

Initialisation

$$\hat{\mathbf{x}}_0 = \mathbb{E}[\mathbf{x}_0], \mathbf{P}_0 = \mathbb{E}[(\mathbf{x}_0 - \hat{\mathbf{x}}_0)(\mathbf{x}_0 - \hat{\mathbf{x}}_0)^T]$$

Time update

Compute a priori state estimate:

$$\hat{\mathbf{x}}_{k|k-1} = \mathbf{\Phi}_{k-1} \hat{\mathbf{x}}_{k-1} + \mathbf{B}_{k-1} \mathbf{u}_{k-1}$$

Compute a priori error covariance:

$$\mathbf{P}_{k|k-1} = \mathbf{\Phi}_{k-1} \mathbf{P}_{k-1} \mathbf{\Phi}_{k-1}^T + \mathbf{Q}_{k-1}$$

Measurement update

Compute Kalman gain:

$$\mathbf{K}_k = \mathbf{P}_{k|k-1} \mathbf{H}_k^T (\mathbf{H}_k \mathbf{P}_{k|k-1} \mathbf{H}_k^T + \mathbf{R}_k)^{-1}$$

Compute a posteriori state estimate:

$$\hat{\mathbf{x}}_k = \hat{\mathbf{x}}_{k|k-1} + \mathbf{K}_k (\mathbf{z}_k - \mathbf{H}_k \hat{\mathbf{x}}_{k|k-1})$$

Update error covariance:

$$\mathbf{P}_k = (\mathbf{I}_n - \mathbf{K}_k \mathbf{H}_k) \mathbf{P}_{k|k-1}$$

Output