Contents 5 String 5.1 KMP 9 5.2 Z函數 9 5.3 Duval Algorithm 10 1 Basic **5.4 Manacher** 10 **5.5 Trie** 10 1.1 install vscode 1.2 default code 1.3 compare fuction 6 Math 1.4 pbds 2 Graph 2.1 DFS跟BFS 2.2 Dijkstra 6.6 Mobius Theorem 2.3 Prim **6.7 莫比烏斯反演** 12 2.4 正權找環 Catalan Theorem 6.8 2.5 BellmanFord Burnside's Lemma 13 2.6 正權最大距離 2.7 負權最大距離 Search and Gready 2.8 FloydWarshall 2.9 歐拉環與歐拉路..... 2.10 SCC 8 Tree 2.11 VBCC 2.12 EBCC 2.13 2-SAT 8.3 樹壓平 2.14 Planets Cycles 8.5 2.15 Planet Queries II 4 9 DP 3 Data Structure 5 **9.1 背包問題** 15 9.2 Bitmask 3.1 BIT 3.2 DSU 3.3 Increasing Array Queries . 6 9.5 **LCS** 15 3.4 線段樹 6 **9.6** LIS 16 3.5 懶標線段樹 **9.7 Projects** 16 **9.8 Removal Game** 16 3.6 莫隊...... **9.9 CF Example** 16 **9.10 Slope Trick** 17 3.7 Treap 4 Flow 10 Geometry 10.1 Basic . . . 4.1 Dinic 4.2 Min Cut 4.3 Bipartite Matching 8 **10.3 MinEuclideanDistance** . . 19 **10.4 LatticePoints** 19

1 Basic

1.1 install vscode [d41d8c]

```
|// 如何安裝 vscode
|// 1. 下載 vscode & msys2
|// 2. 在跳出的 terminal 中 / 或打開 ucrt64 , 打上
    "pacman -S --needed base-devel mingw-w64-x86_64-toolchain"
|// 3. 環境變數加上 C:\\msys64\\ucrt64\\bin
|// 4. 重開 vscode, 載 C/C++, 運行, 編譯器選擇 g++
|// 5. 打開 settings -> compiler -> add compilerPath
    -> 在 "" 裡打上 C:\\msys64\\ucrt64\\bin\\g|++.exe
```

1.2 default code [3cd57c]

```
#include <bits/stdc++.h>
#define all(x) (x).begin(), (x).end()
#define pii pair<int, int>
using namespace std;
using ll = long long;
const int mod = 1e9 + 7;

void solve() {
}
int main() {
   ios_base::sync_with_stdio(0);
   cin.tie(nullptr);
   int t = 1;
   cin >> t;
   while (t--) {
      solve();
   }
}
```

1.3 compare fuction [4bc3e0]

```
// 如果有自定義比較結構就比照以上
};
struct cmp { // 要在 template 的資
  vector <int> &v;
  cmp(vector <int>& vec) : v(vec) {}
                     // 要在 template 的資結用外部變數
     bool operator() (int a, int b) const {
   return v[a] > v[b];
// s
// main: cmp cmp1(vector);
// priority_queue<int, vector<int>, cmp> pq(cmp1);
};
1.4 pbds [e28ae8]
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < typename T >
using pbds_set = tree<T, null_type,
    less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template<typename T>
2
       Graph
2.1 DFS 跟 BFS [cdd1d5]
int main() {
     int n:
      vector<vector<int>> adj(n + 1, vector<int>());
     // dfs_graph
vector<bool> vis(n + 1, 0);
auto dfs = [\&](auto self, int u) -> void {
          if (vis[u]) return;
          vis[u] = true;
for (auto v: adj[u]) {
               self(self, v);
          }
     dfs(dfs, 1);
     // bfs
vector < int > depth(n + 1, 1e9);
     queue<int> q;
auto bfs = [%](auto self, int u) -> void {
          vis[u] = true;
depth[u] = 0;
          q.push(u);
           while (!q.empty()) {
  int u = q.front(); q.pop();
  for (auto v : adj[u]) {
                     if (vis[v]) continue;
                     vis[v] = true;
depth[v] = depth[u] + 1;
                     q.push(v);
               }
          }
     bfs(bfs, 1);
```

2.2 Dijkstra [4e0023]

}

```
Flight Discount
int main() {
     int n, m; cin >> n >> m;
    vector<vector<pair<
          int, int>>> adj(n + 1, vector<pair<int, int>>(n + 1));
    vector < vector < int >>
    dis(n + 1, vector<int>(2, 2e9)); // 0 for not used
for (int i = 1; i <= m; i++) {
          int u, v, w;
          cin >> u >> v >> w
          adj[u].push_back(\{v, w\});
    distrif[0] = distrif[1] = 0,
pq.push({0, 1, 0});
while (!pq.empty()) {
    auto [dist, u, us] = pq.top(); pq.pop();
    if (dis[u][us] < dist) continue;</pre>
         }
               for (auto [v, w] : adj[u]) {
    if (dis[u][0] + w < dis[v][0]) {
        dis[v][0] = dis[u][0] + w;
}</pre>
                         pq.push({dis[v][0], v, 0});
                    if (dis[u][0] + w / 2 < dis[v][1])
    dis[v][1] = dis[u][0] + w / 2;</pre>
                                                 < dis[v][1]) {
                         pq.push({dis[v][1], v, 1});
```

```
National Chung Cheng University Salmon
         }
     cout << min(dis[n][0], dis[n][1]);
2.3 Prim [f00ec0]
auto prim =
       [&](int n, vector<vector<pair<int, int>>> &adj) -> bool {
     int node_sz = 0;
    while (!pq.empty()) {
   auto [u, w] = pq.top(); pq.pop();
   if (vis[u]) continue;
          vis[u] = true;
          node_sz++;
for (auto v : adj[u]) {
    if (!vis[v.first]) {
                                                                                 }
                  pq.push({v.second, v.first});
          }
     }
if (node_sz == n) return true;
};
2.4 正權找環 [0e0fdf]
const int maxn = 1e5+5;
vector < int > graph[maxn];
int color[maxn], parent[maxn];
bool vis[maxn];
int n, m;
void print_ans(int ori) {
    int now = parent[ori];
deque < int > ans;
ans.push_front(ori);
    while (now != ori) {
    ans.push_front(now);
         now = parent[now];
     ans.push_front(ori);
    cout << ans.size() << endl;
for (auto i : ans) {
    cout << i << " ";</pre>
    exit(0):
void dfs(int now) {
    color[now] = 1;
vis[now] = 1;
     for (auto nxt : graph[now]) {
   parent[nxt] = now;
   if (color[nxt] == 1) {
              print_ans(nxt);
          else if (color[nxt] == 0) {
              dfs(nxt);
    color[now] = 2;
void solve() {
    graph[u].push_back(v);
     for (int i = 1; i <= n; i++) {
    if (!vis[i])</pre>
              dfs(i);
    cout << "IMPOSSIBLE";</pre>
2.5 BellmanFord [02f480]
// 用 Bellman Ford 找負環
```

```
|// CSES Longest Flight Route
 // 只能用在 DAG, 用拓樸按順序鬆弛
  void print_ans(int n, vector<int> &par) {
        deque<int> ans;
        int now = n;
while(now != 1) {
              ans.push_front(now);
              now = par[now];
        fans.push_front(1);
cout << ans.size() << "|n";
for(auto i : ans) {
    cout << i << " ";
}</pre>
  int main() {
        int n, m; cin >> n >> m;
vector<vector<int>> graph(n + 1);
vector<int> dis(n + 1, -1e9); dis[1] = 0;
vector<int> par(n + 1), in(n + 1);
        queue < int > q;
for (int i = 1; i <= m; i++) {</pre>
              int u, v; cin >> u >> v;
graph[u].push_back(v);
              in[v]++;
        for (int i = 1; i <= n; i++) {
    if (in[i] == 0) q.push(i);</pre>
        while (!q.empty()) {
   int u = q.front(); q.pop();
   for (auto v : graph[u]) {
                     if (dis[v] < dis[u] + 1) { // 鬆弛 dis[v] = dis[u] + 1; par[v] = u;
                     in[v]--;
                     if (in[v] == 0) q.push(v);
              }
        if (dis[n] == -1e9) {
              // 如果 1 不能到達 n,n 也有可能被鬆弛
              // 所以要看的是 dis[n] < 0 cout << "IMPOSSIBLE";
        else print_ans(n, par);
```

2.7 負權最大距離 [2148ca]

```
// CSES High Score
void dfs(int u, vector<int> &vis, vector<vector<int>> &adj) {
    if (vis[u]) return;
    vis[u] = 1;
    for (int v : adj[u]) {
        dfs(v, vis, adj);
    }
}
signed main() {
    int n, m; cin >> n >> m;
    vector<array<int, 3>> edges;
    vector<vector<int>> adj(n + 1);
    vector<int>> dis(n + 1), vis(n + 1);
    while (m--) {
        int u, v, w;
        cin >> u >> v >> w;
        edges.push_back({u, v, w});
        adj[u].push_back(v);
    }
fill(dis.begin(), dis.end(), -1e18);
    dis[1] = 0;
    for (int i = 1; i <= n; i++) {
        for (auto [u, v, w] : edges) {
            if (dis[u] != -1e18 && dis[v] < dis[u] + w) {
                dis[v] = dis[u] + w;
            if (i == n) {</pre>
```

2.9 <u>歐拉環與歐拉路</u> [0911ed]

```
// 無向圖、尤拉環: 檢查每個點的出度為偶數
// 有向圖、
     尤拉路:可以看成 1 走到 n,所以檢查所有點的出度等於入度
int n, m;
const int maxn = 1e5 + 5;
vector<set<int>> adj;
vector<int> in;
void dfs(int now, vector<int> &road) {
    while (!adj[now].empty()) {
   int nxt = *adj[now].begin();
   adj[now].erase(nxt);
          dfs(nxt, road);
     road.push_back(now);
void solve() {
    cin >> n >> m;
in.assign(n + 1, 0);
adj.assign(n + 1, set<int>());
for (int i = 1; i <= m; i++) {
   int u, v; cin >> u >> v;
   adj[u].insert(v);
   int u = n; interpretation
          in[v]++;
     in[1]++;
    return;
         }
     vector<int> road;
    dfs(1, road);
if (road.size() != m + 1) {
         cout << "IMPOSSIBLE";
     for(auto i : road) cout << i <<</pre>
```

2.10 SCC [b0411e]

```
struct SCC {
   int n, cur, cnt;
   vector < vector < int >> adj;
   vector < int >> stk, dfn, low, bel;
   SCC(int n) {
      init(n);
   }
   void init(int n) {
      this -> n = n;
      adj.assign(n, {});
      dfn.assign(n, -1);
}
```

```
low.resize(n):
           bel.assign(n, -1);
           stk.clear();
           cur = cnt = 0:
      void addEdge(int u, int v) {
   adj[u].push_back(v);
      void dfs(int x) {
    dfn[x] = low[x] = cur++;
    stk.push_back(x);
    for (auto y : adj[x]) {
        if (dfn[x]) == -1) {
                      dfs(y);
low[x] = min(low[x], low[y]);
                 } else if (bel[y] == -1) {
    low[x] = min(low[x], dfn[y]);
                }
           if (dfn[x] == low[x]) {
                 int y;
do {
                      y = stk.back();
                      bel[y] = cnt;
                      stk.pop_back();
                 } while (y != x);
                 cnt++;
          }
      return bel:
      struct Graph {
           int n;
vector<pair<int, int>> edges;
           vector<int> siz;
           vector<int> cnte;
      Graph compress() {
           Graph g;
g.n = cnt;
           g.siz.resize(cnt);
           g.cnte.resize(cnt);
           for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;</pre>
                 for (auto j : adj[i]) {
    if (bel[i] != bel[j]) {
                           g.edges.emplace_back(bel[i], bel[j]);
                      } else {
                           g.cnte[bel[i]]++;
                }
           return g;
     }
};
```

2.11 VBCC [3f9190]

```
struct VBCC {
     int n, cur;
     vector<vector<int>> adj;
     vector <int> dfn, low, parent;
vector <bool> is_cut;
     VBCC(int n) {
          init(n);
     void init(int n) {
          this->n = n;
adj.assign(n, {});
          dfn.assign(n,
          low.resize(n);
          parent.assign(n, -1);
is_cut.assign(n, false);
     void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
     void dfs(int x) {
          int children
          dfn[x] = low[x] = cur++;
          for (int v : adj[x]) {
               if (dfn[v] == -1) {
    children++;
    parent[v] = x;
                     dfs(v);
                     low[x] = min(low[x], low[v]);
                    if (parent[x] != -1 \&\& low[v] >= dfn[x]) {
                          is_cut[x] = true;
               } else if (v != parent[x]) {
                    low[x] = min(low[x], dfn[v]);
          if (parent[x] == -1 && children > 1) {
```

```
is_cut[x] = true;
           }
     void work() {
    for (int i = 0; i < n; i++) {</pre>
                if (dfn[i] == -1) {
    dfs(i);
           }
    }
};
2.12 EBCC [08723d]
struct EBCC { // CF/contest/1986/pF
   int n, cur, cnt;
   vector<vector<int>> adj;
      vector<int> stk, dfn, low, bel;
      EBCC(int n) {
           init(n);
     void init(int n) {
```

```
vector<pair<int, int>> bridges; // 關鍵邊
      adj.assign(n, {});
      dfn.assign(n, -1);
      low.resize(n);
      bel.assign(n, -1);
      stk.clear():
      bridges.clear();
      cur = cnt = 0;
void addEdge(int u, int v) {
    adj[u].push_back(v);
      adj[v].push_back(u);
void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
    stk.push_back(x);
     stk.push_back(x);
for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
        dfs(y, x);
        low[x] = min(low[x], low[y]);
        if (low[y] > dfn[x]) {
            bridges.emplace_back(x, y);
        }
}
           } else if (bel[y] == -1) {
    low[x] = min(low[x], dfn[y]);
      if (dfn[x] == low[x]) {
            int y;
                 y = stk.back();
                 bel[y] = cnt;
           stk.pop_back();
} while (y != x);
           cnt++:
     }
vector<int> work() {
      dfs(0, -1);
return bel;
struct Graph {
      int n:
      vector<pair<int, int>> edges;
      vector<int> siz; // BCC 內節點數
      vector<int> cnte; // BCC 內邊數
};
Graph compress() {
     Graph g;
g.n = cnt;
      g.siz.resize(cnt);
      g.cnte.resize(cnt);
      g.edges.emplace_back(bel[i], bel[j]);
} else if (i < j) {</pre>
                      g.cnte[bel[i]]++;
                 }
           }
      return g;
```

2.13 2-SAT [eeddc1]

}

```
// CSES Giant Pizza
struct TwoSat {
       int n;
        vector < int >> e;
       vector <book ans;
TwoSat(int n) : n(n), e(2 * n), ans(n) {}
void addClause(int u, bool f, int v, bool g) {
    e[2 * u + !f].push_back(2 * v + g);</pre>
```

```
e[2 * v + !g].push_back(2 * u + f);
      bool satisfiable() {
           vector<int> stk;
           int now = 0, cnt = 0;
function < void(int) > tarjan = [&](int u) {
                 stk.push_back(u);
                 dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
                      tariy -- -1) {
    tariy -- -1) {
      tariyan(v);
      low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in stk
      low[u] = min(low[u], dfn[v]);
                 if (dfn[u] == low[u]) {
                       int v;
                      stk.pop_back();
id[v] = cnt;
                      } while (v != u);
                       ++cnt;
                }
           for (int i
           vector < bool > answer() { return ans; }
int main() {
      int m, n; cin >> m >> n;
TwoSat ts(n);
for (int i = 0; i < m; ++i) {</pre>
           int u, v; char x, y;
cin >> x >> u >> y >> v;
ts.addClause(u - 1, x == '+', v - 1, y == '+');
     if (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";
}</pre>
      else cout << "IMPOSSIBLE\n";</pre>
}
```

2.14 Planets Cycles [71ac0e]

```
vector<int> dis, v;
vector<bool> vis;
int step;
queue<int> path:
void dfs(int x) {
     path.push(x);
     if (vis[x]) {
    step += dis[x];
     vis[x] = true;
     step++;
     dfs(v[x]);
// count path_dis to rep
int main() {
    int n; cin >> n;
     tht n; cin >> n;
v.assign(n + 1, 0);
dis.assign(n + 1, 0);
vis.assign(n + 1, false);
for (int i = 1; i <= n; i++) {
    cin >> v[i];
     for (int i = 1; i <= n; i++) {
           step = 0;
           int is_outof_cycle = 1;
          dis[path.front()] = step;
                step -= is_outof_cycle;
path.pop();
     for (int i = 1; i <= n; i++) {
    cout << dis[i] << ' ';</pre>
     cout << '\n';
```

2.15 Planet Queries II [872f72]

```
| // 在有向圖中,從 A 到 B 的最短距離
// 保證出度是 1 所以對 1 個點來說,從他出發只可能遇到一個環
```

```
int n. a:
int dp[200005][30]; // 倍增表
vector<vector<int>>> cycles;
vector<int
> no, cycle_idx, vis; // Order & Can be in cycle, or out
void set_out_of_cycle_no(int now, unordered_set<int> &done) {
    // 把不在環內的也編號, v 是 u 的編號 -1
    if (done.find(now) != done.end()) return;
     set_out_of_cycle_no(dp[now][0], done);
done.insert(now); // post order
no[now] = no[dp[now][0]] - 1;
int wiint_go_to(int u, int k) { // 回傳當 u 走 k 步時會到的地方 for (int i = 0; i <= 18; i++) { if (k & (1 << i)) { u = dp[u][i];
           }
      return u:
void find_cycle(int now) {
     unordered_set < int > appear;
vector < int > v;
     bool flag = true; // 代表有環while (appear.find(now) == appear.end()) {
           appear.insert(now);
           v.push_back(now);
           if (vis[now]) {
    flag = false;
                 break;
           now = dp[now][0];
     for (auto i : v) vis[i] = true;
if (!flag) return;
      cycles.push_back(cycle);
}
int main() {
     cin >> n >> q;
no.assign(n + 1,
      no.assign(n + 1, -1);
cycle_idx.assign(n + 1, -1);
     vis.assign(n + 1, 0);
for (int u = 1; u <= n; u++) cin >> dp[u][0];
     int idx = 0;
      unordered_set<int> done;
      for (auto &i : cycles) {
            int c = 0;
           for (auto &j : i) {
    no[j] = c++;
    cycle_idx[j] = idx;
                 done.insert(j);
           idx++;
     for (int i = 1; i <= n; i++) set_out_of_cycle_no(i, done);
for (int i = 1; i <= q; i++) {
   int u, v; cin >> u >> v;
           // 在同個環內
           if (cycle_idx[u] == cycle_idx
    [v] && cycle_idx[u] != -1 && cycle_idx[v] != -1) {
                 int cyc_size = cycles[cycle_idx[u]].size();
cout <<</pre>
                       (no[v] - no[u] + cyc_size) % cyc_size << "\n";</pre>
           // 都不再環內
           else if (cycle_idx[u] == -1 &&

cycle_idx[v] == -1) { // Both are not in a Cycle
                 if (no[u] > no[v]) {
    cout << -1 << "\n";
                       continue:
                 if (wiint_go_to(u, no[v] - no[u]) == v) {
    cout << no[v] - no[u] << "\n";</pre>
                 else cout << -1 << "\n":
           else if (cycle_idx[u]
                 == -1 && cycle_idx[v] != -1) { // v 在環內, 二分搜 int l = -1, r = n; while (l <= r) { int m = (l + r) / 2; if (cycle idy[wiit = 2 to
                      if (l <= n) {
                 }
```

```
else cout << -1 << "\n";
}
else { // u 在環內 b 不在,直接不可能
cout << -1 << "\n";
}
```

3 Data Structure

3.1 BIT [d41d8c]

```
template <typename T>
struct Fenwick { // 全部以 0 based 使用
      int n:
      vector<T> a;
      Fenwick(int n_ = 0) {
            init(n_);
      void init(int n_) {
            a.assign(n, T{});
      void add(int x, const T &v) {
   for (int i = x + 1; i <= n; i += i & -i) {
      a[i - 1] = a[i - 1] + v;
}</pre>
      T sum(int x) { // 左閉右開查詢
            T ans{};
for (int i = x; i > 0; i -= i & -i) {
                 ans = ans + a[i - 1];
            return ans:
      TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
      int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
            int x = 0;
            T cur{};
            for (int i = 1 << __lg(n); i; i /= 2) {
   if (x + i <= n && cur + a[x + i - 1] <= k) {
      x += i;</pre>
                        cur = cur + a[x - 1];
                  }
            return x;
     }
template <class T>
struct TwoDFenwick { // 全部以 0 based 使用int nx, ny; // row, col 個數 vector <vector <T>> a;
TwoDFenwick(int nx_ = 0, int ny_ = 0) {
            init(nx_, ny_);
      void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
      void add(int x, int y, const T &v) {
            for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        a[i - 1][j - 1] = a[i - 1][j - 1] + v;
           }
      }
      T sum(int x, int y) { // 左閉右開查詢 T ans{};
            for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans + a[i - 1][j - 1];
    }
}
            return ans;
             (int lx, int ly, int rx, int ry) { // 左閉右開查詢
            return sum(
                   (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
     }
```

3.2 DSU [d41d8c]

```
struct DSU {
  vector <int> boss, siz;
  DSU(int n) {  // 0 based
    boss.resize(n);
    iota(boss.begin(), boss.end(), 0);
    siz.assign(n, 1);
}
  int find_boss(int x) {
    if (boss[x] == x) return x;
    return boss[x] = find_boss(boss[x]);
}
  bool same(int x, int y) {
    return find_boss(x) == find_boss(y);
}
```

```
bool merge(int x, int y) {
    x = find_boss(x);
    y = find_boss(y);
               if (x == y) {
    return false;
               if(siz[x] < siz[y]) swap(x, y);
siz[x] += siz[y];
boss[y] = x;</pre>
                return true;
       int size(int x) {
    return siz[find_boss(x)];
};
```

3.3 Increasing Array Queries [d41d8c]

```
const int maxn = 2e5+5;
int n, q;
int nums
[maxn], prefix[maxn], ans[maxn], BIT[maxn], contrib[maxn];
vector<pair<int, int>> queries[maxn];
void update(int pos, int val) {
   for (; pos <= n; pos += pos & -pos) BIT[pos] += val;</pre>
int query(int a, int b) {
   int ans = 0;
   for (; b; b -= b&-b) ans += BIT[b];
     for (a--; a; a -= a&-a) ans -= BIT[a];
     return ans:
void solve() {
     cin >> n >> q;
for (int i = 1; i <= n; i++) {</pre>
          cin >> nums[i];
          prefix[i] = prefix[i-1] + nums[i];
     nums[n + 1] = 1e9;
     prefix[n + 1] = 2e18;
for (int i = 1; i <= q; i++) {
   int a, b; cin >> a >> b;
          queries[a].push_back({b, i});
     deque < int > mono; mono.push_front(n+1);
     contrib[i] = (mono.front() - 1 - i) *
    nums[i] - (prefix[mono.front() - 1] - prefix[i]);
update(i, contrib[i]);
          mono.push_front(i);
          for (auto j : queries
   [i]) { // pos is the index in mono <= end's
   int pos = upper_bound(mono.begin</pre>
               - mono[pos]) * nums[mono[pos]]
- (prefix
                                        [j.first] - prefix[mono[pos]]);
     for (int i = 1; i <= q; i++) {
    cout << ans[i] << endl;</pre>
}
```

3.4 線段樹 [d41d8c]

```
template <class Info>
struct Seg { // 左閉右開寫法
   int n;
    vector < Info > info:
    Seg() : n(0) {}
   Seg(int n_{,} Info v_{,} = Info()) {
       init(n_, v_);
    template <class T>
   Seg(vector<T> init_) {
   init(init_);
    void init(int n_, Info v_ = Info()) {
       init(vector(n_, v_));
   template <class T>
void init(vector<T> init_) {
       n = init_.size();
       info.assign(4 << __lg(n), Info());</pre>
       info[p] = init_[l];
               return:
           int m = (l + r) / 2;
```

```
build(p * 2, l, m);
build(p * 2 + 1, m, r);
               pull(p);
          build(1, 0, n);
     void pull
     return:
          int m = (l + r) / 2;
if (x < m) {
               modify(2 * p, l, m, x, v);
          } else {
               modify(2 * p + 1, m, r, x, v);
          pull(p);
     void modify(int p, const Info &i) {
          modify(1, 0, n, p, i);
     Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    return query(p *</pre>
                2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
           (int ql, int qr) { return query(1, 0, n, ql, qr); }
     template < class F> // 尋找區間內,第一個符合條件的
     int findFirst
          (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
    return -1;</pre>
          if (l >= x && r <= y && !pred(info[p])) {</pre>
               return -1;
          if (r - l == 1) {
               return l;
          int m = (l + r) / 2;
int res = findFirst(2 * p, l, m, x, y, pred);
          if (res == -1) {
    res = findFirst(2 * p + 1, m, r, x, y, pred);
          return res;
     template < class F> // 若要找 last,先右子樹遞廻即可
int findFirst(int l, int r, F & & pred) {
return findFirst(1, 0, n, l, r, pred);
};
// ---define structure and info plus---
struct Info {
     int sum:
Info operator + (const Info &a, const Info &b) {
     return { a.sum + b.sum };
3.5 懶標線段樹 [d41d8c]
```

```
template <class Info, class Tag>
struct LazySeg { // 左閉右開寫法
     int n:
     vector < Info > info;
     vector<Tag> tag;
LazySeg() : n(0) {}
LazySeg(int n_, Info v_ = Info()) {
          init(n_, v_);
     template <class T>
LazySeg(vector<T> init_) {
          init(init_);
     void init(int n_, Info v_ = Info()) {
  init(vector(n_, v_));
     template <class T>
     void init (vector<T> init_) {
    n = init_.size();
          info.assign(4 << __lg(n), Info());
tag.assign(4 << __lg(n), Tag());
          return:
               int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
               pull(p);
          build(1, 0, n);
```

```
void pull
                                                                                                     sum += (r - l) * v.add:
           (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
     void apply(int p, int l, int r, const Tag &v) {
  info[p].apply(l, r, v);
  tag[p].apply(v);
                                                                                          Info operator + (const Info &a, const Info &b) {
                                                                                                return { a.sum + b.sum };
                                                                                          }
     void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
                                                                                          3.6 莫隊 [d41d8c]
                                                                                         struct query {
   int l, r, id;
} typedef query;
void MO(int n, vector<query> &queries) {
           tag[p] = Tag();
                                                                                                int block = sqrt(n);
     void modify(int p, int l, int r, int x, const Info &v) {
                                                                                                function <bool(query, query)> cmp = [&](query a, query b) {
   int block_a = a.l / block;
   int block_b = b.l / block;
          if (r - l == 1) {
    info[p] = v;
                                                                                                     if (block_a != block_b) return block_a < block_b;
return a.r < b.r;</pre>
               return:
          int m = (l + r) / 2;
push(p, l, r);
if (x < m) {</pre>
                                                                                                sort(queries.begin(), queries.end(), cmp);
                modify(2 * p, l, m, x, v);
                                                                                          void compress(vector<int> &nums) {
                                                                                                vector<int> sorted = nums;
                modify(2 * p + 1, m, r, x, v);
                                                                                                sort(sorted.begin(), sorted.end());
                                                                                                sorted.erase
          pull(p);
                                                                                                      (unique(sorted.begin(), sorted.end());
                                                                                                for (int i = 0; i < nums.size(); i++) {
   nums[i] = lower_bound(sorted.begin
          (), sorted.end(), nums[i]) - sorted.begin() + 1;</pre>
     void modify(int p, const Info &i) {
          modify(1, 0, n, p, i);
     Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;</pre>
                                                                                          3.7 Treap [d41d8c]
                                                                                          struct Treap {
   Treap *l, *r;
   int pri, subsize; char val; bool rev_valid;
   Treat(int val) {
           push(p, l, r);
           return query(p *
2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
     Info query
                                                                                                     this->val = val:
           (int ql, int qr) { return query(1, 0, n, ql, qr); }
                                                                                                     pri = rand();
     l = r = nullptr;
                                                                                                     subsize = 1; rev_valid = 0;
                                                                                                void pull() { // update subsize or other information
    subsize = 1;
    for(auto i : {l, r}) {
                apply(p, l, r, v);
                return:
                                                                                                           if (i) subsize += i->subsize;
          int m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
                                                                                               }
                                                                                          int size(Treap *treap) {
   if (treap == NULL) return 0;
           pull(p);
                                                                                                return treap->subsize;
     void range_apply(int l, int r, const Tag &v) {
          range_apply(1, 0, n, l, r, v);
                                                                                          // lazy
                                                                                          void push(Treap *t) {
    if (!t) return;
    if (t->rev_valid) {
     }
     template < class F> // 尋找區間內,第一個符合條件的
     int findFirst
          (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
   return -1;</pre>
                                                                                                     swap(t->l, t->r);
if (t->l) t->l->rev_valid ^= 1;
if (t->r) t->r->rev_valid ^= 1;
           if (l >= x && r <= y && !pred(info[p])) {</pre>
                                                                                                t->rev_valid = false;
                return -1;
                                                                                          Treap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
    // push(a); push(b); // lazy
    if (a->pri > b->pri) {
           if (r - l == 1) {
                return l;
           int m = (l + r) / 2;
                                                                                                     a->r = merge
           push(p);
                                                                                                            (a->r, b); // a->r = new, inorder, make sense
           int res = findFirst(2 * p, l, m, x, y, pred);
                                                                                                     a->pull();
          if (res ==
                                                                                                     return a:
                res = findFirst(2 * p + 1, m, r, x, y, pred);
                                                                                                     b->l = merge
           return res;
                                                                                                     (a, b->l); // new->l = a, inorder, make sense
b->pull();
     template < class F> // 若要找 last <sup>*</sup> 先右子樹遞廻即可
int findFirst(int l, int r, F & pred) {
return findFirst(1, 0, n, l, r, pred);
                                                                                                     return b;
                                                                                               }
                                                                                          // ---define structure and info plus---
struct Tag {
                                                                                                // push(root); // lazy
if (size(root->l) < k) {
     int set_val; int add;
                                                                                                     auto [a, b] = split(root->r, k - size(root->l) - 1);
root->r = a;
     void apply(const Tag& v) {
          if (v.set_val) {
    set_val = v.set_val;
                                                                                                     root->pull();
                add = v.add;
                                                                                                     return {root, b};
           else {
                add += v.add;
                                                                                                else {
                                                                                                     auto [a, b] = split(root->l, k);
root->l = b;
          }
    }
                                                                                                     root->pull();
};
struct Info {
                                                                                                     return {a, root};
                                                                                               }
     int sum;
void apply(int l, int r, const Tag &v) {
                                                                                          void Print(Treap *t) {
          if (v.set_val) {
    sum = (r - l) * v.set_val;
                                                                                                if (t) {
    // push(t);
                                                                                                                         // lazy
                                                                                                     Print(t->l);
```

4 Flow

4.1 Dinic [7f4d14]

```
// template dinic max flow
struct edge {
       int v, w, rev_id;
int n, m, ans = 0;
int n, m, ans = 0;
vector <edge> adj[505];
vector <int> lev(505), vis(505);
bool label_level(){ // 標記深度,如果到不了終點 return false
    fill(all(lev), -1); lev[1] = 0;
    queue <int> q; q.push(1);
    while (!q.empty()) {
        int = frect(); q.push();
        int = frect(); q.push();
        int = frect(); q.push();
              int u = q.front(); q.pop();
for (auto &[v, w, rev_id] : adj[u]) {
   if (w > 0 && lev[v] == -1) {
                             q.push(v);
                             lev[v] = lev[u] + 1;
              }
        return (lev[n] == -1 ? false : true);
int dfs(int u, int flow){
   if (u == n) return flow;
       for (auto &[v, w, rev_id] : adj[u]) {
    if (lev[v] == lev[u] + 1 && !vis[v] && w > 0) {
        vis[v] = true;
}
                      int ret = dfs(v, min(flow, w));
if (ret > 0) {
                             w -= ret:
                             adj[v][rev_id].w += ret;
                     }
              }
       return 0; // 到不了終點就會 return 0
void add_edge(int u, int v, int w) { // 無向圖的話兩邊都是 w adj[u].push_back({v, w, (int)adj[v].size()}); adj[v].push_back({u, 0, (int)adj[u].size() - 1});
void dinic() {
       while (label_level()) {
   while (true) {
     fill(all(vis), 0);
     int tmp = dfs(1, inf);
}
                     if (tmp == 0) break;
ans += tmp;
              }
       cout << ans:
// Distinct Route
// 給你一張有向圖,求從走 1 到 n 的最多方法數,並且邊不重複
// dfs 要改成
int dfs(int u, int flow){
   if (u == n) return flow;
       for (auto &[v, w, rev_id, arg_valid] : adj[u]){
   if (lev[v] == lev[u] + 1 && !vis[v] && w > 0) {
      vis[v] = true;
      int ret = dfs(v, min(flow, w));
      if (ret > 0) {
                             w -= ret:
                             adj[v][rev_id].w += ret;
                             if (arg_valid) { // 走的是 arg 路,Reset arg_valid = 0;
                                    adj[v][rev_id].arg_valid = 0;
                             else adi
                                    [v][rev_id].arg_valid = 1; // 走正常路
                             return ret;
                     }
              }
```

```
| // CSES Police Chase
 int g[505][505]; // 以 0(1) 紀錄存在邊
 void solve(){
     cin >> n >> m;

for (int i = 0; i < m; i++) {

   int u, v; cin >> u >> v;
          add_edge(u, v, 1);
     dinic();
     for (auto [v, w, _] : adj[u]){
    if(w > 0){
        self(self, v);
}
         }
     find(find, 1);
     if (g[
                  u][v] && !w && reach.find(v) == reach.end()) {
cout << u << " " << v << "\n";
                                     << V <<
                  // ans = sum(u_to_v)
              }
         }
}
```

4.3 Bipartite Matching [5e0de5]

```
struct Bipartite_Matching { // 1-based
   int n, m; vector<vector<int>> adj;
   vector<int> match, vis;
     this->m = m;
this->adj = adj;
           match.assign(n + m + 1,
          vis.assign(n + m + 1, \theta);
     [v] == -1 || self(self, match[v])) {
match[v] = u;
                              return true:
                         }
                    }
               return false;
          for (int i = 1; i <= n; i++) {
    fill(all(vis), 0);</pre>
                dfs(dfs, i);
          for (int i = n + 1; i <= n + m; i++) {
    if (match[i] != -1) {</pre>
                    cnt += 1;
          for (int i = n + 1; i <= n + m; i++) {
    if (match[i] != -1) {</pre>
                    ans.push_back({match[i], i - n});
          return { cnt, ans };
     }
};
```

```
int main(){
   int n, m, e; cin >> n >> m >> e;
   vector<vector<int>> adj(n + m + 1);
   for (int i = 1; i <= e; i++) {
      int u, v; cin >> u >> v;
   }
}
                 adj[u].push_back(v + n);
                 adj[v + n].push_back(u);
         Bipartite_Matching bip(n, m, adj);
        auto [cnt, ans] = bip.matching();
cout << cnt << "|n";
for (auto [u, v] : ans) {
    cout << u << " " << v << "|n";</pre>
}
4.4 MCMF [f622a1]
```

template < class Tf, class Tc>

```
struct MCMF {
     int n, cur;
If INF_FlOW = numeric_limits<Tf>::max() / 2;
      Tc INF_COST = numeric_limits < Tc >:: max() / 2;
      struct Edge {
            int from, to;
            Tf flow, cap; // 流量跟容量
            Tc cost;
      vector<vector<int>> adj;
      vector <Edge> edges; // 幫每個 edge 編號
vector <Tc> dis, pot; // johnson algorithm, using spfa
vector <int> par; // 路徑恢復
      vector < bool > vis:
      MCMF() { init(); }
MCMF(int n_) { init(n_); }
void init(int n_ = 0) {
            n = n_;
cur = 0;
             adj.resize(n);
             edges.clear();
            pot.assign(n, 0);
      void add_edge(int u, int v, Tf cap, Tc cost){
  edges.push_back({u, v, 0, cap, cost});
  adj[u].push_back(cur++);
  edges.push_back({v, u, 0, 0, -cost});
             adj[v].push_back(cur++);
      }
      bool spfa(int s, int t) {
    dis.assign(n, INF_COST);
            par.assign(n, -1);
vis.assign(n, false);
            queue < int > q;
dis[s] = 0;
             q.push(s);
            q.pusn(s,,
vis[s] = true;
while (!q.empty()) {
    int u = q.front();
                   q.pop();
vis[u] = false;
for (int id : adj[u]) {
    Edge &e = edges[id];
                          int v = e.to;
if (e.flow < e.cap && dis</pre>
                                  [v] > dis[u] + e.cost + pot[u] - pot[v])
                                 dis[u] = dis[u] + e.cost + pot[u] - pot[v];
par[v] = id;
if (!vis[v]) {
                                        q.push(v);
                                        vis[v] = true;
                                }
                         }
                  }
             return dis[t] != INF_COST;
      }
      // 限定 flow, 最小化 cost
pair<Tf, Tc> work_flow(int s, int t, Tf need = -1) {
    if (need == -1) need = INF_Flow;
    If flow = 0;
             Tc cost = 0;
            while (spfa(s, t)) {
    for (int i = 0; i < n; i++) {
        if (dis[i] != INF_COST) pot[i] += dis[i];</pre>
                   Tf f = INF_Flow;
                   int cur = t;
while (cur != s) {
                         Edge &e = edges[par[cur]];
f = min(f, e.cap - e.flow);
                          cur = e.from;
                      = min<Tf>(f, need);
                   flow += f;

cost += f * (pot[t] - pot[s]);

need -= f;
                   cur = t;
                   while (cur != s) {
```

```
Edge &e = edges[par[cur]];
                        edges[par[cur] ^ 1].flow -= f;
                       cur = e.from:
                  if (need == 0) break;
            return make_pair(flow, cost);
      // 限定 cost, 最大化 flow
pair<Tf, Tc> work_budget(int s, int t, Tc budget = -1) {
    if (budget == -1) budget = INF_COST;
    Tf flow = 0;
            Tc cost = 0;
            while (spfa(s, t)) {
   for (int i = 0; i < n; i++) {
      if (dis[i] != INF_COST) pot[i] += dis[i];</pre>
                  Tf f = INF Flow;
                  int cur = t;
                  while (cur != s) {
                       Edge &e = edges[par[cur]];
f = min(f, e.cap - e.flow);
                  }
f = min<Tf>(f, budget / (pot[t] - pot[s]));
                  flow += f;

cost += f * (pot[t] - pot[s]);

budget -= f * (pot[t] - pot[s]);
                  cur = t;
while (cur != s) {
                       Edge &e = edges[par[cur]];
e.flow += f;
                        edges[par[cur] ^ 1].flow -= f;
                       cur = e.from:
                  if (budget == 0) break;
            return make_pair(flow, cost);
};
```

5 String

5.1 KMP [132b98]

```
struct KMP {
        string sub;
vector<<mark>int</mark>> failure;
        KMP(string &sub) {
                this -> sub = sub:
                failure.resize(sub.size(), -1);
buildFailFunction();
        void buildFailFunction() {
                for (int i = 1; i < sub.size(); i++) {
   int now = failure[i - 1];
   while (now != -1</pre>
                         && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
               }
        vector<int> KMPmatching(string &s) {
                vector <int > match;
for (int i = 0, now = -1; i < s.size(); i++) {</pre>
                        (int i = 0, now = -1; i < s.size(); i++) {
// now is the compare sucessed length -1
while (s[i] !=
    sub[now + 1] && now != -1) now = failure[now];
// f stores if comparison fail, move to where
if (s[i] == sub[now + 1]) now++;
if (now + 1 == sub.size()) {
    match.push_back(i - now);
    now = failure[now];
}</pre>
                        }
                return match;
       }
int main() {
        string s = "xxtxxtxtx";
        string sub = "tx";
KMP kmp(sub);
        vector < int > ans = kmp.KMPmatching(s);
for(auto &i : ans) cout << i << " ";</pre>
5.2 Z函數 [0af76e]
```

```
|// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
 // 的最長公共前綴 (LCP) 的長度
 vector <int> Z(string s) {
   int n = s.size();
   vector <int> z(n + 1);
        vector title 2 (n - 2);
z[0] = n;
for (int i = 1, j = 1; i < n; i++) {
    z[i] = max(0, min(j + z[j] - i, z[i - j]));
    while (i + z[i] < n && s[z[i]] == s[i + z[i]]) {</pre>
                      z[i]++;
               if (i + z[i] > j + z[j]) {
                      j = i;
```

cur = cur->children[idx]:

cur->is_word = true;

```
bool is_in_trie(string &s) {
                                                                                                                              trie_node *cur = root;

for (int i = 0; i < s.size(); i++) {

    if (cur->
        return z; // 最後一格不算
}
                                                                                                                                    children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
 5.3 Duval Algorithm [f9dcca]
// duval_algorithm
 // 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
 vector<string> duval(string s) {
  int i = 0, n = s.size();
  vector<string> res;
                                                                                                                       int search_i_start(string &s, int i, vector<int> &dp) {
    trie_node *cur = root;
    int sz = s.size(), ans = 0;
    for (int j = i; j < sz; j++) {
        if (sure if feet);
    }
}</pre>
       while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
      else k++;
}</pre>
                                                                                                                                     if (cur
                                                                                                                                    ->children[s[j] - 'a'] == nullptr) return ans;
cur = cur->children[s[j] - 'a'];
if (cur->is_word)
    (ans += dp[j + 1]) %= mod;
                     j++;
               while (i <= k) {
    res.push_back(s.substr(i, j - k));
    i += j - k;</pre>
                                                                                                                              return ans:
                                                                                                                      }
              }
                                                                                                                int main() {
                                                                                                                       // 找到 sub 集合裡,可以重複用,組成 s 的組數 Trie trie; string s; cin >> s; int sz = s.size();
       return res;
 // 最小旋轉字串
 string min_round(string s) {
                                                                                                                       // dp 代表 i 開頭到最後的配對總數
        s += s;
int i = 0, n = s.size();
                                                                                                                        // 找到有結尾為 stop 的 dp[i] += dp[j + 1]
        int start = i;
                                                                                                                       int n; cin >> n;
       int start = 1;
while (i < n / 2) {
    start = i;
    int k = i, j = i + 1;
    while (s[k] <= s[j] && j < n) {
        if (s[k] < s[j]) k = i;
        else k++;
    }
}</pre>
                                                                                                                       vector < int > dp(sz + 1, 0);
for (int i = 0; i < n; i++) {
    string sub; cin >> sub;
                                                                                                                              trie.insert(sub);
                                                                                                                       dp[sz] = 1;
                                                                                                                       for (int i = sz - 1; i >= 0; i--) {
    dp[i] = trie.search_i_start(s, i, dp);
                     j++;
              while (i <= k) {
                     i += j - k;
                                                                                                                       cout << dp[0] << endl;
                                                                                                               }
        return s.substr(start, n / 2);
                                                                                                                6
                                                                                                                     Math
}
                                                                                                                6.1 質因數分解 [ee1622]
 5.4 Manacher [9c9ca6]
                                                                                                                    a^{(m-1)} = 1 \pmod{m}
 // 找到對於每個位置的迴文半徑
                                                                                                                // a^(m-1) = 1 (Mod M)

// a^(m-2) = 1/a (mod M)

// EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)

// Filter + DP; DP save min factor 'recur' factor decomposition

// FacNums = (x+1)(y+1)(z+1)...

// FacSum = (a^0+a^1...+a^x)(b^0+...+b^y)

// FacMul = N(x+1)(y+1)(z+1)/2
 vector<int> manacher(string s) {
        string t = "#";
        for (auto c : s) {
              t += c;
t += '#';
        int n = t.size();
                                                                                                                vector<int> is_prime;
        vector < int > r(n);
for (int i = 0, j =
                                                                                                                // 1 代表是質數, 非 1 不是
void init(int n) {
              0; i < n; i++) { // i 是中心, j 是最長回文字串中心 if (2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
                                                                                                                       is\_prime.assign(n + 1,
                                                                                                                       for (int i = 2; i <= (int)sqrt(n) + 1; i++) {
                                                                                                                              if (is_prime[i] == 1) {
    for (int j = i + i; j <= n; j += i) {
        is_prime[j] = i;
    }</pre>
               while (i - r[i] >=
     0 && i + r[i] < n && t[i - r[i]] == t[i + r[i]]) {
    r[i] += 1;</pre>
                                                                                                                              }
                                                                                                                       }
              if (i + r[i] > j + r[j]) {
    j = i;
                                                                                                                int main() {
    init(1000000);
              }
                                                                                                                       ll ans = 1;
        return r;
// # a # b # a #
// 1 2 1 4 1 2 1
                                                                                                                       ll q; cin >> q;
map<ll, ll> mp;
while (is_prime[q] != 1) {
        ,,
// # a # b # b # a #
                                                                                                                             mp[is_prime[q]]++;
q /= is_prime[q];
        // 1 2 1 2 5 2 1 2 1
        // 值 -1 代表原回文字串長度
                                                                                                                       if (q != 1) mp[q]++;
for (auto [a, b] : mp) {
    ans *= b + 1;
       // (id - val + 1) / 2 可得原字串回文開頭
 5.5 Trie [3b3aa0]
                                                                                                                       cout << ans << "\n";
 struct Trie {
        struct trie_node {
                                                                                                                6.2 中國餘數定理 [d41d8c]
              bool is_word;
              vector<trie_node *> children;
trie_node() {
    is_word = false;
                                                                                                                ll exgcd(ll a, ll b, ll &x, ll &y) {
                                                                                                                       if (!b) {
                     children.resize(26, NULL);
                                                                                                                              x = 1, y = 0;
              }
                                                                                                                              return a:
       f;
trie_node *root = new trie_node();
void insert(string &s) {
   trie_node *cur = root;
   for (int i = 0; i < s.size(); i++) {
      int idx = s[i] - 'a';
      if (cur->children[idx] == NULL) {
         cur->children[idx] = new trie_node();
}
                                                                                                                       ll g = exgcd(b, a % b, y, x);
y -= a / b * x;
                                                                                                                       return g;
                                                                                                                Il inv(ll x, ll m){
```

ll`a, b;

return a;

exgcd(x, m, a, b);

a %= m; if (a < 0) a += m;

```
}
// remain, mod

ll CRT(vector<pair<ll, ll>> &a){
    ll prod = 1;
    for (auto x : a) {
        prod *= x.second;
    }
    ll res = 0;
    for (auto x : a) {
        auto t = prod / x.second;
        res += x.first * t % prod * inv(t, x.second) % prod;
        if(res >= prod) res -= prod;
    }
    return res;
}
```

6.3 矩陣快速幕 [d41d8c]

```
struct Mat {
      int m, n;
      vector<vector<ll>> matrix;
      void init(int m, int n) {
    this->m = m; this->n = n;
             matrix.resize(m);
for (int i = 0; i < m; i++) {</pre>
                   matrix[i].resize(n);
      Mat(int m, int n) { init(m, n); }
Mat(int n) { init(n, n); }
      Mat(vector<vector<ll>>> matrix) {
    this->m = matrix.size();
    this->n = matrix[0].size();
             this->matrix = matrix;
      Mat unit(int n) { // 單位矩陣
            for (int i = 0; i < n; i++) {
    res.matrix[i][i] = 1;</pre>
             return res;
      Mat operator * (Mat b) {
             int m = matrix.size
                   (), n = b.matrix[1].size(), k = matrix[0].size();
             Mat ans(m, n);
for (int i = 0; i < m; i++) {</pre>
                   for (int j = 0; j < n; j++) {
    for (int k = 0; k < n; k++) {
        (ans.matrix[i][j] += (matrix[</pre>
                                       i][k] * b.matrix[k][j] % mod)) %= mod;
                   }
             return ans;
      Mat operator
          *= (Mat b) { *this = *this * b; return *this; }
Mat operator ^ (ll p) {
    if (p == 0) return unit(n);
    Mat ans = *this; p--;
    while (p > 0) {
        if (p & 1) {
            ans *= *this;
        }
      Mat operator
                   *this *= *this;
                   p >>= 1;
             return ans:
      Mat operator ^= (ll p) { *this = *this ^ p; return *this; }
signed main() {
      int n; cin >> n; ll ans;
if (n <= 4) {</pre>
             vector < int > v = \{0, 1, 1, 2, 4\};
             ans = v[n];
      else {
             Mat init({{4, 2, 1}, {2, 1, 1}, {1, 1, 0}});
             T.matrix = {{1, 1, 0}, {1, 0, 1}, {1, 0, 0}};

T ^= n - 4;

init *= T;
             ans = init.matrix[0][0];
      cout << ans << "\n";
// 初始矩陣
// f4 f3 f2
// f3 f2 f1
// f2 f1 f0
                      轉移式
                     1 1 0  f5 f4 f3
1 0 1 => f4 f3 f2
1 0 0  f3 f2 f1
```

6.4 模除計算 [961014]

```
using i64 = long long;
template < class T >
constexpr T power(T a, i64 b) {
    T res = 1;
    for (; b; b /= 2, a *= a) {
        if (b % 2) {
```

```
res *= a:
         }
     return res:
}
constexpr i64 mul(i64 a, i64 b, i64 p) {
    i64 res = a * b - i64(1.L * a * b / p) * p;
     res %= p;
     if (res < 0) {
    res += p;
     return res:
template < i64 P>
struct MLong {
     i64 x;
     constexpr MLong() : x{} {}
constexpr MLong(i64 x) : x{norm(x % getMod())} {}
     static i64 Mod:
     constexpr static i64 getMod() {
   if (P > 0) {
               return P:
          } else {
              return Mod;
         }
     constexpr static void setMod(i64 Mod_) {
   Mod = Mod_;
     constexpr i64 norm(i64 x) const {
         if (x < 0) {
    x += getMod();</pre>
          if (x >= getMod()) {
               x -= getMod();
          return x;
     constexpr i64 val() const {
          return x;
     explicit constexpr operator i64() const {
     constexpr MLong operator -() const {
          MLong res;
res.x = norm(getMod() - x);
          return res;
     constexpr MLong inv() const {
          assert(x != 0);
return power(*this, getMod() - 2);
     constexpr MLong &operator*=(MLong rhs) & {
    x = mul(x, rhs.x, getMod());
    return *this;
     constexpr MLong &operator+=(MLong rhs) & {
    x = norm(x + rhs.x);
          return *this;
     constexpr MLong &operator -= (MLong rhs) & {
          x = norm(x - rhs.x);
          return *this:
     constexpr MLong &operator/=(MLong rhs) & {
  return *this *= rhs.inv();
     friend constexpr MLong operator*(MLong lhs, MLong rhs) {
          MLong res = lhs;
          res *= rhs:
          return res:
     friend constexpr MLong operator+(MLong lhs, MLong rhs) {
          MLong res = lhs;
res += rhs;
     friend constexpr MLong operator-(MLong lhs, MLong rhs) {
          MLong res = lhs;
res -= rhs;
          return res;
     friend constexpr MLong operator/(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res /= rhs;
          return res;
           constexpr istream &operator>>(istream &is, MLong &a) {
          i64 v;
is >> v;
          a = MLong(v);
          return is:
     friend constexpr
            ostream &operator << (ostream &os, const MLong &a) {
          return os << a.val();</pre>
     friend constexpr bool operator == (MLong lhs, MLong rhs) {
```

```
return lhs.val() == rhs.val():
        friend constexpr bool operator!=(MLong lhs, MLong rhs) {
   return lhs.val() != rhs.val();
 };
 template<>
 i64 MLong < 0LL >:: Mod = i64(1E18) + 9;
 constexpr i64 P = 998244353;
 using Z = MLong < P >;
// using Z = MLong < OLL >; // change Mod
 struct Comb {
        i64 n;
       t64 n;
vector <Z> _fac;
vector <Z> _invfac;
vector <Z> _inv;
Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
Comb(i64 n) : Comb() { init(n); }
        void init(i64 m) {
              m = min(m, Z::getMod() - 1);
if (m <= n) return;</pre>
              _fac.resize(m + 1);
              _invfac.resize(m + 1);
_inv.resize(m + 1);
              for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;</pre>
              for (int i = _fac[m].inv();
for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
              n = m;
       }
Z fac(i64 m) {
   if (m > n) init(2 * m);
   return _fac[m];
-
       }
Z invfac(i64 m) {
   if (m > n) init(2 * m);
   invfac[m];
       }
Z inv(i64 m) {
   if (m > n) init(2 * m);
   return _inv[m];
       }
Z binom(i64 n, i64 m) {
   if (n < m || m < 0) return 0;
   return fac(n) * invfac(m) * invfac(n - m);</pre>
        |} comb; // 注意宣告, 若要換模數需重新宣告
```

6.5 樹論分塊 [06204a]

6.6 Mobius Theorem

- 數論分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在O(1)內計算f(r)-f(l)或已經預處理 出 f 的前綴時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d|n} \mu(d) = \begin{cases} 1 & \text{for } n=1\\ 0 & \text{for } n \neq 0 \end{cases}$$

2. μ 是常數函數 1 的反元素 $\Rightarrow \mu*1=\epsilon$, $\epsilon(n)$ 只在n=1 時為 1, 其餘情況皆為 0。

- φ歐拉函數: x 以下與 x 互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^{i}) \\ &= 1 + p^{0}(p-1) + p^{1}(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^{c} \\ &= id \end{split}$$

• 莫比烏斯反演公式

-
$$f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$$

- $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

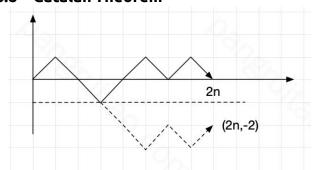
• 例子

$$\begin{split} &\sum_{i=a}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left \lfloor \frac{x}{k} \right \rfloor} \left \lfloor \frac{y}{k} \right \rfloor \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left \lfloor \frac{x}{k} \right \rfloor} [d \mid i] \sum_{j=1}^{y} [d \mid j] \ \mathrm{d} \ \mathrm{PSER} \ \mathrm{i} \ \mathrm{FRA} \ \mathrm{1} \\ &= \sum_{d=1}^{\min(\left \lfloor \frac{x}{k} \right \rfloor, \left \lfloor \frac{y}{k} \right \rfloor)} \\ &= \sum_{d=1}^{\min(\left \lfloor \frac{x}{k} \right \rfloor, \left \lfloor \frac{y}{k} \right \rfloor)} \mu(d) \left \lfloor \frac{x}{kd} \right \rfloor \left \lfloor \frac{y}{kd} \right \rfloor \end{split}$$

6.7 莫比鳥斯反演 [d41d8c]

```
const int maxn = 2e5;
ll mobius_pref[maxn];
 void init() {
       mobius_pref[1] = 1;
vector<ll> wei
        (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
    }
                      continue; // 包含平方
               if (wei[i] == 0) {
                     wet[i] -- 0, {
wet[i] = 1;
for (ll j = 2; i * j < maxn; j++) {
    if (j % i == 0) wet[i * j] = -1;
    else if (wet[i * j] != -1) wet[i * j]++;</pre>
                     }
              mobius_pref[i]
                       = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
       }
 void solve() {
        auto cal = [&](ll x, ll y) -> int {
              for (int l = 1, r; l <= min(x, y); l = r + 1) {
    r = min(x / (x / l), y / (y / l));
    res += (mobius_pref[r] - mobius_pref[l])</pre>
                                - 1]) * (x / l) * (y / l); // 代推出來的式子
              return res;
                (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k,
(c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n";
}
```

6.8 Catalan Theorem



1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$ 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有x 個,往下有y 個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.9 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- X/G:本質不同的方案的集合
- X'^g : 對於某一種操作 g, 所有方案中,經過 g 這種翻轉後保持不變的方案的集合
- 集合取絕對值代表集合數

7 Search and Gready

7.1 二分搜 [d41d8c]

```
int main() {
    int l = 1, r = 10;
    // 1 to tar, find tar
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}</pre>
```

7.2 三分搜 [d41d8c]

```
| // 找極值問題,遞增遞減
| void solve() {
| int | = 0, r = 10, ans = 0; // ans 紀錄答案 |
| while (| <= r) {
| int | d = (r - l) / 3; // 差 |
| int | ml = l + d, mr = r - d; // mr 要用減的 |
| auto | cal = [&](int | m) -> int {
| int | x = 0; |
| return | x; // 計算答案 |
| ; int | ansl = | cal(|ml), ansr = | cal(|mr); if (| ansl | < | ansr) {
| l = | ml + 1; |
| else | r = | mr - 1; |
| }
```

8 Tree

8.1 LCA [9f95b1]

```
}
int lca(int a, int b) {
    if (depth[a] < depth[b]) swap(a, b);
    int pull = depth[a] - depth[b];
    for (int i = 0; i < 18; i++) {
        if (pull & (1 << i)) {
            a = par[a][i];
        }
    if (a == b) return a;
    for (int i = 17; i >= 0; i--) {
        if (par[a][i] != par[b][i]) {
            a = par[a][i], b = par[b][i];
        }
    }
    return par[a][0];
}
```

8.2 樹重心 [30b436]

```
struct centroid_decomposition {
       int n:
        vector<vector<int>> adj;
        vector<bool> vis;
       vector<int> siz;
       centroid_decomposition() {}
centroid_decomposition(int n_) { init(n_); }
       void init(int n_) {
             n = n_;
adj.assign(n, {});
vis.assign(n, false);
             siz.assign(n, 1);
        void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void get_siz(int dep, int x, int p = -1) {
             siz[x] = 1;
             stz[x] = 1;
for (int y : adj[x]) {
    if (y == p || vis[y]) continue;
    get_siz(dep + 1, y, x);
    siz[x] += siz[y];
       return get_cen(y, sz, x);
              return x:
       void work(int x = 0) {
    get_siz(0, x);
    int cen = get_cen(x, siz[x]);
    vis[cen] = true;
              // do something
              for (int y : adj[cen]) {
   if (vis[y]) continue;
   work(y);
1 };
```

8.3 樹壓平 [51199c]

```
點加值 = 所有子節點區間加值,求單點,使用 bit,做前綴差分
CSES 1138_Path Queries
   int n, q; cin >> n >> q;
vector <int> node_value(n + 1), euler_ordered_value(n);
for (int i = 1; i <= n; i++) {</pre>
        cin >> node_value[i];
   vector<vector<int>> tree(n + 1);
   for (int i = 1; i < n; i++) {
  int u, v; cin >> u >> v;
  tree[u].push_back(v);
        tree[v].push_back(u);
   vector<pair<int, int>> tree mapping(n + 1);
   int cnt = 0;
auto dfs = [&](auto self, int u, int par) -> void {
    euler_ordered_value[++cnt] = node_value[u];
        tree_mapping[u].first = cnt;
        for (auto v : tree[u]) {
   if (v == par) continue;
   self(self, v, u);
        tree_mapping[u].second = cnt;
   dfs(dfs,
   BIT bit(n);
for (int i = 1; i <= n; i++) {
        bit.modify(tree_mapping[i].first, node_value[i]);
        if (tree_mapping[i].first < n) { // root 就不用扣了</pre>
                    (tree_mapping[i].second + 1, -node_value[i]);
```

8.4 Heavy Light Decomposition [6791f6]

```
struct HLD {
     vector<int> siz, top, dep, parent, in, out, seq;
     vector<vector<int>> adj;
     int cur;
    HLD() {}
HLD(int n) {
          init(n);
     void init(int n) {
          this ->n = n:
          siz.resize(n);
          top.resize(n);
          dep.resize(n);
parent.resize(n);
          .
in.resize(n);
          out.resize(n);
          seq.resize(n);
          adj.assign(n, {});
     void addEdge(int u, int v) {
          adj[u].push_back(v);
          adj[v].push_back(u);
     void work(int root = 0) {
          top[root] = root;
dep[root] = 0;
          parent[root] = -1;
          dfs1(root);
          dfs2(root):
     void dfs1(int u) {
          if (parent[u] != -1) {
    adj[u].erase(find
                     (adj[u].begin(), adj[u].end(), parent[u]));
          siz[u] = 1;
          for (auto &v : adj[u]) {
    parent[v] = u;
    dep[v] = dep[u] + 1;
               dfs1(v);
               siz[u] += siz[v];
if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
              } // 讓 adj[u][0] 是重子節點
         }
     void dfs2(int u) {
          in[u] = cur++;
          seq[in[u]] = u; // dfn 對應的編號
          dfs2(v):
          out[u] = cur;
     int lca(int u, int v) {
          while (top[u] != top[v]) {
    if (dep[top[u]] > dep[top[v]]) {
        u = parent[top[u]];
}
               } else {
                    v = parent[top[v]];
          return dep[u] < dep[v] ? u : v;</pre>
    int dist(int u, int v) {
   return dep[u] + dep[v] - 2 * dep[lca(u, v)];
     int jump(int u, int k) {
    if (dep[u] < k) {
        return -1;</pre>
          int d = dep[u] - k;
```

```
while (dep[top[u]] > d) {
    u = parent[top[u]];
          return seq[in[u] - dep[u] + d];
     bool isAncester(int u, int v) {
          // 判斷 u 是否是 v 的祖先
          return in[u] <= in[v] && in[v] < out[u];</pre>
      int rootedParent(int u, int v) {
          // 根據新根節點 u 計算 v 的父節點
          swap(u, v);
          if (u == v) {
               return u;
          if (!isAncester(u, v)) {
               return parent[u];
          auto it = upper_bound(adj
    [u].begin(), adj[u].end(), v, [&](int x, int y) {
    return in[x] < in[y];</pre>
          }) - 1;
return *it;
      int rootedSize(int u, int v) {
          // 根據新根節點 u 計算子樹 v 的大小
          if (u == v) {
          if (!isAncester(v, u)) {
              return siz[v];
          return n - siz[rootedParent(u, v)];
      int rootedLca(int a, int b, int c) {
          // 根據新的根節點計算三個節點 a、b 和 c 的最近公共祖先 return lca(a, b) ^ lca(b, c) ^ lca(c, a);
     }
};
```

8.5 Virtual Tree [622e69]

```
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
// 可以建立虚樹達成快速樹 DP
 // 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector <int>stk(maxn);
 int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
        vt[stk[top - 1]].push_back(stk[top]), top--;
    if (stk[top - 1] != l) {
        vt[l] sush back(stk[top]);
        vt[l] sush back(stk[top]);
        vt[l] sush back(stk[top]);
}</pre>
                vt[l].push_back(stk[top]);
                 stk[top] = l;
         } else vt[l].push_back(stk[top--]);
         stk[++top] = u;
  void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
         vt[u].clear();
  void solve(int n, int q) {
         vector g(n + 1, vector<pair<int, int>>());
         vector vt(n + 1, vector vector vt(n + 1, vector <int>()); // dfs 完清除, 否則會退化
vector <ll> dp(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;

                g[u].push_back({v, w});
                 g[v].push_back({u, w});
         build_lca(n, g);
         build(n, g);
for (int i = 0; i < q; i++) {
   int m; top = -1; cin >> m;
                 vector<int> key(m);
                for (int j = 0; j < m; j++) {
    cin >> key[j];
                         iskey[key[j]] = 1;
                key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
                 for (int x : key) insert(x, vt);
                while (top
                           > 0) vt[stk[top - 1]].push_back(stk[top]), --top;
                 // DP
                auto dfs = [&](auto self, int u) -> void {
    for (auto v : vt[u]) {
        self(self, v);
        if (iskey[v]) {
            dp[u] += min_dis[v];
        }
                                       // 砍掉 1 到 v 之間最短的路
                                       dp[u] += min(dp[v], min_dis[v]);
                                iskey[v] = dp[v] = 0;
```

```
vt[u].clear():
          dfs(dfs, key[0]); // key[0] 一定是 root cout << dp[key[0]] << "\n";
          iskey[key[0]] = dp[key[0]] = 0;
     }
}
```

9 DP

9.1 背包問題 [6d6b63]

```
/ 考慮前 i 個,預算有 j 塊錢的最多 page
int main(){
    int n, bud;
cin >> n >> bud;
    vector<vector<int>> dp(n + 1, vector<int>(bud + 1));
vector<int> Page(n + 1, 0);
vector<int> Price(n + 1, 0);
    for(int i = 1; i <= n; i++){
    cin >> Price[i];
    for(int i = 1; i <= n; i++){
    cin >> Page[i];
    for (int i = 1; i <= n; i++) {
    for (int j = 1; j <= bud; j++) {</pre>
              if (j >= Price[i]) { // 買得起
                   // 不買或買
                   else {
                   dp[i][j] = dp[i - 1][j];
    cout << dp[n][bud] << "\n";
```

9.2 Bitmask [b18541]

```
void travel_exactly_once(){
     // [走過的路][終點]
     int u, v; cin >> u >> v;
rev_adj[--v].push_back(--u);
     dp[1][0] = 1;
for (int road = 0; road < (1 << n); road++) {
    // 沒經過起點,不用走
    if (road & 1 == 0) continue;
           // 有終點但沒全部走過
           if (road & (1
                   << (n
                            - 1)) && road != ((1 << n) - 1)) continue;
           // DP,隨便選定一個當前路徑的終點
           for (int end = 0; end < n; end++) {</pre>
                 // 路徑沒包含假定的 end
                 if ((road & (1 << end)) == 0) continue;
// 去除終點,得到 pre_road
int pre_road = road - (1 << end);
                 // 從 rev_adj 找 pre_road 的終點
                 for (int pre_road_end : rev_adj[end]) {
   if ((road & (1 << pre_road_end))) {</pre>
                            dp[road
                                   ][end] += dp[pre_road][pre_road_end];
                            dp[road][end] %= mod;
                      }
                }
           }
     cout << dp[(1 << n) - 1][n - 1];
void elevator_rides(){
  int n, k; cin >> n >> k;
  vector<int> passenger(n);
     for (int i = 0; i < n; i++) cin >> passenger[i];
     vector<int
     > used(1 << n, 0);  // 最後載完人的電梯用了多少空間
vector <int> dp(1 << n, 1);  // bitset
for (int i = 1; i < 1 << n; i++) {
    used[i] = dp[i] = 2e9;
    for (int i = 1; i < 1 << n; i++) {
           for (int j = 0; j < n; j++) {
                 if (i & (1 << j)) { // 有 j
int pre = i ^ (1 << j);
                       // 最後的電梯還能載 j
if (used[pre] + passenger[j] <= k) {
                            // 電梯數先比,再來比用掉的空間 if (dp
                                  [pre] < dp[i] || (dp[pre] == dp[i] &&
  used[pre] + passenger[j] < used[i])) {
  used[i] = used[pre] + passenger[j];</pre>
                                  dp[i] = dp[pre];
                            }
```

```
-
// 搭新的電梯
                        == dp[i] && passenger[j] < used[i])) {
used[i] = passenger[j];
dp[i] = dp[pre] + 1;
                        }
                 }
            }
       cout << dp[(1 << n) - 1];
 int main(){
       travel exactly once();
       elevator_rides();
 9.3 硬幣 [d41d8c]
void coin_combination_II(){
       // 有 n 種錢幣,求組合為 x 的組數,順序不可顛倒
       // 可顛倒的話只要一維, 先 x 廻圈, 再 coin[i] 去加
       int n, x; cin >> n >> x;
vector < int >> coin(n + 1);
       // dp[i][j] 為考慮前 i 個硬幣,組合為 i 的組數
       vector<vector<int>> dp(2, vector<int>(x + 1, 0));
       dp[0][0] = 1;
for (int i = 1; i <= n; i++) cin >> coin[i];
       for (int i = 1; i <= n; i++){</pre>
            for (int j = 0; j <= x; j++) {
    // 壓到 2 * n
                  dp[i & 1][j] = dp[!(i & 1)][j];
if (j >= coin[i]) {
                        (dp[i
                               & 1][j] += dp[i & 1][j - coin[i]]) %= mod;
            }
       cout << dp[n & 1][x];
 void minimize_coins_nums(){
       // 有 n 種錢幣,求組合為 x 的最小硬幣數
      // 分 // 性致市 > n >> n >> x;

int n, x; cin >> n >> x;

vector <int >> coin(n);

for (int i = 0; i < n; i++) cin >> coin[i];

// dp[i] 是組合為 i 的最小硬幣數
       vector < int > dp(x + 1, 0);
       for (int i = 1; i <= x; i++) {
  dp[i] = 2e9;
  for(auto &j : coin){</pre>
                  if(j <= i){
                        dp[i] = min(dp[i], dp[i - j] + 1);
       cout << (dp[x] == 2e9 ? -1 : dp[x]):
 int main(){
       coin_combination_II();
minimize_coins_nums();
 9.4 編輯距離 [4d4a6d]
 int main() {
       string s1, s2; cin >> s1 >> s2;
int size1 = s1.size(), size2 = s2.size();
// dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元
       vector <
             vector<int>> dp(size1 + 1, vector<int>(size2 + 1, 0));
      vector<int> vector<int> (st.)
s1 = "0" + s1, s2 = "0" + s2;
for (int i = 1; i <= size1; i++) dp[i][0] = i;
for (int i = 1; i <= size2; i++) dp[0][i] = i;
for (int i = 1; i <= size1; i++){
    for (int j = 1; j <= size2; j++) {
        if (s1[i] == s2[j]) {
            dp[i][j] = dp[i - 1][j - 1];
        }
}</pre>
                  else {
                        // s1 新增等價於 s2 砍掉
                        // dp[i][j] = min(修改, s1 新增, s2 新増);
dp[i][j] = min({dp[i - 1][
                        dp[i][j] = min({dp[i - 1][
        j - 1], dp[i - 1][j], dp[i][j - 1]}) + 1;
            }
       cout << dp[size1][size2];</pre>
 9.5 LCS [087c0d]
 int main() {
       int m, n; cin >> m >> n;
string s1, s2;
       cin >> s1 >> s2;
       int L = 0:
```

vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0));

par[i] = id:

add[i] = projects[i].id;

```
for (int i = 1; i <= m; i++) {
   for (int j = 1; j <= n; j++) {
     if (s1[i - 1] == s2[j - 1]) {
          dp[i][j] = dp[i - 1][j - 1] + 1;
}</pre>
                                                                                                          cout << i << " " << " | n";
for (int now = n; now > 0; now = par[now])
   if (add[now] != -1)
                                                                                                                      ans.push_back(add[now]);
                                                                                                          sort(all(ans));
for (auto &i : ans) cout << i << " ";</pre>
                        dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
      9.8 Removal Game [211de0]
     int length = dp[m][n];
cout << length << "\n";
string s(length, 'c');
// along to dp to trace back
while (m >= 1 && n >= 1) {
   if (s1[m - 1] == s2[n - 1]) {
        s[length - 1] = s1[m - 1];
        m--, n--, length--;
}
                                                                                                  | // 兩個人比賽,每個人輪流取一個數字且只能是頭尾
                                                                                                    // 問兩人都選得好,第一個人可取得的最大分數int main() {
                                                                                                          vector<vector<int>> dp(n + 1, vector<int>(n + 1));
                                                                                                          int pref = 0:
                                                                                                          vector<int> v(n + 1);
            else {
   if (dp[m - 1][n] > dp[m][n - 1]) m--;
                                                                                                          for (int i = 1; i <= n; i++) {
    cin >> v[i];
                                                                                                          // dp[i][j] 是 i 到 j 區間選完,的最大分數差
      cout << s << "\n";
                                                                                                          for (int i = n; i > 0; i--) {
   for (int j = i; j <= n; j++) {
      if (i == j) {</pre>
9.6 LIS [668131]
                                                                                                                            dp[i][j] = v[i];
int main() {
                                                                                                                      else {
      int n; cin >> n;
      for (int i = 0; i < n; i++) {
    cin >> v[i];
                                                                                                                             // 選左差距大,還是選右差距大
                                                                                                                            dp[i][j] = max(
    v[i] - dp[i + 1][j], v[j] - dp[i][j - 1]);
      int dp[n]; vector<int> mono;
mono.push_back(v[0]);
dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) {
    if (v[i] > mono.back()) {
                                                                                                                }
                                                                                                          // x + y = sum, dp[1][n] = x - y;
cout << (pref + dp[1][n]) / 2;
                  mono.push_back(v[i]);
                                                                                                    9.9 CF Example [7d37ea]
                  dp[i] = ++L;
                                                                                                  | // CF 1932 DF
                  auto it
                                                                                                  // 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
                  = lower_bound(mono.begin(), mono.end(), v[i]);
*it = v[i];
                                                                                                    // 請問在線段不重複的情況下,最多獲得幾分int main() {
                  dp[i] = it - mono.begin() + 1;
                                                                                                          int n, m;
cin >> n >> m;
            }
                                                                                                          // 記錄每點有幾個線段
      vector<int> ans;
                                                                                                          // 再一個紀錄,包含這個點的左界
      cout << L << "\n";
for (int i = n - 1; i >= 0; i--) {
   if (dp[i] == L) {
                                                                                                          vector(int> l_side(n + 1, inf), cnt(n + 5, 0);
for (int i = 0; i < m; i++) {</pre>
                                                                                                                int l, r; cin >> l >> r;
l_side[r] = min(l_side[r], l);
                  ans.push_back(v[i]);
           }
                                                                                                                cnt[l]++;
                                                                                                                cnt[r + 1]--;
      reverse(ans.begin(), ans.end());
for (auto i : ans) {
    cout << i << " ";</pre>
                                                                                                          for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
                                                                                                          for (int i = n; i >= 2; i--) {
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
}
9.7 Projects [18998c]
                                                                                                          vector<int> dp(n + 1);
// 排程有權重問題,輸出價值最多且時間最少
                                                                                                          dp[0] = 0;
                                                                                                          dp[o] - 0,
for (int i = 1; i <= n; i++) {
    dp[i] = cnt[i];
    if (l_side[i] != inf) {</pre>
struct project {
      int from, end, gain, id;
int main() {
    int n; cin >> n;

                                                                                                                      dp[i] += dp[l_side[i] - 1];
      dp[i] = max(dp[i], dp[i - 1]);
                                                                                                          cout << dp[n] << "\n";
                                                                                                    }
      sort(all(projects), [](project a, project b) {
   if (a.end == b.end) return a.gain < b.gain;
   return a.end < b.end;</pre>
                                                                                                    // CF 1935 pC
                                                                                                   |// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
                                                                                                    // 再加上 max(bi) - min(bi)
int main(){
     y);
vector<array<int, 3>> dp(n + 1); // nums, gain, time
vector<int> par(n + 1, 0), ans, add(n + 1, -1);
for (int i = 1; i <= n; i++) {
    int id = --upper_bound(projects.begin
        (), projects.begin() + i, project({0, projects
        [i].from, 0, 0}), [](project &a, project &b) {
    return a.end < b.end;
                                                                                                          int n, k, ans = 0; cin >> n >> k;
vector <pii> v(n + 1);
for (int i = 1; i <= n; i++) {</pre>
                                                                                                                int a, b; cin >> a >> b;
v[i] = {a, b};
if (a <= k) ans = 1;
                   projects.begin(); // 二分搜最接近 from 的 end
                                                                                                          sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
            dp[i] = dp[i - 1];
par[i] = i - 1;
                                                                                                          }); // 用 bi 來排,考慮第 i 個時可以先扣 vector<vector<int>> dp(n + 1, vector<int>(n + 1, inf));
            if (dp
                   // 考慮 v[i] 時,選 j 個的 sum(ai) - min(bi)
                                                                                                          for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
                  // 如果報酬率一樣,比時間少的
                  dp[i] = {dp
                         [id][0] + 1, dp[id][1] + projects[i].gain, dp
[id][2] + projects[i].end - projects[i].from};
```

min(不選,選)

-1][j -1] + v[i].first + v[i].second <= k) {

// 假如可以選,更新 ans 時再加回去 bi

if (dp[i

return *this;

return *this;

x *= v; y *= v;

Point & operator *= (const T & v) & {

Point & operator /= (const T & v) & {

```
x /= v;
y /= v;
return *this;
                 ans = max(ans. i):
         dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
    cout << ans << endl;</pre>
}
 9.10 Slope Trick [2ccb3a]
| // 設 dp[i][j] 為將陣列前
                                                                             return a -= b;
       i 個元素變為非嚴格遞增,並且所有 ai <= bj 所需要花的代價
 #include <bits/stdc++.h>
 using namespace std;
#define int long long
signed main() {
    int n; cin >> n;
vector <int> v(n);
for (int i = 0; i < n; i++) {
    cin >> v[i];
         v[i] -= i;
     vector<int> discrete = v;
     sort(discrete.begin(), discrete.end());
     int m = unique
    dp[1][j] = min(dp[1][j
                   1], dp[0][j] + abs(v[i] - discrete[j - 1]));
                                                                     template < class T>
         swap(dp[0], dp[1]);
                                                                     struct Line {
                                                                         Point<T>
    cout << *min_element(dp[0].begin(), dp[0].end());</pre>
// 當 dp 是凸函數且答案是極值時,可以用 slope trick 優化
// 要注意的是
     如果兩個相鄰段的斜率差異大於 1,那麼這個關鍵點是要存兩次的
 // 例如這題假設在 i-1 時 f{i-1}(x) 是一個 Slope Trick 函數,
                                                                     template < class T>
 // 我們額外定義一個函數 g_i(x
     )表示將前 i 個元素變為非嚴格遞增,且 a_i = x 的最小花費。
   則 g_i(x) = f\{i-1\}(x) + |x-a_i| ,我們可以觀察到
 // f_i(x) = min(g_i(y))
                                                                     template < class T>
     )), for y <= x ,由於 |x-a_i| 是一個 Slope Trickable 函數,
g_i(x) 和 f_i(x) 都是 Slope Trickable 函數,因為 |x-a_i|,
// 分段點是 a_i,且因為斜率一定大於 1,要 push 2 次
                                                                     template < class T>
 // 因為 g_i(x) 最右邊函數的斜率是
      1,因此我們只需去除 g_i(x) 的最大斜率變化點得到 f_i(x)。
                                                                         return dot(p, p);
 int main () {
     priority_queue < int > q;
int n; cin >> n;
for (int i = 0; i < n; i++) {</pre>
                                                                     template < class T>
         int x; cin >> x;
x -= i + 1;
         q.push(x);
         q.push(x);
                                                                     template < class T>
         ans += q.top() - x;
         a.pop():
     cout << ans;
                                                                     template < class T>
 10 Geometry
 10.1 Basic [d41d8c]
 #include <bits/stdc++.h>
 using namespace std;
using i64 = long long;
                                                                     template < class T>
 template < class T>
 struct Point {
    T x;
     Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) \{ \}
                                                                     template < class T>
     template < class U>
     operator Point<U>()
         return Point<U>(U(x), U(y));
                                                                     template < class T>
     Point & operator += (const Point &p) & {
         x += p.x;
y += p.y;
return *this;
     Point & operator -= (const Point &p) & {
         x -= p.x:
         y -= p.y;
```

```
Point operator - () const {
          return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
     friend Point operator - (Point a, const Point &b) {
     friend Point operator*(Point a, const T &b) {
  return a *= b;
     friend Point operator/(Point a, const T &b) {
   return a /= b;
     friend Point operator*(const T &a, Point b) {
   return b *= a;
     friend bool operator==(const Point &a, const Point &b) {
          return a.x == b.x && a.y == b.y;
     friend istream &operator>>(istream &is, Point &p) {
          return is >> p.x >> p.y;
     friend ostream &operator<<(ostream &os, const Point &p) {</pre>
          return os << "(" << p.x << ", " << p.y << ")";
     Point<T> b;
Line(const Point<T> &a_ = Point<T>()
           , const Point<T> ab_{-} = Point<T>()) : a(a_{-}), b(b_{-}) {}
T dot(const Point<T> &a, const Point<T> &b) {
   return a.x * b.x + a.y * b.y;
T cross(const Point<T> &a, const Point<T> &b) {
    return a.x * b.y - a.y * b.x;
T square(const Point<T> &p) {
double length(const Point<T> &p) {
     return sqrt(square(p));
double length(const Line<T> &l) {
     return length(l.a - l.b);
Point<T> normalize(const Point<T> &p) {
     return p / length(p);
bool parallel(const Line<T> &l1, const Line<T> &l2) {
    return cross(l1.b - l1.a, l2.b - l2.a) == 0;
double distance(const Point<T> &a, const Point<T> &b) {
    return length(a - b);
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0) {
      return distance(p, l.a);
}</pre>
     if (dot(p - l.b, l.a - l.b) < 0) {
    return distance(p, l.b);</pre>
     return distancePL(p, l);
}
template < class T>
Point<T> rotate(const Point<T> &a) {
     return Point(-a.v, a.x);
```

```
template < class T>
int sgn(const Point<T> &a) {
      return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
    return cross(l.b - l.a, p - l.a) > 0;
template < class T>
      > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
return l1.a + (l1.b - l1.a) * (cross(l2.b - l2.a, l1.a - l2.a) / cross(l2.b - l2.a, l1.a - l1.b));
template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
   return cross(p - l.a, l.b - l.a) == 0 &&
               min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)
                    (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
}
template < class T>
bool pointInPolygon
    (const Point<T> &a, const vector<Point<T>> &p) {
      int n = p.size();
for (int i = 0; i < n; i++) {</pre>
             if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {
             }
      }
      int t = 0;
for (int i = 0; i < n; i++) {
    auto u = p[i];</pre>
             auto v = p[(i + 1) \% n];
             if (u.x < a.x
                    && v.x >= a.x && pointOnLineLeft(a, Line(v, u))) {
             if (u.x >= a.x
                     && v.x < a.x && pointOnLineLeft(a, Line(u, v))) {
                   t ^= 1;
             }
      }
      return t == 1;
}
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
tuple < int , Point < T > , Point < T >> segmentIntersection
      (const Line<T> &l1, const Line<T> &l2) {
if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x)) {
   return {0, Point<T>(), Point<T>()};
      if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x)) {
    return {0, Point<T>(), Point<T>()};
      if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y)) {
    return {0, Point<T>(), Point<T>()};
      if (min(l1.a.y, l1.b.y) > max(l2.a.y, l
    return {0, Point<T>(), Point<T>()};
      if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
   if (cross(l1.b - l1.a, l2.a - l1.a) != 0) {
      return {0, Point<T>(), Point<T>()};
             } else {
                   auto maxx1 = max(l1.a.x, l1.b.x);
auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
                   auto miny1 = min(l1.a.y, l1.b.y);
auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
                   auto maxy2 = max(l2.a.x, l2.b.x);
auto miny2 = min(l2.a.y, l2.b.y);
Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
if (!pointOnSegment(p1, l1)) {
                          swap(p1.v, p2.v);
                    if (p1 == p2) {
                          return {3, p1, p2};
                   } else {
                          return {2, p1, p2};
            }
      auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
       auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
       if ((cp1 > 0 && cp2 > 0) || (cp1 < 0 && cp2 <
                0) || (cp3 > 0 && cp4 > 0) || (cp3 < 0 && cp4 < 0)) {
```

```
return {0. Point<T>(). Point<T>()}:
     Point p = lineIntersection(l1, l2); if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
          return {1, p, p};
     } else {
    return {3, p, p};
     }
}
template < class T>
double distanceSS(const Line<T> &11, const Line<T> &12) {
   if (get<0>(segmentIntersection(l1, l2)) != 0) {
          return 0.0:
     return min({distancePS(l1.a, l2), distancePS(l1
    .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
template < class T>
bool segmentInPolygon
     (const Line<T> &l, const vector<Point<T>> &p) {
int n = p.size();
if (!pointInPolygon(l.a, p)) {
          return false;
     if (!pointInPolygon(l.b, p)) {
          return false;
     for (int i = 0; i < n; i++) {
          auto u = p[i];
          auto v = p[(i + 1) % n];
auto w = p[(i + 2) % n];
          auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
          if (t == 1) {
               return false;
          if (t == 0) {
               continue;
          if (t == 2) {
               if (pointOnSegment(v, l) && v != l.a && v != l.b) {
   if (cross(v - u, w - v) > 0) {
      return false;
         || pointOnLineLeft(ĺ.b, Line(v, u))) {
               } else if (p1 == v) {
                    if (l.a == v) {
    if (pointOnLineLeft(u, l)) {
                              if (pointOnLineLeft(w, l)
                                  && pointOnLineLeft
                                  (w, Line(u, v))) {
return false;
                        } else {
    if (pointOnLineLeft(w, l)
                                   || pointOnLineLeft
                                  (w, Line(u, v))) {
return false;
                             }
                   } else if (l.b == v) {
   if (pointOnLineLeft(u, Line(l.b, l.a))) {
                              if (pointOnLineLeft(w, Line(l.b, l.a))
                                  && pointOnLineLeft
                                   (w, Line(u, v))) {
return false;
                        || pointOnLineLeft
                                   (w, Line(u, v))) {
return false;
                             }
                    } else {
                         if (pointOnLineLeft(u, l)) {
                              if (pointOnLineLeft(w, Line(l.b, l.a))
                                  || pointOnLineLeft
                                  (w, Line(u, v))) {
return false;
                        } else {
                              if (pointOnLineLeft(w, l)
                                   || pointOnLineLeft
                                   (w, Line(u, v))) {
return false;
                             }
                        }
              }
          }
```

```
}
                                                                                   int main() {
                                                                                        int n; cin >> n;
constexpr i64 inf = 8e18;
vector<Point<i64>> a(n);
template < class T>
vector < Point < T >> hp(vector < Line < T >> lines) {
    sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
    auto d1 = l1.b - l1.a;
    auto d2 = l2.b - l2.a;
                                                                                        for (int i = 0; i < n; i++) cin >> a[i]l
                                                                                        struct sorty {
    bool operator()
          if (sgn(d1) != sgn(d2)) {
                                                                                                  (const Point<i64> &a, const Point<i64> &b) const {
               return sgn(d1) == 1;
                                                                                                  return a.y < b.y;</pre>
                                                                                            }
          return cross(d1, d2) > 0;
                                                                                        struct sortXY {
                                                                                             bool operator()
    });
                                                                                                   (const Point<i64> &a, const Point<i64> &b) const {
     deque<Line<T>> ls;
                                                                                                  return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
     deque<Point<T>> ps;
                                                                                            }
     for (auto l : lines) {
                                                                                        };
          if (ls.empty())
                                                                                        sort(a.begin(), a.end(), sortXY());
               ls.push_back(l);
                                                                                        i64 \text{ ans} = inf;
                                                                                        vector < Point < i64 >> t(n);
               continue:
                                                                                        while (!ps.empty() && !pointOnLineLeft(ps.back(), l)) {
               ps.pop_back();
               ls.pop_back();
                                                                                                            ans = min(ans, distanceSquare(a[i], a[j]));
          }
                                                                                                  sort(a.begin() + l, a.begin() + r + 1, sortY());
          while (!ps.empty() && !pointOnLineLeft(ps[0], l)) {
               ps.pop_front();
               ls.pop_front();
                                                                                             int m = (l + r) >> 1;
int midx = a[m].x;
                                                                                             if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
               if (dot
                                                                                             int tsz = 0;
for (int i = l; i <= r; ++i) {
    if (abs(a[i].x - midx) < ans) {</pre>
                    (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                    if (!pointOnLineLeft(ls.back().a, l)) {
                                                                                                       assert(ls.size() == 1);
                         ls[0] = l;
                    continue;
                                                                                                       t[tsz++] = a[i];
               return {}:
                                                                                            }
                                                                                        devide(devide, 0, n - 1);
cout << ans << "\n";</pre>
          ps.push back(lineIntersection(ls.back(), l));
          ls.push back(l);
                                                                                  10.4 LatticePoints [7750d6]
     while (!ps.emptv() && !pointOnLineLeft(ps.back(), ls[0])) {
          ps.pop_back();
          ls.pop_back();
                                                                                  int main() {
                                                                                        // Polygun 內整數點數
int n; cin >> n;
     if (ls.size() <= 2) {</pre>
                                                                                        vector < Point < i64 >> polygon(n);
                                                                                        for (int i = 0; i < n; i++) cin >> polygon[i];
i64 area = 0;
     ps.push_back(lineIntersection(ls[0], ls.back()));
                                                                                        for (int i = 0; i < n; i++) {</pre>
     return vector(ps.begin(), ps.end());
                                                                                             area += cross(polygon[i], polygon[(i + 1) % n]);
                                                                                        area = abs(area);
using P = Point < i64 >;
                                                                                        auto countBoundaryPoints
                                                                                               = [](const vector<Point<i64>>& polygon) -> i64 {
10.2 Convex Hull [01a63e]
                                                                                             i64 res = 0;
                                                                                             int n = polygon.size();
for (int i = 0; i < n; i++) {
    i64 dx = polygon[(i + 1) % n].x - polygon[i].x;
    i64 dy = polygon((i + 1) % n].y - polygon[i].y;
    i64 dy = polygon((i + 1) % n].y - polygon[i].y;</pre>
int main() {
     int n; cin >> n;
     vector < P > P(n), U, L;
for (int i = 0; i < n; i++) {</pre>
                                                                                                  res += std::gcd(abs(dx), abs(dy));
          cin >> P[i];
         .end(), [](const Point<i64> &a, const Point<i64> &b) {
return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
                                                                                        i64 res = countBoundaryPoints(polygon);
                                                                                        i64 ans = (area - res + 2) / 2;
cout << ans << " " << res << " | n ";
     for (int i = 0; i < n; i++) {
    while (L.size() >= 2 && cross(L.back() -
        L[L.size() - 2], P[i] - L[L.size() - 2]) < 0LL) {</pre>
               L.pop_back();
          while (U.size() >= 2 && cross(U.back()
                  U[U.size() - 2], P[i] - U[U.size() - 2]) > 0LL){
               U.pop_back();
          L.push_back(P[i]);
          U.push_back(P[i]);
    cout << L.size() + U.size() - 2 << "|n";
for (int i = 0; i < L.size() - 1; i++) {
    cout << L[i].x << " " << L[i].y << "|n";</pre>
     for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << "\n";</pre>
    }
```

template < class T> T distanceSquare(const Point<T> %a const Point<T> %b)

10.3 MinEuclideanDistance [e5d775]

```
return square(a - b);
```