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Basic

1.1 Default Code [d41d8c]

```
#include <bits/stdc++.h>
using namespace std;
using ll = long long;
void solve() {
}
int main() {
     ios_base::sync_with_stdio(false);
    cin.tie(nullptr);
     int t = 1;
    cin >> t;
while (t--) {
         solve();
     return 0;
```

1.2 Compare Fuction [d41d8c]

```
|// 1. sort, 二分搜刻在函式內 lambda 就好
 // 2. priority queue 小到大是 >, set 是 <
 // 3. set 不能 = , multiset 必須 =
 // 4. 確保每個成員都要比到
 // 5. pbds_multiset 不要用 lower_bound
 // 6. 如果要用 find, 插入 inf 後使用 upper_bound
 // 7. multiset 可以跟 set 一樣使用, 但請注意第 3、4 點
 auto cmp = [](int i, int j) { return i > j; };
priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
 vector<int> a {1, 2, 5, 4, 3}; // 小心不要改到 a auto cmp = [&a](int i, int j) { return a[i] > a[j]; }; priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
```

1.3 Pbds [d41d8c]

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template <class T>
using pbds_set = tree<T, null_type,
    less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template < class
```

1.4 Double [a94c1c]

```
struct D {
   double x;
     constexpr D() : x{0} {}
constexpr D(double x) : x{x} {}
constexpr static double eps = 1E-12;
explicit operator double() const { return x; }
     constexpr D operator -() const {
   return D(-x);
     constexpr D &operator*=(D rhs) & {
    x *= rhs.x; return *this;
     constexpr D &operator+=(D rhs) & {
          x += rhs.x; return *this;
     constexpr D &operator -= (D rhs) & {
          x -= rhs.x; return *this;
     constexpr D &operator/=(D rhs) & {
          assert(fabs(rhs.x) > eps);
x /= rhs.x; return *this;
     friend constexpr D operator*(D lhs, D rhs) {
    return lhs *= rhs:
      friend constexpr D operator+(D lhs, D rhs) {
          return lhs += rhs;
     friend constexpr D operator-(D lhs, D rhs) {
          return lhs -= rhs;
     friend constexpr D operator/(D lhs, D rhs) {
          return lhs /= rhs;
     friend istream &operator>>(istream &is, D &a) {
          double v; is >> v; a = D(v); return is;
     friend ostream &operator << (ostream &os, const D &a) {</pre>
     friend constexpr bool operator<(D lhs, D rhs) {</pre>
          return lhs.x - rhs.x < -eps;</pre>
     friend constexpr bool operator>(D lhs, D rhs) {
           return lhs.x - rhs.x > eps;
     friend constexpr bool operator==(D lhs, D rhs) {
  return fabs(lhs.x - rhs.x) < eps;</pre>
     friend constexpr bool operator<=(D lhs, D rhs) {
  return lhs < rhs || lhs == rhs;</pre>
     friend constexpr bool operator>=(D lhs, D rhs) {
  return lhs > rhs || lhs == rhs;
     friend constexpr bool operator!=(D lhs, D rhs) {
   return !(lhs == rhs);
```

1.5 Int128 [3c4024]

};

```
using i128 = __int128_t; // 1.7E38
istream &operator>>(istream &is, i128 &a) {
     i128 \text{ sqn} = 1; a = 0;
     string s; is >> s;
     for (auto c : s) {
    if (c == '-') {
              sgn = -1;
         } else {
              a = a * 10 + c - '0';
     a *= sgn;
     return is:
ostream &operator<<(ostream &os, i128 a) {
     string res; int sgn = 1;
if (a < 0) {
         sgn = -1, a = -a;
     while (a) {
         res.push_back(a % 10 + '0');
         a /= 10;
     if (sgn == -1) res.push_back('-');
     reverse(res.begin(), res.end());
```

for (auto x : ans) cout << x + 1 << " ";

```
2.4 Floyd-Warshall [3f61a4]
     cout << res:
     return os;
                                                                                       constexpr ll inf = 1e18;
}
                                                                                       void FloydWarshall(int n, int m) {
   int n, m; cin >> n >> m;
1.6 Rng [401544]
                                                                                            tent 1, w, ctn >> m,
vector < int >> (n, vector < int >(n, inf));
for (int i = 0; i < m; i++) {
   int u, v, w; cin >> u >> v >> w;
   dis[u][v] = min(dis[u][v], w);
   dis[v][u] = min(dis[v][u], w);
}
      (chrono::steady_clock::now().time_since_epoch().count());
ll x = rng(); shuffle(a.begin(), a.end(), rng);
       Graph
                                                                                             for (int i = 0; i < n; i++) dis[i][i] = 0;
2.1 DFS And BFS [e2d856]
                                                                                            int main() {
     int n;
     vector < vector < int >> adj(n);
                                                                                                                   ] = min(dis[i][j], dis[i][k] + dis[k][j]);
     // dfs_graph
vector<bool> vis(n);
                                                                                                       }
     auto dfs = [%](auto self, int u) -> void {
   if (vis[u]) return;
   vis[u] = true;
   for (auto v: adj[u]) {
      self(self, v);
   }
                                                                                                  }
                                                                                       }
                                                                                       const int N = 500; // Floyd 封包
                                                                                       void Floyd(int n, vector<bitset<N>> &dp) {
    for (int k = 0; k < n; k++)
        for (int i = 0; i < n; i++)</pre>
          }
     dfs(dfs, 0);
                                                                                                       if (dp[i][k])
     vector<int> depth(n, 1e9);
                                                                                                            dp[i] |= dp[k];
     queue<int> q;
auto bfs = [&](auto self, int s) -> void {
    vis[s] = true, depth[s] = 0;
                                                                                       2.5 Euler [4177dc]
          q.push(s);
                                                                                      // 1. 無向圖是歐拉圖:
          while (!q.empty()) {
               int u = q.front(); q.pop();
for (auto v : adj[u]) {
    if (vis[v]) continue;
    vis[v] = true;
    depth[v] = depth[u] + 1;
                                                                                      | // 非零度頂點是連通的
                                                                                      // 頂點的度數都是偶數
                                                                                      | // 2. 無向圖是半歐拉圖(有路沒有環):
                                                                                      // 非零度頂點是連通的
                     q.push(v);
               }
                                                                                       // 恰有 2 個奇度頂點
          }
                                                                                       // 3. 有向圖是歐拉圖:
     bfs(bfs, 0);
                                                                                       // 非零度頂點是強連通的
                                                                                       // 每個頂點的入度和出度相等
2.2 Prim [3a3805]
                                                                                       // 4. 有向圖是半歐拉圖(有路沒有環):
auto prim =
                                                                                      | // 非零度頂點是弱連通的
     [&](int n, vector<vector<pair<int, int>>> &adj) -> bool {
int node_sz = 0;
                                                                                       // 至多一個頂點的出度與入度之差為 1
     vector<pair<int, int>,
    vector<pair<int, int>>, greater<pair<int, int>>> pq;
pq.emplace(0, 0); // w, vertex
vector <bool> vis(n);
while (log control);
     priority_queue<pair<int, int>,
                                                                                      // 至多一個頂點的入度與出度之差為 1
                                                                                       // 其他頂點的入度和出度相等
                                                                                       vector<int> ans;
                                                                                       auto dfs = [&](auto &&self, int u) -> void {
     while (!pq.empty()) {
                                                                                            while (g[u].size()) {
   int v = *g[u].begin();
          auto [u, w] = pq.top(); pq.pop();
if (vis[u]) continue;
                                                                                                  g[u].erase(v);
          vis[u] = true;
                                                                                                  self(self, v);
          node_sz++;
for (auto v : adj[u]) {
                                                                                             ans.push_back(u);
               if (!vis[v.first])
                     pq.emplace(v.second, v.first);
                                                                                       dfs(dfs, 0);
                                                                                       reverse(ans.begin(), ans.end());
                                                                                       2.6 DSU [749620]
     if (node_sz == n) return true;
                                                                                       struct DSU {
};
                                                                                             vector<int> boss, siz;
2.3 Bellman-Ford [430ded]
                                                                                            DSU() {}
DSU(int n_) { init(n_); }
   用 Bellman Ford 找負環
                                                                                             void init(int n_) {
    n = n_; boss.resize(n);
int main() {
     int n, m; cin >> n >> m;
vector<array<int, 3>> e;
for (int i = 0; i < m; i++) {</pre>
                                                                                                  iota(boss.begin(), boss.end(), 0);
                                                                                                  siz.assign(n, 1);
          int u, v, w; cin >> u >> v >> w
                                                                                            int find(int x) {
   if (boss[x] == x) return x;
   return boss[x] = find(boss[x]);
          u--, v--; e.push_back({u, v, w});
     bool same(int x, int y) {
    return find(x) == find(y);
                                                                                            bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);</pre>
                     if (i == n) t = v;
               }
                                                                                                              siz[y];
          }
                                                                                                  boss[y] = x;
     if (t == -1) { cout << "NO\n"; return; }
for (int i = 1; i < n; i++) t = par[t];</pre>
     vector < int > ans {t};
                                                                                             int size(int x) {
    return siz[find(x)];
     int i = t;
     }
                                                                                       };
          ans.push_back(i);
     } white (i != t);
reverse(ans.begin(), ans.end());
cout << "YES\n";</pre>
                                                                                       struct DSU {
```

vector<int> boss. siz. stk:

DSU(int n_) { init(n_); }

DSU() {}

```
void init(int n_) {
             n = n_;
              boss.resize(n);
             iota(boss.begin(), boss.end(), 0);
siz.assign(n, 1);
              stk.clear();
      int find(int x) {
   return x == boss[x] ? x : find(boss[x]);
      bool same(int x, int y) {
    return find(x) == find(y);
      bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);
    siz[x] += siz[y];
    boss[y] = x;
}</pre>
             n - -;
             stk.push_back(y);
       void undo(int x) {
   while (stk.size() > x) {
                   int y = stk.back();
                    stk.pop_back();
                     siz[boss[y]] -= siz[y];
                    boss[y] = y;
             }
      int size(int x) {
    return siz[find(x)];
};
```

2.7 SCC [5d3e16]

```
struct SCC {
     int n, cur, cnt;
     vector < int >> adj;
     vector <int> stk, dfn, low, bel;
SCC(int n_ = 0) { init(n_); }
void init(int n_) {
          n = n_;
adj.assign(n, {});
          dfn.assign(n, -1);
low.resize(n);
          bel.assign(n, -1);
stk.clear();
           cur = cnt = 0;
     void addEdge(int u, int v) {
          adj[u].push_back(v);
     void dfs(int x) {
    dfn[x] = low[x] = cur++;
           stk.push_back(x);
           for (auto y : adj[x]) {
   if (dfn[y] == -1) {
                     dfs(y);
                low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
                     low[x] = min(low[x], dfn[y]);
                }
           if (dfn[x] == low[x]) {
                int y;
                do {
                     y = stk.back();
                bel[y] = cnt;
stk.pop_back();
while (y != x);
          }
     vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
           return bel;
     struct Graph {
          vector<pair<int, int>> edges;
           vector<int> siz;
           vector<int> cnte;
     Graph compress() {
          Graph g;
g.n = cnt;
g.siz.resize(cnt);
           g.cnte.resize(cnt);
          g.edges.emplace_back(bel[i], bel[j]);
                     } else {
                          g.cnte[bel[i]]++;
```

```
}
         return g;
    }
};
```

2.8 VBCC [ee1554]

```
struct VBCC {
                int n, cur, cnt;
vector<vector<int>> adj;
vector<vector<int>> bcc;
                vector<int> stk, dfn, low;
                vector < bool > ap;
VBCC(int n_ = 0) { init(n_); }
void init(int n_) {
                             n = n_;
adj.assign(n, {});
bcc.assign(n, {});
                               dfn.assign(n, -1);
                               low.resize(n);
                               ap.assign(n, false);
stk.clear();
                              cur = cnt = 0:
                void addEdge(int u, int v) {
                             adj[u].push_back(v);
adj[v].push_back(u);
                void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
    stk.push_back(x);
                               int child = 0;
                              for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
        dfs(y, x), child++;
        low[x] = min(low[x], low[y]);
        continue;
        low[x] = min(low[x], low[y]);
        continue;
        low[x] = min(low[x], low[y]);
        continue;
        low[x] = min(low[x], low[y]);
        low[x] = min(low[x], low[x], low[y]);
        low[x] = min(low[x], low[x], low[x], low[x]);
        low[x] = min(low[x], low[x], lo
                                                             if (low[y] >= dfn[x]) {
                                                                           int v;
do {
    v = stk.back();
                                                                                           bcc[v].push_back(cnt);
                                                                            stk.pop_back();
} while (v != y);
                                                                             bcc[x].push_back(cnt);
                                                                           cnt++:
                                                            if (low[y] >= dfn[x] && p != -1) {
    ap[x] = true;
                                                            }
                                             } else {
                                                            low[x] = min(low[x], dfn[y]);
                                             }
                               if (p == -1 && child > 1) {
    ap[x] = true;
               fvector < bool > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
            }
}</pre>
                                             }
                               return ap;
                struct Graph {
                               int n;
                              vector<pair<int, int>> edges;
vector<int> bel;
vector<int> siz; // BCC 內節點數
                               vector<int> cnte; // BCC 內邊數
                Graph compress() {
                             Graph g; // 壓完是一棵樹,但不一定每個 bel 都有節點 g.bel.resize(n);
                               g.siz.resize(cnt)
                              g.cnte.resize(cnt);
for (int u = 0; u < n; u++) {
    if (ap[u]) {
        g.bel[u] = cnt++;
    }
}</pre>
                                                            g.siz.emplace_back();
g.cnte.emplace_back();
                                                             for (auto v : bcc[u]) {
                                                                           g.edges.emplace_back(g.bel[u], v);
                                             } else if (bcc[u].size() == 1) {
   g.bel[u] = bcc[u][0];
                                             g.siz[g.bel[u]]++;

}
g.n = cnt;
for (int i = 0; i < n; i++) {
    for (auto j : adj[i]) {
        if (g.bel[i] == g.bel[j] && i < j) {
            g.cnte[g.bel[i]]++;
        }
}
</pre>
                                             }
                               return g;
```

```
2.9 EBCC [59d8ca]
```

| };

```
struct EBCC { // CF/contest/1986/pF
  int n, cur, cnt;
  vector<vector<int>> adj;
              vector<int> stk, dfn, low, bel;
             vector  vect
                           adj.assign(n, {});
                           dfn.assign(n, -1);
                           low.resize(n);
                           bel.assign(n, -1);
                           stk.clear();
bridges.clear();
cur = cnt = 0;
             void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
             void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
                           stk.push_back(x);
                           for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
                                                     dfs(y, x);
low[x] = min(low[x], low[y]);
if (low[y] > dfn[x]) {
                                                                  bridges.emplace_back(x, y);
                                       } else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
                           if (dfn[x] == low[x]) {
                                        int y;
do {
    y = stk.back();
                                                     bel[y] = cnt;
stk.pop_back();
                                        } while (y != x);
                                        cnt++;
                          }
             vector < int > work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
        }
}</pre>
                                       }
                           return bel;
              struct Graph {
                           vector<pair<int, int>> edges;
                           vector<int> siz; // BCC 內節點數
                           vector<int> cnte; // BCC 內邊數
             Graph compress() {
                          Graph g;
g.n = cnt;
                           g.siz.resize(cnt);
                           g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;</pre>
                                        g.stc[vet[t]]++;
for (auto j : adj[i]) {
    if (bel[i] < bel[j]) {
        g.edges.emplace_back(bel[i], bel[j]);
    } else if (i < j) {
        g.cnte[bel[i]]++;
}</pre>
                                       }
                           return g;
            }
};
```

2.10 2-SAT [3f3604]

```
int now = 0, cnt = 0;
function < void(int) > tarjan = [&](int u) {
                 stk.push_back(u);
                 dfn[u] = low[u] = now++;
for (auto v : e[u]) {
                      if (dfn[v] ==
                            tarjan(v);
                      low[u] = min(low[u], low[v]);

else if (id[v] == -1) { // in s
low[u] = min(low[u], dfn[v]);
                 }
if (dfn[u] == low[u]) {
                       int v;
                       do {
                            v = stk.back();
                      stk.pop_back();
id[v] = cnt;
} while (v != u);
                       ++cnt;
                }
           for (int i
           return true;
     vector < bool > answer() { return ans; }
int main() {
     int m, n; cin >> m >> n;
TwoSat ts(n);
     for (int i = 0; i < m; ++i) {</pre>
           int u, v; char x, y;
cin >> x >> u >> y >> v;
ts.addClause(u - 1, x == '+', v - 1, y == '+');
     if (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";
}</pre>
      else cout << "IMPOSSIBLE\n";</pre>
```

2.11 Funtional Graph [e8fd64]

```
constexpr int N = 2E5 + 5;
 int cht[N][31]; // 倍增表, 放外面不然 TLE struct FuntionalGraph {
         int n, cnt;
vector<int> g, bel, id, len, in, top;
FuntionalGraph() : n(0) {}
FuntionalGraph(vector<int> g_) { init(g_); }
          void init(vector<int> g_) {
               n = g_.size(); cnt = 0;

g = g_; bel.assign(n, -1);

id.resize(n); len.clear();

in.assign(n, 0); top.assign(n, -1);
                 build():
          void build() {
    for (int i = 0; i < n; i++) {
        cht[i][0] = g[i];
        reliver.</pre>
                          in[g[i]]++;
                 for (int i = 1; i <= 30; i++)
    for (int u = 0; u < n; u++)
        cht[u][i] = cht[cht[u][i - 1]][i - 1];
for (int i = 0; i < n; i++)
    if (in[i] == 0) label(i);</pre>
                 for (int i = 0; i < n; i++)
if (top[i] == -1) label(i);
          void label(int u) {
                 vector<int> p; int cur = u;
while (top[cur] == -1) {
   top[cur] = u;
                          p.push_back(cur);
                          cur = g[cur];
                  auto s = find(p.begin(), p.end(), cur);
                 auto s = rinu(p.begin(), p.end(), cor,
vector <int> cyc(s, p.end());
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {
    bel[cyc[i]] = cnt;
}</pre>
                          id[cyc[i]] = i;
                 id[p[i - 1]] = id[p[i]] - 1;
          int jump(int u, int k) {
   for (int b = 0; k > 0; b++){
      if (k & 1) u = cht[u][b];
}
                         k >>= 1:
                 return u:
```

```
}
|}:
```

3 Data Structure

3.1 BIT [d41d8c]

```
template < typename T >
struct Fenwick { // 全部以 0 based 使用
  int n; vector<T> a;
  Fenwick(int n_ = 0) { init(n_); }
  void init(int n_) {
            n = n_;
a.assign(n, T{});
       void add(int x, const T &v) {
    for (int i = x + 1; i <= n; i += i & -i) {
        a[i - 1] = a[i - 1] + v;
}</pre>
       }
      T sum(int x) { // 左閉右開查詢
T ans{};
for (int i = x; i > 0; i -= i & -i) {
    ans = ans + a[i - 1];
             return ans;
       TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
       int select(const T &k, int start = 0) {
             cur = cur + a[x - 1];
                   }
             return x;
      }
 template < class T>
 struct TwoDFenwick { // 全部以 0 based 使用
      int nx, ny; // row, col 個數
vector<vector<T>> a;
TwoDFenwick(int nx_ = 0, int ny_ = 0) {
  init(nx_, ny_);
       void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;

             a.assign(nx, vector<T>(ny, T{}));
       for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        a[i - 1][j - 1] = a[i - 1][j - 1] + v;
}</pre>
             }
       T sum(int x, int y) { // 左閉右開查詢
    T ans{};
    for (int i = x; i > 0; i -= i & -i) {
                   for (int j = y; j > 0; j -= j & -j) {
    ans = ans + a[i - 1][j - 1];
             return ans:
      }
T rangeSum
              (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                    (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
};
```

3.2 RangeBit [d41d8c]

```
| template < class T > | struct range Fenwick { // 全部以 0 based 使用 int n; vector < T > d, di; range Fenwick (int n_ = 0) { init(n_); } void init(int n_) { n = n_; d.assign(n, T{}); di.assign(n, T{}); di.assign(n, T{}); } void add(int x, const T &v) { T vi = v * (x + 1); for (int i = x + 1; i <= n; i += i & -i) { d[i - 1] = d[i - 1] + v; di[i - 1] = di[i - 1] + v; } } void range Add(int l, int r, const T &v) { add(l, v); add(r, -v); } T sum(int x) { // 左閉右開查詢
```

```
T ans{};
               for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
               return ans;
       }
       T rangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
        int select(const T &k, int start = 0) {
              if (cur + val <= k) {</pre>
                                     x += i;
                                      cur = cur + val;
                      }
               return x:
       }
template < class T>
struct rangeTwoDFenwick { // 全部以 0 based 使用
        int nx, ny; // row, col 個數
vector < vector < T >> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
                init(nx_, ny_);

void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
}

       }
void add(int x, int y, const T &v) {
    T vi = v * (x + 1);
    T vj = v * (y + 1);
    T vij = v * (y + 1);
    T vij = v * (x + 1) * (y + 1);
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            d[i - 1][j - 1] = d[i - 1][j - 1] + v;
            di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
            dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
            dii[i - 1][j - 1] = dij[i - 1][j - 1] + vi</pre>
                              dij[i - 1][j - 1] = dij[i -
                                                                                              1] + vij;
                      }
               }
        void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
               add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
        T sum(int x, int y) { // 左閉右開查詢
               T`ans{};
               for (int i = x; i > 0; i -= i & -i) {
   for (int j = y; j > 0; j -= j & -j) {
      ans = ans
                              }
                return ans;
        T rangeSum
                (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                return sum(
                        rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
1:
```

3.3 Segment Tree [d41d8c]

```
int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                 pull(p);
            build(1, 0, n);
     void pull(int p) {
   info[p] = info[p * 2] + info[p * 2 + 1];
      void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
      info[p] = v; return;
}
           int m = (l + r) / 2;
if (x < m) modify(2 * p, l, m, x, v);
else modify(2 * p + 1, m, r, x, v);</pre>
           pull(p);
      void modify(int p, const Info &i) {
           modify(1, 0, n, p, i);
     Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];</pre>
           int m = (l + r) / 2;
return query(p *
                 2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
      template < class F> // 尋找區間內,第一個符合條件的
      int findFirst
           (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)
    return -1;</pre>
            if (l >= x && r <= y && !pred(info[p]))</pre>
           return -1;
if (r - l == 1)
           return l;
int m = (l + r) / 2;
int res = findFirst(2 * p, l, m, x, y, pred);
            if (res == -1)
                 res = findFirst(2 * p + 1, m, r, x, y, pred);
            return res;
     template < class F> // 若要找 last, 先右子樹遞迴即可int findFirst(int l, int r, F & pred) {
           return findFirst(1, 0, n, l, r, pred);
}:
struct Info {
   int n = 0;
      int sum = 0;
Info operator+(const Info &a, const Info &b) {
      return { a.n + b.n, a.sum + b.sum };
}
3.4 Lazy Segment Tree [d41d8c]
```

```
template < class Info, class Tag>
struct LazySeg { // 左閉右開寫法
    int n;
vector < Info > info;
    template < class T>
     LazySeg(vector<T> init_) {
          init(init_);
    void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
     template < class T>
     void init (vector<T> init_) {
          n = init_.size();
          info.assign(4 << __lg(n), Info());
tag.assign(4 << __lg(n), Tag());
function <void(
               int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
                    info[p] = init_[l];
                    return;
               int m = (l + r) / 2;
               build(p * 2, l, m);
build(p * 2 + 1, m, r);
               pull(p);
          build(1, 0, n);
     void pull
     (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
          tag[p].apply(v);
```

```
void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
            tag[p] = Tag();
      void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
                  info[p] = v;
                  return;
            int m = (l + r) / 2;
            push(p, l, r);
if (x < m) {
    modify(2 * p, l, m, x, v);</pre>
                 modify(2 * p + 1, m, r, x, v);
            pull(p);
      void modify(int p, const Info &i) {
    modify(1, 0, n, p, i);
      Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l | | ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    push(p, l, r);
    return query(p *</pre>
                   2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      Ínfo query
             (int ql, int qr) { return query(1, 0, n, ql, qr); }
      apply(p, l, r, v);
            fint m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
pull(p);
      void range_apply(int l, int r, const Tag &v) {
    range_apply(1, 0, n, l, r, v);
      template < class F> // 尋找區間內,第一個符合條件的
      int findFirst
            (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
   return -1;</pre>
            if (l >= x && r <= y && !pred(info[p])) {</pre>
                  return -1:
            if (r - l == 1) {
                  return l;
            int m = (l + r) / 2;
            push(p);
             int res = findFirst(2 * p, l, m, x, y, pred);
            if (res == -1) {
    res = findFirst(2 * p + 1, m, r, x, y, pred);
            return res:
      template < class F> // 若要找 last, 先右子樹遞迴即可
int findFirst(int l, int r, F & & pred) {
    return findFirst(1, 0, n, l, r, pred);
};
struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add; void apply(const Tag& v) {
            if (v.set_val) {
                  set_val = v.set_val;
add = v.add;
            else {
                  add += v.add;
     }
};
struct Info {
      int sum;
void apply(int l, int r, const Tag &v) {
            if (v.set_val) {
    sum = (r - l) * v.set_val;
            sum += (r - l) * v.add;
      // Info& operator=(const Info &rhs) {
               // 部分 assignment 使用
return *this;
```

```
};
Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
}

3.5 Persistent Segment Tree [d41d8c]

template<class Info>
```

```
template < class Info >
struct PST {
    struct Node {
             Info info = Info();
              int lc = 0, rc = 0;
       vector<Node> nd;
       int n = 0; vector<int> rt;
PST() : n(0) {}
       PST((): N(0) {}
PST((int n_, Info v_ = Info()) { init(n_, v_); }
template < class T >
PST(vector < T > init_) { init(init_); }
void init(int n_, Info v_ = Info()) {
   init(vector < Info > (n_, v_));
}
       template < class T>
       void init(vector<T> init_) {
              n = init_.size();
nd.clear(); rt.clear();
              nd.emplace_back(); // 讓 root 指向 1-based rt.push_back(build(0, n, init_));
       int build(int l, int r, vector<Info> &init_) {
  int id = nd.size();
              nd.emplace_back();
if (r - l == 1) {
    nd[id].info = init_[l];
                     return id;
              int m = (l + r) >> 1;
nd[id].lc = build(l, m, init_);
nd[id].rc = build(m, r, init_);
              pull(nd[id]);
              return id;
       void pull(Node &t) {
   t.info = nd[t.lc].info + nd[t.rc].info;
       int copy(int t) { // copy 一個 node
   nd.push_back(nd[t]);
              return nd.size() - 1;
       int generate() { // 創立新的 node
nd.emplace_back();
return nd.size() - 1;
       fint modify(int t, int l, int r, int x, const Info &v) {
    t = t ? copy(t) : generate();
    if (r - l == 1) {
        nd[t].info = v;
    }
}
                     return t;
              int m = (l + r) >> 1;
if (x < m) {
                     nd[t].lc = modify(nd[t].lc, l, m, x, v);
              } else
                     nd[t].rc = modify(nd[t].rc, m, r, x, v);
              pull(nd[t]);
              return t:
       void modify(int ver, int pos, const Info &val) {
   if (int(rt.size()) <= ver) rt.resize(ver + 1);
   rt[ver] = modify(rt[ver], 0, n, pos, val);</pre>
       info query(int t, int l, int r, int ql, int qr) {
    if (l >= qr || r <= ql) return Info();
    if (ql <= l && r <= qr) return nd[t].info;</pre>
              int m = (l + r) >> 1;
              return query(nd[t].
                      lc, l, m, ql, qr) + query(nd[t].rc, m, r, ql, qr);
       Info query(int ver, int ql, int qr) {
    return query(rt[ver], 0, n, ql, qr);
       void createVersion(int ori_ver) {
    rt.push_back(copy(rt[ori_ver]));
       void reserve(int n, int q) {
   nd.reserve(n + q * (2 * __lg(n) + 1));
   rt.reserve(q + 1);
       void resize(int n) {
             rt.resize(n);
struct Info {
   int sum = 0;
Info operator+(const Info &a, const Info &b) {
       return { a.sum + b.sum };
```

```
struct Treap {
   Treap *lc, *rc;
      Ireap *lc, *rc;
int pri, siz; bool rev_valid;
int val; int min;
Treap(int val_) {
    min = val = val_;
    pri = rand();
    lc = rc = nullptr;
    siz = 1; rev_valid = 0;
       void pull() { // update siz or other information
             min = val;
             for (auto c : {lc, rc}) {
    if (!c) continue;
                    siz += c->siz;
                    min = std::min(min, c->min);
             }
       void push() {
             if (rev_valid) {
   swap(lc, rc);
   if (lc) lc->rev_valid ^= 1;
   if (rc) rc->rev_valid ^= 1;
              rev_valid = false;
       int find(int k) { // 找到 min 是 k 的位置 (1-based)
             push();
int ls = (lc ? lc->siz : 0) + 1;
             if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
int size(Treap *t) {
    return t ? t->siz : 0;
Treap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
    a->push(); b->push();
    if (a->pri > b->pri) {
        a -> c = merge(a->rc, b);
        a -> c = merge(a -> c, b);
    }
}
             a->pull();
             return a:
       else {
             b->lc = merge(a, b->lc);
b->pull();
      }
pair<Treap*, Treap*> split(Treap *t, int k) {
       // 分割前 k 個在 first, 剩下的在 second if (t == nullptr) return {nullptr, nullptr};
       t->push();
       if (size(t->lc) < k) {
    auto [a, b] = split(t->rc, k - size(t->lc) - 1);
    t->rc = a;
             t->pull();
             return {t, b};
       else {
             auto [a, b] = split(t->lc, k);
t->lc = b;
             t->pull();
             return {a, t};
      }
void Print(Treap *t) {
      if (!t) return;
t->push();
       Print(t->lc);
      cout << t->val;
Print(t->rc);
3.7 RMQ [d41d8c]
template < class T, class Cmp = less < T >>
```

```
template < class T, class Cmp = less < T>>
struct RMQ {
    const Cmp cmp = Cmp();
    static constexpr unsigned B = 64;
    using u64 = unsigned long long;
    int n;
    vector < T>> a;
    vector < T> pre, suf, ini;
    vector < G> stk;
    RMQ() {}
    RMQ(const vector < T> &v) { init(v); }
    void init(const vector < T> &v) {
        n = v.size();
        pre = suf = ini = v;
        stk.resize(n);
        if (!n) {
            return;
        }
        const int M = (n - 1) / B + 1;
        const int lg = __lg(M);
        a.assign(lg + 1, vector < T>(M));
        for (int i = 0; i < M; i++) {
            a[0][i] = v[i * B];
        }
}</pre>
```

3.6 Treap [d41d8c]

```
for (int j = 1; j < B && i * B + j < n; j++) { a[0][i] = min(a[0][i], v[i * B + j], cmp);
          for (int i = 1; i < n; i++) {</pre>
               if (i % B) {
    pre[i] = min(pre[i], pre[i - 1], cmp);
          for (int i = n - 2; i >= 0; i--) {
   if (i % B != B - 1) {
                    suf[i] = min(suf[i], suf[i + 1], cmp);
          ] = min(a[j][i], a[j][i + (1 << j)], cmp);
          for (int i = 0; i < M; i++) {
    const int l = i * B;</pre>
              const int r = nin(1U * n, l + B);
u64 s = 0;
for (int j = l; j < r; j++) {
   while (s && cmp(v[j], v[__lg(s) + l])) {
      s ^= 1ULL << __lg(s);
}</pre>
                    s |= 1ULL << (j - l);
                    stk[j] = s;
              }
          }
     ({ans, a[k][l], a[k][r - (1 << k)]}, cmp);
               return ans:
          } else {
               int x = B * (l / B);
              return ini
  [__builtin_ctzll(stk[r - 1] >> (l - x)) + l];
     }
};
```

3.8 Mo [d41d8c]

4 Flow Matching

4.1 Dinic [d41d8c]

```
// 偶數 id 是正向邊
                  edges.push_back({v, 0, cap});
edges.push_back({u, 0, 0});
                  adj[u].push_back(m++);
adj[v].push_back(m++);
         bool bfs() {
    fill(dis.begin(), dis.end(), -1);
                  dis[s] = 0; queue < int > q;
q.push(s);
                  while (!q.empty() && dis[t] == -1) {
   int u = q.front(); q.pop();
   for (int id : adj[u]) {
     Edge &e = edges[id];
     if (e.flow == e.cap) continue;
                                    if (dis[e.to] == -1) {
    dis[e.to] = dis[u] + 1;
    q.push(e.to);
                           }
                   return dis[t] != -1;
         }
T dfs(int u, T flow) {
   if (flow == 0) return 0;
   if (u == t) return flow;
   for (int &cur = ptr[u]; cur < adj[u].size(); cur++) {
      Edge &e = edges[adj[u][cur]];
      if (dis[u] + 1 != dis[e.to]) continue;
      if (e.cap == e.flow) continue;
      T mn = dfs(e.to, min(flow, e.cap - e.flow));
      if (mn > 0) {
                            if (mn > 0) {
                                    e.flow += mn;
edges[adj[u][cur] ^ 1].flow -= mn;
                                     return mn:
                           }
                  }
                   return 0; // 到不了終點就會 return 0
         T work(int s_, int t_) {
    s = s_; t = t_; T flow = 0;
    while (bfs()) {
        fill(ptr.begin(), ptr.end(), 0);
    }
}
                            while (true) {
   T res = dfs(s, INF_Flow);
   if (res == 0) break;
                           }
                  return flow;
         void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
};
```

4.2 Min Cut [d41d8c]

```
// CSES Police Chase
int main(){
        int n, m; cin >> n >> m;
Dinic < int >> g(n);
for (int i = 0; i < m; i++) {
    int u, v, cap = 1;
    cin >> u >> v;
                  u--; v--;
                  g.add_edge(u, v, cap);
                  g.add_edge(v, u, cap);
         int res = g.work(0, n - 1);

cout << res << "\n";

if (res == 0) return;
         vector < int > vis(n);
auto find = [&](auto self, int u) -> void {
    if (!vis[u]) {
       vis[u] = 1;
}
                           for (int id : g.adj[u]) {
    auto e = g.edges[id];
    if (e.cap - e.flow > 0) {
                                              self(self, e.to);
                          }
                 }
        };
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
        acedes[id];
}</pre>
                            auto e = g.edges[id];
                           if (!vis[e.to]) {
    cout << i + 1 << " " << e.to + 1 << " \n";
                 }
        }
```

4.3 MCMF [d41d8c]

```
template < class Tf, class Tc>
struct MCMF {
```

```
struct Edge {
     int to;
     Tf flow, cap; // 流量跟容量
int n, m, s, t;
const Tf INF_FLOW = 1 << 30;</pre>
const Tc INF_COST = 1 << 30;</pre>
vector<vector<int>> adj;
vector<Edge> edges; // 幫每個 edge 編號
vector<Tc> dis, pot; // johnson algorithm, using spfa
vector < int > rt; // 路徑恢復,對應 id
vector < bool > inq;
MCMF(int n_ = 0) { init(n_); }
void init(int n_)
     n = n_; m = 0;
edges.clear();
     adj.assign(n, {});
void add_edge(int u, int v, Tf cap, Tc cost){
  edges.push_back({v, 0, cap, cost});
  edges.push_back({u, 0, 0, -cost});
  adj[u].push_back(m++);
  adj[v].push_back(m++);
bool spfa() {
     dis.assign(n, INF_COST);
rt.assign(n, -1); inq.assign(n, false);
     queue < int > q;
q.push(s), dis[s] = 0, inq[s] = true;
     while (!q.empty()) {
          dis[v] = ndis; rt[v] = id;
if (!inq[v]) {
    q.push(v); inq[v] = true;
               }
         }
     return dis[t] != INF_COST;
bool dijkstra() {
     dis.assign(n, INF_COST); rt.assign(n, -1);
priority_queue<pair<Tc, int>,
    vector<pair<Tc, int>>, greater<pair<Tc, int>>> pq;
     dis[s] = 0; pq.emplace(dis[s], s);
while (!pq.empty()) {
         pq.emplace(ndis, v);
         }
     return dis[t] != INF_COST;
dis[i] += pot[i] - pot[s];
          Tf f = INF_FLOW;
          for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
              f = min
                     (f, edges[rt[i]].cap - edges[rt[i]].flow);
          f = min<Tf>(f, need);
          for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
          flow += f; need -= f;
cost += f * dis[t]; fr = false;
          swap(dis, pot);
if (need == 0) break;
     return {flow, cost};
dis[i] += pot[i] - pot[s];
          Tf f = INF_FLOW;
          for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
```

4.4 Hungarian [d41d8c]

```
struct Hungarian { // 0-based, O(VE)
        int n, m;
vector < vector < int >> adj;
        vector <int> used, vis;
vector <pair <int, int>> match;
Hungarian(int n = 0, int m = 0) {
                init(n_, m_);
        void init(int n_, int m_) {
    n = n_; m = m_;
    adj.assign(n + m, {});
    used.assign(n + m, -1);
                vis.assign(n + m, 0);
        void addEdge(int u, int v) {
   adj[u].push_back(n + v);
   adj[n + v].push_back(u);
        bool dfs(int u) {
   int sz = adj[u].size();
                for (int i = 0; i < sz; i++) {
   int v = adj[u][i];
   if (vis[v] == 0) {
      vis[v] = 1;
      vis[v] = 1;
}</pre>
                               if (used[v] == -1 || dfs(used[v])) {
    used[v] = u;
                               }
                       }
                return false;
         vector<pair<int, int>> work() {
                match.clear(); used.assign(n + m, -1);
vis.assign(n + m, 0);
for (int i = 0; i < n; i++) {</pre>
                       fill(vis.begin(), vis.end(), 0); dfs(i);
                for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
                               match.emplace_back(used[i], i - n);
                return match;
};
```

4.5 Theorem [d41d8c]

```
// 有向無環圖:
// 最小不相交路徑覆蓋:
// 最小路徑數 = 頂點數 - 最大匹配數
1// 最小相交路徑覆蓋:
| // 先用
   Floyd 求傳遞封包,有連邊就建邊,然後再套最小不相交路徑覆蓋
// 二分圖:
// 最小點
   覆蓋: 選出一些點,讓所有邊至少有一個端點在點集中的最少數量
// 最小點覆蓋 = 最大匹配數
// 還原解, flow 的作法是從源點開始 dfs, 只走 cap - flow > 0
// 的邊,最後挑選左邊還沒被跑過的點和右邊被跑過的點當作覆蓋的點
// 最少邊覆蓋: 選出一些邊,讓所有點都覆蓋到的最少數量
// 最少邊覆蓋 = 點數 - 最大匹配數
1// 最大獨立集: 選出一些點, 使這些點兩兩沒有邊連接的最大數量
| // 最大獨立集 = 點數 - 最大匹配數
```

5 String 5.1 Hash [852711]

```
constexpr int B = 59;
vector<Z> Hash(string &s) {
    vector<Z> ans {0};
    for (auto c : s) {
        ans.push_back(ans.back() * B + (c - 'a' + 1));
    }
    return ans;
}

void solve() {
    string s, sub;
    cin >> s >> sub;
    auto a = Hash(s);
    auto find = q.back();
    int ans = 0;
    int l = 1, r = sub.size(), len = sub.size();
    while (r <= s.size()) {
        if (a[r] - a[l - 1] * power(Z(B), len) == find) {
            ans++;
        }
        l++, r++;
    }
    cout << ans << "\n";
}

5.2 KMP [00726d]</pre>
```

```
struct KMP {
         string sub;
         vector<int> fail;
          // fail 存匹配失敗時,移去哪,也就是最長共同前後綴長度
         KMP(const string &sub_) {
   build(sub_);
        void build(const string &sub_) {
    sub = sub_, fail.resize(sub.size(), -1);
    for (int i = 1; i < sub.size(); i++) {
        int now = fail[i - 1];
        while (now != -1 && sub[now + 1] != sub[i])
            now = fail[now];
        if (subleace = 1) = sub[i]) fail[i] = now be</pre>
                          if (sub[now + 1] == sub[i]) fail[i] = now + 1;
                 }
         vector<int> match(string &s) {
                 rector < int > match;

for (int i = 0, now = -1; i < s.size(); i++) {
    // now 是成功匹配的長度 -1
    while (s[i] != sub[now + 1] && now != -1)
        now = fail[now];
                          if (s[i] == sub[now + 1]) now++;
if (now + 1 == sub.size()) {
   match.push_back(i - now);
                                   now = fail[now];
                          }
                  return match;
        }
};
```

5.3 Z Function [764b31]

```
|// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
|// 的最長公共前綴 (LCP) 的長度
vector cint > Z(string s) {
    int n = s.size();
    vector cint > z(n); z[0] = n;
    for (int i = 1, j = 1; i < n; i++) {
        z[i] = max(0, min(j + z[j] - i, z[i - j]));
        while (i + z[i] < n && s[z[i]] == s[i + z[i]])
        z[i]++;
        if (i + z[i] > j + z[j]) j = i;
    }
    return z; // 最後一格不算
```

5.4 Manacher [9c9ca6]

```
// 1 2 1 4 1 2 1
// # a # b # b # a #
// 1 2 1 2 5 2 1 2 1
// 值 -1 代表原回文字串長度
// (id - val + 1) / 2 可得原字串回文開頭
```

5.5 Trie [31e4ff]

```
constexpr int N = 1E7;
int tot = 0;
int trie[N][26], cnt[N];
void reset() {
    tot = 0, fill_n(trie[0], 26, 0);
int newNode() {
     int x = ++tot;
cnt[x] = 0, fill_n(trie[x], 26, 0);
     return x;
void add(string &s) {
     int p = 0;
for (auto c : s) {
    int &q = trie[p][c - 'a'];
          if (!q) q = newNode();
          p = q;
     cnt[p] += 1;
int find(string &s) {
     int p = 0;
for (auto c : s) {
          int q = trie[p][c - 'a'];
          if (!q) return 0;
          p = q;
     return cnt[p];
```

5.6 SA [b58946]

```
struct SuffixArrav {
      int n; string s;
vector<int> sa, rk, lc;
      // n: 字串長度
      // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置 // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名 // lc: LCP
      數組,lc[i] 表示 sa[i] 和 sa[i + 1] 的最長公共前綴長度
SuffixArray(const string &s_) {
   s = s_; n = s.length();
             sa.resize(n);
            lc.resize(n - 1);
             rk.resize(n):
             iota(sa.begin(), sa.end(), 0);
            sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });
rk[sa[0]] = 0;</pre>
             for (int i = 1; i < n; i++)</pre>
                  rk[sa[i]]
                            = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
            vector<int> tmp, cnt(n);
            tmp.reserve(n);
while (rk[sa[n - 1]] < n - 1) {
                  tmp.clear();
for (int i = 0; i < k; i++)
    tmp.push_back(n - k + i);</pre>
                   for (auto i : sa)
    if (i >= k)
        tmp.push_back(i - k);
                  fill(cnt.begin(), cnt.end(), 0);

for (int i = 0; i < n; i++)

++cnt[rk[i]];

for (int i = 1; i < n; i++)
                   cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; i--)
   sa[--cnt[rk[tmp[i]]]] = tmp[i];
                   swap(rk, tmp);
rk[sa[0]] = 0;
for (int i = 1; i < n; i++)</pre>
                         rk[sa[i]] = rk[sa[i - 1]] + (tmp[sa

[i - 1]] < tmp[sa[i]] || sa[i - 1] + k ==

n || tmp[sa[i - 1] + k] < tmp[sa[i] + k]);
            for (int i = 0, j = 0; i < n; i++) {
   if (rk[i] == 0) {</pre>
                         j = 0;
                   } else {
                         for (j -=
                         }
     }
```

5.7 SAM [b09888]

```
struct SAM {
    // 1 -> initial state
       static constexpr int ALPHABET_SIZE = 26;
       struct Node {
             int len;
int link;
             array<int, ALPHABET_SIZE> next;
Node() : len{}, link{}, next{} {}
       vector<Node> t:
      SAM() {
   init();
      void init() {
    t.assign(2, Node());
    t[0].next.fill(1);
             t[0].len = -1;
       int newNode() {
             t.emplace_back();
return t.size() - 1;
      int extend(int p, int c) {
   if (t[p].next[c]) {
      int q = t[p].next[c];
      if (t[q].len == t[p].len + 1) {
                          return q;
                    int r = newNode();
                    t[r].len = t[p].len + 1;
t[r].link = t[q].link;
t[r].next = t[q].next;
                    t[q].link = r;
                    while (t[p].next[c] == q) {
    t[p].next[c] = r;
    p = t[p].link;
                    return r;
             int cur = newNode();
t[cur].len = t[p].len + 1;
while (!t[p].next[c]) {
    t[p].next[c] = cur;
                    p = t[p].link;
             t[cur].link = extend(p, c);
             return cur;
     }
void solve() {
    string s; cin >> s;
    int n = s.length();
       vector < int > last(n + 1); // s[i - 1] 的後綴終點位置
       last[0] = 1;
      SAM sam;

for (int i = 0; i < n; i++) {

    last[i + 1] = sam.extend(last[i], s[i] - 'a');
       int sz = sam.t.size();
      vector < int > cnt(sz);
for (int i = 1; i <= n; i++) {</pre>
             cnt[last[i]]++; // 去重 = 1
      vector < vector < int >> order(sz);
for (int i = 1; i < sz; i++) {</pre>
             order[sam.t[i].len].push_back(i);
       for (int i = sz - 1; i > 0; i--) {
             for (int u : order[i]) {
    if (sam.t[u].link != -1) {
                          cnt[sam.t[u].link] += cnt[u];
                   }
             }
      vector < ll> dp(sz, -1);
auto dfs = [&](auto self, int u) -> void {
             dp[u] = cnt[u];
for (int c = 0; c < SAM::ALPHABET_SIZE; c++) {
   int v = sam.t[u].next[c];</pre>
                    if (v) {
   if (dp[v] == -1) self(self, v);
   dp[u] += dp[v];
             }
       dfs(dfs, 1);
}
```

5.8 Palindrome Tree [f10e9d]

```
struct PAM {
    // 0 -> even root, 1 -> odd root
    static constexpr int ALPHABET_SIZE = 26;
    struct Node {
        int len;
        int fail;
        array<int, ALPHABET_SIZE> next;
        Node() : len{}, fail{}, next{} {};
    vector<int> s;
```

```
vector < Node > t:
      PAM() {
            init();
      void init() {
           t.assign(2, Node());
            s.clear();
           t[0].len = 0;
t[1].len = -1;
           t[0].fail = 1;
      int newNode() {
           t.emplace_back();
return t.size() - 1;
      int extend(int p, int c) {
            int n = s.size();
           s.push_back(c);
while (s[n - t[p].len - 1] != c) {
    p = t[p].fail;
}
            if (!t[p].next[c])
                 int r = newNode();
t[r].len = t[p].len + 2;
int cur = t[p].fail;
while (s[n - t[cur].len - 1] != c) {
    cur = t[cur].fail;
                  t[r].fail = t[cur].next[c];
                 t[p].next[c] = r;
           p = t[p].next[c];
            return p;
     }
void solve() {
     string s; cin >> s;
int n = s.length();
      vector<int> last(n + 1);
      last[0] = 1;
     PAM pam;
for (int i = 0; i < n; i++) {
    last[i + 1] = pam.extend(last[i], s[i] - 'a');
}</pre>
      int sz = pam.t.size();
     vector <int > cnt(sz);
for (int i = 1; i <= n; i++) {
    cnt[last[i]]++; // 去重 = 1
      for (int i = sz -
                                1; i > 1; i--) {
            cnt[pam.t[i].fail] += cnt[i];
```

5.9 Duval [f9dcca]

```
// duval algorithm
 // duval_algorithm
// 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
vector<string> duval(string s) {
    int i = 0, n = s.size();
    vector<string> res;
    while (i < n) {
        int k = i, j = i + 1;
        while (s[k] <= s[j] && j < n) {
            if (s[k] < s[j]) k = i;
            else k++;
            if++*
                while (i <= k) {
                       res.push_back(s.substr(i, j - k));
                       i += j - k;
               }
         return res;
 }
 // 最小旋轉字串
 string min_round(string s) {
         s += s;
int i = 0, n = s.size();
         int start = i:
         while (i < n / 2) {</pre>
               else k++;
                      i++:
                while (i <= k) {
    i += j - k;</pre>
         return s.substr(start, n / 2);
}
```

6 Math 6.1 Modulo [a55187]

```
template < class T >
constexpr T power(T a, ll b) {
```

```
T res {1};
for (; b; b /= 2, a *= a)
if (b % 2) res *= a;
      return res:
constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
     res %= p;
if (res < 0) res += p;
      return res;
template < ll P >
struct MInt {
    ll x;
     constexpr MInt() : x {0} {}
constexpr MInt(ll x) : x {norm(x % getMod())} {}
static ll Mod;
constexpr static ll getMod() {
   return P > 0 ? P : Mod;
}
     constexpr static void setMod(ll Mod_) {
    Mod = Mod_;
     constexpr ll norm(ll x) const {
   if (x < 0) x += getMod();
   if (x >= getMod()) x -= getMod();
            return x;
     constexpr MInt operator -() const {
    return MInt(norm(getMod() - x));
     constexpr MInt inv() const {
   return power(*this, getMod() - 2);
      constexpr MInt &operator*=(MInt rhs) & {
           if (getMod() < (1ULL << 31)) {
    x = x * rhs.x % int(getMod());</pre>
           } else {
               x = mul(x, rhs.x, getMod());
            return *this;
      constexpr MInt &operator+=(MInt rhs) & {
           x = norm(x + rhs.x);
return *this;
      constexpr MInt & operator -= (MInt rhs) & {
    x = norm(x - rhs.x);
            return *this;
     constexpr MInt &operator/=(MInt rhs) & {
    return *this *= rhs.inv();
      friend constexpr MInt operator*(MInt lhs, MInt rhs) {
  return lhs *= rhs;
     friend constexpr MInt operator+(MInt lhs, MInt rhs) {
   return lhs += rhs;
     friend constexpr MInt operator-(MInt lhs, MInt rhs) {
   return lhs -= rhs;
     friend constexpr MInt operator/(MInt lhs, MInt rhs) {
   return lhs /= rhs;
      friend istream &operator>>(istream &is, MInt &a) {
           ll v; is >> v; a = MInt(v); return is;
      friend ostream &operator<<(ostream &os, const MInt &a) {</pre>
           return os << a.x;
      friend constexpr bool operator==(MInt lhs, MInt rhs) {
   return lhs.x == rhs.x;
      friend constexpr bool operator!=(MInt lhs, MInt rhs) {
  return lhs.x != rhs.x;
     friend constexpr bool operator<(MInt lhs, MInt rhs) {
   return lhs.x < rhs.x;</pre>
     }
};
template<>
ll MInt<0>::Mod = 998244353;
constexpr ll P = 1E9 + 7;
using Z = MInt<P>;
6.2 Combination [6aa734]
```

```
struct Comb {
         ll n; vector<Z> _fac, _invfac, _inv;
Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
Comb(ll n) : Comb() { init(n); }
void init(ll m) {
    m = min(m, Z::getMod() - 1);
    if ( - - - ) coturn.
                     if (m <= n) return;
_fac.resize(m + 1);
_invfac.resize(m + 1);</pre>
                     _inv.resize(m + 1);

for (int i = n + 1; i <= m; i++) {

    _fac[i] = _fac[i - 1] * i;
                     _invfac[m] = _fac[m].inv();
```

```
for (int i = m; i > n; i --) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
           If ac(ll m) {
    if (m > n) init(2 * m);
    return _fac[m];
           Z invfac(ll m) {
   if (m > n) init(2 * m);
   return _invfac[m];
           }
Z inv(ll m) {
    if (m > n) init(2 * m);
    return _inv[m];

           J binom(ll n, ll m) {
   if (n < m || m < 0) return 0;
   return fac(n) * invfac(m) * invfac(n - m);</pre>
           Z lucas(ll n, ll m) { // Mod 要在 1E5 左右
    if (m == 0) return 1;
    return binom(n % Z::getMod(), m % Z::getMod())
    * lucas(n / Z::getMod(), m / Z::getMod());
|} comb; // 注意宣告, 若要換模數需重新宣告
```

6.3 Sieve [37ae54]

```
vector < int > primes , minp;
void sieve(int n) {
    minp.assign(n + 1, 0);
            primes.clear();
           for (int i = 2; i <= n; i++) {
    if (minp[i] == 0) {
        minp[i] = i;
    }
                               primes.push_back(i);
                      for (auto p : primes) {
    if (i * p > n) break;
    minp[i * p] = p;
                                 if (p == minp[i]) break;
                      }
          }
}
// a ^ (m-1) = 1 (Mod m)
// a ^ (m-2) = 1/a (Mod m)
// Exp2: cout << power(x, power(y, p, Mod - 1), Mod)
// Num = (x+1) * (y+1) * (z+1)...
// Sum = (a^0 + a^1+...+ a^x) * (b^0 +...+ b^y)
// Mul = N * (x+1) * (y+1) * (z+1) / 2
```

6.4 MillerRabinPollardRho [b9e5be]

```
constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
       res %= p;
if (res < 0) res += p;
       return res:
template < class T>
constexpr T power(T a, ll b, ll p) {
   T res {1};
   for (; b; b /= 2, a = mul(a, a, p))
      if (b % 2) res = mul(res, a, p);
       return res:
vector<ll
> chk {2, 325, 9375, 28178, 450775, 9780504, 1795265022};
bool check(ll a, ll d, int s, ll n) {
      a = power(a, d, n);
if (a <= 1) return 1;
for (int i = 0; i < s; ++i, a = mul(a, a, n)) {
    if (a == 1) return 0;
    if (a == n - 1) return 1;
}</pre>
bool IsPrime(ll n) {
      if (n < 2) return 0;
if (n % 2 == 0) return n == 2;
ll d = n - 1, s = 0;
while (d % 2 == 0) d >>= 1, ++s;
for (ll i : chk) if (!check(i, d, s, n)) return 0;
       return 1;
 const vector<ll> small = {2, 3, 5, 7, 11, 13, 17, 19};
return (mul(a, a, n) + t) % n;
       for (int l = 2; ; l <<= 1) {
             x = y;
int m = min(l, 32);
             for (int i = 0; i < l; i += m) {
```

```
for (int j = 0; j < m; ++j) {
    y = f(y), d = mul(d, abs(x - y), n);</pre>
                 ll g = gcd(d, n);
                 if (g == n) {
    l = 1, y = 2, ++t;
                 if (g != 1) return g;
           }
    }
map<ll, int> res;
void PollardRho(il n) {
     if (n == 1) return;
if (IsPrime(n)) return ++res[n], void(0);
ll d = FindFactor(n);
     PollardRho(n / d), PollardRho(d);
```

6.5 CRT [d41d8c]

```
ll exgcd(ll a, ll b, ll &x, ll &y) {
      if (!b) {
    x = 1, y = 0;
      ll g = exgcd(b, a % b, y, x);
      y -= a / b * x;
      return g;
ll a, b;
      exgcd(x, m, a, b);
      a %= m;
if (a < 0) a += m;
      return a:
// remain, mod
ll CRT(vector<pair<ll, ll>> &a){
    ll prod = 1;
    for (auto x : a) {
        prod *= x.second;
}
      ll res = 0;
      for (auto x : a) {
   auto t = prod / x.second;
   res += x.first * t % prod * inv(t, x.second) % prod;
   if(res >= prod) res -= prod;
      return res;
}
```

6.6 Matrix [bec759]

assert(a.n == a.m);

```
template < class T>
struct Matrix {
     int n, m;
      vector < vector < T >> mat:
      constexpr Matrix(int n_, int m_) { init(n_, m_); }
constexpr Matrix(vector<vector<T>> mat_) { init(mat_); }
      constexpr void init(int n_, int m_) {
    n = n_; m = m_;

            mat.assign(n, vector<T>(m));
      constexpr void init(vector<vector<T>> mat_) {
           n = mat_.size();
m = mat_[0].size();
            mat = mat_;
      constexpr Matrix & operator*=(const Matrix &rhs) & {
   assert(mat[0].size() == rhs.mat.size());
            int n = mat
                   .size(), k = mat[0].size(), m = rhs.mat[0].size();
           .slze(), K = macloj.scz.,,
Matrix res(n, m);
for (int i = 0; i < n; i++) {
    for (int j = 0; j < m; j++) {
        for (int l = 0; l < k; l++) {
            res.mat[i][j] += mat[i][l] * rhs.mat[l][j];
}
                 }
            }
            mat = res.mat;
            return *this;
      friend constexpr
              Matrix operator*(Matrix lhs, const Matrix &rhs) {
            return lhs *= rhs;
     }
template < class T>
constexpr Matrix < T> unit(int n) {
     Matrix<T> res(n, n);
for (int i = 0; i < n; i++) {
           res.mat[i][i] = 1;
      return res;
template < class T>
constexpr Matrix<T> power(Matrix<T> a, ll b) {
```

```
Matrix<T> res = unit<T>(a.n):
for (; b; b /= 2, a *= a)

if (b % 2) res *= a;
return res:
```

6.7 Mex [4e24ed]

```
template < class T>
int mex(vector<T> &v) {
    unordered_set<T> s;
     for (auto e : v) s.insert(e);
for (T i = 0; ; i++) {
          if (s.find(i) == s.end()) return i;
}
```

6.8 Game Theorem

- sq 值為 0 代表先手必敗
- 當前 sg 值 = 可能的後繼狀態的 mex (例如拿一個或拿兩個, 就等於兩者的 sg 值 mex), 若有互相依賴就兩個後繼狀態 xor 當作一組 sg 值 (例如切開成 兩半,只算一次)
- 單組基礎 nim 的 sg 值為本身的原因: f(0) = 0, f(1) = mex(f(0)) =
- 1,f(2)=mex(f(0),f(1))=2...,都是自己 多組賽局可以把 sg 值 xor 起來,當成最後的 sg 值,nim 也是一樣,且由於 xor 性質, 如果可以快速知道 sg(1)g(2)...g(n), 就可以用 xor 性質處理不連

Integer Partition [595ed2]

```
// CSES_Sum_of_Divisors
const int mod = 1e9 + 7;
const int inv_2 = 500000004;
// n / 1 * 1 + n / 2 * 2 + n / 3 * 3 + ... + n / n * n
int main() {
    ll ans = 0;
      for (ll l = 1, r; l <= n; l = r + 1) {
    r = n / (n / l);
</pre>
           ll val = n / l; // n / l 到 n / r 一樣的值
ll sum = (((l + r) % mod) *
                  ((r - l + 1) % mod)) % mod * inv_2; // l 加到 r
           val %= mod; sum %= mod;
ans += val * sum;
           ans %= mod:
      cout << ans << "\n";
}
```

6.10 Mobius Theorem

- 數論分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在O(1)內計算f(r)-f(l)或已經預處理 出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n} \mu(d) = \begin{cases} 1 & \text{for } n=1\\ 0 & \text{for } n\neq 0 \end{cases}$$

- 2. μ是常數函數1的反元素 $\rightarrow \mu * 1 = \epsilon$, $\epsilon(n)$ 只在n = 1 時為 1 , 其餘情況皆為 0 。
- $-\phi$ 歐拉函數: x以下與x互質的數量

$$\phi*1 = \sum_{d|n} \phi(\frac{n}{d})$$
 質因數分解
$$= \sum_{i=0}^{c} \phi(p^{i})$$

$$= 1 + p^{0}(p-1) + p^{1}(p-1) + \dots + p^{c-1}(p-1)$$

$$= p^{c}$$

$$= id$$

- 莫比烏斯反演公式
 - $f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$
 - $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

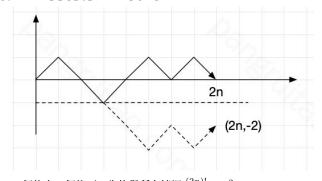
例子

$$\begin{split} &\sum_{i=a}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{y}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.11 Mobius Inverse [d41d8c]

```
const int maxn = 2e5:
ll mobius_pref[maxn];
void init() {
                    mobius_pref[1] = 1;
vector<ll> wei
                     (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
                                                                 continue; // 包含平方
                                           if (wei[i] == 0) {
    wei[i] = 1;
                                                                 }
                                          mobius_pref[i]
                                                                     = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
                    }
void solve() {
                  a solve() {
    ll a, b, c, d, k; cin >> a >> b >> c >> d >> k;
    auto cal = [&](ll x, ll y) -> int {
        int res = 0;
        for (int l = 1, r; l <= min(x, y); l = r + 1) {
            r = min(x / (x / l), y / (y / l));
            res += (mobius_pref[r] - mobius_pref[l] - mobius_p
                                                                                             - 1]) * (x / l) * (y / l); // 代推出來的式子
                                           return res;
                    cout << cal
                                              (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k, (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n";
```

6.12 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2)

假設往上有 x 個,往下有 y 個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.13 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- · G:各種翻轉操作所構成的置換群
- X/G: 本質不同的方案的集合 X/G: 對於某一種操作 g, 所有方案中, 經過 g 這種翻轉後保持不變的方案 的集合
- 集合取絕對值代表集合數

Search and Gready

Binary Search [d41d8c]

```
int main() {
          二分找上界
     while (lo < hi) {
   int x = (lo + hi + 1) / 2;
   if (check(x)) lo = x;</pre>
           else hi = x - 1;
      cout << lo; // 保證有解
     while (lo <= hi) {
   int x = (lo + hi) / 2;
   if (check(x)) lo = x + 1;
}</pre>
           else hi = x - 1;
      cout << hi; // 範圍外代表無解
         二分找下界
      cout << lo; // 保證有解
      while (lo <= hi) {
   int x = (lo + hi) / 2;</pre>
           if (check(m)) hi = x - 1;
           else lo = x + 1;
      cout << lo; // 範圍外代表無解
```

7.2 Ternary Search [d41d8c]

```
int main() {
     int lo = 0, hi = 10;
     while (lo <= hi) {</pre>
          int xl = lo + (hi - lo) / 3;
int xr = hi - (hi - lo) / 3;
          int ansl = check(xl), ansr = check(xr);
if (ansl < ansr) {</pre>
                 lo = xl + 1;
          } else {
    hi = xr - 1;
           // record ans and index
     }
```

Tree 8

8.1 LCA [f45014]

```
vector<vector<int>> par;
vector<int> dep;
void build(int n, vector<vector<int>> &tree, int u = 0) {
       par.assign(n, vector<int>(B + 1, -1));
dep.assign(n, 0);
auto dfs = [&](auto self, int x, int p) -> void {
              for (auto y : tree[x]) {
    if (y == p) continue;
    par[y][0] = x; // 2 ^ 0
    dep[y] = dep[x] + 1;
    self(self, y, x);
}
             }
       par[u][0] = u; dfs(dfs, 0, -1);
       for (int i = 1; i <= B; i++) {
    for (int j = 0; j < n; j++) {
        par[j][i] = par[par[j][i - 1]][i - 1];</pre>
      }
a = par[a][i];
       for (int i = B; i >= 0; i--) {
   if (par[a][i] != par[b][i]) {
      a = par[a][i], b = par[b][i];
}
       }
```

```
return par[a][0];
}
int jump(int x, int k) {
    for (int i = B; i >= 0; i--) {
        if (k >> i & 1) {
            x = par[x][i];
        }
    return x;
}
```

8.2 Centroid Decomposition [ec760b]

```
#include <bits/stdc++.h>
using namespace std;
struct CenDecom {
        vector<vector<int>> adi:
        vector < bool > vis;
        vector < int > siz;
CenDecom(int n_ = 0) { init(n_); }
        void init(int n_) {
                n = n_{;}
                adj.assign(n, {});
vis.assign(n, false);
siz.assign(n, 1);
        void addEdge(int u, int v) {
  adj[u].push_back(v);
  adj[v].push_back(u);
       }
void get_siz(int x, int p = -1) {
    siz[x] = 1;
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        get_siz(y, x);
        siz[x] += siz[y];
}
                }
        int get_cen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz) {
                                 return get_cen(y, sz, x);
                        }
                return x;
        void get_ans(int x, int p) {
                    do something
                for (int y : adj[x]) {
   if (y == p || vis[y]) continue;
   get_ans(y, x);
        void work(int x = 0) {
                get_siz(0, x);
                int cen = get_cen(x, siz[x]);
vis[cen] = true;
for (int y : adj[cen]) {
    if (vis[y]) continue;
    get_ans(y, cen);
}
                for (int y : adj[cen]) {
   if (vis[y]) continue;
                        work(y);
       }
};
```

8.3 Heavy Light Decomposition [41d99e]

```
struct HLD {
      vector<int> siz, top, dep, parent, in, out, seq;
     vector <int> st2, top, dep, parent, th, out, seq;
vector <vector <int>> adj;
HLD(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_; cur = 0;
    siz.resize(n); top.resize(n); dep.resize(n);
    parent.resize(n); in.resize(n); out.resize(n);
    sec.resize(n); dep.resize(n);
            seq.resize(n); adj.assign(n, {});
      void addEdge(int u, int v) {
            adj[u].push_back(v);
            adj[v].push_back(u);
      void work(int rt = 0) {
            top[rt] = rt;
dep[rt] = 0;
            parent[rt]
            dfs1(rt); dfs2(rt);
      void dfs1(int u) {
            if (parent[u] != -1)
                  for (auto &v : adj[u]) {
   parent[v] = u, dep[v] = dep[u] + 1;
   dfs1(v);
                  siz[u] += siz[v];
```

```
if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
                     } // 讓 adj[u][0] 是重子節點
       void dfs2(int u) {
              in[u] = cur++;
              seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
   top[v] = v == adj[u][0] ? top[u] : v;
                      dfs2(v):
              out[u] = cur;
       int lca(int u, int v) {
    while (top[u] != top[v]) {
        if (dep[top[u]] > dep[top[v]]) {
                     u = parent[top[u]];
} else {
                             v = parent[top[v]];
                     }
              return dep[u] < dep[v] ? u : v;</pre>
       int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
       bool isAncester(int u, int v) {
    return in[u] <= in[v] && in[v] < out[u];</pre>
       int rootedParent(int rt. int v) {
              rootedParent(int rt, int v) {
swap(rt, v);
if (rt == v) return rt;
if (!isAncester(rt, v)) return parent[rt];
auto it = upper_bound(adj[
    rt].begin(), adj[rt].end(), v, [&](int x, int y) {
    return in[x] < in[y];
}</pre>
              }) - 1;
return *it;
       int rootedSize(int rt, int v) {
   if (rt == v) return n;
   if (!isAncester(v, rt)) return siz[v];
   return n - siz[rootedParent(rt, v)];
       int rootedLca(int rt, int a, int b) {
  return lca(rt, a) ^ lca(a, b) ^ lca(b, rt);
};
```

8.4 Link Cut Tree [0e9031]

```
template < class Info, class Tag>
struct LinkCutTree { // 1-based
    struct Node {
    Info info = Info();
         Tag tag = Tag();
bool rev = false;
int size = 0;
         int ch[2], p = 0;
     vector < Node > nd:
     LinkCutTree(int n = 0) { init(n); }
     void init(int n) {
        nd.clear();
         nd.emplace_back();
         resize(n);
     void resize(int n) {
         nd.resize(n + 1);
    void make_rev(int t) {
    swap(nd[t].ch[0], nd[t].ch[1]);
    nd[t].rev ^= true;
     void apply(int t, const Tag &v) {
   nd[t].info.apply(nd[t].size, v);
   nd[t].tag.apply(v);
    nd[t].rev = false;
         if (nd[t].ch[0]) apply(nd[t].ch[0], nd[t].tag);
if (nd[t].ch[1]) apply(nd[t].ch[1], nd[t].tag);
nd[t].tag = Tag();
     void pull(int t) {
```

```
nd[t].size
                   1 + nd[nd[t].ch[0]].size + nd[nd[t].ch[1]].size;
           nd[t].info
                 .pull(nd[nd[t].ch[0]].info, nd[nd[t].ch[1]].info);
     int pos(int t) {
    return nd[nd[t].p].ch[1] == t;
      void pushAll(int t) {
          if (!isrt(t)) {
    pushAll(nd[t].p);
          push(t);
      void rotate(int t) {
          int q = nd[t].p;
int x = !pos(t);
nd[q].ch[!x] = nd[t].ch[x];
if (nd[t].ch[x]) nd[nd[t].ch[x]].p = q;
nd[t].p = nd[q].p;
          if (!isrt(q)) nd[nd[q].p].ch[pos(q)] = t;
nd[t].ch[x] = q;
          nd[q].p = t;
pull(q);
      void splay(int t) {
          if (pos(t) == pos(nd[t].p)) {
    rotate(nd[t].p);
                    } else {
                          rotate(t):
                    }
               rotate(t);
          pull(t);
     }
     void access(int t) { // access 後自動 splay
    for (int i = t, q = 0; i; q = i, i = nd[i].p) {
               splay(i);
               nd[i].ch[1] = q;
               pull(i);
           splay(t);
      void makeRoot(int t) {
           access(t);
          make_rev(t);
      int findRoot(int t) {
           access(t);
          int x = t;
while (nd[x].ch[0]) {
               push(x);
               x = nd[x].ch[0];
           access(x);
           return x:
     bool connected(int x, int y) {
    return findRoot(x) == findRoot(y);
     bool neighber(int x, int y) {
           makeRoot(x);
           access(y);
           if (nd[y].ch[0] != x || nd[x].ch[1]) return false;
          return true;
      void split(int rt, int y) {
          makeRoot(y);
access(rt);
      void link(int x, int y) {
          makeRoot(x);
           if (findRoot(y) != x) {
               nd[x].p = y;
     void cut(int x, int y) {
    makeRoot(x);
           access(y);
           nd[y].ch[0] = nd[nd[y].ch[0]].p = 0;
          pull(x);
           pull(y);
      void modify(int x, const Info &v) {
           access(x);
          nd[x].info = v;
     void path_apply(int x, int y, const Tag &v) {
   assert(connected(x, y));
          split(x, y);
           apply(x, v);
      Info path_query(int x, int y) {
           assert(connected(x, y));
          split(x, y);
return nd[x].info;
     }
};
```

```
constexpr int Mod = 51061;
struct Tag {
    ll add = 0; ll mul = 1;
    void apply(const Tag &v) {
        mul = mul * v.mul % Mod;
        add = (add * v.mul % Mod + v.add) % Mod;
    }
};
struct Info {
    ll val = 0; ll sum = 0;
    void apply(int size, const Tag &v) {
        val = (val * v.mul % Mod + v.add) % Mod;
        sum = (sum * v.mul % Mod + v.add * size % Mod) % Mod;
    }
void pull(const Info &l, const Info &r) {
        sum = (l.sum + r.sum + val) % Mod;
    }
};
```

8.5 Virtual Tree [622e69]

```
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
// 可以建立虚樹達成快速樹 DP
 // 可以建立區爾達成快速樹 DP
// 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
        vt[stk[top - 1]].push_back(stk[top]), top--;
    if (stk[top - 1] != l) {
        vt[l].push back(stk[ton]):
                  vt[l].push_back(stk[top]);
          stk[top] = l;

} else vt[l].push_back(stk[top--]);

stk[++top] = u;
  void reset(int u, vector<vector<int>> &vt) {
   for (int i : vt[u]) reset(i, vt);
   vt[u].clear();
  void solve(int n, int q) {
   vector g(n + 1, vector<pair<int, int>>());
         vector vt(n + 1, vector vector vt(n + 1, vector <int>()); // dfs 完清除, 否則會退化
vector <ll> dp(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;

                 g[u].push_back({v, w});
                 g[v].push_back({u, w});
         build_lca(n, g);
          build(n, g);
for (int i = 0; i < q; i++) {
   int m; top = -1; cin >> m;
                  vector<int> key(m);
                 for (int j = 0; j < m; j++) {
   cin >> key[j];
   iskey[key[j]] = 1;
                 key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
                  for (int x : key) insert(x, vt);
                 while (top
                             > 0) vt[stk[top - 1]].push_back(stk[top]), --top;
                  // DP
                 auto dfs = [&](auto self, int u) -> void {
    for (auto v : vt[u]) {
        self(self, v);
    }
}
                                  if (iskey[v])
                                         dp[u] += min_dis[v];
                                          // 砍掉 1 到 v 之間最短的路
                                         dp[u] += min(dp[v], min_dis[v]);
                                  iskey[v] = dp[v] = 0;
                         vt[u].clear();
                 dfs(dfs, key[0]); // key[0] 一定是 root cout << dp[key[0]] << "\n"; iskey[key[0]] = dp[key[0]] = 0;
         }
 }
```

8.6 Dominator Tree [baa540]

```
struct Dominator_tree {
   int n, id;
   vector<vector<int>> adj, radj, bucket;
   vector<int>> sdom, dom, vis, rev, pa, rt, mn, res;
   Dominator_tree(int n_ = 0) { init(n_); }
   void init(int _n) {
        n = _n, id = 0;
        adj.assign(n, vector<int>());
        radj.assign(n, vector<int>());
        bucket.assign(n, vector<int>());
        sdom.resize(n); dom.assign(n, -1);
        vis.assign(n, -1); rev.resize(n);
```

```
pa.resize(n); rt.resize(n);
mn.resize(n); res.resize(n);
       void add_edge(int u, int v) { adj[u].push_back(v); }
int query(int v, int x) {
   if (rt[v] == v) return x ? -1 : v;
              int p = query(rt[v], 1);
if (p == -1) return x ? rt[v] : mn[v];
if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
              rt[v] = p;
return x ? p : mn[v];
       void dfs(int v) {
    vis[v] = id, rev[id] = v;
    rt[id] = mn[id] = sdom[id] = id, id++;
               for (int u : adj[v]) {
   if (vis[u] == -1) dfs(u), pa[vis[u]] = vis[v];
   radj[vis[u]].push_back(vis[v]);
       void build(int s) {
               dfs(s);
              for (int i = id - 1; i >= 0; i--) {
    for (int u : radj[i])
        sdom[i] = min(sdom[i], sdom[query(u, 0)]);
                      if (i) bucket[sdom[i]].push_back(i);
                      for (int u : bucket[i]) {
   int p = query(u, 0);
   dom[u] = sdom[p] == i ? i : p;
                      if (i) rt[i] = pa[i];
              res.assign(n, -1);
for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];</pre>
               for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre>
              res[s] = s;
for (int i = 0; i < n; i++) dom[i] = res[i];
};
```

9 DP

9.1 LCS [5781cf]

9.2 LIS [66d09f]

9.3 Edit Distance [308023]

9.4 Bitmask [a626f9]

```
void hamiltonianPath(){
                                      int n, m; cin >> n >> m;
vector adj(n, vector<int>());
                                      for (int i = 0; i < m; i++) {
  int u, v; cin >> u >> v;
  adj[--v].push_back(--u);
                                       // 以...為終點,走過...
                                         vector dp(n, vector<int>(findBit(n)));
                                   vector dp(n, vector<int>(findbit(n));
dp[0][1] = 1;
for (int mask = 1; mask < findBit(n); mask++) {
    if ((mask & 1) == 0) continue;
    for (int i = 0; i < n; i++) {
        if ((mask & findBit(i)) == 0) continue;
        if (i == n - 1 && mask != findBit(n) - 1) continue;
        int pre_mask = mask ^ findBit(i);
        for (int i = adifil) {</pre>
                                                                                                            for (int j : adj[i]) {
   if ((pre_mask & findBit(j)) == 0) continue;
                                                                                                                                                dp[i][mask
                                                                                                                                                                                          ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
                                                                                                          }
                                      cout << dp[n - 1][findBit(n) - 1] << "\n";
   void elevatorRides() {
                                   | elevatorRides() {
| int n, x; cin >> n >> x; vector<int> a(n); |
| for (int i = 0; i < n; i++) cin >> a[i]; vector<array<int, 2>> dp(findBit(n)); |
| dp[0][0] = 1; // 次數、已使用人數 |
| for (int mask = 1; mask < findBit(n); mask++) {
| dp[mask][0] = dp[mask][1] = 2e9; |
| for (int i = 0; i < n; i++) {
| if ((mask & findBit(i)) == 0) continue; |
| int pre_mask = mask ^ findBit(i); |
| if (dp[pre_mask][1] + a[i] <= x) {
| if (dp[pre_mask][0] < dp[mask |
| findBit(i) == dp[mask][0] | d
                                                                                                                                                                                  application = application
                                                                                                       }
                                      cout << dp[findBit(n) - 1][0] << "\n";
}
```

9.5 Projects [0942aa]

```
int main() { // 排程有權重問題,輸出價值最多且時間最少
struct E {
    int from, to, w, id;
    bool operator <(const E &rhs) {
        return to == rhs.to ? w > rhs.w : to < rhs.to;
};

int n; cin >> n; vector <E> a(n + 1);
    for (int i = 1; i <= n; i++) {
        int u, v, w; cin >> u >> v >> w;
        a[i] = {u, v, w, i};
}

vector <array < ll, 2>> dp(n + 1); // m, time
vector <array < ll, 2>> rec(n + 1); // 有沒選, 上個是誰
sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
    auto it = --lower_bound(all(a), E({0, a[i].from}),
        [](E x, E y){ return x.to < y.to; });
    int id = it - a.begin(); dp[i] = dp[i - 1];
    ln w = dp[id][0] + a[i].w;</pre>
```

```
ll nt = dp[id][1] + a[i].to - a[i].from;

if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {

    dp[i] = {nw, nt}; rec[i] = {1, id};
             }
       }
vector < int > ans;
    ' a + i = n; i != 0;) {
      for (int i = n; i !=
    if (rec[i][0]) {
                    ans.push_back(a[i].id);
                    i = rec[i][1];
             } else i--:
}
9.6 Removal Game [7bb56b]
```

```
| // 兩個人比賽,每個人輪流取一個數字且只能是頭尾
// 問兩人都選得好,第一出手的人可取得的最大分數 int main() {
      int n; cin >> n;
vector <ll> a(n);
for (int i = 0; i < n; i++) cin >> a[i];
      vector dp(n, vector<ll>(n)); // i 到 j 區間的最大 diff
      for (int i = n - 1; i >= 0; i--) {
    dp[i][i] = a[i];
    for (int j = i + 1; j < n; j++)
        dp[i][j] =</pre>
```

max(a[i] - dp[i + 1][j], a[j] - dp[i][j - 1]);

(a.begin(), a.end(), 0LL) + dp[0][n - 1]) / 2 << "\n";

9.7 Monotonic Queue [f4976d]

cout << (accumulate

}
// x + y = sum; // x - y = dp[0][n - 1]

```
// 應用: dp(i) = h(i) + max(A(j)), for l(i) \le j \le r(i)
// A(j) 可能包含 dp(j), h(i) 可 O(1)
void Bounded_Knapsack() {
    int n, k; //O(nk)
vector<int> w(n), v(n), num(n); deque<int> q;
    // 於是我們將同餘的數分在同一組
    // 每次取出連續 num[i] 格中最大值
// g_x = max(_{k=0}^num[i] (g'_{x-k} + v_i*k))
// G_x = g'_{x} - v_i*x
    for (int r = 0; r < w[i]; r++) { // 餘數
            q.clear(); // q 記錄在 x = i 時的 dp 有單調性
for (int x = 0; x * w[i] + r <= k; x++) {
    while (!q.empty() && q.front() < x - num[i])
                q.pop_back();
                }
        swap(dp[0], dp[1]);
    cout << dp[0][k] << "\n";
```

9.8 SOS [93cb19]

```
| // 使用情況: 跟 bit 與(被)包含有關, 且 x 在 1e6 左右
 // 題目: 一數組, 問有多少所有數 & 起來為 \theta 的集合數 // dp[x]代表包含 x 的 y 個數(比x大且bit 1全包含 x 的有幾個)
 // 答案應該包含在 dp[0]内,但是有重複元素,所以考慮容斥
// => ans = \sum _{i=0}^{n} (-1)^{pop_count(i)} 2^{dp[i]-1}
// => 全部為0的個數 - 至少一個為1的個數 + 至少兩個為1的個數
  void solve() {
         int n; cin >> n; Z ans = 0;
vector < int > a(n);
         for (int i = 0; i < n; i++)
    cin >> a[i];
         int m = __lg(*max_element(a.begin(), a.end())) + 1;
         // 定義 dp[mask] 為 mask 被包含於 a[i] 的 a[i] 個數 vector <Z > dp(1 << m);
         for (int i = 0; i < n; i++)</pre>
        for (\int i = 0, i < ii, ...,
    dp[a[i]] += 1;
for (int i = 0; i < m; i++)
    for (int mask = 0; mask < 1 << m; mask++)
        if (mask >> i & 1) {
            int pre = mask ^ (1 << i);
            dp[pre] += dp[mask];
        itlended</pre>
        for (int mask = 0; mask < 1 << m; mask++) {
   int sgn = __builtin_popcount(mask) & 1 ? -1 : 1
   ans += sgn * (power(Z(2), dp[mask].val()) - 1);</pre>
         cout << ans << "\n";
```

9.9 CHT [5f5c25]

```
| // 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \le r(i)
 // A(j), B(j) 可能包含 dp(j), 分別就是 m 跟 b
 struct Line {
     ll m, b;
Line(ll m = 0, ll b = 0) : m(m), b(b) {}
ll eval(ll x) {
    return m * x + b;
};
struct CHT { // 用在查詢單調斜率也單調
      int n, lptr, rptr; vector<Line> hull;
CHT(int n_ = 0, Line init_ = Line()) {
   init(n_, init_);
      void init(int n_ = 0, Line init_ = Line()) {
    n = n_; hull.resize(n); reset(init_);
      void reset(Line init_ = Line()) {
    lptr = rptr = 0; hull[0] = init_;
      bool pop_front(Line &l1, Line &l2, ll x) {
           // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y
           // 代表查詢的當下,右線段的高度已經低於左線段了
return l1.eval(x) >= l2.eval(x);
      bool pop_back(Line &l1, Line &l2, Line &l3) {
           // 本題斜率遞減、上凸包
           // 因此只要 12 跟
           l3 的 X 交點 <= l1 跟 l3 的 X 交點, l2 就用不到了
return (l3.b - l2.b)
* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
      void insert(Line L) {
           while (rptr - lptr
                  > 0 && pop_back(hull[rptr - 1], hull[rptr], L))
                rptr - -
           hull[++rptr] = L;
      Il query(ll x) {
    while (rptr - lptr
                    . 0 && pop_front(hull[lptr], hull[lptr + 1], x))
                lptr++
           return hull[lptr].eval(x);
     }
};
```

9.10 DNC [61c639]

```
// 應用: 切 k 段問題, 且滿足四邊形不等式
// w(a,c) + w(b,d) ≤(≥) w(a,d) + w(b,c)
// dp[k][j] = min(dp[k - 1][i] + cost[i][j])
(tht t = max(k, opti); t <= min(m, opti)

// 注意 i 的範圍 x get_cost 與 dp 的邊界

ll cur = dp[k - 1][i] + get_cost(i, m);

if (cur < dp[k][m]) {

    dp[k][m] = cur, opt = i;
      DNC(k, l, m - 1, optl, opt);
      DNC(k, m + 1, r, opt, optr);
 int main() {
      // first build cost...
for (int i = 1; i <= n; i++) {
            // init dp[1][i]
       for (int i = 2; i <= k; i++) {
            DNC(i, 1, n, 1, n);
      cout << dp[k][n] << "\n";
```

9.11 LiChao Segment Tree [f23ef4]

```
// 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \le r(i)
constexpr il inf = 4e18;
struct Line {
     ll m, b;
     line(|l| m = 0, ll b = inf) : m(m), b(b) {}
ll eval(|l| x) const { return m * x + b; }
};
struct LiChaoSeg { // 取 max 再變換就好
     int n;
     vector<Line> info;
     LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_) {
          info.assign(4 << __lg(n), Line());</pre>
```

```
}
void update(Line line, int node, int l, int r) {
    int m = (l + r) / 2;
    bool left = line.eval(l) < info[node].eval(l);
    bool mid = line.eval(m) < info[node].eval(m);
    if (mid) swap(info[node], line); // 如果新線段比較好
    if (r - l == 1) return;
    else if (left != mid) update(line, 2 * node, l, m);
    // 代表左半有交點
    else update(line, 2 * node + 1, m, r);
    // 代表如果有交點一定在右半
}
void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
    if (r - l == 1) return info[node].eval(x);
    int m = (l + r) / 2;
    if (x < m) return
        min(info[node].eval(x), query(x, 2 * node, l, m));
else return min(
        info[node].eval(x), query(x, 2 * node + 1, m, r));
}
ll query(int x) { return query(x, 1, 0, n); }
};
```

9.12 Codeforces Example [7d37ea]

```
// CF 1932 pF
// 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
// 請問在線段不重複的情況下,最多獲得幾分 int main() {
     int n, m;
    cin >> n >> m;
     // 記錄每點有幾個線段
     // 再一個紀錄,包含這個點的左界
    cnt[l]++;
          cnt[r + 1]--;
     for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
     for (int i = n; i >= 2; i--) {
          l_side[i - 1] = min(l_side[i - 1], l_side[i]);
     vector<int> dp(n + 1):
     dp[0] = 0;
     for (int i = 1; i <= n; i++) {
    dp[i] = cnt[i];
    if (l_side[i] != inf) {</pre>
              dp[i] += dp[l_side[i] - 1];
          dp[i] = max(dp[i], dp[i - 1]);
     cout << dp[n] << "\n";
// CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
// 再加上 max(bi) - min(bi)
int main(){
  int n, k, ans = 0; cin >> n >> k;
  vector <pii> v(n + 1);
  for (int i = 1; i <= n; i++) {
    int a, b; cin >> a >> b;
    v[i] = {a, b};
  if (a = k) ans = 1;
          if (a <= k) ans = 1;
    sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
    }); // 用 bi 來排,考慮第 i 個時可以先扣
     vector < vector < int >> dp(n + 1, vector < int > (n + 1, inf));
     // 考慮 v[i] 時, 選 j 個的 sum(ai) - min(bi)
    for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j, dp[i - 1][j - 1] + v[i].first);
                 ' min(不選, 選)
              if (dp[i
                       1][j - 1] + v[i].first + v[i].second <= k) {
                   // 假如可以選, 更新 ans 時再加回去 bi ans = max(ans, j);
         dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
     cout << ans << endl;
```

10 Geometry

10.1 Basic [d41d8c]

```
template < class T>
struct Point {
    T x, y;
    Point(const T &x_ = 0, const T &y_ = 0) : x(x_), y(y_) {}
```

```
template < class U>
     operator Point<U>() {
          return Point < U > (U(x), U(y));
     Point &operator+=(const Point &p) & {
         x += p.x; y += p.y; return *this;
     Point & operator -= (const Point &p) & {
          x -= p.x; y -= p.y; return *this;
     Point & operator *= (const T &v) & {
          x *= v; y *= v; return *this;
     Point & operator /= (const T &v) & {
          x /= v; y /= v; return *this;
     Point operator -() const
          return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
          return a += b:
     friend Point operator - (Point a, const Point &b) {
          return a -= b:
     friend Point operator*(Point a, const T &b) {
  return a *= b;
     friend Point operator/(Point a, const T &b) {
          return a /= b;
     friend Point operator*(const T &a, Point b) {
          return b *= a;
     friend bool operator == (const Point &a, const Point &b) {
          return a.x == b.x && a.y == b.y;
     friend istream & operator >> (istream & is, Point & p) {
          return is >> p.x >> p.y;
     friend ostream &operator << (ostream &os, const Point &p) {
    return os << "(" << p.x << ", " << p.y << ")";</pre>
template < class T>
T dot(const Point<T> &a, const Point<T> &b) {
    return a.x * b.x + a.y * b.y;
template < class T >
T cross(const Point < T > &a, const Point < T > &b) {
    return a.x * b.y - a.y * b.x;
template < class T>
T square(const Point < T > &p) {
     return dot(p, p);
template < class T>
double length(const Point<T> &p) {
     return sqrt(double(square(p)));
template < class T>
Point<T> normalize(const Point<T> &p) {
    return p / length(p);
Point<T> rotate(const Point<T> &a) {
     return Point(-a.y, a.x);
template < class T>
int sgn(const Point<T> &a) {
    return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
template < class T>
struct Line {
     Point <T> a:
     Point<T> b;
     Line(const Point<T> &a_ = Point<T>()
           , const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
template < class T>
double length(const Line<T> &l) {
     return length(l.a - l.b);
bool parallel(const Line<T> &l1, const Line<T> &l2) {
   return cross(l1.b - l1.a, l2.b - l2.a) == θ;
template < class T>
double distance(const Point < T > & a, const Point < T > & b) {
    return length(a - b);
template < class T>
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)
      return distance(p, l.a);
   if (dot(p - l.b, l.a - l.b) < 0)</pre>
```

return distance(p, l.b);

```
return distancePL(p. l):
template < class T>
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
    return cross(l.b - l.a, p - l.a) > 0;
template < class T>
Point < T
       template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
    return cross(p - l.a, l.b - l.a) == 0 &&
        min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)</pre>
              && min
                       (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
     (const Point<T> &a, const vector<Point<T>> &p) {
       int n = p.size(), t = 0;
for (int i = 0; i < n; i++) {</pre>
               if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {
                      return true;
              }
       for (int i = 0; i < n; i++) {
    auto u = p[i];
    auto v = p[(i + 1) % n];
    if (u.x < a.</pre>
                      x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
t ^= 1;
               if (u.x >= a
                       .x && v.x < a.x && pointOnLineLeft(a, Line(u, v)))
                      t ^= 1;
       return t == 1;
// 0 : not intersect
    1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
tuple<int, Point<T>, Point<T>> segmentIntersection
  (const Line<T> &l1, const Line<T> &l2) {
  if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))</pre>
      IT (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
    return {0, Point<T>()};
if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
    return {0, Point<T>(), Point<T>()};
if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y))
    return {0, Point<T>(), Point<T>()};
if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y))
    return {0, Point<T>(), Point<T>()};
if (cross(l1 b - l1 a l2 b - l2 c) - n) {
       if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
   if (cross(l1.b - l1.a, l2.a - l1.a) != (
        return {0, Point<T>(), Point<T>()};
              } else {
                     auto maxx1 = max(l1.a.x, l1.b.x);
auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
                     auto maxy1 = max(l1.a.y, l1.b.y);
auto miny1 = min(l1.a.y, l1.b.y);
auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.y, l2.b.y);
auto miny2 = min(l2.a.y, l2.b.y);
Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
if (!nointOnSeament(n1 l1))
                      if (!pointOnSegment(p1, l1))
                      swap(p1.y, p2.y);
if (p1 == p2) {
                              return {3, p1, p2};
                      } else {
                             return {2, p1, p2};
             }
       auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
       return {0, Point<T>(), Point<T>()};
Point p = lineIntersection(l1, l2);
if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
               return {1, p, p};
       } else {
              return {3, p, p};
template < class T>
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
       if (get<0>(segmentIntersection(l1, l2)) != 0)
       return 0.0;
return min({distancePS(l1.a, l2), distancePS(l1
    .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
template < class Ta
bool segmentInPolygon
        (const Line<T> &l, const vector<Point<T>> &p) {
```

```
int n = p.size():
      int n = p.size();
if (!pointInPolygon(l.a, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
for (int i = 0; i < n; i++) {
    auto u = p[i];
}</pre>
            auto u = p[i];
auto v = p[(i + 1) % n];
auto w = p[(i + 2) % n];
auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
if (t == 1) return false;
if (t == 0) continue;
if (t == 2) {
                  if (pointOnSegment(v, l) && v != l.a && v != l.b)
    if (cross(v - u, w - v) > 0)
        return false;
            } else {
                  if (p1 != u && p1 != v) {
   if (pointOnLineLeft(l.a, Line(v, u))
                              || pointOnLineLeft(l.b, Line(v, u)))
                 return false;
} else if (p1 == v) {
    if (l.a == v) {
                              if (pointOnLineLeft(u, l)) {
                                    if (pointOnLineLeft(w, l)
    && pointOnLineLeft(w, Line(u, v)))
                                          return false:
                                    return false;
                        } else if (l.b == v)
                              if (pointOnLineLeft(u, Line(l.b, l.a))) {
   if (pointOnLineLeft(w, Line(l.b, l.a))
   && pointOnLineLeft(w, Line(u, v)))
                                          return false:
                                    return false;
                              }
                        }
                 }
           }
      return true;
template < class T>
vector<Point<T>> hp(vector<Line<T>> lines) {
      sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
   auto d1 = l1.b - l1.a;
   auto d2 = l2.b - l2.a;
            if (sgn(d1) != sgn(d2))
    return sgn(d1) == 1
            return cross(d1, d2) > 0;
      deque < Line < T >> ls;
      deque<Point<T>> ps;
for (auto l : lines) {
            if (ls.empty())
                  ls.push_back(l);
            while (!ps.empty() && !pointOnLineLeft(ps.back(), l))
    ps.pop_back(), ls.pop_back();
while (!ps.empty() && !pointOnLineLeft(ps[0], l))
            ps.pop_front(), ls.pop_front();
if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
                  if (dot
                        (1.b - l.a, ls.back().b - ls.back().a) > 0) {
if (!pointOnLineLeft(ls.back().a, l)) {
   assert(ls.size() == 1);
                        continue;
                  return {}:
            ps.push_back(lineIntersection(ls.back(), l));
            ls.push_back(l);
      while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0]))
      ps.pop_back(), ls.pop_back();
if (ls.size() <= 2) return {};
ps.push_back(lineIntersection(ls[0], ls.back()));</pre>
      return vector(ps.begin(), ps.end());
using P = Point<ll>;
10.2 Convex Hull [f99ef6]
```

```
template < class T>
vector < Point < T>> convexHull(vector < Point < T>> a) {
```

10.3 Min Euclidean Distance [d7fdcf]

```
void solve() {
     int n; cin >> n;
constexpr ll inf = 8e18;
      vector<Point<ll>> a(n);
     for (int i = 0; i < n; i++) {
    ll x, y;
    cin >> x >> y;
}
            a[i] = Point < ll>(x, y);
      struct sortY {
            bool operator
                  ()(const Point<ll> &a, const Point<ll> &b) const {
                 return a.v < b.v;</pre>
     struct sortXY {
           bool operator
                   ()(const Point<ll> &a, const Point<ll> &b) const {
                 if (a.x == b.x) return a.y < b.y;
else return a.x < b.x;</pre>
           }
     f;
sort(a.begin(), a.end(), sortXY());
vector < Point < ll >> t(n);
auto devide = [&](auto &&self, int l, int r) -> ll {
    if (l == r) return inf;
    int m = (l + r) / 2;
    ll ans = min(self(self, l, m), self(self, m + 1, r));
}

           ll midval = a[m].x;
            ll p = 0;
            for (int i = l; i <= r; i++) {
   if ((midval - a[i].x) * (midval - a[i].x) <= ans) {
      t[p++] = a[i];</pre>
           if ((t[i].y
                                t[j].y) * (t[i].y - t[j].y) > ans) break;
                 }
            return ans;
```

10.4 Max Euclidean Distance [0a8bec]

cout << devide(devide, 0, n - 1) << "\n";</pre>

10.5 Lattice Points [00db9d]

10.6 Min Circle Cover [02619b]

10.7 Min Rectangle Cover [b80323]

```
template < class T>
pair<T, vector<Point<T>>> minRectangle(vector<Point<T>> a) {
   if (a.size() <= 2) return {0, {}};
   auto get = [&](const Point<T> &p, const Line<T> &l) -> T {
      return abs(cross(l.a - l.b, l.a - p).x);
}
      int n = a.size(), j = 2, l = 1, r = 1;
      a.push_back(a.front());
     D th, tw, area = numeric_limits < double >::infinity();
vector < Point < T >> ans;
for (int i = 0; i < n; i++) {</pre>
           while (dot(a[i + 1] - a[i], a[r] - a[i])
      <= dot(a[i + 1] - a[i], a[(r + 1) % n] - a[i])) {
      r = (r + 1) % n;</pre>
           \tilde{D} th = get(a[j], Line(a[i], a[i + 1]));
           ans.clear
                 (), area = th * tw / square(a[i + 1] - a[i]); Line l1(a[i], a[i + 1]);
                for (auto p : {a[r], a[j], a[l], a[i]}) {
   Line l2 = Line(p, p + rotate(l1.a - l1.b
   if (cross(l1.a - l1.b, p - l1.a) == 0) {
      ans.push_back(p);
   }
}
                                                                        l1.b));
                            l1 = Line(p, p + rotate(l1.a - l1.b));
                      } else {
                            Point<T> res = lineIntersection(l1, l2);
                            ans.push_back(res);
```

```
l1.a = res. l1.b = p:
        }
   }
return {area, ans};
```

11 Polynomial

11.1 FFT [2e8718]

```
const double PI = acos(-1.0);
struct Complex {
       double x, y
       Complex (double x_ = 0, double y_ = 0) : x(x_), y(y_) {}
Complex operator+(const Complex &b) const {
              return Complex(x + b.x, y + b.y);
       Complex operator - (const Complex &b) const {
    return Complex(x - b.x, y - b.y);
       Complex operator*(const Complex &b) const {
   return Complex(x * b.x - y * b.y, x * b.y + y * b.x);
vector<int> rev:
void fft(vector<Complex > &a, bool inv) {
        int n = a.size();
        if (int(rev.size()) != n) {
               int k = __builtin_ctz(n) - 1;
rev.resize(n);
               for (int i = 0; i < n; i++) {
    rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;
       for (int i = 0; i < n; i++) {
    if (rev[i] < i) {</pre>
                      swap(a[i], a[rev[i]]);
       for (int k = 1; k < n; k *= 2) {
    double ang = (inv ? -1 : 1) * PI / k;
    Complex wn(cos(ang), sin(ang));
    for (int i = 0; i < n; i += 2 * k) {</pre>
                      (Int i = 0; i < n; i += 2 * k) {
Complex w(1);
for (int j = 0; j < k; j++, w = w * wn) {
    Complex u = a[i + j];
    Complex v = a[i + j + k] * w;
    a[i + j] = u + v;
    a[i + j + k] = u - v;
}</pre>
              }
       if (inv) {
    for (auto &x : a) {
                     x.x /= n;
x.y /= n;
               }
       }
remplate < class T >
vector < T > mulT(const vector < T > &a, const vector < T > &b) {
       vector<Complex
                > fa(a.begin(), a.end()), fb(b.begin(), b.end());
       int n = 2 << __lg(a.size() + b.size());
fa.resize(n), fb.resize(n);
fft(fa, false), fft(fb, false);
for (int i = 0; i < n; i++) {
    fa[i] = fa[i] * fb[i];
       fft(fa, true);
vector<T> res(n);
       for (int i = 0; i < n; i++) {
    if constexpr (!is_same_v < T, double >) {
        res[i] = round(fa[i].x);
    }
}
               } else {
    res[i] = fa[i].x;
               }
       return res;
11.2 NTT [1c9189]
```

```
template < int V, ll P>
constexpr MInt < P> CInv = MInt < P> (V).inv();
vector<ll> rev;
template<ll P>
vector < MInt < P >> roots { 0 , 1 };
template < int P>
constexpr MInt<P> findPrimitiveRoot() {
     MInt<P> i = 2;
int k = __builtin_ctz(P - 1);
while (true) {
   if (power(i, (P - 1) / 2) != 1) {
                   break:
```

```
return power(i, (P - 1) >> k);
template < ll P >
constexpr MInt<P> primitiveRoot = findPrimitiveRoot<P>();
constexpr MInt<998244353> primitiveRoot<998244353> {31};
template < ll P >
constexpr void dft(vector < MInt < P >> &a) {
   int n = a.size();
   if (int(rev.size()) != n) {
          int k = __builtin_ctz(n) - 1;
rev.resize(n);
for (int i = 0; i < n; i++) {</pre>
               rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;
     for (int i = 0; i < n; i++) {
    if (rev[i] < i) {</pre>
               swap(a[i], a[rev[i]]);
     while ((1 << k) < n) {
    auto e = power(primitiveRoot</pre>
               k++:
          }
     a[i + j] = u + v;
a[i + j + k] = u - v;
         }
     }
}
template < ll P >
constexpr void idft(vector < MInt < P >> &a) {
   int n = a.size();
     reverse(a.begin() + 1, a.end());
     dft(a);
MInt<P> inv = (1 - P) / n;
     for (int i = 0; i < n; i++) {
    a[i] *= inv;
}
template < ll P = 998244353>
struct Poly : public vector < MInt < P >> {
     using Value = MInt<P>;
Poly() : vector<Value>() {}
explicit constexpr Poly(int n) : vector<Value>(n) {}
     explicit constexpr
           Poly(const vector<Value> &a) : vector<Value>(a) {}
     constexor Poly(const
            initializer_list<Value> &a) : vector<Value>(a) {}
     template < class F>
     explicit constexpr Poly(int n, F f) : vector<Value>(n) {
    for (int i = 0; i < n; i++) {
        (*this)[i] = f(i);
    }
}</pre>
     constexpr Poly shift(int k) const {
          if (k >= 0) {
    auto b = *this;
               b.insert(b.begin(), k, 0);
          return b;
} else if (this->size() <= -k) {
  return Poly();</pre>
               return Poly(this->begin() + (-k), this->end());
     constexpr Poly trunc(int k) const {
  Poly f = *this;
  f.resize(k);
          return f;
          friend Poly operator+(const Poly &a, const Poly &b) {
Poly res(max(a.size(), b.size()));
for (int i = 0; i < a.size(); i++) {</pre>
               res[i] += a[i];
          for (int i = 0; i < b.size(); i++) {</pre>
               res[i] += b[i];
```

```
return res:
constexpr
          friend Poly operator-(const Poly &a, const Poly &b) {
       Poly res(max(a.size(), b.size()));
       for (int i = 0; i < a.size(); i++) {
    res[i] += a[i];</pre>
       for (int i = 0; i < b.size(); i++) {
    res[i] -= b[i];</pre>
constexpr friend Poly operator-(const Poly &a) {
       vector < Value > res(a.size());
       for (int i = 0; i < int(res.size()); i++) {</pre>
             res[i] = -a[i];
       return Poly(res);
constexpr friend Poly operator*(Poly a, Poly b) {
   if (a.size() == 0 || b.size() == 0) {
             return Poly();
       if (a.size() < b.size()) swap(a, b);</pre>
       int n = 1, tot = a.size() + b.size() - 1;
while (n < tot) n *= 2;
if (((P - 1) & (n - 1)) != 0 || b.size() < 128) {</pre>
             for (int j = 0; j < b.size() < 1
for (int j = 0; j < b.size(); j++) {
    c[i + j] += a[i] * b[j];</pre>
              return c:
      a.resize(n), b.resize(n);
dft(a), dft(b);
for (int i = 0; i < n; ++i) {
    a[i] *= b[i];</pre>
       idft(a);
       a.resize(tot);
       return a:
constexpr friend Poly operator*(Value a, Poly b) {
   for (int i = 0; i < int(b.size()); i++) {
      b[i] *= a;</pre>
       return b:
constexpr friend Poly operator*(Poly a, Value b) {
   for (int i = 0; i < int(a.size()); i++) {
      a[i] *= b;</pre>
       return a;
constexpr friend Poly operator/(Poly a, Value b) {
       for (int i = 0; i < int(a.size()); i++) {
    a[i] /= b;</pre>
constexpr Poly &operator+=(Poly b) {
      return (*this) = (*this) + b;
constexpr Poly &operator -=(Poly b) {
  return (*this) = (*this) - b;
constexpr Poly &operator*=(Poly b) {
   return (*this) = (*this) * b;
constexpr Poly &operator*=(Value b) {
   return (*this) = (*this) * b;
constexpr Poly &operator/=(Value b) {
  return (*this) = (*this) / b;
constexpr Poly deriv() const {
   if (this->empty()) return Poly();
   Poly res(this->size() - 1);
   for (int i = 0; i < this->size() - 1; ++i) {
      res[i] = (i + 1) * (*this)[i + 1];
}
constexpr Poly integr() const {
   Poly res(this->size() + 1);
       for (int i = 0; i < this->size(); ++i) {
    res[i + 1] = (*this)[i] / (i + 1);
       return res;
constexpr Poly inv(int m) const {
      rote in v (in v (in v in v const {
    Poly x{(*this)[0].inv()};
    int k = 1;
    while (k < m) {
        k *= 2;
        x = (x * (Poly{2} - trunc(k) * x)).trunc(k);
    }
}</pre>
       return x.trunc(m);
```

```
constexpr Poly log(int m) const {
    return (deriv() * inv(m)).integr().trunc(m);
     constexpr Poly exp(int m) const {
          Poly x{1};
         int k = 1;
while (k < m) {
 k *= 2;
               x = (x * (Poly{1} - x.log(k) + trunc(k))).trunc(k);
          return x.trunc(m):
     constexpr Poly pow(int k, int m) const {
         int i = 0:
          while (i < this->size() && (*this)[i] == 0) {
          if (i == this->size() || 1LL * i * k >= m) {
              return Poly(m);
         constexpr Poly sqrt(int m) const {
         Poly x{1};
int k = 1;
          while (k < m) {
    k *= 2;
              x = (x +
                      (trunc(k) * x.inv(k)).trunc(k)) * CInv<2, P>;
         return x.trunc(m):
     constexpr Poly mulT(Poly b) const
         if (b.size() == 0) return Poly();
int n = b.size();
         reverse(b.begin(), b.end());
return ((*this) * b).shift(-(n - 1));
     constexpr vector<Value> eval(vector<Value> x) const {
         if (this->size() == 0) {
   return vector<Value>(x.size(), 0);
         const int n = max(x.size(), this->size());
vector<Poly> q(4 * n);
vector<Value> ans(x.size());
          x.resize(n);
          function < void(</pre>
              int, int, int)> build = [&](int p, int l, int r) {
  if (r - l == 1) {
     q[p] = Poly{1, -x[l]};
} else {
    int m = (l + r) / 2;
}
                    build(2 * p, l, m);
build(2 * p + 1, m, r);
q[p] = q[2 * p] * q[2 * p + 1];
             }
          build(1, 0, n);
         ans[l] = num[0];
              } else {
                   m, r, num.mulT(q[2 * p]).resize(r - m));
              }
          work(1, 0, n, mulT(q[1].inv(n)));
          return ans:
template < ll P = 998244353>
Poly<P> berlekampMassey(const Poly<P> &s) {
    Poly<P> c, oldC;
int f = -1;
for (int i = 0; i < s.size(); i++) {
    auto delta = s[i];
    for (int j = 1; j <= c.size(); j++) {
        delta -= c[j - 1] * s[i - j];
}</pre>
          if (delta == 0) continue;
          if (f == -1) {
               c.resize(i + 1);
               f = i;
         } else {
               auto d = oldC;
              d *= -1:
               d.insert(d.begin(), 1);
               d. diser(c); d. diser(c); d. df1 = d[j - 1] * s[f + 1 - j];
               assert(df1 != 0);
```

};

```
auto coef = delta / df1;
    d *= coef;
    Poly<P> zeros(i - f - 1);
    zeros.insert(zeros.end(), d.begin(), d.end());
    d = zeros;
    auto temp = c;
    c += d;
    if (i - temp.size() > f - oldC.size()) {
        oldC = temp;
        f = i;
    }
}

c *= -1;
c.insert(c.begin(), 1);
return c;
}

template<ll P = 998244353>
MInt<P> linearRecurrence(Poly<P> p, Poly<P> q, ll n) {
    int m = q.size() - 1;
    while (n > 0) {
        auto newq = q;
        for (int i = 1; i <= m; i += 2) {
                 newq[i] *= -1;
        }
        auto newp = p * newq;
        newq = q * newq;
        for (int i = 0; i < m; i++) {
                  p[i] = newp[i * 2 + n % 2];
        }
        for (int i = 0; i <= m; i++) {
                  q[i] = newq[i * 2];
        }
        n /= 2;
    }
    return p[0] / q[0];
}</pre>
```