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Basic 1

1.1 Install VScode [d41d8c]

```
// 如何安裝 vscode
// 1. 下載 vscode & msys2
// 2. 在跳出的 terminal 中 / 或打開 ucrt64,打上
"pacman -S --needed base-devel mingw-w64-x86_64-toolchain"
// 3. 環境變數加上 C:\\msys64\\ucrt64\\bin
// 4. 重開 vscode, 載 C/C++, 運行, 編譯器選擇 g++
// 5. 打開 settings -> compiler -> add compilerPath
       -> 在 "" 裡打上 C:\\msys64\\ucrt64\\bin\\g++.exe
```

1.2 Default Code [d41d8c]

```
#include <bits/stdc++.h>
#Include <olis/stdc++.n>
// #pragma GCC target("popcnt")
// C++ 20 vector grammer will not work
#define all(x) (x).begin(), (x).end()
using namespace std;
using ll = long long;
void solve() {
}
int main() {
        ios_base::sync_with_stdio(false);
        cin.tie(nullptr);
        int t = 1;
        cin >> t;
       while (t--) {
    solve();
}
```

1.3 Compare Fuction [d41d8c]

```
|1. sort, 二分搜刻在函式內 lambda 就好
2. priority queue 小到大是 >, set 是 < 3. set 不能 = , multiset 必須 =
 4. 確保每個成員都要比到
 5. pbds_multiset 不要用 lower_bound
 6. 如果要用 find, 插入 inf 後使用 upper_bound
 7. multiset 可以跟 set 一樣使用, 但請注意第 3、4 點
auto cmp = [](int i, int j) { return i > j; };
priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
```

```
vector <int> a {1, 2, 5, 4, 3}; // 小心不要改到 a
auto cmp = [&a](int i, int j) { return a[i] > a[j]; };
priority_queue <int, vector <int>, decltype(cmp)> pq(cmp);
```

1.4 Pbds [d41d8c]

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < typename T >
using pbds_set = tree < T, null_type,</pre>
less <T>, rb_tree_tag, tree_order_statistics_node_update>;
template < typename T>
using pbds_multiset = tree<T, null_type, less_equal</pre>
       <T>, rb_tree_tag, tree_order_statistics_node_update>;
```

1.5 Double [b44e11]

```
struct D {
   double x;
       constexpr static double eps = 1e-12;
       D(): x{0.0} {}
D(double v): x{v} {}
double val() const { return x; }
explicit operator double() const { return x; }
D operator-() const {
              return D(-x);
       D &operator+=(const D &rhs) & {
               x += rhs.x; return *this;
       D &operator -= (const D &rhs) & {
    x -= rhs.x; return *this;
       D &operator*=(const D &rhs) & {
    x *= rhs.x; return *this;
       D & operator/=(const D &rhs) & {
    assert(fabs(rhs.x) > eps);
    x /= rhs.x; return *this;
       friend D operator+(D lhs, const D &rhs) {
   return lhs += rhs;
       friend D operator - (D lhs, const D &rhs) {
    return lhs -= rhs;
       friend D operator*(D lhs, const D &rhs) {
   return lhs *= rhs;
       friend D operator/(D lhs, const D &rhs) {
  return lhs /= rhs;
       friend bool operator <(const D &lhs, const D &rhs) {
   return lhs.x - rhs.x < -eps;</pre>
       friend bool operator>(const D &lhs, const D &rhs) {
   return lhs.x - rhs.x > eps;
        friend bool operator == (const D &lhs, const D &rhs) {
  return fabs(lhs.x - rhs.x) < eps;</pre>
       friend bool operator <= (const D &lhs, const D &rhs) {
  return lhs < rhs || lhs == rhs;</pre>
        friend bool operator>=(const D &lhs, const D &rhs) {
               return lhs > rhs || lhs == rhs;
       friend bool operator!=(const D &lhs, const D &rhs) {
  return !(lhs == rhs);
       friend istream &operator>>(istream &is, D &a) {
   double v; is >> v; a = D(v); return is;
       friend ostream &operator<<(ostream &os, const D &a) {
   return os << fixed << setprecision(10) << a.val()
   + (a.val() > 0 ? eps : a.val() < 0 ? -eps : 0);
} // eps should < precision</pre>
```

2 Graph

};

2.1 DFS And BFS [e2d856]

```
int main() {
     int n;
     vector < int >> adj(n);
     // dfs_graph
    auto dfs = [&](auto self, int u) -> void {
   if (vis[u]) return;
         vis[u] = true;
         for (auto v: adj[u]) {
    self(self, v);
         }
    dfs(dfs, 0);
     // bfs
    vector<int> depth(n, 1e9);
    queue<int> q;
auto bfs = [&](auto self, int s) -> void {
```

2.3 BellmanFord [430ded]

return false;

};

2.4 FloydWarshall [3f61a4]

2.5 Euler [4177dc]

```
// 1. 無向圖是歐拉圖:
// 非零度頂點是連通的
// 頂點的度數都是偶數
// 2. 無向圖是半歐拉圖(有路沒有環):
| // 非零度頂點是連通的
// 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
// 非零度頂點是強連通的
// 每個頂點的入度和出度相等
// 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
// 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
// 其他頂點的入度和出度相等
vector < int > ans;
auto dfs = [&](auto &&self, int u) -> void {
    while (g[u].size()) {
      int v = *g[u].begin();
g[u].erase(v);
       self(self, v);
    ans.push back(u):
dfs(dfs, 0);
reverse(ans.begin(), ans.end());
2.6 SCC [5d3e16]
```

```
struct SCC {
     int n, cur, cnt;
vector<vector<int>> adj;
     vector<int> stk, dfn, low, bel;
SCC(int n_ = 0) { init(n_); }
void init(int n_) {
         n = n_;
adj.assign(n, {});
          dfn.assign(n,
          low.resize(n);
          bel.assign(n, -1);
          stk.clear();
          cur = cnt = 0;
     void addEdge(int u, int v) {
          adj[u].push_back(v);
     void dfs(int x) {
          dfn[x] = low[x] = cur++;
          stk.push_back(x);
          for (auto y : adj[x]) {
   if (dfn[y] == -1) {
                    dfs(y);
               low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
                    low[x] = min(low[x], dfn[y]);
               }
          if (dfn[x] == low[x]) {
               int y;
do {
                    y = stk.back();
               bel[y] = cnt;
stk.pop_back();
while (y != x);
               cnt++;
         }
     vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
          return bel;
     struct Graph {
          int n;
          vector<pair<int, int>> edges;
          vector<int> siz;
          vector<int> cnte;
     Graph compress() {
          Graph g;
          g.n = cnt;
          g.siz.resize(cnt);
          g.cnte.resize(cnt);
          g.edges.emplace_back(bel[i], bel[j]);
                    } else {
                         g.cnte[bel[i]]++;
                    }
               }
```

return g;

```
2.7 VBCC [170604]
```

```
struct VBCC {
     int n, cur;
vector<vector<int>> adj;
      vector<int> dfn, low, parent;
     vector <bool> is_cut;
VBCC(int n_ = 0) { init(n_); }
void init(int n_) {
           n = n_;
adj.assign(n, {});
            dfn.assign(n, -1);
low.resize(n);
            parent.assign(n, -1);
is_cut.assign(n, false);
cur = 0;
      void addEdge(int u, int v) {
   adj[u].push_back(v);
            adj[v].push_back(u);
      void dfs(int x) {
            int children
                               = 0;
            dfn[x] = low[x] = cur++;
for (int v : adj[x]) {
    if (dfn[v] == -1) {
                        children++;
                        parent[v] = x;
                        dfs(v);
                        low[x] = min(low[x], low[v]);
                        if (parent[x] != -1 && low[v] >= dfn[x]) {
                              is_cut[x] = true;
                 } else if (v != parent[x]) {
   low[x] = min(low[x], dfn[v]);
                  }
            if (parent[x] == -1 && children > 1) {
                  is_cut[x] = true;
           }
      void work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {</pre>
                        dfs(i);
                  }
           }
     }
};
```

2.8 EBCC [59d8ca]

```
struct EBCC { // CF/contest/1986/pF
  int n, cur, cnt;
  vector<vector<int>> adj;
      vector<int> stk, dfn, low, bel;
      vectorvectorvectorvectorvectorvectorvectorvector
vector
pair<int>int
n = 0) { init(n_); }
void init(int n_) {
    n = n_;

             adj.assign(n, {});
            dfn.assign(n, -1);
low.resize(n);
             bel.assign(n, -1);
            stk.clear();
bridges.clear();
cur = cnt = 0;
      void addEdge(int u, int v) {
   adj[u].push_back(v);
             adj[v].push_back(u);
      void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
             stk.push_back(x);
            for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
                         dfs(y, x);
low[x] = min(low[x], low[y]);
if (low[y] > dfn[x]) {
                               bridges.emplace_back(x, y);
                   } else if (bel[y] == -1) {
                         low[x] = min(low[x], dfn[y]);
                   }
             if (dfn[x] == low[x]) {
                   int y;
do {
                         y = stk.back();
                         bel[y] = cnt;
                         stk.pop_back();
                   } while (y != x);
                   cnt++;
            }
      vector<int> work() { // not connected
```

```
for (int i = 0; i < n; i++) {
   if (dfn[i] == -1) {
      dfs(i, -1);
}</pre>
                }
           return bel;
     struct Graph {
          vector<pair<int, int>> edges;
          vector<int> siz; // BCC 內節點數
           vector<int> cnte; // BCC 內邊數
     Graph compress() {
          Graph g;
g.n = cnt;
           g.siz.resize(cnt);
          g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;
}</pre>
                for (auto j : adj[i]) {
    if (bel[i] < bel[j]) {</pre>
                          g.edges.emplace_back(bel[i], bel[j]);
                     } else if (i < j) {
                          g.cnte[bel[i]]++;
                }
           return a:
     }
}:
2.9 2-SAT [eeddc1]
struct TwoSat {
     int n; vector<vector<int>> e;
      vector<bool> ans;
```

```
// CSES Giant Pizza
       vector volus airs,
TwoSat(int n) : n(n), e(2 * n), ans(n) {}
void addClause(int u, bool f, int v, bool g) {
    e[2 * u + !f].push_back(2 * v + g);
    e[2 * v + !g].push_back(2 * u + f);
       bool satisfiable() {
              vector<int
                      > id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
              vector < int > stk;
int now = 0, cnt = 0;
               function < void(int) > tarjan = [&](int u) {
                     stk.push_back(u);
dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
                                   tarjan(v);
                            low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in stk
low[u] = min(low[u], dfn[v]);
                      if (dfn[u] == low[u]) {
                            int v;
do {
                                   v = stk.back();
                            stk.pop_back();
id[v] = cnt;
} while (v != u);
                             ++cnt:
                    }
              for (int i
              return true;
       vector<bool> answer() { return ans; }
};
int main() {
       main() {
  int m, n; cin >> m >> n;
TwoSat ts(n);
for (int i = 0; i < m; ++i) {
    int u, v; char x, y;
    cin >> x >> u >> y >> v;
    ts.addClause(u - 1, x == '+', v - 1, y == '+');
}
       if (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";
}</pre>
       else cout << "IMPOSSIBLE\n";</pre>
}
```

2.10 Funtional Graph [85c464]

```
| constexpr int N = 2e5 + 5;
| int cht[N][31]; // 倍增表, 放外面不然 TLE
| struct FuntionalGraph {
| int n, cnt;
```

```
vector < int> g, bel, id, len, in, top;
FuntionalGraph() : n(0) {}
        FuntionalGraph(vector<int> g_) { init(g_); }
        void init(vector<int> g_) {
    n = g_.size(); cnt = 0;
                g = g_{,} bel.assign(n, -1);
               id.resize(n); len.clear();
in.assign(n, 0); top.assign(n, -1);
                build();
       in[g[i]]++;
               for (int i = 1; i <= 30; i++)
    for (int u = 0; u < n; u++)
        cht[u][i] = cht[cht[u][i - 1]][i - 1];
for (int i = 0; i < n; i++)
    if (in[i] == 0) label(i);
for (int i = 0; i < n; i++)
    if (top[i] == -1) label(i);</pre>
        void label(int u) {
   vector < int > p; int cur = u;
}
                while (top[cur] == -1) {
                       top[cur] = u;
p.push_back(cur);
                       cur = g[cur];
               auto s = std::find(p.begin(), p.end(), cur);
vector < int > cyc(s, p.end());
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {
    bel[cyc[i]] = cnt;
}</pre>
                       id[cyc[i]] = i;
                cnt++; len.push_back(cyc.size());
                for (int i = p.size() - 1; i > 0; i--)
   id[p[i - 1]] = id[p[i]] - 1;
       int jump(int u, int k) {
    for (int b = 0; k > 0; b++){
        if (k & 1) u = cht[u][b];
}
                return u:
       }
};
```

3 Data Structure

3.1 BIT [d41d8c]

```
template <typename T>
struct Fenwick { // 全部以 0 based 使用
  int n; vector<T> a;
     Fenwick(int n_ = 0) { init(n_); }
     void init(int n_) {
           n = n;
           a.assign(n, T{});
     void add(int x, const T &v) {
   for (int i = x + 1; i <= n; i += i & -i) {
      a[i - 1] = a[i - 1] + v;
}</pre>
     T sum(int x) { // 左閉右開查詢 T ans{};
           for (int i = x; i > 0; i -= i & -i) {
    ans = ans + a[i - 1];
     TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
     int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
           int x = 0;
           tit x = 0;
T cur{};
for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n && cur + a[x + i - 1] <= k) {
        x += i;
    }</pre>
                      cur = cur + a[x - 1];
                }
           return x;
     }
template <class T>
struct TwoDFenwick { // 全部以 0 based 使用
     int nx, ny; // row, col 個數 vector < vector < T >> a;
     TwoDFenwick(int nx_ = 0, int ny_ = 0) {
           init(nx_, ny_);
     void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
     void add(int x, int y, const T &v) {
```

```
for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        a[i - 1][j - 1] = a[i - 1][j - 1] + v;
}</pre>
        }
        T sum(int x, int y) { // 左閉右開查詢
              Im(int x, s...),
T ans{};
for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans + a[i - 1][j - 1];
}
               return ans;
        T rangeSum
                (int lx, int ly, int rx, int ry) { // 左閉右開查詢
               return sum(
                      (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
};
```

3.2 RangeBit [d41d8c]

| template <typename T>

```
struct rangeFenwick { // 全部以 0 based 使用
               int n;
                vector <T> d, di;
rangeFenwick(int n_ = 0) { init(n_); }
                void init(int n_) {
                               d.assign(n, T{})
                               di.assign(n, T{});
                Joid add(int x, const T &v) {
   T vi = v * (x + 1);
   for (int i = x + 1; i <= n; i += i & -i) {
      d[i - 1] = d[i - 1] + v;
      di[i - 1] = di[i - 1] + vi;
}</pre>
                              }
                void rangeAdd(int l, int r, const T &v) {
                               add(l, v); add(r, -v);
                T sum(int x) { // 左閉右開查詢
                               T`ans{};
                               for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
                               return ans;
               TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
                int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
                             cur = cur + val:
                                           }
                               return x;
            }
template <class T>
struct rangeTwoDFenwick { // 全部以 0 based 使用
               int nx, ny; // row, col 個數
vector < vector < T >> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
                                init(nx , ny );
               void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
                               dij.assign(nx, vector<T>(ny, T{}));
              }
void add(int x, int y, const T &v) {
    T vi = v * (x + 1);
    T vj = v * (y + 1);
    T vij = v * (x + 1) * (y + 1);
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            d[i - 1][j - 1] = d[i - 1][j - 1] + v;
            di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
            dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
            dij[i - 1][j - 1] = dij[i - 1][j - 1] + vj;
            dij[i - 1][j - 1] = dij[i - 1][j - 1] + vij;
}</pre>
                 void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
                               add(rx, ry, v);
add(lx, ry, -v);
```

| struct Seg { // 左閉右開寫法

```
add(rx, ly, -v);
add(lx, ly, v);
                                                                                                                int n; vector<Info> info;
Seg() : n(0) {}
                                                                                                                Seg(int n_, Info v
template <class T>
                                                                                                                                  Info v_ = Info()) { init(n_, v_); }
      T sum(int x, int y) { // 左閉右開查詢
                                                                                                                Seg(vector<T> init_) { init(init_);
             T ans{};
for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
                                                                                                                void init(int n_, Info v_ = Info()) {
    init(vector(n_, v_));
                         ans = ans

+ T(x * y + x + y + 1) * d[i - 1][j - 1];

ans = ans - T(y + 1) * di[i - 1][j - 1];

ans = ans - T(x + 1) * dj[i - 1][j - 1];

ans = ans + dij[i - 1][j - 1];
                                                                                                                template <class T>
void init(vector<T> init_) {
                                                                                                                      n = init_.size();
                                                                                                                      n = init_.size();
info.assign(4 << __lg(n), Info());
function <void(
    int, int, int)> build = [&](int p, int l, int r) {
    if (r - l == 1) {
                  }
             return ans;
                                                                                                                                  info[p] = init_[l];
      }
T rangeSum
                                                                                                                                  return;
             (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                                                                                                                            int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                    (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
     }
                                                                                                                            pull(p);
};
                                                                                                                      build(1, 0, n);
3.3 DSU [d41d8c]
                                                                                                                void pull(int p) {
    info[p] = info[p * 2] + info[p * 2 + 1];
struct DSU {
      int n;
       vector < int > boss, siz;
                                                                                                                void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
      info[p] = v; return;
}
      DSU() {}
      DSU(int n_) { init(n_); }
      void init(int __) {
    n = n_; boss.resize(n);
    iota(boss.begin(), boss.end(), 0);
                                                                                                                      int m = (l + r) / 2;
if (x < m) modify(2 * p, l, m, x, v);
else modify(2 * p + 1, m, r, x, v);</pre>
             siz.assign(n, 1);
      int find(int x) {
   if (boss[x] == x) return x;
   return boss[x] = find(boss[x]);
                                                                                                                      pull(p);
                                                                                                                void modify(int p, const Info &i) {
                                                                                                                      modify(1, 0, n, p, i);
      bool same(int x, int y) {
    return find(x) == find(y);
                                                                                                               Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    return query(p *</pre>
      bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);
    if (siz[x] < siz[y]) swap(x, y);</pre>
                                                                                                                      return query(p
                                                                                                                             2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
             siz[x] += siz[y];
                                                                                                                Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
             boss[y] = x;
             n - -:
            return true;
                                                                                                                template < class F> // 尋找區間內,第一個符合條件的
                                                                                                                int findFirst
      int size(int x) {
    return siz[find(x)];
                                                                                                                     (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)
    return -1;
if (l >= x && r <= y && !pred(info[p]))</pre>
};
struct DSU {
                                                                                                                            return -1;
                                                                                                                      if (r - l == 1)
    return l;
      int n;
      vector<int> boss, siz, stk;
      DSU() {}
DSU(int n_) { init(n_); }
                                                                                                                      int m = (l + r)
                                                                                                                      int res = findFirst(2 * p, l, m, x, y, pred);
      void init(int n_) {
    n = n_;
    boss.resize(n);
                                                                                                                      if (res == -1)
                                                                                                                            res = findFirst(2 * p + 1, m, r, x, y, pred);
             iota(boss.begin(), boss.end(), 0);
                                                                                                                template < class F> // 若要找 last, 先右子樹遞迴即可
int findFirst(int l, int r, F & pred) {
return findFirst(1, 0, n, l, r, pred);
             siz.assign(n, 1);
             stk.clear();
      int find(int x) {
   return x == boss[x] ? x : find(boss[x]);
                                                                                                             ---define structure and info plus---
      bool same(int x, int y) {
    return find(x) == find(y);
                                                                                                         struct Info {
                                                                                                               int n = 0;
                                                                                                                int sum = 0;
      bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);
    siz[x] += siz[y];
    best[y] - x;</pre>
                                                                                                         Info operator+(const Info &a, const Info &b) {
                                                                                                                return { a.n + b.n, a.sum + b.sum };
                                                                                                         3.5 Lazy Segment [d41d8c]
             boss[v] = x;
                                                                                                        | template <class Info, class Tag>
             stk.push_back(y);
                                                                                                         struct LazySeg { // 左閉右開寫法
             return true:
                                                                                                                int n:
       void undo(int x) {
                                                                                                                vector<Info> info;
            while (stk.size() > x) {
   int y = stk.back();
                                                                                                               vector<Tag> tag;
LazySeg() : n(0) {}
LazySeg(int n_, Info v_ = Info()) {
                   stk.pop_back();
                   n++:
                                                                                                                      init(n_, v_);
                   siz[boss[y]] -= siz[y];
                   boss[y] = y;
                                                                                                                template <class T>
                                                                                                               LazySeg(vector<T> init_) {
   init(init_);
            }
       int size(int x) {
             return siz[find(x)];
                                                                                                                void init(int n_, Info v_ = Info()) {
                                                                                                                     init(vector(n_, v_));
}:
                                                                                                                template <class T>
                                                                                                               void init (vector<T> init_) {
    n = init_.size();
    info.assign(4 << __lg(n), Info());
    tag.assign(4 << __lg(n), Tag());</pre>
3.4 Segment [d41d8c]
template <class Info>
```

```
add = v.add:
                                                                                                              else {
                                                                                                                    add += v.add;
                                                                                                       }
                 int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                                                                                                 };
                                                                                                  struct Info {
                                                                                                       pull(p);
            build(1, 0, n);
                                                                                                             sum += (r - l) * v.add;
      void pull
             (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
      void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
   tag[p].apply(v);
                                                                                                        // Info& operator=(const Info &rhs) {
                                                                                                        //
//
// }
                                                                                                                 // 部分 assignment 使用 return *this;
      void push(int p, int l, int r) {
           int m = (l + r) / 2;
if (r - l >= 1) {
    apply(p * 2, l, m, tag[p]);
    apply(p * 2 + 1, m, r, tag[p]);
                                                                                                 Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
                                                                                                 }
                                                                                                  3.6 Treap [d41d8c]
            tag[p] = Tag();
                                                                                                 struct Treap {
   Treap *lc, *rc;
   int pri, siz; bool rev_valid;
   int val; int min;
     void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
}
                                                                                                        Treap(int val_) {
                 return:
                                                                                                             min = val = val_;
pri = rand();
           int m = (l + r) / 2;
push(p, l, r);
if (x < m) {</pre>
                                                                                                              lc = rc = nullptr;
                                                                                                             siz = 1; rev_valid = 0;
                 modify(2 * p, l, m, x, v);
                                                                                                        void pull() { // update siz or other information
           } else {
                                                                                                             siz = 1;
min = val;
                 modify(2 * p + 1, m, r, x, v);
                                                                                                             for (auto c : {lc, rc}) {
    if (!c) continue;
           pull(p);
      void modify(int p, const Info &i) {
                                                                                                                    siz += c->siz;
           modify(1, 0, n, p, i);
                                                                                                                   min = std::min(min, c->min);
                                                                                                             }
      Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    push(p, l, r);
}</pre>
                                                                                                        void push() {
                                                                                                              if (rev_valid) {
                                                                                                                   if (lc) rc);
if (lc) lc->rev_valid ^= 1;
if (rc) rc->rev_valid ^= 1;
            return query(p *
2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
                                                                                                              rev_valid = false;
      Info query
                                                                                                        int find(int k) { // 找到 min 是 k 的位置 (1-based)
             (int ql, int qr) { return query(1, 0, n, ql, qr); }
      void range_apply
                                                                                                             push();
           (int p, int l, int r, int ql, int qr, const Tag &v) {
if (qr <= l || ql >= r) return;
if (ql <= l && r <= qr) {</pre>
                                                                                                              int ls = (lc ? lc->siz : 0) + 1;
                                                                                                             if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
                 apply(p, l, r, v);
                 return;
                                                                                                       }
                                                                                                 };
int size(Treap *t) {
    return t ? t->siz : 0;
    - .
           int m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
                                                                                                  Treap *merge(Treap *a, Treap *b) {
                                                                                                        if (!a || !b) return a ? a : b;
a->push(); b->push();
if (a->pri > b->pri) {
a->rc = merge(a->rc, b);
            pull(p);
      void range_apply(int l, int r, const Tag &v) {
    range_apply(1, 0, n, l, r, v);
     }
                                                                                                             a->pull();
      template < class F> // 尋找區間內,第一個符合條件的
                                                                                                             return a:
      int findFirst
           (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {</pre>
                                                                                                             b->lc = merge(a, b->lc);
                                                                                                             b->pull();
                 return 1:
                                                                                                             return b;
            if (l >= x && r <= y && !pred(info[p])) {</pre>
                                                                                                       }
                 return -1;
                                                                                                  pair<Treap*, Treap*> split(Treap *t, int k) {
                                                                                                        // 分割前 k 個在 first,剩下的在 second if (t == nullptr) return {nullptr, nullptr};
            if (r - l == 1) {
                 return l:
                                                                                                        t->push();
                                                                                                        t->pusn();
if (size(t->lc) < k) {
    auto [a, b] = split(t->rc, k - size(t->lc) - 1);
    t->rc = a;
    t->pull();
}
            int m = (l + r) / 2;
           push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
           if (res ==
                 res = findFirst(2 * p + 1, m, r, x, y, pred);
                                                                                                             return {t, b};
           return res;
                                                                                                        else {
                                                                                                             auto [a, b] = split(t->lc, k);
t->lc = b;
     template < class F> // 若要找 last , 先右子樹遞迴即可
int findFirst(int l, int r, F & pred) {
    return findFirst(1, 0, n, l, r, pred);
                                                                                                             t->pull();
                                                                                                             return {a, t};
                                                                                                       }
     }
// ---define structure and info plus---
struct Tag { // 有些 Tag 不用 push 例如 sweepLine
   int set_val; int add;
   void apply(const Tag& v) {
      if (v.set_val) {
                                                                                                  void Print(Treap *t) {
   if (!t) return;
                                                                                                        t->push();
                                                                                                        Print(t->lc);
cout << t->val;
                                                                                                        Print(t->rc);
                 set_val = v.set_val;
                                                                                                 }
```

3.7 Mo [d41d8c]

4 Flow

4.1 Dinic [aa12d4]

```
template < class T>
struct Dinic {
      struct Edge {
               int to;
              T flow, cap; // 流量跟容量
       int n, m, s, t;
const T INF_FlOW = 1 << 30;
       vector<vector<int>> adj; // 此點對應的 edges 編號
       vector<Edge> edges; // 幫每個 edge 編號
      vector <Edge> edges; // 幫時個 edg.
vector <int> dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_; m = 0;
    dis.resize(n); ptr.resize(n);
    adj.assign(n, vector <int>{});
    edges.clear();
       void add edge(int u, int v, T cap) {
              // 偶數 id 是正向邊
// 偶數 id 是正向邊
ges.push_back({ v, 0, cap });
edges.push_back({ u, 0, 0 });
adj[u].push_back(m++);
adj[v].push_back(m++);
      bool bfs() {
    fill(dis.begin(), dis.end(), -1);
    dis[s] = 0; queue<int> q;
               q.push(s);
              while (!q.empty() && dis[t] == -1) {
  int u = q.front(); q.pop();
  for (int id : adj[u]) {
    Edge &e = edges[id];
    if (e.flow == e.cap) continue;
                              if (dis[e.to] == -1) {
    dis[e.to] = dis[u] + 1;
                                      q.push(e.to);
                      }
               return dis[t] != -1;
      }
T dfs(int u, T flow) {
   if (flow == 0) return 0;
   if (u == t) return flow;
               for (int
                      &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {
Edge &e = edges[adj[u][cur]];
if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;
T mn = dfs(e.to, min(flow, e.cap - e.flow));</pre>
                       if (mn > 0) {
    e.flow += mn:
                              edges[adj[u][cur] ^ 1].flow -= mn;
                              return mn;
                      }
               }
               return 0; // 到不了終點就會 return 0
       s = s_; t = t_; T flow = 0;
while (bfs()) {
                      fill(ptr.begin(), ptr.end(), 0);
                      while (true) {
   T res = dfs(s, INF_Flow);
   if (res == 0) break;
                              flow += res;
                      }
               return flow;
```

```
void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
        }
};
 4.2 Min Cut [44ae6c]
        int n, m; cin >> n >> m;
Dinic <int >> g(n);
for (int i = 0; i < m; i++) {</pre>
               int u, v, cap = 1;
               cin >> u >> v;
               u--; v--;
               g.add_edge(u, v, cap);
               g.add_edge(v, u, cap);
        int res = g.work(0, n - 1);
cout << res << "\n";
if (res == 0) return;</pre>
         vector<int> vis(n);
        auto find = [&](auto self, int u) -> void {
   if (!vis[u]) {
                      vis[u] = 1;
                      for (int id : g.adj[u])
                            auto e = g.edges[id];
if (e.cap - e.flow > 0) {
                                   self(self, e.to);
                     }
              }
       };
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
        ruto e = g.edges[id];
        ruto e = g.edges[id];
}</pre>
                      auto e = g.edges[id];
if (!vis[e.to]) {
    cout << i + 1 << " " << e.to + 1 << " | n";</pre>
               }
       }
}
 4.3 MCMF [77fc99]
 template < class Tf, class Tc>
  struct MCMF {
        struct Edge {
   int to;
               Tf flow, cap; // 流量跟容量
               Tc cost;
         // 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就好
        int n, m, s, t;

const Tf INF_FLOW = 1 << 30;

const Tc INF_COST = 1 << 30;
         vector<vector<int>> adj;
        vector<Edge> edges; // 幫每個 edge 編號
vector<Tc> dis, pot; // johnson algorithm, using spfa
        vector<int> rt; // 路徑恢復, 對應 id
        vector < tint > (t, // *** | t, // *** | t, // *** |
vector < bool > inq;
MCMF(int n = 0) { init(n_); }
void init(int n_) {
    n = n_; m = 0;
    edges.clear();
    id = coincip | vector < int > {
               adj.assign(n, vector<int>{});
        void add_edge(int u, int v, Tf cap, Tc cost){
   edges.push_back({v, 0, cap, cost});
   edges.push_back({u, 0, 0, -cost});
               adj[u].push_back(m++);
               adj[v].push_back(m++);
              dis.assign(n, INF_COST);
rt.assign(n, -1); inq.assign(n, false);
queue<int> q;
q.push(s), dis[s] = 0, inq[s] = true;
               while (!q.empty()) {
   int u = q.front(); q.pop();
                     q.push(v); inq[v] = true;
                            }
                     }
               return dis[t] != INF_COST;
        bool dijkstra() {
               dis.assign(n, INF_COST); rt.assign(n, -1);
priority_queue<pair<Tc, int>,
```

vector<pair<Tc, int>>, greater<pair<Tc, int>>> pq;

```
dis[s] = 0; pq.emplace(dis[s], s);
              while (!pq.empty()) {
                    auto [d, u] = pq.top(); pq.pop();
if (dis[u] < d) continue;
for (int id : adj[u]) {</pre>
                           pq.emplace(ndis, v);
                    }
              return dis[t] != INF_COST;
       // 限定 flow, 最小化 cost
      pair<If, Tc> work_flow(int s_, int t_, Tf need) {
    s = s_, t = t_; pot.assign(n, 0);
    If flow{}; Tc cost{}; bool fr = true;
    while ((fr ? spfa() : dijkstra())) {
        for (int i = 0; i < n; i++) {
            dis[i] += pot[i] - pot[s];
        }
}</pre>
                    (f, edges[rt[i]].cap - edges[rt[i]].flow);
                     f = min<Tf>(f, need);
                    for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
                    flow += f; need -= f;
cost += f * dis[t]; fr = false;
                    swap(dis, pot);
if (need == 0) break;
              return make_pair(flow, cost);
       // 限定 cost, 最大化 flow
       // MR LE COST, NX 入L flow
pair<Tf, Tc> work_budget(int s_, int t_, Tc budget) {
    s = s_, t = t_; pot.assign(n, 0);
    Tf flow{}; Tc cost{}; bool fr = true;
    while ((fr ? spfa() : dijkstra())) {
        for (int i = 0; i < n; i++) {
            dis[i] += pot[i] - pot[s];
        }
                    Tf f = INF_FLOW;
                    for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                   (f, edges[rt[i]].cap - edges[rt[i]].flow);
                     f = min<Tf>(f, budget / dis[t]);
                    for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
   edges[rt[i]].flow += f;
   edges[rt[i] ^ 1].flow -= f;
                    flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
                    swap(dis, pot);
if (budget == 0 || f == 0) break;
              return make_pair(flow, cost);
       void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
};
```

4.4 Hangarian [dfa1c4]

```
struct Hangarian { // 0-based
      int n, m;
vector<vector<int>> adj;
      vector < vector < int > ag,
vector < int > used, vis;
vector < pair < int , int >> match;
Hangarian(int n_ = 0, int m_ = 0) {
   init(n_, m_);
}
      void init(int n_, int m_) {
            n = n_; m = m_;
adj.assign(n + m, vector<int>());
used.assign(n + m, -1);
             vis.assign(n + m, \theta);
      void addEdge(int u, int v) {
    adj[u].push_back(n + v);
             adj[n + v].push_back(u);
      bool dfs(int u) {
             int sz = adj[u].size();
for (int i = 0; i < sz; i++) {
                    int v = adj[u][i];
                   if (vis[v] == 0) {
    vis[v] = 1;
                          if (used[v] == -1 || dfs(used[v])) {
                                used[v] = u;
                                return true;
                   }
```

```
    return false;
}

vector<pair<int, int>> work() {
    match.clear(); used.assign(n + m, -1);
    vis.assign(n + m, 0);
    for (int i = 0; i < n; i++) {
        fill(vis.begin(), vis.end(), 0); dfs(i);
    }

    for (int i = n; i < n + m; i++) {
        if (used[i] != -1) {
            match.push_back(make_pair(used[i], i - n));
        }
    return match;
}
</pre>
```

4.5 Theorem [d41d8c]

5 String

5.1 Hash [852711]

```
constexpr int B = 59;
vector<Z> Hash(string &s) {
    vector<Z> ans {0};
    for (auto c : s) {
        ans.push_back(ans.back() * B + (c - 'a' + 1));
    }
    return ans;
}
void solve() {
    string s, sub;
    cin >> s >> sub;
    auto a = Hash(s);
    auto q = Hash(sub);
    auto find = q.back();
    int ans = 0;
    int l = 1, r = sub.size(), len = sub.size();
    while (r <= s.size()) {
        if (a[r] - a[l - 1] * power(Z(B), len) == find) {
            ans++;
        }
        l++, r++;
    }
    cout << ans << "|n";
}</pre>
```

5.2 KMP [cddfd9]

```
struct KMP {
       string sub;
vector<int> failure;
       KMP(string sub_) {
    sub_= sub_;
              failure.resize(sub.size(), -1);
buildFailFunction();
       void buildFailFunction() {
    for (int i = 1; i < (int)sub.size(); i++) {
        int now = failure[i - 1];
}</pre>
                     while (now != -1
                     && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
       }
       vector<int> match(string &s) {
              vector<int> match;
              for (int i = 0, now = -1; i < (int)s.size(); i++) {
// now is the compare sucessed length -1
                     while (s[i] !=
                     sub[now + 1] && now != -1) now = failure[now];
// failure stores if comparison fail, move to where
if (s[i] == sub[now + 1]) now++;
if (now + 1 == (int)sub.size()) {
                            match.push_back(i - now);
                            now = failure[now];
              }
```

```
return match:
};
```

Z Function [764b31]

```
|// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
 // 的最長公共前綴 (LCP) 的長度
 vector<int> Z(string s) {
       int n = s.size();
       tht n = S.Stze(),
vector <int> z(n); z[0] = n;
for (int i = 1, j = 1; i < n; i++) {
    z[i] = max(0, min(j + z[j] - i, z[i - j]));
    while (i + z[i] < n && s[z[i]] == s[i + z[i]])</pre>
             if (i + z[i] > j + z[j]) j = i;
       return z; // 最後一格不算
```

5.4 SA [d40e3e]

```
struct SuffixArray {
      int n; string s;
vector<int> sa, rk, lc;
      // n: 字串長度
      // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
       ... // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
      // lc: LCP
      數組,lc[i] 表示 sa[i] 和 sa[i + 1] 的最長公共前綴長度
SuffixArray(const string &s_) {
    s = s_; n = s.length();
    sa.resize(n);
             lc.resize(n - 1):
             rk.resize(n);
             iota(sa.begin(), sa.end(), 0);
             rotida(sa.begin(), sa.ein(), o),
sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });
rk[sa[0]] = 0;
for (int i = 1; i < n; ++i)
    rk[sa[i]]
    rk[sa[i]] + (s[sa[i]] != s[sa[i - 1]]);
int k = 1.</pre>
             int k = 1;
vector<int> tmp, cnt(n);
             tmp.reserve(n);
                                     - 1]] < n - 1) {
             while (rk[sa[n
                   tmp.clear();
for (int i = 0; i < k; ++i)</pre>
                          tmp.push_back(n - k + i);
                   for (auto i : sa)
    if (i >= k)
        tmp.push_back(i - k);
                   fill(cnt.begin(), cnt.end(), 0);
for (int i = 0; i < n; ++i)</pre>
                           ++cnt[rk[i]];
                   for (int i = 1; i < n; ++i)
   cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; --i)
                          sa[--cnt[rk[tmp[i]]]] = tmp[i];
                   for (int i = 0, j = 0; i < n; ++i) {
   if (rk[i] == 0) {</pre>
                   j = 0;
} else {
                          for (j
                                  `-= j > 0; i + j < n && sa[rk[i] - 1] + j
< n && s[i + j] == s[sa[rk[i] - 1] + j]; )
                          lc[rk[i] - 1] = j;
             }
      string getLCP() {
   int cp = 0, k, lcp = 0, p;
   for (int i = 0; i < n; i++) {
      if (!rk[i]) continue;
      k = sa[rk[i] - 1];
}</pre>
                   k = Sa[rK[t] - 1],
if (cp) cp--;
while (s[i + cp] == s[k + cp]) cp++;
if (cp > lcp){
    lcp = cp;
    p = i;
}
             if (lcp) {
             return s.substr(p, lcp);
} else {
                   return "-1";
      }
};
```

5.5 Manacher [9c9ca6]

```
// 找到對於每個位置的迴文半徑
vector < int > manacher(string s) {
    string t = "#";
    for (auto c : s) {
       t += c;
t += '#';
    int n = t.size();
vector<int> r(n);
    for (int i = 0, j =
         if (2
        while (i - r[i] >
             0 \& i + r[i] < n \& t[i - r[i]] == t[i + r[i]]) {
            r[i] += 1;
        if (i + r[i] > j + r[j]) {
        }
    return r;
    // # a # b # a #
// 1 2 1 4 1 2 1
    // # a # b # b # a #
// 1 2 1 2 5 2 1 2 1
    // 值 -1 代表原回文字串長度
    // (id - val + 1) / 2 可得原字串回文開頭
5.6 SAM [d15619]
```

```
struct SAM {
     static constexpr int ALPHABET_SIZE = 26;
     struct Node {
          int len:
          int link;
          array<int, ALPHABET_SIZE> next;
          Node() : len{}, link{}, next{} {}
      vector<Node> t;
     vector Nude > 1;
sam() { init(); }
void init() {
    t.assign(2, Node())
    t[0].next.fill(1);
                          Node());
          t[0].len = -1;
     int newNode() {
    t.emplace_back();
    return t.size() - 1;
     int extend(int p, int c) {
   if (t[p].next[c]) {
                int q = t[p].next[c];
                if (t[q].len == t[p].len + 1) {
                     return q;
                int r = newNode();
t[r].len = t[p].len + 1;
t[r].link = t[q].link;
                t[r].next = t[q].next;
                t[q].link = r;
                while (t[p].next[c] == q) {
                     t[p].next[c] =
p = t[p].link;
          int cur = newNode():
          t[cur].len = t[p].len + 1;
          while (!t[p].next[c]) {
               t[p].next[c] = cur;
p = t[p].link;
          t[cur].link = extend(p, c);
          return cur:
    }
void solve() {
    string s; cin >> s;
     int n = s.length();
     vector < int > pos(n + 1); // s[i - 1] 的後綴終點位置
     pos[0] = 1;
     SAM sam;
     for (int i = 0; i < n; i++) {</pre>
          pos[i + 1] = sam.extend(pos[i], s[i] - 'a');
}
```

5.7 Trie [3b3aa0]

```
struct trie_node {
    bool is_word;
    vector<trie_node *> children;
    trie_node() {
   is_word = false;
         children.resize(26, NULL);
```

Math

6.1 Prime [4e0864]

6

```
a^{(m-1)} = 1 \pmod{m}
                                                                                                   // a^(m-1) = 1 (Mod M)
// a^(m-2) = 1/a (Mod M)
// EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)
// Filter + DP; DP save min factor 'recur' factor decomposition
// FacNums = (x+1)(y+1)(z+1)...
      trie_node *root = new trie_node();
      void insert(string &s) {
    trie_node *cur = root;
            for (int i = 0; i < s.size(); i++) {
   int idx = s[i] - 'a';
   if (cur->children[idx] == NULL) {
      cur->children[idx] = new trie_node();
}
                                                                                                   // FacSum = (a^0+a^1...+a^x)(b^0+...+b^y)

// FacMul = N(x+1)(y+1)(z+1)/2

vector<int> is_prime;
                                                                                                   // 1 代表是質數,非 1 不是
                                                                                                   void init(int n) {
                                                                                                         cur = cur->children[idx]:
            cur->is_word = true;
      bool is_in_trie(string &s) {
                                                                                                                           is_prime[j] = i;
            trie_node *cur = root;

for (int i = 0; i < s.size(); i++) {

    if (cur->
                                                                                                         }
                  children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
                                                                                                   int main() {
                                                                                                          init(1000000);
                                                                                                         ll ans = 1, q; cin >> q;
map<ll, ll> mp;
while (is_prime[q] != 1) {
     int search_i_start(string &s, int i, vector<int> &dp) {
    trie_node *cur = root;
                                                                                                               mp[is_prime[q]]++;
q /= is_prime[q];
            int sz = s.size(), ans = 0;
for (int j = i; j < sz; j++) {
    if (cur</pre>
                                                                                                         if (q != 1) mp[q]++;
for (auto [a, b] : mp) ans *= b + 1;
cout << ans << "\n";</pre>
                 -->children[s[j] - 'a'] == nullptr) return ans;
cur = cur->children[s[j] - 'a'];
if (cur->is_word)
    (ans += dp[j + 1]) %= mod;
                                                                                                   6.2 Modulo [a1aab8]
            return ans:
     }
                                                                                                   constexpr T power(T a, ll b) {
  T res {1};
  for (; b; b /= 2, a *= a)
      if (b % 2) res *= a;
int main() {
     // 找到 sub 集合裡,可以重複用,組成 s 的組數 Trie trie;
     string s; cin >> s;
int sz = s.size();
                                                                                                         return res;
                                                                                                   constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
    res %= p;
      // dp 代表 i 開頭到最後的配對總數
      // 找到有結尾為 stop 的 dp[i] += dp[j + 1]
      int n; cin >> n;
                                                                                                          if (res < 0) res += p;
      vector <int> dp(sz + 1, 0);
for (int i = 0; i < n; i++) {
    string sub; cin >> sub;
                                                                                                         return res;
                                                                                                   template < ll P >
            trie.insert(sub);
                                                                                                   struct MInt {
    ll x;
     dp[sz] = 1;
for (int i = sz - 1; i >= 0; i--) {
                                                                                                         constexpr MInt() : x {0} {}
constexpr MInt(ll x) : x {norm(x % getMod())} {}
static ll Mod;
            dp[i] = trie.search_i_start(s, i, dp);
                                                                                                         constexpr static ll getMod() {
   if (P > 0) return P;
      cout << dp[0] << endl;</pre>
                                                                                                               else return Mod;
5.8 Duval [f9dcca]
                                                                                                         constexpr static void setMod(ll Mod_) {
                                                                                                               Mod = Mod_;
// duval_algorithm
// 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
                                                                                                         constexpr ll norm(ll x) const {
vector<string> duval(string s) {
                                                                                                               if (x < 0) x += getMod();
if (x >= getMod()) x -= getMod();
      int i = 0, n = s.size();
vector<string> res;
     vector < string > res;
while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
   }</pre>
                                                                                                         constexpr ll val() const { return x; }
constexpr MInt operator-() const {
                                                                                                               MInt res;
                  else k++;
                                                                                                               res.x = norm(getMod() - x);
return res;
            while (i <= k) {</pre>
                                                                                                         constexpr MInt inv() const {
   return power(*this, getMod() - 2);
                  res.push_back(s.substr(i, j - k));
                  i += i - k:
                                                                                                         constexpr MInt & operator *= (MInt rhs) & {
    if (getMod() < (1ULL << 31)) {
        x = x * rhs.x % int(getMod());
}</pre>
      return res;
}
                                                                                                               } else {
// 最小旋轉字串
                                                                                                                     x = mul(x, rhs.x, getMod());
string min_round(string s) {
      s += s;
int i = 0, n = s.size();
      int t = 0,
int start = i;
while (i < n / 2) {</pre>
                                                                                                         constexpr MInt & operator += (MInt rhs) & {
    x = norm(x + rhs.x);
           return *this;
                                                                                                         constexpr MInt &operator -= (MInt rhs) & {
                                                                                                               x = norm(x - rhs.x);
                  else k++;
                                                                                                                return *this:
                                                                                                         constexpr MInt &operator/=(MInt rhs) & {
            while (i <= k) {
    i += j - k;</pre>
                                                                                                               return *this *= rhs.inv();
                                                                                                         friend constexpr MInt operator*(MInt lhs, MInt rhs) {
                                                                                                               MInt res = lhs; return res *= rhs;
      return s.substr(start, n / 2);
                                                                                                         friend constexpr MInt operator+(MInt lhs, MInt rhs) {
                                                                                                               MInt res = lhs; return res += rhs;
```

friend constexpr MInt operator - (MInt lhs. MInt rhs) {

MInt res = lhs; return res -= rhs;

```
friend constexpr MInt operator/(MInt lhs, MInt rhs) {
   MInt res = lhs; return res /= rhs;
     friend constexor
            std::istream &operator>>(std::istream &is, MInt &a) {
          ll v; is >> v; a = MInt(v); return is;
     friend constexpr std::
           ostream & operator << (std::ostream &os, const MInt &a) {
          return os << a.val();</pre>
     friend constexpr bool operator==(MInt lhs, MInt rhs) {
          return lhs.val() == rhs.val();
     friend constexpr bool operator!=(MInt lhs, MInt rhs) {
          return lhs.val() != rhs.val();
     rriend constexpr bool operator <(MInt lhs, MInt rhs) {
   return lhs.val() < rhs.val();</pre>
    }
template<>
ll MInt<0>::Mod = 998244353;
constexpr int P = 1e9 + 7;
using Z = MInt<P>;
```

6.3 Combination [878efe]

```
finvfac[m] = _fac[m].inv();
for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i -
            n = m;
      Z fac(ll m) {
   if (m > n) init(2 * m);
   return _fac[m];
      Invfac(ll m) {
   if (m > n) init(2 * m);
   return _invfac[m];
      }
Z inv(ll m) {
   if (m > n) init(2 * m);
   return _inv[m];
       If binom(ll n, ll m) {
   if (n < m || m < 0) return 0;
   return fac(n) * invfac(m) * invfac(n - m);</pre>
       |} comb; // 注意宣告, 若要換模數需重新宣告
```

6.4 CRT [d41d8c]

```
ll exgcd(ll a, ll b, ll &x, ll &y) {
      if (!b) {
    x = 1, y = 0;
    return a;
      il g = exgcd(b, a \% b, y, x);
      y -= a / b * x;
      return g;
il inv(ll x, ll m){
      ll`a, b;
      exgcd(x, m, a, b);
      a %= m;
if (a < 0) a += m;
      return a;
// remain, mod
ll CRT(vector<pair<ll, ll>> &a){
      ll prod = 1;
for (auto x : a) {
    prod *= x.second;
      ll res = 0;
      for (auto x : a) {
   auto t = prod / x.second;
   res += x.first * t % prod * inv(t, x.second) % prod;
   if(res >= prod) res -= prod;
      return res;
```

6.5 Matrix [08b5fe]

```
template < class T>
struct Mat {
      int m, n;
constexpr static ll mod = 1e9 + 7;
vector<vector<!>> matrix;
Mat(int n_ = 0) { init(n_, n_); }
Mat(int m_, int n_) { init(m_, n_); }
Mat(vector<vector<!>> matrix_) { init(matrix_); }
      matrix.assign(m, vector<T>(n));
      void init(vector<vector<T>> &matrix_) {
           m = matrix_.size();
n = matrix_[0].size();
           matrix = matrix_;
      vector<vector<T>> unit(int n) {
           vector<vector<l>> res(n, vector<l>(n));
for (int i = 0; i < n; i++) {
    res[i][i] = 1;</pre>
           return res:
      constexpr Mat &operator*=(const Mat& rhs) & {
           assert(matrix[0].size() == rhs.matrix.size());
int m = matrix.size()
                   , k = matrix[0].size(), n = rhs.matrix[0].size();
           l] * rhs.matrix[l][j] % mod)) %= mod;
                 }
           matrix = ans.matrix;
return *this;
      constexpr Mat &operator^=(ll p) & {
   assert(m == n); assert(p >= 0);
   Mat ans(p-- == 0 ? unit(m) : matrix);
            while (p > 0) {
   if (p & 1) ans *= *this;
   *this *= *this;
                 p >>= 1;
            matrix = ans.matrix;
            return *this;
      friend Mat operator*(Mat lhs, const Mat &rhs) {
           lhs *= rhs:
            return lhs;
      friend Mat operator^(Mat lhs, const ll p) {
            lhs ^= p;
};
// fn = fn-3 + fn-2 + fn-1
// 初始矩陣 轉移式
// f4 f3 f2 f1 1 0 f5 f4 f3
// f3 f2 f1 1 0 1 => f4 f3 f2
// f2 f1 f0 1 0 0 f3 f2 f1
```

6.6 Integer Partition [595ed2]

```
// CSES_Sum_of_Divisors
// C25_3um_0__DtvtSu/s
const int mod = 1e9 + 7;
const int inv_2 = 500000004;
// n / 1 * 1 + n / 2 * 2 + n / 3 * 3 + ... + n / n * n
int main() {
       ll ans = 0;
      ll n; cin >> n;
for (ll l = 1, r; l <= n; l = r + 1) {
    r = n / (n / l);</pre>
             ll val = n / l; // n / l 到 n / r 一樣的值ll sum = (((l + r) % mod) *
                    ((r - l + 1) % mod)) % mod * inv_2; // l 加到 r
             val %= mod; sum %= mod;
ans += val * sum;
             ans %= mod:
       cout << ans << "\n";
}
```

6.7 Mobius Theorem

- 數論分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^{n} f(i)g(\left|\frac{n}{i}\right|)$ 的和式。當可以在O(1)內計算f(r)-f(l)或已經預處理 出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d|n} \mu(d) = \begin{cases} 1 & \text{for } n = 1 \\ 0 & \text{for } n \neq 0 \end{cases}$$

- 2. μ 是常數函數 1 的反元素 $\Rightarrow \mu*1=\epsilon$, $\epsilon(n)$ 只在n=1時為 1,其餘情況皆為 0。
- $-\phi$ 歐拉函數: x 以下與 x 互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^{i}) \\ &= 1 + p^{0}(p-1) + p^{1}(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^{c} \\ &= id \end{split}$$

• 莫比烏斯反演公式

-
$$f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$$

- $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

例子

$$\begin{split} &\sum_{i=a}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \frac{\left\lfloor \frac{y}{k} \right\rfloor}{\left\lfloor \frac{y}{k} \right\rfloor} \\ &= \sum_{d=1}^{\infty} \mu(d) \left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor) \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

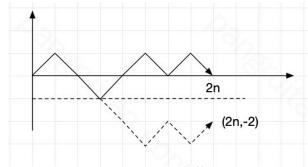
6.8 Mobius Inverse [d41d8c]

const int maxn = 2e5;

```
ll mobius_pref[maxn];
void init() {
      mobius_pref[1] = 1;
      vector<ll> wei
      (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
    }
                  continue; // 包含平方
            if (wei[i] == 0) {
                  wet[i] == 0) {
wei[i] = 1;
for (ll j = 2; i * j < maxn; j++) {
    if (j % i == 0) wei[i * j] = -1;
    else if (wei[i * j] != -1) wei[i * j]++;</pre>
                  }
            mobius pref[i]
                   = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
     }
void solve() {
      ll a, b, c, d, k; cin >> a >> b >> c >> d >> k;

auto cal = [&](ll x, ll y) -> int {
            cout << cal
             (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k, (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n"
}
```

6.9 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有x 個,往下有y 個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.10 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- · X/G:本質不同的方案的集合
- X^g : 對於某一種操作 g,所有方案中,經過 g 這種翻轉後保持不變的方案的集合
- 集合取絕對值代表集合數

7 Search and Gready

7.1 Binary Search [d41d8c]

```
int main() {
    int l = 1, r = 10;
    // 1 to tar, find tar
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}</pre>
```

7.2 Ternary Search [d41d8c]

8 Тгее

8.1 LCA [601e2d]

```
}
}
int lca(int a, int b) {
    if (depth[a] < depth[b]) swap(a, b);
    int pull = depth[a] - depth[b];
    for (int i = 0; i < 18; i++) {
        if (pull & (1 << i)) {
            a = par[a][i];
        }
}
if (a == b) return a;
for (int i = 17; i >= 0; i--) {
        if (par[a][i] != par[b][i]) {
            a = par[a][i], b = par[b][i];
        }
}
return par[a][0];
}
```

8.2 Centroid Decomposition [4a66fb]

```
struct CenDecom {
       int n;
        vector<vector<int>> adj;
       vector < bool > vis;
vector < int > siz;
       CenDecom() {}
CenDecom(int n_) { init(n_); }
        void init(int n_) {
              adj.assign(n, {});
vis.assign(n, false);
siz.assign(n, 1);
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void get_siz(int dep, int x, int p = -1) {
    siz[x] = 1;
              for (int y : adj[x]) {
   if (y == p || vis[y]) continue;
   get_siz(dep + 1, y, x);
                     siz[x] += siz[y];
              }
       fint get_cen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz) {
                            return get_cen(y, sz, x);
                     }
               return x;
       void work(int x = 0) {
              get_siz(0, x);
int cen = get_cen(x, siz[x]);
vis[cen] = true;
               // do something
               for (int y : adj[cen]) {
   if (vis[y]) continue;
                     work(y);
      }
};
```

8.3 Tree Flattening [5293b7]

```
bit.modify(mp[i].second + 1, -val[i]);
}

for (int i = 0; i < q; i++) {
    int op; cin >> op;
    if (op == 1) {
        int s, x; cin >> s >> x;
        int add = x - dfnToVal[mp[s].first];
        dfnToVal[mp[s].first] = x;
        bit.modify(mp[s].first, add);
        if (mp[s].first < n) { // root 就不用扣了
            bit.modify(mp[s].second + 1, -add);
        }
    else {
        int node; cin >> node;
        cout << bit.query(mp[node].first) << "\n";
    }
}
```

```
8.4 Heavy Light Decomposition [ad25b6]
struct HLD {
      int n, cur;
vector<int> siz, top, dep, parent, in, out, seq;
      vector<int> siz, top, dep, parent, in, out, seq;
vector<vector<int>> adj;
HLD(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
    n = n_; cur = 0;
    siz.resize(n); top.resize(n); dep.resize(n);
    parent.resize(n); in.resize(n); out.resize(n);
             seq.resize(n); adj.assign(n, {});
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void work(int root = 0) {
             top[root] = root;
dep[root] = 0;
parent[root] = -1
             parent[root]
             dfs1(root); dfs2(root);
       void dfs1(int u) {
    if (parent[u] != -1)
                    adj[u].erase(find (adj[u].begin(), adj[u].end(), parent[u]));
             for (auto &v : adj[u]) {
                    parent[v] = u, dep[v] = dep[u] + 1;
                    dfs1(v);
siz[u] += siz[v];
                    if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
                   } // 讓 adj[u][0] 是重子節點
       void dfs2(int u) {
             in[u] = cur++;
             seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
   top[v] = v == adj[u][0] ? top[u] : v;
                    dfs2(v);
             out[u] = cur;
      u = parent[top[u]];
} else {
                          v = parent[top[v]];
                   }
             return dep[u] < dep[v] ? u : v;</pre>
       int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
      int jump(int u, int k) {
    if (dep[u] < k) return -1;
    int d = dep[u] - k;
    while (dep[top[u]] > d)
        u = parent[top[u]];
    return seq[in[u] - dep[u] + d];
}
       bool isAncester(int u, int v) {
    // 判斷 u 是否是 v 的祖先
    return in[u] <= in[v] && in[v] < out[u];
       int rootedParent(int u, int v) {
             // 根據新根節點 u 計算 v 的父節點
             swap(u, v);
if (u == v) return u;
if (!isAncester(u, v)) return parent[u];
             auto it = upper_bound(adj
   [u].begin(), adj[u].end(), v, [&](int x, int y) {
   return in[x] < in[y];</pre>
```

}) - 1;
return *it;

```
int rootedSize(int u, int v) {
                // 根據新根節點 u 計算子樹 v 的大小
if (u == v) return n;
if (!isAncester(v, u)) return siz[v];
return n - siz[rootedParent(u, v)];
        int rootedLca(int a, int b, int c) {
   // 根據新的根節點計算三個節點 a \ b 和 c 的最近公共祖先
   return lca(a, b) ^ lca(b, c) ^ lca(c, a);
};
```

8.5 Link Cut Tree [29ae0d]

```
#include <bits/stdc++.h>
using namespace std;
using ll = long long;
constexpr int Mod = 51061;
struct Tag {
     ll add = 0;
     ll mul = 1:
     void apply(const Tag& v) {
    mul = mul * v.mul % Mod;
    add = (add * v.mul % Mod + v.add) % Mod;
    }
struct Info {
     ll val = 1;
ll sum = 1;
     void apply(int size, const Tag &v) {
   val = (val * v.mul % Mod + v.add) % Mod;
   sum = (sum * v.mul % Mod + v.add * size % Mod) % Mod;
     }
};
struct Node {
     Node *ch[2], *p;
int rev = 0;
int size = 1;
     void make_rev() {
    swap(ch[0], ch[1]);
    rev ^= 1;
     Node() : ch {nullptr, nullptr}, p(nullptr) {}
     Info info = Info();
Tag tag = Tag();
     void apply(const Tag &v) {
          info.apply(size, v);
          tag.apply(v);
     void push_tag() {
          if (rev) {
               if (ch[0]) ch[0]->make_rev();
if (ch[1]) ch[1]->make_rev();
               rev = 0;
          if (ch[0]) {
               ch[0]->apply(tag);
          if (ch[1]) {
               ch[1]->apply(tag);
          tag = Tag();
     void pull_info() {
          };
bool isroot(Node *t) {
     return t->p
            == nullptr || (t->p->ch[0] != t && t->p->ch[1] != t);
int pos(Node *t) { // 回傳 1 代表是右子節點 return t->p->ch[1] == t;
void rotate(Node *t) {
     Node *q = t->p;
int x = !pos(t);
     q->ch[!x] = t->ch[x];
if (t->ch[x]) {
          t->ch[x]->p = q;
     t - p = a - p:
     if (!isroot(q)) {
          q \rightarrow p \rightarrow ch[pos(q)] = t;
     t - ch[x] = q;
     q - p - t,
q->pull_info();
void splay(Node *t) { // 單點修改前必須呼叫
    // 把 t 旋轉到目前 splay 的根
```

```
while (!isroot(t)) {
          Node *p = t->p;
p->push_tag();
          t->push_tag();
rotate(t);
     t->push_tag();
t->pull_info();
void access(Node *t) {
     // 把從根到 t 的所有點都放在一條實鏈裡,使根
     // 到 t 成為一條實路徑,並且在同一棵 splay 裡
     for (Node *i = t, *q = nullptr; i; q = i, i = i->p) {
          splay(i);
i->ch[1] = q;
     splay(t);
}
void makeRoot(Node *t) { // 使 t 點成為其所在樹的根
     access(t):
     swap(t->ch[0], t->ch[1]);
     t->rev ^= 1;
Node* findRoot(Node *t) { // 找到 t 的 root
     access(t);
     splay(t);
     t->push_tag();
while (t->ch[0]) {
    t = t->ch[0];
          t->push_tag();
     splay(t);
     return t;
void link(Node *t, Node *p) {
     makeRoot(t);
     if (findRoot(p) != t) {
          makeRoot(p);
          t->p = p;
p->pull_info();
     }
}
bool cut(Node *x, Node *y) { // 不存在邊,回傳 false
     makeRoot(x);
     access(y);
     if( (y->ch[0] != x || x->ch[1]) return false;
y->ch[0]->p = nullptr;
y->ch[0] = nullptr;
     y->pull_info();
     return true:
void split(Node
       *x, Node *y) { // 以 y 做根, 區間修改用, apply 在 y 上
     makeRoot(x):
     access(y);
     splay(y);
}
bool isconnected(Node *x, Node *y) { // 查詢有沒有連通
     access(y);
return findRoot(x) == findRoot(y);
}
int main() {
   int n; cin >> n;
   vector <Node *> nodes(n);
     for (int i = 0; i < n; i++) {
    nodes[i] = new Node();
    nodes[i]->info.val = nodes[i]->info.sum = 1LL;
     for (int i = 0; i < n - 1; i++) {
   int u, v; cin >> u >> v;
   u--; v--;
          link(nodés[u], nodes[v]);
     for (int i = 0; i < q; i++) {</pre>
          char op; cin >> op; if (op == '+') {
               int u, v; cin >> u >> v;
               split(nodes[u], nodes[v]);
               Tag tag;
cin >> tag.add;
               tag.add % Mod;
               nodes[v]->apply(tag);
          else if (op == '-') {
               int u1, v1; cin >> u1 >> v1;
int u2, v2; cin >> u2 >> v2;
u1--; v1--; u2--; v2--;
               cut(nodes[u1], nodes[v1]);
link(nodes[u2], nodes[v2]);
          else if (op == '*') {
               int u, v; cin >> u >> v;
               u - -; v - -
               split(nodes[u], nodes[v]);
               Tag tag;
cin >> tag.mul;
```

mn.resize(n); res.resize(n);

int query(int v, int x) {

void add_edge(int u, int v) { adj[u].push_back(v); }

```
tag.mul % Mod:
                     nodes[v]->apply(tag);
               else {
                      int u, v; cin >> u >> v;
                                                                                                                                 rt[v] = p;
                                                                                                                                 return x ? p : mn[v];
                     split(nodes[u], nodes[v]);
cout << nodes[v]->info.sum << "\n";</pre>
       }
        return 0:
}
 8.6 Virtual Tree [622e69]
                                                                                                                          void build(int s) {
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
 // 可以建立虚樹達成快速樹 DP
 // 例如這題是有權樹,跟 vertex 1 隔開的最小成本
 int top = -1; vector<int>stk(maxn);
int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
        vt[stk[top - 1]].push_back(stk[top]), top--;
    if (stk[top - 1] != l) {
        vt[l] such back(stk[top]);
        vt[l] such back(stk[top]);
    }
}</pre>
              vt[l].push_back(stk[top]);
stk[top] = l;
           else vt[l].push_back(stk[top--]);
        stk[++top] = u;
 void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
    vt[u].clear();
                                                                                                                         }
                                                                                                                   9
                                                                                                                            DP
 void solve(int n, int q) {
        vector g(n + 1, vector<pair<int, int>>());
        vector vt(n + 1, vector <patr <pre>tht > ()); // dfs 完清除, 否則會退化
vector <ll> dp(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;
   g[u].push_back({v, w});
   g[v].push_back({u, w});
}
                                                                                                                  9.1 LCS [5781cf]
                                                                                                                   int main() {
                                                                                                                          int m, n; cin >> m >> n;
                                                                                                                          int L = 0:
        build_lca(n, g);
       build(n, g);
build(n, g);
for (int i = 0; i < q; i++) {
   int m; top = -1; cin >> m;
   vector<int> key(m);
   for (int j = 0; j < m; j++) {
      cin >> key[j];
      i - tour[baufil] = 1;
                     iskey[key[j]] = 1;
               key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
                     return dfn[a] < dfn[b];
               });
for (int x : key) insert(x, vt);
               auto dfs = [&](auto self, int u) -> void {
                                                                                                                                        else n--;
                     for (auto v : vt[u]) {
    self(self, v);
                                                                                                                                }
                                                                                                                          cout << s << "\n";
                             if (iskey[v]) {
                                   dp[u] += min_dis[v];
                                   // 砍掉 1 到 v 之間最短的路
                                                                                                                   9.2 LIS [66d09f]
                                   dp[u] += min(dp[v], min_dis[v]);
                                                                                                                   int main() {
                             iskey[v] = dp[v] = 0;
                                                                                                                          int dp[n]; vector<int> stk;
                      vt[u].clear();
               dfs(dfs, key[0]); // key[0] 一定是 root cout << dp[key[0]] << "\n";
               iskey[key[0]] = dp[key[0]] = 0;
                                                                                                                                        dp[i] = ++L;
                                                                                                                                } else
 8.7 Dominator Tree [baa540]
                                                                                                                                       auto it
 struct Dominator_tree {
        int n, id;
        int n, id;
vector < vector < int >> adj, radj, bucket;
vector < int >> sdom, dom, vis, rev, pa, rt, mn, res;
Dominator_tree(int n_ = 0) { init(n_); }
void init(int _n) {
    n = _n, id = 0;
    adj.assign(n, vector < int >());
    radj.assign(n, vector < int >());
}
              bucket.assign(n, vector<int>());
sdom.resize(n); dom.assign(n, -1);
vis.assign(n, -1); rev.resize(n);
pa.resize(n); rt.resize(n);
```

if (rt[v] == v) return x ? -1 : v; int p = query(rt[v], 1); if (p == -1) return x ? rt[v] : mn[v]; if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]]; dfs(s); for (int i = id - 1; i >= 0; i--) { for (int u : radj[i]) sdom[i] = min(sdom[i], sdom[query(u, 0)]); if (i) bucket[sdom[i]].push_back(i); for (int u : bucket[i]) { int p = query(u, 0); dom[u] = sdom[p] == i ? i : p; if (i) rt[i] = pa[i]; for (int i = 1; i < id; i++) if (dom[i] != sdom[i]) dom[i] = dom[dom[i]]; for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre> for (int i = 0; i < n; i++) dom[i] = res[i];</pre> string s1, s2; cin >> s1 >> s2; vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0)); dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]); int length = dp[m][n]; cout << length << "\n"; string s(length, 'c'); // backtracking while (m >= 1 && n >= 1) { if (s1[m - 1] == s2[n - 1]) { s[length - 1] = s1[m - 1]; m--, n--, length--; } else { if (dp[m - 1][n] > dp[m][n - 1]) m--; int n; cin >> n; vector <int> v(n); for (int i = 0; i < n; i++) cin >> v[i]; tht dp[ii], vector the stk, stk.push_back(v[0]); dp[0] = 1; int L = 1; for (int i = 1; i < n; i++) { if (v[i] > stk.back()) { stk.push_back(v[i]); } = lower_bound(stk.begin(), stk.end(), v[i]); *it = v[i]; dp[i] = it - stk.begin() + 1; vector < int > ans; cout << L << "|n"; for (int i = n - 1; i >= 0; i--) { if (dp[i] == L) { ans.push_back(v[i]), L--; } reverse(ans.begin(), ans.end()); reverse(ans.begin(), ans.end()); for (auto i : ans) cout << i <<</pre> 9.3 Edit Distance [308023] int main() { string s1, s2; cin >> s1 >> s2;

```
int n1 = s1.size(), n2 = s2.size();
      // dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元
vector <int> dp(n2 + 1);
                                                                                                         vector<<mark>int</mark>> ans;
                                                                                                        for (int i = n; i != 0;) {
    if (rec[i][0]) {
     vector <int> dp(n2 + 1);
iota(dp.begin(), dp.end(), 0);
for (int i = 1; i <= n1; i++) {
    vector <int> cur(n2 + 1); cur[0] = i;
    for (int j = 1; j <= n2; j++) {
        if (s1[i - 1] == s2[j - 1]) {
            cur[j] = dp[j - 1];
        }
        cur[j] = dp[j - 1];</pre>
                                                                                                                    ans.push_back(a[i].id);
                                                                                                                    i = rec[i][1];
                                                                                                              } else i--;
                 } else {
                                                                                                  9.6 Removal Game [7bb56b]
                       // s1 新增等價於 s2 砍掉
                        // dp[i][j] = min(s2 新增, 修改, s1 新増);
                                                                                                 | // 兩個人比賽,每個人輪流取一個數字且只能是頭尾
                                                                                                  // 問兩人都選得好,第一出手的人可取得的最大分數 int main() {
                        cur[j]
                               = min({cur[j - 1], dp[j - 1], dp[j]}) + 1;
                 }
                                                                                                        int n; cin >> n;
vector <ll> a(n);
for (int i = 0; i < n; i++) cin >> a[i];
            swap(dp. cur):
                                                                                                        vector dp(n, vector<ll>(n)); // i 到 j 區間的最大 diff
for (int i = n - 1; i >= 0; i--) {
      cout << dp[n2] << "\n";
                                                                                                              dp[i][i] = a[i];
9.4 Bitmask [a626f9]
                                                                                                              for (int j = i + 1; j < n; j++)
    dp[i][j] =</pre>
void hamiltonianPath(){
                                                                                                                           max(a[i] - dp[i + 1][j], a[j] - dp[i][j - 1]);
     int n, m; cin >> n >> m;
vector adj(n, vector <int >());
for (int i = 0; i < m; i++) {
    int u, v; cin >> u >> v;
                                                                                                        ^{\prime}// x + y = sum; // x - y = dp[0][n - 1] cout << (accumulate
                                                                                                                (a.begin(), a.end(), 0LL) + dp[0][n - 1]) / 2 << "\n";
                                                                                                  }
            adj[--v].push_back(--u);
                                                                                                  9.7 CHT [5f5c25]
      // 以...為終點,走過..
      vector dp(n, vector < int > (findBit(n)));
dp[0][1] = 1;
                                                                                                  struct Line {
    ll m, b;
      for (int mask = 1; mask < findBit(n); mask++) {
   if ((mask & 1) == 0) continue;
   for (int i = 0; i < n; i++) {</pre>
                                                                                                         Line(ll m = 0, ll b = 0) : m(m), b(b) {}
                                                                                                        ll eval(ll x) {
    return m * x + b;
                 if ((mask & findBit(i)) == 0) continue;
if (i == n - 1 && mask != findBit(n) - 1) continue;
int pre_mask = mask ^ findBit(i);
for (int j : adj[i]) {
    if ((pre_mask & findBit(j)) == 0) continue;
                                                                                                  };
                                                                                                  struct CHT { // 用在查詢單調斜率也單調
                                                                                                        int n, lptr, rptr; vector<Line> hull;
CHT(int n_ = 0, Line init_ = Line()) {
                        dp[i][mask
                               ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
                                                                                                              init(n_, init_);
                 }
           }
                                                                                                        void init(int n_ = 0, Line init_ = Line()) {
    n = n_; hull.resize(n); reset(init_);
      cout << dp[n - 1][findBit(n) - 1] << "\n";</pre>
                                                                                                        void reset(Line init_ = Line()) {
    lptr = rptr = 0; hull[0] = init_;
     void elevatorRides() {
                                                                                                        bool pop_front(Line &l1, Line &l2, ll x) {
                                                                                                              // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y
                                                                                                               // 代表查詢的當下,右線段的高度已經低於左線段了
                                                                                                               return l1.eval(x) >= l2.eval(x);
                                                                                                        bool pop_back(Line &l1, Line &l2, Line &l3) {
    // 本題斜率遞減、上凸包
                                                                                                              // 因此只要 12 跟
                                                                                                                      13 的 X 交點 <= 11 跟 13 的 X 交點, 12 就用不到了
                                                                                                              return (13.b - 12.b)

* (11.m - 13.m) <= (13.b - 11.b) * (12.m - 13.m);
                                                                                                         void insert(Line L) {
                                                                                                              while (rptr - lptr
                 } else if (dp[pre_mask
                                                                                                                      > 0 && pop_back(hull[rptr - 1], hull[rptr], L))
                       rptr - -;
                                                                                                              hull[++rptr] = L;
                                                                                                         ll query(ll x) {
                                                                                                               while (rptr
                                                                                                                                - lptr
                                                                                                                        0 && pop_front(hull[lptr], hull[lptr + 1], x))
            }
                                                                                                                    lptr+-
     cout << dp[findBit(n) - 1][0] << "\n";
                                                                                                              return hull[[lptr].eval(x);
                                                                                                  }:
9.5 Projects [0942aa]
                                                                                                  9.8 DNC [61c639]
int main() { // 排程有權重問題,輸出價值最多且時間最少
                                                                                                  constexpr int N = 3e3 + 5;
struct E {
                                                                                                  constexpr ll in = 3es + 5;
constexpr ll inf = 4e18;
// dp[k][j] = min(dp[k - 1][i] + cost[i][j])
// cost: (i, j]
ll dp[N][N]; // 1-based
ll get_cost(int l, int r) {}
      int from, to, w, id;
      bool operator < (const E &rhs) {</pre>
           return to == rhs.to ? w > rhs.w : to < rhs.to;
     int n; cin >> n; vector <E> a(n + 1);
for (int i = 1; i <= n; i++) {
   int u, v, w; cin >> u >> v >> w;
   a[i] = {u, v, w, i};
                                                                                                  void DNC(int k, int l, int r, int optl, int optr) {
    if (l > r) return;
    int m = (l + r) >> 1, opt = -1;
                                                                                                        dp[k][m] = inf;
for (int i = max(k, optl); i <= min(m, optr); i++) {</pre>
      vector<array<ll, 2>> dp(n + 1); // w, time
     vector<array<int, 2>> rec(n + 1); // 有沒選, 上個是誰
sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
    auto it = --lower_bound(all(a), E({0, a[i].from}),
                                                                                                              // 注意 i 的範圍、 get_cost 與 dp 的邊界
ll cur = dp[k - 1][i] + get_cost(i, m);
if (cur < dp[k][m]) {
                                                                                                                    dp[k][m] = cur, opt = i;
           lift = --tower_bound(at(a), E({0}, a[t].from}),
[](E x, E y){ return x.to < y.to; });
int id = it - a.begin(); dp[i] = dp[i - 1];
ll nw = dp[id][0] + a[i].w;
ll nt = dp[id][1] + a[i].to - a[i].from;
if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
    dp[i] = {nw, nt}; rec[i] = {1, id};
}
                                                                                                        DNC(k, l, m - 1, optl, opt);
DNC(k, m + 1, r, opt, optr);
```

int main() {

// first build cost...

9.9 LiChaoSegmentTree [a6e320]

```
constexpr ll Inf = 4e18;
// dp[i] = min(f[j] * s[i] + dp[j])
// y =
struct Line {
    ll m, b;
    Line(ll m = 0, ll b = Inf) : m(m), b(b) {}
ll eval(ll x) const { return m * x + b; }
struct LiChaoSeg { // 取 max 再變換就好
    int n;
vector<Line> info;
LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
          n = n_;
          info.assign(4 << __lg(n), Line());</pre>
     void update(Line line, int node, int l, int r) {
          int m = (l + r) / 2;
bool left = line.eval(l) < info[node].eval(l);</pre>
          bool mid = line.eval(m) < info[node].eval(m);</pre>
          if (mid) swap(info[node], line); // 如果新線段比較好
          if (r - l == 1) return;
          else if (left != mid) update(line, 2 * node, l, m);
          // 代表左半有交點
          else update(line, 2 * node + 1, m, r);
          // 代表如果有交點一定在右半
    void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
    if (r - l == 1) return info[node].eval(x);
    int m = (l + r) / 2;
          if (x < m) return
               min(info[node].eval(x), query(x, 2 * node, l, m));
          else return min(
   info[node].eval(x), query(x, 2 * node + 1, m, r));
     il query(int x) { return query(x, 1, 0, n); }
```

9.10 Codeforces Example [7d37ea]

```
// CF 1932 pF
 // 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
 // 請問在線段不重複的情況下,最多獲得幾分 int main() {
     int n, m;
cin >> n >> m;
     // 記錄每點有幾個線段
     // 再一個紀錄,包含這個點的左界
     cnt[l]++;
          cnt[r + 1]--;
     for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
     for (int i = n; i >= 2; i--) {
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
     vector < int > dp(n + 1);
     dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
          dp[i] = cnt[i];
if (l_side[i] != inf) {
    dp[i] += dp[l_side[i] - 1];
          dp[i] = max(dp[i], dp[i - 1]);
     cout << dp[n] << "\n";
}
 // CF 1935 pC
 // 給你每個事件的 a, b, 挑事件會把 a 全部加起來
 // 再加上 max(bi) - min(bi)
int main(){
   int n, k, ans = 0; cin >> n >> k;
     for (int i = 1; i <= n; i++) {
   int a, b; cin >> a >> b;
   v[i] = {a, b};
   if (a <= k) ans = 1;</pre>
     sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
     }); // 用 bi 來排,考慮第 i 個時可以先扣
     vector < vector < int >> dp(n + 1, vector < int > (n + 1, inf));
```

10 Geometry

10.1 Basic [d41d8c]

```
template < class T>
struct Point {
     Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) \{ \}
     template < class U>
     operator Point<U>() {
         return Point<U>(U(x), U(y));
     Point & operator += (const Point &p) & {
        x += p.x; y += p.y; return *this;
     Point &operator -= (const Point &p) & {
        x -= p.x; y -= p.y; return *this;
     Point &operator*=(const T &v) & {
    x *= v; y *= v; return *this;
     Point &operator/=(const T &v) & {
    x /= v; y /= v; return *this;
     Point operator - () const {
    return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
         return a += b;
     friend Point operator - (Point a, const Point &b) {
         return a -= b;
     friend Point operator*(Point a, const T &b) {
   return a *= b;
     friend Point operator/(Point a, const T &b) {
         return a /= b;
     friend Point operator*(const T &a, Point b) {
   return b *= a;
     friend bool operator == (const Point &a, const Point &b) {
         return a.x == b.x && a.y == b.y;
     friend istream &operator>>(istream &is, Point &p) {
         return is >> p.x >> p.y;
     friend ostream & operator << (ostream & os, const Point & p) {
   return os << "(" << p.x << ", " << p.y << ")";</pre>
    }
template < class T>
struct Line {
    Point <T> a:
     T dot(const Point<T> &a, const Point<T> &b) {
   return a.x * b.x + a.y * b.y;
T cross(const Point<T> &a, const Point<T> &b) {
   return a.x * b.y - a.y * b.x;
template < class T>
T square(const Point < T > &p) {
     return dot(p, p);
template < class T>
double length(const Point<T> &p)
    return sqrt(double(square(p)));
double length(const Line<T> &l) {
     return length(l.a - l.b);
template < class T>
Point<T> normalize(const Point<T> &p) {
    return p / length(p);
template < class T>
```

```
template < class T>
double distance(const Point<T> &a, const Point<T> &b) {
          return length(a - b);
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
 template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)
     return distance(p, l.a);</pre>
          if (dot(p - l.b, l.a - l.b) < 0)
    return distance(p, l.b);</pre>
           return distancePL(p, l);
template < class T>
Point<T> rotate(const Point<T> &a) {
           return Point(-a.y, a.x);
template < class T>
int sgn(const Point<T> &a) {
         return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
          return cross(l.b - l.a, p - l.a) > 0;
Point<T
    > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
    return l1.a + (l1.b - l1.a) * (cross(l2.b - l2.b) * (l2.b) * (l2.b)
                       l2.a, l1.a - l2.a) / cross(l2.b - l2.a, l1.a - l1.b));
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
           return cross(p - l.a, l.b - l.a) == 0 &&
    min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)</pre>
                                  (l.a.y, l.b.y) \ll p.y \ll max(l.a.y, l.b.y);
template < class T:
bool pointInPolygon
           (const Point<T> &a, const vector < Point < T>> &p) {
int n = p.size(), t = 0;
for (int i = 0; i < n; i++) {</pre>
           for (int i = 0; i < n; i++) {
   if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {</pre>
                                return true:
           for (int i = 0; i < n; i++) {
    auto u = p[i];
                      auto v = p[(i + 1) % n];
                      if (u.x < a.
                                  x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
                                 t ^= 1;
                      if (u.x >= a
                                   .x && v.x < a.x && pointOnLineLeft(a, Line(u, v)))</pre>
           return t == 1;
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
 // 3 : intersect at endpoint
template < class T>
tuple < int , Point < T > , Point < T >> segmentIntersection
             (const Line<T> &l1, const Line<T> &l2) {
          if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
    return {0, Point<T>(), Point<T>()};
if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
    return {0, Point<T>(), Point<T>());
           if (max(l1.a.y, l1.b.y) < min(l2.a.y, l
    return {0, Point<T>(), Point<T>()};
                                                                                                                  12.b.v))
          if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y))
  return {0, Point<T>(), Point<T>()};
if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
    return {0, Point<T>(), Point<T>()};
}
                     less {
    auto maxx1 = max(l1.a.x, l1.b.x);
    auto minx1 = min(l1.a.x, l1.b.x);
    auto maxy1 = max(l1.a.y, l1.b.y);
    auto miny1 = min(l1.a.y, l1.b.y);
    auto miny1 = min(l1.a.y, l1.b.y);
                                auto miny1 = min(l1.a.y, l1.b.y);
auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.y, l2.b.y);
auto miny2 = min(l2.a.y, l2.b.y);
Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
                                 if (!pointOnSegment(p1, l1))
                                 swap(p1.y, p2.y);
if (p1 == p2) {
                                           return {3, p1, p2};
                                           return {2, p1, p2};
                     }
```

```
auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
      Point p = lineIntersection(l1, l2);
if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
            return {1, p, p};
            return {3, p, p};
template < class T>
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
   if (get<0>(segmentIntersection(l1, l2)) != 0)
      return 0.0;
return min({distancePS(l1.a, l2), distancePS(l1
    .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
template < class T>
bool segmentInPolygon
       (const Line<T> &l, const vector<Point<T>> &p) {
      int n = p.size();
      if (!pointInPolygon(l.a, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
for (int i = 0; i < n; i++) {
    auto u = p[i];
}</pre>
            auto v = p[(i + 1) % n];
auto w = p[(i + 2) % n];
            auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
if (t == 1) return false;
if (t == 0) continue;
            if (t == 2) {
                  if (pointOnSegment(v, l) && v != l.a && v != l.b)
    if (cross(v - u, w - v) > 0)
        return false;
           || pointOnLineLeft(l.b, Line(v, u)))
                  } else if (p1 == v) {
                        if (l.a == v) {
    if (pointOnLineLeft(u, l)) {
        if (pointOnLineLeft(w, l))
}
                                          && pointOnLineLeft(w, Line(u, v)))
                                          return false:
                              } else {
   if (pointOnLineLeft(w, l)
        || pointOnLineLeft(w, Line(u, v)))
        return false;
                        } else if (l.b == v) {
    if (pointOnLineLeft(u, Line(l.b, l.a))) {
        if (pointOnLineLeft(w, Line(l.b, l.a)))
        && pointOnLineLeft(w, Line(u, v)))
                                          return false:
                              } else
                                    if (pointOnLineLeft(w, Line(l.b, l.a))
    || pointOnLineLeft(w, Line(u, v)))
    return false;
                       }
                 }
           }
      return true:
template < class T>
vector<Point<T>> hp(vector<Line<T>> lines) {
      auto d1 = l1.b - l1.a;
auto d2 = l2.b - l2.a;
            if (sgn(d1) != sgn(d2))
return sgn(d1) == 1
            return cross(d1, d2) > 0;
      deque<Line<T>> ls;
      deque < Point < T >> ps;
for (auto l : lines) {
    if (ls.empty()) {
                  ls.push_back(l);
                  continue:
            while (!ps.empty() && !pointOnLineLeft(ps.back(), l))
            ps.pop_back(), ls.pop_back();
while (!ps.empty() && !pointOnLineLeft(ps[θ], l))
ps.pop_front(), ls.pop_front();
            if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
```

10.2 Convex Hull [b5758d]

```
int main() {
      int n; cin >> n;
vector <P> P(n), U, L;
for (int i = 0; i < n; i++) {</pre>
             cin >> P[i];
            .end(), [](const Point<i64> &a, const Point<i64> &b) {
return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
      for (int i = 0; i < n; i++) {
    while (L.size() >= 2 && cross(L.back() -
        L[L.size() - 2], P[i] - L[L.size() - 2]) <= 0LL) {</pre>
                   L.pop_back();
             while (U.size() >= 2 && cross(U.back() -
                     U[U.size() - 2], P[i] - U[U.size() - 2]) >= 0LL){
                   U.pop_back();
                    empty() || !(L.back() == P[i])) L.push_back(P[i]);
            if (U.
                    empty() || !(U.back() == P[i])) U.push_back(P[i]);
      if (L.size() <= 2 && U.size() <= 2) {
            // No Hull
      cout << L.size() + U.size() - 2 << "|n";
for (int i = 0; i < L.size() - 1; i++) {
    cout << L[i].x << " " << L[i].y << "|n";</pre>
      for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << "\n";</pre>
```

10.3 MinEuclideanDistance [3020bc]

```
T distanceSquare(const Point<T> &a, const Point<T> &b) {
      return square(a - b);
for (int i = 0; i < n; i++) {
    ll x, y;
    cin >> x >> y;
    a[i] = Point<ll>(x, y);
      struct sortY {
           bool operator
   ()(const Point<ll> &a, const Point<ll> &b) const {
                  return a.y < b.y;</pre>
           }
      struct sortXY {
            bool operator
                  ()(const Point<ll> &a, const Point<ll> &b) const {
if (a.x == b.x) return a.y < b.y;
else return a.x < b.x;</pre>
           }
      sort(a.begin(), a.end(), sortXY());
      vector < Point < ll >> t(n);
auto devide = [&](auto &&self, int l, int r) -> ll {
    if (l == r) return inf;
    int m = (l + r) / 2;
    ll ans = min(self(self, l, m), self(self, m + 1, r));
}
            ll midval = \hat{a}[m].\hat{x};
           sort(t.begin(), t.begin() + p, sortY());
for (int i = 0; i < p; i++){</pre>
```

10.4 LatticePoints [00db9d]

10.5 MinCoverCircle [c9ca81]