Introduction to Alignment, Mapping and Indexing

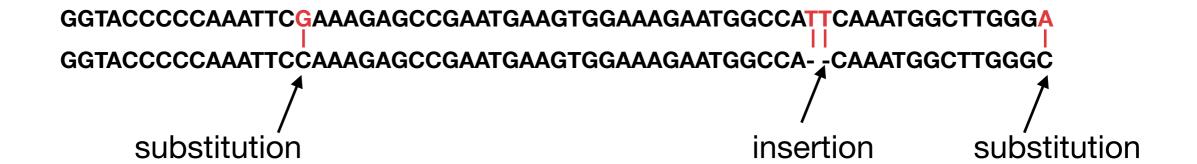


GGTACCCCCAAATTCGAAAGAGCCGAATGAAGTGGAAAGAATGGCCATTCAAATGGCTTGGGA

TCTGTGTGAAGATTTTTAGCTGTCTGTCGGACTTGGGGGGTCTCAGGGAAACTCACTTTGCCCCCCAGCTGAGGTTTTCAGGAAATCTGGAAACCTACAG GCCGAGCCTGTCTCAGCTCCACACACGCTTGGGAGCTGCAGATGCCTCCGCCCCTCCTCTCTCCCAGGCTCTTCCTGCCGTTGAACCCCGGCGGCGGCG TCTCGGCCAGCGGCGCGCCCTGGTACCCCCAAATTCCAAAGAGCCGAATGAAGTGGAAAGAATGGCCACAAATGGCTTGGGCCCGAGTGACCATGGGAT GGTTAGGTAGGATTTTAGAGGCGACTGCTCCTGGAATTAGAGAAAGAGTTTCATTACAACCGCTACCTGACCCGAAGGCACTCGGGCCCATGCCTTCCT CTCCTTCGCTGTTTGATTTCTATTCTGTTTAGCCTGAGTTGGAGATGCCGGAGGTGCCGTGGTGGAAGAAGTCTTGAACGAATTTGGAGGCGTCTCCGT GGCAGCTAAGCGAGCACGGGTTCTGCTGGTGCAGGATGACACTGGCAGCCACTGCCGCGGACTTGTATCTCTTGTCTTCCTGCTTTTATAGAGAATAGA GGACTGTCTGGGGAGCGCCTCGTAGCCATAGAATTCCACCGCCGCCGCCGCCGCCGCGTAGTCGTACTTGAAGCCGAGCGCAGGCGGGTGGTTCATTAACT CTGACTTTGCCTTTGATTTTGCTCGACCTCTGCTTCGTCAAAATCTGGTTTCAGAATCGAAGGATGAAGATGAAAAAGATGAATAAAGGAGGAAAAAGGA AGAAAACAAGGACTAAGCAAAAAAAGAAAGACCCCCCCTATAGCAGGATTTTAAAATTTTTCTCTTTTTTCTAAGATTATTGCAAGGCGAGCGTGG TCACGTATACAATACAAAGTACTTGGACCAGGAACAGGGTCTTTAATCCTTATTTGACACGAAAACGTCGGATTGAAGTCTCTCATGCCCAACTAGTGG TAAACCCTACCCAGCCTGCTGCCTCAGCACAGCCAAGGGAAAATCAGCAAGGGCTATGCTGTGATTCTGTCTCTGAGTGACTTGGACCACTGTTGATTT TTATTTTTTTTTTTTTTTTTTCTCCTATAGCAGGATTTTAAAATCGGGCCCACCTTAACTCGGGAGGGCCGCGCGCTGAGGCTGGGAGCCGGAGATTCGGGC GAGGGCAGTGTCTGCGGGGCGCGGTCGCGCAGCTCCCCGGGCGAGCCAGGTGCAGCCTTGGCGGGGGTCTGTTTGGTGGGCGATGTCACCATTTCCCGCC GCCGCCGTCGCCACCGCCGCCGCCGCCGCGTAGTCGTACTTGAATAGCTGGACATAAAGACAAATGACAAAAAATTATTATTATAGATATTTTGGTC TGTGTGTTATGTCCTAAGGTGTTTTGTCTGCAGTTTGAGAGCATGTTGCTGGTAGCCTGAGTTGGAGAT

GGTACCCCCAAATTCGAAAGAGCCGAATGAAGTGGAAAGAATGGCCATTCAAATGGCTTGGGA

TCTGTGTGAAGATTTTTAGCTGTCTGTCGGACTTGGGGGGTCTCAGGGAAACTCACTTTGCCCCCCAGCTGAGGTTTTCAGGAAATCTGGAAACCTACAG GCCGAGCCTGTCTCAGCTCCACACACGCTTGGGAGCTGCAGATGCCTCCGCCCCTCCTCTCTCCCAGGCTCTTCCTGCCGTTGAACCCCGGCGGCGGCG TCTCGGCCAGCGGCGCGCCCTGGTACCCCCAAATTCCAAAGAGCCGAATGAAGTGGAAAGAATGGCCACAAATGGCTTGGGCCCGAGTGACCATGGGAT GGTTAGGTAGGATTTTAGAGGCGACTGCTCCTGGAATTAGAGAAAGAGTTTCATTACAACCGCTACCTGACCCGAAGGCACTCGGGCCCATGCCTTCCT CTCCTTCGCTGTTTGATTTCTATTCTGTTTAGCCTGAGTTGGAGATGCCGGAGGTGCCGTGGTGGAAGAAGTCTTGAACGAATTTGGAGGCGTCTCCGT GGCAGCTAAGCGAGCACGGGTTCTGCTGGTGCAGGATGACACTGGCAGCCACTGCCGCGGACTTGTATCTCTTGTCTTCCTGCTTTTATAGAGAATAGA GGACTGTCTGGGGAGCGCCTCGTAGCCATAGAATTCCACCGCCGCCGCCGCCGCCGCGTAGTCGTACTTGAAGCCGAGCGCAGGCGGGTGGTTCATTAACT CTGACTTTGCCTTTGATTTTGCTCGACCTCTGCTTCGTCAAAATCTGGTTTCAGAATCGAAGGATGAAGATGAAAAAGATGAATAAAGGAGGAAAAAGGA AGAAAACAAGGACTAAGCAAAAAAAGAAAGACCCCCCCTATAGCAGGATTTTAAAATTTTTCTCTTTTTTCTAAGATTATTGCAAGGCGAGCGTGG TCACGTATACAATACAAAGTACTTGGACCAGGAACAGGGTCTTTAATCCTTATTTGACACGAAAACGTCGGATTGAAGTCTCTCATGCCCAACTAGTGG TAAACCCTACCCAGCCTGCTGCCTCAGCACAGCCAAGGGAAAATCAGCAAGGGCTATGCTGTGATTCTGTCTCTGAGTGACTTGGACCACTGTTGATTT TTATTTTTTTTTTTTTTTTTTCTCCTATAGCAGGATTTTAAAATCGGGCCCACCTTAACTCGGGAGGGCCGCGCGCTGAGGCTGGGAGCCGGAGATTCGGGC GAGGGCAGTGTCTGCGGGGCGCGGTCGCGCAGCTCCCCGGGCGAGCCAGGTGCAGCCTTGGCGGGGGTCTGTTTGGTGGGCGATGTCACCATTTCCCGCC GCCGCCGTCGCCACCGCCGCCGCCGCCGCGTAGTCGTACTTGAATAGCTGGACATAAAGACAAATGACAAAAAATTATTATTATAGATATTTTGGTC TGTGTGTTATGTCCTAAGGTGTTTTGTCTGCAGTTTGAGAGCATGTTGCTGGTAGCCTGAGTTGGAGAT



GGTACCCCAAATTCGAAAGAGCCGAATGAAGTGGAAAGAATGGCCATTCAAATGGCTTGGGAGGTACCCCCAAATTCCAAAGAGCCGAATGAAGTGGAAAGAAGAATGGCCA--CAAATGGCTTGGGC

substitution insertion substitution

Given: A reference text (e.g. genome) and a query (e.g. read)

Find: The location in the reference with the "most similarity" / "smallest distance" to the query.

The Language of Strings

A string s is a finite sequence of characters

|s| denotes the length of the string — the number of characters in the sequence.

A string is defined over an alphabet, Σ

```
\begin{split} &\Sigma_{DNA} = \{A,T,C,G\} \\ &\Sigma_{RNA} = \{A,U,C,G\} \\ &\Sigma_{AminoAcid} = \{A,R,N,D,C,E,Q,G,H,I,L,K,M,F,P,S,T,W,Y,V\} \end{split}
```

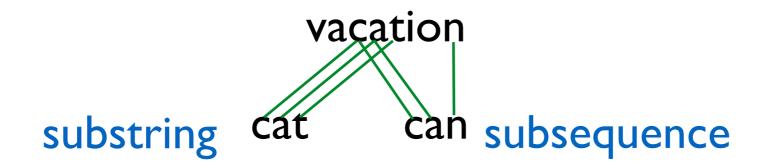
The empty string is denoted $\epsilon - |\epsilon| = 0$

The Language of Strings

Given two strings $\mathbf{s,t}$ over the same alphabet Σ , we denote the concatenation as \mathbf{st} — this is the sequence of \mathbf{s} followed by the sequence of \mathbf{t}

String **s** is a substring of **t** if there exist two (potentially empty) strings **u** and **v** such that $\mathbf{t} = \mathbf{usv}$

String $\bf s$ is a subsequence of $\bf t$ if the characters of $\bf s$ appear in order (but not necessarily consecutively) in $\bf t$



String **s** is a prefix/suffix of **t** if t = su/us — if neither **s** nor **u** are ϵ , then **s** is a proper prefix/suffix of **t**

+

The Simplest String Comparison Problem

Given: Two strings

$$a = a_1 a_2 a_3 a_4 ... a_m$$

 $b = b_1 b_2 b_3 b_4 ... b_n$

where a_i , b_i are letters from some alphabet, Σ , like {A,C,G,T}.

Compute how similar the two strings are.

What do we mean by "similar"?

Edit distance between strings a and b = the smallest number of the following operations that are needed to transform a into b:

- mutate (replace) a character
- delete a character
- insert a character

$$riddle \xrightarrow{delete} ridle \xrightarrow{mutate} riple \xrightarrow{insert} triple$$

The String Alignment Problem

Parameters:

- "gap" is the cost of inserting a "-" character, representing an insertion or deletion (insertion/deletion are dual operations depending on the string)
- cost(x,y) is the cost of aligning character x with character y. In the simplest case, cost(x,x) = 0 and cost(x,y) = mismatch penalty.

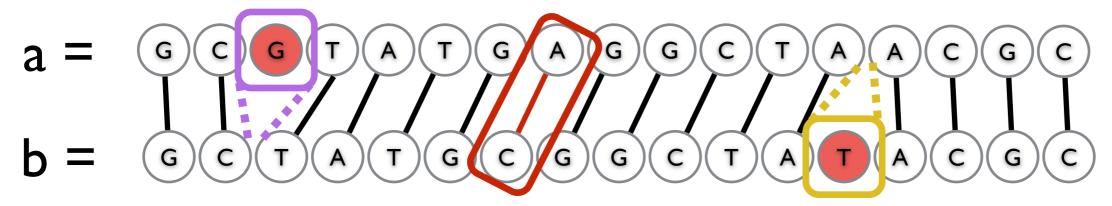
Goal:

- Can compute the edit distance by finding the **lowest cost** alignment. (often phrased as finding **highest scoring alignment**.)
- Cost of an alignment is: sum of the cost(x,y) for the pairs of characters that are aligned + $gap \times$ number of characters inserted.

Another View: Alignment as a Matching

Each string is a set of nodes, one for each character.

Looking for a low-cost matching (pairing) between the sequences.



The operations at our disposal

Insertion (into a ~ deletion from b)

Mutation

Deletion (from $a \sim insertion into b$)

When we "delete a" character in $\bf a$ this is the same as inserting the character "-" in $\bf b$. Conceptually, you can think of this as aligning the deleted character with "-". Under this model cost(x,'-') = cost('-',x) = gap for any $\bf x \in \Sigma$

Another View: Alignment as a Matching

Each string is a set of nodes, one for each character.

Looking for a low-cost matching (pairing) between the sequences.

$$a = GCGTATGAGGCTAAACGC$$

$$b = GCTATGCGGCTATACGC$$

Cost of a matching is:

$$gap \times #unmatched + \sum_{(a_i,b_j)} cost(a_i,b_j)$$

Edges are not allowed to cross!

Representing alignments as edit transcripts

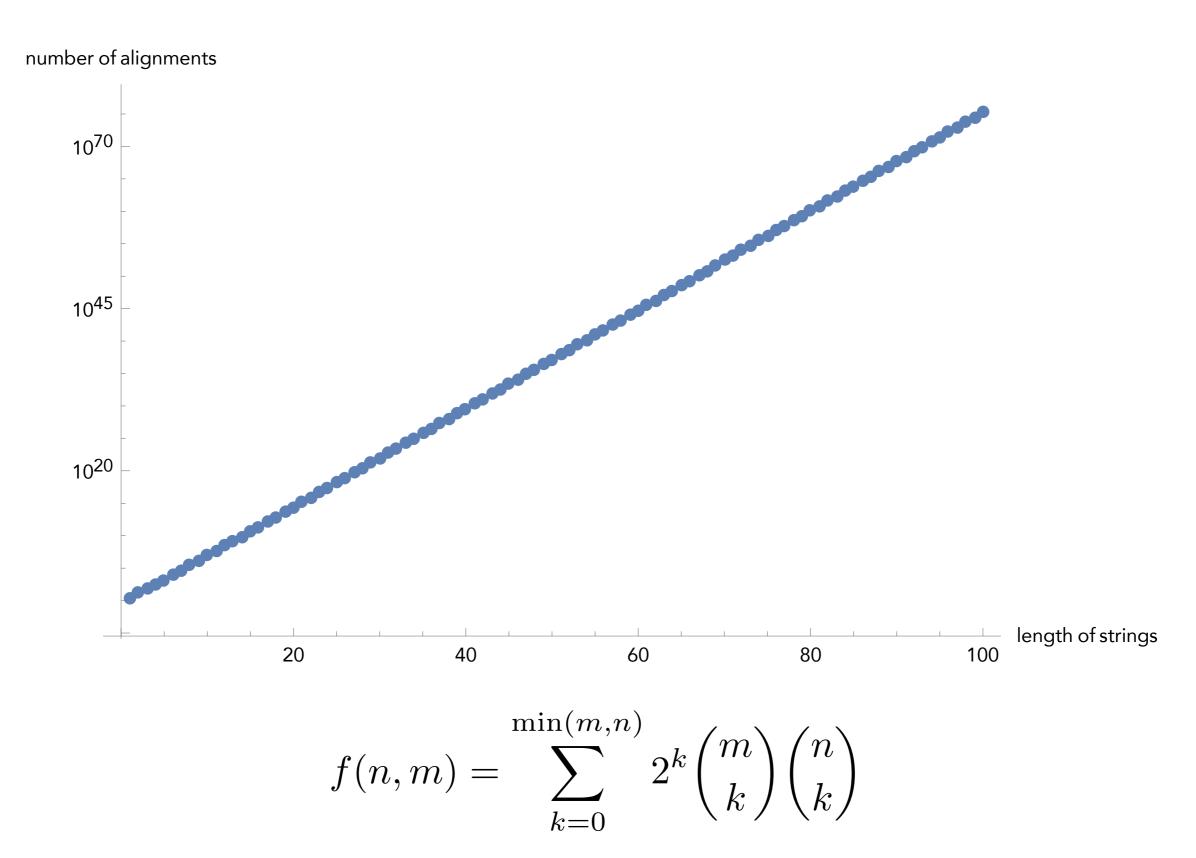
Can think of edits as being introduced by an *optimal editor* working left-to-right. *Edit transcript* describes how editor turns *x* into *y*.

```
Operations:
x: G'CGTATGCGGCTAACGC
                                  M = match, R = replace,
y: GCT♠TGCGGCTATACGC
                                  I = insert into x, D = delete from x
x: GCGTATGCGGCTAACGC
                                 MMD
y: GC-TATGCGGCTATACGC
y: GC-TATGCGGCTATACG
y: GC-TATGCGGCTATACGC
```

Representing edits as alignments

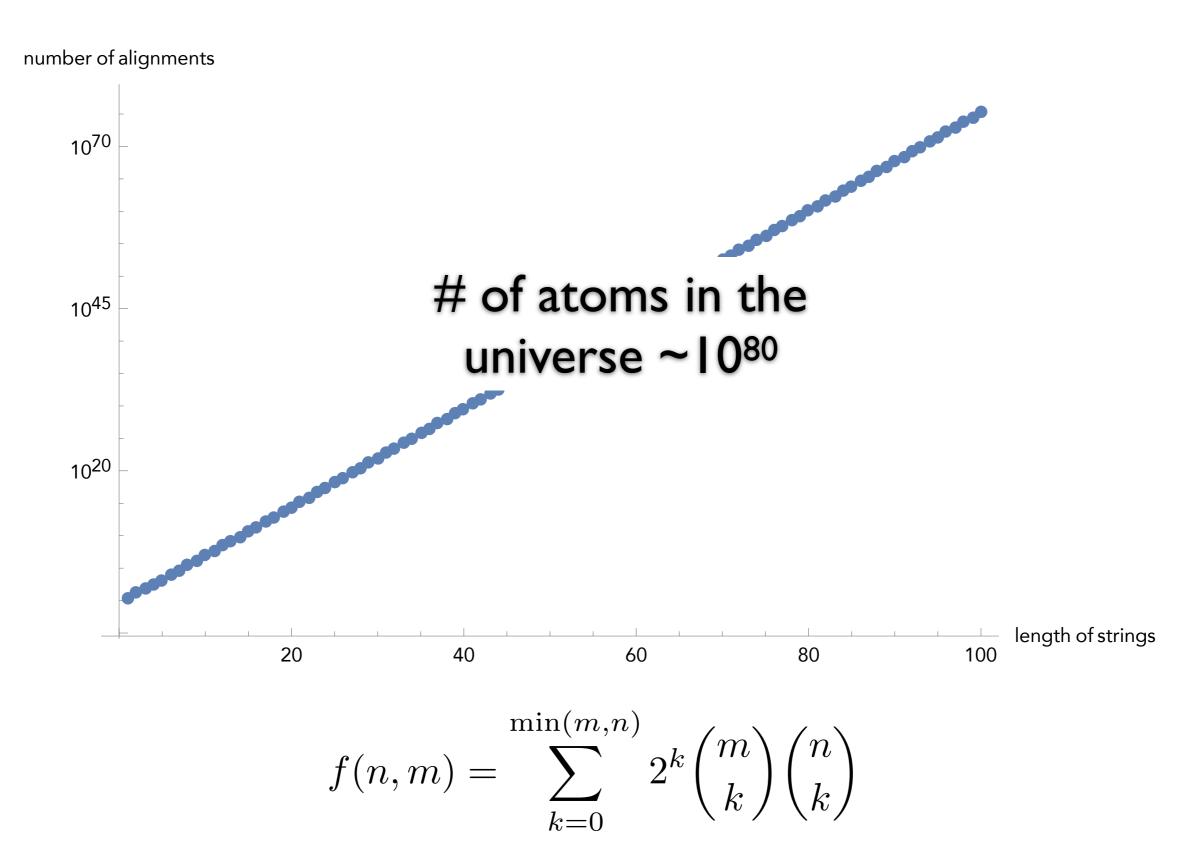
```
prin-ciple
                         prin-cip-le
prinncipal
                         prinncipal-
(1 gap, 2 mm)
                          (3 gaps, 0 mm)
MMMMIMMMRR
                         MMMMTMMTMD
misspell
                          prehistoric
mis-pell
                          ---historic
 (1 gap)
                          (3 gaps)
MMMTMMMM
                          DDDMMMMMMM
aa-bb-ccaabb
                         al-go-rithm-
                          XX X
ababbbc-a-b-
                         alKhwariz-mi
(5 gaps, 1 mm)
                          (4 gaps, 3 mm)
MRIMMIMDMDMD
                         MMIRRIMMRDMI
```

How many alignments are there?



Andrade, Helena, et al. "The number of reduced alignments between two DNA sequences." BMC bioinformatics 15.1 (2014): 94.

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Algorithm for Computing Edit Distance

Consider the last characters of each string:

$$a = a_1 a_2 a_3 a_4 ... a_m$$

 $b = b_1 b_2 b_3 b_4 ... b_n$

One of these possibilities must hold:

- 1. (a_m,b_n) are matched to each other
- 2. a_m is not matched at all
- 3. b_n is not matched at all
- 4. a_m is matched to some b_i ($j \ne n$) and b_n is matched to some a_k ($k \ne m$).

Algorithm for Computing Edit Distance

Consider the last characters of each string:

$$a = a_1 a_2 a_3 a_4 ... a_m$$

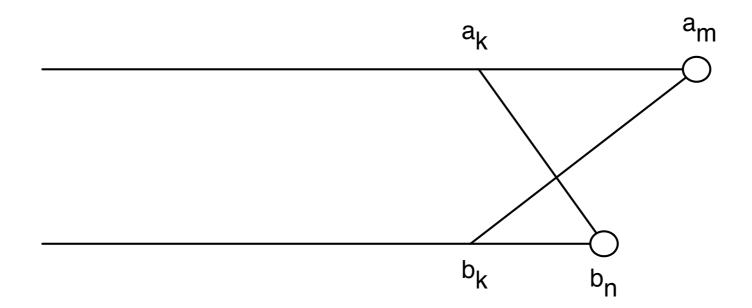
 $b = b_1 b_2 b_3 b_4 ... b_n$

One of these possibilities must hold:

- 1. (a_m,b_n) are matched to each other
- 2. a_m is not matched at all
- 3. b_n is not matched at all
- 4. a_m is matched to some b_j ($j \neq n$) and b_n is matched to some a_k ($k \neq m$).

No Crossing Rule Forbids #4

4. a_m is matched to some b_j ($j \neq n$) and b_n is matched to some a_k ($k \neq m$).



So, the only possibilities for what happens to the last characters are:

- 1. (a_m, b_n) are matched to each other
- 2. a_m is not matched at all
- 3. b_n is not matched at all

Recursive Solution

Turn the 3 possibilities into 3 cases of a recurrence:

$$OPT(i,j) = \min egin{cases} \cos t(a_i,b_j) + OPT(i-1,j-1) & \operatorname{match}\ a_i,b_j \ \operatorname{gap} + OPT(i-1,j) & a_i & \operatorname{is not matched}\ \operatorname{gap} + OPT(i,j-1) & b_j & \operatorname{is not matched}\ \operatorname{gap} + \operatorname{optimal}\ \operatorname{alignment}\ \operatorname{between}\ a_1...a_i & \operatorname{and}\ b_1...b_j & \operatorname{the costs of smaller}\ \operatorname{problems} \end{cases}$$

Key: we don't know which of the 3 possibilities is the right one, so we try them all.

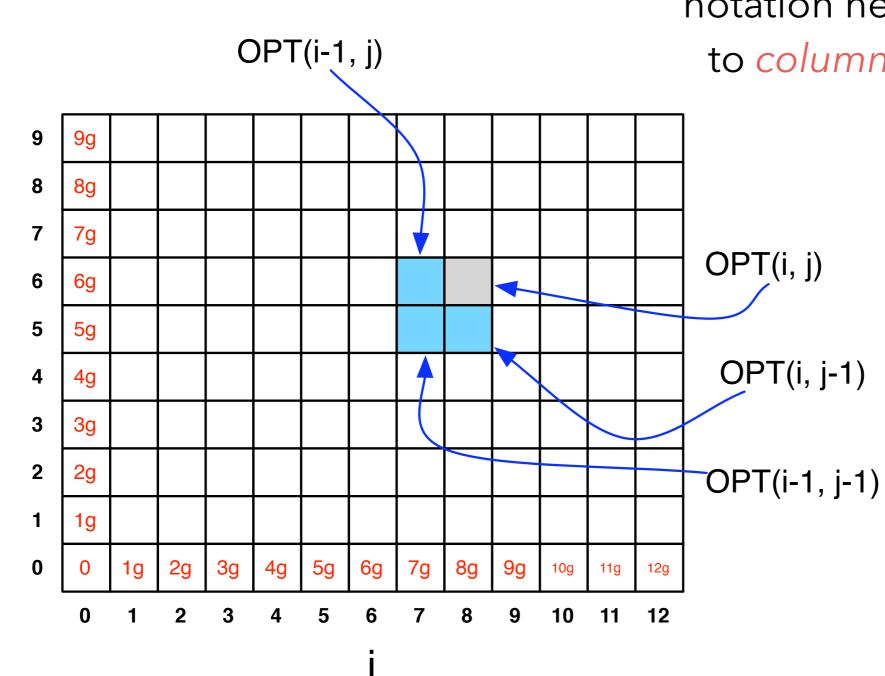
Base case:
$$OPT(i,0) = i \times gap$$
 and $OPT(0,j) = j \times gap$.

(Aligning *i* characters to o characters must use *i* gaps.)

Computing OPT(i,j) Efficiently

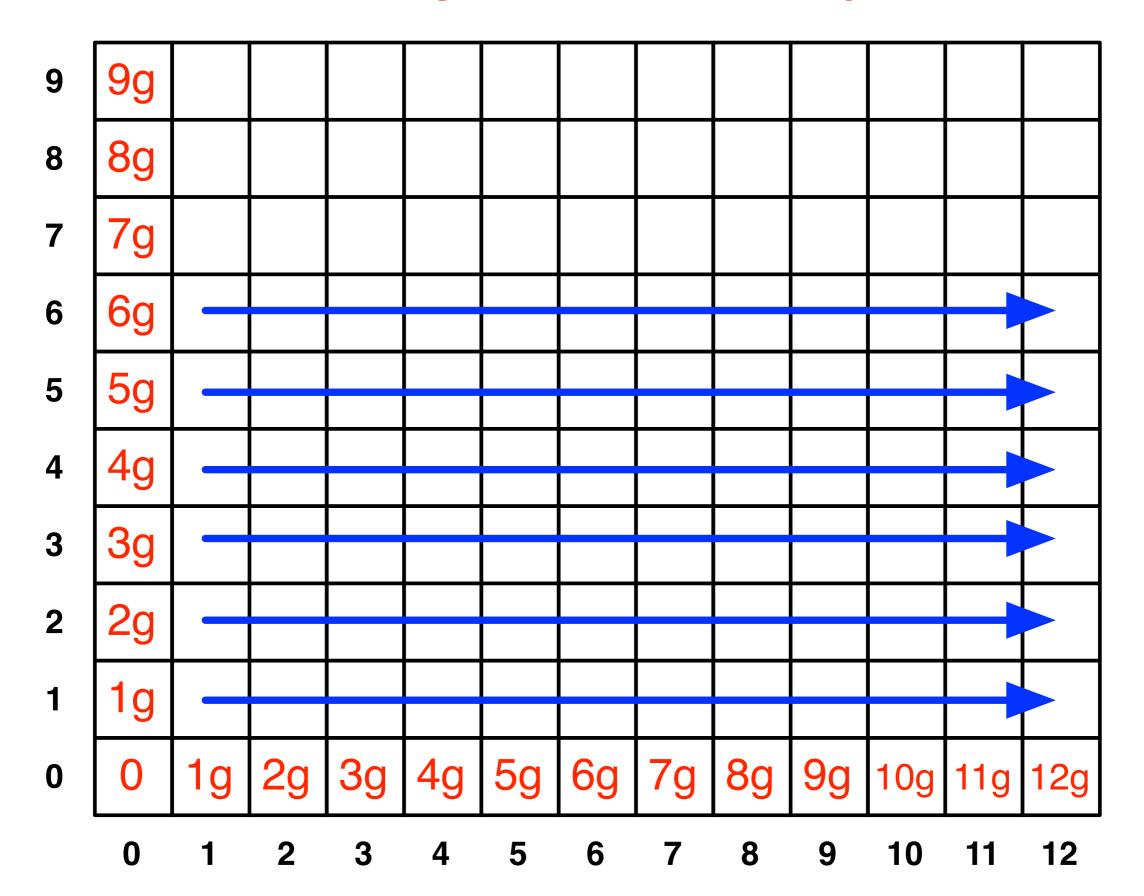
We're ultimately interested in OPT(n,m), but we will compute all other OPT(i,j) $(i \le n, j \le m)$ on the way to computing OPT(n,m).

Store those values in a 2D array:



NOTE: observe the non-standard notation here; OPT(**i**,**j**) is referring to *column* i, *row* j of the matrix.

Filling in the 2D Array



Edit Distance Computation

```
EditDistance(X,Y):
   For i = 1, ..., m: A[i, 0] = i*qap
   For j = 1, ..., n: A[0,j] = j*qap
   For i = 1, ..., m:
      For j = 1, ..., n:
         A[i,j] = min(
             cost(a[i],b[j]) + A[i-1,j-1],
             qap + A[i-1,j],
            gap + A[i,j-1]
      EndFor
   EndFor
   Return A[m,n]
```

Where's the answer?

OPT(n,m) contains the edit distance between the two strings.

Why? By induction: EVERY cell contains the optimal edit distance between some prefix of string 1 with some prefix of string 2.

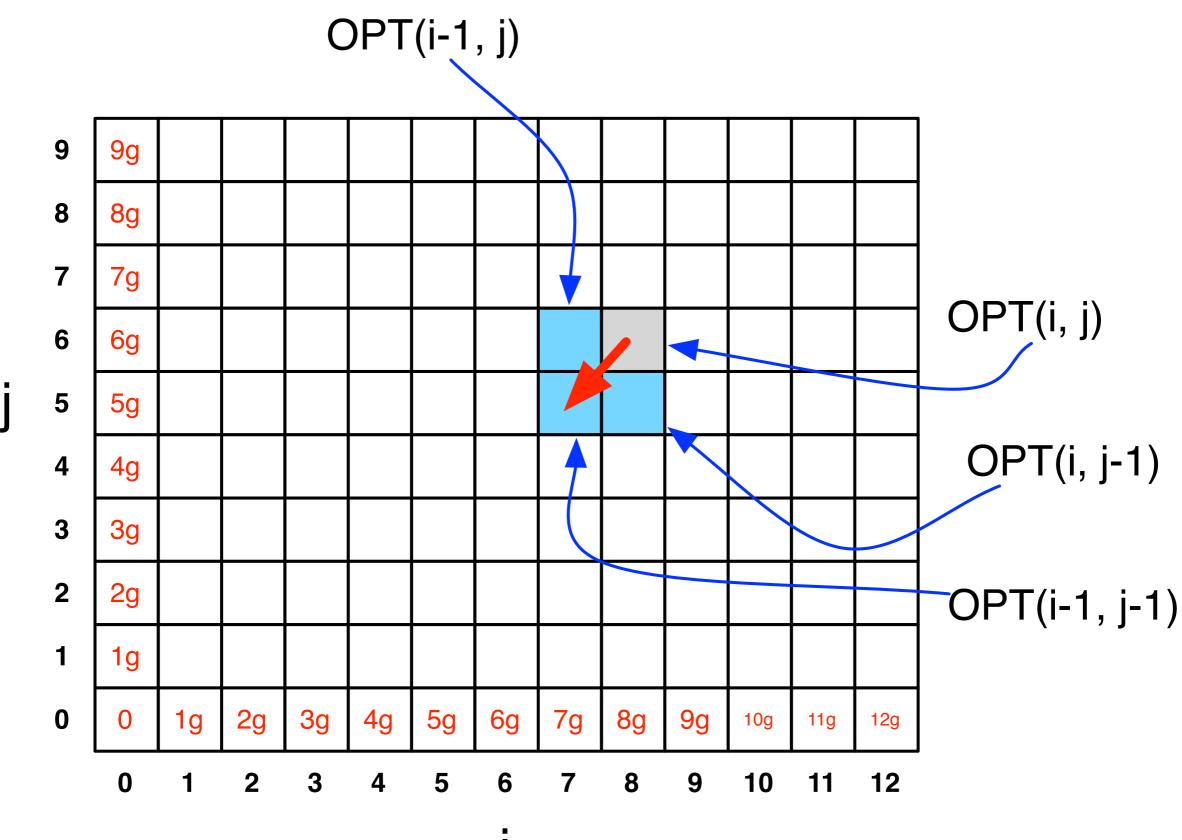
Running Time

Number of entries in array = $O(m \times n)$, where m and n are the lengths of the 2 strings.

Filling in each entry takes constant O(1) time.

Total running time is O(mn).

Finding the actual alignment



Outputting the Alignment

Build the alignment from right to left.

ACGT

A-GA

Follow the backtrack pointers starting from entry (n,m).

- If you follow a diagonal pointer, add both characters to the alignment,
- If you follow a left pointer, add a gap to the y-axis string and add the x-axis character
- If you follow a down pointer, add the y-axis character and add a gap to the x-axis string.

gap cost = 3 mismatch cost = 1

С	27												
А	24												
G	21												
Т	18												
Т	15												
G	12												
С	9												
А	6												
А	3 🕶	0											
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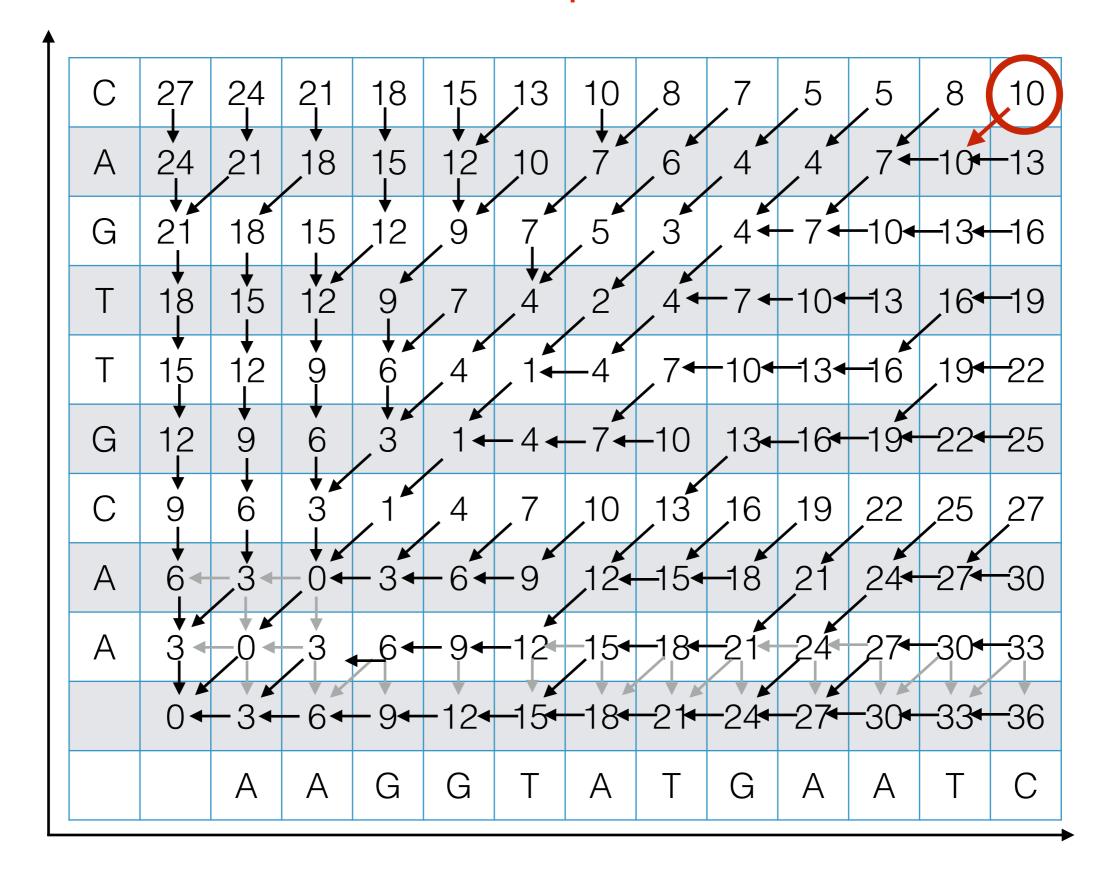
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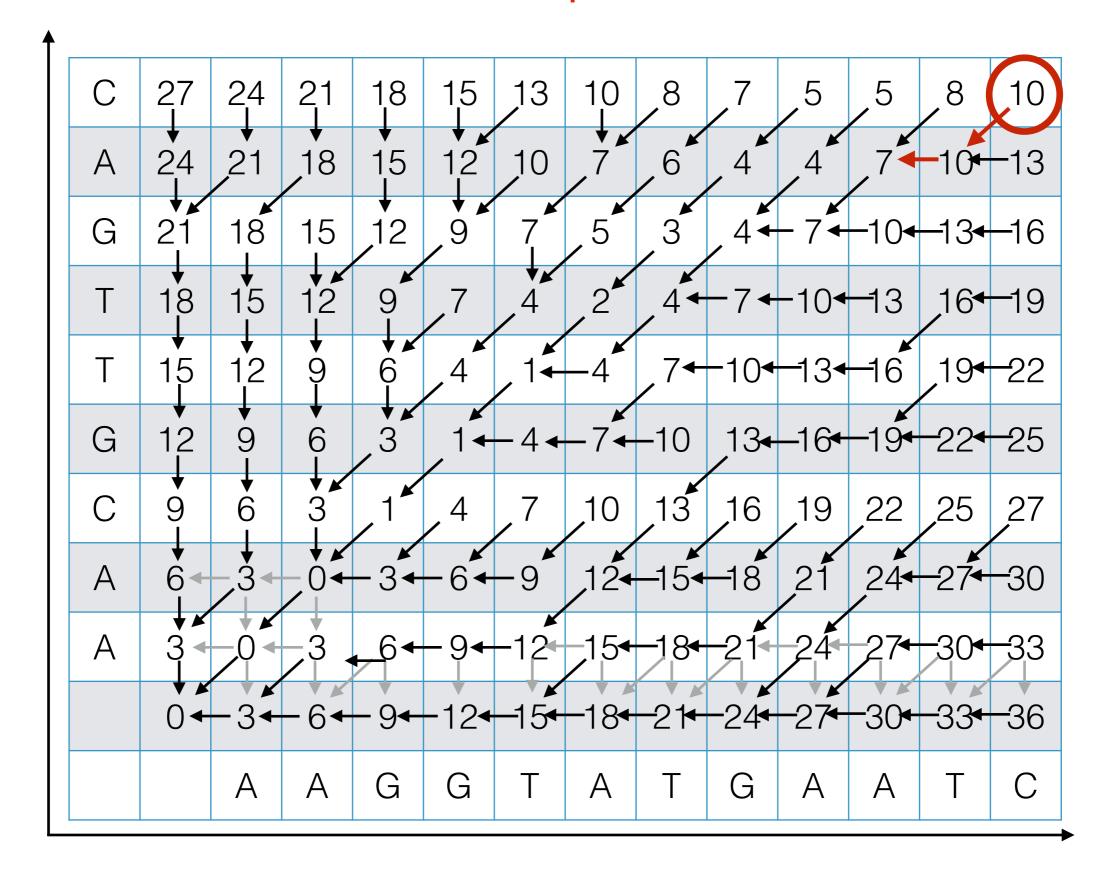
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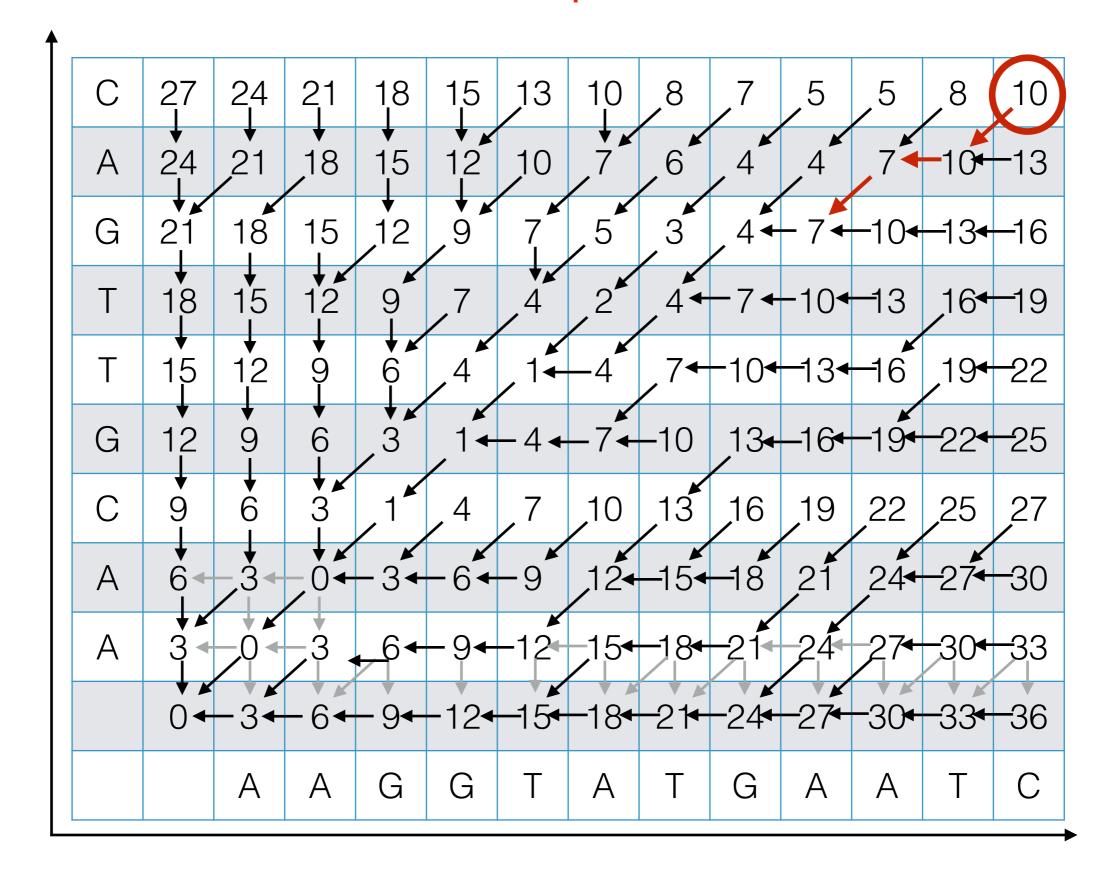
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		А	А	G	G	Т	Α	Т	G	Α	Α	Т	С

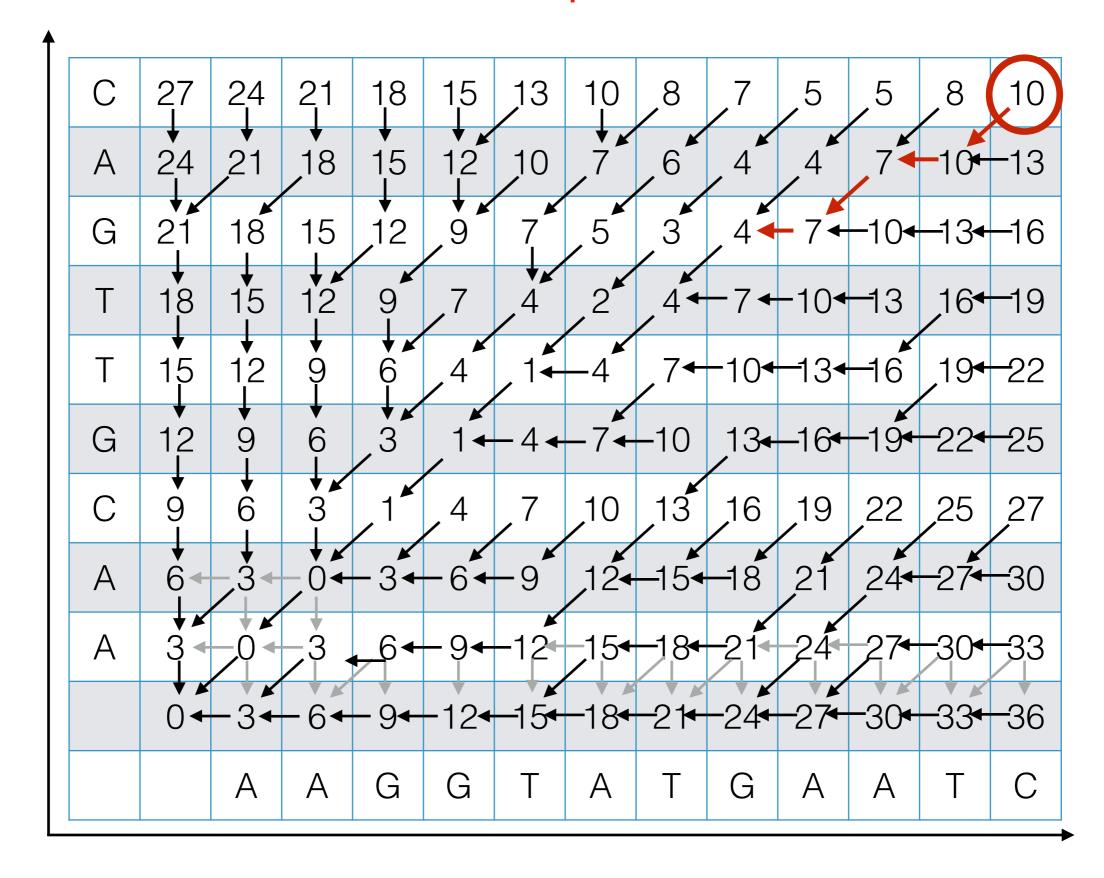
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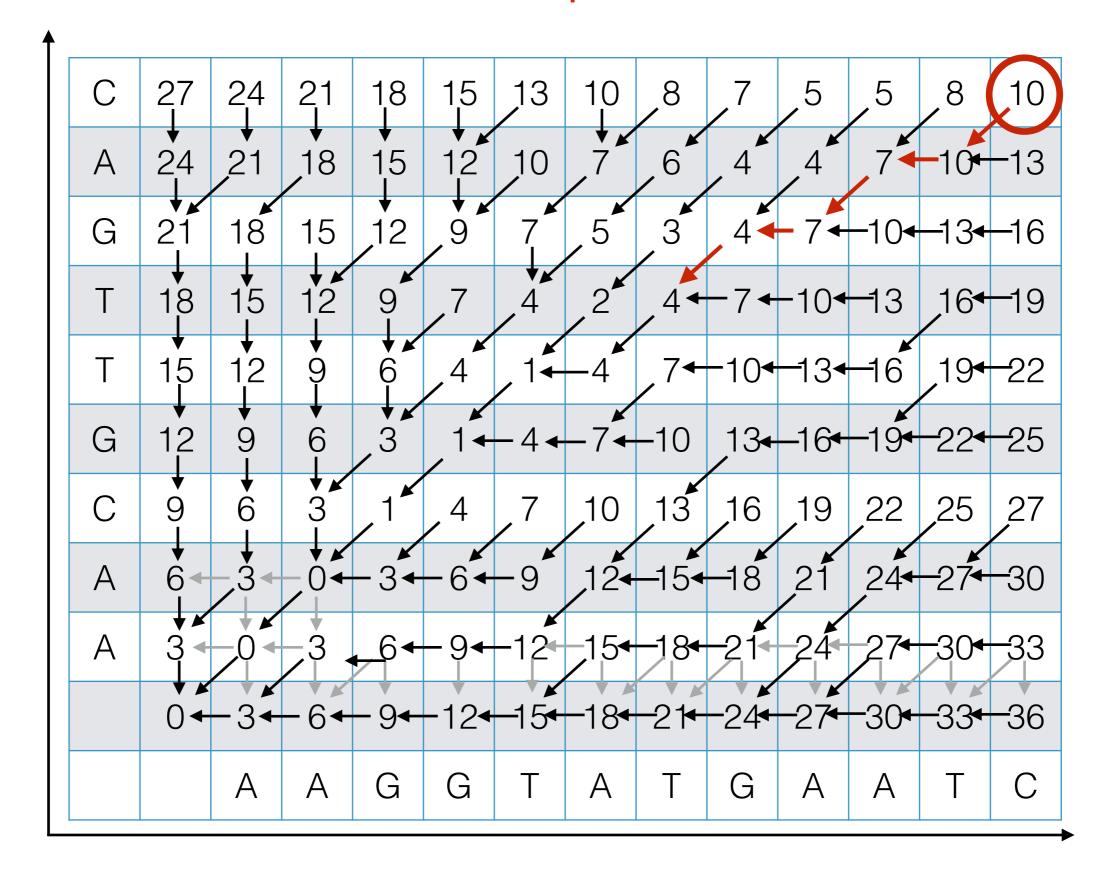
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С	9												
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	0	3	6	9	12	15	18	21		27	30	33	36
		А	А	G	G	Т	Α	Т	G	А	А	Т	С

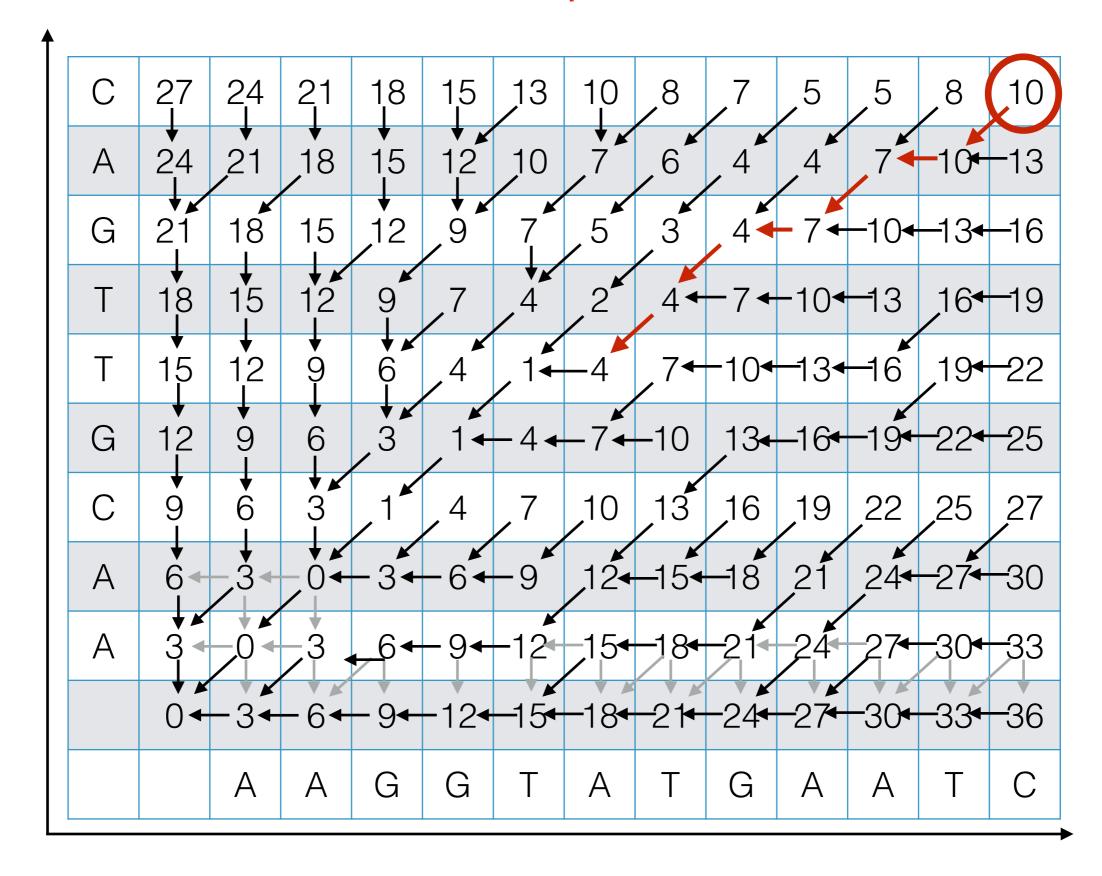


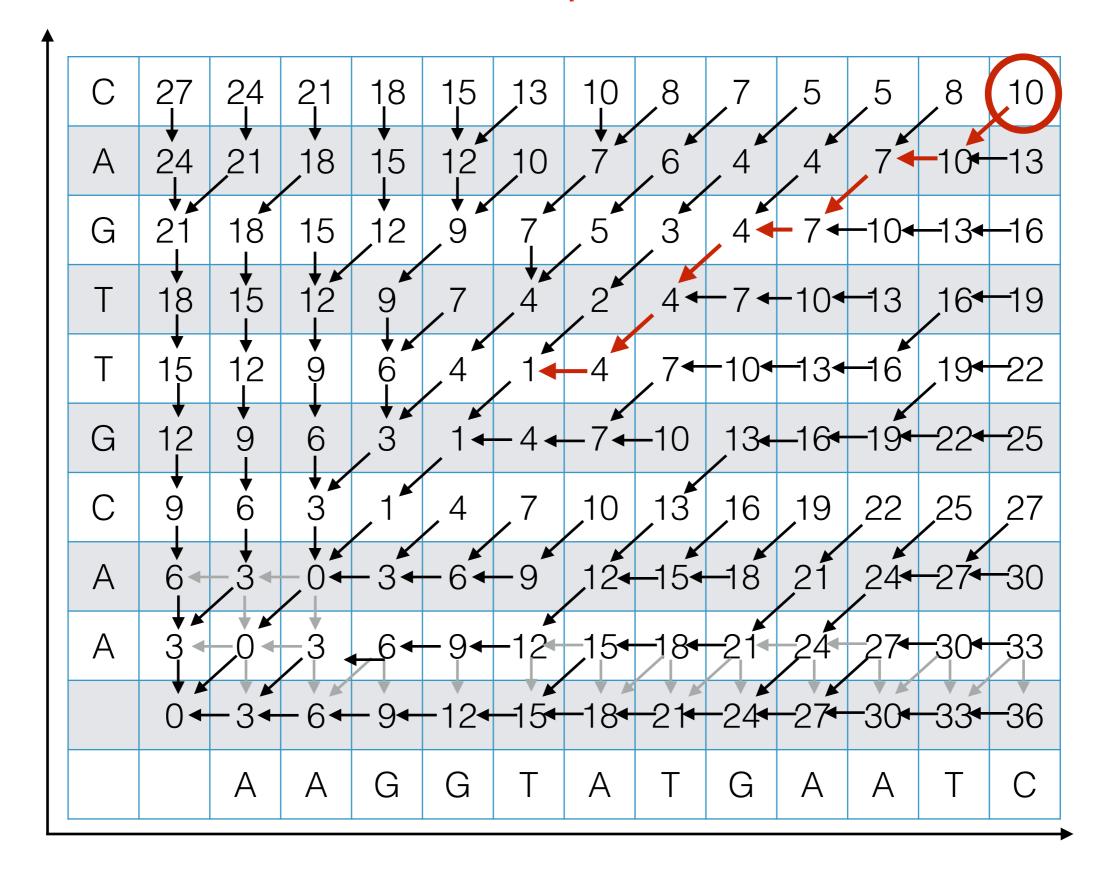


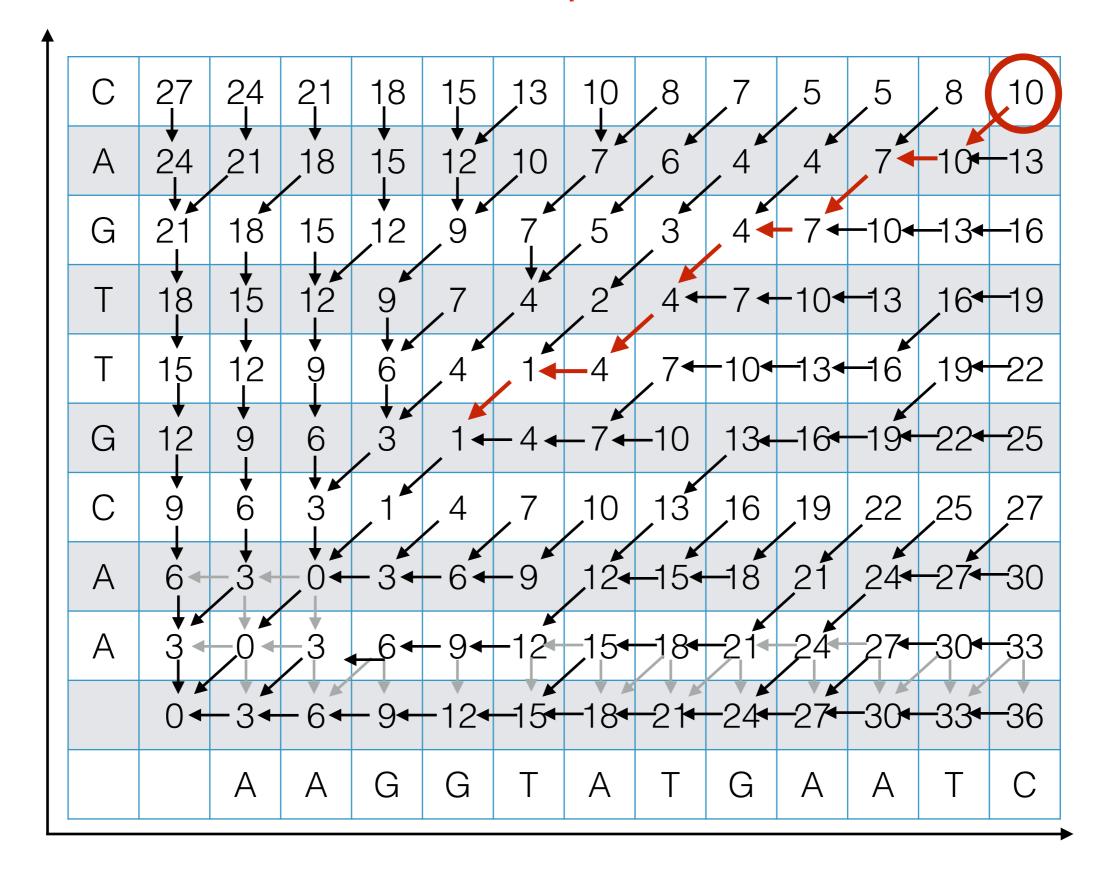


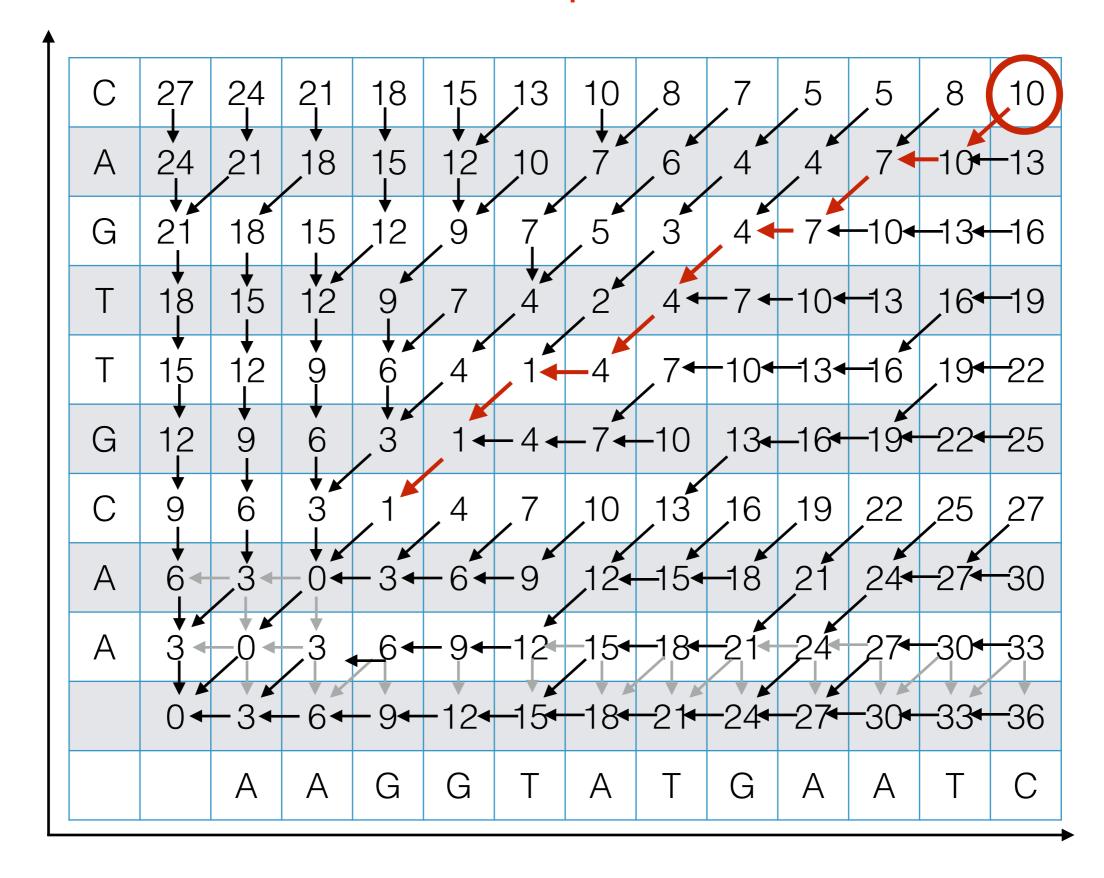


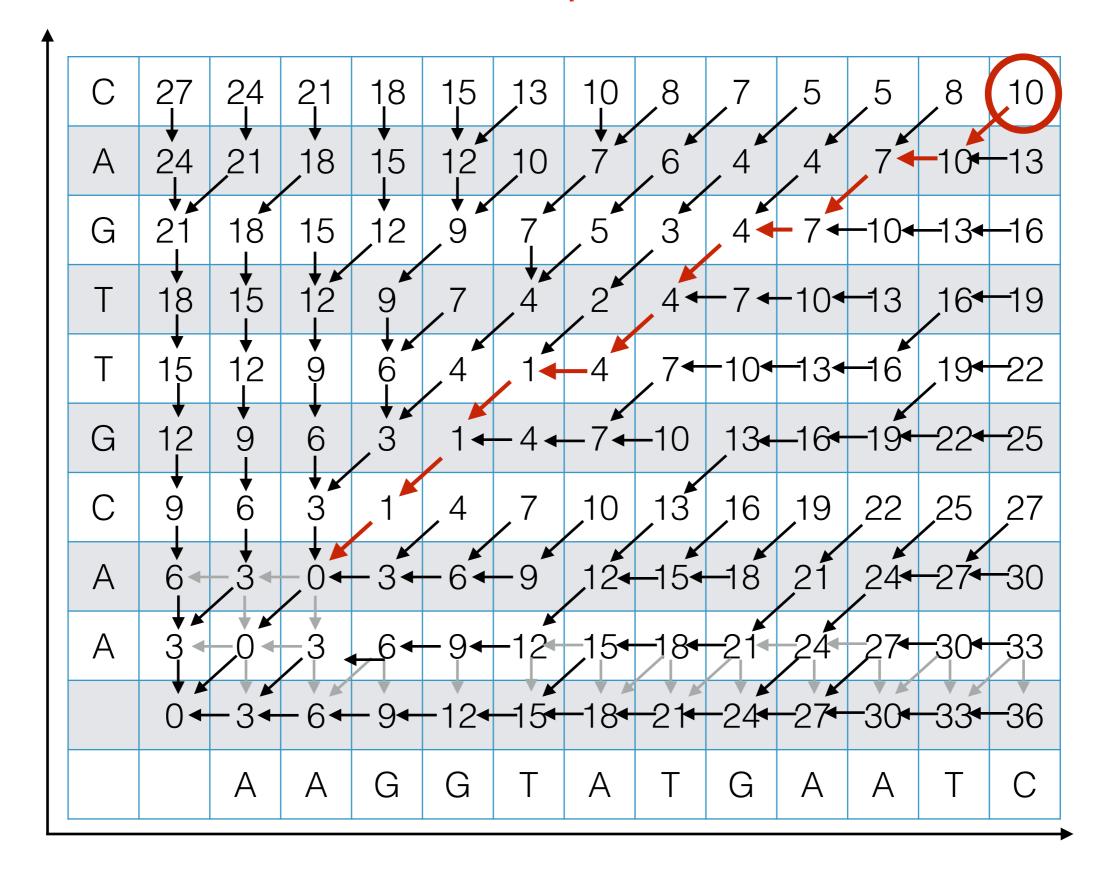


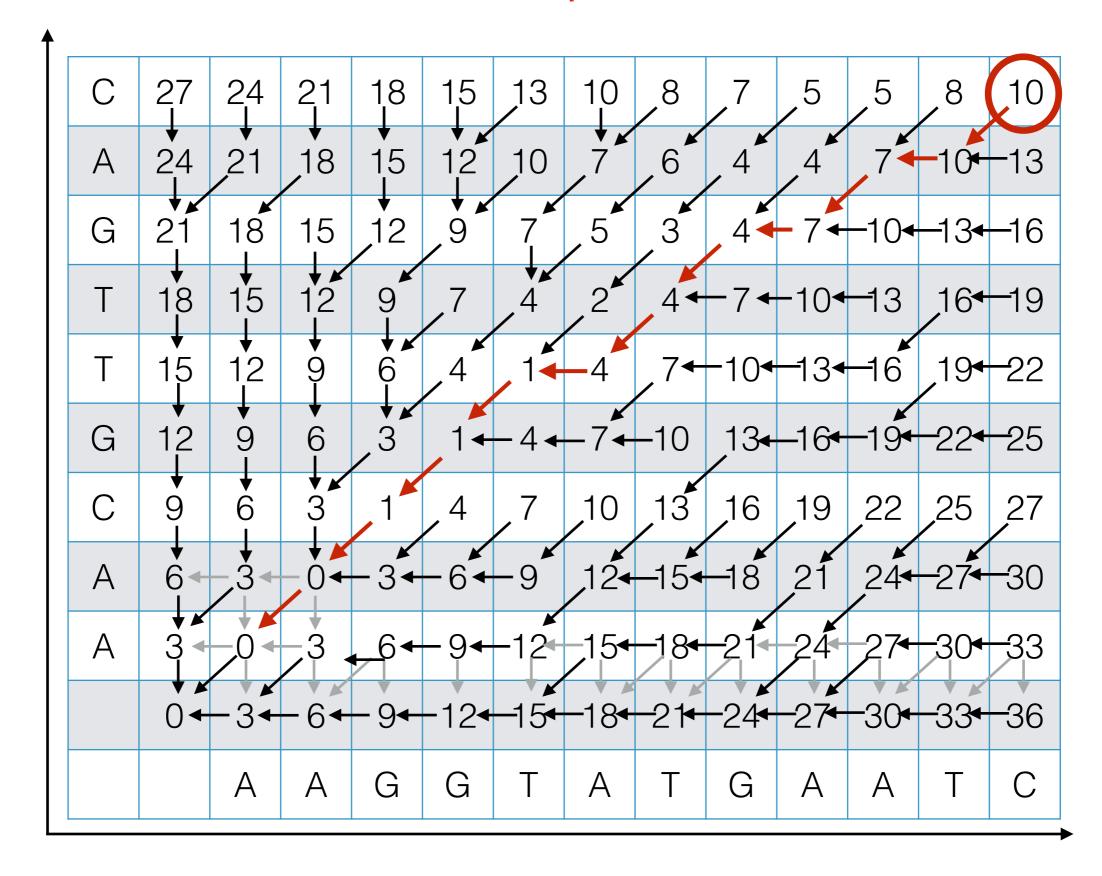


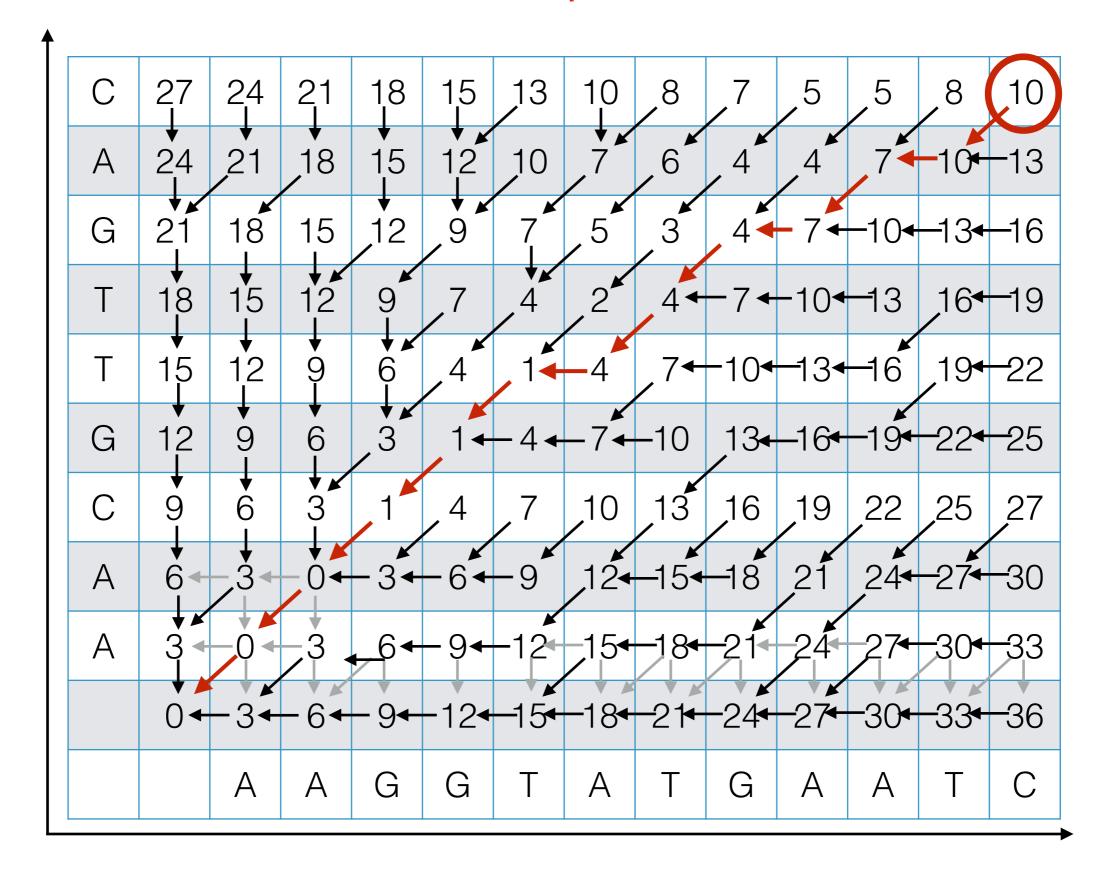












Recap: Dynamic Programming

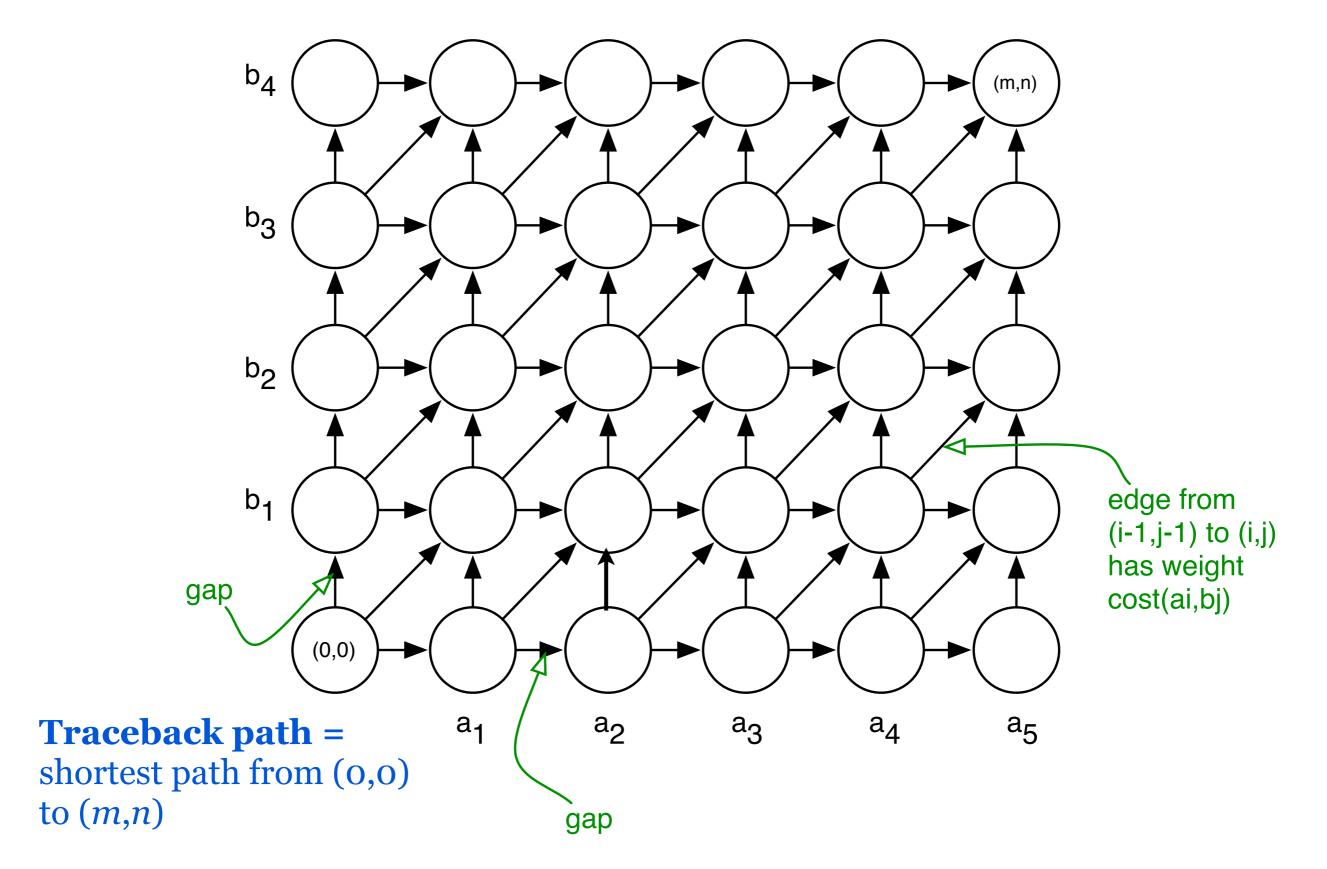
The previous sequence alignment / edit distance algorithm is an example of dynamic programming.

Main idea of dynamic programming: solve the subproblems in an order so that when you need an answer, it's ready.

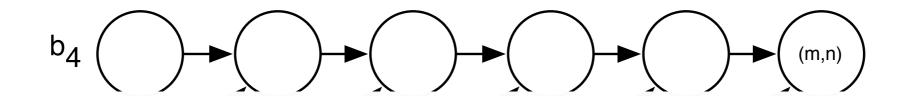
Requirements for DP to apply:

- 1. Optimal value of the original problem can be computed from some similar subproblems.
- 2. There are only a polynomial # of subproblems
- 3. There is a "natural" ordering of subproblems, so that you can solve a subproblem by only looking at **smaller** subproblems.

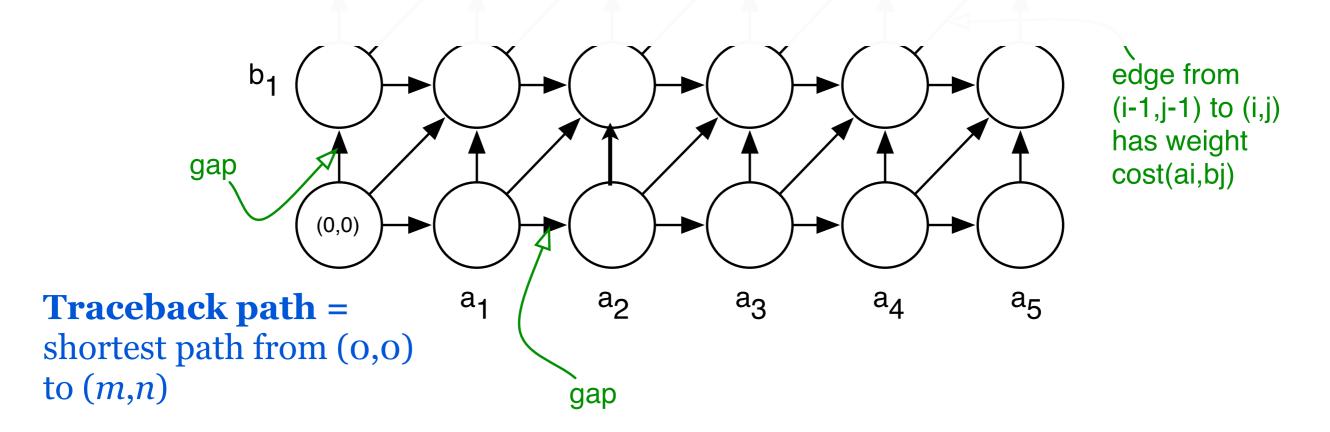
Another View: Recasting as a Graph



Another View: Recasting as a Graph



How would you find a shortest path in this graph *efficiently?*



*

Semi-global Alignment Example

Semi-global (glocal): Gaps at the beginning or end of **x** or **y** are free — one useful case is when one string is significantly shorter than the other

x y

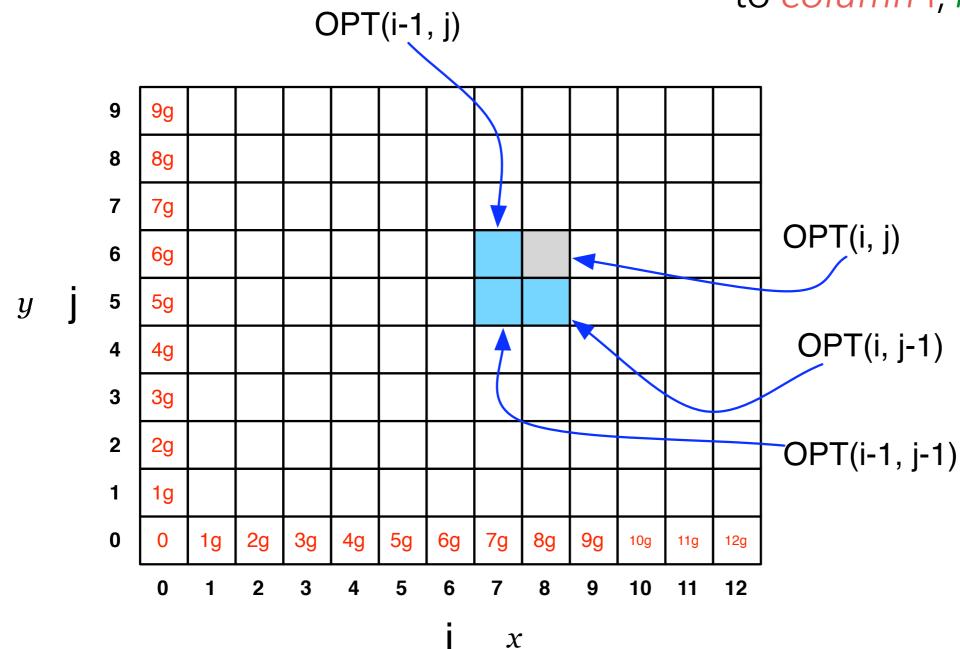
We'll discuss the "fitting" variant for in the next few slides for simplicity, but the same basic idea applies for the "overlap" variant as well.

Recall: Global Alignment Matrix

OPT(i,j) contains the score for the best alignment between:

the first *i* characters of string *x* [**prefix** *i* of *x*] the first *j* character of string *y* [**prefix** *j* of *y*]

NOTE: observe the non-standard notation here; OPT(**i**,**j**) is referring to *column* i, *row* j of the matrix.



How to do semi-global alignment?

y

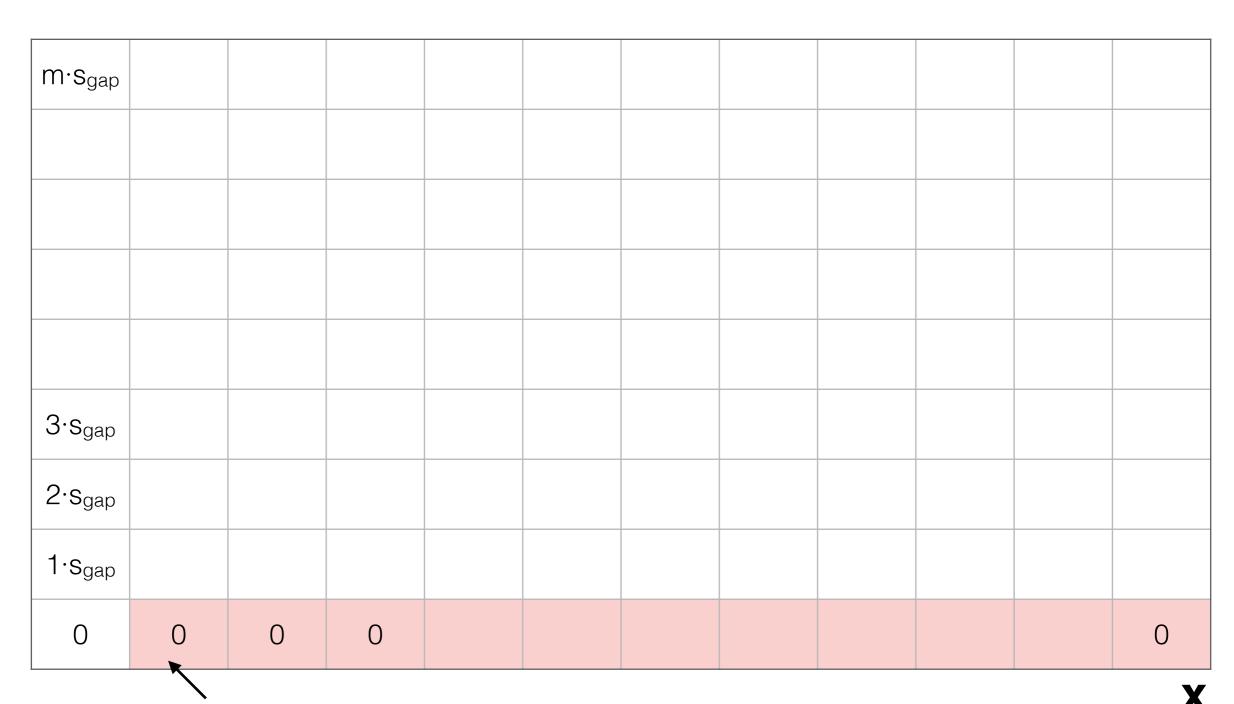
m·s _{gap}							
3·s _{gap}							
2·s _{gap}							
1·s _{gap}							
0	1·s _{gap}	2·s _{gap}	3·s _{gap}				n·s _{gap}

X

Start with the original global alignment matrix

How to do semi-global alignment?

y



change the base case — allow gaps before y

How to do semi-global alignment?

У

m·s _{gap}							O(n,m)
3·s _{gap}							
2·s _{gap}							
1·s _{gap}							
0	0	0	0				0

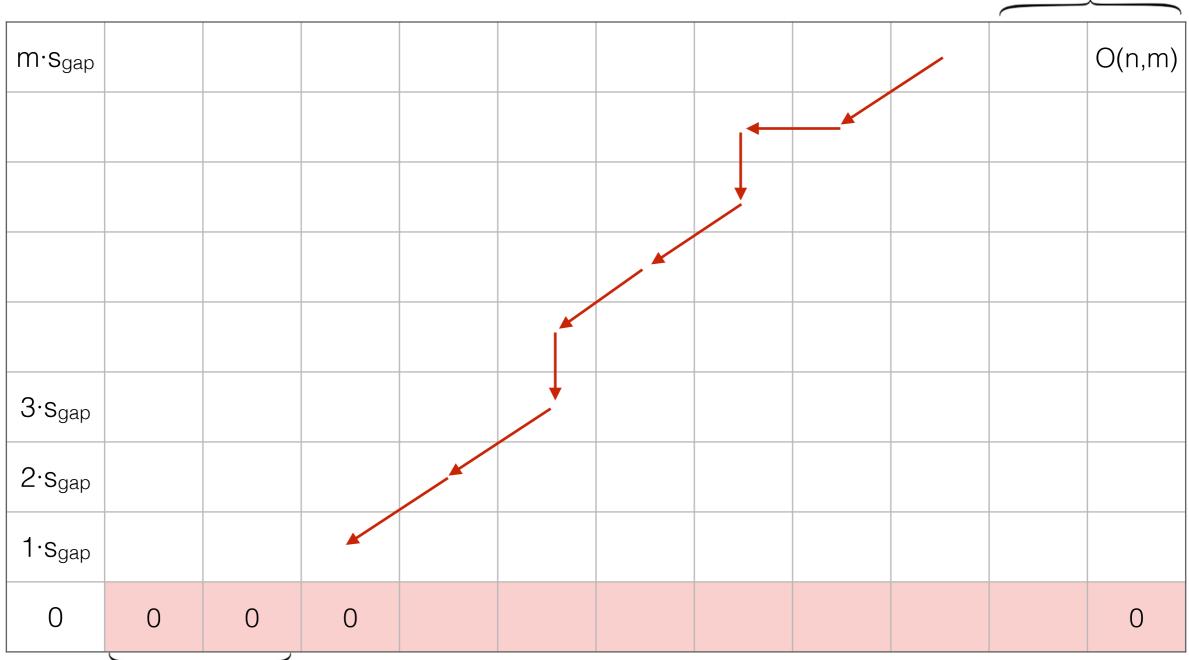
X

start traceback at $\max_{0 < i \le n} \mathsf{OPT}(i,m)$ — this allows gaps after \boldsymbol{y} ; why?

Semi-global alignment example

and this gap after y

y



We allow this gap before **y**

X

Semi-global Alignment

What is the same and different between the "global" and semi-global ("fitting") alignment problems?

*assuming |y| < |x| and we are "fitting" y into x

Global

Semi-global ("fitting")

$$OPT(i, j) = \max \begin{cases} score(x_i, y_j) + OPT(i - 1, j - 1) \\ s_{gap} + OPT(i - 1, j) \\ s_{gap} + OPT(i, j - 1) \end{cases}$$

$$OPT(i, j) = \max \begin{cases} score(x_i, y_j) + OPT(i - 1, j - 1) \\ s_{gap} + OPT(i - 1, j) \\ s_{gap} + OPT(i, j - 1) \end{cases}$$

Base case: $OPT(i,0) = i \times s_{gap}$

Base case: OPT(i,0) = 0

Traceback starts at OPT(n,m)

Traceback starts at **max** OPT(j,m) _{0<j≤n}

Semi-global Alignment

The recurrence remains the *same*, we only change the base case of the recurrence and the origin of the backtrack

1) Ignore gaps before x ——— change base case; OPT(0,i) = 0

2) Ignore gaps after x ——— change traceback; start from max OPT(n,j) $0 < j \le m$

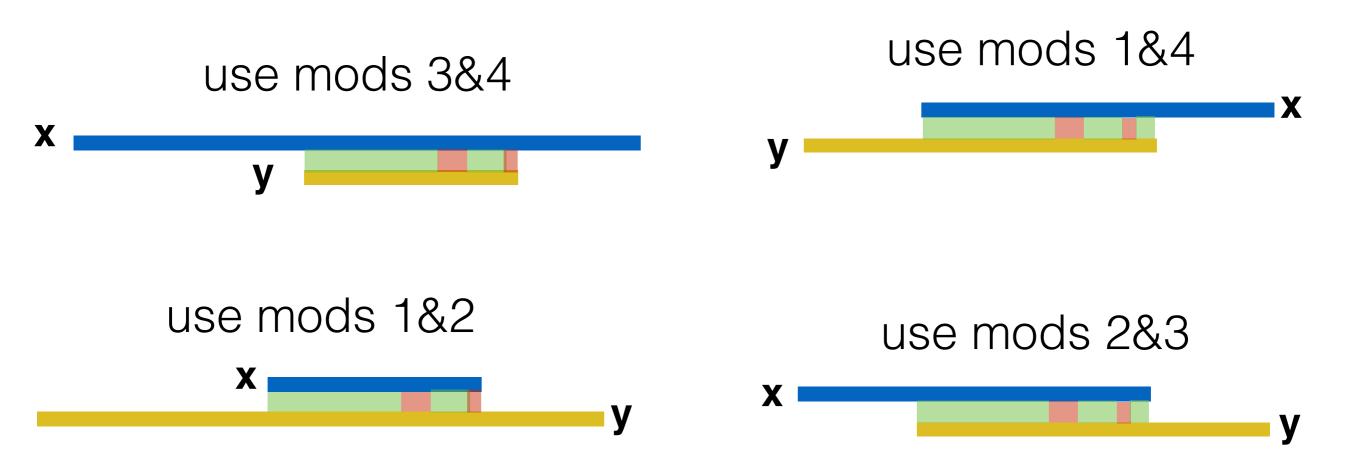
3) Ignore gaps before y
OPT(i,0) = 0

4) Ignore gaps after y — → change traceback; start from max OPT(i,m)

Semi-global Alignment

- 1) Ignore gaps before x
- 2) Ignore gaps after x
- 3) Ignore gaps before y
- 4) Ignore gaps after y

Types of semi-global alignments



Side Note: Lower Bounds

- Suppose the lengths of x and y are n.
- Clearly, need at least $\Omega(n)$ time to find their global alignment (have to read the strings!)
- The DP algorithms show global alignment can be done in $O(n^2)$ time.
- A trick called the "Four Russians Speedup" can make a similar dynamic programming algorithm run in O(n² / log n) time.
 - We probably won't talk about the Four Russians Speedup.
 - The important thing to remember is that only one of the four authors is Russian...
 (Alrazarov, Dinic, Kronrod, Faradzev, 1970)
- Open questions: Can we do better? Can we prove that we can't do better? No#

*

Using semi-global alignment is not feasible for read mapping

The best algorithms we have (and like the best that could exist) to compute the optimal alignment of two strings are *quadratic*

If we have N reads, each of length ℓ , and the genome is of length L, then applying the optimal algorithm at each possible position (to test the edit distance) is $O(N \cdot \ell \cdot L)$

Consider a dataset with:

 $N = 20 \times 10^6 \text{ reads}$

ℓ = 100

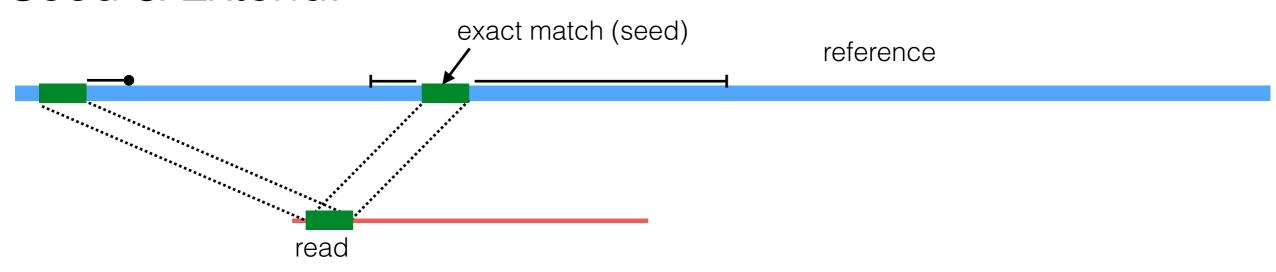
 $L = 3x10^9$ nucleotides

and a processor that can do $X = 3 \times 10^9$ operations / sec.

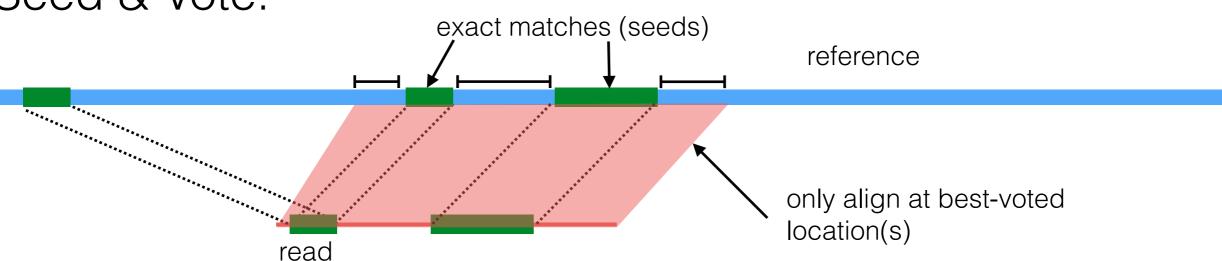
You'd wait about $(N \cdot \ell \cdot L) / X = 200,000,000$ sec = 6.34 **years** to align your reads.

How can exact matching help?

Seed & Extend:



Seed & Vote:



How can exact matching help?

GGTACCCCAAATTCGAAAGAGCCGAATGAAGTGGAAAGAATGGCCATTCAAATGGCTTGGGA

CGGCGCGCAGGACCTCCGCGCCTCCATTATGCTATTCTGCCCGCCGTGGGTGACAAACAGACGGATGCTACCAGCCCAGCCCAGT CCCGGGGAGCCAGCTGGCCTGGGGTTCGGTCCCGCGTCTTCCCTCATTCTGTGCCGCTGCCGAGCCTGTCTCAGCTCCACACACG CTTGGGAGCTGCAGATGCCTCCGCCCCTCCTCTCCCAGGCTCTTCCTGCCGTTGAACCCCGGCGGCGGCTCTCGGCCAGCGG CGCGCCCT**GGTACCCCCAAATTCCAAAGAGCCGAATGAAGTGGAAAGAATGGCCACAAATGGCTTGGGC**CCGAGTGACCATGGGA TGGTTAGGTAGGATTTTAGAGGCGACTGCTCCTGGAATTAGAGAAAGAGTTTCATTACAACCGCTACCTGACCCGAAGGCACTCGGGC CCATGCCTTCCTCCTCCGCTGTTTGATTTCTATTCTGTTTAGCCTGAGTTGGAGATGCCGGAGGTGCCGTGGTGGAAGAAGTCTTGA ACGAATTTGGAGGCGTCTCCGTGGCAGCTAAGCGAGCACGGGTTCTGCTGGTGCAGGATGACACTGGCAGCCACTGCCGCGGACTT CCTAAAGGGAACCTGCAATAATCTTGAAAAAGGACTTCAATCCGACGTTTTCGTGTCAAATAAGGATTAAAGAGAAACTCCTCCGCGAGC CGTGCGCCGAGGGTGGCGGGGGGCCTGAAGCGTGAGGAGCCTTCAATATGTATTTAACCAGGGACCGTCGGTATGAGGTGGCCC GGGTTCTTATTTGTTTGGGGGGCTGGAGGGGGGGAGACGGAGAAACAGTGAAAAGTTCCTGAGCCCCATAAAGGGACTGTCTGGGGAGC GCCTCGTAGCCATAGAATTCCACCGCCGCCGCCCCCCCCGCGTAGTCGTACTTGAAGCCGAGCGCAGGCGGGTGGTTCATTAACTCTGA CTTTGCCTTTGATTTTGCTCGACCTCTGCTTCGTCAAAATCTGGTTTCAGAATCGAAGGATGAAGATGAAAAAAGATGAATAAAGGAGGAA AAGGAAGAAACAAGGACTAAGCAAAAAAGAAAGACCCCCCCTATAGCAGGATTTTAAAATTTTTCTCTTTTTCTCAAGATTATTGCA GATTGAAGTCTCTCATGCCCAACTAGTGGGGTTTCCTGGCACTGGACCCCAGCAAGTGGTCCTAGAGGCGAAAAAGGAAGAAAACAAG GACTAAGCAAAAAAGAAGACCCCCCCCCCCCCGAAAGGATATCATGGATTCCTTAAAGAATGAGAACTTCGACATGGTGATATCACATGG GGATTTTAAAATCGGGCCCACCTTAACTCGGGAGGGCCGCGCGCTGAGGCTGGGAGCCGGAGAGTTCGGGCGAGGGCAGTGTCTGCGG GGCGCGGTCGCGCAGCTCCCCGGGCGAGCCAGGTGCAGCCTTGGCGGGGTCTGTTTGGTGGGCGATGTCACCATTTCCCGCCGCC GCCGTCGCCACCGCCGCCGCCGCCGCGTAGTCGTACTTGAATAGCTGGACATAAAGACAAAATGACAAAAAAATTATTATTATAGATATATT TGGTCTGTGTGTTATGTCCTAAGGTGTTTTGTCTGCAGTTTGAGAGCATGTTGCTGGTAGCCTGAGTTGGAGAT

How can exact matching help?

List of tuples of 13-mers;

(position in the query, position in the reference)

-1 indicates not found (Python behavior)

```
(0, 615); (1, 616); (2, 617); (3, 618);

(4, -1); (5, -1); (6, -1); (7, -1);

(8, -1); (9, -1); (10, -1); (11, -1);

(12, -1); (13, -1); (14, -1); (15, -1);

(16, 631); (17, 632); (18, 633); (19, 634);

(20, 635); (21, 636); (22, 637); (23, 638);

(24, 639); (25, 640); (26, 641); (27, 642);

(28, 643); (29, 644); (30, 645); (31, 646);

(32, 647); (33, 648); (34, 649); (35, 650);

(36, -1); (37, -1); (38, -1); (39, -1);

(40, -1); (41, -1); (42, -1); (43, -1);

(44, -1); (45, -1); (46, -1); (47, -1);

(48, -1); (49, 662); (50, 663); (51, -1);
```

So the basic strategy is:

Find exact matches shared between the read and reference

Group exact matches into regions likely to support a high-quality alignment

Score / validate each hit location, and filter the ones that fail to yield a high-quality alignment.

There are **many** variations on this theme. What is a good type of seed? How should we search for seeds? How should we group seeds? How aggressively should we filter potential loci?

all 13-mers

K-mers: fixed substrings of length k.

string

AGATTACGACATAGAGCCAATATTTAGACAGATAGC

In some sense, k-mers are the "simplest" type of seed.

K-mers in the text are independent of the query.

How might we "index" k-mers in the text?

AGATTACGACAT GATTACGACATA ATTACGACATAG TTACGACATAGA TACGACATAGAG ACGACATAGAGC CGACATAGAGCC GACATAGAGCCA ACATAGAGCCAA CATAGAGCCAAT **ATAGAGCCAATA** TAGAGCCAATAT **AGAGCCAATATT** GAGCCAATATTT **AGCCAATATTTA GCCAATATTTAG** CCAATATTTAGA CAATATTTAGAC **AATATTTAGACA ATATTTAGACAG TATTTAGACAGA ATTTAGACAGAT** TTTAGACAGATA TTAGACAGATAG TAGACAGATAGC

MEMs: Maximal Exact Matches

AGATTACGACATAGAGCCAATATTTGGACAGATAGC

Query

GCCAGATTACGACATAGAGCCAATATTTAGACAGATAGCTT

Ref

An exact match shared between the query and the reference that cannot be extended, in either direction, without introducing a mismatch.

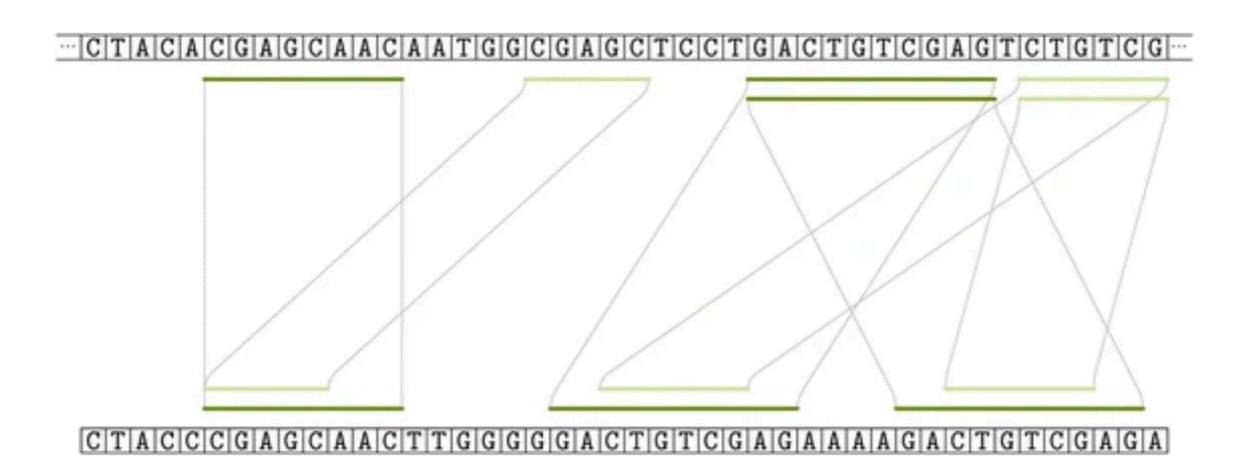
Unlike k-mers, the MEMs depend on both the reference and the specific query.

To find MEMs efficiently, we'll need a "full-text" index, not just a token / k-mer index.

Because of their "context dependence", MEMs can be more specific than k-mers, though we don't often deal with individual seeds in isolation.

SMEMs: Super-Maximal Exact Matches





An exact match shared between the query and the reference that cannot be extended, in either direction, without introducing a mismatch. Also, an SMEM is not contained within any other exact match on either the query or reference.

MMPs: Maximum Mappable Prefixes

MMP from index 2 on query

TCATTACGACATAGAGCCAATATTTGGACAGATAGC

GCCAGATTACGACATAGAGCCCAATATTTAGACAGATAGCTT

A prefix of (some suffix of) a query that is an exact match with a substring of the reference, and which cannot be extended further without introducing a mismatch.

Similar to a MEM, but extension only works in one direction — the MMP depends on the query, reference and start position. Originally introduced in STAR aligner. Useful for mapping read "pieces" across exons.

Indexing

Hopefully, I've convinced you of the importance of being able to quickly find different types of exact matches (seeds).

The next few lectures will be about data structures, and the corresponding search algorithms, that will enable this on genome-scale data.

We will consider both "full-text" indexing and inverted "token-based" indexing (k-mers).

There are many amazing results in the literature about indexing large text corpora; but there are likely still improvements to be made!