Contents

```
6 Math
                                                             10
  Basic
                                   6.1 Prime . . . . . . . . . . . . . 10
  1.1 Install VScode . . . . . . .
                                   6.2 Modulo . . . . . . . . . . . 10
  6.3 Combination . . . . . . . . 11
                                   2 Graph
  2.1 DFS And BFS . . . . . . . . .
                                   6.9 Catalan Theorem .... 12
  6.10 Burnside's Lemma . . . . . 12
  2.4 FloydWarshall . . . . . .
                                7 Search and Gready 12
7.1 Binary Search . . . . . 12
7.2 Ternary Search . . . . . 12
  2.5 Euler . . . . . . . . . . .
  2.6 SCC . . . . . . . . . . . . . .
      VBCC . . . . . . . . . . . . . .
  2.7
  2.8 EBCC . . . . . . . . . . . .
                                  Тгее
                                8
                                   2.9 2-SAT . .
  2.10 Funtional Graph . . . . . .
                                      Tree Flattening . . . .
                                   8.3
3 Data Structure
                                   8.4 Heavy Light Decomposition 13
                                   3.1 BIT . .
  3.2 RangeBit . . . . . . . . . .
  3.3 DSU . . . . . . . . . . . .
  3.4 Segment . . . . . . . . . .
  3.5 Lazy Segment . . . . . . .
                                  DP
      Treap . . . . . . . . . . . . . . . . . .
                                   9.1 LCS . . . . . . . . . . . . . 15
                                   3.7 Mo . . . . . . . . . . . . . . .
  9.6 Removal Game . . . . . .
                                                             16
                                   9.7 CHT . . . . . . . . . . . . 16 9.8 DNC . . . . . . . . . . . . 16
                                   MCMF .......
  String
  10 Geometry
  5.3 Z Function . . . . . . . .
                                   5.4 SA . . . . . . . . . . . . . . .
  5.5 SAM . . .
                                   10.3 MinEuclideanDistance . . 19
  5.6 Duval Algorithm . . . . . 9
5.7 Manacher . . . . . . . 10
```

5.8 Trie 10

1 Basic

1.1 Install VScode [d41d8c]

1.2 Default Code [d41d8c]

```
#include <bits/stdc++.h>
// #pragma GCC target("popcnt")
// C++ 20 vector grammer will not work
#define all(x) (x).begin(), (x).end()
using namespace std;
using ll = long long;

void solve() {
}

int main() {
    ios_base::sync_with_stdio(false);
    cin.tie(nullptr);
    int t = 1;
    cin >> t;
    while (t--) {
        solve();
    }
}
```

1.3 Compare Fuction [d41d8c]

```
// 如果有自定義比較結構就比照以上
};
struct cmp {
                     // 要在 template 的資結用外部變數
     vector<int> &v;
     cmp(vector<int>& vec) : v(vec) {}
bool operator() (int a, int b) const {
   return v[a] > v[b];
// mutil: cmp cmp1(vector);
// priority_queue<int, vector<int>, cmp> pq(cmp1);
};
1.4 Pbds [d41d8c]
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < typename T >
using pbds_set = tree<T, null_type,</pre>
        less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template < typename T>
using pbds_multiset = tree<T, null_type, less_equal</pre>
      <T>, rb_tree_tag, tree_order_statistics_node_update>;
1.5 Double [b44e11]
struct D {
     double x;
     constexpr static double eps = 1e-12;
     constexpr static double eps = 1e-12;
D() : x{0.0} {}
D(double v) : x{v} {}
double val() const { return x; }
explicit operator double() const { return x; }
D operator-() const {
           return D(-x);
     D & operator += (const D & rhs) & {
           x += rhs.x; return *this;
     D & operator -= (const D & rhs) & {
           x -= rhs.x; return *this;
     D & operator *= (const D & rhs) & {
           x *= rhs.x; return *this;
     D & operator/=(const D &rhs) & {
    assert(fabs(rhs.x) > eps);
    x /= rhs.x; return *this;
      friend D operator+(D lhs, const D &rhs) {
           return lhs += rhs;
      friend D operator - (D lhs, const D &rhs) {
           return lhs -= rhs;
      friend D operator*(D lhs, const D &rhs) {
           return lhs *= rhs;
      friend D operator/(D lhs, const D &rhs) {
          return lhs /= rhs;
     friend bool operator<(const D &lhs, const D &rhs) {
   return lhs.x - rhs.x < -eps;</pre>
     friend bool operator > (const D &lhs, const D &rhs) {
   return lhs.x - rhs.x > eps;
      friend bool operator == (const D &lhs, const D &rhs) {
           return fabs(lhs.x - rhs.x) < eps;</pre>
     friend bool operator <= (const D &lhs, const D &rhs) {
   return lhs < rhs || lhs == rhs;</pre>
      friend bool operator>=(const D &lhs, const D &rhs) {
           return lhs > rhs || lhs == rhs;
      friend bool operator!=(const D &lhs, const D &rhs) {
           return !(lhs == rhs);
      friend istream &operator>>(istream &is, D &a) {
           double v; is >> v; a = D(v); return is;
      friend ostream &operator<<(ostream &os, const D &a) {</pre>
     return os << fixed << setprecision(10) << a.val() + (a.val() > 0 ? eps : a.val() < 0 ? -eps : 0); } // eps should < precision
```

2 Graph

};

2.1 DFS And BFS [e2d856]

```
int main() {
    int n;
    vector<vector<int>> adj(n);
    // dfs_graph
    vector<bool> vis(n);
    auto dfs = [&](auto self, int u) -> void {
        if (vis[u]) return;
        vis[u] = true;
        for (auto v: adj[u]) {
```

```
self(self, v);
}

};
dfs(dfs, 0);
// bfs

vector<int> depth(n, 1e9);
queue<int> q;
auto bfs = [&](auto self, int s) -> void {
    vis[s] = true, depth[s] = 0;
    q.push(s);
    while (!q.empty()) {
        int u = q.front(); q.pop();
        for (auto v : adj[u]) {
            if (vis[v]) continue;
            vis[v] = true;
            depth[v] = depth[u] + 1;
            q.push(v);
        }
}

};
bfs(bfs, 0);
}
```

2.2 Prim [3a3805]

2.3 BellmanFord [430ded]

```
|// 用 Bellman Ford 找負環
int main() {
    int n, m; cin >> n >> m;
    vector <array <int, 3>> e;
    for (int i = 0; i < m; i++) {
        int u, v, w; cin >> u >> v >> w;
        u--, v--; e.push_back({u, v, w});
    }
    vector <ll>    dis(n, inf), par(n);
    int t = -1; dis[0] = 0;
    for (int i = 1; i <= n; i++) {
        for (auto [u, v, w] : e) {
            if (dis[v] > dis[u] + w) {
                 dis[v] = dis[u] + w;
                 par[v] = u;
                 if (i == n) t = v;
                 }
        }
        if (t == -1) { cout << "NO\n"; return; }
        for (int i = 1; i < n; i++) t = par[t];
        vector <int > ans {t};
        int i = t;
        do {
            i = par[i];
                 ans.push_back(i);
        } while (i != t);
        reverse(ans.begin(), ans.end());
        cout << "YES\n";
        for (auto x : ans) cout << x + 1 << " ";
}
```

2.4 FloydWarshall [3a24ad]

```
const int inf = 1e18;
int main() {
    int n, m, q; cin >> n >> m >> q;
    vector <vector <int>> graph(n, vector <int>(n, inf));
    vector <vector <int>> dis(n, vector <int>(n));
    for (int i = 0; i < m; i++) {
        int u, v, w; cin >> u >> v >> w;
        graph[u][v] = min(graph[u][v], w);
        graph[v][u] = min(graph[v][u], w);
    }
    for (int i = 0; i < n; i++) {
        for(int j = 0; j < n; j++) {
            dis[i][j] = graph[i][j];
        }
    }
    for (int i = 0; i < n; i++) // 自己到自己是 0
        dis[i][i] = 0;
    for (int k = 0; k < n; k++) {
        for (int i = 0; i < n; i++) {</pre>
```

2.5 Euler [4177dc]

```
/// 1. 無向圖是歐拉圖:
// 非零度頂點是連通的
// 頂點的度數都是偶數
// 2. 無向圖是半歐拉圖(有路沒有環):
// 非零度頂點是連通的
// 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
| // 非零度頂點是強連通的
// 每個頂點的入度和出度相等
// 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
// 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
 ...
// 其他頂點的入度和出度相等
vector<int> ans;
auto dfs = [&](auto &&self, int u) -> void {
    while (g[u].size()) {
   int v = *g[u].begin();
   g[u].erase(v);
        self(self, v);
    ans.push_back(u);
dfs(dfs, 0);
reverse(ans.begin(), ans.end());
```

2.6 SCC [5d3e16]

```
struct SCC {
      int n, cur, cnt;
vector<vector<int>> adj;
      vector < int > stk, dfn, low, bel;
SCC(int n = 0) { init(n); }
void init(int n) {
           n = n_;
adj.assign(n, {});
            dfn.assign(n,
            low.resize(n);
           bel.assign(n,
            stk.clear():
           cur = cnt = 0;
      void addEdge(int u, int v) {
           adj[u].push_back(v);
      void dfs(int x) {
    dfn[x] = low[x] = cur++;
            stk.push_back(x);
           for (auto y : adj[x]) {
    if (dfn[y] == -1) {
                       dfs(y);
                 low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
            if (dfn[x] == low[x]) {
                  int y;
                  do {
                       y = stk.back();
bel[y] = cnt;
                       stk.pop_back();
                 } while (y != x);
           }
      for (int i = 0; i < n; i++) {
    if (dfn[i] == -1) dfs(i);</pre>
            return bel:
      struct Graph {
            int n:
            vector<pair<int, int>> edges;
           vector < int > siz;
vector < int > cnte;
      Graph compress() {
           Graph g;
g.n = cnt;
            g.siz.resize(cnt);
```

```
g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;
    for (auto j : adj[i]) {
        if (bel[i] != bel[j]) {
            g.edges.emplace_back(bel[i], bel[j]);
        } else {
            g.cnte[bel[i]]++;
        }
    }
   return g;
}</pre>
```

2.7 VBCC [170604]

```
struct VBCC {
      int n, cur;
      vector < int >> adj;
      vector < int > dfn, low, parent;
vector < bool > is_cut;
      VBCC(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_;
            adj.assign(n, {});
            dfn.assign(n, -1);
low.resize(n);
            parent.assign(n, -1);
            is_cut.assign(n, false);
            cur = 0:
      void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
     void dfs(int x) {
   int children = 0;
   dfn[x] = low[x] = cur++;
            for (int v : adj[x]) {
   if (dfn[v] == -1) {
                       children++;
                        parent[v] = x;
                        dfs(v);
low[x] = min(low[x], low[v]);
                       if (parent[x] != -1 && low[v] >= dfn[x]) {
    is_cut[x] = true;
                 } else if (v != parent[x]) {
    low[x] = min(low[x], dfn[v]);
            if (parent[x] == -1 && children > 1) {
    is_cut[x] = true;
            }
     }
     }
};
```

2.8 EBCC [59d8ca]

```
struct EBCC { // CF/contest/1986/pF
      int n, cur, cnt;
vector<vector<int>> adj;
      vector<int> stk, dfn, low, bel;
      vector<pair<int, int>> bridges; // 關鍵邊
EBCC(int n_ = 0) { init(n_); }
      void init(int n_) {
           n = n_;
adj.assign(n, {});
            dfn.assign(n, -1);
            low.resize(n);
            bel.assign(n, -1);
            stk.clear();
            bridges.clear();
            cur = cnt = 0;
      void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
     void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
            stk.push_back(x);
            for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
                        dfs(y, x);
low[x] = min(low[x], low[y]);
if (low[y] > dfn[x]) {
                              bridges.emplace_back(x, y);
                  } else if (bel[y] == -1) {
    low[x] = min(low[x], dfn[y]);
```

```
if (dfn[x] == low[x]) {
              int y;
do {
                  y = stk.back();
                  bel[y] = cnt;
             stk.pop_back();
} while (y != x);
         }
     for (int i = 0; i < n; i++) {
    if (dfn[i] == -1) {
        dfs(i, -1);
    }
}</pre>
         return bel;
     struct Graph {
         int n:
         vector<pair<int, int>> edges;
         vector<int> siz; // BCC 內節點數
         vector<int> cnte; // BCC 內邊數
     Graph compress() {
         Graph g;
         a.n = cnt:
         g.siz.resize(cnt);
         g.cnte.resize(cnt);
         for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;</pre>
              g.cnte[bel[i]]++;
              }
         return g;
    }
};
```

2.9 2-SAT [eeddc1]

```
// CSES Giant Pizza
struct TwoSat {
     int n; vector<vector<int>> e;
vector<body>
vector<body>
void addClause(int u, bool f, int v, bool g) {
        e[2 * u + !f].push_back(2 * v + g);
        e[2 * v + !g].push_back(2 * u + f);
}
      bool satisfiable() {
           vector<int> stk;
           int now = 0, cnt = 0;
function<void(int)> tarjan = [&](int u) {
                 stk.push_back(u);
                 dfn[u] = low[u] = now++;
for (auto v : e[u]) {
                       if (dfn[v] ==
                             tarjan(v);
                       low[u] = min(low[u], low[v]);

else if (id[v] == -1) { // in s
low[u] = min(low[u], dfn[v]);
                 if (dfn[u] == low[u]) {
                       int v;
                       do {
                             v = stk.back();
                            stk.pop_back();
id[v] = cnt;
                       } while (v != u);
                       ++cnt;
                }
           for (int i
           return true;
      vector < bool > answer() { return ans; }
int main() {
      int m, n; cin >> m >> n;
TwoSat ts(n);
      for (int i = 0; i < m; ++i) {</pre>
           int u, v; char x, y;
cin >> x >> u >> y >> v;
ts.addClause(u - 1, x == '+', v - 1, y == '+');
      if (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";</pre>
```

```
else cout << "IMPOSSIBLE\n";</pre>
}
2.10 Funtional Graph [85c464]
constexpr int N = 2e5 + 5;
int cht[N][31]; // 倍增表, 放外面不然 TLE struct FuntionalGraph {
      int n, cnt;
vector < int > g, bel, id, len, in, top;
FuntionalGraph() : n(0) {}
      FuntionalGraph(vector<int> g_) { init(g_); }
      void init(vector<int> g_) {
    n = g_.size(); cnt = 0;
            g = g_{,} bel.assign(n, -1);
            id.resize(n); len.clear();
in.assign(n, 0); top.assign(n, -1);
            build();
     for (int i = 1; i <= 30; i++)
                  for (int u = 0; u < n; u++)
    cht[u][i] = cht[cht[u][i - 1]][i - 1];</pre>
            for (int i = 0; i < n; i++)
   if (in[i] == 0) label(i);
for (int i = 0; i < n; i++)</pre>
                  if (top[i] == -1) label(i);
      void label(int u) {
    vector<int> p; int cur = u;
            while (top[cur] == -1) {
                  top[cur] = u;
p.push_back(cur);
                  cur = g[cur];
            auto s = std::find(p.begin(), p.end(), cur);
            vector <int> cyc(s, p.end());
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {
    bel[cyc[i]] = cnt;
}</pre>
                  id[cyc[i]] = i;
            cnt++; len.push_back(cyc.size());
            for (int i = p.size() - 1; i > 0; i--)
   id[p[i - 1]] = id[p[i]] - 1;
      int jump(int u, int k) {
   for (int b = 0; k > 0; b++){
      if (k & 1) u = cht[u][b];
            return u:
```

Data Structure

3.1 BIT [d41d8c]

};

```
struct Fenwick { // 全部以 0 based 使用
int n; vector<T> a;
Fenwick(int n_ = 0) { init(n_); }
void init(int n_) {
            n = n_;
             a.assign(n, T{});
      void add(int x, const T &v) {
   for (int i = x + 1; i <= n; i += i & -i) {
      a[i - 1] = a[i - 1] + v;
}</pre>
      T sum(int x) { // 左閉右開查詢
             T ans{};
for (int i = x; i > 0; i -= i & -i) {
   ans = ans + a[i - 1];
             return ans;
      T rangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
      int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
            int x = 0;
T cur{};
for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n && cur + a[x + i - 1] <= k) {</pre>
                         `x += i;
                         cur = cur + a[x - 1];
                  }
             return x;
      }
template <class T>
```

```
struct TwoDFenwick { // 全部以 θ based 使用
int nx, ny; // row, col 個數
vector<vector<T>>> a;
        TwoDFenwick(int nx_ = 0, int ny_ = 0) {
              init(nx_, ny_);
        void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
        void add(int x, int y, const T &v) {
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            a[i - 1][j - 1] = a[i - 1][j - 1] + v;
        }
}</pre>
               }
        T sum(int x, int y) { // 左閉右開查詢
               Im(int x, s...),
T ans{};
for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans + a[i - 1][j - 1];
}
               return ans;
        T rangeSum
                 (int lx, int ly, int rx, int ry) { // 左閉右開查詢
               return sum(
    rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
};
```

3.2 RangeBit [d41d8c]

```
template <typename T>
  struct rangeFenwick { // 全部以 0 based 使用
         int n;
vector<T> d, di;
rangeFenwick(int n_ = 0) { init(n_); }
         void init(int n_) {
                n = n_;
d.assign(n, T{});
di.assign(n, T{});
         Joid add(int x, const T &v) {
   T vi = v * (x + 1);
   for (int i = x + 1; i <= n; i += i & -i) {
      d[i - 1] = d[i - 1] + v;
      di[i - 1] = di[i - 1] + v;
}</pre>
         void rangeAdd(int l, int r, const T &v) {
  add(l, v); add(r, -v);
         T sum(int x) { // 左閉右開查詢
  T ans{};
  for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
         TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
         int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
                int x = 0;
T cur{};
                for (int i = 1 << __lg(n); i; i /= 2) {
   if (x + i <= n) {
        T val = T(</pre>
                               x + i + 1) * d[x + i - 1] - di[x + i - 1];
if (cur + val <= k) {
 x += i;
                                       cur = cur + val;
                      }
                return x;
        }
 template <class T>
  struct rangeTwoDFenwick { // 全部以 0 based 使用
         int nx, ny; // row, col 個數
vector<vector<T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
                init(nx_, ny_);
         void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
                di.assign(nx, vector<T>(ny, T{}));
dj.assign(nx, vector<T>(ny, T{}));
dij.assign(nx, vector<T>(ny, T{}));
         T void add(int x, int y, const T &v) {
   T vi = v * (x + 1);
   T vj = v * (y + 1);
   T vij = v * (x + 1) * (y + 1);
```

```
National Chung Cheng University Salmon
           for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        d[i - 1][j - 1] = d[i - 1][j - 1] + v;
        di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
        dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;</pre>
                      dij[i - 1][j - 1] = dij[i -
                                                                        1] +
                }
          }
     void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
          add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
     T sum(int x, int y) { // 左閉右開查詢
           T ans{};
           for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans
                      }
           return ans;
     }
T rangeSum
            (int lx, int ly, int rx, int ry) { // 左閉右開查詢
           return sum(
    rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
     }
};
3.3 DSU [d41d8c]
struct DSU {
     int n;
     vector<int> boss, siz;
     DSU() {}
     DSU(int n_) { init(n_); }
void init(int n_) {
           n = n_;
           boss.resize(n);
           iota(boss.begin(), boss.end(), 0);
           siz.assign(n, 1);
     int find(int x) {
   if (boss[x] == x) return x;
   return boss[x] = find(boss[x]);
     bool same(int x, int y) {
    return find(x) == find(y);
     bool merge(int x, int y) {
           x = find(x);
y = find(y);
           if (x == y)
                return false:
           if(siz[x] < siz[y]) swap(x, y);
siz[x] += siz[y];
boss[y] = x;</pre>
           return true;
      int size(int x) {
   return siz[find(x)];
     }
};
struct DSU {
      vector<int> boss, siz, stk;
     DSU() {}
DSU(int n_) { init(n_); }
      void init(int n_) {
           n = n_;
           boss.resize(n):
           iota(boss.begin(), boss.end(), 0);
           siz.assign(n, 1);
           stk.clear():
     int find(int x) {
           return x == boss[x] ? x : find(boss[x]);
     bool same(int x, int y) {
   return find(x) == find(y);
```

bool merge(int x, int y) {

return false;

siz[x] += siz[y]; boss[y] = x;

stk.push_back(y);
return true;

if (siz[x] < siz[y]) swap(x, y);</pre>

x = find(x); y = find(y); if (x == y)

```
  void undo(int x) {
      while (stk.size() > x) {
            int y = stk.back();
            stk.pop_back();
            n++;
            siz[boss[y]] -= siz[y];
            boss[y] = y;
      }
  }
  int size(int x) {
      return siz[find(x)];
  }
};
```

3.4 Segment [d41d8c]

```
template <class Info>
 struct Seg { // 左閉右開寫法
int n; vector<Info> info;
        Seg() : n(0) {}
Seg(int n_, Info v_ = Info()) { init(n_, v_); }
template <class T>
        Seg(vector<T> init_) { init(init_); }
void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
        template <class T>
void init(vector<T> init_) {
             n = init_.size();
              info.assign(4 << __lg(n), Info());</pre>
             function <void(
   int, int, int)> build = [&](int p, int l, int r) {
   if (r - l == 1) {
      info[p] = init_[l];
}
                          return:
                   int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                   pull(p);
              build(1, 0, n);
        void pull(int p) {
    info[p] = info[p * 2] + info[p * 2 + 1];
        void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
             if (r
                    info[p] = v; return;
             int m = (l + r) / 2;
if (x < m) modify(2 * p, l, m, x, v);
else modify(2 * p + 1, m, r, x, v);</pre>
              int m = (l + r)
              pull(p):
        void modify(int p, const Info &i) {
             modify(1, 0, n, p, i);
        info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];</pre>
             int m = (l + r) / 2;
return query(p *
                     2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
        Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
        template < class F> // 尋找區間內,第一個符合條件的
        int findFirst
             (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)</pre>
                    return -1;
              if (l >= x && r <= y && !pred(info[p]))</pre>
             return -1;
if (r - l == 1)
                    return l;
             int m = (l + r) / 2;
int res = findFirst(2 * p, l, m, x, y, pred);
if (res == -1)
                    res = findFirst(2 * p + 1, m, r, x, y, pred);
              return res;
       template < class F> // 若要找 last, 先右子樹遞廻即可int findFirst(int l, int r, F & & pred) {
             return findFirst(1, 0, n, l, r, pred);
 };
// ---define structure and info plus---
 struct Info {
   int n = 0;
        int sum = 0;
 Info operator+(const Info &a, const Info &b) {
    return { a.n + b.n, a.sum + b.sum };
```

3.5 Lazy Segment [d41d8c]

```
| template <class Info, class Tag>
```

```
// 左閉右開寫法
struct LazySeg {
      int n;
      vector < Info > info;
      vector <Tag> tag;
LazySeg() : n(0) {}
       LazySeg(int n_, Info v_ = Info()) {
             init(n_, v_);
      template <class T>
LazySeg(vector<T> init_) {
   init(init_);
      void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
      template <class T>
void init (vector<T> init_) {
    n = init_.size();
    info.assign(4 << __lg(n), Info());
    tag.assign(4 << __lg(n), Tag());
    function <vaid(</pre>
             function <void(
   int, int, int)> build = [&](int p, int l, int r) {
   if (r - l == 1) {
      info[p] = init_[l];
}
                           return:
                    int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                    pull(p);
             build(1, 0, n);
      void pull
               (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
       void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
   tag[p].apply(v);
      void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
             tag[p] = Tag();
      void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
}
                   return:
             int m = (l + r) / 2;
push(p, l, r);
if (x < m) {</pre>
                    modify(2 * p, l, m, x, v);
             } else
                    modify(2 * p + 1, m, r, x, v);
             pull(p);
       void modify(int p, const Info &i) {
             modify(1, 0, n, p, i);
      Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    push(p, l, r);
    return query(p *</pre>
             return query(p *
2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      .
Info query
              (int ql, int qr) { return query(1, 0, n, ql, qr); }
       void range_apply
             (int p, int l, int r, int ql, int qr, const Tag &v) {
if (qr <= l || ql >= r) return;
if (ql <= l && r <= qr) {</pre>
                    apply(p, l, r, v);
                    return:
             int m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
             pull(p);
      void range_apply(int l, int r, const Tag &v) {
    range_apply(1, 0, n, l, r, v);
       template < class F> // 尋找區間內,第一個符合條件的
      int findFirst
             (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {</pre>
                    return -1;
             if (l >= x && r <= y && !pred(info[p])) {
                    return -1;
             if (r - l == 1) {
                    return l;
```

```
int m = (l + r) / 2;
          push(p);
           int res = findFirst(2 * p, l, m, x, y, pred);
          if (res ==
               res = findFirst(2 * p + 1, m, r, x, y, pred);
          return res;
     template < class F> // 若要找 last, 先右子樹遞廻即可
int findFirst(int l, int r, F & & pred) {
    return findFirst(1, 0, n, l, r, pred);
};
// ---define structure and info plus---
struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add; void apply(const Tag& v) { if (v.set_val) {
               set_val = v.set_val;
add = v.add;
          else {
                add += v.add;
     }
struct Info {
     int sum;
     void apply(int l, int r, const Tag &v) {
          if (v.set_val) {
    sum = (r - l) * v.set_val;
          sum += (r - l) * v.add;
     // Info& operator=(const Info &rhs) {
             // 部分 assignment 使用
return *this;
     //
     // }
Info operator+(const Info &a, const Info &b) {
     return { a.sum + b.sum };
}
3.6 Treap [d41d8c]
```

```
struct Treap {
      Treap *lc, *rc;
      int pri, siz; bool rev_valid;
int val; int min;
Treap(int val_) {
           min = val = val_;
pri = rand();
            lc = rc = nullptr;
siz = 1; rev_valid = 0;
      void pull() { // update siz or other information
            siz = 1;
min = val;
            for (auto c : {lc, rc}) {
    if (!c) continue;
                  siz += c->siz;
min = std::min(min, c->min);
            }
      void push() {
            if (rev_valid) {
                  swap(lc, rc);
if (lc) lc->rev_valid ^= 1;
if (rc) rc->rev_valid ^= 1;
            rev_valid = false;
      int find(int k) { // 找到 min 是 k 的位置 (1-based)
            push();
            int ls = (lc ? lc->siz : 0) + 1;
            if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
     }
int size(Treap *t) {
    return t ? t->siz : 0;
Treap *merge(Treap *a, Treap *b) {
     if (!a || !b) return a ? a : b;
a->push(); b->push();
if (a->pri > b->pri) {
    a->rc = merge(a->rc, b);
}
            a->pull();
            return a;
      b->lc = merge(a, b->lc);
            b->pull();
     }
pair<Treap*, Treap*> split(Treap *t, int k) {
      // 分割前 k 個在 first,剩下的在 second if (t == nullptr) return {nullptr, nullptr};
      t->push();
```

```
if (size(t->lc) < k) {
    auto [a, b] = split(t->rc, k - size(t->lc) - 1);
    t->rc = a;
    t->pull();
    return {t, b};
}
else {
    auto [a, b] = split(t->lc, k);
    t->lc = b;
    t->pull();
    return {a, t};
}

void Print(Treap *t) {
    if (!t) return;
    t->push();
    Print(t->lc);
    cout << t->val;
    Print(t->rc);
}
```

3.7 Mo [d41d8c]

4 Flow

4.1 Dinic [44ef80]

```
template < class T>
struct Dinic {
      struct Edge {
   int to;
             T flow, cap; // 流量跟容量
       tht n, m, s, t;
const T INF_FloW = 1 << 30;
vector<vector<int>> adj; // 此點對應的 edges 編號
       vector<Edge> edges; // 幫每個 edge 編號
      vector <int> dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
    n = n_; m = 0;
}
              dis.resize(n); ptr.resize(n);
              adj.assign(n, vector<int>{});
edges.clear();
      yoid add_edge(int u, int v, T cap) {
    // 偶數 id 是正向邊
    edges.push_back({ v, 0, cap });
    edges.push_back({ u, 0, 0 });
              adj[u].push_back(m++);
              adj[v].push_back(m++);
       bool bfs() {
              fill(dis.begin(), dis.end(), -1);
dis[s] = 0; queue<int> q;
              q.push(s);
              while (!q.empty() && dis[t] == -1) {
   int u = q.front(); q.pop();
   for (int id : adj[u]) {
                            Edge &e = edges[id];
                            if (e.flow == e.cap) continue;
if (dis[e.to] == -1) {
    dis[e.to] = dis[u] + 1;
                                   q.push(e.to);
                           }
                    }
              return dis[t] != -1;
       T dfs(int u, T flow) {
              if (flow == 0) return 0;
if (u == t) return flow;
              for (int
                    &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {
Edge &e = edges[adj[u][cur]];
if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;</pre>
```

4.2 Min Cut [44ae6c]

```
// CSES Police Chase
int main(){
       int n, m; cin >> n >> m;
Dinic <int >> g(n);
for (int i = 0; i < m; i++) {</pre>
              int u, v, cap = 1;
cin >> u >> v;
              u--; v--;
              g.add_edge(u, v, cap);
               g.add_edge(v, u, cap);
       int res = g.work(0, n - 1);
cout << res << "\n";
if (res == 0) return;</pre>
       vector < int > vis(n);
auto find = [&](auto self, int u) -> void {
              if (!vis[u]) {
                      self(self, e.to);
                     }
              }
       };
       f;
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
    }
        are dees[id];</pre>
                      auto e = g.edges[id];
if (!vis[e.to]) {
    cout << i + 1 << " " << e.to + 1 << "\n";</pre>
              }
      }
}
```

4.3 Hangarian [350fc3]

```
National Chung Cheng University Salmon

return false;
};
for (int i = 0; i < n; i++) {
    fill(vis.begin(), vis.end(), 0);
    dfs(dfs, i);
}
for (int i = n; i < n + m; i++) {
    if (used[i] != -1) {
        match.emplace_back(used[i], i - n);
    }
}
return match;
}

4.4 MCMF [c18f36]

template < class Tf, class Tc >
struct MCMF {
    struct Edge {
        int to;
        If flow, cap; // 流量跟容量
        Tc cost;
    };
    // 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就int n, m, s, t;
    const Tf INF_FLOW = 1 << 30;
    const Tc INF_COST = 1 << 30;
    const Tc INF_COST = 1 << 30;
```

```
// 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就好
int n, m, s, t;
const Tf INF_FLOW = 1 << 30;
const Tc INF_COST = 1 << 30;
vector<vector<int>> adj;
vector<Edge> edges; // 幫每個 edge 編號
vector<Tc> dis, pot; // johnson algorithm, using spfa
vector<int> rt; // 路徑恢復,對應 id
vector < bool > inq;
MCMF(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
     n = n_;
m = 0;
     edges.clear();
     adj.assign(n, vector<int>{});
void add_edge(int u, int v, Tf cap, Tc cost){
     edges.push_back({v, 0, cap, cost});
edges.push_back({u, 0, 0, -cost});
adj[u].push_back(m++);
      adj[v].push_back(m++);
bool spfa() {
      dis.assign(n, INF_COST);
      rt.assign(n, -1); inq.assign(n, false);
     queue <int> q;
q.push(s), dis[s] = 0, inq[s] = true;
      while (!q.empty()) {
           int u = q.front(); q.pop();
inq[u] = false;
           for (int id : adj[u]) {
    auto [v, flow, cap, cost] = edges[id];
    Tc ndis = dis[u] + cost + pot[u] - pot[v];
    if (flow < cap && dis[v] > ndis) {
                      dis[v] = ndis; rt[v] = id;
if (!inq[v]) {
    q.push(v); inq[v] = true;
                }
          }
      return dis[t] != INF_COST;
bool dijkstra() {
     }
          }
      return dis[t] != INF_COST;
dis[i] += pot[i] - pot[s];
           Tf f = INF_FLOW;
           for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                       (f, edges[rt[i]].cap - edges[rt[i]].flow);
           f = min<Tf>(f, need);
```

```
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
                       flow += f; need -= f;
                       cost += f * dis[t]; fr = false;
                       swap(dis, pot);
if (need == 0) break;
               return make_pair(flow, cost);
       // 限定 cost, 最大化 flow
pair<Tf, Tc> work_budget(int s_, int t_, Tc budget) {
    s = s_, t = t_; pot.assign(n, 0);
               Tf flow{}; Tc cost{}; bool fr = true
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] += pot[i] - pot[s];
    }
}</pre>
                       Tf f = INF_FLOW;
                       for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
                              f = min
                                      (f, edges[rt[i]].cap - edges[rt[i]].flow);
                      }
f = min<Tf>(f, budget / dis[t]);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
}
                      flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
swap(dis, pot);
if (budget == 0 || f == 0) break;
               return make_pair(flow, cost);
       void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
};
```

5 String

5.1 Hash [852711]

```
constexpr int B = 59;
vector<Z> Hash(string &s) {
    vector<Z> ans {0};
    for (auto c : s) {
        ans.push_back(ans.back() * B + (c - 'a' + 1));
    }
    return ans;
}

void solve() {
    string s, sub;
    cin >> s >> sub;
    auto a = Hash(s);
    auto find = q.back();
    int ans = 0;
    int l = 1, r = sub.size(), len = sub.size();
    while (r <= s.size()) {
        if (a[r] - a[l - 1] * power(Z(B), len) == find) {
            ans++;
        }
        l++, r++;
    }
    cout << ans << "\n";
}</pre>
```

5.2 KMP [cddfd9]

```
return match;
}
};
```

5.3 **Z Function** [764b31]

```
| // z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
| // 的最長公共前綴 (LCP) 的長度
vector < int > Z(string s) {
    int n = s.size();
    vector < int > z(n); z[0] = n;
    for (int i = 1, j = 1; i < n; i++) {
        z[i] = max(0, min(j + z[j] - i, z[i - j]));
        while (i + z[i] < n && s[z[i]] == s[i + z[i]])
        z[i]++;
    if (i + z[i] > j + z[j]) j = i;
    }
    return z; // 最後一格不算
```

5.4 SA [d40e3e]

```
struct SuffixArray {
      int n; string s;
vector<int> sa, rk, lc;
      // n: 字串長度
      // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
       ... // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
      // lc: LCP
      数組, lc[i] 表示 sa[i] 和 sa[i + 1] 的最長公共前綴長度
SuffixArray(const string &s_) {
    s = s_; n = s.length();
    sa.resize(n);
             lc.resize(n - 1):
             rk.resize(n);
             iota(sa.begin(), sa.end(), 0);
             rot(asa.begin(), sa.ein(), o),
sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });
rk[sa[0]] = 0;
for (int i = 1; i < n; ++i)
    rk[sa[i]]
    rk[sa[i]] + (s[sa[i]] != s[sa[i - 1]]);
int k = 1.</pre>
             int k = 1;
vector<int> tmp, cnt(n);
             tmp.reserve(n);
                                     - 1]] < n - 1) {
             while (rk[sa[n
                   tmp.clear();
for (int i = 0; i < k; ++i)</pre>
                          tmp.push_back(n - k + i);
                   for (auto i : sa)
    if (i >= k)
        tmp.push_back(i - k);
                   fill(cnt.begin(), cnt.end(), 0);
for (int i = 0; i < n; ++i)</pre>
                           ++cnt[rk[i]];
                   for (int i = 1; i < n; ++i)
   cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; --i)
                          sa[--cnt[rk[tmp[i]]]] = tmp[i];
                   for (int i = 0, j = 0; i < n; ++i) {
   if (rk[i] == 0) {</pre>
                   j = 0;
} else {
                          for (j
                                  `-= j > 0; i + j < n && sa[rk[i] - 1] + j
< n && s[i + j] == s[sa[rk[i] - 1] + j]; )
                          lc[rk[i] - 1] = j;
                   }
            }
      string getLCP() {
   int cp = 0, k, lcp = 0, p;
   for (int i = 0; i < n; i++) {
      if (!rk[i]) continue;
      k = sa[rk[i] - 1];
}</pre>
                   k = Sa[rK[t] - 1],
if (cp) cp--;
while (s[i + cp] == s[k + cp]) cp++;
if (cp > lcp){
    lcp = cp;
    p = i;
}
             if (lcp) {
             return s.substr(p, lcp);
} else {
                   return "-1";
      }
};
```

5.5 SAM [d15619]

```
struct SAM {
     static constexpr int ALPHABET_SIZE = 26;
     struct Node {
           int len;
int link;
           array<int, ALPHABET_SIZE> next;
           Node() : len{}, link{}, next{} {}
     vector < Node > t;
     SAM() { init(); }
void init() {
           t.assign(2, Node());
t[0].next.fill(1);
           t[0].len = -1;
      int newNode() {
           t.emplace_back();
           return t.size() - 1;
     int extend(int p, int c) {
   if (t[p].next[c]) {
                 int q = t[p].next[c];
if (t[q].len == t[p].len + 1) {
                       return q;
                  int r = newNode();
                 t[r].len = t[p].len + 1;
t[r].link = t[q].link;
t[r].next = t[q].next;
                 t[q].link = r;
                 while (t[p].next[c] == q) {
                      t[p].next[c] = r;
p = t[p].link;
                 return r;
           int cur = newNode();
t[cur].len = t[p].len + 1;
while (!t[p].next[c]) {
    t[p].next[c] = cur;
    p = t[p].link;
           t[cur].link = extend(p, c);
           return cur;
     }
void solve() {
     string s; cin >> s;
int n = s.length();
     vector < int > pos(n + 1); // s[i - 1] 的後綴終點位置
     pos[0] = 1;
     for (int i = 0; i < n; i++) {
    pos[i + 1] = sam.extend(pos[i], s[i] - 'a');</pre>
```

5.6 Duval Algorithm [f9dcca]

```
|// duval_algorithm

// 將字串分解成若干個非嚴格遞減的非嚴格遞增字串

vector<string> duval(string s) {
    int i = 0, n = s.size();
    vector<string> res;
    while (i < n) {
        int k = i, j = i + 1;
        while (s[k] < s[j]) k = i;
        else k++;
        j++;
    }
    while (i <= k) {
        res.push_back(s.substr(i, j - k));
        i += j - k;
    }
}

return res;
}

// 最小旋轉字串

string min_round(string s) {
    s += s;
    int i = 0, n = s.size();
    int start = i;
    while (i < n / 2) {
        start = i;
        int k = i, j = i + 1;
        while (s[k] <= s[j] && j < n) {
            if (s[k] < s[j]) k = i;
            else k++;
            j++;
        }
        while (i <= k) {
            i += j - k;
        }
        return s.substr(start, n / 2);
}
```

5.7 Manacher [9c9ca6]

```
// 找到對於每個位置的迴文半徑
vector<int> manacher(string s) {
     string t = "#"
     for (auto c : s) {
          t += c;
          t += '#';
     int n = t.size();
     vector<int> r(n);
     for (int i = 0, j =
          0; i < n; i++) { // i 是中心, j 是最長回文字串中心 if (2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
          while (i - r[i] >=
    0 && i + r[i] < n && t[i - r[i]] == t[i + r[i]]) {
    r[i] += 1;</pre>
          if (i + r[i] > j + r[j]) {
                j = i;
    return r;

// # a # b # a #

// 1 2 1 4 1 2 1

// # a # b # b # a #

// 1 2 1 2 5 2 1 2 1
     // 值 -1 代表原回文字串長度
     // (id - val + 1) / 2 可得原字串回文開頭
```

5.8 Trie [3b3aa0]

```
struct Trie {
      struct trie_node {
            bool is_word;
vector<trie_node *> children;
trie_node() {
    is_word = false;
    children.resize(26, NULL);
             }
      f;
trie_node *root = new trie_node();
void insert(string &s) {
    trie_node *cur = root;
    for (int i = 0; i < s.size(); i++) {
        int idx = s[i] - 'a';
    }
}</pre>
                   if (cur->children[idx] == NULL) {
    cur->children[idx] = new trie_node();
                   cur = cur->children[idx];
             cur->is word = true;
      bool is_in_trie(string &s) {
             trie_node *cur = root;
for (int i = 0; i < s.size(); i++) {</pre>
                   if (cur->
                   children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
             return true;
       int search_i_start(string &s, int i, vector<int> &dp) {
             trie_node *cur = root;
int sz = s.size(), ans = 0;
for (int j = i; j < sz; j++) {</pre>
                   ->children[s[j] - 'a'] == nullptr) return ans;
cur = cur->children[s[j] - 'a'];
                   if (cur->is_word)
          (ans += dp[j + 1]) %= mod;
             return ans;
      }
};
int main() {
      // 找到 sub 集合裡,可以重複用,組成 s 的組數 Trie trie;
      string s; cin >> s;
int sz = s.size();
// dp 代表 i 開頭到最後的配對總數
       // 找到有結尾為 stop 的 dp[i] += dp[j + 1]
      trie.insert(sub);
      dp[sz] = 1;
for (int i = sz - 1; i >= 0; i--) {
    dp[i] = trie.search_i_start(s, i, dp);
       cout << dp[0] << endl;
}
```

Math

6.1 Prime [4e0864]

```
a^{(m-1)} = 1 \pmod{m}
// a^(m-1) = 1 (Mod M)
// a^(m-2) = 1/a (Mod M)
// EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)
// Filter + DP; DP save min factor 'recur' factor decomposition
// FacNums = (x+1)(y+1)(z+1)...
// FacSum = (a^0+a^1...+a^x)(b^0+...+b^y)

// FacMul = N(x+1)(y+1)(z+1)/2

vector<int> is_prime;
// 1 代表是質數,非 1 不是
void init(int n) {
       is_prime[j] = i;
      }
int main() {
       init(1000000);
       ll ans = 1, q; cin >> q;
map<ll, ll> mp;
while (is_prime[q] != 1) {
             mp[is_prime[q]]++;
q /= is_prime[q];
       if (q != 1) mp[q]++;
for (auto [a, b] : mp) ans *= b + 1;
cout << ans << "\n";</pre>
```

6.2 Modulo [a1aab8]

```
constexpr T power(T a, ll b) {
  T res {1};
  for (; b; b /= 2, a *= a)
      if (b % 2) res *= a;
      return res;
constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
    res %= p;
      if (res < 0) res += p;</pre>
      return res;
template < ll P >
struct MInt {
    ll x;
      constexpr MInt() : x {0} {}
constexpr MInt(ll x) : x {norm(x % getMod())} {}
static ll Mod;
      constexpr static ll getMod() {
   if (P > 0) return P;
           else return Mod;
      constexpr static void setMod(ll Mod_) {
           Mod = Mod_;
      constexpr ll norm(ll x) const {
           if (x < 0) x += getMod();
if (x >= getMod()) x -= getMod();
      constexpr ll val() const { return x; }
constexpr MInt operator-() const {
           MInt res;
           res.x = norm(getMod() - x);
return res;
      constexpr MInt inv() const {
   return power(*this, getMod() - 2);
     constexpr MInt & operator *= (MInt rhs) & {
    if (getMod() < (1ULL << 31)) {
        x = x * rhs.x % int(getMod());
    }
}</pre>
           } else {
                 x = mul(x, rhs.x, getMod());
      constexpr MInt & operator += (MInt rhs) & {
    x = norm(x + rhs.x);
           return *this;
      constexpr MInt &operator -=(MInt rhs) & {
           x = norm(x - rhs.x);
            return *this:
      constexpr MInt &operator/=(MInt rhs) & {
           return *this *= rhs.inv();
      friend constexpr MInt operator*(MInt lhs, MInt rhs) {
           MInt res = lhs; return res *= rhs;
      friend constexpr MInt operator+(MInt lhs, MInt rhs) {
           MInt res = lhs; return res += rhs;
      friend constexpr MInt operator - (MInt lhs. MInt rhs) {
           MInt res = lhs; return res -= rhs;
```

```
friend constexpr MInt operator/(MInt lhs, MInt rhs) {
   MInt res = lhs; return res /= rhs;
     friend constexor
            std::istream &operator>>(std::istream &is, MInt &a) {
          ll v; is >> v; a = MInt(v); return is;
     friend constexpr std::
           ostream & operator << (std::ostream &os, const MInt &a) {
          return os << a.val();</pre>
     friend constexpr bool operator==(MInt lhs, MInt rhs) {
          return lhs.val() == rhs.val();
     friend constexpr bool operator!=(MInt lhs, MInt rhs) {
          return lhs.val() != rhs.val();
     rriend constexpr bool operator < (MInt lhs, MInt rhs) {
   return lhs.val() < rhs.val();</pre>
    }
template<>
ll MInt<0>::Mod = 998244353;
constexpr int P = 1e9 + 7;
using Z = MInt<P>;
```

6.3 Combination [878efe]

```
finvfac[m] = _fac[m].inv();
for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i -
            n = m;
      Z fac(ll m) {
   if (m > n) init(2 * m);
   return _fac[m];
      Invfac(ll m) {
   if (m > n) init(2 * m);
   return _invfac[m];
      }
Z inv(ll m) {
   if (m > n) init(2 * m);
   return _inv[m];
       If binom(ll n, ll m) {
   if (n < m || m < 0) return 0;
   return fac(n) * invfac(m) * invfac(n - m);</pre>
       |} comb; // 注意宣告, 若要換模數需重新宣告
```

6.4 CRT [d41d8c]

```
ll exgcd(ll a, ll b, ll &x, ll &y) {
      if (!b) {
    x = 1, y = 0;
    return a;
      il g = exgcd(b, a \% b, y, x);
      y -= a / b * x;
      return g;
il inv(ll x, ll m){
      ll`a, b;
      exgcd(x, m, a, b);
      a %= m;
if (a < 0) a += m;
      return a;
// remain, mod
ll CRT(vector<pair<ll, ll>> &a){
      ll prod = 1;
for (auto x : a) {
    prod *= x.second;
      ll res = 0;
      for (auto x : a) {
   auto t = prod / x.second;
   res += x.first * t % prod * inv(t, x.second) % prod;
   if(res >= prod) res -= prod;
      return res;
```

6.5 Matrix [08b5fe]

```
template < class T>
struct Mat {
      int m, n;
constexpr static ll mod = 1e9 + 7;
vector<vector<!>> matrix;
Mat(int n_ = 0) { init(n_, n_); }
Mat(int m_, int n_) { init(m_, n_); }
Mat(vector<vector<!>> matrix_) { init(matrix_); }
      matrix.assign(m, vector<T>(n));
      void init(vector<vector<T>> &matrix_) {
           m = matrix_.size();
n = matrix_[0].size();
           matrix = matrix_;
      vector<vector<T>> unit(int n) {
           vector<vector<l>> res(n, vector<l>(n));
for (int i = 0; i < n; i++) {
    res[i][i] = 1;</pre>
           return res:
      constexpr Mat &operator*=(const Mat& rhs) & {
           assert(matrix[0].size() == rhs.matrix.size());
int m = matrix.size()
                   , k = matrix[0].size(), n = rhs.matrix[0].size();
           l] * rhs.matrix[l][j] % mod)) %= mod;
                 }
           matrix = ans.matrix;
return *this;
      constexpr Mat &operator^=(ll p) & {
   assert(m == n);   assert(p >= 0);
   Mat ans(p-- == 0 ? unit(m) : matrix);
            while (p > 0) {
   if (p & 1) ans *= *this;
   *this *= *this;
                 p >>= 1;
            matrix = ans.matrix;
            return *this;
      friend Mat operator*(Mat lhs, const Mat &rhs) {
           lhs *= rhs:
            return lhs;
      friend Mat operator^(Mat lhs, const ll p) {
            lhs ^= p;
};
// fn = fn-3 + fn-2 + fn-1
// 初始矩陣 轉移式
// f4 f3 f2 f1 1 0 f5 f4 f3
// f3 f2 f1 1 0 1 => f4 f3 f2
// f2 f1 f0 1 0 0 f3 f2 f1
```

6.6 Integer Partition [595ed2]

```
// CSES_Sum_of_Divisors
// C25_3um_0__DtvtSu/s

const int mod = 1e9 + 7;

const int inv_2 = 500000004;

// n / 1 * 1 + n / 2 * 2 + n / 3 * 3 + ... + n / n * n

int main() {
       ll ans = 0;
      ll n; cin >> n;
for (ll l = 1, r; l <= n; l = r + 1) {
    r = n / (n / l);</pre>
             ll val = n / l; // n / l 到 n / r 一樣的值ll sum = (((l + r) % mod) *
                    ((r - l + 1) % mod)) % mod * inv_2; // l 加到 r
             val %= mod; sum %= mod;
ans += val * sum;
             ans %= mod:
       cout << ans << "\n";
}
```

6.7 Mobius Theorem

- 數論分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left|\frac{n}{i}\right|)$ 的和式。當可以在O(1)內計算f(r)-f(l)或已經預處理 出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d|n} \mu(d) = \begin{cases} 1 & \text{for } n = 1 \\ 0 & \text{for } n \neq 0 \end{cases}$$

- 2. μ 是常數函數 1 的反元素 $\Rightarrow \mu*1=\epsilon$, $\epsilon(n)$ 只在n=1時為 1, 其餘情況皆為 0。
- $-\phi$ 歐拉函數: x以下與x互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^i) \\ &= 1 + p^0(p-1) + p^1(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^c \\ &= id \end{split}$$

• 莫比烏斯反演公式

-
$$f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$$

- $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

例子

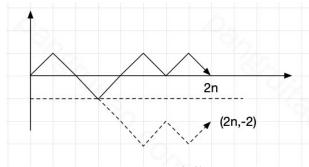
$$\begin{split} &\sum_{i=a}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \frac{\left\lfloor \frac{y}{k} \right\rfloor}{\sum_{j=1}^{y} [d \mid j]} \ \mathbf{d} \ \mathbf{T}$$
 答除 i 時為 1
$$& \min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor) \\ &= \sum_{d=1}^{min} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.8 Mobius Inverse [d41d8c]

const int maxn = 2e5;

```
ll mobius_pref[maxn];
void init() {
      mobius_pref[1] = 1;
      vector<ll> wei
      (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
    }
                  continue; // 包含平方
            if (wei[i] == 0) {
                  wet[i] == 0) {
wei[i] = 1;
for (ll j = 2; i * j < maxn; j++) {
    if (j % i == 0) wei[i * j] = -1;
    else if (wei[i * j] != -1) wei[i * j]++;</pre>
                  }
            mobius pref[i]
                   = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
     }
void solve() {
      ll a, b, c, d, k; cin >> a >> b >> c >> d >> k;
auto cal = [&](ll x, ll y) -> int {
            int res = 0;
            cout << cal
             (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k, (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n"
}
```

6.9 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有x 個,往下有y 個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.10 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- · X/G:本質不同的方案的集合
- X^g : 對於某一種操作 g,所有方案中,經過 g 這種翻轉後保持不變的方案的集合
- 集合取絕對值代表集合數

7 Search and Gready

7.1 Binary Search [d41d8c]

```
int main() {
    int l = 1, r = 10;
    // 1 to tar, find tar
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}</pre>
```

7.2 Ternary Search [d41d8c]

8 Тгее

8.1 LCA [9f95b1]

```
}
}
int lca(int a, int b) {
    if (depth[a] < depth[b]) swap(a, b);
    int pull = depth[a] - depth[b];
    for (int i = 0; i < 18; i++) {
        if (pull & (1 << i)) {
            a = par[a][i];
        }
    if (a == b) return a;
    for (int i = 17; i >= 0; i--) {
        if (par[a][i] != par[b][i]) {
            a = par[a][i], b = par[b][i];
        }
    return par[a][0];
}
```

8.2 Centroid Decomposition [30b436]

```
struct centroid_decomposition {
       int n;
       vector<vector<int>> adj;
       vector<bool> vis;
       vector<int> siz;
       centroid_decomposition() {}
centroid_decomposition(int n_) { init(n_); }
       void init(int n_) {
              n = n_;
adj.assign(n, {});
vis.assign(n, false);
              siz.assign(n, 1);
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void get_siz(int dep, int x, int p = -1) {
             siz[x] += siz[y];
              }
      fint get_cen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz) {
            return get_cen(y, sz, x);
        }
}
                    }
              return x;
       void work(int x = 0) {
    get_siz(0, x);
    int_cen = get_cen(x, siz[x]);
}
              vis[cen] = true;
// do something
for (int y : adj[cen]) {
    if (vis[y]) continue;
                     work(y);
}:
```

8.3 Tree Flattening [51199c]

```
|// 父節
      點加值 = 所有子節點區間加值,求單點,使用 bit,做前綴差分
 // CSES 1138_Path Queries
 int main(){
      int n, q; cin >> n >> q;
vector <int> node_value(n + 1), euler_ordered_value(n);
for (int i = 1; i <= n; i++) {</pre>
          cin >> node_value[i];
      vector<vector<int>> tree(n + 1);
      for (int i = 1; i < n; i++) {</pre>
          int u, v; cin >> u >> v;
          tree[u].push_back(v);
          tree[v].push back(u);
      vector<pair<int, int>> tree_mapping(n + 1);
      int cnt = 0;
      auto dfs = [&](auto self, int u, int par) -> void {
          euler_ordered_value[++cnt] = node_value[u];
          for (auto v : tree[u]) {
    if (v == par) continue;
    self(self, v, u);
          tree_mapping[u].second = cnt;
     dfs(dfs, 1, 0);
      BIT bit(n);
      for (int i = 1; i <= n; i++)
          (int i = 1; i <= n; i++) {
bit.modify(tree_mapping[i].first, node_value[i]);</pre>
          if (tree_mapping[i].first < n) { // root 就不用扣了</pre>
```

8.4 Heavy Light Decomposition [ad25b6]

```
struct HLD {
      int n, cur;
vector<int> siz, top, dep, parent, in, out, seq;
       vector<vector<<mark>int</mark>>> adj;
      HLD(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
    n = n_; cur = 0;
            siz.resize(n); top.resize(n); dep.resize(n);
parent.resize(n); in.resize(n); out.resize(n);
            seq.resize(n); adj.assign(n, {{}});
      void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
      void work(int root = 0) {
            top[root] = root;
dep[root] = 0;
            parent[root] =
            dfs1(root); dfs2(root);
      void dfs1(int u) {
            if (parent[u] != -1)
                  adj[u].erase(find
                         (adj[u].begin(), adj[u].end(), parent[u]));
            for (auto &v : adj[u]) {
                  parent[v] = u, dep[v] = dep[u] + 1;
                  | dfs1(v);
| siz[u] += siz[v];
| if (siz[v] > siz[adj[u][0]]) {
| swap(v, adj[u][0]);
                  } // 讓 adj[u][0] 是重子節點
      void dfs2(int u) {
            in[u] = cur++;
            seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
   top[v] = v == adj[u][0] ? top[u] : v;
            out[u] = cur;
      int lca(int u, int v) {
    while (top[u] != top[v]) {
        if (dep[top[u]] > dep[top[v]]) {
            u = parent[top[u]];
        } else {
                        v = parent[top[v]];
                  }
            return dep[u] < dep[v] ? u : v;</pre>
      int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
      int jump(int u, int k) {
   if (dep[u] < k) return -1;
   int d = dep[u] - k;</pre>
            while (dep[top[u]] > d)
            u = parent[top[u]];
return seq[in[u] - dep[u] + d];
      bool isAncester(int u, int v) {
            // 判斷 u 是否是 v 的祖先
return in[u] <= in[v] && in[v] < out[u];
      int rootedParent(int u, int v) {
            // 根據新根節點 u 計算 v 的父節點
            if (!isAncester(u, v)) return parent[u];
auto it = upper_bound(adj
```

[u].begin(), adj[u].end(), v, [&](int x, int y) {

```
8.5 Link Cut Tree [c26f51]
#include <bits/stdc++.h>
using namespace std;
using i64 = long long;
constexpr i64 Mod = 51061;
struct Tag {
    i64 add = 0;
      i64 mul = 1;
     void apply(const Tag& v) {
  mul = mul * v.mul % Mod;
  add = (add * v.mul % Mod + v.add) % Mod;
     }
};
struct Info {
     i64 val = 1;
     i64 \text{ sum} = 1:
     void apply(int size, const Tag &v) {
    val = (val * v.mul % Mod + v.add) % Mod;
    sum = (sum * v.mul % Mod + v.add * size % Mod) % Mod;
     }
};
struct Node -
     Node *ch[2], *p;
     int rev = 0;
     int size = 1;
void make_rev() {
           swap(ch[0], ch[1]);
           rev ^= 1;
     Node() : ch {nullptr, nullptr}, p(nullptr) {}
     Info info = Info();
Tag tag = Tag();
     void apply(const Tag &v) {
           info.apply(size, v);
           tag.apply(v);
     void push_tag() {
           if (rev) {
   if (ch[0]) ch[0]->make_rev();
   if (ch[1]) ch[1]->make_rev();
           if (ch[0]) {
                ch[0]->apply(tag);
           if (ch[1]) {
    ch[1]->apply(tag);
           tag = Tag();
      void pull_info() {
           }
bool isroot(Node *t) {
             == nullptr || (t->p->ch[0] != t && t->p->ch[1] != t);
int pos(Node *t) { // 回傳 1 代表是右子節點 return t->p->ch[1] == t;
void rotate(Node *t)
     Node *q = t->p;

int x = !pos(t);

q->ch[!x] = t->ch[x];

if (t->ch[x]) {
           t->ch[x]->p = q;
     t->p = q->p;
if (!isroot(q)) {
    q->p->ch[pos(q)] = t;
     t - ch[x] = q;
     a -> p = t:
     q->pull_info();
}
```

```
Node *p = \hat{t} - \hat{p};
         p->push_tag();
         t->push tag();
         rotate(t);
    t->push_tag();
t->pull_info();
void access(Node *t) {
     // 把從根到 t 的所有點都放在一條實鏈裡,使根
     // 到 t 成為一條實路徑,並且在同一棵 splay 裡
     for (Node *i = t, *q = nullptr; i; q = i, i = i->p) {
         splay(i);
         i->ch[1] = q;
     splay(t);
}
void makeRoot(Node *t) { // 使 t 點成為其所在樹的根
     access(t);
     swap(t->ch[0], t->ch[1]);
t->rev ^= 1;
}
Node* findRoot(Node *t) { // 找到 t 的 root
     access(t):
     splay(t);
    t->push_tag();
while (t->ch[0]) {
    t = t->ch[0];
         t->push_tag();
     splay(t);
void link(Node *t, Node *p) {
     makeRoot(t);
     if (findRoot(p) != t) {
         makeRoot(p);
         t - p = p;
         p->pull_info();
}
bool cut(Node *x, Node *y) { // 不存在邊,回傳 false
    makeRoot(x);
     access(y);
    if (y->ch[0] != x || x->ch[1]) return false;
y->ch[0]->p = nullptr;
y->ch[0] = nullptr;
     y->pull_info();
     return true:
void split(Node
      *x, Node *y) { // 以 y 做根, 區間修改用, apply 在 y 上
     makeRoot(x);
     access(v);
     splay(y);
}
bool isconnected(Node *x, Node *y) { // 查詢有沒有連通
     makeRoot(x);
    access(y);
return findRoot(x) == findRoot(y);
}
int main() {
     int n; cin >> n;
vector <Node *> nodes(n);
    for (int i = 0; i < n; i++) {
    nodes[i] = new Node();
    nodes[i] ->info.val = nodes[i]->info.sum = 1LL;
     for (int i = 0; i < n - 1; i++) {
         int u, v; cin >> u >> v;
u--; v--;
          link(nodes[u], nodes[v]);
     for (int i = 0; i < q; i++) {
         char op; cin >> op;
if (op == '+') {
              int u, v; cin >> u >> v;
              split(nodes[u], nodes[v]);
              Tag tag;
cin >> tag.add;
tag.add % Mod;
              nodes[v]->apply(tag);
         else if (op == '-') {
   int u1, v1; cin >> u1 >> v1;
              int u2, v2; cin >> u2 >> v2;
u1--; v1--; u2--; v2--;
cut(nodes[u1], nodes[v1]);
link(nodes[u2], nodes[v2]);
          else if (op == '*') {
              int u, v; cin >> u >> v;
              split(nodes[u], nodes[v]);
```

```
Tag tag;
cin >> tag.mul;
tag.mul % Mod;
                      nodes[v]->apply(tag);
                      int u, v; cin >> u >> v;
                       split(nodes[u], nodes[v]);
                      cout << nodes[v]->info.sum << "\n";</pre>
        return 0:
 8.6 Virtual Tree [622e69]
1// 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
 // 可以建立虚樹達成快速樹 DP
 // 例如這題是有權樹,跟 vertex 1 隔開的最小成本
 int top = -1; vector < int > stk(maxn);
 int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
   if (top == -1) return stk[++top] = u, void();
   int l = lca(stk[top], u);
   if (l == stk[top]) return stk[++top] = u, void();
        while (dfn[l] < dfn[stk[top -</pre>
                                                             1]])
        vt[stk[top - 1]].push_back(stk[top]), top--;
if (stk[top - 1] != l) {
               vt[l].push_back(stk[top]);
        stk[top] = l;
} else vt[l].push_back(stk[top--]);
stk[++top] = u;
 void reset(int u, vector<vector<int>> &vt) {
   for (int i : vt[u]) reset(i, vt);
                                                                                                                             }
                                                                                                                     1:
        vt[u].clear();
 void solve(int n, int q) {
                                                                                                                      9
        vector g(n + 1, vector<pair<int, int>>());
        vector vt(n + 1, vector <int>()); // dfs 完清除, 否則會退化
vector <ll> dp(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;
               g[u].push_back({v, w});
               g[v].push_back({u, w});
        build_lca(n, g);
       build_lca(n, g);
build(n, g);
for (int i = 0; i < q; i++) {
   int m; top = -1; cin >> m;
   vector<int> key(m);
   for (int j = 0; j < m; j++) {
      cin >> key[j];
      iskey[key[j]] = 1;
}
               key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
               for (int x : key) insert(x, vt);
               while (top
                         > 0) vt[stk[top - 1]].push_back(stk[top]), --top;
               // DP
               if (iskey[v]) {
                                    dp[u] += min_dis[v];
                                    // 砍掉 1 到 v 之間最短的路
                                    dp[u] += min(dp[v], min_dis[v]);
                              iskey[v] = dp[v] = 0;
                      vt[u].clear();
               dfs(dfs, key[0]); // key[0] 一定是 root
cout << dp[key[0]] << "\n";
iskey[key[0]] = dp[key[0]] = 0;
 }
 8.7 Dominator Tree [baa540]
       uct Dominator_tree {
  int n, id;
  vector<vector<int>> adj, radj, bucket;
  vector<int>> sdom, dom, vis, rev, pa, rt, mn, res;
  Dominator_tree(int n_ = 0) { init(n_); }
  void init(int _n) {
      n = _n, id = 0;
      adj.assign(n, vector<int>());
      radj.assign(n, vector<int>());
      bucket.assign(n, vector<int>());
      sdom.resize(n); dom.assign(n, -1);
      vis.assign(n, -1); rev.resize(n);
      pa.resize(n); rt.resize(n);
      mn.resize(n); res.resize(n);
}
 struct Dominator_tree {
```

```
void add_edge(int u, int v) { adj[u].push_back(v); }
int query(int v, int x) {
   if (rt[v] == v) return x ? -1 : v;
}
        int p = query(rt[v], 1);
if (p == -1) return x ? rt[v] : mn[v];
        if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
        rt[v] = p;
return x ? p : mn[v];
void dfs(int v) {
    vis[v] = id, rev[id] = v;
    rt[id] = mn[id] = sdom[id] = id, id++;
    for (int u : adj[v]) {
        if (vis[u] == -1) dfs(u), pa[vis[u]] = vis[v];
        radj[vis[u]].push_back(vis[v]);
}
 void build(int s) {
        dfs(s);
        for (int i = id - 1; i >= 0; i--) {
    for (int u : radj[i])
        sdom[i] = min(sdom[i], sdom[query(u, 0)]);
                if (i) bucket[sdom[i]].push_back(i);
for (int u : bucket[i]) {
   int p = query(u, 0);
                        dom[u] = sdom[p] == i ? i : p;
                if (i) rt[i] = pa[i];
        res.assign(n, -1);
for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];
for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre>
        res[s] = s:
        for (int i = 0; i < n; i++) dom[i] = res[i];</pre>
```

DP

9.1 LCS [5781cf]

```
int main() {
        int m, n; cin >> m >> n;
string s1, s2; cin >> s1 >> s2;
        int L = 0:
        vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0));
        for (int i = 1; i <= m; i++) {
    for (int j = 1; j <= n; j++) {
        if (s1[i - 1] == s2[j - 1])
            dp[i][j] = dp[i - 1][j - 1] + 1;
                               dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
               }
        fint length = dp[m][n]; cout << length << "\n";
string s(length, 'c'); // backtracking
while (m >= 1 && n >= 1) {
   if (s1[m - 1] == s2[n - 1]) {
      s[length - 1] = s1[m - 1];
      m--, n--, length--;
}
                else {
    if (dp[m - 1][n] > dp[m][n - 1]) m--;
                        else n--;
               }
        cout << s << "\n";
```

9.2 LIS [66d09f]

```
int main() {
      main() {
  int n; cin >> n;
  vector <int> v(n);
  for (int i = 0; i < n; i++) cin >> v[i];
  int dp[n]; vector <int> stk;
       stk.push_back(v[0]);
       dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) {
   if (v[i] > stk.back()) {
                    stk.push_back(v[i]);
dp[i] = ++L;
                     = lower_bound(stk.begin(), stk.end(), v[i]);
*it = v[i]; dp[i] = it - stk.begin() + 1;
       vector<int> ans; cout << L << "\n";
       for (int i = n - 1; i >= 0; i--) {
   if (dp[i] == L) {
                     ans.push_back(v[i]), L--;
       reverse(ans.begin(), ans.end());
for (auto i : ans) cout << i << " ";
```

9.3 Edit Distance [308023]

9.4 Bitmask [a626f9]

```
void hamiltonianPath(){
   int n, m; cin >> n >> m;
vector adj(n, vector<int>());
   for (int i = 0; i < m; i++) {
   int u, v; cin >> u >> v;
       adj[--v].push_back(--u);
   // 以...為終點,走過...
   vector dp(n, vector<int>(findBit(n)));
   for (int j : adj[i]) {
   if ((pre_mask & findBit(j)) == 0) continue;
              dp[i][mask
                   ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
       }
   cout << dp[n - 1][findBit(n) - 1] << "\n";
void elevatorRides() {
   int n, x; cin >> n >> x; vector<int> a(n);
for (int i = 0; i < n; i++) cin >> a[i];
   vector<array<int, 2>> dp(findBit(n));
   }
   cout << dp[findBit(n) - 1][0] << "\n";
}
```

9.5 Projects [0942aa]

```
ll nt = dp[id][1] + a[i].to - a[i].from;
    if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
          dp[i] = {nw, nt}; rec[i] = {1, id};
    }
}
vector < int > ans;
for (int i = n; i != 0;) {
    if (rec[i][0]) {
          ans.push_back(a[i].id);
          i = rec[i][1];
    } else i--;
}
```

9.6 Removal Game [7bb56b]

9.7 CHT [5f5c25]

```
struct Line {
    line(ll m = 0, ll b = 0) : m(m), b(b) {}
ll eval(ll x) {
    return m * x + b;
}:
struct CHT { // 用在查詢單調斜率也單調
    int n, lptr, rptr; vector<Line> hull;
CHT(int n_ = 0, Line init_ = Line()) {
   init(n_, init_);
        i init(int n_ = 0, Line init_ = Line()) {
n = n_; hull.resize(n); reset(init_);
    void init(int n
    void reset(Line init_ = Line()) {
   lptr = rptr = 0; hull[0] = init_;
    // 代表查詢的當下,右線段的高度已經低於左線段了
         return l1.eval(x) >= l2.eval(x);
     bool pop_back(Line &l1, Line &l2, Line &l3) {
        // 本題斜率遞減、上凸包
        // 因此只要 l2 跟
        l3 的 X 交點 <= l1 跟 l3 的 X 交點, l2 就用不到了
return (l3.b - l2.b)
* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
     void insert(Line L) {
        hull[++rptr] = L;
    return hull[lptr].eval(x);
    }
};
```

9.8 DNC [61c639]

```
constexpr int N = 3e3 + 5;
constexpr ll inf = 4e18;
// dp[k][j] = min(dp[k - 1][i] + cost[i][j])
// cost: (i, j]
ll dp[N][N]; // 1-based
ll get_cost(int l, int r) {}
void DNC(int k, int l, int r, int optl, int optr) {
    if (l > r) return;
    int m = (l + r) >> 1, opt = -1;
    dp[k][m] = inf;
    for (int i = max(k, optl); i <= min(m, optr); i++) {
        // 注意 i 的範圍 \ get_cost 與 dp 的邊界
        ll cur = dp[k - 1][i] + get_cost(i, m);
        if (cur < dp[k][m]) {
            dp[k][m] = cur, opt = i;
        }
    }
    DNC(k, l, m - 1, optl, opt);</pre>
```

9.9 LiChaoSegmentTree [a6e320]

```
constexpr ll Inf = 4e18;
// dp[i] = min(f[j] * s[i] + dp[j])
// v = m x + b
// y =
struct Line {
     ll m, b;
li m, b;
Line(ll m = 0, ll b = Inf) : m(m), b(b) {}
ll eval(ll x) const { return m * x + b; }
struct LiChaoSeg { // 取 max 再變換就好
     int n;
vector <Line > info;
     LiChaoSeg(int n_ = 0) { init(n_); }

void init(int n_ = 0) {
           n = n_;
           info.assign(4 << \__lg(n), Line());
     void update(Line line, int node, int l, int r) {
   int m = (l + r) / 2;
   bool left = line.eval(l) < info[node].eval(l);</pre>
           bool mid = line.eval(m) < info[node].eval(m);</pre>
           if (mid) swap(info[node], line); // 如果新線段比較好
           else if (left != mid) update(line, 2 * node, l, m);
           // 代表左半有交點
           else update(line, 2 * node + 1, m, r);
           // 代表如果有交點一定在右半
     void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
   if (r · l == 1) return info[node].eval(x);
   int m = (l + r) / 2;
   if (x < m) return</pre>
                 min(info[node].eval(x), query(x, 2 * node, l, m));
           else return min(
                 info[node].eval(x), query(x, 2 * node + 1, m, r));
     ill query(int x) { return query(x, 1, 0, n); }
```

9.10 Codeforces Example [7d37ea]

```
// CF 1932 pF
// 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
// 請問在線段不重複的情況下,最多獲得幾分
int main() {
    int n, m;
    cin >> n >> m;
    // 記錄每點有幾個線段
     // 再一個紀錄,包含這個點的左界
    cnt[l]++;
         cnt[r + 1]--;
    for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
    for (int i = n; i >= 2; i--) {
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
    vector<int> dp(n + 1);
    for (int i = 1; i <= n; i++) {
    dp[i] = cnt[i];
    if (l_side[i] != inf) {</pre>
              dp[i] += dp[l_side[i] - 1];
         dp[i] = max(dp[i], dp[i - 1]);
    cout << dp[n] << "\n";
// CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
// 再加上 max(bi) - min(bi)
int main(){
    int n, k, ans = 0; cin >> n >> k;
vector <pri>v(n + 1);
for (int i = 1; i <= n; i++) {</pre>
         int a, b; cin >> a >> b;
v[i] = {a, b};
         if (a <= k) ans = 1;
```

10 Geometry

10.1 Basic [d41d8c]

```
template < class T>
struct Point {
     T x, y;
Point(const T &x_ = 0, const T &y_ = 0) : x(x_), y(y_) {}
template < class U >
         return Point <U >(U(x), U(y));
     Point &operator+=(const Point &p) & {
    x += p.x; y += p.y; return *this;
     Point &operator -= (const Point &p) & {
    x -= p.x; y -= p.y; return *this;
     Point & operator *= (const T & v) & {
          x *= v; y *= v; return *this
     Point & operator /= (const T & v) & {
          x /= v; y /= v; return *this;
     Point operator - () const {
    return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
   return a += b;
     friend Point operator - (Point a, const Point &b) {
    return a -= b;
     friend Point operator*(Point a, const T &b) {
    return a *= b;
     friend Point operator/(Point a, const T &b) {
     friend Point operator*(const T &a, Point b) {
   return b *= a;
     friend bool operator==(const Point &a, const Point &b) {
          return a.x == b.x && a.y == b.y;
     friend istream &operator>>(istream &is, Point &p) {
          return is >> p.x >> p.y;
     friend ostream & operator < <(ostream & os, const Point & p) {
    return os << "(" << p.x << ", " << p.y << ")";</pre>
template < class T>
struct Line {
     Point<T>
     Point<T> b;
     template < class T>
T dot(const Point<T> &a, const Point<T> &b) {
   return a.x * b.x + a.y * b.y;
template < class T>
T cross(const Point < T > &a, const Point < T > &b) {
    return a.x * b.y - a.y * b.x;
template < class T>
T square(const Point<T> &p) {
     return dot(p, p);
double length(const Point<T> &p)
     return sqrt(double(square(p)));
double length(const Line<T> &l) {
     return length(l.a - l.b);
template < class T>
```

```
Point<T> normalize(const Point<T> &p) {
      return p / length(p);
template < class T>
bool parallel(const Line<T> &l1, const Line<T> &l2) {
      return cross(l1.b - l1.a, l2.b - l2.a) == 0;
double distance(const Point<T> &a, const Point<T> &b) {
      return length(a - b);
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)</pre>
      return distance(p, l.a);

if (dot(p - l.b, l.a - l.b) < 0)

return distance(p, l.b);
       return distancePL(p, 1);
template < class T>
Point < T > rotate(const Point < T > &a) {
      return Point(-a.y, a.x);
template < class T>
int sgn(const Point<T> &a) {
      return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
      return cross(l.b - l.a, p - l.a) > 0;
template < class T>
Point < T
       > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
       return l1.a + (l1.b - l1.a) * (cross(l2.b - l2.a, l1.a - l1.b));
template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
    return cross(p - l.a, l.b - l.a) == 0 &&
      return cross(p - l.a, l.b - l.a) == 0 \& \& \min(l.a.x, l.b.x) <= p.x \& p.x <= max(l.a.x, l.b.x)
                     (l.a.y, l.b.y) \ll p.y \ll max(l.a.y, l.b.y);
template<class T>
bool pointInPolygon
       (const Point<T> &a, const vector<Point<T>> &p) {
      int n = p.size(), t = 0;
for (int i = 0; i < n; i++) {
    if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {</pre>
                   return true;
       for (int i = 0; i < n; i++) {
             auto u = p[i];
             auto v = p[(i + 1) \% n];
             if (u.x < a.
                     x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
                   t ^= 1;
             if (u.x >= a
                     .x && v.x < a.x && pointOnLineLeft(a, Line(u, v)))</pre>
                   t ^= 1:
       return t == 1;
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
tuple < int , Point < T > , Point < T >> segmentIntersection
      (const Line<T> &l1, const Line<T> &l2) {
if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
   return {0, Point<T>(), Point<T>()};
      return {0, Point<T>(), Point<T>()};
if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
    return {0, Point<T>(), Point<T>()};
if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y))
    return {0, Point<T>(), Point<T>()};
if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y))
    return {0, Point<T>(), Point<T>()};
if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
    if (cross(l1.b - l1.a, l2.a - l1.a) != 0) {
        return {0, Point<T>(), Point<T>()};
} else {
             } else {
                   auto maxx1 = max(l1.a.x, l1.b.x);
auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
                   auto miny1 = min(l1.a.y, l1.b.y);
auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.y, l2.b.y);
auto miny2 = min(l2.a.y, l2.b.y);
auto miny2 = min(l2.a.y, l2.b.y);
                   Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
                    if (!pointOnSegment(p1, l1))
                    swap(p1.y, p2.y);
if (p1 == p2) {
                          return {3, p1, p2};
```

```
} else {
                                         return {2, p1, p2};
                   }
         return {1, p, p};
                    return {3, p, p};
template < class T>
double distanceSS(const Line<T> &11, const Line<T> &12) {
   if (get<0>(segmentIntersection(l1, l2)) != 0)
                     return 0.0;
          return min({distancePS(l1.a, l2), distancePS(l1
                      .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
template < class T>
bool segmentInPolygon
          (const Line<T> &l, const vector<Point<T>> &p) {
int n = p.size();
          int n = p.size();
if (!pointInPolygon(l.a, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
for (int i = 0; i < n; i++) {
    auto u = p[i];
    if i = 0; i < n; i + n
                     auto v = p[(i + 1) \% n];
                    auto v = p[(i + 1) % n];
auto w = p[(i + 2) % n];
auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
if (t == 1) return false;
if (t == 0) continue;
if (t == 2) {
                               if (pointOnSegment(v, l) && v != l.a && v != l.b)
    if (cross(v - u, w - v) > 0)
        return false;
                    } else {
                               if (p1 != u && p1 != v) {
    if (pointOnLineLeft(l.a, Line(v, u))
                                                    || pointOnLineLeft(l.b, Line(v, u)))
                                                    return false;
                              } else if (p1 == v) {
   if (l.a == v) {
                                                   if (pointOnLineLeft(u, l)) {
    if (pointOnLineLeft(w, l))
                                                                        && pointOnLineLeft(w, Line(u, v)))
                                                                        return false:
                                                              return false;
                                         } else if (l.b == v) {
                                                    if (pointOnLineLeft(u, Line(l.b, l.a))) {
    if (pointOnLineLeft(w, Line(l.b, l.a))
                                                                         && pointOnLineLeft(w, Line(u, v)))
                                                                         return false:
                                                  } else {
   if (pointOnLineLeft(w, Line(l.b, l.a))
        || pointOnLineLeft(w, Line(u, v)))
        return false;
                                         } else {
   if (pointOnLineLeft(u, l)) {
                                                              return false:
                                                   }
                                         }
                             }
                   }
          return true:
template<class T>
vector<Point<T>> hp(vector<Line<T>> lines) {
          auto d1 = l1.b - l1.a;
auto d2 = l2.b - l2.a;
                     if (sgn(d1) != sgn(d2))
                               return sgn(d1)
                    return cross(d1, d2) > \theta;
          deque<Line<T>> ls;
          deque<Point<T>> ps;
for (auto l : lines) {
                    if (ls.empty())
                               ls.push_back(l);
                               continue:
                    while (!ps.empty() && !pointOnLineLeft(ps.back(), l))
```

10.2 Convex Hull [b5758d]

```
int main() {
    int n; cin >> n;
      vector <P> P(n), U, L;
for (int i = 0; i < n; i++) {
    cin >> P[i];
      sort(P.begin(), P
            .end(), [](const Point<i64> &a, const Point<i64> &b) {
return a.x == b.x ? a.y < b.y : a.x < b.x;
      for (int i = 0; i < n; i++) {
   while (L.size() >= 2 && cross(L.back() -
        L[L.size() - 2], P[i] - L[L.size() - 2]) <= 0LL) {</pre>
                  L.pop_back();
            while (U.size() >= 2 && cross(U.back() -
    U[U.size() - 2], P[i] - U[U.size() - 2]) >= 0LL){
                  U.pop_back();
            if (L.
                   empty() || !(L.back() == P[i])) L.push_back(P[i]);
            if (U.
                   empty() || !(U.back() == P[i])) U.push_back(P[i]);
      if (L.size() <= 2 && U.size() <= 2) {
            // No Hull
      cout << L.size() + U.size() - 2 << "\n";
      for (int i = 0; i < L.size() - 1; i++) {
    cout << L[i].x << " " << L[i].y << " | n";
      for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << " | n";</pre>
}
```

10.3 MinEuclideanDistance [3020bc]

```
template < class T>
T distanceSquare(const Point<T> &a, const Point<T> &b) {
     return square(a - b);
void solve() {
     ll x, y;
          cin >> x >> y;
a[i] = Point<ll>(x, y);
     struct sortY {
          bool operator
    ()(const Point<ll> &a, const Point<ll> &b) const {
                return a.y < b.y;</pre>
          }
     struct sortXY {
          bool operator
    ()(const Point<ll> &a, const Point<ll> &b) const {
                if (a.x == b.x) return a.y < b.y;
else return a.x < b.x;</pre>
          }
     sort(a.begin(), a.end(), sortXY());
vector<Point<ll>> t(n);
auto devide = [&](auto &&self, int l, int r) -> ll {
          if (l == r) return inf;
int m = (l + r) / 2;
ll ans = min(self(self, l, m), self(self, m + 1, r));
          ll midval = a[m].x;
          ll p = 0;
          for (int i = l; i <= r; i++) {
   if ((midval - a[i].x) * (midval - a[i].x) <= ans) {</pre>
                     t[p++] = a[i];
```

10.4 LatticePoints [00db9d]

10.5 MinCoverCircle [c9ca81]