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## DP

## 1.1 背包問題

```
int dp[1005][100005];
vector < int > Page(1005, 0);
vector<int> Price(1005, 0);
int main(){
    int n, bud;
    cin >> n >> bud;
    for(int i = 1; i <= n; i++){</pre>
         int tmp; cin >> tmp;
        Price[i] = tmp;
    for(int i = 1; i <= n; i++){</pre>
        int tmp; cin >> tmp;
        Page[i] = tmp;
    memset(dp, 0, sizeof(dp));
    for(int i = 1; i <= n; i++){</pre>
        for(int j = 1; j <= bud; j++){</pre>
             if(j >= Price[i]){
                 dp[i][j] = max(dp[i-1][
                      j], dp[i-1][j-Price[i]]+Page[i]);
             else {
                 dp[i][j] = dp[i-1][j];
        }
    cout << dp[n][bud] << endl;</pre>
```

#### 1.2 Bitmask DP

```
// Bit_Mask_DP, Travel Exactly Once
int dp[(1 << 20) - 1][20];
vector < int > rev_adj[20];
int n, m;
const int mod = 1e9 + 7;
void solve(){
    cin >> n >> m;
    for(int i = 0; i < m; i++){</pre>
         int u, v; cin >> u >> v;
         rev_adj[--v].push_back(--u);
    dp[1][0] = 1;
    for(int road = 0; road < (1 << n); road++){</pre>
         // Not include 1
         if(road & 1 == 0) continue;
         // include n but not all walked
         if(road & (1 << (n
               - 1)) && road != ((1 << n) - 1)) continue;
         // DP
         for (int end = 0; end < n; end++) {</pre>
              // Not include end
      if ((road & (1 << end)) == 0) continue;</pre>
              // exclude end point is last road
      int pre_road = road - (1 << end);
for (int pre_road_end : rev_adj[end]) {</pre>
                  // pre_road_end is prev's end
         if ((road & (1 << pre_road_end))) {
  dp[road][end] += dp[pre_road][pre_road_end];</pre>
            dp[road][end] %= mod;
      }
    }
    }
    cout << dp[(1 << n) - 1][n - 1];</pre>
    // elevator rides
// for(int i = 1; i < 1 << n; i++){
             used[i] = dp[i] = inf;
    //
    //
             for(int j = 0; j < n; j++){}
                 if(i & (1 << j)){ // 有j
int last = i ^ (1 << j);
    //
    //
                      if(used[last] + s[j] \ll x)
```

```
if(dp[last] < dp[i] || dp[
last] == dp[i] && used[last] + s[j] < used[i]){</pre>
     //
                                 used[i] = used[last] + s[j];
                                 dp[i] = dp[last];
    //
//
//
                       else {
                            if(dp[last] + 1 < dp[
     //
          i] || dp[last] + 1 == dp[i] && s[j] < used[i]){
                                 used[i] = s[j];
    //
//
//
                                 dp[i] = dp[last] + 1;
                       }
    11
     ;;
}
     // cout << dp[(1 << n) - 1];
}
```

#### 1.3 硬幣

```
// combine
// arrange: nested loop exchange
ll dp[2][1000001];
void solve(){
    int n, x; cin >> n >> x;
    vector<int> coin(n + 1);
    for(int i = 1; i <= n; i++){</pre>
         cin >> coin[i];
    dp[0][0] = 1;
    for(int i = 1; i <= n; i++){</pre>
         for(int j = 0; j <= x; j++){</pre>
             dp[i & 1][j] = dp[!(i & 1)][j];
             if(j >= coin[i]){
                  (dp[i & 1][j]
                       += dp[i & 1][j - coin[i]]) %= mod;
             }
         }
    cout << dp[n & 1][x];</pre>
// Minimize coins nums
void solve(){
    int n, x; cin >> n >> x;
    vector<int> coin(n);
    for(int i = 0; i < n; i++){</pre>
        cin >> coin[i];
    ll dp[x+1]; // init(dp, 0);
    dp[0] = 0;
    for(int i = 1; i <= x; i++){</pre>
         dp[i] = llinf;
         for(auto &j : coin){
   if(j <= i){</pre>
                  dp[i] = min(dp[i], dp[i - j] + 1);
             }
        }
     cout << (dp[x] == llinf ? -1 : dp[x]);
```

#### 1.4 編輯距離

```
ll dp[maxn][maxn]:
void solve(){
    init(dp, 0);
    string s1, s2; cin >> s1 >> s2;
    int size1 = s1.sz, size2 = s2.sz;
    s1 = "0" + s1, s2 = "0" + s2;

for(int i = 1; i <= size2
         ; i++) dp[0][i] = i; // s2 = {}, s1 = ...;
    for(int i = 1; i <= size1</pre>
         ; i++) dp[i][0] = i; // <math>s1 = {}, s2 = ...;
    for(int i = 1; i <= size1; i++){</pre>
         for(int j = 1; j <= size2; j++){</pre>
             if(s1[i] == s2[j]){
                 dp[i][j] = dp[i-1][j-1];
             else {
                  dp[i][j] = min(min(dp[i-1][
                      j-1], dp[i-1][j]), dp[i][j-1]) + 1;
                                   // modify
                                        // s1 del / s2 add
                                            // s1 add s2 del
             }
```

```
}
    cout << dp[size1][size2];</pre>
}
1.5 LCS
void solve(){
    int m, n; cin >> m >> n;
    string s1, s2;
    cin >> s1 >> s2:
    s1.insert(s1.begin(), '1');
    s2.insert(s2.begin(), '1');
    int L = 0;
    vector
        <vector<int>> dp(m + 1, vector<int>(n + 1, 0));
    for(int i = 1; i <= m; i++){</pre>
        for(int j = 1; j <= n; j++){</pre>
             if(s1[i] == s2[j]){
                dp[i][j] = dp[i-1][j-1] + 1;
                 dp[i][j] = max(dp[i-1][j], dp[i][j-1]);
        }
    int length = dp[m][n];
    cout << length << "\n";</pre>
    vector < char > s(length);
    // along to dp to trace back
    while(m >= 1 && n >= 1){
        if(s1[m] == s2[n]){
             s[length - 1] = s1[m];
            m - -:
             n - -:
             length--;
             if(dp[m-1][n] > dp[m][n-1]){
                m - -;
             else n--;
        }
    for(auto c : s){
        cout << c;
1.6 LIS
// Rec Sequence LIS
void solve(){
    int n; cin >> n;
    vector<int> v(n);
    for(int i = 0; i < n; i++){</pre>
        cin >> v[i];
    int dp[n]; vector<int> mono;
    mono.push_back(v[0]);
    dp[0] = 1; int L = 1;
    for(int i = 1; i < n; i++){</pre>
        if(v[i] > mono.back()){
             mono.push_back(v[i]);
             dp[i] = ++L;
```

auto it = lower\_bound(all(mono), v[i]);

dp[i] = it - mono.begin() + 1;

else {

vector < int > ans;
cout << L << endl;</pre>

}

}

\*it = v[i];

**if**(dp[i] == L){

L--;

for(int i = n - 1; i >= 0; i--){

ans.push\_back(v[i]);

# 1.7 Projects

```
const int maxn = 2e5+5;
int n;
ll from[maxn], to[maxn], gain[maxn];
ll dp[400005];
vector<ll> rev_proj[400005];
void compress(map<int, int> mp){
    int now = 0;
    for(auto &i : mp){
        mp[i.first] = ++now;
    for(int i = 1; i <= n; i++){</pre>
        rev_proj[mp
             [to[i]]].push_back({mp[from[i]], gain[i]});
    }
void solve(){cin >> n;
    map<int, int> comp;
    for(int i = 1; i <= n; i++){</pre>
        cin >> from[i] >> to[i] >> gain[i];
        comp[from[i]] = 1, comp[to[i]] = 1;
    compress(comp);
    for(int i = 1; i <= 400004; i++){</pre>
        dp[i] = dp[i - 1];
        for(auto [from, gain] : rev_proj[i]){
             dp[i] = max(dp[i], dp[from - 1] + gain);
    cout << dp[400004];
// Monotonic DP in campus contest, use monotonic stack
// first is lowest mountain, second is pref in stack
```

#### 1.8 Removal Game

```
ll dp[5005][5005];
void solve(){
    int n; cin >> n;
    ll pref = 0;
    vector<ll> v(n+1);
    for(int i = 1; i <= n; i++){</pre>
         cin >> v[i];
        pref += v[i];
    // dp[i][j] = max_diff(i to j);
    for(int i = n; i > 0; i--){
         for(int j = 1; j <= n; j++){</pre>
             if(i > j) continue;
             else if(i == j){
                  dp[i][j] = v[i];
             else {
                  dp[i][j] = max(v[
                      i] - dp[i+1][j], v[j] - dp[i][j-1])
                          // i+1, j-1, care dp's order
         }
    // x + y = sum, dp[1][n] = x - y;
cout << (pref + dp[1][n]) / 2;
```