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1 Basic

1.1 install vscode [d41d8c]

1.2 default code [3cd57c]

```
#include <bits/stdc++.h>
#define all(x) (x).begin(), (x).end()
#define pip pair <int, int>
using namespace std;
using ll = long long;
const int mod = 1e9 + 7;

void solve() {
}

int main() {
   ios_base::sync_with_stdio(0);
   cin.tie(nullptr);
   int t = 1;
   cin >> t;
   while (t--) {
      solve();
   }
}
```

1.3 compare fuction [4bc3e0]

```
struct cmp { // 在有 template 的資結使用 bool operator()(const int &a, const int &b) const { return a < b; } 
// sort, bound 不用 struct
// priority queue 小到大是 > , set 是 < 
// set 不能 = , multiset 要 = 
// 每個元素都要比到,不然會不見 
// pbds_multiset 不要用 lower_bound 
// 如果要 find, 插入 inf 後使用 upper_bound 
// 內建 multiset 可以跟 set 一樣正常使用 
// 如果有自定義比較結構就比照以上
```

```
struct cmp { // 要在 template 的資結用外部變數 vector <int> &v;
     cmp(vector<int>& vec) : v(vec) {}
bool operator() (int a, int b) const {
   return v[a] > v[b];
// mutil: cmp cmp1(vector);
// priority_queue<int, vector<int>, cmp> pq(cmp1);
};
1.4 pbds [e28ae8]
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using pbds_set = tree<T, null_type,
    less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template < typename T>
using pbds_multiset = tree<T, null_type, less_equal</pre>
      <T>, rb_tree_tag, tree_order_statistics_node_update>;
2
       Graph
2.1 DFS 跟 BFS [cdd1d5]
int main() {
      int n
     vector<vector<int>> adj(n + 1, vector<int>());
     // dfs_graph
     vis[u] = true;
for (auto v: adj[u]) {
    self(self, v);
     dfs(dfs, 1);
     vector<int> depth(n + 1, 1e9);
     queue int > q;

auto bfs = [&](auto self, int u) -> void {
          vis[u] = true;
depth[u] = 0;
           q.push(u);
           while (!q.empty()) {
   int u = q.front(); q.pop();
   for (auto v : adj[u]) {
                     if (vis[v]) continue;
                     vis[v] = true;
depth[v] = depth[u] + 1;
                     q.push(v);
                }
          }
```

2.2 Dijkstra [4e0023]

bfs(bfs, 1);

```
// Flight Discount
int main() {
     int n, m; cin >> n >> m;
vector<vector<pair<</pre>
            int, int>>> adj(n + 1, vector<pair<int, int>>(n + 1));
     vector<vector<int>>
     dis(n + 1, vector<int>(2, 2e9));
for (int i = 1; i <= m; i++) {
                                                              // O for not used
           int u, v, w;
cin >> u >> v >> w;
           adj[u].push_back({v, w});
     priority queue
     while (!pq.empty()) {
    auto [dist, u, us] = pq.top(); pq.pop();
    if (dis[u][us] < dist) continue;</pre>
           if (us) {
                pq.push({dis[v][1], v, 1});
                for (auto [v, w] : adj[u]) {
   if (dis[u][0] + w < dis[v][0]) {
      dis[v][0] = dis[u][0] + w;
      pq.push({dis[v][0], v, 0});</pre>
                      if (dis[u][0] + w / 2 < dis[v][1]) {
   dis[v][1] = dis[u][0] + w / 2;
   pq.push({dis[v][1], v, 1});</pre>
```

```
National Chung Cheng University Salmon
    cout << min(dis[n][0], dis[n][1]);</pre>
2.3 Prim [f00ec0]
auto prim =
       [&](int n, vector<vector<pair<int, int>>> &adj) -> bool {
     int node_sz = 0;
     priority_queue<pair<int, int>,
     while (!pq.empty()) {
         auto [u, w] = pq.top(); pq.pop();
if (vis[u]) continue;
          vis[u] = true;
          node_sz++;
for (auto v : adj[u]) {
               if (!vis[v.first]) {
                   pq.push({v.second, v.first});
         }
    if (node_sz == n) return true;
return false;
2.4 正權找環 [0e0fdf]
const int maxn = 1e5+5;
vector < int > graph[maxn];
int color[maxn], parent[maxn];
bool vis[maxn];
int n, m;
void print_ans(int ori) {
  int now = parent[ori];
  deque<int> ans;
  ans.push_front(ori);
  while (now != ori) {
                                                                                        ans.push_front(now);
          now = parent[now];
                                                                                         queue<int> q;
                                                                                         for (int i = 1; i <= m; i++) {
   int u, v; cin >> u >> v;
   graph[u].push_back(v);
     ans.push_front(ori);
     cout << ans.size() << endl;
for (auto i : ans) {
    cout << i << " ";</pre>
                                                                                         for (int i = 1; i <= n; i++) {
   if (in[i] == 0) q.push(i);</pre>
     exit(0);
void dfs(int now) {
                                                                                        while (!q.empty()) {
   int u = q.front(); q.pop();
    color[now] = 1;
vis[now] = 1;
     for (auto nxt : graph[now]) {
  parent[nxt] = now;
  if (color[nxt] == 1) {
               print_ans(nxt);
          else if (color[nxt] == 0) {
               dfs(nxt);
                                                                                         if (dis[n] == -1e9) {
    color[now] = 2;
void solve() {
    cin >> n >> m;
for (int i = 1; i <= m; i++) {
   int u, v; cin >> u >> v;
                                                                                         else print_ans(n, par);
          graph[u].push_back(v);
                                                                                   2.7 負權最大距離 [2148ca]
     for (int i = 1; i <= n; i++) {
          if (!vis[i])
               dfs(i):
     cout << "IMPOSSIBLE";</pre>
}
2.5 BellmanFord [02f480]
// 用 Bellman Ford 找負環
                                     // u, v, w
vector<array<int, 3>> graph;
int main() {
     int src = 0;
```

```
int n, m; cin >> n >> m;
vector <int > par(n + 1), dis(n + 1, 1e9);
for (int i = 0; i < m; i++) {
   int a, b, w; cin >> a >> b >> w;
   graph.push_back({a, b, w});
}
dis[1] = 0;
for (int i = 0; i <= n; i++) {</pre>
            \dot{s}rc = 0;
            for (auto [u, v, w] : graph) {
    if (dis[v] > dis[u] + w) {
        dis[v] = dis[u] + w;
        par[v] = u;
                                   src = v;
                      }
           }
```

```
if (src) { // 到第 n + 1 次還在鬆弛 vector<int> ans;
          cout << "YES" << endl;
for (int</pre>
                 i = 0; i <= n; i++) src = par[src]; // 找那個負環
          ans.push_back(src);
           for (int
                i = par[src]; i != src; i = par[i]) { // 輸出負環
               ans.push_back(i);
          ans.push back(src):
           reverse(ans.begin(), ans.end());
          for (auto i : ans) {
    cout << i << " ";</pre>
      else {
          cout << "NO" << "\n";
 2.6 正權最大距離 [454dba]
// CSES Longest Flight Route
// 只能用在 DAG,用拓樸按順序鬆弛
void print_ans(int n, vector<int> &par) {
      deque < int > ans;
      int now = n;
      while(now != 1) {
          ans.push_front(now);
now = par[now];
      ans.push front(1):
     cout << ans.size() << "\n";
for(auto i : ans) {
    cout << i << " ";</pre>
```

// 如果 1 不能到達 n,n 也有可能被鬆弛 // 所以要看的是 dis[n] < 0 cout << "IMPOSSIBLE";

in[v]--;

for (auto v : graph[u]) {

par[v] = u;

if (in[v] == 0) q.push(v);

if (dis[v] < dis[u] + 1) { // 鬆弛 dis[v] = dis[u] + 1;

```
void dfs(int u, vector<int> &vis, vector<vector<int>> &adj) {
   if (vis[u]) return;
     vis[u] = 1;
     for (int v : adj[u]) {
          dfs(v, vis, adj);
signed main() {
   int n, m; cin >> n >> m;
     vector<array<int, 3>> edges;
vector<vector<int>> adj(n + 1);
vector<int> dis(n + 1), vis(n + 1);
     while (m--) {
   int u, v, w;
   cin >> u >> v >> w;
   edges.push_back({u, v, w});
          adj[u].push_back(v);
    fill(dis.begin(), dis.end(), -1e18);
```

```
}
}
if (vis[n]) cout << -1;
else cout << dis[n];
}
```

2.8 FloydWarshall [206b76]

2.9 <u>歐拉環與歐拉路</u> [0911ed]

```
| // 無向圖、尤拉環:檢查每個點的出度為偶數
 // 有向圖、
       尤拉路: 可以看成 1 走到 n, 所以檢查所有點的出度等於入度
 int n, m;
 const int maxn = 1e5 + 5;
 vector<set<int>> adj;
vector<int> in;
 void dfs(int now, vector<int> &road) {
      while (!adj[now].empty()) {
   int nxt = *adj[now].begin();
            adj[now].erase(nxt);
            dfs(nxt, road);
      road.push_back(now);
 void solve() {
    cin >> n >> m;
    in.assign(n + 1, 0);
    adj.assign(n + 1, set<int>());
    for (int i = 1; i <= m; i++) {
        int u, v; cin >> u >> v;
        adj[u] incort(v);
}
            adj[u].insert(v);
            in[v]++;
      in[1]++;
      }
      vector<int> road;
      dfs(1, road);
      if (road.size() != m + 1) {
    cout << "IMPOSSIBLE";</pre>
            return:
      reverse(road.begin(), road.end());
for(auto i : road) cout << i << " ";</pre>
```

2.10 SCC [b0411e]

```
struct SCC {
    int n, cur, cnt;
    vector <vector <int>> adj;
    vector <int>> stk, dfn, low, bel;
    SCC(int n) {
        init(n);
    }
    void init(int n) {
        this -> n = n;
        adj.assign(n, {});
        dfn.assign(n, -1);
        low.resize(n);
        bel.assign(n, -1);
```

```
stk.clear():
            cur = cnt = 0;
       void addEdge(int u, int v) {
            adj[u].push_back(v);
       void dfs(int x) {
    dfn[x] = low[x] = cur++;
            stk.push_back(x);
            for (auto y : adj[x]) {
   if (dfn[y] == -1) {
                       dfs(y);
                 low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
            if (dfn[x] == low[x]) {
                  int y;
                  do {
                       v = stk.back():
                       bel[y] = cnt;
                       stk.pop_back();
                  } while (y != x);
           }
      for (int i = 0; i < n; i++) {
    if (dfn[i] == -1) dfs(i);</pre>
            return bel;
       struct Graph {
            vector<pair<int, int>> edges;
            vector < int > siz;
vector < int > cnte;
       Graph compress() {
            Graph g;
g.n = cnt;
            g.siz.resize(cnt);
            g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {</pre>
                  g.siz[bel[i]]++;
                  for (auto j : adj[i]) {
    if (bel[i] != bel[j]) {
                             g.edges.emplace_back(bel[i], bel[j]);
                       } else {
                            g.cnte[bel[i]]++;
                 }
            return g;
      }
};
```

2.11 VBCC [3f9190]

```
struct VBCC {
     int n, cur;
vector<vector<int>> adj;
     vector<int> dfn, low, parent;
     vector<bool> is_cut;
     VBCC(int n) {
    init(n);
     void init(int n) {
           this ->n = n:
           adj.assign(n, {});
           dfn.assign(n, -1);
           low.resize(n):
           parent.assign(n, -1);
           is_cut.assign(n, false);
           cur = 0;
     void addEdge(int u, int v) {
   adj[u].push_back(v);
           adj[v].push_back(u);
     void dfs(int x) {
   int children = 0;
   dfn[x] = low[x] = cur++;
           for (int v : adj[x]) {
   if (dfn[v] == -1) {
      children++;
                      parent[v] = x;
                      dfs(v);
low[x] = min(low[x], low[v]);
                      if (parent[x] != -1 && low[v] >= dfn[x]) {
    is_cut[x] = true;
                } else if (v != parent[x]) {
    low[x] = min(low[x], dfn[v]);
           if (parent[x] == -1 && children > 1) {
    is_cut[x] = true;
```

```
}
void work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i);
        }
    }
};</pre>
```

2.12 EBCC [08723d]

```
struct EBCC { // CF/contest/1986/pF
  int n, cur, cnt;
  vector<vector<int>> adj;
      vector<int> stk, dfn, low, bel;
      vector<pair<<mark>int, int</mark>>> bridges; // 關鍵邊
      EBCC(int n) {
            init(n);
      void init(int n) {
            this->n = n;
adj.assign(n, {});
            dfn.assign(n, -1);
            low.resize(n);
            bel.assign(n, -1);
            stk.clear();
            bridges.clear();
            cur = cnt = 0:
      void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
      void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
            stk.push_back(x);
            for (auto y : adj[x]) {
   if (y == p) continue;
   if (dfn[y] == -1) {
                        dfs(y, x);
low[x] = min(low[x], low[y]);
if (low[y] > dfn[x]) {
                             bridges.emplace_back(x, y);
                  } else if (bel[y] == -1) {
                        low[x] = min(low[x], dfn[y]);
                 }
            if (dfn[x] == low[x]) {
                  int y;
                  do {
                        y = stk.back();
                        bel[y] = cnt;
stk.pop_back();
                  } while (y != x);
            }
      vector<int> work() {
            dfs(0, -1);
return bel;
      struct Graph {
            int n;
            vector<pair<int, int>> edges;
            vector<int> siz; // BCC 內節點數
            vector<int> cnte; // BCC 內邊數
      Graph compress() {
            Graph g;
g.n = cnt;
            g.siz.resize(cnt);
            g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {</pre>
                  g.siz[bel[i]]++;
                  g.stc[bet[i]] + ,
for (auto j : adj[i]) {
    if (bel[i] < bel[j]) {
        g.edges.emplace_back(bel[i], bel[j]);
    } else if (i < j) {
        restrict [i] [i];
}</pre>
                             g.cnte[bel[i]]++;
                       }
                 }
            return a:
     }
};
```

2.13 2-SAT [eeddc1]

```
// CSES Giant Pizza
struct TwoSat {
    int n;
    vector<vector<int>> e;
    vector<bool> ans;
    TwoSat(int n) : n(n), e(2 * n), ans(n) {}
    void addClause(int u, bool f, int v, bool g) {
        e[2 * u + !f].push_back(2 * v + g);
        e[2 * v + !g].push_back(2 * u + f);
    }
}
```

```
bool satisfiable() {
            vector < int

> id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
             int now = 0, cnt = 0;
             function < void(int) > tarjan = [&](int u) {
                   stk.push_back(u);
dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
                         tarjan(v);
  low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in stk
  low[u] = min(low[u], dfn[v]);
                   if (dfn[u] == low[u]) {
                          int v;
                          do {
                                v = stk.back();
                         stk.pop_back();
id[v] = cnt;
} while (v != u);
                          ++cnt:
                  }
             for (int i
            return true:
       vector<bool> answer() { return ans; }
int main() {
      main() {
  int m, n; cin >> m >> n;
TwoSat ts(n);
for (int i = 0; i < m; ++i) {
    int u, v; char x, y;
    cin >> x >> u >> y >> v;
    ts.addClause(u - 1, x == '+', v - 1, y == '+');
}
      if (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";</pre>
      else cout << "IMPOSSIBLE\n";</pre>
```

2.14 Planets Cycles [71ac0e]

```
vector<int> dis, v;
vector<bool> vis:
int step;
void dfs(int x) {
    path.push(x);
       if (vis[x]) {
    step += dis[x];
             return:
       vis[x] = true;
       step++;
       dfs(v[x]);
// count path_dis to rep
int main() {
   int n; cin >> n;
      v.assign(n + 1, 0);
dis.assign(n + 1, 0);
vis.assign(n + 1, false);
for (int i = 1; i <= n; i++) {</pre>
             cin >> v[i];
       for (int i = 1; i <= n; i++) {
             step = 0;
int is_outof_cycle = 1;
             dfs(t);
while (!path.empty()) {
   if (path.front() == path.back()) {
                          is_outof_cycle = 0;
                    dis[path.front()] = step;
step -= is_outof_cycle;
                   path.pop();
            }
       for (int i = 1; i <= n; i++) {
    cout << dis[i] << ' ';</pre>
       cout << '\n';
}
```

2.15 Planet Queries II [872f72]

```
| // 在有向圖中,從 A 到 B 的最短距離
| // 保證出度是 1 所以對 1 個點來說,從他出發只可能遇到一個環
| int n, q;
| int dp[200005][30]; // 倍增表
```

```
vector<vector<int>> cvcles:
vector<int
> no, cycle_idx, vis; // Order & Can be in cycle, or out
void set_out_of_cycle_no(int now, unordered_set<int> &done) {
    // 把不在環內的也編號, v 是 u 的編號 -1
    if (done.find(now) != done.end()) return;
    set_out_of_cycle_no(dp[now][0], done);
     done.insert(now); // post order
no[now] = no[dp[now][0]] - 1;
int wiint_go_to(int u, int k) { // 回傳當 u 走 k 步時會到的地方
    for (int i = 0; i <= 18; i++) {
        if (k & (1 << i)) {</pre>
                 u = dp[u][i];
           }
      return u;
void find_cycle(int now) {
      unordered_set<int> appear;
      vector<int> v:
      bool flag = true;
                                  // 代表有環
      while (appear.find(now) == appear.end()) {
            appear.insert(now);
            v.push_back(now);
           if (vis[now]) {
    flag = false;
           now = dp[now][0];
     for (auto i : v) vis[i] = true;
if (!flag) return;
// now 是環的起點,我們先找到他在 v 的哪裡
      int z = find(v.begin(), v.end(), now) - v.begin();
vector <int> cycle(v.begin() + z, v.end());
      cycles.push_back(cycle);
int main() {
    cin >> n >> q;
    no.assign(n + 1, -1);
      cycle_idx.assign(n + 1, -1);
vis.assign(n + 1, 0);
for (int u = 1; u <= n; u++) cin >> dp[u][0];
      for (int i = 1; i <= 18; i++) // 倍增表
           for (int u = 1; u <= n; u++)
    dp[u][i] = dp[dp[u][i - 1]][i - 1];
(int i = 1; i <= n; i++) {
    if (!vis[i]) find_cycle(i);</pre>
      int idx = 0;
      unordered_set<int> done;
      for (auto &i : cycles) {
   int c = 0;
            for (auto &j : i) {
    no[j] = c++;
    cycle_idx[j] = idx;
                 done.insert(j);
     for (int i = 1; i <= n; i++) set_out_of_cycle_no(i, done);
for (int i = 1; i <= q; i++) {
   int u, v; cin >> u >> v;
               在同個環內
            if (cycle_idx[u] == cycle_idx
    [v] && cycle_idx[u] != -1 && cycle_idx[v] != -1) {
    int cyc_size = cycles[cycle_idx[u]].size();
                 cout <<
                        (no[v] - no[u] + cyc_size) % cyc_size << "\n";</pre>
            // 都不再環內
           continue:
                 if (wiint_go_to(u, no[v] - no[u]) == v) {
   cout << no[v] - no[u] << "\n";</pre>
                  else cout << -1 << "\n";
            else if (cycle_idx[u]
                 if (l <= n) {
                              ] + cycle_size) % cycle_size << "\n";
                 else cout << -1 << "\n";
```

```
else { // u 在環內 b 不在,直接不可能 cout << -1 << "\n"; } }
```

3 Data Structure

3.1 BIT [d41d8c]

```
struct BIT {
                                                                        // BIT 都是 1-based 的查詢
                        vector<int> bit:
                       BIT(int n) { // 有幾個數
this->n = n;
                                          bit.resize(n + 1, 0);
                                                                                                                                                        // 必須是 0-based
                        BIT(vector<int> &init) {
                                           this ->n = init.size();
                                          bit.resize(n + 1, 0);
for (int i = 1; i <= n; i++) {
    modify(i, init[i - 1]);</pre>
                        void modify(int i, int val) {
    for (; i <= n; i += i & -i) {
        bit[i] += val;
}</pre>
                                          }
                        int query(int r) {
   int ans = 0;
   for (; r; r -= r & -r) ans += bit[r];
                                          return ans;
                        int query(int l, int r) {
                                          return query(r) - query(l - 1);
                      }
     struct TwoDimensionBIT {
                       int nx, ny;
vector<vector<int>> bit;
                        TwoDimensionBIT(int x, int y) {
                                          nx = x; ny = y;
bit.resize(x + 1, vector<int>(y + 1, 0));
                       for (int tmp = y; tmp <= ny; tmp += tmp & -tmp) {
    for (int tmp = y; tmp <= ny; tmp += tmp & -tmp) {
        bit[x][tmp] += mod;
}</pre>
                                          }
                       int query(int r1, int r2) {
    int ans = 0;
    for (; r1; r1 -= r1 & -r1) {
        for (int tmp = r2; tmp; tmp -= tmp & -tmp) {
            ans += bit[r1][tmp];
            rank for the formula of the formula
                                          return ans:
1 };
```

3.2 DSU [d41d8c]

```
struct DSU {
   vector <int> boss, siz;
   DSU(int n) {      // 0 based
        boss.resize(n);
        iota(boss.begin(), boss.end(), 0);
        siz.assign(n, 1);
}
int find_boss(int x) {
        if (boss[x] == x) return x;
        return boss[x] = find_boss(boss[x]);
}
bool same(int x, int y) {
        return find_boss(x) == find_boss(y);
}
bool merge(int x, int y) {
        x = find_boss(x);
        y = find_boss(y);
        if (x == y) {
            return false;
        }
        if(siz[x] < siz[y]) swap(x, y);
        siz[x] += siz[y];
        boss[y] = x;
        return true;
}
int size(int x) {
        return siz[find_boss(x)];
};</pre>
```

3.3 Increasing Array Queries [d41d8c]

```
const int maxn = 2e5+5;
int n, q;
int nums
     [maxn], prefix[maxn], ans[maxn], BIT[maxn], contrib[maxn];
```

```
vector<pair<int, int>> queries[maxn];
void update(int pos, int val) {
   for (; pos <= n; pos += pos & -pos) BIT[pos] += val;</pre>
 int query(int a, int b) {
                  int ans = 0;
for (; b; b -= b&-b) ans += BIT[b];
for (a--; a; a -= a&-a) ans -= BIT[a];
 void solve() {
                  cin >> q;
for (int i = 1; i <= n; i++) {
    cin >> nums[i];
                                    prefix[i] = prefix[i-1] + nums[i];
                  nums[n + 1] = 1e9;
                  for (int i = 1; i <= q; i++) {
    int a, b; cin >> a >> b;
                                    queries[a].push_back({b, i});
                   deque < int > mono; mono.push_front(n+1);
                 deque<int> mono, mo
                                                     mono.pop_front();
                                  contrib[i] = (mono.front() - 1 - i) *
                                                                                                                   + (j.first
                                                                                                                                           - mono[pos]) * nums[mono[pos]]
                                                                                                                   - (prefix
                                                                                                                                        [j.first] - prefix[mono[pos]]);
                   for (int i = 1; i <= q; i++) {
                                     cout << ans[i] << endl;
                  }
}
```

3.4 線段樹 [d41d8c]

```
template <class Info>
struct Seg { // 左開右閉寫法
      int n;
       vector < Info > info;
      Seg(int n_, Info v_ = Info()) {
            init(n_, v_);
      template <class T>
      Seg(vector<T> init_) {
  init(init_);
      void init(int n_, Info v_ = Info()) {
  init(vector(n_, v_));
      template <class T>
void init(vector<T> init_) {
    n = init_.size();
             in = intl_iste(),
info.assign(4 << __lg(n), Info());
function <void(
    int, int, int)> build = [&](int p, int l, int r) {
    if (r - l == 1) {
        info[p] = init_[l];
        return();
}
                         return:
                   int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                   pull(p);
             build(1, 0, n);
      void pull
      (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
                  `info[p] = v;
                   return:
             int m = (l + r) / 2;
if (x < m) {
                   modify(2 * p, l, m, x, v);
             } else {
                   modify(2 * p + 1, m, r, x, v);
             pull(p);
      void modify(int p, const Info &i) {
             modify(1, 0, n, p, i);
```

```
Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    return query(p *</pre>
               2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
           (int ql, int qr) { return query(1, 0, n, ql, qr); }
      emplate < class F> // 尋找區間內,第一個符合條件的
     int findFirst
          (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {</pre>
              return -1;
          if (l >= x && r <= y && !pred(info[p])) {</pre>
              return -1:
          if (r - l == 1) {
              return l;
          int m = (l + r) / 2;
          int res = findFirst(2 * p, l, m, x, y, pred);
          if (res == -1) {
    res = findFirst(2 * p + 1, m, r, x, y, pred);
          return res;
     }
     template < class F> // 若要找 last, 先右子樹遞廻即可
int findFirst(int l, int r, F & & pred) {
    return findFirst(1, 0, n, l, r, pred);
};
// ---define structure and info plus---
 struct Info {
     int sum;
 Info operator + (const Info &a, const Info &b) {
     return { a.sum + b.sum };
// ---pizza_queries--
// 左邊的店(s < t): dis_l = (pizza[s] - s) + t;
// 右邊的店(t < s): dis_r = (pizza[s] + s) - t;
// 實作: 建左查詢線段樹跟右查詢線段樹, 用最小值pull
// 答案是 min(left_query(1, s) + t, right_query(s, end) + t);
// ---List Removals
// 維護區間內有幾個數字被選過
// 用二分
      搜找右區間最小位,使得 ans - query == 1 ~ ans 被選過的數量
      -- CSES subarray queries:---
// tree[now].prefix
       = max(tree[lc].sum + tree[rc].prefix, tree[lc].prefix);
// tree[now].suffix
= max(tree[lc].suffix+tree[rc].sum, tree[rc].suffix);
// tree[now].middle_max
       = max(lc 中, rc 中, lc 後 + rc 前, now 前, now 後)
```

3.5 懶標線段樹 [d41d8c]

```
template <class Info, class Tag>
struct LazySeg { // 左閉右開寫法
     vector < Info > info:
     vector <Tag> tag;
LazySeg(int n_, Info v_ = Info()) {
          init(n_, v_);
     template <class T>
LazySeg(vector<T> init_) {
          init(init_);
     void init(int n_, Info v_ = Info()) {
          init(vector(n_, v_));
     template <class T>
void init (vector<T> init_) {
          n = init_.size();
info.assign(4 << __lg(n), Info());
tag.assign(4 << __lg(n), Tag());</pre>
           info[p] = init_[l];
                     return:
                int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                pull(p);
          build(1, 0, n);
     void pull
     (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
          tag[p].apply(v);
     void push(int p, int l, int r) {
```

```
int m = (l + r) / 2;
if (r - l >= 1) {
    apply(p * 2, l, m, tag[p]);
    apply(p * 2 + 1, m, r, tag[p]);
}
            tag[p] = Tag();
     void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
}
                return:
            int m = (l + r) / 2;
           push(p);
if (x < m) {</pre>
                 modify(2 * p, l, m, x, v);
           } else {
                 modify(2 * p + 1, m, r, x, v);
           pull(p);
      void modify(int p, const Info &i) {
           modify(1, 0, n, p, i);
      Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    push(p, l, r);
}</pre>
            return query(p *
                  2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      Info query
            (int ql, int qr) { return query(1, 0, n, ql, qr); }
      void range_apply
           (int p, int l, int r, int ql, int qr, const Tag &v) {
if (qr <= l || ql >= r) return;
if (ql <= l && r <= qr) {</pre>
                 apply(p, l, r, v);
                 return:
           fint m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
            pull(p);
      void range_apply(int l, int r, const Tag &v) {
    range_apply(1, 0, n, l, r, v);
      template < class F> // 尋找區間內,第一個符合條件的
      int findFirst
           (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {</pre>
                 return -1:
            if (l >= x && r <= y && !pred(info[p])) {</pre>
                 return -1;
            if (r - l == 1) {
                 return l;
            int m = (l + r) / 2;
           push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
            if (res == -1)
                 res = findFirst(2 * p + 1, m, r, x, y, pred);
            return res;
     template < class F> // 若要找 last , 先右子樹遞迴即可
int findFirst(int l, int r, F & pred) {
    return findFirst(1, 0, n, l, r, pred);
// ---define structure and info plus---
struct Tag {
   int set_val; int add;
      void apply(const Tag& v) {
           if (v.set_val) {
    set_val = v.set_val;
    add = v.add;
            else {
                 add += v.add;
     }
};
struct Info {
     int sum;
     void apply(int l, int r, const Tag &v) {
           if (v.set_val) {
    sum = (r - l) * v.set_val;
           sum += (r - l) * v.add;
Info operator + (const Info &a, const Info &b) {
     return { a.sum + b.sum };
// polynomial queries
```

```
|// 設置梯形的底跟加了幾次, apply_tag 時底為 l 的合, d 為加給次
// 所以 sum += (底 * 2 + 次 * 區間) * 區間 / 2;
 3.6 莫隊 [d41d8c]
struct query {
   int l, r, id;
} typedef query;
void MO(int n, vector<query> &queries) {
   int block = sqrt(n);
}
      int block_ = sqr(in),
function <bool(query, query)> cmp = [&](query a, query b) {
  int block_a = a.l / block;
  int block_b = b.l / block;
}
            if (block_a != block_b) return block_a < block_b;</pre>
            return a.r < b.r;
       sort(queries.begin(), queries.end(), cmp);
 void compress(vector<int> &nums) {
      vector < int > sorted = nums;
sort(sorted.begin(), sorted.end());
       sorted.erase
             (unique(sorted.begin(), sorted.end()), sorted.end());
       for (int i = 0; i < nums.size(); i++) {
    nums[i] = lower_bound(sorted.begin</pre>
                  (), sorted.end(), nums[i]) - sorted.begin() + 1;
 3.7 Treap [d41d8c]
 struct Treap {
       Treap *l, *r;
int pri, subsize; char val; bool rev_valid;
       Treap(int val) {
            this->val =
                            val:
            pri = rand();
l = r = nullptr;
            subsize = 1; rev_valid = 0;
       void pull() {      // update subsize or other information
      subsize = 1;
      for(auto i : {l, r}) {
            if (i) subsize += i->subsize;
      }
      }
 int size(Treap *treap) {
   if (treap == NULL) return 0;
       return treap->subsize:
 // lazy
 void push(Treap *t) {
   if (!t) return;
       if (t->rev_valid) {
            swap(t->l, t->r);
if (t->l) t->l->rev_valid ^= 1;
if (t->r) t->r->rev_valid ^= 1;
       t->rev_valid = false;
 Treap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
    // push(a); push(b); // lazy
    if (a->pri > b->pri) {
            a->r = merge
                  (a \rightarrow r, b); // a \rightarrow r = new, inorder, make sense
            a->pull();
            return a;
            b->l = merge
                  (a, b->l); // new->l = a, inorder, make sense
            b->pull();
      }
      pair<Treap*, Treap*> split(Treap *root, int k) {
            auto [a, b] = split(root->r, k - size(root->l) - 1);
root->r = a;
            root->pull();
            return {root, b};
            auto [a, b] = split(root->l, k);
root->l = b;
            root->pull();
            return {a, root};
 void Print(Treap *t) {
      // lazy
            cout << t->val;
            Print(t->r);
```

}

```
void substring_rev() {
   int n, m; cin >> n >> m;
   Treap *root = nullptr;
         string str; cin >> str;
for(auto c : str) {
                  root = merge(root, new Treap(c));
         for (int i = 1; i <= m; i++) {
                 (int t = 1; t <= m, t...,
int x, y; cin >> x >> y;
auto [a, b] = split(root, x-1); // a: 1~x-1, b: x~n
auto [c, d] = split(b, y-x+1); // Use b to split
                 auto [c, d] = split(b, y-x+1); // use //
// c->rev_valid ^= true;
// push(c);
b = merge(a, d); // Notice the order
root = merge(b, c);
        Print(root);
```

4 Flow

4.1 Dinic [7f4d14]

```
' template dinic max flow
struct edge {
     int v, w, rev_id;
int n, m, ans = 0
int n, m, ans = 0;
vector <edge> adj[505];
vector <int> lev(505), vis(505);
bool label_level(){ // 標記深度,如果到不了終點 return false
    fill(all(lev), -1); lev[1] = 0;
    queue<int> q, q.push(1);
    while (in ampty()) {
     q.push(v);
                      lev[v] = lev[u] + 1;
          }
     return (lev[n] == -1 ? false : true);
int dfs(int u, int flow){
     if (u == n) return flow;
for (auto &[v, w, rev_id] : adj[u]) {
    if (lev[v] == lev[u] + 1 && !vis[v] && w > 0) {
        vis[v] = true;
    }
}
                int ret = dfs(v, min(flow, w));
if (ret > 0) {
                     w -= ret;
                      adj[v][rev_id].w += ret;
                      return ret;
                }
          }
     }
     return 0; // 到不了終點就會 return 0
void add_edge(int u, int v, int w) { // 無向圖的話兩邊都是 w
   adj[u].push_back({v, w, (int)adj[v].size()});
   adj[v].push_back({u, 0, (int)adj[u].size() - 1});
void dinic() {
     while (label_level()) {
   while (true) {
      fill(all(vis), 0);
      int tmp = dfs(1, inf);
      if (tmp == 0) break;
                ans += tmp;
          }
     cout << ans;
// Distinct Route
// 給你一張有向圖,求從走 1 到 n 的最多方法數,並且邊不重複
// dfs 要改成
int dfs(int u, int flow){
     int ret = dfs(v, min(flow, w));
if (ret > 0) {
                      w -= ret;
                      adj[v][rev_id].w += ret;
                      if (arg_valid) { // 走的是 arg 路,Reset arg_valid = 0;
                           adj[v][rev_id].arg_valid = 0;
                           [v][rev_id].arg_valid = 1;
                                                                 // 走正常路
                }
          }
     return 0:
                    // 到不了終點就會 return 0
bool get_road(int now, vector<int> &ans, vector<bool> &vis) {
```

```
if (now == 1) return true;
for (auto &[v, w, rev_id, arg_valid] : adj[now]) {
    if (arg_valid_&& !vis[v]){
            ans.push_back(v);
vis[v] = true;
            bool flag = get_road(v, ans, vis);
if (flag) {
                  arg_valid = false;
            ans.pop_back();
     }
return false:
```

4.2 Min Cut [0ab707]

```
// CSES Police Chase
 int g[505][505]; // 以 0(1) 紀錄存在邊
  void solve(){
        cin >> n >> m;
        for (int i = 0; i < m; i++) {
    int u, v; cin >> u >> v;
              add_edge(u, v, 1);
        dinic()
        fill(all(vis), 0);
unordered_set<int> reach;
auto find = [&](auto self, int u) -> void {
              if (!vis[u]) {
                     vis[u] = 1;
reach.insert(u);
                     for (auto [v, w, _] : adj[u]){
   if(w > 0){
      self(self, v);
   }
}
              }
        find(find, 1);
        cout << ans << "\n";
for (auto u : reach) {
              for (auto [v, w, _] : adj[u]) {
   if (g[
        u][v] && !w && reach.find(v) == reach.end()) {
      cout << u << " " << v << " | n";</pre>
                           // ans = sum(u_to_v)
                     }
              }
 }
```

4.3 Bipartite Matching [5e0de5]

```
struct Bipartite_Matching { // 1-based
  int n, m; vector<vector<int>> adj;
  vector<int> match, vis;
       Bipartite_Matching
             (int n, int m, vector<vector<int>> &adj) {
this->n = n;
             this->m = m;
             this->adj = adj;
match.assign(n + m + 1, -1);
             vis.assign(n + m + 1, 0);
       pair<int, vector<pair<int, int>>> matching() {
             int cnt = 0; vector<pair<int, int>> matching() {
  int cnt = 0; vector<pair<int, int>> ans;
auto dfs = [8](auto self, int u) -> bool {
  for (int v : adj[u]) {
    if (vis[v] == 0) {
                                 vis[v] = 1;
                                 if (match
                                         [v] == -1 || self(self, match[v])) {
                                       match[v] = u;
                                       return true;
                                 }
                          }
                   return false:
             for (int i = 1; i <= n; i++) {
    fill(all(vis), 0);
    dfs(dfs, i);</pre>
             for (int i = n + 1; i <= n + m; i++) {
    if (match[i] != -1) {</pre>
                          cnt += 1;
                   }
             for (int i = n + 1; i <= n + m; i++) {
    if (match[i] != -1) {</pre>
                          ans.push_back({match[i], i - n});
             return { cnt, ans };
     }
int main(){
       int n, m, e; cin >> n >> m >> e;
vector<vector<int>>> adj(n + m + 1);
       for (int i = 1; i <= e; i++) {</pre>
```

int u. v: cin >> u >> v:

adj[u].push_back(v + n);

```
adj[v + n].push_back(u);
    Bipartite_Matching bip(n, m, adj);
    auto [cnt, ans] = bip.matching();
cout << cnt << "\n";</pre>
    for (auto [u, v] : ans) {
    cout << u << " " << v << "\n";
4.4 MCMF [c21886]
// 郵差要送 k 個包裹到 n 地,每個邊有最大量跟, Cost per parcel
// 求 1 到 n 的最小成本
struct edge {
   int from, to, w, cost;
int n, m, parcel;
                      // 幫每個 edge 編號
vector<edge> adj;
vector<int> p[505]; // u 存 edge 編號
int now_edge = 0;
void add_edge(int u, int v, int w, int cost){
   adj.push_back({u, v, w, cost});
    p[u].push_back(now_edge);
    now_edge++;
    adj.push_back({v, u, 0, -cost});
    p[v].push_back(now_edge);
    now edge++;
int Bellman_Ford(){
    flag = 0;
                  dis[to] = dis[from] + cost;
                   par[to] = i; // 紀錄編號
flow_rec[to] = min(flow_rec[from], w);
             }
         if (flag) break;
    if (dis[n] == 1e9) return 0;
    int mn_flow = flow_rec[n];
    int v = n;
while(v != 1){
         int u = adj[par[v]].from;
adj[par[v]].w -= mn_flow;
adj[par[v] ^ 1].w += mn_flow;
    mn_flow = min(mn_flow, parcel);
    parcel -= mn_flow;
    return mn_flow * dis[n];
int main(){
    cin >> n >> m >> parcel;
    int ans = 0;
for (int i = 1; i < m; i++) {</pre>
         int u, v, w, cost; cin >> u >> v >> w >> cost;
add_edge(u, v, w, cost);
    while (parcel > 0){
   int tmp = Bellman_Ford();
   if (tmp == 0) break;
   ans += tmp;
    cout << (parcel > 0 ? -1 : ans);
    String
5.1 KMP [132b98]
struct KMP {
```

```
while (s[i] !=
                 sub[now + 1] && now != -1) now = failure[now];
// f stores if comparison fail, move to where
if (s[i] == sub[now + 1]) now++;
if (now + 1 == sub.size()) {
                      match.push_back(i - now);
now = failure[now];
           return match;
     }
 int main() {
      string s = "xxtxxtxtx";
string sub = "tx";
      KMP kmp(sub);
      vector < int > ans = kmp.KMPmatching(s);
for(auto &i : ans) cout << i << " ";</pre>
}
 5.2 Z函數 [0af76e]
|// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
 // 的最長公共前綴 (LCP) 的長度
 vector<int> Z(string s) {
      int n = s.size();
      vector<int> z(n + 1);
      if (i + z[i] > j + z[j]) {
                j = i;
      }
      return z; // 最後一格不算
}
 5.3 Duval Algorithm [f9dcca]
// duval_algorithm
 // 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
 vector<string> duval(string s) {
  int i = 0, n = s.size();
  vector<string> res;
      while (i < n) {
  int k = i, j = i + 1;
  while (s[k] <= s[j] && j < n) {
    if (s[k] < s[j]) k = i;
    else k++;
    ;...</pre>
            while (i <= k) {
                 res.push_back(s.substr(i, j - k));
                 i += j - k;
           }
      return res;
 }
 // 最小旋轉字串
 string min_round(string s) {
        += s;
       int i = 0, n = s.size();
      int start = i;
while (i < n / 2) {</pre>
```

5.4 Manacher [9c9ca6]

else k++;
i++:

while (i <= k) {
 i += j - k;</pre>

return s.substr(start, n / 2);

```
if (i + r[i] > j + r[j]) {
        j = i;
    }
}
return r;
// # a # b # a #
// 1 2 1 4 1 2 1
// # a # b # b # a #
// 1 2 1 2 5 2 1 2 1
// 值 -1 代表原回文字串長度
// (id - val + 1) / 2 可得原字串回文開頭
}
```

5.5 Trie [3b3aa0]

```
struct Trie {
    struct trie_node {
             bool is_word;
             vector<trie_node *> children;
trie_node() {
   is_word = false;
                    children.resize(26, NULL);
            }
       trie_node *root = new trie_node();
      void insert(string &s) {
    trie_node *cur = root;
    for (int i = 0; i < s.size(); i++) {
        int idx = s[i] - 'a';
        if (cur->children[idx] == NULL) {
                          cur->children[idx] = new trie_node();
                    cur = cur->children[idx]:
             cur->is_word = true;
      bool is_in_trie(string &s) {
             trie_node *cur = root;
for (int i = 0; i < s.size(); i++) {
    if (cur->
                    children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
             return true;
      int search_i_start(string &s, int i, vector<int> &dp) {
    trie_node *cur = root;
    int sz = s.size(), ans = 0;
    for (int j = i; j < sz; j++) {
        if (cur</pre>
                    ->children[s[j] - 'a'] == nullptr) return ans;
cur = cur->children[s[j] - 'a'];
                    if (cur->is_word)
      (ans += dp[j + 1]) %= mod;
             return ans:
      }
};
int main() {
       // 找到 sub 集合裡,可以重複用,組成 s 的組數
      Trie trie;
string s; cin >> s;
int sz = s.size();
      // dp 代表 i 開頭到最後的配對總數
       // 找到有結尾為 stop 的 dp[i] += dp[j + 1]
int n; cin >> n;
      vector <int> dp(sz + 1, 0);
for (int i = 0; i < n; i++) {
    string sub; cin >> sub;
             trie.insert(sub);
      dp[sz] = 1;
for (int i = sz - 1; i >= 0; i--) {
    dp[i] = trie.search_i_start(s, i, dp);
}
       cout << dp[0] << endl;
```

6 Math

6.1 質因數分解 [ee1622]

```
| // a^(m-1) = 1 (mod m)
| // a^(m-2) = 1/a (mod m)
| // EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)
| // Filter + DP; DP save min factor 'recur' factor decomposition
| // FacSum = (a^0+a^1...+a^x)(b^0+...+b^y)
| // FacMul = N(x+1)(y+1)(z+1)/2
| vector < int > is_prime;
| // 1 代表是質數 '非 1 不是
| void init(int n) {
| is_prime.assign(n + 1, 1);
| for (int i = 2; i <= (int)sqrt(n) + 1; i++) {
| if (is_prime[i] == 1) {
| for (int j = i + i; j <= n; j += i) {
| is_prime[j] = i;
| }
| }
```

```
}
int main() {
    init(1000000);
    ll ans = 1;
    ll q; cin >> q;
    map<ll, ll> mp;
    while (is_prime[q] != 1) {
        mp[is_prime[q]]++;
        q /= is_prime[q];
    }
    if (q != 1) mp[q]++;
    for (auto [a, b] : mp) {
        ans *= b + 1;
    }
    cout << ans << "\n";
}</pre>
```

6.2 中國餘數定理 [d41d8c]

```
ll exgcd(ll a, ll b, ll &x, ll &y) {
    if (!b) {
        x = 1, y = 0;
        return a;
    }
    ll g = exgcd(b, a % b, y, x);
    y -= a / b * x;
    return g;
}
ll inv(ll x, ll m){
    ll a, b;
    exgcd(x, m, a, b);
    a %= m;
    if (a < 0) a += m;
    return a;
}
// remain, mod
ll CRT(vector<pair<ll, ll>> &a){
    ll prod = 1;
    for (auto x : a) {
        prod *= x.second;
    }
    ll res = 0;
    for (auto x : a) {
        auto t = prod / x.second;
        res += x.first * t % prod * inv(t, x.second) % prod;
        if(res >= prod) res -= prod;
    }
    return res;
}
```

6.3 矩陣快速幕 [d41d8c]

```
struct Mat {
      int m, n;
      vector<vector<ll>> matrix;
      void init(int m, int n) {
    this->m = m; this->n = n;
           matrix.resize(m);
for (int i = 0; i < m; i++) {
    matrix[i].resize(n);</pre>
     Mat(int m, int n) { init(m, n); }
Mat(int n) { init(n, n); }
Mat(vector<vector<ll>> matrix) {
    this->m = matrix.size();
    this->n = matrix[0].size();
}
            this->matrix = matrix;
      Mat unit(int n) { // 單位矩陣
           Mat res(n);
for (int i = 0; i < n; i++) {</pre>
                  res.matrix[i][i] = 1;
           return res;
      Mat operator * (Mat b) {
           int m = matrix.size
          *= (Mat b) { *this = *this * b; return *this; }
     Mat operator ^ (ll p) {
    if (p == 0) return unit(n);
    Mat ans = *this; p--;
    while (p > 0) {
                 if (p & 1) {
    ans *= *this;
                 }
*this *= *this;
```

```
return ans;
     Mat operator ^= (ll p) { *this = *this ^ p; return *this; }
signed main() {
    int n; cin >> n; ll ans;
if (n <= 4) {</pre>
          vector<int> v = {0, 1, 1, 2, 4};
          ans = v[n]:
     else {
          Mat init({{4, 2, 1}, {2, 1, 1}, {1, 1, 0}});
          T.matrix = \{\{1, 1, 0\}, \{1, 0, 1\}, \{1, 0, 0\}\};
          T ^= n - 4;
init *= T;
          ans = init.matrix[0][0];
    cout << ans << "\n";
// 初始矩陣
                轉移式
// f4 f3 f2 1 1 0 f5 f4 f3

// f3 f2 f1 1 0 1 => f4 f3 f2

// f2 f1 f0 1 0 0 f3 f2 f1
```

6.4 模除計算 [9b1014]

```
using i64 = long long;
template < class T>
constexpr T power(T a, i64 b) {
    for (; b; b /= 2, a *= a) {
    if (b % 2) {
        res *= a;
    }
     return res;
constexpr i64 mul(i64 a, i64 b, i64 p) {
   i64 res = a * b - i64(1.L * a * b / p) * p;
   res %= p;
     if (res < 0) {
          res += p;
     return res;
template < i64 P>
struct MLong {
    i64 x;
     constexpr MLong() : x{} {}
constexpr MLong(i64 x) : x{norm(x % getMod())} {}
     static i64 Mod;
constexpr static i64 getMod() {
   if (P > 0) {
               return P;
          } else {
    return Mod;
          }
     constexpr static void setMod(i64 Mod_) {
         Mod = Mod_;
     constexpr i64 norm(i64 x) const {
          if (x < 0) {
               x += getMod();
          if (x >= getMod()) {
               x -= getMod();
          return x:
     constexpr i64 val() const {
          return x;
     explicit constexpr operator i64() const {
          return x:
     constexpr MLong operator -() const {
          MLong res;
res.x = norm(getMod() - x);
          return res;
     constexpr MLong inv() const {
   assert(x != 0);
   return power(*this, getMod() - 2);
     constexpr MLong &operator*=(MLong rhs) & {
          x = mul(x, rhs.x, getMod());
return *this;
     constexpr MLong &operator+=(MLong rhs) & {
          x = norm(x + rhs.x);
return *this;
     constexpr MLong &operator -= (MLong rhs) & {
          x = norm(x - rhs.x);
return *this;
```

```
constexpr MLong &operator/=(MLong rhs) & {
    return *this *= rhs.inv();
       friend constexpr MLong operator*(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res *= rhs;
             return res;
       friend constexpr MLong operator+(MLong lhs, MLong rhs) {
   MLong res = lhs;
             res += rhs:
             return res:
       friend constexpr MLong operator-(MLong lhs, MLong rhs) {
   MLong res = lhs;
             res -= rhs;
             return res;
       friend constexpr MLong operator/(MLong lhs, MLong rhs) {
   MLong res = lhs;
             res /= rhs:
       friend
              constexpr istream &operator>>(istream &is, MLong &a) {
             i64 v;
             is >> v;
a = MLong(v);
             return is;
       friend constexpr
                ostream &operator << (ostream &os, const MLong &a) {
             return os << a.val();</pre>
       friend constexpr bool operator==(MLong lhs, MLong rhs) {
             return lhs.val() == rhs.val();
       friend constexpr bool operator!=(MLong lhs, MLong rhs) {
  return lhs.val() != rhs.val();
 };
 template<>
 i64 MLong<0LL>::Mod = i64(1E18) + 9;
 constexpr i64 P = 998244353;
using Z = MLong <P>;
// using Z = MLong <0LL>; // change Mod
 struct Comb {
       i64 n;
       to4 n;
vector <Z> _fac;
vector <Z> _invfac;
vector <Z> _inv;
Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
Comb(i64 n) : Comb() { init(n); }
       void init(i64 m) {
             m = min(m, Z::getMod() - 1);
if (m <= n) return;
_fac.resize(m + 1);</pre>
             _invfac.resize(m +
             _inv.resize(m + 1);
             for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;</pre>
             for (int i = _fac[m].inv();
for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
             n = m:
       If fac(i64 m) {
   if (m > n) init(2 * m);
             return _fac[m];
       Z invfac(i64 m) {
   if (m > n) init(2 * m);
   return _invfac[m];
       Z inv(i64 m) {
   if (m > n) init(2 * m);
   return _inv[m];
       Joinom(i64 n, i64 m) {
   if (n < m || m < 0) return 0;
   return fac(n) * invfac(m) * invfac(n - m);</pre>
       |} comb; // 注意宣告, 若要換模數需重新宣告
 6.5 樹論分塊 [06204a]
 // CSES Sum of Divisors
```

```
const int mod = 1e9 + 7;
const int inv_2 = 500000004;
// n / 1 * 1 + n / 2 * 2 + n / 3 * 3 + ... + n / n * n
```

6.6 Mobius Theorem

- 數論 分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n}\!\mu(d)\!=\!\begin{cases} 1 & \text{for } n\!=\!1\\ 0 & \text{for } n\!\neq\!0 \end{cases}$$

- 2. μ是常數函數1的反元素
- $\Rightarrow \mu * 1 = \epsilon$, $\epsilon(n)$ 只在n = 1時為 1 , 其餘情況皆為 0 。
- φ歐拉函數: x以下與 x 互質的數量

$$\phi*1 = \sum_{d|n} \phi(\frac{n}{d})$$
 質因數分解
$$= \sum_{i=0}^{c} \phi(p^{i})$$

$$= 1 + p^{0}(p-1) + p^{1}(p-1) + \dots + p^{c-1}(p-1)$$

$$= p^{c}$$

$$= id$$

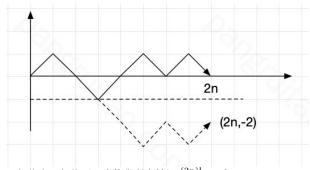
- 莫比烏斯反演公式
 - $f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$
 - $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$
- 例子

$$\begin{split} &\sum_{i=a}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{x} [d|i] \sum_{j=1}^{y} [d|j] \text{ d 可整除 i 時為 1} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{d} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.7 其比烏斯反演 [d41d8c]

```
| const int maxn = 2e5;
| ll mobius_pref[maxn];
| void init() {
| mobius_pref[1] = 1;
| vector < ll > wei | 0 代表是質數, -1 代表可被平方數整除
| for (ll i = 2; i < maxn; i++) {
| if (wei[i] == -1) {
| mobius_pref[i] = mobius_pref[i - 1];
| continue; // 包含平方
| }
| if (wei[i] == 0) {
| wei[i] = 1;
| for (ll j = 2; i * j < maxn; j++) {
| if (j % i == 0) wei[i * j] = -1;
| else if (wei[i * j] != -1) wei[i * j]++;
| }
```

6.8 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有 x 個,往下有 y 個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.9 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- X/G: 本質不同的方案的集合
- X^g : 對於某一種操作 g ,所有方案中,經過 g 這種翻轉後保持不變的方案的集合
- 集合取絕對值代表集合數

7 Search and Gready

7.1 二分搜 [d41d8c]

```
int main() {
    int l = 1, r = 10;
    // 1 to tar, find tar
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}</pre>
```

7.2 三分搜 [d41d8c]

8 Tree

8.1 LCA [9f95b1]

8.2 樹重心 [833d90]

```
const int maxn = 2e5+5;
vector <int> tree[maxn];
int cen = 0, n;
int dfs(int par, int now) {
   bool flag = 1;
   int size = 0;
   for (auto nxt : tree[now]) {
        if (par != nxt) {
            int subsize = dfs(now, nxt);
            if (subsize > n / 2) flag = false;
            size += subsize;
        }
   }
   if (n - 1 - size > n / 2) flag = false;
   if (flag) cen = now;
   return size + 1;
}
int main() {
   cin >> n;
   for (int i = 1; i < n; i++) {
        int u, v; cin >> u >> v;
        tree[u].push_back(v);
        tree[v].push_back(u);
   }
   for (int i = 1; i <= n; i++) {
        for (auto nxt : tree[i])
            dfs(i, nxt);
        if (cen) break;
   }
}</pre>
```

8.3 樹壓平 [51199c]

```
dfs(dfs.
      BIT bit(n);

for (int i = 1; i <= n; i++) {
    bit.modify(tree_mapping[i].first, node_value[i]);
            if (tree_mapping[i].first < n) { // root 就不用扣了</pre>
                 bit.modify
                        (tree_mapping[i].second + 1, -node_value[i]);
      for (int i = 0; i < q; i++) {
            int op; cin >> op;
           if (op == 1) {
    int s, x; cin >> s >> x;
                  int add = x
                 - euler_ordered_value[tree_mapping[s].first];
euler_ordered_value[tree_mapping[s].first] = x;
bit.modify(tree_mapping[s].first, add);
if (tree_mapping[s].first < n) { // root 就不用扣了
                       bit.modify(tree_mapping[s].second + 1, -add);
                 int node; cin >> node;
                 cout <<
                         bit.query(tree_mapping[node].first) << "\n";</pre>
     }
}
```

8.4 Heavy Light Decomposition [6791f6]

```
struct HLD {
     vector<int> siz, top, dep, parent, in, out, seq;
     vector<vector<int>> adi:
     HLD() {}
HLD(int n) {
          init(n);
     void init(int n) {
          this->n = n;
           siz.resize(n):
           top.resize(n):
           dep.resize(n);
           parent.resize(n);
           in.resize(n);
          out.resize(n);
           seq.resize(n);
          cur = 0:
          adj.assign(n, {});
     void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
     void work(int root = 0) {
  top[root] = root;
  dep[root] = 0;
           parent[root] = -1;
           dfs1(root);
           dfs2(root);
     void dfs1(int u) {
    if (parent[u] != -1) {
                adj[u].erase(find
                      (adj[u].begin(), adj[u].end(), parent[u]));
           siz[u] = 1;
           for (auto &v : adj[u]) {
                parent[v] = u;
                dep[v] = dep[u] + 1;
                dfs1(v):
                siz[u] += siz[v];
                if (siz[v] > siz[adj[u][0]]) {
                     swap(v, adj[u][0]);
                } // 讓 adj[u][0] 是重子節點
          }
      void dfs2(int u) {
          in[u] = cur++;
           seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
  top[v] = v == adj[u][0] ? top[u] : v;
                dfs2(v);
          out[u] = cur;
     int lca(int u, int v) {
    while (top[u] != top[v]) {
        if (dep[top[u]] > dep[top[v]]) {
                u = parent[top[u]];
} else {
   v = parent[top[v]];
                }
           return dep[u] < dep[v] ? u : v;</pre>
```

```
int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
     int jump(int u, int k) {
    if (dep[u] < k) {</pre>
           int d = dep[u] - k;
while (dep[top[u]] > d) {
    u = parent[top[u]];
           return seq[in[u] - dep[u] + d];
     bool isAncester(int u, int v) {
           // 判斷 u 是否是 v 的祖先
return in[u] <= in[v] && in[v] < out[u];
      int rootedParent(int u, int v) {
           // 根據新根節點 u 計算 v 的父節點
           swap(u, v);
if (u == v) {
                 return u;
           if (!isAncester(u, v)) {
    return parent[u];
           auto it = upper_bound(adj
   [u].begin(), adj[u].end(), v, [&](int x, int y) {
   return in[x] < in[y];</pre>
           }) - 1;
return *it;
     int rootedSize(int u, int v) {
           // 根據新根節點 u 計算子樹 v 的大小
           if (u == v) {
                 return n:
           if (!isAncester(v, u)) {
                 return siz[v];
           return n - siz[rootedParent(u, v)];
     int rootedLca(int a, int b, int c) {
    // 根據新的根節點計算三個節點 a \ b 和 c 的最近公共祖先
    return lca(a, b) ^ lca(b, c) ^ lca(c, a);
};
```

8.5 Virtual Tree [622e69]

```
1// 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
 // 可以建立虚樹達成快速樹 DP
 ...
// 例如這題是有權樹,跟 vertex 1 隔開的最小成本
// 例如這題是有權爾,跟 vertex 1 隔開的最小成本
int top = -1; vector < int > stk (maxn);
void insert(int u, vector < vector < int >> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
    vtf(stk[top - 1])    vtf(stk[top - 1])
        vt[stk[top - 1]].push_back(stk[top]), top--;
if (stk[top - 1] != l) {
               vt[l].push_back(stk[top]);
           stk[top] = l;
else vt[l].push_back(stk[top--]);
        stk[++top] = u;
 void reset(int u, vector<vector<int>> &vt) {
   for (int i : vt[u]) reset(i, vt);
   vt[u].clear();
 void solve(int n, int q) {
   vector g(n + 1, vector<pair<int, int>>());
        vector vt(n + 1, vector vector vt(n + 1, vector vector vt(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;
   g[u].push_back({v, w});
   [u].push_back({v, w});
               g[v].push_back({u, w});
        build_lca(n, g);
        build(n, g);

for (int i = 0; i < q; i++) {

   int m; top = -1; cin >> m;
               vector <int> key(m);
for (int j = 0; j < m; j++) {
    cin >> key[j];
                       iskey[key[j]] = 1;
               key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
               });
               for (int x : key) insert(x, vt);
               auto dfs = [&](auto self, int u) -> void {
                      for (auto v : vt[u]) {
    self(self, v);
                              if (iskey[v]) {
```

9 DP

9.1 背包問題 [6d6b63]

```
// 考慮前 i 個,預算有 j 塊錢的最多 page
int main(){
    int n, bud;
cin >> n >> bud;
     vector<vector<int>> dp(n + 1, vector<int>(bud + 1));
    vector<int> Page(n + 1, 0);
vector<int> Price(n + 1, 0);
    for(int i = 1; i <= n; i++){
    cin >> Price[i];
    for(int i = 1; i <= n; i++){
    cin >> Page[i];
     for (int i = 1; i <= n; i++) {
         for (int j = 1; j <= bud; j++) {</pre>
              if (j >= Price[i]) { // 買得起
                  // 不買或買
                   dp[i][j] = max(dp[i
                        1][j], dp[i - 1][j - Price[i]] + Page[i]);
              else {
                  dp[i][j] = dp[i - 1][j];
         }
    cout << dp[n][bud] << "\n";
```

9.2 Bitmask [b18541]

```
void travel_exactly_once(){
      // [走過的路][終點]
      vector<vector<int>> dp(1 << 20, vector<int>> (20, 0));
      vector < int > rev_adj[20];
int n, m; cin >> n >> m;
for(int i = 0; i < m; i++){</pre>
            int u, v; cin >> u >> v;
rev_adj[--v].push_back(--u);
      dp[1][0] = 1;
for (int road = 0; road < (1 << n); road++) {</pre>
            // 沒經過起點,不用走
if (road & 1 == 0) continue;
            // DP,隨便選定一個當前路徑的終點
            for (int end = 0; end < n; end++) {</pre>
                  // 路徑沒包含假定的 end
                  if ((road & (1 << end)) == 0) continue;</pre>
                  // 去除終點,得到 pre_road
int pre_road = road - (1 << end);
// 從 rev_adj 找 pre_road 的終點
                  for (int pre_road_end : rev_adj[end]) {
    if ((road & (1 << pre_road_end))) {</pre>
                              dp[road
                              [][end] += dp[pre_road][pre_road_end];
dp[road][end] %= mod;
                        }
                 }
           }
      cout << dp[(1 << n) - 1][n - 1];
void elevator_rides(){
      int n, k; cin >> n >> k;
vector <int >> passenger(n);
for (int i = 0; i < n; i++) cin >> passenger[i];
      vector<int
      > used(1 << n, 0);  // 最後載完人的電梯用了多少空間
vector <int > dp(1 << n, 1);  // bitset
for (int i = 1; i < 1 << n; i++) {
    used[i] = dp[i] = 2e9;
    for (int j = 0; j < n; j++) {
        if (i & (1 << i)) [ // 与 :
                  if (i & (1 << j)) { // 有 j
int pre = i ^ (1 << j);
                        // 最後的電梯還能載 j
```

```
_____, passenger[j] <= k) // 電梯數先比,再來比用掉的空間if (dp
                   if (used[pre] + passenger[j] <= k) {</pre>
                             [pre] < dp[i] || (dp[pre] == dp[i] &&
                            used[pre] + passenger[j] < used[i])) {
used[i] = used[pre] + passenger[j];</pre>
                            dp[i] = dp[pre];
                       }
                  }
                   // 搭新的電梯
                  else
                       used[i] = passenger[j];
dp[i] = dp[pre] + 1;
                  }
             }
         }
    cout << dp[(1 << n) - 1];
int main(){
    travel_exactly_once();
elevator_rides();
9.3 硬幣 [d41d8c]
void coin_combination_II(){
```

```
// 有 n 種錢幣,求組合為 x 的組數,順序不可顛倒
    ,,
// 可顛倒的話只要一維,先 x 迴圈,再 coin[i] 去加
    int n, x; cin >> n >> x;
    vector < int > coin(n + 1);
    // dp[i][j] 為考慮前 i 個硬幣,組合為 i 的組數
    vector < vector < int >> dp(2, vector < int > (x + 1, 0));
   dp[i & 1][j] = dp[!(i & 1)][j];
if (j >= coin[i]) {
                    & 1][j] += dp[i & 1][j - coin[i]]) %= mod;
           }
       }
   cout << dp[n & 1][x];
void minimize_coins_nums(){
   // 有 n 種錢幣, 求組合為 x 的最小硬幣數
int n, x; cin >> n >> x;
vector <int >> coin(n);
for (int i = 0; i < n; i++) cin >> coin[i];
    // dp[i] 是組合為 i 的最小硬幣數
   dp[i] = min(dp[i], dp[i - j] + 1);
   cout << (dp[x] == 2e9 ? -1 : dp[x]);
int main(){
   coin combination_II();
   minimize_coins_nums();
```

9.4 編輯距離 [4d4a6d]

```
int main() {
    string s1, s2; cin >> s1 >> s2;
    int size1 = s1.size(), size2 = s2.size();
    // dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元
            vector <int>> dp(size1 + 1, vector <int>(size2 + 1, 0));
s1 = "0" + s1. s2 = "0" + s2.
           vector <int> op(size1 + 1, vector <int> (st)
s1 = "θ" + s1, s2 = "θ" + s2;
for (int i = 1; i <= size1; i++) dp[i][θ] = i;
for (int i = 1; i <= size2; i++) dp[θ][i] = i;
for (int i = 1; i <= size1; i++){
    for (int j = 1; j <= size2; j++) {
        if (s1[i] == s2[j]) {
            dp[i][j] = dp[i - 1][j - 1];
        }
}</pre>
                                           // s1 新增等價於 s2 砍掉
                                            // dp[i][j] = min(修改, s1 新增, s2 新增);
dp[i][j] = min({dp[i - 1][
j - 1], dp[i - 1][j], dp[i][j - 1]}) + 1;
                      }
            cout << dp[size1][size2];
```

```
9.5 LCS [087c0d]
```

```
int main() {
       int m, n; cin >> m >> n;
       string s1, s2;
       cin >> s1 >> s2;
int L = 0;
       vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0));
       for (int i = 1; i <= m; i++) {
   for (int j = 1; j <= n; j++) {
     if (s1[i - 1] == s2[j - 1]) {
        dp[i][j] = dp[i - 1][j - 1] + 1;
}</pre>
                              dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
                      }
       int length = dp[m][n];
cout << length << "\n";
string s(length, 'c');</pre>
       // along to dp to trace back
while (m >= 1 && n >= 1) {
   if (s1[m - 1] == s2[n - 1]) {
      s[length - 1] = s1[m - 1];
      m--, n--, length--;
               else {
    if (dp[m - 1][n] > dp[m][n - 1]) m--;
       cout << s << "\n";
```

9.6 LIS [668131]

```
int main() {
     int n; cin >> n;
vector <int> v(n);
for (int i = 0; i < n; i++) {</pre>
           cin >> v[i];
     int dp[n]; vector<int> mono;
     mono.push_back(v[0]);
dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) +
    if (v[i] > mono.back()) +
                mono.push_back(v[i]);
                 dp[i] = ++L;
                *it = v[i];
dp[i] = it - mono.begin() + 1;
     vector<int> ans;
     cout << L << "\n";
for (int i = n - 1; i >= 0; i--) {
   if (dp[i] == L) {
                ans.push_back(v[i]);
           }
      reverse(ans.begin(), ans.end());
     for (auto i : ans) {
    cout << i << " "</pre>
```

9.7 **Projects** [18998c]

```
// 排程有權重問題,輸出價值最多且時間最少
struct project {
      int from, end, gain, id;
int main() {
       int n; cin >> n;
       for (int i = 1; i <= n; i++) {
   int f, e, g; cin >> f >> e >> g;
   projects[i] = {f, e, g, i};
}
       sort(all(projects), [](project a, project b) {
             if (a.end == b.end) return a.gain < b.gain;
return a.end < b.end;</pre>
      vector<array<int, 3>> dp(n + 1); // nums, gain, time
vector<int> par(n + 1, 0), ans, add(n + 1, -1);
for (int i = 1; i <= n; i++) {
   int id = --upper_bound(projects.begin</pre>
                    (), projects.begin() + i, project({0, projects
[i].from, 0, 0}), [](project &a, project &b) {
return a.end < b.end;</pre>
             }) - projects.begin(); // 二分搜最接近 from 的 end dp[i] = dp[i - 1]; par[i] = i - 1;
              if (dp
                     [i][1] < dp[id][1] + projects[i].gain || (dp[i][1]
== dp[id][1] + projects[i].gain && dp[i][2] >
                      dp[id][2] - projects[i].from + projects[i].end)) {
```

```
如果報酬率一樣,比時間少的
                     dp[i] = {dp
    [id][0] + 1, dp[id][1] + projects[i].gain, dp
    [id][2] + projects[i].end - projects[i].from};
par[i] = id;
                     add[i] = projects[i].id;
              }
       for (auto i : dp[n])
    cout << i << " " << " \n";
for (int now = n; now > 0; now = par[now])
    if (add[now] != -1)
                     ans.push_back(add[now]);
       sort(all(ans));
for (auto &i : ans) cout << i << " ";</pre>
}
```

9.8 Removal Game [211de0]

```
| // 兩個人比賽,每個人輪流取一個數字且只能是頭尾
 // 問兩人都選得好,第一個人可取得的最大分數
 int main() {
   int n; cin >> n;
      vector<vector<int>> dp(n + 1, vector<int>(n + 1));
      int pref = 0;
      vector < int > v(n + 1);
for (int i = 1; i <= n; i++) {
    cin >> v[i];
          pref += v[i];
      // dp[i][j] 是 i 到 j 區間選完,的最大分數差
     for (int i = n; i > 0; i--) {
    for (int j = i; j <= n; j++) {
        if (i == j) {
                    dp[i][j] = v[i];
                else {
                    // 選左差距大,還是選右差距大
                    dp[i][j] = max(
    v[i] - dp[i + 1][j], v[j] - dp[i][j - 1]);
               }
     // x + y = sum, dp[1][n] = x - y;
cout << (pref + dp[1][n]) / 2;
```

9.9 CF Example [7d37ea]

```
| // CF 1932 DF
// 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
 // 請問在線段不重複的情況下,最多獲得幾分 int main() {
      int n, m;
cin >> n >> m;
      // 記錄每點有幾個線段
      // 再一個紀錄,包含這個點的左界
vector<int> l_side(n + 1, inf), cnt(n + 5, 0);
for (int i = 0; i < m; i++) {
    int l, r; cin >> l >> r;
    l_side[r] = min(l_side[r], l);
    cnt[]|++:
            cnt[l]++;
            cnt[r + 1]--;
      for (int i = 2; i <= n; i++) {
            cnt[i] += cnt[i - 1];
      for (int i = n; i >= 2; i--) {
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
      vector<int> dp(n + 1);
      for (int i = 1; i <= n; i++) {
    dp[i] = cnt[i];
    if (l_side[i] != inf) {</pre>
                 dp[i] += dp[l_side[i] - 1];
            dp[i] = max(dp[i], dp[i - 1]);
      cout << dp[n] << "\n";
 }
// CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
 // 再加上 max(bi) - min(bi)
 int main(){
      int n, k, ans = 0; cin >> n >> k;
vector < pii >> v(n + 1);
for (int i = 1; i <= n; i++) {</pre>
           int a, b; cin >> a >> b;
v[i] = {a, b};
if (a <= k) ans = 1;</pre>
      sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
      }); // 用 bi 來排,考慮第 i 個時可以先扣
      vector < vector < int >> dp(n + 1, vector < int > (n + 1, inf));
      // 考慮 v[i] 時, 選 j 個的 sum(ai) - min(bi)
      for (int i = 1; i <= n; i++) { // 滾動 dp
```

```
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
                / min(不選, 選)
              if (dp[i
                   - 1][j - 1] + v[i].first + v[i].second <= k) {
                   // 假如可以選, 更新 ans 時再加回去 bi
                  ans = max(ans, j);
         dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
    cout << ans << endl:
}
```

9.10 Slope Trick [2ccb3a]

```
|// 設 dp[i][j] 為將陣列前
      i 個元素變為非嚴格遞增,並且所有 ai <= bj 所需要花的代價
#include <bits/stdc++.h>
using namespace std;
#define int long long
 signed main() {
    int n; cin >> n;
vector <int >> v(n);
for (int i = 0; i < n; i++) {</pre>
        cin >> v[i];
        v[i] -= i;
    vector<int> discrete = v
    sort(discrete.begin(), discrete.end());
    int m = unique
         (discrete.begin(), discrete.end()) - discrete.begin();
    - 1], dp[0][j] + abs(v[i] - discrete[j - 1]));
        swap(dp[0], dp[1]);
    cout << *min_element(dp[0].begin(), dp[0].end());</pre>
}
|// 當 dp 是凸函數且答案是極值時,可以用 slope trick 優化
// 要注意的是
     如果兩個相鄰段的斜率差異大於 1,那麼這個關鍵點是要存兩次的
// 例如這題假設在 i-1 時 f{i-1}(x) 是一個 Slope Trick 函數,
// 我們額外定義一個函數 g_i(x
     )表示將前 i 個元素變為非嚴格遞增,且 a_i = x 的最小花費。
// 則 g_{-i}(x) = f\{i-1\}(x) + |x-a_{-i}| ,我們可以觀察到 // f_{-i}(x) = min(g_{-i}(y)
     )), for y <= x ' 由於 /x-a_i/ 是一個 Slope Trickable 函數,
// 因此
     g_i(x) 和 f_i(x) 都是 Slope Trickable 函數,因為 /x-a_i/,
|// 分段點是 a_i,且因為斜率一定大於 1,要 push 2 次
|// 因為 g_i(x) 最右邊函數的斜率是
      1,因此我們只需去除 g_i(x) 的最大斜率變化點得到 f_i(x)。
int main () {
    priority_queue < int > q;
    int n; cin >> n;
for (int i = 0; i < n; i++) {
        int x; cin >> x;
x -= i + 1;
        q.push(x);
        q.push(x);
        ans += q.top() - x;
        q.pop();
    cout << ans;
```

Geometry

10.1 Cross Product [8113ac]

```
const double eps = 1e-8;
struct point {
   double x, y;
   point operator * (int a){ return {a * x, a * y}; }
      point operator * (the a){ return {a * x, a * y, y}, }
point operator * (point b){ return {x * b.x, y * b.y}; }
point operator * (point b){ return x * b.x + y * b.y; }
double operator * (point b){ return x * b.x + y * b.y; }
double operator ^ (point b){ return x * b.y - y * b.x; }
      bool operator
                . < (point b){ return x == b.x ? y < b.y : x < b.x; }</pre>
double abs(point a) { return sqrt(a * a); }
int sign
       (double a) { return fabs(a) < eps ? 0 : a > 0 ? 1 : -1; }
int ori(point
            bool colinear(point a,
       point b, point c) { return sign((b - a) ^ (c - a)) == 0; }
bool between(point a, point b, point c){ // c between a and b
   if (!colinear(a, b, c)) return false;
   return sign((a - c) * (b - c)) <= 0;</pre>
```

10.2 Convex Hull [e84f76]

```
}
int Andrew_monotone_chain(int n){
    while (l >= 2 && cross(L[l-2], L[l-1], P[i]) <= 0){
    l--;</pre>
            L.pop_back();
        while (u >= 2 && cross(U[u-2], U[u-1], P[i]) >= 0){
            U.pop_back();
        }
l++;
        u++;
        L.push_back(P[i]);
U.push_back(P[i]);
    cout << l << ' ' << u << '\n';
    return l + u;
}
int main(){
    int n, x, y;
cin >> n;
for(int i = 0;i < n;i++){</pre>
       cin >> x >> y;
P.push_back({x, y});
    int ans = Andrew_monotone_chain(n) - 2;
cout << ans << "\n";
return 0;</pre>
```