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```

# 1 Basic

# 1.1 Install VScode [d41d8c]

## 1.2 Default Code [d41d8c]

```
#include <bits/stdc++.h>
#pragma GCC optimize("03")
// #pragma GCC target("popent")
// C++ 20 vector grammer will not work
#define all(x) (x).begin(), (x).end()
using namespace std;
using ll = long long;

void solve() {
}
int main() {
   ios_base::sync_with_stdio(false);
   cin.tie(nullptr);
   int t = 1;
   cin >> t;
   while (t--) {
      solve();
   }
}
```

#### 1.3 Compare Fuction [d41d8c]

```
struct cmp {
    vector < int > &v;
                    // 要在 template 的資結用外部變數
     cmp(vector<int>& vec) : v(vec) {}
bool operator() (int a, int b) const {
   return v[a] > v[b];
// main: cmp cmp1(vector);
// main. cmp cmp1(vector),
// priority_queue<int, vector<int>, cmp> pq(cmp1);
};
1.4 Pbds [d41d8c]
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < typename T>
using pbds_set = tree<T, null_type,</pre>
using pdds_set = tree<\(\), nutl_type,
  less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template<typename T>
using pbds_multiset = tree<T, null_type, less_equal
  <T>, rb_tree_tag, tree_order_statistics_node_update>;
1.5 Edouble [d41d8c]
struct EDouble {
     constexpr static double Eps = 1e-9;
constexpr EDouble() : x{} {}
constexpr EDouble(double v) : x{v} {}
      constexpr double val() const {
          return x:
     explicit constexpr operator double() const {
          return x;
     constexpr EDouble operator-() const {
          return EDouble(-x);
     constexpr EDouble &operator+=(const EDouble &rhs) & {
          x += rhs.x
           return *this:
     constexpr EDouble &operator -=(const EDouble &rhs) & {
          x -= rhs.x;
return *this;
     constexpr EDouble &operator*=(const EDouble &rhs) & {
          x *= rhs.x:
           return *this;
     constexpr EDouble &operator/=(const EDouble &rhs) & {
   assert(fabs(rhs.x) > Eps);
          x /= rhs.x;
return *this;
             EDouble operator+(EDouble lhs, const EDouble &rhs) {
           lhs += rhs;
     friend constexpr
            EDouble operator - (EDouble lhs, const EDouble &rhs) {
           lhs -= rhs;
           return lhs:
             EDouble operator*(EDouble lhs, const EDouble &rhs) {
           lhs *= rhs;
           return lhs;
      friend constexor
             EDouble operator/(EDouble lhs, const EDouble &rhs) {
          lhs /= rhs;
return lhs;
      friend constexpr bool
             operator <(const EDouble &lhs, const EDouble &rhs) {</pre>
           return lhs.x - rhs.x < -Eps:
      friend constexpr bool
             operator > (const EDouble &lhs, const EDouble &rhs) {
           return lhs.x - rhs.x > Eps;
     friend constexpr bool
    operator==(const EDouble &lhs, const EDouble &rhs) {
           return fabs(lhs.x - rhs.x) < Eps;</pre>
     friend constexpr bool
             operator <= (const EDouble &lhs, const EDouble &rhs) {</pre>
           return lhs < rhs || lhs == rhs;</pre>
      friend constexpr bool
             operator >=(const EDouble &lhs, const EDouble &rhs) {
           return lhs > rhs || lhs == rhs;
           operator!=(const EDouble &lhs, const EDouble &rhs) {
return !(lhs == rhs);
     friend istream & operator >> (istream &is, EDouble &a) {
```

# 2 Graph

# 2.1 DFS And BFS [cdd1d5]

```
int main() {
       vector < vector < int >> adi(n + 1, vector < int >());
       // dfs graph
       // afs_graph
vector <bool> vis(n + 1, 0);
auto dfs = [&](auto self, int u) -> void {
    if (vis[u]) return;
    vis[u] = true;
    for (auto v: adj[u]) {
        self(self, v);
    }
}
             }
       dfs(dfs, 1);
       // bfs
       vector<int> depth(n + 1, 1e9);
       queue <int> q;
auto bfs = [&](auto self, int u) -> void {
             vis[u] = true;
depth[u] = 0;
             q.push(u);
while (!q.empty()) {
                    int u = q.front(); q.pop();
                    for (auto v : adj[u]) {
    if (vis[v]) continue;
                           vis[v] = true;
depth[v] = depth[u] + 1;
                           q.push(v);
             }
       bfs(bfs, 1);
}
```

#### 2.2 Prim [f00ec0]

# 2.3 BellmanFord [430ded]

```
|// 用 Bellman Ford 找負環
int main() {
    int n, m; cin >> n >> m;
    vector <array <int, 3>> e;
    for (int i = 0; i < m; i++) {
        int u, v, w; cin >> u >> v >> w;
        u--, v--; e.push_back({u, v, w});
    }
    vector <ll>    dis(n, inf), par(n);
    int t = -1; dis[0] = 0;
    for (int i = 1; i <= n; i++) {
        for (auto [u, v, w] : e) {
            if (dis[v] > dis[u] + w) {
                  dis[v] = dis[u] + w;
                  par[v] = u;
```

```
if (i == n) t = v;
}
}
if (t == -1) { cout << "NO\n"; return; }
for (int i = 1; i < n; i++) t = par[t];
vector<int> ans {t};
int i = t;
do {
    i = par[i];
    ans.push_back(i);
} white (i != t);
reverse(ans.begin(), ans.end());
cout << "YES[n";
for (auto x : ans) cout << x + 1 << " ";</pre>
```

# 2.4 FloydWarshall [206b76]

}

#### 2.5 Euler [4177dc]

```
| // 1. 無向圖是歐拉圖:
// 非零度頂點是連通的
// 頂點的度數都是偶數
// 2. 無向圖是半歐拉圖(有路沒有環):
// 非零度頂點是連通的
// 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
// 非零度頂點是強連通的
// 每個頂點的入度和出度相等
// 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
| // 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
// 其他頂點的入度和出度相等
vector <int> ans;
auto dfs = [&](auto &&self, int u) -> void {
    while (g[u].size()) {
       int v = *g[u].begin();
       g[u].erase(v);
       self(self, v):
    ans.push_back(u);
dfs(dfs, 0);
reverse(ans.begin(), ans.end());
```

#### 2.6 SCC [5d3e16]

```
struct SCC {
    int n, cur, cnt;
    vector<vector<int>> adj;
    vector<int>> stk, dfn, low, bel;
    SCC(int n_ = 0) {
        init(n_);
    }
    void init(int n_) {
        n = n_;
        adj.assign(n, {});
        dfn.assign(n, -1);
        low.resize(n);
        bel.assign(n, -1);
        stk.clear();
```

```
cur = cnt = 0:
        void addEdge(int u, int v) {
   adj[u].push_back(v);
        void dfs(int x) {
    dfn[x] = low[x] = cur++;
               stk.push_back(x);

for (auto y : adj[x]) {

    if (dfn[y] == -1) {
                      dfs(y);
  dfs(y);
  low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
  low[x] = min(low[x], dfn[y]);
               if (dfn[x] == low[x]) {
                      int y;
do {
                              y = stk.back();
                      bel[y] = cnt;
stk.pop_back();
} while (y != x);
                      cnt++:
       vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
    }
}</pre>
               return bel:
        struct Graph {
               int n:
               vector<pair<int, int>> edges;
               vector < int > siz;
vector < int > cnte;
        Graph compress() {
               Graph g;
g.n = cnt;
               g.siz.resize(cnt);
               g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;</pre>
                       for (auto j : adj[i]) {
    if (bel[i] != bel[j]) {
        g.edges.emplace_back(bel[i], bel[j]);
}
                              } else {
                                     g.cnte[bel[i]]++;
                      }
               return g;
};
```

# 2.7 VBCC [170604]

```
struct VBCC {
     int n, cur;
     vector<vector<int>> adj;
     vector < int > dfn, low, parent;
vector < bool > is_cut;
     VBCC(int n_ = 0) {
    init(n_);
     void init(int n_) {
          n = n_;
adj.assign(n, {});
          dfn.assign(n, -1);
low.resize(n);
          parent.assign(n, -1);
is_cut.assign(n, false);
     void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
     void dfs(int x) {
          int children = 0;
dfn[x] = low[x] = cur++;
for (int v : adj[x]) {
                if (dfn[v] == -1) {
                     children++:
                     parent[v] = x;
                      low[x] = min(low[x], low[v]);
                      if (parent[x] != -1 && low[v] >= dfn[x]) {
                           is_cut[x] = true;
                } else if (v != parent[x]) {
                     low[x] = min(low[x], dfn[v]);
           if (parent[x] == -1 && children > 1) {
                is_cut[x] = true;
          }
     void work() {
```

```
for (int i = 0; i < n; i++) {
    if (dfn[i] == -1) {
        dfs(i);
     }
}
};</pre>
```

#### 2.8 EBCC [49d862]

```
struct EBCC { // CF/contest/1986/pF
   int n, cur, cnt;
       vector<int>> adj;
       vector <int> stk, dfn, low, bel;
vector<pair<int, int>> bridges; // 關鍵邊
       EBCC(int n_) {
   init(n_);
       void init(int n_) {
             n = n_;
              adj.assign(n, {});
             dfn.assign(n, -1);
low.resize(n);
             bel.assign(n,
              stk.clear();
              bridges.clear();
             cur = cnt = 0;
       void addEdge(int u, int v) {
             adj[u].push_back(v);
              adj[v].push_back(u);
       }
void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
    stk.push_back(x);
    for (auto y : adj[x]) {
        if (y == p) continue;
        if (dfn[y] == -1) {
            dfs(y, x);
            low[x] = min(low[x], low[y]);
        if (low[v] > dfn[x]) {
                          if (low[y] > dfn[x]) {
    bridges.emplace_back(x, y);
                    } else if (bel[y] == -1) {
    low[x] = min(low[x], dfn[y]);
              if (dfn[x] == low[x]) {
                    int y;
do {
                          y = stk.back();
                          bel[y] = cnt;
                          stk.pop_back();
                    } while (y != x);
                    cnt++;
             }
       vector < int > work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {</pre>
                          dfs(i, -1);
              return bel;
       struct Graph {
             vector<pair<int, int>> edges;
             vector<int> siz; // BCC 內節點數
             vector<int> cnte; // BCC 內邊數
       Graph compress() {
             Graph g;
             g.n = cnt;
             g.siz.resize(cnt);
g.cnte.resize(cnt);
              for (int i = 0; i < n; i++) {
                    g.siz[bel[i]]++;
                    for (auto j : adj[i]) {
    if (bel[i] < bel[j]) {</pre>
                                g.edges.emplace_back(bel[i], bel[j]);
                          } else if (i < j) {
   g.cnte[bel[i]]++;</pre>
                    }
              return g;
       }
1:
```

#### 2.9 2-SAT [eeddc1]

```
// CSES Giant Pizza
struct TwoSat {
  int n;
  vector<vector<int>> e;
  vector<bool> ans;
  TwoSat(int n) : n(n), e(2 * n), ans(n) {}
  void addClause(int u, bool f, int v, bool g) {
    e[2 * u + !f].push_back(2 * v + g);
    e[2 * v + !g].push_back(2 * u + f);
```

```
bool satisfiable() {
             \verb|vector<| \textbf{int}|
             > id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
vector<int> stk;
             int now = 0, cnt = 0;
function<void(int)> tarjan = [&](int u) {
                  stk.push_back(u);
dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
                                tarjan(v);
                         low[u] = min(low[u], low[v]);

else if (id[v] == -1) { // in some low[u] = min(low[u], dfn[v]);
                    if (dfn[u] == low[u]) {
                          do {
                                v = stk.back();
                         stk.pop_back();
id[v] = cnt;
} while (v != u);
                  }
            };
for (int i
             return true:
       vector < bool > answer() { return ans; }
};
int main() {
      int m, n; cin >> m >> n;
TwoSat ts(n);
for (int i = 0; i < m; ++i) {</pre>
            int u, v; char x, y;
cin >> x >> u >> y >> v;
ts.addClause(u - 1, x == '+', v - 1, y == '+');
      if (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";</pre>
      else cout << "IMPOSSIBLE\n";</pre>
```

#### 2.10 Funtional Graph [85c464]

```
constexpr int N = 2e5 + 5;
int cht[N][31]; // 倍增表, 放外面不然 TLE struct FuntionalGraph {
        int n, cnt;
vector < int > g, bel, id, len, in, top;
FuntionalGraph() : n(0) {}
         FuntionalGraph(vector<int> g_) { init(g_); }
        void init(vector <int> g_) {
    n = g_.size(); cnt = 0;
    g = g_; bel.assign(n, -1);
    id.resize(n); len.clear();
    in.assign(n, 0); top.assign(n, -1);
    id.id.)
                 build();
        in[g[i]]++;
                 for (int i = 1; i <= 30; i++)
    for (int u = 0; u < n; u++)
        cht[u][i] = cht[cht[u][i - 1]][i - 1];
for (int i = 0; i < n; i++)
    if (in[i] == 0) label(i);
for (int i = 0; i < n; i++)
    if (top[i] == -1) label(i);</pre>
        void label(int u) {
   vector < int > p; int cur = u;
}
                 while (top[cur] == -1) {
                         top[cur] = u;
p.push_back(cur);
                         cur = g[cur];
                 auto s = std::find(p.begin(), p.end(), cur);
vector < int > cyc(s, p.end());
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {
    bel[cyc[i]] = cnt;
}</pre>
                         id[cyc[i]] = i;
                 for (int i = p.size() - 1; i > 0; i--)
   id[p[i - 1]] = id[p[i]] - 1;
         int jump(int u, int k) {
   for (int b = 0; k > 0; b++){
```

## 3 Data Structure

#### 3.1 BIT [d41d8c]

```
| template <typename T>
 struct Fenwick { // 全部以 0 based 使用
        int n;
        vector<T> a;
        Fenwick(int n_ = 0) {
             init(n_);
        void init(int n_) {
              a.assign(n, T{});
        void add(int x, const T &v) {
   for (int i = x + 1; i <= n; i += i & -i) {
      a[i - 1] = a[i - 1] + v;
}</pre>
        T sum(int x) { // 左閉右開查詢
              T ans{};
for (int i = x; i > 0; i -= i & -i) {
    ans = ans + a[i - 1];
       TrangeSum(int l, int r) { // 左閉右開查詢return sum(r) - sum(l);
        int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
             int x = 0;
T cur{};
for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n && cur + a[x + i - 1] <= k) {</pre>
                          `x += i;
                           cur = cur + a[x - 1];
                    }
              return x;
       }
 template <class T>
 struct TwoDFenwick { // 全部以 0 based 使用
        int nx, ny; // row, col 個數
vector<vector<T>> a;
       TwoDFenwick(int nx_ = 0, int ny_ = 0) {
   init(nx_, ny_);
        void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
        void add(int x, int y, const T &v) {
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            a[i - 1][j - 1] = a[i - 1][j - 1] + v;
        }
}</pre>
             }
       T sum(int x, int y) { // 左閉右開查詢

T ans{};

for (int i = x; i > 0; i -= i & -i) {

   for (int j = y; j > 0; j -= j & -j) {

      ans = ans + a[i - 1][j - 1];
              return ans:
        T rangeSum
               (int lx, int ly, int rx, int ry) { // 左閉右開查詢
              return sum(
    rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
1:
 3.2 RangeBit [d41d8c]
```

```
| template <typename T>
| struct rangeFenwick { // 全部以 0 based 使用 int n; vector <T> d, di; rangeFenwick(int n_ = 0) { init(n_); }
| void init(int n_) { n = n_; d.assign(n, T{}); di.assign(n, T{}); }
| void add(int x, const T &v) { T vi = v * (x + 1); for (int i = x + 1; i <= n; i += i & -i) {
```

siz.assign(n, 1);

```
d[i - 1] = d[i - 1] + v;
di[i - 1] = di[i - 1] + vi;
                                                                                                                 int find_boss(int x) {
                                                                                                                       if (boss[x] == x) return x;
return boss[x] = find_boss(boss[x]);
             }
       void rangeAdd(int l, int r, const T &v) {
                                                                                                                bool same(int x, int y) {
    return find_boss(x) == find_boss(y);
             add(l, v); add(r, -v);
      T sum(int x) { // 左閉右開查詢
                                                                                                                bool merge(int x, int y) {
    x = find_boss(x);
    y = find_boss(y);
    if (x == y) {
             T ans{};
             for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
                                                                                                                             return false;
                                                                                                                       if(siz[x] < siz[y]) swap(x, y);</pre>
                                                                                                                       siz[x] += siz[y];
      TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
                                                                                                                       boss[y] = x;
                                                                                                                       return true;
      int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
                                                                                                                int size(int x) {
    return siz[find_boss(x)];
             int x = 0:
            int x - 0,
T cur{};
for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n) {
        real - T(</pre>
                                                                                                          };
                          x + i + 1) * d[x + i - 1] - di[x + i - 1];

if (cur + val <= k) {

x += i;
                                                                                                          struct DSU {
                                                                                                                int n;
vector<int> boss, siz, stk;
                                cur = cur + val;
                                                                                                                DSU() {}
                         }
                                                                                                                DSU(int n_) {
                  }
                                                                                                                       init(n_);
             return x:
                                                                                                                void init(int n_) {
      }
                                                                                                                       n = n_;
boss.resize(n);
template <class T>
                                                                                                                       iota(boss.begin(), boss.end(), \theta);
struct rangeTwoDFenwick { // 全部以 0 based 使用
                                                                                                                       siz.assign(n, 1);
stk.clear();
      int nx, ny; // row, col 個數
vector<vector<T>> d, di, dj, dij;
      rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
  init(nx_, ny_);
                                                                                                                int find(int x) {
    return x == boss[x] ? x : find(boss[x]);
      void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
}
                                                                                                                bool same(int x, int y) {
    return find(x) == find(y);
                                                                                                                bool merge(int x, int y) {
                                                                                                                      x = find(x);
y = find(y);
                                                                                                                       if (x == y) {
    return false;
      }
void add(int x, int y, const T &v) {
    T vi = v * (x + 1);
    T vj = v * (y + 1);
    T vij = v * (x + 1) * (y + 1);
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            d[i - 1][j - 1] = d[i - 1][j - 1] + v;
            di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
            dj[i - 1][j - 1] = dj[i - 1][j - 1] + vi;
            dij[i - 1][j - 1] = dij[i - 1][j - 1] + vi;
}</pre>
                                                                                                                       if (siz[x] < siz[y]) swap(x, y);</pre>
                                                                                                                       siz[x] += siz[y];
boss[y] = x;
                                                                                                                       stk.push_back(y);
                                                                                                                       return true:
                                                                                                                void undo(int x) {
    while (stk.size() > x) {
        int y = stk.back();
}
                   }
            }
                                                                                                                             stk.pop_back();
       void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
            add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
                                                                                                                             siz[boss[y]] -= siz[y];
                                                                                                                             boss[y] = y;
                                                                                                                      }
                                                                                                                int size(int x) {
      T sum(int x, int y) { // 左閉右開查詢 T_ans{};
                                                                                                                       return siz[find(x)];
                                                                                                                }
                                                                                                        1:
             for (int i = x; i > 0; i -= i & -i) {
                   for (int j = y; j > 0; j -= j & -j) {
    ans = ans
                                                                                                          3.4 Segment [d41d8c]
                          + T(x * y + x + y + 1) * d[i - 1][j - 1];  ans = ans - T(y + 1) * d[i - 1][j - 1];  ans = ans - T(x + 1) * d[i - 1][j - 1]; 
                                                                                                         template <class Info>
                                                                                                          struct Seg { // 左閉右開寫法
int n; vector<Info> info;
Seg(): n(0) {}
                          ans = ans + dij[i - 1][j - 1];
                   }
                                                                                                                Seg(int n_{-}, Info v_{-} = Info()) {
             return ans;
                                                                                                                       init(n_, v_);
      T rangeSum
                                                                                                                 template <class T>
                                                                                                                Seg(vector<T> init_) {
   init(init_);
              (int lx, int ly, int rx, int ry) { // 左閉右開查詢
             return sum(
                    rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
                                                                                                                void init(int n_, Info v_ = Info()) {
  init(vector(n_, v_));
};
3.3 DSU [d41d8c]
                                                                                                                template <class T>
void init(vector<T> init_) {
struct DSU {
                                                                                                                       n = init_.size();
      int n;
vector<int> boss, siz;
                                                                                                                       info.assign(4 << __lg(n), Info());</pre>
                                                                                                                       DSU() {}
DSU(int n_) {
             init(n_);
                                                                                                                                   return:
       void init(int n_) {
                                                                                                                             int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
             boss.resize(n):
             iota(boss.begin(), boss.end(), 0);
```

pull(p);

tag[p].apply(v);

void push(int p, int l, int r) {

```
int m = (l + r) / 2;
if (r - l >= 1) {
    apply(p * 2, l, m, tag[p]);
    apply(p * 2 + 1, m, r, tag[p]);
           build(1, 0, n);
     void pull
    (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
           modify(int p, int l, int r, int x, const Info &v) {
if (r - l == 1) {
   info[p] = v;
                                                                                                         tag[p] = Tag();
                                                                                                    void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
                                                                                                         if (r - l == 1)
    info[p] = v;
           int m = (l + r) / 2;
if (x < m) {
    modify(2 * p, l, m, x, v);</pre>
                                                                                                               return;
                                                                                                         int m = (l + r) / 2;
push(p, l, r);
if (x < m) {</pre>
           } else {
                modify(2 * p + 1, m, r, x, v);
                                                                                                               modify(2 * p, l, m, x, v);
           pull(p);
                                                                                                         } else {
                                                                                                               modify(2 * p + 1, m, r, x, v);
     void modify(int p, const Info &i) {
                                                                                                         pull(p);
           modify(1, 0, n, p, i);
     Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    return query(p *</pre>
                                                                                                    void modify(int p, const Info &i) {
                                                                                                         modify(1, 0, n, p, i);
                                                                                                    Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;</pre>
                 2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
                                                                                                          push(p, l, r);
                                                                                                          return query(p *
            (int ql, int qr) { return query(1, 0, n, ql, qr); }
                                                                                                                2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
     template < class F> // 尋找區間內,第一個符合條件的
     int findFirst
           (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)</pre>
                                                                                                    Info query
                                                                                                          (int ql, int qr) { return query(1, 0, n, ql, qr); }
                                                                                                    void range_apply
           return -1;
if (l >= x && r <= y && !pred(info[p]))
                                                                                                         (int p, int l, int r, int ql, int qr, const Tag &v) {
if (qr <= l || ql >= r) return;
if (ql <= l && r <= qr) {</pre>
                return -1;
           if (r - l == 1)
    return l;
int m = (l + r) / 2;
                                                                                                               apply(p, l, r, v);
                                                                                                               return:
           int res = findFirst(2 * p, l, m, x, y, pred);
                                                                                                         int m = (l + r) / 2;
           if (res == -1)
                                                                                                         push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
                res = findFirst(2 * p + 1, m, r, x, y, pred);
           return res;
     }
                                                                                                         pull(p);
     template < class F> // 若要找 last,先右子樹遞迴即可
int findFirst(int l, int r, F & & pred) {
    return findFirst(1, 0, n, l, r, pred);
                                                                                                    void range_apply(int l, int r, const Tag &v) {
    range_apply(1, 0, n, l, r, v);
                                                                                                    }
                                                                                                                              // 尋找區間內,第一個符合條件的
   ---define structure and info plus---
                                                                                                    template < class F>
                                                                                                    int findFirst
struct Info {
                                                                                                         (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
   return -1;</pre>
     int n = 1;
     int sum = 0;
Info operator+(const Info &a, const Info &b) {
                                                                                                         if (l >= x && r <= y && !pred(info[p])) {</pre>
     return { a.n + b.n, a.sum + b.sum };
                                                                                                               return -1:
3.5 Lazy Segment [d41d8c]
                                                                                                         if (r - l == 1) {
                                                                                                               return l;
template <class Info, class Tag>
struct LazySeg { // 左閉右開寫法
                                                                                                         int m = (l + r) / 2;
                                                                                                         push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
     int n;
     vector < Info > info;
     vector < Tag > tag;
LazySeg() : n(0) {}
LazySeg(int n_, Info v_ = Info()) {
                                                                                                         if (res ==
                                                                                                               res = findFirst(2 * p + 1, m, r, x, y, pred);
                                                                                                         return res;
           init(n_, v_);
     template <class T>
LazySeg(vector<T> init_) {
   init(init_);
                                                                                                    template < class F> // 若要找 last,先右子樹遞廻即可
int findFirst(int l, int r, F & pred) {
    return findFirst(1, 0, n, l, r, pred);
     void init(int n_, Info v_ = Info()) {
    init(vector(n_, v_));
                                                                                              };
// ---define structure and info plus---
                                                                                             struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add; void apply(const Tag& v) { if (v.set_val) {
     template <class T>
void init (vector<T> init_) {
           n = init_.size();
info.assign(4 << __lg(n), Info());
tag.assign(4 << __lg(n), Tag());</pre>
                                                                                                               `set_val =´v.set_val;
add = v.add;
           else {
                                                                                                               add += v.add;
                      info[p] = init_[l];
                                                                                                         }
                      return;
                                                                                                   }
                int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                                                                                              struct Info {
                                                                                                    int sum;
                                                                                                    pull(p);
           build(1, 0, n);
                                                                                                         sum += (r - l) * v.add;
     void pull
     (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
}
                                                                                                    // Info& operator=(const Info &rhs) {
                                                                                                             // 部分 assignment 使用 return *this;
```

// // // }

1:

sort(sorted.begin(), sorted.end());

```
Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
                                                                                                                    sorted.erase
                                                                                                                    }
3.6 Treap [d41d8c]
                                                                                                            }
struct Treap {
      Treap t
Treap *lc, *rc;
int pri, siz; bool rev_valid;
int val; int_min;
                                                                                                             4 Flow
       Treap(int val_) {
    min = val = val_;
    pri = rand();
                                                                                                             4.1 Dinic [287fe8]
                                                                                                             template < class T >
             lc = rc = nullptr;
siz = 1; rev_valid = 0;
                                                                                                             struct Dinic {
                                                                                                                   struct Edge {
                                                                                                                          int to;
       void pull() { // update siz or other information
                                                                                                                          T flow, cap; // 流量跟容量
             siz = 1:
                                                                                                                    int n, m, s, t;
T INF_FlOW = numeric_limits<T>::max() / 2;
             for (auto c : {lc, rc}) {
   if (!c) continue;
   siz += c->siz;
                                                                                                                    vector<vector<int>> adj; // 此點對應的 edges 編號
                                                                                                                    vector<Edge> edges; // 幫每個 edge 編號
                    min = std::min(min, c->min);
                                                                                                                    vector < Edge > edges; // 吊時間 edg
vector < int > dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
    n = n_; m = 0;
    dis.resize(n); ptr.resize(n);
             }
       void push() {
   if (rev_valid) {
                    swap(lc, rc);
if (lc) lc->rev_valid ^= 1;
if (rc) rc->rev_valid ^= 1;
                                                                                                                          adj.assign(n, vector<int>{});
                                                                                                                          edges.clear();
                                                                                                                    void add_edge(int u, int v, T cap) {
             rev_valid = false;
                                                                                                                          // 偶數 id 是正向邊
                                                                                                                          edges.push_back({ v, 0, cap });
edges.push_back({ u, 0, 0 });
adj[u].push_back(m++);
      int find(int k) { // 找到 min 是 k 的位置 (1-based)
             pusn();
int ls = (lc ? lc->siz : 0) + 1;
if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
                                                                                                                          adj[v].push_back(m++);
                                                                                                                    bool bfs() {
                                                                                                                          fill(dis.begin(), dis.end(), -1);
dis[s] = 0; queue<int> q;
      }
                                                                                                                          q.push(s);
int size(Treap *t) {
    return t ? t->siz : 0;
                                                                                                                           while (!q.empty() && dis[t] == -1) {
                                                                                                                                 int u = q.front(); q.pop();
for (int id : adj[u]) {
    Edge &e = edges[id];
Treap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
    a->push(); b->push();
    if (a->pri > b->pri) {
        a->rc = merge(a->rc, b);
        a->reli().
                                                                                                                                       if (e.flow == e.cap) continue;
if (dis[e.to] == -1) {
    dis[e.to] = dis[u] + 1;
                                                                                                                                              q.push(e.to);
             a->pull();
             return a;
                                                                                                                                 }
       else {
                                                                                                                           return dis[t] != -1;
             b->lc = merge(a, b->lc);
             b->pull();
                                                                                                                    T dfs(int u, T flow) {
             return b:
                                                                                                                          if (flow == 0) return 0;
if (u == t) return flow;
pair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first *, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
    t->push();
                                                                                                                          for (int
                                                                                                                                 &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {
Edge &e = edges[adj[u][cur]];
if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;
T mn = dfs(e.to, min(flow, e.cap - e.flow));
if (max = 20) [</pre>
       if (size(t->lc) < k) {
             auto [a, b] = split(t->rc, k - size(t->lc) - 1);
                                                                                                                                 if (mn > 0) {
             t - > rc = a:
                                                                                                                                       e.flow += mn;
             t->pull();
                                                                                                                                        edges[adj[u][cur] ^ 1].flow -= mn;
             return {t, b};
                                                                                                                                       return mn;
                                                                                                                                }
       else {
             auto [a, b] = split(t->lc, k);
t->lc = b;
                                                                                                                          return 0; // 到不了終點就會 return 0
             t->pull();
                                                                                                                    T work(int s_, int t_) {
    s = s_; t = t_; T flow = 0;
    while (bfs()) {
             return {a, t};
      }
                                                                                                                                 fill(ptr.begin(), ptr.end(), 0);
void Print(Treap *t) {
                                                                                                                                 while (true) {
   T res = dfs(s, INF_Flow);
   if (res == 0) break;
   flow += res;
      if (!t) return;
t->push();
       Print(t->lc);
      cout << t->val;
Print(t->rc);
                                                                                                                                 }
                                                                                                                          return flow:
3.7 Mo [d41d8c]
                                                                                                                           for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
struct query {
   int l, r, id;
} typedef query;
void MO(int n, vector<query> &queries) {
   int block = sqrt(n);
   firstice = sheal(query = query)> cmp = [
                                                                                                             };
                                                                                                             4.2 Min Cut [44ae6c]
                                                                                                          // CSES Police Chase
int main(){
  int n, m; cin >> n >> m;
  Dinic<int> g(n);
  for (int i = 0; i < m; i++) {
    int u, v, cap = 1;
    cin >> u >> v;
}
       function <bool(query, query)> cmp = [&](query a, query b) {
   int block_a = a.l / block;
   int block_b = b.l / block;
             if (block_a != block_b) return block_a < block_b;
return a.r < b.r;</pre>
       sort(queries.begin(), queries.end(), cmp);
                                                                                                                          u--: v--:
void compress(vector<int> &nums) {
                                                                                                                          q.add edge(u, v, cap);
       vector<int> sorted = nums;
                                                                                                                          g.add_edge(v, u, cap);
```

```
int res = g.work(0, n - 1);
cout << res << "\n";
if (res == 0) return;

vector <int> vis(n);
auto find = [&](auto self, int u) -> void {
    if (!vis[u]) {
        vis[u] = 1;
        for (int id : g.adj[u]) {
            auto e = g.edges[id];
            if (e.cap - e.flow > 0) {
                self(self, e.to);
            }
        }
     }
};
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
        auto e = g.edges[id];
        if (!vis[e.to]) {
            cout << i + 1 << " " << e.to + 1 << " \n";
        }
     }
}
</pre>
```

# 4.3 Hangarian [350fc3]

```
struct Hangarian { // 0-based
      int n, m; // 最小路徑覆蓋,二分匹配
vector<vector<int>>> adj;
      vector <int>> adj;
vector <int>> used, vis;
vector <pair <int, int>> match;
Hangarian(int n_ = 0, int m_ = 0) {
   init(n_, m_);
      void init(int n_ = 0, int m_ = 0) {
    n = n_; m = m_;
    adj.assign(n + m, vector<int>());
    used.assign(n + m, -1);
    vis.assign(n + m, 0);
      void addEdge(int u, int v) {
   adj[u].push_back(n + v);
   adj[n + v].push_back(u);
      vector<pair<int, int>> work() {
    match.clear();
             vis[v] = 1;
                                 if (used[v] == -1 || self(self, used[v])) {
                                        used[v] = u;
                                        return true:
                          }
                    return false;
             for (int i = 0; i < n; i++) {
    fill(vis.begin(), vis.end(), 0);</pre>
                    dfs(dfs, i);
             for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
                           match.emplace_back(used[i], i - n);
             return match;
}:
```

#### 4.4 MCMF [f667f8]

```
template < class Tf, class Tc>
struct MCMF {

    // 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就好
    int n, m, s, t;

    If INF_FLOW = numeric_limits < Tf>::max() / 2;

    Tc INF_COST = numeric_limits < Tc>::max() / 2;

    struct Edge {
        int to;

        If flow, cap; // 流量跟容量
        Tc cost;

    };

    vector < vector < int >> adj;

    vector < Edge > edges; // 幫每個 edge 編號
    vector < Tc > dis, pot; // johnson algorithm, using spfa

    vector < int > rt; // 路徑恢復, 對應 id
    vector < bool > inq;

    MCMF(int n_ = 0) {
        n = n_;
        m = 0;
        edges.clear();
```

```
adj.assign(n, vector<int>{});
void add_edge(int u, int v, Tf cap, Tc cost){
   edges.push_back({v, 0, cap, cost});
   edges.push_back({u, 0, 0, -cost});
       adj[u].push_back(m++);
       adj[v].push_back(m++);
bool spfa() {
       dis.assign(n, INF_COST);
rt.assign(n, -1); inq.assign(n, false);
       question q,
q.push(s), dis[s] = 0, inq[s] = true;
while (!q.empty()) {
   int u = q.front(); q.pop();
              q.push(v); inq[v] = true;
                      }
              }
       return dis[t] != INF_COST;
bool dijkstra() {
    dis.assign(n, INF_COST); rt.assign(n, -1);
    priority_queue<pair<Tc, int>,
        vector<pair<Tc, int>>> pq;
    dis[s] = 0; pq.emplace(dis[s], s);
    while (!pq.empty()) {
        vector(); respectively.
              auto [d, u] = pq.top(); pq.pop();
if (dis[u] < d) continue;
for (int id : adj[u]) {
    auto [v, flow, cap, cost] = edges[id];
    Tc ndis = dis[u] + cost + pot[u] - pot[v];
    if (flow < cap && dis[v] > ndis) {
        dis[v] = ndis; rt[v] = id;
        cap = captace(edis[v]);
}
                              pq.emplace(ndis, v);
       return dis[t] != INF_COST;
// 限定 flow,最小化 cost
pair<Tf, Tc> work_flow(int s_,
                                                         int t_, Tf need) {
       s = s_, t = t_; pot.assign(n, 0);
If flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] + potfil cost[]</pre>
                      dis[i] += pot[i] - pot[s];
               Tf f = INF_FLOW;
               for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                               (f, edges[rt[i]].cap - edges[rt[i]].flow);
               f = min<Tf>(f, need);
               for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
               flow += f; need -= f;
cost += f * dis[t]; fr = false;
               swap(dis, pot);
if (need == 0) break;
       return make_pair(flow, cost);
// 限定 cost,最大化 flow
pair<Tf, Tc> work_budget(int s_, int t_, Tc budget) {
       s = s_, t = t_; pot.assign(n, 0);
If flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] += pot[i] - pot[s];
}</pre>
               ff f = INF_FLOW;
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
                               (f, edges[rt[i]].cap - edges[rt[i]].flow);
               f = min<Tf>(f, budget / dis[t]);
               for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
   edges[rt[i]].flow += f;
   edges[rt[i] ^ 1].flow -= f;
               flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
               swap(dis, pot);
if (budget == 0 || f == 0) break;
       return make_pair(flow, cost);
void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
```

```
):
5 String
```

#### 5.1 KMP [cddfd9]

```
struct KMP {
       string sub;
vector<<mark>int</mark>> failure;
        KMP(string sub_) {
              sub = sub_;
failure.resize(sub.size(), -1);
               buildFailFunction();
       void buildFailFunction() {
    for (int i = 1; i < (int)sub.size(); i++) {</pre>
                      int now = failure[i - 1];
                      while (now != -1
     && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
              }
       vector<int> match(string &s) {
              vector <int> match;
for (int i = 0, now = -1; i < (int)s.size(); i++) {
    // now is the compare sucessed length -1</pre>
                      while (s[i] !=
                      sub[now + 1] && now != -1) now = failure[now];
// failure stores if comparison fail, move to where
if (s[i] == sub[now + 1]) now++;
                      if (now + 1 == (int)sub.size()) {
  match.push_back(i - now);
  now = failure[now];
                      }
               return match;
};
```

#### 5.2 Z Function [8dd6ac]

# **5.3 SA** [32e429]

```
struct SuffixArray {
     int n: vector<int> sa. rk. lc:
      // n: 字串長度
     // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
      // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
      // lc: LCP
              數組,lc[i] 表示 sa[i] 和 sa[i+1] 的最長公共前綴長度
     SuffixArray(const string &s) {
    n = s.length();
            sa.resize(n);
            lc.resize(n
            rk.resize(n);
            iota(sa.begin(), sa.end(), 0);
            sort(sa.begin(), sa.
end(), [&](int a, int b) { return s[a] < s[b]; });</pre>
            rk[sa[0]] = 0;
for (int i = 1; i < n; ++i)
                 rk[sa[i]]
                          = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
            vector<int> tmp, cnt(n);
            tmp.reserve(n);
while (rk[sa[n - 1]] < n - 1) {</pre>
                  tmp.clear();
                 for (int i = 0; i < k; ++i)
    tmp.push_back(n - k + i);
for (auto i : sa)
    if (i >= k)
                 tmp.push_back(i - k);
fill(cnt.begin(), cnt.end(), 0);
for (int i = 0; i < n; ++i)</pre>
                 for (tht t = 0; t < h; ++t)
    ++cnt[rk[i]];
for (int i = 1; i < n; ++i)
    cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; --i)
    sa[--cnt[rk[tmp[i]]]] = tmp[i];
swap(rk, tmp);
for [coll = 0;
                 rk[sa[0]] = 0;
```

## 5.4 Duval Algorithm [f9dcca]

```
// 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
vector<string> duval(string s) {
  int i = 0, n = s.size();
  vector<string> res;
      while (i < n) {
            int k = i, j = i + 1;
while (s[k] <= s[j] && j < n) {
    if (s[k] < s[j]) k = i;
    else k++;
                  j++;
            while (i <= k) {</pre>
                  res.push_back(s.substr(i, j - k));
                  i += j - k;
      return res;
// 最小旋轉字串
string min_round(string s) {
      s += s;
int i = 0, n = s.size();
      int start = i;
      while (i < n / 2) {
            start = i;
int k = i, j = i + 1;
while (s[k] <= s[j] && j < n) {
   if (s[k] < s[j]) k = i;
   else k++;</pre>
            while (i <= k) {</pre>
                  i += j - k;
      return s.substr(start, n / 2);
}
```

#### 5.5 Manacher [9c9ca6]

```
/ 找到對於每個位置的廻文半徑
vector < int > manacher(string s) {
    string t = "#";
    for (auto c : s) {
       t += c;
t += '#':
    int n = t.size();
   vector < int > r(n);
for (int i = 0, j =
        if (2
       r[i] += 1;
       if (i + r[i] > j + r[j]) {
       }
   return r;
   // # a # b # a #
// 1 2 1 4 1 2 1
// # a # b # b # a #
   // 1 2 1 2 5 2 1 2 1
   // 值 -1 代表原回文字串長度
   // (id - val + 1) / 2 可得原字串回文開頭
5.6 Trie [3b3aa0]
struct Trie {
```

```
struct Trie {
    struct trie_node {
        bool is_word;
        vector<trie_node *> children;
        trie_node() {
```

```
is word = false:
                children.resize(26, NULL);
           }
      trie_node *root = new trie_node();
      void insert(string &s) {
           trie_node *cur = root;
for (int i = 0; i < s.size(); i++) {
   int idx = s[i] - 'a';
                if (cur->children[idx] == NULL) {
                      cur->children[idx] = new trie_node();
                 cur = cur->children[idx];
           cur->is_word = true;
     fool is_in_trie(string &s) {
    trie_node *cur = root;
    for (int i = 0; i < s.size(); i++) {</pre>
                if (cur->
                children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
           return true:
      int search_i_start(string &s, int i, vector<int> &dp) {
           trie_node *cur = root;
int sz = s.size(), ans = 0;
for (int j = i; j < sz; j++) {
    if (cur</pre>
                ->children[s[j] - 'a'] == nullptr) return ans;

cur = cur->children[s[j] - 'a'];

if (cur->is_word)
                      (ans += dp[j + 1]) %= mod;
           return ans;
     }
};
int main() {
     // 找到 sub 集合裡,可以重複用,組成 s 的組數 Trie trie;
     string s; cin >> s;
int sz = s.size();
     // dp 代表 i 開頭到最後的配對總數
     // 找到有結尾為 stop 的 dp[i] += dp[j + 1] int n; cin >> n;
      vector < int > dp(sz + 1, 0);
     for (int i = 0; i < n; i++) {
    string sub; cin >> sub;
    trie.insert(sub);
     dp[sz] = 1;
for (int i = sz - 1; i >= 0; i--) {
           dp[i] = trie.search_i_start(s, i, dp);
     cout << dp[0] << endl;
```

# 6 Math

# 6.1 Prime [ee1622]

```
// a^(m-1) = 1 (mod m)
// a^(m-2) = 1/a (mod m)
// EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)
// Filter + DP; DP save min factor 'recur' factor decomposition
// FacNums = (x+1)(y+1)(z+1)...
// FacSum = (a^0+a^1...+a^x)(b^0+...+b^y)
// FacMul = N(x+1)(y+1)(z+1)/2

vector < int > is_prime;
// 1 代表是質數 , 非 1 不是
void init(int n) {
    is_prime.assign(n + 1, 1);
    for (int i = 2; i <= (int)sqrt(n) + 1; i++) {
        if (is_prime[i] == 1) {
            for (int j = i + i; j <= n; j += i) {
                 is_prime[j] = i;
            }
        }
    }
}
int main() {
    init(1000000);
    ll ans = 1;
    ll q; cin >> q;
    map<ll, ll> mp;
    while (is_prime[q]!= 1) {
            mp[is_prime[q]!+;
            q /= is_prime[q];
    }
    if (q!= 1) mp[q]++;
    for (auto [a, b]: mp) {
            ans *= b + 1;
    }
    cout << ans << "\n";
}
```

#### 6.2 Modulo [9b1014]

```
using i64 = long long;
```

```
template < class T>
constexpr T power(T a, i64 b) {
  T res = 1;
     for (; b; b /= 2, a *= a) {
    if (b % 2) {
               res *=
          }
     return res;
}
constexpr i64 mul(i64 a, i64 b, i64 p) {
   i64 res = a * b - i64(1.L * a * b / p) * p;
   res %= p;
   if (res < 0) {</pre>
         res += p;
     return res;
template < i64 P>
struct MLong {
     i64 x;
     constexpr MLong() : x{} {}
constexpr MLong(i64 x) : x{norm(x % getMod())} {}
     static i64 Mod;
     constexpr static i64 getMod() {
   if (P > 0) {
               return P;
          } else {
               return Mod:
     constexpr static void setMod(i64 Mod_) {
          Mod = Mod_;
     constexpr i64 norm(i64 x) const {
          if (x < 0) {
              x += getMod();
          if (x >= getMod()) {
               x -= getMod();
          return x:
     constexpr i64 val() const {
          return x;
     explicit constexpr operator i64() const {
          return x;
     constexpr MLong operator-() const {
          MLong res;
res.x = norm(getMod() - x);
          return res;
     constexpr MLong inv() const {
   assert(x != 0);
          return power(*this, getMod() - 2);
     constexpr MLong &operator*=(MLong rhs) & {
          x = mul(x, rhs.x, getMod());
return *this;
     constexpr MLong &operator+=(MLong rhs) & {
    x = norm(x + rhs.x);
          return *this;
     constexpr MLong &operator -= (MLong rhs) & {
          x = norm(x - rhs.x);
return *this;
     constexpr MLong &operator/=(MLong rhs) & {
    return *this *= rhs.inv();
     friend constexpr MLong operator*(MLong lhs, MLong rhs) {
          MLong res = lhs;
res *= rhs;
     friend constexpr MLong operator+(MLong lhs, MLong rhs) {
          MLong res = lhs;
res += rhs;
          return res;
     friend constexpr MLong operator-(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res -= rhs;
          return res;
     friend constexpr MLong operator/(MLong lhs, MLong rhs) {
          MLong res = lhs;
res /= rhs;
          return res;
     friend
           constexpr istream &operator>>(istream &is, MLong &a) {
          is >> v;
a = MLong(v);
          return is;
```

```
friend constexor
                 ostream & operator << (ostream &os, const MLong &a) {
              return os << a.val();</pre>
        friend constexpr bool operator==(MLong lhs, MLong rhs) {
              return lhs.val() == rhs.val();
        friend constexpr bool operator!=(MLong lhs, MLong rhs) {
              return lhs.val() != rhs.val();
 };
 template<>
 i64 MLong<0LL>::Mod = i64(1E18) + 9;
 constexpr i64 P = 998244353;
using Z = MLong <P>;
// using Z = MLong <0LL>; // change Mod
 struct Comb {
       i64 n:
       to4 n;
vector <Z> _fac;
vector <Z> _invfac;
vector <Z> _inv;
Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
Comb(i64 n) : Comb() { init(n); }
        void init(i64 m) {
              int((to4 m) {
    m = min(m, Z::getMod() - 1);
    if (m <= n) return;
    _fac.resize(m + 1);
    _invfac.resize(m + 1);</pre>
              _inv.resize(m + 1);
              for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;</pre>
              for (int i = _fac[m].inv();
for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
              n = m;
       J
Z fac(i64 m) {
    if (m > n) init(2 * m);
    return _fac[m];
        J invfac(i64 m) {
    if (m > n) init(2 * m);
    return _invfac[m];
       Z inv(i64 m) {
   if (m > n) init(2 * m);
   return _inv[m];
       Z binom(i64 n, i64 m) {
   if (n < m || m < 0) return 0;
   return fac(n) * invfac(m) * invfac(n - m);</pre>
       |} comb; // 注意宣告, 若要換模數需重新宣告
```

# 6.3 CRT [d41d8c]

```
ll exgcd(ll a, ll b, ll &x, ll &y) {
     if (!b) {
    x = 1, y = 0;
           return a:
     ll g = exgcd(b, a % b, y, x);
y -= a / b * x;
return g;
ll inv(ll x, ll m){
     ll a, b;
     exgcd(x, m, a, b);
     a %= m;
if (a < 0) a += m;
     return a;
// remain, mod
ll CRT(vector<pair<ll, ll>> &a){
     ll prod = 1;
for (auto x : a) {
          prod *= x.second;
     ll res = 0;
     for (auto x : a) {
           auto t = prod / x.second;
res += x.first * t % prod * inv(t, x.second) % prod;
if(res >= prod) res -= prod;
     return res;
```

```
template < class T>
 struct Mat {
      int m, n;
      constexpr static ll mod = 1e9 + 7;
      vector < vector < T >> matrix;
      Mat(int n_ = 0) { init(n_, n_); }
Mat(int m_, int n_) { init(m_, n_); }
Mat(vector<vector<T>> matrix_) { init(matrix_); }
       void init(int m_, int n_) {
            m = m_; n = n_;
            matrix.assign(m, vector<T>(n));
      void init(vector<vector<T>> &matrix_) {
           m = matrix_.size();
n = matrix_[0].size();
                                                     // 單位矩陣
      vector<vector<T>> unit(int n) { // 單位矩
    vector<vector<T>> res(n, vector<T>(n));
    for (int i = 0; i < n; i++) {</pre>
               res[i][i] = 1;
            return res;
      constexpr Mat & operator *= (const Mat& rhs) & {
   assert(matrix[0].size() == rhs.matrix.size());
            int m = matrix.size()
                   , k = matrix[0].size(), n = rhs.matrix[0].size();
           l] * rhs.matrix[l][j] % mod)) %= mod;
                 }
            matrix = ans.matrix;
return *this;
      Constexpr Mat & operator^=(ll p) & {
    assert(m == n); assert(p >= 0);
    Mat ans(p-- == 0 ? unit(m) : matrix);
    while (p > 0) {
        if (p & 1) ans *= *this;
        *this *= *this;
    }
}
                 p >>= 1;
            matrix = ans.matrix;
            return *this;
      friend Mat operator*(Mat lhs, const Mat &rhs) {
            lhs *= rhs;
            return lhs;
      friend Mat operator^(Mat lhs, const ll p) {
            return lhs;
// fn = fn-3 + fn-2 + fn-1
1 1 0 f5 f4 f3
1 0 1 => f4 f3 f2
1 0 0 f3 f2 f1
```

#### 6.5 Integer Partition [06204a]

#### 6.6 Mobius Theorem

• 數論分塊可以快速計算一些含有除法向下取整的和式,就是像  $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理 出  $\mathbf{F}$  的前綴和時,數論分塊就可以在  $O(\sqrt{n})$  的時間內計算上述和式的值。

• 迪利克雷捲積  $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$ 

• 積性函數

- 莫比烏斯函數

1. 定義

$$\sum_{d|n} \mu(d) = \begin{cases} 1 & \text{for } n = 1 \\ 0 & \text{for } n \neq 0 \end{cases}$$

- 2.  $\mu$ 是常數函數 1 的反元素  $\Rightarrow \mu*1=\epsilon$  ,  $\epsilon(n)$ 只在n=1時為 1 , 其餘情況皆為 0 。
- $-\phi$ 歐拉函數: x以下與x互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^i) \\ &= 1 + p^0(p-1) + p^1(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^c \\ &= id \end{split}$$

• 莫比烏斯反演公式

- 
$$f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$$
  
-  $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$ 

例子

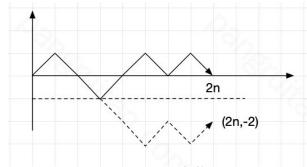
$$\begin{split} &\sum_{i=aj=c}^{b} \sum_{j=1}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{\infty} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

# 6.7 Mobius Inverse [d41d8c]

const int maxn = 2e5;

```
ll mobius_pref[maxn];
void init() {
      mobius_pref[1] = 1;
      vector<ll> wei
      (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
    }
                  continue; // 包含平方
            if (wei[i] == 0) {
                  wet[i] == 0) {
wei[i] = 1;
for (ll j = 2; i * j < maxn; j++) {
    if (j % i == 0) wei[i * j] = -1;
    else if (wei[i * j] != -1) wei[i * j]++;</pre>
                  }
            mobius pref[i]
                   = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
     }
void solve() {
      ll a, b, c, d, k; cin >> a >> b >> c >> d >> k;
auto cal = [&](ll x, ll y) -> int {
            int res = 0;
            cout << cal
             (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k, (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n"
}
```

#### 6.8 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況  $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有x 個,往下有y 個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 $C_{n-1}^{2n}$ 即可

#### 6.9 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$ 

- G:各種翻轉操作所構成的置換群
- · X/G:本質不同的方案的集合
- $X^g$ : 對於某一種操作 g,所有方案中,經過 g 這種翻轉後保持不變的方案的集合
- 集合取絕對值代表集合數

# 7 Search and Gready

# 7.1 Binary Search [d41d8c]

```
int main() {
    int l = 1, r = 10;
    // 1 to tar, find tar
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}</pre>
```

## 7.2 Ternary Search [d41d8c]

#### 8 Tree

# 8.1 LCA [9f95b1]

```
vector < vector < int >> par (maxn, vector < int > (18));
vector < int > depth (maxn + 1);
vector < int > dfn (maxn);
void build_lca(int n, vector < vector < pair < int , int >>> & tree) {
    auto dfs = [&](auto self, int u, int pre) -> void {
        for (auto [v, w] : tree[u]) {
            if (v == pre) continue;
            par[v][0] = u; // 2 ^ 0
            depth[v] = depth[u] + 1;
            self(self, v, u);
        }
};
dfs(dfs, 1, 0);
for (int i = 1; i <= 18; i++) {
        par[j][i] = par[par[j][i - 1]][i - 1];
}</pre>
```

```
}
int lca(int a, int b) {
    if (depth[a] < depth[b]) swap(a, b);
    int pull = depth[a] - depth[b];
    for (int i = 0; i < 18; i++) {
        if (pull & (1 << i)) {
            a = par[a][i];
        }
    if (a == b) return a;
    for (int i = 17; i >= 0; i--) {
        if (par[a][i] != par[b][i]) {
            a = par[a][i], b = par[b][i];
        }
    return par[a][0];
}
```

# 8.2 Tree Centroid Decomposition [30b436]

```
struct centroid_decomposition {
       vector<vector<int>> adj;
       vector<bool> vis;
       vector<int> siz;
       centroid_decomposition() {}
centroid_decomposition(int n_) { init(n_); }
       void init(int n_) {
             n = n_;
adj.assign(n, {});
vis.assign(n, false);
              siz.assign(n, 1);
       void addEdge(int u, int v) {
              adj[u].push_back(v);
adj[v].push_back(u);
       void get_siz(int dep, int x, int p = -1) {
    siz[x] = 1;
              for (int y : adj[x]) {
   if (y == p || vis[y]) continue;
   get_siz(dep + 1, y, x);
   siz[x] += siz[y];
              }
       fint get_cen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz) {
                           return get_cen(y, sz, x);
              return x:
       void work(int x = 0) {
              get_siz(0, x);
int cen = get_cen(x, siz[x]);
vis[cen] = true;
              // do something
              for (int y : adj[cen]) {
    if (vis[y]) continue;
    work(y);
};
```

#### 8.3 Tree Flattening [51199c]

```
點加值 = 所有子節點區間加值,求單點,使用 bit,做前綴差分
CSES 1138_Path Queries
  int n, q; cin >> n >> q;
vector <int> node_value(n + 1), euler_ordered_value(n);
for (int i = 1; i <= n; i++) {</pre>
        cin >> node_value[i];
   vector<vector<int>> tree(n + 1);
   for (int i = 1; i < n; i++) {
  int u, v; cin >> u >> v;
  tree[u].push_back(v);
        tree[v].push_back(u);
  vector<pair<int, int>> tree mapping(n + 1);
  int cnt = 0;
auto dfs = [&](auto self, int u, int par) -> void {
    euler_ordered_value[++cnt] = node_value[u];
        tree_mapping[u].first = cnt;
        for (auto v : tree[u]) {
   if (v == par) continue;
   self(self, v, u);
        tree_mapping[u].second = cnt;
   dfs(dfs,
  BIT bit(n);
for (int i = 1; i <= n; i++) {
        bit.modify(tree_mapping[i].first, node_value[i]);
        if (tree_mapping[i].first < n) { // root 就不用扣了</pre>
                    (tree_mapping[i].second + 1, -node_value[i]);
```

# 8.4 Heavy Light Decomposition [ad25b6]

```
int n, cur;
vector<int> siz, top, dep, parent, in, out, seq;
vector<vector<int>> adj;
HLD(int n_ = 0) { init(n_); }
void init(int n_ = 0) {    int(n_); }
void init(int n_ = 0) {
    n = n_; cur = 0;
    siz.resize(n); top.resize(n); dep.resize(n);
    parent.resize(n); in.resize(n); out.resize(n);
      seq.resize(n); adj.assign(n, {{}});
void addEdge(int u, int v) {
      adj[u].push_back(v);
adj[v].push_back(u);
void work(int root = 0) {
      top[root] = root;
dep[root] = 0;
      parent[root] = -1
      dfs1(root); dfs2(root);
void dfs1(int u) {
      if (parent[u] != -1)
            adj[u].erase(find
                   (adj[u].begin(), adj[u].end(), parent[u]));
      for (auto &v : adj[u]) {
   parent[v] = u, dep[v] = dep[u] + 1;
            dfs1(v);
            siz[u] += siz[v];
if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
            } // 讓 adj[u][0] 是重子節點
void dfs2(int u) {
      in[u] = cur++;
      seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
    top[v] = v == adj[u][0] ? top[u] : v;
            dfs2(v):
      out[u] = cur;
int lca(int u, int v) {
    while (top[u] != top[v]) {
           if (dep[top[u]] > dep[top[v]]) {
    u = parent[top[u]];
} else {
                  v = parent[top[v]];
            }
      return dep[u] < dep[v] ? u : v;
int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
int jump(int u, int k) {
   if (dep[u] < k) return -1;
   int d = dep[u] - k;
   while (dep[top[u]] > d)
            u = parent[top[u]];
      return seq[in[u] - dep[u] + d];
bool isAncester(int u, int v) {
      // 判斷 u 是否是 v 的祖先
return in[u] <= in[v] && in[v] < out[u];
int rootedParent(int u, int v) {
    // 根據新根節點 u 計算 v 的父節點
      swap(u, v);
if (u == v) return u;
if (!isAncester(u, v)) return parent[u];
      auto it = upper_bound(adj
   [u].begin(), adj[u].end(), v, [&](int x, int y) {
   return in[x] < in[y];</pre>
```

```
return *it:
      int rootedSize(int u, int v) {
             // 根據新根節點 u 計算子樹 v 的大小
             if (u == v) return n;
if (!isAncester(v, u)) return siz[v];
return n - siz[rootedParent(u, v)];
      int rootedLca(int a, int b, int c) {
    // 根據新的根節點計算三個節點 a \ b 和 c 的最近公共祖先
    return lca(a, b) ^ lca(b, c) ^ lca(c, a);
};
```

# 8.5 Link Cut Tree [c26f51]

```
#include <bits/stdc++.h>
 using namespace std;
using i64 = long long;
constexpr i64 Mod = 51061;
 struct Tag {
    i64 add = 0;
      i64 mul = 1:
      void apply(const Tag& v) {
   mul = mul * v.mul % Mod;
   add = (add * v.mul % Mod + v.add) % Mod;
      }
 struct Info {
      i64 val = 1;
i64 sum = 1;
      void apply(int size, const Tag &v) {
  val = (val * v.mul % Mod + v.add) % Mod;
  sum = (sum * v.mul % Mod + v.add * size % Mod) % Mod;
 struct Node {
      Node *ch[2], *p;
int rev = 0;
int size = 1;
       void make_rev() {
            swap(ch[0], ch[1]);
rev ^= 1;
       Node() : ch {nullptr, nullptr}, p(nullptr) {}
      Info info = Info();
Tag tag = Tag();
      void apply(const Tag &v) {
    info.apply(size, v);
             tag.apply(v);
       void push_tag() {
            if (rev) {
   if (ch[0]) ch[0]->make_rev();
   if (ch[1]) ch[1]->make_rev();
                  rev = 0:
             if (ch[0]) {
                  ch[0]->apply(tag);
             if (ch[1]) {
                  ch[1]->apply(tag);
             tag = Tag();
       void pull_info() {
            };
 bool isroot(Node *t) {
              == nullptr || (t->p->ch[0] != t && t->p->ch[1] != t);
 int pos(Node *t) { // 回傳 1 代表是右子節點 return t->p->ch[1] == t;
 void rotate(Node *t) {
      Node *q = t->p;
int x = !pos(t);
      q->ch[!x] = t->ch[x];
if (t->ch[x]) {
    t->ch[x]->p = q;
       t - p = q - p;
       if (!isroot(q)) {
            q \rightarrow p \rightarrow ch[pos(q)] = t;
      t \rightarrow ch[x] = q;
      q->p = t;
q->pull_info();
| void splay(Node *t) { // 單點修改前必須呼叫
```

```
把 t 旋轉到目前 splay 的根
      while (!isroot(t)) {
          Node *p = t \rightarrow p;
          p->push_tag();
t->push_tag();
          rotate(t);
     t->push_tag();
t->pull_info();
void access(Node *t) {
     // 把從根到 t 的所有點都放在一條實鏈裡,使根
     // 到 t 成為一條實路徑,並且在同一棵 splay 裡 for (Node *i = t, *q = nullptr; i; q = i, i = i->p) {    splay(i);
           i->ch[1] = q;
     splay(t);
}
void makeRoot(Node *t) { // 使 t 點成為其所在樹的根
     access(t);
     swap(t->ch[0], t->ch[1]);
t->rev ^= 1;
Node* findRoot(Node *t) { // 找到 t 的 root
     access(t):
     splay(t);
     t->push_tag();
     while (t->ch[0]) {
    t = t->ch[0];
          t->push_tag();
     splay(t);
     return t;
void link(Node *t, Node *p) {
     makeRoot(t);
if (findRoot(p) != t) {
          makeRoot(p);
          p->pull_info();
bool cut(Node *x, Node *y) { // 不存在邊,回傳 false
     makeRoot(x);
     access(y);
if (y->ch[0] != x || x->ch[1]) return false;
     y - > ch[\theta] - > p = nullptr;
     y->ch[0] = nullptr;
y->pull_info();
     return true;
void split(Node
       *x, Node *y) { // 以 y 做根, 區間修改用, apply 在 y 上
     makeRoot(x);
     access(y);
}
bool isconnected(Node *x, Node *y) { // 查詢有沒有連通
     makeRoot(x);
     access(v);
     return findRoot(x) == findRoot(y);
}
int main() {
    int n; cin >> n;
     vector < Node *> nodes(n);
     vector<Node *> nodes(n);
int q; cin >> q;
for (int i = 0; i < n; i++) {
    nodes[i] = new Node();
    nodes[i]->info.val = nodes[i]->info.sum = 1LL;
     for (int i = 0; i < n - 1; i++) {
   int u, v; cin >> u >> v;
           link(nodes[u], nodes[v]);
      for (int i = 0; i < q; i++) {
           char op; cin >> op;
if (op == '+') {
                int u, v; cin >> u >> v;
                split(nodes[u], nodes[v]);
                Tag tag;
cin >> tag.add;
tag.add % Mod;
                nodes[v]->apply(tag);
           else if (op == '-') {
                int u1, v1; cin >> u1 >> v1;
int u2, v2; cin >> u2 >> v2;
u1--; v1--; u2--; v2--;
cut(nodes[u1], nodes[v1]);
link(nodes[u2], nodes[v2]);
           else if (op == '*') {
   int u, v; cin >> u >> v;
                split(nodes[u], nodes[v]);
                Tag tag;
```

void add\_edge(int u, int v) { adj[u].push\_back(v); }

```
cin >> tag.mul;
                                                                                                                                 int query(int v, int x) {
   if (rt[v] == v) return x ? -1 : v;
                      tag.mul % Mod;
                                                                                                                                        int p = query(rt[v], 1);
if (p == -1) return x ? rt[v] : mn[v];
if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
                      nodes[v]->apply(tag);
                      int u, v; cin >> u >> v;
                                                                                                                                         rt[v] = p;
                      u - -:
                                                                                                                                        return x ? p : mn[v];
                      split(nodes[u], nodes[v]);
                                                                                                                                }
void dfs(int v) {
    vis[v] = id, rev[id] = v;
    rt[id] = mn[id] = sdom[id] = id, id++;
    for (int u : adj[v]) {
        if (vis[u] == -1) dfs(u), pa[vis[u]] = vis[v];
        radj[vis[u]].push_back(vis[v]);
}
                      cout << nodes[v]->info.sum << "\n";</pre>
              }
      }
       return 0;
8.6 Virtual Tree [622e69]
                                                                                                                                 void build(int s) {
                                                                                                                                       // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
// 可以建立虚樹達成快速樹 DP
// 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector<int>stk(maxn);
                                                                                                                                                suom[u] = min(soom[i], sdom[quer;
if (i) bucket[sdom[i]].push_back(i);
for (int u : bucket[i]) {
   int p = query(u, 0);
   dom[u] = sdom[p] == i ? i : p;
int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
   if (top == -1) return stk[++top] = u, void();
   int l = lca(stk[top], u);
   if (l == stk[top]) return stk[++top] = u, void();
   while (dfn[l] < dfn[stk[top - 1]])</pre>
                                                                                                                                                if (i) rt[i] = pa[i];
       vt[stk[top - 1]].push_back(stk[top]), top--;
if (stk[top - 1] != l) {
   vt[l].push_back(stk[top]);
   stk[top] = l;
                                                                                                                                        res.assign(n, -1);
for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];
for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre>
       } else vt[l].push_back(stk[top--]);
       stk[++top] = u;
                                                                                                                                        res[s] = s;
                                                                                                                                         for (int i = 0; i < n; i++) dom[i] = res[i];</pre>
void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
    vt[u].clear();
                                                                                                                        };
void solve(int n, int q) {
    vector g(n + 1, vector<pair<int, int>>());
                                                                                                                         9
                                                                                                                                    DP
       vector g(n + 1, vector<pair<int, int>>());
vector vt(n + 1, vector<int>()); // dfs 完清除, 否則會退化
vector<ll> dp(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;
   g[u].push_back({v, w});
   g[v].push_back({u, w});
}
                                                                                                                          9.1 LCS [5781cf]
                                                                                                                                 int m, n; cin >> m >> n;
                                                                                                                                 string s1, s2; cin >> s1 >> s2;
int L = 0;
                                                                                                                                 vector<vector<int>> dp(m + 1,
                                                                                                                                                                                        vector < int > (n + 1, 0));
                                                                                                                                 for (int i = 1; i <= m; i++) {
    for (int j = 1; j <= n; j++) {
        if (s1[i - 1] == s2[j - 1])
            dp[i][j] = dp[i - 1][j - 1] + 1;
       build_lca(n, g);
       build_lca(n, g);
build(n, g);
for (int i = 0; i < q; i++) {
   int m; top = -1; cin >> m;
   vector < int >> key(m);
   for (int j = 0; j < m; j++) {
      cin >> key[j];
                                                                                                                                                       dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
                                                                                                                                        }
                      iskey[key[j]] = 1;
                                                                                                                                 int length = dp[m][n]; cout << length << "\n";</pre>
                                                                                                                                 tht tength = upfm[n], could keep tength
string s(length, 'c'); // backtracking
while (m >= 1 && n >= 1) {
    if (s1[m - 1] == s2[n - 1]) {
        s[length - 1] = s1[m - 1];
    }
}
              key.push_back(1); // 看題目,需要才放
sort(all(key), [%](int a, int b) {
    return dfn[a] < dfn[b];
                                                                                                                                               m--, n--, length--;
               for (int x : key) insert(x, vt);
              while (top
              > θ) vt[stk[top - 1]].push_back(stk[top]), --top;
// DP
                                                                                                                                        else {
    if (dp[m - 1][n] > dp[m][n - 1]) m--;
               auto dfs = [&](auto self, int u) -> void {
    for (auto v : vt[u]) {
        self(self, v);
}
                                                                                                                                 cout << s << "\n":
                              if (iskey[v]) {
                                    dp[u] += min_dis[v];
                                    // 砍掉 1 到 v 之間最短的路
                                                                                                                         9.2 LIS [66d09f]
                              else {
                                    dp[u] += min(dp[v], min_dis[v]);
                                                                                                                          int main() {
                                                                                                                                 int n; cin >> n;
vector <int> v(n);
for (int i = 0; i < n; i++) cin >> v[i];
int dp[n]; vector <int> stk;
                             iskey[v] = dp[v] = 0;
                      vt[u].clear();
                                                                                                                                 stk.push_back(v[0]);
              };
                                                                                                                                 dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) {
    if (v[i] > stk.back()) {
              dfs(dfs, key[0]); // key[0] 一定是 root
cout << dp[key[0]] << "\n";
iskey[key[0]] = dp[key[0]] = 0;
                                                                                                                                               stk.push_back(v[i]);
                                                                                                                                                dp[i] = ++L;
}
                                                                                                                                        } else {
8.7 Dominator Tree [baa540]
                                                                                                                                               auto it
                                                                                                                                                         = lower_bound(stk.begin(), stk.end(), v[i]);
                                                                                                                                                *it = v[i]; dp[i] = it - stk.begin() + 1;
struct Dominator_tree {
                                                                                                                                        }
       int n, lo;
vector<vector<int>> adj, radj, bucket;
vector<vector<int>> sdom, dom, vis, rev, pa, rt, mn, res;
Dominator_tree(int n_ = 0) { init(n_); }
void init(int _n) {
    n = _n, id = 0;
    adj.assign(n, vector<int>());
    redi assign(n, vector<int>());
                                                                                                                                 vector < int > ans; cout << L << "\n";
for (int i = n - 1; i >= 0; i--) {
    if (dp[i] == L) {
                                                                                                                                                ans.push_back(v[i]), L--;
               radj.assign(n, vector<int>());
                                                                                                                                 reverse(ans.begin(), ans.end());
for (auto i : ans) cout << i << " ";</pre>
              bucket.assign(n, vector<int>());
sdom.resize(n); dom.assign(n, -1)
vis.assign(n, -1); rev.resize(n);
              pa.resize(n); rt.resize(n);
                                                                                                                         9.3 Edit Distance [308023]
               mn.resize(n); res.resize(n);
```

int main() {

sort(a.begin(), a.end());

for (int i = 1; i <= n; i++) {
 auto it = --lower\_bound(all(a), E({0, a[i].from}),
 [](E x, E y){ return x.to < y.to; });
 int id = it - a.begin(); dp[i] = dp[i - 1];</pre>

dp[i] = {nw, nt}; rec[i] = {1, id};

ll nw = dp[id][0] + a[i].w; ll nt = dp[id][1] + a[i].to - a[i].from; if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {

```
string s1, s2; cin >> s1 >> s2;
int n1 = s1.size(), n2 = s2.size();
                                                                                  }
    // dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元
vector<int> dp(n2 + 1);
                                                                             vector < int > ans;
for (int i = n; i != 0;) {
    if (rec[i][0]) {
    ans.push_back(a[i].id);
                                                                                 i = rec[i][1];
} else i--;
                                                                         }
                 cur[j] = dp[j - 1];
             } else {
                                                                         9.6 Removal Game [7bb56b]
                 // s1 新增等價於 s2 砍掉
                  // dp[i][j] = min(s2 新增, 修改, s1 新增);
                                                                        | // 兩個人比賽,每個人輪流取一個數字且只能是頭尾
                 cur[j]
                                                                         // 問兩人都選得好,第一出手的人可取得的最大分數
                       = min({cur[j - 1], dp[j - 1], dp[j]}) + 1;
                                                                         int main() {
                                                                             int n; cin >> n;
vector <ll> a(n);
for (int i = 0; i < n; i++) cin >> a[i];
         swap(dp, cur);
                                                                             for (int i = 0, t < n, t++) tin >> a[t],

vector dp(n, vector<ll>(n)); // i 到 j 區間的最大 diff

for (int i = n - 1; i >= 0; i--) {
    dp[i][i] = a[i];
    for (int j = i + 1; j < n; j++)
    cout << dp[n2] << "\n";
9.4 Bitmask [a626f9]
                                                                                      dp[i][j] =
void hamiltonianPath(){
                                                                                           max(a[i] - dp[i + 1][j], a[j] - dp[i][j - 1]);
    int n, m; cin >> n >> m;
vector adj(n, vector<int>());
                                                                             // x + y = sum; // x - y = dp[0][n - 1]
    for (int i = 0; i < m; i++) {
   int u, v; cin >> u >> v;
                                                                             cout << (accumulate
                                                                                   (a.begin(), a.end(), 0LL) + dp[0][n - 1]) / 2 << "\n";
        adj[--v].push_back(--u);
                                                                         }
                                                                         9.7 CHT [5f5c25]
    // 以...為終點,走過...
    vector dp(n, vector<int>(findBit(n)));
   struct Line {
                                                                             ll m, b;
ll m, b;
Line(ll m = 0, ll b = 0) : m(m), b(b) {}
ll eval(ll x) {
    return m * x + b;
                                                                         };
             for (int j : adj[i]) {
   if ((pre_mask & findBit(j)) == 0) continue;
                                                                         struct CHT { // 用在查詢單調斜率也單調
  int n, lptr, rptr; vector<Line> hull;
  CHT(int n_ = 0, Line init_ = Line()) {
                  dp[i][mask
                       ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
                                                                                  init(n_, init_);
             }
        }
                                                                             void init(int n_ = 0, Line init_ = Line()
    n = n_; hull.resize(n); reset(init_);
                                                                                               = 0, Line init = Line()) {
    cout << dp[n - 1][findBit(n) - 1] << "\n";
                                                                             void reset(Line init_ = Line()) {
   lptr = rptr = 0; hull[0] = init_;
void elevatorRides() {
    int n, x; cin >> n >> x; vector<int> a(n);
for (int i = 0; i < n; i++) cin >> a[i];
                                                                             vector<array<int, 2>> dp(findBit(n));
    // 代表查詢的當下,右線段的高度已經低於左線段了
                                                                                  return l1.eval(x) >= l2.eval(x);
                                                                              bool pop_back(Line &l1, Line &l2, Line &l3) {
                                                                                  // 本題斜率遞減、上凸包
                                                                                  // 因此只要 12 跟
                                                                                  l3 的 X 交點 <= l1 跟 l3 的 X 交點, l2 就用不到了return (l3.b - l2.b)
* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
                                                                              void insert(Line L) {
                                                                                  while (rptr - lptr
> 0 && pop_back(hull[rptr - 1], hull[rptr], L))
            hull[++rptr] = L;
                                                                             dp[mask][1] = a[i];
        }
    cout << dp[findBit(n) - 1][0] << "\n";
                                                                                  return hull[lptr].eval(x);
                                                                             }
                                                                        };
9.5 Projects [0942aa]
                                                                         9.8 DNC [61c639]
int from, to, w, id;
bool operator <(const E &rhs) {
    return to == rhs.to ? w > rhs.w : to < rhs.to;</pre>
    int n; cin >> n; vector <E> a(n + 1);
for (int i = 1; i <= n; i++) {
   int u, v, w; cin >> u >> v >> w;
   a[i] = {u, v, w, i};
    vector<array<ll, 2>> dp(n + 1); // w, time
                                                                                  // 注意 i 的範圍、 get_cost 與 dp 的邊界
ll cur = dp[k - 1][i] + get_cost(i, m);
    vector<array<int, 2>> rec(n + 1); // 有沒選, 上個是誰
```

if (cur < dp[k][m]) {</pre>

DNC(k, l, m - 1, optl, opt);
DNC(k, m + 1, r, opt, optr);

int main() {

dp[k][m] = cur, opt = i;

```
// first build cost...
for (int i = 1; i <= n; i++) {
     // init dp[1][i]
}
for (int i = 2; i <= k; i++) {
     DNC(i, 1, n, 1, n);
}
cout << dp[k][n] << "\n";
}</pre>
```

# 9.9 LiChaoSegmentTree [a6e320]

```
ll m, b;
Line(ll m = 0, ll b = Inf) : m(m), b(b) {}
ll eval(ll x) const { return m * x + b; }
struct LiChaoSeg { // 取 max 再變換就好
      int n;
vector < Line > info;
       LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
             info.assign(4 << __lg(n), Line());
      void update(Line line, int node, int l, int r) {
  int m = (l + r) / 2;
  bool left = line.eval(l) < info[node].eval(l);
  bool mid = line.eval(m) < info[node].eval(m);</pre>
             if (mid) swap(info[node], line); // 如果新線段比較好
             if (r - l == 1) return;
else if (left != mid) update(line, 2 * node, l, m);
             // 代表左半有交點
             else update(line, 2 * node + 1, m, r);
             // 代表如果有交點一定在右半
      void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
    if (r - l == 1) return info[node].eval(x);
    int m = (l + r) / 2;
    if (x < m) return
        min(info[node].eval(x), query(x, 2 * node, l, m));
else return min(</pre>
                     info[node].eval(x), query(x, 2 * node + 1, m, r));
       il query(int x) { return query(x, 1, 0, n); }
};
```

#### 9.10 Codeforces Example [7d37ea]

```
| // CF 1932 pF
// 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
 // 請問在線段不重複的情況下,最多獲得幾分
 int main() {
     int n, m;
cin >> n >> m;
     // 記錄每點有幾個線段
     // 再一個紀錄,包含這個點的左界
     cnt[l]++;
          cnt[r + 1]--;
     for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
     vector < int > dp(n + 1);
     dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
         dp[i] = cnt[i];
if (l_side[i] != inf) {
    dp[i] += dp[l_side[i] - 1];
          dp[i] = max(dp[i], dp[i - 1]);
     cout << dp[n] << "\n";
 // CF 1935 pC
 // 給你每個事件的 a, b, 挑事件會把 a 全部加起來
// 再加上 max(bi) - min(bi)
int main(){
    int n, k, ans = 0; cin >> n >> k;
    vector<pii> v(n + 1);
    for (int i = 1; i <= n; i++) {
          int a, b; cin >> a >> b;
v[i] = {a, b};
if (a <= k) ans = 1;</pre>
     sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
     }); // 用 bi 來排,考慮第 i 個時可以先扣
```

# 10 Geometry

#### **10.1** Basic [d41d8c]

```
template < class T>
struct Point {
     T x;
T y;
      Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) \{ \}
      template < class U>
      operator Point<U>() {
          return Point<U>(U(x), U(y));
      Point &operator+=(const Point &p) & {
           x += p.x;
y += p.y;
return *this;
      Point & operator -= (const Point &p) & {
           x -= p.x;
y -= p.y;
return *this;
      Point &operator*=(const T &v) & {
           x *= v;
y *= v;
return *this;
      Point & operator /= (const T & v) & {
           x /= v;
y /= v;
return *this;
      Point operator -() const {
           return Point(-x, -y);
      friend Point operator+(Point a, const Point &b) {
      friend Point operator - (Point a, const Point &b) {
           return a -= b;
      friend Point operator*(Point a, const T &b) {
  return a *= b;
      friend Point operator/(Point a, const T &b) {
   return a /= b;
      friend Point operator*(const T &a, Point b) {
   return b *= a;
      friend bool operator == (const Point &a, const Point &b) {
   return a.x == b.x && a.y == b.y;
      friend istream &operator>>(istream &is, Point &p) {
           return is >> p.x >> p.y;
      friend ostream & operator << (ostream & os, const Point & p) {
    return os << "(" << p.x << ", " << p.y << ")";</pre>
     }
}:
template < class T>
struct Line {
     Point<T>
     Point<7 a,
Point<7 b;
Line(const Point<7 > &a_ = Point<7 > ()
, const Point<7 > &b_ = Point<7 > () : a(a_), b(b_) {}
};
T dot(const Point<T> &a, const Point<T> &b) {
   return a.x * b.x + a.y * b.y;
template < class T >
T cross(const Point < T > &a, const Point < T > &b) {
    return a.x * b.y - a.y * b.x;
template < class T>
T square(const Point<T> &p) {
```

```
return dot(p. p):
 template < class T>
 double length(const Point<T> &p) {
     return sqrt(square(p));
 template < class T >
double length(const Line < T > &l) {
    return length(l.a - l.b);
 template < class T>
 Point<T> normalize(const Point<T> &p) {
    return p / length(p);
 template < class T>
 bool parallel(const Line<T> &l1, const Line<T> &l2) {
   return cross(l1.b - l1.a, l2.b - l2.a) == θ;
 template < class T>
 double distance(const Point<T> &a, const Point<T> &b) {
     return length(a - b);
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
 template < class T>
 double distancePS(const Point<T> &p, const Line<T> &l) {
    if (dot(p - l.a, l.b - l.a) < 0) {
    return distance(p, l.a);</pre>
     if (dot(p - l.b, l.a - l.b) < 0) {
    return distance(p, l.b);</pre>
     return distancePL(p, l);
 }
 template < class T>
 Point<T> rotate(const Point<T> &a) {
     return Point(-a.y, a.x);
 template < class T>
 int sgn(const Point<T> &a) {
     return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
 bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
     return cross(l.b - l.a, p - l.a) > 0;
 template < class T>
 Point < T
     template < class T>
 bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
     return cross(p - l.a, l.b - l.a) == 0 &&
min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)
               (l.a.y, l.b.y) \ll p.y \ll max(l.a.y, l.b.y);
 }
 template<class T>
 bool pointInPolygon
      (const Point<T> &a, const vector<Point<T>> &p) {
     int n = p.size();
                       í < n; i++) {
     for (int i = 0;
          if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {
              return true;
     }
     for (int i = 0; i < n; i++) {
    auto u = p[i];</pre>
          auto v = p[(i + 1) % n];
          if (u.x < a.x
               && v.x >= a.x && pointOnLineLeft(a, Line(v, u))) {
          if (u.x >= a.x
                && v.x < a.x && pointOnLineLeft(a, Line(u, v))) {
              t ^= 1;
          }
     }
     return t == 1;
// 0 : not intersect
```

```
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
tuple < int , Point < T > , Point < T >> segmentIntersection
      (const Line<T> &l1, const Line<T> &l2) {
   if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x)) {
      return {0, Point<T>(), Point<T>()};
      if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x)) {
    return {0, Point<T>(), Point<T>()};
      if (max(l1.a.y, l1.b.y) < min(l2.a.y, l
    return {0, Point<T>(), Point<T>()};
                                                            l2.b.y)) {
      if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y)) {
    return {0, Point<T>(), Point<T>()};
      if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
    if (cross(l1.b - l1.a, l2.a - l1.a) != 0) {
        return {0, Point<T>(), Point<T>()};
}
           } else {
                 auto maxx1 = max(l1.a.x, l1.b.x);
                 auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
                  auto miny1 = min(l1.a.y, l1.b.y);
                  auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
                  auto maxy2 = max(l2.a.y, l2.b.y);
                 auto miny2 = min(l2.a.y, l2.b.y);
Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
                  if (!pointOnSegment(p1, l1)) {
                       swap(p1.y, p2.y);
                  if (p1 == p2) {
                       return {3, p1, p2};
                 } else {
                       return {2, p1, p2};
          }
      auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
      auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
      if ((cp1 > 0 && cp2 > 0) || (cp1 < 0 && cp2 <
           0) || (cp3 > 0 && cp4 > 0) || (cp3 < 0 && cp4 < 0)) {
return {0, Point<T>(), Point<T>()};
      Point p = lineIntersection(l1, l2); if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
            return {1, p, p};
           return {3, p, p};
}
template < class T>
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
     if (get<\theta>(segmentIntersection(l1, l2)) != 0) {
            return 0.0:
      return min({distancePS(l1.a, l2), distancePS(l1
            .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
}
template < class T>
bool segmentInPolygon
       (const Line<T> &l, const vector<Point<T>> &p) {
      int n = p.size();
if (!pointInPolygon(l.a, p)) {
            return false;
      if (!pointInPolygon(l.b, p)) {
            return false;
      for (int i = 0; i < n; i++) {</pre>
            auto u = p[i];
            auto v = p[(i + 1) % n];
auto w = p[(i + 2) % n];
            auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
           if (t == 1) {
                  return false:
            if (t == 0) {
                  continue;
                  if (pointOnSegment(v, l) && v != l.a && v != l.b) {
   if (cross(v - u, w - v) > 0) {
      return false;
}
           || pointOnLineLeft(l.b, Line(v, u))) {
```

```
} else if (p1 == v) {
                 if (l.a == v)
                     if (pointOnLineLeft(u, l)) {
                          if (pointOnLineLeft(w, l)
                              && pointOnLineLeft
                              (w, Line(u, v))) {
return false;
                     } else {
    if (pointOnLineLeft(w, l)
                              || pointOnLineLeft
                              (w, Line(u, v))) {
return false;
                         }
                 } else if (l.b == v) {
   if (pointOnLineLeft(u, Line(l.b, l.a))) {
                          if (pointOnLineLeft(w, Line(l.b, l.a))
                              && pointOnLineLeft
                              (w, Line(u, v))) {
return false;
                     || pointOnLineLeft
                              (w, Line(u, v))) {
return false;
                         }
                     }
                (w, Line(u, v))) {
return false;
                     } else {
                          if (pointOnLineLeft(w, l)
                              || pointOnLineLeft
                              (w, Line(u, v))) {
return false;
                         }
                     }
                }
            }
        }
    return true;
}
vector<Point<T>> hp(vector<Line<T>> lines) {
   sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
   auto d1 = l1.b - l1.a;
        auto d2 = l2.b - l2.a;
        if (sgn(d1) != sgn(d2)) {
            return sgn(d1) == 1;
        return cross(d1, d2) > 0;
    });
    deque<Line<T>> ls;
    deque<Point<T>> ps;
    for (auto l : lines) {
    if (ls.empty()) {
            ls.push_back(l);
            continue:
        }
        while (!ps.empty() && !pointOnLineLeft(ps.back(), l)) {
    ps.pop_back();
             ls.pop_back();
        }
        while (!ps.empty() && !pointOnLineLeft(ps[\theta], l)) {
            ps.pop_front();
             ls.pop_front():
        if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
             if (dot
                 (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                 if (!pointOnLineLeft(ls.back().a, l)) {
                     assert(ls.size() == 1);
                     ls[0] = l;
                 continue:
            return {};
        ps.push_back(lineIntersection(ls.back(), l));
        ls.push_back(l);
    while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0])) {
        ps.pop_back();
        ls.pop_back();
```

```
if (ls.size() <= 2) {
            return {};
      ps.push_back(lineIntersection(ls[0], ls.back()));
      return vector(ps.begin(), ps.end());
using P = Point<ll>;
10.2 Convex Hull [b5758d]
int main() {
   int n; cin >> n;
      vector <P> P(n), U, L;
for (int i = 0; i < n; i++) {</pre>
           cin >> P[i];
      sort(P.begin(), P
    .end(), [](const Point<i64> &a, const Point<i64> &b) {
    return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
      for (int i = 0; i < n; i++) {
   while (L.size() >= 2 && cross(L.back() -
        L[L.size() - 2], P[i] - L[L.size() - 2]) <= 0LL) {</pre>
                 L.pop_back();
           while (U.size() >= 2 && cross(U.back() -
    U[U.size() - 2], P[i] - U[U.size() - 2]) >= 0LL){
                 U.pop_back();
            if (L.
                  empty() || !(L.back() == P[i])) L.push_back(P[i]);
           if (U.
                  empty() || !(U.back() == P[i])) U.push_back(P[i]);
      if (L.size() <= 2 && U.size() <= 2) {
           // No Hull
      cout << L.size() + U.size() - 2 << "\n";
      for (int i = 0; i < L.size() - 1; i++) {
   cout << L[i].x << " " << L[i].y << " | n";</pre>
      for (int i = U.size() - 1; i > 0; i--) {
    cout << U[i].x << " " << U[i].y << " | n";</pre>
}
10.3 MinEuclideanDistance [469a8f]
template < class T>
T distanceSquare(const Point<T> &a, const Point<T> &b) {
      return square(a - b);
void solve() {
      int n; cin >> n;
constexpr i64 inf = 8e18;
vector<Point<i64>> a(n);
      for (int i = 0; i < n; i++) {</pre>
           i64 x, y;
cin >> x >> y;
           a[i] = Point < i64 > (x, y);
      struct sortY {
           bool operator()
                  (const Point<i64> &a, const Point<i64> &b) const {
                 return a.y < b.y;</pre>
           }
      struct sortXY {
           bool operator()
                  (const Point<i64> &a, const Point<i64> &b) const {
                 if (a.x == b.x) return a.y < b.y;
else return a.x < b.x;</pre>
      sort(a.begin(), a.end(), sortXY());
vector<Point<i64>> t(n);
      auto devide = [&](auto &&self, int l, int r) -> i64 {
    if (l == r) return inf;
    int m = (l + r) / 2;
    i64 ans = min(self(self, l, m), self(self, m + 1, r));
}
            i64 midval = a[m].x;
            i64 p = 0;
for (int i = l; i <= r; i++) {
                 if ((midval - a[i].x) * (midval - a[i].x) <= ans) {
    t[p++] = a[i];</pre>
           for (int j = 0; i < p; i++) {
    for (int j = i + 1; j < p; j++) {
        ans = min(ans, distanceSquare(t[i], t[j]));
        if ('fill')</pre>
                       if ((t[i].y
                                t[j].y) * (t[i].y - t[j].y) > ans) break;
                 }
            return ans;
```

cout << devide(devide. 0. n - 1) << "\n":

#### 10.4 LatticePoints [7750d6]

```
int main() {
    // Polygun 內整數點數
    int n; cin >> n;
    vector < Point < i64 >> polygon(n);
    for (int i = 0; i < n; i++) cin >> polygon[i];
    i64 area = 0;
    for (int i = 0; i < n; i++) {
        area += cross(polygon[i], polygon[(i + 1) % n]);
    }
    area = abs(area);
    auto countBoundaryPoints
        = [](const vector < Point < i64 >> & polygon) -> i64 {
        i64 res = 0;
        int n = polygon.size();
        for (int i = 0; i < n; i++) {
            i64 dx = polygon[(i + 1) % n].x - polygon[i].x;
            i64 dy = polygon[(i + 1) % n].y - polygon[i].y;
            res += std::gcd(abs(dx), abs(dy));
        }
    return res;
    };
    i64 res = countBoundaryPoints(polygon);
    i64 ans = (area - res + 2) / 2;
    cout << ans << " " << res << " | n";
}</pre>
```

## 10.5 MinRadiusCoverCircle [a9fa76]

```
constexpr double Eps = 1e-7;
void solve(int n, vector<P> a, double maxR) {
    auto cal = [&](P center) {
        double mx = 0;
        for (auto& p : a)
            mx = max(mx, distance(center, p));
        return mx;
    };
    auto searchY = [&](double x) {
        double l = -maxR, r = maxR;
        while (r - l > Eps) {
            double ad = (r - l) / 3;
            double ml = l + d, mr = r - d;
            double ansl > aasr) l = ml;
            else r = mr;
        }
        return (l + r) / 2;
    };
    double l = -maxR, r = maxR;
    while (r - l > Eps) {
        double d = (r - l) / 3;
        double d = (r - l) / 3;
        double d = r - maxR, r = maxR;
    while (r - l > Eps) {
        double d = l + d, mr = r - d;
        double ml = l + d, mr = r - d;
        double ansl = cal({ml, yl}), ansr = cal({mr, yr});
        if (ansl > ansr) l = ml;
        else r = mr;
    }
    double ansX = (l + r) / 2, ansY = searchY(ansX);
}
```