
plot(zt14,main="Série Temporal das Frutas", xlab= "Anos", ylab="IPCA")
plot(zt15,main="Série Temporal das Horticulas", xlab= "Anos", ylab="IPCA")
plot(zt16,main="Série Temporal de Indefinido", xlab= "Anos", ylab="IPCA")
plot(zt17,main="Série Temporal do Laranja e Citrus", xlab= "Anos", ylab="IPCA")
plot(zt18,main="Série Temporal da Lácteos", xlab= "Anos", ylab="IPCA")
```

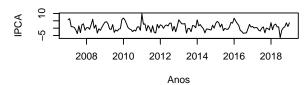
Série Temporal do Feijão

2008 2010 2012 2014 2016 2018 Anos

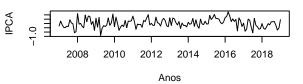
Série Temporal das Frutas



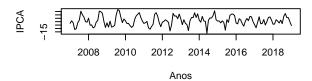
Série Temporal das Horticulas



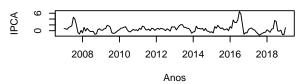
Série Temporal de Indefinido



Série Temporal do Laranja e Citrus



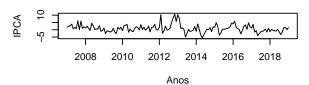
Série Temporal da Lácteos



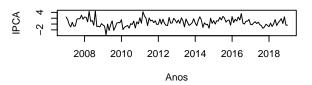
```
par(mfrow = c(3, 2))

plot(zt19,main="Série Temporal da Mandioca", xlab= "Anos", ylab="IPCA")
plot(zt20,main="Série Temporal do Milho", xlab= "Anos", ylab="IPCA")
plot(zt21,main="Série Temporal do Pescado", xlab= "Anos", ylab="IPCA")
plot(zt22,main="Série Temporal da Suínocultura", xlab= "Anos", ylab="IPCA")
plot(zt23,main="Série Temporal do Tomate", xlab= "Anos", ylab="IPCA")
plot(zt24,main="Série Temporal do Trigo", xlab= "Anos", ylab="IPCA")
```

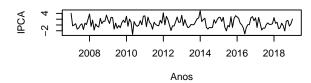
Série Temporal da Mandioca



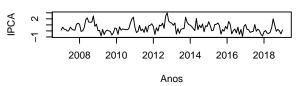
Série Temporal do Milho



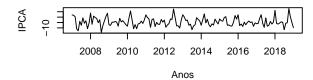
Série Temporal do Pescado



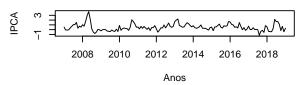
Série Temporal da Suínocultura



Série Temporal do Tomate

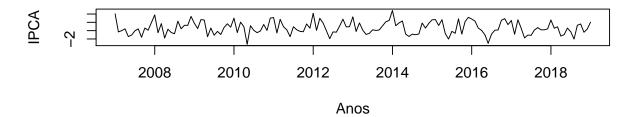


Série Temporal do Trigo

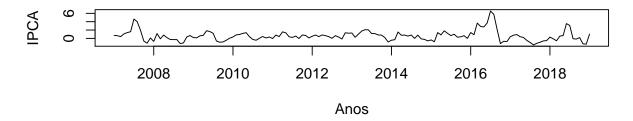


```
par(mfrow = c(2, 1))
plot(zt21,main="Série Temporal do Pescado", xlab= "Anos", ylab="IPCA")
plot(zt18,main="Série Temporal do Lácteos", xlab= "Anos", ylab="IPCA")
```

Série Temporal do Pescado



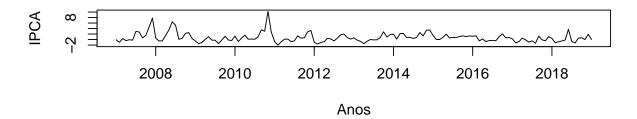
Série Temporal do Lácteos



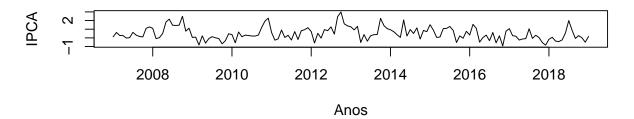
#900#650

```
par(mfrow = c(2, 1))
plot(zt7,main="Série Temporal da Bovinocultura", xlab= "Anos", ylab="IPCA")
plot(zt22,main="Série Temporal da Suínocultura", xlab= "Anos", ylab="IPCA")
```

Série Temporal da Bovinocultura

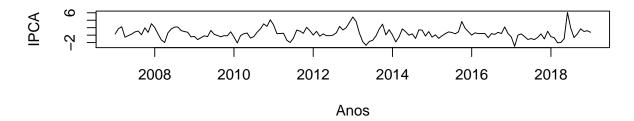


Série Temporal da Suínocultura

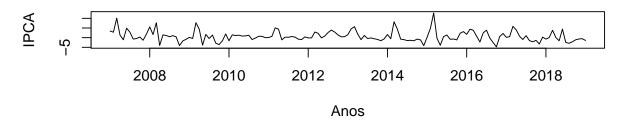


```
par(mfrow = c(2, 1))
plot(zt3,main="Série Temporal de Avicultura de Corte", xlab= "Anos", ylab="IPCA")
plot(zt4,main="Série Temporal de Avicultura de Postura", xlab= "Anos", ylab="IPCA")
```

Série Temporal de Avicultura de Corte



Série Temporal de Avicultura de Postura

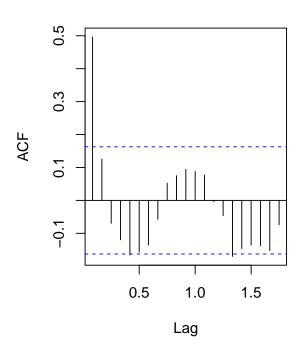


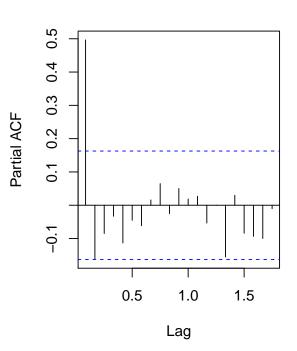
Funções de Autocorrelações

```
par(mfrow = c(1, 2))
acf(zt3, main="ACF Avicultura de Corte")
pacf(zt3, main="PACF Avicultura de Corte")
```

ACF Avicultura de Corte

PACF Avicultura de Corte

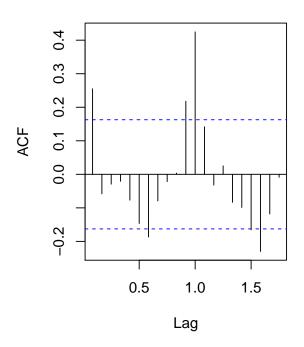


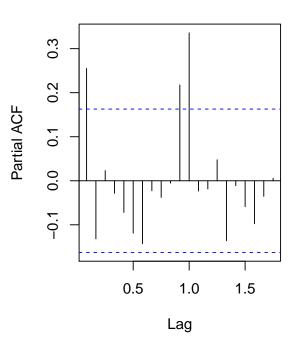


```
par(mfrow = c(1, 2))
acf(zt4, main="ACF Avicultura de Postura")
pacf(zt4, main="PACF Avicultura de Postura")
```

ACF Avicultura de Postura

PACF Avicultura de Postura

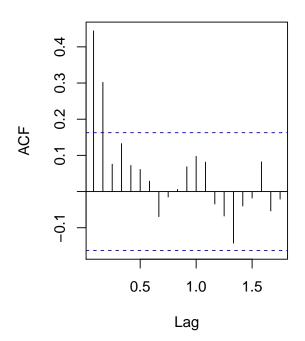


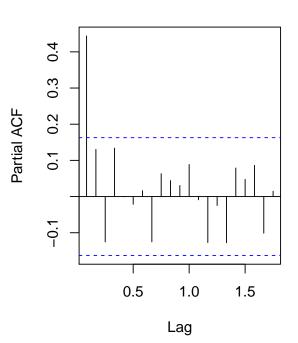


```
par(mfrow = c(1, 2))
acf(zt22, main="ACF Suinocultura")
pacf(zt22, main="PACF Suinocultura")
```

ACF Suínocultura

PACF Suínocultura

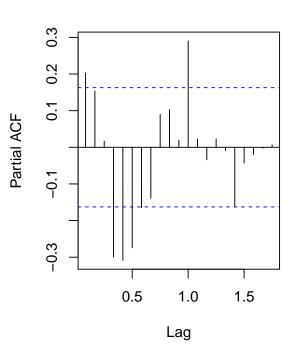




```
par(mfrow = c(1, 2))
acf(zt21, main="ACF Pescado")
pacf(zt21, main="PACF Pescado")
```

ACF Pescado

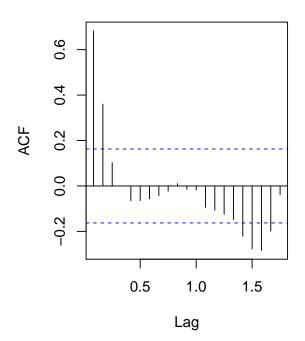
PACF Pescado

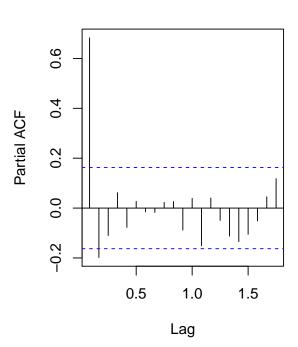


```
par(mfrow = c(1, 2))
acf(zt18, main="ACF Lácteos")
pacf(zt18, main="PACF Lácteos")
```

ACF Lácteos

PACF Lácteos

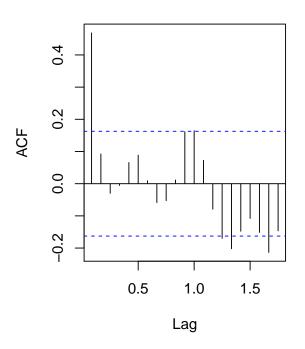


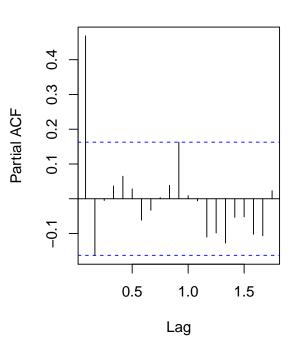


```
par(mfrow = c(1, 2))
acf(zt7, main="ACF Bovinocultura")
pacf(zt7, main="PACF Bovinocultura")
```

ACF Bovinocultura

PACF Bovinocultura





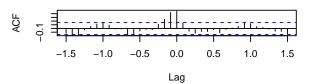
Análise Correlação Cruzada

```
#Correlaões cruzadas da Bovincultura
par(mfrow = c(3,2))
acf(zt7,main="ACF Bovinocultura")
ccf(zt7,zt3,main="Bovinocultura e Avicultura de Corte")
ccf(zt7,zt4,main="Bovinocultura e Avicultura de Postura")
ccf(zt7,zt18,main="Bovinocultura e Lácteos")
ccf(zt7,zt21,main="Bovinocultura e Pescados")
ccf(zt7,zt22,main="Bovinocultura e Suinocultura")
```

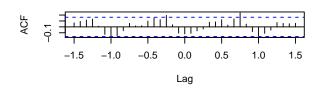
ACF Bovinocultura

0.5 1.0 1.5

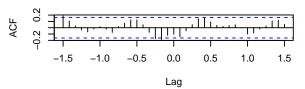
Bovinocultura e Avicultura de Corte



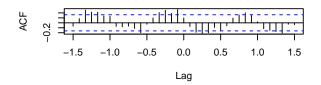
Bovinocultura e Avicultura de Postura



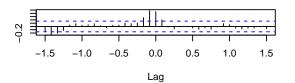
Bovinocultura e Lácteos



Bovinocultura e Pescados



Bovinocultura e Suinocultura

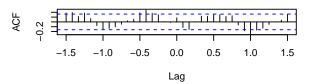


```
#Correlações cruzadas da Avicultura de Corte
par(mfrow = c(3,2))
acf(zt3,main="ACF Avicultura de Corte")
ccf(zt3,zt4,main="Avivultura de Corte e Avicultura de Postura")
ccf(zt3,zt7,main="Avicultura de Corte e Bovinocultura")
ccf(zt3,zt18,main="Avicultura de Corte e Lácteos")
ccf(zt3,zt21,main="Avicultura de Corte e Pescados")
ccf(zt3,zt22,main="Avicultura de Corte e Suinocultura")
```

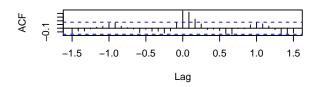
ACF Avicultura de Corte

0.5 1.0 1.5

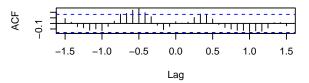
Avivultura de Corte e Avicultura de Postura



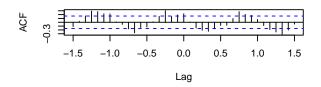
Avicultura de Corte e Bovinocultura



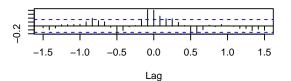
Avicultura de Corte e Lácteos



Avicultura de Corte e Pescados



Avicultura de Corte e Suinocultura

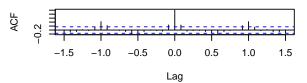


```
#Correlações cruzadas da Avicultura de Postura
par(mfrow = c(3,2))
acf(zt4,main="ACF Avicultura de Postura")
ccf(zt4,zt4,main="Avicultura de Postura e Avicultura de Corte")
ccf(zt4,zt7,main="Avicultura de Postura e Bovinocultura")
ccf(zt4,zt18,main="Avicultura de Postura e Lácteos")
ccf(zt4,zt21,main="Avicultura de Postura e Pescados")
ccf(zt4,zt22,main="Avicultura de Postura e Suinocultura")
```

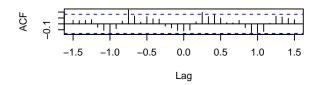
ACF Avicultura de Postura

0.5 1.0 1.5 Lag

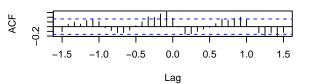
Avicultura de Postura e Avicultura de Corte



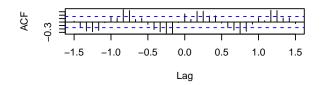
Avicultura de Postura e Bovinocultura



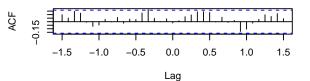
Avicultura de Postura e Lácteos



Avicultura de Postura e Pescados

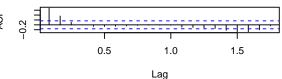


Avicultura de Postura e Suinocultura

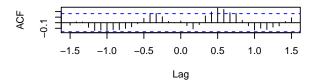


```
#Correlações cruzadas dos Lácteos
par(mfrow = c(3,2))
acf(zt18,main="ACF Lácteos")
ccf(zt18,zt3,main="Lácteos e Avicultura de Corte")
ccf(zt18,zt4,main="Lácteos e Avicultura de Postura ")
ccf(zt18,zt7,main="Lácteos e Bovinocultura")
ccf(zt18,zt21,main="Lácteos e Pescados")
ccf(zt18,zt22,main="Lácteos e Suinocultura")
```

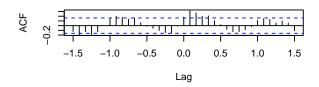
ACF Lácteos



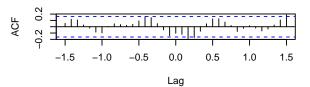
Lácteos e Avicultura de Corte



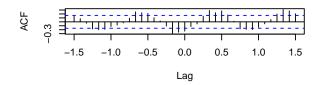
Lácteos e Avicultura de Postura



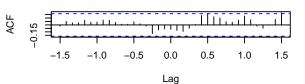
Lácteos e Bovinocultura



Lácteos e Pescados



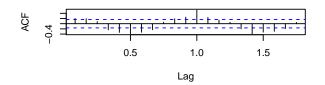
Lácteos e Suinocultura

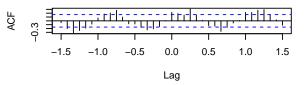


```
# Correlaões cruzadas dos Pescados
par(mfrow = c(3,2))
acf(zt21,main="ACF Pescados")
ccf(zt21,zt3,main="Pescados e Avicultura de Corte")
ccf(zt21,zt4,main="Pescados e Avicultura de Postura")
ccf(zt21,zt7,main="Pescados e Bovinocultura")
ccf(zt21,zt18,main="Pescados e Lácteos")
ccf(zt21,zt22,main="Pescados e Suinocultura")
```

ACF Pescados

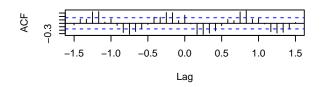
Pescados e Avicultura de Corte

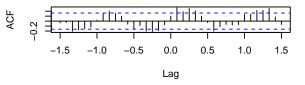




Pescados e Avicultura de Postura

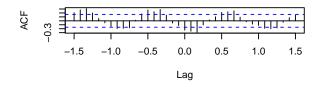
Pescados e Bovinocultura

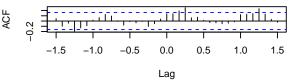




Pescados e Lácteos

Pescados e Suinocultura





```
#Correlações cruzadas da Suinocultura
par(mfrow = c(3,2))
acf(zt22,main="ACF Suinocultura")
ccf(zt22,zt3,main="Suinocultura e Avicultura de Corte")
ccf(zt22,zt4,main="Suinocultura e Avicultura de Postura")
ccf(zt22,zt7,main="Suinocultura e Bovinocultura")
ccf(zt22,zt18,main="Suinocultura e Lacteos")
ccf(zt22,zt21,main="Suinocultura e Pescados")
```

Suinocultura e Avicultura de Corte **ACF Suinocultura** 0.5 1.0 1.5 -0.5 0.0 0.5 1.0 -1.5 -1.0Lag Lag Suinocultura e Avicultura de Postura Suinocultura e Bovinocultura -1.5 -1.0 -0.5 0.0 0.5 1.0 1.5 -1.5 -1.0 -0.5 0.0 0.5 1.0 1.5 Lag Lag Suinocultura e Lacteos Suinocultura e Pescados -1.5 -1.0 -0.5 0.0 0.5 1.0 1.5 -1.5 -1.0 -0.5 0.0 0.5 1.0 1.5 Lag Lag combinar = function(df,coluna,nome,lag){ n = nrow(df)pre = rep(NA,lag) newcol = c(pre,coluna) for (k in 1:lag){ df = rbind(df,rep(NA,ncol(df))) df[nome] = newcol return (df) } data_cut = data[,c("Bovinocultura","Avicultura de Corte","Avicultura de Postura","Pescado","Lácteos","S df1<- combinar(data_cut, data_cut\$'Avicultura de Postura', 'avp9', 9)

Regressão LASSO

df2 <- na.omit(df1)</pre>

df1 <- combinar(df1, df1\$Pescado, 'p3', 3)
df1 <- combinar(df1, df1\$Pescado, 'p10', 10)
df1 <- combinar(df1, df1\$Bovinocultura, 'b1', 1)</pre>

```
library(glmnet)
```

```
## Loading required package: Matrix

##
## Attaching package: 'Matrix'

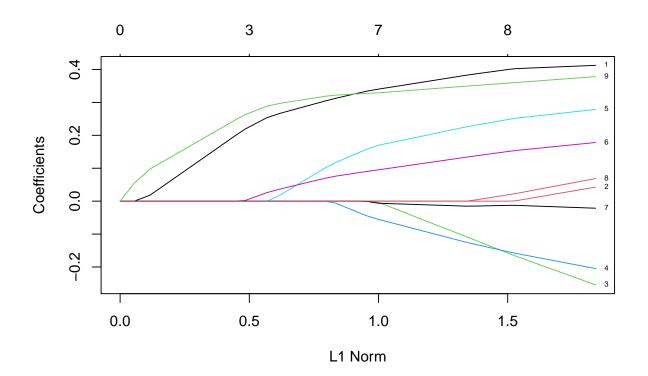
## The following objects are masked from 'package:tidyr':

##
## expand, pack, unpack

## Loaded glmnet 4.0-2

x = model.matrix(Bovinocultura~.,df2)[,-1]
y = df2$Bovinocultura

grid = 10^seq(10,-2, length = 100)
lasso.mod = glmnet(x,y,alpha = 1)
plot(lasso.mod, xvar = "norm", label = TRUE)
```



```
set.seed(123)

cv.lasso <- cv.glmnet(x, y, alpha = 1, family = "gaussian")
print(cv.lasso)

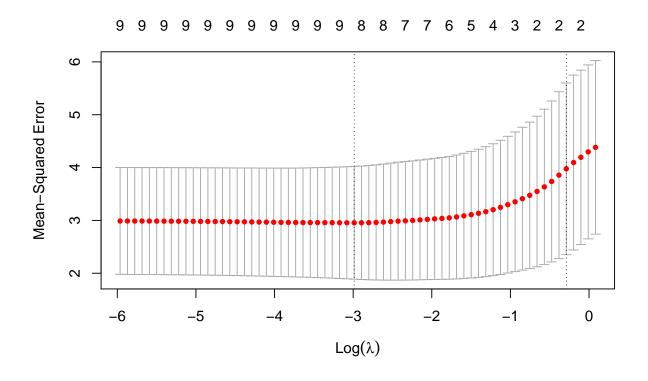
##

## Call: cv.glmnet(x = x, y = y, alpha = 1, family = "gaussian")
##

## Measure: Mean-Squared Error
##

## Lambda Measure SE Nonzero
## min 0.0504 2.955 1.067 8
## 1se 0.7489 3.976 1.625 2

plot(cv.lasso)</pre>
```



```
cv.lasso$lambda.min
## [1] 0.05043405
cv.lasso$lambda.1se
## [1] 0.7489297
```

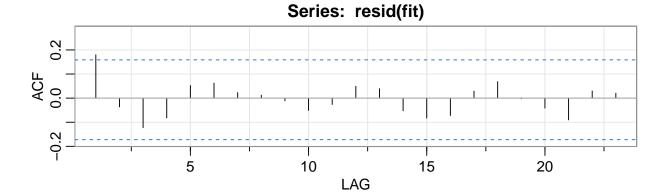
```
coef(cv.lasso, cv.lasso$lambda.min)
## 10 x 1 sparse Matrix of class "dgCMatrix"
## (Intercept)
                           0.31262107
## 'Avicultura de Corte'
                           0.39843764
## 'Avicultura de Postura' .
## Pescado
                         -0.15329263
                         -0.15094180
## Lácteos
## Suinocultura
                         0.24605653
## avp9
                          0.14932952
## p3
                         -0.01311084
## p10
                           0.01739267
## b1
                           0.35784156
coef(cv.lasso, cv.lasso$lambda.1se)
## 10 x 1 sparse Matrix of class "dgCMatrix"
##
                                   1
## (Intercept)
                          0.68566274
## 'Avicultura de Corte'
                          0.08952851
## 'Avicultura de Postura' .
## Pescado
## Lácteos
## Suinocultura
## avp9
## p3
## p10
## b1
                          0.15648256
```

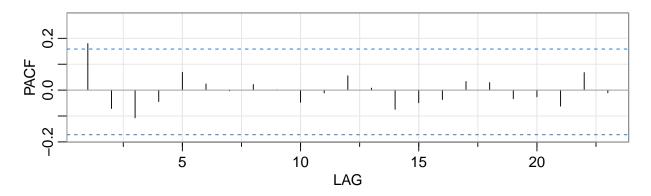
Regressão classifica no contexto de Séries Temporais

```
set.seed(1234)
summary(fit <- lm(y~x))</pre>
##
## Call:
## lm(formula = y \sim x)
##
## Residuals:
             1Q Median
                           3Q
## -3.5314 -0.9189 -0.0157 0.5586 8.5757
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
##
                         0.28536 0.20364 1.401 0.163405
## (Intercept)
## x'Avicultura de Corte' 0.41328 0.11349 3.642 0.000384 ***
## x'Avicultura de Postura' 0.04542 0.06035 0.753 0.452982
```

```
0.11194 -2.326 0.021498 *
## xPescado
                           -0.26037
## xLácteos
                           -0.20785
                                       0.12322 -1.687 0.093939 .
## xSuinocultura
                                       0.21162 1.325 0.187266
                            0.28048
## xavp9
                            0.17980
                                       0.05358 3.356 0.001026 **
## xp3
                           -0.02202
                                       0.10186 -0.216 0.829147
## xp10
                            0.07166
                                       0.10163 0.705 0.481954
## xb1
                            0.37950
                                       0.09758 3.889 0.000157 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.636 on 136 degrees of freedom
## Multiple R-squared: 0.4224, Adjusted R-squared: 0.3841
## F-statistic: 11.05 on 9 and 136 DF, p-value: 8.134e-13
library(astsa)
##
## Attaching package: 'astsa'
## The following objects are masked from 'package:fma':
##
##
       chicken, sales
## The following object is masked from 'package:forecast':
##
##
      gas
## The following object is masked from 'package:fpp2':
##
##
      oil
## The following object is masked from 'package:faraway':
##
##
      star
## The following object is masked from 'package:gamlss.data':
##
##
      oil
```

acf2(resid(fit))

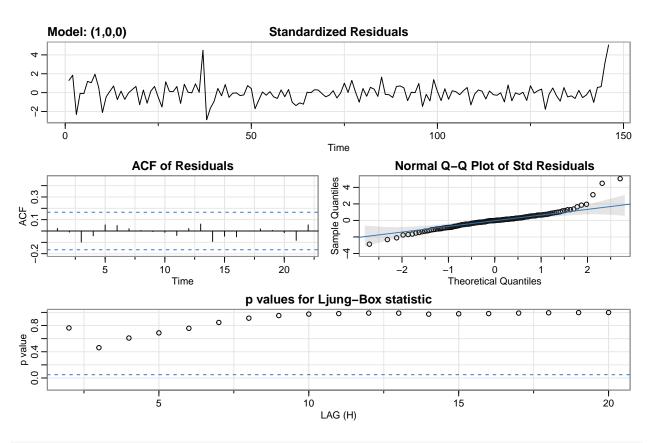




```
set.seed(12345)
fit2 <- sarima(y, 1,0,0, xreg=x)</pre>
```

```
## initial value 0.453951
## iter
         2 value 0.433468
## iter
          3 value 0.420315
          4 value 0.411120
## iter
## iter
          5 value 0.410309
## iter
          6 value 0.410165
## iter
          7 value 0.410127
## iter
          8 value 0.410120
          9 value 0.410117
## iter
## iter
        10 value 0.410117
         11 value 0.410116
        12 value 0.410116
## iter
## iter 12 value 0.410116
## iter 12 value 0.410116
## final value 0.410116
```

```
## converged
## initial value 0.414187
         2 value 0.413832
## iter
          3 value 0.413745
## iter
          4 value 0.413714
## iter
## iter
          5 value 0.413707
## iter
          6 value 0.413704
          7 value 0.413704
## iter
## iter
          8 value 0.413704
## iter
          9 value 0.413704
## iter
        10 value 0.413704
        10 value 0.413704
## iter
## iter 10 value 0.413704
## final value 0.413704
## converged
```



```
fit2
```

```
## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
## Q), period = S), xreg = xreg, transform.pars = trans, fixed = fixed, optim.control = list(trace = REPORT = 1, reltol = tol))
##
## Coefficients:
```

```
ar1 intercept 'Avicultura de Corte' 'Avicultura de Postura'
##
        0.4691
                   0.4196
                                         0.5589
                                                                 0.0076
                   0.2895
                                         0.1131
                                                                 0.0540
## s.e. 0.1227
        Pescado Lácteos Suinocultura
                                                  рЗ
##
                                         avp9
                                                                 b1
                                                         p10
##
        -0.1639 -0.1834
                          0.3054 0.1548 0.0282 0.1139 0.0712
## s.e. 0.0963 0.1454
                               0.2012 0.0492 0.0856 0.0844 0.1194
## sigma^2 estimated as 2.283: log likelihood = -267.57, aic = 559.13
## $degrees_of_freedom
## [1] 135
##
## $ttable
##
                                      SE t.value p.value
                         Estimate
                           0.4691 0.1227 3.8246 0.0002
## ar1
                           0.4196 0.2895 1.4497 0.1495
## intercept
## 'Avicultura de Corte'
                         0.5589 0.1131 4.9432 0.0000
## 'Avicultura de Postura' 0.0076 0.0540 0.1400 0.8889
## Pescado
                          -0.1639 0.0963 -1.7023 0.0910
## Lácteos
                          -0.1834 0.1454 -1.2614 0.2093
## Suinocultura
                           0.3054 0.2012 1.5182 0.1313
## avp9
                          0.1548 0.0492 3.1468 0.0020
## p3
                          0.0282 0.0856 0.3290 0.7427
## p10
                          0.1139 0.0844 1.3496 0.1794
## b1
                          0.0712 0.1194 0.5960 0.5521
## $AIC
## [1] 3.829668
##
## $AICc
## [1] 3.843162
##
## $BIC
## [1] 4.074896
```