Contents 6 Math 6.1 Modulo **6.2** Combination 11 1 Basic 6.3 Miller Rabin Pollard Rho . 11 1.1 Compare Fuction 1.2 Pbds 1.3 Double 1.4 Int128 1.5 Rng 6.11 Dynamic Modulo 13 6.12 Integer Partition 13 6.13 Mobius Theorem 13 2 Graph **2.1 DFS And BFS** 1 2.2 Prim **6.14 Mobius Inverse** 14 2.3 Bellman-Ford 6.15 Catalan Theorem 2.4 Floyd-Warshall 6.16 Burnside's Lemma 14 2.5 Euler Search and Gready 2.6 DSU 7.1 Binary Search 14 2.7 SCC 2.8 VBCC Тгее 8.1 Binary Lifting LCA. 2.9 EBCC 8.2 Centroid Decomposition . 14 8.3 Heavy Light Decomposition 15 2.10 2-SAT 2.11 Functional Graph Link Cut Tree Virtual Tree 8.4 3 Data Structure 8.6 Dominator Tree 16 3.1 Segment Tree 9 DP 3.2 Fenwick 3.3 Range Fenwick 3.4 Persistent Segment Tree . 6 3.5 Treap **9.4 Bitmask** 17 **9.5 Projects** 18 **3.6 RMQ** 7 **Proiects** 18 Removal Game 18 3.7 Mo 9.7 Monotonic Queue 4 Flow Matching 4.1 Dinic **4.2** Min Cut 7 9.12 Codeforces Example . . . 19 4.3 MCMF 4.4 Hungarian 10 Geometry **4.5** Theorem 8 10.1 Basic . . 10.2 Min Euclidean Distance . . 10.3 Max Euclidean Distance . . 21 5 String **10.4 Lattice Points** 22 5.1 Hash 10.5 Min Circle Cover 5.2 KMP 10.6 Min Rectangle Cover . . . 22 5.3 Z Function 5.4 Manacher 11 Polvnomial 5.5 Trie 5.6 SA 5.7 SAM **5.8 Palindrome Tree** 10 **5.9 Duval** 10

1 Basic

1.1 Compare Fuction [d41d8c]

```
// 1. sort, 二分搜刻在函式內 lambda 就好
// 2. priority queue 小到大是 >, set 是 <
// 3. set 不能 = , multiset 必須 =
// 4. 確保每個成員都要比到
// 5. pbds_multiset 不要用 lower_bound
// 6. 如果要用 find, 插入 inf 後使用 upper_bound
// 7. multiset 可以跟 set 一樣使用, 但請注意第 3、4 點
auto cmp = [](int i, int j) { return i > j; };
priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);

vector<int> a {1, 2, 5, 4, 3}; // 小心不要改到 a
auto cmp = [&a](int i, int j) { return a[i] > a[j]; };
priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
```

1.2 Pbds [d41d8c]

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template <class T>
using pbds_set = tree <T, null_type,
    less <T>, rb_tree_tag, tree_order_statistics_node_update>;
template <class T>
using pbds_multiset = tree <T, null_type, less_equal
    <T>, rb_tree_tag, tree_order_statistics_node_update>;
```

1.3 Double [93fa38]

```
struct D {
    double x;
    D(double x = 0.0) : x{x} {};
    constexpr static double eps = 1E-12;
    explicit operator double() const { return x; }
```

```
D operator -() const {
    return D(-x);
D & operator += (D rhs) & {
    x += rhs.x; return *this;
D &operator -= (D rhs) & {
    x -= rhs.x; return *this;
D & operator *= (D rhs) & {
    x *= rhs.x; return *this;
D &operator/=(D rhs) & {
   assert(fabs(rhs.x) > eps);
   x /= rhs.x; return *this;
friend D operator+(D lhs, D rhs) {
    return lhs += rhs;
friend D operator - (D lhs, D rhs) {
    return lhs -= rhs;
friend D operator*(D lhs, D rhs) {
    return lhs *= rhs;
friend D operator/(D lhs, D rhs) {
    return lhs /= rhs;
friend istream &operator>>(istream &is, D &a) {
    double v; is >> v; a = D(v); return is;
friend ostream &operator<<(ostream &os, const D &a) {
  friend bool operator<(D lhs, D rhs) {</pre>
    return lhs.x - rhs.x < -eps;</pre>
friend bool operator>(D lhs, D rhs) {
    return lhs.x - rhs.x > eps;
friend bool operator==(D lhs, D rhs) {
    return fabs(lhs.x - rhs.x) < eps;</pre>
```

1.4 Int128 [85923a]

```
using i128 = __int128_t; // 1.7E38
istream & operator >> (istream & is, i128 & a) {
    i128 sgn = 1; a = 0;
    string s; is >> s;
    for (auto c : s) {
        if (c == '-') {
            sgn = -1;
        } else {
            a = a * 10 + c - '0';
        }
    }
    a *= sgn;
    return is;
}
ostream & operator << (ostream & os, i128 a) {
    string res;
    if (a < 0) os << '-', a = -a;
    while (a) {
        res.push_back(a % 10 + '0');
        a /= 10;
    }
    reverse(res.begin(), res.end());
    os << res;
    return os;
}</pre>
```

1.5 Rng [401544]

```
mt19937_64 rng
          (chrono::steady_clock::now().time_since_epoch().count());
ll x = rng();
shuffle(a.begin(), a.end(), rng);
```

2 Graph

2.1 **DFS And BFS** [1f02d8]

```
void dfsBfs() {
    int n;
    vector<vector<int>> adj(n);
    // dfs_graph
    vector<bool> vis(n);
    auto dfs = [&](auto self, int u) -> void {
        if (vis[u]) return;
        vis[u] = true;
        for (auto v: adj[u]) {
            self(self, v);
        }
    };
    dfs(dfs, 0);
    // bfs
    vector<int> dep(n, -1);
    auto bfs = [&](auto self, int s) -> void {
```

2.2 Prim [7e2d87]

2.3 Bellman-Ford [430de2]

```
用 Bellman Ford 找負環
void bellmanFord() {
     int n, m; cin >> n >> m;
     vector < array < int, 3 >> e;
for (int i = 0; i < m; i++) {</pre>
          int u, v, w; cin >> u >> v >> w;
u--, v--; e.push_back({u, v, w});
    if (i == n) t = v;
               }
          }
     if (t == -1) { cout << "NO\n"; return;
for (int i = 1; i < n; i++) t = par[t];
vector <int> ans {t};
     int i = t;
     do {
    i = par[i];
           ans.push_back(i);
     } while (i != t);
reverse(ans.begin(), ans.end());
                "YES\n"
     for (auto x : ans) cout << x + 1 << " ";</pre>
```

2.4 Floyd-Warshall [2f66b9]

};

2.5 Euler [4177dc]

```
// 1. 無向圖是歐拉圖:
// 非零度頂點是連通的
// 頂點的度數都是偶數
| // 2. 無向圖是半歐拉圖(有路沒有環):
// 非零度頂點是連通的
// 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
// 非零度頂點是強連通的
// 每個頂點的入度和出度相等
// 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
// 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
// 其他頂點的入度和出度相等
vector < int > ans;
auto dfs = [&](auto &&self, int u) -> void {
    while (g[u].size()) {
        int v = *g[u].begin();
}
           g[u].erase(v);
           self(self, v);
      ans.push_back(u);
 dfs(dfs, 0);
reverse(ans.begin(), ans.end());
 2.6 DSU [b7ac4a]
 struct DSU {
      vector < int > boss, siz;
DSU(int n_ = 0) { init(n_); }
void init(int n_) {
           n = n_; boss.resize(n);
           iota(boss.begin(), boss.end(), \theta);
           siz.assign(n, 1);
      int find(int x) {
   if (boss[x] == x) return x;
           return boss[x] = find(boss[x]);
      bool same(int x, int y) {
    return find(x) == find(y);
      bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);
    siz[x] += siz[y];
    if (siz[x] += siz[y];</pre>
           boss[y] = x;
           return true;
      int size(int x) {
           return siz[find(x)];
     }
 struct DSU {
      int n;
      vector < int > boss, siz, stk;
DSU(int n_ = 0) { init(n_); }
void init(int n_) {
           boss.resize(n);
           iota(boss.begin(), boss.end(), \theta);
           siz.assign(n, 1);
           stk.clear();
      int find(int x) {
           return x == boss[x] ? x : find(boss[x]);
      bool same(int x, int y) {
    return find(x) == find(y);
      bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);
    siz[x] += siz[y];</pre>
           boss[y] = x;
           stk.push_back(y);
      stk.pop_back();
                siz[boss[y]] -= siz[y];
                boss[y] = y;
          }
      int size(int x) {
    return siz[find(x)];
```

2.7 SCC [26d711]

```
struct SCC {
       int n, cur, cnt;
vector<vector<int>> adj;
       vector <int> stk, dfn, low, bel;
SCC(int n_ = 0) { init(n_); }
void init(int n_) {
              n = n_;
              adj.assign(n, {});
dfn.assign(n, -1), low.resize(n);
bel.assign(n, -1), stk.clear();
       void addEdge(int u, int v) {
   adj[u].push_back(v);
       void dfs(int x) {
    dfn[x] = low[x] = cur++;
              stk.push_back(x);
              for (auto y : adj[x]) {
    if (dfn[y] == -1) {
                            dfs(y);
                    low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
                     }
              if (dfn[x] == low[x]) {
                     int y;
do {
                           y = stk.back();
                    bel[y] = cnt;
stk.pop_back();
while (y != x);
                     cnt++;
             }
       fvector < int > work() {
    for (int i = 0; i < n; i++)
        if (dfn[i] == -1) dfs(i);
    return bel;</pre>
       struct Graph {
              int n;
              vector<pair<int, int>> edges;
              vector<int> siz, cnte;
       Graph compress() {
             Graph g;
g.n = cnt;
              g.siz.resize(cnt);
              g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;</pre>
                     for (auto j : adj[i]) {
    if (bel[i] != bel[j]) {
                                  g.edges.emplace_back(bel[i], bel[j]);
                            } else {
                                  g.cnte[bel[i]]++;
                    }
              return g;
};
```

2.8 VBCC [2d1f9d]

```
struct VBCC {
        int n, cur, cnt;
       vector < int >> adj, bcc;
       vector <int>> adj, bcc;
vector <int> stk, dfn, low;
vector <bool> ap;
VBCC(int n_ = 0) { init(n_); }
void init(int n_) {
              1 int((int n_);
n = n_;
adj.assign(n, {});
dfn.assign(n, -1), low.resize(n);
bcc.assign(n, {}), ap.assign(n, false);
                stk.clear();
                cur = cnt = 0;
       void addEdge(int u, int v) {
   adj[u].push_back(v);
                adj[v].push_back(u);
       void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
    stk.push_back(x);
    int child = 0;
               for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
                               dfs(y, x), child++;
low[x] = min(low[x], low[y]);
if (low[y] >= dfn[x]) {
                                        int v;
                                       do {
                                               v = stk.back():
                                               bcc[v].push_back(cnt);
                                               stk.pop_back();
```

```
} while (v != y);
bcc[x].push_back(cnt);
                             cnt++;
                       if (low[y] >= dfn[x] && p != -1)
                 ap[x] = true;
} else {
                       low[x] = min(low[x], dfn[y]);
           if (p == -1 && child > 1)
                 ap[x] = true;
     fvector < bool > work() {
    for (int i = 0; i < n; i++)
        if (dfn[i] == -1) dfs(i, -1);</pre>
           return ap;
      struct Graph {
           int n;
vector<pair<int, int>> edges;
vector<int> bel, siz, cnte;
      Graph compress() {
    Graph g; // 壓完是一棵樹,但不一定每個 bel 都有節點 g.bel.resize(n);
           g.siz.resize(cnt);
            g.cnte.resize(cnt);
            for (int u = 0; u < n; u++) {
   if (ap[u]) {
      g.bel[u] = cnt++;
}</pre>
                       g.siz.emplace_back();
g.cnte.emplace_back();
for (auto v : bcc[u]) {
                            g.edges.emplace_back(g.bel[u], v);
                 } else if (bcc[u].size() == 1) {
                      g.bel[u] = bcc[u][0];
                 g.siz[g.bel[u]]++;
          }
g.n = cnt;
for (int i = 0; i < n; i++)
    for (auto j : adj[i])
        if (g.bel[i] == g.bel[j] && i < j)
            g.cnte[g.bel[i]]++;</pre>
     }
};
2.9 EBCC [9d70fc]
struct EBCC { // CF/contest/1986/pF
     int n, cur, cnt;
vector<vector<int>> adj;
      vector<int> stk, dfn, low, bel;
      vector<pair<int, int>> bridges; // 關鍵邊 EBCC(int n_= 0) { init(n_-); }
      void init(int n_) {
           n = n_;
adj.assign(n, {});
           dfn.assign(n, -1), low.resize(n);
bel.assign(n, -1), stk.clear();
bridges.clear();
           cur = cnt = 0;
      void addEdge(int u, int v) {
           adj[u].push_back(v);
           adj[v].push_back(u);
     bridges.emplace_back(x, y);
                 } else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
```

if (dfn[x] == low[x]) {

} while (y != x);

y = stk.back(); bel[y] = cnt; stk.pop_back();

vector<int> work() { // not connected
 for (int i = 0; i < n; i++)
 if (dfn[i] == -1) dfs(i, -1);</pre>

int y;
do {

cnt++:

return bel;

struct Graph {

int n;

2.10 2-SAT [28688f]

```
struct TwoSat {
     int n; vector<vector<int>> e;
vector<bool>
     vector < bool > ans;
TwoSat(int n) : n(n), e(2 * n), ans(n) {}
void addClause(int u, bool f, int v, bool g) {
    e[2 * u + !f].push_back(2 * v + g);
    e[2 * v + !g].push_back(2 * u + f);
      void ifThen(int u, bool f, int v, bool g) {
           // 必取 A: not A -> A
e[2 * u + !f].push_back(2 * v + g);
      bool satisfiable() {
           vector<int> stk;
            int now = 0, cnt = 0;
function < void(int) > tarjan = [&](int u) {
                 stk.push_back(u);
dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
                             tarjan(v);
                       low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in stk
low[u] = min(low[u], dfn[v]);
                       }
                  if (dfn[u] == low[u]) {
                       int v;
do {
                             v = stk.back();
                       stk.pop_back();
id[v] = cnt;
} while (v != u);
                       ++cnt;
                 }
            for (int i
           return true;
      vector < bool > answer() { return ans; }
};
```

2.11 Functional Graph [e8fd64]

```
void label(int u) {
    vector <int> p; int cur = u;
    while (top[cur] == -1) {
        top[cur] = u;
        p.push_back(cur);
        cur = g[cur];
    }
    auto s = find(p.begin(), p.end(), cur);
    vector <int> cyc(s, p.end());
    p.erase(s, p.end()); p.push_back(cur);
    for (int i = 0; i < (int)cyc.size(); i++) {
        bel[cyc[i]] = ir;
        id[cyc[i]] = ir;
    }
    if (!cyc.empty())
        ++cnt, len.push_back(cyc.size());
    for (int i = p.size() - 1; i > 0; i--)
        id[p[i - 1]] = id[p[i]] - 1;
}
int jump(int u, int k) {
    for (int b = 0; k > 0; b++) {
        if (k & 1) u = cht[u][b];
        k >>= 1;
    }
    return u;
};
```

3 Data Structure

3.1 Segment Tree [d41d8c]

```
template < class Info, class Tag = bool()>
struct SegmentTree { // [l, r), uncomment /**/ to lazy
      vector < Info > info;
      vector<Tag> tag;
     SegmentTree(): n(0) {}
SegmentTree(int n_, Info v_ = Info()) {
           init(n_, v_);
      template < class T>
      SegmentTree(vector<T> init_) {
            init(init_);
     void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
      }
      template < class T>
      void init(vector<T> init_) {
           n = init_.size();
info.assign(4 << __lg(n), Info());</pre>
            tag.assign(4 << __lg(n), Tag());
                  int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
                        info[p] = init_[l];
                  int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                 pull(p);
           build(1, 0, n);
      void pull(int p) {
            info[p] = info[p * 2] + info[p * 2 + 1];
      void apply(int p, int l, int r, const Tag &v) {
    info[p].apply(l, r, v);
            tag[p].apply(v);
     f
void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
            tag[p] = Tag();
      void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
}
                  return;
            int m = (l + r) / 2;
            push(p, l, r);
           if (x < m) {
    modify(2 * p, l, m, x, v);</pre>
           } else {
```

```
modify(2 * p + 1, m, r, x, v);
           pull(p);
      void modify(int p, const Info &i) {
           modify(1, 0, n, p, i);
     Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    int m = (l + r) / 2;</pre>
            ,
push(p, l, г);
            return query(p *
                2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
      ,
void rangeApply
            (int p, int l, int r, int ql, int qr, const Tag &v) {
if (qr <= l || ql >= r) return;
if (ql <= l && r <= qr) {
                 apply(p, l, r, v);
                 return;
           f
int m = (l + r) / 2;
push(p, l, r);
rangeApply(p * 2, l, m, ql, qr, v);
rangeApply(p * 2 + 1, m, r, ql, qr, v);
            pull(p);
      void rangeApply(int l, int r, const Tag &v) {
           rangeApply(1, 0, n, l, r, v);
      template < class F> // 尋找區間內,第一個符合條件的
      int findFirst
           (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) return -1;
if (l >= x && r <= y && !pred(info[p])) return -1;
if (r - l == 1) return l;</pre>
            int m = (l + r) / 2;
            push(p, l, r);
           int res = findFirst(2 * p, l, m, x, y, pred);
           if (res == -1)
    res = findFirst(2 * p + 1, m, r, x, y, pred);
            return res:
     template < class F> // 若要找 last , 先右子樹遞迴即可int findFirst(int l, int r, F & pred) {
           return findFirst(1, 0, n, l, r, pred);
// 有些 Tag 不用 push 例如 sweepLine
/*
struct Tag {
     bool set_val = false;
int add = 0;
      void apply(const Tag& t) & {
           if (t.set_val) {
    set_val = t.set_val;
    add = t.add;
           else {
                 add += t.add;
     }
};
*/
struct Info {
    ll sum = 0;
    /*
      void apply(int l, int r, const Tag &t) & {
    if (t.set_val) {
        sum = (r - l) * t.set_val;
           sum += (r - l) * t.add;
     // 部分 assignment 使用
     // Info &operator=(const Info &rhs) & {
              return *this;
      Info &operator=(const ll &rhs) & {
           sum = rhs;
return *this;
Info operator+(const Info &a, const Info &b) {
     Info c;
     c.n = a.n + b.n;
     c.sum = a.sum + b.sum;
     return c:
```

```
template < class T>
 struct Fenwick { // 全部以 0 based 使用int n; vector<T> a; Fenwick(int n_ = 0) {
              init(n_);
        void init(int n_) {
              a.assign(n, T{});
        void add(int x, const T &v) {
   for (int i = x + 1; i <= n; i += i & -i)
        a[i - 1] = a[i - 1] + v;</pre>
        T sum(int x) { // 左閉右開查詢
              T ans{);
for (int i = x; i > 0; i -= i & -i)
    ans = ans + a[i - 1];
              return ans:
        T rangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
        int select(const T &k, int start = 0) {
              int x = 0; T cur = -sum(start) > k

int x = 0; T cur = -sum(start);

for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n && cur + a[x + i - 1] <= k) {
        x += i;
                            cur = cur + a[x - 1];
                     }
       }
 template < class T>
 struct TwoDFenwick { // 全部以 0 based 使用
        int nx, ny; // row, col 個數 vector<vector<T>> a;
        TwoDFenwick(int nx_ = 0, int ny_ = 0) {
              init(nx_, ny_);
        void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
        void add(int x, int y, const T &v) {
    for (int i = x + 1; i <= nx; i += i & -i)
        for (int j = y + 1; j <= ny; j += j & -j)
        a[i - 1][j - 1] = a[i - 1][j - 1] + v;</pre>
        T sum(int x, int y) { // 左閉右開查詢
              Im(int x, s...)
I ans{};
for (int i = x; i > 0; i -= i & -i)
    for (int j = y; j > 0; j -= j & -j)
        ans = ans + a[i - 1][j - 1];
        T rangeSum
                (int lx, int ly, int rx, int ry) { // 左閉右開查詢
               return sum(
                      (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
};
```

3.3 Range Fenwick [d41d8c]

```
template < class T >
struct RangeFenwick { // 全部以 0 based 使用
    int n;
    vector <T > d, di;
    RangeFenwick(int n_ = 0) {
        init(n_);
    }
    void init(int n_) {
        n = n_;
        d.assign(n, T{});
        di.assign(n, T{});
    }
    void add(int x, const T &v) {
        T vi = v * (x + 1);
        for (int i = x + 1; i <= n; i += i & -i) {
            d[i - 1] = d[i - 1] + v;
            di[i - 1] = di[i - 1] + v;
            di[i - 1] = di[i - 1] + v;
            di[i - 1] = di[i - 1] + vi;
        }
    }
    void rangeAdd(int l, int r, const T &v) {
        add(l, v); add(r, -v);
    }
    T sum(int x) { // 左閉右開查詢
        T ans{};
        for (int i = x; i > 0; i -= i & -i) {
            ans = ans + T(x + 1) * d[i - 1];
            ans = ans - di[i - 1];
        }
        return ans;
}
T rangeSum(int l, int r) { // 左閉右開查詢
        return sum(r) - sum(l);
```

3.2 Fenwick [d41d8c]

```
int select(const T &k, int start = 0) {
                              x + i + 1) * d[x + i - 1] - di[x + i - 1];

if (cur + val <= k) {

x += i;
                                                                           cur = cur + val;
                                            }
                               return x;
              }
template < class T>
struct rangeTwoDFenwick { // 全部以 0 based 使用
              int nx, ny; // row, col 個數
vector <vector <T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
                              init(nx_, ny_);
              food init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
                               dij.assign(nx, vector<T>(ny, T{}));
                void add(int x, int y, const T &v) {
   T vi = v * (x + 1);
   T vj = v * (y + 1);
                               T vij = v * (x + 1) * (y + 1);
                              for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        d[i - 1][j - 1] = d[i - 1][j - 1] + v;
        di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
        dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
        dij[i - 1][j - 1] = dij[i - 1][j - 1] + vj;
        dij[i - 1][j - 1] = dij[i - 1][j - 1] + vij;
}</pre>
                                            }
                             }
                void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
                             add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
              T sum(int x, int y) { // 左閉右開查詢
                               T ans{};
                               for (int i = x; i > 0; i -= i & -i) {
                                              for (int j = y; j > 0; j -= j & -j) {
                                                            ans = ans
+ T(x *
                                                           }
                              return ans:
                                (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                                               rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
};
```

3.4 Persistent Segment Tree [d41d8c]

```
template < class Info > struct PST {
    struct Node {
        Info info = Info();
        int lc = 0, rc = 0;
    };
    int n = 0;
    vector < Node > nd;
    vector < Info > nd;
    pST() : n(0) {}
    pST(int n_, Info v_ = Info()) {
        init(n_, v_);
    }

    template < class T >
    PST(vector < T > init_) {
        init(init_);
    }

    void init(int n_, Info v_ = Info()) {
        init(vector < Info > (n_, v_));
    }

    template < class T >
    void init(vector < T > init_) {
        n = init_.size();
        nd.elear(); rt.clear();
        nd.emplace_back(); // 讓 root 指向 1-based rt.push_back(build(0, n, init_));
}
```

```
int build(int l, int r, vector<Info> &init_) {
   int id = nd.size();
            nd.emplace_back();
            if (r - l == 1) {
    nd[id].info = init_[l];
                   return id;
            nd[id].lc = build(l, m, init_);
nd[id].rc = build(m, r, init_);
pull(nd[id]);
             return id:
      void pull(Node &t) {
             t.info = nd[t.lc].info + nd[t.rc].info;
      int copy(int t) { // copy 一個 node
  nd.push_back(nd[t]);
             return nd.size() - 1;
      int generate() { // 創立新的 node
    nd.emplace_back();
             return nd.size() - 1;
      int modify(int t, int l, int r, int x, const Info &v) {
   t = t ? copy(t) : generate();
   if (r - l == 1) {
                   nd[t].info = v;
            int m = (l + r) >> 1;
if (x < m) {
                   nd[t].lc = modify(nd[t].lc, l, m, x, v);
            } else {
                  nd[t].rc = modify(nd[t].rc, m, r, x, v);
            pull(nd[t]);
            return t;
      void modify(int ver, int pos, const Info &val) {
   if (int(rt.size()) <= ver) rt.resize(ver + 1
   rt[ver] = modify(rt[ver], 0, n, pos, val);</pre>
      Info query(int t, int l, int r, int ql, int qr) {
    if (l >= qr || r <= ql) return Info();
    if (ql <= l && r <= qr) return nd[t].info;
    int m = (l + r) >> 1;
             return query(nd[t].
                    lc, l, m, ql, qr) + query(nd[t].rc, m, r, ql, qr);
      Info query(int ver, int ql, int qr) {
    return query(rt[ver], 0, n, ql, qr);
      void createVersion(int ori_ver) {
    rt.push_back(copy(rt[ori_ver]));
      void reserve(int n, int q) {
   nd.reserve(n + q * (2 * __lg(n) + 1));
   rt.reserve(q + 1);
      void resize(int n) {
            rt.resize(n);
struct Info {
Info operator+(const Info &a, const Info &b) {
      return { a.sum + b.sum };
3.5 Treap [d41d8c]
struct Treap {
      Treap *lc, *rc;
int pri, siz; bool rev_valid;
int val; int min;
      Treap(int val_) {
   min = val = val_;
            pri = rand();
lc = rc = nullptr;
siz = 1; rev_valid = 0;
      void pull() { // update siz or other information
            siz = 1;
min = val;
             for (auto c : {lc, rc}) {
    if (!c) continue;
    siz += c->siz;
                   min = std::min(min, c->min);
            }
      void push() {
            if (rev_valid) {
    swap(lc, rc);
    if (lc) lc->rev_valid ^= 1;
    if (rc) rc->rev_valid ^= 1;
             rev valid = false;
```

int find(int k) { // 找到 min 是 k 的位置 (1-based)

push();

```
int ls = (lc ? lc->siz : 0) + 1;
              if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
int size(Treap *t) {
    return t ? t->siz : 0;
freap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
    a->push(); b->push();
    if (a->pri > b->pri) {
        a -> c = merge(a->rc, b);
        a -> c = merge(a->rc, b);
    }
}
               a->pull();
       else {
              b->lc = merge(a, b->lc);
b->pull();
              return b:
pair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
       t->push();
       if (size(t->lc) < k) {
   auto [a, b] = split(t->rc, k - size(t->lc) - 1);
   t->rc = a;
               t->pull();
               return {t, b};
              auto [a, b] = split(t->lc, k);
t->lc = b;
               t->pull();
              return {a, t};
      }
void Print(Treap *t) {
       if (!t) return;
       t->push();
       Print(t->lc);
       cout << t->val;
Print(t->rc);
3.6 RMQ [d41d8c]
```

```
template < class T, class F = less < T >>
struct RMQ {
      int n;
       F cmp = F();
vector<vector<T>> g;
       RMQ() {}
RMQ(const vector<T> &a, F cmp = F()) : cmp(cmp) {
   init(a);
       void init(const vector<T> &a) {
             int(const vector() &a) {
    n = a.size();
    int lg = __lg(n);
    g.resize(lg + 1);
    g[0] = a;
    for (int j = 1; j <= lg; j++) {</pre>
                     for (int i = 0; i <= n - (1 << j) + 1);
for (int i = 0; i <= n - (1 << j); i++)
    g[j][i] = min(g[j -</pre>
                                     1][i], g[j - 1][i + (1 << (j - 1))], cmp);
              }
       Joperator()(int l, int r) {
   assert(0 <= l && l < r && r <= n);
   int lg = __lg(r - l);</pre>
              return min(g[lg][l], g[lg][r - (1 << lg)], cmp);</pre>
}:
```

3.7 Mo [d41d8c]

```
struct Query {
       int l, r, id;
void Mo(vector<Query> &q) {
   int blk = sqrt(q.size());
       sort(q.begin
              (), q.end(), [&](const Query &a, const Query &b) {
int x = a.l / blk, y = b.l / blk;
return x == y ? a.r < b.r : x < y;
```

4 Flow Matching

4.1 Dinic [d41d8c]

```
template < class T>
struct Dinic {
   struct _Edge {
   int to;
        T f, cap; // 流量跟容量
```

```
int n, m, s, t;
const T INF_FlOW = 1LL << 60;
vector < vector < int >> g;
        vector<_Edge> e;
       vector <_Ltdge> e;
vector <int> h, cur;
Dinic(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_; m = 0;
    h.resize(n); cur.resize(n);
    g.assign(n, {});
    c.loar();
              e.clear():
       void add_edge(int u, int v, T cap) {
    e.push_back({v, 0, cap});
    e.push_back({u, 0, 0});
              g[u].push_back(m++);
g[v].push_back(m++);
        bool bfs() {
              fill(h.begin(), h.end(), -1);
h[s] = 0; queue<int> q;
               q.push(s);
              q.push(v);
                             }
                     }
               return false;
        T dfs(int u, T flow) {
              if (flow == 0) return 0;
if (u == t) return flow;
for (int &i = cur[u]; i < g[u].size(); i++) {</pre>
                      T mn = dfs(v, min(flow, cap - f));
if (mn > 0) {
    e[j].f += mn;
    e[j ^ 1].f -= mn;
                             return mn;
                     }
               return 0:
        T work(int s_, int t_) {
    s = s_; t = t_; T f = 0;
    while (bfs()) {
        fill(cur.begin(), cur.end(), 0);
}
                      while (true) {
   T res = dfs(s, INF_FlOW);
   if (res == 0) break;
                     }
               return f;
       void reset() {
    for (int i = 0; i < m; i++) e[i].f = 0;</pre>
        void reuse(int n_) { // 走殘留網路, res += f while (n < n_) {
                     g.emplace_back();
h.emplace_back();
                      cur.emplace_back();
                      n += 1;
              }
};
```

4.2 Min Cut [d41d8c]

```
void minCut() {
       int n, m; cin >> n >> m;
Dinic < int >> g(n);
for (int i = 0; i < m; i++) {
    int u, v, cap = 1;
    cin >> u >> v;
              g.add_edge(u, v, cap);
              g.add_edge(v, u, cap);
       int res = g.work(0, n - 1);
cout << res << "\n";
if (res == 0) return;</pre>
       vector<int> vis(n);
auto find = [&](auto self, int u) -> void {
   if (!vis[u]) {
                       vis[u] = 1;
                       for (int id : g.adj[u])
                              auto e = g.edges[id];
if (e.cap - e.flow > 0) {
```

```
self(self. e.to):
                         }
                }
         find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    if (!vis[i]) continue;</pre>
                  for (int id : g.adj[i]) {
    if (id & 1) continue;
                          auto e = g.edges[id];
if (!vis[e.to]) {
    cout << i + 1 << " " << e.to + 1 << " | n";</pre>
                 }
       }
}
```

```
4.3 MCMF [d41d8c]
 template < class Tf, class Tc>
 struct MCMF {
       struct _Edge {
   int to;
              Tf f, cap; // 流量跟容量
              Tc cost;
       int n, m, s, t;
const Tf INF_FLOW = 1 << 30;
const Tc INF_COST = 1 << 30;</pre>
        vector<_Edge> e;
        vector < vector < int >> g;
       vector < vector < Int>> g;
vector < Tc> dis;
vector < int> rt, inq;
MCMF(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_; m = 0;
    e.clear();
}
              g.assign(n, {});
        void addEdge(int u, int v, Tf cap, Tc cost) {
              e.push_back({v, 0, cap, cost});
e.push_back({u, 0, 0, -cost});
               g[u].push_back(m++);
               g[v].push_back(m++);
       bool spfa() {
              dis.assign(n, INF_COST);
rt.assign(n, -1), inq.assign(n, 0);
queue<int> q; q.push(s);
               dis[s] = 0;
              while (!q.empty()) {
   int u = q.front(); q.pop();
   inq[u] = 0;
                     dis[v] = ndis, rt[v] = id;
if (!inq[v])
                                         q.push(v), inq[v] = 1;
                            }
                    }
              return dis[t] != INF_COST;
       // 限定 flow, 最小化 cost
pair<Tf, Tc> workFlow(int s_, int t_, Tf need) {
    s = s_, t = t_;
    Tf flow{}; Tc cost{};
}
              while (spfa()) {
    Tf f = need;
                     for (int i = t; i != s; i = e[rt[i] ^ 1].to)
    f = min(f, e[rt[i]].cap - e[rt[i]].f);
for (int i = t; i != s; i = e[rt[i] ^ 1].to)
                     e[rt[i]].f += f, e[rt[i] ^ 1].f -= f;
flow += f, need -= f;
cost += f * dis[t];
                     if (need == 0) break;
              return {flow, cost};
        // 限定 cost, 最大化 flow
       If f = budget / dis[t];
for (int i = t; i != s; i = e[rt[i] ^ 1].to)
    f = min(f, e[rt[i]].cap - e[rt[i]].f);
for (int i = t; i != s; i = e[rt[i] ^ 1].to)
    e[rt[i]].f += f, e[rt[i] ^ 1].f -= f;
flow += f, budget -= f * dis[t];
cost += f * dis[t];
f (budget -= l | f = r 0) beach;
                     if (budget == 0 || f == 0) break;
               return {flow, cost};
        void reset() {
               for (int i = 0; i < m; i++) e[i].f = 0;
};
```

4.4 Hungarian [d41d8c]

```
struct Hungarian { // 0-based, O(VE)
        int n, m;
vector<vector<int>> adj;
        vector <int> used, vis;
vector <pair <int, int>> match;
Hungarian(int n = 0, int m = 0) {
               init(n_, m_);
        void init(int n_, int m_) {
    n = n_; m = m_;
              adj.assign(n + m, {});
used.assign(n + m, -1)
vis.assign(n + m, 0);
        void addEdge(int u, int v) {
   adj[u].push_back(n + v);
   adj[n + v].push_back(u);
        bool dfs(int u) {
               int sz = adj[u].size();
              for (int i = 0; i < sz; i++) {
   int v = adj[u][i];</pre>
                     if (vis[v] == 0) {
    vis[v] = 1;
                            if (used[v] == -1 || dfs(used[v])) {
    used[v] = u;
                            }
                     }
               return false;
        vector<pair<int, int>> work() {
               match.clear();
               used.assign(n + m, -1);
               vis.assign(n + m, 0);
for (int i = 0; i < n; i++) {
    fill(vis.begin(), vis.end(), 0);</pre>
                     dfs(i);
               for (int i = n; i < n + m; i++)
    if (used[i] != -1)</pre>
                            match.emplace_back(used[i], i - n);
               return match;
};
```

4.5 Theorem [d41d8c]

```
|// 有向無環圖:
| // 最小不相交路徑覆蓋:
// 最小路徑數 = 頂點數 - 最大匹配數
| // 最小相交路徑覆蓋:
// 先用
   Floyd 求傳遞封包,有連邊就建邊,然後再套最小不相交路徑覆蓋
// 二分圖:
// 最小點
   覆蓋: 選出一些點,讓所有邊至少有一個端點在點集中的最少數量
// 最小點覆蓋 = 最大匹配數
|// 還原解, flow 的作法是從源點開始 dfs, 只走 cap - flow > 0
// 的邊,最後挑選左邊還沒被跑過的點和右邊被跑過的點當作覆蓋的點
| // 最少邊覆蓋: 選出一些邊,讓所有點都覆蓋到的最少數量
| // 最少邊覆蓋 = 點數 - 最大匹配數
| // 最大獨立集: 選出一些點, 使這些點兩兩沒有邊連接的最大數量
// 最大獨立集 = 點數 - 最大匹配數
```

String 5

5.1 Hash [7a28d1]

```
constexpr int B = 59;
vector<Z> hash(string &s) {
       vector<Z> ans {0};
        for (auto c : s) {
    ans.push_back(ans.back() * B + (c - 'a' + 1));
        return ans:
void solve() {
       string`s, sub;
cin >> s >> sub;
        auto a = hash(s);
       auto a = nasn(s);
auto q = hash(sub);
auto find = q.back();
int ans = 0;
int l = 1, r = sub.size(), len = sub.size();
while (r <= s.size()) {
    if (a[r] - a[l - 1] * power(Z(B), len) == find) {</pre>
```

int newNode() {

```
l++. r++:
                                                                                                                                                           int x = ++tot
                                                                                                                                                           cnt[x] = 0, fill_n(trie[x], 26, 0);
           cout << ans << "\n";
                                                                                                                                                           return x;
 }
                                                                                                                                                   void add(const string &s) {
                                                                                                                                                           int p = 0;
for (auto c : s) {
   int &q = trie[p][c - 'a'];
  5.2 KMP [731acf]
  struct KMP {
                                                                                                                                                                    if (!q) q = newNode();
          string sub;
vector<int> fail;
                                                                                                                                                                    p = q;
           // fail 存匹配失敗時,移去哪
                                                                                                                                                           cnt[p] += 1;
           int find(const string &s) {
          KMP() {}
KMP(const string &sub_) {
                                                                                                                                                           for (auto c : s) {
                                                                                                                                                                    int q = trie[p][c - 'a'];
                   build(sub_);
                                                                                                                                                                    if (!q) return 0;
          feet of sub_new fail.

// sub = sub_, fail.resize(sub.size(), -1);

// for (int i = 1; i < sub.size(); i++) {
    int now = fail[i - 1];
    while (now != -1 && sub[now + 1] != sub[i])
    now = fail[now];
    if (sub[now + 1] == sub[i])
        fail[i] = now + 1;
}</pre>
                                                                                                                                                           return cnt[p]:
                                                                                                                                                  5.6 SA [f9b5d1]
                                                                                                                                                  struct SuffixArray {
                                     fail[i] = now + 1;
                                                                                                                                                           int n; string s;
                                                                                                                                                           vector<int> sa, rk, lc;
                                                                                                                                                           // n: 字串長度
                                                                                                                                                           // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置 // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
           vector < int > match(const string &s) {
                  cor<int> match(const string as) {
  vector<int> match;
  for (int i = 0, now = -1; i < s.size(); i++) {
     while (s[i] != sub[now + 1] && now != -1)
         now = fail[now];
     if (s[i] == sub[now + 1]) now++;
     if (now + 1 == sub.size()) {
         match.push_back(i - now);
         row = fail[now];
         row = 
                                                                                                                                                           // lc: LCP
                                                                                                                                                           數組, lc[i] 表示 sa[i] 和 sa[i + 1] 的最長公共前綴長度
SuffixArray(const string &s_) {
                                                                                                                                                                   s = s_; n = s.length();
                                                                                                                                                                    sa.resize(n);
                                                                                                                                                                    lc.resize(n - 1):
                                     now = fail[now];
                                                                                                                                                                     rk.resize(n);
                           }
                                                                                                                                                                     iota(sa.begin(), sa.end(), 0);
                                                                                                                                                                    sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });</pre>
                    return match;
                                                                                                                                                                    rk[sa[0]] = 0;

for (int i = 1; i < n; i++)

rk[sa[i]]
 };
  5.3 Z Function [5b63dc]
                                                                                                                                                                                         = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
                                                                                                                                                                    int k = 1:
|// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
                                                                                                                                                                    vector<int> tmp, cnt(n);
  // 的最長公共前綴 (LCP) 的長度
                                                                                                                                                                     tmp.reserve(n);
                                                                                                                                                                    while (rk[sa[n - 1]] < n - 1) {
  vector<int> Z(const string &s) {
                                                                                                                                                                            tmp.clear();
for (int i = 0; i < k; i++)</pre>
           int n = s.size();
          tht n = s.stze(),
vector <int> z(n);
z[0] = n; // lcp(s, s), -1 or n
for (int i = 1, j = 1; i < n; i++) {
    z[i] = max(0, min(j + z[j] - i, z[i - j]));
    while (i + z[i] < n && s[z[i]] == s[i + z[i]])</pre>
                                                                                                                                                                                    tmp.push_back(n - k + i);
                                                                                                                                                                             for (auto i : sa)
    if (i >= k)
                                                                                                                                                                                              tmp.push_back(i - k);
                                                                                                                                                                            fill(cnt.begin(), cnt.end(),
for (int i = 0; i < n; i++)
    ++cnt[rk[i]];</pre>
                   if (i + z[i] > j + z[j]) j = i;
                                                                                                                                                                             for (int i = 1; i < n; i++)
   cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; i--)
          return z;
  5.4 Manacher [958661]
                                                                                                                                                                                     sa[--cnt[rk[tmp[i]]]] = tmp[i];
                                                                                                                                                                             swap(rk, tmp);
rk[sa[0]] = 0;
       找到對於每個位置的廻文半徑
                                                                                                                                                                             string t = "#";
for (auto c : s) {
                   t += c;
                   t += '#';
                                                                                                                                                                     for (int i = 0, j = 0; i < n; i++) {
           int n = t.size();
                                                                                                                                                                             if (rk[i] == 0) {
           vector<int> r(n);
                                                                                                                                                                                     j = 0;
           for (int i = 0,
                   j = 0; i < n; i++) { // i 是中心, j 是最長回文字串中心
if (2 * j - i >= 0 && j + r[j] > i)
r[i] = min(r[2 * j - i], j + r[j] - i);
while (i - r[i] >=
0 && i + r[i] < n && t[i - r[i]] == t[i + r[i]])
                                                                                                                                                                             } else {
                                                                                                                                                                                     }
                   r[i] += 1;
if (i + r[i] > j + r[j])
j = i;
                                                                                                                                                                   }
                                                                                                                                                  RMQ < int > rmq(sa.lc);
auto lcp = [&](int i, int j) { // [i, j]
          return r;
                                                                                                                                                           i = sa.rk[i];
j = sa.rk[j];
 // # a # b # a #
// 1 2 1 4 1 2 1
                                                                                                                                                           if (i > j) swap(i, j);
assert(i != j);
  // # a # b # b # a #
// 1 2 1 2 5 2 1 2 1
                                                                                                                                                           return rmq(i, j);
 // 值 -1 代表原回文字串長度
// (id - val + 1) / 2 可得原字串回文開頭
                                                                                                                                                  5.7 SAM [c9e6e0]
  5.5 Trie [72392f]
                                                                                                                                                           // 1 -> initial state
static constexpr int ALPHABET_SIZE = 26;
  constexpr int N = 1E7;
int tot = 0;
                                                                                                                                                           static constexpr int ALPHABEI_SIZE = 26;
// node -> strings with the same endpos set
// link -> longest suffix with different endpos set
// len -> state's longest suffix
// fpos -> first endpos
// range-> [len(link) + 1, len]
  int trie[N][26], cnt[N];
  void reset()
          tot = 0, fill_n(trie[0], 26, 0);
```

```
struct Node {
   int len, link, fpos;
   array<int, ALPHABET_SIZE> next;
   Node() : len{}, link{}, fpos{}, next{} {}
        vector<Node> t;
       SAM() { init(); }
void init() {
              t.assign(2, Node());
t[0].len = -1;
       int newNode() {
              t.emplace_back();
return t.size() - 1;
       int extend(int p, int c) {
   if (!p) t[p].next[c] = 1;
   if (t[p].next[c]) {
                      int q = t[p].next[c];
                      if (t[q].len == t[p].len + 1) {
                             return a:
                      int r = newNode();
t[r] = t[q];
t[r].len = t[p].len + 1;
                      t[q].link = r;
                      while (t[p].next[c] == q) {
    t[p].next[c] = r;
                            p = t[p].link;
                      return r:
              int cur = newNode();
t[cur].len = t[p].len + 1;
t[cur].fpos = t[p].len;
               while (!t[p].next[c]) {
                     t[p].next[c] = cur;
p = t[p].link;
              t[cur].link = extend(p, c);
// distinct substr += t[cur].len - t[t[cur].link].len;
void solve() { // Substring Order II: build
       string s; cin >> s;
int n = s.length();
       vector < int > last(n + 1); // s[i - 1] 的後綴終點位置
       last[0] = 1;
       SAM sam;
       for (int i = 0; i < n; i++)
    last[i + 1] = sam.extend(last[i], s[i] - 'a');</pre>
       int sz = sam.t.size();
       // without this part for distinct substr
vector <int> cnt(sz);
// endpos size: substr occurence
for (int i = 1; i <= n; i++)
    cnt[last[i]]++;</pre>
       cnt[tdst[t]]++;
vector < vector < int >> g(sz);
for (int i = 1; i < sz; i++)
    g[sam.t[i].len].push_back(i);
for (int i = n; i > 0; i--)
    for (int u : g[i])
                      cnt[sam.t[u].link] += cnt[u];
      vector<ll> dp(sz, -1);
auto rec = [&](auto self, int u) -> ll {
   if (dp[u] != -1) return dp[u];
   dp[u] = cnt[u]; // = 1 for distinct
   for (int c = 0; c < SAM::ALPHABET_SIZE; c++) {
     int v = sam.t[u].next[c];
     if (v) dp[u] += self(self, v);
}</pre>
              return dp[u];
       rec(rec, 1);
       int k, p = 1; cin >> k;
       string ans;
while (k > 0) {
              for (int c = 0; c < SAM::ALPHABET_SIZE; c++) {
   int v = sam.t[p].next[c];</pre>
                      if (v) {
    if (k >= dp[v]) {
                                     k -= dp[v];
                             } else {
                                     ans.push_back('a' + c);
                                     k--, p = v;
break;
                             }
                    }
              }
       cout << ans << "\n";
```

5.8 Palindrome Tree [52fd3d]

```
struct PAM {
   // 0 -> even root, 1 -> odd root
```

```
static constexpr int ALPHABET_SIZE = 26;
// fail -> longest prefix(suffix) palindrome
// number end at i = end at link[last[i]] + 1
       struct Node {
   int len, fail, cnt;
              array<int, ALPHABET_SIZE> next;
             Node() : len{}, fail{}, next{} {}
       vector < Node > t;
PAM() { init(); }
       void init()
             s.clear();
             t.assign(2, Node());
t[0].len = 0, t[0].fail = 1;
             t[1].len = -1;
       int newNode() {
              t.emplace_back();
             return t.size() - 1;
       return p;
       int extend(int p, int c) {
   int i = s.size();
             s.push_back(c);
             p = getFail(p, i);
if (!t[p].next[c]) {
    int r = newNode();
                   int v = getFail(t[p].fail, i);
t[r].len = t[p].len + 2;
t[r].fail = t[v].next[c];
                    t[p].next[c] = r;
             return p = t[p].next[c];
      }
};
 f;
void solve() {
    string s; cin >> s;
    int n = s.length();
    vector<int> last(n + 1);
       last[0] = 1;
       PAM pam;
for (int i = 0; i < n; i++)
    last[i + 1] = pam.extend(last[i], s[i] - 'a');</pre>
       int sz = pam.t.size();
vector<int> cnt(sz);
for (int i = 1; i <= n; i++)</pre>
       cnt[last[i]]++; // 去重 = 1
for (int i = sz - 1; i > 1; i--)
              cnt[pam.t[i].fail] += cnt[i];
}
 5.9 Duval [86ac44]
```

```
// duval_algorithm
 // 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
 vector<string> duval(string s) {
   int i = 0, n = s.size();
        vector<string> res;
       while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
}</pre>
                    else k++:
             while (i <= k) {
    res.push_back(s.substr(i, j - k));</pre>
       return res;
 }
 // 最小旋轉字串
 string minRound(string s) {
       s += s;
int i = 0, n = s.size();
        int start = i;
while (i < n / 2) {
    start = i;</pre>
             int k = i, j = i + 1;
while (s[k] <= s[j] && j < n) {
   if (s[k] < s[j]) k = i;</pre>
              while (i <= k) {</pre>
                    i += j - k;
        return s.substr(start, n / 2);
```

Math

6.1 Modulo [1db779]

```
constexpr int Mod = 1E9 + 7;
 struct Z {
    explicit operator int() const { return x; }
Z operator -() const {
   return Z(norm(Mod - x));
     Z inv() const {
          return power(*this, Mod - 2);
     }
Z &operator+=(Z rhs) & {
    x = norm(x + rhs.x);
    ++hic.
          return *this;
     Z &operator -= (Z rhs) & {
          x = norm(x - rhs.x);
return *this;
     Z &operator*=(Z rhs) & {
          x = x * rhs.x % Mod;
return *this;
     Z &operator/=(Z rhs) & {
    return *this *= rhs.inv();
     friend Z operator+(Z lhs, Z rhs) {
         return lhs += rhs;
     friend Z operator -(Z lhs, Z rhs) {
         return lhs -= rhs;
     friend Z operator*(Z lhs, Z rhs) {
          return lhs *= rhs;
     friend Z operator/(Z lhs, Z rhs) {
    return lhs /= rhs;
     friend istream & operator >> (istream &is. Z &a) {
          ll v; is >> v; a = Z(v); return is;
     friend ostream &operator << (ostream &os. const Z &a) {
1 };
```

6.2 Combination [6aa734]

6.3 Sieve [37ae54]

6.4 Miller Rabin Pollard Rho [394cfb]

```
ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
         res %= p;
        if (res < 0) res += p;
return res;</pre>
fll power(ll a, ll b, ll p) {
    ll res {1};
    for (; b; b /= 2, a = mul(a, a, p))
        if (b & 1) res = mul(res, a, p);
        return res;
vector<ll
return 0:
bool isPrime(ll n) {
    if (n < 2) return 0;
    if (n % 2 == 0) return n == 2;
    ll d = n - 1, s = 0;
    while (d % 2 == 0) d /= 2, s++;
    for (ll i: chk)
        if (!check(i, d, s, n)) return 0;
}</pre>
        return 1:
 const vector<ll> small = {2, 3, 5, 7, 11, 13, 17, 19};
ll findFactor(ll n) {
   if (isPrime(n)) return 1;
   for (ll p : small)
      if (n % p == 0) return p;
   ll x, y = 2, d, t = 1;
   auto f = [&](ll a) {
      return (mul/a = 2, 2, 3, 5)
}
               return (mul(a, a, n) + t) % n;
         for (int l = 2; ; l *= 2) {
               int m = min(l, 32);
for (int i = 0; i < l; i += m) {
                       d = 1;
for (int j = 0; j < m; j++)
    y = f(y), d = mul(d, abs(x - y), n);
ll g = __gcd(d, n);
if (g == n) {
    l = 1, y = 2, ++t;
    break;</pre>
                        if (g != 1) return g;
               }
map<ll, int> res;
void pollardRho(ll n) {
   if (n == 1) return;
   if (isPrime(n)) {
               res[n]++;
               return;
        Il d = findFactor(n);
        pollardRho(n / d), pollardRho(d);
```

6.5 CRT [6b1b59]

```
| ll exgcd(ll a, ll b, ll &x, ll &y) {
    if (!b) {
        x = 1, y = 0;
        return a;
    }
```

6.6 Matrix [2856cb]

6.7 Mex [14628f]

```
template < class T>
int mex(vector < T > &v) {
    unordered_set < T > s;
    for (auto e : v) s.insert(e);
    for (T i = 0; ; i++)
        if (s.find(i) == s.end()) return i;
}
```

6.8 Game Theorem

- · sq 值為 0 代表先手必敗
- 當前 sg 值 = 可能的後繼狀態的 mex (例如拿一個或拿兩個, 就等於兩者的 sg 值 mex), 若有互相依賴就兩個後繼狀態 xor 當作一組 sg 值 (例如切開成兩半, 只算一次)
- 單組基礎 nim 的 sg 值為本身的原因: f(0)=0, f(1)=mex(f(0))=1, f(2)=mex(f(0),f(1))=2...,都是自己 • 多組賽局可以把 sg 值 xor 起來,當成最後的 sg 值,nim 也是一樣,且由於
- 多組賽局可以把 sg 值 xor 起來,當成最後的 sg 值, nim 也是一樣,且由於 xor 性質,如果可以快速知道 sg(1)g(2)...g(n),就可以用 xor 性質處理不連 續組合

續組合 **6.9 Fraction** [3f8970]

```
template < class T>
struct Fraction {
    T n, d;
    void reduce() {
        T g = gcd(abs(n), abs(d));
        n /= g, d /= g;
        if (d < 0) n = -n, d = -d;
}
Fraction(T n_ = 0, T d_ = 1) : n(n_), d(d_) {
        assert(d != 0);
        reduce();
}
Fraction(const string & str) {
        istringstream ss(str);
        char slash;
        if (str.find('/') != -1) {
            ss >> n >> slash >> d;
        } else {
            ss >> n;
            d = 1;
        }
}
```

```
Fraction(n. d):
     Fraction operator+=(Fraction rhs) & {
    n = n * rhs.d + rhs.n * d;
    d *= rhs.d;
           reduce();
           return *this:
     Fraction operator -= (Fraction rhs) & {
    n = n * rhs.d - rhs.n * d;
    d *= rhs.d;
          reduce();
return *this;
     Fraction operator*=(Fraction rhs) & {
          n *= rhs.n;
d *= rhs.d;
          reduce();
return *this;
     Fraction operator/=(Fraction rhs) & {
          assert(rhs.n != 0);
          n *= rhs.d;
d *= rhs.n;
           reduce();
           return *this;
      friend Fraction operator+(Fraction lhs, Fraction rhs) {
           return lhs += rhs;
      friend Fraction operator - (Fraction lhs, Fraction rhs) {
           return lhs -= rhs;
     friend Fraction operator*(Fraction lhs, Fraction rhs) {
   return lhs *= rhs;
     friend Fraction operator/(Fraction lhs, Fraction rhs) {
   return lhs /= rhs;
     friend istream & operator >> (istream &is, Fraction &f) {
          string s;
           f = Fraction(s);
           return is:
             ostream & operator << (ostream &os, const Fraction &f) {
           if (f.d == 1) {
                os << f.n;
          } else {
               os << f.n << "/" << f.d;
           return os:
      friend bool operator==(Fraction lhs, Fraction rhs) {
           return lhs.n * rhs.d == rhs.n * lhs.d;
     friend bool operator!=(Fraction lhs, Fraction rhs) {
  return lhs.n * rhs.d != rhs.n * lhs.d;
     friend bool operator < (Fraction lhs, Fraction rhs) {
  return lhs.n * rhs.d < rhs.n * lhs.d;</pre>
};
```

6.10 Gaussian Elimination [a5e69e]

```
det = (zeroDet ? 0 : det * sgn);
       for (int r = rk; r < n; r++)
   if (a[r][m - 1] != 0) return {det, 0, {}};
if (rk < n) return {det, -1, {}};</pre>
        vector<T> ans(n);
        for (int i = 0; i < n; i++) ans[i] = a[i][m - 1];</pre>
        return {det, 1, ans};
 template < class T>
tuple<int, vector
         <T>, vector<vector<T>>> findBasis(vector<vector<T>>> a) {
       int n = a.size(), m = a[0].size(), rk = 0;
vector<int> pos(m - 1, -1);
for (int c = 0; c < m - 1; c++) {
   int p = -1;</pre>
                for (int r = rk; r < n; r++) {
    if (a[r][c] != 0) {</pre>
                               p = r;
                       }
               f (p == -1) continue;
if (p != rk) swap(a[rk], a[p]);
pos[c] = rk;
T inv = 1 / a[rk][c];
                for (int j = c; j < m; j++) a[rk][j] *= inv;
for (int r = 0; r < n; r++) {
    if (r == rk || a[r][c] == 0) continue;</pre>
                       T fac = a[r][c];

for (int j = c; j < m; j++)

a[r][j] -= fac * a[rk][j];
                rk++;
        vector<T> sol(m - 1);
        vector < vector < T >> basis;
       for (int r = rk; r < n; r++)
    if (a[r][m - 1] != 0)
        return {-1, sol, basis};
for (int c = 0; c < m - 1; c++)
    if (pos[c] != -1)
        sol[c] = a[pos[c]][m - 1];
for (int c = 0; c < m - 1; c++)</pre>
       for (int c = 0; c < m - 1; c++)
if (pos[c] == -1)
                       vector<T> v(m - 1);
                       vectors...
v[c] = 1;
for (int j = 0; j < m - 1; j++)
    if (pos[j] != -1)
     v[j] = -a[pos[j]][c];</pre>
                       basis.push_back(v);
        return {rk, sol, basis};
template < class T>
using Matrix = vector < vector < T>>;
```

6.11 Dynamic Modulo [24c243]

```
template < class T>
T power(T a, ll b) {
    T res {1};
     for (; b; b /= 2, a *= a)

if (b & 1) res *= a;
res %= p;
if (res < 0) res += p;
     return res;
template < ll P >
struct Mint {
    ll x;
     Mint(ll x = 0) : x \{norm(x \% getMod())\} \{\}
     static ll Mod;
static ll getMod() {
   return P > 0 ? P : Mod;
     static void setMod(ll Mod_) {
          Mod = Mod_;
     il norm(ll x) const {
    if (x < 0) x += getMod();
    if (x >= getMod()) x -= getMod();
     explicit operator int() const { return x; }
     Mint operator -() const {
          return Mint(norm(getMod() - x));
     Mint inv() const {
    return power(*this, getMod() - 2);
     Mint & operator += (Mint rhs) & {
          x = norm(x + rhs.x);
return *this;
     Mint &operator -= (Mint rhs) & {
          x = norm(x - rhs.x);
return *this;
     Mint & operator *= (Mint rhs) & {
```

```
if (getMod() < (1ULL << 31)) {
    x = x * rhs.x % int(getMod());</pre>
           } else {
                 x = mul(x, rhs.x, getMod());
           return *this;
      Mint & operator /= (Mint rhs) & {
    return *this *= rhs.inv();
      friend Mint operator+(Mint lhs, Mint rhs) {
           return lhs += rhs;
      friend Mint operator - (Mint lhs, Mint rhs) {
    return lhs -= rhs;
      friend Mint operator*(Mint lhs, Mint rhs) {
  return lhs *= rhs;
      friend Mint operator/(Mint lhs, Mint rhs) {
  return lhs /= rhs;
      friend istream &operator>>(istream &is, Mint &a) {
    ll v; is >> v; a = Mint(v); return is;
      friend ostream &operator<<(ostream &os, const Mint &a) {</pre>
           return os << a.x;
      // following operators are not necessary
friend bool operator==(Mint lhs, Mint rhs) {
    return lhs.x == rhs.x;
      friend bool operator!=(Mint lhs, Mint rhs) {
   return lhs.x != rhs.x;
      friend bool operator < (Mint lhs, Mint rhs) {</pre>
           return lhs.x < rhs.x;</pre>
     }
template<>
ll Mint<0>::Mod = 998244353;
constexpr ll P = 1E9 + 7;
using Z = Mint<P>;
```

6.12 Integer Partition [a2c848]

6.13 Mobius Theorem

- ・數論分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d|n} \mu(d) = \begin{cases} 1 & \text{for } n=1\\ 0 & \text{for } n \neq 0 \end{cases}$$

- 2. μ 是常數函數 1 的反元素
- $\Rightarrow \mu * 1 = \epsilon$, $\epsilon(n)$ 只在n = 1 時為 1 , 其餘情況皆為 0 。
- φ歐拉函數: x以下與 x 互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^i) \\ &= 1 + p^0(p-1) + p^1(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^c \\ &= id \end{split}$$

- 莫比烏斯反演公式
 - $f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$
 - $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

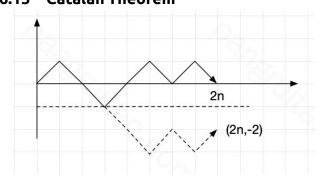
例子

$$\begin{split} &\sum_{i=aj=c}^{b} \sum_{j=1}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{\infty} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.14 Mobius Inverse [d41d8c]

```
const int maxn = 2E5:
ll mobiusPref[maxn];
void init() {
    mobiusPref[1] = 1;
    vector<ll> wei
    continue; // 包含平方
         if (wei[i] == 0) {
    wei[i] = 1;
             }
         mobiusPref[i]
               = mobiusPref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
    }
void solve() {
    for (int l = 1, r; l <= min(x, y); l = r + 1) {
    r = min(x / (x / l), y / (y / l));
    res += (mobiusPref[r] - mobiusPref[l]</pre>
                   - 1]) * (x / l) * (y / l); // 代推出來的式子
         return res;
    cout << cal
         (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k, (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n";
}
```

6.15 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2)

假設往上有 x 個,往下有 y 個,會有:

$$\begin{cases} x + y = 2n \\ y - x = 2 \end{cases} \Rightarrow \begin{cases} x = n - 1 \\ y = n + 1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.16 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- · G:各種翻轉操作所構成的置換群
- X/G: 本質不同的方案的集合 X/G: 對於某一種操作 g,所有方案中,經過 g 這種翻轉後保持不變的方案 的集合
- 集合取絕對值代表集合數

Search and Gready

Binary Search [d41d8c]

```
void binarySearch() {
      // 二分找上界
while (lo < hi) {
    int x = (lo + hi + 1) / 2;
    if (check(x)) lo = x;
           else hi = x - 1;
      cout << lo; // 保證有解
      while (lo <= hi) {
   int x = (lo + hi) / 2;
   if (check(x)) lo = x + 1;
}</pre>
           else hi = x - 1;
      cout << hi; // 範圍外代表無解
          二分找下界
      cout << lo; // 保證有解
      while (lo <= hi) {
   int x = (lo + hi) / 2;</pre>
           if (check(m)) hi = x - 1;
           else lo = x + 1;
      cout << lo; // 範圍外代表無解
}
```

Tree 8

Binary Lifting LCA [4273df]

```
const int Q = 20; // log(q) or log(n)
vector < vector < int >> par;
vector<int> dep, dfn;
void build(int n, vector<vector<int>> &tree, int u = 0) {
     par.assign(n, vector<int>(Q + 1, -1));
dep.assign(n, 0), dfn.assign(n, 0);
     int cur = 0;
auto dfs = [&](auto self, int x, int p) -> void {
         p dfs = [&](auto sec, ...
dfn[x] = cur++;
for (auto y : tree[x]) {
    if (y == p) continue;
    par[y][0] = x;
    dep[y] = dep[x] + 1;
    self(self, y, x);
         }
     };
     par[u][0] = u;
     a = par[a][i];

if (a == b) return a;

for (int i = Q; i >= 0; i--)

if (par[a][i] != par[b][i])
     x = par[x][i];
```

8.2 Centroid Decomposition [4f8836]

```
struct CentriodDecomposition {
    int n;
    vector<vector<int>> adj;
    vector<bool> vis;
    vector<int> siz;
    CentriodDecomposition(int n_ = 0) { init(n_); }
    void init(int n_) {
       n = n_;
```

```
adj.assign(n, {});
vis.assign(n, false);
                 siz.assign(n, 1);
         void addEdge(int u, int v) {
                 adj[u].push_back(v);
                 adj[v].push_back(u);
         void getSiz(int x, int p = -1) {
                | getstctut x, sur r
siz[x] = 1;
for (int y : adj[x]) {
    if (y == p || vis[y]) continue;
      getSiz(y, x);
    siz[x] += siz[y];
}
        int getCen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz)
                                 return getCen(y, sz, x);
                 return x;
         void getAns(int x, int p) {
                // do something
for (int y : adj[x]) {
    if (y == p || vis[y]) continue;
    getAns(y, x);
                }
         void work(int x = 0) {
                getSiz(0, x);
int cen = getCen(x, siz[x]);
vis[cen] = true;
for (int y : adj[cen]) {
   if (vis[y]) continue;
   getAns(y, cen);
                for (int y : adj[cen]) {
   if (vis[y]) continue;
                        work(y);
        }
};
```

8.3 Heavy Light Decomposition [41d99e]

struct HLD {

```
int n, cur;
vector<int> siz, top, dep, parent, in, out, seq;
vector <int> st2, top, dep, parent, th, out, seq;
vector <vector <int>> adj;
HLD(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_; cur = 0;
    siz.resize(n); top.resize(n); dep.resize(n);
    parent.resize(n); in.resize(n); out.resize(n);
       seq.resize(n); adj.assign(n, {});
void addEdge(int u, int v) {
   adj[u].push_back(v);
       adj[v].push_back(u);
void work(int rt = 0) {
       top[rt] = rt;
dep[rt] = 0;
parent[rt] = -1;
       dfs1(rt); dfs2(rt);
void dfs1(int u) {
   if (parent[u] != -1)
        adj[u].erase(find
                      (adj[u].begin(), adj[u].end(), parent[u]));
       siz[u] = \hat{1};
       for (auto &v : adj[u]) {
   parent[v] = u, dep[v] = dep[u] + 1;
   dfs1(v);
              siz[u] += siz[v];
if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
             } // 讓 adj[u][0] 是重子節點
      }
void dfs2(int u) {
       in[u] = cur++;
       seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
   top[v] = v == adj[u][0] ? top[u] : v;
              dfs2(v);
       out[u] = cur;
int lca(int u, int v) {
    while (top[u] != top[v]) {
             if (dep[top[u]] > dep[top[v]]) {
             u = parent[top[u]];
} else {
                    v = parent[top[v]];
       return dep[u] < dep[v] ? u : v;</pre>
```

8.4 Link Cut Tree [510da5]

```
template < class Info, class Tag>
struct LinkCutTree { // 1-based
      struct Node {
            Info info = Info();
            Tag tag = Tag();
bool rev = false;
int size = 0;
            int ch[2], p = 0;
      vector<Node> nd;
LinkCutTree(int n = 0) { init(n); }
void init(int n) {
            nd.clear();
            nd.emplace_back();
            resize(n);
       void resize(int n) {
            nd.resize(n + 1);
            return !nd[t].p || (
	nd[nd[t].p].ch[0] != t && nd[nd[t].p].ch[1] != t);
      void makeRev(int t) {
    swap(nd[t].ch[0], nd[t].ch[1]);
    nd[t].rev ^= true;
      void apply(int t, const Tag &v) {
    nd[t].info.apply(nd[t].size, v);
             nd[t].tag.apply(v);
      void push(int t) {
            if (nd[t].rev) {
                   if (nd[t].ch[0]) makeRev(nd[t].ch[0]);
if (nd[t].ch[1]) makeRev(nd[t].ch[1]);
nd[t].rev = false;
            if (nd[t].ch[0]) apply(nd[t].ch[0], nd[t].tag);
if (nd[t].ch[1]) apply(nd[t].ch[1], nd[t].tag);
             nd[t].tag = Tag();
      void pull(int t) {
            nd[t].size
                    = 1 + nd[nd[t].ch[0]].size + nd[nd[t].ch[1]].size;
             nd[t].info
                     .pull(nd[nd[t].ch[0]].info, nd[nd[t].ch[1]].info);
      int pos(int t) {
    return nd[nd[t].p].ch[1] == t;
      void pushAll(int t) {
   if (!isrt(t)) pushAll(nd[t].p);
             push(t);
      void rotate(int t) {
   int q = nd[t].p, x = !pos(t);
   nd[q].ch[!x] = nd[t].ch[x];
   if (nd[t].ch[x]) nd[nd[t].ch[x]].p = q;
   nd[t].p = nd[q].p;
            if (!isrt(q)) nd[nd[q].p].ch[pos(q)] = t;
nd[t].ch[x] = q, nd[q].p = t;
pull(q);
      void splay(int t) {
    pushAll(t);
             while (!isrt(t)) {
                  if (!isrt(nd[t].p)) {
```

```
if (pos(t) == pos(nd[t].p)) {
    rotate(nd[t].p);
                     } else {
                          rotate(t):
               rotate(t);
          pull(t);
     void access(int t) { // access 後自動 splay
    for (int i = t, q = 0; i; q = i, i = nd[i].p) {
               splay(i);
               nd[i].ch[1] = q;
               pull(i);
          splay(t);
     void makeRoot(int t) {
          access(t), makeRev(t);
     int findRoot(int t) {
          access(t);
          int x = t;
while (nd[x].ch[0]) {
               push(x);
               x = nd[x].ch[0];
          access(x);
          return x;
     bool connected(int x, int y) {
    return findRoot(x) == findRoot(y);
     bool neighber(int x, int y) {
          makeRoot(x), access(y);
if (nd[y].ch[0] != x || nd[x].ch[1]) return false;
          return true;
     void split(int rt, int y) {
    makeRoot(y), access(rt);
     void link(int x, int y) {
          makeRoot(x);
          if (findRoot(y) != x) nd[x].p = y;
     void cut(int x, int y) {
    makeRoot(x), access(y);
    nd[y].ch[0] = nd[nd[y].ch[0]].p = 0;
          pull(x), pull(y);
     void modify(int x, const Info &v) {
          access(x);
          nd[x].info = v;
     void pathApply(int x, int y, const Tag &v) {
   assert(connected(x, y));
          split(x, y), apply(x, v);
     Info pathQuery(int x, int y) {
          assert(connected(x, y));
          split(x, y);
return nd[x].info;
     }
constexpr int Mod = 51061;
struct Tag {
    ll add = 0; ll mul = 1;
     void apply(const Tag &v) {
   mul = mul * v.mul % Mod;
   add = (add * v.mul % Mod + v.add) % Mod;
    }
struct Info {
     void pull(const Info &l, const Info &r) {
   sum = (l.sum + r.sum + val) % Mod;
};
```

8.5 Virtual Tree [c3a0b3]

```
// 多次詢問給某些關鍵點, 虚樹可達成快速樹 DP (前處理每個點)
// 例如這題是有權樹,給一些關鍵點,求跟 vertex 1 隔開的最小成本
// 前處理 root 到所有點的最小邊權
vector<int> stk:
void insert(int key, vector<vector<int>> &vt) {
   if (stk.empty()) {
       stk.push_back(key);
        return:
   int l = lca(stk.back(), key);
if (l == stk.back()) {
        stk.push_back(key);
        return:
    while (
        stk.size() > 1 && dfn[stk[stk.size() - 2]] > dfn[l]) {
```

```
vt[stk[stk.size() - 2]].push_back(stk.back());
           stk.pop_back();
      if (stk.size() < 2 || stk[stk.size() - 2] != l) {
   vt[l].push_back(stk.back());</pre>
           stk.back() = l;
     stk.push back(kev):
int work(vector<vector<int>> &vt) {
   while (stk.size() > 1) {
     vt[stk[stk.size() - 2]].push_back(stk.back());
           stk.pop_back();
      int rt = stk[0];
      stk.clear();
      return rt;
void solve() {
     int n; cin >> n;
vector<vector<int>> g(n);
vector<vector<pair<int, int>>> wg(n);
      vector<vector<int>> vt(n);
      for (int i = 1; i < n; i++) {
  int u, v, w;
  cin >> u >> v >> w;
           u--, v--;
g[u].push_back(v), g[v].push_back(u);
wg[u].emplace_back(v, w), wg[v].emplace_back(u, w);
      build(n, g); // build LCA
     self(self, y, x);
          }
      dfs_dis(dfs_dis, 0, -1);
      vector<bool> isKey(n);
      vector<ll> dp(n);
      int q; cin >> q;
while (q--) {
           < m; i++) {
                 isKey[key[i]] = true;
           key.push_back(0); // 固定 0 為 root, 看題目需求
sort(key.begin(), key.end(), [&](int a, int b) {
    return dfn[a] < dfn[b];
}); // 要 sort 再 insert
for (auto x : key) insert(x, vt);
prock(x);
           work(vt);
           auto dfs = [&](auto &&self, int x) -> void {
                 for (auto y : vt[x]) {
    self(self, y);
                      if (isKey[y]) { // 直接砍了
dp[x] += dis[y];
} else { // 不砍 or 砍
dp[x] += min<ll>(dp[y], dis[y]);
                          // 記得 reset
                      isKey[y] = dp[y] = 0;
                }
                vt[x].clear(); // 記得 reset
           dfs(dfs, 0);
cout << dp[0] << "\n";</pre>
           dp[0] = 0; // 最後 reset root
}
```

8.6 Dominator Tree [1babd0]

```
// dom
          存起點到達此點的必經的上個節點(起點 = 自己), 無法到達 = -1
  struct DominatorTree {
         int n, id;
        vector < vector < int >> adj, radj, bucket;
vector < int >> sdom, dom, vis, rev, pa, rt, mn, res;
DominatorTree(int n_ = 0) { init(n_); }
void init(int n_) {
               n = n_, id = 0;
adj.assign(n, {});
radj.assign(n, {});
               bucket.assign(n, {});
sdom.resize(n), dom.assign(n, -1);
vis.assign(n, -1), rev.resize(n);
pa.resize(n), rt.resize(n);
               mn.resize(n), res.resize(n);
         void add_edge(int u, int v) {
               adj[u].push_back(v);
```

ans.push_back(v[i]), L--;

reverse(ans.begin(), ans.end());

== 1 && (g[i] & bitset<N>(pre)) == pre) {

dp[mask] = 1; // i 有連到所有 pre

```
for (auto i : ans) cout << i << " ";</pre>
     9.3 Edit Distance [b13609]
                                                                                         void editDistance() {
                                                                                              string s1, s2; cin >> s1 >> s2;
int n1 = s1.size(), n2 = s2.size();
vector<int> dp(n2 + 1);
           mn[v] = mn[rt[v]];
rt[v] = p;
return x ? p : mn[v];
                                                                                              cur[j] = dp[j -
                     dfs(u), pa[vis[u]] = vis[v];
                                                                                                         } else {
                radj[vis[u]].push_back(vis[v]);
                                                                                                              // s1 新增等價於 s2 砍掉
                                                                                                              // dp[i][j] = min(s2 新增, 修改, s1 新增);
                                                                                                               cur[j]
     vector<int> build(int s) {
                                                                                                                     = min({cur[j - 1], dp[j - 1], dp[j]}) + 1;
           dfs(s);
for (int i = id - 1; i >= 0; i--) {
                                                                                                         }
                for (int u : radj[i])
    sdom[i] = min(sdom[i], sdom[query(u, 0)]);
if (i) bucket[sdom[i]].push_back(i);
                                                                                                    swap(dp, cur);
                                                                                              cout << dp[n2] << "\n";
                for (int u : bucket[i]) {
                     int p = query(u, 0);
dom[u] = sdom[p] == i ? i : p;
                                                                                         9.4 Bitmask [da8000]
                if (i) rt[i] = pa[i];
                                                                                         void hamiltonianPath() {
                                                                                              int n, m; cin >> n >> m;
vector <vector <int>> adj(n);
for (int i = 0; i < m; i++) {
    int u, v; cin >> u >> v;
          fres.assign(n, -1);
for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i])
        dom[i] = dom[dom[i]];</pre>
                                                                                                    adj[--v].push_back(--u);
                             1; i < id; i++)
                res[rev[i]] = rev[dom[i]];
                                                                                              // 以...為終點,走過...
vector dp(n, vector<int>(1 << n));
           res[s] = s;
for (int i = 0; i < n; i++)
dom[i] = res[i];
                                                                                             }
};
9 DP
9.1 LCS [6ef49c]
void LCS() {
     int m, n; cin >> m >> n;
string s1, s2; cin >> s1 >> s2;
int L = 0;
                                                                                                   }
                                                                                              cout << dp[n - 1][(1 << n) - 1] << "\n";
      vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0));
     for (int i = 1; i <= m; i++) {
    for (int j = 1; j <= n; j++) {
        if (s1[i - 1] == s2[j - 1]) {
            dp[i][j] = dp[i - 1][j - 1] + 1;
        }
                                                                                         void elevatorRides() {
   int n, x; cin >> n >> x;
   vector<int> a(n);
   for (int i = 0; i < n; i++) {
      cin >> a[i];
}
                     dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
                }
                                                                                               vector<int> dp(1 << n), f(1 << n);
                                                                                              }
     fint length = dp[m][n];
cout << length << "|n";
string s(length, 'c'); // backtracking
while (m >= 1 && n >= 1) {
   if (s1[m - 1] == s2[n - 1]) {
      s[length - 1] = s1[m - 1];
      man not length...
                m--, n--, length--;
           else {
    if (dp[m - 1][n] > dp[m][n - 1]) m--;
                                                                                                         } else if (dp[pre] + 1 < dp[mask] ||
    dp[pre] + 1 == dp[mask] && a[i] < f[mask]) {
    dp[mask] = dp[pre] + 1;
    f[mask] = a[i];</pre>
                else n--;
     cout << s << "\n";
9.2 LIS [2b086e]
                                                                                              cout << dp[(1 << n) - 1] << "\n";
void LIS() {
     int n; cin >> n;
vector <int> v(n);
for (int i = 0; i < n; i++) cin >> v[i];
                                                                                         void minClique() { // 移掉一些邊, 讓整張圖由最少團組成
                                                                                              int n, m;
cin >> n >> m;
      int dp[n], L = 1;
                                                                                              vector < bitset < N >> g(n);
     for (int i = 0; i < m; i++) {
                                                                                                   int u, v;
cin >> u >> v;
               stk.push_back(v[i]);
dp[i] = ++L;
                                                                                                   g[u][v] = g[v][u] = 1;
           } else
                                                                                              vector<int> dp(1 << n. inf):
                auto it
                                                                                              dp[0] = 1;
                        = lower_bound(stk.begin(), stk.end(), v[i]);
                                                                                              for (int mask = 0; mask < 1 << n; mask++) { // 先正常 dp
                *it = v[i]; dp[i] = it - stk.begin() + 1;
                                                                                                    for (int i = 0; i < n; i++) {
   if (mask & (1 << i)) {
     int pre = mask ^ (1 << i);
}</pre>
          }
      vector<<mark>int</mark>> ans; cout << L << "\n";
                                                                                                               if (dp[pre]
     for (int i = n - 1; i >= 0; i--)
   if (dp[i] == L)
```

```
}

for (int

mask = 0; mask < 1 << n; mask++) { // 然後枚舉子集 dp
for (int sub = mask; sub; --sub &= mask) {
    dp[mask] = min(dp[mask], dp[sub] + dp[mask ^ sub]);
}

cout << dp[(1 << n) - 1] << "\n";
}
```

9.5 Projects [f34a85]

```
void projects() { // 排程有權重問題,輸出價值最多且時間最少
      struct E {
            int from, to, w, id;
      int n; cin >> n; vector<E> a(n + 1);
for (int i = 1; i <= n; i++) {</pre>
            int u, v, w;
cin >> u >> v >> w:
            a[i] = {u, v, w, i};
      vector<array<ll, 2>> dp(n + 1); // w, time
      vector<array<int, 2>> rec(n + 1); // 有沒選,上個是誰
      sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
   int id = --</pre>
                   lower_bound(all(a), \{0, a[i].from\}, [](E x, E y) \{
                 return x.to < y.to;</pre>
            return x.to < y.to;

)) - a.begin();

dp[i] = dp[i - 1];

ll nw = dp[id][0] + a[i].w;

ll nt = dp[id][1] + a[i].to - a[i].from;
            if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
    dp[i] = {nw, nt};
    rec[i] = {1, id};
      vector < int > ans;
for (int i = n; i != 0;) {
    if (rec[i][0]) {
                  ans.push_back(a[i].id);
i = rec[i][1];
            } else { i--;
}
```

9.6 Removal Game [c4b594]

9.7 Monotonic Queue [c9ba14]

9.8 SOS [7a4936]

```
| // 使用情況: 跟 bit 與(被)包含有關, 且 x 在 1E6 左右
 // 題目:一數組, 問有多少所有數 & 起來為 0 的集合數
// dp[
       x] 代表包含 x 的 y 個數(比 x 大且 bit 1 全包含 x 的有幾個)
// 答案應該包含在 dp[0] 内,但是有重複元素,所以考慮容斥 // => ans = \sum_{i=0}^{n} (-1)^{pop\_count(i)} 2^{dp[i]-1}
      部為 0 的個數 - 至少一個為 1 的個數 + 至少兩個為 1 的個數
void solve() {
   int n; cin >> n; Z ans = 0;
   vector<int> a(n);
   for (int i = 0; i < n; i++) cin >> a[i];
      int m = __lg(*max_element(a.begin(), a.end())) + 1;
      // 定義 dp[mask] 為 mask 被包含於 a[i] 的 i 個數
     }
      for (int mask = 0; mask < 1 << m; mask++) {
    int sgn = __builtin_popcount(mask) & 1 ? -1 : 1;
    ans += sgn * (power(Z(2), dp[mask].val()) - 1);</pre>
      cout << ans << "\n";
}
//x / y = x, 代表包含於 x 的 y 個數, 定義為 dp[x][0]
| // x & y = x, 代表包含 x 的 y 個數, 定義為 dp[x][1]
// x & y != 0, 代表至
      少有一個位元都為 1 的 y 個數, = n - 與自己相同 - \sim dp[x][0]
 void solve() {
      int n; cin >> n;
vector < int > a(n);
      map < int , int > mp;
for (int i = 0; i < n; i++) {</pre>
           cin >> a[i];
           mp[a[i]]++;
      int m = __lg(*max_element(a.begin(), a.end())) + 1;
vector<array<ll, 2>> dp(1 << m);
for (int i = 0; i < n; i++) {
    dp[a[i]][0] += 1;
    dp[a[i]][1] += 1;</pre>
           dp[a[i]][1] += 1;
      for (int i = 0; i < m; i++) {
    for (int mask = 0; mask < 1 << m; mask++) {
      if (mask >> i & 1) {
        int pre = mask ^ (1 << i);
    }
}</pre>
                     dp[mask][0] += dp[pre][0];
dp[pre][1] += dp[mask][1];
               }
```

9.9 CHT [5f5c25]

```
| // 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for jsr(i)
| // A(j), B(j) 可能包含 dp(j), 分別就是 m 跟 b

struct Line {
    ll m, b;
    Line(ll m = 0, ll b = 0) : m(m), b(b) {}
    ll eval(ll x) {
        return m * x + b;
    }
};

struct CHT { // 用在查詢單調斜率也單調
    int n, lptr, rptr;
    vector<Line> hull;
    CHT(int n_ = 0, Line init_ = Line()) {
        init(n_, init_);
    }
    void init(int n_ = 0, Line init_ = Line()) {
        n = n_; hull.resize(n); reset(init_);
    }
    void reset(Line init_ = Line()) {
        lptr = rptr = 0; hull[0] = init_;
    }
    bool pop_front(Line &l1, Line &l2, ll x) {
        // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y
```

```
// 代表查詢的當下,右線段的高度已經低於左線段了return l1.eval(x) >= l2.eval(x);
    bool pop_back(Line &l1, Line &l2, Line &l3) {
        // 本題斜率遞減、上凸包
        // 因此只要 12 跟
             13 的 X 交點 <= 11 跟 13 的 X 交點, 12 就用不到了
        return (l3.b - l2.b)

* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
    void insert(Line L) {
        while (rptr - lptr
             > 0 && pop_back(hull[rptr - 1], hull[rptr], L))
        hull[++rptr] = L;
    Il query(ll x) {
        while (rptr
              > 0 && pop_front(hull[lptr], hull[lptr + 1], x))
           lptr++
        return hull[[lptr].eval(x);
};
```

9.10 DNC [49f715]

9.11 LiChao Segment Tree [588aa3]

```
// 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \le r(i)
constexpr ll inf = 4E18;
struct Line {
    ll m, b;
    Line(ll m = 0, ll b = inf) : m(m), b(b) {}
    ll eval(ll x) const {
        return m * x + b;
    }
}
};
struct LiChaoSeg { // 取 max 再變換就好
      vector <Line > info;
LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_) {
            n = n_;
            info.assign(4 << __lg(n), Line());</pre>
      void update(Line line, int node, int l, int r) {
  int m = (l + r) / 2;
  bool left = line.eval(l) < info[node].eval(l);
  bool mid = line.eval(m) < info[node].eval(m);</pre>
            if (mid) swap(info[node], line); // 如果新線段比較好
            if (r - l == 1) return;
else if (left != mid) update(line, 2 * node, l, m);
             // 代表左半有交點
            else update(line, 2 * node + 1, m, r);
            // 代表如果有交點一定在右半
      void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
   if (r - l == 1) return info[node].eval(x);
   int m = (l + r) / 2;
            if (x < m) {
                  return min(
                         info[node].eval(x), query(x, 2 * node, l, m));
                  return min(info
                         [node].eval(x), query(x, 2 * node + 1, m, r));
      }
```

```
ll query(int x) {
          return query(x, 1, 0, n);
};
```

9.12 Codeforces Example [08fee8]

```
| // 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
 // 請問在線段不重複的情況下,最多獲得幾分
 void solve() {
       int n, m;
cin >> n >> m;
        // 記錄每點有幾個線段
        // 再一個紀錄,包含這個點的左界
        cnt[l]++;
cnt[r + 1]--;
       for (int i = 2; i <= n; i++)
    cnt[i] += cnt[i - 1];
for (int i = n; i >= 2; i--)
    lside[i - 1] = min(lside[i - 1], lside[i]);
vector<int> dp(n + 1);
dr[o] = 0;
        dp[0] = 0;
       dp[d] = 0;
for (int i = 1; i <= n; i++) {
    dp[i] = cnt[i];
    if (lside[i] != inf)
        dp[i] += dp[lside[i] - 1];
    dp[i] = max(dp[i], dp[i - 1]);
}</pre>
        cout << dp[n] << "\n";
 }
 // CF 1935 pC
 // 給你每個事件的 a, b, 挑事件會把 a 全部加起來
 // 再加上 max(bi) - min(bi)
void solve() {
   int n, k, ans = 0; cin >> n >> k;
        vector<pair<int, int>> v(n + 1);
for (int i = 1; i <= n; i++) {
   int a, b; cin >> a >> b;
   v[i] = {a, b};
   if (a <= k) ans = 1;</pre>
        sort(v.begin() +
             1, v.end(), [](pair<int, int> &a, pair<int, int> &b) {
return a.second < b.second;</pre>
       }); // 用 bi 來排,考慮第 i 個時可以先扣 vector<vector<int>> dp(n + 1, vector<int>(n + 1, inf)); // 考慮 v[i] 時,選 j 個的 sum(ai) - min(bi)
       for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
                       min(不選,選)
                              1][j - 1] + v[i].first + v[i].second <= k) {
                           // 假如可以選,更新 ans 時再加回去 bi
                          ans = max(ans, j);
             dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
        cout << ans << "\n";
```

10 Geometry

10.1 Basic [d41d8c]

```
template < class T>
struct Point {
    T x, y;
    Point(const T &x_ = 0, const T &y_ = 0) : x(x_), y(y_) {}
    template < class U>
    operator Point < U>() {
        return Point < U>(U(x), U(y));
    }
    Point &operator += (const Point &p) & {
            x += p.x; y += p.y; return *this;
    }
    Point &operator -= (const Point &p) & {
            x -= p.x; y -= p.y; return *this;
    }
    Point &operator *= (const T &v) & {
            x *= v; y *= v; return *this;
    }
    Point &operator /= (const T &v) & {
            x /= v; y /= v; return *this;
    }
    Point operator -() const {
            return Point(-x, -y);
    }
    friend Point operator + (Point a, const Point &b) {
            return a += b;
    }
}
```

```
friend Point operator - (Point a, const Point &b) {
          return a -= b;
     friend Point operator*(Point a, const T &b) {
          return a *= b;
     friend Point operator/(Point a, const T &b) {
          return a /= b;
     friend Point operator*(const T &a, Point b) {
    return b *= a;
     friend bool operator==(const Point &a, const Point &b) {
          return a.x == b.x && a.y == b.y;
     friend istream &operator>>(istream &is, Point &p) {
          return is >> p.x >> p.y;
     friend ostream & operator < <(ostream & os, const Point & p) {
    return os << "(" << p.x << ", " << p.y << ")";</pre>
template < class T>
T dot(const Point<T> &a, const Point<T> &b) {
     return a.x * b.x + a.y * b.y;
template < class T>
T cross(const Point<T> &a, const Point<T> &b) {
    return a.x * b.y - a.y * b.x;
template < class T>
T square(const Point < T > &p) {
     return dot(p, p);
template < class T>
double length(const Point < T > & p) {
    return sqrt(double(square(p)));
template < class T>
Point<T> normalize(const Point<T> &p) {
    return p / length(p);
template < class T>
Point<T> rotate(const Point<T> &a) {
     return Point(-a.y, a.x);
template < class T>
int sgn(const Point<T> &a) {
     return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
template < class T >
struct Line {
     Point<T>
     Point<T> b;
Line(const Point<T> &a_ = Point<T>()
           , const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
template < class T>
double length(const Line<T> &l) {
     return length(l.a - l.b);
template<class T>
bool parallel(const Line<T> &l1, const Line<T> &l2) {
   return cross(l1.b - l1.a, l2.b - l2.a) == θ;
double distance(const Point<T> &a, const Point<T> &b) {
     return length(a - b);
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)</pre>
     return distance(p, l.a);
if (dot(p - l.b, l.a - l.b) < 0)</pre>
          return distance(p, l.b);
     return distancePL(p, l);
template < class T>
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
     return cross(l.b - l.a, p - l.a) > 0;
Point < T
     > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
return l1.a + (l1.b - l1.a) * (cross(l2.b -
           l2.a, l1.a - l2.a) / cross(l2.b - l2.a, l1.a - l1.b));
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
     return cross(p - l.a, l.b - l.a) == 0 &&
    min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)</pre>
                (l.a.y, l.b.y) \ll p.y \ll max(l.a.y, l.b.y);
template < class T>
```

```
bool pointInPolygon
          (const Point<T> &a, const vector<Point<T>> &p) {
        int n = p.size(), t = 0;
for (int i = 0; i < n; i++)
    if (pointOnSegment(a, Line(p[i], p[(i + 1) % n])))</pre>
       return true;

for (int i = 0; i < n; i++) {

    auto u = p[i];

    auto v = p[(i + 1) % n];
                if (u.x < a.
                       x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
t ^= 1;
               return t == 1;
// 0 : strictly outside
// 1 : on boundary
// 2 : strictly inside template < class T>
int pointInConvexPolygon
         (const Point<T> &a, const vector<Point<T>> &p) {
        int n = p.size();
       if (n == 0) {
    return 0;
} else if (n <= 2) {</pre>
               return pointOnSegment(a, Line(p[0], p.back()));
        if (pointOnSegment(a, Line(p[0],
       p[1])) || pointOnSegment(a, Line(p[0], p[n - 1]))) {
   return 1;
} else if (pointOnLineLeft(a, Line(p[1],
        p[0])) || pointOnLineLeft(a, Line(p[0], p[n - 1]))) {
        int lo = 1, hi = n - 2;
       while (lo < hi) {
   int x = (lo + hi + 1) / 2;
   if (pointOnLineLeft(a, Line(p[0], p[x]))) {</pre>
                       lo = x;
               } else {
    hi = x - 1;
               }
        if (pointOnLineLeft(a, Line(p[lo], p[lo + 1]))) {
               return 2;
        } else {
               return pointOnSegment(a, Line(p[lo], p[lo + 1]));
template < class T>
bool lineIntersectsPolygon
          (const Line<T> &l, const vector<Point<T>> &p) {
        int n = p.size();
Point<T> a = l.a, b = l.b;
for (int i = 0; i < n; i++) {</pre>
               Line<T> seg(p[i], p[(i + 1) % n]);
               if (cross(b - a
    , seg.a - a) == 0 || cross(b - a, seg.b - a) == 0)
                       return true;
               if (cross(b
                       - a, seg.a - a) > 0 ^ cross(b - a, seg.b - a) > 0)
return true;
        return false:
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
tuple < int , Point < T > , Point < T >> segmentIntersection
       le<int, Point<T>, Point<T>> segmentIntersection
  (const line<T> &l1, const Line<T> &l2) {
  if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
    return {0, Point<T>(), Point<T>()};
  if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
    return {0, Point<T>(), Point<T>()};
  if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y))
    return {0, Point<T>(), Point<T>()};
  if (min(l1.a.y, l1.b.y) < max(l2.a.y, l2.b.y))
    return {0, Point<T>(), Point<T>()};
  if (cross(l1.b.y) > max(l2.a.y, l2.b.y))
    return {0, Point<T>(), Point<T>()};
  if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
        if (cross(l1.b - l1.a, l2.a - l1.a) != 0) {
            return {0, Point<T>(), Point<T>()};
        } else {
               } else {
                       auto maxx1 = max(l1.a.x, l1.b.x);
                       auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
auto miny1 = min(l1.a.y, l1.b.y);
                       auto miny1 = min(li.a.y, li.b.y),
auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.y, l2.b.y);
auto miny2 = min(l2.a.y, l2.b.y);
                       Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
if (!pointOnSegment(p1, l1))
                       swap(p1.y, p2.y);
if (p1 == p2) {
                               return {3, p1, p2};
                       } else {
```

```
return {2, p1, p2};
          }
     auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
     auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
     if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
          return {1, p, p};
     } else {
          return {3, p, p};
template < class T>
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
   if (get<0>(segmentIntersection(l1, l2)) != 0)
     return 0.0;
return min({distancePS(l1.a, l2), distancePS(l1
    .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
template < class T>
bool segmentInPolygon
      (const Line<T> &l, const vector<Point<T>> &p) {
     int n = p.size();
     if (!pointInPolygon(l.a, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
for (int i = 0; i < n; i++) {
    auto u = p[i];
    auto v = p[(i + 1) % n];
    auto w = p[(i + 2) % n];
}</pre>
          auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
if (t == 1) return false;
if (t == 0) continue;
          if (t == 2) {
               if (pointOnSegment(v, l) && v != l.a && v != l.b)
    if (cross(v - u, w - v) > 0)
        return false;
          if (pointOnLineLeft(l.a, Line(v, u))
                         || pointOnLineLeft(l.b, Line(v, u)))
               return false;
} else if (p1 == v) {
   if (l.a == v) {
                         if (pointOnLineLeft(u, l)) {
    if (pointOnLineLeft(w, l))
                                   && pointOnLineLeft(w, Line(u, v)))
                                   return false;
                         } else {
                              if (pointOnLineLeft(w, l)
                                   || pointOnLineLeft(w, Line(u, v)))
                                   return false:
                    } else if (l.b == v) {
   if (pointOnLineLeft(u, Line(l.b, l.a))) {
      if (pointOnLineLeft(w, Line(l.b, l.a)))
                                   && pointOnLineLeft(w, Line(u, v)))
                                   return false;
                         } else {
                              return false:
                    return false;
                         } else {
                              return false:
                         }
                    }
              }
          }
     return true:
template < class T>
vector<Point<T>> convexHull(vector<Point<T>> a) {
     sort(a.begin()
            a.end(), [](const Point<T> &l, const Point<T> &r) {
          return l.x == r.x ? l.y < r.y : l.x < r.x;
     a.resize(unique(a.begin(), a.end()) - a.begin());
     if (a.size() <= 1) return a;
vector < Point < T >> h(a.size() + 1);
     h[t++] = p;
          reverse(a.begin(), a.end());
```

```
return {h.begin(), h.begin() + t}:
template < class T>
vector<Point<T>> hp(vector<Line<T>> lines) {
    return cross(d1, d2) > 0;
     deaue<Line<T>> ls:
     deque<Point<T>> ps;
for (auto l : lines) {
          if (ls.empty())
                ls.push_back(l);
                continue:
          while (!ps.empty() && !pointOnLineLeft(ps.back(), l))
    ps.pop_back(), ls.pop_back();
while (!ps.empty() && !pointOnLineLeft(ps[0], l))
          ps.pop_front(), ls.pop_front();
if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
                if (dot
                      (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                     if (!pointOnLineLeft(ls.back().a, l)) {
                          assert(ls.size() == 1);
                          ls[0] = l;
                     continue;
                return {};
          ps.push back(lineIntersection(ls.back(), l)):
          ls.push_back(l);
    while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0]))
    ps.pop_back(), ls.pop_back();
if (ls.size() <= 2) return {};
ps.push_back(lineIntersection(ls[0], ls.back()));</pre>
     return vector(ps.begin(), ps.end());
using P = Point<ll>:
```

10.2 Min Euclidean Distance [478e73]

```
void minEuclideanDistance() {
     int n; cin >> n;
constexpr ll inf = 8E18;
      vector<Point<ll>> a(n);
     for (int i = 0; i < n; i++) {
    ll x, y;
    cin >> x >> y;
           a[i] = Point < ll>(x, y);
     struct sortY {
           bool operator
     ()(const Point<ll> &a, const Point<ll> &b) const {
                 return a.y < b.y;</pre>
     struct sortXY {
           bool operator
()(const Point<ll> &a, const Point<ll> &b) const {
                 return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
     f;
sort(a.begin(), a.end(), sortXY());
vector < Point < ll >> t(n);
auto devide = [&](auto &&self, int l, int r) -> ll {
    if (l == r) return inf;
    int m = (l + r) / 2;
    ll ans = min(self(self, l, m), self(self, m + 1, r));
    ll midual = a[m] v:
           ll midval = a[m].x;
           ll p = 0;
for (int i = l; i <= r; i++)</pre>
           if ((t[i].y
                               t[j].y) * (t[i].y - t[j].y) > ans) break;
                }
           return ans:
     }:
     cout << devide(devide, 0, n - 1) << "\n";</pre>
```

10.3 Max Euclidean Distance [4aa1f0]

```
template < class T >
tuple < T, int, int > maxEuclideanDistance(vector < Point < T >> a) {
    auto get = [&](const Point < T > &p, const Line < T > &l) -> T {
        return abs(cross(l.a - l.b, l.a - p));
    };
    T res = 0; int n = a.size(), x, y, id = 2;
    a.push_back(a.front());
    if (n <= 2) return {square(a[0] - a[1]), 0, 1};
    for (int i = 0; i < n; i++) {</pre>
```

```
while (get(a[id], Line(a[i], a[i + 1])
        ) <= get(a[(id + 1) % n], Line(a[i], a[i + 1])))
        id = (id + 1) % n;
    if (res < square(a[i] - a[id])) {
        res = square(a[i] - a[id]);
        x = i, y = id;
    }
    if (res < square(a[i + 1] - a[id])) {
        res = square(a[i + 1] - a[id]);
        x = i + 1, y = id;
    }
}
return {res, x, y};
}</pre>
```

10.4 Lattice Points [46d224]

10.5 Min Circle Cover [9380bf]

10.6 Min Rectangle Cover [8bd345]

11 Polynomial

11.1 FFT [e258ad]

```
const double PI = acos(-1.0);
using cd = complex < double >;
vector < int > rev;
 void fft(vector<cd> &a, bool inv) {
          int n = a.size();
          if (int(rev.size()) != n) {
   int k = __builtin_ctz(n) - 1;
   rev.resize(n);
                   for (int i = 0; i < n; i++)
    rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;</pre>
         for (int i = 0; i < n; i++)
    if (rev[i] < i)
        swap(a[i], a[rev[i]]);
for (int k = 1; k < n; k *= 2) {
    double ang = (inv ? -1 : 1) * PI / k;
    cd wn(cos(ang), sin(ang));
    for (int i = 0; i < n; i += 2 * k) {
        cd w(1);
    }
}</pre>
                             cd w(1);
                             for (int j = 0; j < k; j++, w = w * wn) {
    cd u = a[i + j];
    cd v = a[i + j + k] * w;</pre>
                                       a[i + j] = u + v;
a[i + j + k] = u - v;
                   }
          if (inv) for (auto &x : a) x /= n;
template < class T>
remplate <ctass 1>
vector <T> Multiple(const vector <T> &a, const vector <T> &b) {
   vector <cd> fa(a.begin(), a.end()), fb(b.begin(), b.end());
   int n = 1, tot = a.size() + b.size() - 1;
   while (n < tot) n *= 2;</pre>
          fa.resize(n), fb.resize(n);
fft(fa, false), fft(fb, false);
for (int i = 0; i < n; i++)
    fa[i] = fa[i] * fb[i];</pre>
         fft(fa, true);
vector<T> res(tot);
for (int i = 0; i < tot; i++)
    res[i] = fa[i].real(); // use llround if need</pre>
          return res:
```

11.2 NTT [065a5b]

```
template < int V, ll P>
Mint < P > CInv = Mint < P > (V).inv();
template < ll P >
vector < Mint < P >> roots { 0, 1 };
template < int P>
Mint<P> findPrimitiveRoot() {
     Mint<P> i =
     int k = __builtin_ctz(P - 1);
while (true) {
          if (power(i, (P - 1) / 2) != 1) break;
     return power(i, (P - 1) >> k);
template < ll P >
Mint<P> primitiveRoot = findPrimitiveRoot<P>();
template <>
Mint<998244353> primitiveRoot<998244353> {31}:
template < ll P>
void dft(vector<Mint<P>> &a) {
     int n = a.size();
     if (int(rev.size()) != n) {
          int k = __builtin_ctz(n) - 1;
rev.resize(n);
for (int i = 0; i < n; i++)
    rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;</pre>
```

```
for (int i = 0; i < n; i++)
    if (rev[i] < i) swap(a[i], a[rev[i]]);
if (roots<P>.size() < n) {
    int k = __builtin_ctz(roots<P>.size());
    roots<P>.resize(n);
    ith interpolation of the content of the c
                        k++:
                        }
           a[i + j] = u + v;
a[i + j + k] = u - v;
                                   }
                      }
          }
}
template < ll P >
void idft(vector<Mint<P>> &a) {
           int n = a.size();
reverse(a.begin() + 1, a.end());
           dft(a);
Mint<P> inv = (1 - P) / n;
for (int i = 0; i < n; i++) a[i] *= inv;</pre>
template < ll P = 998244353>
struct Poly : public vector<Mint<P>>> {
    using Value = Mint<P>;
           Poly() : vector<Value>() {}
explicit Poly(int n) : vector<Value>(n) {}
            explicit Poly(const vector<Value> &a) : vector<Value>(a) {}
            Poly(const
                            initializer_list<Value> &a) : vector<Value>(a) {}
            template < class InputIt, class = _RequireInputIter < InputIt >>
explicit Poly(InputIt
                             first, InputIt last) : vector<Value>(first, last) {}
            template < class F>
            Poly shift(int k) const {
                       if (k >= 0) {
    auto b = *this;
    b.insert(b.begin(), k, 0);
                                    return b;
                       } else if (this->size() <= -k) {
    return Poly();</pre>
                        } else {
                                    return Poly(this->begin() + (-k), this->end());
                        }
            Poly trunc(int k) const {
    Poly f = *this;
    f.resize(k);
                        return f
            friend Poly operator+(const Poly &a, const Poly &b) {
  Poly res(max(a.size(), b.size()));
                        for (int i = 0; i < a.size(); i++)
    res[i] += a[i];
for (int i = 0; i < b.size(); i++)</pre>
                                    res[i] += b[i];
                        return res:
            friend Poly operator-(const Poly &a, const Poly &b) {
                        Poly res(max(a.size(), b.size()));

for (int i = 0; i < a.size(); i++)

res[i] += a[i];
                        for (int i = 0; i < b.size(); i++)
    res[i] -= b[i];
return res;</pre>
            friend Poly operator (const Poly &a) {
                        vector<Value> res(a.size());
for (int i = 0; i < int(res.size()); i++)
    res[i] = -a[i];</pre>
                        return Poly(res);
            friend Poly operator*(Poly a, Poly b) {
  if (a.size() == 0 || b.size() == 0)
    return Poly();
                       return Poly();
if (a.size() < b.size()) swap(a, b);
int n = 1, tot = a.size() + b.size() - 1;
while (n < tot) n *= 2;
if (((P - 1) & (n - 1)) != 0 || b.size() < 128) {
   Poly c(a.size() + b.size() - 1);
   for (int i = 0; i < a.size(); i++)
        for (int j = 0; j < b.size(); j++)
        c[i + j] += a[i] * b[j];
```

```
return c:
      f
a.resize(n), b.resize(n);
dft(a), dft(b);
for (int i = 0; i < n; ++i)
    a[i] *= b[i];</pre>
      idft(a);
a.resize(tot);
      return a;
friend Poly operator*(Value a, Poly b) {
    for (int i = 0; i < int(b.size()); i++)
        b[i] *= a;</pre>
      return b:
friend Poly operator*(Poly a, Value b) {
    for (int i = 0; i < int(a.size()); i++)
        a[i] *= b;</pre>
friend Poly operator/(Poly a, Value b) {
    for (int i = θ; i < int(a.size()); i++)
        a[i] /= b;</pre>
      return a:
Poly & operator += (Poly b) {
    return (*this) = (*this) + b;
Poly & operator -= (Poly b) {
    return (*this) = (*this) - b;
Poly & operator *= (Poly b) {
      return (*this) = (*this) * b;
Poly &operator*=(Value b) {
      return (*this) = (*this) * b;
Poly &operator/=(Value b) {
    return (*this) = (*this) / b;
Polv deriv() const {
      if (this->empty()) return Poly();
      Poly res(this->size() - 1);

for (int i = 0; i < this->size() - 1; ++i)

res[i] = (i + 1) * (*this)[i + 1];
      return res;
Poly integr() const {
      Poly res(this->size() + 1);

for (int i = 0; i < this->size(); ++i)

res[i + 1] = (*this)[i] / (i + 1);
Polv inv(int m) const {
      Poly x{(*this)[0].inv()};
      int k = 1;
while (k < m) {
    k *= 2;</pre>
             x = (x * (Poly{2} - trunc(k) * x)).trunc(k);
      return x.trunc(m);
Poly log(int m) const {
    return (deriv() * inv(m)).integr().trunc(m);
Poly exp(int m) const {
     Poly x{1};
int k = 1;
while (k < m) {
k *= 2;
             x = (x * (Poly{1} - x.log(k) + trunc(k))).trunc(k);
      return x.trunc(m);
Poly pow(int k, int m) const {
      int i = 0;
while (i < this->size() && (*this)[i] == 0) i++;
if (i == this->size() || 1LL * i * k >= m)
      return Poly(m);
Value v = (*this)[i];
auto f = shift(-i) *
                                        v.inv();
      return (f.log(m - i * k) * k) * k).exp(m - i * k).shift(i * k) * power(v, k);
Poly sqrt(int m) const {
      Poly x{1};
int k = 1;
      while (k < m) {
    k *= 2;
            x = (x +
                      (trunc(k) * x.inv(k)).trunc(k)) * CInv<2, P>;
      return x.trunc(m):
Poly mulT(Poly b) const {
     if (b.size() == 0) return Poly();
int n = b.size();
reverse(b.begin(), b.end());
return ((*this) * b).shift(-(n - 1));
vector<Value> eval(vector<Value> x) const {
      if (this->size() == 0)
```

```
return vector < Value > (x.size(). 0):
           const int n = max(x.size(), this->size());
vector<Poly> q(4 * n);
           vector < Value > 'ans(x.size());
           x.resize(n):
           function < void(</pre>
                int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
                     q[p] = Poly(1, -x[l]);
               qlpj = .c.,
} else {
  int m = (l + r) / 2;
  build(2 * p, l, m);
  build(2 * p + 1, m, r);
  q[p] = q[2 * p] * q[2 * p + 1];
}
          ans[l] = num[0];
               m, num.mulT(q[2 * p + 1]).resize(m - l));
work(2 * p + 1,
                            m, r, num.mulT(q[2 * p]).resize(r - m));
          };
           work(1, 0, n, mulT(q[1].inv(n)));
    }
}:
template < ll P = 998244353>
Poly<P> berlekampMassey(const Poly<P> &s) {
     Poly<P> c, oldC;
     if (f == -1) {
          c.resize(i + 1);
f = i;
} else {
                auto d = oldC;
d *= -1;
                d.insert(d.begin(), 1);
                auto coef = delta / df1;
d *= coef;
                Poly<P> zeros(i - f - 1);
                zeros.insert(zeros.end(), d.begin(), d.end());
                d = zeros;
                auto temp = c:
                if (i - temp.size() > f - oldC.size()) {
    oldC = temp;
                     f = i;
               }
          }
     c *= -1;
     c.insert(c.begin(), 1);
template < ll P = 998244353>
Mint<P> linearRecurrence(Poly<P> p, Poly<P> q, ll n) {
    t<P> linearRecurrence(Poly<P> p, Poly
int m = q.size() - 1;
while (n > 0) {
    auto newq = q;
    for (int i = 1; i <= m; i += 2)
        newq[i] *= -1;
    auto newp = p * newq;
    newq = q * newq;
    for (int i = 0; i < m; i++)
        p[i] = newp[i * 2 + n % 2];
    for (int i = 0; i <= m; i++)
        q[i] = newq[i * 2];
    n /= 2;</pre>
          n /= 2;
     return p[0] / q[0];
```

12 Else

12.1 Python [6f660a]

```
| from decimal import * # 無誤差浮點數
| from fractions import * # 分數
| from random import *
| from math import *
| # set decimal prec if it could overflow in precision
| setcontext(Context(prec=10, rounding=ROUND_FLOOR))
```

```
# read and print
x = int(input())
a, b, c = list(map(Fraction, input().split()))
arr = list(map(Decimal, input().split()))
print(x)
print(a, b, c)
print(*arr)
# set
S = set(); S.add((a, b)); S.remove((a, b))
if not (a, b) in S:
# dict
D = dict(); D[(a, b)] = 1; del D[(a, b)]
for (a, b) in D.items():
# random
arr = [randint(l, r) for i in range(size)]
choice([8, 6, 4, 1]) # random pick one
shuffle(arr)
```

12.2 Big Number [6ff5e4]

```
struct BigNum { // require Mint and NTT ~idft
       deque<int> x:
       BigNum() : x {0}, sgn(1) {}
BigNum(deque<int> x, int sgn = 1) : x(norm(x)), sgn(sgn) {
       BigNum(string s) {
             if (s.empty()) {
    *this = BigNum();
} else if (s[0] == '-') {
                    sgn = -1;
for (auto &c : s) x.push_back(c - '0');
                    x.pop_front();
             } else {
                    sgn = 1;
                    for (auto &c : s) x.push_back(c - '0');
             x = norm(x);
       void resign() {
             sgn = x[0] == 0 ? 1 : sgn;
       int cmp(const
             deque<int> &a, const deque<int> &b) const { // abs cmp
if (a.size() != b.size()) {
                    return a.size() - b.size();
                    return (a < b ? -1 : 1);
             }
       deque < int > norm(deque < int > s) {
    if (s.empty()) return s = {0};
    for (int i = s.size() - 1; i >= 0; i--) {
                     int c = s[i];
                    tht = s[t],
s[i] = c % 10;
c /= 10;
if (c) {
   if (i == 0) s.push_front(c), i++;
   else s[i - 1] += c;
              while (s.size() > 1 && s.front() == 0) s.pop_front();
       deque < int > Add(deque < int > a, deque < int > b) {
   int i = a.size() - 1, j = b.size() - 1;
             deque<int> res;
while (i >= 0 || j >= 0) {
   int x = i >= 0 ? a[i] : 0, y = j >= 0 ? b[j] : 0;
                     res.push_front(x + y);
       deque<int> Minus(deque<int> a, deque<int> b) {
   int i = a.size() - 1, j = b.size() - 1;
              deque<int> res;
             while (i >= 0) {
   int x = a[i], y = j >= 0 ? b[j] : 0;
   if (x < y) x += 10, a[i - 1]--;</pre>
                     res.push_front(x - y);
                    i--, j--;
              return res;
       J
vector < Z > Multiple(vector < Z > a , vector < Z > b) {
    if (a.size() < b.size()) swap(a, b);
    int n = 1, tot = a.size() + b.size() - 1;
    while (n < tot) n *= 2;
    if (((P - 1) & (n - 1)) != 0 || b.size() < 128) {</pre>
                    for (int j = 0; j < b.size(); j++)
for (int j = 0; j < b.size(); j++)</pre>
                                 c[i + j] += a[i] * b[j];
                    return c;
             }
             fa.resize(n), b.resize(n);
dft(a), dft(b);
for (int i = 0; i < n; i++) a[i] *= b[i];
idft(a);</pre>
             a.resize(tot);
```

```
return a;
BigNum operator -() const {
    return BigNum(x, -sgn);
BigNum & operator += (const BigNum &rhs) & {
     if (sgn == 1) {
   if (rhs.sgn == -1) {
                (rns.sgn == -1) {
  if (cmp(x, rhs.x) < 0) {
    sgn = -1, x = Minus(rhs.x, x);
  }
  else {
    sgn = 1, x = Minus(x, rhs.x);
}</pre>
          } else {
   sgn = 1, x = Add(x, rhs.x);
          }
     } else {
   if (rhs.sgn == -1) {
          sgn = -1, x = Add(x, rhs.x);
else {
   if (cmp(x, rhs.x) <= 0) {
      sgn = 1, x = Minus(rhs.x, x);
}</pre>
                sgn = 1, x = Mthus(fis.x, x);
} else {
   sgn = -1, x = Minus(x, rhs.x);
          }
     }
x = norm(x), resign();
return *this;
BigNum &operator -= (const BigNum &rhs) & {
    return *this += -rhs;
}
friend BigNum operator+(BigNum lhs, BigNum rhs) {
     return lhs += rhs;
}
friend BigNum operator-(BigNum lhs, BigNum rhs) {
     return lhs -= rhs;
}
friend BigNum operator*(BigNum lhs, BigNum rhs) {
    return lhs *= rhs;
friend istream &operator>>(istream &is, BigNum &a) {
   string v; is >> v; a = BigNum(v); return is;
for (auto x : a.x) os << x;</pre>
     return os;
```