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1 前言

1.1 Attention

```
// Construct VScode
// 1. instaint
// vscode & msys2, check desktop path of vscode
// 2. open mingw64, not ucrt64, "pacman
// -S --needed base-devel mingw-w64-x86_64-toolchain"
// 3. add C:\msys64\mingw64\bin to environment path
// 4. (re)open vscode, instaint C/C++, run, choose g++
// 5. open settings -> compiler -> add
// compilerPath "C:\msys64\mingw64\bin\g++.exe"

// Make Codebook
// notebook-generator ./ --author "Salmon" --initials
// Salmon --columns 3 --output "CodeBook.pdf" --size 8

// Init
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#define all(x) (x).begin(), (x).end()
#define pii pair<int, int>
#define endl "\n"
#define int long long
using namespace std;
using namespace __gnu_pbds;
template<typename T>
using pbds_set = tree<T, null_type, less_equal<T
>, rb_tree_tag, tree_order_statistics_node_update>;
template<typename T>
using pbds_multiset = tree<T, null_type, less_equal<T
>, rb_tree_tag, tree_order_statistics_node_update>;
struct cmp { // 在有 template 的資結使用
    bool operator()(const int &a, const int &b) const {
        return a < b;
    }
    // sort, bound 不用 struct
    // priority queue 小到大是 >, set 是 <
    // set 不能 =, multiset 要 =
    // 每個元素都要比到，不然會不見
};
struct edge {
    int from; int to;
    int weight;
};
struct node {
    int sum;
};
const int llinf = 4e18;
const int inf = 2e9;
```

```
const int mod = 1e9 + 7;
const int maxn = 2e5 + 5;
void solve(){
```

```
}
signed main(){
    ios_base::sync_with_stdio(0);
    cin.tie(nullptr);
    int t = 1;
    cin >> t;
    while(t--){
        solve();
    }
}
```

2 動態規劃

2.1 背包問題

```
#include <bits/stdc++.h>
using namespace std;
int dp[1005][100005];
// 考慮前 i 個，預算有 j 塊錢的最多 page
vector<int> Page(1005, 0);
vector<int> Price(1005, 0);
int main(){
    int n, bud;
    cin >> n >> bud;
    for(int i = 1; i <= n; i++){
        int tmp; cin >> tmp;
        Price[i] = tmp;
    }
    for(int i = 1; i <= n; i++){
        int tmp; cin >> tmp;
        Page[i] = tmp;
    }
    for(int i = 1; i <= n; i++){
        for(int j = 1; j <= bud; j++){
            if(j >= Price[i]){ // 買得起
                // 不買或買
                dp[i][j] = max(dp[i - 1][j],
                    dp[i - 1][j - Price[i]] + Page[i]);
            }
            else {
                dp[i][j] = dp[i - 1][j];
            }
        }
    }
    cout << dp[n][bud] << "\n";
}
```

2.2 Bitmask DP

```
#include <bits/stdc++.h>
using namespace std;
const int mod = 1e9 + 7;
void travel_exactly_once(){
    // [走過的路][終點]
    vector
        <vector<int>> dp(1 << 20, vector<int> (20, 0));
    vector<int> rev_adj[20];
    int n, m; cin >> n >> m;
    for(int i = 0; i < m; i++){
        int u, v; cin >> u >> v;
        rev_adj[-v].push_back(-u);
    }
    dp[1][0] = 1;
    for(int road = 0; road < (1 << n); road++){
        // 沒經過起點，不用走
        if(road & 1 == 0) continue;
        // 有終點但沒全部走過
        if(road & (1 << (n
            - 1)) && road != ((1 << n) - 1)) continue;
        // DP，隨便選定一個當前路徑的終點
        for (int end = 0; end < n; end++) {
            // 路徑沒包含假定的 end
            if ((road & (1 << end)) == 0) continue;
            // 去除終點，得到 pre_road
            int pre_road = road - (1 << end);
            // 從 rev_adj 找 pre_road 的終點
            for (int pre_road_end : rev_adj[end]) {
                if ((road & (1 << pre_road_end))) {
                    dp[road][end] += dp[pre_road][pre_road_end];
                    dp[road][end] %= mod;
                }
            }
        }
    }
}
```

```

    }
    }
    }
    cout << dp[(1 << n) - 1][n - 1];
}

void elevator_rides(){
    int n, k; cin >> n >> k;
    vector<int> passenger(n);
    for(int i = 0; i < n; i++) cin >> passenger[i];
    vector<int> used
        (1 << n, 0); // 最後載完人的電梯用了多少空間
    vector<int> dp(1 << n, 1); // bitset
    for(int i = 1; i < 1 << n; i++){
        used[i] = dp[i] = 2e9;
        for(int j = 0; j < n; j++){
            if(i & (1 << j)){ // 有 j
                int pre = i ^ (1 << j);
                // 最後的電梯還能載 j
                if(used[pre] + passenger[j] <= k){
                    // 電梯數先比，再來比用掉的空間
                    if(dp[pre] < dp[i] ||
                       (dp[pre] == dp[i] && used[pre]
                        + passenger[j] < used[i])){
                        used[i] = used[pre] + passenger[j];
                        dp[i] = dp[pre];
                    }
                }
            }
            // 搭新的電梯
            else {
                if(dp[pre] + 1
                   < dp[i] || (dp[pre] + 1 == dp[i]
                               && passenger[j] < used[i])){
                    used[i] = passenger[j];
                    dp[i] = dp[pre] + 1;
                }
            }
        }
    }
    cout << dp[(1 << n) - 1];
}

int main(){
    travel_exactly_once();
    elevator_rides();
}

```

2.3 硬幣

```

#include <bits/stdc++.h>
using namespace std;
const int mod = 1e9 + 7;
void coin_combination_II(){
    // 有 n 種錢幣，求組合為 x 的組數，順序不可顛倒
    // 可顛倒的話只要一維，先 x 迴圈，再 coin[i] 去加
    int n, x; cin >> n >> x;
    vector<int> coin(n + 1);
    // dp[i][j] 為考慮前 i 個硬幣，組合為 i 的組數
    vector<vector<int>> dp(2, vector<int>(x + 1, 0));
    dp[0][0] = 1;
    for(int i = 1; i <= n; i++) cin >> coin[i];
    for(int i = 1; i <= n; i++){
        for(int j = 0; j <= x; j++){
            // 壓到 2 * n
            dp[i & 1][j] = dp[!(i & 1)][j];
            if(j >= coin[i]){
                (dp[i & 1][j]
                 += dp[i & 1][j - coin[i]]) %= mod;
            }
        }
    }
    cout << dp[n & 1][x];
}

void minimize_coins_nums(){
    // 有 n 種錢幣，求組合為 x 的最小硬幣數
    int n, x; cin >> n >> x;
    vector<int> coin(n);
    for(int i = 0; i < n; i++) cin >> coin[i];
    // dp[i] 是組合為 i 的最小硬幣數
    vector<int> dp(x + 1, 0);
    for(int i = 1; i <= x; i++){
        dp[i] = 2e9;
        for(auto &j : coin){

```

```

            if(j <= i){
                dp[i] = min(dp[i], dp[i - j] + 1);
            }
        }
    }
    cout << (dp[x] == 2e9 ? -1 : dp[x]);
}

int main(){
    coin_combination_II();
    minimize_coins_nums();
}

2.4 編輯距離

#include <bits/stdc++.h>
using namespace std;
void solve(){
    string s1, s2; cin >> s1 >> s2;
    int size1 = s1.size(), size2 = s2.size();
    // dp
    // [i][j] 為 s1 的前 i 個字元，跟 s2 的前 j 個字元
    vector<vector<
        int>> dp(size1 + 1, vector<int>(size2 + 1, 0));
    s1 = "0" + s1, s2 = "0" + s2;
    for(int i = 1; i <= size1; i++) dp[i][0] = i;
    for(int i = 1; i <= size2; i++) dp[0][i] = i;
    for(int i = 1; i <= size1; i++){
        for(int j = 1; j <= size2; j++){
            if(s1[i] == s2[j]){
                dp[i][j] = dp[i - 1][j - 1];
            }
            else {
                // s1 新增等價於 s2 砍掉
                // dp[i]
                // [j] = min(修改, s1 新增, s2 新增);
                dp[i][j] = min({dp[i - 1][j - 1],
                               dp[i - 1][j], dp[i][j - 1]}) + 1;
            }
        }
    }
    cout << dp[size1][size2];
}

```

2.5 LCS

```

#include <bits/stdc++.h>
using namespace std;
int main(){
    int m, n; cin >> m >> n;
    string s1, s2;
    cin >> s1 >> s2;
    s1.insert(s1.begin(), '1');
    s2.insert(s2.begin(), '1');
    int L = 0;
    vector
        <vector<int>> dp(m + 1, vector<int>(n + 1, 0));

    for(int i = 1; i <= m; i++){
        for(int j = 1; j <= n; j++){
            if(s1[i] == s2[j]){
                dp[i][j] = dp[i - 1][j - 1] + 1;
            }
            else {
                dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
            }
        }
    }
    int length = dp[m][n];
    cout << length << "\n";
    vector<char> s(length);
    // along to dp to trace back
    while(m >= 1 && n >= 1){
        if(s1[m] == s2[n]){
            s[length - 1] = s1[m];
            m--;
            n--;
            length--;
        }
        else {
            if(dp[m - 1][n] > dp[m][n - 1]){
                m--;
            }
            else n--;
        }
    }
}

```

```

    for(auto c : s){
        cout << c;
    }
}

```

2.6 LIS

```

#include <bits/stdc++.h>
using namespace std;
// Rec Sequence LIS
void solve(){
    int n; cin >> n;
    vector<int> v(n);
    for(int i = 0; i < n; i++){
        cin >> v[i];
    }
    int dp[n]; vector<int> mono;
    mono.push_back(v[0]);
    dp[0] = 1; int L = 1;
    for(int i = 1; i < n; i++){
        if(v[i] > mono.back()){
            mono.push_back(v[i]);
            dp[i] = ++L;
        }
        else {
            auto it = lower_bound
                (mono.begin(), mono.end(), v[i]);
            *it = v[i];
            dp[i] = it - mono.begin() + 1;
        }
    }
    vector<int> ans;
    cout << L << endl;
    for(int i = n - 1; i >= 0; i--){
        if(dp[i] == L){
            ans.push_back(v[i]);
            L--;
        }
    }
    reverse(ans.begin(), ans.end());
    for(auto i : ans){
        cout << i << " ";
    }
}

```

2.7 Projects

```

#include <bits/stdc++.h>
using namespace std;
#define int long long
#define pii pair<int, int>
const int maxn = 2e5 + 5;
typedef struct {
    int u, v, w;
} project;
void compress(vector<int> &sorted, vector<project>
    & projects, vector<vector<pii>> &EndProjects){
    sort(sorted.begin(), sorted.end());
    sorted.erase(unique
        (sorted.begin(), sorted.end()), sorted.end());
    for(int i = 0; i < projects.size(); i++){
        EndProjects[lower_bound(sorted.begin(), sorted.
            end(), projects[i].v) - sorted.begin() + 1]
            .push_back({lower_bound(sorted.begin(), sorted.
                end(), projects[i].u) - sorted.begin() + 1,
                projects[i].w});
    }
}
signed main(){
    int n; cin >> n;
    vector<project> projects(n);
    vector<vector<pii>> EndProjects(2 * n + 1);
    vector<int> nums;
    for(int i = 0; i < n; i++){
        cin >> projects
            [i].u >> projects[i].v >> projects[i].w;
        nums.push_back(projects[i].u);
        nums.push_back(projects[i].v);
    }
    compress(nums, projects, EndProjects);
    vector<int> dp(nums.size() + 1, 0);
    for(int end = 1; end <= nums.size(); end++){
        dp[end] = dp[end - 1];
        for(auto [from, gain] : EndProjects[end]){
            dp[end] = max(dp[end], dp[from - 1] + gain);
        }
    }
}

```

```

    }
    cout << dp[nums.size()];
}
// Monotonic DP in campus contest, use monotonic stack
// first is lowest mountain, second is pref in stack

```

2.8 Removal Game

```

#include <bits/stdc++.h>
using namespace std;
int dp[5005][5005];
void solve(){
    int n; cin >> n;
    int pref = 0;
    vector<int> v(n+1);
    for(int i = 1; i <= n; i++){
        cin >> v[i];
        pref += v[i];
    }
    // dp[i][j] = max_diff(i to j);
    for(int i = n; i > 0; i--){
        for(int j = 1; j <= n; j++){
            if(i > j) continue;
            else if(i == j){
                dp[i][j] = v[i];
            }
            else {
                dp[i][j] = max(v[
                    i] - dp[i+1][j], v[j] - dp[i][j-1]
                ); // i+1, j-1, care dp's order
            }
        }
    }
    // x + y = sum, dp[1][n] = x - y;
    cout << (pref + dp[1][n]) / 2;
}

```

3 最大流

3.1 Dinic

```

#include <bits/stdc++.h>
using namespace std;
bool vis[505];
int lev[505], n, m, ans;
typedef struct {
    int to, w, rev_ind;
} edge;
vector<edge> adj[505];
bool label_level(){ //
    Tag the depth, if can't reach end => return false
    memset(lev, -1, sizeof(lev));
    lev[1] = 0;
    queue<int> q; q.push(1);
    while(!q.empty()){
        int u = q.front(); q.pop();
        for(auto i : adj[u]){
            if(i.w > 0 && lev[i.to] == -1){
                q.push(i.to);
                lev[i.to] = lev[u] + 1;
            }
        }
    }
    return (lev[n] == -1 ? false : true);
}
int dfs(int u, int flow){
    if(u == n) return flow;
    for(auto &i : adj[u]){
        if(lev[i.to]
            == lev[u] + 1 && !vis[i.to] && i.w > 0) {
            vis[i.to] = true;
            int ret = dfs(i.to, min(flow, i.w));
            if(ret > 0) {
                i.w -= ret;
                adj[i.to][i.rev_ind].w += ret;
                return ret;
            }
        }
    }
    return 0; // if can't reach end => return 0
}
void dinic(){
    while(label_level()){
        while(1){
            init(vis, 0);
        }
    }
}

```

```

        int tmp = dfs(1, inf);
        if(tmp == 0) break;
        ans += tmp;
    }
}
void build(){
    for(int i = 1; i <= m; i++) {
        int u, v, w; cin >> u >> v >> w;
        adj[u].push_back({v, w,
            (int)adj[v].sz}); // inverse flow's index
        adj[v].push_back({u, 0, (int)adj[u].sz-1}); // have pushed one, need to -1
    }
}
// Police Chase, need to open
// adj to Augment && ori to determine what pb give
// Dinic's dfs2, then use reach as u, if the edge pb has
// given && w == 0 && v is not in reach, is the ans
void dfs2(int now, unordered_set<int> &reach){
    if(!vis[now]){
        vis[now] = 1;
        reach.insert(now);
        for(auto i : adj[now]){
            if(i.w > 0){
                dfs2(i.to, reach);
            }
        }
    }
}
// two two pair // School Dance
// Dinic
// , then w == 0's edge, which pb has given is the ans

// Distinct Route
// edge set valid var, if we need to argument
// pos road, the reverse edge set true valid;
// if we need argument the argumented
// edge, both set false. Last, from v dfs ans times
bool get_road
(int now, vector<int> &ans, vector<bool> &vis){
    if(now == 1) return true;
    for(auto &v : adj[now]){
        if(v.arg_valid && !vis[v.to]){
            ans.push_back(v.to);
            vis[v.to] = true;
            bool flag = get_road(v.to, ans, vis);
            if(flag){
                v.arg_valid = false;
                return true;
            }
            ans.pop_back();
        }
    }
    return false;
}
}

```

3.2 MCMF

```

// Ceiled MinCostMaxFlow, if not, use dinic
typedef struct {
    int from, to, w, cost;
} edge;
int n, m, parcel;
vector<edge> adj; // set num to each edge
vector<int> p[505]; // p[u] has edge's num
int now_edge = 0;
void add_edge(int u, int v, int w, int cost){
    adj.push_back({u, v, w, cost});
    p[u].push_back(now_edge);
    now_edge++;
    adj.push_back({v, u, 0, -cost}); // argumenting path use -
    p[v].push_back(now_edge);
    now_edge++;
}
ll Bellman_Ford(){
    vector<ll> dis(n+1, inf); dis[1] = 0;
    vector<int> par(m);
    vector<int> flow_rec(n+1, 0); flow_rec[1] = 1e9;
    for(int i = 1; i < n; i++){
        bool flag = 1;
        int size = adj.sz;
        for(int i = 0; i < size; i++){
            auto &[from, to, w, cost] = adj[i];
            if(w > 0 && dis[to] > dis[from] + cost){

```

```

                flag = 0;
                dis[to] = dis[from] + cost;
                par[to] = i; // record num
                flow_rec[to] = min(flow_rec[from], w);
            }
        }
        if(flag) break;
    }
    if(dis[n] == 1e9) return 0;
    int mn_flow = flow_rec[n];
    int v = n;
    while(v != 1){
        int u = adj[par[v]].from;
        adj[par[v]].w -= mn_flow;
        adj[par[v]^1].w += mn_flow;
        v = u;
    }
    mn_flow = min(mn_flow, parcel);
    parcel -= mn_flow;
    return mn_flow * dis[n];
}
void solve(){
    cin >> n >> m >> parcel;
    ll ans = 0;
    for(int i = 1; i <= m; i++){
        int u, v, w, cost; cin >> u >> v >> w >> cost;
        add_edge(u, v, w, cost);
    }
    while(parcel > 0){
        int tmp = Bellman_Ford();
        if(tmp == 0) break;
        ans += tmp;
    }
    cout << (parcel > 0 ? -1 : ans);
}

```

4 向量

4.1 Cross Product

```

#include <bits/stdc++.h>
using namespace std;
#define int long long
const double EPS = 1e-9;
template <typename T>
struct Point {
    struct component {
        T val;
        bool operator == (component a) { return fabs(val - a.val) < EPS; }
        bool operator < (component a) { return a.val - val > EPS; }
        bool operator <= (component a) { return *this < a || *this == a; }
        component () : val (0) {}
        component (T val) : val (val) {}
    };
    component x, y;
    component new_component() { return component(); }
    Point () : x(0), y(0) {}
    Point (T x, T y) : x(x), y(y) {}
    Point operator * (T a) { return { a * x.val, a * y.val }; }
    Point operator + (Point b) { return { x.val + b.x.val, y.val + b.y.val }; }
    Point operator - (Point b) { return { x.val - b.x.val, y.val - b.y.val }; }
    bool operator == (Point b) { return x == b.x && y == b.y; }
    bool operator < (Point b) { return x == b.x ? y < b.y : x < b.x; }
    component dot (Point b) { return x.val * b.x.val + y.val * b.y.val; }
    component cross (Point b) { return x.val * b.y.val - y.val * b.x.val; }
    double length () { return sqrt(x.val * x.val + y.val * y.val); }
};
template <class Point>
struct Geometry {
    int destination (
        Point a, Point b, Point c) { // c 在 ab 的哪裡

```

```

    if ((b - a).cross(c - a) ==
        Point().new_component()) return 0; // 共線
    else if ((b - a).cross(c - a) < Point
        ().new_component()) return -1; // 左邊
    else return 1; // 右邊
}
bool between(Point a, Point b, Point c) {
    if (destination(a, b, c) != 0) return false;
    else return (c
        - a).dot(c - b) <= Point().new_component();
}
bool intersect(Point a, Point
    b, Point c, Point d) { // ab 跟 cd 是否相交
    if(between
        (a, b, c) || between(a, b, d) || between
        (c, d, a) || between(c, d, b)) return true;
    bool
        check1 = destination(a, b, c) * destination
        (a, b, d) < 0; // c, d 在 ab 的不同方位
    bool
        check2 = destination(c, d, a) * destination
        (c, d, b) < 0; // a, b 在 cd 的不同方位
    return check1 & check2;
}
};
signed main(){
    ios::sync_with_stdio(false);
    cin.tie(nullptr);
    int n; cin >> n;
    Geometry<Point<int>> geometry;
    while(n--){
        Point<int> a, b, c, d;
        cin >>
            a.x.val >> a.y.val >> b.x.val >> b.y.val >>
            c.x.val >> c.y.val >> d.x.val >> d.y.val;
        cout << (geometry.intersect
            (a, b, c, d) ? "YES\n" : "NO\n") << endl;
    }
}

```

4.2 Convex Hull

```

vector<pii> P, L, U;
ll cross(pii o, pii a, pii b){ // OA OB >0 counterclock
    return (a.first - o.first) * (b.second - o.second
        ) - (a.second - o.second) * (b.first - o.first);
}
ll Andrew_monotone_chain(ll n){
    sort(P.begin(), P.end());
    ll l = 0, u = 0; // upper and lower hull
    for (ll i=0; i<n; ++i){
        while (l
            >= 2 && cross(L[l-2], L[l-1], P[i]) <= 0){
            l--;
            L.pop_back();
        }
        while (u
            >= 2 && cross(U[u-2], U[u-1], P[i]) >= 0){
            u--;
            U.pop_back();
        }
        l++;
        u++;
        L.push_back(P[i]);
        U.push_back(P[i]);
    }
    cout << l << ' ' << u << '\n';
    return l + u;
}
int main(){
    ll n, x, y;
    cin >> n;
    for (ll i = 0; i < n; i++){
        cin >> x >> y;
        P.push_back({x, y});
    }
    ll ans = Andrew_monotone_chain(n) - 2;
    cout << ans << "\n";
    return 0;
}

```

5 圖論

5.1 2-SAT

```

#include <bits/stdc++.h>
using namespace std;
// +(-) u or +(-) v
const int maxn = 1e5 + 5;
vector<int> adj[2 * maxn], rev_adj[2 * maxn];
vector<int> order;
int cat[2 * maxn];
int k = 1;
bool vis[2 * maxn];
void dfs(int now){
    if (!vis[now]){
        vis[now] = 1;
        for (auto v : adj[now]){
            dfs(v);
        }
        order.push_back(now);
    }
}
void rev_dfs(int now){
    if (!vis[now]){
        cat[now] = k;
        vis[now] = 1;
        for (auto v : rev_adj[now]){
            rev_dfs(v);
        }
    }
}
int main(){
    int n, m;
    cin >> n >> m;
    for (int i = 1; i <= m; i++){
        int u, v;
        char a, b;
        cin >> a >> u >> b >> v;
        if (a == '-'){
            u = 2 * n - u + 1; // reverse
        }
        if (b == '-'){
            v = 2 * n - v + 1; // reverse
        }
        adj[2 * n - u + 1].push_back
            (v); // from -u to v; // if -u, then v
        adj[2 * n - v + 1].push_back
            (u); // from -v to u; // if -v, then u
        rev_adj[v].push_back(2 * n - u + 1);
        rev_adj[u].push_back(2 * n - v + 1);
    }
    for (int i = 1; i <= 2 * n; i++){
        if (!vis[i]){
            dfs(i);
        }
    }
    memset(vis, 0, sizeof(vis));
    reverse(order.begin(), order.end());
    for (auto i : order){
        if (!vis[i]){
            rev_dfs(i);
            k++;
        }
    }
    char ans[2 * n + 1];
    for (int i = 1; i <= n; i++){
        if (cat[i] == cat[2 * n - i + 1]){
            cout << "IMPOSSIBLE";
            return;
        }
        if (cat[i] > cat[2 * n - i + 1]){
            ans[i] = '+';
        }
        else ans[i] = '-';
    }
    for (int i = 1; i <= n; i++){
        cout << ans[i] << " ";
    }
}

```

5.2 DFS 跟 BFS

```

#include <bits/stdc++.h>
using namespace std;
const int maxn = 1e6;
vector<int> adj[maxn];
bool vis[maxn];
void DFS(int s){
    if (vis[s]) return;
    vis[s] = true;
}

```

```

    for(auto u: adj[s]){
        DFS(u);
    }
}
queue<int> q;
int dis[maxn];
void BFS(int x){
    vis[x] = true;
    dis[x] = 0;
    q.push(x);
    while(!q.empty()){
        int now = q.front(); q.pop();
        for(auto nxt: adj[now]){
            if(vis[nxt]) continue;
            vis[nxt] = true;
            dis[nxt] = dis[now] + 1;
            q.push(nxt);
        }
    }
}
}
}

```

5.3 DSU

```

#include <bits/stdc++.h>
using namespace std;
// After each day, print the number of components
// and the size of the largest component
struct DSU {
    vector<int> boss, siz;
    DSU (int n){
        boss.resize(n + 1);
        iota(boss.begin(), boss.end(), 0);
        siz.assign(n + 1, 1);
    }
    int find_boss(int x){
        if(boss[x] == x) return x;
        return boss[x] = find_boss(boss[x]);
    }
    bool same(int x, int y) {
        return find_boss(x) == find_boss(y);
    }
    bool merge(int x, int y){
        x = find_boss(x);
        y = find_boss(y);
        if (x == y) {
            return false;
        }
        if(siz[x] < siz[y]) swap(x, y);
        siz[x] += siz[y];
        boss[y] = x;
        return true;
    }
    int size(int x){
        return siz[find_boss(x)];
    }
};

```

5.4 EulerRoad

```

#include <bits/stdc++.h>
using namespace std;
// Undirected: check adj[i].sz
// == odd => IMPOSSIBLE, road.sz != m+1 => IMPOSSIBLE
// Directed: minimize
// to 1 -> 2, so check in_degree == out_degree
int n, m;
const int maxn = 1e5 + 5;
set<int> adj[maxn]; // rev_adj[maxn];
int in[maxn];
void dfs(int now, vector<int> &road){
    while(!adj[now].empty()){
        int nxt = *adj[now].begin();
        adj[now].erase(nxt);
        dfs(nxt, road);
    }
    road.push_back(now);
}
void solve(){
    cin >> n >> m;
    memset(in, sizeof(in), 0);
    for(int i = 1; i <= m; i++){
        int u, v; cin >> u >> v;
        adj[u].insert(v);
        in[v]++;
    }
    in[1]++;
}

```

```

in[n]--;
for(int i = 1; i <= n; i++){
    if(adj[i].size() != in[i]){
        cout << "IMPOSSIBLE";
        return;
    }
}
vector<int> road;
dfs(1, road);
if(road.size() != m+1){
    cout << "IMPOSSIBLE";
    return;
}
reverse(road.begin(), road.end());
for(auto i: road) cout << i << " ";
}
}

```

5.5 FloydWarshall

```

#include <bits/stdc++.h>
using namespace std;
const int maxn = 505;
int graph[maxn][maxn];
int dis[maxn][maxn];
int n, m, q; int a, b, c;
const int INF = 1e18;
int main(){
    cin >> n >> m >> q;
    for(int i = 0; i <= n; i++) {
        for(int j = 0; j <= n; j++) {
            graph[i][j] = INF;
        }
    }
    for(int i = 0; i < m; i++){
        cin >> a >> b >> c;
        graph[a][b] = min(graph[a][b], c);
        graph[b][a] = min(graph[b][a], c);
    }
    for(int i = 0; i <= n; i++) {
        for(int j = 0; j <= n; j++) {
            dis[i][j] = graph[i][j];
        }
    }
    for(int i = 0; i <= n; i++) // self to self is 0
        dis[i][i] = 0;

    for(int k = 1; k <= n; k++){
        for(int i = 1; i <= n; i++){
            for(int j = 1; j <= n; j++){
                dis[i][j] = min(
                    (dis[i][j], dis[i][k] + dis[k][j]));
            }
        }
    }
    for(int i = 0; i < q; i++){
        cin >> a >> b;
        cout << (
            dis[a][b] >= INF ? -1 : dis[a][b]) << "\n";
    }
}

```

5.6 用 Bellman 找負環

```

#include <bits/stdc++.h>
using namespace std;
typedef struct{
    int from; int to;
    int weight;
} edge;
// NegCyc_Finding_Road
vector<edge> graph;
int main(){
    int src = 0;
    int n, m; cin >> n >> m;
    vector<int> par(n + 1), dis(n + 1);
    for(int i = 0; i < m; i++){
        int a, b, w; cin >> a >> b >> w;
        graph.push_back({a, b, w});
    }
    for(int i = 1; i <= n; i++){
        dis[i] = 1e9 + 5;
    }
    dis[1] = 0;
    for(int i = 0; i <= n; i++){
        src = 0;
        for(auto [a, b, w]: graph){

```



```

        if(dis[b] > dis[a] + w){
            dis[b] = dis[a] + w;
            par[b] = a;
            src = b;
        }
    }
}
if(src){
    vector<int> ans;
    cout << "YES" << endl;
    for(int i = 0; i <= n; i++) src = par[src];
    ans.push_back(src);
    for(int i = par[src]; i != src; i = par[i]){
        ans.push_back(i);
    }
    ans.push_back(src);
    reverse(ans.begin(), ans.end());
    for (auto i : ans){
        cout << i << " ";
    }
}
else {
    cout << "NO" << endl;
}
}
}

```

5.7 最大距離

```

#include <bits/stdc++.h>
using namespace std;
// Max_Dis, Use Topo, Use queue
// If 1 can
// 't reach n, still may be relaxed, Should dis[n] < 0
// Only Directed Graph
void print_ans(int n, vector<int> &par){
    deque<int> ans;
    int now = n;
    while(now != 1){
        ans.push_front(now);
        now = par[now];
    }
    ans.push_front(1);
    cout << ans.size() << endl;
    for(auto i : ans){
        cout << i << " ";
    }
}
void solve(){
    int n, m;
    cin >> n >> m;
    vector<int> dis(n + 1, -1e9); dis[1] = 0;
    vector<int> graph[n+1];
    vector<bool> vis(n+1, 0);
    vector<int> par(n+1);
    vector<int> in(n+1, 0);
    queue<int> q;
    for(int i = 1; i <= m; i++){
        int u, v; cin >> u >> v;
        graph[u].push_back(v);
        in[v]++;
    }
    for(int i = 1; i <= n; i++){
        if(in[i] == 0) q.push(i);
    }
    while(!q.empty()){
        int u = q.front(); q.pop();
        for(auto nxt : graph[u]){
            if(dis[nxt] < dis[u] + 1){
                dis[nxt] = dis[u] + 1;
                par[nxt] = u;
            }
            in[nxt]--; if(in[nxt] == 0) q.push(nxt);
        }
        vis[u] = 1;
    }
    if(dis[n] < 0){
        cout << "IMPOSSIBLE";
    }
    else print_ans(n, par);
}
}

```

5.8 負權最大距離

```

#include <bits/stdc++.h>
using namespace std;
const int maxn = 2505;

```

```

typedef struct {
    int u, v, w;
} edge;
int m, n;
vector<edge> graph;
vector<pair<int, int>> adj[maxn];
vector<int> rev_adj[maxn];
int dis[maxn];
bool vis[maxn] = {0};
bool nvis[maxn] = {0};
void dfs(int par, int now){
    if (vis[now] == 1) return;
    vis[now] = 1;
    for (auto [i, w] : adj[now]){
        if (i != par){
            dfs(now, i);
        }
    }
}
void rev_dfs(int par, int now){
    if (nvis[now] == 1) return;
    nvis[now] = 1;
    for (auto i : rev_adj[now]){
        if (i != par){
            rev_dfs(now, i);
        }
    }
}
void solve(){
    cin >> n >> m;
    for(int i = 1; i <= m; i++){
        int u, v, w;
        cin >> u >> v >> w;
        graph.push_back({u, v, w});
        adj[u].push_back({v, w});
        rev_adj[v].push_back(u);
    }
    for(int i = 1; i <= n; i++) dis[i] = -1e9;
    dis[1] = 0;
    for(int i = 1; i <= n; i++){
        for (auto [u, v, w] : graph){
            if (dis[u] + w > dis[v]){
                dis[v] = dis[u] + w;
            }
        }
    }
    dfs(0, 1);
    rev_dfs(0, n);
    for (auto [u, v, w] : graph){
        if (dis[u] + w > dis[v]
            && nvis[u] && nvis[v] && vis[u] && vis[v]){
            cout << -1;
            return;
        }
    }
    cout << dis[n];
}

```

5.9 Planet Queries II

```

#include <bits/stdc++.h>
using namespace std;
// now
// on a and want to reach b, the min steps, directed
int n, q;
const int maxn = 2e5 + 5;
int dp[30][maxn];
vector<vector<int>> cycles;
int no[maxn]; // Order & Can be in cycle, or out
int cycle_idx[maxn];
bool vis[maxn];
void set_out_of_cycle_no(
    (int now, unordered_set<int> &done){
    if (done.find(now) != done.end()){
        return;
    }
    set_out_of_cycle_no(dp[0][now], done);
    done.insert(now);
    no[now] = no[dp[0][now]] - 1;
}
}
int wiint_go_to(
    (int u, int k){ // return the node when walk k
    for(int i = 0; i <= 18; i++){
        if (k & (1 << i)){
            u = dp[i][u];
        }
    }
}
}

```

```

    return u;
}
void find_cycle(int now){
    unordered_set<int> appear;
    vector<int> vec;
    bool flag = true;
    while (appear.find(now) == appear.end()){
        appear.insert(now);
        vec.push_back(now);
        if (vis[now]){ // Didn't Find Cycle
            flag = false;
            break;
        }
        now = dp[0][now];
    }
    for (auto i : vec) vis[i] = true;
    if (!flag) return;
    int z = find(vec.begin(), vec.end(), now) - vec.begin(); // start pushing from last now
    int m = vec.size();
    vector<int> cycle;
    for (int i = z; i < m; i++){
        cycle.push_back(vec[i]);
    }
    cycles.push_back(cycle);
}
void solve(){
    cin >> n >> q;
    for(int u = 1; u <= n; u++){
        cin >> dp[0][u];
    }
    for(int i = 1; i <= 18; i++){ // Make Chart
        for(int u = 1; u <= n; u++){
            dp[i][u] = dp[i - 1][dp[i - 1][u]];
        }
    }
    for(int i = 1; i <= n; i++){
        if (!vis[i]) find_cycle(i);
    }
    int idx = 0;
    memset(no, -1, sizeof(no));
    memset(cycle_idx, -1, sizeof(cycle_idx));
    unordered_set<int> done;
    for (auto &i : cycles){
        int c = 0;
        for (auto &j : i){
            no[j] = c++;
            cycle_idx[j] = idx;
            done.insert(j);
        }
        idx++;
    }
    for(int i = 1; i <= n; i++) set_out_of_cycle_no(i, done);
    for(int i = 1; i <= q; i++){
        int u, v; cin >> u >> v;
        // Same Cycle
        if (cycle_idx[u] == cycle_idx[v] &&
            cycle_idx[u] != -1 && cycle_idx[v] != -1){
            int cyc_size = cycles[cycle_idx[u]].size();
            cout << (no[v] - no[u] + cyc_size) % cyc_size << "\n";
        }
        else if (cycle_idx[u] == -1 && cycle_idx[v] == -1){ // Both are not in a Cycle
            if (no[u] > no[v]){
                cout << -1 << "\n";
                continue;
            }
            int jump = no[v] - no[u];
            if (wiint_go_to(u, jump) == v){
                cout << jump << "\n";
            }
            else cout << -1 << "\n";
        }
        else if (cycle_idx[u] == -1 && cycle_idx[v] != -1)
        { // v is in cycle, Smainter Binary Search
            int l = -1, r = n;
            while (l <= r){
                int m = (l + r) / 2;
                if (cycle_idx[wiint_go_to(u, m)] == cycle_idx[v]){
                    r = m - 1;
                }
            }
            else

```

```

                l = m + 1;
            }
            if (l != -1 && l <= n){
                int in_cycle_of_u = wiint_go_to(u, l);
                int cycle_size = cycles[cycle_idx[v]].size();
                cout << l + (no[v] - no[in_cycle_of_u] + cycle_size) % cycle_size << "\n";
            }
            else cout << -1 << "\n";
        }
        else { // u is death in the cycle, can't reach
            cout << -1 << "\n";
        }
    }
}

```

5.10 Planets Cycles

```

#include <bits/stdc++.h>
using namespace std;
vector<int> dis, v;
vector<bool> vis;
int step;
queue<int> path;
void dfs(int x){
    path.push(x);
    if (vis[x]){
        step += dis[x];
        return;
    }
    vis[x] = true;
    step++;
    dfs(v[x]);
}
// count path_dis to rep
int main(){
    int n; cin >> n;
    v.assign(n + 1, 0);
    dis.assign(n + 1, 0);
    vis.assign(n + 1, false);
    for (int i = 1; i <= n; i++){
        cin >> v[i];
    }
    for (int i = 1; i <= n; i++){
        step = 0;
        int is_outof_cycle = 1;
        dfs(i);
        while (!path.empty()){
            if (path.front() == path.back()){
                is_outof_cycle = 0;
            }
            dis[path.front()] = step;
            step -= is_outof_cycle;
            path.pop();
        }
    }
    for (int i = 1; i <= n; i++){
        cout << dis[i] << ' ';
    }
    cout << '\n';
}

```

5.11 找環

```

#include <bits/stdc++.h>
using namespace std;
const int maxn = 1e5 + 5;
vector<int> graph[maxn];
int color[maxn], parent[maxn];
bool vis[maxn];
int n, m;
void print_ans(int ori){
    int now = parent[ori];
    deque<int> ans;
    ans.push_front(ori);
    while (now != ori){
        ans.push_front(now);
        now = parent[now];
    }
    ans.push_front(ori);
    cout << ans.size() << endl;
    for (auto i : ans){
        cout << i << " ";
    }
    exit(0);
}

```



```

}
void dfs(int now){
    color[now] = 1;
    vis[now] = 1;
    for(auto nxt : graph[now]){
        parent[nxt] = now;
        if(color[nxt] == 1){
            print_ans(nxt);
        }
        else if(color[nxt] == 0){
            dfs(nxt);
        }
    }
    color[now] = 2;
}
void solve(){
    cin >> n >> m;
    for(int i = 1; i <= m; i++){
        int u, v; cin >> u >> v;
        graph[u].push_back(v);
    }
    for(int i = 1; i <= n; i++){
        if(!vis[i])
            dfs(i);
    }
    cout << "IMPOSSIBLE";
}
}

```

5.12 Prim

```

#include <bits/stdc++.h>
using namespace std;
#define pii pair<int, int>
int n, m;
int ans = 0;
const int maxn = 2e5 + 5;
vector<pair<int, int>> adj[maxn];
bool Prim(){
    int node_sz = 0;
    priority_queue<pii, vector<pii>, greater<pii>> pq;
    pq.push({0, 1});
    bool vis[maxn] = {false};
    while(!pq.empty()){
        auto [cost, u] = pq.top(); pq.pop();
        if(vis[u]) continue;
        vis[u] = true;
        ans += cost;
        node_sz++;
        for(auto [v, cost] : adj[u]){
            if(!vis[v])
                pq.push({cost, v});
        }
    }
    if(node_sz == n) return true;
    return false;
}
void solve(){
    cin >> n >> m;
    for(int i = 1; i <= m; i++){
        int u, v, cost; cin >> u >> v >> cost;
        adj[u].push_back({v, cost});
        adj[v].push_back({u, cost});
    }
    if(Prim()) cout << ans;
    else cout << "IMPOSSIBLE";
}
}

```

5.13 SCC 跟拓撲 DP

```

#include <bits/stdc++.h>
using namespace std;
#define int long long
// 找到所有 SCC 然後結合原圖重建一個 DAG，然後拓撲 DP
void dfs(int u, vector<int> &vis, vector<int> &kosaraju, vector<vector<int>> &adj){
    if(!vis[u]){
        vis[u] = 1;
        for(auto v : adj[u]){
            dfs(v, vis, kosaraju, adj);
        }
        kosaraju.push_back(u);
    }
}
void rev_dfs(int u, vector<int> &vis, vector<int> &order, vector<vector<int>> &rev_adj, int &scc_num){
    if(!vis[u]){

```

```

        vis[u] = 1;
        order[u] = scc_num;
        for(auto v : rev_adj[u]){
            rev_dfs(v, vis, order, rev_adj, scc_num);
        }
    }
}
signed main(){
    int n, m, scc_num = 0;
    cin >> n >> m;
    vector<int> coin(n + 1), order(n + 1), vis(n + 1, 0);
    vector<vector<int>> adj(n + 1, vector<int>());
    vector<int> kosaraju;
    for(int i = 1; i <= n; i++){
        cin >> coin[i];
    }
    for(int i = 1; i <= m; i++){
        int u, v; cin >> u >> v;
        adj[u].push_back(v);
        rev_adj[v].push_back(u);
    }
    for(int i = 1; i <= n; i++){
        if(!vis[i]){
            dfs(i, vis, kosaraju, adj);
        }
    }
    reverse(kosaraju.begin(), kosaraju.end());
    vis.assign(n + 1, 0);
    for(auto &u : kosaraju){
        if(!vis[u]){
            scc_num++;
            rev_dfs(u, vis, order, rev_adj, scc_num);
        }
    }
    // 重新建 DAG
    vector<vector<int>> DAG(scc_num + 1, vector<int>());
    vector<int> in_degree(scc_num + 1, 0);
    vector<int> sum_coin(scc_num + 1, 0);
    set<pair<int, int>> st;
    int ans = -1e9;
    for(int i = 1; i <= n; i++){
        sum_coin[order[i]] += coin[i];
        for(auto j : adj[i]){
            if(order[i] != order[j] && st.find({order[i], order[j]}) == st.end()){
                DAG[order[i]].push_back(order[j]);
                in_degree[order[j]]++;
                st.insert({order[i], order[j]});
            }
        }
    }
    // 對 DAG 拓撲 DP
    queue<int> q;
    for(int i = 1; i <= scc_num; i++){
        if(in_degree[i] == 0){
            q.push(i);
        }
    }
    while(!q.empty()){
        int now = q.front(); q.pop();
        dp_coin[now] += sum_coin[now];
        ans = max(ans, dp_coin[now]);
        for(auto v : DAG[now]){
            in_degree[v]--;
            dp_coin[v] = max(dp_coin[v], dp_coin[now]);
            if(in_degree[v] == 0) q.push(v);
        }
    }
    cout << ans;
}
}

```

5.14 狀態 Dijkstra

```

#include <bits/stdc++.h>
using namespace std;
#define pii pair<int, int>
// Flight Discount
int n, m;
const int maxn = 2e5 + 5;
vector<pii> graph[maxn];
int dis[maxn][2]; // 0 for not used
void dijkstra(){

```

```

priority_queue<vector
<int>, vector<vector<int>>, greater<vector<
int>>> pq; // 0 for w, 1 for u, 2 for discount
for(int i = 1; i <= n; i++){
    dis[i][0] = dis[i][1] = 1e9;
}
dis[1][0] = dis[1][1] = 0;
pq.push({0, 1, 0});
while(!pq.empty()){
    auto nxt = pq.top(); pq.pop();
    int dist
        = nxt[0], u = nxt[1]; bool us = nxt[2];
    if(dis[u][us] < dist) continue; // is out of time, pass
    if(us){
        for(auto [v, w] : graph[u]){
            if(dis[u][1] + w < dis[v][1]){
                dis[v][1] = dis[u][1] + w;
                pq.push({dis[v][1], v, 1});
            }
        }
    }
    else {
        for(auto [v, w] : graph[u]){
            if(dis[u][0] + w < dis[v][0]){
                dis[v][0] = dis[u][0] + w;
                pq.push({dis[v][0], v, 0});
            }
            if(dis[u][0] + w / 2 < dis[v][1]){
                dis[v][1] = dis[u][0] + w / 2;
                pq.push({dis[v][1], v, 1});
            }
        }
    }
}
cout << min(dis[n][0], dis[n][1]);
}
void solve(){
    cin >> n >> m;
    for(int i = 1; i <= m; i++){
        int u, v, w;
        cin >> u >> v >> w;
        graph[u].push_back({v, w});
    }
    dijkstra();
}

```

5.15 Vis Dijkstra

```

#include <bits/stdc++.h>
using namespace std;
void solve(){
    int n, m, noon, night;
    cin >> n >> m >> noon >> night;
    int dis[n + 1];
    vector<int> graph[n + 1];
    bool vis[n + 1];
    for(int i = 1; i <= m; i++){
        int u, v, w; cin >> u >> v >> w;
        graph[u].push_back({v, w});
        graph[v].push_back({u, w});
    }
    priority_queue<vector<int>,
        vector<vector<int>>, greater<vector<int>>> pq;
    // noon is -
    for(int i = 1; i <= n; i++){
        dis[i] = 1e9; vis[i] = 0;
    }
    pq.push({0, -noon, 1});
    dis[1] = 0;
    while(!pq.empty()){
        vector<int> now = pq.top(); pq.pop();
        int now_noon = -now[1], u = now[2];
        if(vis[u]) continue;
        for(auto [nxt, w] : graph[u]){
            if(noon < w) continue; // never pass
            int tmp = dis[u] + (now_noon
                >= w ? w : now_noon + night + w);
            if(tmp < dis[nxt]){
                dis[nxt] = tmp;
                pq.push({dis[nxt], -(now_noon >= w
                    ? now_noon - w : noon - w), nxt});
            }
        }
        vis[u] = true;
    }
}

```

```

if(dis[n] == 1e9) cout << -1 << endl;
else cout << dis[n] << endl;
}
// Investigation
void Investigation(){
    vector<vector<
        for(auto [v, w] : graph[u]){
            if(dis[u] + w < dis[v]){
                dis[v] = dis[u] + w;
                pq.push({dis[v], v});
                min_price_nums[v] = min_price_nums[u];
                max_dis_min_price
                    [v] = max_dis_min_price[u] + 1;
                min_dis_min_price
                    [v] = min_dis_min_price[u] + 1;
            }
            else if(dis[u] + w == dis[v]){
                min_price_nums[v] = (min_price_nums
                    [u] + min_price_nums[v]) % mod;
                max_dis_min_price
                    [v] = max(max_dis_min_price
                        [u] + 1, max_dis_min_price[v]);
                min_dis_min_price
                    [v] = min(min_dis_min_price
                        [u] + 1, min_dis_min_price[v]);
            }
        }
    }
}
int main(){
    solve();
    Investigation();
}

```

6 數學

6.1 質因數分解

```

#include <bits/stdc++.h>
using namespace std;
// a^(m-1) ≡ 1 (mod m)
// a^(m-2) ≡ 1/a (mod m)
// EXP2
// : cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)
// Filter +
// DP; DP save min factor, recur, factor decomposition
// FacNums = (x+1)(y+1)(z+1)...
// FacSum = (a^0+a^1+...+a^x)(b^0+...+b^y)
// FacMul = N(x+1)(y+1)(z+1)/2
int main(){
    vector<int> is_prime(2e6 + 1, 1);
    // 1 代表是質數，非 1 不是
    for(int i = 2; i <= 1000; i++){
        if(is_prime[i] == 1){
            for(int j = i + i; j <= 1000000; j += i){
                is_prime[j] = 0;
            }
        }
    }
    int ans = 1;
    int q; cin >> q;
    map<int, int> mp;
    while(is_prime[q] != 1){
        mp[is_prime[q]]++;
        q /= is_prime[q];
    }
    if(q != 1) mp[q]++;
    for(auto [a, b] : mp){
        ans *= b + 1;
    }
    cout << ans << "\n";
}

```

6.2 盧卡斯定理

```

struct nCr {
    int mod;
    nCr(int mod) : mod(mod){};
    int inverse(int num){
        if(num == 1) return 1;
        return (mod - ((mod
            / num) * inverse(mod % num)) % mod) % mod;
    }
    int fast_exp(int x, int p){
        int ans = 1;
        while(p > 0){
            if(p & 1) ans = (ans * x) % mod;
        }
    }
}

```

```

        x = x * x % mod;
        p >>= 1;
    }
    return ans;
}
vector<int> fac;
void BuildLucas(int n){
    fac.resize(n + 1);
    fac[0] = 1;
    for(int i = 1; i <= n; i++){
        fac[i] = fac[i - 1] * i % mod;
    }
}
int C(int m, int n){
    return m < n ? 0 : fac[m] * inverse
        (fac[n]) % mod * inverse(fac[m - n]) % mod;
}
int Lucas(int m, int n){
    return n == 0 ? 1 % mod : Lucas(m /
        mod, n / mod) * C(m % mod, n % mod) % mod;
}
};

```

7 Queries

7.1 BIT

```

#include <bits/stdc++.h>
using namespace std;
struct BIT {
    int n;
    vector<int> bit;
    BIT(int n) {
        this->n = n;
        bit.resize(n + 1, 0);
    }
    BIT(vector<int> &init) {
        this->n = init.size();
        bit.resize(n + 1, 0);
        for (int i = 0; i < n; i++) {
            modify(i + 1, init[i]);
        }
    }
    void modify(int i, int val) {
        for (; i <= n; i += i & -i) {
            bit[i] += val;
        }
    }
    int query(int r) {
        int ans = 0;
        for (; r; r -= r & -r) ans += bit[r];
        return ans;
    }
    int query(int l, int r) {
        return query(r) - query(l - 1);
    }
};
struct TwoDimensionBIT {
    int nx, ny;
    vector<vector<int>> bit;
    TwoDimensionBIT(int x, int y) {
        nx = x; ny = y;
        bit.resize(x + 1, vector<int>(y + 1, 0));
    }
    void modify(int x, int y, int mod){
        for(; x <= nx; x += x & -x){
            for(int
                tmp = y; tmp <= ny; tmp += tmp & -tmp){
                bit[x][tmp] += mod;
            }
        }
    }
    int query(int r1, int r2){
        int ans = 0;
        for(; r1; r1 -= r1 & -r1){
            for(int tmp = r2; tmp; tmp -= tmp & -tmp){
                ans += bit[r1][tmp];
            }
        }
        return ans;
    }
};

```

7.2 Increasing Array Queries

```

#include <bits/stdc++.h>
using namespace std;
const int maxn = 2e5+5;
int n, q;
int nums[maxn],
    prefix[maxn], ans[maxn], BIT[maxn], contrib[maxn];
vector<pair<int, int>> queries[maxn];
void update(int pos, int val) {
    for (; pos <= n; pos += pos & -pos) BIT[pos] += val;
}
int query(int a, int b) {
    int ans = 0;
    for (; b; b -= b & -b) ans += BIT[b];
    for (a--; a; a -= a & -a) ans -= BIT[a];
    return ans;
}
void solve(){
    cin >> n >> q;
    for(int i = 1; i <= n; i++){
        cin >> nums[i];
        prefix[i] = prefix[i-1] + nums[i];
    }
    nums[n + 1] = 1e9;
    prefix[n + 1] = 2e18;
    for(int i = 1; i <= q; i++){
        int a, b; cin >> a >> b;
        queries[a].push_back({b, i});
    }
    deque<int> mono; mono.push_front(n+1);
    for(int i = n; i > 0;
        i--){ // question from start at n to start at 1
        while (nums[i] >= nums[mono.front()]) {
            update(mono.front(), -contrib[mono.front
                ()]); // mono.front's contrib become 0
            mono.pop_front();
        }
        contrib[i] = (mono.front() - 1 - i) * nums
            [i] - (prefix[mono.front() - 1] - prefix[i]);
        update(i, contrib[i]);
        mono.push_front(i);
        for (auto j : queries[
            i]) { // pos is the index in mono <= end's
            int pos = upper_bound(mono.begin
                (), mono.end(), j.first) - mono.begin() - 1;
            ans[j.second] = (pos ? query(i, mono
                [pos - 1]) : 0) // smainter than y's mono
                // mono
                to y caculate directly
                + (j.first
                    - mono[pos]) * nums[mono[pos]]
                    - (prefix[j.first
                        ] - prefix[mono[pos]]);
            }
        }
    }
    for(int i = 1; i <= q; i++){
        cout << ans[i] << endl;
    }
}

```

7.3 線段樹

```

#include <bits/stdc++.h>
using namespace std;
template <class Node>
struct Seg {
    int n;
    vector<Node> tree;
    Seg (vector<Node> init_){
        n = init_.size() - 1;
        tree.resize(4 * n);
        function <void(int, int,
            int)> build = [&](int now, int l, int r) {
            if (l == r) {
                tree[now] = init_[l];
                return;
            }
            int m = (l + r) / 2;
            build(now << 1, l, m);
            build((now << 1) + 1, m + 1, r);
            pull(now);
        };
        build(1, 1, n);
    }
    Node query(int l, int r, int ql, int qr, int now){
        int m = (l + r) >> 1;
        if(qr < l || ql > r){

```

```

        return Node();
    }
    if(ql <= l && r <= qr){
        return tree[now];
    }
    return query(l, m, ql, qr, now <<
        1) + query(m + 1, r, ql, qr, (now << 1) + 1);
}
Node query
(int l, int r) { return query(1, n, l, r, 1); }
void pull(int now){
    tree[now]
        = tree[now << 1] + tree[(now << 1) + 1];
}
void modify
(int l, int r, int idx, int now, int add){
    if(l == r){
// -----
// how to modify ?-----
        tree[now].sum = add;
// -----
// -----

        return;
    }
    int m = (l + r) >> 1;
    if(idx <= m){
        modify(l, m, idx, now << 1, add);
    }
    else {
        modify(m + 1, r, idx, (now << 1) + 1, add);
    }
    pull(now);
}
void modify(int
    idx, int add) { modify(1, n, idx, 1, add); }
};
// -----define
// structure and info plus-----
struct Node {
    int sum;
    Node () {
        sum = 0;
    }
};
Node operator + (const Node &a, const Node &b) {
    Node c;
    c.sum = a.sum + b.sum;
    return c;
    // use lc、rc to undate now
    // tree[now].sum = tree[lc].sum + tree[rc].sum;
    // tree[now].prefix = max(
    //     tree[lc].sum+tree[rc].prefix, tree[lc].prefix);
    // tree[now].suffix = max(
    //     tree[lc].suffix+tree[rc].sum, tree[rc].suffix);
    // tree[now].middle_max
    //     = max(max(tree[lc].middle_max, tree[rc].
    //         middle_max), tree[lc].suffix+tree[rc].prefix);
    // tree
    //     [now].middle_max = max(max(tree[now].middle_max
    //         , tree[now].prefix), tree[now].suffix);
}
// -----
// -----

// pizza_queries
// 左邊的店(s < t): dis_l = (pizza[s] - s) + t;
// 右邊的店(t < s): dis_r = (pizza[s] + s) - t;
// 實作: 建左查詢線段樹跟右查詢線段樹, 用最小值pull
// 答案是
//     min(left_query(1, s) + t, right_query(s, end) + t);

// List Removals
// 維護區間內有幾個數字被選過
// 用二分搜找右
// 區間最小位, 使得 ans - query == 1~ans 被選過的數量

```

7.4 懶標線段樹

```

#include <bits/stdc++.h>
using namespace std;
template <class Node, class Lazy>

```

```

struct LazySeg {
    int n;
    vector<Node> tree;
    vector<Lazy> lazy;
    template <typename T>
    LazySeg (vector<T> init_){
        n = init_.size() - 1;
        tree.resize(4 * n);
        lazy.resize(4 * n);
        function <void(int, int,
            int)> build = [&](int now, int l, int r) {
            if (l == r) {
                tree[now] = init_[l];
                return;
            }
            int m = (l + r) / 2;
            build(now << 1, l, m);
            build((now << 1) + 1, m + 1, r);
            pull(now);
        };
        build(1, 1, n);
    }
    Node query(int l, int r, int ql, int qr, int now){
        int m = (l + r) >> 1;
        if(qr < l || ql > r){
// -----out of
// range, return what-----
            return Node();
// -----
// -----

        }
        push(now, l, r);
        if(ql <= l && r <= qr){
            return tree[now];
        }
        return query(l, m, ql, qr, now <<
            1) + query(m + 1, r, ql, qr, (now << 1) + 1);
    }
    Node query
        (int l, int r) { return query(1, n, l, r, 1); }
    void pull(int now){
        tree[now]
            = tree[now << 1] + tree[(now << 1) + 1];
    }
    void modify_add(int
        l, int r, int ql, int qr, int now, int add){
        int m = (l + r) >> 1;
        if(qr < l || ql > r){
            return;
        }
        if(ql <= l && r <= qr){
// -----
// how to modify ?-----
            lazy[now].add += add;
// -----
// -----

            return;
        }
        push(now, l, r);
        modify_add(l, m, ql, qr, now << 1, add);
        modify_add
            (m + 1, r, ql, qr, (now << 1) + 1, add);
        push(now << 1, l, m);
        push((now << 1) + 1, m + 1, r);
        pull(now);
    }
    void modify_add(int l, int
        r, int add) { modify_add(1, n, l, r, 1, add); }
    void modify_set(int
        l, int r, int ql, int qr, int now, int val){
        int m = (l + r) >> 1;
        if(qr < l || ql > r){
            return;
        }
        if(ql <= l && r <= qr){
// -----
// how to modify ?-----
            lazy[now].set_val = val;
            lazy[now].add = 0;
// -----
// -----

        }
    }
};

```

```

        return;
    }
    push(now, l, r);
    modify_set(l, m, ql, qr, now << 1, val);
    modify_set
        (m + 1, r, ql, qr, (now << 1) + 1, val);
    push(now << 1, l, m);
    push((now << 1) + 1, m + 1, r);
    pull(now);
}
void modify_set(int l, int
    r, int val) { modify_set(1, n, l, r, 1, val); }
void push(int now, int l, int r){
    apply(now, l, r);
}
// -----how to
// push down ?-----
if(l != r){
    if(lazy[now].set_val){
        lazy[now
            << 1].set_val = lazy[now].set_val;
        lazy[(now << 1)
            + 1].set_val = lazy[now].set_val;
        lazy[now << 1].add = lazy[now].add;
        lazy[(
            now << 1) + 1].add = lazy[now].add;
    }
    else {
        lazy[now << 1].add += lazy[now].add;
        lazy[(now
            << 1) + 1].add += lazy[now].add;
    }
}
//
// -----define
// structure and info plus-----
struct Node {
    int sum;
};
struct Lazy {
    int set_val; int add;
};
Node operator+(const Node &a, const Node &b) {
    return {{a.sum + b.sum}};
}
//
// -----
// polynomial queries
// 設置梯形的底跟加了幾次, apply_tag時底為l的合,
// d為加給次, 所以sum += (底*2 + 次*區間) * 區間 / 2;

```

7.5 莫隊

```

#include <bits/stdc++.h>
using namespace std;
struct query {
    int l, r, id;
} typedef query;
void MO(int n, vector<query> &queries){
    int block = sqrt(n);
    function <bool
        (query, query)> cmp = [&](query a, query b) {
        int block_a = a.l / block;
        int block_b = b.l / block;
        if(block_a
            != block_b) return block_a < block_b;
        return a.r < b.r;
    };
    sort(queries.begin(), queries.end(), cmp);
}

```

```

void compress(vector<int> &nums){
    vector<int> sorted = nums;
    sort(sorted.begin(), sorted.end());
    sorted.erase(unique
        (sorted.begin(), sorted.end()), sorted.end());
    for(int i = 0; i < nums.size(); i++){
        nums[i] = lower_bound(sorted.begin(), sorted
            .end(), nums[i]) - sorted.begin() + 1;
    }
}

```

7.6 Treap

```

#include <bits/stdc++.h>
using namespace std;
struct Treap {
    Treap *l, *r;
    int pri, subsize; char val; bool rev_valid;
    Treap(int val){
        this->val = val;
        pri = rand();
        l = r = nullptr;
        subsize = 1; rev_valid = 0;
    }
    void pull
        () { // update subsize or other information
        subsize = 1;
        for(auto i : {l, r}){
            if(i) subsize += i->subsize;
        }
    };
    int size(Treap *treap) {
        if (treap == NULL) return 0;
        return treap->subsize;
    }
    // lazy
    void push(Treap *t){
        if(!t) return;
        if(t->rev_valid){
            swap(t->l, t->r);
            if(t->l) t->l->rev_valid ^= 1;
            if(t->r) t->r->rev_valid ^= 1;
        }
        t->rev_valid = false;
    }
    Treap *merge(Treap *a, Treap *b){
        if(!a || !b) return a ? a : b;
        // push(a); push(b); // lazy
        if(a->pri > b->pri){
            a->r = merge(a->
                r, b); // a->r = new, inorder, make sense
            a->pull();
            return a;
        }
        else {
            b->l = merge(a,
                b->l); // new->l = a, inorder, make sense
            b->pull();
            return b;
        }
    }
}
pair<Treap*,
    Treap*> split(Treap *root, int k) { // find 1~k
    if (root == nullptr) return {nullptr, nullptr};
    // push(root); // lazy
    if (size(root->l) < k) {
        auto
            [a, b] = split(root->r, k - size(root->l) - 1);
        root->r = a;
        root->pull();
        return {root, b};
    }
    else {
        auto [a, b] = split(root->l, k);
        root->l = b;
        root->pull();
        return {a, root};
    }
}
void Print(Treap *t){
    if(t){
        // push(t); // lazy
        Print(t->l);
        cout << t->val;
    }
}

```

```

        Print(t->r);
    }
}
void substring_rev(){
    int n, m; cin >> n >> m;
    Treap *root = nullptr;
    string str; cin >> str;
    for(auto c : str){
        root = merge(root, new Treap(c));
    }
    for(int i = 1; i <= m; i++){
        int x, y; cin >> x >> y;
        auto [a,
              b] = split(root, x-1); // a: 1~x-1, b: x~n
        auto [
              c, d] = split(b, y-x+1); // Use b to split
        // c->rev_valid ^= true;
        // push(c);
        b = merge(a, d); // Notice the order
        root = merge(b, c);
    }
    Print(root);
}
}

```

8 搜尋與貪心

8.1 二分搜

```

int main(){
    int l = 1, r = 10;
    // 1 to tar, find tar
    while(l <= r){
        int m = (l + r) / 2;
        if(check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while(l <= r){
        int m = (l + r) / 2;
        if(check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}

```

8.2 Concert Ticket

```

// Better than Binary Search
int main(){
    int n, m; cin >> n >> m;
    multiset<int> tik;
    for(int i = 0; i < n; i++){
        int tmp; cin >> tmp;
        tik.insert(tmp);
    }
    while(m--){
        int x; cin >> x;
        auto it = tik.upper_bound(x);
        if(it == tik.begin()){
            cout << -1 << " ";
            continue;
        }
        it--;
        cout << *it << " ";
        tik.erase(it);
    }
}

```

8.3 Restaurant Customers

```

int main(){
    vector<pair<int, int>> times;
    int n; cin >> n;
    for(int i = 0; i < n; i++){
        int u, v; cin >> u >> v;
        times.push_back({u, 1});
        times.push_back({v, -1});
    }
    sort(times.begin(), times.end());
    int now_people = 0, ans = 0;
    for(auto [t, x] : times){
        ans = max(ans, (now_people += x));
    }
    cout << ans;
}

```

9 字串演算法

9.1 KMP

```

#include <bits/stdc++.h>
using namespace std;
struct KMP {
    string sub;
    vector<int> failure;
    KMP(string &sub) {
        this->sub = sub;
        failure.resize(sub.size(), -1);
        buildFailFunction();
    }
    void buildFailFunction() {
        for(int i = 1; i < sub.size(); i++) {
            int now = failure[i - 1];
            while(now != -1 && sub[
                now + 1] != sub[i]) now = failure[now];
            if (sub[now
                + 1] == sub[i]) failure[i] = now + 1;
        }
    }
    vector<int> KMPmatching(string &s) {
        vector<int> match;
        for(int i = 0, now = -1; i < s.size(); i++) {
            // now is the compare suceeded length -1
            while (s[i] != sub[now
                + 1] && now != -1) now = failure[now];
            // f stores
            if comparison fail, move to where
            if (s[i] == sub[now + 1]) now++;
            if (now + 1 == sub.size()) {
                match.push_back(i - now);
                now = failure[now];
            }
        }
        return match;
    }
};
int main(){
    string s = "xxtxtxtxtx";
    string sub = "tx";
    KMP kmp(sub);
    vector<int> ans = kmp.KMPmatching(s);
    for(auto &i : ans) cout << i << " ";
}

```

9.2 Trie

```

#include <bits/stdc++.h>
using namespace std;
#define all(x) (x).begin(), (x).end()
#define endl "\n"
#define int long long
typedef pair<int, int> pii;
const int llinf = 4e18;
const int inf = 2e9;
const int mod = 1e9 + 7;
const int maxn = 2e5 + 5;

struct Trie {
    struct trie_node {
        bool is_word;
        vector<trie_node*> children;
        trie_node() {
            is_word = false;
            children.resize(26, NULL);
        }
    };
    trie_node *root = new trie_node();
    void insert(string &s) {
        trie_node *cur = root;
        for (int i = 0; i < s.size(); i++) {
            int idx = s[i] - 'a';
            if (cur->children[idx] == NULL) {
                cur->children[idx] = new trie_node();
            }
            cur = cur->children[idx];
        }
        cur->is_word = true;
    }
    bool is_in_trie(string &s) {
        trie_node *cur = root;
        for(int i = 0; i < s.size(); i++) {
            if(cur->children
                [s[i] - 'a'] == nullptr) return false;
        }
    }
};

```

```

        cur = cur->children[s[i] - 'a'];
    }
    return true;
}
int search_i_start
(string &s, int i, vector<int> &dp) {
    trie_node *cur = root;
    int sz = s.size(), ans = 0;
    for(int j = i; j < sz; j++) {
        if(cur->children
            [s[j] - 'a'] == nullptr) return ans;
        cur = cur->children[s[j] - 'a'];
        if(cur->is_word)
            (ans += dp[j + 1]) %= mod;
    }
    return ans;
}
};
void solve(){
    // 找到 sub 集合裡，可以重複用，組成 s 的組數
    Trie trie;
    string s; cin >> s;
    int sz = s.size();
    // dp 代表 i 開頭到最後的配對總數
    // 找到有結尾為 stop 的 dp[i] += dp[j + 1]
    int n; cin >> n;
    vector<int> dp(sz + 1, 0);
    for(int i = 0; i < n; i++){
        string sub; cin >> sub;
        trie.insert(sub);
    }
    dp[sz] = 1;
    for(int i = sz - 1; i >= 0; i--){
        dp[i] = trie.search_i_start(s, i, dp);
    }
    cout << dp[0] << endl;
}
signed main(){
    ios_base::sync_with_stdio(0);
    cin.tie(nullptr);
    int t = 1;
    // cin >> t;
    while(t--){
        solve();
    }
}

```

10 樹論

10.1 LCA

```

#include <bits/stdc++.h> // LCA from 1
using namespace std;
const int maxn = 2e5+5;
int boss[maxn];
int height[maxn];
int arr[18][maxn];
vector<int> tree[maxn];
void Calculate_H(int now_node){
    for(auto nxt_node : tree[now_node]){
        height[nxt_node] = height[now_node] + 1;
        Calculate_H(nxt_node);
    }
}
int Find_Ancessor(int k, int h){
    for(int i = 0; i <= 17; i++){
        if(h & (1 << i)) k = arr[i][k];
    }
    return k;
}
int main(){
    memset(arr, 0, sizeof(arr));
    int n, q; cin >> n >> q;
    boss[1] = 1;
    for(int i = 2; i <= n; i++){
        int tmp; cin >> tmp; // tmp to i
        boss[i] = tmp;
        tree[tmp].push_back(i);
    }
    Calculate_H(1);
    for(int i = 2; i <= n; i++){
        arr[0][i] = boss[i];
    }
    for(int i = 1; i <= 17; i++){ // make chart
        for(int j = 1; j <= n; j++){
            arr[i][j] = arr[i - 1][arr[i - 1][j]];
        }
    }
}

```

```

    }
}
while(q--){
    int a, b; cin >> a >> b;
    if(height[a] < height[b]) swap(a, b);
    a = Find_Ancessor(a, height
        [a] - height[b]); // same depth from 1
    if(a == b) { // same point
        cout << a << "\n";
        continue;
    }
    for(int i = 17; i >= 0; i--){
        if(arr[i][a] != arr[i][b]){
            // if a, b up 2 ^ i not the same point
            a = arr[i][a];
            b = arr[i][b];
        }
    }
    cout << arr[0][a] << "\n"; // more one
}
}
}

```

10.2 子樹 DP

```

#include <bits/stdc++.h>
using namespace std;
const int maxn = 2e5+5;
vector<int> tree[maxn];
int sub[maxn];
void dfs(int now){
    for(auto nxt : tree[now]){
        dfs(nxt);
        sub[now] += sub[nxt] + 1;
    }
}
int main(){
    memset(sub, 0, sizeof(sub));
    int n; cin >> n;
    for(int i = 2; i <= n; i++){
        int b; cin >> b;
        tree[b].push_back(i);
    }
    dfs(1);
    for(int i = 1; i <= n; i++){
        cout << sub[i] << " ";
    }
}

```

10.3 樹重心

```

#include <bits/stdc++.h>
using namespace std;
const int maxn = 2e5+5;
vector<int> tree[maxn];
int cen = 0, n;
int dfs(int par, int now){
    bool flag = 1;
    int size = 0;
    for(auto nxt : tree[now]){
        if(par != nxt){
            int subsize = dfs(now, nxt);
            if(subsize > n / 2) flag = false;
            size += subsize;
        }
    }
    if(n - 1 - size > n / 2) flag = false;
    if(flag) cen = now;
    return size + 1;
}
int main(){
    cin >> n;
    for(int i = 1; i < n; i++){
        int u, v; cin >> u >> v;
        tree[u].push_back(v);
        tree[v].push_back(u);
    }
    for(int i = 1; i <= n; i++){
        for(auto nxt : tree[i])
            dfs(i, nxt);
        if(cen) break;
    }
}

```

10.4 節點距離總和


```

#include <bits/stdc++.h>
using namespace std;
const int maxn = 2e5+5;
vector<int> tree[maxn];
vector<int> subtree(maxn, 1);
long long ans[maxn];
int n;
void dfs(int par, int now, int depth){
    ans[1] += depth;
    for(auto nxt : tree[now]){
        if(par != nxt){
            dfs(now, nxt, depth + 1);
            subtree[now] += subtree[nxt];
        }
    }
}
void find_ans(int par, int now){
    // each sub's dis make - 1, non subnode + 1
    for(auto nxt : tree[now]){
        if(par != nxt){
            ans[nxt] = ans[now]
                + (n - subtree[nxt]) - subtree[nxt];
            find_ans(now, nxt);
        }
    }
}
int main(){
    cin >> n;
    for(int i = 1; i < n; i++){
        int u, v; cin >> u >> v;
        tree[u].push_back(v);
        tree[v].push_back(u);
    }
    dfs(0, 1, 0);
    find_ans(0, 1);
    for(int i = 1; i <= n; i++){
        cout << ans[i] << " ";
    }
}

```

10.5 無權樹直徑

```

#include <bits/stdc++.h>
using namespace std;
const int maxn = 2e5+5;
int dep1[maxn], dep2[maxn];
vector<int> tree[maxn];
int start, maxdep = 1, End;
void dfs1(int par, int now){
    for(auto nxt : tree[now]){
        if(par != nxt){
            dep1[nxt] = dep1[now] + 1;
            if(dep1[nxt] > maxdep){
                maxdep = dep1[nxt];
                start = nxt;
            }
            dfs1(now, nxt);
        }
    }
}
void find_depth1(int par, int now){
    for(auto nxt : tree[now]){
        if(par != nxt){
            dep1[nxt] = dep1[now] + 1;
            if(dep1[nxt] > maxdep){
                maxdep = dep1[nxt];
                End = nxt;
            }
            find_depth1(now, nxt);
        }
    }
}
void find_depth2(int par, int now){
    for(auto nxt : tree[now]){
        if(par != nxt){
            dep2[nxt] = dep2[now] + 1;
            find_depth2(now, nxt);
        }
    }
}
int main(){
    int n; cin >> n;
    for(int i = 1; i < n; i++){
        int u, v; cin >> u >> v;
        tree[u].push_back(v);
        tree[v].push_back(u);
    }
}

```

```

    }
    dep1[1] = 1;
    dfs1(0, 1);
    dep1[start] = 1;
    maxdep = 1;
    find_depth1(start, start);
    dep2[End] = 1;
    find_depth2(End, End);
    for(int i = 1; i <= n; i++){
        cout << max(dep1[i], dep2[i]) - 1 << " ";
    }
}

```

10.6 有權樹直徑

```

#include <bits/stdc++.h> // weighted tree centroid
using namespace std;
const int maxn = 1e5+5;
using ll = long long;
vector<pair<int, int>> tree[maxn];
ll dp[maxn];
ll ans = 0;
void DP(int now, int par){
    ll mx1 = 0; ll mx2 = 0;
    for(auto [nxt, w] : tree[now]){
        if(nxt == par) continue;
        DP(nxt, now);
        if(mx1 < w + dp[nxt]){ // mx2 = mx1, mx1 = new mx
            mx2 = mx1; mx1 = w + dp[nxt];
        }
        else if(mx2 < w + dp[nxt]){ // mx2 = new
            mx2 = w + dp[nxt];
        }
    }
    dp[now] = mx1;
    ans = max(ans, mx1 + mx2);
}
int main(){
    int n; cin >> n;
    memset(dp, 0, sizeof(dp));
    for(int i = 1; i < n; i++){
        int u, v, w; cin >> u >> v >> w;
        tree[u].push_back({v, w});
        tree[v].push_back({u, w});
    }
    DP(1, 0);
    cout << (ans < 0 ? 0 : ans);
}

```