HWK 0

Due January 27, 2017 Instructions for submission into your class SVN repository are on the webpage.

The purpose of this assignment is to give you a chance to refresh the math skills we expect you to have learned in prior classes. These particular skills will be essential to mastery of CS225, and we are unlikely to take much class time reminding you how to solve similar problems. Though you are not required to work independently on this assignment, we encourage you to do so because we think it may help you diagnose and remedy some things you might otherwise find difficult later on in the course. If this homework is difficult, please consider completing the discrete math requirement (CS173 or MATH 213) before taking CS225.

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Section (circle one):

Regular Sections:

Wednesday (5–7pm AYT	7–9pm AYB	
Thursday	9-11am AYC	11–1pm AYD	1–3pm AYE
	3–5pm AYF	5–7pm AYG	7–9pm AYH
Friday	9–11am AYQ	9–11am AYI	11–1pm AYJ
	1–3pm AYS	1–3pm AYK	3–5pm AYL
Laptop Sections:			
Wednesday	5–7pm AYM	7–9pm AYR	
Thursday	1–3pm AYN	3–5pm AYO	5–7pm AYP

Grade	Out of 60
Grader	

1. (3 points) Using 140 characters or less, post a synopsis of your favorite movie to the course piazza space under the "HW0 tell me something!" notice, so that your post is visible to everyone in the class, and tagged by #HW0num1. Also, use Piazza's code-formatting tools to write a private post to course staff that includes at least 5 lines of code. It can be code of your own or from a favorite project—it doesn't even have to be syntactically correct—but it must be formatted as a code block in your post, and also include the tag #HW0num1. (Hint: Check http://support.piazza.com/customer/portal/articles/1774756-code-blocking). Finally, please write the 2 post numbers corresponding to your posts here:

Favorite Movie Post (Public) number:	1420
Formatted Code Post (Private) number:	1423

2. (12 points) Simplify the following expressions as much as possible, without using an calculator (either hardware or software). Do not approximate. Express all rational numbers as improper fractions. Show your work in the space provided, and write your answer in the box provided.

(a)
$$\prod_{k=2}^{n} \left(1 - \frac{1}{k^2}\right)$$
Answer for (a):
$$\prod_{k=2}^{n+1} \left(1 - \frac{1}{k^2}\right)$$

$$\left(1 - \frac{1}{k^2}\right) = \left(1 - \frac{1}{k^2}\right)$$

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(b) 3¹⁰⁰⁰ mod 7 Answer for (b):

$$3 = 3 \pmod{7}$$

 $3^2 = 2 \pmod{7}$
 $3^3 = 2 \times 3$
 $= -1 \pmod{7}$
 $3^6 = 1 \pmod{7}$

1000 = 6 (166)+4. 3 1000 = 3 6 (166) +4 - 126) 46624

 $(c) \sum_{r=1}^{\infty} (\frac{1}{2})^r$

Answer for (c):

91 = 1/2 1-1 = 1-1/2 = 1/2 = 1

 $(d) \frac{\log_7 81}{\log_7 9}$

Answer for (d):

109781 = 109792

2 log 2 9 log 2 9 = J

(e) $\log_2 4^{2n}$

Answer for (e):

yn

- Zn(10924)
- (f) $\log_{17} 221 \log_{17} 13$

log (221/13)

log 17 = 1

Answer for (f):

3. (8 points) Find the formula for $1+\sum_{j}j!j$, and show work proving the formula is correct using induction.

Claimi 1+ & j! i = (n+1)! Formula:

when
$$n=1$$
 $1+\sum_{j=1}^{N} |j-1| = (1-1)! = 2! = 2$

induction: suppose 1 + \(\frac{2}{5},\)! \(= (n+1)! \) for n=1,2,3,...k-1

need to show that I + & i! = (n+1)! for n= k

1+ 2 !!; = k!

1+ \(\frac{1}{2}\) = (1+ \(\frac{1}{2}\)) + K! \(= \K! \(K+1) - \frac{1}{2}\) = (\(K+1)\)!

4. (8 points) Indicate for each of the following pairs of expressions (f(n), g(n)), whether f(n) is $O, \Omega, \text{ or } \Theta \text{ of } g(n).$ Prove your answers to the first two items, but just GIVE an answer to the last two.

(a) $f(n) = 4^{\log_4 n}$ and g(n) = 2n + 1.

 $f(n) \quad \bigcap \quad g(n)$ Answer for (a):

UT (SVH)-C FOL WSF MSZNHI C=1, K=1 2nH 43n (=3, K=

(b) $f(n) = n^2$ and $g(n) = (\sqrt{2})^{\log_2 n}$.

6= n=(2n+1) So n is o (2n+1) iff (n) is o (g (n) and g (n) is o f(n) then f(n) is o g(m) Answer for (b): $f(n) \subseteq g(n)$

f(n)=n2 g(n)=vn lets show that g(n)=f(n) Vn ≤ c. n2 for n≥k

VN S WZ

80 Jn is o (n2) and n2 is 1 (Jn)

(c) $f(n) = \log_2(n!)$ and $g(n) = n \log_2 n$.

Answer for (c):	f(n)	g(n)	

(d) $f(n) = n^k$ and $g(n) = c^n$ where k and c are constants and c > 1.

Answer for (d):	f(n) () $g(n)$
Allswer for (d).	$f(n) \qquad g(n)$

- 5. (9 points) Solve the following recurrence relations for integer n. If no solution exists, please explain the result.
 - (a) $T(n) = T(\frac{n}{2}) + 5$, T(1) = 1; assume n is a power of 2.

Answer for (a):	5/09 A+1
	02

(b) $T(n) = T(n-1) + \frac{1}{n}$, T(0) = 0.

Answer for (b):	No	solution	14 3
	0	harmonis	series o
	do	es not	conege

(c) Prove that your answer to part (a) is correct using induction.

Induction: Suppose
$$T(n) = Slog_2n + 1$$
for $n = 1/2$, ... $k - 1$ we must show
that $T(k) = Slog_2k + 1$
So $T(k) = T(k/2) + S$
from recursive def

recurse def:

$$T(N) = T(N_2) + 5$$

 $T(N) = 1$
 $T(N) = 1$
 $T(N) = 1$
 $T(N) = 1$
 $\log_2(K/2) = \log_2(K - \log_2 2$
 $T(N) = 5(\log_2(K/2) + 1) + 1$
 $= 5\log_2(K - 1) + 1$
 $= 5\log_2(K - 1) + 1$
 $= 10$

- 6. (10 points) Suppose function call parameter passing costs constant time, independent of the size of the structure being passed.
 - (a) Give a recurrence for worst case running time of the recursive Binary Search function in terms of n, the size of the search array. Assume n is a power of 2. Solve the recurrence.

Recurrence:	T(u)= T(n/2)+1
Base case:	T(1)=1
Recurrence Solution:	log2N+1

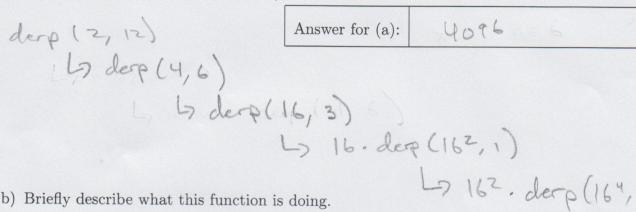
(b) Give a recurrence for worst case running time of the recursive Merge Sort function in terms of n, the size of the array being sorted. Solve the recurrence.

Recurrence:	T(n) = 27 (nb)+h
Base case:	T(1)=1
Running Time:	O(nlogan)

7. (10 points) Consider the pseudocode function below.

derp(x, n) if (n == 0)return 1; if (n % 2 == 0) return derp(x^2, n/2); return $x * derp(x^2, (n-1)/2);$

(a) What is the output when passed the following parameters: x = 2, n = 12? Show your work (activation diagram or similar).



(b) Briefly describe what this function is doing.

(c) Write a recurrence that models the running time of this function. Assume checks, returns, and arithmetic are constant time, but be sure to evaluate all function calls. Hint: what is the most n could be at each level of the recurrence?

(d) Solve the above recurrence for the running time of this function.