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Basic

1.1 Default Code [d41d8c]

```
#include <bits/stdc++.h>
using namespace std;
using ll = long long;
void solve() {
int main() {
     ios_base::sync_with_stdio(false);
     cin.tie(nullptr);
     int t = 1;
     cin >> t;
     while (t--) {
         solve();
     return 0;
}
```

1.2 Compare Fuction [d41d8c]

```
// 1. sort, 二分搜刻在函式內 lambda 就好
// 2. priority queue 小到大是 >, set 是 <
// 3. set 不能 = , multiset 必須 =
// 4. 確保每個成員都要比到
// 5. pbds_multiset 不要用 lower_bound
// 6. 如果要用 find, 插入 inf 後使用 upper_bound
// 7. multiset 可以跟 set 一樣使用, 但請注意第 3、4 點
auto cmp = [](int i, int j) { return i > j; };
priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
vector<int> a {1, 2, 5, 4, 3}; // 小心不要改到 a
auto cmp = [&a](int i, int j) { return a[i] > a[j]; };
priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
```

1.3 Pbds [d41d8c]

#include <ext/pb_ds/assoc_container.hpp>

```
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < class T>
using pbds_set = tree<T, null_type,
    less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template < class T>
1.4 Double [7db939]
     double x;
D() : x{0} {}
D(double x) : x{x} {}
constexpr static double eps = 1E-12;
     explicit operator double() const { return x; }
D operator-() const {
   return D(-x);
     D & operator*=(D rhs) & {
           x *= rhs.x; return *this;
     D &operator+=(D rhs) & {
    x += rhs.x; return *this;
     D &operator -= (D rhs) & {
    x -= rhs.x; return *this;
     D & operator /= (D rhs) & {
    assert(fabs(rhs.x) > eps);
           x /= rhs.x; return *this;
      friend D operator*(D lhs, D rhs) {
           return lhs *= rhs;
      friend D operator+(D lhs, D rhs) {
           return lhs += rhs;
     friend D operator - (D lhs, D rhs) {
    return lhs -= rhs;
     friend D operator/(D lhs, D rhs) {
   return lhs /= rhs;
     friend istream &operator>>(istream &is, D &a) {
   double v; is >> v; a = D(v); return is;
     } // eps should < precision
friend bool operator <(D lhs, D rhs) {
   return lhs.x - rhs.x < -eps;</pre>
      friend bool operator>(D lhs, D rhs) {
           return lhs.x - rhs.x > eps;
     friend bool operator == (D lhs, D rhs) {
    return fabs(lhs.x - rhs.x) < eps;</pre>
      friend bool operator!=(D lhs, D rhs) {
           return fabs(lhs.x - rhs.x) > eps:
     friend bool operator <= (D lhs, D rhs) {
    return lhs < rhs || lhs == rhs;</pre>
      friend bool operator>=(D lhs, D rhs) {
           return lhs > rhs || lhs == rhs;
};
```

1.5 Int128 [85923a]

```
using i128 = __int128_t; // 1.7F38
istream &operator>>(istream &is, i128 &a) {
     i128 sgn = 1; a = 0;
string s; is >> s;
for (auto c : s) {
   if (c == '-') {
                 sgn = -1;
           } else {
                 a = a * 10 + c - '0';
           }
     a *= sgn;
     return is;
ostream &operator<<(ostream &os. i128 a) {
     string res;
if (a < 0) os << '-', a = -a;
while (a) {
           res.push_back(a % 10 + '0');
           a /= 10;
     reverse(res.begin(), res.end());
     os << res; return os;
```

1.6 Rng [401544]

2 Graph

2.1 DFS And BFS [e2d856]

2.2 Prim [7e2d87]

2.3 Bellman-Ford [430ded]

```
// 用 Bellman Ford 找負環
int main() {
    int n, m; cin >> n >> m;
    vector <array <int, 3>> e;
    for (int i = 0; i < m; i++) {
        int u, v, w; cin >> u >> v >> w;
        u --, v --; e.push_back({u, v, w});
}

vector <ll> dis(n, inf), par(n);
int t = -1; dis[0] = 0;
for (int i = 1; i <= n; i++) {
        for (auto [u, v, w] : e) {
            if (dis[v] > dis[u] + w) {
                 dis[v] = dis[u] + w;
                 par[v] = u;
                 if (i == n) t = v;
            }
        }
}

if (t == -1) { cout << "NO|n"; return; }
for (int i = 1; i < n; i++) t = par[t];
vector <int> ans {t};
int i = t;
do {
        i = par[i];
        ans.push_back(i);
} while (i != t);
reverse(ans.begin(), ans.end());
cout << "YES|n";
for (auto x : ans) cout << x + 1 << " ";
}</pre>
```

2.4 Floyd-Warshall [da23ad]

2.5 Euler [4177dc]

```
// 1. 無向圖是歐拉圖:
// 非零度頂點是連通的
// 頂點的度數都是偶數
// 2. 無向圖是半歐拉圖(有路沒有環):
// 非零度頂點是連通的
// 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
// 非零度頂點是強連通的
// 每個頂點的入度和出度相等
| // 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
// 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
// 其他頂點的入度和出度相等
vector<int> ans;
auto dfs = [&](auto &&self, int u) -> void {
   while (g[u].size()) {
   int v = *g[u].begin();
       g[u].erase(v);
       self(self, v);
    ans.push_back(u);
dfs(dfs, 0);
reverse(ans.begin(), ans.end());
```

2.6 DSU [749620]

```
struct DSU {
      vector<int> boss, siz;
      DSU() {}
                 n_) { init(n_); }
      void init(int n_) {
    n = n_; boss.resize(n);
            iota(boss.begin(), boss.end(), 0);
            siz.assign(n, 1);
      int find(int x) {
   if (boss[x] == x) return x;
   return boss[x] = find(boss[x]);
      bool same(int x, int y) {
    return find(x) == find(y);
      bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);</pre>
            siz[x] += siz[y];
            boss[y] = x;
            return true;
      int size(int x) {
   return siz[find(x)];
      }
};
struct DSU {
      vector<int> boss, siz, stk;
      DSU() {}
      DSU(int n_) { init(n_); }
      void init(int n_) {
```

boss.resize(n):

```
iota(boss.begin(), boss.end(), 0);
           siz.assign(n, 1);
           stk.clear();
      int find(int x) {
           return x == boss[x] ? x : find(boss[x]);
     bool same(int x,
           . same(int x, int y) {
  return find(x) == find(y);
     bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);
    siz[x] += siz[y];</pre>
           boss[y] = x;
           stk.push_back(y);
     stk.pop_back();
                 siz[boss[y]] -= siz[y];
                boss[y] = y;
           }
     int size(int x) {
   return siz[find(x)];
};
```

```
2.7 SCC [5d3e16]
struct SCC {
     int n, cur, cnt;
vector<vector<int>> adj;
      vector <int> stk, dfn, low, bel;
SCC(int n_ = 0) { init(n_); }
void init(int n_) {
            n = n_;
adj.assign(n, {});
            dfn.assign(n, -1);
            low.resize(n);
            bel.assign(n, -1);
            stk.clear();
            cur = cnt = 0;
      void addEdge(int u, int v) {
            adj[u].push_back(v);
      void dfs(int x) {
            dfn[x] = low[x] = cur++;
            stk.push_back(x);
for (auto y : adj[x]) {
    if (dfn[y] == -1) {
                         dfs(y);
                        low[x] = min(low[x], low[y]);
se if (bel[y] == -1) {
low[x] = min(low[x], dfn[y]);
                  }
            if (dfn[x] == low[x]) {
                  int y;
                  do {
                         y = stk.back();
                  bel[y] = cnt;
stk.pop_back();
while (y != x);
                  cnt++;
            }
      vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
            return bel;
      struct Graph {
            int n;
            vector<pair<int, int>> edges;
            vector<int> siz;
            vector<int> cnte;
      Graph compress() {
            Graph g;
g.n = cnt;
            g.siz.resize(cnt);
            g.cnte.resize(cnt);
            g.the.restze(ctn),
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;
    for (auto j : adj[i]) {
        if (bel[i] != bel[j]) {
    }
}</pre>
                              g.edges.emplace_back(bel[i], bel[j]);
                         } else {
                              g.cnte[bel[i]]++;
                  }
            return g;
```

```
}: }
```

2.8 VBCC [bce8f5]

```
struct VBCC {
   int n, cur, cnt;
   vector<vector<int>> adj;
   vector<vector<int>> bcc;
       vector<int> stk, dfn, low;
      n = n_;
             adj.assign(n, {});
             bcc.assign(n, {});
             dfn.assign(n,
             low.resize(n);
             ap.assign(n, false);
             stk.clear();
             cur = cnt = 0;
       void addEdge(int u, int v) {
   adj[u].push_back(v);
             adj[v].push_back(u);
       void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
             stk.push_back(x);
int child = 0;
             int child = 0;
for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
        dfs(y, x), child++;
        low[x] = min(low[x], low[y]);
        if (low[y]) >= dfn[x]) {
        int v:
                                low[y] >= din[x]/ \
int v;

do {
    v = stk.back();
    bcc[v].push_back(cnt);
    stk.pop_back();
} while (v != y);
bcc[x].push_back(cnt);
                          if (low[y] >= dfn[x] && p != -1) {
    ap[x] = true;
                   } else {
                          low[x] = min(low[x], dfn[y]);
             if (p == -1 && child > 1) {
                    ap[x] = true;
             }
       vector < bool > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i, -1);
}</pre>
             return ap;
       struct Graph {
             vector<pair<int, int>> edges;
             vector<int> bel;
             vector<int> siz; // BCC 內節點數
             vector<int> cnte; // BCC 內邊數
       Graph compress() {
Graph g; // 壓完是一棵樹,但不一定每個 bel 都有節點 g.bel.resize(n);
             g.siz.resize(cnt);
             g.cnte.resize(cnt);
for (int u = 0; u < n; u++) {
    if (ap[u]) {
        g.bel[u] = cnt++;
        resize(cnt);
}</pre>
                          g.siz.emplace_back();
g.cnte.emplace_back();
                          for (auto v : bcc[u])
                                g.edges.emplace_back(g.bel[u], v);
                   } else if (bcc[u].size() == 1) {
   g.bel[u] = bcc[u][0];
                   g.siz[g.bel[u]]++;
            }
             return g;
}:
```

2.9 EBCC [59d8ca]

```
struct EBCC { // CF/contest/1986/pF
   int n, cur, cnt;
        vector < int >> adj;
        vector<int> stk, dfn, low, bel;
        vector<pair<int, int>> bridges; // 關鍵邊
EBCC(int n_ = θ) { init(n_); }
void init(int n_) {
               adj.assign(n, {});
               dfn.assign(n, -1);
               low.resize(n);
               bel.assign(n, -1);
stk.clear();
               bridges.clear();
               cur = cnt = 0;
        void addEdge(int u, int v) {
   adj[u].push_back(v);
               adj[v].push_back(u);
        void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
    stk.push_back(x);
              for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
        dfs(y, x);
        low[x] = min(low[x], low[y]);
        if (low[y] > dfn[x]) {
            bridges.emplace_back(x, y);
        l
                     } else if (bel[y] == -1) {
    low[x] = min(low[x], dfn[y]);
               if (dfn[x] == low[x]) {
                      int y;
do {
                            y = stk.back();
                            bel[y] = cnt;
                     stk.pop_back();
} while (y != x);
                      cnt++;
        fvector < int> work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {</pre>
                            dfs(i, -1);
                     }
               return bel:
        struct Graph {
               int n;
vector<pair<int, int>> edges;
               vector<int> siz; // BCC 內節點數
               vector<int> cnte; // BCC 內邊數
       Graph compress() {
              Graph g;
g.n = cnt;
g.siz.resize(cnt);
               g.cnte.resize(cnt);
               for (int i = 0; i < n; i++) {
   g.siz[bel[i]]++;</pre>
                      g.stz[bet[i]]++,
for (auto j : adj[i]) {
    if (bel[i] < bel[j]) {
        g.edges.emplace_back(bel[i], bel[j]);
    } else if (i < j) {</pre>
                                   g.cnte[bel[i]]++;
                     }
               return g;
       }
};
```

2.10 2-SAT [28688f]

2.11 Funtional Graph [e8fd64]

```
constexpr int N = 2E5 + 5;
int cht[N][31]; // 倍增表, 放外面不然 TLE struct FuntionalGraph {
        int n, cnt;
vector<int> g, bel, id, len, in, top;
FuntionalGraph() : n(0) {}
         FuntionalGraph(vector<int> g_) { init(g_); }
void init(vector<int> g_) {
    n = g_.size(); cnt = 0;
                g = g; bel.assign(n, -1);
id.resize(n); len.clear();
in.assign(n, 0); top.assign(n, -1);
                build();
        void build() {
    for (int i = 0; i < n; i++) {
        cht[i][0] = g[i];
        in[g[i]]++;
}</pre>
                for (int i = 1; i <= 30; i++)
    for (int u = 0; u < n; u++)
        cht[u][i] = cht[cht[u][i - 1]][i - 1];
for (int i = 0; i < n; i++)
    if (in[i] == 0) label(i);
for (int i = 0; i < n; i++)
    if (top[i] == -1) label(i);</pre>
         void label(int u) {
   vector<int> p; int cur = u;
   while (top[cur] == -1) {
                         top[cur] = u:
                         p.push_back(cur);
                         cur = g[cur];
                id[cyc[i]] = i;
                 if (!cyc.empty())
                ++cnt, len.push_back(cyc.size());

for (int i = p.size() - 1; i > 0; i--)

id[p[i - 1]] = id[p[i]] - 1;
         int jump(int u, int k) {
   for (int b = 0; k > 0; b++){
     if (k & 1) u = cht[u][b];
                         k >>= 1;
                 return u;
        }
};
```

3 Data Structure

3.1 BIT [d41d8c]

```
a[i - 1] = a[i - 1] + v:
    T sum(int x) { // 左閉右開查詢
          T`ans{};
         for (int i = x; i > 0; i -= i & -i)
    ans = ans + a[i - 1];
    T rangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
     int select(const T &k, int start = 0) {
         int x = 0; T cur = -sum(start) > k
int x = 0; T cur = -sum(start);
for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n && cur + a[x + i - 1] <= k) {
                   x += i;
                   cur = cur + a[x - 1];
              }
          return x;
    }
template < class T>
struct TwoDFenwick { // 全部以 0 based 使用
    int nx, ny; // row, col 個數
vector <vector <T>> a;
TwoDFenwick(int nx_ = 0, int ny_ = 0) {
         init(nx_, ny_);
     void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
}
     T sum(int x, int y) { // 左閉右開查詢
         }
T rangeSum
          (int lx, int ly, int rx, int ry) { // 左閉右開查詢
          return sum(
               rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
};
```

3.2 RangeBit [d41d8c]

```
template < class T>
struct rangeFenwick { // 全部以 0 based 使用
     int n;
vector<T> d, di;
     rangeFenwick(int n_ = 0) {
           init(n_);
     void init(int n_) {
          d.assign(n, T{});
di.assign(n, T{});
     Joid add(int x, const T &v) {
   T vi = v * (x + 1);
   for (int i = x + 1; i <= n; i += i & -i) {
      d[i - 1] = d[i - 1] + v;
      di[i - 1] = di[i - 1] + v;
}</pre>
          }
     void rangeAdd(int l, int r, const T &v) {
  add(l, v); add(r, -v);
     T sum(int x) { // 左閉右開查詢
           T`ans{};
           for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
           return ans;
     TrangeSum(int l, int r) { // 左閉右開查詢return sum(r) - sum(l);
     int select(const T &k, int start = 0) {
          if (cur + val <= k) {
                           x += i;
cur = cur + val;
                }
```

```
return x;
         }
 template < class T>
 struct rangeTwoDFenwick { // 全部以 0 based 使用
          init(nx_, ny_);
          void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
                   dij.assign(nx, vector<T>(ny, T{}));
           void add(int x, int y, const T &v) {
                  d add(int x, int y, const T &v) {
    T vi = v * (x + 1);
    T vj = v * (y + 1);
    T vij = v * (x + 1) * (y + 1);
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            d[i - 1][j - 1] = d[i - 1][j - 1] + v;
            di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
            dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
            dij[i - 1][j - 1] = dij[i - 1][j - 1] + vij;
            dij[i - 1][j - 1] = dij[i - 1][j - 1] + vij;
            reconstants.</pre>
                 }
           void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
                   add(rx, ry, v);
                   add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
          }
          T sum(int x, int y) { // 左閉右開查詢
                   T ans{};
for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
                                    ans = ans
                                    ans = ans 
+ T(x * y + x + y + 1) * d[i - 1][j - 1];
ans = ans - T(y + 1) * di[i - 1][j - 1];
ans = ans - T(x + 1) * dj[i - 1][j - 1];
ans = ans + dij[i - 1][j - 1];
                   return ans:
          T rangeSum
                    (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                             (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
          }
};
```

3.3 Segment Tree [d41d8c]

```
template < class Info >
struct Seg { // 左閉右開寫法
    int n:
    vector<Info> info;
    Seg() : n(0) {}
Seg(int n_, Info v_ = Info()) {
   init(n_, v_);
    template < class T>
    template < class T>
    void init(vector<T> init_) {
        `info[p] = init_[l];
                 return;
             int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
             pull(p);
        build(1, 0, n);
    void pull(int p) {
    info[p] = info[p * 2] + info[p * 2 + 1];
    void modify(int p, int l, int r, int x, const Info &v) {
        if (r - l == 1) {
    info[p] = v;
            return:
         int m = (l + r) / 2;
        if (x < m) {
    modify(2 * p, l, m, x, v);</pre>
        } else {
```

tag[p] = Tag():

return;

int m = (l + r) / 2; push(p, l, r);

void modify(int p, int l, int r, int x, const Info &v) {
 if (r - l == 1) {
 info[p] = v;
}

```
modify(2 * p + 1, m, r, x, v);
                                                                                                                      if (x < m) {
    modify(2 * p, l, m, x, v);</pre>
            pull(p);
                                                                                                                      } else {
                                                                                                                            modify(2 * p + 1, m, r, x, v);
      void modify(int p, const Info &i) {
            modify(1, 0, n, p, i);
                                                                                                                      pull(p);
      Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    return query(p *</pre>
                                                                                                                void modify(int p, const Info &i) {
                                                                                                                      modify(1, 0, n, p, i);
                                                                                                               Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    push(p, l, r);</pre>
             return query(p
                   2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
                                                                                                                      return query(p *
                                                                                                                             2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      template < class F> // 尋找區間內,第一個符合條件的
                                                                                                                Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
      int findFirst
            (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) return -1;
if (l >= x && r <= y && !pred(info[p])) return -1;
if (r - l == 1) return l;</pre>
                                                                                                                void range_apply
                                                                                                                      (int p, int l, int r, int ql, int qr, const Tag &v) {
if (qr <= l || ql >= r) return;
if (ql <= l && r <= qr) {</pre>
             int m = (l + r) / 2;
            int res = findfirst(2 * p, l, m, x, y, pred);
if (res == -1) {
                                                                                                                             apply(p, l, r, v);
                  res = findFirst(2 * p + 1, m, r, x, y, pred);
                                                                                                                            return:
                                                                                                                      int m = (l + r) / 2;
             return res;
                                                                                                                      push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
      template < class F> // 若要找 last , 先右子樹遞廻即可
int findFirst(int l, int r, F &&pred) {
    return findFirst(1, 0, n, l, r, pred);
                                                                                                                      pull(p);
                                                                                                                void range_apply(int l, int r, const Tag &v) {
};
                                                                                                                      range_apply(1, 0, n, l, r, v);
struct Info {
   int n = 1;
                                                                                                                template < class F> // 尋找區間內,第一個符合條件的
                                                                                                                int findFirst
      int sum = 0;
                                                                                                                      (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) return -1;
if (l >= x && r <= y && !pred(info[p])) return -1;
if (r - l == 1) return l;</pre>
Info operator+(const Info &a, const Info &b) {
   return { a.n + b.n, a.sum + b.sum };
                                                                                                                      int m = (l + r) / 2;
3.4 Lazy Segment Tree [d41d8c]
                                                                                                                      push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
                                                                                                                      if (res == -1) {
    res = findFirst(2 * p + 1, m, r, x, y, pred);
template < class Info, class Tag>
struct LazySeg { // 左閉右開寫法
      int n;
      vector < Info > info:
                                                                                                                      return res:
      vector <Inio tind,
vector <Injo tind,
vector <Injo tind,
LazySeg() : n(0) {}
LazySeg(int n_, Info v_ = Info()) {
   init(n_, v_);</pre>
                                                                                                               template < class F> // 若要找 last,先右子樹遞迴即可int findFirst(int l, int r, F & pred) {
    return findFirst(1, 0, n, l, r, pred);
      template < class T >
LazySeg(vector < T > init_) {
                                                                                                         };
                                                                                                         struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add; void apply(const Tag& v) {
            init(init_);
      void init(int n_, Info v_ = Info()) {
  init(vector(n_, v_));
                                                                                                                      if (v.set_val) {
                                                                                                                            `set_val =´v.
add = v.add:
      template < class T>
      void init (vector<T> init_) {
                                                                                                                      else {
             n = init_.size();
                                                                                                                             add += v.add;
            info.assign(4 << __lg(n), Info());
tag.assign(4 << __lg(n), Tag());</pre>
             function < void(</pre>
                   int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
                                                                                                         struct Info {
                                                                                                                int sum;
                          info[p] = init_[l];
                                                                                                                void apply(int l, int r, const Tag &v) {
    if (v.set_val) {
        sum = (r - l) * v.set_val;
    }
}
                         return;
                   int m = (l + r) / 2;
                  build(p * 2, l, m);
build(p * 2 + 1, m, r);
                                                                                                                      sum += (r - l) * v.add;
                  pull(p);
                                                                                                                // Info &operator=(const Info &rhs) {
                                                                                                                         // 部分 assignment 使用
return *this;
            build(1, 0, n);
      void pull(int p) {
   info[p] = info[p * 2] + info[p * 2 + 1];
                                                                                                         Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
      void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
             tag[p].apply(v);
                                                                                                         3.5 Persistent Segment Tree [d41d8c]
      void push(int p, int l, int r) {
            int m = (l + r) / 2;
if (r - l >= 1) {
    apply(p * 2, l, m, tag[p]);
    apply(p * 2 + 1, m, r, tag[p]);
}
                                                                                                         template < class Info >
struct PST {
    struct Node {
                                                                                                                     Info info = Info();
int lc = 0, rc = 0;
```

vector<Node> nd;

PST(int n_, Info v_ = Info()) { init(n_, v_); }
template < class T>

PST(vector<T> init_) { init(init_); }
void init(int n_, Info v_ = Info()) {

int n = 0; vector<int> rt; PST() : n(0) {}

```
if (rev_valid) {
    swap(lc, rc);
    if (lc) lc->rev_valid ^= 1;
    if (rc) rc->rev_valid ^= 1;
             init(vector<Info>(n . v )):
      template < class T>
      void init(vector<T> init_) {
            n = init_.size();
             nd.clear(); rt.clear();
                                                                                                                     rev valid = false;
            nd.emplace_back(); // 讓 root 指向 1-based rt.push_back(build(0, n, init_));
                                                                                                               int find(int k) { // 找到 min 是 k 的位置 (1-based)
                                                                                                                     push();
int ls = (lc ? lc->siz : 0) + 1;
      int build(int l, int r, vector<Info> &init_) {
  int id = nd.size();
                                                                                                                     if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
            nd.emplace_back();
if (r - l == 1) {
                  nd[id].info = init_[l];
                   return id;
                                                                                                        int size(Treap *t) {
    return t ? t->siz : 0;
            int m = (l + r) >> 1;
nd[id].lc = build(l, m, init_);
nd[id].rc = build(m, r, init_);
                                                                                                         Treap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
             pull(nd[id]);
            return id;
                                                                                                               a->push(); b->push();
if (a->pri > b->pri) {
      void pull(Node &t) {
                                                                                                                     a->rc = merge(a->rc, b);
            t.info = nd[t.lc].info + nd[t.rc].info;
                                                                                                                     a->pull();
                                                                                                                     return a:
      int copy(int t) { // copy 一個 node
  nd.push_back(nd[t]);
  return nd.size() - 1;
                                                                                                               else {
                                                                                                                     b->lc = merge(a, b->lc);
b->pull();
                                                                                                                     return b;
      int generate() { // 創立新的 node
    nd.emplace_back();
             return nd.size() - 1;
                                                                                                        pair<Treap*, Treap*> split(Treap *t, int k) {
                                                                                                               // 分割前 k 個在 first, 剩下的在 second if (t == nullptr) return {nullptr, nullptr};
      int modify(int t, int l, int r, int x, const Info &v) {
            t = t ? copy(t) : generate();
if (r - l == 1) {
    nd[t].info = v;
                                                                                                               t->push();
                                                                                                               if (size(t->lc) < k) {
    auto [a, b] = split(t->rc, k - size(t->lc) - 1);
    t->rc = a;
             int m = (l + r) >> 1;
                                                                                                                     t->pull();
             if (x < m) {
                                                                                                                     return {t, b};
                   nd[t].lc = modify(nd[t].lc, l, m, x, v);
                                                                                                               else {
             } else
                                                                                                                     auto [a, b] = split(t->lc, k);
t->lc = b;
                  nd[t].rc = modify(nd[t].rc, m, r, x, v);
                                                                                                                     t->pull();
            pull(nd[t]);
                                                                                                                     return {a, t};
             return t;
                                                                                                              }
      void modify(int ver, int pos, const Info &val) {
   if (int(rt.size()) <= ver) rt.resize(ver + 1);
   rt[ver] = modify(rt[ver], 0, n, pos, val);</pre>
                                                                                                        void Print(Treap *t) {
    if (!t) return;
    t->push();
      Info query(int t, int l, int r, int ql, int qr) {
    if (l >= qr || r <= ql) return Info();
    if (ql <= l && r <= qr) return nd[t].info;
    int m = (l + r) >> 1;
                                                                                                               Print(t->lc);
                                                                                                               cout << t->val;
Print(t->rc);
            return query(nd[t].
                                                                                                        3.7 RMQ [d41d8c]
                   lc, l, m, ql, qr) + query(nd[t].rc, m, r, ql, qr);
      Info query(int ver, int ql, int qr) {
    return query(rt[ver], 0, n, ql, qr);
                                                                                                         template < class T, class Cmp = less < T >>
                                                                                                         struct RMQ {
                                                                                                               const Cmp cmp = Cmp();
                                                                                                               static constexpr unsigned B = 64; using u64 = unsigned long long;
      void createVersion(int ori ver) {
            rt.push_back(copy(rt[ori_ver]));
                                                                                                               vector<vector<T>> a;
vector<T> pre, suf, ini;
      void reserve(int n, int q) {
   nd.reserve(n + q * (2 * __lg(n) + 1));
   rt.reserve(q + 1);
                                                                                                               vector<u64> stk;
                                                                                                               RMQ() {}
RMQ(const vector<T> &v) { init(v); }
void init(const vector<T> &v) {
      void resize(int n) {
            rt.resize(n);
                                                                                                                     n = v.size();
pre = suf = ini = v;
     }
                                                                                                                     stk.resize(n);
struct Info {
                                                                                                                     if (!n) {
      int sum = 0;
                                                                                                                           return;
Info operator+(const Info &a, const Info &b) {
                                                                                                                     for const int M = (n - 1) / B + 1;
const int lg = __lg(M);
a.assign(lg + 1, vector < T > (M));
for (int i = 0; i < M; i++) {
    a[0][i] = v[i * B];
    for (int j = 1; j < B && i * B + j < n; j++) {
        a[0][i] = min(a[0][i], v[i * B + j], cmp);
}</pre>
      return { a.sum + b.sum };
}
3.6 Treap [d41d8c]
struct Treap {
   Treap *lc, *rc;
      int pri, siz; bool rev_valid;
int val; int min;
Treap(int val_) {
    min = val = val_;
    pri = rand();
    lc = rc = nullptr;
                                                                                                                     for (int i = 1; i < n; i++) {
    if (i % B) {</pre>
                                                                                                                                pre[i] = min(pre[i], pre[i - 1], cmp);
             siz = 1; rev_valid = 0;
                                                                                                                     for (int i = n - 2; i >= 0; i--) {
   if (i % B != B - 1) {
      void pull() { // update siz or other information
                                                                                                                                  1 % B != B - 1) {
suf[i] = min(suf[i], suf[i + 1], cmp);
             siz = 1;
             min = val;
            for (auto c : {lc, rc}) {
   if (!c) continue;
                                                                                                                     for (int j = 0; j < lg; j++) {
    for (int i = 0; i + (2 << j) <= M; i++) {
        a[j + 1][i</pre>
                   siz += c->siz;
                   min = std::min(min, c->min);
            }
                                                                                                                                         ] = min(a[j][i], a[j][i + (1 << j)], cmp);
      void push() {
                                                                                                                     }
```

```
for (int i = 0; i < M; i++) {
   const int l = i * B;
   const int r = min(1U * n, l + B);</pre>
                u64 s = 0;
for (int j = l; j < r; j++) {
                      while (s && cmp(v[j], v[__lg(s) + l])) {
    s ^= 1ULL << __lg(s);</pre>
                      s |= 1ULL << (j - l);
                      stk[j] = s;
                }
          }
     T ans = min(suf[l], pre[r - 1], cmp);
l = l / B + 1;
r = r / B;
if (l < r) {</pre>
                     int k = __lg(r - l);
ans = min
                           ({ans, a[k][l], a[k][r - (1 << k)]}, cmp);
                return ans:
           } else {
                int x = B * (l / B);
return ini
                      [__builtin_ctzll(stk[r - 1] >> (l - x)) + l];
     }
}:
```

3.8 Mo [d41d8c]

4 Flow Matching

4.1 Dinic [d41d8c]

```
template < class T>
struct Dinic {
      struct Edge {
            int to;
             T flow, cap; // 流量跟容量
      int n, m, s, t;

const T INF_FloW = 1 << 30;
      vector<vector<int>> adj; // 此點對應的 edges 編號
      vector <Edge> edges; // 幫每個 edge 編號
vector <int> dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_; m = 0;
             dis.resize(n); ptr.resize(n);
adj.assign(n, {});
edges.clear();
       void add_edge(int u, int v, T cap) {
              // 偶數 id 是正向邊
             // Image to Learning
edges.push_back({v, 0, cap});
edges.push_back({u, 0, 0});
adj[u].push_back(m++);
adj[v].push_back(m++);
      bool bfs() {
             fill(dis.begin(), dis.end(), -1);
dis[s] = 0; queue<int> q;
              a.push(s):
              while (!q.empty() && dis[t] == -1) {
                    int u = q.front(); q.pop();
for (int id : adj[u]) {
    Edge &e = edges[id];
                            if (e.flow == e.cap) continue;
                           if (dis[e.to] == -1) {
    dis[e.to] = dis[u] + 1;
                                  q.push(e.to);
                           }
                   }
              return dis[t] != -1;
      }
T dfs(int u, T flow) {
             if (flow == 0) return 0;
if (u == t) return flow;
for (int &cur = ptr[u]; cur < adj[u].size(); cur++) {
   Edge &e = edges[adj[u][cur]];
}</pre>
                    if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;
T mn = dfs(e.to, min(flow, e.cap - e.flow));
                    if (mn > 0) {
```

```
e.flow += mn:
                    edges[adj[u](cur] ^ 1].flow -= mn;
                    return mn;
              }
          }
          return 0; // 到不了終點就會 return 0
      T work(int s_, int t_) {
    s = s_; t = t_; T flow = 0;
    while (bfs()) {
               fill(ptr.begin(), ptr.end(), 0);
               while (true) {
   T res = dfs(s, INF_Flow);
                    if (res == 0) break;
                    flow += res;
               }
          return flow;
     edges[i].flow = 0;
      void reuse(int n_) { // 走殘留網路, res += flow
    while (n < n_) {
        adj.emplace_back();</pre>
               dis.emplace_back();
               ptr.emplace_back();
          }
     }
1:
```

4.2 Min Cut [d41d8c]

4.3 MCMF [d41d8c]

```
template < class Tf, class Tc>
struct MCMF {
    struct Edge {
        int to;
        Tf flow, cap; // 流量跟容量
        Tc cost;
    };
    int n, m, s, t;
    const Tf INF_FLOW = 1 << 30;
    const Tc INF_COST = 1 << 30;
    vector < vector < int>> adj;
    vector < Tc> dis, pot; // johnson algorithm, using spfa
    vector <Tc> dis, pot; // johnson algorithm, using spfa
    vector <Tc> dis, pot; // johnson algorithm, using spfa
    vector <br/>
    vector obool> inq;
    MCMF(int n_ = 0) { init(n_); }
    void init(int n_) {
        n = n_; m = 0;
        edges.clear();
        adj.assign(n, {});
    }
    void add_edge(int u, int v, Tf cap, Tc cost){
        edges.push_back({v, 0, cap, cost});
        edges.push_back({u, 0, 0, -cost});
```

struct Hungarian { // 0-based, O(VE)

int n, m;

```
adj[u].push_back(m++);
adj[v].push_back(m++);
                                                                                                                   vector<vector<int>> adi:
                                                                                                                   vector <int> adj,
vector <int> used, vis;
vector <pair <int, int> match;
Hungarian(int n_ = 0, int m_ = 0) {
   init(n_, m_);
      bool spfa() {
             dis.assign(n, INF_COST);
             rt.assign(n, -1); inq.assign(n, false);
queue<int> q;
q.push(s), dis[s] = 0, inq[s] = true;
                                                                                                                   void init(int n_, int m_) {
                                                                                                                         n = n_; m = m_;
adj.assign(n + m, {});
used.assign(n + m, -1)
vis.assign(n + m, 0);
             q.push(s), dis[s] = 0, inq[s] = true;
while (!q.empty()) {
   int u = q.front(); q.pop();
   inq[u] = false;
   for (int id : adj[u]) {
      auto [v, flow, cap, cost] = edges[id];
      Tc ndis = dis[u] + cost + pot[u] - pot[v];
      if (flow < cap && dis[v] > ndis) {
                                                                                                                   void addEdge(int u, int v) {
   adj[u].push_back(n + v);
   adj[n + v].push_back(u);
                                 dis[v] = ndis; rt[v] = id;
                                                                                                                   bool dfs(int u) {
                                 if (!inq[v]) {
                                                                                                                         int sz = adj[u].size();
for (int i = 0; i < sz; i++) {
   int v = adj[u][i];</pre>
                                       q.push(v);
                                       inq[v] = true;
                                }
                                                                                                                                if (vis[v] == 0) {
    vis[v] = 1;
                          }
                  }
                                                                                                                                       if (used[v] == -1 || dfs(used[v])) {
    used[v] = u;
             return dis[t] != INF_COST;
       bool dijkstra() {
             dis.assign(n, INF_COST); rt.assign(n, -1);
priority_queue<pair<Tc, int>,
    vector<pair<Tc, int>>, greater<pair<Tc, int>>> pq;
                                                                                                                                }
                                                                                                                          return false;
             vector<pair<Tc, int>>, greater<pair<Tc, int>>;
dis[s] = 0; pq.emplace(dis[s], s);
while (!pq.empty()) {
    auto [d, u] = pq.top(); pq.pop();
    if (dis[u] < d) continue;
    for (int id : adj[u]) {
        auto [v, flow, cap, cost] = edges[id];
        Tc ndis = dis[u] + cost + pot[u] - pot[v];
        if (flow < cap && dis[v] > ndis) {
            dis[v] = ndis; rt[v] = id;
            pa emplace(ddis v):
                                                                                                                   vector<pair<int. int>> work() {
                                                                                                                          match.clear();
                                                                                                                          vased.assign(n + m, -1);
vis.assign(n + m, 0);
for (int i = 0; i < n; i++) {
    fill(vis.begin(), vis.end(), 0);
    fill(vis.begin(), vis.end(), 0);</pre>
                                                                                                                                 dfs(i);
                                                                                                                          for (int i = n; i < n + m; i++)
    if (used[i] != -1)</pre>
                                 pq.emplace(ndis, v);
                          }
                   }
                                                                                                                                       match.emplace_back(used[i], i - n);
             return dis[t] != INF_COST;
                                                                                                            };
      }
// 限定 flow, 最小化 cost
pair<Tf, Tc> work_flow(int s_, int t_, Tf need) {
    s = s_, t = t_; pot.assign(n, 0);
    Tf flow{}; Tc cost{}; bool fr = true;
    while ((fr ? spfa() : dijkstra())) {
        for (int i = 0; i < n; i++) {
            dis[i] += pot[i] - pot[s];
    }
                                                                                                                     Theorem [d41d8c]
                                                                                                            4.5
                                                                                                           // 有向無環圖:
                                                                                                            // 最小不相交路徑覆蓋:
                                                                                                            // 最小路徑數 = 頂點數 - 最大匹配數
                   If f = INF_FLOW;
for (int i = t; i != s; i = edges[rt[i] ^ 1].to)
    f = min
                                                                                                            // 最小相交路徑覆蓋:
                                                                                                           // 先用
                                                                                                                    Floyd 求傳遞封包,有連邊就建邊,然後再套最小不相交路徑覆蓋
                                  (f, edges[rt[i]].cap - edges[rt[i]].flow);
                   // 二分圖:
                                                                                                            // 最小點
                                                                                                                    覆蓋:選出一些點,讓所有邊至少有一個端點在點集中的最少數量
                   flow += f; need -= f;
cost += f * dis[t]; fr = false;
                                                                                                            // 最小點覆蓋 = 最大匹配數
                                                                                                            // 還原解, flow 的作法是從源點開始 dfs, 只走 cap - flow > 0
                   swap(dis, pot);
if (need == 0) break;
                                                                                                            // 的邊,最後挑選左邊還沒被跑過的點和右邊被跑過的點當作覆蓋的點
                                                                                                            // 最少邊覆蓋: 選出一些邊,讓所有點都覆蓋到的最少數量
             return {flow, cost};
      }
                                                                                                            // 最少邊覆蓋 = 點數 - 最大匹配數
      // 限定 cost,最大化 flow
pair<Tf, Tc> work_budget(int s_, int t_, Tc budget) {
                                                                                                            // 最大獨立集: 選出一些點, 使這些點兩兩沒有邊連接的最大數量
             Tr flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {</pre>
                                                                                                           // 最大獨立集 = 點數 - 最大匹配數
                                                                                                             5
                                                                                                                     String
                          dis[i] += pot[i] - pot[s];
                                                                                                            5.1 Hash [852711]
                   constexpr int B = 59;
vector<Z> Hash(string &s) {
                   (f, edges[rt[i]].cap - edges[rt[i]].flow);
f = min<Tf>(f, budget / dis[t]);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
   edges[rt[i]].flow += f;
   edges[rt[i] ^ 1].flow -= f;
}
                                                                                                                   vector<Z> ans {0};
for (auto c : s) {
                                                                                                                          ans.push_back(ans.back() * B + (c - 'a' + 1));
                                                                                                                   return ans;
                                                                                                             void solve() {
                   flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
                                                                                                                   string s, sub;
cin >> s >> sub;
                    swap(dis, pot);
                                                                                                                   auto a = Hash(s);
auto q = Hash(sub);
auto find = q.back();
                    if (budget == 0 || f == 0) break;
             return {flow, cost};
                                                                                                                   int ans = 0;
int l = 1, r = sub.size(), len = sub.size();
      void reset() {
    for (int i = 0; i < m; i++)</pre>
                                                                                                                   while (r <= s.size()) {
   if (a[r] - a[l - 1] * power(Z(B), len) == find) {</pre>
                   edges[i].flow = 0;
                                                                                                                                ans++:
}:
4.4 Hungarian [d41d8c]
                                                                                                                   cout << ans << "\n":
```

5.2 KMP [731acf]

```
struct KMP {
         string sub;
vector<int> fail;
          // fail 存匹配失敗時,移去哪
           // 也就是 sub(0, i) 的最長共同前後綴長度
         KMP() {}
KMP(const string &sub_) {
                   build(sub_);
         }
vector < int > build(const string & sub_) {
    sub = sub_, fail.resize(sub.size(), -1);
    for (int i = 1; i < sub.size(); i++) {
        int now = fail[i - 1];
        while (now != -1 && sub[now + 1] != sub[i])
            now = fail[now];
        if (sub[now + 1] == sub[i])
            fail[i] = now + 1;
}</pre>
                   return fail;
          vector<int> match(const string &s) {
                   vector < int > match;
for (int i = 0, now = -1; i < s.size(); i++) {</pre>
                            (int i = 0, now = -1; i < s.size(); i++) :
// now 是成功匹配的長度 -1
while (s[i] != sub[now + 1] && now != -1)
    now = fail[now];
if (s[i] == sub[now + 1]) now++;
if (now + 1 == sub.size()) {
    match.push_back(i - now);
    now = fail[now];
                                      now = fail[now];
                            }
                    return match;
        }
};
```

5.3 Z Function [5b63dc]

```
| // z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
| // 的最長公共前綴 (LCP) 的長度
| vector < int > Z(const string & s) {
        int n = s.size();
        vector < int > z(n);
        z[0] = n; // lcp(s, s), -1 or n
        for (int i = 1, j = 1; i < n; i++) {
             z[i] = max(0, min(j + z[j] - i, z[i - j]));
            while (i + z[i] < n & s[z[i]] == s[i + z[i]]);
            z[i]++;
        if (i + z[i] > j + z[j]) j = i;
        }
        return z;
}
```

5.4 Manacher [958661]

5.5 Trie [31e4ff]

```
constexpr int N = 1E7;
int tot = 0;
int trie[N][26], cnt[N];
void reset() {
   tot = 0, fill_n(trie[0], 26, 0);
}
int newNode() {
   int x = ++tot;
   cnt[x] = 0, fill_n(trie[x], 26, 0);
   return x;
}
void add(string &s) {
   int p = 0;
```

```
for (auto c : s) {
    int &q = trie[p][c - 'a'];
    if (!q) q = newNode();
    p = q;
  }
  cnt[p] += 1;
}
int find(string &s) {
  int p = 0;
  for (auto c : s) {
    int q = trie[p][c - 'a'];
    if (!q) return 0;
    p = q;
  }
  return cnt[p];
}
```

5.6 SA [b58946]

```
struct SuffixArray {
                  int n; string s;
vector<int> sa, rk, lc;
                  // n: 字串長度
                  // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
                   // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
                  數組, lc[i] 表示 sa[i] 和 sa[i + 1] 的最長公共前綴長度
SuffixArray(const string &s_) {
                              s = s_; n = s.length();
sa.resize(n);
lc.resize(n - 1);
                                    rk.resize(n);
                                  iota(sa.begin(), sa.end(), 0);
sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });
rk[sa[0]] = 0;
for (int i = 1; i < n; i++)</pre>
                                                 rk[sa[i]]
                                                                            = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
                                   vector < int > tmp, cnt(n);
                                  two converses the converse that the converse the converse that the converse tha
                                                                  tmp.push_back(n - k + i);
                                                    for (auto i : sa)
    if (i >= k)
                                                                                     tmp.push_back(i - k);
                                                    fill(cnt.begin(), cnt.end(), 0);
for (int i = 0; i < n; i++)
+-cnt[rk[i]];
                                                   for (int i = 1; i < n; i++)
  cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; i--)
  sa[--cnt[rk[tmp[i]]]] = tmp[i];
                                                 for (int i = 0, j = 0; i < n; i++) {
   if (rk[i] == 0) {</pre>
                                                                    j = 0;
                                                    } else {
                                                                    for (j -=

    j > 0; i + j < n && sa[rk[i] - 1] + j < n

    && s[i + j] == s[sa[rk[i] - 1] + j]; j++);
                                                   }
                                 }
};
```

5.7 SAM [3bdfeb]

```
struct SAM {
    // 1 -> initial state
    static constexpr int ALPHABET_SIZE = 26;
    struct Node {
        int len;
        int link;
        array<int, ALPHABET_SIZE> next;
        Node() : len{}, link{}, next{} {}
};

vector<Node> t;
SAM() {
        init();
}

void init() {
        t.assign(2, Node());
        t[0].next.fill(1);
        t[0].len = -1;
}
int newNode() {
        t.emplace_back();
        return t.size() - 1;
}
```

```
int extend(int p, int c) {
   if (t[p].next[c]) {
                      int q = t[p].next[c];
                      if (t[q].len == t[p].len + 1) {
                             return q;
                      int r = newNode();
t[r].len = t[p].len + 1;
t[r].link = t[q].link;
t[r].next = t[q].next;
t[q].link = r;
                      while (t[p].next[c] == q) {
                            t[p].next[c] = r;
p = t[p].link;
                      return r;
               int cur = newNode();
               tht cur = newhoue();
t[cur].len = t[p].len + 1;
while (!t[p].next[c]) {
    t[p].next[c] = cur;
    p = t[p].link;
               t[cur].link = extend(p, c);
               return cur:
       }
vector < int > last(n + 1); // s[i - 1] 的後綴終點位置
        last[0] = 1;
SAM sam;
        for (int i = 0; i < n; i++)
    last[i + 1] = sam.extend(last[i], s[i] - 'a');
int sz = sam.t.size();</pre>
        vector < int > cnt(sz);
for (int i = 1; i <= n; i++)</pre>
        cnt[last[i]]++; // 去重 = 1
vector < vector < int >> order(sz);
for (int i = 1; i < sz; i++)
    order[sam.t[i].len].push_back(i);
        for (int i = sz - 1; i > 0; i--)
    for (int u : order[i])
        if (sam.t[u].link != -1)
            cnt[sam.t[u].link] += cnt[u];
        vector < ll> dp(sz, -1);
auto dfs = [&](auto self, int u) -> void {
    dp[u] = cnt[u];
               for (int c = 0; c < SAM::ALPHABET_SIZE; c++) {
   int v = sam.t[u].next[c];</pre>
                      dp[u] += dp[v];
               }
        dfs(dfs, 1);
```

5.8 Palindrome Tree [77b763]

```
struct PAM {
   // 0 -> even root, 1 -> odd root
        static constexpr int ALPHABET_SIZE = 26;
       struct Node {
    int len;
    int fail;
               array<int, ALPHABET_SIZE> next;
Node() : len{}, fail{}, next{} {}
       vector<int> s;
        vector < Node > t;
       PAM() {
               init();
       void init() {
               t.assign(2, Node());
               s.clear();
               t[0].len = 0;
t[1].len = -1;
t[0].fail = 1;
        int newNode() {
               t.emplace_back();
               return t.size() - 1;
       int extend(int p, int c) {
               int n = s.size();
s.push_back(c);
while (s[n - t[p].len - 1] != c)
    p = t[p].fail;
if (!t[p].next[c]) {
    int r = newNode();
    t[l].len + f[l].len + 2.
                      tht | - newhole();
t[r].len = t[p].len + 2;
int cur = t[p].fail;
while (s[n - t[cur].len - 1] != c)
    cur = t[cur].fail;
t[r].fail = t[cur].next[c];
t[n].next[c] - r.
                       t[p].next[c] = r;
               p = t[p].next[c];
```

```
return p;
}
};
void solve() {
    string s; cin >> s;
    int n = s.length();
    vector < int > last(n + 1);
    last[0] = 1;
    PAM pam;
    for (int i = 0; i < n; i++)
        last[i + 1] = pam.extend(last[i], s[i] - 'a');
    int sz = pam.t.size();
    vector < int > cnt(sz);
    for (int i = 1; i <= n; i++)
        cnt[last[i]]++; // 去重 = 1
    for (int i = sz - 1; i > 1; i--)
        cnt[pam.t[i].fail] += cnt[i];
}
```

5.9 Duval [f9dcca]

```
|// duval_algorithm
 // 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
 vector<string> duval(string s) {
        int i = 0, n = s.size();
vector<string> res;
        while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
      else k++;</pre>
                    j++;
               while (i <= k) {
                    res.push_back(s.substr(i, j - k));
i += j - k;
        return res:
 // 最小旋轉字串
 string min_round(string s) {
        s += s;
int i = 0, n = s.size();
        int start = i;
while (i < n / 2) {</pre>
              start = i:
              start = 1;
int k = i, j = i + 1;
while (s[k] <= s[j] && j < n) {
   if (s[k] < s[j]) k = i;
   else k++;</pre>
                    j++;
              while (i <= k) {
    i += j - k;</pre>
        return s.substr(start, n / 2);
```

6 Math

6.1 Modulo [bbc481]

```
template < class T>
constexpr T power(T a, ll b) {
   T res {1};
      for (; b; b /= 2, a *= a)
if (b & 1) res *= a;
      return res:
constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
      res %= p;
if (res < 0) res += p;
      return res;
template < ll P >
struct MInt {
      ll x;
      constexpr MInt() : x {0} {}
constexpr MInt(ll x) : x {norm(x % getMod())} {}
static ll Mod;
      constexpr static ll getMod() {
   return P > 0 ? P : Mod;
      constexpr static void setMod(ll Mod_) {
    Mod = Mod_;
      constexpr ll norm(ll x) const {
            if (x < 0) x += getMod();
if (x >= getMod()) x -= getMod();
return x;
      constexpr MInt operator-() const {
   return MInt(norm(getMod() - x));
      constexpr MInt inv() const {
   return power(*this, getMod() - 2);
      constexpr MInt &operator*=(MInt rhs) & {
```

```
if (getMod() < (1ULL << 31)) {
    x = x * rhs.x % int(getMod());
} else {
    ...</pre>
                x = mul(x, rhs.x, getMod());
           return *this;
     constexpr MInt &operator+=(MInt rhs) & {
           x = norm(x + rhs.x);
return *this;
     constexpr MInt &operator -= (MInt rhs) & {
           x = norm(x - rhs.x);
return *this;
     constexpr MInt &operator/=(MInt rhs) & {
  return *this *= rhs.inv();
     friend constexpr MInt operator*(MInt lhs, MInt rhs) {
   return lhs *= rhs;
     friend constexpr MInt operator+(MInt lhs, MInt rhs) {
           return lhs += rhs;
     friend constexpr MInt operator-(MInt lhs, MInt rhs) {
           return lhs -= rhs;
     friend constexpr MInt operator/(MInt lhs, MInt rhs) {
   return lhs /= rhs;
     friend istream &operator>>(istream &is, MInt &a) {
    ll v; is >> v; a = MInt(v); return is;
     friend ostream &operator<<(ostream &os, const MInt &a) {</pre>
     friend constexpr bool operator==(MInt lhs, MInt rhs) {
   return lhs.x == rhs.x;
     friend constexpr bool operator!=(MInt lhs, MInt rhs) {
   return lhs.x != rhs.x;
     friend constexpr bool operator<(MInt lhs, MInt rhs) {
   return lhs.x < rhs.x;</pre>
template <>
ll MInt < 0 > :: Mod = 998244353;
constexpr ll P = 1E9 + 7;
using Z = MInt<P>;
6.2 Combination [6aa734]
struct Comb {
```

```
_invfac.resize(m + 1);
                 _inv.resize(m + 1);
for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;
                 for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
}
                 n = m;
         If ac(ll m) {
    if (m > n) init(2 * m);
    return _fac[m];
         Z invfac(ll m) {
   if (m > n) init(2 * m);
   return _invfac[m];
         Z inv(ll m) {
   if (m > n) init(2 * m);
   return _inv[m];
        }
Z binom(ll n, ll m) {
    if (n < m || m < 0) return 0;
    return fac(n) * invfac(m) * invfac(n - m);
}</pre>
        J lucas(ll n, ll m) { // Mod 要在 1E5 左右
    if (m == 0) return 1;
    return binom(n % Z::getMod(), m % Z::getMod())
    * lucas(n / Z::getMod(), m / Z::getMod());
|} comb; // 注意宣告, 若要換模數需重新宣告
```

6.3 Sieve [37ae54]

```
vector<int> primes, minp;
void sieve(int n) {
    minp.assign(n + 1, 0);
     primes.clear();
```

```
// minp[i] == i, 質數
for (int i = 2; i <= n; i++) {
    if (minp[i] == 0) {
                             minp[i] = i;
                             primes.push_back(i);
                   for (auto p : primes) {
    if (i * p > n) break;
    minp[i * p] = p;
    if (p == minp[i]) break;
}
          }
}
// a ^ (m-1) = 1 (Mod m)
// a ^ (m-2) = 1/a (Mod m)
// Exp2: cout << power(x, power(y, p, Mod - 1), Mod)
// Num = (x+1) * (y+1) * (z+1)...
// Sum = (a^0 + a^1+...+ a^x) * (b^0 +...+ b^y)
// Mul = N * (x+1) * (y+1) * (z+1) / 2
 6.4 MillerRabinPollardRho [40f4c1]
 template < class T>
```

```
res = mul(res, a, p);
          }
      return res;
constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
      res %= p;
if (res < 0) res += p;
vector<ll
return 0:
bool IsPrime(ll n) {
     if (n < 2) return 0;

if (n % 2 == 0) return n == 2;

ll d = n - 1, s = 0;

while (d % 2 == 0) {

    d /= 2, s++;
      for (ll i : chk) {
    if (!check(i, d, s, n)) return 0;
      return 1;
const vector<ll> small = {2, 3, 5, 7, 11, 13, 17, 19};
ll FindFactor(ll n) {
    if (IsPrime(n)) return 1;
    for (ll p : small) {
        if (n % p == 0) return p;
}
      }
ll x, y = 2, d, t = 1;
auto f = [&](ll a) {
           return (mul(a, a, n) + t) % n;
      for (int l = 2; ; l *= 2) {
           x = y;
int m = min(l, 32);
for (int i = 0; i < l; i += m) {</pre>
                 for (int j = 0; j < m; ++j) {
    y = f(y), d = mul(d, abs(x - y), n);</pre>
                 ll g = gcd(d, n);
                 if (g == n) {
    l = 1, y = 2, ++t;
    break;
                 if (g != 1) return g;
          }
     }
map<ll, int> res;
void PollardRho(ll n) {
     if (n == 1) return;
if (IsPrime(n)) {
           res[n]++;
           return;
      ll d = FindFactor(n);
      PollardRho(n / d), PollardRho(d);
```

6.5 CRT [d41d8c]

```
| ll exgcd(ll a, ll b, ll &x, ll &y) {
```

```
if (!b) {
          x = 1, y = 0;
          return a;
}
ll g = exgcd(b, a % b, y, x);
y -= a / b * x;
return g;
}
ll inv(ll x, ll m){
    ll a, b;
    exgcd(x, m, a, b);
    a %= m;
    if (a < 0) a += m;
    return a;
}
// remain, mod
ll CRT(vector < pair < ll, ll >> & a) {
        ll prod = 1;
        for (auto x : a) {
            prod *= x.second;
        }
        ll res = 0;
        for (auto x : a) {
                auto t = prod / x.second;
                res += x.first * t % prod * inv(t, x.second) % prod;
                if(res >= prod) res -= prod;
}
return res;
}
```

6.6 Matrix [a97208]

```
template < class T >
struct Matrix {
     int n, m;
      vector<vector<T>> mat;
     constexpr Matrix(int n_, int m_) { init(n_, m_); }
constexpr Matrix(vector<vector<T>> mat_) { init(mat_); }
      constexpr void init(int n_, int m_) {
    n = n_; m = m_;

           mat.assign(n, vector<T>(m));
      constexpr void init(vector<vector<T>> mat_) {
   n = mat_.size();
   m = mat_[0].size();
           mat = mat_;
     constexpr Matrix &operator*=(const Matrix &rhs) & {
           assert(mat[0].size() == rhs.mat.size());
           int n = mat
                  .size(), k = mat[0].size(), m = rhs.mat[0].size();
           .size(), K - mar[0].size(), ...
Matrix res(n, m);
for (int i = 0; i < n; i++)
    for (int j = 0; j < m; j++)
    for (int l = 0; l < k; l++)
                            res.mat[i][j] += mat[i][l] * rhs.mat[l][j];
           mat = res.mat;
return *this;
      friend constexpr
           Matrix operator*(Matrix lhs, const Matrix &rhs) {
return lhs *= rhs;
template < class T>
constexpr Matrix<T> unit(int n) {
     Matrix<T> res(n, n);
for (int i = 0; i < n; i++)
   res.mat[i][i] = 1;</pre>
      return res;
constexpr Matrix<T> power(Matrix<T> a, ll b) {
     assert(a.n == a.m);
     for (; b; b /= 2, a *= a)
    if (b % 2) res *= a;
      return res;
```

6.7 Mex [14628f]

```
template < class T>
int mex(vector < T > &v) {
    unordered_set < T > s;
    for (auto e : v) s.insert(e);
    for (T i = 0; ; i++)
        if (s.find(i) == s.end()) return i;
}
```

6.8 Game Theorem

- sg 值為 0 代表先手必敗
- 當前 sg 值 = 可能的後繼狀態的 mex (例如拿一個或拿兩個, 就等於兩者的 sg 值 mex), 若有互相依賴就兩個後繼狀態 xor 當作一組 sg 值 (例如切開成 兩半, 只算一次)
- ・ 單組基礎 nim 的 sg 值為本身的原因: f(0)=0, f(1)=mex(f(0))=1, f(2)=mex(f(0),f(1))=2...,都是自己 ・ 多組賽局可以把 sg 值 xor 起來,當成最後的 sg 值, nim 也是一樣,且由於
- 多組賽局可以把 sg 值 xor 起來, 當成最後的 sg 值, nim 也是一樣, 且由於 xor 性質, 如果可以快速知道 sg(1)g(2)...g(n), 就可以用 xor 性質處理不連續組合

6.9 Integer Partition [595ed2]

6.10 Mobius Theorem

- 數論 分塊 可以快速 計算 一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d) g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n}\!\mu(d)\!=\!\begin{cases} 1 & \text{for } n\!=\!1\\ 0 & \text{for } n\!\neq\!0 \end{cases}$$

- 2. μ是常數函數1的反元素
- $\Rightarrow \mu * 1 = \epsilon , \epsilon(n)$ 只在n = 1時為 1,其餘情況皆為 0。
- $-\phi$ 歐拉函數: x以下與x互質的數量

$$\phi*1 = \sum_{d|n} \phi(\frac{n}{d})$$
 質因數分解
$$= \sum_{i=0}^{c} \phi(p^{i})$$

$$= 1 + p^{0}(p-1) + p^{1}(p-1) + \dots + p^{c-1}(p-1)$$

$$= p^{c}$$

$$= id$$

• 莫比烏斯反演公式

-
$$f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$$

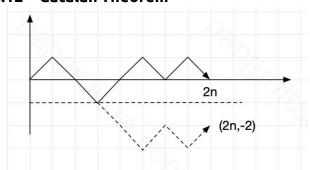
- $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

例子

$$\begin{split} &\sum_{i=aj=c}^{b} \sum_{j=1}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \frac{y}{k} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{x} [d|i] \sum_{j=1}^{y} [d|j] \text{ d 可整除 i 時為 1} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.11 Mobius Inverse [d41d8c]

6.12 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$ 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有x 個,往下有y 個,會有:
 - $\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$

所以只要扣掉 C_{n-1}^{2n} 即可

6.13 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- · X/G:本質不同的方案的集合
- X'^g : 對於某一種操作 g, 所有方案中, 經過 g 這種翻轉後保持不變的方案的集合
- 集合取絕對值代表集合數

7 Search and Gready

7.1 Binary Search [d41d8c]

```
int main() {
     // 二分找上界
while (lo < hi) {
   int x = (lo + hi + 1) / 2;
          if (check(x)) lo = x;
          else hi = x - 1;
     }
     cout << lo; // 保證有解
     while (lo <= hi) {
          int x = (lo + hi) / 2;
if (check(x)) lo = x + 1;
else hi = x - 1;
     cout << hi; // 範圍外代表無解
     // 二分找下界
     while (lo < hi) {
   int x = (lo + hi) / 2;
   if (check(m)) hi = x;</pre>
          else lo = x + 1;
     cout << lo; // 保證有解
     while (lo <= hi) {</pre>
          int x = (lo + hi) / 2;
if (check(m)) hi = x - 1;
          else lo = x + 1;
     cout << lo; // 範圍外代表無解
```

7.2 Ternary Search [d41d8c]

```
int main() {
    int lo = 0, hi = 10;
    while (lo <= hi) {
        int xl = lo + (hi - lo) / 3;
        int xr = hi - (hi - lo) / 3;
        int ansl = check(xl), ansr = check(xr);
        if (ansl < ansr) {
            lo = xl + 1;
        } else {
            hi = xr - 1;
        }
        // record ans and index
    }
}</pre>
```

8 Tree

8.1 Binary Lifting LCA [4273df]

```
const int Q = 20; // log(q) or log(n)
vector<vector<int>> par;
vector<cint> dep, dfn;
void build(int n, vector<vector<int>> &tree, int u = 0) {
    par.assign(n, vector<int>(Q + 1, -1));
    dep.assign(n, 0), dfn.assign(n, 0);
    int cur = 0;
    auto dfs = [&](auto self, int x, int p) -> void {
        dfn[x] = cur++;
        for (auto y : tree[x]) {
            if (y == p) continue;
            par[y][0] = x;
            dep[y] = dep[x] + 1;
            self(self, y, x);
        }
    };
    par[u][0] = u;
    dfs(dfs, 0, -1);
    for (int i = 1; i <= Q; i++)
        for (int j = 0; j < n; j++)
            par[j][i] = par[par[j][i - 1]][i - 1];
}
int lca(int a, int b) {
    if (dep[a] < dep[b]) swap(a, b);
    int pull = dep[a] - dep[b];
    for (int i = 0; i <= Q; i++)
        if (pull & (1 << i))
            a = par[a][i];
    if (a == b) return a;
    for (int i = Q; i >= 0; i--)
            if (par[a][i] != par[b][i])
            a = par[a][i], b = par[b][i];
    return par[a][0];
}
int jump(int x, int k) {
    for (int i = Q; i >= 0; i--)
            if (k >> i & 1)
                 x = par[x][i];
    return x;
}
```

8.2 Centroid Decomposition [c40feb]

```
#include <bits/stdc++.h>
using namespace std;
struct CenDecom {
       int n;
       vector<vector<int>> adj;
       vector < bool > vis;
vector < int > siz;
       CenDecom(int n_ = 0) { init(n_); }
void init(int n_) {
             n = n:
             adj.assign(n, {});
vis.assign(n, false);
siz.assign(n, 1);
      void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void get_siz(int x, int p = -1) {
             siz[\bar{x}] = 1;
             for (int y : adj[x]) {
   if (y == p || vis[y]) continue;
   get_siz(y, x);
   siz[x] += siz[y];
             }
       int get_cen(int x, int sz, int p = -1) {
             for (int y : adj[x]) {
    if (y == p || vis[y]) continue;
    if (siz[y] * 2 > sz)
                         return get_cen(y, sz, x);
             return x;
       void get_ans(int x, int p) {
             // do something
for (int y : adj[x]) {
                    if (y == p || vis[y]) continue;
```

```
get_ans(y, x);
}

void work(int x = 0) {
    get_siz(0, x);
    int cen = get_cen(x, siz[x]);
    vis[cen] = true;
    for (int y : adj[cen]) {
        if (vis[y]) continue;
        get_ans(y, cen);
    }
    for (int y : adj[cen]) {
        if (vis[y]) continue;
        work(y);
    }
};
```

8.3 Heavy Light Decomposition [41d99e]

```
struct HLD {
      int n, cur;
vector <int> siz, top, dep, parent, in, out, seq;
vector <vector <int>> adj;
      vector < vector < int >> adj;
HLD(int n = 0) { init(n ); }
void init(int n = 0;
    n = n = n; cur = 0;
    siz.resize(n); top.resize(n); dep.resize(n);
    parent.resize(n); in.resize(n); out.resize(n);
    seq.resize(n); adj.assign(n, {});
}
      void addEdge(int u, int v) {
  adj[u].push_back(v);
  adj[v].push_back(u);
       void work(int rt = 0) {
              top[rt] = rt;
dep[rt] = 0;
              parent[rt] = -1;
              dfs1(rt); dfs2(rt);
      void dfs1(int u) {
    if (parent[u] != -1)
        adj[u] erase(find
              (adj[u].begin(), adj[u].end(), parent[u]));
siz[u] = 1;
              for (auto &v : adj[u]) {
                     parent[v] = u, dep[v] = dep[u] + 1;
                     dfs1(v);
siz[u] += siz[v];
                     if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
                     } // 讓 adj[u][0] 是重子節點
             }
       void dfs2(int u) {
              in[u] = cur++;
              seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
   top[v] = v == adj[u][0] ? top[u] : v;
   dfs2(v);
              out[u] = cur;
       int lca(int u, int v) {
    while (top[u] != top[v]) {
        if (dep[top[u]] > dep[top[v]]) {
                            u = parent[top[u]];
                    } else {
                            v = parent[top[v]];
                    }
              return dep[u] < dep[v] ? u : v;</pre>
       int dist(int u, int v) {
   return dep[u] + dep[v] - 2 * dep[lca(u, v)];
       int jump(int u, int k) {
   if (dep[u] < k) return -1;
   int d = dep[u] - k;
   while (dep[top[u]] > d)
                    u = parent[top[u]]
              return seq[in[u] - dep[u] + d];
      bool isAncester(int u, int v) {
    return in[u] <= in[v] && in[v] < out[u];</pre>
       int rootedParent(int rt, int v) {
              swap(rt, v);
if (rt == v) return rt;
if (!isAncester(rt, v)) return parent[rt];
              auto it = upper_bound(adj[
    rt].begin(), adj[rt].end(), v, [&](int x, int y) {
    return in[x] < in[y];</pre>
              }) - 1;
return *it;
       int rootedSize(int rt, int v) {
              if (rt == v) return n;
if (!isAncester(v, rt)) return siz[v];
return n - siz[rootedParent(rt, v)];
```

```
int rootedLca(int rt, int a, int b) {
    return lca(rt, a) ^ lca(a, b) ^ lca(b, rt);
};
```

8.4 Link Cut Tree [96c213]

```
template < class Info, class Tag>
struct LinkCutTree { // 1-based
             struct Node {
                        Info info = Info();
Tag tag = Tag();
bool rev = false;
                         int size = 0;
int ch[2], p = 0;
             vector<Node> nd;
             LinkCutTree(int n = 0) { init(n); }
             void init(int n) {
                         nd.clear();
                         nd.emplace_back();
                         resize(n):
             void resize(int n) {
                        nd.resize(n + 1);
             bool isrt(int t) {
    return !nd[t].p || (
        nd[nd[t].p].ch[0] != t && nd[nd[t].p].ch[1] != t);
             void make_rev(int t) {
    swap(nd[t].ch[0], nd[t].ch[1]);
    nd[t].rev ^= true;
             void apply(int t, const Tag &v) {
                         nd[t].info.apply(nd[t].size, v);
                         nd[t].tag.apply(v);
             void push(int t) {
                         if (nd[t].rev) {
                                     if (nd[t].ch[0]) make_rev(nd[t].ch[0]);
if (nd[t].ch[1]) make_rev(nd[t].ch[1]);
nd[t].rev = false;
                         if (nd[t].ch[0]) apply(nd[t].ch[0], nd[t].tag);
if (nd[t].ch[1]) apply(nd[t].ch[1], nd[t].tag);
                         nd[t].tag = Tag();
             void pull(int t) {
                         nd[t].size
                                       = 1 + nd[nd[t].ch[0]].size + nd[nd[t].ch[1]].size;
                         nd[t].info
                                        .pull(nd[nd[t].ch[0]].info, nd[nd[t].ch[1]].info);
             int pos(int t) {
                         return nd[nd[t].p].ch[1] == t;
             void pushAll(int t) {
                         if (!isrt(t))
                                     pushAll(nd[t].p);
                         push(t);
             void rotate(int t) {
                         int q = nd[t].p;
int x = !pos(t);
                         nd[q].ch[ix] = nd[t].ch[x];
if (nd[t].ch[x]) nd[nd[t].ch[x]].p = q;
nd[t].p = nd[q].p;
                        nu_().p = nd[q].p;
if (!isrt(q)) nd[nd[q].p].ch[pos(q)] = t;
nd[t].ch[x] = q;
nd[q].p = t;
pull(q);
             void splay(int t) {
                         pushAll(t);
                         pushAll(t);
while (!isrt(t)) {
    if (!isrt(nd[t].p)) {
        if (pos(t) == pos(nd[t].p)) {
            rotate(nd[t].p);
            rotate(nd[t].p);

                                                              rotate(t);
                                                  }
                                     rotate(t);
                         pull(t);
             void access(int t) { // access 後自動 splay
    for (int i = t, q = 0; i; q = i, i = nd[i].p) {
                                      splay(i);
                                     nd[i].ch[1] = q;
                                     pull(i);
                         splay(t);
             void makeRoot(int t) {
                         make_rev(t);
             int findRoot(int t) {
                         access(t);
```

```
while (nd[x].ch[0]) {
                push(x)
                 x = nd[x].ch[0];
           access(x);
           return x;
      bool connected(int x, int y) {
    return findRoot(x) == findRoot(y);
      bool neighber(int x, int y) {
           makeRoot(x);
           access(y);
if (nd[y].ch[\theta] != x || nd[x].ch[1]) return false;
      void split(int rt, int y) {
           makeRoot(y);
           access(rt);
      void link(int x, int y) {
           makeRoot(x);
if (findRoot(y) != x)
                 nd[x].p = y;
      void cut(int x, int y) {
    makeRoot(x);
           access(y);
           nd[y].ch[0] = nd[nd[y].ch[0]].p = 0;
pull(x);
           pull(y);
      void modify(int x, const Info &v) {
           access(x):
           nd[x].info = v;
      void path_apply(int x, int y, const Tag &v) {
           assert(connected(x, y));
           split(x, y);
           applv(x, v):
     Info path_query(int x, int y) {
    assert(connected(x, y));
           split(x, y);
           return nd[x].info;
     }
};
 constexpr int Mod = 51061;
struct Tag {
    ll add = 0; ll mul = 1;
      void apply(const Tag &v) {
  mul = mul * v.mul % Mod;
  add = (add * v.mul % Mod + v.add) % Mod;
struct Info {
    ll val = 0; ll sum = 0;
     void apply(int size, const Tag &v) {
  val = (val * v.mul % Mod + v.add) % Mod;
  sum = (sum * v.mul % Mod + v.add * size % Mod) % Mod;
      void pull(const Info &l, const Info &r) {
   sum = (l.sum + r.sum + val) % Mod;
};
```

8.5 Virtual Tree [41e291]

```
// 多次詢問給某些關鍵點, 虛樹可達成快速樹 DP (前處理每個點)
// 例如這題是有權樹,給一些關鍵點,求跟 vertex 1 隔開的最小成本
// 前處理 root 到所有點的最小邊權
vector<int> stk:
void insert(int key, vector<vector<int>> &vt) {
    if (stk.empty()) {
    stk.push_back(key);
         return:
    int l = lca(stk.back(), key);
    if (l == stk.back())
         stk.push_back(key);
         return:
         stk.size() > 1 && dfn[stk[stk.size() - 2]] > dfn[l]) {
vt[stk[stk.size() - 2]].push_back(stk.back());
stk.pop_back();
    if (stk.size() < 2 || stk[stk.size() - 2] != l) {
   vt[l].push_back(stk.back());
   stk.back() = l;</pre>
    } else {
   vt[l].push_back(stk.back());
         stk.pop_back();
    stk.push_back(key);
int work(vector<vector<int>>> &vt) {
    while (stk.size() > 1) {
  vt[stk[stk.size() - 2]].push_back(stk.back());
         stk.pop_back();
```

```
int rt = stk[0];
        stk.clear();
        return rt;
void solve() {
       int n; cin >> n;
vector<vector<int>> g(n);
vector<vector<pair<int, int>>> wg(n);
vector<vector<int>> vt(n);
        for (int i = 1; i < n; i++) {
   int u, v, w;
   cin >> u >> v >> w;
                u--, v--;
g[u].push_back(v), g[v].push_back(u);
wg[u].emplace_back(v, w), wg[v].emplace_back(u, w);
        build(n, g); // build LCA
       vector<int> dis(n, 1E9); // root 到各點的最小邊權
auto dfs_dis = [&](auto &&self, int x, int p) -> void {
    for (auto [y, w] : wg[x]) {
        if (y == p) continue;
        dis[y] = min(w, dis[x]);
        self(self, y, x);
               }
        };
dfs_dis(dfs_dis, 0, -1);
        vector<bool> iskey(n);
        vector<ll> dp(n):
        int q; cin >> q;
        int q; cin >> q;
while (q--) {
   int m; cin >> m;
   vector cint > key(m);
   for (int i = 0; i < m; i++) {
      cin >> key[i];
      key[i] -= 1;
}
                        iskey[key[i]] = true;
                key.push_back(0); // 固定 0 為 root, 看題目需求
sort(key.begin(), key.end(), [&](int a, int b) {
    return dfn[a] < dfn[b];
}); // 要 sort 再 insert
for (auto x : key) insert(x, vt);
                work(vt);
                auto dfs = [&](auto &&self, int x) -> void {
    for (auto y : vt[x]) {
        self(self, y);
    }
}
                                if (iskey[y]) { // 直接砍了
dp[x] += dis[y];
                                } else { // 不敬 or 敬 dp[x] += min<ll>(dp[y], dis[y]);
                                } // 記得 reset
                                 iskey[y] = dp[y] = 0;
                        vt[x].clear(); // 記得 reset
                dfs(dfs, 0);
cout << dp[0] << "\n";</pre>
                dp[0] = 0; // 最後 reset root
}
```

8.6 Dominator Tree [0b03d9]

```
存起點到達此點的必經的上個節點(起點 = 自己), 無法到達 = -1
struct Dominator_tree {
       int n. id:
       vector<vector<int>> adj, radj, bucket;
vector<int> sdom, dom, vis, rev, pa, rt, mn, res;
Dominator_tree(int n_ = 0) { init(n_); }
        void init(int n_) {
               n = n_, id = 0;
adj.assign(n, {});
radj.assign(n, {});
               radj.assign(n, {});
bucket.assign(n, {});
sdom.resize(n), dom.assign(n, -1);
vis.assign(n, -1), rev.resize(n);
pa.resize(n), rt.resize(n);
               mn.resize(n), res.resize(n);
        void add_edge(int u, int v) {
               adj[u].push_back(v);
       fint query(int v, int x) {
    if (rt[v] == v) return x ? -1 : v;
    int p = query(rt[v], 1);
    if (p == -1) return x ? rt[v] : mn[v];
    if (sdom[mn[v]] > sdom[mn[rt[v]]])
        mn[v] = mn[rt[v]];
    rt[v] = p;
    return x ? p : mn[v];
}
```

```
National Chung Cheng University Salmon
       vector<int> build(int s) {
             dfs(s);
for (int i = id - 1; i >= 0; i--) {
                   for (int u : radj[i])
    sdom[i] = min(sdom[i], sdom[query(u, 0)]);
if (i) bucket[sdom[i]].push_back(i);
                   for (int u : bucket[i])
                         int p = query(u, 0);
dom[u] = sdom[p] == i ? i : p;
                   if (i) rt[i] = pa[i];
             res.assign(n, -1);
            for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i])
        dom[i] = dom[dom[i]];
for (int i = 1; i < id; i++)
    res[rev[i]] = rev[dom[i]];</pre>
             res[s] = s;
for (int i = 0; i < n; i++)
                   dom[i] = res[i];
             return dom:
};
9
      DP
9.1 LCS [087c0d]
int main() {
      int m, n; cin >> m >> n;
string s1, s2; cin >> s1 >> s2;
```

9.2 LIS [91741b]

9.3 Edit Distance [308023]

```
| int main() {
    string s1, s2; cin >> s1 >> s2;
    int n1 = s1.size(), n2 = s2.size();

    // dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元
    vector <int > dp(n2 + 1);
    iota(dp.begin(), dp.end(), 0);
    for (int i = 1; i <= n1; i++) {
        vector <int > cur(n2 + 1); cur[0] = i;
        for (int j = 1; j <= n2; j++) {
            if (s1[i - 1] == s2[j - 1]) {
                cur[j] = dp[j - 1];
```

```
9.4 Bitmask [da8000]
void hamiltonianPath() {
      int n, m; cin >> n >> m;
vector<vector<int>> adj(n);
      for (int i = 0; i < m; i++) {
    int u, v; cin >> u >> v;
            adj[--v].push_back(--u);
      // 以...為終點,走過...
      vector dp(n, vector<int>(1 << n));</pre>
     dp[0][1] = 1;
for (int mask = 1; mask < 1 << n; mask++) {
    if ((mask & 1) == 0) continue;
    for (int i = 0; i < n; i++) {
        if ((mask >> i & 1) == 0) continue;
        if (i == n - 1 && mask != (1 << n) - 1) continue;
        int pre = mask ^ (1 << i);
        for (int j : adj[i]) {
            if ((pre >> j & 1) == 0) continue;
            dp[i][mask] = (dp[i][mask] + dp[j][pre]) % Mod;
        }
}
      dp[0][1] = 1;
           }
      cout << dp[n - 1][(1 << n) - 1] << "\n";
void elevatorRides() {
      int n, x; cin >> n >> x;
vector < int >> a(n);
for (int i = 0; i < n; i++) {</pre>
      vector<int> dp(1 << n), f(1 << n);
dp[0] = 1; // 次數、已使用人數
for (int mask = 1; mask < 1 << n; mask++) {
            dp[mask] = 2E9;
for (int i = 0; i < n; i++) {
    if ((mask >> i & 1) == 0) continue;
    int pre = mask ^ (1 << i);</pre>
                  f[mask] = a[i];
           }
      cout << dp[(1 << n) - 1] << "\n";
}
void minClique() { // 移掉一些邊,讓整張圖由最少團組成
      int n, m;
cin >> n >> m;
       vector<bitset<N>> g(n);
      for (int i = 0; i < m; i++) {</pre>
            int u, v;
cin >> u >> v;
            g[u][v] = g[v][u] = 1;
       vector<int> dp(1 << n, inf);
      dp[0] = 1;
      for (int mask = 0; mask < 1 << n; mask++) { // 先正常 dp
            for (int i = 0; i < n; i++) {
   if (mask & (1 << i)) {
     int pre = mask ^ (1 << i);
}</pre>
                        dp[mask] = 1; // i 有連到所有 pre
                        }
           }
            mask = 0; mask < 1 << n; mask++) { // 然後枚舉子集 dp
for (int sub = mask; sub; --sub &= mask) {
                  dp[mask] = min(dp[mask], dp[sub] + dp[mask ^ sub]);
      cout << dp[(1 << n) - 1] << "\n";
```

9.5 Projects [469e4a]

```
int from, to, w, id;
       int n; cin >> n; vector<E> a(n + 1);
       for (int i = 1; i <= n; i++) {</pre>
             int u, v, w;
cin >> u >> v >> w
              a[i] = \{u, v, w, i\};
       vector<array<ll, 2>> dp(n + 1); // w, time
      vector<array<int, 2>> rec(n + 1), // 有沒選, 上個是誰
sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
    int id = --lower_bound
        (all(a), E({0, a[i].from}), [](E x, E y) {
        return x.to < y.to;
    }
                 return ...
- a.begin();
- do[i - 1];
             dp[i] = dp[i - 1];
ll nw = dp[id][0] + a[i].w;
ll nt = dp[id][1] + a[i].to - a[i].from;
if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
    dp[i] = {nw, nt};
                    rec[i] = {1, id};
              }
       vector<int> ans;
       for (int i = n; i != 0;) {
   if (rec[i][0]) {
                  ans.push_back(a[i].id);
                    i = rec[i][1];
             } else { i--;
1
```

9.6 Removal Game [588f62]

9.7 Monotonic Queue [f4976d]

```
| // 應用: dp(i) = h(i) + max(A(j)), for l(i)≤j≤r(i)
| // A(j) 可能包含 dp(j), h(i) 可 O(1)
| void Bounded_Knapsack() {
| int n, k; // O(nk) |
| vector<int> w(n), v(n), num(n); |
| deque<int> q; |
| // 於是我們將同餘的數分在同一組 |
| // 每次取出連續 num[i] 格中最大值 |
| // g_x = max(_{{k=0}}^num[i] (g'_{x-k} + v_i*k)) |
| // G_x = g'_{x} - v_i*x |
| // x 代 x-k => v_i*(x-k) |
| // g_x = max(_{{k=0}}^num[i] (G_{x-k} + v_i*x)) |
| vector<vector<ll>> dp(2, vector<ll>>(k + 1)); |
| for (int i = 0; i < n; i++) { | // 餘數 |
| q.clear(); // q 記錄在 x = i 時的 dp 有單調性 |
| for (int x = 0; x * w[i] + r <= k; x++) { |
| while (!q.empty() && q.front() < x - num[i]) |
| q.pop_front(); // 維護遞減 |
| l nxt = dp[0][x * w[i] + r] - x * v[i]; |
| while (!q.empty() && dp[0][q.back |
| () * w[i] + r] - q.back() * v[i] < nxt) |
| q.pop_back(); |
| q.push_back(x); |
| dp[1][x * w[i] + r] = dp[0][q.front() |
| * w[i] + r] - q.front() * v[i] + x * v[i]; |
| } |
| swap(dp[0], dp[1]); |
| cout << dp[0][k] << "\n"; |
```

9.8 SOS [7a4936]

```
| // 使用情況: 跟 bit 與(被)包含有關,且 x 在 1E6 左右
| // 題目: 一數組,問有多少所有數 & 起來為 o 的集合數
| // dp[
| x] 代表包含 x 的 y 個數(比 x 大且 bit 1 全包含 x 的有幾個)
```

```
// 答案應該包含在 dp[0] 内,但是有重複元素,所以考慮容斥 // => ans = \{i=0\}^{n} (-1)^{pop\_count(i)} 2^{dp[i]-1}
|// => 全
                部為 0 的個數 - 至少一個為 1 的個數 + 至少兩個為 1 的個數
   void solve() {
                 int n; cin >> n; Z ans = 0;
vector <int> a(n);
for (int i = 0; i < n; i++) cin >> a[i];
                 int m = __lg(*max_element(a.begin(), a.end())) + 1;
                 // 定義 dp[mask] 為 mask 被包含於 a[i] 的 i 個數
                  vector < Z > dp(1 << m);
                for (int i = 0; i < n; i++)
    dp[a[i]] += 1;
for (int i = 0; i < m; i++) {
    for (int mask = 0; mask < 1 << m; mask++) {
        if (mask >> i & 1) {
            int pre = mask ^ (1 << i);
            int
                                                         dp[pre] += dp[mask];
                             }
                 for (int mask = 0; mask < 1 << m; mask++) {
    int sgn = __builtin_popcount(mask) & 1 ? -1 : 1;
    ans += sgn * (power(Z(2), dp[mask].val()) - 1);</pre>
                 cout << ans << "\n":
  }
 // x / y = x, 代表包含於 x 的 y 個數, 定義為 dp[x][0]
| / / x & y = x,代表包含 x 的 y 個數,定義為 dp[x][1]
  // x & y != 0, 代表至
                  少有一個位元都為 1 的 y 個數, = n - 與自己相同 - \sim dp[x][0]
   void solve() {
                int n; cin >> n;
vector < int > a(n);
                 map <int, int> mp;
for (int i = 0; i < n; i++) {
    cin >> a[i];
                              mp[a[i]]++;
                 int m = __lg(*max_element(a.begin(), a.end())) + 1;
vector<array<ll, 2>> dp(1 << m);
for (int i = 0; i < n; i++) {
    dp[a[i]][0] += 1;
    dp[a[i]][1] += 1;</pre>
                 for (int i = 0; i < m; i++) {
    for (int mask = 0; mask < 1 << m; mask++) {</pre>
                                           if (mask >> i & 1) {
   int pre = mask ^ (1 << i);
   dp[mask][0] += dp[pre][0];</pre>
                                                         dp[pre][1] += dp[mask][1];
                                           }
                 << n - (dp[((1 << m) - 1) ^ a[i]][0]) << "\n";</pre>
 }
```

9.9 CHT [5f5c25]

```
|// 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \le r(i)
// A(j), B(j) 可能包含 dp(j), 分別就是 m 跟 b
 struct Line {
     ll m,
     line(ll m = 0, ll b = 0) : m(m), b(b) {}
ll eval(ll x) {
   return m * x + b;
1:
struct CHT { // 用在查詢單調斜率也單調
int n, lptr, rptr;
vector<Line> hull;
      CHT(int n_ = 0, Line init_ = Line()) {
   init(n_, init_);
      void init(int n_ = 0, Line init_ = Line()) {
    n = n_; hull.resize(n); reset(init_);
      void reset(Line init_ = Line()) {
    lptr = rptr = 0; hull[0] = init_;
      bool pop_front(Line &l1, Line &l2, ll x) {
          // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y
           // 代表查詢的當下,右線段的高度已經低於左線段了
          return l1.eval(x) >= l2.eval(x);
      bool pop_back(Line &l1, Line &l2, Line &l3) {
          // 本題斜率遞減、上凸包
          // 因此只要 12 跟
          l3 的 X 交點 <= l1 跟 l3 的 X 交點, l2 就用不到了
return (l3.b - l2.b)
* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
      void insert(Line L)
          while (rptr - ĺptr
                 > 0 && pop_back(hull[rptr - 1], hull[rptr], L))
```

9.10 DNC [d2ed4d]

9.11 LiChao Segment Tree [588aa3]

```
// 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \le r(i)
                                            m x
constexpr ll inf = 4E18;
struct Line {
    ll m, b;
      Line(ll'm = 0, ll b = inf) : m(m), b(b) {}
      ll eval(ll x) const {
    return m * x + b;
     }
struct LiChaoSeg { // 取 max 再變換就好
     vector <Line > info;
LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_) {
           info.assign(4 << __lg(n), Line());
      void update(Line line, int node, int l, int r) {
   int m = (l + r) / 2;
   bool left = line.eval(l) < info[node].eval(l);</pre>
           bool mid = line.eval(m) < info[node].eval(m);</pre>
           if (mid) swap(info[node], line); // 如果新線段比較好
           if (r - l == 1) return;
else if (left != mid) update(line, 2 * node, l, m);
           // 代表左半有交點
           else update(line, 2 * node + 1, m, r);
           // 代表如果有交點一定在右半
     void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
   if (r - l == 1) return info[node].eval(x);
   int m = (l + r) / 2;
           if (x < m) {
                return min(
                      info[node].eval(x), query(x, 2 * node, l, m));
                return min(info
                      [node].eval(x), query(x, 2 * node + 1, m, r));
      ll query(int x) {
           return query(x, 1, 0, n);
};
```

9.12 Codeforces Example [a0184a]

```
// CF 1932 pr
// 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
// 請問在線段不重複的情況下,最多獲得幾分
int main() {
    int n, m;
    cin >> n >> m;
```

```
// 記錄每點有幾個線段
      // 再一個紀錄,包含這個點的左界
      for (int i = 0; i < m; i++) {</pre>
           int l, r; cin >> l >> r;
l_side[r] = min(l_side[r], l);
           cnt[l]++;
           cnt[r + 1]--;
      for (int i = 2; i <= n; i++)
      cnt[i] += cnt[i - 1];
for (int i = n; i >= 2; i--)
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
      vector < int > dp(n + 1);
      dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
           dp[i] = cnt[i];
if (l_side[i] != inf)
    dp[i] += dp[l_side[i] - 1];
dp[i] = max(dp[i], dp[i - 1]);
      cout << dp[n] << "\n";
}
 // CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
 // 再加上 max(bi) - min(bi)
 int main(){
      int n, k, ans = 0; cin >> n >> k;
vector<pii> v(n + 1);
for (int i = 1; i <= n; i++) {</pre>
           int a, b; cin >> a >> b;
v[i] = {a, b};
if (a <= k) ans = 1;</pre>
      sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
      }); // 用 bi 來排,考慮第 i 個時可以先扣
      vector<vector<int>> dp(n + 1, vector<int>(n + 1, inf));
      // 考慮 v[i] 時,選 j 個的 sum(ai) - min(bi)
      for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
                     min(不選,選)
                 if (dp[i
                         1][j - 1] + v[i].first + v[i].second <= k) {
                       // 假如可以選,更新 ans 時再加回去 bi
                      ans = max(ans, j);
           dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
      cout << ans << "\n";
```

10 Geometry

10.1 Basic [d41d8c]

```
template < class T>
struct Point {
    Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) {} template < class U >
     operator Point<U>() {
         return Point < U > (U(x), U(y));
     Point & operator += (const Point &p) & {
        x += p.x; y += p.y; return *this;
     Point &operator -= (const Point &p) & {
        x -= p.x; y -= p.y; return *this;
     Point &operator*=(const T &v) & {
    x *= v; y *= v; return *this;
     Point &operator/=(const T &v) & {
    x /= v; y /= v; return *this;
     Point operator -() const {
    return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
   return a += b;
     friend Point operator - (Point a, const Point &b) {
         return a -= b;
     friend Point operator*(Point a, const T &b) {
   return a *= b;
     friend Point operator/(Point a, const T &b) {
         return a /= b;
     friend Point operator*(const T &a, Point b) {
   return b *= a;
     friend bool operator==(const Point &a, const Point &b) {
         return a.x == b.x && a.y == b.y;
```

```
friend istream &operator>>(istream &is, Point &p) {
          return is >> p.x >> p.y;
     friend ostream &operator<<(ostream &os, const Point &p) {</pre>
          return os << "(" << p.x << ", " << p.y << ")";
template < class T>
T dot(const Point<T> &a, const Point<T> &b) {
   return a.x * b.x + a.y * b.y;
Template < class T >
T cross(const Point < T > &a, const Point < T > &b) {
    return a.x * b.y - a.y * b.x;
template < class T>
T square(const Point < T > &p) {
     return dot(p, p);
template < class T>
double length(const Point<T> &p)
    return sqrt(double(square(p)));
Point<T> normalize(const Point<T> &p) {
     return p / length(p);
template < class T>
Point<T> rotate(const Point<T> &a) {
     return Point(-a.y, a.x);
Jemplate < class T >
int sgn(const Point < T > & a) {
    return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
template < class T >
struct Line {
     Point <T> a:
     Point <T> b;
     Line(const Point<T> &a_ = Point<T>()
           , const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
template < class T>
double length(const Line<T> &l) {
     return length(l.a - l.b);
bool parallel(const Line<T> &l1, const Line<T> &l2) {
   return cross(l1.b - l1.a, l2.b - l2.a) == 0;
template < class T>
double distance(const Point < T > & a, const Point < T > & b) {
     return length(a - b);
template < class Ta
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)
     return distance(p, l.a);</pre>
     if (dot(p - l.b, l.a - l.b) < 0)
    return distance(p, l.b);</pre>
     return distancePL(p, l);
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
   return cross(l.b - l.a, p - l.a) > 0;
template<class T>
Point < T
      > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
     return ll.a + (ll.b - ll.a) * (cross(l2.b - l2.a, ll.a - l2.a) / cross(l2.b - l2.a, ll.a - l1.b));
template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
    return cross(p - l.a, l.b - l.a) == 0 &&
            min(l.a.x, l.b.x) \ll p.x \ll p.x \ll max(l.a.x, l.b.x)
                (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
template < class T>
int n = p.size(), t = 0;
for (int i = 0; i < n; i++)</pre>
          if (pointOnSegment(a, Line(p[i], p[(i + 1) % n])))
     return true;
for (int i = 0; i < n; i++) {
    auto u = p[i];</pre>
          auto v = p[(i + 1) \% n];
          if (u.x < a.
               x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
t ^= 1;
          t ^= 1;
```

```
return t == 1:
// 0 : not inside
// 1 : on boundary
// 2 : strictly inside
template < class T>
int pointInConvexPolygon
        (const Point<T> &a, const vector<Point<T>> &p) {
       int n = p.size();
       if (n == 0) {
              return 0;
       } else if (n == 1)
              return a == p[0];
       if (pointOnSegment(a, Line(p[0],
                p[1])) || pointOnSegment(a, Line(p[0], p[n - 1]))) {
       return 0;
       int lo = 1, hi = n - 2;
while (lo < hi) {
   int x = (lo + hi + 1) / 2;</pre>
              if (pointOnLineLeft(a, Line(p[0], p[x]))) {
              lo = x;
} else {
                    hi = x - 1;
       if (pointOnLineLeft(a, Line(p[lo], p[lo + 1]))) {
              return 2;
       } else {
              return pointOnSegment(a, Line(p[lo], p[lo + 1]));
template < class T>
bool lineIntersectsPolygon
        (const Line<T> &l, const vector<Point<T>> &p) {
       int n = p.size();
Point<T> a = l.a, b = l.b;
for (int i = 0; i < n; i++) {
    Line<T> seg(p[i], p[(i + 1) % n]);
if (cross(b));
              if (cross(b - a , seg.a - a) == 0 || cross(b - a, seg.b - a) == 0)
                     return true;
              if (cross(b
                      - a, seg.a - a) > 0 ^ cross(b - a, seg.b - a) > 0)
                     return true;
       return false;
// 0 : not intersect
// 1 : strictly inter
// 2 : overlap
     1 : strictly intersect
// 3 : intersect at endpoint
template < class T>
tuple < int , Point < T > , Point < T >> segmentIntersection
      le<int, Point<T>, Point<T>> segmentIntersection
  (const Line<T> &l1, const Line<T> &l2) {
   if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
      return {0, Point<T>(), Point<T>()};
  if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
      return {0, Point<T>(), Point<T>()};
  if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y))
      return {0, Point<T>(), Point<T>()};
  if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y))
      return {0, Point<T>(), Point<T>()};
  if (cons(l1.b - l1.a, l2.b - l2.a) == 0) {
    if (cross(l1.b - l1.a, l2.a - l1.a) != 0) }
              if (cross(l1.b - l1.a, l2.a - l1.a) !=
    return {0, Point<T>(), Point<T>()};
              } else {
                     auto maxx1 = max(l1.a.x, l1.b.x);
                     auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
auto miny1 = min(l1.a.y, l1.b.y);
                     auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.y, l2.b.y);
                     auto miny2 = min(l2.a.y, l2.b.y);
                     Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
                     if (!pointOnSegment(p1, l1))
                    swap(p1.y, p2.y);
if (p1 == p2) {
                            return {3, p1, p2};
                    } else {
                            return {2, p1, p2};
             }
       auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
       if ((cp1 > 0 && cp2 > 0) || (cp1 < 0 && cp2 
 < 0) || (cp3 > 0 && cp4 > 0) || (cp3 < 0 && cp4 < 0)) 
   return {0, Point<T>(), Point<T>()};
       Point p = lineIntersection(l1, l2);
if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
              return {1, p, p};
       } else {
              return {3, p, p};
```

```
template < class T>
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
   if (get<0>(segmentIntersection(l1, l2)) != 0)
           return 0.0;
     return min({distancePS(l1.a, l2), distancePS(l1
    .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
template < class T>
bool segmentInPolygon
    l segmentInPolygon
  (const Line<T> &l, const vector<Point<T>> &p) {
  int n = p.size();
  if (!pointInPolygon(l.a, p)) return false;
  if (!pointInPolygon(l.b, p)) return false;
  if (int i = 0; i < n; i++) {
    auto u = p[i];
    auto v = p[(i + 1) % n];
    auto w = p[(i + 2) % n];
    auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
    if (t == 1) return false;
    if (t == 0) continue;
    if (t == 2) {</pre>
           if (t == 2) {
                if (pointOnSegment(v, l) && v != l.a && v != l.b)
    if (cross(v - u, w - v) > θ)
        return false;
          || pointOnLineLeft(l.b, Line(v, u)))
                           return false:
               return Talse;
} else if (p1 == v) {
   if (l.a == v) {
      if (pointOnLineLeft(u, l)) {
         if (pointOnLineLeft(w, l))
}
                                      && pointOnLineLeft(w, Line(u, v)))
                                      return false;
                           } else {
                                 return false;
                     && pointOnLineLeft(w, Line(u, v)))
                                      return false:
                           } else {
                                 return false;
                     return false:
                                 return false;
                           }
                     }
               }
         }
     }
     return true:
template < class T>
vector < Point < T >> convexHull(vector < Point < T >> a) {
     sort(a.begin()
          , a.end(), [](const Point<T> &l, const Point<T> &r) {
return l.x == r.x ? l.y < r.y : l.x < r.x;</pre>
     a.resize(unique(a.begin(), a.end()) - a.begin());
     if (a.size() <= 1) return a;
vector <Point <T>> h(a.size() + 1);
     int s = 0, t = 0;
for (int i = 0; i < 2; i++, s = --t) {
    for (Point<T> p : a) {
        while (t >= s + 2 && cross
                       (h[t - 1] - h[t - 2], p - h[t - 2]) \le 0) t--;
                h[t++] = p;
           reverse(a.begin(), a.end());
     return {h.begin(), h.begin() + t};
template < class T>
vector<Point<T>> hp(vector<Line<T>> lines) {
     auto d1 = l1.b - l1.a;
auto d2 = l2.b - l2.a;
           if (sgn(d1) != sgn(d2))
                return sgn(d1)
          return cross(d1, d2) > 0;
     });
     deque<Line<T>> ls;
     deque < Point < T >> ps;
for (auto l : lines) {
           if (ls.empty()) {
                ls.push_back(l);
```

10.2 Min Euclidean Distance [82650f]

```
void solve() {
     int n; cin >> n;
constexpr ll inf = 8E18;
     vector<Point<ll>> a(n);
     for (int i = 0; i < n; i++) {</pre>
          ll x, y;
cin >> x >> y;
a[i] = Point<ll>(x, y);
     struct sortY {
          bool operator
                ()(const Point<ll> &a, const Point<ll> &b) const {
                return a.y < b.y;</pre>
          }
     struct sortXY {
          bool operator
                ()(const Point<ll> &a, const Point<ll> &b) const {
return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
          }
     s,
sort(a.begin(), a.end(), sortXY());
vector<Point<ll>> t(n);
auto devide = [&](auto &&self, int l, int r) -> ll {
    if (l == r) return inf;
    int m = (l + r) / 2;
}
          ll ans = min(self(self, l, m), self(self, m + 1, r));
          ll midval = a[m].x;
          ll p = 0;
for (int i = l; i <= r; i++)
    if ((midval - a[i].x) * (midval - a[i].x) <= ans)</pre>
          if ((t[i].y
                             t[j].y) * (t[i].y - t[j].y) > ans) break;
                }
          return ans:
     cout << devide(devide, 0, n - 1) << "\n";
```

10.3 Max Euclidean Distance [5abbe1]

10.4 Lattice Points [b14b2b]

```
int main() {
      // Area 求法與 Polygun 內整數點數
     int n; cin >> n;
vector < Point < ll >> polygon(n);
      for (int i = 0; i < n; i++) cin >> polygon[i];
     ll area = 0;
for (int i = 0; i < n; i++)</pre>
            area += cross(polygon[i], polygon[(i + 1) % n]);
      area = abs(area);
     auto countBoundaryPoints
              = [](const vector<Point<ll>>& polygon) -> ll {
            ll res = 0;
            int n = polygon.size();
for (int i = 0; i < n; i++) {
    ll dx = polygon[(i + 1) % n].x - polygon[i].x;
    ll dy = polygon[(i + 1) % n].y - polygon[i].y;
    res += std::gcd(abs(dx), abs(dy));</pre>
            return res;
      il res = countBoundaryPoints(polygon);
     ll ans = (area - res + 2) / 2;
cout << ans << " " << res << "\n";
```

10.5 Min Circle Cover [02619b]

```
template < class T >
pair<T, Point<T>> minCircle(vector<Point<T>> &a) {
   random_shuffle(a.begin(), a.end());
                    }
                 }
             }
          }
      }
   return {r, c};
}
```

10.6 Min Rectangle Cover [fb3bca]

```
template < class Ta
remplate <ctass 1>
pair <T, vector <Point <T>>> minRectangle(vector <Point <T>>> a) {
   if (a.size() <= 2) return {0, {}};
   auto get = [&](const Point <T> &p, const Line <T> &l) -> T {
      return abs(cross(l.a - l.b, l.a - p).x);
}
      int n = a.size(), j = 2, l = 1, r = 1;
      a.push_back(a.front());
        th, tw, area = numeric_limits < double > :: infinity();
     ans.clear
                  (), area = th * tw / square(a[i + 1] - a[i]);
Line l1(a[i], a[i + 1]);
for (auto p : {a[r], a[j], a[l], a[i]}) {
    Line l2 = Line(p, p + rotate(l1.a - l1.b));
    if (cross(l1.a - l1.b, p - l1.a) == 0) {
        ans outh back(p);
                              ans.push_back(p);
                              l1 = Line(p, p + rotate(l1.a - l1.b));
                              Point <T > res = lineIntersection(l1, l2);
                              ans.push_back(res);
                              l1.a = res, l1.b = p;
                       }
                 }
```

```
return {area, ans};
```

11 Polynomial

11.1 FFT [9172ce]

```
const double PI = acos(-1.0);
using cd = complex<double>;
vector<int> rev;
void fft(vector<cd> &a, bool inv) {
         int n = a.size();
if (int(rev.size()) != n) {
   int k = __builtin_ctz(n) - 1;
                 rev.resize(n);

for (int i = 0; i < n; i++)

rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;
         for (int i = 0; i < n; i++)
    if (rev[i] < i)</pre>
        cd w(1):
                          for (int j = 0; j < k; j++, w = w * wn) {
                                  cd u = a[i + j];
cd v = a[i + j + k] * w;
                                  a[i + j] = u + v;
a[i + j + k] = u - v;
                         }
                 }
         if (inv) for (auto &x : a) x /= n;
template <class !>
vector <double > mulT(const vector <T > &a, const vector <T > &b) {
   vector <do > fa(a.begin(), a.end()), fb(b.begin(), b.end());
   int n = 2 << __lg(a.size() + b.size());
   fa.resize(n), fb.resize(n);
   fft(fa, false), fft(fb, false);
   for (int i = 0; i < n; i++)
        fa[i] = fa[i] * fb[i];
   fft(fa.false), fft(fb.false);
}</pre>
        fft(fa, true);
vector<double> res(n);
for (int i = 0; i < n; i++)
    res[i] = fa[i].real();</pre>
         return res; // use llround if need
```

11.2 NTT [20d911]

```
template < int V, ll P>
constexpr MInt < P> CInv = MInt < P>(V).inv();
template < ll P >
vector<MInt<P>> roots{0. 1}:
template < int P>
constexpr MInt<P> findPrimitiveRoot() {
     MInt<P> i = 2;
     int k = __builtin_ctz(P - 1);
     while (true) {
   if (power(i, (P - 1) / 2) != 1) break;
     return power(i, (P - 1) >> k);
template < ll P >
constexpr MInt<P> primitiveRoot = findPrimitiveRoot<P>();
template<>
constexpr MInt<998244353> primitiveRoot<998244353> {31};
constexpr void dft(vector<MInt<P>> &a) {
  int n = a.size();
  if (int(rev.size()) != n) {
          int k = __builtin_ctz(n) - 1;
rev.resize(n);
for (int i = 0; i < n; i++)
    rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;</pre>
     for (int i = 0; i < n; i++)
    if (rev[i] < i) swap(a[i], a[rev[i]]);
if (roots < P > . size() < n) {</pre>
          int k = __builtin_ctz(roots<P>.size());
roots<P>.resize(n);
          k++:
          }
     for (int k = 1; k < n; k *= 2) {
```

```
for (int i = 0; i < n; i += 2 * k) {</pre>
                     (Int i = 0; i < n; i += 2 ^ k) {
for (int j = 0; j < k; j++) {
   MInt<P> u = a[i + j];
   MInt<P> v = a[i + j + k] * roots<P>[k + j];
   a[i + j] = u + v;
                            a[i + j + k] = u - v;
                    }
             }
      }
}
template < ll P>
constexpr void idft(vector < MInt < P>> & a) {
   int n = a.size();
       reverse(a.begin() + 1, a.end());
      dft(a);
MInt<P> inv = (1 - P) / n;
for (int i = 0; i < n; i++) a[i] *= inv;</pre>
template < ll P = 998244353>
struct Poly : public vector<MInt<P>>> {
      using Value = MInt<P>;
Poly() : vector<Value>() {}
explicit constexpr Poly(int n) : vector<Value>(n) {}
       explicit constexpr
       Poly(const vector<Value> &a) : vector<Value>(a) {} constexpr Poly(const
                 initializer_list<Value> &a) : vector<Value>(a) {}
      template < class InputIt, class = _RequireInputIter < InputIt>>
explicit constexpr Poly(InputIt
                first, InputIt last) : vector<Value>(first, last) {}
      constexpr Poly shift(int k) const {
   if (k >= 0) {
      auto b = *this;
}
                    b.insert(b.begin(), k, 0);
                     return b;
             } else if (this->size() <= -k) {
    return Poly();</pre>
              } else {
                    return Poly(this->begin() + (-k), this->end());
       constexpr Poly trunc(int k) const {
   Poly f = *this;
   f.resize(k);
       constexor
                 friend Poly operator+(const Poly &a, const Poly &b) {
             Poly res(max(a.size(), b.size()));

for (int i = 0; i < a.size(); i++)

    res[i] += a[i];

for (int i = 0; i < b.size(); i++)

    res[i] += b[i];
              return res:
       constexpr
                 friend Poly operator-(const Poly &a, const Poly &b) {
             retend Poly Operator - (const Poly
Poly res(max(a.size(), b.size()));
for (int i = 0; i < a.size(); i++)
    res[i] += a[i];
for (int i = 0; i < b.size(); i++)
    res[i] -= b[i];</pre>
              return res:
       constexpr friend Poly operator - (const Poly &a) {
  vector < Value > res(a.size());
  for (int i = 0; i < int(res.size()); i++)</pre>
                     res[i] = -a[i];
              return Poly(res);
      constexpr friend Poly operator*(Poly a, Poly b) {
  if (a.size() == 0 || b.size() == 0)
    return Poly();
  if (a.size() < b.size()) swap(a, b);</pre>
              int n = 1, tot = a.size() + b.size() - 1;
while (n < tot) n *= 2;
if (((P - 1) & (n - 1)) != 0 || b.size() < 128) {</pre>
                     for (int i = 0; i < a.size(); i++)
    for (int j = 0; j < b.size(); j++)
        c[i + j] += a[i] * b[j];</pre>
                     return c;
              a.resize(n), b.resize(n);
              dft(a), dft(b);
for (int i = 0; i < n; ++i)
    a[i] *= b[i];</pre>
              idft(a);
              a.resize(tot):
              return a;
       constexpr friend Poly operator*(Value a, Poly b) {
   for (int i = 0; i < int(b.size()); i++)
      b[i] *= a;</pre>
```

```
constexpr friend Poly operator*(Poly a, Value b) {
   for (int i = 0; i < int(a.size()); i++)
       a[i] *= b;</pre>
constexpr friend Poly operator/(Poly a, Value b) {
  for (int i = 0; i < int(a.size()); i++)
     a[i] /= b;</pre>
constexpr Poly & operator += (Poly b) {
   return (*this) = (*this) + b;
constexpr Poly &operator -=(Poly b) {
      return (*this) = (*this) - b;
constexpr Poly &operator*=(Poly b) {
   return (*this) = (*this) * b;
constexpr Poly & operator*=(Value b) {
  return (*this) = (*this) * b;
constexpr Poly &operator/=(Value b) {
  return (*this) = (*this) / b;
constexpr Poly deriv() const {
   if (this->empty()) return Poly();
       Poly res(this->size() - 1);

for (int i = 0; i < this->size() - 1; ++i)

res[i] = (i + 1) * (*this)[i + 1];
constexpr Poly integr() const {
  Poly res(this->size() + 1);
  for (int i = 0; i < this->size(); ++i)
      res[i + 1] = (*this)[i] / (i + 1);
      res[i + 1]
       return res;
constexpr Poly inv(int m) const {
  Poly x{(*this)[0].inv()};
  int k = 1;
       while (k < m) {
    k *= 2:</pre>
              x = (x * (Poly{2} - trunc(k) * x)).trunc(k);
       return x.trunc(m);
constexpr Poly log(int m) const {
    return (deriv() * inv(m)).integr().trunc(m);
constexpr Poly exp(int m) const {
       Poly x{1};
int k = 1;
       while (k < m) {
             k *= 2;
x = (x * (Poly{1} - x.log(k) + trunc(k))).trunc(k);
       return x.trunc(m);
constexpr Poly pow(int k, int m) const {
       while (i < this->size() && (*this)[i] == 0) i++;
if (i == this->size() || 1LL * i * k >= m)
       constexpr Poly sqrt(int m) const {
      Poly x{1};
int k = 1;
while (k < m) {
   k *= 2;
              x = (x +
                        (trunc(k) * x.inv(k)).trunc(k)) * CInv<2. P>:
       return x.trunc(m);
constexpr Poly mulT(Poly b) const {
      if (b.size() == 0) return Poly();
int n = b.size();
reverse(b.begin(), b.end());
return ((*this) * b).shift(-(n - 1));
constexpr vector<Value> eval(vector<Value> x) const {
  if (this->size() == 0)
    return vector<Value>(x.size(), 0);
  const int n = max(x.size(), this->size());
  vector<Poly> q(4 * n);
       vector < Value > ans(x.size());
       x.resize(n);
function < void(</pre>
             int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
    q[p] = Poly{1, -x[l]};
}
              } else {
                     int m = (l + r) / 2;
build(2 * p, l, m);
build(2 * p + 1, m, r);
q[p] = q[2 * p] * q[2 * p + 1];
```

```
} else {
                      int m = (l + r) / 2;
                      work(2 * p, l,

m, num.mulT(q[2 * p + 1]).resize(m - l));

work(2 * p + 1,
                              m, r, num.mulT(q[2 * p]).resize(r - m));
                }
           work(1, 0, n, mulT(q[1].inv(n)));
           return ans;
};
template < ll P = 998244353>
Poly<P> berlekampMassey(const Poly<P> &s) {
     Poly<P> c, oldC;
int f = -1;
     for (int i = 0; i < s.size(); i++) {</pre>
           (int i = 0; i < s.size(); i++) {
auto delta = s[i];
for (int j = 1; j <= c.size(); j++)
    delta -= c[j - 1] * s[i - j];
if (delta == 0) continue;
if (f == -1) {
    c.resize(i + 1);
    f = i.</pre>
           f = i;
} else {
                auto d = oldC;
                d *= -1;
d.insert(d.begin(), 1);
                auto coef = delta / df1;
                 d *= coef;
                Poly<P> zeros(i - f - 1);
                 zeros.insert(zeros.end(), d.begin(), d.end());
                d = zeros;
                auto temp = c;
c += d;
if (i - temp.size() > f - oldC.size()) {
    oldC = temp;
                      f = i;
                }
          }
     c *= -1;
     c.insert(c.begin(), 1);
     return c;
template < ll P = 998244353>
MInt<P> linearRecurrence(Poly<P> p, Poly<P> q, ll n) {
     int m = q.size() - 1;
     while (n > 0) {
    auto newq = q;
    for (int i = 1; i <= m; i += 2)
        newq[i] *= -1;
    auto newp = p * newq;
    newq = q * newq;
    for (int i = 1; i <= m; i += 2)</pre>
           for (int i = 0; i < m; i++)
    p[i] = newp[i * 2 + n % 2];
for (int i = 0; i <= m; i++)</pre>
                q[i] = newq[i * 2];
           n /= 2:
     return p[0] / q[0];
12 Else
```

12.1 Python [6f660a]

```
from decimal import * # 無誤差浮點數
from fractions import * # 分數
from random import *
from math import *
# set decimal prec if it could overflow in precision
setcontext(Context(prec=10, rounding=ROUND_FLOOR))
# read and print
x = int(input())
a, b, c = list(map(Fraction, input().split()))
arr = list(map(Decimal, input().split()))
print(x)
print(a, b, c)
print(*arr)
# set
S = set(); S.add((a, b)); S.remove((a, b))
if not (a, b) in S:
# dict
D = dict(); D[(a, b)] = 1; del D[(a, b)]
for (a, b) in D.items():
# random
```

```
arr = [randint(l, r) for i in range(size)]
choice([8, 6, 4, 1]) # random pick one
shuffle(arr)
```

12.2 Fraction [3f8970]

```
template < class T>
 struct Fraction {
      T n, d; void reduce() {
            T g = gcd(abs(n), abs(d));
n /= g, d /= g;
if (d < 0) n = -n, d = -d;
       Fraction(T n_ = 0, T d_ = 1) : n(n_), d(d_) {
    assert(d != 0);
            reduce();
       Fraction(const string &str) {
            istringstream ss(str);
            char slash;
            if (str.find('/') != -1) {
    ss >> n >> slash >> d;
                 ss >> n;
                 d = 1;
            Fraction(n, d);
       Fraction operator+=(Fraction rhs) & {
            n = n * rhs.d + rhs.n * d;
d *= rhs.d:
            reduce();
return *this;
       Fraction operator -= (Fraction rhs) & {
    n = n * rhs.d - rhs.n * d;
    d *= rhs.d;
            reduce();
return *this;
       Fraction operator*=(Fraction rhs) & {
            n *= rhs.n;
d *= rhs.d;
            reduce();
return *this;
       Fraction operator/=(Fraction rhs) & {
            assert(rhs.n != 0);
            n *= rhs.d;
d *= rhs.n;
            reduce();
return *this;
       friend Fraction operator+(Fraction lhs, Fraction rhs) {
   return lhs += rhs;
       friend Fraction operator - (Fraction lhs, Fraction rhs) {
            return lhs -= rhs;
       friend Fraction operator*(Fraction lhs, Fraction rhs) {
   return lhs *= rhs;
       friend Fraction operator/(Fraction lhs, Fraction rhs) {
   return lhs /= rhs;
       friend istream &operator>>(istream &is, Fraction &f) {
            string s;
            is >> s;
f = Fraction(s);
            return is;
              ostream & operator << (ostream &os, const Fraction &f) {
            if (f.d == 1) {
                  os << f.n;
            } else {
                 os << f.n << "/" << f.d;
            return os;
       friend bool operator == (Fraction lhs, Fraction rhs) {
  return lhs.n * rhs.d == rhs.n * lhs.d;
       friend bool operator!=(Fraction lhs, Fraction rhs) {
  return lhs.n * rhs.d != rhs.n * lhs.d;
       friend bool operator <(Fraction lhs, Fraction rhs) {
   return lhs.n * rhs.d < rhs.n * lhs.d;</pre>
};
```