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1 Basic

1.1 install vscode [d41d8c]

1.2 default code [708fe0]

```
#include <bits/stdc++.h>
#pragma GCC optimize("03")
#pragma GCC target("popcnt")
#define all(x) (x).begin(), (x).end()
#define pii pair<int, int>
using namespace std;
using ll = long long;

void solve() {
}
int main() {
   ios_base::sync_with_stdio(false);
   cin.tie(nullptr);
   int t = 1;
   cin >> t;
   while (t--) {
      solve();
   }
}
```

1.3 compare fuction [4bc3e0]

```
// 要在 template 的資結用外部變數
struct cmp {  // }
  vector < int > &v;
     cmp(vector<int>& vec) : v(vec) {}
     bool operator() (int a, int b) const {
    return v[a] > v[b];
// main: cmp cmp1(vector);
// priority_queue<int, vector<int>, cmp> pq(cmp1);
};
1.4 pbds [e28ae8]
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < typename T >
using pbds_set = tree<T, null_type,
    less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template<typename T>
1.5 浮點數誤差 [a0d4e5]
struct EDouble {
     double x;
     constexpr static double Eps = 1e-9;
     constexpr EDouble() : x{} {}
constexpr EDouble(double v) : x{v} {}
     constexpr double val() const {
     explicit constexpr operator double() const {
     constexpr EDouble operator-() const {
        return EDouble(-x);
     constexpr EDouble &operator+=(const EDouble &rhs) & {
         x += rhs.x;
         return *this:
     constexpr EDouble &operator -=(const EDouble &rhs) & {
         return *this;
     constexpr EDouble &operator*=(const EDouble &rhs) & {
         x *= rhs.x;
return *this;
     constexpr EDouble &operator/=(const EDouble &rhs) & {
         assert(fabs(rhs.x) > Eps);
         x /= rhs.x;
     friend constexpr
           EDouble operator+(EDouble lhs, const EDouble &rhs) {
         lhs += rhs;
         return lhs:
     friend constexpr
           EDouble operator - (EDouble lhs, const EDouble &rhs) {
         lhs -= rhs;
         return lhs;
     friend constexpr
           EDouble operator*(EDouble lhs, const EDouble &rhs) {
         lhs *= rhs;
         return lhs;
     friend constexpr
          EDouble operator/(EDouble lhs, const EDouble &rhs) {
     friend constexpr bool
           operator <(const EDouble &lhs, const EDouble &rhs) {</pre>
         return lhs.x - rhs.x < -Eps;</pre>
     friend constexpr bool
           operator > (const EDouble &lhs, const EDouble &rhs) {
         return lhs.x - rhs.x > Eps;
     friend constexpr bool
    operator==(const EDouble &lhs, const EDouble &rhs) {
    return fabs(lhs.x - rhs.x) < Eps;</pre>
     friend constexpr bool
           operator <=(const EDouble &lhs, const EDouble &rhs) {</pre>
         return lhs < rhs || lhs == rhs;
     friend constexpr bool
           operator >= (const EDouble &lhs, const EDouble &rhs) {
         return lhs > rhs || lhs == rhs;
     return !(lhs == rhs);
```

friend istream &operator>>(istream &is, EDouble &a) {

double v; is >> v;

2 Graph

2.1 DFS 跟 BFS [cdd1d5]

```
int main() {
      int n;
      vector < vector < int >> adj(n + 1, vector < int >());
      // dfs_graph
      vector < bool > vis(n + 1, 0);
auto dfs = [&](auto self, int u) -> void {
           if (vis[u]) return;
vis[u] = true;
for (auto v: adj[u]) {
    self(self, v);
           }
      dfs(dfs, 1);
      // bfs
      vector<int> depth(n + 1, 1e9);
     queue <int> depth(u + 1, 1e9),
queue <int> q;
auto bfs = [&](auto self, int u) -> void {
    vis[u] = true;
    depth[u] = 0;
            q.push(u);
            vis[v] = true;
depth[v] = depth[u] + 1;
                        q.push(v);
                 }
           }
     bfs(bfs, 1);
```

2.2 Prim [f00ec0]

2.3 BellmanFord [430ded]

```
}
}
if (t == -1) { cout << "NO\n"; return; }
for (int i = 1; i < n; i++) t = par[t];
vector cint> ans {t};
int i = t;
do {
    i = par[i];
    ans.push_back(i);
} while (i != t);
reverse(ans.begin(), ans.end());
cout << "YES\n";
for (auto x : ans) cout << x + 1 << " ";
}</pre>
```

2.4 FloydWarshall [206b76]

```
const int inf = 1e18;
int main() {
      int n, m, q; cin >> n >> m >> q;
vector<vector<int>> graph(n + 1, vector<int>(n + 1, inf));
vector<vector<int>> dis(n + 1, vector<int>(n + 1));
      for (int i = 0; i < m; i++) {
            int u, v, w; cin >> u >> v >> w;
cin >> u >> v >> w;
graph[u][v] = min(graph[u][v], w);
             graph[v][u] = min(graph[v][u], w);
      for (int i = 0; i <= n; i++) {
    for(int j = 0; j <= n; j++) {
        dis[i][j] = graph[i][j];
}</pre>
      for (int i = 0; i <= n; i++) // 自己到自己是 Ø dis[i][i] = 0;
      for (int k = 1; k <= n; k++) {</pre>
             for (int i = 1; i <= n; i++) {
    for (int j = 1; j <= n; j++) {
        dis[i][j</pre>
                                 ] = min(dis[i][j], dis[i][k] + dis[k][j]);
                   }
            }
      for (int i = 0; i < q; i++) {
             int u. v: cin >> u >>
             cout << (dis[u][v] >= inf ? -1 : dis[u][v]) << "\n";</pre>
}
```

2.5 **歐拉環與歐拉路** [0911ed]

```
| // 無向圖、尤拉環:檢查每個點的出度為偶數
// 有向圖、
       尤拉路:可以看成 1 走到 n,所以檢查所有點的出度等於入度
 int n, m;
const int maxn = 1e5 + 5;
 vector<set<int>> adj;
 vector<int> in;
void dfs(int now, vector<int> &road) {
      while (!adj[now].empty()) {
  int nxt = *adj[now].begin();
  adj[now].erase(nxt);
            dfs(nxt, road);
       road.push_back(now);
 void solve() {
       cin >> n >> m;
      in >> m;
in.assign(n + 1, 0);
adj.assign(n + 1, set<int>());
for (int i = 1; i <= m; i++) {
   int u, v; cin >> u >> v;
   adj[u].insert(v);
}
            in[v]++;
       in[1]++;
       in[n]--;
       for (int i = 1; i <= n; i++) {
    if(adj[i].size() != in[i]) {</pre>
                 cout << "IMPOSSIBLE";
                  return;
           }
       vector<int> road;
       dfs(1, road);
       if (road.size() != m + 1) {
            cout << "IMPOSSIBLE";
            return:
       reverse(road.begin(), road.end());
road.cout < i << " ";</pre>
       for(auto i : road) cout << i <<</pre>
```

2.6 SCC [5d3e16]

```
struct SCC {
    int n, cur, cnt;
    vector<vector<int>> adj;
    vector<int>> stk, dfn, low, bel;
```

```
SCC(int n_ = 0) {
    init(n_);
      void init(int n_) {
           n = n_;
           adj.assign(n, {});
           dfn.assign(n, -1);
low.resize(n);
           bel.assign(n, -1);
           stk.clear();
           cur = cnt = 0:
     void addEdge(int u, int v) {
   adj[u].push_back(v);
      void dfs(int x) {
    dfn[x] = low[x] = cur++;
    stk.push_back(x);
           for (auto y : adj[x]) {
    if (dfn[y] == -1) {
                      else if (bel[y] == -1) {
    low[x] = min(low[x], dfn[y]);
           if (dfn[x] == low[x]) {
                 int y;
                bel[y] = cnt;
                      stk.pop_back();
                 } while (y != x);
                 cnt++:
           }
      vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
           return bel:
      struct Graph {
           int n:
           vector<pair<int, int>> edges;
           vector<int> siz;
vector<int> cnte;
      Graph compress() {
           Graph g;
g.n = cnt;
           g.siz.resíze(cnt);
           g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
                 g.siz[bel[i]]++;
                 for (auto j : adj[i]) {
    if (bel[i] != bel[j]) {
                           g.edges.emplace_back(bel[i], bel[j]);
                           g.cnte[bel[i]]++;
                }
           return a:
};
```

2.7 VBCC [170604]

```
struct VBCC {
     int n, cur;
     vector < int >> adj;
     vector <int> dfn, low, parent;
vector <bool> is_cut;
     VBCC(int n_ = 0) 
          init(n_);
     void init(int n_) {
          n = n_;
adj.assign(n, {});
dfn.assign(n, -1);
          low.resize(n);
          parent.assign(n, -1);
          is_cut.assign(n, false);
          cur = 0;
     void addEdge(int u, int v) {
   adj[u].push_back(v);
          adj[v].push_back(u);
     void dfs(int x) {
          int children = 0;
dfn[x] = low[x] = cur++;
for (int v : adj[x]) {
               if (dfn[v] == -1) {
                    children++;
parent[v] = x;
                    low[x] = min(low[x], low[v]);
                     if (parent[x] != -1 && low[v] >= dfn[x]) {
                          is_cut[x] = true;
```

```
} else if (v != parent[x]) {
   low[x] = min(low[x], dfn[v]);
              }
          if (parent[x] == -1 && children > 1) {
    is_cut[x] = true;
         }
    }
    }
};
```

2.8 EBCC [49d862]

```
struct EBCC { // CF/contest/1986/pF
   int n, cur, cnt;
       vector<vector<int>> adj;
       vector<int> stk, dfn, low, bel;
       vector<pair<int, int>> bridges; // 關鍵邊
       EBCC(int n_) {
             init(n_);
       void init(int n_) {
            n = n_;
adj.assign(n, {});
             dfn.assign(n, -1);
             low.resize(n);
             bel.assign(n, -1);
             stk.clear();
             bridges.clear();
             cur = cnt = 0;
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
             stk.push_back(x);
             for (auto y : adj[x]) {
   if (y == p) continue;
   if (dfn[y] == -1) {
                          dfs(y, x);
low[x] = min(low[x], low[y]);
if (low[y] > dfn[x]) {
                                 bridges.emplace_back(x, y);
                   } else if (bel[y] == -1) {
    low[x] = min(low[x], dfn[y]);
                    }
             if (dfn[x] == low[x]) {
                    int y;
do {
                          y = stk.back();
                          bel[y] = cnt;
                   stk.pop_back();
} while (y != x);
            }
       fvector<int> work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
        }
}</pre>
             return bel;
       struct Graph {
             int n:
             vector<pair<int, int>> edges;
             vector<int> siz; // BCC 內節點數
             vector<int> cnte; // BCC 內邊數
       Graph compress() {
             Graph g;
             g.n = cnt;
             g.siz.resize(cnt);
             g.cnte.resize(cnt);
             g.chte.restze(chr),
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;
    for (auto j : adj[i]) {
        if (bel[i] < bel[j]) {
            g.edges.emplace_back(bel[i], bel[j]);
        } else if (i < j) {
            g.cnte[bel[i]]++;
        }
}</pre>
                          }
                   }
             return g;
      }
```

2.9 2-SAT [eeddc1]

```
// CSES Giant Pizza
struct TwoSat {
     int n;
      vector<vector<int>> e:
      vector<bool> ans;
      vector volus airs,
TwoSat(int n) : n(n), e(2 * n), ans(n) {}
void addClause(int u, bool f, int v, bool g) {
    e[2 * u + !f].push_back(2 * v + g);
    e[2 * v + !g].push_back(2 * u + f);
      bool satisfiable() {
             vector<int
                   > id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
             vector<int> stk;
             int now = 0, cnt = 0;
function<void(int)> tarjan = [&](int u) {
                  stk.push_back(u);

dfn[u] = low[u] = now++;

for (auto v : e[u]) {

    if (dfn[v] == -1) {
                          tarjan(v);
  low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in stk
  low[u] = min(low[u], dfn[v]);
                    if (dfn[u] == low[u]) {
                          int v;
                          do {
    v = stk.back();
                                stk.pop_back();
id[v] = cnt;
                          } while (v != u);
                          ++cnt:
                  }
             for (int i
             return true:
      vector < bool > answer() { return ans; }
int main() {
     main() {
int m, n; cin >> m >> n;
TwoSat ts(n);
for (int i = 0; i < m; ++i) {
   int u, v; char x, y;
   cin >> x >> u >> y >> v;
   ts.addClause(u - 1, x == '+', v - 1, y == '+');
}
      if (ts.satisfiable()) {
             for (int i = 0; i < n; ++i) {
   cout << (ts.answer()[i] ? '+' : '-') << " ";</pre>
      else cout << "IMPOSSIBLE\n";</pre>
```

2.10 Funtional Graph [85c464]

```
constexpr int N = 2e5 + 5;
int cht[N][31]; // 倍增表,放外面不然 TLE struct FuntionalGraph {
       int n, cnt;
vector <int> g, bel, id, len, in, top;
FuntionalGraph() : n(0) {}
FuntionalGraph(vector <int> g_) { init(g_); }
        void init(vector < int > g_) {
    n = g_.size(); cnt = 0;
    g = g_; bel.assign(n, -
                id.resize(n); len.clear();
in.assign(n, 0); top.assign(n, -1);
                build();
        in[g[i]]++;
                for (int i = 1; i <= 30; i++)
               for (int i = 1; t <= 30; t++)
    for (int u = 0; u < n; u++)
        cht[u][i] = cht[cht[u][i - 1]][i - 1];
for (int i = 0; i < n; i++)
    if (in[i] == 0) label(i);
for (int i = 0; i < n; i++)
    if (top[i] == -1) label(i);</pre>
        void label(int u) {
   vector<int> p; int cur = u;
   while (top[cur] == -1) {
                       top[cur] = u;
                       p.push_back(cur);
cur = g[cur];
                auto s = std::find(p.begin(), p.end(), cur);
                vector <int> cyc(s, p.end());
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {</pre>
```

```
bel[cyc[i]] = cnt;
id[cyc[i]] = i;
        cnt++; len.push_back(cyc.size());
for (int i = p.size() - 1; i > 0; i--)
    id[p[i - 1]] = id[p[i]] - 1;
int jump(int u, int k) {
   for (int b = 0; k > 0; b++){
      if (k & 1) u = cht[u][b];
                 k >>= 1:
         return u:
```

3 **Data Structure**

3.1 BIT [d41d8c]

```
template <typename T>
 struct Fenwick { // 全部以 0 based 使用 int n;
       vector<T> a;
       Fenwick(int n_ = 0) {
             init(n_);
       void init(int n_) {
             a.assign(n, T{});
       void add(int x, const T &v) {
   for (int i = x + 1; i <= n; i += i & -i) {
      a[i - 1] = a[i - 1] + v;
}</pre>
       T sum(int x) { // 左閉右開查詢
T ans{};
for (int i = x; i > 0; i -= i & -i) {
ans = ans + a[i - 1];
             return ans;
       TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
       int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
             int x = 0;
T cur{};
             for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n && cur + a[x + i - 1] <= k) {
        x += i;</pre>
                         cur = cur + a[x - 1];
                   }
             return x:
      }
 };
 template <class T>
 struct TwoDFenwick { // 全部以 0 based 使用
       int nx, ny; // row, col 個數
vector<vector<T>> a;
TwoDFenwick(int nx_ = 0, int ny_ = 0) {
  init(nx_, ny_);
       void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;

             a.assign(nx, vector<T>(ny, T{}));
       void add(int x, int y, const T &v) {
             for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        a[i - 1][j - 1] = a[i - 1][j - 1] + v;
            }
       T sum(int x, int y) { // 左閉右開查詢 T ans{};
             for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans + a[i - 1][j - 1];
}
             }
return ans;
       T rangeSum
              (int lx, int ly, int rx, int ry) { // 左閉右開查詢
             return sum(
                   rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
       }
};
```

3.2 RangeBit [d41d8c]

```
| template <typename T>
struct rangeFenwick { // 全部以 0 based 使用
     int n;
     vector <T> d, di;
     rangeFenwick(int n_ = 0) {
        init(n_);
```

vector < int > boss, siz;

```
DSU() {}
DSU(int n_) {
       void init(int n_) {
                                                                                                                               init(n_);
             d.assign(n, T{});
di.assign(n, T{});
                                                                                                                        void init(int n_) {
      Joid add(int x, const T &v) {
   T vi = v * (x + 1);
   for (int i = x + 1; i <= n; i += i & -i) {
        d[i - 1] = d[i - 1] + v;
        di[i - 1] = di[i - 1] + vi;
}</pre>
                                                                                                                               boss.resize(n);
iota(boss.begin(), boss.end(), 0);
                                                                                                                               siz.assign(n, 1);
                                                                                                                        int find_boss(int x) {
   if (boss[x] == x) return x;
   return boss[x] = find_boss(boss[x]);
      void rangeAdd(int l, int r, const T &v) {
  add(l, v); add(r, -v);
                                                                                                                        bool same(int x, int y) {
    return find_boss(x) == find_boss(y);
      T sum(int x) { // 左閉右開查詢
                                                                                                                        bool merge(int x, int y) {
    x = find_boss(x);
    y = find_boss(y);
    ...
             for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
                                                                                                                               if (x == y) {
    return false;
             return ans;
                                                                                                                               if(siz[x] < siz[y]) swap(x, y);
siz[x] += siz[y];</pre>
      TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
                                                                                                                               boss[y] = x;
                                                                                                                               return true;
       int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
              int x = 0;
                                                                                                                        int size(int x) {
    return siz[find_boss(x)];
              T cur{};
              for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n) {
        T val = T(</pre>
                                                                                                                       }
                                                                                                                 };
                           x + i + 1) * d[x + i - 1] - di[x + i - 1];

if (cur + val <= k) {

x += i;
                                                                                                                 struct DSU {
                                                                                                                        int n;
                                                                                                                        vector<int> boss, siz, stk;
                                  cur = cur + val;
                                                                                                                        DSU() {}
DSU(int n_) {
                           }
                   }
                                                                                                                               init(n_);
              return x;
                                                                                                                        void init(int n_) {
     }
                                                                                                                               boss.resize(n);
template <class T>
                                                                                                                               iota(boss.begin(), boss.end(), 0);
struct rangeTwoDFenwick { // 全部以 0 based 使用
                                                                                                                               siz.assign(n, 1);
      int nx, ny; // row, col 個數
vector <vector <T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
                                                                                                                               stk.clear():
                                                                                                                        int find(int x) {
   return x == boss[x] ? x : find(boss[x]);
             init(nx_, ny_);

void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
}

                                                                                                                        bool same(int x, int y) {
   return find(x) == find(y);
                                                                                                                        bool merge(int x, int y) {
                                                                                                                              x = find(x);
y = find(y);
                                                                                                                               if (x == y)
       T void add(int x, int y, const T &v) {
   T vi = v * (x + 1);
   T vj = v * (y + 1);
   T vij = v * (x + 1) * (y + 1);
   T vij = v * (x + 1) * (y + 1);
                                                                                                                                      return false;
                                                                                                                               if (siz[x] < siz[y]) swap(x, y);
                                                                                                                               siz[x] += siz[y];
             for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        d[i - 1][j - 1] = d[i - 1][j - 1] + v;
        di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
        dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
        dij[i - 1][j - 1] = dij[i - 1][j - 1] + vj;
}</pre>
                                                                                                                               boss[y] = x;
                                                                                                                               stk.push_back(y);
                                                                                                                               return true;
                                                                                                                        void undo(int x) {
                                                                                                                               while (stk.size() > x) {
    int y = stk.back();
                   }
             }
                                                                                                                                      stk.pop_back();
       void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
             add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
                                                                                                                                      siz[boss[y]] -= siz[y];
                                                                                                                                      boss[y] = y;
                                                                                                                        int size(int x) {
    return siz[find(x)];
      T sum(int x, int y) { // 左閉右開查詢
              T ans{};
                                                                                                                };
              for (int i = x; i > 0; i -= i & -i) {
                    for (int j = y; j > 0; j -= j & -j) {
                           ans = ans

+ T(x * y + x + y + 1) * d[i - 1][j - 1];

ans = ans - T(y + 1) * di[i - 1][j - 1];

ans = ans - T(x + 1) * dj[i - 1][j - 1];

ans = ans + dij[i - 1][j - 1];
                                                                                                                 3.4 線段樹 [d41d8c]
                                                                                                               | template <class Info>
                                                                                                                 struct Seg { // 左閉右開寫法
int n; vector xInfo > info;
Seg(): n(0) {}
Seg(int n_, Info v_ = Info()) {
                   }
             return ans:
                                                                                                                               init(n_, v_);
       }
T rangeSum
                                                                                                                        template <class T>
Seg(vector<T> init_) {
   init(init_);
              (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                     (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
                                                                                                                        void init(int n_, Info v_ = Info()) {
  init(vector(n_, v_));
3.3 DSU [d41d8c]
                                                                                                                        template <class T>
                                                                                                                        void init(vector<T> init_) {
struct DSU {
                                                                                                                               n = init_.size();
```

info.assign(4 << __lg(n), Info());</pre>

```
info[p] = init_[l];
                int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                pull(p);
           build(1, 0, n);
     void pull
     (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
                info[p] = v;
           int m = (l + r) / 2;
                modify(2 * p, l, m, x, v);
               modify(2 * p + 1, m, r, x, v);
          pull(p);
     void modify(int p, const Info &i) {
          modify(1, 0, n, p, i);
     Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;</pre>
           return query(p *
                2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
           (int ql, int qr) { return query(1, 0, n, ql, qr); }
     template < class F> // 尋找區間內,第一個符合條件的
     int findFirst
          (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)</pre>
          return -1;
if (l >= x && r <= y && !pred(info[p]))</pre>
                return -1;
          if (r - l == 1)
               return l;
           int m = (l + r) / 2;
           int res = findFirst(2 * p, l, m, x, y, pred);
          if (res == -1)
                res = findFirst(2 * p + 1, m, r, x, y, pred);
          return res;
     template < class F> // 若要找 last, 先右子樹遞迴即可
int findFirst(int l, int r, F & & pred) {
    return findFirst(1, 0, n, l, r, pred);
};
// ---define structure and info plus---
struct Info {
     int n = 1;
     int sum = 0;
Info operator+(const Info &a, const Info &b) {
   return { a.n + b.n, a.sum + b.sum };
```

3.5 懶標線段樹 [d41d8c]

```
pull(p):
            build(1, 0, n);
      (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
  info[p].apply(l, r, v);
            tag[p].apply(v);
      void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
            tag[p] = Tag();
      void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
                   info[p] = v;
            int m = (l + r) / 2;
            push(p, l, r);
            if (x < m) {
                  modify(2 * p, l, m, x, v);
            } else {
                  modify(2 * p + 1, m, r, x, v);
            pull(p);
      void modify(int p, const Info &i) {
    modify(1, 0, n, p, i);
      Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];</pre>
            int m = (l + r) / 2;
push(p, l, r);
            return query(p *
                   2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      Info query
    (int ql, int qr) { return query(1, 0, n, ql, qr); }
            inlange_apply
  (int p, int l, int r, int ql, int qr, const Tag &v) {
  if (qr <= l || ql >= r) return;
  if (ql <= l && r <= qr) {</pre>
                  apply(p, l, r, v);
                  return:
            int m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
            pull(p):
      void range_apply(int l, int r, const Tag &v) {
    range_apply(1, 0, n, l, r, v);
      template < class F> // 尋找區間內,第一個符合條件的
      int findFirst
            (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
   return -1;</pre>
             if (l >= x && r <= y && !pred(info[p])) {</pre>
                   return -1;
            if (r - l == 1) {
                   return l:
            int m = (l + r) / 2;
            push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
                  res = findFirst(2 * p + 1, m, r, x, y, pred);
      template < class F> // 若要找 last,先右子樹遞迴即可int findFirst(int l, int r, F & pred) {
    return findFirst(1, 0, n, l, r, pred);
};
// ---define structure and info plus---
struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add;
      void apply(const Tag& v) {
            if (v.set_val) {
    set_val = v.set_val;
                  add = v.add;
            else {
                  add += v.add;
     }
struct Info {
      int sum;
```

```
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void apply(int l, int r, const Tag &v) {
    if (v.set_val) {
        sum = (r - l) * v.set_val;
    }
    sum += (r - l) * v.add;
}

// Info& operator=(const Info &rhs) {
    // 部分 assignment 使用
    // return *this;

// }

};

Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
}

3.6 莫隊 [d41d8c]

struct query {
    int l, r, id;
} typedef query;
void MO(int n, vector<query> &queries) {
    int block = sqrt(n);
    function <bool(query, query)> cmp = [&](query a, query b) {
        int block_a = a.l / block;
        int block_b = b.l / block;
        if (block_a != block_b) return block_a < block_b;
        return a.r < b.r;
```

sort(queries.begin(), queries.end(), cmp);

(unique(sorted.begin(), sorted.end()), sorted.end());

(), sorted.end(), nums[i]) - sorted.begin() + 1;

sort(sorted.begin(), sorted.end());

for (int i = 0; i < nums.size(); i++) {
 nums[i] = lower_bound(sorted.begin</pre>

void compress(vector<int> &nums) {
 vector<int> sorted = nums;

3.7 Treap [d41d8c]

sorted.erase

```
Treap(int val_) {
    min = val = val_;
    pri = rand();
            lc = rc = nullptr;
siz = 1; rev_valid = 0;
      void pull() { // update siz or other information
            siz = 1;
min = val;
            for (auto c : {lc, rc}) {
                 if (!c) continue;
siz += c->siz;
                  min = std::min(min, c->min);
            }
       void push() {
            if (rev_valid) {
                  if (lc, rc);
if (lc) lc->rev_valid ^= 1;
if (rc) rc->rev_valid ^= 1;
            rev_valid = false;
      int find(int k) { // 找到 min 是 k 的位置 (1-based)
            push();
int ls = (lc ? lc->siz : 0) + 1;
            if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
     }
int size(Treap *t) {
    return t ? t->siz : 0;
Treap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
    a->push(); b->push();
      if (a->pri > b->pri) {
            a->rc = merge(a->rc, b);
a->pull();
            return a;
      else {
            b->lc = merge(a, b->lc);
            b->pull();
            return b;
      }
pair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
      t->push();
      if (size(t->lc) < k) {
    auto [a, b] = split(t->rc, k - size(t->lc) - 1);
```

```
t->rc = a;
t->pull();
return {t, b};
}
else {
    auto [a, b] = split(t->lc, k);
    t->lc = b;
    t->pull();
    return {a, t};
}

void Print(Treap *t) {
    if (!t) return;
    t->push();
    Print(t->lc);
    cout << t->val;
    Print(t->rc);
}
```

4 Flow

4.1 Dinic [287fe8]

```
template < class T>
struct Dinic {
     struct Edge {
         int to;
          T flow, cap; // 流量跟容量
     int n, m, s, t;
T INF_FlOW = numeric_limits<T>::max() / 2;
     vector<vector<int>> adj; // 此點對應的 edges 編號
     vector<Edge> edges; // 幫每個 edge 編號
     vector <int> dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
    n = n_; m = 0;
}
          dis.resize(n); ptr.resize(n);
          adj.assign(n, vector<int>{});
edges.clear();
     void add_edge(int u, int v, T cap) {
          // 偶數 id 是正向邊
          edges.push_back({ v, 0, cap });
edges.push_back({ u, 0, 0 });
           adj[u].push_back(m++);
          adj[v].push_back(m++);
          fill(dis.begin(), dis.end(), -1);
dis[s] = 0; queue<int> q;
          q.push(s);
          if (e.flow == e.cap) continue;
if (dis[e.to] == -1) {
                          dis[e.to] = dis[u] + 1;
                          q.push(e.to);
                     }
               }
          return dis[t] != -1;
     T dfs(int u, T flow) {
          if (flow == 0) return 0;
if (u == t) return flow;
           for (int
               &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {
Edge &e = edges[adj[u][cur]];
if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;
T mn = dfs(e.to, min(flow, e.cap - e.flow));
if (re.co)</pre>
                if (mn > 0) {
                     e.flow += mn;
                     edges[adj[u][cur] ^ 1].flow -= mn;
                     return mn;
               }
          return 0; // 到不了終點就會 return 0
     flow += res;
               }
          }
return flow;
     void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
}:
```

4.2 Min Cut [44ae6c]

```
' CSES Police Chase
 int main(){
         int n, m; cin >> n >> m;
Dinic < int >> g(n);
for (int i = 0; i < m; i++) {</pre>
                  int u, v, cap = 1;
cin >> u >> v;
                   u--; v--;
                   g.add_edge(u, v, cap);
                   g.add_edge(v, u, cap);
         int res = g.work(0, n - 1);
cout << res << "\n";
if (res == 0) return;</pre>
         vector <int> vis(n);
auto find = [&](auto self, int u) -> void {
   if (!vis[u]) {
                           vis[u] =
                           for (int id : g.adj[u]) {
   auto e = g.edges[id];
   if (e.cap - e.flow > 0) {
                                             self(self, e.to);
                           }
                 }
        };
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
        ruth e = g.edges[id];
        ruth e = g.edges[id];</pre>
                           auto e = g.edges[id];
if (!vis[e.to]) {
   cout << i + 1 << " " << e.to + 1 << " | n ";
                  }
         }
}
```

4.3 Hangarian [350fc3]

```
struct Hangarian { // 0-based
      int n, m; // 最小路徑覆蓋,二分匹配
vector<vector<int>> adj;
      vector <int>> auj,
vector <int> used, vis;
vector <pair <int, int>> match;
      Hangarian(int n_ = 0, int m_ = 0) {
   init(n_, m_);
       void init(int n_ = 0, int m_ = 0) {
            n = n_; m = m_;
adj.assign(n + m, vector < int >());
used.assign(n + m, -1);
vis.assign(n + m, 0);
       void addEdge(int u, int v) {
   adj[u].push_back(n + v);
   adj[n + v].push_back(u);
      vector<pair<int, int>>
    match.clear();
    used.assign(n + m,
                                int>> work() {
            return true:
                               }
                        }
                   return false;
             for (int i = 0; i < n; i++) {
    fill(vis.begin(), vis.end(), 0);
    dfs(dfs, i);</pre>
             for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
                         match.emplace_back(used[i], i - n);
             return match;
}:
```

4.4 MCMF [f667f8]

```
template < class Tf, class Tc > struct MCMF {
    // 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就好 int n, m, s, t;
    If INF_FLOW = numeric_limits < Tf >:: max() / 2;
    Tc INF_COST = numeric_limits < Tc >:: max() / 2;
    struct Edge {
        int to;
        If flow, cap; // 流量跟容量
        Tc cost;
```

```
vector < vector < int >> adj;
vector<Edge> edges; // 幫每個 edge 編號
vector<Tc> dis, pot; // johnson algorithm, using spfa
vector<int> rt; // 路徑恢復,對應 id
vector <book
vector <book
MCMF(int n_ = 0) { init(n_); }
void init(int n_ = 0) {</pre>
     n = n_;
m = 0;
       edges.clear();
adj.assign(n, vector<int>{});
void add_edge(int u, int v, Tf cap, Tc cost){
   edges.push_back({v, 0, cap, cost});
   edges.push_back({u, 0, 0, -cost});
       adj[u].push_back(m++);
adj[v].push_back(m++);
Jool spfa() {
    dis.assign(n, INF_COST);
    rt.assign(n, -1); inq.assign(n, false);
      q.push(v); inq[v] = true;
             }
       return dis[t] != INF_COST;
bool dijkstra() {
    dis.assign(n, INF_COST); rt.assign(n, -1);
      dis.assign(n, INF_COST); rt.assign(n, -1);
priority_queue<pair<Tc, int>,
    vector<pair<Tc, int>>, greater<pair<Tc, int>>> pq;
dis[s] = 0; pq.emplace(dis[s], s);
while (!pq.empty()) {
    auto [d, u] = pq.top(); pq.pop();
    if (dis[u] < d) continue;
    for (int id : adj[u]) {
        auto [v, flow, cap, cost] = edges[id];
        Tc ndis = dis[u] + cost + pot[u] - pot[v];
        if (flow < cap && dis[v] > ndis) {
            dis[v] = ndis; rt[v] = id;
            pq.emplace(ndis, v);
                            pq.emplace(ndis, v);
             }
       return dis[t] != INF_COST;
}
// 限定 flow, 最小化 cost
pair<Tf, Tc> work_flow(int s_, int t_, Tf need) {
       s = s_, t = t_; pot.assign(n, 0);
If flow{}; Tc cost{}; bool fr = true
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] += pot[i] - pot[s];
}</pre>
              (f, edges[rt[i]].cap - edges[rt[i]].flow);
              f = min<Tf>(f, need);
              for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
   edges[rt[i]].flow += f;
   edges[rt[i] ^ 1].flow -= f;
              flow += f; need -= f;
cost += f * dis[t]; fr = false;
              swap(dis, pot);
if (need == 0) break;
       return make_pair(flow, cost);
}
// 限定 cost, 最大化 flow
dis[i] += pot[i] - pot[s];
              ff f = INF_FLOW;
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                             (f, edges[rt[i]].cap - edges[rt[i]].flow);
              f = min < Tf > (f, budget / dis[t]);
              for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
   edges[rt[i]].flow += f;
```

```
edges[rt[i] ^ 1].flow -= f;
              flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
               swap(dis, pot);
              if (budget == 0 || f == 0) break;
          return make_pair(flow, cost);
     void reset() {
          for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
};
```

String 5

5.1 KMP [cddfd9]

```
struct KMP {
      string sub;
      vector <int> failure;
KMP(string sub_) {
    sub = sub_;
             failure.resize(sub.size(), -1);
             buildFailFunction();
      void buildFailFunction() {
   for (int i = 1; i < (int)sub.size(); i++) {
     int now = failure[i - 1];</pre>
                   while (now != -1
    && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
      vector < int > match(string &s) {
            for (int i = 0, now = -1; i < (int)s.size(); i++) {
    // now is the compare sucessed length -1
    while (s[i] !=</pre>
                           sub[now + 1] && now != -1) now = failure[now];
                   // failure stores if comparison fail, move to where if (s[i] == sub[now + 1]) now++;
                                + 1 == (int)sub.size()) {
                          match.push_back(i - now);
                          now = failure[now];
             return match;
};
```

5.2 Z Function [8dd6ac]

```
// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
// 的最長公共前綴 (LCP) 的長度
vector < int > Z(string s) {
   int n = s.size();
      vector<int> z(n);
      z[0] = n;
for (int i = 1, j = 1; i < n; i++) {
    z[i] = max(0, min(j + z[j] - i, z[i - j]));
    while (i + z[i] < n && s[z[i]] == s[i + z[i]]) {
        z[i]++;
}</pre>
            if (i + z[i] > j + z[j]) {
    j = i;
      return z; // 最後一格不算
```

5.3 Duval Algorithm [f9dcca]

```
// duval alaorithm
// 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
vector<string> duval(string s) {
   int i = 0, n = s.size();
   vector<string> res;
      while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
      else k++;
}</pre>
                  j++;
            while (i <= k) {
                  res.push_back(s.substr(i, j - k));
                  i += j - k;
           }
      return res;
// 最小旋轉字串
string min_round(string s) {
      s += s;
int i = 0, n = s.size();
      int start = i;
while (i < n / 2) {
    start = i;</pre>
            int k = i, j = i + 1;
```

```
while (s[k] <= s[j] && j < n) {
   if (s[k] < s[j]) k = i;</pre>
             else k++;
            j++;
      while (i <= k) {
    i += j - k;</pre>
return s.substr(start, n / 2);
```

5.4 Manacher [9c9ca6]

```
// 找到對於每個位置的迴文半徑
vector <int> manacher(string s) {
   string t = "#";
   for (auto c : s) {
           t += c;
           t += '#';
     int n = t.size();
      vector<int> r(n);
     for (int i = 0, j =
           0; i < n; i++) { // i 是中心, j 是最長回文字串中心 if (2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
           while (i - r[i] >=
      0 && i + r[i] < n && t[i - r[i]] == t[i + r[i]]) {</pre>
                 r[i] += 1;
           if (i + r[i] > j + r[j]) {
                j = i;
           }
     return r;
     // # a # b # a #

// 1 2 1 4 1 2 1

// # a # b # b # a #

// 1 2 1 2 5 2 1 2 1
     // 值 -1 代表原回文字串長度
     // (id - val + 1) / 2 可得原字串回文開頭
```

5.5 Trie [3b3aa0]

```
struct Trie {
      struct trie_node {
   bool is_word;
   vector<trie_node *> children;
   trie_node() {
      is_word = false;
      children.resize(26, NULL);
}
      trie_node *root = new trie_node();
void insert(string &s) {
            trie_node *cur = root;
for (int i = 0; i < s.size(); i++) {
   int idx = s[i] - 'a';
   if (cur->children[idx] == NULL) {
                          cur->children[idx] = new trie_node();
                    cur = cur->children[idx];
             cur->is_word = true;
      bool is_in_trie(string &s) {
    trie_node *cur = root;
    for (int i = 0; i < s.size(); i++) {
        if (cur->
                    children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
             return true:
       int search_i_start(string &s, int i, vector<int> &dp) {
             trie_node *cur = root;
int sz = s.size(), ans = 0;
for (int j = i; j < sz; j++) {
    if (cur</pre>
                    ->children[s[j] - 'a'] == nullptr) return ans;
cur = cur->children[s[j] - 'a'];
                    if (cur->is_word)
        (ans += dp[j + 1]) %= mod;
             return ans;
     }
int main() {
      // 找到 sub 集合裡,可以重複用,組成 s 的組數
Trie trie;
      string s; cin >> s;
int sz = s.size();
      // dp 代表 i 開頭到最後的配對總數
       ,,
// 找到有結尾為 stop 的 dp[i] += dp[j + 1]
      int n; cin >> n;
      vector < int > dp(sz + 1, 0);
for (int i = 0; i < n; i++) {
```

string sub; cin >> sub;

```
trie.insert(sub);
}
dp[sz] = 1;
for (int i = sz - 1; i >= 0; i--) {
    dp[i] = trie.search_i_start(s, i, dp);
}
cout << dp[0] << endl;
}</pre>
```

6 Math

6.1 質因數分解 [ee1622]

6.2 模除計算 [9b1014]

```
using i64 = long long;
template < class T>
constexpr T power(T a, i64 b) {
     for (; b; b /= 2, a *= a) {
    if (b % 2) {
        res *= a;
    }
          }
     return res;
}
constexpr i64 mul(i64 a, i64 b, i64 p) {
   i64 res = a * b - i64(1.L * a * b / p) * p;
   res %= p;
   if (res < 0) {</pre>
          res += p;
     return res:
template < i64 P>
struct MLong {
     i64 x;
     constexpr MLong() : x{} {}
constexpr MLong(i64 x) : x{norm(x % getMod())} {}
     static i64 Mod;
     constexpr static i64 getMod() {
   if (P > 0) {
               return P;
          } else {
               return Mod;
     constexpr static void setMod(i64 Mod_) {
   Mod = Mod_;
     constexpr i64 norm(i64 x) const {
          if (x < 0) {
              x += getMod();
           if (x >= getMod()) {
               x -= getMod();
           return x;
     constexpr i64 val() const {
          return x:
     explicit constexpr operator i64() const {
```

```
return x:
      constexpr MLong operator -() const {
            MLong res;
res.x = norm(getMod() - x);
            return res;
      constexpr MLong inv() const {
   assert(x != 0);
   return power(*this, getMod() - 2);
      constexpr MLong &operator*=(MLong rhs) & {
            x = mul(x, rhs.x, getMod());
return *this;
      constexpr MLong &operator+=(MLong rhs) & {
            x = norm(x + rhs.x);
return *this;
      constexpr MLong &operator -= (MLong rhs) & {
           x = norm(x - rhs.x);
return *this;
      constexpr MLong &operator/=(MLong rhs) & {
    return *this *= rhs.inv();
      friend constexpr MLong operator*(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res *= rhs;
            return res;
      friend constexpr MLong operator+(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res += rhs;
            return res:
      friend constexpr MLong operator-(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res -= rhs;
            return res;
      friend constexpr MLong operator/(MLong lhs, MLong rhs) {
           MLong res = lhs;
res /= rhs;
      friend
             constexpr istream &operator>>(istream &is, MLong &a) {
            i64 v;
            is >> v;
a = MLong(v);
            return is;
      friend constexpr
              ostream &operator<<(ostream &os, const MLong &a) {
            return os << a.val();</pre>
      friend constexpr bool operator==(MLong lhs, MLong rhs) {
           return lhs.val() == rhs.val();
      friend constexpr bool operator!=(MLong lhs, MLong rhs) {
   return lhs.val() != rhs.val();
}:
template<>
i64 MLong<0LL>::Mod = i64(1E18) + 9;
constexpr i64 P = 998244353;
using Z = MLong <P>;
// using Z = MLong <0LL>; // change Mod
struct Comb {
      i64 n;
     to4 n,
vector <Z> _fac;
vector <Z> _invfac;
vector <Z> _inv;
Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
Comb(i64 n) : Comb() { init(n); }
      void init(i64 m) {
           m = min(m, Z::getMod() - 1);
if (m <= n) return;
_fac.resize(m + 1);</pre>
            _invfac.resize(m + 1);
            _inv.resize(m + 1);
            for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;</pre>
            for (int i = _fac[m].inv();
for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
            n = m;
      If ac(i64 m) {
   if (m > n) init(2 * m);
   return _fac[m];
      Z invfac(i64 m) {
```

6.3 中國餘數定理 [d41d8c]

```
ll exgcd(ll a, ll b, ll &x, ll &y) {
   if (!b) {
      x = 1, y = 0;
}
             return a;
      ll g = exgcd(b, a % b, y, x);
y -= a / b * x;
      return g;
ll inv(ll x, ll m){
      ll a, b;
      exgcd(x, m, a, b);
      a \% = m;
if (a < 0) a += m;
      return a;
// remain, mod
ll CRT(vector<pair<ll, ll>> &a){
   remain, mod
      ll prod = 1;
for (auto x : a) {
    prod *= x.second;
      }
ll res = 0;
      for (auto x : a) {
   auto t = prod / x.second;
   res += x.first * t % prod * inv(t, x.second) % prod;
   if(res >= prod) res -= prod;
       return res;
}
```

6.4 矩陣與快速幕 [08b5fe]

```
template < class T>
struct Mat {
     int m, n;
     constexpr static ll mod = 1e9 + 7;
     constexpr stattc it mou = les + /,
vector <vector <T>> matrix;
Mat(int n_ = 0) { init(n_, n_); }
Mat(int m_, int n_) { init(m_, n_); }
Mat(vector <vector <T>> matrix_) { init(matrix_); }
     void init(int m_, int n_) {
    m = m_; n = n_;
           matrix.assign(m, vector<T>(n));
     void init(vector<vector<T>> &matrix_) {
          m = matrix_.size();
n = matrix_[0].size();
           matrix = matrix_;
                                                   // 單位矩陣
     vector<vector<T>> unit(int n) {
          vector < r >> vector < r >> res(n, vector < T > (n));

for (int i = 0; i < n; i++) {
               res[i][i] = 1;
           return res;
     constexpr Mat &operator*=(const Mat& rhs) & {
           assert(matrix[0].size() == rhs.matrix.size());
int m = matrix.size()
                 , k = matrix[0].size(), n = rhs.matrix[0].size();
           Mat ans(m, n);
for (int i = 0; i < m; i++) {
                }
                }
           matrix = ans.matrix;
return *this;
     constexpr Mat &operator^=(ll p) & {
           assert(m == n); assert(p >= 0);
Mat ans(p-- == 0 ? unit(m) : matrix);
           while (p > 0) {
   if (p & 1) ans *= *this;
   *this *= *this;
```

```
matrix = ans.matrix;
return *this;
}
friend Mat operator*(Mat lhs, const Mat &rhs) {
    lhs *= rhs;
    return lhs;
}
friend Mat operator*(Mat lhs, const ll p) {
    lhs ^= p;
    return lhs;
}
;
// fn = fn - 3 + fn - 2 + fn - 1
// 初始矩陣 轉移式
// f4 f3 f2 1 1 0 f5 f4 f3
// f3 f2 f1 1 0 1 => f4 f3 f2
// f2 f1 f0 1 0 0 f3 f2 f1
```

6.5 樹論分塊 [06204a]

6.6 Mobius Theorem

- 數 論 分塊 可 以 快 速 計 算 一 些 含 有 除 法 向 下 取 整 的 和 式 , 就 是 像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理 出 f 的 前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d|n} \mu(d) = \begin{cases} 1 & \text{for } n = 1 \\ 0 & \text{for } n \neq 0 \end{cases}$$

- 2. μ 是常數函數 1 的反元素 $\Rightarrow \mu*1=\epsilon$, $\epsilon(n)$ 只在n=1時為 1 , 其餘情況皆為 0 。
- $-\phi$ 歐拉函數: x以下與x互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^i) \\ &= 1 + p^0(p-1) + p^1(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^c \\ &= id \end{split}$$

• 莫比烏斯反演公式

```
- f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})

- f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)
```

例子

$$\begin{split} &\sum_{i=a}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

莫比烏斯反演 [d41d8c]

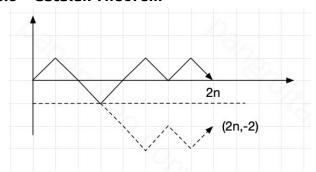
```
const int maxn = 2e5;
ll mobius_pref[maxn];
void init() {
       mobius_pref[1] = 1;
       vector<ll> wei
       (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
}
                     continue; // 包含平方
              fif (wei[i] == 0) {
    wei[i] = 1;
    for (ll j = 2; i * j < maxn; j++) {
        if (j % i == 0) wei[i * j] = -1;
        else if (wei[i * j] != -1) wei[i * j]++;
}</pre>
              mobius_pref[i]
                      = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
}
void solve() {
       ll a, b, c, d, k; cin >> a >> b >> c >> d >> k;
auto cal = [&](ll x, ll y) -> int {
             int res = 0;

for (int l = 1, r; l <= min(x, y); l = r + 1) {

    r = min(x / (x / l), y / (y / l));

    res += (mobius_pref[r] - mobius_pref[l
                              - 1]) * (x / l) * (y / l); // 代推出來的式子
              return res;
       cout << cal
               (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k, (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n";
}
```

Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2)

假設往上有x個,往下有y個,會有:

$$\begin{cases} x\!+\!y\!=\!2n \\ y\!-\!x\!=\!2 \end{cases} \Rightarrow \begin{cases} x\!=\!n\!-\!1 \\ y\!=\!n\!+\!1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.9 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- · G:各種翻轉操作所構成的置換群
- X/G: 本質不同的方案的集合 X/G: 對於某一種操作 g, 所有方案中, 經過 g 這種翻轉後保持不變的方案 的集合
- 集合取絕對值代表集合數

Search and Gready

二分搜 [d41d8c]

```
int main() {
          int l = 1, r = 10;
// 1 to tar, find tar
while (l <= r) {
   int m = (l + r) / 2;
   int m = (l + r) / 2;
}</pre>
                     if (check(m)) l = m + 1;
else r = m - 1;
          cout << r;
          // tar to end
while (l <= r) {
    int m = (l + r) / 2;
    if (check(m)) r = m - 1;
    else l = m + 1;
          cout << 1:
```

7.2 三分搜 [d41d8c]

```
// 找極值問題,遞增遞減
void solve() {
     int l = 0, r = 10, ans = 0; // ans 紀錄答案
while (l <= r) {
          int d = (r - l) / 3; // 差
          int ml = l + d, mr = r - d; // mr 要用減的
auto cal = [&](int m) -> int {
               int x = 0;
               return x; // 計算答案
          int ansl = cal(ml), ansr = cal(mr);
if (ansl < ansr) {
    l = ml + 1;</pre>
          else r = mr - 1;
     }
```

Tree 8

LCA [9f95b1]

```
vector<vector<int>> par(maxn, vector<int>(18));
vector < int > depth(maxn + 1);
vector < int > dfn(maxn);
vector<int> dfn(maxn);
void build_lca(int n, vector<vector<pair<int, int>>> &tree) {
   auto dfs = [&](auto self, int u, int pre) -> void {
     for (auto [v, w] : tree[u]) {
        if (v == pre) continue;
        par[v][0] = u; // 2 ^ 0
        depth[v] = depth[u] + 1;
        self(self, v, u);
}
                     }
          f;
dfs(dfs, 1, 0);
for (int i = 1; i <= 18; i++) {
    for (int j = 1; j <= n; j++) {
        par[j][i] = par[par[j][i - 1]][i - 1];
}</pre>
          }
int lca(int a, int b) {
          if (depth[a] < depth[b]) swap(a, b);
int pull = depth[a] - depth[b];
for (int i = 0; i < 18; i++) {
    if (pull & (1 << i)) {
        a = par[a][i];
}</pre>
          fif (a == b) return a;
for (int i = 17; i >= 0; i--) {
    if (par[a][i] != par[b][i])
                                a = par[a][i], b = par[b][i];
           return par[a][0];
```

8.2 樹重心 [30b436]

```
struct centroid_decomposition {
    int n;
    vector<vector<int>> adj;
    vector < bool > vis;
    vector<int> siz;
    centroid_decomposition() {}
    centroid_decomposition(int n_) { init(n_); }
```

```
void init(int n_) {
           n = n_{j}
           adj.assign(n, {});
vis.assign(n, false);
siz.assign(n, 1);
     void addEdge(int u, int v) {
   adj[u].push_back(v);
           adj[v].push_back(u);
     void get_siz(int dep, int x, int p = -1) {
           }
     fint get_cen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz) {
                       return get_cen(y, sz, x);
                 }
           return x;
      void work(int x = 0) {
           get_siz(0, x);
           int cen = get_cen(x, siz[x]);
vis[cen] = true;
            // do something
           for (int y : adj[cen]) {
   if (vis[y]) continue;
                 work(y);
           }
}:
```

8.3 樹壓平 [51199c]

```
| // 父節
      點加值 = 所有子節點區間加值,求單點,使用 bit,做前綴差分
 // CSES 1138_Path Queries
 int main(){
     int n, q; cin >> n >> q;
vector <int >> node_value(n + 1), euler_ordered_value(n);
for (int i = 1; i <= n; i++) {
    cin >> node_value[i];
}
      vector<vector<int>> tree(n + 1);
      for (int i = 1; i < n; i++) {
   int u, v; cin >> u >> v;
           tree[u].push_back(v);
           tree[v].push_back(u);
      vector<pair<int, int>> tree_mapping(n + 1);
      int cnt = 0;
auto dfs = [&](auto self, int u, int par) -> void {
    euler_ordered_value[++cnt] = node_value[u];
           tree_mapping[u].first = cnt;
           for (auto v : tree[u]) {
   if (v == par) continue;
   self(self, v, u);
           tree_mapping[u].second = cnt;
      dfs(dfs, 1, 0);
      BIT bit(n);
for (int i = 1; i <= n; i++) {
           bit.modify(tree_mapping[i].first, node_value[i]);
           if (tree_mapping[i].first < n) { // root 就不用扣了</pre>
                bit.modify
                     (tree_mapping[i].second + 1, -node_value[i]);
           }
      for (int i = 0; i < q; i++) {
           int op; cin >> op;
if (op == 1) {
                int s, x; cin >> s >> x;
int add = x
                       euler_ordered_value[tree_mapping[s].first];
                euler_ordered_value[tree_mapping[s].first] = x;
                bit.modify(tree_mapping[s].first, add);
                if (tree_mapping[s].first < n) { // root 就不用扣了</pre>
                     bit.modify(tree_mapping[s].second + 1, -add);
               }
           else {
                int node; cin >> node;
                cout <<
                       bit.query(tree_mapping[node].first) << "\n";</pre>
           }
      }
}
```

8.4 Heavy Light Decomposition [ad25b6]

```
struct HLD {
   int n, cur;
   vector<int> siz, top, dep, parent, in, out, seq;
```

```
vector<vector<int>> adi:
      Vector < Vector < Int >> adj;
HLD(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
    n = n_; cur = 0;
    siz.resize(n); top.resize(n); dep.resize(n);
             parent.resize(n); in.resize(n); out.resize(n); seq.resize(n); adj.assign(n, {});
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void work(int root = 0) {
   top[root] = root;
   dep[root] = 0;
             parent[root] = -1
             dfs1(root); dfs2(root);
       void dfs1(int u) {
   if (parent[u] != -1)
        adj[u].erase(find
                           (adj[u].begin(), adj[u].end(), parent[u]));
             siz[u] = 1;
for (auto &v : adj[u]) {
    parent[v] = u, dep[v] = dep[u] + 1;
                    dfs1(v);
                    siz[u] += siz[v];
if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
                   } // 讓 adj[u][0] 是重子節點
       void dfs2(int u) {
             in[u] = cur++;
             seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
    top[v] = v == adj[u][0] ? top[u] : v;
                    dfs2(v):
             out[u] = cur;
       int lca(int u, int v) {
             while (top[u] != top[v]) {
   if (dep[top[u]] > dep[top[v]]) {
        u = parent[top[u]];
   } else {
                          v = parent[top[v]];
                   }
             return dep[u] < dep[v] ? u : v;</pre>
       int dist(int u, int v) {
             return dep[u] + dep[v] - 2 * dep[lca(u, v)];
       return seq[in[u] - dep[u] + d];
       bool isAncester(int u, int v) {
             // 判斷 u 是否是 v 的祖先
return in[u] <= in[v] && in[v] < out[u];
       int rootedParent(int u, int v) {
             // 根據新根節點 u 計算 v 的父節點
             swap(u, v);
if (u == v) return u;
if (!isAncester(u, v)) return parent[u];
             auto it = upper_bound(adj
   [u].begin(), adj[u].end(), v, [&](int x, int y) {
   return in[x] < in[y];</pre>
             }) - 1;
return *it;
       int rootedSize(int u, int v) {
             // 根據新根節點 u 計算子樹 v 的大小
if (u == v) return n;
if (!isAncester(v, u)) return siz[v];
return n - siz[rootedParent(u, v)];
      int rootedLca(int a, int b, int c) {
    // 根據新的根節點計算三個節點 a \ b 和 c 的最近公共祖先
    return lca(a, b) ^ lca(b, c) ^ lca(c, a);
      }
};
```

8.5 Virtual Tree [622e69]

```
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
| // 可以建立虛樹達成快速樹 DP
| // 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
        vt[stk[top - 1]].push_back(stk[top]), top--;
```

```
if (stk[top - 1] != l) +
          vt[l].push_back(stk[top]);
stk[top] = l;
     } else vt[l].push_back(stk[top--]);
stk[++top] = u;
void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
     vt[u].clear();
void solve(int n, int q) {
   vector g(n + 1, vector<pair<int, int>>());
     vector vt(n + 1, vector < int >()); // dfs 完清除, 否則會退化
     vector <ll> dp(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;
   g[u].push_back({v, w});
          g[v].push_back({u, w});
     build_lca(n, g);
    for (int j = 0; j < m; j++) {
    cin >> key[j];
               iskey[key[j]] = 1;
          key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
return dfn[a] < dfn[b];
          for (int x : key) insert(x, vt);
          // DP
          auto dfs = [&](auto self, int u) -> void {
    for (auto v : vt[u]) {
        self(self, v);
    }
}
                     if (iskey[v])
                          dp[u] += min_dis[v];
                          // 砍掉 1 到 v 之間最短的路
                          dp[u] += min(dp[v], min_dis[v]);
                     iskey[v] = dp[v] = 0;
               vt[u].clear();
          };
          dfs(dfs, key[0]); // key[0] 一定是 root cout << dp[key[0]] << "\n";
          iskey[key[0]] = dp[key[0]] = 0;
```

8.6 Dominator Tree [baa540]

struct Dominator_tree {

```
int n, id;
vector <vector <int>> adj, radj, bucket;
vector <int>> sdom, dom, vis, rev, pa, rt, mn, res;
Dominator_tree(int n_ = 0) { init(n_); }
Dominator_tree(int n_ = 0) { init(n_);
void init(int _n) {
    n = _n, id = 0;
    adj.assign(n, vector<int>());
    radj.assign(n, vector<int>());
    bucket.assign(n, vector<int>());
    sdom.resize(n); dom.assign(n, -1);
    vis.assign(n, -1); rev.resize(n);
    pa.resize(n); rt.resize(n);
    mn.resize(n); res.resize(n);
}

}
void add_edge(int u, int v) { adj[u].push_back(v); }
int query(int v, int x) {
    if (rt[v] == v) return x ? -1 : v;
    int p = query(rt[v], 1);
    if (p == -1) return x ? rt[v] : mn[v];
    if (sdom[mn[v]) > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
    rt[v] = n.

           rt[v] = p;
return x ? p : mn[v];
 void dfs(int v) {
           rus(tht v) {
vis[v] = id, rev[id] = v;
rt[id] = mn[id] = sdom[id] = id, id++;
for (int u : adj[v]) {
    if (vis[u] == -1) dfs(u), pa[vis[u]
                                                                       dfs(u), pa[vis[u]] = vis[v];
                      radj[vis[u]].push_back(vis[v]);
 void build(int s) {
           dfs(s);
            for (int i = id - 1; i >= 0; i--) {
                      for (int u : radj[i])
    sdom[i] = min(sdom[i], sdom[query(u, 0)]);
if (i) bucket[sdom[i]].push_back(i);
                       for (int u : bucket[i]) {
   int p = query(u, 0);
   dom[u] = sdom[p] == i ? i : p;
                       if (i) rt[i] = pa[i];
```

```
14
              for (int i = 1; i < id; i++)
   if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];
for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre>
              res[s] = s;
              for (int i = 0; i < n; i++) dom[i] = res[i];</pre>
      }
};
9
         DP
9.1 LCS [5781cf]
int main() {
       int m, n; cin >> m >> n;
string s1, s2; cin >> s1 >> s2;
       int L = 0:
       vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0));
       for (int i = 1; i <= m; i++) {
    for (int j = 1; j <= n; j++) {
        if (s1[i - 1] == s2[j - 1])
            dp[i][j] = dp[i - 1][j - 1] + 1;
}</pre>
                            dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
      fint length = dp[m][n]; cout << length << "\n";
string s(length, 'c'); // backtracking
while (m >= 1 && n >= 1) {
    if (s1[m - 1] == s2[n - 1]) {
        s[length - 1] = s1[m - 1];
        m--, n--, length--;
}
              else {
    if (dp[m - 1][n] > dp[m][n - 1]) m--;
             }
       cout << s << "\n";
9.2 LIS [66d09f]
int main() {
    int n; cin >> n;
       vector < int > v(n);
for (int i = 0; i < n; i++) cin >> v[i];
int dp[n]; vector < int >> stk;
       stk.push_back(v[0]);
       dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) {
    if (v[i] > stk.back()) {
                    stk.push_back(v[i]);
dp[i] = ++L;
              } else {
                              = lower_bound(stk.begin(), stk.end(), v[i]);
                     *it = v[i]; dp[i] = it - stk.begin() + 1;
       vector < int > ans; cout << L << "|n";
for (int i = n - 1; i >= 0; i--) {
    if (dp[i] == L) {
                     ans.push_back(v[i]), L--;
       reverse(ans.begin(), ans.end());
for (auto i : ans) cout << i << " ";</pre>
9.3 Edit Distance [308023]
int main() {
       string s1, s2; cin >> s1 >> s2;
int n1 = s1.size(), n2 = s2.size();
       // dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元 vector <int> dp(n2 + 1);
       vector < int> dp(n2 + 1);
iota(dp.begin(), dp.end(), 0);
for (int i = 1; i <= n1; i++) {
    vector < int> cur(n2 + 1); cur[0] = i;
    for (int j = 1; j <= n2; j++) {
        if (s1[i - 1] == s2[j - 1]) {
            cur[j] = dp[j - 1];
        } else {</pre>
                     } else {
                            // s1 新增等價於 s2 砍掉
                             // dp[i][j] = min(s2 新增, 修改, s1 新增);
                            cur[j]
                                     = min({cur[j - 1], dp[j - 1], dp[j]}) + 1;
                     }
              swap(dp, cur);
       cout << dp[n2] << "\n";
9.4 Bitmask [a626f9]
```

void hamiltonianPath(){

int n, m; cin >> n >> m;
vector adj(n, vector<int>());

} // x + y = sum; // x - y = dp[0][n - 1]

```
for (int i = 0; i < m; i++) {
   int u, v; cin >> u >> v;
                                                                                             cout << (accumulate
                                                                                                    (a.begin(), a.end(), 0LL) + dp[0][n - 1]) / 2 << "\n";
                                                                                       }
           adj[--v].push_back(--u);
                                                                                       9.7 Codeforces Example [7d37ea]
      // 以...為終點,走過.
      vector dp(n, vector<int>(findBit(n)));
dp[0][1] = 1;
           (int mask = 1; mask < findBit(n); mask++) {
if ((mask & 1) == 0) continue;
for (int i = 0; i < n; i++) {</pre>
                                                                                      // 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
                                                                                       // 請問在線段不重複的情況下,最多獲得幾分int main() {
                if ((mask & findBit(i)) == 0) continue;
if (i == n - 1 && mask != findBit(n) - 1) continue;
int pre_mask = mask ^ findBit(i);
for (int j : adj[i]) {
   if ((pre_mask & findBit(j)) == 0) continue;
   do[i][mask defindBit(j)]
                                                                                             int n, m;
cin >> n >> m;
                                                                                             // 記錄每點有幾個線段
                                                                                             // 再一個紀錄,包含這個點的左界
                                                                                             dp[i][mask
                            ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
                }
           }
                                                                                                  cnt[l]++;
cnt[r + 1]--;
      cout << dp[n - 1][findBit(n) - 1] << "\n";
 void elevatorRides() {
     for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
                                                                                             for (int i = n; i >= 2; i--) {
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
                                                                                             vector<int> dp(n + 1);
                                                                                             dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
                                                                                                  dp[i] = cnt[i];
if (l_side[i] != inf) {
                                                                                                        dp[i] += dp[l_side[i] - 1];
                                                                                                  dp[i] = max(dp[i], dp[i - 1]);
                                                                                             cout << dp[n] << "\n";
                // CF 1935 DC
                                                                                       // 給你每個事件的 a, b, 挑事件會把 a 全部加起來
                                                                                        // 再加上 max(bi) - min(bi)
                      dp[mask][1] = a[i];
                                                                                       int main(){
  int n, k, ans = 0; cin >> n >> k;
  vector<pii> v(n + 1);
                }
           }
                                                                                             for (int i = 1; i <= n; i++) {
  int a, b; cin >> a >> b;
  v[i] = {a, b};
      cout << dp[findBit(n) - 1][0] << "\n";</pre>
                                                                                                  if (a <= k) ans = 1;
9.5 Projects [0942aa]
                                                                                             sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
 int main() { // 排程有權重問題,輸出價值最多且時間最少
struct E {
   int from, to, w, id;
   bool operator < (const E &rhs) {</pre>
                                                                                             }); // 用 bi 來排,考慮第 i 個時可以先扣
                                                                                             vector<vector<int>> dp(n + 1, vector<int>(n + 1, inf));
// 考慮 v[i] 時, 選 j 個的 sum(ai) - min(bi)
           return to == rhs.to ? w > rhs.w : to < rhs.to;</pre>
                                                                                             for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
      int n; cin >> n; vector<E> a(n + 1);
for (int i = 1; i <= n; i++) {</pre>
           int u, v, w; cin >> u >> v >> w;
a[i] = {u, v, w, i};
                                                                                                        // min(不選, 選)
                                                                                                        if (dp[i
      vector<array<ll, 2>> dp(n + 1); // w, time
                                                                                                                1][j
                                                                                                                         1] + v[i].first + v[i].second <= k) {
      vector<array<int, 2>> rec(n + 1); // 有沒選, 上個是誰
                                                                                                             // 假如可以選, 更新 ans 時再加回去 bi
      sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
    auto it = --lower_bound(all(a), E({0, a[i].from})),</pre>
                                                                                                             ans = max(ans, j);
           int id = i-tower_bound(at(a), a[t],
[](E x, E y){ return x.to < y.to; });
int id = it - a.begin(); dp[i] = dp[i - 1];
ll nw = dp[id][0] + a[i].w;
ll nt = dp[id][1] + a[i].to - a[i].from;</pre>
                                                                                                  dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
                                                                                             cout << ans << endl;
           if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
    dp[i] = {nw, nt}; rec[i] = {1, id};
                                                                                       9.8 CHT [5f5c25]
      vector < int > ans;
for (int i = n; i != 0;) {
    if (rec[i][0]) {
                                                                                       struct Line {
    ll m, b;
                                                                                             Line(ll'm = 0, ll b = 0) : m(m), b(b) {}
                                                                                             ll eval(ll x) {
    return m * x + b;
                ans.push_back(a[i].id);
                 i = rec[i][1];
                                                                                             }
           } else i--;
                                                                                       };
                                                                                        struct CHT { // 用在查詢單調斜率也單調
}
                                                                                             int n, lptr, rptr; vector<Line> hull;
CHT(int n_ = 0, Line init_ = Line()) {
   init(n_, init_);
9.6 Removal Game [7bb56b]
| // 兩個人比賽,每個人輪流取一個數字且只能是頭尾
                                                                                             void init(int n_ = 0, Line init_ = Line()) {
    n = n_; hull.resize(n); reset(init_);
 void reset(Line init_ = Line()) {
    lptr = rptr = 0; hull[0] = init_;
      vector < ll > a(n);
for (int i = 0; i < n; i++) cin >> a[i];
      vector dp(n, vector<ll>(n)); // i 到 j 區間的最大 diff
for (int i = n - 1; i >= 0; i--) {
    dp[i][i] = a[i];
    for (int j = i + 1; j < n; j++)
        dp[i][j] =
                                                                                             bool pop_front(Line &l1, Line &l2, ll x) {
                                                                                                  // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y
                                                                                                  // 代表查詢的當下,右線段的高度已經低於左線段了
                                                                                                   return l1.eval(x) >= l2.eval(x);
                       max(a[i] - dp[i + 1][j], a[j] - dp[i][j - 1]);
```

bool pop_back(Line &l1, Line &l2, Line &l3) {

// 本題斜率遞減、上凸包

9.9 LiChaoSegmentTree [a6e320]

```
constexpr ll Inf = 4e18;
    dp[i] = min(f[j] * s[i] + dp[j])
// y =
struct Line {
       ll m, b;
      Line(ll m = 0, ll b = Inf) : m(m), b(b) {} ll eval(ll x) const { return m * x + b; }
struct LiChaoSeg { // 取 max 再變換就好
      int n;
       vector < Line > info;
      LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
               = n_;
            info.assign(4 << __lg(n), Line());</pre>
      void update(Line line, int node, int l, int r) {
   int m = (l + r) / 2;
   bool left = line.eval(l) < info[node].eval(l);</pre>
            bool mid = line.eval(m) < info[node].eval(m);</pre>
            if (mid) swap(info[node], line); // 如果新線段比較好
if (r - l == 1) return;
else if (left != mid) update(line, 2 * node, l, m);
            // 代表左半有交點
            else update(line, 2 * node + 1, m, r);
            // 代表如果有交點一定在右半
      void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
   if (r - l == 1) return info[node].eval(x);
   int m = (l + r) / 2;
   if (x < m) return</pre>
                   min(info[node].eval(x), query(x, 2 * node, l, m));
            else return min(
                   info[node].eval(x), query(x, 2 * node + 1, m, r));
       il query(int x) { return query(x, 1, 0, n); }
1:
```

10 Geometry

10.1 Basic [d41d8c]

```
#include <bits/stdc++.h>
using namespace std;
using i64 = long long;
template < class T>
struct Point {
    T x;
     Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) \{ \}
    template < class U>
operator Point < U > () {
          return Point<U>(U(x), U(y));
     Point & operator += (const Point &p) & {
          x += p.x;
          y += p.y;
return *this;
     Point &operator -= (const Point &p) & {
         x -= p.x;
y -= p.y;
return *this;
     Point & operator *= (const T &v) & {
          x *= v;
          y *= v;
return *this;
     Point &operator/=(const T &v) & {
         x /= v;
y /= v;
     Point operator - () const {
         return Point(-x, -y);
```

```
friend Point operator+(Point a, const Point &b) {
     friend Point operator - (Point a, const Point &b) {
          return a -= b;
     friend Point operator*(Point a, const T &b) {
   return a *= b;
     friend Point operator/(Point a, const T &b) {
   return a /= b;
     friend Point operator*(const T &a, Point b) {
   return b *= a;
     friend bool operator==(const Point &a, const Point &b) {
          return a.x == b.x && a.y == b.y;
     friend istream &operator>>(istream &is, Point &p) {
          return is >> p.x >> p.y;
     friend ostream & operator < <(ostream & os, const Point & p) {
    return os << "(" << p.x << ", " << p.y << ")";</pre>
     }
}:
template < class T>
struct Line {
     Point<T>
     Point<T> b;

Line(const Point<T> &a_ = Point<T>()

, const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
};
template < class T>
T dot(const Point<T> &a, const Point<T> &b) {
   return a.x * b.x + a.y * b.y;
template < class T>
T cross(const Point<T> &a, const Point<T> &b) {
   return a.x * b.y - a.y * b.x;
template < class T>
T square(const Point<T> &p) {
     return dot(p, p);
template < class T>
double length(const Point<T> &p) {
     return sqrt(square(p));
template < class T>
double length(const Line<T> &l) {
    return length(l.a - l.b);
template < class T>
Point<T> normalize(const Point<T> &p) {
     return p / length(p);
bool parallel(const Line<T> &l1, const Line<T> &l2) {
   return cross(l1.b - l1.a, l2.b - l2.a) == θ;
template < class T>
double distance(const Point<T> &a, const Point<T> &b) {
     return length(a - b);
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
     if (dot(p - l.a, l.b - l.a) < 0) {
    return distance(p, l.a);</pre>
     if (dot(p - l.b, l.a - l.b) < 0) {
    return distance(p, l.b);</pre>
     return distancePL(p, l);
}
template < class T>
Point<T> rotate(const Point<T> &a) {
     return Point(-a.y, a.x);
template < class T>
int sgn(const Point<T> &a) {
     return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
template < class T>
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
```

```
return cross(l.b - l.a. p - l.a) > 0:
template < class T >
Point < T
       > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
      return l1.a + (l1.b - l1.a) * (cross(l2.b - l2.a, l1.a - l2.a) / cross(l2.b - l2.a, l1.a - l1.b));
template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
      return cross(p - l.a, l.b - l.a) == 0 &&
min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)
                    (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
template < class T >
bool pointInPolygon
       (const Point<T> &a. const vector<Point<T>> &p) {
      int n = p.size();
      for (int i = 0; i < n; i++) {
   if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {</pre>
     }
      for (int i = 0; i < n; i++) {
   auto u = p[i];
   auto v = p[(i + 1) % n];</pre>
             if (u.x < a.x
                   && v.x >= a.x && pointOnLineLeft(a, Line(v, u))) {
                  t ^= 1;
             if (u.x >= a.x
                     && v.x < a.x && pointOnLineLeft(a, Line(u, v))) {
      }
      return t == 1;
}
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
tuple<int, Point<T>, Point<T>> segmentIntersection
  (const Line<T> &l1, const Line<T> &l2) {
  if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x)) {
    return {0, Point<T>(), Point<T>()};
}
      if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x)) {
    return {0, Point<T>(), Point<T>()};
      if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y)) {
    return {0, Point<T>(), Point<T>()};
      if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y)) {
    return {0, Point<T>(), Point<T>()};
      if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
    if (cross(l1.b - l1.a, l2.a - l1.a) != 0) {
        return {0, Point<T>(), Point<T>()};
}
             } else {
                   auto maxx1 = max(l1.a.x, l1.b.x);
                   auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
                   auto miny1 = min(l1.a.y, l1.b.y);
                   auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.y, l2.b.y);
                   auto miny2 = min(l2.a.y, l2.b.y);
Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
                   if (!pointOnSegment(p1, l1)) {
                         swap(p1.y, p2.y);
                   if (p1 == p2) {
                  return {3, p1, p2};
} else {
                        return {2, p1, p2};
                  }
           }
      auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
      if ((cp1 > 0 && cp2 > 0) || (cp1 < 0 && cp2 <
            0) || (cp3 > 0 && cp4 > 0) || (cp3 < 0 && cp4 < 0)) {
return {0, Point<T>(), Point<T>()};
      Point p = lineIntersection(l1, l2); if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
             return {1, p, p};
      } else {
```

```
return {3, p, p};
}
template < class T>
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
   if (get<0>(segmentIntersection(l1, l2)) != 0) {
         return 0.0;
    template < class T>
bool segmentInPolygon
     (const Line<T> &l, const vector<Point<T>> &p) {
    int n = p.size();
if (!pointInPolygon(l.a, p)) {
    if (!pointInPolygon(l.b, p)) {
    for (int i = 0; i < n; i++) {
         auto u = p[i];
         auto v = p[(i + 1) % n];
auto w = p[(i + 2) % n];
         auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
         if (t == 1) {
    return false;
         if (t == 0) {
              continue:
              if (pointOnSegment(v, l) && v != l.a && v != l.b) {
   if (cross(v - u, w - v) > 0) {
      return false;
             if (p1 != u && p1 != v) {
   if (pointOnLineLeft(l.a, Line(v, u))
                       || pointOnLineLeft(l.b, Line(v, u))) {
                       return false;
             if (pointOnLineLeft(w, l)
                                && pointOnLineLeft
                               (w, Line(u, v))) {
return false;
                      } else {
    if (pointOnLineLeft(w, l)
                               || pointOnLineLeft
                               (w, Line(u, v))) {
return false;
                           }
                  && pointOnLineLeft
                                (w, Line(u, v))) {
return false;
                      } else {
   if (pointOnLineLeft(w, Line(l.b, l.a))
                               || pointOnLineLeft
                               (w, Line(u, v))) {
return false;
                  (w, Line(u, v))) {
return false;
                      } else {
   if (pointOnLineLeft(w, l)
                                || pointOnLineLeft
                                (w, Line(u, v))) {
return false;
                           }
                      }
                 }
             }
        }
     return true;
template < class T>
vector <Point <T>> hp(vector <Line <T>> lines) {
    sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
        auto d1 = l1.b - l1.a;
}
         auto d2 = l2.b - l2.a;
```

```
if (sgn(d1) != sgn(d2)) {
             return sgn(d1) == 1;
        return cross(d1, d2) > 0;
    }):
    deque < Line < T >> ls;
    deque < Point < T >> ps;
for (auto l : lines) {
        if (ls.empty())
             ls.push_back(l);
             continue:
        while (!ps.empty() && !pointOnLineLeft(ps.back(), l)) {
             ps.pop back();
        while (!ps.empty() && !pointOnLineLeft(ps[0], l)) {
             ps.pop_front();
ls.pop_front();
        if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
                  (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                 if (!pointOnLineLeft(ls.back().a. l)) {
                      assert(ls.size() == 1);
                     ls[0] = l;
                 continue:
             return {};
        ps.push_back(lineIntersection(ls.back(), l));
        ls.push back(l):
    while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0])) {
        ps.pop_back();
        ls.pop_back();
    if (ls.size() <= 2) {</pre>
        return {\, \bar{\, \} ;
    ps.push back(lineIntersection(ls[0]. ls.back()));
    return vector(ps.begin(), ps.end());
using P = Point<i64>;
10.2 Convex Hull [01a63e]
int main() {
```

```
int n; cin >> n;
vector <P> P(n), U, L;
for (int i = 0; i < n; i++) {</pre>
      cin >> P[i];
sort(P.begin(),
       .end(), [](const Point<i64> &a, const Point<i64> &b) {
      return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
for (int i = 0; i < n; i++) {
   while (L.size() >= 2 && cross(L.back() -
        L[L.size() - 2], P[i] - L[L.size() - 2]) < 0LL) {</pre>
            L.pop_back();
      while (U.size() >= 2 && cross(U.back()
    - U[U.size() - 2], P[i] - U[U.size() - 2]) > 0LL){
            U.pop_back();
      L.push_back(P[i]);
      U.push_back(P[i]);
cout << L.size() + U.size() - 2 << "\n";
      (int i = 0; i < L.size() - 1; i++) {
cout << L[i].x << " " << L[i].y << "\n";
for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << "\n";</pre>
```

10.3 MinEuclidean Distance [469a8f]

```
T distanceSquare(const Point<T> &a, const Point<T> &b) {
    return square(a - b);
void solve() {
    int n; cin >> n;
constexpr i64 inf = 8e18;
    vector < Point < i64 >> a(n);
    for (int i = 0; i < n; i++) {
         i64 x, y;
```

```
cin >> x >> y;
a[i] = Point<i64>(x, y);
struct sortY {
    bool operator()
          (const Point<i64> &a, const Point<i64> &b) const {
         return a.y < b.y;</pre>
    }
struct sortXY {
    bool operator()
    (const Point<i64> &a, const Point<i64> &b) const {
         if (a.x == b.x) return a.y < b.y;</pre>
         else return a.x < b.x:
    }
sort(a.begin(), a.end(), sortXY());
vector<Point<i64>> t(n);
auto devide = [&](auto &&self, int l, int r) -> i64 {
   if (l == r) return inf;
   int m = (l + r) / 2;
    i64 ans = min(self(self, l, m), self(self, m + 1, r));
    i64 midval = a[m].x;
    t[p++] = a[i];
    for (int j = 0; i < p; i++){
    for (int j = i + 1; j < p; j++) {</pre>
              ans = min(ans, distanceSquare(t[i], t[j])); if ((t[i].y -
                     t[j].y) * (t[i].y - t[j].y) > ans) break;
        }
    return ans:
cout << devide(devide, 0, n - 1) << "\n";</pre>
```

10.4 LatticePoints [7750d6]

```
int main() {
       // Polygun 內整數點數
       int n; cin >> n;
       vector < Point < i64 >> polygon(n);
       for (int i = 0; i < n; i++) cin >> polygon[i];
i64 area = 0;
       for (int i = 0; i < n; i++) {</pre>
             area += cross(polygon[i], polygon[(i + 1) % n]);
       area = abs(area):
       auto countBoundaryPoints
               = [](const vector<Point<i64>>& polygon) -> i64 {
             i64 res = 0;
            int n = polygon.size();
            for (int i = 0; i < n; i++) {
    i64 dx = polygon[(i + 1) % n].x - polygon[i].x;
    i64 dy = polygon[(i + 1) % n].y - polygon[i].y;</pre>
                  res += std::gcd(abs(dx), abs(dy));
            return res:
       i64 res = countBoundaryPoints(polygon);
i64 ans = (area - res + 2) / 2;
cout << ans << " " << res << " | n";</pre>
```

10.5 MinRadiusCoverCircle [a9fa76]

```
constexpr double Eps = 1e-7;
  void solve(int n, vector<P> a, double maxR) {
  auto cal = [&](P center) {
                                                     double mx = 0;
                                                     for (auto& p : a)
                                                                              mx = max(mx, distance(center, p));
                                                      return mx;
                             auto searchY = [&](double x) {
                                                    double l = -maxR, r = maxR;
while (r - l > Eps) {
    double d = (r - l) / 3;
    double ml = l + d, mr = r - d;
    double ansl = cal({x, ml}), ansr = cal({x, mr});
    if (assl = assl 
                                                                                if (ansl > ansr) l = ml;
                                                                                else r = mr:
                                                    return (l + r) / 2;
                           };
                         fy
double l = -maxR, r = maxR;
while (r - l > Eps) {
    double d = (r - l) / 3;
    double ml = l + d, mr = r - d;
    double yl = searchY(ml), yr = searchY(mr);
    double ansl = cal({ml, yl}), ansr = cal({mr, yr});
    if (ansl > ansr) l = ml;
else = maxR.
                                                      else r = mr:
                           double ansX = (l + r) / 2, ansY = searchY(ansX);
}
```