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In [10]: ### Bootstrap

observations_two = [[0, 0, 0]]*50

for i in np.arange(50):

    sample14 = merged.sample(n=len(merged), replace = True)

    def final_olley_pakes(df):
        alphas = np.arange(0.05, 0.96, 0.01)
        betas = np.arange(0.05, 0.96, 0.01)
        minimum = float("inf")
        optimal_alpha = 10
        optimal_beta = 10
        optimal_gamma = 10

        for alpha in alphas:
            for beta in betas:
                #w x denotes 2013, y denotes 2012
                df["eta_y"] = df["LogVA_y"] - alpha*df["LogK_y"] - beta*df["LogL_y"]
                df["eta_x"] = df["LogVA_x"] - alpha*df["LogK_x"] - beta*df["LogL_x"]
                df["eta"] = df["LogVA"] - alpha*df["LogK"] - beta*df["LogL"]
                df["delta_eta_x"] = df["eta"] - df["eta_x"]
                df["delta_eta_y"] = df["eta"] - df["eta_y"]

                #y, x = dmatrices("eta ~ eta_x + eta_y", data=df, return_type = "dataframe")

                #mod = sm.OLS(y, x)
                mod = sm.OLS(df[["delta_eta_x"]], df[["delta_eta_y"]])
                res = mod.fit()

                gamma = res.params[0]

                moment_vector = matrix(array([[0, 0, 0, 0]])).transpose()
                for ind, row in df.iterrows():
                    arr = array([
                        1, row["LogK_y"], row["LogK_x"], row["LogL_y"], row["LogVA_y"]])
                    m = matrix(arr).transpose()
                    moment_vector = ((row["eta"] - (gamma*row["eta_x"] - (row["eta_x"] - (gamma*row["eta_y"]))))' * m) + moment_vector

                sample_moment_vector = moment_vector / len(final_df) / 3
                sample_moment = sample_moment_vector.transpose() * sample_moment_vector
                if sample_moment.item(0) < minimum:
                    minimum = sample_moment.item(0)
                    optimal_alpha = alpha
                    optimal_beta = beta
                    optimal_coe = coe
                    optimal_gamma = gamma

        return optimal_alpha, optimal_beta, optimal_gamma, minimum

aa, bb, gg, mm = final_olley_pakes(sample14)
print(mm, sep=" ", end=" ")
observations_two[i] = [aa, bb, gg]
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In [11]: ### Printed the minimums above to check how my values looked and keep track of progress

In [12]: boot_alph_t = []
boot_beta_t = []
boot_gamma_t = []
for i in np.arange(50):
    boot_alph_t += [observations_two[i][0]]
    boot_beta_t += [observations_two[i][1]]
    boot_gamma_t += [observations_two[i][2]]

In [13]: bootstrapped_theta_t = pd.DataFrame({"alpha": boot_alph_t, "beta": boot_beta_t, "gamma": boot_gamma_t })

In [14]: bootstrapped_theta_t.describe()
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Out[14]:

	alpha	beta	gamma
count	50.000000	50.000000	50.000000
mean	0.752000	0.5803000	0.041708
std	0.290047	0.405665	0.138028
min	0.050000	0.050000	-0.223005
25%	0.685000	0.050000	-0.056781
50%	0.950000	0.850000	0.038581
75%	0.950000	0.950000	0.138588
max	0.950000	0.950000	0.453310

In [15]: bootstrapped_theta_t.head()

Out[15]:

	alpha	beta	gamma
0	0.71	0.95	0.210361
1	0.95	0.05	0.023332
2	0.53	0.05	0.040179
3	0.43	0.05	-0.064402
4	0.95	0.20	0.000758

[h] What have you learned about the distribution of productivity across large U.S. semiconductor firms? What else are you interested in learning? What data/methods might help you do so?

In our first model, I found that the distribution of productivity across semiconductor firms appeared to be a normal distribution with some degree of skewness. In the second model, I found that the firm productivities were similarly distributed, but the second model found almost half of firm productivities in 2014 to be negative. I am uncertain if my second model is correct, as I am not convinced that this many firms would have productivity factors that reflect lower output after considering their capital and labor expenditures. I am more convinced of the first model, which describes a plausible situation where firms varied in productivity but did not demonstrate productivities that reflected overall negative revenue during the period. However, if done correctly, I think the second model best captures firm productivity, as the time-invariant component of productivity should vary from firm to firm in my opinion. The second model reflects this condition, and demonstrates a wider distribution in firm productivities which I find both plausible and interesting. I am interested in the evolution of productivity and understanding the Markov Process. I will have to read on the theory of these processes, but after reading I hope to apply these statistical methods elsewhere as I think they may be useful in applications of time series theory

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In [ ]:
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