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Basic

1.1 Default Code [d41d8c]

```
#include <bits/stdc++.h>
using namespace std;
using ll = long long;
void solve() {
}
int main() {
     ios_base::sync_with_stdio(false);
     cin.tie(nullptr);
     int t = 1;
     cin >> t;
while (t--) {
    solve();
     return 0;
}
```

1.2 Compare Fuction [d41d8c]

```
|// 1. sort, 二分搜刻在函式內 lambda 就好
// 2. priority queue 小到大是 >, set 是 <
 // 3. set 不能 = , multiset 必須 =
 // 4. 確保每個成員都要比到
 // 5. pbds_multiset 不要用 lower_bound
 // 6. 如果要用 find, 插入 inf 後使用 upper_bound
 // 7. multiset 可以跟 set 一樣使用, 但請注意第 3、4 點
auto cmp = [](int i, int j) { return i > j; };
priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
 vector<int> a {1, 2, 5, 4, 3}; // 小心不要改到 a auto cmp = [&a](int i, int j) { return a[i] > a[j]; }; priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
```

1.3 Pbds [d41d8c]

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < class T>
using pbds_set = tree<T, null_type,
    less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template < class T>
1.4 Double [a94c1c]
     double x;
constexpr D() : x{0} {}
constexpr D(double x) : x{x} {}
constexpr static double eps = 1E-12;
      explicit operator double() const { return x; }
constexpr D operator-() const {
           return D(-x);
      constexpr D &operator*=(D rhs) & {
           x *= rhs.x; return *this;
      constexpr D &operator+=(D rhs) & {
           x += rhs.x; return *this;
      constexpr D &operator -=(D rhs) & {
    x -= rhs.x; return *this;
      constexpr D & operator/=(D rhs) & {
   assert(fabs(rhs.x) > eps);
   x /= rhs.x; return *this;
      friend constexpr D operator*(D lhs, D rhs) {
           return lhs *= rhs;
      friend constexpr D operator+(D lhs, D rhs) {
           return lhs += rhs;
      friend constexpr D operator - (D lhs, D rhs) {
    return lhs -= rhs;
      friend constexpr D operator/(D lhs, D rhs) {
    return lhs /= rhs;
      friend istream &operator>>(istream &is, D &a) {
   double v; is >> v; a = D(v); return is;
      } // eps should < precision
friend constexpr bool operator <(D lhs, D rhs) {
   return lhs.x - rhs.x < -eps;</pre>
      friend constexpr bool operator>(D lhs, D rhs) {
           return lhs.x - rhs.x > eps:
      friend constexpr bool operator==(D lhs, D rhs) {
    return fabs(lhs.x - rhs.x) < eps;</pre>
      friend constexpr bool operator <= (D lhs, D rhs) {
    return lhs < rhs || lhs == rhs;</pre>
      friend constexpr bool operator>=(D lhs, D rhs) {
   return lhs > rhs || lhs == rhs;
      friend constexpr bool operator!=(D lhs, D rhs) {
   return !(lhs == rhs);
};
1.5 Int128 [85923a]
using i128 = __int128_t; // 1.7F38
istream &operator>>(istream &is, i128 &a) {
     i128 sgn = 1; a = 0;
string s; is >> s;
for (auto c : s) {
   if (c == '-') {
                sgn = -1;
           } else {
                 a = a * 10 + c - '0';
           }
      a *= sgn;
      return is;
ostream &operator<<(ostream &os. i128 a) {
```

string res; if (a < 0) os << '-', a = -a; while (a) {

a /= 10;

os << res; return os;

res.push_back(a % 10 + '0');

reverse(res.begin(), res.end());

1.6 Rng [401544]

2 Graph

2.1 DFS And BFS [e2d856]

```
int main() {
       vector<vector<int>> adj(n);
       // dfs_graph
vector<bool> vis(n);
       auto dfs = [&](auto self, int u) -> void {
  if (vis[u]) return;
  vis[u] = true;
             for (auto v: adj[u]) {
    self(self, v);
             }
       dfs(dfs, 0);
       // bfs
       vector < int > depth(n, 1e9);
       queue < int > q;
auto bfs = [&](auto self, int s) -> void {
   vis[s] = true, depth[s] = 0;
              q.push(s);
             while (!q.empty()) {
   int u = q.front(); q.pop();
   for (auto v : adj[u]) {
                           if (vis[v]) continue;
vis[v] = true;
depth[v] = depth[u] + 1;
                           q.push(v);
                    }
             }
      };
bfs(bfs, 0);
```

2.2 Prim [3a3805]

2.3 Bellman-Ford [430ded]

2.4 Floyd-Warshall [3f61a4]

2.5 **Euler** [4177dc]

```
// 1. 無向圖是歐拉圖:
| // 非零度頂點是連通的
// 頂點的度數都是偶數
| // 2. 無向圖是半歐拉圖(有路沒有環):
// 非零度頂點是連通的
// 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
// 非零度頂點是強連通的
// 每個頂點的入度和出度相等
// 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
// 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
// 其他頂點的入度和出度相等
vector<int> ans;
auto dfs = [&](auto &&self, int u) -> void {
   while (g[u].size()) {
   int v = *g[u].begin();
       g[u].erase(v);
       self(self, v);
    ans.push_back(u);
dfs(dfs, 0);
reverse(ans.begin(), ans.end());
```

2.6 DSU [749620]

```
struct DSU {
       vector<int> boss, siz;
      DSU() {}
DSU(int n_) { init(n_); }
       void init(int n_) {
    n = n_; boss.resize(n);
             iota(boss.begin(), boss.end(), 0);
             siz.assign(n, 1);
      int find(int x) {
   if (boss[x] == x) return x;
   return boss[x] = find(boss[x]);
       bool same(int x, int y) {
    return find(x) == find(y);
      bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);</pre>
                            siz[y];
             boss[y] = x;
       int size(int x) {
    return siz[find(x)];
      }
};
struct DSU {
       vector<int> boss. siz. stk:
       DSU() {}
```

DSU(int n_) { init(n_); }

```
void init(int n_) {
             n = n_;
              boss.resize(n);
             iota(boss.begin(), boss.end(), 0);
siz.assign(n, 1);
              stk.clear();
      int find(int x) {
   return x == boss[x] ? x : find(boss[x]);
      bool same(int x, int y) {
    return find(x) == find(y);
      bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);
    siz[x] += siz[y];
    boss[y] = x;
}</pre>
             n - -;
             stk.push_back(y);
       void undo(int x) {
   while (stk.size() > x) {
                   int y = stk.back();
                    stk.pop_back();
                     siz[boss[y]] -= siz[y];
                    boss[y] = y;
             }
      int size(int x) {
    return siz[find(x)];
};
```

2.7 SCC [5d3e16]

```
struct SCC {
     int n, cur, cnt;
     vector < int >> adj;
     vector <int> stk, dfn, low, bel;
SCC(int n_ = 0) { init(n_); }
void init(int n_) {
          n = n_;
adj.assign(n, {});
          dfn.assign(n, -1);
low.resize(n);
          bel.assign(n, -1);
stk.clear();
           cur = cnt = 0;
     void addEdge(int u, int v) {
          adj[u].push_back(v);
     void dfs(int x) {
    dfn[x] = low[x] = cur++;
           stk.push_back(x);
           for (auto y : adj[x]) {
   if (dfn[y] == -1) {
                     dfs(y);
                low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
                     low[x] = min(low[x], dfn[y]);
                }
           if (dfn[x] == low[x]) {
                int y;
                do {
                     y = stk.back();
                bel[y] = cnt;
stk.pop_back();
while (y != x);
          }
     vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
           return bel;
     struct Graph {
          vector<pair<int, int>> edges;
           vector<int> siz;
           vector<int> cnte;
     Graph compress() {
          Graph g;
g.n = cnt;
g.siz.resize(cnt);
           g.cnte.resize(cnt);
          g.edges.emplace_back(bel[i], bel[j]);
                     } else {
                          g.cnte[bel[i]]++;
```

```
}
         return g;
    }
};
```

2.8 VBCC [ee1554]

```
struct VBCC {
                int n, cur, cnt;
vector<vector<int>> adj;
vector<vector<int>> bcc;
                vector<int> stk, dfn, low;
                vector < bool > ap;
VBCC(int n_ = 0) { init(n_); }
void init(int n_) {
                             n = n_;
adj.assign(n, {});
bcc.assign(n, {});
                               dfn.assign(n, -1);
                               low.resize(n);
                               ap.assign(n, false);
stk.clear();
                              cur = cnt = 0:
                void addEdge(int u, int v) {
                             adj[u].push_back(v);
adj[v].push_back(u);
                void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
    stk.push_back(x);
                               int child = 0;
                              for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
        dfs(y, x), child++;
        low[x] = min(low[x], low[y]);
        continue;
        low[x] = min(low[x], low[y]);
        continue;
        low[x] = min(low[x], low[y]);
        continue;
        low[x] = min(low[x], low[y]);
        low[x] = min(low[x], low[x], low[y]);
        low[x] = min(low[x], low[x], low[x], low[x]);
        low[x] = min(low[x], low[x], lo
                                                             if (low[y] >= dfn[x]) {
                                                                           int v;
do {
    v = stk.back();
                                                                                           bcc[v].push_back(cnt);
                                                                            stk.pop_back();
} while (v != y);
                                                                             bcc[x].push_back(cnt);
                                                                           cnt++:
                                                            if (low[y] >= dfn[x] && p != -1) {
    ap[x] = true;
                                                            }
                                             } else {
                                                            low[x] = min(low[x], dfn[y]);
                                             }
                               if (p == -1 && child > 1) {
    ap[x] = true;
               fvector < bool > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
            }
}</pre>
                                             }
                               return ap;
                struct Graph {
                               int n;
                              vector<pair<int, int>> edges;
vector<int> bel;
vector<int> siz; // BCC 內節點數
                               vector<int> cnte; // BCC 內邊數
                Graph compress() {
                             Graph g; // 壓完是一棵樹,但不一定每個 bel 都有節點 g.bel.resize(n);
                               g.siz.resize(cnt)
                              g.cnte.resize(cnt);
for (int u = 0; u < n; u++) {
    if (ap[u]) {
        g.bel[u] = cnt++;
    }
}</pre>
                                                            g.siz.emplace_back();
g.cnte.emplace_back();
                                                             for (auto v : bcc[u]) {
                                                                           g.edges.emplace_back(g.bel[u], v);
                                             } else if (bcc[u].size() == 1) {
   g.bel[u] = bcc[u][0];
                                             g.siz[g.bel[u]]++;

}
g.n = cnt;
for (int i = 0; i < n; i++) {
    for (auto j : adj[i]) {
        if (g.bel[i] == g.bel[j] && i < j) {
            g.cnte[g.bel[i]]++;
        }
}
</pre>
                                             }
                               return g;
```

2.9 EBCC [59d8ca]

| };

```
struct EBCC { // CF/contest/1986/pF
  int n, cur, cnt;
  vector<vector<int>> adj;
       vector<int> stk, dfn, low, bel;
      adj.assign(n, {});
              dfn.assign(n, -1);
              low.resize(n);
              bel.assign(n, -1);
             stk.clear();
bridges.clear();
cur = cnt = 0;
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
      void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
              stk.push_back(x);
             for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
                          dfs(y, x);
low[x] = min(low[x], low[y]);
if (low[y] > dfn[x]) {
                                 bridges.emplace_back(x, y);
                    } else if (bel[y] == -1) {
    low[x] = min(low[x], dfn[y]);
              if (dfn[x] == low[x]) {
                    int y;
                    bel[y] = cnt;
stk.pop_back();
                    } while (y != x);
                    cnt++;
             }
      vector < int > work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
        }
}</pre>
                    }
              return bel;
       struct Graph {
             vector<pair<int, int>> edges;
              vector<int> siz; // BCC 內節點數
              vector<int> cnte; // BCC 內邊數
       Graph compress() {
             Graph g;
g.n = cnt;
              g.siz.resize(cnt);
             g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;</pre>
                    g.stz[bet[t]]++;
for (auto j : adj[i]) {
    if (bel[i] < bel[j]) {
        g.edges.emplace_back(bel[i], bel[j]);
    } else if (i < j) {
        g.cnte[bel[i]]++;
}</pre>
                          }
                    }
              return g;
      }
};
```

2.10 2-SAT [28688f]

2.11 Funtional Graph [e8fd64]

```
constexpr int N = 2E5 + 5;
constexpr int N = 2tb + 5;
int cht[N][31]; // 倍增表, 放外面不然 TLE
struct FuntionalGraph {
  int n, cnt;
  vector<int> g, bel, id, len, in, top;
  FuntionalGraph(): n(0) {}
  FuntionalGraph(vector<int> g_) { init(g_); }
  vaid init(vector<int> a_) {
          build();
          for (int i = 0; i < n; i++) {
    cht[i][0] = g[i];
    in[g[i]]++;</pre>
                   for (int i = 1; i <= 30; i++)
    for (int u = 0; u < n; u++)
        cht[u][i] = cht[cht[u][i - 1]][i - 1];
for (int i = 0; i < n; i++)
        if (in[i] == 0) label(i);</pre>
                   for (int i = 0; i < n; i++)
    if (top[i] == -1) label(i);</pre>
           void label(int u) {
                   vector <int > p; int cur = u;
while (top[cur] == -1) {
   top[cur] = u;
                             p.push_back(cur);
                             cur = g[cur];
                    auto s = find(p.begin(), p.end(), cur);
                   vector s = rind(p.begin(), p.end());
vector sint> cyc(s, p.end());
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {
    bel[cyc[i]] = cnt;
    id[cyc[i]] = i;</pre>
                    if (!cyc.empty())
                   ++cnt, len.push_back(cyc.size());

for (int i = p.size() - 1; i > 0; i--)

id[p[i - 1]] = id[p[i]] - 1;
          int jump(int u, int k) {
    for (int b = 0; k > 0; b++){
        if (k & 1) u = cht[u][b];
}
                            k >>= 1:
                   return u;
         }
};
```

3 Data Structure

3.1 BIT [d41d8c]

```
template < typename T>
struct Fenwick { // 全部以 0 based 使用
int n; vector < T> a;
Fenwick(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_;
    a.assign(n, T{});
}
```

```
void add(int x, const T &v) {
   for (int i = x + 1; i <= n; i += i & -i) {
      a[i - 1] = a[i - 1] + v;
}</pre>
      T sum(int x) { // 左閉右開查詢
            T ans{};
            for (int i = x; i > 0; i -= i & -i) {
    ans = ans + a[i - 1];
      T rangeSum(int l, int r) { // 左閉右開查詢
            return sum(r) - sum(l);
      int select(const T &k, int start = 0) {
           `x += i;
                      cur = cur + a[x - 1];
                 }
            }
            return x;
     }
};
template < class T>
struct TwoDFenwick { // 全部以 0 based 使用
     int nx, ny; // row, col 個數 vector < vector < T >> a;
      TwoDFenwick(int nx_ = 0, int ny_ = 0) {
            init(nx_, ny_);
      void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
      void add(int x, int y, const T &v) {
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            a[i - 1][j - 1] = a[i - 1][j - 1] + v;
        }
}</pre>
           }
     }
      T sum(int x, int y) { // 左閉右開查詢
           Im(int x, c..., );
T ans{};
for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans + a[i - 1][j - 1];
}
            return ans;
     }
T rangeSum
            (int lx, int ly, int rx, int ry) { // 左閉右開查詢
            return sum(
                  (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
}:
```

3.2 RangeBit [d41d8c]

```
T \text{ val} = T(
                           x + i + 1) * d[x + i - 1] - di[x + i - 1];
if (cur + val <= k) {
x += i;
                                  cur = cur + val:
                    }
              return x;
     }
template < class T>
struct rangeTwoDFenwick { // 全部以 0 based 使用
       int nx, ny; // row, col 個數
vector<vector<T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
             init(nx_, ny_);
       void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
              dj.assign(nx, vector<T>(ny, T{}));
             dij.assign(nx, vector<T>(ny, T{}));
       T vi = v * (x + 1);
T vj = v * (y + 1);
             T vj = v * (y + 1);
T vij = v * (x + 1) * (y + 1);
for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        d[i - 1][j - 1] = d[i - 1][j - 1] + v;
        di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
        dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
        dij[i - 1][j - 1] = dij[i - 1][j - 1] + vj;
}</pre>
                    }
             }
       void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
             add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
             add(lx, ly, v);
       T sum(int x, int y) { // 左閉右開查詢
              T ans{}:
              for (int i = x; i > 0; i -= i & -i) {
                     for (int j = y; j > 0; j -= j & -j) {
                           ans = ans
                            + T(x * y + x + y + 1) * d[i - 1][j - 1];  ans = ans - T(y + 1) * d[i - 1][j - 1];  ans = ans - T(x + 1) * d[i - 1][j - 1]; 
                           ans = ans + dij[i - 1][j - 1];
                    }
             return ans;
       T rangeSum
               (int lx, int ly, int rx, int ry) { // 左閉右開查詢
              return sum(
                     (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
      }
};
```

3.3 Segment Tree [d41d8c]

```
if (x < m) {
    modify(2 * p, l, m, x, v);</pre>
             } else {
                   modify(2 * p + 1, m, r, x, v);
            pull(p);
      void modify(int p, const Info &i) {
            modify(1, 0, n, p, i);
      info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    return query(p *</pre>
             return query(p
                   2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
      template < class F> // 尋找區間內,第一個符合條件的
      int findFirst
            (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)
    return -1;
if (l >= x && r <= y && !pred(info[p]))</pre>
            return -1;

if (r - l == 1)

return l;

int m = (l + r) / 2;
             int res = findFirst(2 * p, l, m, x, y, pred);
            if (res == -1)
    res = findFirst(2 * p + 1, m, r, x, y, pred);
      template < class F> // 若要找 last,先右子樹遞迴即可
int findFirst(int l, int r, F & pred) {
    return findFirst(1, 0, n, l, r, pred);
};
struct Info {
      int n = 1;
      int sum = 0;
Info operator+(const Info &a, const Info &b) {
   return { a.n + b.n, a.sum + b.sum };
3.4 Lazy Segment Tree [d41d8c]
```

```
template < class Info, class Tag>
struct LazySeg { // 左閉右開寫法
       int n;
       vector < Info > info;
       vector < Tag > tag;
LazySeg() : n(0) {}
LazySeg(int n_, Info v_ = Info()) {
              init(n_, v_);
       template < class T>
       LazySeg(vector<T> init_) {
              init(init_);
       void init(int n_, Info v_ = Info()) {
    init(vector(n_, v_));
       template < class T>
       void init (vector<T> init_) {
             int( (vector=r) tint(_) {
    n = init_.size();
    info.assign(4 << __lg(n), Info());
    tag.assign(4 << __lg(n), Tag());
    function <void(
        int, int, int)> build = [&](int p, int l, int r) {
        if (r - l == 1) {
            info[p] = init_[l];
            return.
                            return;
                     int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                     pull(p);
              build(1, 0, n);
       void pull(int p) {
   info[p] = info[p * 2] + info[p * 2 + 1];
       void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
   tag[p].apply(v);
      void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
              tag[p] = Tag();
       void modify(int p, int l, int r, int x, const Info &v) {
              if (r - l == 1) {
```

```
info[p] = v;
            int m = (l + r) / 2;
            push(p, l, r);
            if (x < m) {
                  modify(2 * p, l, m, x, v);
            } else {
                  modify(2 * p + 1, m, r, x, v);
            pull(p);
      void modify(int p, const Info &i) {
    modify(1, 0, n, p, i);
      Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;</pre>
            push(p, l, r);
            return query(p
                   2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
      void range_apply
    (int p, int l, int r, int ql, int qr, const Tag &v) {
    if (qr <= l || ql >= r) return;
    if (ql <= l && r <= qr) {</pre>
                  apply(p, l, r, v);
                  return;
           fint m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
pull(p);
      void range_apply(int l, int r, const Tag &v) {
    range_apply(1, 0, n, l, r, v);
      template < class F> // 尋找區間內,第一個符合條件的
      int findFirst
            (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
    return -1;</pre>
            if (l >= x && r <= y && !pred(info[p])) {</pre>
                  return -1;
            if (r - l == 1) {
                  return l;
            int m = (l + r) / 2;
            push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
            if (res ==
                  res = findFirst(2 * p + 1, m, r, x, y, pred);
            return res;
      template < class F> // 若要找 last, 先右子樹遞迴即可
int findFirst(int l, int r, F & & pred) {
    return findFirst(1, 0, n, l, r, pred);
};
struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add; void apply(const Tag& v) {
            if (v.set_val) {
                 set_val = v.set_val;
add = v.add;
            else {
                  add += v.add;
     }
};
struct Info {
      int sum;
void apply(int l, int r, const Tag &v) {
           if (v.set_val) {
    sum = (r - l) * v.set_val;
            sum += (r - l) * v.add;
      // Info &operator=(const Info &rhs) {
               // 部分 assignment 使用
return *this;
     //
// }
Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
3.5 Persistent Segment Tree [d41d8c]
```

```
template < class Info >
struct PST {
    struct Node {
```

```
Info info = Info();
                                                                                                                         void pull() { // update siz or other information
              int lc = 0, rc = `
                                                                                                                               min = val;
                                                                                                                               for (auto c : {lc, rc}) {
    if (!c) continue;
       vector < Node > nd:
       int n = 0; vector<int> rt;
       PST() : n(0) {}
                                                                                                                                       siz += c->siz;
      PST(int n_, Info v_ = Info()) { init(n_, v_); }
template < class T >
                                                                                                                                      min = std::min(min, c->min);
                                                                                                                               }
       PST(vector<T> init_) { init(init_); }
void init(int n_, Info v_ = Info()) {
   init(vector<Info>(n_, v_));
                                                                                                                        }
void push() {
    if (rev_valid) {
        swap(lc, rc);
        if (lc) lc->rev_valid ^= 1;
        if (rc) rc->rev_valid ^= 1;
}
      femplate < class T >
void init(vector < T > init_) {
    n = init_.size();
    nd.clear(); rt.clear();
                                                                                                                               rev_valid = false;
             nd.emplace_back(); // 讓 root 指向 1-based rt.push_back(build(0, n, init_));
                                                                                                                         int find(int k) { // 找到 min 是 k 的位置 (1-based)
                                                                                                                               push();
int ls = (lc ? lc->siz : 0) + 1;
       int build(int l, int r, vector<Info> &init_) {
                                                                                                                               if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
              int id = nd.size();
             nd.emplace_back();
if (r - l == 1) {
    nd[id].info = init_[l];
                                                                                                                        }
                    return id;
                                                                                                                 int size(Treap *t) {
    return t ? t->siz : 0;
             int m = (l + r) >> 1;
nd[id].lc = build(l, m, init_);
nd[id].rc = build(m, r, init_);
pull(nd[id]);
                                                                                                                  Treap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
    a->push(); b->push();
    if (a->pri > b->pri) {
        a -> c = merge(a->rc, b);
        a -> c = merge(a -> c, b);
    }
}
       void pull(Node &t) {
             t.info = nd[t.lc].info + nd[t.rc].info;
                                                                                                                               a->pull();
                                                                                                                               return a:
       int copy(int t) { // copy 一個 node
  nd.push_back(nd[t]);
                                                                                                                         else {
                                                                                                                               b->lc = merge(a, b->lc);
b->pull();
              return nd.size() - 1;
                                                                                                                               return b;
      int generate() { // 創立新的 node
    nd.emplace_back();
                                                                                                                        }
              return nd.size() - 1;
                                                                                                                 pair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
       int modify(int t, int l, int r, int x, const Info &v) {
   t = t ? copy(t) : generate();
   if (r - l == 1) {
                                                                                                                         t->push();
                                                                                                                         if (size(t->lc) < k) {
   auto [a, b] = split(t->rc, k - size(t->lc) - 1);
   t->rc = a;
                    nd[t].info = v;
                                                                                                                               t->pull();
              int m = (l + r) >> 1;
                                                                                                                               return {t, b};
              if (x < m) {
                    nd[t].lc = modify(nd[t].lc, l, m, x, v);
                                                                                                                         else {
                                                                                                                               auto [a, b] = split(t->lc, k);
t->lc = b;
                    nd[t].rc = modify(nd[t].rc, m, r, x, v);
                                                                                                                               t->pull();
             pull(nd[t]);
                                                                                                                               return {a, t};
              return t;
                                                                                                                        }
       void modify(int ver, int pos, const Info &val) {
   if (int(rt.size()) <= ver) rt.resize(ver + 1);</pre>
                                                                                                                  void Print(Treap *t) {
                                                                                                                         if (!t) return:
              rt[ver] = modify(rt[ver], 0, n, pos, val);
                                                                                                                         t->push();
      Info query(int t, int l, int r, int ql, int qr) {
    if (l >= qr || r <= ql) return Info();
    if (ql <= l && r <= qr) return nd[t].info;
    int m = (l + r) >> 1;
                                                                                                                         Print(t->lc);
                                                                                                                         cout << t->val;
                                                                                                                         Print(t->rc);
              return query(nd[t].
                                                                                                                 3.7 RMQ [d41d8c]
                     lc, l, m, ql, qr) + query(nd[t].rc, m, r, ql, qr);
      Info query(int ver, int ql, int qr) {
    return query(rt[ver], 0, n, ql, qr);
                                                                                                                  template < class T, class Cmp = less < T >>
                                                                                                                  struct RMQ {
                                                                                                                         const Cmp cmp = Cmp();
                                                                                                                         static constexpr unsigned B = 64; using u64 = unsigned long long;
      void createVersion(int ori ver)
             rt.push_back(copy(rt[ori_ver]));
                                                                                                                         vector<vector<T>> a;
      void reserve(int n, int q) {
   nd.reserve(n + q * (2 * __lg(n) + 1));
   rt.reserve(q + 1);
                                                                                                                         vector < Vector < 1>> a,
vector < T> pre, suf, ini;
vector < u64> stk;
                                                                                                                         RMQ() {}
RMQ(const vector<T> &v) { init(v); }
void init(const vector<T> &v) {
       void resize(int n) {
             rt.resize(n);
                                                                                                                               n = v.size();
pre = suf = ini = v;
      }
                                                                                                                                stk.resize(n);
struct Info {
   int sum = 0;
                                                                                                                               if (!n) {
                                                                                                                                      return:
Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
                                                                                                                                const int M = (n - 1) / B + 1;
                                                                                                                               const int W = (N - 1) / B + 1;
const int Ug = __lg(M);
a.assign(lg + 1, vector < T > (M));
for (int i = 0; i < M; i++) {
    a[0][i] = v[i * B];
    for (int j = 1; j < B && i * B + j < n; j++) {
        a[0][i] = min(a[0][i], v[i * B + j], cmp);
}</pre>
3.6 Treap [d41d8c]
struct Treap {
      ict Treap {
   Treap *lc, *rc;
   int pri, siz; bool rev_valid;
   int val; int min;
   Treap(int val_) {
      min = val = val_;
      pri = rand();
      le = re = rand();
      le = re = rand();
}
                                                                                                                               for (int i = 1; i < n; i++) {
    if (i % B) {</pre>
                                                                                                                                             pre[i] = min(pre[i], pre[i - 1], cmp);
              lc = rc = nullptr;
              siz = 1; rev_valid = 0;
```

for (int i = n - 2; i >= 0; i--) {

```
if (i % B != B - 1) {
             suf[i] = min(suf[i], suf[i + 1], cmp);
    ] = min(a[j][i], a[j][i + (1 << j)], cmp);
    for (int i = 0; i < M; i++) {
    const int l = i * B;
    const int r = min(1U * n, l + B);</pre>
        tent :
u64 s = 0;
for (int j = l; j < r; j++) {
    while (s && cmp(v[j], v[__lg(s) + l])) {
        s ^= 1ULL << __lg(s);
}</pre>
             s |= 1ULL << (j - l);
             stk[j] = s;
        }
    }
int k = __lg(r - l);
ans = min
                  ({ans, a[k][l], a[k][r - (1 << k)]}, cmp);
         return ans;
    } else {
        int x = B * (l / B);
         return ini
              [__builtin_ctzll(stk[r - 1] >> (l - x)) + l];
    }
```

3.8 Mo [d41d8c]

```
struct query {
    int l, r, id;
};
void Mo(vector<query> &q) {
    int block = sqrt(q.size());
    sort(q.begin
            (), q.end(), [&](const query &a, const query &b) {
         int x = a.l / block;
        int y = b.l / block;
        if (x != y) return x < y;
        return a.r < b.r;
    });
}</pre>
```

4 Flow Matching

4.1 Dinic [d41d8c]

```
template < class T>
struct Dinic {
      struct Edge {
            int to;
            T flow, cap; // 流量跟容量
      int n, m, s, t;
const T INF_FloW = 1 << 30;
      vector<vector<int>> adj; // 此點對應的 edges 編號
      vector <Edge> edges; // 幫每個 edge 編號
vector <int> dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_) {
            n = n_; m = 0;
dis.resize(n); ptr.resize(n);
adj.assign(n, {});
             edges.clear();
      void add_edge(int u, int v, T cap) {
             // 偶數 id 是正向邊
             edges.push_back({v, 0, cap});
             edges.push_back({u, 0, 0});
adj[u].push_back(m++);
adj[v].push_back(m++);
      bool bfs() {
             fill(dis.begin(), dis.end(), -1);
dis[s] = 0; queue<int> q;
             q.push(s);
             while (!q.empty() && dis[t] == -1) {
   int u = q.front(); q.pop();
                   for (int id : adj[u]) {
   Edge &e = edges[id];
   if (e.flow == e.cap) continue;
   if (dis[e.to] == -1) {
        dis[e.to] = dis[u] + 1;
   }
}
                                 q.push(e.to);
                   }
```

4.2 Min Cut [d41d8c]

```
' CSES Police Chase
  int main(){
         int n, m; cin >> n >> m;
Dinic < int >> g(n);
for (int i = 0; i < m; i++) {
    int u, v, cap = 1;
    cin >> u >> v;
                 g.add_edge(u, v, cap);
                 g.add_edge(v, u, cap);
          int res = g.work(0, n - 1);
          cout << res << "\n";
if (res == 0) return;</pre>
          vector < int > vis(n);
auto find = [&](auto self, int u) -> void {
                 if (!vis[u]) {
                          vis[u]
                          for (int id : g.adj[u])
                                 auto e = g.edges[id];
if (e.cap - e.flow > 0) {
                                         self(self, e.to);
                         }
                }
         };
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
        auto e = g.edges[id];
        if (!vis[e.to]) {
            cout << i + 1 <<</pre>
                                  cout << i + 1 << " " << e.to + 1 << "\n";
                 }
         }
}
```

4.3 MCMF [d41d8c]

```
template < class Tf, class Tc>
struct MCMF {
    struct Edge {
        int to;
        Tf flow, cap; // 流量跟容量
        Tc cost;
    };
    int n, m, s, t;
    const Tf INF_FLOW = 1 << 30;
    const Tc INF_COST = 1 << 30;
    vector < vector < int>> adj;
    vector < Edge > edges; // 幫每個 edge 編號
    vector <Tc > dis, pot; // johnson algorithm, using spfa
    vector <int>> rt; // 路徑恢復,對應 id
    vector <bool> inq;
    MCMF(int n_ = 0) { init(n_); }
    void init(int n_) {
        n = n_; m = 0;
        edges.clear();
        adj.assign(n, {});
}
```

```
void add_edge(int u, int v, Tf cap, Tc cost){
  edges.push_back({v, 0, cap, cost});
  edges.push_back({u, 0, 0, -cost});
                                 adj[u].push_back(m++);
adj[v].push_back(m++);
                 bool spfa() {
    dis.assign(n, INF_COST);
    rt.assign(n, -1); inq.assign(n, false);
    queue<int> q;
    q.push(s), dis[s] = 0, inq[s] = true;
    rt.assign(n, -1);
    rt.assign(n, -1);

                                  while (!q.empty()) {
                                               le (!q.empty()) {
  int u = q.front(); q.pop();
  inq[u] = false;
  for (int id : adj[u]) {
    auto [v, flow, cap, cost] = edges[id];
    Tc ndis = dis[u] + cost + pot[u] - pot[v];
    if (flow < cap && dis[v] > ndis) {
        dis[v] = ndis; rt[v] = id;
        if (!inq[v]) {
            q.push(v); inq[v] = true;
        }
}
                                                                }
                                               }
                                  return dis[t] != INF_COST;
                   bool dijkstra() {
                                  dis.assign(n, INF_COST); rt.assign(n, -1);
                                 priority_queue<pair<Tc, int>,
    vector<pair<Tc, int>>, greater<pair<Tc, int>>> pq;
dis[s] = 0; pq.emplace(dis[s], s);
                               pq.emplace(ndis, v);
                                               }
                                  return dis[t] != INF_COST;
                 }
// 限定 flow, 最小化 cost
pairxTf, Tc> work_flow(int s_, int t_, Tf need) {
    s = s_, t = t_; pot.assign(n, 0);
    Tf flow{}; Tc cost{}; bool fr = true;
    while ((fr ? spfa() : dijkstra())) {
        for (int i = 0; i < n; i++) {
            dis[i] += pot[i] - pot[s];
    }
                                                 If f = INF_FLOW;
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                                                                 (f, edges[rt[i]].cap - edges[rt[i]].flow);
                                                 f = min<Tf>(f, need);
                                                 for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
                                                 flow += f; need -= f;
cost += f * dis[t]; fr = false;
                                                 swap(dis, pot);
if (need == 0) break;
                                  return {flow. cost}:
                   // 限定 cost, 最大化 flow
                 // 限定 cost, 最大化 flow
pair<Tf, Tc> work_budget(int s_, int t_, Tc budget) {
    s = s_, t = t_; pot.assign(n, 0);
    Tf flow{}; Tc cost{}; bool fr = true;
    while ((fr ? spfa() : dijkstra())) {
        for (int i = 0; i < n; i++) {
            dis[i] += pot[i] - pot[s];
    }
                                                 Tf f = INF_FLOW;
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
                                                                f = min
                                                                                   (f. edges[rt[i]].cap - edges[rt[i]].flow):
                                                 f = min<Tf>(f, budget / dis[t]);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
                                                 flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
                                                 swap(dis, pot);
if (budget == 0 || f == 0) break;
                                  return {flow, cost};
                   void reset() {
                                  for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
};
```

4.4 Hungarian [d41d8c]

```
struct Hungarian { // 0-based, O(VE)
        int n, m;
vector<vector<int>> adj;
        vector <int> used, vis;
vector <pair <int, int> match;
Hungarian(int n = 0, int m = 0) {
               init(n_, m_);
        void init(int n_, int m_) {
    n = n_; m = m_;
              adj.assign(n + m, {});
used.assign(n + m, -1)
vis.assign(n + m, 0);
        void addEdge(int u, int v) {
   adj[u].push_back(n + v);
   adj[n + v].push_back(u);
        bool dfs(int u)
               int sz = adj[u].size();
              for (int i = 0; i < sz; i++) {
   int v = adj[u][i];</pre>
                      if (vis[v] == 0) {
    vis[v] = 1;
                            if (used[v] == -1 || dfs(used[v])) {
    used[v] = u;
    return true;
                            }
                     }
               return false;
        vector<pair<int, int>> work() {
              match.clear(); used.assign(n + m, -1);
vis.assign(n + m, 0);
for (int i = 0; i < n; i++) {</pre>
                      fill(vis.begin(), vis.end(), 0); dfs(i);
               for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
                            match.emplace_back(used[i], i - n);
                     }
               return match;
       }
};
```

4.5 Theorem [d41d8c]

```
// 有向無環圖:
| // 最小不相交路徑覆蓋:
// 最小路徑數 = 頂點數 - 最大匹配數
// 最小相交路徑覆蓋:
// 先用
   Floyd 求傳遞封包,有連邊就建邊,然後再套最小不相交路徑覆蓋
// 二分圖:
// 最小點
   覆蓋:選出一些點,讓所有邊至少有一個端點在點集中的最少數量
// 最小點覆蓋 = 最大匹配數
// 還原解, flow 的作法是從源點開始 dfs, 只走 cap - flow > 0
// 的邊,最後挑選左邊還沒被跑過的點和右邊被跑過的點當作覆蓋的點
// 最少邊覆蓋: 選出一些邊,讓所有點都覆蓋到的最少數量
// 最少邊覆蓋 = 點數 - 最大匹配數
1// 最大獨立集: 選出一些點, 使這些點兩兩沒有邊連接的最大數量
// 最大獨立集 = 點數 - 最大匹配數
```

5 String

5.1 Hash [852711]

```
constexpr int B = 59;
vector < Z> Hash(string &s) {
    vector < Z> ans {0};
    for (auto c : s) {
        ans.push_back(ans.back() * B + (c - 'a' + 1));
    }
    return ans;
}
void solve() {
    string s, sub;
    cin >> s >> sub;
    auto a = Hash(s);
    auto q = Hash(sub);
    auto find = q.back();
    int ans = 0;
    int l = 1, r = sub.size(), len = sub.size();
    while (r <= s.size()) {
        if (a[r] - a[l - 1] * power(Z(B), len) == find) {
            ans++;
        }
}</pre>
```

void reset() {

tot = 0, fill_n(trie[0], 26, 0);

```
l++. r++:
                                                                                          int newNode() {
                                                                                               int x = ++tot;
cnt[x] = 0, fill_n(trie[x], 26, 0);
      cout << ans << "\n";
}
5.2 KMP [3a8e3d]
                                                                                          void add(string &s) {
struct KMP {
                                                                                                int p = 0;
for (auto c : s) {
      string sub:
                                                                                                     int &q = trie[p][c - 'a'];
      vector<int> fail;
                                                                                                     if (!q) q = newNode();
      // fail 存匹配失敗時,移去哪,也就是最長共同前後綴長度
      KMP() {}
      KMP(const string &sub_) {
                                                                                                cnt[p] += 1;
           build(sub_);
      fvector <int> build(const string &sub_) {
    sub = sub_, fail.resize(sub.size(), -1);
    for (int i = 1; i < sub.size(); i++) {
        int now = fail[i - 1];
        while (now != -1 && sub[now + 1] != sub[i]) {
            now = fail[now];
        }
}</pre>
                                                                                          int find(string &s) {
                                                                                               int p = 0;
for (auto c : s) {
   int q = trie[p][c - 'a'];
   int q = trie[p][c - 'a'];
                                                                                                     if (!q) return 0;
                                                                                                     D = 0:
                                                                                                return cnt[p];
                 if (sub[now + 1] == sub[i]) {
    fail[i] = now + 1;
                                                                                          5.6 SA [b58946]
            return fail:
                                                                                          struct SuffixArray {
                                                                                                int n; string s;
vector<int> sa, rk, lc;
      vector<int> match(string &s) {
           rector < int > match;

for (int i = 0, now = -1; i < s.size(); i++) {
    // now 是成功匹配的長度 -1
    while (s[i] != sub[now + 1] && now != -1)
        now = fail[now];
                                                                                                // n: 字串長度
                                                                                                // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
                                                                                                // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
                                                                                                // lc: LCP
                 if (s[i] == sub[now + 1]) now++;
if (now + 1 == sub.size()) {
   match.push_back(i - now);
                                                                                                      數組,lc[i] 表示 sa[i] 和 sa[i+1] 的最長公共前綴長度
                                                                                                {\tt SuffixArray(const\ string\ \&s\_)\ \{}
                                                                                                    s = s_; n = s.length();
sa.resize(n);
                      now = fail[now];
                }
                                                                                                     lc.resize(n
                                                                                                     rk.resize(n):
            return match;
                                                                                                     iota(sa.begin(), sa.end(), 0);
                                                                                                    lota(sa.beg(in(), sa.ein(), %),

sort(sa.beg(in(), sa.

end(), [&](int a, int b) { return s[a] < s[b]; });

rk[sa[0]] = 0;

for (int i = 1; i < n; i++)
     }
};
5.3 Z Function [764b31]
                                                                                                     = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
int k = 1;
|// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
 // 的最長公共前綴 (LCP) 的長度
 vector < int > Z(string s) {
   int n = s.size();
                                                                                                     vector<int> tmp, cnt(n);
                                                                                                     tmp.reserve(n);
while (rk[sa[n - 1]] < n - 1) {</pre>
      vector < int > z(n); z[0] = n;
      for (int i = 1, j = 1; i < n; i++) {
    z[i] = max(0, min(j + z[j] - i, z[i - j]));
    while (i + z[i] < n && s[z[i]] == s[i + z[i]])
                                                                                                          tmp.clear();
for (int i = 0; i < k; i++)
    tmp.push_back(n - k + i);</pre>
                                                                                                          for (auto i : sa)
if (i >= k)
           if (i + z[i] > j + z[j]) j = i;
                                                                                                                     tmp.push_back(i - k);
                                                                                                          fill(cnt.begin(), cnt.end(), 0);

for (int i = 0; i < n; i++)
      return z; // 最後一格不算
                                                                                                          5.4 Manacher [9c9ca6]
 // 找到對於每個位置的迴文半徑
                                                                                                                sa[--cnt[rk[tmp[i]]]] = tmp[i];
 vector<int> manacher(string s) {
                                                                                                          string t = "#";
      for (auto c : s) {
           t += c;
t += '#';
      int n = t.size();
      vector<int> r(n);
      for (int i = 0, j =
                                                                                                     for (int i = 0, j = 0; i < n; i++) {
   if (rk[i] == 0) {</pre>
           0; i < n; i++) { // i 是中心, j 是最長回文字串中心 if (2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
                                                                                                          } else {
                                                                                                                for (j -=
            while (i - r[i] >=
    0 && i + r[i] < n && t[i - r[i]] == t[i + r[i]]) {
    r[i] += 1;</pre>
                                                                                                                      j > 0; i + j < n && sa[rk[i] - 1] + j < n
                                                                                                                && s[i + j] == s[sa[rk[i] - 1] + j]; j++);
lc[rk[i] - 1] = j;
            if (i + r[i] > j + r[j]) {
                 j = i;
                                                                                               }
           }
      return r;
// # a # b # a #
// 1 2 1 4 1 2 1
                                                                                          5.7 SAM [b09888]
                                                                                          struct SAM {
   // 1 -> initial state
   static constexpr int ALPHABET_SIZE = 26;
      .
// # a # b # b # a #
      // 1 2 1 2 5 2 1 2 1
      // 值 -1 代表原回文字串長度
                                                                                                struct Node {
      // (id - val + 1) / 2 可得原字串回文開頭
                                                                                                     int len;
int link;
                                                                                                     array<int, ALPHABET_SIZE> next;
 5.5 Trie [31e4ff]
                                                                                                     Node() : len{}, link{}, next{} {}
 constexpr int N = 1E7;
                                                                                                vector<Node> t;
 int tot = 0:
                                                                                                SAM() {
 int trie[N][26], cnt[N];
```

init():

void init() {

```
t.assign(2, Node());
t[0].next.fill(1);
             t[0].len = -1;
      int newNode() {
             t.emplace_back();
             return t.size() - 1;
      int extend(int p, int c) {
    if (t[p].next[c]) {
                   int q = t[p].next[c];
if (t[q].len == t[p].len + 1) {
                          return q;
                    int r = newNode();
                   t[r].len = t[p].len + 1;
t[r].link = t[q].link;
t[r].next = t[q].next;
                    t[q].link = r;
                   while (t[p].next[c] == q) {
    t[p].next[c] = r;
    p = t[p].link;
                   return r:
             int cur = newNode();
             t[cur].len = t[p].len + 1;
while (!t[p].next[c]) {
                   t[p].next[c] = cur;
                   p = t[p].link;
             t[cur].link = extend(p, c);
             return cur;
     }
void solve() {
      string s; cin >> s;
int n = s.length();
      vector < int > last(n + 1); // s[i - 1] 的後綴終點位置
      last[0] = 1;
      SAM sam;
for (int i = 0; i < n; i++) {
    last[i + 1] = sam.extend(last[i], s[i] - 'a');</pre>
      int sz = sam.t.size();
vector < int > cnt(sz);
for (int i = 1; i <= n; i++) {</pre>
            cnt[last[i]]++; // 去重 = 1
      vector < vector < int >> order(sz);
for (int i = 1; i < sz; i++) {
    order[sam.t[i].len].push_back(i);
}</pre>
      for (int i = sz - 1; i > 0; i--) {
    for (int u : order[i]) {
        if (sam.t[u].link != -1) {
            cnt[sam.t[u].link] += cnt[u];
        }
}
            }
      vector<ll> dp(sz. -1):
      auto dfs = [&](auto self, int u) -> void {
             dp[u] = cnt[u];
             for (int c = 0; c < SAM::ALPHABET_SIZE; c++) {
  int v = sam.t[u].next[c];</pre>
                   if (v) {
   if (dp[v] == -1) self(self, v);
   dp[u] += dp[v];
            }
      dfs(dfs, 1);
```

5.8 Palindrome Tree [f10e9d]

```
struct PAM {
   // 0 -> even root, 1 -> odd root
   static constexpr int ALPHABET_SIZE = 26;
   struct Node {
            int fail;
            array<int, ALPHABET_SIZE> next;
Node() : len{}, fail{}, next{} {}
      vector < int > s;
vector < Node > t;
      PAM() {
            init();
      void init() {
           t.assign(2, Node());
            s.clear():
            t[0].len = 0;
            t[1].len = -1;
            t[0].fail = 1;
      int newNode() {
            t.emplace_back();
            return t.size() - 1;
      int extend(int p, int c) {
```

```
int n = s.size():
             s.push_back(c);
while (s[n - t[p].len - 1] != c) {
    p = t[p].fail;
             if (!t[p].next[c]) {
                   int r = newNode();
t[r].len = t[p].len + 2;
int cur = t[p].fail;
while (s[n - t[cur].len - 1] != c) {
    cur = t[cur].fail;
                   t[r].fail = t[cur].next[c];
t[p].next[c] = r;
             p = t[p].next[c];
             return p;
      }
void solve() {
      string s; cin >> s;
int n = s.length();
      vector<int> last(n + 1);
      last[0] = 1;
PAM pam;
      for (int i = 0; i < n; i++) {
    last[i + 1] = pam.extend(last[i], s[i] - 'a');</pre>
       int sz = pam.t.size();
      vector < int > cnt(sz);
for (int i = 1; i <= n; i++) {</pre>
             cnt[last[i]]++; // 去重 = 1
      for (int i = sz - 1; i > 1; i--) {
    cnt[pam.t[i].fail] += cnt[i];
```

5.9 Duval [f9dcca]

```
|// duval_algorithm
 // 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
 vector<string> duval(string s) {
       int i = 0, n = s.size();
vector<string> res;
       vector<string> ies,
while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
   }</pre>
                    else k++;
              while (i <= k) {</pre>
                    res.push_back(s.substr(i, j - k));
                    i += i - k:
       return res:
 }
 // 最小旋轉字串
 string min_round(string s) {
       s += s;
int i = 0, n = s.size();
       int start = i;
while (i < n / 2) {</pre>
             start = i;
int k = i, j = i + 1;
while (s[k] <= s[j] && j < n) {
    if (s[k] < s[j]) k = i;</pre>
                    else k++:
                   j++;
             while (i <= k) {
    i += j - k;</pre>
       return s.substr(start, n / 2);
```

6 Math

6.1 Modulo [a55187]

```
template < class T >
constexpr T power(T a, ll b) {
    T res {1};
    for (; b; b /= 2, a *= a)
        if (b % 2) res *= a;
    return res;
}
constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
    res %= p;
    if (res < 0) res += p;
    return res;
}
template < ll P >
struct MInt {
    ll x;
    constexpr MInt() : x {0} {}
constexpr MInt(ll x) : x {norm(x % getMod())} {}
}
```

```
static ll Mod:
     constexpr static ll getMod() {
         return P > 0 ? P : Mod;
     constexpr static void setMod(ll Mod_) {
         Mod = Mod_;
     constexpr ll norm(ll x) const {
         if (x < 0) x += getMod();
if (x >= getMod()) x -= getMod();
          return x:
     constexpr MInt operator -() const {
    return MInt(norm(getMod() - x));
     constexpr MInt inv() const {
   return power(*this, getMod() - 2);
     constexpr MInt &operator*=(MInt rhs) & {
   if (getMod() < (1ULL << 31)) {</pre>
              x = x * rhs.x % int(getMod());
          } else {
              x = mul(x, rhs.x, getMod());
          return *this:
     constexpr MInt &operator+=(MInt rhs) & {
          x = norm(x + rhs.x);
          return *this;
     constexpr MInt &operator -= (MInt rhs) & {
          x = norm(x - rhs.x);
return *this;
     constexpr MInt &operator/=(MInt rhs) & {
          return *this *= rhs.inv();
     friend constexpr MInt operator*(MInt lhs, MInt rhs) {
          return lhs *= rhs;
     friend constexpr MInt operator+(MInt lhs. MInt rhs) {
          return lhs += rhs;
     friend constexpr MInt operator (MInt lhs, MInt rhs) {
          return lhs -= rhs;
     friend constexpr MInt operator/(MInt lhs, MInt rhs) {
   return lhs /= rhs;
     friend istream &operator>>(istream &is, MInt &a) {
    ll v; is >> v; a = MInt(v); return is;
     friend ostream &operator<<(ostream &os, const MInt &a) {</pre>
          return os << a.x;
     friend constexpr bool operator==(MInt lhs, MInt rhs) {
   return lhs.x == rhs.x;
     friend constexpr bool operator!=(MInt lhs, MInt rhs) {
   return lhs.x != rhs.x;
     friend constexpr bool operator<(MInt lhs, MInt rhs) {</pre>
         return lhs.x < rhs.x;</pre>
    }
template<>
ll MInt<0>::Mod = 998244353;
constexpr ll P = 1E9 + 7;
using Z = MInt<P>;
6.2 Combination [6aa734]
struct Comb {
```

```
set Comb {
    ll n; vector < Z > _fac , _invfac , _inv;
    Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
    comb(ll n) : Comb() { init(n); }
    void init(ll m) {
        m = min(m, Z::getMod() - 1);
        if (m <= n) return;
        _fac.resize(m + 1);
        invfac.resize(m + 1);
        inv.resize(m + 1);
    }
}</pre>
              _inv.resize(m + 1);
for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;
              for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
}
               n = m:
}
Z fac(ll m) {
   if (m > n) init(2 * m);
        fac[m];
}
Z invfac(ll m) {
    if (m > n) init(2 * m);
    return _invfac[m];
 Z inv(ll m) {
   if (m > n) init(2 * m);
```

```
return _inv[m];
       Z binom(ll n, ll m) {
   if (n < m || m < 0) return 0;
   return fac(n) * invfac(m) * invfac(n - m);</pre>
        Z lucas(ll n, ll m) { // Mod 要在 1E5 左右
              if (m == 0) return 1;
return binom(n % Z::getMod(), m % Z::getMod())
* lucas(n / Z::getMod(), m / Z::getMod());
[] comb; // 注意宣告, 若要換模數需重新宣告
```

6.3 Sieve [37ae54]

```
vector < int > primes , minp;
void sieve(int n) {
   minp.assign(n + 1, 0);
          primes.clear();
          for (int i = 2; i <= n; i++) {
    if (minp[i] == 0) {
        minp[i] = i;
    }
                             primes.push_back(i);
                   for (auto p : primes) {
    if (i * p > n) break;
    minp[i * p] = p;
    if (p == minp[i]) break;
         }
}
// a ^ (m-1) = 1 (Mod m)
// a ^ (m-2) = 1/a (Mod m)
// Exp2: cout << power(x, power(y, p, Mod - 1), Mod)
// Num = (x+1) * (y+1) * (z+1)...
// Sum = (a^0 + a^1+...+ a^x) * (b^0 +...+ b^y)</pre>
// Mul = N * (x+1) * (y+1) * (z+1) / 2
```

6.4 MillerRabinPollardRho [b9e5be]

```
constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
        res %= p;
if (res < 0) res += p;
        return res;
template < class T>
constexpr T power(T a, ll b, ll p) {
   T res {1};
        for (; b; b /= 2, a = mul(a, a, p))
    if (b % 2) res = mul(res, a, p);
        return res;
vector<ll
> chk {2, 325, 9375, 28178, 450775, 9780504, 1795265022};
bool check(ll a, ll d, int s, ll n) {
    a = power(a, d, n);
       a = power(a, u, n),
if (a <= 1) return 1;
for (int i = 0; i < s; ++i, a = mul(a, a, n)) {
   if (a == 1) return 0;
   if (a == n - 1) return 1;</pre>
       return 0;
bool IsPrime(ll n) {
       if (n < 2) return 0;
if (n % 2 == 0) return n == 2;
ll d = n - 1, s = 0;
while (d % 2 == 0) d >>= 1, ++s;
for (ll i : chk) if (!check(i, d, s, n)) return 0;
const vector<ll> small = {2, 3, 5, 7, 11, 13, 17, 19};
ll FindFactor(ll n) {
    if (IsPrime(n)) return 1;
    for (ll p : small) if (n % p == 0) return p;
    ll x, y = 2, d, t = 1;
    auto f = [&](ll a) {
               return (mul(a, a, n) + t) % n;
        for (int l = 2: : l <<= 1) {
               x = y;
int m = min(l, 32);
'-- i - 0: i <
               for (int i = 0; i < l; i += m) {
    d = 1;</pre>
                       for (int j = 0; j < m; ++j) {
    y = f(y), d = mul(d, abs(x - y), n);
}</pre>
                      if (g == n) {
    l = 1, y = 2, ++t;
    break;
                       if (g != 1) return g;
               }
      }
map<ll,
              int> res:
void PollardRho(ll n) {
      if (n == 1) return;
```

if (IsPrime(n)) return ++res[n], void(0);

```
ll d = FindFactor(n);
      PollardRho(n / d), PollardRho(d);
}
6.5 CRT [d41d8c]
ll exgcd(ll a, ll b, ll &x, ll &y) {
     if (!b) {
           x = 1, y = 0;
           return a;
     \hat{l}lg = exgcd(b, a % b, y, x);
     y -= a / b * x;
      return g;
}
ll inv(ll x, ll m){
     ll a, b;
     exgcd(x, m, a, b);
     a %= m;
if (a < 0) a += m;
// remain, mod
ll CRT(vector spair < ll, ll >> &a){
    ll prod = 1;
    for (auto x : a) {
        prod *= x.second;
}
      ĺl res = 0;
     for (auto x : a) {
   auto t = prod / x.second;
   res += x.first * t % prod * inv(t, x.second) % prod;
           if(res >= prod) res -= prod;
      return res:
}
```

6.6 Matrix [bec759]

```
template < class T>
struct Matrix {
     int n, m;
vector<vector<T>> mat;
      constexpr Matrix(int n_, int m_) { init(n_, m_); }
     constexpr Matrix(vector<vector<T>> mat_) { init(mat_); }
     constexpr void init(int n_, int m_) {
    n = n_; m = m_;
           mat.assign(n, vector<T>(m));
     constexpr void init(vector<vector<T>> mat_) {
           n = mat_.size();
m = mat_[0].size();
           mat = mat_;
     constexpr Matrix &operator*=(const Matrix &rhs) & {
           assert(mat[0].size() == rhs.mat.size());
          .slze(), k = nector.

Matrix res(n, m);

for (int i = 0; i < n; i++) {
    for (int j = 0; j < m; j++) {
        for (int l = 0; l < k; l++) {
            res.mat[i][j] += mat[i][l] * rhs.mat[l][j];
        }
                  .size(), k = mat[0].size(), m = rhs.mat[0].size();
                }
           mat = res.mat;
           return *this:
           Matrix operator*(Matrix lhs, const Matrix &rhs) {
return lhs *= rhs;
     }
template < class T>
constexpr Matrix<T> unit(int n) {
     Matrix < T > res(n, n);
for (int i = 0; i < n; i++) {
   res.mat[i][i] = 1;</pre>
     return res;
constexpr Matrix<T> power(Matrix<T> a, ll b) {
   assert(a.n == a.m);
     Matrix<T> res = unit<T>(a.n);
     for (; b; b /= 2, a *= a)
if (b % 2) res *= a;
     return res;
```

6.7 Mex [4e24ed]

```
template < class T >
int mex(vector < T > &v) {
    unordered_set < T > s;
    for (auto e : v) s.insert(e);
    for (T i = 0; ; i++) {
        if (s.find(i) == s.end()) return i;
    }
}
```

6.8 Game Theorem

- sg 值為 0 代表先手必敗
- 當前 sg 值 = 可能的後繼狀態的 mex (例如拿一個或拿兩個, 就等於兩者的 sg 值 mex), 若有互相依賴就兩個後繼狀態 xor 當作一組 sg 值 (例如切開成 兩半, 只算一次)
- 單組基礎 nim 的 sg 值為本身的原因: f(0)=0, f(1)=mex(f(0))=1, f(2)=mex(f(0),f(1))=2...,都是自己 • 多組賽局可以把 sg 值 xor 起來,當成最後的 sg 值,nim 也是一樣,且由於
- 多組賽局可以把 sg 值 xor 起來,當成最後的 sg 值, nim 也是一樣,且由於 xor 性質,如果可以快速知道 sg(1)g(2)...g(n),就可以用 xor 性質處理不連 續組合

6.9 Integer Partition [595ed2]

6.10 Mobius Theorem

- 數論 分塊 可以快速 計算 一些 含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理 出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n}\!\!\mu(d)\!=\!\begin{cases} 1 & \text{for } n\!=\!1\\ 0 & \text{for } n\!\neq\!0 \end{cases}$$

- 2. μ是常數函數1的反元素
 - $\Rightarrow \mu * 1 = \epsilon$, $\epsilon(n)$ 只在n = 1時為 1 , 其餘情況皆為 0 。
- $-\phi$ 歐拉函數: x以下與x互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^{i}) \\ &= 1 + p^{0}(p-1) + p^{1}(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^{c} \\ &= id \end{split}$$

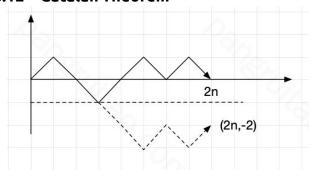
- 莫比烏斯反演公式
 - $f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$
 - $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$
- 例子

$$\begin{split} &\sum_{i=aj=c}^{b} \sum_{j=1}^{a} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{i=1}^{\infty} \sum_{j=1}^{i} \sum_{d \mid gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{d=1}^{\min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \\ &= \sum_{d=1}^{\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.11 Mobius Inverse [d41d8c]

```
const int maxn = 2e5;
ll mobius_pref[maxn];
void init() {
     mobius_pref[1] = 1;
vector<ll> wei
     (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
                 mobius_pref[i] = mobius_pref[i - 1];
                 continue; // 包含平方
           if (wei[i] == 0) {
                 wei[i] == 0; {
wei[i] = 1;
for (ll j = 2; i * j < maxn; j++) {
    if (j % i == 0) wei[i * j] = -1;
    else if (wei[i * j] != -1) wei[i * j]++;</pre>
           mobius_pref[i]
                  = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
     }
void solve() {
     ll a, b, c, d, k; cin >> a >> b >> c >> d >> k;
auto cal = [&](ll x, ll y) -> int {
           return res;
     cout << cal
            (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k,
(c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n"
}
```

6.12 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有 x 個,往下有 y 個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.13 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- · X/G:本質不同的方案的集合
- X^g : 對於某一種操作 g,所有方案中,經過 g 這種翻轉後保持不變的方案的集合
- 集合取絕對值代表集合數

7 Search and Gready

7.1 Binary Search [d41d8c]

```
if (check(m)) hi = x;
else lo = x + 1;
}
cout << lo; // 保證有解
while (lo <= hi) {
   int x = (lo + hi) / 2;
   if (check(m)) hi = x - 1;
   else lo = x + 1;
}
cout << lo; // 範圍外代表無解
```

7.2 Ternary Search [d41d8c]

```
int main() {
   int lo = 0, hi = 10;
   while (lo <= hi) {
      int xl = lo + (hi - lo) / 3;
      int xr = hi - (hi - lo) / 3;
      int ansl = check(xl), ansr = check(xr);
      if (ansl < ansr) {
            lo = xl + 1;
      } else {
            hi = xr - 1;
      }
      // record ans and index
   }
}</pre>
```

8 Tree

8.1 Binary Lifting LCA [57457f]

```
const int Q = 20; // log(q) or log(n)
vector<vector<int>> par;
vector <int> par,
vector <int> dep, dfn;
void build(int n, vector <vector <int>> &tree, int u = 0) {
   par.assign(n, vector <int>(Q + 1, -1));
   dep.assign(n, 0), dfn.assign(n, 0);
}
      int cur = 0;
      auto dfs = [&](auto self, int x, int p) -> void {
           dfn[x] = cur++;
for (auto y : tree[x]) {
    if (y == p) continue;
                 par[y][0] = x;
dep[y] = dep[x] + 1;
self(self, y, x);
           }
      par[u][0] = u;
     par[j][i] = u;
dfs(dfs, 0, -1);
for (int i = 1; i <= Q; i++) {
    for (int j = 0; j < n; j++) {
        par[j][i] = par[par[j][i - 1]][i - 1];
}</pre>
     }
a = par[a][i];
     a = par[a][i], b = par[b][i];
      return par[a][0];
int jump(int x, int k) {
      return x;
```

8.2 Centroid Decomposition [ec760b]

```
#include <bits/stdc++.h>
using namespace std;
struct CenDecom {
   int n;
   vector<vector<int>> adj;
   vector<bool> vis;
   vector<int>> siz;
   CenDecom(int n_ = 0) { init(n_); }
   void init(int n_) {
        n = n_;
        adj.assign(n, {});
        vis.assign(n, false);
        siz.assign(n, 1);
   }
   void addEdge(int u, int v) {
        adj[u].push_back(v);
```

```
adj[v].push_back(u);
         void get_siz(int x, int p = -1) {
                 siz[x] = 1;
for (int y : adj[x]) {
                        if (y == p || vis[y]) continue;
get_siz(y, x);
siz[x] += siz[y];
        int get_cen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz) {
                                 return get_cen(y, sz, x);
                 return x;
         void get_ans(int x, int p) {
                 fget_ans(y, x);
// do something
for (int y : adj[x]) {
    if (y == p || vis[y]) continue;
    get_ans(y, x);
       }
void work(int x = 0) {
    get_siz(0, x);
    int cen = get_cen(x, siz[x]);
    vis[cen] = true;
    for (int y : adj[cen]) {
        if (vis[y]) continue;
        cet_aps(v_cen);
}
                         get_ans(y, cen);
                 for (int y : adj[cen]) {
                         if (vis[y]) continue;
                         work(y);
        }
};
```

8.3 Heavy Light Decomposition [41d99e]

```
int n, cur;
vector <int> siz, top, dep, parent, in, out, seq;
vector <vector <int>> adj;
HLD(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_; cur = 0;
    siz.resize(n); top.resize(n); dep.resize(n);
       parent.resize(n); in.resize(n); out.resize(n);
seq.resize(n); adj.assign(n, {});
void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
void work(int rt = 0) {
      top[rt] = rt;
dep[rt] = 0;
       parent[rt] = -1;
       dfs1(rt); dfs2(rt);
void dfs1(int u) {
   if (parent[u] != -1)
      adj[u].erase(find
                      (adj[u].begin(), adj[u].end(), parent[u]));
       for (auto &v : adj[u]) {
    parent[v] = u, dep[v] = dep[u] + 1;
              dfs1(v);
siz[u] += siz[v];
if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
             } // 讓 adj[u][0] 是重子節點
       }
void dfs2(int u) {
       in[u] = cur++;
       seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
    top[v] = v == adj[u][0] ? top[u] : v;
       out[u] = cur;
fint lca(int u, int v) {
    while (top[u] != top[v]) {
        if (dep[top[u]] > dep[top[v]]) {
            u = parent[top[u]];
        } else {
                    v = parent[top[v]];
             }
       return dep[u] < dep[v] ? u : v;</pre>
int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
int jump(int u, int k) {
   if (dep[u] < k) return -1;</pre>
```

```
8.4 Link Cut Tree [0e9031]
template < class Info, class Tag>
struct LinkCutTree { // 1-based
    struct Node {
         Info info = Info();
         Tag tag = Tag();
bool rev = false;
int size = 0;
         int ch[2], p = 0;
     vector < Node > nd:
     LinkCutTree(int n = 0) { init(n); }
     void init(int n) {
         nd.clear():
         nd.emplace_back();
         resize(n);
     void resize(int n) {
     void make_rev(int t) {
    swap(nd[t].ch[0], nd[t].ch[1]);
    nd[t].rev ^= true;
     void apply(int t, const Tag &v) {
         nd[t].info.apply(nd[t].size, v);
nd[t].tag.apply(v);
     void push(int t) {
         if (nd[t].rev) {
    if (nd[t].ch[0]) make_rev(nd[t].ch[0]);
    if (nd[t].ch[1]) make_rev(nd[t].ch[1]);
    nd[t].rev = false;
         if (nd[t].ch[0]) apply(nd[t].ch[0], nd[t].tag);
if (nd[t].ch[1]) apply(nd[t].ch[1], nd[t].tag);
         nd[t].tag = Tag();
     void pull(int t) {
         nd[t].info
                .pull(nd[nd[t].ch[0]].info, nd[nd[t].ch[1]].info);
     int pos(int t)
          return nd[nd[t].p].ch[1] == t;
     void pushAll(int t) {
    if (!isrt(t)) {
        pushAll(nd[t].p);
}
         push(t);
     void rotate(int t) {
         nd[q].p = t;
         pull(q);
     void splay(int t) {
         pushAll(t);
while (!isrt(t)) {
    if (!isrt(nd[t].p)) {
                   if (pos(t) == pos(nd[t].p)) {
```

```
rotate(nd[t].p);
                       rotate(t);
                  }
              rotate(t);
         pull(t);
    nd[i].ch[1] = q;
              pull(i);
         splay(t);
     void makeRoot(int t) {
         access(t):
         make_rev(t);
    int findRoot(int t) {
         access(t);
         int x = t;
while (nd[x].ch[0]) {
             push(x);
              \dot{x} = \dot{n}d[\dot{x}].ch[0];
         access(x);
         return x;
    bool connected(int x, int y) {
    return findRoot(x) == findRoot(y);
    bool neighber(int x, int y) {
         makeRoot(x);
         access(y);
         if (nd[y].ch[0] != x || nd[x].ch[1]) return false;
         return true;
     void split(int rt, int y) {
         makeRoot(y);
         access(rt);
     void link(int x, int y) {
         makeRoot(x);
         if (findRoot(y) != x) {
             nd[x].p = y;
         }
     void cut(int x, int y) {
         makeRoot(x);
         access(y);
         nd[y].ch[0] = nd[nd[y].ch[0]].p = 0;
         pull(x);
         pull(v);
     void modify(int x, const Info &v) {
         access(x);
         nd[x].info = v;
    void path_apply(int x, int y, const Tag &v) {
   assert(connected(x, y));
         split(x, y);
         apply(x, v);
     Info path_query(int x, int y) {
         assert(connected(x, y));
         split(x, y);
         return nd[x].info;
constexpr int Mod = 51061;
constexpr the nod - struct Tag {
    ll add = 0; ll mul = 1;
    void apply(const Tag &v) {
        mul = mul * v.mul % Mod;
        add = (add * v.mul % Mod + v.add) % Mod;
}
void pull(const Info &l, const Info &r) {
   sum = (l.sum + r.sum + val) % Mod;
    }
}:
8.5 Virtual Tree [41e291]
```

```
|// 多次詢問給某些關鍵點,虚樹可達成快速樹 DP (前處理每個點)
// 例如這題是有權樹,給一些關鍵點,求跟 vertex 1 隔開的最小成本
// 前處理 root 到所有點的最小邊權
vector<int> stk;
void insert(int key, vector<vector<int>>> &vt) {
   if (stk.empty()) {
       stk.push_back(key);
   }
```

```
int l = lca(stk.back(), key);
      if (l == stk.back())
            stk.push_back(key);
            return:
      while (
           stk.size() > 1 && dfn[stk[stk.size() - 2]] > dfn[l]) {
vt[stk[stk.size() - 2]].push_back(stk.back());
            stk.pop_back();
      if (stk.size() < 2 || stk[stk.size() - 2] != l) {
   vt[l].push_back(stk.back());</pre>
           stk.back() = l;
      } else {
            vt[l].push_back(stk.back());
            stk.pop_back();
      stk.push_back(key);
int work(vector<vector<int>>> &vt) {
     while (stk.size() > 1) {
  vt[stk[stk.size() - 2]].push_back(stk.back());
           stk.pop_back();
      int rt = stk[0];
      stk.clear();
      return rt;
void solve() {
     int n; cin >> n;
vector<vector<int>>> g(n);
vector<vector<pair<int, int>>> wg(n);
vector<vector<int>>> vt(n);
      for (int i = 1; i < n; i++) {
            int u, v, w;
           cin >> u >> v >> w;
           g[u]. v, g[v]. push_back(v), g[v]. push_back(u); wg[u]. emplace_back(v, w), wg[v]. emplace_back(u, w);
      build(n. a): // build LCA
     vector <int> dis(n, 1E9); // root 到各點的最小邊權
auto dfs_dis = [&](auto &&self, int x, int p) -> void {
   for (auto [y, w] : wg[x]) {
      if (y == p) continue;
      dis[y] = min(w, dis[x]);
}
                  self(self, y, x);
           }
      dfs_dis(dfs_dis, 0, -1);
      vector < bool > iskey(n);
      vector<ll> dp(n);
      int q; cin >> q;
while (q--) {
           int m; cin >> m;
           tit m; cti >> m;
vector <int > key(m);
for (int i = 0; i < m; i++) {
    cin >> key[i];
    key[i] -= 1;
                  iskey[key[i]] = true;
           key.push_back(0); // 固定 0 為 root, 看題目需求
sort(key.begin(), key.end(), [&](int a, int b) {
return dfn[a] < dfn[b];
           }); // 要 sort 再 insert
            for (auto x : key) insert(x, vt);
           for (auto x . ..., work(vt);
auto dfs = [&](auto &&self, int x) -> void {
    for (auto y : vt[x]) {
        self(self, y);
        r // 直接砍了
                        if (iskey[y]) { // 直接砍了 dp[x] += dis[y];
                        } else { // 不砍 or 砍
                           iskey[y] = dp[y] = 0;
                 vt[x].clear(); // 記得 reset
           dfs(dfs, 0);
cout << dp[0] << "\n";</pre>
           dp[0] = 0; // 最後 reset root
8.6 Dominator Tree [0b03d9]
```

```
// dom
          存起點到達此點的必經的上個節點(起點 = 自己),無法到達 = -1
 struct Dominator_tree {
        int n, id;
        vector < vector < int >> adj, radj, bucket;
vector < int >> sdom, dom, vis, rev, pa, rt, mn, res;
Dominator_tree(int n_ = 0) { init(n_); }
void init(int n_) {
              n = n_, id = 0;
adj.assign(n, {});
radj.assign(n, {});
               bucket.assign(n, {});
```

ans.push_back(v[i]), L--;

```
sdom.resize(n), dom.assign(n, -1);
vis.assign(n, -1), rev.resize(n);
pa.resize(n), rt.resize(n);
                                                                                                                           }
                                                                                                                     mn.resize(n), res.resize(n);
                                                                                                                    for (auto i : ans) cout << i <<</pre>
        void add_edge(int u, int v) {    adj[u].push_back(v);    }
                                                                                                              9.3 Edit Distance [308023]
      int query(int v, int x) {
    if (rt[v] == v) return x ? -1 : v;
             int p = query(rt[v], 1);
if (p == -1) return x ? rt[v] : mn[v];
if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
                                                                                                              int main() {
                                                                                                                    string s1, s2; cin >> s1 >> s2;
int n1 = s1.size(), n2 = s2.size();
                                                                                                                     // dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元
             return x ? p : mn[v];
                                                                                                                     vector<int> dp(n2 + 1);
                                                                                                                    vector <int> dp(n2 + 1);
iota(dp.begin(), dp.end(), 0);
for (int i = 1; i <= n1; i++) {
    vector <int> cur(n2 + 1); cur[0] = i;
    for (int j = 1; j <= n2; j++) {
        if (s1[i - 1] == s2[j - 1]) {
            cur[j] = dp[j - 1];
        lelse {</pre>
      void dfs(int v) {
             rus(ut v) {
vis[v] = id, rev[id] = v;
rt[id] = mn[id] = sdom[id] = id, id++;
for (int u : adj[v]) {
    if (vis[u] == -1) dfs(u), pa[vis[u]] = vis[v];
                    radj[vis[u]].push_back(vis[v]);
                                                                                                                                  } else {
             }
                                                                                                                                       // s1 新增等價於 s2 砍掉
                                                                                                                                         // dp[i][j] = min(s2 新增, 修改, s1 新增);
       vector < int > build(int s) {
                                                                                                                                        cur[i]
             dfs(s);
for (int i = id - 1; i >= 0; i--) {
                                                                                                                                                 = min({cur[j - 1], dp[j - 1], dp[j]}) + 1;
                                                                                                                                 }
                    for (int u : radj[i])
                    sdom[i] = min(sdom[i], sdom[query(u, 0)]);
if (i) bucket[sdom[i]].push_back(i);
for (int u : bucket[i]) {
                                                                                                                           swap(dp, cur);
                                                                                                                    cout << dp[n2] << "\n";
                          int p = query(u, 0);
dom[u] = sdom[p] == i ? i : p;
                                                                                                              9.4 Bitmask [da8000]
                    if (i) rt[i] = pa[i];
                                                                                                              void hamiltonianPath() {
             res.assign(n, -1);
             for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i])
        dom[i] = dom[dom[i]];
for (int i = 1; i < id; i++)</pre>
                                                                                                                    int n, m; cin >> n >> m;
                                                                                                                     vector<vector<int>> adj(n);
                                                                                                                    for (int i = 0; i < m; i++) {
    int u, v; cin >> u >> v;
                                                                                                                           adj[--v].push_back(--u);
                    res[rev[i]] = rev[dom[i]];
             res[s] = s;
for (int i = 0; i < n; i++)
                                                                                                                    // 以...為終點,走過...
                                                                                                                    vector dp(n, vector < int > (1 << n));
dp[0][1] = 1;
for (int mask = 1; mask < 1 << n; mask++) {</pre>
             dom[i] = res[i];
return dom;
      }
                                                                                                                           if ((mask & 1) == 0) continue;
for (int i = 0; i < n; i++) {
    if ((mask >> i & 1) == 0) continue;
};
9 DP
                                                                                                                                 if (i == n - 1 && mask != (1 << n) - 1) continue;
int pre = mask ^ (1 << i);
for (int j : adj[i]) {
    if ((pre >> j & 1) == 0) continue;
    dp[i][mask] = (dp[i][mask] + dp[j][pre]) % Mod;
}
9.1 LCS [5781cf]
int main() {
       int m, n; cin >> m >> n;
       string s1, s2; cin >> s1 >> s2; int L = 0;
                                                                                                                                 }
                                                                                                                          }
       vector < vector < int >> dp(m + 1, vector < int > (n + 1, 0));
                                                                                                                    cout << dp[n - 1][(1 << n) - 1] << "\n";
      for (int i = 1; i <= m; i++) {
    for (int j = 1; j <= n; j++) {
        if (s1[i - 1] == s2[j - 1])
            dp[i][j] = dp[i - 1][j - 1] + 1;
}</pre>
                                                                                                              void elevatorRides() {
                                                                                                                    int n, x; cin >> n >> x;
vector <int> a(n);
for (int i = 0; i < n; i++) {</pre>
                           dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
                                                                                                                          cin >> a[i];
             }
                                                                                                                    vector<int> dp(1 << n), f(1 << n);
      int length = dp[m][n]; cout << length << "\n";
string s(length, 'c'); // backtracking
while (m >= 1 && n >= 1) {
   if (s1[m - 1] == s2[n - 1]) {
                                                                                                                    dp[0] = 1; // 次數、已使用人數
for (int mask = 1; mask < 1 << n; mask++) {
                                                                                                                           (Int mask = 1; mask < 1 << n; mask++) {
dp[mask] = 2E9;
for (int i = 0; i < n; i++) {
    if ((mask >> i & 1) == 0) continue;
    int pre = mask ^ (1 << i);</pre>
                   s[length - 1] = s1[m - 1];
m--, n--, length--;
                                                                                                                                 else {
    if (dp[m - 1][n] > dp[m][n - 1]) m--;
                    else n--;
      cout << s << "\n";
                                                                                                                                 } else if (dp[pre] + 1 < dp[mask] ||
    dp[pre] + 1 == dp[mask] && a[i] < f[mask]) {
    dp[mask] = dp[pre] + 1;
    f[mask] = a[i];</pre>
9.2 LIS [66d09f]
                                                                                                                                 }
int main() {
                                                                                                                          }
      int n; cin >> n;
vector <int> v(n);
                                                                                                                    cout << dp[(1 << n) - 1] << "\n";
      for (int i = 0; i < n; i++) cin >> v[i];
int dp[n]; vector < int >> stk;
stk.push_back(v[0]);
                                                                                                             }
                                                                                                              void minClique() { // 移掉一些邊,讓整張圖由最少團組成
      dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) {
    if (v[i] > stk.back()) {
                                                                                                                    int n, m;
cin >> n >> m;
                                                                                                                    vector < bitset < N >> g(n);
for (int i = 0; i < m; i++) {</pre>
                    stk.push_back(v[ij);
                                                                                                                          int u, v;
                    dp[i] = ++L;
                                                                                                                           cin >> u >> v;
             } else {
                    auto it
                                                                                                                           g[u][v] = g[v][u] = 1;
                            = lower_bound(stk.begin(), stk.end(), v[i]);
                    *it = v[i]; dp[i] = it - stk.begin() + 1;
                                                                                                                     vector<int> dp(1 << n, inf);</pre>
             }
                                                                                                                    dp[0] = 1;
      vector < int > ans; cout << L << "\n";
for (int i = n - 1; i >= 0; i--) {
   if (dp[i] == L) {
                                                                                                                    for (int mask = 0; mask < 1 << n; mask++) { // 先正常 dp
for (int i = 0; i < n; i++) {
    if (mask & (1 << i)) {
        int pre = mask ^ (1 << i);
```

9.5 Projects [0942aa]

```
int main() { // 排程有權重問題,輸出價值最多且時間最少
 struct E {
        int from, to, w, id;
        bool operator <(const E &rhs) {
    return to == rhs.to ? w > rhs.w : to < rhs.to;</pre>
       int n; cin >> n; vector<E> a(n + 1);
for (int i = 1; i <= n; i++) {
   int u, v, w; cin >> u >> v >> w;
   a[i] = {u, v, w, i};
        vector<array<ll, 2>> dp(n + 1); // w, time
        vector<array<int, 2>> rec(n + 1); // 有沒選,上個是誰
        sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
    auto it = --lower_bound(all(a), E({0, a[i].from}),</pre>
               [](E x, E y){ return x.to < y.to; });
int id = it - a.begin(); dp[i] = dp[i - 1];
              int td = it - a.begin(); up[i] - up[i - i],
ll nw = dp[id][0] + a[i].w;
ll nt = dp[id][1] + a[i].to - a[i].from;
if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
    dp[i] = {nw, nt}; rec[i] = {1, id};
        vector<int> ans;
       for (int i = n; i != 0;) {
    if (rec[i][0]) {
                     ans.push_back(a[i].id);
                     i = rec[i][1];
               } else i--;
}
```

9.6 Removal Game [7bb56b]

9.7 Monotonic Queue [f4976d]

```
| // 應用: dp(i) = h(i) + max(A(j)), for l(i)≤j≤r(i)
| // A(j) 可能包含 dp(j), h(i) 可 O(1)
| void Bounded_Knapsack() {
| int n, k; // O(nk)
| vector<int> w(n), v(n), num(n); deque<int> q;
| // 於是我們將同餘的數分在同一組
| // 每次取出連續 num[i] 格中最大值
| // g_x = max(_{{k=0}^num[i] (g'_{x-k} + v_i*k))
| // G_x = g'_{x} - v_i*x
| // x 代 x - k = v_i*(x-k)
| // g_x = max(_{{k=0}^num[i] (G_{x-k} + v_i*x))
| vector<vector<ll>> dp(2, vector<ll>(k + 1));
| for (int i = 0; i < n; i++) {
| for (int r = 0; r < w[i]; r++) { // 餘數
| q.clear(); // q 記錄在 x = i 時的 dp 有單調性
| for (int x = 0; x * w[i] + r <= k; x++) {
| while (!q.empty() && q.front() < x - num[i])
| q.pop_front(); // 維護遞減
| ll nxt = dp[0][x * w[i] + r] - x * v[i];
| while (!q.empty() && dp[0][q.back
| () * w[i] + r] - q.back() * v[i] < nxt)
| q.pop_back();
| q.push_back(x);
| dp[1][x * w[i] + r] = dp[0][q.front() * v[i] + x * v[i];
| }
```

```
}
swap(dp[0], dp[1]);
}
cout << dp[0][k] << "\n";
}</pre>
```

9.8 SOS [16fdf0]

```
|// 使用情況: 跟 bit 與(被)包含有關, 且 x 在 1E6 左右
// 題目:一數組,問有多少所有數 & 起來為 ø 的集合數 // dp[
      x] 代表包含 x 的 y 個數(比 x 大且 bit 1 全包含 x 的有幾個)
 // 答案應該包含在 dp[0] 内,但是有重複元素,所以考慮容斥 // => ans = \sum_{i=0}^{n} (-1)^{pop\_count(i)} 2^{dp[i]-1}
      部為 θ 的個數 - 至少一個為 1 的個數 + 至少兩個為 1 的個數
 void solve() {
   int n; cin >> n; Z ans = 0;
   vector<int> a(n);
     dp[pre] += dp[mask];
      for (int mask = 0; mask < 1 << m; mask++) {
   int sgn = __builtin_popcount(mask) & 1 ? -1 : 1
   ans += sgn * (power(Z(2), dp[mask].val()) - 1);</pre>
      cout << ans << "\n":
 //x / y = x, 代表包含於 x 的 y 個數, 定義為 dp[x][0]
| / / x & y = x, 代表包含 x 的 y 個數, 定義為 dp[x][1]
 // x & y != 0, 代表至
      少有一個位元都為 1 的 y 個數, = n - 與自己相同 - \sim dp[x][0]
 void solve() {
      int n; cin >> n;
vector < int > a(n);
      map < int , int > mp;
for (int i = 0; i < n; i++) {
    cin >> a[i];
          mp[a[i]]++;
      int m = __lg(*max_element(a.begin(), a.end())) + 1;
      vector<array<ll, 2>> dp(1 << m);
for (int i = 0; i < n; i++) {
    dp[a[i]][0] += 1;</pre>
          dp[a[i]][1] += 1;
      for (int i = 0; i < m; i++) {
   for (int mask = 0; mask < 1 << m; mask++) {
     if (mask >> i & 1) {
        int pre = mask ^ (1 << i);
     }
}</pre>
                    dp[mask][0] += dp[pre][0];
dp[pre][1] += dp[mask][1];
               }
          }
      }
```

9.9 CHT [5f5c25]

```
| // 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for jsr(i)
| // A(j), B(j) 可能包含 dp(j), 分別就是 m 跟 b
| struct Line {
| ll m, b;
| Line(ll m = 0, ll b = 0) : m(m), b(b) {}
| ll eval(ll x) {
| return m * x + b;
| }
| };
| struct CHT { // 用在查詢單調斜率也單調
| int n, lptr, rptr; vector<Line> hull;
| CHT(int n_ = 0, Line init_ = Line()) {
| init(n_, init_);
| }
| void init(int n_ = 0, Line init_ = Line()) {
| n = n_; hull.resize(n); reset(init_);
| }
| void reset(Line init_ = Line()) {
| lptr = rptr = 0; hull[0] = init_;
| }
| bool pop_front(Line &l1, Line &l2, ll x) {
| // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y // 代表查詢的當下,右線段的高度已經低於左線段了
```

9.10 DNC [61c639]

9.11 LiChao Segment Tree [f23ef4]

```
// 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \le r(i)
// y = c + constexpr ll inf = 4e18;
struct Line {
     ll m, b;
     line(ll m = 0, ll b = inf) : m(m), b(b) {}
ll eval(ll x) const { return m * x + b; }
struct LiChaoSeg { // 取 max 再變換就好
     vector<Line> info;
     LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_) {
          info.assign(4 << __lg(n), Line());</pre>
     void update(Line line, int node, int l, int r) {
          int m = (l + r) / 2;
bool left = line.eval(l) < info[node].eval(l);</pre>
          bool mid = line.eval(m) < info[node].eval(m);</pre>
          if (mid) swap(info[node], line); // 如果新線段比較好
          if (r - l == 1) return;
else if (left != mid) update(line, 2 * node, l, m);
          // 代表左半有交點
          else update(line, 2 * node + 1, m, r);
          // 代表如果有交點一定在右半
     // you'd add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
    if (r - l == 1) return info[node].eval(x);
    int m = (l + r) / 2;
          if (x < m) return
                min(info[node].eval(x), query(x, 2 * node, l, m));
          else return min(
   info[node].eval(x), query(x, 2 * node + 1, m, r));
     ll query(int x) { return query(x, 1, 0, n); }
};
```

9.12 Codeforces Example [7d37ea]

```
// CF 1932 pF
// 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
 // 請問在線段不重複的情況下,最多獲得幾分 int main() {
      int n, m;
cin >> n >> m;
      // 記錄每點有幾個線段
      // 再一個紀錄,包含這個點的左界
      cnt[l]++;
cnt[r + 1]--;
      for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
      for (int i = n; i >= 2; i--) {
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
      vector<int> dp(n + 1);
      dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
          dp[i] = cnt[i];
          if (l_side[i] != inf) {
    dp[i] += dp[l_side[i] - 1];
          dp[i] = max(dp[i], dp[i - 1]);
      cout << dp[n] << "\n";
 }
 // CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
 // 再加上 max(bi) - min(bi)
 int main(){
     main(){
int n, k, ans = 0; cin >> n >> k;
vector<pii> v(n + 1);
for (int i = 1; i <= n; i++) {
   int a, b; cin >> a >> b;
   v[i] = {a, b};
   if (a <= k) ans = 1;
}</pre>
      sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
      }); // 用 bi 來排,考慮第 i 個時可以先扣
      for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
                // min(不選, 選)
               if (dp[i
                       1][j -
                               1] + v[i].first + v[i].second <= k) {
                    // 假如可以選, 更新 ans 時再加回去 bi
                    ans = max(ans, j);
          dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
      cout << ans << endl;
```

10 Geometry

10.1 Basic [d41d8c]

```
template < class T >
struct Point {
    T x, y;
    Point(const T &x_ = 0, const T &y_ = 0) : x(x_), y(y_) {}
    template < class U >
    operator Point < U > () {
        return Point < U > (U(x), U(y));
    }
    Point & operator + = (const Point &p) & {
            x += p.x; y += p.y; return *this;
    }
    Point & operator - = (const Point &p) & {
            x -= p.x; y -= p.y; return *this;
}
    Point & operator * = (const T &v) & {
            x *= v; y *= v; return *this;
}
    Point & operator / = (const T &v) & {
            x /= v; y /= v; return *this;
}
    Point operator / (const T &v) & {
            x /= v; y /= v; return *this;
}
    Point operator - () const {
            return Point(-x, -y);
}
    friend Point operator + (Point a, const Point &b) {
            return a += b;
}
friend Point operator - (Point a, const Point &b) {
            return a -= b;
}
```

```
friend Point operator*(Point a, const T &b) {
          return a *= b;
     friend Point operator/(Point a, const T &b) {
          return a /= b;
     friend Point operator*(const T &a, Point b) {
    return b *= a;
     friend bool operator == (const Point &a. const Point &b) {
          return a.x == b.x && a.y == b.y;
     friend istream &operator>>(istream &is. Point &p) {
          return is >> p.x >> p.y;
     friend ostream &operator << (ostream &os, const Point &p) {
    return os << "(" << p.x << ", " << p.y << ")";</pre>
template < class T>
T dot(const Point < T> &a, const Point < T> &b) {
     return a.x * b.x + a.y * b.y;
T cross(const Point<T> &a, const Point<T> &b) {
   return a.x * b.y - a.y * b.x;
template < class T>
T square(const Point < T > & p) {
     return dot(p, p);
template < class T>
double length(const Point < T > & p)
     return sqrt(double(square(p)));
template < class T>
Point<T> normalize(const Point<T> &p) {
    return p / length(p);
template < class T>
Point<T> rotate(const Point<T> &a) {
     return Point(-a.y, a.x);
int sgn(const Point<T> &a) {
     return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
template < class T>
struct Line {
     Point<T>
     Point < T > b;
Line (const Point < T > &a_
                                  = Point<T>()
           , const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
template < class T>
double length(const Line<T> &l) {
     return length(l.a - l.b);
template < class T>
bool parallel(const Line<T> &l1, const Line<T> &l2) {
   return cross(l1.b - l1.a, l2.b - l2.a) == θ;
double distance(const Point<T> &a, const Point<T> &b) {
     return length(a - b);
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)</pre>
     return distance(p, l.a);
if (dot(p - l.b, l.a - l.b) < 0)</pre>
          return distance(p, l.b);
     return distancePL(p, l);
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
     return cross(l.b - l.a, p - l.a) > 0;
Point < T
     > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
return l1.a + (l1.b - l1.a) * (cross(l2.b -
           l2.a, l1.a - l2.a) / cross(l2.b - l2.a, l1.a - l1.b));
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
     return cross(p - l.a, l.b - l.a) == 0 &&
    min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)</pre>
                (l.a.y, l.b.y) \le p.y \& p.y \le max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
     (const Point<T> &a, const vector <Point <T>> &p) {
int n = p.size(), t = 0;
     for (int i = 0; i < n; i++) {</pre>
```

```
if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {
                      return true:
              }
        for (int i = 0; i < n; i++) {
              auto u = p[i];
              auto v = p[(i + 1) % n];
if (u.x < a.</pre>
                       x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
                      t ^= 1;
              if (u.x >= a
                       .x && v.x < a.x && pointOnLineLeft(a, Line(u, v)))</pre>
                      t ^= 1;
       return t == 1:
// 0 : not inside
// 1 : on boundary
// 2 : strictly inside
template < class T>
int
pointInConvexPolygon
         (const Point<T> &a, const vector<Point<T>> &p) {
       int n = p.size();
       if (n == 0) {
              return 0;
       } else if (n == 1) {
              return a == p[0];
       if (pointOnSegment(a, Line(p[0],
    p[1])) || pointOnSegment(a, Line(p[0], p[n - 1]))) {
               return 1;
       } else if (pointOnLineLeft(a, Line(p[1],
        p[0])) || pointOnLineLeft(a, Line(p[0], p[n - 1]))) {
    return 0;
       int lo = 1, hi = n - 2;
while (lo < hi) {
   int x = (lo + hi + 1) / 2;</pre>
              if (pointOnLineLeft(a, Line(p[0], p[x]))) {
                      lo = x;
              } else {
                     hi = x - 1;
              }
        if (pointOnLineLeft(a, Line(p[lo], p[lo + 1]))) {
               return 2;
       } else {
    return pointOnSegment(a, Line(p[lo], p[lo + 1]));
template < class T>
bool lineIntersectsPolygon
       (const Line<T> &l, const vector<Point<T>> &p) {
int n = p.size();
Point<T> a = l.a, b = l.b;
       for (int i = 0; i < n; i++) {
    Line<T> seg(p[i], p[(i + 1) % n]);
              if (cross(b - a, seg.b - a) == 0) {
                      return true;
                     a, seg.a - a) > 0 ^ cross(b - a, seg.b - a) > 0) {
return true;
       return false:
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
tuple < int , Point < T > , Point < T >> segmentIntersection
      le<int, Point<T>, Point<T>> segmentIntersection
  (const Line<T> &l1, const Line<T> &l2) {
   if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
      return {0, Point<T>(), Point<T>()};
   if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
      return {0, Point<T>(), Point<T>()};
   if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y))
      return {0, Point<T>(), Point<T>()};
   if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y))
      return {0, Point<T>(), Point<T>()};
   if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
      if (cross(l1.b - l1.a, l2.a - l1.a) != 0) {
            return {0, Point<T>(), Point<T>()};
   }
}
                      return {0, Point<T>(), Point<T>()};
              } else {
                     auto maxx1 = max(l1.a.x, l1.b.x);
                      auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
auto miny1 = min(l1.a.y, l1.b.y);
                     auto miny1 = min(l1.a.y, l1.b.y),
auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.y, l2.b.y);
auto miny2 = min(l2.a.y, l2.b.y);
                     Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
if (!pointOnSegment(p1, l1))
                      swap(p1.y, p2.y);
if (p1 == p2) {
                             return {3, p1, p2};
                     } else {
```

```
return {2, p1, p2};
         }
    auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
    auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
    if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
         return {1, p, p};
    } else {
         return {3, p, p};
template < class T>
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
   if (get<0>(segmentIntersection(l1, l2)) != 0)
    return 0.0;
return min({distancePS(l1.a, l2), distancePS(l1
    .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
template < class T>
bool segmentInPolygon
     (const Line<T> &l, const vector<Point<T>> &p) {
     int n = p.size();
    if (!pointInPolygon(l.a, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
for (int i = 0; i < n; i++) {
    auto u = p[i];
    auto v = p[(i + 1) % n];
    auto w = p[(i + 2) % n];
}</pre>
         auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
if (t == 1) return false;
if (t == 0) continue;
         if (t == 2) {
              if (pointOnSegment(v, l) && v != l.a && v != l.b)
    if (cross(v - u, w - v) > 0)
        return false;
         if (pointOnLineLeft(l.a, Line(v, u))
                        || pointOnLineLeft(l.b, Line(v, u)))
              return false;
} else if (p1 == v) {
   if (l.a == v) {
                        if (pointOnLineLeft(u, l)) {
    if (pointOnLineLeft(w, l))
                                 && pointOnLineLeft(w, Line(u, v)))
                                 return false;
                        } else {
                             if (pointOnLineLeft(w, l)
                                  || pointOnLineLeft(w, Line(u, v)))
                                 return false:
                  return false;
                        } else {
                             return false:
                  return false;
                        } else {
                            return false:
                       }
                  }
             }
         }
     return true:
template < class T>
vector<Point<T>> convexHull(vector<Point<T>> a) {
    sort(a.begin()
           a.end(), [](const Point<T> &l, const Point<T> &r) {
         return l.x == r.x ? l.y < r.y : l.x < r.x;
     a.resize(unique(a.begin(), a.end()) - a.begin());
    if (a.size() <= 1) return a;
vector < Point < T >> h(a.size() + 1);
    h[t++] = p;
         reverse(a.begin(), a.end());
```

```
return {h.begin(), h.begin() + t}:
template < class T>
vector<Point<T>> hp(vector<Line<T>> lines) {
     return cross(d1, d2) > 0;
     deaue<Line<T>> ls:
     deque<Point<T>> ps;
for (auto l : lines) {
          if (ls.empty())
                ls.push_back(l);
                continue:
          while (!ps.empty() && !pointOnLineLeft(ps.back(), l))
    ps.pop_back(), ls.pop_back();
while (!ps.empty() && !pointOnLineLeft(ps[0], l))
          ps.pop_front(), ls.pop_front();
if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
                if (dot
                      (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                     if (!pointOnLineLeft(ls.back().a, l)) {
                          assert(ls.size() == 1);
                          ls[0] = l;
                     continue;
                return {};
          ps.push back(lineIntersection(ls.back(), l)):
           ls.push_back(l);
     while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0]))
    ps.pop_back(), ls.pop_back();
if (ls.size() <= 2) return {};
ps.push_back(lineIntersection(ls[0], ls.back()));</pre>
     return vector(ps.begin(), ps.end());
using P = Point<ll>:
```

10.2 Min Euclidean Distance [d7fdcf]

```
void solve() {
       int n; cin >> n;
constexpr ll inf = 8e18;
       vector < Point < ll >> a(n);
       for (int i = 0; i < n; i++) {
    ll x, y;
    cin >> x >> y;
              a[i] = Point < ll>(x, y);
       struct sortY {
              bool operator
     ()(const Point<ll> &a, const Point<ll> &b) const {
                       return a.y < b.y;</pre>
       struct sortXY {
              bool operator
   ()(const Point<ll> &a, const Point<ll> &b) const {
   if (a.x == b.x) return a.y < b.y;
   else return a.x < b.x;</pre>
              }
       sort(a.begin(), a.end(), sortXY());
vector<Point<ll>> t(n);
       auto devide = [%](auto &&self, int l, int r) -> ll {
    if (l == r) return inf;
    int m = (l + r) / 2;
    ll ans = min(self(self, l, m), self(self, m + 1, r));
    ll midval = a[m].x;
}
              ll midvat - ci..,
ll p = 0;
for (int i = l; i <= r; i++) {
   if ((midval - a[i].x) * (midval - a[i].x) <= ans) {
      t[p++] = a[i];
   }</pre>
              for (t.begin(), t.begin() + p, sortY());
for (int i = 0; i < p; i++){
    for (int j = i + 1; j < p; j++) {
        ans = min(ans, square(t[i] - t[j]));
}</pre>
                              if ((t[i].y
                                          t[j].y) * (t[i].y - t[j].y) > ans) break;
                      }
               return ans;
       1:
       cout << devide(devide, 0, n - 1) << "\n";</pre>
```

10.3 Max Euclidean Distance [0a8bec]

```
template < class T>
tuple<T, int, int> mxdisPair(vector<Point<T>> a) {
   auto get = [&](const Point<T> &p, const Line<T> &l) -> T {
      return abs(cross(l.a - l.b, l.a - p));
}
       T res = 0; int n = a.size(), x, y, id = 2;
```

10.4 Lattice Points [00db9d]

10.5 Min Circle Cover [02619b]

10.6 Min Rectangle Cover [b80323]

11 Polynomial

11.1 FFT [2e8718]

```
const double PI = acos(-1.0);
struct Complex {
         double x, y;
Complex(double x_ = 0, double y_ = 0) : x(x_), y(y_) {}
Complex operator+(const Complex &b) const {
                 return Complex(x + b.x, y + b.y);
         Complex operator - (const Complex &b) const {
    return Complex(x - b.x, y - b.y);
         Complex operator*(const Complex &b) const {
    return Complex(x * b.x - y * b.y, x * b.y + y * b.x);
        }
void fft(vector<Complex> &a, bool inv) {
         int n = a.size();
         if (int(rev.size()) != n) {
                 int k = _builtin_ctz(n) - 1;
rev.resize(n);
for (int i = 0; i < n; i++) {
    rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;</pre>
         for (int i = 0; i < n; i++) {
    if (rev[i] < i) {</pre>
                          swap(a[i], a[rev[i]]);
       }
for (int k = 1; k < n; k *= 2) {
    double ang = (inv ? -1 : 1) * PI / k;
    Complex wn(cos(ang), sin(ang));
    for (int i = 0; i < n; i += 2 * k) {
        Complex w(1);
        for (int j = 0; j < k; j++, w = w * wn) {
            Complex u = a[i + j];
            Complex v = a[i + j + k] * w;
            a[i + j] = u + v;
            a[i + j + k] = u - v;
    }
}</pre>
                 }
         if (inv) {
    for (auto &x : a) {
                          x.x /= n;
x.y /= n;
                 }
template < class T>
vector<T> mulT(const vector<T> &a, const vector<T> &b) {
        vector<Complex
        rectification
> fa(a.begin(), a.end()), fb(b.begin(), b.end());
int n = 2 << __lg(a.size() + b.size());
fa.resize(n), fb.resize(n);
fft(fa, false), fft(fb, false);
for (int i = 0; i < n; i++) {
    fa[i] = fa[i] * fb[i];
}</pre>
         fft(fa. true):
         frt(fa, true);
vector<T> res(n);
for (int i = 0; i < n; i++) {
    if constexpr (!is_same_v<T, double>) {
        res[i] = round(fa[i].x);
}
                          res[i] = fa[i].x;
         return res;
```

11.2 NTT [1c9189]

| }

```
template < int V, ll P>
constexpr MInt < P > CInv = MInt < P > (V).inv();
template < ll P >
vector<MInt<P>> roots{0, 1}:
constexpr MInt<P> findPrimitiveRoot() {
     MInt<P> i = 2;
int k = __builtin_ctz(P - 1);
while (true) {
   if (power(i, (P - 1) / 2) != 1) {
            i += 1:
      return power(i, (P - 1) >> k);
}
constexpr MInt<P> primitiveRoot = findPrimitiveRoot<P>();
constexpr MInt<998244353> primitiveRoot<998244353> {31};
template < ll P >
constexpr void dft(vector<MInt<P>> &a) {
  int n = a.size();
      if (int(rev.size()) != n) {
    int k = __builtin_ctz(n) - 1;
            rev.resize(n);
            for (int i = 0; i < n; i++) {
    rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;
     for (int i = 0; i < n; i++) {
    if (rev[i] < i) {
        swap(a[i], a[rev[i]]);
    }
}</pre>
      if (roots<P>.size() < n) {
   int k = __builtin_ctz(roots<P>.size());
   roots<P>.resize(n);
            while ((1 << k) < n) {
                 auto e = power(primitiveRoot
                 }
      a[i + j] = u + v;
a[i + j + k] = u - v;
                 }
           }
     }
}
template < ll P >
constexpr void idft(vector<MInt<P>> &a) {
   int n = a.size();
   reverse(a.begin() + 1, a.end());
      dft(a);
     MInt<P> inv = (1 - P) / n;
for (int i = 0; i < n; i++) {
    a[i] *= inv;</pre>
}
template < ll P = 998244353>
struct Poly : public vector<MInt<P>> {
    using Value = MInt<P>;
    Poly() : vector<Value>() {}
      explicit constexpr Poly(int n) : vector<Value>(n) {}
      explicit constexpr
    Poly(const vector<Value> &a) : vector<Value>(a) {}
                    Poly(const
      initializer_list<Value> &a) : vector<Value>(a) {}
template<class InputIt, class = _RequireInputIter<InputIt>>
explicit constexpr Poly(InputIt
             first, InputIt last) : vector<Value>(first, last) {}
      template < class F>
      templicit constexpr Poly(int n, F f) : vector<Value>(n) {
    for (int i = 0; i < n; i++) {
        (*this)[i] = f(i);
    }
}</pre>
      constexpr Poly shift(int k) const {
  if (k >= 0) {
    auto b = *this;
}
                 b.insert(b.begin(), k, 0);
```

```
return b;
} else if (this->size() <= -k) {</pre>
           return Poly();
      } else {
           return Poly(this->begin() + (-k), this->end());
constexpr Poly trunc(int k) const {
   Poly f = *this;
      f.resize(k);
      return f:
for (int i = 0; i < a.size(); i++) {
    res[i] += a[i];</pre>
      for (int i = 0; i < b.size(); i++) {
    res[i] += b[i];</pre>
constexor
         friend Poly operator - (const Poly &a, const Poly &b) {
      Poly res(max(a.size(), b.size()));
      for (int i = 0; i < a.size(); i++) {
    res[i] += a[i];</pre>
      for (int i = 0; i < b.size(); i++) {
    res[i] -= b[i];</pre>
      return res:
constexpr friend Poly operator - (const Poly &a) {
      vector<Value> res(a.size());
      for (int i = 0; i < int(res.size()); i++) {
    res[i] = -a[i];</pre>
      return Poly(res);
constexpr friend Poly operator*(Poly a, Poly b) {
   if (a.size() == 0 || b.size() == 0) {
      return Poly();
}
     }
if (a.size() < b.size()) swap(a, b);
int n = 1, tot = a.size() + b.size() - 1;
while (n < tot) n *= 2;
if (((P - 1) & (n - 1)) != 0 || b.size() < 128) {
    Poly c(a.size() + b.size() - 1);
    for (int i = 0; i < a.size(); i++) {
        for (int j = 0; j < b.size(); j++) {
            c[i + j] += a[i] * b[j];
        }
}</pre>
             return c;
      a.resize(n), b.resize(n);
      dft(a), dft(b);
for (int i = 0; i < n; ++i) {
    a[i] *= b[i];</pre>
      idft(a);
      a.resize(tot);
constexpr friend Poly operator*(Value a, Poly b) {
   for (int i = 0; i < int(b.size()); i++) {
      b[i] *= a;</pre>
constexpr friend Poly operator*(Poly a, Value b) {
    for (int i = 0; i < int(a.size()); i++) {
        a[i] *= b;
}</pre>
      return a:
constexpr friend Poly operator/(Poly a, Value b) {
  for (int i = 0; i < int(a.size()); i++) {
    a[i] /= b;</pre>
      return a:
constexpr Poly &operator+=(Poly b) {
   return (*this) = (*this) + b;
constexpr Poly &operator -=(Poly b) {
      return (*this) = (*this) - b;
constexpr Poly &operator*=(Poly b) {
      return (*this) = (*this) * b;
constexpr Poly & operator*=(Value b) {
      return (*this) = (*this) * b;
constexpr Poly &operator/=(Value b) {
  return (*this) = (*this) / b;
constexpr Poly deriv() const {
      if (this->empty()) return Poly();
      Poly res(this->size() - 1);
```

```
for (int i = 0; i < this->size() - 1;
res[i] = (i + 1) * (*this)[i + 1];
                                                                       ++i) {
            return res:
      constexpr Poly integr() const {
  Poly res(this->size() + 1);
  for (int i = 0; i < this->size(); ++i) {
                  res[i + 1] = (*this)[i] / (i + 1);
            return res:
      constexpr Poly inv(int m) const {
  Poly x{(*this)[0].inv()};
  int k = 1;
            while (k < m) {
    k *= 2;
    x = (x * (Poly{2} - trunc(k) * x)).trunc(k);</pre>
            return x.trunc(m);
      constexpr Poly log(int m) const {
   return (deriv() * inv(m)).integr().trunc(m);
      constexpr Poly exp(int m) const {
           Poly x{1};
int k = 1;
while (k < m) {
    k *= 2;
    x = (x * (Poly{1} - x.log(k) + trunc(k))).trunc(k);</pre>
            return x.trunc(m);
      constexpr Poly pow(int k, int m) const {
            while (i < this->size() && (*this)[i] == 0) {
            if (i == this->size() || 1LL * i * k >= m) {
                  return Poly(m);
            Value v = (*this)[i];
            auto f = shift(-i) *
return (f.log(m - i *
                                            v.inv();
                    k) * k).exp(m - i * k).shift(i * k) * power(v, k);
      constexpr Poly sqrt(int m) const {
            Poly x{1};
            int k = 1;
while (k < m) {
    k *= 2;
                  x = (x)
                           (trunc(k) * x.inv(k)).trunc(k)) * CInv<2, P>;
            return x.trunc(m);
      constexpr Poly mulT(Poly b) const {
   if (b.size() == 0) return Poly();
            int n = b.size();
reverse(b.begin(), b.end());
return ((*this) * b).shift(-(n - 1));
      constexpr vector<Value> eval(vector<Value> x) const {
   if (this->size() == 0) {
      return vector<Value>(x.size(), 0);
}
            const int n = max(x.size(), this->size());
vector<Poly> q(4 * n);
            vector<Value> ans(x.size());
             x.resize(n):
             function < void (
                  int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
    q[p] = Poly{1, -x[l]};
                  a(p) = roty(1, 'x[t]),
else {
  int m = (l + r) / 2;
  build(2 * p, l, m);
  build(2 * p + 1, m, r);
  q[p] = q[2 * p] * q[2 * p + 1];
                  }
            function < void(int, int, int, const Poly &) >
    work = [&](int p, int l, int r, const Poly & num) {
    if (r - l == 1) {
        if (l < int(ans.size())) {
            ase[ll = num[0]:</pre>
                               ans[l] = num[0];
                  } else {
                         int m = (l + r) / 2;
work(2 * p, l,
                         }
            work(1, 0, n, mulT(q[1].inv(n)));
            return ans;
};
template < ll P = 998244353>
```

```
Poly<P> berlekampMassey(const Poly<P> &s) {
     Poly<P> c, oldC;
int f = -1;
for (int i = 0; i < s.size(); i++) {</pre>
           auto delta = s[i];
          for (int j = 1; j <= c.size(); j++) {
    delta -= c[j - 1] * s[i - j];</pre>
           if (delta == 0) continue;
          if (f == -1) {
               c.resize(i + 1);
                f = i;
          } else {
               auto d = oldC;
                d.insert(d.begin(), 1);
                MInt<P> df1 = 0;
for (int j = 1; j <= d.size(); j++) {
    df1 += d[j - 1] * s[f + 1 - j];
                assert(df1 != 0);
                auto coef = delta / df1;
                d *= coef;
                Poly<P> zeros(i - f - 1);
                zeros.insert(zeros.end(), d.begin(), d.end());
                d = zeros;
               }
     c *= -1;
     c.insert(c.begin(), 1);
     return c;
template < ll P = 998244353>
MInt<P> linearRecurrence(Poly<P> p, Poly<P> q, ll n) {
     int m = q.size() - 1;
while (n > 0) {
          auto newq = q;
for (int i = 1; i <= m; i += 2) {</pre>
               newq[i] *=
          Jauto newp = p * newq;
newq = q * newq;
for (int i = 0; i < m; i++) {
    p[i] = newp[i * 2 + n % 2];</pre>
          for (int i = 0; i <= m; i++) {
   q[i] = newq[i * 2];</pre>
          n /= 2;
     return p[0] / q[0];
```

12 Else

12.1 Python [44ab0e]