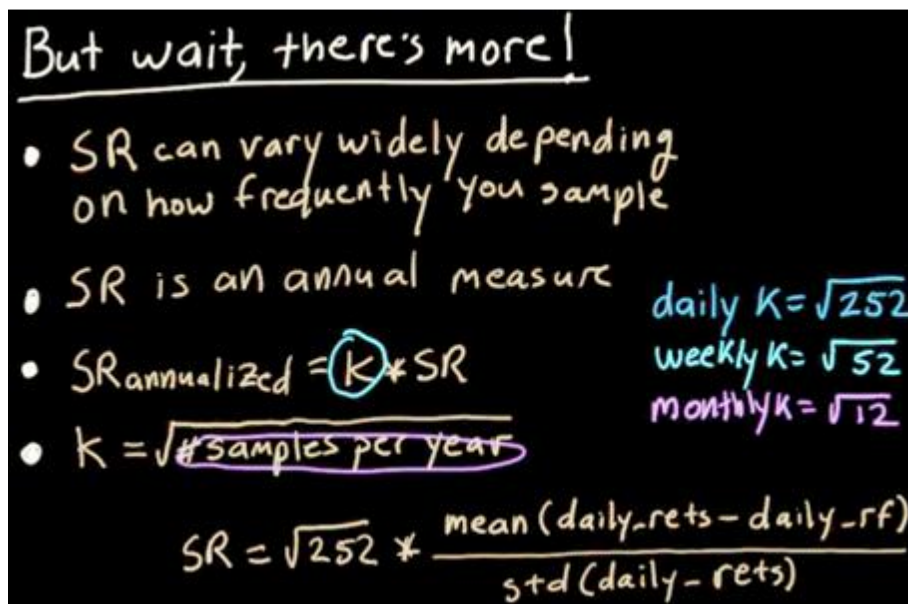


I. INTRODUCTION

The goal of this assignment is to apply our knowledge about optimizers to optimize a portfolio. For this assignment, portfolio optimization involves defining an allocation (long positions) of stocks that optimize its performance over a time interval. Optimize can be defined for many different metrics. This assignment will maximize Sharpe Ratio (SR) to select an allocation of securities that optimize the portfolio returns.

The Sharpe Ratio is defined by the following equation, and implemented by the code snippet below:



But wait, there's more!

- SR can vary widely depending on how frequently you sample
- SR is an annual measure
- $SR_{\text{annualized}} = K * SR$

$K = \sqrt{\text{\#samples per year}}$

daily $K = \sqrt{252}$
weekly $K = \sqrt{52}$
monthly $K = \sqrt{12}$

$$SR = \sqrt{252} * \frac{\text{mean}(\text{daily_rets} - \text{daily_rf})}{\text{std}(\text{daily_rets})}$$

```
def optimize_portfolio_sr(allocs, prices, rfr=0.0, sf=252.0):
    pvs = prices.copy()
    pvs = pvs / pvs.ix[0,:]          # normalize
    pvs = pvs.multiply(allocs, axis=1) # portfolio * allocations
    pv = pvs.sum(axis=1)
    dr = pv.copy()
    dr = (pv / pv.shift(1)) - 1      # calculate directly via Pandas
    dr.ix[0] = 0                    # set daily returns for row 0 to 0
    dr = dr[1:]                     # eliminate zeros in first row
    cr = (dr.ix[-1,:] / dr.ix[0,:]) - 1
    adr = dr.mean()                 # for entire dataframe, all positions
    sddr = dr.std()                  # for entire dataframe, all positions
    k = sf**(1/2.)
    sr = k * ((adr - rfr) / sddr)
    return -sr                      # Require MAX(sr): return MIN(-sr) == MAX(sr)
```

II. Explore the Optimal Portfolio and Make Some Charts

Figure 1: Charts a comparison of the optimal portfolio with SPY using the following parameters: Start Date: 2008-06-01, End Date: 2009-06-01, Symbols: ['IBM', 'X', 'GLD', 'JPM'].

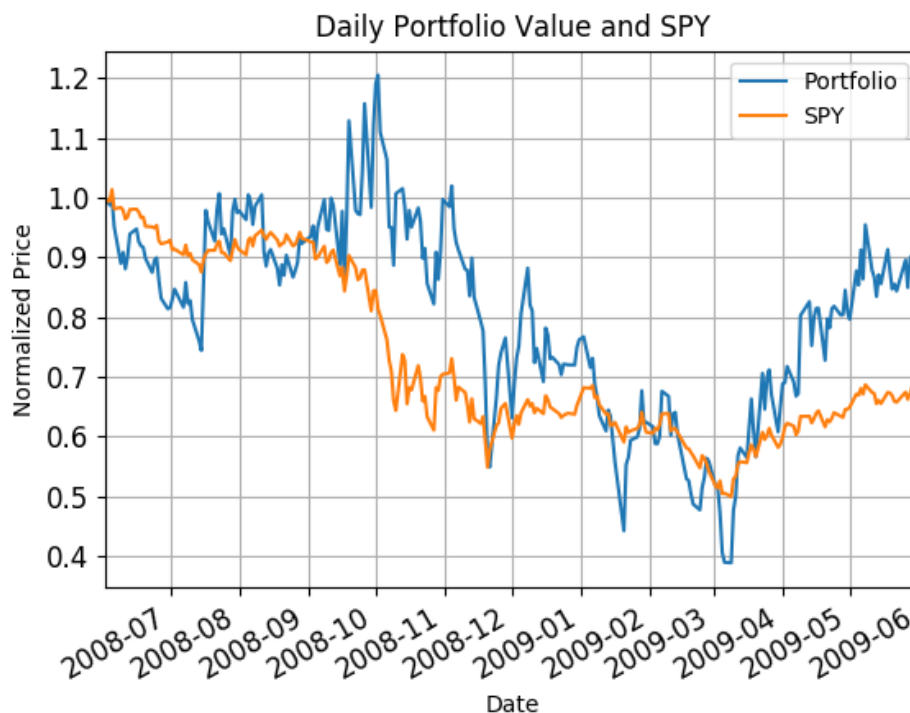
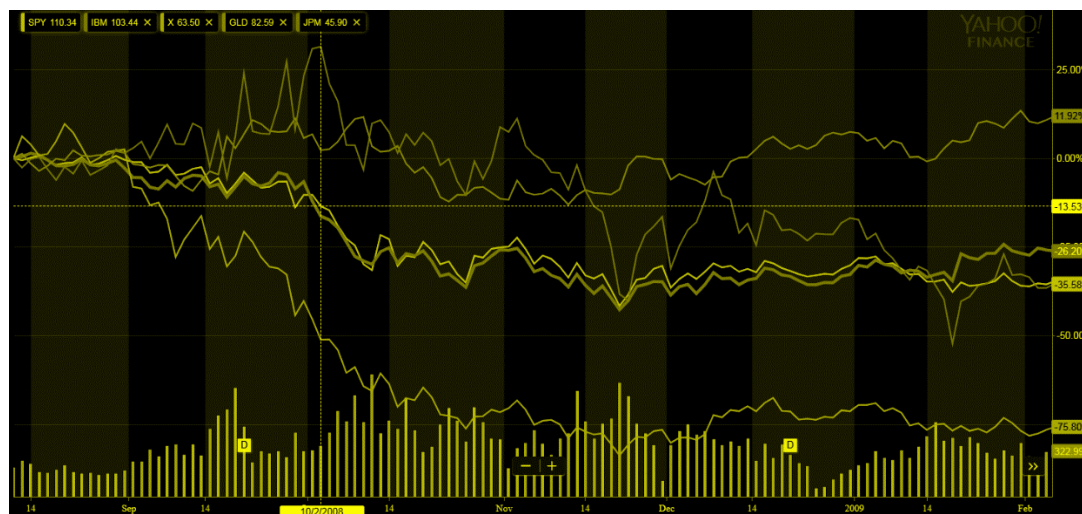


Figure 2: A chart from Yahoo Finance¹ that compares SPY with stocks in the optimal portfolio, ['IBM', 'X', 'GLD', 'JPM'] over the same time interval: Start Date: 2008-06-01, End Date: 2009-06-01. This chart was used to validate the chart in **Figure 1**, More specifically, the data at ~10/2008, which was the heart of the “Great Recession”.



¹ <https://finance.yahoo.com>