VQEDriver Documentation

v0.0.0

Python3 driver for the Variational Quantum Eigensolver (VQE) algorithm implemented in IBM's Qiskit for the calculation of the ground-state energy of a molecule. The driver reads a structured input file (commonly named [MOLECULE].inp) and runs a complete VQE calculation using IBM's Qiskit and PySCF libraries.

Usage of the program from terminal:

```
$ vqedriver [INPUTFILE] > vqe.out &
```

Contents

1 VQE Calculation		E Calculation	1
	1.1	Geometry	2
	1.2	Basis set	2
	1.3	Self-Consistent Field (SCF)	2
	1.4	VQE Settings	3
		1.4.1 Qubit Operator	4
		1.4.2 <i>Ansatz</i>	4
		1.4.3 Optimizer	5
	1.5	Simulation Setup	Ę

1 VQE Calculation

The input file follows a line by line structure, using keywords for each block and their options. In general, keywords are added in the format:

```
%keyword option_keyword1=option option_keyword2=option [...]
```

The input file accepts blank lines and comments beginning with the # character. The keywords can be added in any order.

1.1 Geometry

Added using the **%geometry** keyword. Currently, the geometry of the molecule has to be specified using an external XYZ file using the **xyzfile** option keyword.

Optional keywords:

• charge (int) – charge of the molecule.

Default: charge=0

• spin (int) -2S, where S is the total spin angular momentum. Same as the number of unpaired electrons in the molecule.

Default: spin=0

• units (str) – length units of the coordinate file.

Available options: angstrom, bohr

Default: units=angstrom

Example:

%geometry xyzfile=h2.xyz charge=1 spin=1 units=bohr

1.2 Basis set

Contains the basis set information for the molecule, added using the keyword %basis. Currently, only a single basis set can be added for all the atoms in the molecule using the option keyword all=[BASIS SET]. ECPs are not available.

Example:

%basis all=def2-TZVP

1.3 Self-Consistent Field (SCF)

Specifies the options for the SCF calculations, added by the **%scf** keyword. By default, the program sets a Restricted Hartree-Fock (RHF) calculation for closed-shell molecules and a Restricted-Open Hartree-Fock (ROHF) for open-shell molecule. Unrestricted Hartree-Fock (UHF) method is also

available for open- and close-shell molecules.

Optional keywords:

• method (str) – Hartree-Fock method for SCF calculations.

Available options: rhf, rohf, uhf

Default: method=rhf if spin==0 (closed-shell), method=rohf if spin!=0 (open-shell)

• conv (int) – convergence criteria for the SCF calculations to 10^{-conv} Hartree.

Default: conv=9

• maxcycles (int) - maximum number of SCF cycles.

Default: maxcycles=50

• maxcore (int) – maximum memory in MB that PySCF should use.

Default: maxcore=1000

Example:

%scf method=uhf conv=6 maxcycles=100 maxcore=7500

1.4 VQE Settings

The VQE algorithm requires a qubit operator (mapped from the fermionic operator representing the hamiltonian in the second quantization formalism), a trial wavefunction (ansatz) written as a unitary variational form and a classical optimizer. VQEDriver sets up and runs the full VQE calculation on a selected digital simulator.

VQEDriver prints not only the ground-state energy, but also the eigenstate in the qubit base (along with its count histogram), and the optimal parameters. Also, it saves a PNG file of the

VQE circuit as set up, and decomposed in the base of I, U1, U2, U3 and CNOT gates, where:

$$U1(\lambda) = \begin{bmatrix} 1 & 0 \\ 0 & e^{i\lambda} \end{bmatrix}$$

$$U2(\phi, \lambda) = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & -e^{i\lambda} \\ e^{i\phi} & e^{i(\phi + \lambda)} \end{bmatrix}$$

$$U3(\theta, \phi, \lambda) = \begin{bmatrix} \cos\frac{\theta}{2} & -e^{i\lambda}\sin\frac{\theta}{2} \\ e^{i\phi}\sin\frac{\theta}{2} & e^{i(\phi + \lambda)}\cos\frac{\theta}{2} \end{bmatrix}$$

Notice that $H = U2(0, \pi)$ and $P(\lambda) = U1(\lambda)$.

1.4.1 Qubit Operator

Contains general settings for the qubit operator setup, built mapping the fermionic operator to the qubit operator. Options are added by the "qubitop keyword. The qubit operator is printed as a Python3 dictionary in a text file [INPUTFILE].qubit_operator.txt.

Optional keywords:

• map (str) - mapping to convert the fermionic operator to a qubit operator.

Available options: jw (Jordan-Wigner), parity, bk (Braviy-Kitaev)

Default: map=parity

• threshold (int) – threshold for Pauli simplification, eliminate the real and imaginary parts of the weight in each Pauli Operator mapped by 10^{-threshold}. If a weight is less than 10^{-threshold}, the Pauli is removed from the WeightedPauliOperator object.

Default: threshold=8

Example:

1 %qubitop map=bk threshold=9

1.4.2 Ansatz

Builds the trial wavefunction variational form to be optimized. Added using the keyword %ansatz. Currently, there are two options available: UCCSD (Unitary Coupled-Cluster Single and Double

excitations) and CHC (Compact Heuristic for Chemistry), which aims to approximate the UCCSD ansatz while reducing the number of CNOTs involved.

Optional keywords:

• method (str) – variational form to be used.

Available options: uccsd, chc

Default: method=uccsd

• exctype (str) – excitation types to include in the active space to build the variational form.

Available options: s (singles), d (doubles), sd (singles and doubles)

Default: exctype=sd

Example:

```
% ansatz method=uccsd exctype=sd
```

1.4.3 Optimizer

Selects the classical optimizer for the VQE algorithm using the keyword **%optimizer**. The optimizer is selected using the optional keyword **method**. All available optimizers and their particular optional keywords are detailed on table I.

Example:

```
%optimizer method=cg print=false conv=6 maxiter=1500
```

Table I: Available classical optimizers for the VQE algorithm.

Optimizer	Description	Optional Keywords
cg	Conjugate Gradient	maxiter (int) – Maximum number of iterations
		print (bool) – Whether to print convergence messages
		conv (int) – Convergence tolerance

1.5 Simulation Setup

The VQE calculation is executed on a digital simulator of the quantum circuit. The simulator is added using the keyword %sim.

Currently, available backends are the ideal statevector simulator and the Qasm simulator (noisy quantum circuit simulator).

Optional keywords:

• backend (str) – simulator to be used.

Available options: statevector, qasm

Default: method=qasm

• shots (int) – number of repetitions of quantum circuit measurements for sampling and averaging.

Defaul: shots=1024

• exact (bool) - if true, print the exact result calculated by classical diagonalization using the NumPyEigensolver. Useful for comparisons to classical techniques.

Default: exact=true

Example:

%sim backend=qasm exact=true shots=8192