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```

1 Basic

1.1 Install VScode [d41d8c]

```
// 如何安裝 vscode
// 1. 下載 vscode & msys2
// 2. 在跳出的 terminal 中 / 或打開 ucrt64,打上
     "pacman -S --needed base-devel mingw-w64-x86_64-toolchain"
// 3. 環境變數加上 C:\\msys64\\ucrt64\\bin
// 4. 重開 vscode, 載 C/C++, 運行, 編譯器選擇 g++
// 5. 打開 settings -> compiler -> add compilerPath
-> 在 "" 裡打上 C:\\msys64\\ucrt64\\bin\\g++.exe
```

1.2 Default Code [d41d8c]

```
#include <bits/stdc++.h>
// #pragma GCC target("popcnt")
// C++ 20 vector grammer will not work
using namespace std;
using ll = long long;
void solve() {
}
int main() {
      ios_base::sync_with_stdio(false);
cin.tie(nullptr);
       int t = 1;
      cin >> t;
while (t--) {
             solve();
      }
}
```

1.3 Compare Fuction [d41d8c]

```
// 1. sort, 二分搜刻在函式內 lambda 就好
// 2. priority queue 小到大是 >, set 是 <
// 3. set 不能 = , multiset 必須 =
// 4. 確保每個成員都要比到
// 7. mellower_bound
// 5. pbds_multiset 不要用 lower_bound
// 6. 如果要用 find, 插入 inf 後使用 upper_bound
// 7. multiset 可以跟 set 一樣使用, 但請注意第 3、4 點
auto cmp = [](int i, int j) { return i > j; };
priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
vector<int> a {1, 2, 5, 4, 3}; // 小心不要改到 a auto cmp = [&a](int i, int j) { return a[i] > a[j]; }; priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
```

1.4 Pbds [d41d8c]

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
wsing namespace __gnu_pbds;
template<typename T>
using pbds_set = tree<T, null_type,
    less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template<typename T>
```

1.5 Double [b44e11]

```
struct D {
     double x;
     constexpr static double eps = 1e-12;
     D() : x{0.0} {}
D(double v) : x{v} {}
double val() const { return x; }
     explicit operator double() const { return x; }
       operator -() const {
  return D(-x);
     D &operator+=(const D &rhs) & {
    x += rhs.x; return *this;
     D &operator -= (const D &rhs) & {
    x -= rhs.x; return *this;
     D & operator *= (const D & rhs) & {
          x *= rhs.x; return *this;
     D & operator/=(const D & rhs) & {
    assert(fabs(rhs.x) > eps);
    x /= rhs.x; return *this;
     friend D operator+(D lhs, const D &rhs) {
          return lhs += rhs;
      friend D operator-(D lhs, const D &rhs) {
          return lhs -= rhs;
     friend D operator*(D lhs, const D &rhs) {
          return lhs *= rhs;
     friend D operator/(D lhs, const D &rhs) {
          return lhs /= rhs;
     friend bool operator<(const D &lhs, const D &rhs) {
          return lhs.x - rhs.x < -eps;</pre>
     friend bool operator > (const D &lhs. const D &rhs) {
          return lhs.x - rhs.x > eps;
     friend bool operator == (const D &lhs. const D &rhs) {
          return fabs(lhs.x - rhs.x) < eps;</pre>
     friend bool operator <= (const D &lhs, const D &rhs) {
   return lhs < rhs || lhs == rhs;</pre>
     friend bool operator>=(const D &lhs, const D &rhs) {
   return lhs > rhs || lhs == rhs;
     friend bool operator!=(const D &lhs, const D &rhs) {
   return !(lhs == rhs);
     friend istream &operator>>(istream &is, D &a) {
          double v; is >> v; a = D(v); return is;
     } // eps should < precision
};
```

2 Graph

2.1 DFS And BFS [e2d856]

```
int n;
vector<vector<int>> adj(n);
// dfs_graph
vector<bool> vis(n);
auto dfs = [&](auto self, int u) -> void {
   if (vis[u]) return;
      vis[u] = true;
for (auto v: adj[u]) {
    self(self, v);
     }
dfs(dfs, 0);
vector<int> depth(n, 1e9);
queue<int> q;
auto bfs = [&](auto self, int s) -> void {
    vis[s] = true, depth[s] = 0;
      q.push(s);
      while (!q.empty()) {
    int u = q.front(); q.pop();
             for (auto v : adj[u]) {
```

```
if (vis[v]) continue;
    vis[v] = true;
    depth[v] = depth[u] + 1;
    q.push(v);
    }
};
bfs(bfs, 0);
}
```

2.2 Prim [3a3805]

2.3 BellmanFord [430ded]

```
|// 用 Bellman Ford 找負環
int main() {
    int n, m; cin >> n >> m;
    vector<array<int, 3>> e;
    for (int i = 0; i < m; i++) {
        int u, v, w; cin >> v >> v >> w;
        u--, v--; e.push_back({u, v, w});
}

vector<ll> dis(n, inf), par(n);
int t = -1; dis[0] = 0;
for (int i = 1; i < n; i++) {
        for (auto [u, v, w] : e) {
            if (dis[v] > dis[u] + w) {
                dis[v] = dis[u] + w;
                 par[v] = u;
                if (i == n) t = v;
            }
      }

if (t == -1) { cout << "NO\n"; return; }
for (int i = 1; i < n; i++) t = par[t];
vector<int> ans {t};
int i = t;
do {
        i = par[i];
        ans.push_back(i);
} while (i != t);
reverse(ans.begin(), ans.end());
cout << "YES\n";
for (auto x : ans) cout << x + 1 << " ";
```

2.4 FloydWarshall [3f61a4]

2.5 Euler [4177dc]

```
|// 1. 無向圖是歐拉圖:
|// 非零度頂點是連通的
| // 頂點的度數都是偶數
| // 2. 無向圖是半歐拉圖(有路沒有環):
// 非零度頂點是連通的
 // 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
// 非零度頂點是強連通的
 // 每個頂點的入度和出度相等
// 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
// 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
 // 其他頂點的入度和出度相等
 vector < int > ans;
auto dfs = [&](auto &&self, int u) -> void {
    while (g[u].size()) {
        int v = *g[u].begin();
}
          g[u].erase(v);
          self(self, v);
      ans.push back(u);
 dfs(dfs, 0);
reverse(ans.begin(), ans.end());
 2.6 SCC [5d3e16]
 struct SCC {
   int n, cur, cnt;
   vector<vector<int>> adj;
      vector <int> stk, dfn, low, bel;
SCC(int n_ = 0) { init(n_); }
void init(int n_) {
          n = n_;
adj.assign(n, {});
          low.resize(n);
          bel.assign(n, -1);
          stk.clear();
          cur = cnt = 0;
      void addEdge(int u, int v) {
          adj[u].push_back(v);
     void dfs(int x) {
    dfn[x] = low[x] = cur++;
          stk.push_back(x);
          for (auto y : adj[x]) {
   if (dfn[y] == -1) {
                   dfs(y);
               low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
                    low[x] = min(low[x], dfn[y]);
               }
          if (dfn[x] == low[x]) {
               int y;
do {
                   y = stk.back();
                   bel[y] = cnt;
                   stk.pop_back();
               } while (y != x);
          }
      vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
          return bel:
      struct Graph {
          vector<pair<int, int>> edges;
          vector<int> siz;
          vector<int> cnte;
      Graph compress() {
          Graph g;
          g.n = cnt;
          a.siz.resize(cnt):
          g.cnte.resize(cnt);
          g.edges.emplace_back(bel[i], bel[j]);
                   } else {
                        g.cnte[bel[i]]++;
              }
          return g;
```

};

2.7 VBCC [170604]

```
struct VBCC {
    int n, cur;
vector<vector<int>> adj;
    vector <int> dfn, low, parent;
vector <bool> is_cut;
VBCC(int n_ = 0) { init(n_); }
void init(int n_) {
         n = n_;
adj.assign(n, {});
         dfn.assign(n, -1);
low.resize(n);
         parent.assign(n.
         is_cut.assign(n, false);
         cur = 0;
    void addEdge(int u, int v) {
         adj[u].push_back(v);
         adj[v].push_back(u);
    parent[v] = x;
                  dfs(v);
                  low[x] = min(low[x], low[v]);
                  if (parent[x] != -1 && low[v] >= dfn[x]) {
   is_cut[x] = true;
             } else if (v != parent[x])
                  low[x] = min(low[x], dfn[v]);
             }
         if (parent[x] == -1 && children > 1) {
              is_cut[x] = true;
         }
    dfs(i);
             }
         }
};
```

2.8 EBCC [59d8ca]

```
struct EBCC { // CF/contest/1986/pF
   int n, cur, cnt;
   vector<vector<int>> adj;
     vector<int> stk, dfn, low, bel;
     vector<pair<int, int>> bridges; // 關鍵邊
EBCC(int n_ = 0) { init(n_); }
void init(int n_) {
           n = n_;
           adj.assign(n, {});
           dfn.assign(n, -1);
low.resize(n);
           bel.assign(n, -1);
           stk.clear();
bridges.clear();
           cur = cnt = 0;
     void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
     void dfs(int x, int p) {
           dfn[x] = low[x] = cur++;
          bridges.emplace_back(x, y);
                } else if (bel[y] == -1) {
                      low[x] = min(low[x], dfn[y]);
           if (dfn[x] == low[x]) {
                int y;
do {
    y = stk.back();
                      bel[y] = cnt;
                      stk.pop_back();
                } while (y != x);
                cnt++;
          }
     vector < int> work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {</pre>
                      dfs(i, -1);
```

```
}
           return bel;
      struct Graph {
           vector<pair<int, int>> edges;
           vector<int> siz; // BCC 內節點數
           vector<int> cnte; // BCC 內邊數
      Graph compress() {
           Graph g;
           g.n = cnt;
           g.siz.resize(cnt);
           g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;</pre>
                for (auto j : adj[i]) {
    if (bel[i] < bel[j]) {</pre>
                        g.edges.emplace_back(bel[i], bel[j]);
else if (i < j) {
  g.cnte[bel[i]]++;</pre>
                }
           return q;
     }
};
2.9 2-SAT [eeddc1]
// CSES Giant Pizza
```

```
struct TwoSat {
        int n; vector<vector<int>> e;
        vector<bool> ans;
       vector volume ans,
TwoSat(int n): n(n), e(2 * n), ans(n) {}
void addClause(int u, bool f, int v, bool g) {
    e[2 * u + !f].push_back(2 * v + g);
    e[2 * v + !g].push_back(2 * u + f);
        bool satisfiable() {
               vector < int
> id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
               vector <int> stk;
int now = 0, cnt = 0;
function <void(int)> tarjan = [&](int u) {
                      stk.push_back(u);
dfn[u] = low[u] = now++;
                       for (auto v : e[u]) {
    if (dfn[v] == -1)
                                     tarjan(v);
                              low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in stk
low[u] = min(low[u], dfn[v]);
                      }
if (dfn[u] == low[u]) {
                              int v;
                              do {
                                     v = stk.back();
                              stk.pop_back();
id[v] = cnt;
} while (v != u);
                              ++cnt:
                     }
               for (int i
                         = 0; i < 2 * n; ++i) if (dfn[i] == -1) tarjan(i);
               for (int i = 0; i < n; ++i) {
   if (id[2 * i] == id[2 * i + 1]) return false;
   ans[i] = id[2 * i] > id[2 * i + 1];
               return true:
        vector<bool> answer() { return ans; }
};
int main() {
       main() {
int m, n; cin >> m >> n;
TwoSat ts(n);
for (int i = 0; i < m; ++i) {
    int u, v; char x, y;
    cin >> x >> u >> y >> v;
    ts.addClause(u - 1, x == '+', v - 1, y == '+');
}
        if (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";</pre>
        else cout << "IMPOSSIBLE\n";</pre>
}
```

2.10 Funtional Graph [85c464]

```
| constexpr int N = 2e5 + 5;
| int cht[N][31]; // 倍增表,放外面不然 TLE
| struct FuntionalGraph {
| int n, cnt;
| vector<int> g, bel, id, len, in, top;
| FuntionalGraph() : n(0) {}
| FuntionalGraph(vector<int> g_) { init(g_); }
```

```
id.resize(n); len.clear();
in.assign(n, 0); top.assign(n, -1);
              build();
      in[g[i]]++;
              for (int i = 1; i <= 30; i++)
    for (int u = 0; u < n; u++)
        cht[u][i] = cht[cht[u][i - 1]][i - 1];</pre>
             for (int i = 0; i < n; i++)
   if (in[i] == 0) label(i);
for (int i = 0; i < n; i++)
   if (top[i] == -1) label(i);</pre>
      void label(int u) {
  vector<int> p; int cur = u;
  while (top[cur] == -1) {
                    top[cur] = u:
                    p.push_back(cur);
                    cur = g[cur];
              auto s = std::find(p.begin(), p.end(), cur);
             vector < int> cyc(s, p.end());
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {
    bel[cyc[i]] = cnt;</pre>
                    id[cyc[i]] = i;
              cnt++; len.push_back(cyc.size());
              for (int i = p.size() - 1; i > 0; i--)
   id[p[i - 1]] = id[p[i]] - 1;
      int jump(int u, int k) {
    for (int b = 0; k > 0; b++){
        if (k & 1) u = cht[u][b];
}
              return u:
};
```

3 Data Structure

3.1 BIT [d41d8c]

```
template <typename T>
struct Fenwick { // 全部以 0 based 使用
int n; vector<T> a;
Fenwick(int n_ = 0) { init(n_); }
       void init(int n_) {
            n = n_;
             a.assign(n, T{});
      void add(int x, const T &v) {
   for (int i = x + 1; i <= n; i += i & -i) {
      a[i - 1] = a[i - 1] + v;
   }</pre>
      T sum(int x) { // 左閉右開查詢
              T`ans{};
             for (int i = x; i > 0; i -= i & -i) {
    ans = ans + a[i - 1];
              return ans;
      T rangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
      int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
              int x = 0;
             int x - 0,
T cur{};
for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n && cur + a[x + i - 1] <= k) {
        x += i;
        --- - cur + a[x - 1];
</pre>
                    }
              return x;
      }
template <class T>
struct TwoDFenwick { // 全部以 0 based 使用
      int nx, ny; // row, col 個數
vector<vector<T>> a;
      TwoDFenwick(int nx_ = 0, int ny_ = 0) {
             init(nx_, ny_);
       void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
      void add(int x, int y, const T &v) {
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            a[i - 1][j - 1] = a[i - 1][j - 1] + v;
        }
}</pre>
```

```
}
}

T sum(int x, int y) { // 左閉右開查詢
    T ans{};
    for (int i = x; i > 0; i -= i & -i) {
        for (int j = y; j > 0; j -= j & -j) {
            ans = ans + a[i - 1][j - 1];
        }
    return ans;
}

T rangeSum
    (int lx, int ly, int rx, int ry) { // 左閉右開查詢
    return sum(
        rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
}

}

Decomplishment

T sum (and but and but are an are a
```

3.2 RangeBit [d41d8c]

| template <typename T>

```
struct rangeFenwick { // 全部以 0 based 使用
        int n;
        rector<T> d, di;
rangeFenwick(int n_ = 0) { init(n_); }
void init(int n_) {
                d.assign(n, T{});
di.assign(n, T{});
        Joid add(int x, const T &v) {
   T vi = v * (x + 1);
   for (int i = x + 1; i <= n; i += i & -i) {
      d[i - 1] = d[i - 1] + v;
      di[i - 1] = di[i - 1] + vi;
}</pre>
         void rangeAdd(int l, int r, const T &v) {
  add(l, v); add(r, -v);
         T sum(int x) { // 左閉右開查詢
                return ans:
        TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
         int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
                int x = 0;
                T cur{};
                for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n) {
        T val = T(</pre>
                                           x + i + 1) * d[x + i - 1] - di[x + i - 1];
                                  if (cur + val <= k) {</pre>
                                          x += i:
                                          cur = cur + val:
                        }
                return x;
       }
}:
template <class T>
struct rangeTwoDFenwick { // 全部以 0 based 使用
        int nx, ny; // row, col 個數
vector <vector <T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
                 init(nx_, ny_);
        }
void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
}
        }
void add(int x, int y, const T &v) {
    T vi = v * (x + 1);
    T vj = v * (y + 1);
    T vij = v * (x + 1) * (y + 1);
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            d[i - 1][j - 1] = d[i - 1][j - 1] + v;
            di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
            dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
            dij[i - 1][j - 1] = dij[i - 1][j - 1] + vj;
            reconstructions.</pre>
               }
         void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
                add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
```

Seg(int n_, Info v_ = Info()) { init(n_, v_); }

```
T sum(int x, int y) { // 左閉右開查詢
                                                                                                                                                     template <class T>
                                                                                                                                                     Seg(vector<T> init_) { init(init_); }
void init(int n_, Info v_ = Info()) {
                 T`ans{};
                 for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans
                                                                                                                                                             init(vector(n_, v_));
                                   + T(x * y + x + y + 1) * d[i - 1][j - 1]; \\ ans = ans - T(y + 1) * d[i - 1][j - 1]; \\ ans = ans - T(x + 1) * d[i - 1][j - 1]; \\
                                                                                                                                                     template <class T>
void init(vector<T> init_) {
                                                                                                                                                             n = init_.size();
                                                                                                                                                             ans = ans + dij[i - 1][j
                         }
                 return ans:
                                                                                                                                                                              info[p] = init_[l];
         ,
T rangeSum
                                                                                                                                                                             return;
                  (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                                                                                                                                                                     int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                 return sum(
                          (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
        }
                                                                                                                                                                     pull(p);
};
                                                                                                                                                             build(1, 0, n);
3.3 DSU [d41d8c]
                                                                                                                                                     void pull(int p) {
    info[p] = info[p * 2] + info[p * 2 + 1];
struct DSU {
        int n;
         vector < int > boss, siz;
                                                                                                                                                     void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
      info[p] = v; return;
}
        DSU() {}
DSU(int n_) { init(n_); }
         void init(int n_) {
    n = n_; boss.resize(n);
                 iota(boss.begin(), boss.end(), 0);
                                                                                                                                                             int m = (l + r) / 2;
if (x < m) modify(2 * p, l, m, x, v);
else modify(2 * p + 1, m, r, x, v);</pre>
                 siz.assign(n, 1);
         int find(int x) {
   if (boss[x] == x) return x;
   return boss[x] = find(boss[x]);
                                                                                                                                                             pull(p);
                                                                                                                                                     void modify(int p, const Info &i) {
                                                                                                                                                             modify(1, 0, n, p, i);
        bool same(int x, int y) {
    return find(x) == find(y);
                                                                                                                                                     Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];</pre>
        bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);</pre>
                                                                                                                                                             int m = (l + r) / 2;
                                                                                                                                                             return query(p
                                                                                                                                                                      2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
                 siz[x] += siz[y];
                                                                                                                                                     Info query(int ql, int qr) {
                 boss[y] = x;
                                                                                                                                                             return query(1, 0, n, ql, qr);
                 return true;
                                                                                                                                                     template < class F> // 尋找區間內,第一個符合條件的
        int size(int x) {
   return siz[find(x)];
                                                                                                                                                     int findFirst
                                                                                                                                                             (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)
    return -1;</pre>
        }
};
                                                                                                                                                             if (l >= x && r <= y && !pred(info[p]))</pre>
struct DSU {
                                                                                                                                                                      return -1;
         int n;
                                                                                                                                                             if (r - l == 1)
         vector<int> boss, siz, stk;
                                                                                                                                                                     return l:
                                                                                                                                                             int m = (l + r) / 2;
int res = findFirst(2 * p, l, m, x, y, pred);
if (res == -1)
                    {}
        DSU(int n_) { init(n_); }
         void init(int n_) {
                 n = n_;
                                                                                                                                                                      res = findFirst(2 * p + 1, m, r, x, y, pred);
                 boss.resize(n);
                                                                                                                                                             return res:
                 iota(boss.begin(), boss.end(), 0);
                 siz.assign(n, 1);
                                                                                                                                                    template < class F> // 若要找 last, 先右子樹遞迴即可
int findFirst(int l, int r, F & & pred) {
    return findFirst(1, 0, n, l, r, pred);
                 stk.clear();
        int find(int x) {
                 return x == boss[x] ? x : find(boss[x]);
                                                                                                                                            // ---define structure and info plus---
        bool same(int x, int y) {
                                                                                                                                            struct Info {
                 return find(x) == find(y);
                                                                                                                                                    int n = 0;
        bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);
    siz[x] += siz[y];
    if (siz[x] < siz[y];
    if (siz[x] < siz[y]);
    if (siz[x] < siz[x] < siz[y]);
    if (siz[x] < siz[x] < 
                                                                                                                                                     int sum = 0:
                                                                                                                                            Info operator+(const Info &a, const Info &b) {
                                                                                                                                                     return { a.n + b.n, a.sum + b.sum };
                 boss[y] = x;
                                                                                                                                            3.5 Lazy Segment [d41d8c]
                 stk.push_back(y);
                                                                                                                                            template <class Info, class Tag>
                 return true;
                                                                                                                                            struct LazySeg { // 左閉右開寫法
                                                                                                                                                     int n;
         void undo(int x) {
                                                                                                                                                     vector<Info> info;
                 while (stk.size() > x) {
    int y = stk.back();
                                                                                                                                                     vector < Tag > tag;
LazySeg() : n(0) {}
                         stk.pop_back();
                                                                                                                                                     LazySeg(int n_, Info v_ = Info()) {
                                                                                                                                                             init(n_, v_);
                         siz[boss[y]] -= siz[y];
                         boss[y] = y;
                                                                                                                                                     template <class T>
                 }
                                                                                                                                                     LazySeg(vector<T> init_) {
                                                                                                                                                             init(init_);
         int size(int x) {
                 return siz[find(x)];
                                                                                                                                                     void init(int n_, Info v_ = Info()) {
                                                                                                                                                            init(vector(n_, v_));
};
                                                                                                                                                    femplate <class T>
void init (vector<T> init_) {
    n = init_.size();
    info.assign(4 << __lg(n), Info());
    tag.assign(4 << __lg(n), Tag());
    function <void(
        int, int, int)> build = [&](int p, int l, int r) {
        if (r - l == 1) {
3.4 Segment [d41d8c]
template <class Info>
struct Seg { // 左閉右開寫法
int n; vector<Info> info;
Seg(): n(0) {}
```

```
info[p] = init_[l];
                                                                                                    }
                int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                                                                                               struct Info {
                 pull(p);
           build(1, 0, n);
                                                                                                          sum += (r - l) * v.add;
     void pull
     (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
                                                                                                    //
//
// }
           tag[p].apply(v);
     void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
                                                                                               }
                                                                                               3.6 Treap [d41d8c]
           tag[p] = Tag();
                                                                                               struct Treap {
     void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
}
                                                                                                     Treap *lc, *rc;
                                                                                                    int pri, siz; bool rev_valid;
int val; int min;
                return:
                                                                                                     Treap(int val_) {
    min = val = val_;
           int m = (l + r) / 2;
push(p, l, r);
if (x < m) {</pre>
                                                                                                          pri = rand();
lc = rc = nullptr;
siz = 1; rev_valid = 0;
                 modify(2 * p, l, m, x, v);
           } else {
                modify(2 * p + 1, m, r, x, v);
                                                                                                          siz = 1;
                                                                                                          min = val;
           pull(p);
                                                                                                          for (auto c : {lc, rc}) {
    if (!c) continue;
     void modify(int p, const Info &i) {
                                                                                                                siz += c->siz:
           modify(1, 0, n, p, i);
                                                                                                          }
     Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;</pre>
           push(p, l, r);
           return query(p *
2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
                                                                                                          rev_valid = false;
     Ínfo query
            (int ql, int qr) { return query(1, 0, n, ql, qr); }
     apply(p, l, r, v);
                return:
           int m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
                                                                                               int size(Treap *t) {
    return t ? t->siz : 0;
           pull(p):
     void range_apply(int l, int r, const Tag &v) {
  range_apply(1, 0, n, l, r, v);
                                                                                                    if (a->pri > b->pri) {
    a->rc = merge(a->rc, b);
     }
                                                                                                          a->pull();
     template < class F> // 尋找區間內,第一個符合條件的
                                                                                                          return a:
     int findFirst
           (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
                                                                                                     else {
                                                                                                          b->lc = merge(a, b->lc);
b->pull();
                 return 1:
                                                                                                          return b;
           if (l >= x && r <= y && !pred(info[p])) {</pre>
                                                                                                    }
                 return -1;
           if (r - l == 1) {
                 return l;
                                                                                                     t->push();
           int m = (l + r) / 2;
           push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
           if (res ==
                                                                                                          t->pull();
                 res = findFirst(2 * p + 1, m, r, x, y, pred);
                                                                                                          return {t, b};
           return res;
                                                                                                     else {
     template < class F> // 若要找 last,先右子樹遞迴即可
int findFirst(int l, int r, F & pred) {
    return findFirst(1, 0, n, l, r, pred);
                                                                                                          t->pull();
                                                                                                          return {a, t};
                                                                                                    }
// ---define structure and info plus---
                                                                                               void Print(Treap *t) {
struct Tag { // 有些 Tag 不用 push 例如 sweepLine
  int set_val; int add;
  void apply(const Tag& v) {
                                                                                                    if (!t) return;
                                                                                                     t->push();
                                                                                                    Print(t->lc);
           if (v.set_val) {
                                                                                                     cout << t->val:
                 set_val = v.set_val;
                                                                                                     Print(t->rc);
                 add = v.add:
           else {
```

```
add += v.add:
       void apply(int l, int r, const Tag &v) {
    if (v.set_val) {
        sum = (r - l) * v.set_val;
}
       // Info& operator=(const Info &rhs) {
                  // 部分 assignment 使用
return *this;
Info operator+(const Info &a, const Info &b) {
   return { a.sum + b.sum };
       void pull() { // update siz or other information
                     min = std::min(min, c->min);
       }
void push() {
    if (rev_valid) {
        swap(lc, rc);
        if (lc) lc->rev_valid ^= 1;
        if (rc) rc->rev_valid ^= 1;
       int find(int k) { // 找到 min 是 k 的位置 (1-based)
              push();
int ls = (lc ? lc->siz : 0) + 1;
              if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
Treap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
    a->push(); b->push();
fpair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
       if (size(t->lc) < k) {
    auto [a, b] = split(t->rc, k - size(t->lc) - 1);
    t->rc = a;
              auto [a, b] = split(t->lc, k);
t->lc = b;
```

3.7 Mo [d41d8c]

```
struct query {
   int l, r, id;
} typedef query;
void MO(int n, vector<query> &queries) {
   int block = sqrt(n);
}
     int block_a = a.l / block;
int block_b = b.l / block;
         if (block_a != block_b) return block_a < block_b;</pre>
         return a.r < b.r;</pre>
     sort(queries.begin(), queries.end(), cmp);
void compress(vector<int> &nums) {
    vector < int > sorted = nums;
sort(sorted.begin(), sorted.end());
     sorted.erase
          (unique(sorted.begin(), sorted.end()), sorted.end());
```

4 Flow

4.1 Dinic [aa12d4]

```
template < class T>
struct Dinic {
     struct Edge {
           int to;
           T flow, cap; // 流量跟容量
     int n, m, s, t;
const T INF_FlOW = 1 << 30;
     vector < vector < int >> adj; // 此點對應的 edges 編號
     vector <Edge> edges; // 幫每個 edge 編號
vector <int> dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_) {
           n = n_; m = 0;
dis.resize(n); ptr.resize(n);
adj.assign(n, vector<int>{});
           edges.clear();
     void add_edge(int u, int v, T cap) {
           // 偶數 id 是正向邊
           edges.push_back({ v, 0, cap });
edges.push_back({ u, 0, 0 });
adj[u].push_back(m++);
adj[v].push_back(m++);
     bool bfs() {
           fill(dis.begin(), dis.end(), -1);
           dis[s] = 0; queue < int > q;
q.push(s);
           while (!q.empty() && dis[t] == -1) {
                 int u = q.front(); q.pop();
for (int id : adj[u]) {
    Edge &e = edges[id];
                       if (e.flow == e.cap) continue;
if (dis[e.to] == -1) {
    dis[e.to] = dis[u] + 1;
                            q.push(e.to);
                      }
                }
           return dis[t] != -1;
     T dfs(int u, T flow) {
           if (flow == 0) return 0;
if (u == t) return flow;
           for (int
                   &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {
                 Edge &e = edges[adj[u][cur]];
if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;
                 if (e.cap == e.flow) continue;
T mn = dfs(e.to, min(flow, e.cap - e.flow));
                 if (mn > 0) {
    e.flow += mn;
                       edges[adj[u][cur] ^ 1].flow -= mn;
                       return mn:
                }
           return 0; // 到不了終點就會 return 0
     while (true) {
   T res = dfs(s, INF_Flow);
                       if (res == 0) break;
                       flow += res;
                }
           return flow;
     void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
```

4.2 Min Cut [44ae6c]

```
// CSES Police Chase
int main(){
            int n, m; cin >> n >> m;
Dinic < int > g(n);
for (int i = 0; i < m; i++) {</pre>
                    int u, v, cap = 1;
cin >> u >> v;
                    u--; v--;
                    g.add_edge(u, v, cap);
                    g.add_edge(v, u, cap);
            int res = g.work(0, n - 1);
cout << res << "\n";
if (res == 0) return;</pre>
            vector<int> vis(n);
auto find = [&](auto self, int u) -> void {
   if (!vis[u]) {
                              vis[u] =
                             for (int id : g.adj[u]) {
   auto e = g.edges[id];
   if (e.cap - e.flow > 0) {
                                               self(self, e.to);
                                      }
                            }
                    }
           };
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
    }
        arde = -a edges[id];</pre>
                             auto e = g.edges[id];
if (!vis[e.to]) {
    cout << i + 1 << " " << e.to + 1 << " \n";</pre>
                    }
           }
  }
```

4.3 MCMF [77fc99]

```
template < class Tf, class Tc>
struct MCMF {
        struct Edge {
                 int to;
                 Tf flow, cap; // 流量跟容量
                 Tc cost:
        // 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就好
int n, m, s, t;
const Tf INF_FLOW = 1 << 30;
const Tc INF_COST = 1 << 30;
vector<vector<int>>> adj;
        vector<Edge> edges; // 幫每個 edge 編號
vector<Tc> dis, pot; // johnson algorithm, using spfa
vector<int> rt; // 路徑恢復, 對應 id
        vector<int> rt; // 所程恢復/更
vector<bool> inq;
MCMF(int n_ = 0) { init(n_); }
void init(int n_) {
n = n_; m = 0;
edges.clear();
                 adj.assign(n, vector<int>{});
         void add_edge(int u, int v, Tf cap, Tc cost){
  edges.push_back({v, 0, cap, cost});
  edges.push_back({u, 0, 0, -cost});
  adj[u].push_back(m++);
                  adj[v].push_back(m++)
        bool spfa() {
    dis.assign(n, INF_COST);
    rt.assign(n, -1); inq.assign(n, false);
                 queue<int> q;
q.push(s), dis[s] = 0, inq[s] = true;
                  while ('q.empty()) {
   int u = q.front(); q.pop();
   inq[u] = false;
                         Inq[u] = false;
for (int id : adj[u]) {
    auto [v, flow, cap, cost] = edges[id];
    Tc ndis = dis[u] + cost + pot[u] - pot[v];
    if (flow < cap && dis[v] > ndis) {
        dis[v] = ndis; rt[v] = id;
        if (!inq[v]) {
            q.push(v); inq[v] = true;
        }
}
                                  }
                         }
                 return dis[t] != INF_COST;
         bool dijkstra() {
                 dis.assign(n, INF_COST); rt.assign(n, -1);
priority_queue<pair<Tc, int>,
    vector<pair<Tc, int>>, greater<pair<Tc, int>>> pq;
                 dis[s] = 0; pq.emplace(dis[s], s);
```

```
pq.emplace(ndis, v);
                       }
                 }
            return dis[t] != INF_COST;
     }
     .// 限定 flow,最小化 cost
pair<Tf, Tc> work_flow(int s_, int t_, Tf need) {
           dis[i] += pot[i] - pot[s];
                  Tf f = INF_FLOW;
                 for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                             (f, edges[rt[i]].cap - edges[rt[i]].flow);
                 f = min<Tf>(f, need);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
                 flow += f; need -= f;
cost += f * dis[t]; fr = false;
swap(dis, pot);
if (need == 0) break;
            return make_pair(flow, cost);
     .// 限定 cost,最大化 flow
pair<Tf, Tc> work_budget(int s_, int t_, Tc budget) {
           s = s_, t = t_; pot.assign(n, 0);
Tf flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] += pot[i] - pot[s];
}</pre>
                  Tf f = INF_FLOW;
                 for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                             (f, edges[rt[i]].cap - edges[rt[i]].flow);
                 for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
   edges[rt[i]].flow += f;
   edges[rt[i] ^ 1].flow -= f;
}
                 flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
swap(dis, pot);
if (budget == 0 || f == 0) break;
            return make_pair(flow, cost);
      void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
     }
};
```

4.4 Hangarian [dfa1c4]

```
struct Hangarian { // 0-based
       int n, m;
       vector<vector<int>> adj;
       vector <int> used, vis;
vector <pair <int, int>> match;
Hangarian(int n_ = 0, int m_ = 0) {
   init(n_, m_);
       f void init(int n_, int m_) {
    n = n_; m = m_;
    adj.assign(n + m, vector<int>());
    used.assign(n + m, -1);
}
               vis.assign(n + m, 0);
       void addEdge(int u, int v) {
   adj[u].push_back(n + v);
               adj[n + v].push_back(u);
       bool dfs(int u)
               int sz = adj[u].size();
for (int i = 0; i < sz; i++) {
   int v = adj[u][i];</pre>
                      if (vis[v] == 0) {
  vis[v] == 1;
  if (used[v] == -1 || dfs(used[v])) {
     used[v] = u;
                                      return true;
                              }
                      }
               }
```

```
8
           return false:
      fvector<pair<int, int>> work() {
    match.clear(); used.assign(n + m, -1);
    vis.assign(n + m, 0);
    for (int i = 0; i < n; i++) {
        fill(vis.begin(), vis.end(), 0); dfs(i);
}</pre>
           for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
                    match.push_back(make_pair(used[i], i - n));
           return match:
     }
};
 4.5
       Theorem [d41d8c]
| // 有向無環圖:
// 最小不相交路徑覆蓋:
 // 最小路徑數 = 頂點數 - 最大匹配數
| // 最小相交路徑覆蓋:
// 先用
       Floyd 求傳遞封包,有連邊就建邊,然後再套最小不相交路徑覆蓋
// 二分圖:
// 最小點覆蓋 = 最大匹配數
 // 選出一些點,讓所有邊至少有一個端點在點集中的最少數量
 // 最少邊覆蓋: 選出一些邊,讓所有點都覆蓋到的最少數量
 // 最少邊覆蓋 = 點數 - 最大匹配數
1// 最大獨立集: 選出一些點, 使這些點兩兩沒有邊連接的最大數量
// 最大獨立集 = 點數 - 最大匹配數
 5
       String
 5.1 Hash [852711]
 constexpr int B = 59;
vector<Z> Hash(string &s) {
      vector < Z > ans {0};
for (auto c : s) {
           ans.push_back(ans.back() * B + (c - 'a' + 1));
      return ans;
 void solve() {
      string s, sub;
cin >> s >> sub;
      auto a = Hash(s);
auto q = Hash(sub);
auto find = q.back();
      int ans = 0;
int l = 1, r = sub.size(), len = sub.size();
while (r <= s.size()) {
    if (a[r] - a[l - 1] * power(Z(B), len) == find) {</pre>
               ans++;
      cout << ans << "\n":
 5.2 KMP [cddfd9]
 struct KMP {
      string sub;
vector<int> failure;
      KMP(string sub_) {
           sub = sub_;
failure.resize(sub.size(), -1);
           buildFailFunction();
      void buildFailFunction() {
   for (int i = 1; i < (int)sub.size(); i++) {
     int now = failure[i - 1];</pre>
                while (now != -1
                      && sub[now + 1] != sub[i]) now = failure[now];
```

if (sub[now + 1] == sub[i]) failure[i] = now + 1;

sub[now + 1] && now != -1) now = failure[now];
// failure stores if comparison fail, move to where

vector <int> match;
for (int i = 0, now = -1; i < (int)s.size(); i++) {
 // now is the compare sucessed length -1</pre>

if (s[i] == sub[now + 1]) now++;
if (now + 1 == (int)sub.size()) {
 match.push_back(i - now);

now = failure[now];

}

}

}

1:

return match;

vector<<mark>int</mark>> match(string &s) {

while (s[i] !=

lc.resize(n - 1);

rk.resize(n);

```
5.3 Z Function [764b31]
// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
// 的最長公共前綴 (LCP) 的長度
vector < int > Z(string s) {
     int n = s.size():
     tht n = S.stze();
vector <int> z(n); z[0] = n;
for (int i = 1, j = 1; i < n; i++) {
    z[i] = max(0, min(j + z[j] - i, z[i - j]));
    while (i + z[i] < n && s[z[i]] == s[i + z[i]])</pre>
               z[i]++;
          if (i + z[i] > j + z[j]) j = i;
     return z; // 最後一格不算
}
5.4 SA [d40e3e]
struct SuffixArray {
     int n; string s;
vector<int> sa, rk, lc;
     // n: 字串長度
     // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
     // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
     // lc: LCP
           數組,lc[i] 表示 sa[i] 和 sa[i+1] 的最長公共前綴長度
     SuffixArray(const string &s_) {
   s = s_; n = s.length();
   sa.resize(n);
```

```
iota(sa.begin(), sa.end(), 0);
     tota(sa.begin(), sa.end(), 0);
sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });
rk[sa[0]] = 0;
for (int i = 1; i < n; ++i)</pre>
            rk[sa[i]]
                     = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
      int k = 1;
      vector<int> tmp, cnt(n);
      tmp.reserve(n);
while (rk[sa[n - 1]] < n - 1) {</pre>
            tmp.clear();
for (int i = 0; i < k; ++i)
            tmp.push_back(n - k + i);
for (auto i : sa)
    if (i >= k)
                        tmp.push_back(i - k);
           tmp.push_back(i - k);
fill(cnt.begin(), cnt.end(), 0);
for (int i = 0; i < n; ++i)
    ++cnt[rk[i]];
for (int i = 1; i < n; ++i)
    cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; --i)
           sa[--cnt[rk[tmp[i]]]] = tmp[i];
      for (int i = 0, j = 0; i < n; ++i) {</pre>
            if (rk[i] == 0) {
           j = 0;
} else {
                  for (j
                           -= j > 0; i + j < n && sa[rk[i] - 1] + j
                          < n && s[i + j] == s[sa[rk[i] - 1] + j]; )
                  lc[rk[i] - 1] = j;
     }
string getLCP() {
   int cp = 0, k, lcp = 0, p;
   for (int i = 0; i < n; i++) {
      if (!rk[i]) continue;
}</pre>
            if (cp) cp--;
while (s[i + cp] == s[k + cp]) cp++;
            if (cp`> lcp){
                  lcp = cp;
                 p = i;
      if (lcp) {
    return s.substr(p, lcp);
```

5.5 Manacher [9c9ca6]

} else {

};

```
// 找到對於每個位置的迴文半徑
vector < int > manacher(string s) {
    string t = "#";
    for (auto c : s) {
```

return "-1";

```
int n = t.size():
vector<int> r(n);
for (int i = 0, j :
      0; i < n; i++) { // i 是中心, j 是最長回文字串中心 if (2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
      while (i - r[i] >=
    0 && i + r[i] < n && t[i - r[i]] == t[i + r[i]]) {
    r[i] += 1;</pre>
      if (i + r[i] > j + r[j]) {
      }
}
return r;
// # a # b # a #
// 1 2 1 4 1 2 1
// # a # b # b # a #
// 1 2 1 2 5 2 1 2 1
// 值 -1 代表原回文字串長度
// (id - val + 1) / 2 可得原字串回文開頭
```

5.6 SAM [d15619]

```
struct SAM {
     static constexpr int ALPHABET_SIZE = 26;
struct Node {
           int link;
           array<int, ALPHABET_SIZE> next;
           Node(): len{}, link{}, next{} {}
     vector < Node > t:
     vector<wode> t;
SAM() { init(); }
void init() {
    t.assign(2, Node());
    t[0].next.fill(1);
           t[0].len = -1;
     int newNode() {
    t.emplace_back();
           return t.size() - 1;
     int extend(int p, int c) {
    if (t[p].next[c]) {
                 int q = t[p].next[c];
if (t[q].len == t[p].len + 1) {
                 int r = newNode():
                 t[r].len = t[p].len + 1;
t[r].link = t[q].link;
t[r].next = t[q].next;
                 t[q].link = r;
                 while (t[p].next[c] == q) {
                      t[p].next[c] = r;
p = t[p].link;
                 return r;
           int cur = newNode();
           t[cur].len = t[p].len + 1;
while (!t[p].next[c]) {
                 t[p].next[c] = cur;
                 p = t[p].link;
           t[cur].link = extend(p, c);
    }
void solve() {
     string s; cin >> s;
int n = s.length();
     vector < int > pos(n + 1); // s[i - 1] 的後綴終點位置
     pos[0] = 1;
     for (int i = 0; i < n; i++) {
   pos[i + 1] = sam.extend(pos[i], s[i] - 'a');</pre>
```

5.7 Trie [3b3aa0]

```
struct Trie {
      struct trie_node {
            trie_node {
bool is_word;
vector<trie_node *> children;
trie_node() {
   is_word = false;
}
                  children.resize(26, NULL);
      trie_node *root = new trie_node();
      void insert(string &s) {
    trie_node *cur = root;
            for (int i = 0; i < s.size(); i++) {</pre>
```

```
int idx = s[i] -
                 if (cur->children[idx] == NULL) {
                       cur->children[idx] = new trie_node();
                 cur = cur->children[idx]:
           cur->is_word = true;
     bool is_in_trie(string &s) {
           trie_node *cur = root;
for (int i = 0; i < s.size(); i++) {</pre>
                 if (cur->
                 children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
           return true;
     int search_i_start(string &s, int i, vector<int> &dp) {
           int sz = s.size(), ans = 0;
for (int j = i; j < sz; j++) {
    if (cur</pre>
                 ->children[s[j] - 'a'] == nullptr) return ans;
cur = cur->children[s[j] - 'a'];
                 if (cur->is_word)
                      (ans += dp[j + 1]) %= mod;
           return ans;
     }
};
int main() {
     // 找到 sub 集合裡,可以重複用,組成 s 的組數
Trie trie;
      string s; cin >> s;
     int sz = s.size();
     // dp 代表 i 開頭到最後的配對總數
     // 找到有結尾為 stop 的 dp[i] += dp[j + 1]
int n; cin >> n;
vector <int> dp(sz + 1, 0);
for (int i = 0; i < n; i++) {
    string sub; cin >> sub;
    tring sub; cin >> sub;
           trie.insert(sub);
     dp[sz] = 1;
for (int i = sz - 1; i >= 0; i--) {
    dp[i] = trie.search_i_start(s, i, dp);
     cout << dp[0] << endl;</pre>
5.8 Duval [f9dcca]
// duval_algorithm
// 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
vector<string> duval(string s) {
    int i = 0, n = s.size();
     vector<string> res;
     while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
      else k++;
}</pre>
           while (i <= k) {
    res.push_back(s.substr(i, j - k));</pre>
                 i += j - k;
           }
     return res;
// 最小旋轉字串
string min_round(string s) {
     int i = 0, n = s.size();
int start = i;
      while (i < n / 2) {
           start = i;
int k = i, j = i + 1;
while (s[k] <= s[j] && j < n) {
    if (s[k] < s[j]) k = i;
}</pre>
                 else k++;
                 j++;
           while (i <= k) {
    i += j - k;</pre>
     return s.substr(start, n / 2);
    Math
6
6.1 Prime [4e0864]
   a^{(m-1)} = 1 \pmod{m}
```

```
// a^(m-1) = 1 (MOU M)
// a^(m-2) = 1/a (mod m)
// EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)
// Filter + DP; DP save min factor 'recur' factor decomposition
// FacNums = (x+1)(y+1)(z+1)...
// FacSum = (a^0+a^1...+a^x)(b^0+...+b^y)
```

```
// FacMul = N(x+1)(v+1)(z+1)/2
vector<int> is_prime;
// 1 代表是質數,非 1 不是
void init(int n) {
     }
int main() {
     init(1000000);
     ll ans = 1, q; cin >> q;
map<ll, ll> mp;
while (is_prime[q] != 1) {
          mp[is_prime[q]]++;
q /= is_prime[q];
     if (q != 1) mp[q]++;
for (auto [a, b] : mp) ans *= b + 1;
cout << ans << "\n";</pre>
6.2 Modulo [a1aab8]
template < class T>
constexpr T power(T a, ll b) {
   T res {1};
     for (; b; b /= 2, a *= a)
if (b % 2) res *= a;
     return res;
constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
     res %= p;
if (res < 0) res += p;
     return res;
template < ll P >
struct MInt {
    ll x;
     constexpr MInt() : x {0} {}
constexpr MInt(ll x) : x {norm(x % getMod())} {}
static ll Mod;
     constexpr static ll getMod() {
   if (P > 0) return P;
          else return Mod:
     constexpr static void setMod(ll Mod_) {
    Mod = Mod_;
     constexpr ll norm(ll x) const {
          if (x < 0) x += getMod();
if (x >= getMod()) x -= getMod();
     constexpr ll val() const { return x; }
constexpr MInt operator-() const {
          MInt res;
           res.x = norm(getMod() - x);
           return res;
     constexpr MInt inv() const {
   return power(*this, getMod() - 2);
     constexpr MInt &operator*=(MInt rhs) & {
   if (getMod() < (1ULL << 31)) {</pre>
                x = x *
                          rhs.x % int(getMod());
          } else {
               x = mul(x, rhs.x, getMod());
           return *this;
     constexpr MInt &operator+=(MInt rhs) & {
          x = norm(x + rhs.x);
return *this;
     constexpr MInt &operator -=(MInt rhs) & {
          x = norm(x - rhs.x);
return *this;
     constexpr MInt &operator/=(MInt rhs) & {
          return *this *= rhs.inv();
     friend constexpr MInt operator*(MInt lhs, MInt rhs) {
   MInt res = lhs; return res *= rhs;
      friend constexpr MInt operator+(MInt lhs, MInt rhs) {
          MInt res = lhs; return res += rhs;
      friend constexpr MInt operator-(MInt lhs, MInt rhs) {
          MInt res = lhs; return res -= rhs;
     friend constexpr MInt operator/(MInt lhs, MInt rhs) {
   MInt res = lhs; return res /= rhs;
      friend constexor
```

std::istream &operator>>(std::istream &is, MInt &a) {

ll v; is >> v; a = MInt(v); return is;

```
friend constexpr std::
    ostream &operator<<(std::ostream &os, const MInt &a) {
    return os << a.val();
}
friend constexpr bool operator==(MInt lhs, MInt rhs) {
    return lhs.val() == rhs.val();
}
friend constexpr bool operator!=(MInt lhs, MInt rhs) {
    return lhs.val() != rhs.val();
}
friend constexpr bool operator<(MInt lhs, MInt rhs) {
    return lhs.val() < rhs.val();
}
friend constexpr bool operator<(MInt lhs, MInt rhs) {
    return lhs.val() < rhs.val();
}
}
template<>
ll MInt<0>::Mod = 998244353;
constexpr int P = 1e9 + 7;
using Z = MInt<P>;
```

6.3 Combination [878efe]

6.4 CRT [d41d8c]

```
Ill exgcd(ll a, ll b, ll &x, ll &y) {
    if (!b) {
        x = 1, y = 0;
        return a;
    }
    ll g = exgcd(b, a % b, y, x);
    y -= a / b * x;
    return g;
}

Il inv(ll x, ll m){
    ll a, b;
    exgcd(x, m, a, b);
    a %= m;
    if (a < 0) a += m;
    return a;
}

// remain, mod

Il CRT(vector < pair < ll, ll >> &a) {
        ll prod = 1;
        for (auto x : a) {
            prod *= x.second;
        }
        ll res = 0;
        for (auto x : a) {
            auto t = prod / x.second;
            res += x.first * t % prod * inv(t, x.second) % prod;
            if(res >= prod) res -= prod;
        }
        return res;
}
```

6.5 Matrix [08b5fe]

```
template < class T>
struct Mat {
    int m, n;
```

```
constexpr static ll mod = 1e9 + 7;
      constexpr stattc it mod = le9 + 7;
vector<vector<T>> matrix;
Mat(int n_ = 0) { init(n_, n_); }
Mat(int m_, int n_) { init(m_, n_); }
Mat(vector<vector<T>> matrix_) { init(matrix_); }
      void init(int m_, int n_) {
           m = m_; n = n_;
matrix.assign(m, vector<T>(n));
      void init(vector<vector<T>> &matrix_) {
           m = matrix_.size();
n = matrix_[0].size();
           matrix = matrix_;
      return res;
      constexpr Mat & operator*=(const Mat& rhs) & {
  assert(matrix[0].size() == rhs.matrix.size());
            int m = matrix.size()
                   , k = matrix[0].size(), n = rhs.matrix[0].size();
           l] * rhs.matrix[l][j] % mod)) %= mod;
                }
           matrix = ans.matrix:
           return *this;
      constexpr Mat &operator^=(ll p) & {
   assert(m == n); assert(p >= 0);
   Mat ans(p-- == 0 ? unit(m) : matrix);
            while (p > 0) {
   if (p & 1) ans *= *this;
   *this *= *this;
           matrix = ans.matrix;
return *this;
      friend Mat operator*(Mat lhs, const Mat &rhs) {
            return lhs;
      friend Mat operator^(Mat lhs, const ll p) {
           lhs ^= p;
return lhs;
// fn = fn-3 + fn-2 + fn-1
// 初始矩陣 轉移式
// f4 f3 f2 1 1 0
// f3 f2 f1 1 0 1 :
// f2 f1 f0 1 0 0
                   1 1 0  f5 f4 f3
1 0 1 => f4 f3 f2
1 0 0  f3 f2 f1
```

6.6 Integer Partition [595ed2]

6.7 Mobius Theorem

- 數論 分塊 可以快速 計算 一些 含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理 出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d) g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n}\!\mu(d)\!=\!\begin{cases} 1 & \text{for } n\!=\!1\\ 0 & \text{for } n\!\neq\!0 \end{cases}$$

2. μ 是常數函數 1 的反元素 $\Rightarrow \mu*1=\epsilon$, $\epsilon(n)$ 只在n=1 時為 1 , 其餘情況皆為 0 。

- φ歐拉函數: x以下與 x 互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^i) \\ &= 1 + p^0(p-1) + p^1(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^c \\ &= id \end{split}$$

• 莫比烏斯反演公式

-
$$f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$$

- $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

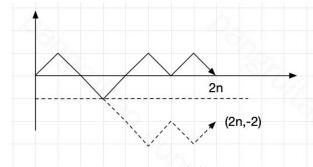
例子

$$\begin{split} &\sum_{i=aj=c}^{b} \sum_{j=1}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{\infty} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.8 Mobius Inverse [d41d8c]

const int maxn = 2e5;

6.9 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有x 個,往下有y 個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.10 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- X/G:本質不同的方案的集合
- X^g : 對於某一種操作 g,所有方案中,經過 g 這種翻轉後保持不變的方案的集合
- 集合取絕對值代表集合數

7 Search and Gready

7.1 Binary Search [d41d8c]

```
int main() {
    int l = 1, r = 10;
    // 1 to tar, find tar
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}</pre>
```

7.2 Ternary Search [d41d8c]

8 Tree

8.1 LCA [601e2d]

```
vector < vector < int >> par(maxn, vector < int > (18));
vector < int > depth(maxn + 1);
vector < int > dfn(maxn);
void build(int n, vector < vector < pair < int, int >>> & tree) {
    auto dfs = [&](auto self, int u, int pre) -> void {
        for (auto [v, w] : tree[u]) {
            if (v == pre) continue;
            par[v][0] = u; // 2 ^ 0
            depth[v] = depth[u] + 1;
            self(self, v, u);
        }
    };
    dfs(dfs, 1, 0);
    for (int i = 1; i <= 18; i++) {
        for (int j = 1; j <= n; j++) {
            par[j][i] = par[par[j][i - 1]][i - 1];
    }
}</pre>
```

```
}
}
int lca(int a, int b) {
    if (depth[a] < depth[b]) swap(a, b);
    int pull = depth[a] - depth[b];
    for (int i = 0; i < 18; i++) {
        if (pull & (1 << i)) {
            a = par[a][i];
        }
}
if (a == b) return a;
for (int i = 17; i >= 0; i--) {
        if (par[a][i] != par[b][i]) {
            a = par[a][i], b = par[b][i];
        }
}
return par[a][0];
}
```

8.2 Centroid Decomposition [4a66fb]

```
struct CenDecom {
       int n;
        vector<vector<int>> adj;
       vector < bool > vis;
vector < int > siz;
       CenDecom() {}
CenDecom(int n_) { init(n_); }
        void init(int n_) {
              adj.assign(n, {});
vis.assign(n, false);
siz.assign(n, 1);
       void addEdge(int u, int v) {
  adj[u].push_back(v);
  adj[v].push_back(u);
       void get_siz(int dep, int x, int p = -1) {
    siz[x] = 1;
              for (int y : adj[x]) {
   if (y == p || vis[y]) continue;
   get_siz(dep + 1, y, x);
                     siz[x] += siz[y];
              }
       fint get_cen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz) {
                            return get_cen(y, sz, x);
                     }
               return x;
       void work(int x = 0) {
              get_siz(0, x);
int cen = get_cen(x, siz[x]);
vis[cen] = true;
               // do something
               for (int y : adj[cen]) {
    if (vis[y]) continue;
                     work(y);
      }
};
```

8.3 Tree Flattening [5293b7]

```
bit.modify(mp[i].second + 1, -val[i]);
}

for (int i = 0; i < q; i++) {
    int op; cin >> op;
    if (op == 1) {
        int s, x; cin >> s >> x;
        int add = x - dfnToVal[mp[s].first];
        dfnToVal[mp[s].first] = x;
        bit.modify(mp[s].first, add);
        if (mp[s].first < n) { // root 就不用扣了
            bit.modify(mp[s].second + 1, -add);
        }
    else {
        int node; cin >> node;
        cout << bit.query(mp[node].first) << "\n";
    }
}
```

```
8.4 Heavy Light Decomposition [ad25b6]
struct HLD {
      int n, cur;
vector<int> siz, top, dep, parent, in, out, seq;
      vector<int> siz, top, dep, parent, in, out, seq;
vector<vector<int>> adj;
HLD(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
    n = n_; cur = 0;
    siz.resize(n); top.resize(n); dep.resize(n);
    parent.resize(n); in.resize(n); out.resize(n);
             seq.resize(n); adj.assign(n, {});
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void work(int root = 0) {
             top[root] = root;
dep[root] = 0;
parent[root] = -1
             parent[root]
             dfs1(root); dfs2(root);
       void dfs1(int u) {
    if (parent[u] != -1)
                    adj[u].erase(find (adj[u].begin(), adj[u].end(), parent[u]));
             for (auto &v : adj[u]) {
                    parent[v] = u, dep[v] = dep[u] + 1;
                    dfs1(v);
siz[u] += siz[v];
                    if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
                   } // 讓 adj[u][0] 是重子節點
       void dfs2(int u) {
             in[u] = cur++;
             seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
   top[v] = v == adj[u][0] ? top[u] : v;
                    dfs2(v);
             out[u] = cur;
      u = parent[top[u]];
} else {
                          v = parent[top[v]];
                   }
             return dep[u] < dep[v] ? u : v;</pre>
       int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
      int jump(int u, int k) {
    if (dep[u] < k) return -1;
    int d = dep[u] - k;
    while (dep[top[u]] > d)
        u = parent[top[u]];
    return seq[in[u] - dep[u] + d];
}
       bool isAncester(int u, int v) {
    // 判斷 u 是否是 v 的祖先
    return in[u] <= in[v] && in[v] < out[u];
       int rootedParent(int u, int v) {
             // 根據新根節點 u 計算 v 的父節點
             swap(u, v);
if (u == v) return u;
if (!isAncester(u, v)) return parent[u];
             auto it = upper_bound(adj
   [u].begin(), adj[u].end(), v, [&](int x, int y) {
   return in[x] < in[y];</pre>
```

}) - 1;
return *it;

```
int rootedSize(int u, int v) {
                // 根據新根節點 u 計算子樹 v 的大小
if (u == v) return n;
if (!isAncester(v, u)) return siz[v];
return n - siz[rootedParent(u, v)];
        int rootedLca(int a, int b, int c) {
   // 根據新的根節點計算三個節點 a \ b 和 c 的最近公共祖先
   return lca(a, b) ^ lca(b, c) ^ lca(c, a);
};
```

8.5 Link Cut Tree [29ae0d]

```
#include <bits/stdc++.h>
using namespace std;
using ll = long long;
constexpr int Mod = 51061;
struct Tag {
     ll add = 0;
     ll mul = 1:
     void apply(const Tag& v) {
    mul = mul * v.mul % Mod;
    add = (add * v.mul % Mod + v.add) % Mod;
    }
struct Info {
     ll val = 1;
ll sum = 1;
     void apply(int size, const Tag &v) {
   val = (val * v.mul % Mod + v.add) % Mod;
   sum = (sum * v.mul % Mod + v.add * size % Mod) % Mod;
     }
};
struct Node {
     Node *ch[2], *p;
int rev = 0;
int size = 1;
     void make_rev() {
    swap(ch[0], ch[1]);
    rev ^= 1;
     Node() : ch {nullptr, nullptr}, p(nullptr) {}
     Info info = Info();
Tag tag = Tag();
     void apply(const Tag &v) {
          info.apply(size, v);
          tag.apply(v);
     void push_tag() {
          if (rev) {
               if (ch[0]) ch[0]->make_rev();
if (ch[1]) ch[1]->make_rev();
               rev = 0;
          if (ch[0]) {
               ch[0]->apply(tag);
          if (ch[1]) {
               ch[1]->apply(tag);
          tag = Tag();
     void pull_info() {
          };
bool isroot(Node *t) {
     return t->p
            == nullptr || (t->p->ch[0] != t && t->p->ch[1] != t);
int pos(Node *t) { // 回傳 1 代表是右子節點 return t->p->ch[1] == t;
void rotate(Node *t) {
     Node *q = t->p;
int x = !pos(t);
     q->ch[!x] = t->ch[x];
if (t->ch[x]) {
          t->ch[x]->p = q;
     t - p = a - p:
     if (!isroot(q)) {
          q \rightarrow p \rightarrow ch[pos(q)] = t;
     t - ch[x] = q;
     q - p - t,
q->pull_info();
void splay(Node *t) { // 單點修改前必須呼叫
    // 把 t 旋轉到目前 splay 的根
```

```
while (!isroot(t)) {
          Node *p = t->p;
p->push_tag();
          t->push_tag();
rotate(t);
     t->push_tag();
t->pull_info();
void access(Node *t) {
     // 把從根到 t 的所有點都放在一條實鏈裡,使根
     // 到 t 成為一條實路徑,並且在同一棵 splay 裡
     for (Node *i = t, *q = nullptr; i; q = i, i = i->p) {
          splay(i);
i->ch[1] = q;
     splay(t);
}
void makeRoot(Node *t) { // 使 t 點成為其所在樹的根
     access(t):
     swap(t->ch[0], t->ch[1]);
     t->rev ^= 1;
Node* findRoot(Node *t) { // 找到 t 的 root
     access(t);
     splay(t);
     t->push_tag();
while (t->ch[0]) {
    t = t->ch[0];
          t->push_tag();
     splay(t);
     return t;
void link(Node *t, Node *p) {
     makeRoot(t);
     if (findRoot(p) != t) {
          makeRoot(p);
          t->p = p;
p->pull_info();
     }
}
bool cut(Node *x, Node *y) { // 不存在邊,回傳 false
     makeRoot(x);
     access(y);
     if( (y->ch[0] != x || x->ch[1]) return false;
y->ch[0] ->p = nullptr;
y->ch[0] = nullptr;
     y->pull_info();
     return true:
void split(Node
       *x, Node *y) { // 以 y 做根, 區間修改用, apply 在 y 上
     makeRoot(x):
     access(y);
     splay(y);
}
bool isconnected(Node *x, Node *y) { // 查詢有沒有連通
     access(y);
return findRoot(x) == findRoot(y);
}
int main() {
   int n; cin >> n;
   vector <Node *> nodes(n);
     for (int i = 0; i < n; i++) {
    nodes[i] = new Node();
    nodes[i]->info.val = nodes[i]->info.sum = 1LL;
     for (int i = 0; i < n - 1; i++) {
   int u, v; cin >> u >> v;
   u--; v--;
          link(nodés[u], nodes[v]);
     for (int i = 0; i < q; i++) {</pre>
          char op; cin >> op; if (op == '+') {
               int u, v; cin >> u >> v;
               split(nodes[u], nodes[v]);
               Tag tag;
cin >> tag.add;
               tag.add % Mod;
               nodes[v]->apply(tag);
          else if (op == '-') {
               int u1, v1; cin >> u1 >> v1;
int u2, v2; cin >> u2 >> v2;
u1--; v1--; u2--; v2--;
               cut(nodes[u1], nodes[v1]);
link(nodes[u2], nodes[v2]);
          else if (op == '*') {
               int u, v; cin >> u >> v;
               u - -; v - -
               split(nodes[u], nodes[v]);
               Tag tag;
cin >> tag.mul;
```

mn.resize(n); res.resize(n);

int query(int v, int x) {

void add_edge(int u, int v) { adj[u].push_back(v); }

```
tag.mul % Mod:
                     nodes[v]->apply(tag);
               else {
                      int u, v; cin >> u >> v;
                                                                                                                                 rt[v] = p;
                                                                                                                                 return x ? p : mn[v];
                     split(nodes[u], nodes[v]);
cout << nodes[v]->info.sum << "\n";</pre>
       }
        return 0:
}
 8.6 Virtual Tree [622e69]
                                                                                                                          void build(int s) {
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
 // 可以建立虚樹達成快速樹 DP
 // 例如這題是有權樹,跟 vertex 1 隔開的最小成本
 int top = -1; vector<int>stk(maxn);
int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
        vt[stk[top - 1]].push_back(stk[top]), top--;
    if (stk[top - 1] != l) {
        vt[l] such back(stk[top]);
        vt[l] such back(stk[top]);
    }
}</pre>
              vt[l].push_back(stk[top]);
stk[top] = l;
           else vt[l].push_back(stk[top--]);
        stk[++top] = u;
 void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
    vt[u].clear();
                                                                                                                         }
                                                                                                                   9
                                                                                                                            DP
 void solve(int n, int q) {
        vector g(n + 1, vector<pair<int, int>>());
        vector vt(n + 1, vector <patr <pre>tht > ()); // dfs 完清除, 否則會退化
vector <ll> dp(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;
   g[u].push_back({v, w});
   g[v].push_back({u, w});
}
                                                                                                                  9.1 LCS [5781cf]
                                                                                                                   int main() {
                                                                                                                          int m, n; cin >> m >> n;
                                                                                                                          int L = 0:
        build_lca(n, g);
       build(n, g);
build(n, g);
for (int i = 0; i < q; i++) {
   int m; top = -1; cin >> m;
   vector<int> key(m);
   for (int j = 0; j < m; j++) {
      cin >> key[j];
      i - tour[baufil] = 1;
                     iskey[key[j]] = 1;
               key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
                     return dfn[a] < dfn[b];
               });
for (int x : key) insert(x, vt);
               auto dfs = [&](auto self, int u) -> void {
                                                                                                                                        else n--;
                     for (auto v : vt[u]) {
    self(self, v);
                                                                                                                                }
                                                                                                                          cout << s << "\n";
                             if (iskey[v]) {
                                   dp[u] += min_dis[v];
                                   // 砍掉 1 到 v 之間最短的路
                                                                                                                   9.2 LIS [66d09f]
                                   dp[u] += min(dp[v], min_dis[v]);
                                                                                                                   int main() {
                             iskey[v] = dp[v] = 0;
                                                                                                                          int dp[n]; vector<int> stk;
                      vt[u].clear();
               dfs(dfs, key[0]); // key[0] 一定是 root cout << dp[key[0]] << "\n";
               iskey[key[0]] = dp[key[0]] = 0;
                                                                                                                                        dp[i] = ++L;
                                                                                                                                } else
 8.7 Dominator Tree [baa540]
                                                                                                                                       auto it
 struct Dominator_tree {
        int n, id;
        int n, id;
vector < vector < int >> adj, radj, bucket;
vector < int >> sdom, dom, vis, rev, pa, rt, mn, res;
Dominator_tree(int n_ = 0) { init(n_); }
void init(int _n) {
    n = _n, id = 0;
    adj.assign(n, vector < int >());
    radj.assign(n, vector < int >());
}
              bucket.assign(n, vector<int>());
sdom.resize(n); dom.assign(n, -1);
vis.assign(n, -1); rev.resize(n);
pa.resize(n); rt.resize(n);
```

if (rt[v] == v) return x ? -1 : v; int p = query(rt[v], 1); if (p == -1) return x ? rt[v] : mn[v]; if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]]; dfs(s); for (int i = id - 1; i >= 0; i--) { for (int u : radj[i]) sdom[i] = min(sdom[i], sdom[query(u, 0)]); if (i) bucket[sdom[i]].push_back(i); for (int u : bucket[i]) { int p = query(u, 0); dom[u] = sdom[p] == i ? i : p; if (i) rt[i] = pa[i]; for (int i = 1; i < id; i++) if (dom[i] != sdom[i]) dom[i] = dom[dom[i]]; for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre> for (int i = 0; i < n; i++) dom[i] = res[i];</pre> string s1, s2; cin >> s1 >> s2; vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0)); vector < vector < int >> dp(m + 1, vector < int >< n + 1 for (int i = 1; i <= m; i++) { for (int j = 1; j <= n; j++) { if (s1[i - 1] == s2[j - 1]) dp[i][j] = dp[i - 1][j - 1] + 1;</pre> dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]); int length = dp[m][n]; cout << length << "\n"; string s(length, 'c'); // backtracking while (m >= 1 && n >= 1) { if (s1[m - 1] == s2[n - 1]) { s[length - 1] = s1[m - 1]; m--, n--, length--; } else { if (dp[m - 1][n] > dp[m][n - 1]) m--; int n; cin >> n; vector <int> v(n); for (int i = 0; i < n; i++) cin >> v[i]; tht dp[ii], vector the stk, stk.push_back(v[0]); dp[0] = 1; int L = 1; for (int i = 1; i < n; i++) { if (v[i] > stk.back()) { stk.push_back(v[i]); } = lower_bound(stk.begin(), stk.end(), v[i]); *it = v[i]; dp[i] = it - stk.begin() + 1; vector < int > ans; cout << L << "|n"; for (int i = n - 1; i >= 0; i--) { if (dp[i] == L) { ans.push_back(v[i]), L--; } reverse(ans.begin(), ans.end()); reverse(ans.begin(), ans.end()); for (auto i : ans) cout << i <<</pre> 9.3 Edit Distance [308023] int main() { string s1, s2; cin >> s1 >> s2;

```
int n1 = s1.size(), n2 = s2.size();
      // dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元
vector <int> dp(n2 + 1);
                                                                                                    vector<<mark>int</mark>> ans;
                                                                                                   for (int i = n; i != 0;) {
    if (rec[i][0]) {
      iota(dp.begin(), dp.end(), 0);
     for (int i = 1; i <= n1; i++) {
    vector <int> cur(n2 + 1); cur[0] = i;
    for (int j = 1; j <= n2; j++) {
        if (s1[i - 1] == s2[j - 1]) {
                                                                                                              ans.push_back(a[i].id);
                                                                                                              i = rec[i][1];
                                                                                                        } else i--;
                      cur[j] = dp[j - 1];
                 } else {
                                                                                             9.6 Removal Game [7bb56b]
                      // s1 新增等價於 s2 砍掉
                       // dp[i][j] = min(s2 新增, 修改, s1 新増);
                                                                                            | // 兩個人比賽,每個人輪流取一個數字且只能是頭尾
                      cur[j]
                                                                                             // 問兩人都選得好,第一出手的人可取得的最大分數
                             = min({cur[j - 1], dp[j - 1], dp[j]}) + 1;
                                                                                             int main() {
    int n; cin >> n;
                }
                                                                                                   vector < ll > a(n);
for (int i = 0; i < n; i++) cin >> a[i];
           swap(dp. cur):
                                                                                                   vector dp(n, vector<ll>(n)); // i 到 j 區間的最大 diff
for (int i = n - 1; i >= 0; i--) {
    dp[i][i] = a[i];
    for (int j = i + 1; j < n; j++)
     cout << dp[n2] << "\n";
                                                                                                              (int j = i + 1; j < n; j++)
dp[i][j] =
9.4 Bitmask [a626f9]
void hamiltonianPath(){
                                                                                                                     \max(a[i] - dp[i + 1][j], a[j] - dp[i][j - 1]);
     int n, m; cin >> n >> m;
vector adj(n, vector <int >());
for (int i = 0; i < m; i++) {
   int u, v; cin >> u >> v;
   int u, v; cin >> u >> v;
}
                                                                                                   \frac{1}{2} / x + y = sum; // x - y = dp[0][n - 1]
cout << (accumulate
                                                                                                          (a.begin(), a.end(), 0LL) + dp[0][n - 1]) / 2 << "\n";
           adj[--v].push_back(--u);
                                                                                             9.7 SOS [7f44af]
      // 以...為終點,走過..
     vector dp(n, vector < int > (findBit(n)));
dp[0][1] = 1;
                                                                                            | // 使用情況: 跟 bit 與(被)包含有關, 且 x 在 1e6 左右
                                                                                             // 題目:一數組, 問有多少所有數 & 起來為 0 的集合數
     for (int mask = 1; mask < findBit(n); mask++) {
   if ((mask & 1) == 0) continue;
   for (int i = 0; i < n; i++) {</pre>
                                                                                                    x] 代表包含 x 的 y 個數(比 x 大且 bit 1 全包含 x 的有幾個)
                if ((mask & findBit(i)) == 0) continue;
if (i == n - 1 && mask != findBit(n) - 1) continue;
int pre_mask = mask ^ findBit(i);
for (int j : adj[i]) {
    if ((pre_mask & findBit(j)) == 0) continue;
                                                                                             // 答案應該包含在 dp[0]内, 但是有重複元素, 所以考慮容斥
                                                                                                    就是 ans = \sum _{i=0}^{n} (-1)^{pop_count(i)} 2^{dp[i]-1}
                                                                                             // => 全部
                      dp[i][mask
                                                                                                    為 0 的個數 - 至少一個為 1 的個數 + 至少兩個為 1 的個數...
                             ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
                                                                                             void solve() {
                                                                                                   int n; cin >> n; Z ans = 0;
vector <int> a(n);
for (int i = 0; i < n; i++)
    cin >> a[i];
                }
          }
     cout << dp[n - 1][findBit(n) - 1] << "\n";</pre>
                                                                                                   int m = __lg(*max_element(a.begin(), a.end())) + 1;
void elevatorRides() {
                                                                                                   // 定義 dp[mask] 為 mask 被包含於 a[i] 的 a[i] 個數 vector<Z> dp(1 << m);
for (int i = 0; i < n; i++)
     int n, x; cin >> n >> x; vector<int> a(n);
for (int i = 0; i < n; i++) cin >> a[i];
vector<array<int, 2>> dp(findBit(n));
                                                                                                   for (int mask = 0; mask < 1 << m; mask++) {
   int sgn = __builtin_popcount(mask) & 1 ? -1 : 1;
   ans += sgn * (power(Z(2), dp[mask].val()) - 1);</pre>
                                                                                                   cout << ans << "\n":
                 } else if (dp[pre_mask
                                                                                             9.8 CHT [5f5c25]
                      ll m, b;
ll m, b;
Line(ll m = 0, ll b = 0) : m(m), b(b) {}
ll eval(ll x) {
    return m * x + b;
           }
     cout << dp[findBit(n) - 1][0] << "\n";
                                                                                             };
                                                                                             struct CHT { // 用在查詢單調斜率也單調
  int n, lptr, rptr; vector<line> hull;
  CHT(int n_ = 0, Line init_ = Line()) {
     init(n_, init_);
}
9.5 Projects [0942aa]
int main() { // 排程有權重問題,輸出價值最多且時間最少
                                                                                                   void init(int n_ = 0, Line init_ = Line()) {
    n = n_; hull.resize(n); reset(init_);
struct E {
      int from, to, w, id;
      bool operator < (const E &rhs) {</pre>
           return to == rhs.to ? w > rhs.w : to < rhs.to;
                                                                                                   void reset(Line init_ = Line()) {
    lptr = rptr = 0; hull[0] = init_;
     int n; cin >> n; vector <E> a(n + 1);
for (int i = 1; i <= n; i++) {
   int u, v, w; cin >> u >> v >> w;
   a[i] = {u, v, w, i};
                                                                                                   bool pop_front(Line &l1, Line &l2, ll x) {
                                                                                                        // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y
                                                                                                         // 代表查詢的當下,右線段的高度已經低於左線段了
                                                                                                         return l1.eval(x) >= l2.eval(x);
     vector<array<ll, 2>> dp(n + 1); // w, time
     vector<array<int, 2>> rec(n + 1); // 有沒選, 上個是誰
sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
    auto it = --lower_bound(all(a), E({0, a[i].from}),
                                                                                                   bool pop_back(Line &l1, Line &l2, Line &l3) {
                                                                                                        // 本題斜率遞減、上凸包
                                                                                                        // 因此只要 12 跟
           auto it = --lower_bound(al(a), c({0}, a[t]...om}),
[](E x, E y){ return x.to < y.to; });
int id = it - a.begin(); dp[i] = dp[i - 1];
ll nw = dp[id][0] + a[i].w;
ll nt = dp[id][1] + a[i].to - a[i].from;
if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
    dp[i] = {nw, nt}; rec[i] = {1, id};
                                                                                                        l3 的 X 交點 <= l1 跟 l3 的 X 交點, l2 就用不到了
return (l3.b - l2.b)
* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
                                                                                                   void insert(Line L)
```

while (rptr - ĺptr

> 0 && pop_back(hull[rptr - 1], hull[rptr], L))

```
National Chung Cheng University Salmon
           hull[++rptr] = L;
     fl query(ll x) {
    while (rptr - lptr
                  > 0 && pop_front(hull[lptr], hull[lptr + 1], x))
                lptr++
           return hull[lptr].eval(x);
};
9.9 DNC [61c639]
constexpr int N = 3e3 + 5;
constexpr ll inf = 4e18;
// dp[k][j] = min(dp[k - 1][i] + cost[i][j])
def[k][m] = inf;
for (int i = max(k, optl); i <= min(m, optr); i++) {</pre>
           // 注意 i 的範圍、 get_cost 與 dp 的邊界
ll cur = dp[k - 1][i] + get_cost(i, m);
if (cur < dp[k][m]) {
                dp[k][m] = cur, opt = i;
     DNC(k, l, m - 1, optl, opt);
DNC(k, m + 1, r, opt, optr);
for (int i = 2; i <= k; i++) {
          DNC(i, 1, n, 1, n);
     cout << dp[k][n] << "\n";
9.10 LiChaoSegmentTree [a6e320]
constexpr ll Inf = 4e18;
// dp[i] = min(f[j] * s[i] + dp[j])
// v = m x + b
// y = struct Line {
     ll m, b;
Line(ll m = 0, ll b = Inf) : m(m), b(b) {}
      ll eval(ll x) const { return m * x + b; }
struct LiChaoSeg { // 取 max 再變換就好
     int n;
vector < Line > info;
LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
           info.assign(4 << __lg(n), Line());</pre>
     void update(Line line, int node, int l, int r) {
   int m = (l + r) / 2;
   bool left = line.eval(l) < info[node].eval(l);</pre>
           bool mid = line.eval(m) < info[node].eval(m);</pre>
           if (mid) swap(info[node], line); // 如果新線段比較好if (r - l == 1) return;
           if (r - l == 1) return;
else if (left != mid) update(line, 2 * node, l, m);
           // 代表左半有交點
           else update(line, 2 * node + 1, m, r);
// 代表如果有交點一定在右半
     void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
   if (r - l == 1) return info[node].eval(x);
           int m = (l + r) / 2;
           if (x < m) return</pre>
```

9.11 Codeforces Example [7d37ea]

il query(int x) { return query(x, 1, 0, n); }

```
| // CF 1932 pF
| // 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
| // 請問在線段不重複的情況下,最多獲得幾分
int main() {
    int n, m;
    cin >> n >> m;
| // 記錄每點有幾個線段
| // 再一個紀錄,包含這個點的左界
    vector<int> l_side(n + 1, inf), cnt(n + 5, 0);
    for (int i = 0; i < m; i++) {
        int l, r; cin >> l >> r;
        l_side[r] = min(l_side[r], l);
        cnt[l]++;
```

min(info[node].eval(x), query(x, 2 * node, l, m));

info[node].eval(x), query(x, 2 * node + 1, m, r));

```
cnt[r + 1]--:
     for (int i = 2; i <= n; i++) {
         cnt[i] += cnt[i - 1];
     for (int i = n; i >= 2; i--) {
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
     vector<int> dp(n + 1);
    dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
         dp[i] = cnt[i];
if (l_side[i] != inf) {
    dp[i] += dp[l_side[i] - 1];
         dp[i] = max(dp[i], dp[i - 1]);
    cout << dp[n] << "\n";
}
// CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
// 再加上 max(bi) - min(bi)
if (a <= k) ans = 1;
     sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
     }); // 用 bi 來排,考慮第 i 個時可以先扣
     vector<vector<int>> dp(n + 1, vector<int>(n + 1, inf));
     // 考慮 v[i] 時, 選 j 個的 sum(ai) - min(bi)
    for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
              // min(不選, 選)
if (dp[i
                    - 1][j - 1] + v[i].first + v[i].second <= k) {
                   // 假如可以選, 更新 ans 時再加回去 bi
                   ans = max(ans, j);
         dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
     cout << ans << endl;
```

10 Geometry

10.1 Basic [d41d8c]

```
template < class T>
struct Point {
    Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) \{ \}
    template < class U>
    operator Point<U>() {
        return Point < U > (U(x), U(y));
    Point &operator+=(const Point &p) & {
    x += p.x; y += p.y; return *this;
    Point & operator -= (const Point &p) & {
        x -= p.x; y -= p.y; return *this;
    Point & operator *= (const T &v) & {
        x *= v; y *= v; return *this;
    Point &operator/=(const T &v) & {
    x /= v; y /= v; return *this;
    Point operator - () const {
         return Point(-x, -y);
    friend Point operator+(Point a, const Point &b) {
         return a += b;
    friend Point operator - (Point a, const Point &b) {
         return a -= b;
    friend Point operator*(Point a, const T &b) {
  return a *= b;
    friend Point operator/(Point a, const T &b) {
         return a /= b;
    friend Point operator*(const T &a, Point b) {
         return b *= a;
    friend bool operator==(const Point &a, const Point &b) {
         return a.x == b.x && a.y == b.y;
    friend istream & operator >> (istream & is. Point &p) {
         return is >> p.x >> p.y;
```

```
friend ostream &operator < <(ostream &os, const Point &p) {
    return os << "(" << p.x << ", " << p.y << ")";</pre>
template < class T>
struct Line {
   Point<T>
      Point <T> b;
     T dot(const Point<T> &a, const Point<T> &b) {
   return a.x * b.x + a.y * b.y;
template < class T>
T cross(const Point < T > &a, const Point < T > &b) {
    return a.x * b.y - a.y * b.x;
template < class T>
T square(const Point < T > &p) {
     return dot(p, p);
template < class T>
double length(const Point<T> &p) {
     return sqrt(double(square(p)));
template < class T>
double length(const Line<T> &l) {
     return length(l.a - l.b);
Point<T> normalize(const Point<T> &p) {
     return p / length(p);
template < class T >
bool parallel(const Line < T > &l1, const Line < T > &l2) {
    return cross(l1.b - l1.a, l2.b - l2.a) == 0;
template < class T>
double distance(const Point<T> &a, const Point<T> &b) {
     return length(a - b);
template < class T>
double distancePL(const Point<T> &p, const Line<T> &l) {
     return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)
      return distance(p, l.a);
   if (dot(p - l.b, l.a - l.b) < 0)
      return distance(p, l.b);
   const Line<T> &l) {
      if (dot(p - l.b, l.a - l.b) < 0)
      return distance(p, l.b);
   }
}</pre>
     return distancePL(p, l);
template < class T>
Point < T> rotate(const Point < T> &a) {
     return Point(-a.y, a.x);
template < class T>
int sgn(const Point<T> &a) {
    return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
     return cross(l.b - l.a, p - l.a) > 0;
template < class T>
Point < T
      > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
return l1.a + (l1.b - l1.a) * (cross(l2.b -
            l2.a, l1.a - l2.a) / cross(l2.b - l2.a, l1.a - l1.b));
template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
     return cross(p - l.a, l.b - l.a) == 0 &&
    min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)</pre>
                 (l.a.y, l.b.y) \ll p.y \ll max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
     (const Point<T> &a, const vector<Point<T>> &p) {
int n = p.size(), t = 0;
for (int i = 0; i < n; i++) {
           if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {
                return true:
     auto v = p[(i + 1) \% n];
           if (u.x < a.
                x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
                t ^= 1;
           return t == 1;
// 0 : not intersect
```

```
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
tuple <int , Point <T > , Point <T >> segmentIntersection
       le<int, Point<T>, Point<T>> segmentIntersection
  (const Line<T> &l1, const Line<T> &l2) {
   if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
      return {0, Point<T>(), Point<T>()};
   if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
      return {0, Point<T>(), Point<T>()};
   if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y))
      return {0, Point<T>(), Point<T>()};
   if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y))
      return {0, Point<T>(), Point<T>()};
   if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
      if (cross(l1.b - l1.a, l2.a - l1.a) != 0) {
         return {0, Point<T>(), Point<T>()};
    }
   else {
      auto maxx1 = max(l1.a.x, l1.b.x);
   }
}
                        auto maxx1 = max(l1.a.x, l1.b.x);
auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
auto miny1 = min(l1.a.y, l1.b.y);
auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.y, l2.b.y);
                        auto maxy2 = max(t2.a.y, t2.b.y);
Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
if (!pointOnSegment(p1, l1))
                         swap(p1.y, p2.y);
if (p1 == p2) {
    return {3, p1, p2};
                         } else {
                                return {2, p1, p2};
               }
       auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
        if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
                 return {1, p, p};
        } else {
                return {3, p, p};
        }
 template < class T>
double distanceSS(const Line<T> &11, const Line<T> &12) {
   if (get<0>(segmentIntersection(l1, l2)) != 0)
        return min({distancePS(l1.a, l2), distancePS(l1
    .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
template < class T>
bool segmentInPolygon
          (const Line<T> &l, const vector<Point<T>> &p) {
        int n = p.size();
        int n = p.size();
if (!pointInPolygon(l.a, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
for (int i = 0; i < n; i++) {
    auto u = p[i];
    auto v = p[(i + 1) % n];
    auto w = p[(i + 2) % n];
}</pre>
                 auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
if (t == 1) return false;
if (t == 0) continue;
                 if (t == 2) {
                         if (pointOnSegment(v, l) && v != l.a && v != l.b)
   if (cross(v - u, w - v) > 0)
      return false;
                } else {
                         if (p1 != u && p1 != v) {
   if (pointOnLineLeft(l.a, Line(v, u))
                                          || pointOnLineLeft(l.b, Line(v, u)))
                                          return false:
                                } else if (p1 == v) {
                                                 if (pointOnLineLeft(w, l)
                                                          || pointOnLineLeft(w, Line(u, v)))
                                                          return false:
                                 } else if (l.b == v) {
   if (pointOnLineLeft(u, Line(l.b, l.a))) {
      if (pointOnLineLeft(w, Line(l.b, l.a)))
                                                          && pointOnLineLeft(w, Line(u, v)))
                                                          return false:
                                         } else {
                                                 return false:
                                 } else {
```

```
if (pointOnLineLeft(u, l)) {
   if (pointOnLineLeft(w, Line(l.b, l.a))
                                 || pointOnLineLeft(w, Line(u, v)))
                                 return false:
                            return false;
                       }
                  }
             }
         }
    return true:
template < class T>
vector<Point<T>> hp(vector<Line<T>> lines) {
    auto d1 = l1.b - l1.a;
auto d2 = l2.b - l2.a;
         if (sgn(d1) != sgn(d2))
    return sgn(d1) == 1;
         return cross(d1, d2) > 0;
    }):
    deque<Line<T>> ls;
    deque<Point<T>> ps;
for (auto l : lines) {
    if (ls.empty()) {
              ls.push_back(l);
              continue:
         while (!ps.empty() && !pointOnLineLeft(ps.back(), l))
         ps.pop_back(), ls.pop_back();
while (!ps.empty() && !pointOnLineLeft(ps[0], l))
              ps.pop_front(), ls.pop_front();
         if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
              if (dot
                   (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                   if (!pointOnLineLeft(ls.back().a, l)) {
                       assert(ls.size() == 1);
                       ls[0] = l:
                   continue:
              return {};
         ps.push_back(lineIntersection(ls.back(), l));
ls.push_back(l);
    while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0]))
    ps.pop_back(), ls.pop_back();
if (ls.size() <= 2) return {};</pre>
    ps.push_back(lineIntersection(ls[0], ls.back()));
    return vector(ps.begin(), ps.end());
using P = Point<ll>;
10.2 Convex Hull [b5758d]
```

```
int main() {
    int n; cin >> n;
vector <P> P(n), U, L;
for (int i = 0; i < n; i++) {</pre>
         cin >> P[i];
    sort(P.begin(),
          .end(), [](const Point<i64> &a, const Point<i64> &b) {
         return a.x == b.x ? a.y < b.y : a.x < b.x;
    L.pop_back();
         U.pop_back();
         if (L.
              empty() || !(L.back() == P[i])) L.push_back(P[i]);
         if (U.
              empty() || !(U.back() == P[i])) U.push_back(P[i]);
    if (L.size() <= 2 && U.size() <= 2) {
    // No Hull
    cout << L.size() + U.size() - 2 << "|n";
for (int i = 0; i < L.size() - 1; i++) {
    cout << L[i].x << " " << L[i].y << "|n";</pre>
    for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << "\n";</pre>
```

10.3 MinEuclideanDistance [3020bc]

```
mplate < class Ta
T distanceSquare(const Point<T> &a, const Point<T> &b) {
    return square(a - b);
void solve() {
```

```
int n; cin >> n;
constexpr ll inf = 8e18;
       vector < Point < ll >> a(n);
       for (int i = 0; i < n; i++) {
    ll x, y;</pre>
             cin >> x >> y;
a[i] = Point<ll>(x, y);
       struct sortY {
             bool operator
     ()(const Point<ll> &a, const Point<ll> &b) const {
                    return a.y < b.y;</pre>
       struct sortXY {
             bool operator
                    ()(const Point<ll> &a, const Point<ll> &b) const {
if (a.x == b.x) return a.y < b.y;</pre>
             }
       sort(a.begin(), a.end(), sortXY());
      sort(a.begin(), a.end(), sortxY());
vector<Point<ll>> t(n);
auto devide = [&](auto &&self, int l, int r) -> ll {
    if (l == r) return inf;
    int m = (l + r) / 2;
    ll ans = min(self(self, l, m), self(self, m + 1, r));
    ll midval = a[m].x;
}
             for (int i = 1; i <= r; i++) {
   if ((midval - a[i].x) * (midval - a[i].x) <= ans) {
      t[p++] = a[i];
}</pre>
              sort(t.begin(), t.begin() + p, sortY());
             for (int i = 0; i < p; i++){
    for (int j = i + 1; j < p; j++) {
        ans = min(ans, distanceSquare(t[i], t[j]));
}</pre>
                           if ((t[i].y
                                    t[j].y) * (t[i].y - t[j].y) > ans) break;
                    }
              return ans;
       cout << devide(devide, 0, n - 1) << "\n";</pre>
}
10.4 LatticePoints [00db9d]
       // Polygun 內整數點數
```

```
int main() {
        int n; cin >> n;
vector <Point < ll>> polygon(n);
for (int i = 0; i < n; i++) cin >> polygon[i];
        ll area = 0;
        for (int i = 0; i < n; i++) {
    area += cross(polygon[i], polygon[(i + 1) % n]);</pre>
        area = abs(area):
        auto countBoundaryPoints
                  = [](const vector<Point<ll>>& polygon) -> ll {
               ll res = 0;
int n = polygon.size();
               for (int i = 0; i < n; i++) {
    ll dx = polygon[(i + 1) % n].x - polygon[i].x;
    ll dy = polygon[(i + 1) % n].y - polygon[i].y;
    res += std::gcd(abs(dx), abs(dy));</pre>
               return res:
         ĺĺ res = countBoundaryPoints(polygon);
        ll ans = (area - res + 2) / 2;
cout << ans << " " << res << "\n";
```

10.5 MinCoverCircle [c9ca81]

```
pair<T, Point<T>> MinCircular(vector<Point<T>> &a) {
      random_shuffle(a.begin(), a.end());
int n = a.size();
Point<T> c = a[0]; T r = 0;
for (int i = 1; i < n; i++) {
    if (T(length(c - a[i]) - r) > 0.0) {
                p + rotate(a[j] - a[i])), Line
  (q, q + rotate(a[k] - a[j])));
r = length(c - a[i]);
                                     }
                              }
                        }
                 }
```

```
}
return make_pair(r, c);
}
```