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```

1 Basic

1.1 install vscode [d41d8c]

1.2 default code [3cd57c]

```
#include <bits/stdc++.h>
#define all(x) (x).begin(), (x).end()
#define pii pair<int, int>
using namespace std;
using ll = long long;
const int mod = 1e9 + 7;

void solve() {
}

int main() {
   ios_base::sync_with_stdio(0);
   cin.tie(nullptr);
   int t = 1;
   cin >> t;
   while (t--) {
      solve();
   }
}
```

1.3 compare fuction [4bc3e0]

```
struct cmp {
    vector < int > &v;
                  // 要在 template 的資結用外部變數
     cmp(vector<int>& vec) : v(vec) {}
bool operator() (int a, int b) const {
   return v[a] > v[b];
// main: cmp cmp1(vector);
// math. cmp cmp1(vector),
// priority_queue<int, vector<int>, cmp> pq(cmp1);
};
1.4 pbds [e28ae8]
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template<typename T>
using pbds_set = tree<T, null_type,</pre>
       less<T>, rb_tree_tag, tree_order_statistics_node_update>;
1.5 浮點數誤差 [a0d4e5]
struct EDouble {
     constexpr static double Eps = 1e-9;
constexpr EDouble() : x{} {}
constexpr EDouble(double v) : x{v} {}
     constexpr double val() const {
         return x;
     explicit constexpr operator double() const {
         return x;
     constexpr EDouble operator-() const {
         return EDouble(-x);
     constexpr EDouble &operator+=(const EDouble &rhs) & {
         x += rhs.x
          return *this:
     constexpr EDouble &operator -=(const EDouble &rhs) & {
         x -= rhs.x;
return *this;
     constexpr EDouble &operator*=(const EDouble &rhs) & {
         x *= rhs.x:
         return *this;
     constexpr EDouble &operator/=(const EDouble &rhs) & {
   assert(fabs(rhs.x) > Eps);
         x /= rhs.x;
          return *this;
           EDouble operator+(EDouble lhs, const EDouble &rhs) {
          lhs += rhs;
     friend constexpr
           EDouble operator - (EDouble lhs, const EDouble &rhs) {
         lhs -= rhs;
         return lhs:
           EDouble operator*(EDouble lhs, const EDouble &rhs) {
          lhs *= rhs;
          return lhs;
     friend constexor
           EDouble operator/(EDouble lhs, const EDouble &rhs) {
         lhs /= rhs;
return lhs;
     friend constexpr bool
           operator < (const EDouble &lhs, const EDouble &rhs) {</pre>
          return lhs.x - rhs.x < -Eps:
     friend constexpr bool
           operator > (const EDouble &lhs, const EDouble &rhs) {
          return lhs.x - rhs.x > Eps;
     friend constexpr bool
    operator==(const EDouble &lhs, const EDouble &rhs) {
          return fabs(lhs.x - rhs.x) < Eps;</pre>
     friend constexpr bool
            operator <= (const EDouble &lhs, const EDouble &rhs) {</pre>
          return lhs < rhs || lhs == rhs;</pre>
     friend constexpr bool
           operator >=(const EDouble &lhs, const EDouble &rhs) {
          return lhs > rhs || lhs == rhs;
            operator!=(const EDouble &lhs, const EDouble &rhs) {
          return !(lhs == rhs);
     friend istream & operator >> (istream &is, EDouble &a) {
```

2 Graph

2.1 DFS 跟 BFS [cdd1d5]

2.2 Prim [f00ec0]

```
auto prim =
    [&](int n, vector<vector<pair<int, int>>> &adj) -> bool {
    int node_sz = 0;
    priority_queue<pair<int, int>,
        vector<pair<int, int>,
        vector<pair<int, int>>> pq;
    pq.push({0, 1}); // w, vertex
    vector<bool>    vis(n);
    while (!pq.enpty()) {
        auto [u, w] = pq.top(); pq.pop();
        if (vis[u]) continue;
        vis[u] = true;
        node_sz++;
        for (auto v : adj[u]) {
              if (!vis[v.first]) {
                  pq.push({v.second, v.first});
              }
        }
        if (node_sz == n) return true;
        return false;
};
```

2.3 BellmanFord [02f480]

```
//用 Bellman Ford 找負環
vector<array<int, 3>> graph; // u, v, w
int main() {
    int src = 0;
    int n, m;    cin >> n >> m;
    vector<int> par(n + 1), dis(n + 1, 1e9);
    for (int i = 0; i < m; i++) {
        int a, b, w; cin >> a >> b >> w;
        graph.push_back({a, b, w});
    }
    dis[1] = 0;
    for (int i = 0; i <= n; i++) {
        src = 0;
        for (auto [u, v, w] : graph) {
            if (dis[v] > dis[u] + w) {
```

```
dis[v] = dis[u] + w;
par[v] = u;
                   src = v:
             }
         }
                  // 到第 n + 1 次還在鬆弛
     if (src) {
         vector < int > ans;
cout << "YES" << endl;
for (int
               i = 0; i <= n; i++) src = par[src]; // 找那個負環
         ans.push_back(src);
         for (int
               i = par[src]; i != src; i = par[i]) { // 輸出負環
              ans.push_back(i);
         ans.push back(src):
         reverse(ans.begin(), ans.end());
         for (auto i : ans) {
    cout << i << " ";</pre>
     else {
         cout << "NO" << "\n";
}
```

2.4 負權最大距離 [2148ca]

```
// CSES High Score
void dfs(int u, vector<int> &vis, vector<vector<int>> &adj) {
   if (vis[u]) return;
   vis[u] = 1;
   for (int v : adj[u]) {
            dfs(v, vis, adj);
signed main() {
   int n, m; cin >> n >> m;
   vector<array<int, 3>> edges;
      vector<vector<int>> adj(n + 1);
      vector<int> dis(n + 1), vis(n + 1);
      while (m--) {
            int u, v, w;
cin >> u >> v >> w;
            edges.push_back({u, v, w});
adj[u].push_back(v);
      fill(dis.begin(), dis.end(), -1e18);
      dis[1] = 0;
for (int i = 1; i <= n; i++) {
            for (auto [u, v, w] : edges) {
   if (dis[u] != -1e18 && dis[v] < dis[u] + w) {
      dis[v] = dis[u] + w;
}</pre>
                        if (i == n) {
                               dfs(v, vis, adj);
                        }
                  }
            }
      if (vis[n]) cout << -1;</pre>
      else cout << dis[n];</pre>
```

2.5 FloydWarshall [206b76]

```
2.6 <u>歐拉環與歐拉路</u> [0911ed]
// 無向圖、尤拉環: 檢查每個點的出度為偶數
// 有向圖、
      尤拉路: 可以看成 1 走到 n, 所以檢查所有點的出度等於入度
int n, m;
const int maxn = 1e5 + 5;
vector<set<int>> adj;
vector<<mark>int</mark>> in;
void dfs(int now, vector<int> &road) {
     while (!adj[now].empty()) {
   int nxt = *adj[now].begin();
   adj[now].erase(nxt);
           dfs(nxt, road);
     road.push_back(now);
void solve() {
     cin >> n >> m;
in.assign(n + 1, 0);
adj.assign(n + 1, set<int>());
for (int i = 1; i <= m; i++) {</pre>
           int u, v; cin >> u >> v;
adj[u].insert(v);
           in[v]++;
     }
in[1]++;
     }
     vector<int> road;
      dfs(1, road);
     if (road.size() != m + 1) {
    cout << "IMPOSSIBLE";</pre>
           return;
     reverse(road.begin(), road.end());
for(auto i : road) cout << i << " ";</pre>
2.7 SCC [5d3e16]
struct SCC {
     int n, cur, cnt;
vector <vector <int>> adj;
vector <int>> stk, dfn, low, bel;
SCC(int n_ = 0) {
   init(n_);
}
      void init(int n_) {
           n = n_;
adj.assign(n, {});
           dfn.assign(n, -1);
low.resize(n);
           bel.assign(n, -1);
```

```
stk.clear();
cur = cnt = 0;
void addEdge(int u, int v) {
   adj[u].push_back(v);
void dfs(int x) {
    dfn[x] = low[x] = cur++;
       stk.push_back(x);
       for (auto y : adj[x]) {
   if (dfn[y] == -1) {
      dfs(y);
}
             low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
             }
       if (dfn[x] == low[x]) {
              int y;
             do {
                    y = stk.back();
bel[y] = cnt;
                    stk.pop_back();
             } while (y != x);
      }
vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
       return bel;
struct Graph {
       int n:
       vector<pair<int, int>> edges;
       vector < int > siz;
vector < int > cnte;
Graph compress() {
      Graph g;
g.n = cnt;
       g.siz.resize(cnt);
```

```
g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;
    for (auto j : adj[i]) {
        if (bel[i] != bel[j]) {</pre>
                                        g.edges.emplace_back(bel[i], bel[j]);
                                } else {
                                        g.cnte[bel[i]]++;
                        }
                 return g;
        }
};
```

2.8 VBCC [170604]

```
struct VBCC {
      int n, cur;
vector<vector<int>> adj;
      vector <int>> adj;
vector <int> dfn, low, parent;
vector <bool> is_cut;
VBCC(int n_ = 0) {
   init(n_);
}
       void init(int n_) {
            n = n_;
adj.assign(n, {});
dfn.assign(n, -1);
            low.resize(n);
            parent.assign(n, -1);
             is_cut.assign(n, false);
      void addEdge(int u, int v) {
            adj[u].push_back(v);
            adj[v].push_back(u);
       void dfs(int x) {
            int children = 0;
dfn[x] = low[x] = cur++;
for (int v : adj[x]) {
    if (dfn[v] == -1) {
                        children++:
                        parent[v] = x;
                         dfs(v);
                         low[x] = min(low[x], low[v]);
                        if (parent[x] != -1 && low[v] >= dfn[x]) {
    is_cut[x] = true;
                  } else if (v != parent[x]) {
                         low[x] = min(low[x], dfn[v]);
            if (parent[x] == -1 && children > 1) {
    is_cut[x] = true;
            }
      void work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {</pre>
                  if (dfn[i] == -1) {
                        dfs(i);
                  }
            }
      }
}:
```

2.9 EBCC [49d862]

```
struct EBCC { // CF/contest/1986/pF
      int n, cur, cnt;
vector<vector<int>> adj;
      vector<int> stk, dfn, low, bel;
       vector<pair<int, int>> bridges; // 關鍵邊
      EBCC(int n_) {
   init(n_);
      void init(int n_) {
            n = n_;
adj.assign(n, {});
dfn.assign(n, -1);
             low.resize(n):
             bel.assign(n, -1);
             stk.clear();
            bridges.clear();
cur = cnt = 0;
      void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
      void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
             stk.push_back(x);
             for (auto y : adj[x]) {
   if (y == p) continue;
   if (dfn[y] == -1) {
                         dfs(y, x);
low[x] = min(low[x], low[y]);
if (low[y] > dfn[x]) {
                               bridges.emplace_back(x, y);
```

```
} else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
                   }
             if (dfn[x] == low[x]) {
                    int y;
                   do {
                          y = stk.back();
                   bel[y] = cnt;
stk.pop_back();
while (y != x);
                    cnt++;
             }
      fvector<int> work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
        }
}</pre>
                   }
             return bel;
       struct Graph {
             int n;
             vector<pair<int, int>> edges;
             vector<int> siz; // BCC 內節點數
             vector<int> cnte; // BCC 內邊數
      Graph compress() {
             Graph g;
g.n = cnt;
             g.siz.resize(cnt);
             g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
                   g.siz[bel[i]]++;
                    for (auto j : adj[i]) {
    if (bel[i] < bel[j]) {
        g.edges.emplace_back(bel[i], bel[j]);
}</pre>
                          } else if (i < j) {
   g.cnte[bel[i]]++;</pre>
                   }
             return g;
};
```

2.10 2-SAT [eeddc1]

```
// CSES Giant Pizza
 struct TwoSat {
              int n:
               vector<vector<int>> e;
               vector<bool> ans;
              vector v
               bool satisfiable() {
                             \verb|vector<| \textbf{int}|
                             > id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
vector<int> stk;
                             int now = 0, cnt = 0;
function<void(int)> tarjan = [&](int u) {
                                         stk.push_back(u);
dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
                                                                       tarjan(v);
                                                         low[u] = min(low[u], low[v]);

else if (id[v] == -1) { // in s
low[u] = min(low[u], dfn[v]);
                                                         }
                                            if (dfn[u] == low[u]) {
                                                          int v;
                                                         do {
                                                                       v = stk.back();
                                                         stk.pop_back();
id[v] = cnt;
} while (v != u);
                                         }
                            };
for (int i
                            return true:
               vector < bool > answer() { return ans; }
};
int main() {
              main() {
int m, n; cin >> m >> n;
TwoSat ts(n);
for (int i = 0; i < m; ++i) {
   int u, v; char x, y;
   cin >> x >> u >> y >> v;
```

```
ts.addClause(u - 1, x == '+', v - 1, y == '+');
if (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";</pre>
else cout << "IMPOSSIBLE\n";</pre>
```

2.11 Planets Cycles [71ac0e]

```
vector<int> dis, v;
vector<bool> vis:
int step;
queue < int > path;
void dfs(int x) {
      path.push(x);
       if (vis[x]) {
             step += dis[x];
             return;
       vis[x] = true;
       step++:
       dfs(v[x]);
// count path_dis to rep
int main() {
   int n; cin >> n;
      v.assign(n + 1, 0);
dis.assign(n + 1, 0);
vis.assign(n + 1, false);
for (int i = 1; i <= n; i++) {
    cin >> v[i];
       for (int i = 1; i <= n; i++) {
             step = 0;
             int is_outof_cycle = 1;
            int is_out _
dfs(i);
while (!path.empty()) {
    if (path.front() == path.back()) {
        is_outof_cycle = 0;
}
                    step -= is_outof_cycle;
                    path.pop();
       for (int i = 1; i <= n; i++) {
    cout << dis[i] << ' ';</pre>
       cout << '\n';
}
```

2.12 Planet Queries II [872f72]

```
| // 在有向圖中,從 A 到 B 的最短距離
 // 保證出度是 1 所以對 1 個點來說,從他出發只可能遇到一個環 int n, q;
 int dp[200005][30]; // 倍增表
vector<vector<int>>> cycles;
 vector<int
 > no, cycle_idx, vis; // Order & Can be in cycle, or out
void set_out_of_cycle_no(int now, unordered_set<int> &done) {
    // 把不在環內的也編號, v 是 u 的編號 -1
    if (done.find(now) != done.end()) return;
       set_out_of_cycle_no(dp[now][0], done);
done.insert(now); // post order
no[now] = no[dp[now][0]] - 1;
 }
 return u;
 void find_cycle(int now) {
       unordered_set<int> appear;
       vector<int> v;
       bool flag = true; // 代表有環
while (appear.find(now) == appear.end()) {
    appear.insert(now);
             v.push_back(now);
            if (vis[now]) {
    flag = false;
                  break;
            now = dp[now][0];
       for (auto i : v) vis[i] = true;
if (!flag) return;
       // now 是環的起點,我們先找到他在 v 的哪裡
       int z = find(v.begin(), v.end(), now) - v.begin();
vector<int> cycle(v.begin() + z, v.end());
       cycles.push_back(cycle);
 int main() {
    cin >> n >> q;
       no.assign(n + 1, -1);
```

```
cycle_idx.assign(n + 1, -1);
    vis.assign(n + 1, 0);
for (int u = 1; u <= n; u++) cin >> dp[u][0];
     for (int i = 1; i <= 18; i++) // 倍增表
    if (!vis[i]) find_cycle(i);
    int idx = 0;
     unordered_set < int > done;
    for (auto &i : cycles) {
   int c = 0;
         for (auto &j : i) {
              no[j] = c++;
cycle_idx[j] = idx;
              done.insert(j);
         idx++:
    for (int i = 1; i <= n; i++) set_out_of_cycle_no(i, done);
for (int i = 1; i <= q; i++) {
   int u, v; cin >> u >> v;
          // 在同個環內
         if (cycle_idx[u] == cycle_idx
   [v] && cycle_idx[u] != -1 && cycle_idx[v] != -1) {
              int cyc_size = cycles[cycle_idx[u]].size();
              cout <<
                   (no[v] - no[u] + cyc_size) % cyc_size << "\n";</pre>
         // 都不再環內
         if (wiint_go_to(u, no[v] - no[u]) == v) {
   cout << no[v] - no[u] << "\n";</pre>
              else cout << -1 << "\n";
         else if (cycle_idx[u]
               == -1 && cycle_idx[v] != -1) { // v 在環內,二分搜
              l <= n) { // 如果 n 步內可以到
int in_cycle_of_u = wiint_go_to(u, l);
int cycle_size = cycles[cycle_idx[v]].size();
cout << l + (no[v] - no[in_cycle_of_u
] + cycle_size) % cycle_size << "|n";
              if (l <= n) {
              else cout << -1 << "\n";
         else { // u 在環內 b 不在,直接不可能 cout << -1 << "\n";
}
```

3 Data Structure

3.1 BIT [d41d8c]

```
template <typename T>
struct Fenwick { // 全部以 0 based 使用
    int n;
vector<T> a;
     Fenwick(int n_ = 0) {
          init(n_);
     void init(int n_) {
          n = n_
          a.assign(n, T{});
     void add(int x, const T &v) {
   for (int i = x + 1; i <= n; i += i & -i) {
      a[i - 1] = a[i - 1] + v;
}</pre>
     T sum(int x) { // 左閉右開查詢
          T ans{};
for (int i = x; i > 0; i -= i & -i) {
               ans = ans + a[i - 1];
          return ans:
    T rangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
     int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
          int x = 0;
          T cur{};
for (int i = 1 << _
               (int i = 1 << __lg(n); i; i /= 2) {
if (x + i <= n && cur + a[x + i - 1] <= k) {
```

```
x += i:
                       cur = cur + a[x - 1];
                 }
            return x:
     }
};
template <class T>
struct TwoDFenwick { // 全部以 0 based 使用
      int nx, ny; // row, col 個數
vector<vector<T>> a;
      TwoDFenwick(int nx_ = 0, int ny_ = 0) {
           init(nx_, ny_);
      void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
      void add(int x, int y, const T &v) {
           for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        a[i - 1][j - 1] = a[i - 1][j - 1] + v;
           }
      }
      T sum(int x, int y) { // 左閉右開查詢 T ans{};
            for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans + a[i - 1][j - 1];
    }
}
           return ans:
      T rangeSum
            (int lx, int ly, int rx, int ry) { // 左閉右開查詢
            return sum(
                  (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
     }
}:
```

3.2 RangeBit [d41d8c]

```
| template <typename T>
 struct rangeFenwick { // 全部以 0 based 使用
      int n;
      vector < T > d, di;
rangeFenwick(int n_ = 0) {
          init(n_);
      void init(int n_) {
           d.assign(n, T{})
           di.assign(n, T{});
      void add(int x, const T &v) {
          for (int i = x + 1);

for (int i = x + 1; i <= n; i += i & -i) {

    d[i - 1] = d[i - 1] + v;

    di[i - 1] = di[i - 1] + vi;
          }
      void rangeAdd(int l, int r, const T &v) {
          add(l, v); add(r, -v);
      }
      T sum(int x) { // 左閉右開查詢
          for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
      }
      TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
      int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
          int x = 0;
                         cur = cur + val;
                    }
               }
           return x;
     }
 template <class T>
 struct rangeTwoDFenwick { // 全部以 0 based 使用
      int nx, ny; // row, col 個數
vector<vector<T>> d, di, dj, dij;
      rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
          init(nx_, ny_);
      void init(int nx_, int ny_) {
```

```
nx = nx_; ny = ny_;
d.assign(nx, vector<T>(ny, T{}));
di.assign(nx, vector<T>(ny, T{}));
dj.assign(nx, vector<T>(ny, T{}));
dj.assign(nx, vector<T>(ny, T{}));

void add(int x, int y, const T &v) {
    T vi = v * (x + 1);
    T vj = v * (y + 1);
    T vij = v * (y + 1);
    T vij = v * (x + 1) * (y + 1);
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            d[i - 1][j - 1] = d[i - 1][j - 1] + v;
            di[i - 1][j - 1] = d[i - 1][j - 1] + v;
            dj[i - 1][j - 1] = d[i - 1][j - 1] + v;
            di[i - 1][i - 1] = d[i - 1][j - 1] + v;
            di[i - 1][i - 1] = d[i - 1][i - 1] + v;
            di[i - 1][i - 1] = d[i - 1][i - 1] + v;
            di[i - 1][i - 1] = d[i - 1][i - 1] + v;
            di[i - 1][i - 1] = d[i - 1][i - 1] + v;
            di[i - 1][i - 1] = d[i - 1][i - 1] + v;
            di[i - 1][i - 1] = d[i - 1][i - 1] + v;
            di[i - 1][i - 1][i - 1] = d[i - 1][i - 1][i - 1] + v;
            di[i - 1][i - 1][i - 1] = d[i - 1][i - 1][i - 1] + v;
            di[i - 1][i 
                                                                                  dij[i - 1][j - 1] = dij[i - 1][j - 1] + vij;
                                                            }
                                        }
                      void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
                                        add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
                    T sum(int_x, int y) { // 左閉右開查詢
                                          T`ans{};
                                         for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans
                                                                                 ans = ans + dij[i - 1][j
                                                            }
                                          return ans;
                    T rangeSum
                                            (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                                          return sum(
                                                                 (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
};
 3.3 DSU [d41d8c]
```

```
struct DSU {
     int n;
     vector<int> boss, siz;
     DSU() {}
DSU(int n_) {
           init(n_);
     void init(int n_) {
           boss.resize(n);
           iota(boss.begin(), boss.end(), 0);
           siz.assign(n, 1);
     int find_boss(int x) {
           if (boss[x] == x) return x;
return boss[x] = find_boss(boss[x]);
     bool same(int x, int y) {
    return find_boss(x) == find_boss(y);
     bool merge(int x, int y) {
    x = find_boss(x);
    y = find_boss(y);
    if (x == y) {
        return false;
    }
}
           if(siz[x] < siz[y]) swap(x, y);</pre>
           siz[x] += siz[y];
           boss[y] = x;
           return true;
     int size(int x) {
    return siz[find_boss(x)];
};
struct DSU {
     int n;
vector<int> boss, siz, stk;
     DSU() {}
DSU(int n_) {
          init(n_);
     void init(int n_) {
          n = n_;
boss.resize(n);
           iota(boss.begin(), boss.end(), 0);
          siz.assign(n, 1);
stk.clear();
     int find(int x) {
   return x == boss[x] ? x : find(boss[x]);
     bool same(int x, int y) {
```

```
return find(x) == find(v):
       bool merge(int x, int y) {
            x = find(x);
y = find(y);
             if (x == y)
                   return false;
            if (siz[x] < siz[y]) swap(x, y);
siz[x] += siz[y];
boss[y] = x;</pre>
            stk.push_back(y);
            return true:
       void undo(int x) {
    while (stk.size() > x) {
        int y = stk.back();
}
                   stk.pop_back();
                  n++;
                  siz[boss[y]] -= siz[y];
boss[y] = y;
            }
       int size(int x) {
             return siz[find(x)];
       }
};
```

3.4 線段樹 [d41d8c]

```
| template <class Info>
 struct Seg { // 左閉右開寫法
       int n:
       vector < Info > info;
        Seg() : n(0) {}
       Seg(int n_, Info v_ = Info()) {
   init(n_, v_);
        template <class T>
       Seg(vector<T> init_) {
   init(init_);
       void init(int n_, Info v_ = Info()) {
  init(vector(n_, v_));
       template <class T>
void init(vector<T> init_) {
             n = init_.size();
             in = intc_state(),
info.assign(4 << __lg(n), Info());
function <void(
    int, int, int)> build = [&](int p, int l, int r) {
    if (r - l == 1) {
        info[p] = init_[l];
        returned.
                          return;
                   int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                   pull(p);
             build(1, 0, n);
       void pull
       (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
             if (r - l == 1)
    info[p] = v;
                   return;
             int m = (l + r) / 2;
if (x < m) {
                    modify(2 * p, l, m, x, v);
             } else {
                   modify(2 * p + 1, m, r, x, v);
             pull(p);
       void modify(int p, const Info &i) {
             modify(1, 0, n, p, i);
       Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    return query(p *</pre>
             return query(p
                    2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
              (int ql, int qr) { return query(1, 0, n, ql, qr); }
        template < class F> // 尋找區間內,第一個符合條件的
       int findFirst
             (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
                   return -1;
              if (l >= x && r <= y && !pred(info[p])) {
                    return -1;
              if (r - l == 1) {
                    return l;
```

```
int m = (l + r) / 2
                                                                                                                  apply(p, l, r, v);
            int res = findFirst(2 * p, l, m, x, y, pred);
            if (res == -1) {
                                                                                                           int m = (l + r) / 2;
                 res = findFirst(2 * p + 1, m, r, x, y, pred);
                                                                                                           push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
            return res;
     }
                                                                                                            pull(p);
     template < class F> // 若要找 last,先右子樹遞迴即可
int findFirst(int l, int r, F & pred) {
    return findFirst(1, 0, n, l, r, pred);
                                                                                                      void range_apply(int l, int r, const Tag &v) {
    range_apply(1, 0, n, l, r, v);
};
// ---define structure and info plus---
                                                                                                      template < class F> // 尋找區間內,第一個符合條件的
struct Info {
                                                                                                      int findFirst
                                                                                                           (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
    return -1;</pre>
     int n = 1;
     int sum = 0;
info operator+(const Info &a, const Info &b) {
    return { a.n + b.n, a.sum + b.sum };
                                                                                                            if (l >= x && r <= y && !pred(info[p])) {
}
                                                                                                                 return -1;
3.5 懶標線段樹 [d41d8c]
                                                                                                            if (r - l == 1) {
                                                                                                                  return l;
template <class Info, class Tag>
struct LazySeg { // 左閉右開寫法
                                                                                                            int m = (l + r) / 2;
                                                                                                           push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
     int n;
vector < Info > info;
     if (res ==
                                                                                                                 res = findFirst(2 * p + 1, m, r, x, y, pred);
                                                                                                            return res;
                                                                                                      template < class F> // 若要找 last,先右子樹遞迴即可
int findFirst(int l, int r, F & & pred) {
    return findFirst(1, 0, n, l, r, pred);
      template <class T>
      LazySeg(vector<T> init_) {
           init(init_);
      void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
                                                                                                };
// ---define structure and info plus---
                                                                                                struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add;
      template <class T>
      void init (vector<T> init_) {
                                                                                                      void apply(const Tag& v) {
           n = init_.size();
                                                                                                           if (v.set_val) {
    set_val = v.set_val;
    add = v.add;
           info.assign(4 << __lg(n), Info());
tag.assign(4 << __lg(n), Tag());
function <void(
                 int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
                                                                                                            else {
                                                                                                                  add += v.add;
                       info[p] = init_[l];
                       return;
                                                                                                     }
                                                                                                };
                 int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                                                                                                struct Info {
                                                                                                      int sum:
                                                                                                      void apply(int l, int r, const Tag &v) {
                 pull(p);
                                                                                                           if (v.set_val) {
    sum = (r - l) * v.set_val;
           build(1, 0, n);
                                                                                                            sum += (r - l) * v.add;
      (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
                                                                                                      // Info& operator=(const Info &rhs) {
                                                                                                     //
//
// }
                                                                                                               // 部分 assignment 使用
return *this;
            tag[p].apply(v);
      void push(int p, int l, int r) {
                                                                                                Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
           int m = (l + r) / 2;
if (r - l >= 1) {
    apply(p * 2, l, m, tag[p]);
    apply(p * 2 + 1, m, r, tag[p]);
}
                                                                                                3.6 莫隊 [d41d8c]
            tag[p] = Tag();
                                                                                                struct query {
                                                                                                  int l, r, id;
typedef query;
      void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
}
                                                                                                void MO(int n, vector < query > & queries) {
  int block = sqrt(n);
                 return;
                                                                                                      function <book = sqrt(n);
function <book(query, query)> cmp = [&](query a, query b) {
  int block_a = a.l / block;
  int block_b = b.l / block;
  if (block_a != block_b) return block_a < block_b;</pre>
            int m = (l + r) / 2;
           push(p, l, r);
if (x < m) {
                                                                                                            return a.r < b.r;
                 modify(2 * p, l, m, x, v);
                                                                                                      sort(queries.begin(), queries.end(), cmp);
                 modify(2 * p + 1, m, r, x, v);
                                                                                                void compress(vector<int> &nums) {
           pull(p);
                                                                                                      vector<int> sorted = nums
      void modify(int p, const Info &i) {
    modify(1, 0, n, p, i);
                                                                                                      sort(sorted.begin(), sorted.end());
                                                                                                      sorted.erase
                                                                                                      (unique(sorted.begin(), sorted.end());
for (int i = 0; i < nums.size(); i++) {
   nums[i] = lower_bound(sorted.begin</pre>
     Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    push(p, l, r);
    return query(p *</pre>
                                                                                                                  (), sorted.end(), nums[i]) - sorted.begin() + 1;
                                                                                                     }
            return query(p *
                                                                                                3.7 Treap [d41d8c]
                 2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
```

struct Treap {

Treap *lc, *rc;

int pri, siz; bool rev_valid;
int val; int min;
Treap(int val_) {
 min = val = val_;

(int ql, int qr) { return query(1, 0, n, ql, qr); }

void range_apply
 (int p, int l, int r, int ql, int qr, const Tag &v) {
 if (qr <= l || ql >= r) return;
 if (ql <= l && r <= qr) {</pre>

```
pri = rand():
            lc = rc = nullptr;
            siz = 1; rev_valid = 0;
      void pull() { // update siz or other information
            siz = 1;
min = val;
            for (auto c : {lc, rc}) {
    if (!c) continue;
    siz += c->siz;
                  min = std::min(min. c->min):
      void push() {
   if (rev_valid) {
                  swap(lc, rc);
if (lc) lc->rev_valid ^= 1;
if (rc) rc->rev_valid ^= 1;
            rev valid = false:
      int find(int k) { // 找到 min 是 k 的位置 (1-based)
            push();
             int ls = (lc ? lc->siz : 0) + 1;
            if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
      }
int size(Treap *t) {
    return t ? t->siz : 0;
Treap *merge(Treap *a, Treap *b) {
     if (!a || !b) return a ? a : b;
a->push(); b->push();
if (a->pri > b->pri) {
    a->rc = merge(a->rc, b);
}
            a->pull();
            return a;
      else {
    b->lc = merge(a, b->lc);
            b->pull();
     }
pair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
      t->push();

if (size(t->lc) < k) {

    auto [a, b] = split(t->rc, k - size(t->lc) - 1);
            t->rc = a;
            t->pull();
            return {t, b};
      else {
            auto [a, b] = split(t->lc, k);
            t->pull();
            return {a, t};
void Print(Treap *t) {
   if (!t) return;
      t->push();
      Print(t->lc);
cout << t->val;
      Print(t->rc);
```

4 Flow

4.1 Dinic [287fe8]

```
template < class T>
struct Dinic {
      struct Edge {
            int to;
            T flow, cap; // 流量跟容量
      int n, m, s, t;
T INF_FlOW = numeric_limits<T>::max() / 2;
      vector<vector<int>> adj; // 此點對應的 edges 編號
      vector<Edge> edges; // 幫每個 edge 編號
      vector < Lage > eages; // 開發间 e
vector < int > dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
    n = n_; m = 0;
             dis.resize(n); ptr.resize(n);
            adj.assign(n, vector<int>{});
edges.clear();
      void add_edge(int u, int v, T cap) {
             // 偶數 id 是正向邊
            // Image to Tell.In/Ze
edges.push_back({ v, 0, cap });
edges.push_back({ u, 0, 0 });
adj[u].push_back(m++);
adj[v].push_back(m++);
```

```
bool bfs() {
             fill(dis.begin(), dis.end(), -1);
             dis[s] = 0; queue < int > q;
             q.push(s);
             while (!q.empty() && dis[t] == -1) {
                   int u = q.front(); q.pop();
for (int id : adj[u]) {
    Edge &e = edges[id];
                        if (e.flow == e.cap) continue;
if (dis[e.to] == -1) {
    dis[e.to] = dis[u] + 1;
                              q.push(e.to);
                  }
             return dis[t] != -1;
       f
    dfs(int u, T flow) {
        if (flow == 0) return 0;
        if (u == t) return flow;
        for (int
                  &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {
Edge &e = edges[adj[u][cur]];
if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;</pre>
                   T mn = dfs(e.to, min(flow, e.cap - e.flow));
                   if (mn > 0) {
    e.flow += mn;
                         edges[adj[u][cur] ^ 1].flow -= mn;
                        return mn;
                  }
             return 0; // 到不了終點就會 return 0
       while (true) {
   T res = dfs(s, INF_Flow);
                        if (res == 0) break;
flow += res:
                  }
             return flow;
       void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
};
 4.2 Min Cut [44ae6c]
 // CSES Police Chase
int main(){
       int n, m; cin >> n >> m;
```

```
for (int i = 0; i < m; i++) {
   int u, v, cap = 1;
   cin >> u >> v;
}
             u--: v--:
            g.add_edge(u, v, cap);
g.add_edge(v, u, cap);
      int res = g.work(0, n - 1);
cout << res << "\n";
if (res == 0) return;</pre>
       vector<int> vis(n);
       auto find = [&](auto self, int u) -> void {
   if (!vis[u]) {
                    vis[u] = 1;
                   for (int id : g.adj[u]) {
   auto e = g.edges[id];
   if (e.cap - e.flow > 0) {
                                self(self, e.to);
                   }
            }
      if (!vis[e.to]) {
    cout << i + 1 << " " << e.to + 1 << "\n";
             }
      }
}
```

4.3 Hangarian [350fc3]

```
| struct Hangarian { // 0-based
        int n, m; // 最小路徑覆蓋,二分匹配
vector<vector<int>>> adj;
        vector <int> used, vis;
vector <pair <int, int>> match;
Hangarian(int n_ = 0, int m_ = 0) {
              init(n_, m_);
```

```
National Chung Cheng University Salmon
     void init(int n_ = 0, int m_ = 0) {
    n = n_; m = m_;
    adj.assign(n + m, vector < int > ());
    used.assign(n + m, -1);
           vis.assign(n + m, 0);
                                                                                                          }
      void addEdge(int u, int v) {
           adj[u].push_back(n + v)
           adj[n + v].push_back(u);
      vector<pair<int, int>> work() {
           match.clear();
           used.assign(n + m, -1);
vis.assign(n + m, 0);
           if (used[v] == -1 || self(self, used[v])) {
                                used[v] = u;
                           }
                     }
                return false;
           for (int i = 0; i < n; i++) {
    fill(vis.begin(), vis.end(), 0);</pre>
                dfs(dfs, i);
           for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
                      match.emplace_back(used[i], i - n);
           return match;
     }
};
4.4 MCMF [a7998c]
template < class Tf, class Tc>
struct MCMF {
   int n, m, s, t;
                                                                                                                f = min
     Tf INF_FLOW = numeric_limits<Tf>::max() / 2;
Tc INF_COST = numeric_limits<Tc>::max() / 2;
struct Edge {
           int to;
           Tf flow, cap; // 流量跟容量
Tc cost;
     vector<vector<int>> adi:
     vector < Edge > edges; // 幫每個 edge 編號 vector < Tc > dis, pot; // johnson algorithm, using spfa vector < int > rt; // 路徑恢復,對應 id
     vector < bool > vis;
MCMF(int n = 0) { init(n_); }
      void init(\overline{int} n' = 0) {
          n = n_;
m = 0;
           edges.clear();
adj.assign(n, vector<int>{});
                                                                                         };
      void add_edge(int u, int v, Tf cap, Tc cost){
   edges.push_back({v, 0, cap, cost});
   edges.push_back({u, 0, 0, -cost});
                                                                                          5 String
                                                                                          5.1 KMP [cddfd9]
           adj[u].push_back(m++);
           adj[v].push_back(m++);
                                                                                                string sub;
      bool spfa() {
           dis.assign(n, INF_COST);
rt.assign(n, -1); vis.assign(n, false);
queue<int> q;
                                                                                                vector<int> failure:
                                                                                                KMP(string sub_) {
   sub = sub_;
           while (now != -1
```

q.push(v); vis[v] = true;

Tc ndis = dis[u] + cost + pot[u] - pot[v];

}

return dis[t] != INF_COST;

} }

```
if (flow < cap && dis[v] > ndis) {
    dis[v] = ndis; rt[v] = id;
                                  pq.emplace(ndis, v);
       return dis[t] != INF_COST;
// 限定 flow,最小化 cost
pair<Tf, Tc> work_flow(int s_,
                                                               int t_, Tf need) {
       s = s_, t = t_; pot.assign(n, 0);
If flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] += pot[i] - pot[s];
}</pre>
                Tf f = INF_FLOW;
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                   (f, edges[rt[i]].cap - edges[rt[i]].flow);
               }
f = min<Tf>(f, need);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
}
                flow += f; need -= f;
cost += f * dis[t]; fr = false;
for (int i = 0; i < n; i++) swap(dis[i], pot[i]);
if (need == 0) break;</pre>
        return make_pair(flow, cost);
.
// 限定 cost,最大化 flow
pair<Tf, Tc> work_budget(<mark>int</mark> s_, <mark>int</mark> t_, Tc budget) {
       s = s_, t = t_; pot.assign(n, 0);
If flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] += pot[i] - pot[s];
}</pre>
                If f = INF_FLOW;
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
                                  (f, edges[rt[i]].cap - edges[rt[i]].flow);
                f = min<Tf>(f, budget / dis[t]);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
}
                flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
for (int i = 0; i < n; i++) swap(dis[i], pot[i]);
if (budget == 0 || f == 0) break;</pre>
        return make_pair(flow, cost);
void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
```

```
failure.resize(sub.size(), -1);
buildFailFunction();
           void buildFailFunction() {
   for (int i = 1; i < (int)sub.size(); i++) {
     int now = failure[i - 1];</pre>
                               && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
            vector<int> match(string &s) {
                    vector < int > match(st ting as) {
vector < int > match(st ting as) {
    for (int i = 0, now = -1; i < (int)s.size(); i++) {
        // now is the compare sucessed length -1
        while (s[i] !=</pre>
                              sub[now + 1] && now != -1) now = failure[now];
// failure stores if comparison fail, move to where
if (s[i] == sub[now + 1]) now++;
if (now + 1 == (int)sub.size()) {
                                       match.push_back(i - now);
now = failure[now];
                    return match;
1 };
```

5.2 Z Function [8dd6ac]

```
// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
// 的最長公共前綴 (LCP) 的長度
vector < int > Z(string s) {
    int n = s.size();
     vector<int> z(n);
     vector time 2(n),
z[0] = n;
for (int i = 1, j = 1; i < n; i++) {
    z[i] = max(0, min(j + z[j] - i, z[i - j]));
    while (i + z[i] < n && s[z[i]] == s[i + z[i]]) {</pre>
            if (i + z[i] > j + z[j]) {
     return z; // 最後一格不算
```

5.3 Duval Algorithm [f9dcca]

```
// duval_algorithm
// 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
vector<string> duval(string s) {
   int i = 0, n = s.size();
     vector<string> res;
    while (i <= k) {
    res.push_back(s.substr(i, j - k));
    i += j - k;</pre>
         }
     return res;
// 最小旋轉字串
string min_round(string s) {
    s += s;
int i = 0, n = s.size();
    int start = i;
while (i < n / 2) {</pre>
        else k++;
         while (i <= k) {</pre>
             i += j - k;
     return s.substr(start, n / 2);
```

5.4 Manacher [9c9ca6]

```
' 找到對於每個位置的廻文半徑
vector <int> manacher(string s) {
    string t = "#";
    for (auto c : s) {
         t += c;
t += '#';
    int n = t.size();
     vector<int> r(n);
    for (int i = 0, j =
         0; i < n; i++) { // i 是中心, j 是最長回文字串中心 if (2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
         r[i] += 1;
         if (i + r[i] > j + r[j]) {
              `j = i;
         }
    return r;
    // # a # b # a #
// 1 2 1 4 1 2 1
// # a # b # b # a #
// 1 2 1 2 5 2 1 2 1
    // 值 -1 代表原回文字串長度
     ..
// (id - val + 1) / 2 可得原字串回文開頭
```

5.5 Trie [3b3aa0]

```
struct Trie {
    struct trie_node {
        bool is_word;
        vector < trie_node *> children;
```

```
trie_node() {
    is_word = false;
                  children.resize(26, NULL);
      trie_node *root = new trie_node();
      void insert(string &s) {
  trie_node *cur = root;
  for (int i = 0; i < s.size(); i++) {
    int idx = s[i] - 'a';
    if (cur->children[idx] == NULL) {
        cur->children[idx] = new trie_node();
    }
}
                 cur = cur->children[idx]:
            cur->is_word = true;
      bool is_in_trie(string &s) {
           trie_node *cur = root;
for (int i = 0; i < s.size(); i++) {
                 if (cur-
                        children[s[i] - 'a'] == nullptr) return false;
                  cur = cur->children[s[i] - 'a'];
      int search_i_start(string &s, int i, vector<int> &dp) {
    trie_node *cur = root;
           int sz = s.size(), ans = 0;
for (int j = i; j < sz; j++) {
    if (cur
                 return ans;
     }
int main() {
      // 找到 sub 集合裡,可以重複用,組成 s 的組數 Trie trie; string s; cin >> s; int sz = s.size();
      // dp 代表 i 開頭到最後的配對總數
      // 找到有結尾為 stop 的 dp[i] += dp[j + 1]
      int n; cin >> n;
      vector <int> dp(sz + 1, 0);
for (int i = 0; i < n; i++) {
    string sub; cin >> sub;
            trie.insert(sub);
     dp[sz] = 1;
for (int i = sz - 1; i >= 0; i--) {
    dp[i] = trie.search_i_start(s, i, dp);
}
      cout << dp[0] << endl;
```

6 Math

6.1 質因數分解 [ee1622]

```
a^{(m-1)} = 1 \pmod{m}
// a^(m-1) = 1 (MOU M)
// a^(m-2) = 1/a (mod m)
// EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)
// Filter + DP; DP save min factor 'recur' factor decomposition
// FacNums = (x+1)(y+1)(z+1)...
// FacSum = (a^0+a^1...+a^x)(b^0+...+b^y)
// FacMul = N(x+1)(y+1)(z+1)/2
vector<int> is_prime;
// 1 代表是質數, 非 1 不是
void init(int n) {
        is_prime.assign(n + 1, 1);
for (int i = 2; i <= (int)sqrt(n) + 1; i++) {
                 if (is_prime[i] == 1) {
    for (int j = i + i; j <= n; j += i) {
        is_prime[j] = i;
    }</pre>
                }
        }
int main() {
    init(1000000);
         ll ans = 1;
        ll q; cin >> q;
map<ll, ll> mp;
while (is_prime[q] != 1) {
    mp[is_prime[q]]++;
    q /= is_prime[q];
}
         if (q != 1) mp[q]++;
for (auto [a, b] : mp) {
   ans *= b + 1;
         cout << ans << "\n";
```

6.2 模除計算 [9b1014]

```
using i64 = long long;
template < class T >
constexpr T power(T a, i64 b) {
    for (; b; b /= 2, a *= a) {
    if (b % 2) {
        res *= a;
    }
     return res;
constexpr i64 mul(i64 a, i64 b, i64 p) {
   i64 res = a * b - i64(1.L * a * b / p) * p;
}
     res %= p;
     if (res < 0) {
          res += p;
     return res;
template < i64 P>
struct MLong {
    i64 x;
     constexpr MLong() : x{} {}
constexpr MLong(i64 x) : x{norm(x % getMod())} {}
     static i64 Mod;
constexpr static i64 getMod() {
   if (P > 0) {
          return P;
} else {
               return Mod;
          }
     constexpr static void setMod(i64 Mod_) {
           Mod = Mod_;
     constexpr i64 norm(i64 x) const {
          if (x < 0) {
                x += getMod();
           if (x >= getMod()) {
                x -= getMod();
           return x;
     constexpr i64 val() const {
           return x;
     explicit constexpr operator i64() const {
           return x;
     constexpr MLong operator-() const {
          MLong res;
res.x = norm(getMod() - x);
           return res;
     constexpr MLong inv() const {
           assert(x != 0);
return power(*this, getMod() - 2);
     constexpr MLong &operator*=(MLong rhs) & {
  x = mul(x, rhs.x, getMod());
  return *this;
     constexpr MLong &operator+=(MLong rhs) & {
          x = norm(x + rhs.x);
return *this;
     constexpr MLong &operator -= (MLong rhs) & {
    x = norm(x - rhs.x);
           return *this;
     constexpr MLong &operator/=(MLong rhs) & {
  return *this *= rhs.inv();
     friend constexpr MLong operator*(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res *= rhs;
           return res:
     friend constexpr MLong operator+(MLong lhs, MLong rhs) {
          MLong res = lhs;
res += rhs;
     friend constexpr MLong operator - (MLong lhs, MLong rhs) {
   MLong res = lhs;
   res -= rhs;
           return res;
     friend constexpr MLong operator/(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res /= rhs;
           return res;
     friend
            constexpr istream &operator>>(istream &is, MLong &a) {
           i64 v;
is >> v;
           a = MLong(v);
           return is;
```

```
ostream & operator << (ostream &os, const MLong &a) {
             return os << a.val():</pre>
       friend constexpr bool operator==(MLong lhs, MLong rhs) {
   return lhs.val() == rhs.val();
       friend constexpr bool operator!=(MLong lhs, MLong rhs) {
   return lhs.val() != rhs.val();
 };
 template<>
 i64 MLong<0LL>::Mod = i64(1E18) + 9;
 constexpr i64 P = 998244353;
using Z = MLong <P>;
// using Z = MLong <0LL>; // change Mod
 struct Comb {
       i64 n;
       vector < Z > _ fac;
vector < Z > _ invfac;
vector < Z > _ inv;
       void init(i64 m) {
            m = min(m, Z::getMod() - 1);
if (m <= n) return;</pre>
            _fac.resize(m + 1);
            _invfac.resize(m + 1);
             _inv.resize(m + 1);
            for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;</pre>
            }
            for (int i = _fac[m].inv();
for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
            n = m:
       Z fac(i64 m) {
   if (m > n) init(2 * m);
   return _fac[m];
       J invfac(i64 m) {
   if (m > n) init(2 * m);
   return _invfac[m];
       If inv(i64 m) {
   if (m > n) init(2 * m);
             return _inv[m];
       Joinom(i64 n, i64 m) {
   if (n < m || m < 0) return 0;
   return fac(n) * invfac(m) * invfac(n - m);</pre>
       |} comb; // 注意宣告, 若要換模數需重新宣告
 6.3 中國餘數定理 [d41d8c]
```

```
ll exgcd(ll a, ll b, ll &x, ll &y) {
     if (!b) {
    x = 1, y = 0;
           return a:
     ll g = exgcd(b, a % b, y, x);
y -= a / b * x;
     return g;
ll inv(ll x, ll m){
     ll a, b;
     exgcd(x, m, a, b);
     a %= m; if (a < \theta) a += m;
     return a;
// remain, mod
ll CRT(vector<pair<ll, ll>> &a){
     ll prod = 1;
for (auto x : a) {
           prod *= x.second;
      ll res = 0;
     for (auto x : a) {
           auto t = prod / x.second;
res += x.first * t % prod * inv(t, x.second) % prod;
if(res >= prod) res -= prod;
     return res:
```

6.4 矩陣與快速幕 [08b5fe]

```
template < class T>
struct Mat {
     int m, n;
     constexpr static ll mod = 1e9 + 7;
vector < vector < T >> matrix;
Mat(int n_ = 0) { init(n_, n_); }
     Mat(int m_, int n_) { init(m_, n_); }
Mat(vector<vector<T>> matrix_) { init(matrix_); }
     matrix.assign(m, vector<T>(n));
     void init(vector<vector<T>> &matrix_) {
          m = matrix_.size();
n = matrix_[0].size();
          matrix = matrix_;
                                                // 單位矩陣
     vector<vector<T>> unit(int n) {
          vector < vector < T >> res(n, vector < T >(n));
for (int i = 0; i < n; i++) {
    res[i][i] = 1;</pre>
          return res:
     constexpr Mat &operator*=(const Mat& rhs) & {
          assert(matrix[0].size() == rhs.matrix.size());
int m = matrix.size()
         }
          matrix = ans.matrix;
return *this;
     constexpr Mat &operator^=(ll p) & {
          assert(m == n); assert(p >= 0);
Mat ans(p-- == 0 ? unit(m) : matrix);
          while (p > 0) {
   if (p & 1) ans *= *this;
   *this *= *this;
               p >>= 1;
          matrix = ans.matrix;
return *this;
     friend Mat operator*(Mat lhs, const Mat &rhs) {
          lhs *= rhs:
          return lhs;
     friend Mat operator^(Mat lhs, const ll p) {
    lhs ^= p;
    return lhs;
     }
// fn = fn-3 + fn-2 + fn-1
```

6.5 樹論分塊 [06204a]

6.6 Mobius Theorem

- 數論 分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1)內計算 f(r)-f(l) 或已經預處理出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數1. 定義

$$\sum_{d|n} \mu(d) = \begin{cases} 1 & \text{for } n = 1 \\ 0 & \text{for } n \neq 0 \end{cases}$$

- 2. μ 是常數函數 1 的反元素 $\Rightarrow \mu*1=\epsilon$, $\epsilon(n)$ 只在n=1時為 1,其餘情況皆為 0。
- φ歐拉函數: x以下與 x 互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^i) \\ &= 1 + p^0(p-1) + p^1(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^c \\ &= id \end{split}$$

• 莫比烏斯反演公式

-
$$f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$$

- $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

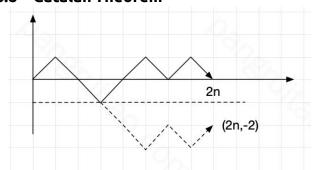
• 例子

$$\begin{split} &\sum_{i=aj=c}^{b} \sum_{j=1}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{\infty} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \left\lfloor d|j| \right\rfloor \, \mathrm{d} \, \mathrm{可整除} \, \mathrm{i} \, \mathrm{B} \, \mathrm{A} \, \mathrm{1} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.7 其比烏斯反演 [d41d8c]

```
const int maxn = 2e5;
    ll mobius_pref[maxn];
     void init() {
                        mobius_pref[1] = 1;
                        vector<ll> wei
                       (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除 for (ll i = 2; i < maxn; i++) {    if (wei[i] == -1) {
                                                             mobius_pref[i] = mobius_pref[i - 1];
                                                               continue; // 包含平方
                                         fif (wei[i] == 0) {
    wei[i] = 1;
    for (ll j = 2; i * j < maxn; j++) {
        if (j % i == 0) wei[i * j] = -1;
        else if (wei[i * j] != -1) wei[i * j]++;
        relation of the content of the conten
                                                             }
                                           mobius pref[i]
                                                                   = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
                      }
     void solve() {
                        ll a, b, c, d, k; cin >> a >> b >> c >> d >> k;
auto cal = [&](ll x, ll y) -> int {
                                           int res = 0;
                                            for (int l = 1, r; l <= min(x, y); l = r + 1) {
    r = min(x / (x / l), y / (y / l));
    res += (mobius_pref[r] - mobius_pref[l]</pre>
                                                                                          - 1]) * (x / l) * (y / l); // 代推出來的式子
                                           return res;
                        cout << cal
                                              (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k, (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n";
}
```

6.8 Catalan Theorem



1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$ 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有x 個,往下有y 個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.9 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- X/G:本質不同的方案的集合
- X'^g : 對於某一種操作 g, 所有方案中,經過 g 這種翻轉後保持不變的方案的集合
- 集合取絕對值代表集合數

7 Search and Gready

7.1 二分搜 [d41d8c]

```
int main() {
    int l = 1, r = 10;
    // 1 to tar, find tar
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}</pre>
```

7.2 三分搜 [d41d8c]

```
| // 找極值問題,遞增遞減
| void solve() {
| int | = 0, r = 10, ans = 0; // ans 紀錄答案 |
| while (| <= r) {
| int | d = (r - l) / 3; // 差 |
| int | ml = l + d, mr = r - d; // mr 要用減的 |
| auto | cal = [&](int | m) -> int {
| int | x = 0; |
| return | x; // 計算答案 |
| ; int | ansl = | cal(|ml), ansr = | cal(|mr); if (| ansl | < | ansr) {
| l = | ml + 1; |
| else | r = | mr - 1; |
| }
```

8 Tree

8.1 LCA [9f95b1]

```
}
int lca(int a, int b) {
    if (depth[a] < depth[b]) swap(a, b);
    int pull = depth[a] - depth[b];
    for (int i = 0; i < 18; i++) {
        if (pull & (1 << i)) {
            a = par[a][i];
        }
    if (a == b) return a;
    for (int i = 17; i >= 0; i--) {
        if (par[a][i] != par[b][i]) {
            a = par[a][i], b = par[b][i];
        }
    }
    return par[a][0];
}
```

8.2 樹重心 [30b436]

```
struct centroid_decomposition {
       int n:
        vector<vector<int>> adj;
        vector<bool> vis;
       vector<int> siz;
       centroid_decomposition() {}
centroid_decomposition(int n_) { init(n_); }
       void init(int n_) {
             n = n_;
adj.assign(n, {});
vis.assign(n, false);
             siz.assign(n, 1);
        void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void get_siz(int dep, int x, int p = -1) {
             siz[x] = 1;
             stz[x] = 1;
for (int y : adj[x]) {
    if (y == p || vis[y]) continue;
    get_siz(dep + 1, y, x);
    siz[x] += siz[y];
       return get_cen(y, sz, x);
              return x:
       void work(int x = 0) {
    get_siz(0, x);
    int cen = get_cen(x, siz[x]);
    vis[cen] = true;
              // do something
              for (int y : adj[cen]) {
   if (vis[y]) continue;
   work(y);
1 };
```

8.3 樹壓平 [51199c]

```
點加值 = 所有子節點區間加值,求單點,使用 bit,做前綴差分
CSES 1138_Path Queries
   int n, q; cin >> n >> q;
vector <int> node_value(n + 1), euler_ordered_value(n);
for (int i = 1; i <= n; i++) {</pre>
        cin >> node_value[i];
   vector<vector<int>> tree(n + 1);
   for (int i = 1; i < n; i++) {
  int u, v; cin >> u >> v;
  tree[u].push_back(v);
        tree[v].push_back(u);
   vector<pair<int, int>> tree mapping(n + 1);
   int cnt = 0;
auto dfs = [&](auto self, int u, int par) -> void {
    euler_ordered_value[++cnt] = node_value[u];
        tree_mapping[u].first = cnt;
        for (auto v : tree[u]) {
   if (v == par) continue;
   self(self, v, u);
        tree_mapping[u].second = cnt;
   dfs(dfs,
   BIT bit(n);
for (int i = 1; i <= n; i++) {
        bit.modify(tree_mapping[i].first, node_value[i]);
        if (tree_mapping[i].first < n) { // root 就不用扣了</pre>
                    (tree_mapping[i].second + 1, -node_value[i]);
```

8.4 Heavy Light Decomposition [6791f6]

```
struct HLD {
     vector<int> siz, top, dep, parent, in, out, seq;
      vector<vector<int>> adj;
     int cur;
     HLD() {}
HLD(int n) {
           init(n);
     void init(int n) {
           this ->n = n:
           siz.resize(n);
           top.resize(n);
           dep.resize(n);
parent.resize(n);
           .
in.resize(n);
           out.resize(n);
           seq.resize(n);
           adj.assign(n, {});
     void addEdge(int u, int v) {
           adj[u].push_back(v);
           adj[v].push_back(u);
     void work(int root = 0) {
           top[root] = root;
dep[root] = 0;
           parent[root] = -1;
           dfs1(root);
           dfs2(root):
     void dfs1(int u) {
           if (parent[u] != -1) {
    adj[u].erase(find
                       (adj[u].begin(), adj[u].end(), parent[u]));
           siz[u] = 1;
           for (auto &v : adj[u]) {
    parent[v] = u;
    dep[v] = dep[u] + 1;
                dfs1(v);
                siz[u] += siz[v];
if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
                } // 讓 adj[u][0] 是重子節點
          }
     void dfs2(int u) {
           in[u] = cur++;
           seq[in[u]] = u; // dfn 對應的編號
           seq[in[u]] - u, // u// same as a seq[in[u]] - u, // u// same as a seq[in] (a) {
    top[v] = v == adj[u][0] ? top[u] : v;
                dfs2(v):
           out[u] = cur;
     int lca(int u, int v) {
           while (top[u] != top[v]) {
    if (dep[top[u]] > dep[top[v]]) {
        u = parent[top[u]];
}
                } else {
                      v = parent[top[v]];
           return dep[u] < dep[v] ? u : v;</pre>
     int dist(int u, int v) {
   return dep[u] + dep[v] - 2 * dep[lca(u, v)];
     int jump(int u, int k) {
    if (dep[u] < k) {
        return -1;</pre>
           int d = dep[u] - k;
```

```
while (dep[top[u]] > d) {
    u = parent[top[u]];
          return seq[in[u] - dep[u] + d];
     bool isAncester(int u, int v) {
          // 判斷 u 是否是 v 的祖先
          return in[u] <= in[v] && in[v] < out[u];</pre>
      int rootedParent(int u, int v) {
          // 根據新根節點 u 計算 v 的父節點
          swap(u, v);
          if (u == v) {
               return u;
          if (!isAncester(u, v)) {
               return parent[u];
          auto it = upper_bound(adj
    [u].begin(), adj[u].end(), v, [&](int x, int y) {
    return in[x] < in[y];</pre>
          }) - 1;
return *it;
      int rootedSize(int u, int v) {
          // 根據新根節點 u 計算子樹 v 的大小
          if (u == v) {
          if (!isAncester(v, u)) {
              return siz[v];
          return n - siz[rootedParent(u, v)];
      int rootedLca(int a, int b, int c) {
          // 根據新的根節點計算三個節點 a、b 和 c 的最近公共祖先 return lca(a, b) ^ lca(b, c) ^ lca(c, a);
     }
};
```

8.5 Virtual Tree [622e69]

```
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
// 可以建立虚樹達成快速樹 DP
 // 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector <int>stk(maxn);
 int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
        vt[stk[top - 1]].push_back(stk[top]), top--;
    if (stk[top - 1] != l) {
        vt[l] sush back(stk[top]);
        vt[l] sush back(stk[top]);
        vt[l] sush back(stk[top]);
}</pre>
                vt[l].push_back(stk[top]);
                 stk[top] = l;
         } else vt[l].push_back(stk[top--]);
         stk[++top] = u;
  void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
         vt[u].clear();
  void solve(int n, int q) {
         vector g(n + 1, vector<pair<int, int>>());
         vector vt(n + 1, vector vector vt(n + 1, vector <int>()); // dfs 完清除, 否則會退化
vector <ll> dp(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;

                g[u].push_back({v, w});
                 g[v].push_back({u, w});
         build_lca(n, g);
         build(n, g);
for (int i = 0; i < q; i++) {
   int m; top = -1; cin >> m;
                 vector<int> key(m);
                for (int j = 0; j < m; j++) {
    cin >> key[j];
                         iskey[key[j]] = 1;
                key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
                 for (int x : key) insert(x, vt);
                while (top
                           > 0) vt[stk[top - 1]].push_back(stk[top]), --top;
                 // DP
                auto dfs = [&](auto self, int u) -> void {
    for (auto v : vt[u]) {
        self(self, v);
        if (iskey[v]) {
            dp[u] += min_dis[v];
        }
                                       // 砍掉 1 到 v 之間最短的路
                                       dp[u] += min(dp[v], min_dis[v]);
                                iskey[v] = dp[v] = 0;
```

```
vt[u].clear();
};

dfs(dfs, key[0]); // key[0] 一定是 root
cout << dp[key[0]] << "\n";
iskey[key[0]] = dp[key[0]] = 0;
}
}
```

8.6 Dominator Tree [baa540]

```
struct Dominator_tree {
       int n, id;
       vector <vector <int>> adj, radj, bucket;
vector <int>> sdom, dom, vis, rev, pa, rt, mn, res;
Dominator_tree(int n_ = 0) { init(n_); }
       void init(int _n) {
    n = _n, id = 0;
    adj.assign(n, vector<int>());
    radj.assign(n, vector<int>());
               bucket.assign(n, vector<int>());
sdom.resize(n); dom.assign(n, -1)
vis.assign(n, -1); rev.resize(n);
pa.resize(n); rt.resize(n);
               mn.resize(n); res.resize(n);
       void add_edge(int u, int v) { adj[u].push_back(v); }
int query(int v, int x) {
    if (rt[v] == v) return x ? -1 : v;
    int p = query(rt[v], 1);
    if (p == -1) return x ? rt[v] : mn[v];
    if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
    rt[v] = p.
               rt[v] = p;
return x ? p : mn[v];
       dfs(u), pa[vis[u]] = vis[v];
                       radj[vis[u]].push_back(vis[v]);
               }
        void build(int s) {
               dfs(s);
               for (int i = id - 1; i >= 0; i--) {
                       (Int i = tu - 1, color
for (int u : radj[i])
    sdom[i] = min(sdom[i], sdom[query(u, 0)]);
                       if (i) bucket[sdom[i]].push_back(i);
for (int u : bucket[i]) {
                              int p = query(u, 0);
dom[u] = sdom[p] == i ? i : p;
                       }
if (i) rt[i] = pa[i];
               res.assign(n, -1);
               for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];
for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre>
               for (int i = 0; i < n; i++) dom[i] = res[i];</pre>
};
```

9 DP

9.1 LCS [5781cf]

9.2 LIS [66d09f]

```
int main() {
   int n; cin >> n;
   vector < int > v(n);
   for (int i = 0; i < n; i++) cin >> v[i];
```

9.3 Edit Distance [308023]

9.4 Bitmask [b18541]

```
void travel_exactly_once(){
      // [走過的路][終點]
      vector<vector<int>> dp(1 << 20, vector<int> (20, 0));
     vector<int> rev_adj[20];
     for(int i = 0; i < m; i++){
   int u, v; cin >> u >> v;
   rev_adj[--v].push_back(--u);
     | dp[1][0] = 1;
| for (int road = 0; road < (1 << n); road++) {
| // 沒經過起點,不用走
           if (road & 1 == 0) continue;
          // 有終點但沒全部走過
if (road & (1
                  << (n
                            1)) && road != ((1 << n) - 1)) continue;
           // DP ,随便選定一個當前路徑的終點
for (int end = 0; end < n; end++) {
                (Int end = 0; end < n; end++) {
// 路徑沒包含假定的 end
if ((road & (1 << end)) == 0) continue;
// 去除終點,得到 pre_road
int pre_road = road - (1 << end);
// 從 rev_adj 找 pre_road 的終點
                for (int pre_road_end : rev_adj[end]) {
   if ((road & (1 << pre_road_end))) {</pre>
                           dp[road
                           ][end] += dp[pre_road][pre_road_end];
dp[road][end] %= mod;
                     }
          }
     cout << dp[(1 << n) - 1][n - 1];
void elevator_rides(){
     int n, k; cin >> n >> k;
vector<int> passenger(n);
      for (int i = 0; i < n; i++) cin >> passenger[i];
     vector<int
     for (int j = 0; j < n; j++) {
                if (i & (1 << j)) { // 有 j
int pre = i ^ (1 << j);
                      // 最後的電梯還能載 j
                      if (used[pre] + passenger[j] <= k) {</pre>
                           // 電梯數先比,再來比用掉的空間
```

9.5 Projects [0942aa]

```
int main() { // 排程有權重問題,輸出價值最多且時間最少
struct E {
    int from, to, w, id;
    bool operator <(const E &rhs) {
        return to == rhs.to ? w > rhs.w : to < rhs.to;
}};
    int n; cin >> n; vector <E> a(n + 1);
    for (int i = 1; i <= n; i++) {
        int u, v, w; cin >> u >> v >> w;
        a[i] = {u, v, w, i};
    }
    vector <array<ll, 2>> dp(n + 1); // w, time
    vector <array<ll, 2>> rec(n + 1); // 有沒選, 上個是誰
    sort(a.begin(), a.end());
    for (int i = 1; i <= n; i++) {
        auto it = --lower_bound(all(a), E({0, a[i].from}),
        [](E x, E y){ return x.to < y.to; });
        int id = it - a.begin(); dp[i] = dp[i - 1];
        ll nw = dp[id][0] + a[i].w;
        ll nw = dp[id][1] + a[i].to - a[i].from;
        if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
            dp[i] = {nw, nt}; rec[i] = {1, id};
        }
}
vector <int> ans;
for (int i = n; i != 0;) {
        if (rec[i][0]) {
            ans.push_back(a[i].id);
            i = rec[i][1];
        } else i--;
}
```

9.6 Removal Game [7bb56b]

}

9.7 CF Example [7d37ea]

```
| // CF 1932 pF
| // 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
| // 請問在線段不重複的情况下,最多獲得幾分
int main() {
    int n, m;
    cin >> n >> m;
| // 記錄每點有幾個線段
| // 再一個紀錄,包含這個點的左界
    vector <int> l_side(n + 1, inf), cnt(n + 5, 0);
    for (int i = 0; i < m; i++) {
        int l, r; cin >> l >> r;
        l_side[r] = min(l_side[r], l);
        cnt[l]++;
        cnt[r + 1]--;
    }
    for (int i = 2; i <= n; i++) {
        cnt[i] += cnt[i - 1];
    }
```

```
for (int i = n; i >= 2; i--) {
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
      vector<int> dp(n + 1):
      dp[0] = 0;
      for (int i = 1; i <= n; i++) {
           dp[i] = cnt[i];
if (l_side[i] != inf)
                dp[i] += dp[l_side[i] - 1];
           dp[i] = max(dp[i], dp[i - 1]);
      cout << dp[n] << "\n";
}
// CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
// 再加上 max(bi) - min(bi)
int main(){
      int n, k, ans = 0; cin >> n >> k;
vector <pii> v(n + 1);
for (int i = 1; i <= n; i++) {</pre>
           int a, b; cin >> a >> b;
v[i] = {a, b};
if (a <= k) ans = 1;</pre>
      sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
      }); // 用 bi 來排,考慮第 i 個時可以先扣 vector<vector<int>> dp(n + 1, vector<int>(n + 1, inf));
      // 考慮 v[i] 時, 選 j 個的 sum(ai) - min(bi)
     for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
                 // min(不選, 選)
                         1][j - 1] + v[i].first + v[i].second <= k) {
                       // 假如可以選,更新 ans 時再加回去 bi
                      ans = max(ans, j);
           dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
      cout << ans << endl;
```

10 Geometry

10.1 Basic [d41d8c]

```
#include <bits/stdc++.h>
using namespace std;
using i64 = long long;
struct Point {
    T x;
T v:
     Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) \{ \}
     operator Point<U>()
         return Point<U>(U(x), U(y));
     Point & operator += (const Point &p) & {
         x += p.x;
         y += p.y;
return *this;
     Point & operator -= (const Point &p) & {
         x -= p.x;
         y -= p.y;
return *this;
     Point & operator *= (const T & v) & {
         x *= v;
         y *= v;
return *this;
     Point & operator /= (const T &v) & {
         y /= v;
         return *this;
     Point operator - () const {
         return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
         return a += b;
     friend Point operator - (Point a, const Point &b) {
         return a -= b;
     friend Point operator*(Point a, const T &b) {
   return a *= b;
     friend Point operator/(Point a, const T &b) {
         return a /= b;
```

```
friend Point operator*(const T &a, Point b) {
   return b *= a;
     friend bool operator == (const Point &a, const Point &b) {
          return a.x == b.x && a.y == b.y;
     friend istream &operator>>(istream &is, Point &p) {
   return is >> p.x >> p.y;
     friend ostream & operator < <(ostream & os, const Point & p) {
    return os << "(" << p.x << ", " << p.y << ")";</pre>
};
template < class T>
struct Line {
     Point <T> a:
     Point<T> b;
     Line(const Point<T> &a_ = Point<T>()
          , const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
}:
template < class T>
T dot(const Point<T> &a. const Point<T> &b) {
     return a.x * b.x + a.y * b.y;
template < class T>
 cross(const Point<T> &a, const Point<T> &b) {
  return a.x * b.y - a.y * b.x;
                                                                                   }
template < class T>
T square(const Point < T > & p) {
     return dot(p, p);
template < class T>
double length(const Point<T> &p) {
     return sqrt(square(p));
template < class T>
double length(const Line < T > & l) {
    return length(l.a - l.b);
template < class T>
Point<T> normalize(const Point<T> &p) {
     return p / length(p);
template < class T>
bool parallel(const Line<T> &l1, const Line<T> &l2) {
     return cross(l1.b - l1.a, l2.b - l2.a) == 0;
template < class T>
double distance(const Point<T> &a, const Point<T> &b) {
    return length(a - b);
template < class T>
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class Ta
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0) {
      return distance(p, l.a);
}</pre>
     if (dot(p - l.b, l.a - l.b) < 0) {
    return distance(p, l.b);</pre>
     return distancePL(p, l);
}
template < class T>
Point<T> rotate(const Point<T> &a) {
    return Point(-a.y, a.x);
template < class T>
int sgn(const Point<T> &a) {
     return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
    return cross(l.b - l.a, p - l.a) > 0;
                                                                                   }
template < class T>
     template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
```

```
return cross(p - l.a, l.b - l.a) == 0 &&
    min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)</pre>
             && min
                    (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
        .
(const Point<T> &a, const vector<Point<T>> &p) {
      int n = p.size();
for (int i = 0; i < n; i++) {
    if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {</pre>
                    return true;
      }
      int t = 0;
for (int i = 0; i < n; i++) {</pre>
             auto u = p[i];
             auto v = p[(i + 1) \% n];
             if (u.x < a.x)
                    && v.x >= a.x && pointOnLineLeft(a, Line(v, u))) {
                   t ^= 1;
             if (u.x >= a.x
                     && v.x < a.x && pointOnLineLeft(a, Line(u, v))) {
                   t ^= 1;
      return t == 1:
// 0 : not intersect
    1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
tuple<int, Point<T>, Point<T>> segmentIntersection
  (const Line<T> &11, const Line<T> &12) {
  if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
    return {0, Point<T>(), Point<T>()};
                                                                    l2.b.x)) {
      if (min(l1.a.x, l1.b.x) > max(l2.a.x, l.
    return {0, Point<T>(), Point<T>()};
                                                                   l2.b.x)) {
      if (max(l1.a.y, l1.b.y) < min(l2.a.y, l
    return {0, Point<T>(), Point<T>()};
                                                                   l2.b.y)) {
      if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y)) {
   return {0, Point<T>(), Point<T>()};
      if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
   if (cross(l1.b - l1.a, l2.a - l1.a) != 0) {
                    return {0, Point<T>(), Point<T>()};
             } else {
                   auto maxx1 = max(l1.a.x, l1.b.x);
auto minx1 = min(l1.a.x, l1.b.x);
                   auto maxy1 = max(l1.a.y, l1.b.y);
auto miny1 = min(l1.a.y, l1.b.y);
auto maxx2 = max(l2.a.x, l2.b.x);
                   auto maxx2 = max(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.x, l2.b.x);
auto miny2 = max(l2.a.y, l2.b.y);
auto miny2 = min(l2.a.y, l2.b.y);
Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
if (logintOSSagment(n1, l1))
                   if (!pointOnSegment(p1, l1)) {
                          swap(p1.y, p2.y);
                    if (p1 == p2) {
                         return {3, p1, p2};
                   } else {
                          return {2, p1, p2};
            }
      auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
      Point p = lineIntersection(l1, l2); if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
             return {1, p, p};
      } else {
             return {3, p, p};
      }
 template<class T
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
   if (get<0>(segmentIntersection(l1, l2)) != 0) {
             return 0.0;
       return min({distancePS(l1.a, l2), distancePS(l1
              .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
```

```
template < class T>
bool segmentInPolygon
     (const Line<T> &l, const vector < Point < T>> &p) {
int n = p.size();
     if (!pointInPolygon(l.a, p)) {
          return false;
     if (!pointInPolygon(l.b, p)) {
          return false;
     for (int i = 0; i < n; i++) {
    auto u = p[i];
    auto v = p[(i + 1) % n];
    auto w = p[(i + 2) % n];</pre>
          auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
          if (t == 1) {
    return false;
          if (t == 0) {
               continue;
          if (t == 2) {
               if (pointOnSegment(v, l) && v != l.a && v != l.b) {
   if (cross(v - u, w - v) > 0) {
      return false;
              }
         || pointOnLineLeft(l.b, Line(v, u))) {
              } else if (p1 == v) {
    if (l.a == v) {
        if (pointOnLineLeft(u, l)) {
                              if (pointOnLineLeft(w, l)
                                   && pointOnLineLeft
                                   (w, Line(u, v))) {
return false;
                         } else {
                              if (pointOnLineLeft(w, l)
                                   || pointOnLineLeft
                                   (w, Line(u, v))) {
return false;
                    } else if (l.b == v) {
                         if (pointOnLineLeft(u, Line(l.b, l.a))) {
   if (pointOnLineLeft(w, Line(l.b, l.a))
    && pointOnLineLeft
                                   (w, Line(u, v))) {
return false;
                        (w, Line(u, v))) {
return false;
                              }
                    } else {
   if (pointOnLineLeft(u, l)) {
        if (pointOnLineLeft(w, L)) }
                              (w, Line(u, v))) {
return false;
                        (w, Line(u, v))) {
return false;
                             }
                        }
                   }
              }
         }
     return true:
template < class T>
vector<Point<T>> hp(vector<Line<T>> lines) {
    sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
    auto d1 = l1.b - l1.a;
    auto d2 = l2.b - l2.a;
          if (sgn(d1) != sgn(d2)) {
    return sgn(d1) == 1;
          return cross(d1, d2) > 0;
    });
     deque<Line<T>> ls:
     deque<Point<T>> ps;
     for (auto l : lines) {
          if (ls.empty()) {
```

```
ls.push back(l):
        }
        while (!ps.empty() && !pointOnLineLeft(ps.back(), l)) {
             ps.pop_back();
             ls.pop_back();
        while (!ps.empty() && !pointOnLineLeft(ps[0], l)) {
             ps.pop_front();
ls.pop_front();
        }
        if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
                  (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                 if (!pointOnLineLeft(ls.back().a, l)) {
                     assert(ls.size() == 1);
                     ls[0] = l;
                 continue;
             return {}:
        ps.push_back(lineIntersection(ls.back(), l));
         ls.push_back(l);
    }
    while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0])) {
        ps.pop_back();
ls.pop_back();
    if (ls.size() <= 2) {</pre>
        return {};
    ps.push_back(lineIntersection(ls[0], ls.back()));
    return vector(ps.begin(), ps.end());
using P = Point<i64>:
10.2 Convex Hull [01a63e]
int main() {
   int n; cin >> n;
    vector <P> P(n), U, L;
for (int i = 0; i < n; i++) {
   cin >> P[i];
    sort(P.begin()
        .end(), [](const Point<i64> &a, const Point<i64> &b) {
return a.x == b.x ? a.y < b.y : a.x < b.x;
    L.pop_back();
        U.pop_back();
        L.push_back(P[i])
        U.push_back(P[i]);
    cout << L.size() + U.size() - 2 << "\n";
    for (int i = 0; i < L.size() - 1; i++) {
  cout << L[i].x << " " << L[i].y << " | n";</pre>
```

10.3 MinEuclideanDistance [469a8f]

for (int i = U.size() - 1; i > 0; i--) {
 cout << U[i].x << " " << U[i].y << "\n";</pre>

```
template <class I >
T distanceSquare(const Point < T > & a, const Point < T > & b) {
    return square(a - b);
}
void solve() {
    int n; cin >> n;
    constexpr i64 inf = 8e18;
    vector < Point < i64 >> a(n);
    for (int i = 0; i < n; i++) {
        i64 x, y;
        cin >> x >> y;
        a[i] = Point < i64 > (x, y);
}
struct sortY {
    bool operator()
        (const Point < i64 > & a, const Point < i64 > & b) const {
        return a.y < b.y;
    }
};
struct sortXY {
    bool operator()
        (const Point < i64 > & a, const Point < i64 > & b) const {
        bool operator()
        (const Point < i64 > & a, const Point < i64 > & b) const {
        const Point < i64 > & a, const Point < i64 > & b) const {
        const Point < i64 > & a, const Point < i64 > & b) const {
        const Point < i64 > & a, const Point < i64 > & b) const {
        const Point < i64 > & a, const Point < i64 > & b) const {
        const Point < i64 > & a, const Point < i64 > & b) const {
        const Point < i64 > & a, const Point < i64 > & b) const {
        const Point < i64 > & a, const Point < i64 > & b) const {
        const Point < i64 > & a, const Point < i64 > & b) const {
        const Point < i64 > & a, const Point < i64 > & b) const {
        const Point < i64 > & a, const Point < i64 > & b) const {
        const Point < i64 > & a, const Point < i
```

10.4 LatticePoints [7750d6]