Indexing interlude: Bitvector Rank & Select: Primitives of succinct data structures



NOTE: This lecture is being recorded

Thinking theoretically about data structure size

Assume that storing some data, in an information-theoretically optimal manner, requires Z bits

Representation of this data is:

Implicit: Z + O(1) bits

Only a constant size larger than the theoretical minimum

Succinct: Z + o(Z) bits

Z bits, plus some term strictly smaller than Z bits

Compact: O(Z) bits

On the order of Z bits (grows linearly in Z)

Thinking theoretically about data structure size

The idea of succinct data structures was first introduced by Jacobson in his thesis "Succinct static data structures"*

In this thesis, among other things, he introduced succinct representations of trees and graphs that could be efficiently navigated.

As data sizes grow large, data structures that consume a lot of extra space become increasingly less feasible and so succinct data structures become increasingly important.

The *rank* and *select* operations become the basic building blocks of succinct data structures.

Slides for the following taken from: https://www.cs.helsinki.fi/u/puglisi/dct2015/slides10.pdf

credit to Simon J. Puglisi, University of Helsinki

Succinct Data Structures

- Succinct data structure
 - = succinct representation of data + a succinct index
- (usually static)
- High-level goal: reduce space so the data structure might fit in RAM and therefore be faster to use
- Examples
 - Sets
 - Trees, graphs
 - Strings
 - Permutations, functions

Succinct Representation

- A representation of data whose size (roughly) matches the information-theoretic lower bound
- If the input is taken from L distinct possible inputs, then its information-theoretic lower bound is ceil(log L) bits
 - To be considered succinct a data structure must use:
 ceil(logL) + o(logL) bits
- Example: a lower bound for a set S, subset of {1,2,...,n}
 - $-\log(2^n) = n$ bits
 - n = 3 we have 8 distinct sets... so d.s. will need at least 3 bits

Succinct Index

- Auxiliary data structure to support queries on the succinct representation
- Size: o(logL) bits
- The index should allow queries/operations on the succinct representation in (almost) the same time complexity as using a conventional data structure
 - This is the aim anyway
- Computational model is the word RAM
 - Assume word length w = loglogL
 - (this is the same pointer size as conventional data structures)
 - read/write w bits of memory in O(1) time
 - arithmetic/logical operations on w bit numbers take O(1) time
 - +,-,*,/,log,&,|,!,>>,<<

Binary rank and select

- The ability to answer *rank* and *select* queries over bit vectors (binary strings, bit arrays) is essential for implementing succinct data structures
- Given a binary string B[1..n]
 - $rank_B(i)$ returns the number of 1 bits in B[1..i]
 - select_B(i) returns the position of the ith 1 bit in B

Naïve rank

- To answer rank(i) scan B[1..i] and count 1-bits
- Simple but slow
 - O(i) time = O(n) time in the worst case
- How can we do better?
 - After all, what are we?

(Slightly) Less naïve rank

Store an table A[1..n], containing the rank answers

- A[i] = rank(i)
 - Now rank(i) takes constant time just an array lookup!
- Drawback:
 - A requires nlogn bits logn times the size of B not succinct!
 - We'd like a solution with O(1) queries and o(n) extra space...

We want O(1) queries with o(n) extra bits...

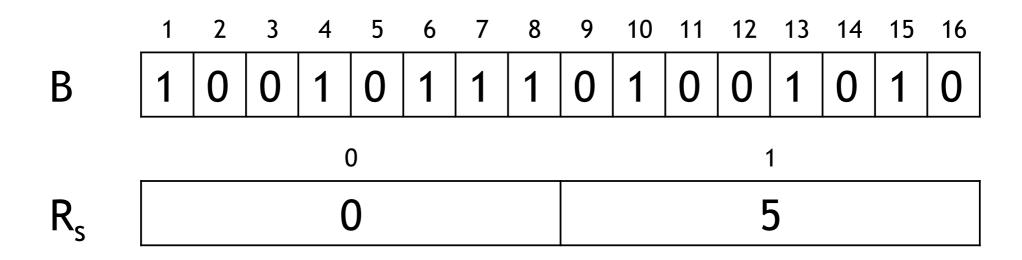
- General approach will be to precompute some tables
- Each table stores part of the answer to every query
 - For any given query, we can extract needed parts in O(1) time
 - The total size of the tables is o(n) bits

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
В	1	0	0	1	0	1	1	1	0	1	0	0	1	0	1	0

- Premise:
 - Can read O(logn) bits into an integer in range 1..n in O(1) time
 - However, to inspect each of those bits take O(logn) time

Tables: Superblocks

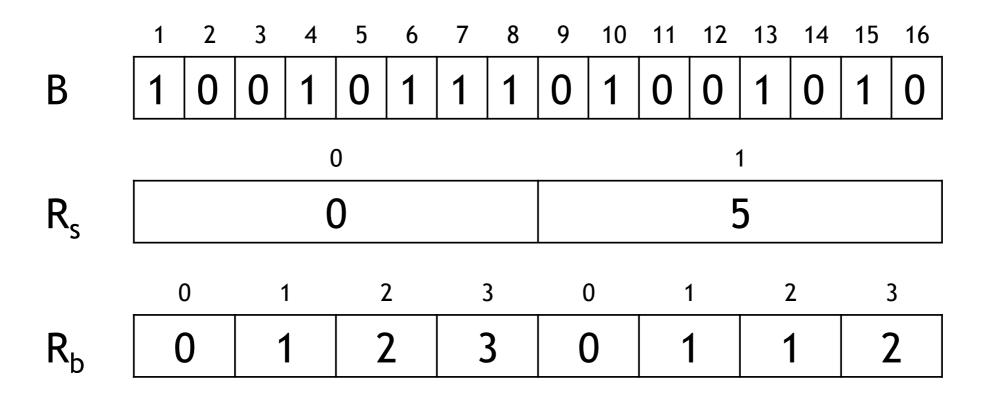
- Divide B into superblocks of size $s = log^2n/2 = 4*4/2 = 8$
- Build a small table R_s containing ranks for only some positions



Store in R_s[j] = rank_B(j*s), for all 0 ≤ j < n/s

Tables: Blocks

- Divide each superblock into blocks of size b = logn/2 = 2
- Build a table R_b which contains the rank from the start of each block to the start of its superblock

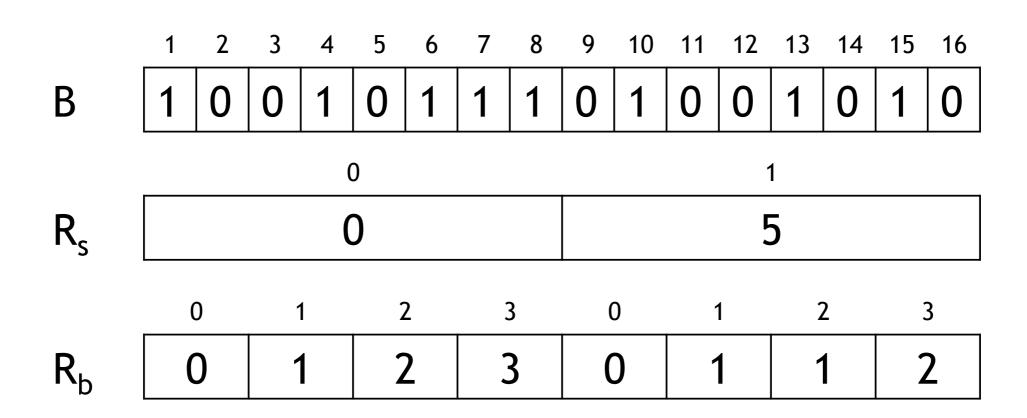


• Store $R_b[k/b] = rank_B(k*s) - rank_B(j*s)$, for all $0 \le k < n/b$

credit to Simon J. Puglisi, University of Helsinki

Intermission

• What we have so far (tables R_s and R_b) almost gets us the answer we're after



- $\operatorname{rank}_{B}(i) \approx R_{s}[i/s] + R_{b}[i/b]$
 - Just need to answer in-block queries in O(1) time

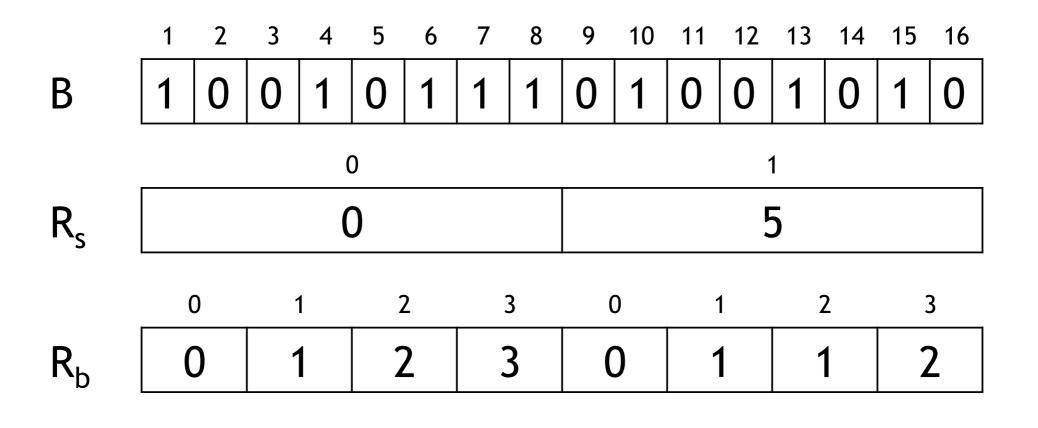
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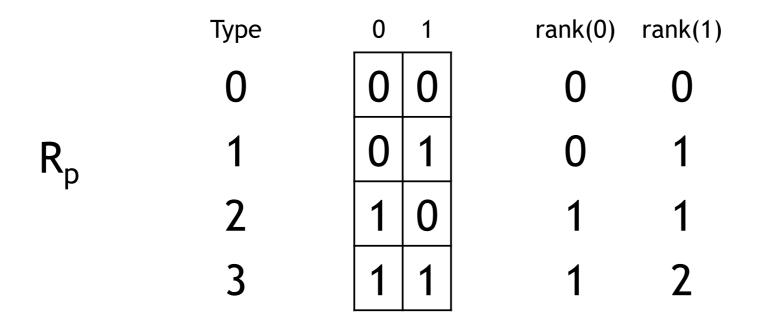
Tables: Resolving in-block queries

- Solution? Use another table!
- Blocks have size b = log₂n/2
 - There are 2^b such blocks possible
 - In each block there are b possible rank queries
 - Each answer (relative to the block) is in the range 1..b

	Туре	0	1	rank(0)	rank(1)
	0	0	0	0	0
R_{D}	1	0	1	0	1
r	2	1	0	1	1
	3	1	1	1	2

Final Data Structure





Size of table for within-block queries

- Blocks have size $b = log_2 n/2$
 - There are 2^b such blocks possible
 - In each block there are b possible rank queries
 - Each answer (relative to the block) is in the range 1..b

	Type	0	1	rank(0)	rank(1)
	0	0	0	0	0
R_{D}	1	0	1	0	1
P	2	1	0	1	1
	3	1	1	1	2

- Therefore size of R_p, the in-block data structure is
 - $2^b * b * logb = n^{1/2}*logn*loglogn/2 bits = o(n) bits$

Summing up sizes...

- The size of R_s, the superblock data structure is
 - 2n/log²n superblocks, each of size logn bits
 - $(n/\log^2 n)^*\log n = 2n/\log n$ bits = o(n) bits
- The size of R_b, the block data structure is
 - 2n/logn blocks, each of size loglogn bits
 - 2nloglogn/logn bits = o(n) bits
- $R_s + R_b + R_p = o(n)$ extra bits for O(1) time rank queries
 - It is possible to construct this data structure in O(n) time

Variations

- Just store R_s + use manual counting within superblocks
 - Saves space for R_b and R_p, takes time O(log²n) per query
- Store R_s and R_b + use manual counting within blocks
 - Saves only space for R_D, takes time O(logn) per query
- Use different superblock & block sizes
 - No more theoretical guarantees, but...
 - Perhaps faster in practice: blocks that are multiples of word sizes (32-bits) can be faster to handle

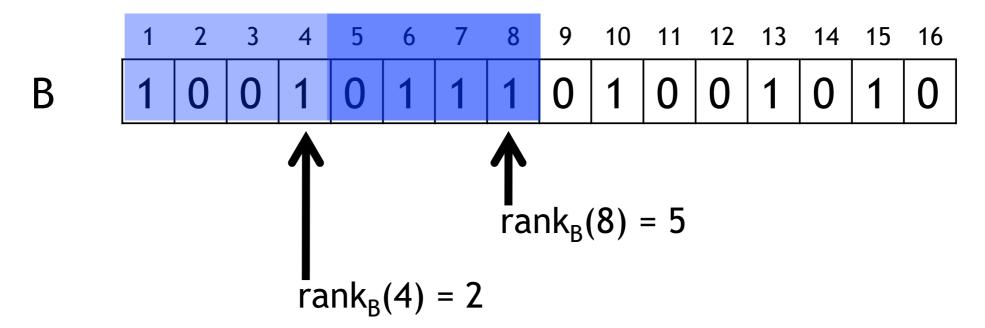
Summary of rank

- Rank index takes O(nloglogn/logn) = o(n) bits so we use n + o(n) overall and can answer queries in O(1) time
- While it is sublinear, we'd still like the o(n) term to be small
 - Best is by Patrastcu: $O(n/log^k n)$ bits, O(k) time queries
- Dynamic solutions exist
 - Queries no longer constant: O(logn/loglogn) time (Raman et al.)

Relationship to select(i)

- We can use our solution to rank to get a (fairly) efficient solution to select(i), with this observation:
- If rank(n/2) > i, then the ith 1-bit is in B[1..n/2]
 - Otherwise it is in B[n/2+1..n]

 $select_B(3)$



Relationship to select(i)

- Applying this idea recursively to arrive at select(i)
 - O(log₂n) time, o(n) space
- O(1) time, o(n) space solutions for select also exist
 - Slightly more complicated than O(1) rank
 - (Munro and Clark)
- Similar variations as we discussed with rank (trading space for query time) are also possible

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Rank and select: Another lesson learned

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Check for updates

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These rank & select operations work over a binary alphabet — can be extended

High-Order Entropy-Compressed Text Indexes

Roberto Grossi*

Ankur Gupta[†]

Jeffrey Scott Vitter[‡]

Introduces the idea of the wavelet tree, a versatile index that can be extended to arbitrary alphabets. We'll discuss the simplest of variants according to the exposition of:

Wavelet Trees for All *

Gonzalo Navarro

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Preliminaries

 $S[1,n] = s_1 s_2 \dots s_n$ is a sequence of symbols where s_i in Σ

 $\Sigma = [1 \dots \sigma]$ is an alphabet of symbols

Representing S requires $n * \lceil \lg \sigma \rceil = n * \lg \sigma + O(n)$ bits.

Wavelet tree: balanced binary tree with σ nodes, where each subtree is also a wavelet tree (i.e. it is recursive)

Preliminaries

Structure. A wavelet tree [54] for sequence S[1,n] over alphabet $[1..\sigma]$ can be described recursively, over a sub-alphabet range $[a..b] \subseteq [1..\sigma]$. A wavelet tree over alphabet [a..b] is a binary balanced tree with b-a+1 leaves. If a=b, the tree is just a leaf labeled a. Else it has an internal root node, v_{root} , that represents S[1,n]. This root stores a bitmap $B_{v_{root}}[1,n]$ defined as follows: if $S[i] \le (a+b)/2$ then $B_{v_{root}}[i] = 0$, else $B_{v_{root}}[i] = 1$. We define $S_0[1,n_0]$ as the subsequence of S[1,n] formed by the symbols $c \le (a+b)/2$, and $S_1[1,n_1]$ as the subsequence of S[1,n] formed by the symbols c > (a+b)/2. Then, the left child of v_{root} is a wavelet tree for $S_0[1,n_0]$ over alphabet $[a..\lfloor (a+b)/2\rfloor]$ and the right child of v_{root} is a wavelet tree for $S_1[1,n_1]$ over alphabet $[1+\lfloor (a+b)/2\rfloor..b]$.

Preliminaries

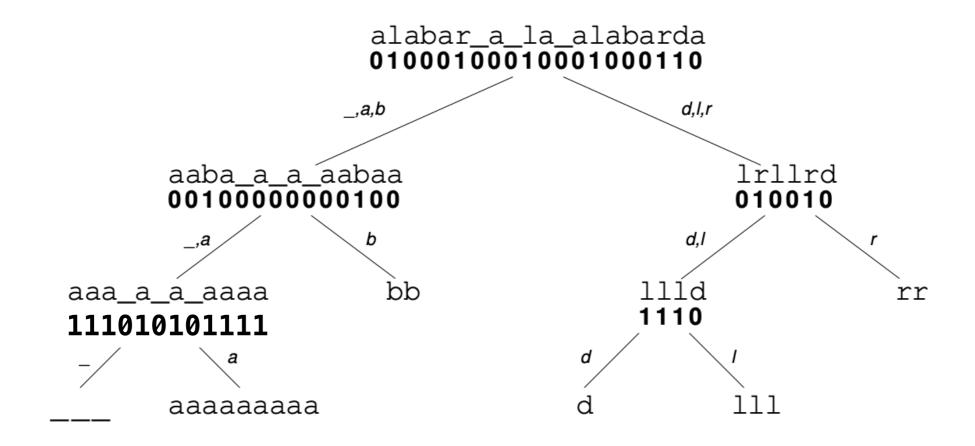
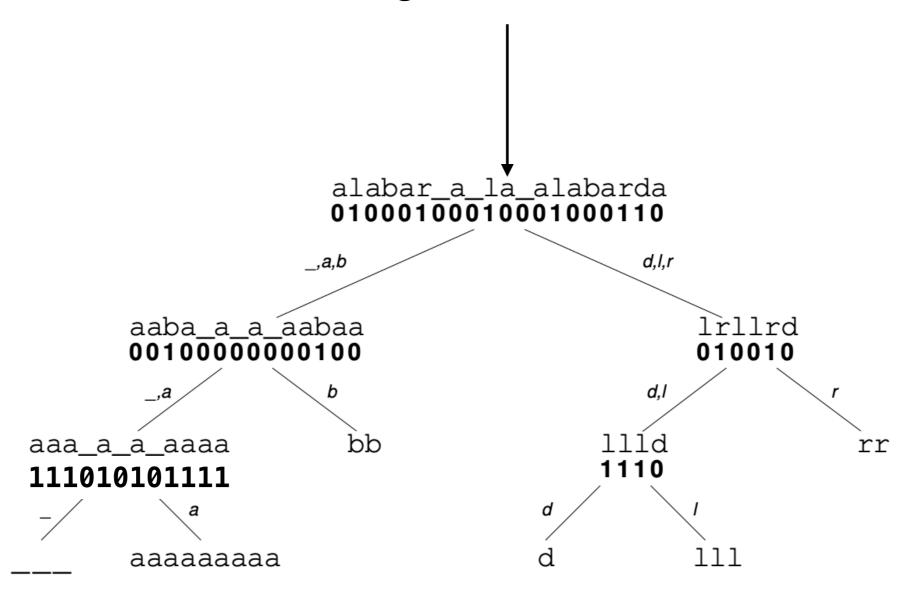
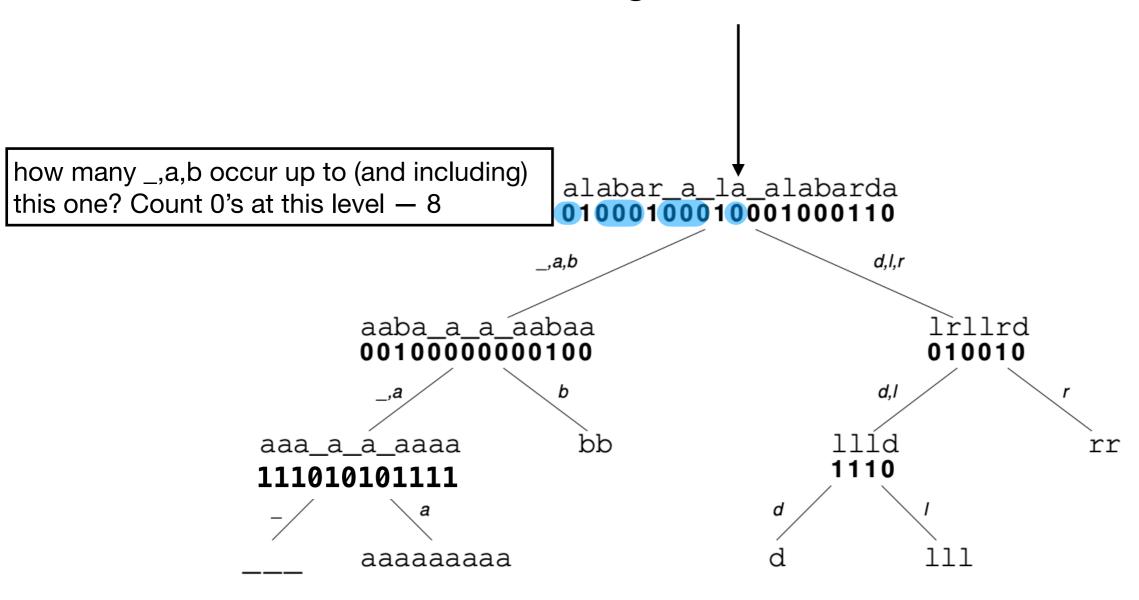
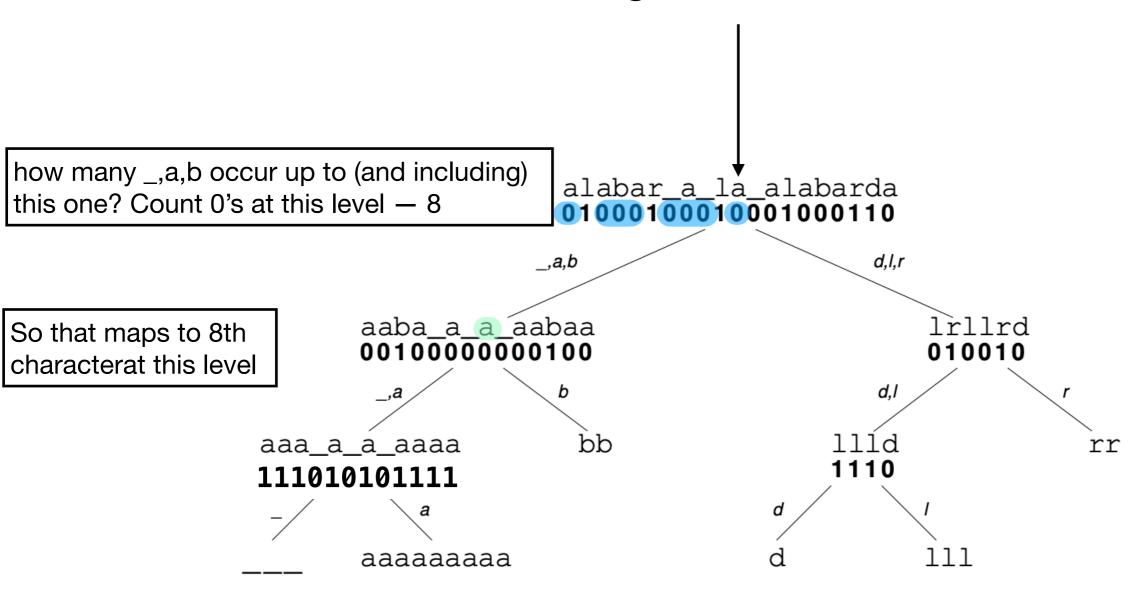
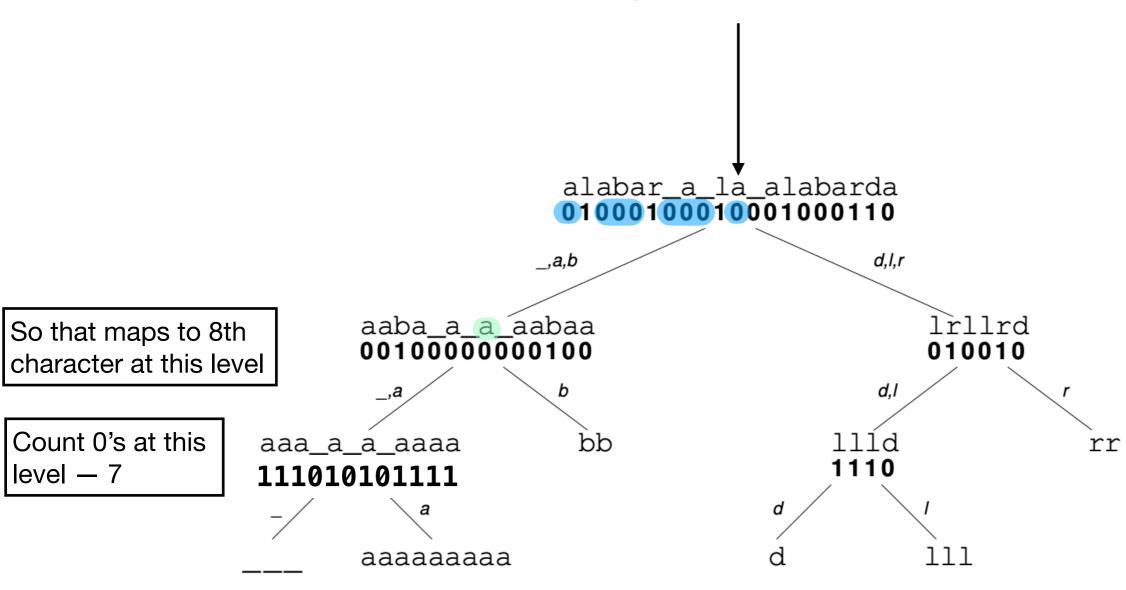


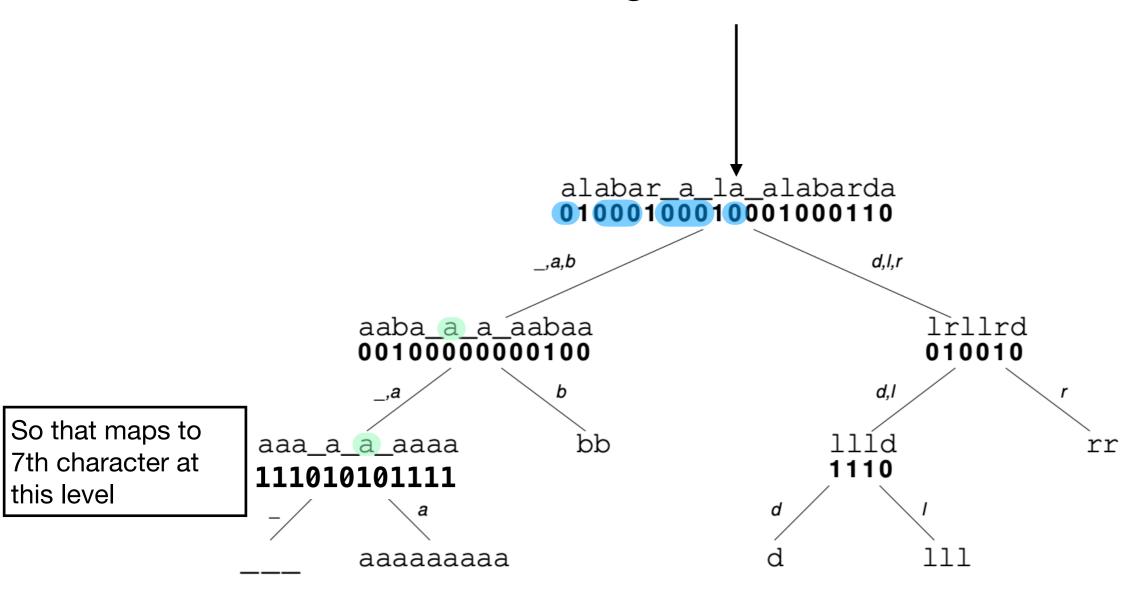
Fig. 1. A wavelet tree on string S = "alabar a la alabarda". We draw the spaces as underscores. The subsequences of S and the subsets of Σ labeling the edges are drawn for illustration purposes; the tree stores only the topology and the bitmaps.

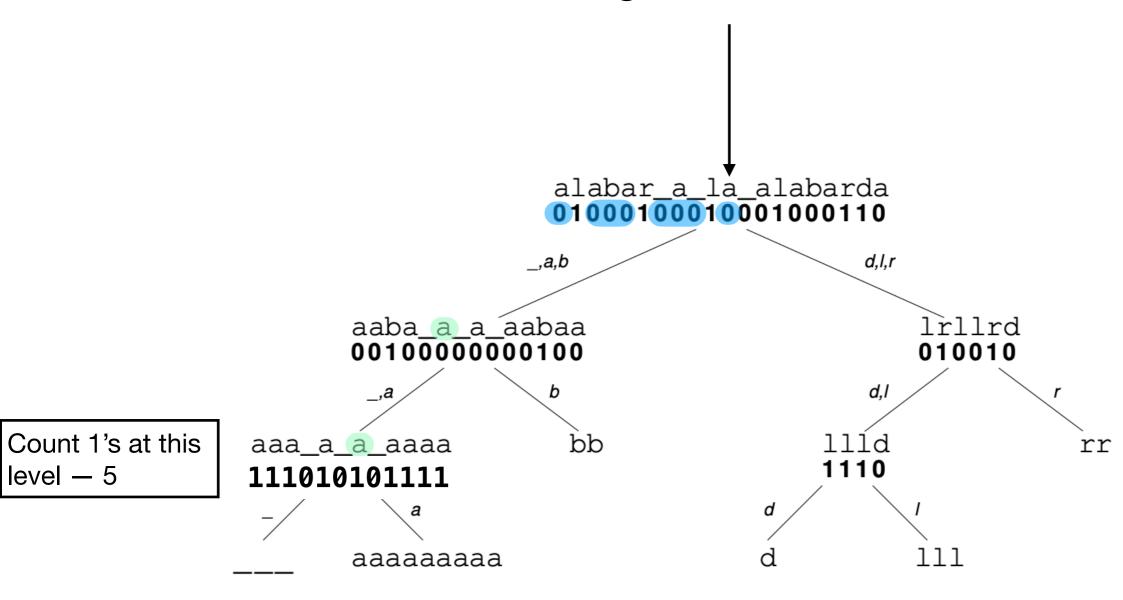


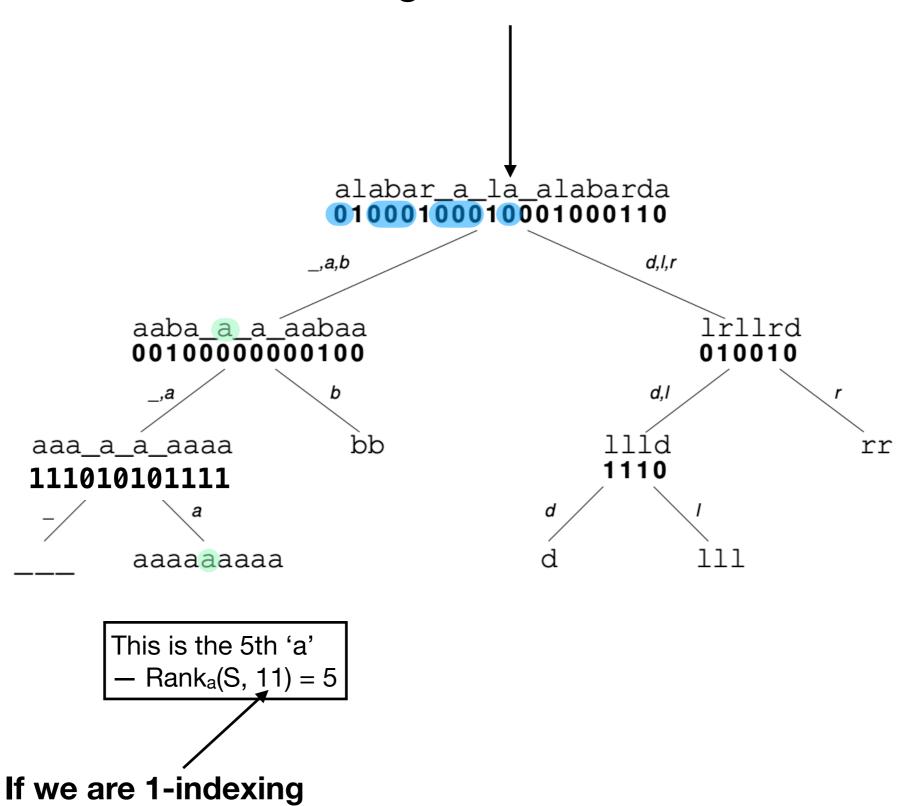




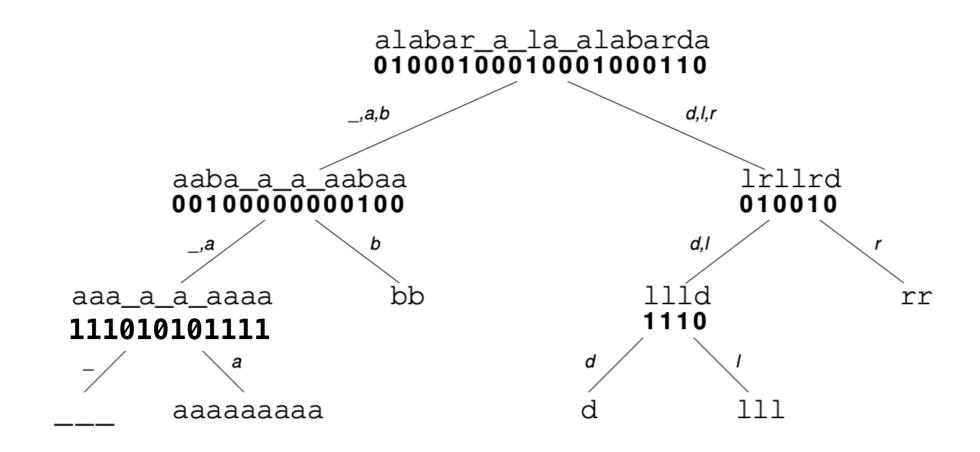






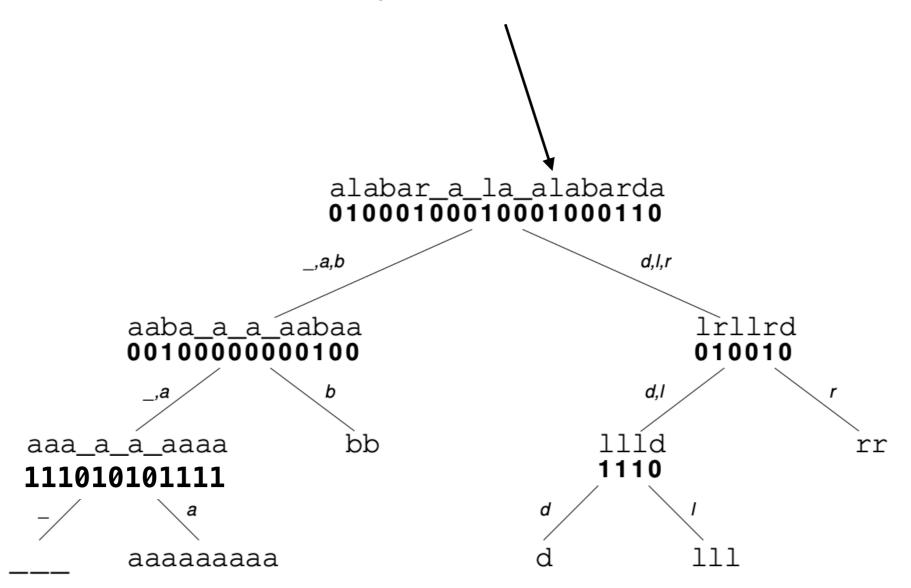


This procedure turns rank for any character in the alphabet into $\log \sigma$ rank calculations over bitvectors.

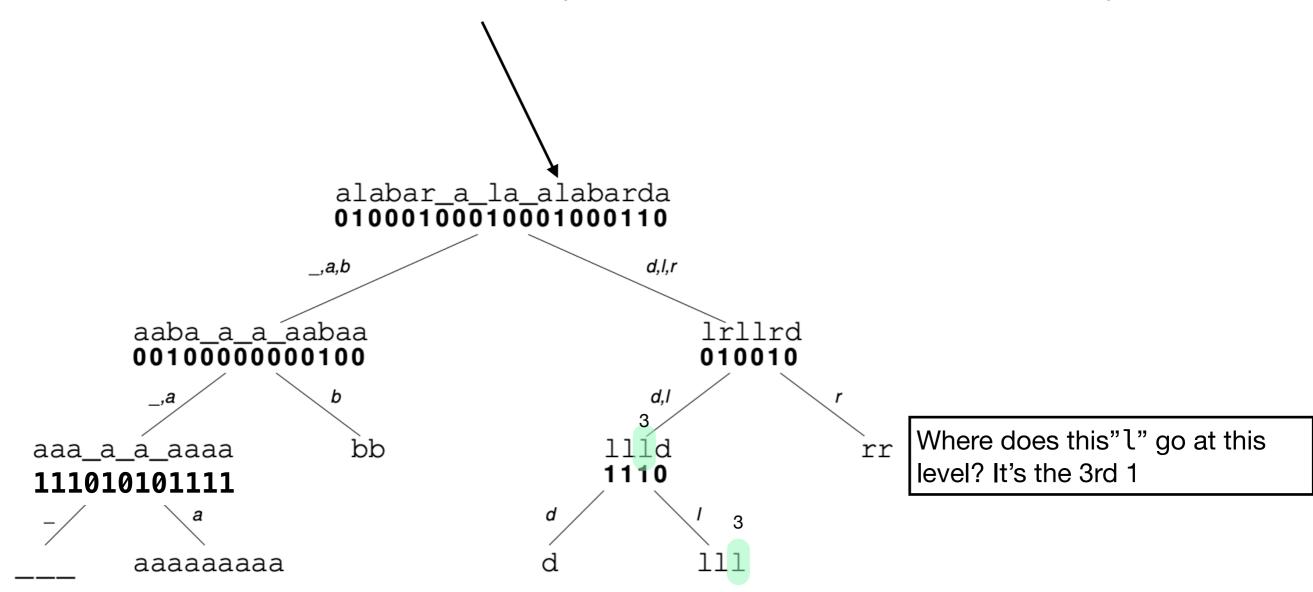


We can answer rank queries for an arbitrary character in $\log \sigma * O(1) = O(\log \sigma)$ time. For small, constant alphabets, through the magic of Big-O, this is *constant time*. :)

Select the 3rd "l" (at what index does it occur?)

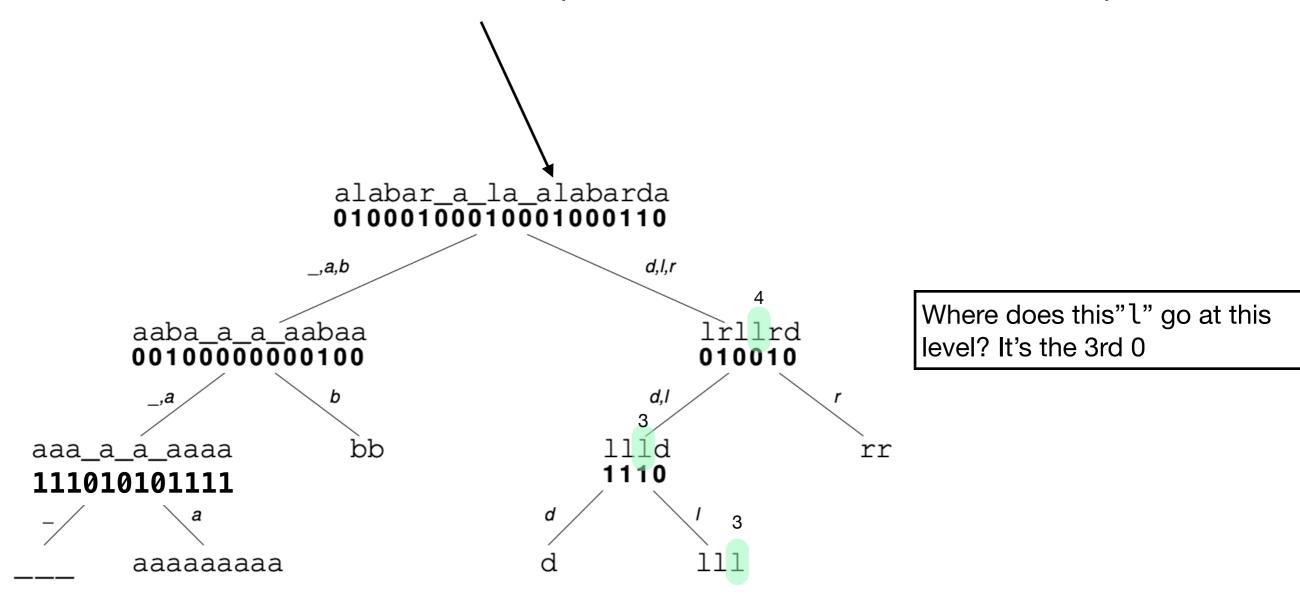


Select the 3rd "l" (at what index does it occur?)



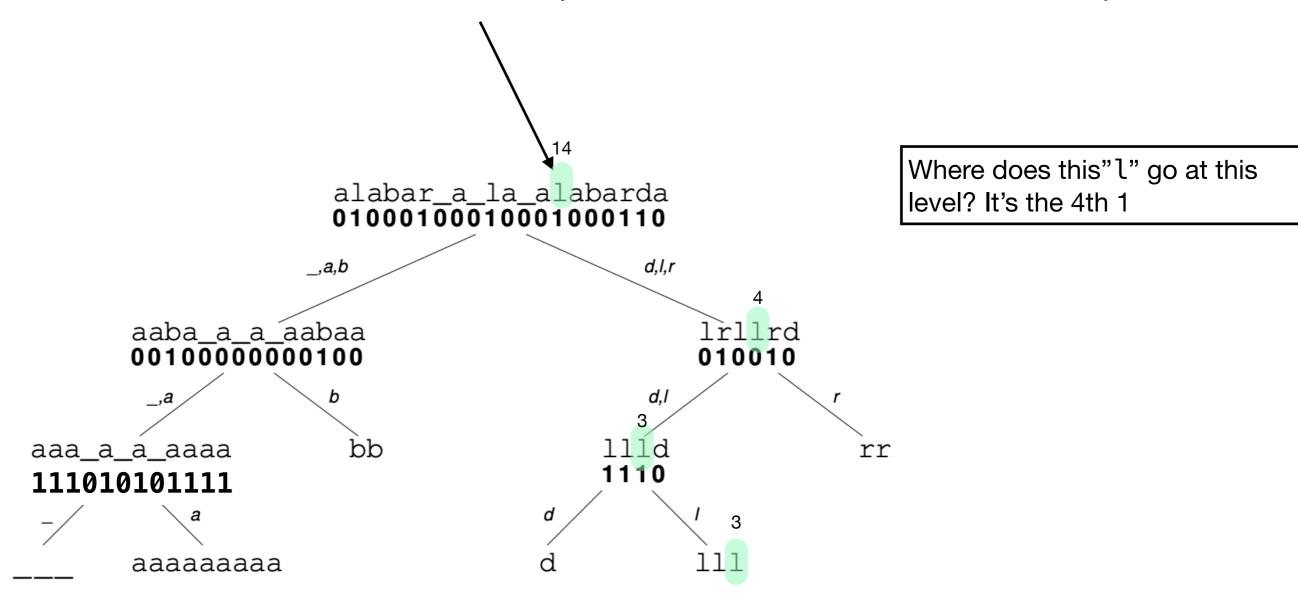
Here, we start at the bottom of the tree and work up.

Select the 3rd "1" (at what index does it occur?)



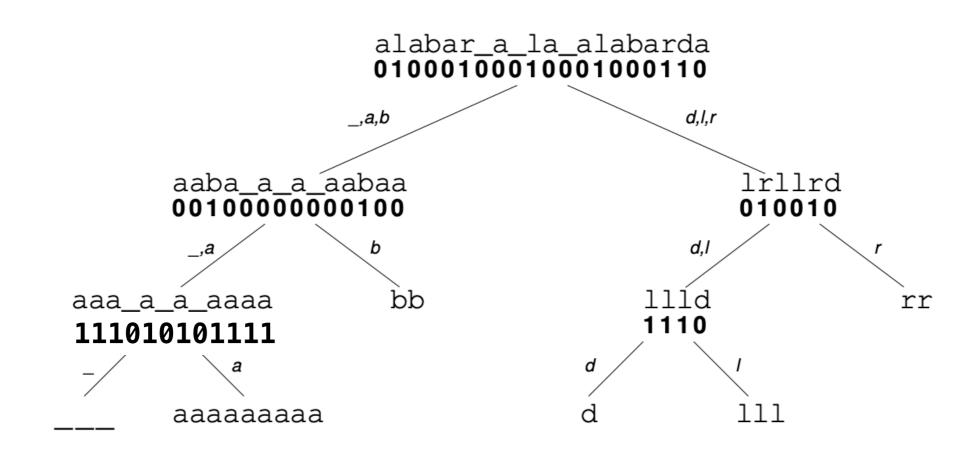
Here, we start at the bottom of the tree and work up.

Select the 3rd "1" (at what index does it occur?)



Here, we start at the bottom of the tree and work up.

This procedure turns select for any character in the alphabet into $lg\ \sigma$ select calculations over bitvectors.



We can answer select queries for an arbitrary character in $lg \sigma * O(1) = O(lg \sigma)$ time. For small, constant alphabets, through the magic of Big-O, this is *constant time*. :)

Succinct Data Structures

We have only scratched the surface on what is possible with rank & select and succinct data structures in general.

However, we'll assume familiarity with rank and select moving forward as we talk about data structures in Comp Bio that use them.

Gonzalo Navarro alone publishes 14-24 papers / year in this field :):

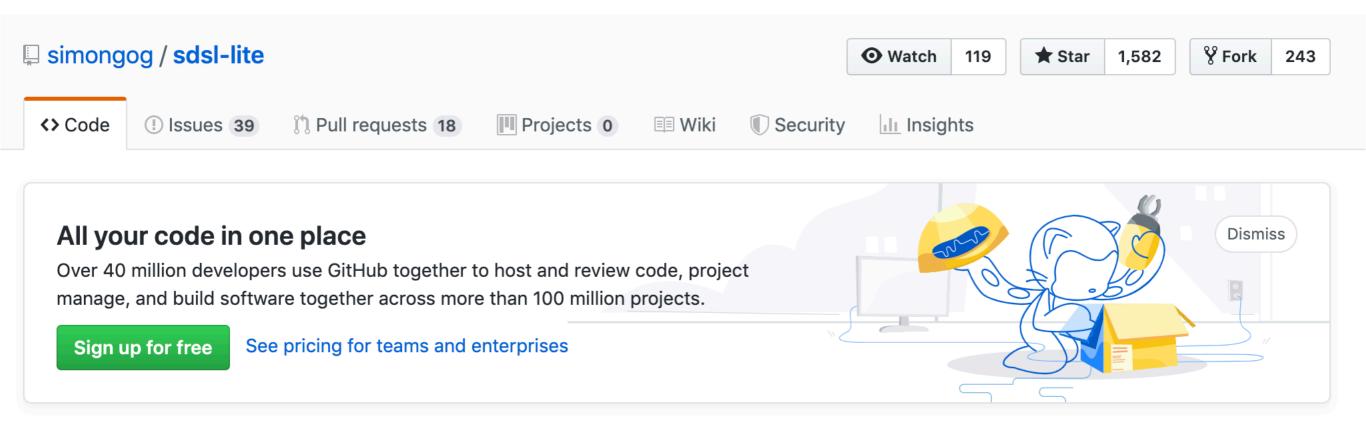
```
2019 (21) 2018 (14)
```

2017 (21) 2016 (19)

A google search on Gonzalo, and succinct data structures will send you down a wonderful rabbit-hole; I recommend you try it!

Succinct data structure papers tend to be quite theoretical (go figure!).

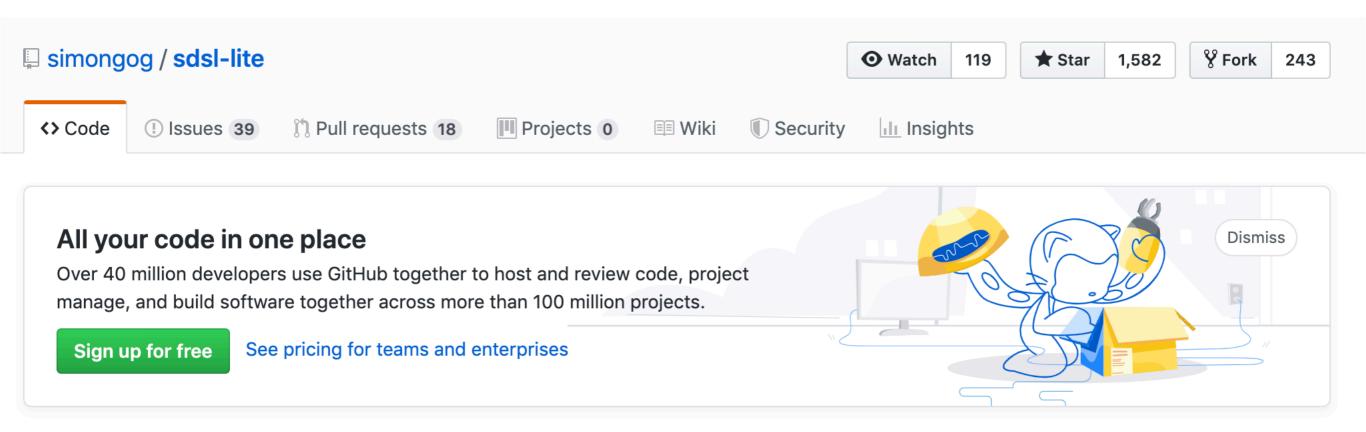
Luckily, there is a *go-to* library for implementation of these ideas.



Succinct Data Structure Library 2.0

Succinct data structure papers tend to be quite theoretical (go figure!).

Luckily, there is a go-to library for implementation of these ideas.



Succinct Data Structure Library 2.0

Provides a modern, modular C++ implementation of many different succinct data structures.

Create an FM-index over some text?

```
#include <sdsl/suffix_arrays.hpp>
#include <string>
#include <iostream>

string index_file = string(argv[1])+index_suffix;
csa_wt<wt_huff<rrr_vector<127> >, 512, 1024> fm_index;

if (!load_from_file(fm_index, index_file)) {
    ifstream in(argv[1]);
    if (!in) {
        cout << "ERROR: File " << argv[1] << " does not exist. Exit." << endl;
        return 1;
    }
    cout << "No index "<<index_file<" located. Building index now." << endl;
    construct(fm_index, argv[1], 1); // generate index
        store_to_file(fm_index, index_file); // save it
}</pre>
```

Perform rank queries over a bit vector?

```
#include <iostream>
#include <sdsl/bit_vectors.hpp>
using namespace std;
using namespace sdsl;
int main()
    bit_vector b = bit_vector(8000, 0);
    for (size_t i=0; i < b.size(); i+=100)</pre>
        b[i] = 1;
    rank_support_v<1> b_rank(&b);
    for (size_t i=0; i<=b.size(); i+= b.size()/4)</pre>
        cout << "(" << i << ", " << b_rank(i) << ") ";
    cout << endl;</pre>
}
```

How about select₀

```
#include <iostream>
#include <sdsl/bit_vectors.hpp>
using namespace std;
using namespace sdsl;
int main()
{
    bit_vector b = \{0,1,0,1,1,1,0,0,0,1,1\};
    size_t zeros = rank_support_v<0>(&b)(b.size());
    bit_vector::select_0_type b_sel(&b);
    for (size_t i=1; i <= zeros; ++i) {</pre>
        cout << b_sel(i) << " ";
    cout << endl;</pre>
}
```

You get the idea! An incredibly powerful library, at your fingertips.

sds Cheat Sheet

Data structures

The library code is in the sdsl namespace. Either import the namespace in your program (using namespace sdsl;) or qualify all identifieres by a sdsl::-prefix.

Each section corresponds to a header file. The file is hyperlinked as part of the section heading.

We have two types of data structures in sdsl. Self-contained and support structures. A support object s can extend a self-contained object o (e.g. add functionality), but requires access to o. Support structures contain the substring support in their class names.

Integer Vectors (IV)

The core of the library is the class $\operatorname{int_vector} < w >$. Parameter w corresponds to the fixed length of each element in bits. For w=8,16,32,64,1 the length is fixed during compile time and the vectors correspond to $\operatorname{std}:\operatorname{vector} < \operatorname{uint} w_- \operatorname{t} > \operatorname{resp.}$ std::vector $<\operatorname{bool}>$. If w=0 (default) the length can be set during runtime. Constructor: $\operatorname{int_vector} < (n,x,\ell)$, with n equals size, x default integer value, ℓ width of integer (has no effect for w>0).

Public methods: operator[i], size(), width(), data().

Manipulating int_vector < w > v

Method	Description
v[i] = x	Set entry $v[i]$ to x .
$v.width(\ell)$	Set width to ℓ , if $w = 0$.
v.resize(n)	Resize v to n elements.
Useful methods in nar	mespace sdsl::util:
$set_{to_value(v,k)}$	Set $v[i]=k$ for each i .
set_to_id(v)	Set $v[i]=i$ for each i .
set_random_bits(v)	Set elements to random bits.
mod(v, m)	Set $v[i]=v[i] \mod m$ for each i .
<pre>bit_compress(v)</pre>	Gets $x = \max_{i} \mathbf{v}[i]$ and $\ell = \lceil \log(x-1) \rceil + 1$
	and packs the entries in ℓ -bit integers.
$expand_width(v,\ell)$	Expands the width of each integer to &
	bits, if $\ell > v$, width().

Compressed Integer Vectors (CIV)

For a vector \mathbf{v} , $\mathbf{enc_vector}$ stores the self-delimiting coded deltas ($\mathbf{v}[i+1]-\mathbf{v}[i]$). Fast random access is achieved by sampling values of \mathbf{v} at rate $\mathbf{t_dens}$. Available coder are \mathbf{coder} ::elias_delta, \mathbf{coder} ::elias_gamma, and \mathbf{coder} ::fibonacci.

Class vlc_vector stores each v[i] as self-delimiting codeword. Samples at rate t_dens are inserted for fast random access.

Class dac_vector stores for each value x the least (t_b-1) significant bits plus a bit which is set if $x \ge 2^{b-1}$. In the latter case, the process is repeated with $x' = x/2^{b-1}$.

Bitvectors (BV)

Representations	for a bitvector of length n	with m set bits.
Class	Description	Space
bit_vector	plain bitvector	64[n/64+1]
bit_vector_il	interleaved bitvector	$\approx n(1+64/K)$
rrr_vector	H_0 -compressed bitvector	$\approx \lceil \log \binom{n}{m} \rceil$
sd_vector	sparse bitvector	$\approx m \cdot (2 + \log \frac{n}{m})$
hyb_vector	hybrid bitvector	116

bit_vector equals int_vector<1> and is therefore dynamic.
Public Methods: operator[i], size(), begin(), end()
Public Types: rank_1_type, select_1_type, select_0_type¹.
Each bitvector can be constructed out of a bit_vector object.

Rank Supports (RS)

RSs add rank functionality to BV. Methods rank(i) and operator(i) return the number of set bits² in the prefix [0..i) of the supported BV for $i \in [0, n]$.

Class	$Compatible\ BV$	+Bits	Time
rank_support_v	bit_vector	0.25n	$\mathcal{O}(1)$
rank_support_v5	bit_vector	0.0625n	$\mathcal{O}(1)$
rank_support_scan	bit_vector	64	$\mathcal{O}(n)$
rank_support_il	bit_vector_il	128	$\mathcal{O}(1)$
rank_support_rrr	rrr_vector	80	$\mathcal{O}(k)$
rank_support_sd	sd_vector	64	$O(\log \frac{n}{m})$
rank_support_hyb	hyb_vector	64	-
CT 11			

Call util::init_support(rs,bv) to initialize rank structure rs to bitvector bv. Call rs(i) to get rank(i) = $\sum_{k=0}^{k < 0} \text{bv}[k]$

Select Supports (SLS)

SLSs add select functionality to BV. Let m be the number of set bits in BV. Methods select(i) and operator(i) return the position of the i-th set bit³ in BV for $i \in [1..m]$.

Class	Compatible BV	+Bits	Time
select_support_mcl	bit_vector	$\leq 0.2n$	$\mathcal{O}(1)$
select_support_scan	bit_vector	64	$\mathcal{O}(n)$
select_support_il	bit_vector_il	64	$\mathcal{O}(\log n)$
select_support_rrr	rrr_vector	64	$\mathcal{O}(\log n)$
select_support_sd	sd_vector	64	$\mathcal{O}(1)$
Call util::init_suppo	ort(sls,bv) to in	nitialize sl	ls to bitvecto

Call util::init_support(sls,bv) to initialize sls to bitvecto bv. Call sls(i) to get select(i) = $\min\{j \mid \text{rank}(j+1) = i\}$.

Wavelet Trees (WT=BV+RS+SLS)

Wavelet trees represent sequences over byte or integer alphabets of size σ and consist of a tree of BVs. Rank and select on the sequences is reduced to rank and select on BVs, and the runtime is multiplied by a factor in $[H_0, \log \sigma]$.

Class Shape lex ordered Default Travers-

Ciass	Snape	lex_ordered	alphabet	able	opening/closing
wt_rlmn	underl	ying WT depen	dent	×	Class
wt_gmr	none	×	integer	×	bp_support_g
wt_ap	none	×	integer	×	bp_support_gg
wt_huff	Huffman	×	byte	✓	bp_support_sad
wm_int	Balanced	×	integer	✓	Public methods:
wt_blcd	Balanced	✓	byte	✓	double_enclose
wt_hutu	Hu-Tucker	✓	byte	✓	select(i).
wt_int	Balanced	✓	integer	✓	Call util::init
Public typ	es: value_ty	pe, size_type, a	and node_ty	pe (if WT is	bit_vector bv.

Suffix Arrays (CSA=IV+WT)

Compressed suffix arrays use CIVs or WTs to represent the suffix arrays (SA), its inverse (ISA), BWT, Ψ , and LF. CSAs can be built over byte and integer alphabets.

can be built over byte and integer alphabets.

Class

Description

csa_bitcompressed

Based on SA and ISA stored in a IV.

csa_sada

Based on Ψ stored in a CIV.

csa_wt

Based on the BWT stored in a WT.

Public methods: operator[i], size(), begin(), end().

Public members: isa, bwt, lf, psi, text, L, F, C, char2comp, comp2char, sigma.

Policy classes: alphabet strategy (e.g. byte_alphabet, succinct_byte_alphabet, int_alphabet) and SA sampling strategy (e.g. sa_order_sa_sampling, text_order_sa_sampling)

Longest Common Prefix (LCP) Arrays

Class	Description
lcp_bitcompressed	Values in a int_vector<>.
lcp_dac	Direct accessible codes used.
lcp_byte	Small values in a byte; 2 words per large
lcp_wt	Small values in a WT; 1 word per large.
lcp_vlc	Values in a vlc_vector.
<pre>lcp_support_sada</pre>	Values stored permuted. CSA needed.
<pre>lcp_support_tree</pre>	Only depths of CST inner nodes stored.
<pre>lcp_support_tree2</pre>	+ large values are sampled using LF.
Public methods: open	rator[i], $size()$, $begin()$, $end()$

Balanced Parentheses Supports (BPS)

We represent a sequence of parentheses as a bit_vector. An opening/closing parenthesis corresponds to 1/0.

Class Description

bp_support_g Two-level pioneer structure.

bp_support_gad Multi-level pioneer structure.

bp_support_sada Min-max-tree over excess sequence.

Public methods: find_open(i), find_close(i), enclose(i), double_enclose(i,j), excess(i), rr_enclose(i,j), rank(i)^4, select(i).

Call util::init_support(bps,bv) to initialize a BPS bps to

You get the idea! An incredibly powerful library, at your fingertips.

Suffix Trees (CST=CSA+LCP+BPS)

A CST can be parametrized by any combination of CSA ,LCP, and BPS. The operation of each part can still be accessed through member varaibles. The additional operations are listed below. CSTs can be built for byte or integer alphabets. ClassDescription

cst_sada Represents a node as position in BPS. Navigational operations are fast (they are directly translated in BPS operations on the DFS-BPS). Space: 4n+o(n)+|CSA|+|LCP| bits.

cst_sct3 Represents nodes as intervals. Fast construction, but slower navigational operations. Space: 3n +o(n) + |CSA| + |LCP|

Public types: node_type. In the following let v and w be nodes and i, d, lb, rb integers.

Public methods: size(), nodes(), root(), begin(), end(), $begin_bottom_up(), end_bottom_up, size(v), is_leaf(v),$ $degree(v), depth(v), node_depth(v), edge(v, d), lb(v),$ rb(v), id(v), $inv_id(i)$, sn(v), $select_leaf(i)$, node(lb)rb), parent(v), sibling(v), lca(v, w), select_child(v, i), child(v, c), children(v), sl(v), wl(v, c), $leftmost_leaf(v), rightmost_leaf(v)$

Public members: csa, lcp.

The traversal example shows how to use the DFS-iterator.

Range Min/Max Query (RMQ)

A RMQ rmq can be used to determine the position of the minimum value⁵ in an arbitrary subrange [i, j] of an preprocessed vector v. Operator operator (i,j) returns $x = \min\{\mathbf{r} | r \in [i, j] \land \mathbf{v}[r] \le \mathbf{v}[k] \ \forall k \in [i, j]\}$

Class	Space	Time
rmq_support_sparse_table	$n \log^2 n$	$\mathcal{O}(1)$
rmq_succint_sada	4n + o(n)	$\mathcal{O}(1)$
rmq_succint_sct	2n + o(n)	$\mathcal{O}(1)$

Constructing data structures

Let o be a WT-, CSA-, or CST-object. Object o is built with construct(o,file,num_bytes=0) from a sequence stored in file. File is interpreted dependent on the value of num_bytes: ValueFile interpreted as

num_bytes=0 serialized int_vector<>.

num_bytes=1 byte sequence of length util::file_size(file)

num_bytes=2 16-bit word sequence.

num_bytes=4 32-bit word sequence.

num_bytes=8 64-bit word sequence.

num_bytes=d Parse decimal numbers.

Note: construct writes/reads data to/from disk during construction. Accessing disk for small instances is a considerable overhead. construct_im(o,data,num_bytes=0) will build o using only main memory. Have a look at this handy tool for an example.

Configuring construction

The locations and names of the intermediate files can be configured by a cache_config object. It is constructed by cache_config(del,tmp_dir,id, map) where del is a boolean variable which specifies if the intermediate files should be deleted after construction, tmp_dir is a path to the directory

where the intermediate files should be stored, id is used as part of the file names, and map contains a mapping of keys (e.g. conf::KEY_BWT, conf::KEY_SA,...) to file paths.

The cache_config parameter extends the construction method to: construct(o,file,config,num_bytes).

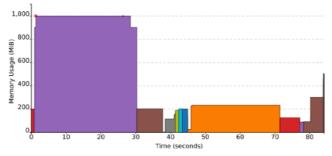
The following methods (key is a key string, config represent a cache_config object, and o a sdsl object) should be handy in customized construction processes:

cache_file_name(key,config) cache_file_exists(key,config) register_cache_file(key,config) load_from_cache(o,key,config) store_to_cache(o,key,config)

Resource requirements

Memory: The memory peak of CSA and CST construction occurs during the SA construction, which is 5 times the texts size for byte-alphabets and inputs < 2 GiB (see the Figure below for a 200 MB text) and 9 times for larger inputs. For integer alphabets the construction takes about twice the space of the resulting output.

Time: A CST construction processes at about 2 MB/s. The Figure below shows the resource consumption during the construction of a cst_sct3<> CST for 200 MB English text. For a detailed description of the phases click on the figure.



This diagram was generated using the sample program memory-visualization.cpp.

Reading and writing data

Importing data into sdsl structures

load_vector_from_file(v, file, num_bytes) Load file into an int_vector v. Interpretation of file depends on num_bytes; see method construct.

Store sds structures

Use store_to_file(o, file) to store an sdsl object o to file. Object o can also be serialized into a std::ostream-object out Notes by the call o.serialize(out).

Load sdsl structures

Use load_from_file(o, file) to load an sdsl object o, which is stored in file. Call o.load(in) reads o from std::istream-object in.

Utility methods

More useful methods in the sdsl::util namespace:

MethodDescription

Id of current process. pid()

id() Get unique id inside the process. basename(p) Get filename part of a path p. dirname(p) Get directory part of a path p.

demangle(o) Demangles output of typeid(o).name(). demangle2(o) Simplifies output of demangle. E.g. removes

sdsl::-prefixes, ...

to_string(o) Transform object o to a string.

assign(o1,o2) Assign o1 to o2, or swap o1 and o2 if the objects

are of the same type.

clear(o) Set o to the empty object.

Measuring and Visualizing Space

size_in_bytes(o) returns the space used by an sdsl object o. Call write_structure<JSON_FORMAT>(o,out) to get a detailed space breakdown written in JSON format to stream out. <HTML_FORMAT> will write a HTML page (like this), which includes an interactive SVG-figure.

Methods on words

Class bits contains various fast methods on a 64-bit word x. Here the most important ones.

MethodDescription

bits::cnt(x)Number of set bits in x.

bits::sel(x,i) Position of i-th set bit, $i \in [0, cnt(x) - 1)$. Position of least significant set bit. bits::lo(x)

bits::hi(x)Position of most significant set bit.

Note: Positions in x start at 0. lo and hi return 0 for x = 0.

Tests

A make test call in the test directory, downloads test inputs, compiles tests, and executes them.

Benchmarks

Directory benchmark contains configurable benchmarks for various data structure, like WTs, CSAs/FM-indexes (measuring time and space for operations count, locate, and extract).

Debugging

You get the gdb command pv <int_vector> <idx1> <idx2>, which displays the elements of an int_vector in the range [idx1, idx2] by appending the file sdsl.gdb to your .gdbinit.

Cheatsheet template provided by Winston Chang http://www.stdout.org/~winston/latex/

- 1 select_0_type not defined for sd_vector.
- 2 It is also possible to rank 0 or the patterns 10 and 01.
- 3 It is also possible to select 0 or the patterns 10 and 01.
- 4 For PBS the bits are counted in the prefix [0..i].
- 5 Or maximum value; can be set by a template parameter.