Contents 5 String 5.1 KMP 1 Basic 1.1 install vscode 1.2 default code 1.3 compare fuction Math 1.4 pbds 2 Graph 2.1 DFS跟BFS 2.4 正權找環 2.5 BellmanFord 6.8 Catalan Theorem 6.9 Burnside's Lemma 13 7 Search and Gready 2.8 FloydWarshall 2.9 歐拉環與歐拉路 2.10 SCC 2.11 VBCC Tree 8.1 LCA 13 8.2 樹重心 13 8.3 樹壓平 13 2.12 EBCC 2.13 2-SAT 2.14 Planets Cycles 8.4 Heavy Light Decomposition 14 2.15 Planet Queries II 8.5 Virtual Tree 14 3 Data Structure q DΡ 9.1 背包問題 15 9.2 Bitmask 15 9.3 硬幣 15 9.4 編輯距離 15 9.5 LCS 15 3.3 Increasing Array Queries . 6 6 **9.6 LIS** 16 3.7 Treap Flow 4.1 Dinic 4.2 Min Cut 10 Geometry 4.3 Bipartite Matching **10.1 Cross Product** 17 **10.2 Convex Hull** 17 4.4 MCMF

1 Basic

1.1 install vscode [d41d8c]

1.2 default code [3cd57c]

```
#include <bits/stdc++.h>
#define all(x) (x).begin(), (x).end()
#define pip pair <int, int>
using namespace std;
using ll = long long;
const int mod = 1e9 + 7;

void solve() {
}

int main() {
   ios_base::sync_with_stdio(0);
   cin.tie(nullptr);
   int t = 1;
   cin >> t;
   while (t--) {
      solve();
   }
}
```

1.3 compare fuction [4bc3e0]

```
struct cmp { // 要在 template 的資結用外部變數 vector <int> &v;
     cmp(vector<int>& vec) : v(vec) {}
bool operator() (int a, int b) const {
   return v[a] > v[b];
// mutil: cmp cmp1(vector);
// priority_queue<int, vector<int>, cmp> pq(cmp1);
};
1.4 pbds [e28ae8]
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using pbds_set = tree<T, null_type,
    less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template < typename T>
using pbds_multiset = tree<T, null_type, less_equal</pre>
      <T>, rb_tree_tag, tree_order_statistics_node_update>;
2
       Graph
2.1 DFS 跟 BFS [cdd1d5]
int main() {
      int n
     vector<vector<int>> adj(n + 1, vector<int>());
     // dfs_graph
     vis[u] = true;
for (auto v: adj[u]) {
    self(self, v);
     dfs(dfs, 1);
     vector<int> depth(n + 1, 1e9);
     queue int > q;

auto bfs = [&](auto self, int u) -> void {
          vis[u] = true;
depth[u] = 0;
           q.push(u);
           while (!q.empty()) {
   int u = q.front(); q.pop();
   for (auto v : adj[u]) {
                     if (vis[v]) continue;
                     vis[v] = true;
depth[v] = depth[u] + 1;
                     q.push(v);
                }
          }
```

2.2 Dijkstra [4e0023]

bfs(bfs, 1);

```
// Flight Discount
int main() {
      int n, m; cin >> n >> m;
vector<vector<pair<</pre>
              int, int>>> adj(n + 1, vector<pair<int, int>>(n + 1));
      vector<vector<int>>
      dis(n + 1, vector<int>(2, 2e9));
for (int i = 1; i <= m; i++) {
                                                                        // O for not used
            int u, v, w;
cin >> u >> v >> w;
             adj[u].push_back({v, w});
      priority queue
     while (!pq.empty()) {
    auto [dist, u, us] = pq.top(); pq.pop();
    if (dis[u][us] < dist) continue;</pre>
             if (us) {
                   for (auto [v, w] : adj[u]) {
    if (dis[u][1] + w < dis[v][1]) {
        dis[v][1] = dis[u][1] + w;
    }
}</pre>
                                pq.push({dis[v][1], v, 1});
                   for (auto [v, w] : adj[u]) {
   if (dis[u][0] + w < dis[v][0]) {
      dis[v][0] = dis[u][0] + w;
      pq.push({dis[v][0], v, 0});</pre>
                          if (dis[u][0] + w / 2 < dis[v][1]) {
   dis[v][1] = dis[u][0] + w / 2;
   pq.push({dis[v][1], v, 1});</pre>
```

```
National Chung Cheng University Salmon
    cout << min(dis[n][0], dis[n][1]);</pre>
2.3 Prim [f00ec0]
auto prim =
       [&](int n, vector<vector<pair<int, int>>> &adj) -> bool {
     int node_sz = 0;
     priority_queue<pair<int, int>,
     while (!pq.empty()) {
         auto [u, w] = pq.top(); pq.pop();
if (vis[u]) continue;
          vis[u] = true;
          node_sz++;
for (auto v : adj[u]) {
               if (!vis[v.first]) {
                   pq.push({v.second, v.first});
         }
    if (node_sz == n) return true;
return false;
2.4 正權找環 [0e0fdf]
const int maxn = 1e5+5;
vector < int > graph[maxn];
int color[maxn], parent[maxn];
bool vis[maxn];
int n, m;
void print_ans(int ori) {
  int now = parent[ori];
  deque<int> ans;
  ans.push_front(ori);
  while (now != ori) {
                                                                                        ans.push_front(now);
          now = parent[now];
                                                                                         queue<int> q;
                                                                                         for (int i = 1; i <= m; i++) {
   int u, v; cin >> u >> v;
   graph[u].push_back(v);
     ans.push_front(ori);
     cout << ans.size() << endl;
for (auto i : ans) {
    cout << i << " ";</pre>
                                                                                         for (int i = 1; i <= n; i++) {
   if (in[i] == 0) q.push(i);</pre>
     exit(0);
void dfs(int now) {
                                                                                        while (!q.empty()) {
   int u = q.front(); q.pop();
    color[now] = 1;
vis[now] = 1;
     for (auto nxt : graph[now]) {
  parent[nxt] = now;
  if (color[nxt] == 1) {
               print_ans(nxt);
          else if (color[nxt] == 0) {
               dfs(nxt);
                                                                                         if (dis[n] == -1e9) {
    color[now] = 2;
void solve() {
    cin >> n >> m;
for (int i = 1; i <= m; i++) {
   int u, v; cin >> u >> v;
                                                                                         else print_ans(n, par);
          graph[u].push_back(v);
                                                                                   2.7 負權最大距離 [2148ca]
     for (int i = 1; i <= n; i++) {
          if (!vis[i])
               dfs(i):
     cout << "IMPOSSIBLE";</pre>
}
2.5 BellmanFord [02f480]
// 用 Bellman Ford 找負環
                                     // u, v, w
vector<array<int, 3>> graph;
int main() {
     int src = 0;
```

```
int n, m; cin >> n >> m;
vector <int > par(n + 1), dis(n + 1, 1e9);
for (int i = 0; i < m; i++) {
   int a, b, w; cin >> a >> b >> w;
   graph.push_back({a, b, w});
}
dis[1] = 0;
for (int i = 0; i <= n; i++) {</pre>
            \dot{s}rc = 0;
            for (auto [u, v, w] : graph) {
    if (dis[v] > dis[u] + w) {
        dis[v] = dis[u] + w;
        par[v] = u;
                                   src = v;
                      }
           }
```

```
if (src) { // 到第 n + 1 次還在鬆弛 vector<int> ans;
          cout << "YES" << endl;
for (int</pre>
                 i = 0; i <= n; i++) src = par[src]; // 找那個負環
          ans.push_back(src);
           for (int
                i = par[src]; i != src; i = par[i]) { // 輸出負環
               ans.push_back(i);
          ans.push back(src):
           reverse(ans.begin(), ans.end());
          for (auto i : ans) {
    cout << i << " ";</pre>
      else {
          cout << "NO" << "\n";
 2.6 正權最大距離 [454dba]
// CSES Longest Flight Route
// 只能用在 DAG,用拓樸按順序鬆弛
void print_ans(int n, vector<int> &par) {
      deque < int > ans;
      int now = n;
      while(now != 1) {
          ans.push_front(now);
now = par[now];
      ans.push front(1):
     cout << ans.size() << "\n";
for(auto i : ans) {
    cout << i << " ";</pre>
```

// 如果 1 不能到達 n,n 也有可能被鬆弛 // 所以要看的是 dis[n] < 0 cout << "IMPOSSIBLE";

in[v]--;

for (auto v : graph[u]) {

par[v] = u;

if (in[v] == 0) q.push(v);

if (dis[v] < dis[u] + 1) { // 鬆弛 dis[v] = dis[u] + 1;

```
void dfs(int u, vector<int> &vis, vector<vector<int>> &adj) {
   if (vis[u]) return;
     vis[u] = 1;
     for (int v : adj[u]) {
          dfs(v, vis, adj);
signed main() {
   int n, m; cin >> n >> m;
     vector<array<int, 3>> edges;
vector<vector<int>> adj(n + 1);
vector<int>> dis(n + 1), vis(n + 1);
     while (m--) {
   int u, v, w;
   cin >> u >> v >> w;
   edges.push_back({u, v, w});
          adj[u].push_back(v);
    fill(dis.begin(), dis.end(), -1e18);
```

```
}
}
if (vis[n]) cout << -1;
else cout << dis[n];
}
```

2.8 FloydWarshall [206b76]

2.9 <u>歐拉環與歐拉路</u> [0911ed]

```
| // 無向圖、尤拉環:檢查每個點的出度為偶數
 // 有向圖、
       尤拉路: 可以看成 1 走到 n, 所以檢查所有點的出度等於入度
 int n, m;
 const int maxn = 1e5 + 5;
 vector<set<int>> adj;
vector<int> in;
 void dfs(int now, vector<int> &road) {
      while (!adj[now].empty()) {
   int nxt = *adj[now].begin();
            adj[now].erase(nxt);
            dfs(nxt, road);
      road.push_back(now);
 void solve() {
    cin >> n >> m;
    in.assign(n + 1, 0);
    adj.assign(n + 1, set<int>());
    for (int i = 1; i <= m; i++) {
        int u, v; cin >> u >> v;
        adj[u] incort(v);
}
            adj[u].insert(v);
            in[v]++;
      in[1]++;
      }
      vector<int> road;
      dfs(1, road);
      if (road.size() != m + 1) {
    cout << "IMPOSSIBLE";</pre>
            return:
      reverse(road.begin(), road.end());
for(auto i : road) cout << i << " ";</pre>
```

2.10 SCC [b0411e]

```
struct SCC {
    int n, cur, cnt;
    vector <vector <int>> adj;
    vector <int>> stk, dfn, low, bel;
    SCC(int n) {
        init(n);
    }
    void init(int n) {
        this -> n = n;
        adj.assign(n, {});
        dfn.assign(n, -1);
        low.resize(n);
        bel.assign(n, -1);
```

```
stk.clear():
            cur = cnt = 0;
       void addEdge(int u, int v) {
            adj[u].push_back(v);
       void dfs(int x) {
    dfn[x] = low[x] = cur++;
            stk.push_back(x);
            for (auto y : adj[x]) {
   if (dfn[y] == -1) {
                       dfs(y);
                 low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
            if (dfn[x] == low[x]) {
                  int y;
                  do {
                       v = stk.back():
                       bel[y] = cnt;
                       stk.pop_back();
                  } while (y != x);
           }
      for (int i = 0; i < n; i++) {
    if (dfn[i] == -1) dfs(i);</pre>
            return bel;
       struct Graph {
            vector<pair<int, int>> edges;
            vector < int > siz;
vector < int > cnte;
       Graph compress() {
            Graph g;
g.n = cnt;
            g.siz.resize(cnt);
            g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {</pre>
                  g.siz[bel[i]]++;
                  for (auto j : adj[i]) {
    if (bel[i] != bel[j]) {
                             g.edges.emplace_back(bel[i], bel[j]);
                       } else {
                            g.cnte[bel[i]]++;
                 }
            return g;
      }
};
```

2.11 VBCC [3f9190]

```
struct VBCC {
     int n, cur;
vector<vector<int>> adj;
     vector<int> dfn, low, parent;
     vector<bool> is_cut;
     VBCC(int n) {
    init(n);
     void init(int n) {
           this ->n = n:
           adj.assign(n, {});
           dfn.assign(n, -1);
           low.resize(n):
           parent.assign(n, -1);
           is_cut.assign(n, false);
           cur = 0;
     void addEdge(int u, int v) {
   adj[u].push_back(v);
           adj[v].push_back(u);
     void dfs(int x) {
   int children = 0;
   dfn[x] = low[x] = cur++;
           for (int v : adj[x]) {
   if (dfn[v] == -1) {
      children++;
                      parent[v] = x;
                      dfs(v);
low[x] = min(low[x], low[v]);
                      if (parent[x] != -1 && low[v] >= dfn[x]) {
    is_cut[x] = true;
                } else if (v != parent[x]) {
    low[x] = min(low[x], dfn[v]);
           if (parent[x] == -1 && children > 1) {
    is_cut[x] = true;
```

```
}
void work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i);
        }
    }
};</pre>
```

2.12 EBCC [08723d]

```
struct EBCC { // CF/contest/1986/pF
  int n, cur, cnt;
  vector<vector<int>> adj;
      vector<int> stk, dfn, low, bel;
      vector<pair<<mark>int, int</mark>>> bridges; // 關鍵邊
      EBCC(int n) {
            init(n);
      void init(int n) {
            this->n = n;
adj.assign(n, {});
            dfn.assign(n, -1);
            low.resize(n);
            bel.assign(n, -1);
            stk.clear();
            bridges.clear();
            cur = cnt = 0:
      void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
      void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
            stk.push_back(x);
            for (auto y : adj[x]) {
   if (y == p) continue;
   if (dfn[y] == -1) {
                        dfs(y, x);
low[x] = min(low[x], low[y]);
if (low[y] > dfn[x]) {
                             bridges.emplace_back(x, y);
                  } else if (bel[y] == -1) {
                        low[x] = min(low[x], dfn[y]);
                 }
            if (dfn[x] == low[x]) {
                  int y;
                  do {
                        y = stk.back();
                        bel[y] = cnt;
stk.pop_back();
                  } while (y != x);
            }
      vector<int> work() {
            dfs(0, -1);
return bel;
      struct Graph {
            int n;
            vector<pair<int, int>> edges;
            vector<int> siz; // BCC 內節點數
            vector<int> cnte; // BCC 內邊數
      Graph compress() {
            Graph g;
g.n = cnt;
            g.siz.resize(cnt);
            g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {</pre>
                  g.siz[bel[i]]++;
                  g.stc[bet[i]] + ,
for (auto j : adj[i]) {
    if (bel[i] < bel[j]) {
        g.edges.emplace_back(bel[i], bel[j]);
    } else if (i < j) {
        restrict [i] [i];
}</pre>
                             g.cnte[bel[i]]++;
                       }
                 }
            return a:
     }
};
```

2.13 2-SAT [eeddc1]

```
// CSES Giant Pizza
struct TwoSat {
    int n;
    vector<vector<int>> e;
    vector<bool> ans;
    TwoSat(int n) : n(n), e(2 * n), ans(n) {}
    void addClause(int u, bool f, int v, bool g) {
        e[2 * u + !f].push_back(2 * v + g);
        e[2 * v + !g].push_back(2 * u + f);
    }
}
```

```
bool satisfiable() {
            vector < int

> id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
             int now = 0, cnt = 0;
             function < void(int) > tarjan = [&](int u) {
                   stk.push_back(u);
dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
                         tarjan(v);
  low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in stk
  low[u] = min(low[u], dfn[v]);
                   if (dfn[u] == low[u]) {
                          int v;
                          do {
                                v = stk.back();
                         stk.pop_back();
id[v] = cnt;
} while (v != u);
                          ++cnt:
                  }
             for (int i
            return true:
       vector<bool> answer() { return ans; }
int main() {
      main() {
  int m, n; cin >> m >> n;
TwoSat ts(n);
for (int i = 0; i < m; ++i) {
    int u, v; char x, y;
    cin >> x >> u >> y >> v;
    ts.addClause(u - 1, x == '+', v - 1, y == '+');
}
      if (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";</pre>
      else cout << "IMPOSSIBLE\n";</pre>
```

2.14 Planets Cycles [71ac0e]

```
vector<int> dis, v;
vector<bool> vis:
int step;
void dfs(int x) {
    path.push(x);
       if (vis[x]) {
    step += dis[x];
             return:
       vis[x] = true;
       step++;
       dfs(v[x]);
// count path_dis to rep
int main() {
   int n; cin >> n;
      v.assign(n + 1, 0);
dis.assign(n + 1, 0);
vis.assign(n + 1, false);
for (int i = 1; i <= n; i++) {</pre>
             cin >> v[i];
       for (int i = 1; i <= n; i++) {
             step = 0;
int is_outof_cycle = 1;
             dfs(t);
while (!path.empty()) {
   if (path.front() == path.back()) {
                          is_outof_cycle = 0;
                    dis[path.front()] = step;
step -= is_outof_cycle;
                   path.pop();
            }
       for (int i = 1; i <= n; i++) {
    cout << dis[i] << ' ';</pre>
       cout << '\n';
}
```

2.15 Planet Queries II [872f72]

```
| // 在有向圖中,從 A 到 B 的最短距離
| // 保證出度是 1 所以對 1 個點來說,從他出發只可能遇到一個環
| int n, q;
| int dp[200005][30]; // 倍增表
```

```
vector<vector<int>> cvcles:
vector<int
set_out_of_cycle_no(dp[now][0], done);
     done.insert(now); // post order
no[now] = no[dp[now][0]] - 1;
int wiint_go_to(int u, int k) { // 回傳當 u 走 k 步時會到的地方
    for (int i = 0; i <= 18; i++) {
        if (k & (1 << i)) {</pre>
                u = dp[u][i];
     return u;
void find_cycle(int now) {
     unordered_set<int> appear;
     vector<int> v:
     bool flag = true;
                                // 代表有環
     while (appear.find(now) == appear.end()) {
           appear.insert(now);
          v.push_back(now);
if (vis[now]) {
    flag = false;
          now = dp[now][0];
     for (auto i : v) vis[i] = true;
if (!flag) return;
// now 是環的起點,我們先找到他在 v 的哪裡
     int z = find(v.begin(), v.end(), now) - v.begin();
vector <int> cycle(v.begin() + z, v.end());
     cycles.push_back(cycle);
int main() {
    cin >> n >> q;
    no.assign(n + 1, -1);
     cycle_idx.assign(n + 1, -1);
     vis.assign(n + 1, 0);

for (int u = 1; u <= n; u++) cin >> dp[u][0];
     for (int i = 1; i <= 18; i++) // 倍增表
          for (int u = 1; u <= n; u++)
    dp[u][i] = dp[dp[u][i - 1]][i - 1];
(int i = 1; i <= n; i++) {
    if (!vis[i]) find_cycle(i);</pre>
     int idx = 0;
     unordered_set<int> done;
     for (auto &i : cycles) {
   int c = 0;
           for (auto &j : i) {
    no[j] = c++;
    cycle_idx[j] = idx;
                done.insert(j);
     for (int i = 1; i <= n; i++) set_out_of_cycle_no(i, done);
for (int i = 1; i <= q; i++) {
   int u, v; cin >> u >> v;
              在同個環內
          if (cycle_idx[u] == cycle_idx
   [v] && cycle_idx[u] != -1 && cycle_idx[v] != -1) {
   int cyc_size = cycles[cycle_idx[u]].size();
                cout <<
                      (no[v] - no[u] + cyc_size) % cyc_size << "\n";</pre>
           // 都不再環內
          continue:
                if (wiint_go_to(u, no[v] - no[u]) == v) {
   cout << no[v] - no[u] << "\n";</pre>
                else cout << -1 << "\n";
           else if (cycle_idx[u]
                 == -1 && cycle_idx[v] != -1) { // v 在環內,二分搜
                == -1 && cycle_tux[v] ;- -2/
int l = -1, r = n;
while (l <= r) {
   int m = (l + r) / 2;
   if (cycle_idx[wiint_go_to
                     (u, m)] == cycle_idx[v]) r = m - 1;
else l = m + 1;
                     if (l <= n) {
                           ] + cycle_size) % cycle_size << "\n";
                else cout << -1 << "\n";
```

```
else { // u 在環內 b 不在,直接不可能 cout << -1 << "\n"; } }
```

3 Data Structure

3.1 BIT [d41d8c]

```
template < class T>
struct BIT {
                   // 全部以 0 based 使用
      int n:
      vector<T> bit;
           int n = 0) {      // 有幾個數
init(vector<T>(n));
      BIT(int n = 0) {
      BIT(vector<T> init_) { // 必須是 0-based
           init(init_);
      void init(int n_ = 0) {
   init(vector<T>(n_));
      }
      void init(vector<T> init_) { // 必須是 0-based
           n = init_.size();
bit.assign(n + 1, T());
for (int i = 0; i < n; i++) {</pre>
                modify(i, init_[i]);
           }
      void modify(int i, T val) {
    for (i++; i <= n; i += i & -i) {
        bit[i] += val;
    }</pre>
           }
      T query(int r) {
           T ans = 0;
for (r++; r; r -= r & -r) ans += bit[r];
return ans;
     T query(int l, int r) {
    return query(r) - query(l - 1);
template <class T>
struct TwoDimensionBIT {
     int nx, ny;
      vector < vector < T >> bit;
TwoDimensionBIT(int x = 0, int y = 0) {
           init(vector < vector < T >> (x + 1, vector < T > (y + 1)));
      TwoDimensionBIT
            (vector<vector<T>> init_) { // 必須是 0-based
           init(init_);
      void init(int x = 0, int y = 0) {
   init(vector<vector<T>>(x + 1, vector<T>(y + 1)));
      void init(vector<vector<T>> init_) { // 必須是 0-based
          }
      void modify(int x, int y, T mod) {
    for (x++; x <= nx; x += x & -x) {
        for (int</pre>
                        tmp = y + 1; tmp <= ny; tmp += tmp & -tmp) {
                      bit[x][tmp] += mod;
                }
           }
      T query(int rx, int ry) {
          for (rx++; rx; rx -= rx & -rx) {
    for (int tmp = ry + 1; tmp; tmp -= tmp & -tmp) {
        ans += bit[rx][tmp];
    }
}
           return ans;
      T query(int lx, int ly, int rx, int ry) {
           return query(rx, ry) - query(lx - 1,
ry) - query(rx, ly - 1) + query(lx - 1, ly - 1);
     }
}:
```

3.2 **DSU** [d41d8c]

```
struct DSU {
   vector < int > boss, siz;
   DSU(int n) { // 0 based
   boss.resize(n);
   iota(boss.begin(), boss.end(), 0);
   siz.assign(n, 1);
```

```
}
int find_boss(int x) {
    if (boss[x] == x) return x;
    return boss[x] = find_boss(boss[x]);
}
bool same(int x, int y) {
    return find_boss(x) == find_boss(y);
}
bool merge(int x, int y) {
    x = find_boss(x);
    y = find_boss(y);
    if (x == y) {
        return false;
    }
    if(siz[x] < siz[y]) swap(x, y);
    siz[x] += siz[y];
    boss[y] = x;
    return true;
}
int size(int x) {
    return siz[find_boss(x)];
}
};
</pre>
```

3.3 Increasing Array Queries [d41d8c]

```
const int maxn = 2e5+5;
int n, q;
[maxn], prefix[maxn], ans[maxn], BIT[maxn], contrib[maxn];
vector<pair<int, int>> queries[maxn];
void update(int pos, int val) {
    for (; pos <= n; pos += pos & -pos) BIT[pos] += val;</pre>
int query(int a, int b) {
    int ans = 0;
for (; b; b -= b&-b) ans += BIT[b];
for (a--; a; a -= a&-a) ans -= BIT[a];
void solve() {
    cin >> n >> q;
for (int i = 1; i <= n; i++) {
         cin >> nums[i];
         prefix[i] = prefix[i-1] + nums[i];
    formums[n + 1] = 1e9;
prefix[n + 1] = 2e18;
for (int i = 1; i <= q; i++) {
   int a, b; cin >> a >> b;
   queries[a].push_back({b, i});
    deque<int> mono; mono.push_front(n+1);
    mono.pop_front();
         contrib[i] = (mono.front() - 1 - i) *
        + (j.first
                                    - mono[pos]) * nums[mono[pos]]
                              - (prefix
                                   [j.first] - prefix[mono[pos]]);
    for (int i = 1; i <= q; i++) {
         cout << ans[i] << endl;</pre>
    }
```

3.4 線段樹 [d41d8c]

```
info.assign(4 << __lg(n), Info());</pre>
           function <void(
   int, int) > build = [&](int p, int l, int r) {
   if (r - l == 1) {
                     info[p] = init_[l];
                int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                pull(p);
          build(1, 0, n);
      (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
          if (r - l == 1)
  info[p] = v;
                return:
           int m = (l + r) / 2;
          if (x < m) {
                modify(2 * p, l, m, x, v);
                modify(2 * p + 1, m, r, x, v);
          pull(p);
      void modify(int p, const Info &i) {
          modify(1, 0, n, p, i);
      info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];</pre>
          int m = (l + r) / 2;
return query(p *
    2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
     Ínfo query
      (int ql, int qr) { return query(1, 0, n, ql, qr); } template < class F> // 尋找區間內,第一個符合條件的
      int findFirst
          (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
   return -1;</pre>
           if (l >= x && r <= y && !pred(info[p])) {</pre>
                return -1;
           if (r - l == 1) {
                return l;
           int m = (l + r) / 2;
          int res = findFirst(2 * p, l, m, x, y, pred);
if (res == -1) {
                res = findFirst(2 * p + 1, m, r, x, y, pred);
          return res;
      template < class F> // 若要找 last, 先右子樹遞迴即可
int findFirst(int l, int r, F & pred) {
    return findFirst(1, 0, n, l, r, pred);
};
// ---define structure and info plus---
struct Info {
   int sum;
Info operator + (const Info &a, const Info &b) {
    return { a.sum + b.sum };
// ---pizza_queries---
// 左邊的店(s < t): dis_l = (pizza[s] - s) + t;
// 右邊的店(t < s): dis_r = (pizza[s] + s) - t;
// 實作: 建左查詢線段樹跟右查詢線段樹, 用最小值pull
// 答案是 min(left_query(1, s) + t, right_query(s, end) + t);
// ---List Removals
// 維護區間內有幾個數字被選過
|// 用二分
      搜找右區間最小位,使得 ans - query == 1 ~ ans 被選過的數量
     --- CSES subarray queries:--
// tree[now].prefix
        = max(tree[lc].sum + tree[rc].prefix, tree[lc].prefix);
// tree[now].suffix
        = max(tree[lc].suffix+tree[rc].sum, tree[rc].suffix);
// tree[now].middle_max
        = max(lc 中, rc 中, lc 後 + rc 前, now 前, now 後)
```

3.5 懶標線段樹 [d41d8c]

```
| template <class Info, class Tag>
| struct LazySeg { // 左閉右開寫法
| int n;
| vector<Info> info;
| vector<Tag> tag;
| LazySeg() : n(0) {}
| LazySeg(int n_, Info v_ = Info()) {
| init(n_, v_);
| }
```

```
template < class F> // 若要找 last, 先右子樹遞廻即可
int findFirst(int l, int r, F &&pred) {
    return findFirst(1, 0, n, l, r, pred);
template <class T>
LazySeg(vector<T> init_) {
        init(init_);
void init(int n_, Info v_ = Info()) {
        init(vector(n_, v_));
                                                                                                                                   // ---define structure and info plus---
                                                                                                                                   struct Tag {
   int set_val; int add;
template <class T>
                                                                                                                                            void apply(const Tag& v) {
   if (v.set_val) {
        void init (vector<T> init_) {
        info.assign(4 << __lg(n), Info());
tag.assign(4 << __lg(n), Tag());
function <void(
   int, int, int)> build = [&](int p, int l, int r) {
   if (r - l == 1) {
                                                                                                                                                             set_val = v.set_val;
add = v.add;
                                                                                                                                                     else {
                                                                                                                                                             add += v.add;
                         info[p] = init_[l];
                         return;
                                                                                                                                           }
                                                                                                                                   };
                 int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                                                                                                                                    struct Info {
                                                                                                                                            int sum;
                                                                                                                                            void apply(int l, int r, const Tag &v) {
                                                                                                                                                    if (v.set_val) {
    sum = (r - l) * v.set_val;
                 pull(p);
        build(1, 0, n);
                                                                                                                                                     sum += (r - l) * v.add;
void pull
                                                                                                                                           }
(int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
                                                                                                                                   Info operator + (const Info &a, const Info &b) {
                                                                                                                                            return { a.sum + b.sum };
         tag[p].apply(v);
                                                                                                                                   // polvnomial aueries
void push(int p, int l, int r) {
                                                                                                                                   // 設置梯形的底跟加了幾次, apply_tag 時底為 l 的合, d 為加給次
        int m = (l + r) / 2;
if (r - l >= 1) {
    apply(p * 2, l, m, tag[p]);
    apply(p * 2 + 1, m, r, tag[p]);
}
                                                                                                                                  |// 所以 sum += (底 * 2 + 次 * 區間) * 區間 / 2;
                                                                                                                                   3.6 莫隊 [d41d8c]
         tag[p] = Tag();
                                                                                                                                   struct query {
                                                                                                                                   int l, r, id;
} typedef query;
void MO(int n, vector<query> &queries) {
  int block = sqrt(n);
void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
    }
}
                                                                                                                                            function <bool(query, query)> cmp = [&](query a, query b) {
   int block_a = a.l / block;
   int block_b = b.l / block;
   if (block_a != block_b) return block_a < block_b;
   return a.r < b.r;</pre>
                 return;
         int m = (l + r) / 2;
         push(p);
         if (x < m) {
                 modify(2 * p, l, m, x, v);
         } else {
                                                                                                                                            sort(queries.begin(), queries.end(), cmp);
                modify(2 * p + 1, m, r, x, v);
                                                                                                                                    void compress(vector<int> &nums) {
                                                                                                                                            vector < int > sorted = nums;
sort(sorted.begin(), sorted.end());
        pull(p);
void modify(int p, const Info &i) {
                                                                                                                                            sorted.erase
         modify(1, 0, n, p, i);
                                                                                                                                                       (unique(sorted.begin(), sorted.end()), sorted.end());
                                                                                                                                            for (int i = 0; i < nums.size(); i++) {
    nums[i] = lower_bound(sorted.begin</pre>
info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    push(p, l, r);
}</pre>
                                                                                                                                                               (), sorted.end(), nums[i]) - sorted.begin() + 1;
                                                                                                                                           }
                                                                                                                                   }
        return query(p *
2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
                                                                                                                                   3.7 Treap [d41d8c]
                                                                                                                                    struct Treap {
                                                                                                                                            Treap *1,
                                                                                                                                            (int ql, int qr) { return query(1, 0, n, ql, qr); }
(Int qt, the qt, the qt, the const and 
                                                                                                                                                    pri = rand();
l = r = nullptr;
                                                                                                                                                     subsize = 1; rev_valid = 0;
                                                                                                                                            fint m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
                                                                                                                                                    for(auto i : {l, r}) {
    if (i) subsize += i->subsize;
                                                                                                                                   }:
void range_apply(int l, int r, const Tag &v) {
    range_apply(1, 0, n, l, r, v);
                                                                                                                                   int size(Treap *treap) {
   if (treap == NULL) return 0;
                                                                                                                                            return treap->subsize;
template < class F> // 尋找區間內,第一個符合條件的
int findFirst
                                                                                                                                    // lazy
        (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
    return -1;</pre>
                                                                                                                                    void push(Treap *t) {
                                                                                                                                           if (!t) return;
if (!t) return;
if (t->rev_valid) {
    swap(t->l, t->r);
    if (t->l) t->l->rev_valid ^= 1;
    if (t->r) t->r->rev_valid ^= 1;
         if (l >= x && r <= y && !pred(info[p])) {</pre>
                return -1:
        if (r - l == 1) {
                                                                                                                                            t->rev_valid = false;
                return l;
                                                                                                                                   int m = (l + r) / 2;
        push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
         if (res == -1)
                 res = findFirst(2 * p + 1, m, r, x, y, pred);
                                                                                                                                                             (a->r, b); // a->r = new, inorder, make sense
                                                                                                                                                    a->pull();
         return res;
                                                                                                                                                    return a;
```

```
b->l = merge
        (a, b->l); // new->l = a, inorder, make sense
b->pull();
        return b;
auto [a, b] = split(root->r, k - size(root->l) - 1);
root->r = a;
        root->pull();
        return {root, b};
    else {
        auto [a, b] = split(root->l, k);
root->l = b;
        root->pull();
        return {a, root};
   }
void Print(Treap *t) {
    if (t) {
    // push(t);
    Print(t->l);
                       // lazy
        cout << t->val;
        Print(t->r);
void substring_rev() {
   int n, m; cin >> n >> m;
   Treap *root = nullptr;
    for (auto c : str) {
    root = merge(root, new Treap(c));
    - - merge(a, d); // Notice the order
root = merge(b, c);
    Print(root);
```

4 Flow

4.1 Dinic [7f4d14]

```
// template dinic max flow
struct edge {
   int v, w, rev_id;
int n, m, ans = 0;
int n, m, ans = 0;
vector<edge> adj[505];
vector<int> lev(505), vis(505);
bool label_level(){    // 標記深度, 如果到不了終點    return false
    fill(all(lev), -1); lev[1] = 0;
    queue<int> q;    q.push(1);
    while (!q.empty()) {
             int u = q.front(); q.pop();
for (auto &[v, w, rev_id] : adj[u]) {
   if (w > 0 && lev[v] == -1) {
                          q.push(v);
                          lev[v] = lev[u] + 1;
                   }
      return (lev[n] == -1 ? false : true);
int dfs(int u, int flow){
      if (u == n) return flow;
for (auto &[v, w, rev_id] : adj[u]) {
    if (lev[v] == lev[u] + 1 && !vis[v] && w > 0) {
                   vis[v] = true;
int ret = dfs(v, min(flow, w));
if (ret > 0) {
                          w -= ret:
                          adj[v][rev_id].w += ret;
                   }
            }
      }
      return 0; // 到不了終點就會 return 0
void add_edge(int u, int v, int w) { // 無向圖的話兩邊都是 w adj[u].push_back({v, w, (int)adj[v].size()});
       adj[v].push_back({u, 0, (int)adj[u].size() - 1});
void dinic() {
       while (label_level()) {
             while (true) {
                   fill(all(vis), 0);

int tmp = dfs(1, inf);
                   if (tmp == 0) break;
```

```
ans += tmp:
       cout << ans:
 }
 // Distinct Route
// 給你一張有向圖,求從走 1 到 n 的最多方法數,並且邊不重複
// dfs 要改成
int dfs(int u, int flow){
    if (u == n) return flow;
    for (auto &[v, w, rev_id, arg_valid] : adj[u]){
        if (lev[v] == lev[u] + 1 && !vis[v] && w > 0) {
            vis[v] - true:
                   vis[v] = true;
int ret = dfs(v, min(flow, w));
if (ret > 0) {
                         w -= ret;
                         adj[v][rev_id].w += ret;
                         if (arg_valid) {  // 走的是 arg 路, Reset
    arg_valid = 0;
    adj[v][rev_id].arg_valid = 0;
                               [v][rev_id].arg_valid = 1; // 走正常路
                         return ret;
                  }
            }
      }
       return 0; // 到不了終點就會 return 0
 bool get_road(int now, vector<int> &ans, vector<bool> &vis) {
       if (now == 1) return true;
for (auto &[v, w, rev_id, arg_valid] : adj[now]) {
    if (arg_valid && !vis[v]){
                   ans.push_back(v);
                  vis[v] = true;
bool flag = get_road(v, ans, vis);
if (flag) {
    arg_valid = false;
}
                         return true;
                   ans.pop_back();
            }
       return false;
 4.2 Min Cut [0ab707]
```

```
| // CSES Police Chase
 int g[505][505]; // 以 O(1) 紀錄存在邊
void solve(){
        cin >> n >> m;
        for (int i = 0; i < m; i++) {
   int u, v; cin >> u >> v;
               add_edge(u, v, 1);
        dinic();
        fill(all(vis), 0);
unordered_set<int> reach;
        auto find = [&](auto self, int u) -> void {
   if (!vis[u]) {
      vis[u] = 1;
   }
                      reach.insert(u);
                     for (auto [v, w, _] : adj[u]){
   if(w > 0){
                                   self(self, v);
                     }
              }
        find(find, 1);
        renu(ring, 1);
cout << ans << "|n";
for (auto u : reach) {
    for (auto [v, w, _] : adj[u]) {
        if (g[</pre>
                            u][v] && !w && reach.find(v) == reach.end()) {
cout << u << " " << v << "\n";
// ans = sum(u_to_v)
                     }
               }
        }
```

4.3 Bipartite Matching [5e0de5]

```
if (vis[v] == 0) {
    vis[v] = 1;
                                                                                                                   }
                            if (match
                                 [v] == -1 || self(self, match[v])) {
match[v] = u;
                                  return true;
                           }
                     }
                return false;
           for (int i = 1; i <= n; i++) {
                 fill(all(vis), 0);
                dfs(dfs, i);
                                                                                                             Tf f = INF_Flow;
           for (int i = n + 1; i <= n + m; i++) {
    if (match[i] != -1) {</pre>
                                                                                                             int cur = t;
while (cur != s) {
                      cnt += 1;
                                                                                                                   cur = e.from;
           for (int i = n + 1; i <= n + m; i++) {
    if (match[i] != -1) {</pre>
                                                                                                             }
f = min<Tf>(f, need);
                      ans.push_back({match[i], i - n});
                                                                                                             need -= f;
           return { cnt, ans };
                                                                                                             cur = t;
     }
                                                                                                             while (cur != s) {
int main(){
     int n, m, e; cin >> n >> m >> e;
vector<vector<int>> adj(n + m + 1);
                                                                                                                   cur = e.from;
     for (int i = 1; i <= e; i++) {
   int u, v; cin >> u >> v;
   adj[u].push_back(v + n);
   adj[v + n].push_back(u);
                                                                                                             if (need == 0) break;
     Bipartite_Matching bip(n, m, adj);
auto [cnt, ans] = bip.matching();
cout << cnt << "\n";</pre>
     for (auto [u, v] : ans) {
    cout << u << " " << v << "\n";
                                                                                                       Tf flow = 0;
Tc cost = 0;
}
4.4 MCMF [f622a1]
                                                                                                             Tf f = INF_Flow;
template < class Tf, class Tc>
struct MCMF {
     int from, to;
           Tf flow, cap; // 流量跟容量
           Tc cost;
     vector<vector<int>> adj;
                                                                                                             cur = t;
while (cur != s) {
     vector<Edge> edges; // 幫每個 edge 編號
vector<Tc> dis, pot; // johnson algorithm, using spfa
     vector<int> par; // 路徑恢復 vector<bool> vis;
     MCMF() { init(); }
MCMF(int n_) { init(n_); }
      void init(int n_ = 0) {
           n = n_;
cur = 0;
                                                                                                 }
           adj.resize(n);
                                                                                            };
           edges.clear();
           pot.assign(n, 0);
                                                                                                    String
                                                                                            5
                                                                                            5.1 KMP [132b98]
     void add_edge(int u, int v, Tf cap, Tc cost){
           edges.push_back({u, v, 0, cap, cost});
adj[u].push_back(cur++);
                                                                                            struct KMP {
           edges.push_back({v, u, 0, 0, -cost});
adj[v].push_back(cur++);
                                                                                                  string sub;
vector<int> failure;
                                                                                                  KMP(string &sub) {
                                                                                                       this - > sub = sub;
     bool spfa(int s, int t) {
    dis.assign(n, INF_COST);
    par.assign(n, -1);
    vis.assign(n, false);
    queue<int> q;
                                                                                                        buildFailFunction();
           dis[s] = 0;
q.push(s);
vis[s] = true;
           while (!q.empty()) {
    int u = q.front();
                                                                                                       }
                q.pop();
vis[u] = false;
                for (int id : adj[u]) {
    Edge &e = edges[id];
                      int v = e.to;
                      if (!vis[v]) {
```

a.push(v): vis[v] = true;

}

```
return dis[t] != INF_COST;
// 限定 flow, 最小化 cost
pair<ff, Tc> work_flow(int s, int t, Tf need = -1) {
    if (need == -1) need = INF_Flow;
    If flow = 0;
    Tc cost = 0;
        while (spfa(s, t)) {
    for (int i = 0; i < n; i++) {
        if (dis[i] != INF_COST) pot[i] += dis[i];</pre>
                       Edge &e = edges[par[cur]];
f = min(f, e.cap - e.flow);
                flow += f;
cost += f * (pot[t] - pot[s]);
                       Edge &e = edges[par[cur]];
e.flow += f;
                       edges[par[cur] ^ 1].flow -= f;
        return make_pair(flow, cost);
// 限定 cost, 最大化 flow
pair<Tf, Tc> work_budget(int s, int t, Tc budget = -1) {
    if (budget == -1) budget = INF_COST;
        while (spfa(s, t)) {
    for (int i = 0; i < n; i++) {
        if (dis[i] != INF_COST) pot[i] += dis[i];</pre>
                int cur = t;
while (cur != s) {
    Edge &e = edges[par[cur]];
    f = min(f, e.cap - e.flow);
    cur = e.from;
                }
f = min<Tf>(f, budget / (pot[t] - pot[s]));
                flow += f;
cost += f * (pot[t] - pot[s]);
budget -= f * (pot[t] - pot[s]);
                       te (cul := s) {
   Edge &e = edges[par[cur]];
   e.flow += f;
   edges[par[cur] ^ 1].flow -= f;
   cur = e.from;
                if (budget == 0) break;
        return make_pair(flow, cost);
```

```
failure.resize(sub.size(), -1);
void buildFailFunction() {
    for (int i = 1; i < sub.size(); i++) {
        int now = failure[i - 1];
}</pre>
                  while (now != -1
     && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
 ,
vector<<mark>int</mark>> KMPmatching(string &s) {
        vector < int > match;
for (int i = 0, now = -1; i < s.size(); i++) {</pre>
                  // now is the compare sucessed length -1
while (s[i] !=
                 while (s[i] !=
    sub[now + 1] && now != -1) now = failure[now];
// f stores if comparison fail, move to where
if (s[i] == sub[now + 1]) now++;
if (now + 1 == sub.size()) {
    match.push_back(i - now);
    now = failure[now];
}
                  }
```

5.3 Duval Algorithm [f9dcca]

```
// duval_algorithm
 // 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
 vector<string> duval(string s) {
   int i = 0, n = s.size();
       vector<string> res;
       while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
      else k++;
}</pre>
             while (i <= k) {
                   res.push_back(s.substr(i, j - k));
i += j - k;
             }
       return res;
 // 最小旋轉字串
 string min_round(string s) {
      s += s;
int i = 0, n = s.size();
       int start = i;
       while (i < n / 2) {
    start = i;</pre>
             int k = i, j = i + 1;
while (s[k] <= s[j] && j < n) {
    if (s[k] < s[j]) k = i;
    else k++;
             while (i <= k) {</pre>
                   i += j - k;
       return s.substr(start, n / 2);
```

5.4 Manacher [9c9ca6]

5.5 Trie [3b3aa0]

```
struct trie_node {
          bool is_word;
vector<trie_node *> children;
          trie_node() {
   is_word = false;
   children.resize(26, NULL);
     trie_node *root = new trie_node();
     void insert(string &s) {
          trie_node *cur = root;
for (int i = 0; i < s.size(); i++) {</pre>
               int idx = s[i] - 'a';
               if (cur->children[idx] == NULL) {
                    cur->children[idx] = new trie node();
               cur = cur->children[idx];
          cur->is_word = true;
     bool is_in_trie(string &s) {
    trie_node *cur = root;
          for (int i = 0; i < s.size(); i++) {</pre>
               if (cur->
               children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
          return true;
     int search_i_start(string &s, int i, vector<int> &dp) {
          trie_node *cur = root;
int sz = s.size(), ans = 0;
          for (int j = i; j < sz; j++) {
   if (cur</pre>
                                             ->children[s[i]
               cur = cur->children[s[j] -
               if (cur->is_word)
                    (ans += dp[j + 1]) \% = mod;
          return ans;
    }
};
int main() {
     // 找到 sub 集合裡,可以重複用,組成 s 的組數
     Trie trie;
     string s; cin >> s;
int sz = s.size();
     // dp 代表 i 開頭到最後的配對總數
     // 找到有結尾為 stop 的 dp[i] += dp[j + 1]
     int n; cin >> n;
vector<int> dp(sz + 1, 0);
for (int i = 0; i < n; i++) {
    string sub; cin >> sub;
          trie.insert(sub);
     dp[sz] = 1;
for (int i = sz - 1; i >= 0; i--) {
    dp[i] = trie.search_i_start(s, i, dp);
     cout << dp[0] << endl;</pre>
```

6 Math

6.1 質因數分解 [ee1622]

```
| // a^(m-1) = 1 (mod m)
| // a^(m-2) = 1/a (mod m)
| // EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)
| // Filter + DP; DP save min factor 'recur' factor decomposition
| // FacNums = (x+1)(y+1)(z+1)...
| // FacSum = (a^0+a^1...+a^x)(b^0+...+b^y)
| // FacMul = N(x+1)(y+1)(z+1)/2
| vector < int > is_prime;
| // 1 代表是質數 , 非 1 不是
| void init(int n) {
| is_prime.assign(n + 1, 1);
| for (int i = 2; i <= (int)sqrt(n) + 1; i++) {
| if (is_prime[i] == 1) {
| for (int j = i + i; j <= n; j += i) {
| is_prime[j] = i;
| }
| }
| }
| int main() {
| init(10000000);
| column | long | long
```

```
if (n <= 4) {
    vector < int > v = {0, 1, 1, 2, 4};
          mp[is_prime[q]]++;
q /= is_prime[q];
                                                                                                    ans = v[n];
     if (q != 1) mp[q]++;
for (auto [a, b] : mp) {
    ans *= b + 1;
                                                                                                   Mat init({{4, 2, 1}, {2, 1, 1}, {1, 1, 0}});
                                                                                                   Mat T(3);
     cout << ans << "\n";
                                                                                                    T.matrix = \{\{1, 1, 0\}, \{1, 0, 1\}, \{1, 0, 0\}\};
                                                                                                   T ^= n - 4;
init *= T;
6.2 中國餘數定理 [d41d8c]
                                                                                                   ans = init.matrix[0][0];
ll exgcd(ll a, ll b, ll &x, ll &y) {
                                                                                              cout << ans << "\n";
                                                                                        }
     if (!b) {
    x = 1, y = 0;
                                                                                        // 初始矩陣
// f4 f3 f2
// f3 f2 f1
// f2 f1 f0
                                                                                                            轉移式
                                                                                                          1 1 0  f5 f4 f3
1 0 1 => f4 f3 f2
1 0 0  f3 f2 f1
     ll g = exgcd(b, a % b, y, x);
                                                                                         6.4 模除計算 [9b1014]
     y -= a / b * x;
     return g;
                                                                                        using i64 = long long;
template < class T >
ĺl inv(ll x, ll m){
     ll a, b;
exgcd(x, m, a, b);
                                                                                         constexpr T power(T a, i64 b) {
                                                                                                         1;
     a %= m;
if (a < 0) a += m;
                                                                                              for (; b; b /= 2, a *= a) {
    if (b % 2) {
        res *= a;
}
     return a:
                                                                                                   }
// remain, mod
ll CRT(vector<pair<ll, ll>> &a){
    ll prod = 1;
    for (auto x : a) {
        prod *= x.second;
}
                                                                                              return res;
                                                                                        }
                                                                                         constexpr i64 mul(i64 a, i64 b, i64 p) {
   i64 res = a * b - i64(1.L * a * b / p) * p;
     il res = 0;
                                                                                              res %= p;
if (res < 0) {
    res += p;
     for (auto x : a) {
    auto t = prod / x.second;
    res += x.first * t % prod * inv(t, x.second) % prod;
           if(res >= prod) res -= prod;
                                                                                              return res:
     return res;
                                                                                         template < i64 P>
}
                                                                                         struct MLong {
                                                                                              i64 x;
6.3 矩陣快速幕 [d41d8c]
                                                                                              constexpr MLong() : x{} {}
constexpr MLong(i64 x) : x{norm(x % getMod())} {}
struct Mat {
     int m. n:
                                                                                              static i64 Mod;
      vector<vector<ll>> matrix;
                                                                                              constexpr static i64 getMod() {
   if (P > 0) {
      void init(int m, int n) {
    this->m = m; this->n = n;
                                                                                                         return P;
           matrix.resize(m);
                                                                                                   } else {
           for (int i = 0; i < m; i++) {
    matrix[i].resize(n);</pre>
                                                                                                        return Mod:
          }
                                                                                              constexpr static void setMod(i64 Mod_) {
    Mod = Mod_;
     Mat(int m, int n) { init(m, n); }
Mat(int n) { init(n, n); }
Mat(vector<vector<ll>> matrix) {
                                                                                              constexpr i64 norm(i64 x) const {
          this->m = matrix.size();
this->n = matrix[0].size();
                                                                                                   if (x < 0) {
    x += getMod();</pre>
           this -> matrix = matrix;
                                                                                                   if (x >= getMod()) {
                                                                                                         x -= getMod();
     Mat unit(int n) { // 單位矩陣
           Mat res(n);
for (int i = 0; i < n; i++) {
    res.matrix[i][i] = 1;</pre>
                                                                                                   return x;
                                                                                              constexpr i64 val() const {
           return res;
                                                                                                   return x;
     Mat operator * (Mat b) {
                                                                                              explicit constexpr operator i64() const {
           int m = matrix.size
   (), n = b.matrix[1].size(), k = matrix[0].size();
                                                                                                   return x;
           Mat ans(m, n);
                                                                                              constexpr MLong operator -() const {
           MLong res;
res.x = norm(getMod() - x);
                                                                                                   return res;
                                                                                              constexpr MLong inv() const {
                                                                                                   assert(x != 0);
return power(*this, getMod() - 2);
                     }
               }
                                                                                              constexpr MLong &operator*=(MLong rhs) & {
    x = mul(x, rhs.x, getMod());
           return ans:
                                                                                                   return *this;
     constexpr MLong &operator+=(MLong rhs) & {
  x = norm(x + rhs.x);
  return *this;
           while (p > 0) {
    if (p & 1) {
        ans *= *this;

                                                                                              constexpr MLong &operator -=(MLong rhs) & {
                                                                                                   x = norm(x - rhs.x);
return *this;
                *this *= *this;
                p >>= 1;
                                                                                              constexpr MLong &operator/=(MLong rhs) & {
                                                                                                   return *this *= rhs.inv();
           return ans;
                                                                                              friend constexpr MLong operator*(MLong lhs, MLong rhs) {
```

MLong res = lhs;
res *= rhs;

return res;

Mat operator ^= (ll p) { *this = *this ^ p; return *this; }

signed main() {

int n; cin >> n; ll ans;

```
friend constexpr MLong operator+(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res += rhs;
            return res;
      friend constexpr MLong operator-(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res -= rhs;
            return res;
      friend constexpr MLong operator/(MLong lhs, MLong rhs) {
   MLong res = lhs;
            res /= rhs;
            return res:
              constexpr istream &operator>>(istream &is, MLong &a) {
            a = MLong(v);
            return is:
      friend constexpr
               ostream & operator << (ostream & os, const MLong & a) {
            return os << a.val();</pre>
      friend constexpr bool operator==(MLong lhs, MLong rhs) {
   return lhs.val() == rhs.val();
      friend constexpr bool operator!=(MLong lhs, MLong rhs) {
   return lhs.val() != rhs.val();
};
i64 MLong<0LL>::Mod = i64(1E18) + 9;
constexpr i64 P = 998244353;
using Z = MLong < P >;
// using Z = MLong<OLL>; // change Mod
struct Comb {
      i64 n;
vector <Z> _fac;
vector <Z> _invfac;
vector <Z> _inv;
Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
Comb(i64 n) : Comb() { init(n); }
      void init(i64 m) {
    m = min(m, Z::getMod() - 1);
            if (m <= n) return;
  fac.resize(m + 1);
    _invfac.resize(m + 1);</pre>
            _
_inv.resize(m + 1);
            for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;</pre>
            }
_invfac[m] = _fac[m].inv();
for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
            n = m;
      }
Z fac(i64 m) {
   if (m > n) init(2 * m);
        fac[m];
      Z invfac(i64 m) {
            if (m > n) init(2 * m);
return _invfac[m];
     }
Z inv(i64 m) {
   if (m > n) init(2 * m);
   return _inv[m];
      Z binom(i64 n, i64 m) {
   if (n < m || m < 0) return 0;
   return fac(n) * invfac(m) * invfac(n - m);</pre>
      } comb; // 注意宣告, 若要換模數需重新宣告
```

6.5 樹論分塊 [06204a]

```
val %= mod; sum %= mod;
ans += val * sum;
ans %= mod;
}
cout << ans << "\n";
}
```

6.6 Mobius Theorem

- 數論分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理 出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d|n} \mu(d) = \begin{cases} 1 & \text{for } n = 1 \\ 0 & \text{for } n \neq 0 \end{cases}$$

2. μ是常數函數1的反元素

 $\Rightarrow \mu * 1 = \epsilon$, $\epsilon(n)$ 只在n = 1時為 1 , 其餘情況皆為 0 。

 $-\phi$ 歐拉函數: x以下與x互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^{i}) \\ &= 1 + p^{0}(p-1) + p^{1}(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^{c} \\ &= id \end{split}$$

• 莫比烏斯反演公式

- $f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$ - $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

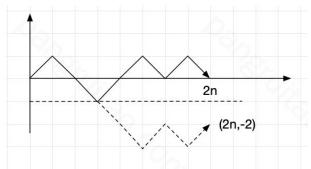
• 例子

$$\begin{split} &\sum_{i=a}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \frac{y}{k} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{x} [d|i] \sum_{j=1}^{y} [d|j] \ \mathrm{d} \ \mathrm{PBER} \ \mathrm{i} \ \mathrm{FRA} \ \mathrm{1} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.7 **莫比烏斯反演** [d41d8c]

```
cout << cal
    (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k,
(c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "|n";
```

6.8 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2)

假設往上有 x 個,往下有 y 個,會有:

$$\begin{cases} x + y = 2n \\ y - x = 2 \end{cases} \Rightarrow \begin{cases} x = n - 1 \\ y = n + 1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.9 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- X/G:本質不同的方案的集合
- X^g :對於某一種操作g,所有方案中,經過g這種翻轉後保持不變的方案 的集合
- 集合取絕對值代表集合數

Search and Gready

7.1 二分搜 [d41d8c]

```
int main() {
    int l = 1, r = 10;
    // 1 to tar, find tar
    while (l <= r) {
        int m = (l + r) / 2;
    }
}</pre>
                  if (check(m)) l = m + 1;
                  else r = m -
         cout << r;
         // tar to end
while (l <= r) {
   int m = (l + r) / 2;
   if (check(m)) r = m - 1;
                  else l = m + 1;
         cout << l;
}
```

7.2 三分搜 [d41d8c]

```
' 找極值問題, 遞增遞減
void solve() {
    int l = 0, r = 10, ans = 0; // ans 紀錄答案 while (l <= r) {
         int d = (r - l) / 3; // 差
         int ml = l + d, mr = r - d; // mr 要用減的
auto cal = [&](int m) -> int {
             int x = 0;
              return x; // 計算答案
         int ansl = cal(ml), ansr = cal(mr);
         if (ansl < ansr) {
    l = ml + 1;</pre>
         else r = mr - 1;
    }
```

8 Tree

8.1 LCA [9f95b1]

```
vector<vector<int>> par(maxn. vector<int>(18));
vector <int> depth(maxn + 1);
vector <int> dfn(maxn);
void build_lca(int n, vector<vector<pair<int, int>>> &tree) {
   auto dfs = [&](auto self, int u, int pre) -> void {
              for (auto [v, w] : tree[u]) {
   if (v == pre) continue;
   par[v][0] = u; // 2 ^ 0
   depth[v] = depth[u] + 1;
   self(self, v, u);
}
              }
       fs(dfs, 1, 0);
for (int i = 1; i <= 18; i++) {
    for (int j = 1; j <= n; j++) {
        par[j][i] = par[par[j][i - 1]][i - 1];
}</pre>
       }
a = par[a][i];
       f( a == b) return a;
for (int i = 17; i >= 0; i--) {
   if (par[a][i] != par[b][i])
                     a = par[a][i], b = par[b][i];
       return par[a][0];
```

8.2 樹重心 [79e16c]

```
int get_centroid(vector<vector<int>> &
     adj, vector int> &vis, vector int> &siz, int u, int pre) {
auto get_sz = [&](auto &&self, int u, int pre) -> void {
    siz[u] = 1;
          for (int v : adj[u]) {
   if (v == pre) continue;
   if (vis[v]) continue;
   self(self, v, u);
                siz[u] += siz[v];
          }
     return self(self, tot_sz, v, u);
                }
          return u;
     get_sz(get_sz, u, pre);
return get_cen(get_cen, siz[u], u, pre);
```

8.3 樹壓平 [51199c]

```
點加值 = 所有子節點區間加值,求單點,使用 bit,做前綴差分
// CSES 1138_Path Queries
int main(){
     int n, q; cin >> n >> q;
vector <int> node_value(n + 1), euler_ordered_value(n);
for (int i = 1; i <= n; i++) {</pre>
          cin >> node_value[i];
     vector<vector<int>> tree(n + 1);
     for (int i = 1; i < n; i++) {
   int u, v; cin >> u >> v;
          tree[u].push_back(v);
tree[v].push_back(u);
      vector<pair<<mark>int</mark>, <mark>int</mark>>> tree_mapping(n + 1);
     int cnt = 0:
     auto dfs = [&](auto self, int u, int par) -> void {
    euler_ordered_value[++cnt] = node_value[u];
          tree_mapping[u].first = cnt;
for (auto v : tree[u]) {
   if (v == par) continue;
                self(self, v, u);
          tree_mapping[u].second = cnt;
     dfs(dfs, 1, 0);
     if (tree_mapping[i].first < n) { // root 就不用扣了</pre>
                bit.modify
                      (tree mapping[i].second + 1. -node value[i]):
     }
```

8.4 Heavy Light Decomposition [6791f6]

```
vector < int > siz, top, dep, parent, in, out, seq;
vector<vector<int>> adi:
int cur:
HLD() {}
HLD(int n) {
     init(n);
void init(int n) {
     this - > n = n;
     siz.resize(n);
     top.resize(n);
     dep.resize(n);
     parent.resize(n);
     in.resize(n);
     out.resize(n);
     seq.resize(n);
     cur = 0:
     adj.assign(n, {});
void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
void work(int root = 0) {
  top[root] = root;
  dep[root] = 0;
     parent[root] = -1;
     dfs1(root):
     dfs2(root);
void dfs1(int u) {
    if (parent[u] != -1) {
          adj[u].erase(find
                 (adj[u].begin(), adj[u].end(), parent[u]));
     }
     siz[u] = 1;
     for (auto &v : adj[u]) {
    parent[v] = u;
          dep[v] = dep[u] + 1;
          dfs1(v);
siz[u] += siz[v];
          if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
          } // 讓 adj[u][0] 是重子節點
     }
void dfs2(int u) {
     in[u] = cur++;
     seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
  top[v] = v == adj[u][0] ? top[u] : v;
     out[u] = cur;
u = parent[top[u]];
} else {
               v = parent[top[v]];
     return dep[u] < dep[v] ? u : v;</pre>
int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
int jump(int u, int k) {
    if (dep[u] < k) {</pre>
     int d = dep[u]
     int d = dep[u] - k;
while (dep[top[u]] > d) {
          u = parent[top[u]];
```

```
return seq[in[u] - dep[u] + d];
     bool isAncester(int u. int v) {
          // 判斷 u 是否是 v 的祖先
return in[u] <= in[v] && in[v] < out[u];
     int rootedParent(int u, int v) {
          // 根據新根節點 u 計算 v 的父節點
          swap(u, v);
          if (u == v) {
              `return´u;
          if (!isAncester(u, v)) {
               return parent[u];
          auto it = upper_bound(adj
   [u].begin(), adj[u].end(), v, [&](int x, int y) {
   return in[x] < in[y];</pre>
          }) - 1;
return *it;
     int rootedSize(int u, int v) {
          // 根據新根節點 u 計算子樹 v 的大小
          if (u == v) {
               return n;
          if (!isAncester(v, u)) {
               return siz[v];
          return n - siz[rootedParent(u, v)];
     int rootedLca(int a, int b, int c) {
    // 根據新的根節點計算三個節點 a > b 和 c 的最近公共祖先
    return lca(a, b) ^ lca(b, c) ^ lca(c, a);
};
```

8.5 Virtual Tree [622e69]

```
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
// 可以建立虚樹達成快速樹 DP
 | // 可以建立虛樹達成快速樹 DP

// 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
        vt[stk[top - 1]].push_back(stk[top]), top--;
    if (stk[top - 1] != l) {
        vt[l].push_back(stk[top]);
        stk[top] = l;
    } else vt[l].push_back(stk[top--]);
    stk[++top] = u;
            stk[++top] = u:
  void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
    vt[u].clear();
  }
void solve(int n, int q) {
    vector g(n + 1, vector<pair<int, int>>());
    vector vt(n + 1, vector<int>()); // dfs 完清除, 否則會退化
    vector<tl> dp(n + 1), iskey(n + 1);
    for (int i = 0; i < n - 1; i++) {
        int u, v, w; cin >> u >> v >> w;
        g[u].push_back({v, w});
        g[v].push_back({u, w});
}
           build_lca(n, g);
           build(n, g);
build(n, g);
for (int i = 0; i < q; i++) {
   int m; top = -1; cin >> m;
   vector<int> key(m);
                    for (int j = 0; j < m; j++) {
    cin >> key[j];
                              iskey[key[j]] = 1;
                    key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
                    });
for (int x : key) insert(x, vt);
                     while (top
                                 > 0) vt[stk[top - 1]].push_back(stk[top]), --top;
                     auto dfs = [&](auto self, int u) -> void {
                              for (auto v : vt[u]) {
    self(self, v);
                                       if (iskey[v]) {
                                                dp[u] += min_dis[v];
                                                 // 砍掉 1 到 v 之間最短的路
                                                dp[u] += min(dp[v], min_dis[v]);
                                       iskev[v] = dp[v] = 0;
                              vt[u].clear();
```

```
dfs(dfs, key[0]); // key[0] 一定是 root
cout << dp[key[0]] << "\n";
iskey[key[0]] = dp[key[0]] = 0;
}
```

9 DP

9.1 背包問題 [6d6b63]

```
// 考慮前 i 個,預算有 j 塊錢的最多 page
int main(){
    int n, bud;
cin >> n >> bud;
    vector <int> dod,
vector <int> dp(n + 1, vector <int> (bud + 1));
vector <int> Page(n + 1, 0);
vector <int> Price(n + 1, 0);
    for(int i = 1; i <= n; i++){</pre>
         cin >> Price[i];
    for(int i = 1; i <= n; i++){
    cin >> Page[i];
     for (int i = 1; i <= n; i++) {</pre>
          for (int j = 1; j <= bud; j++) {</pre>
              if (j >= Price[i]) { // 買得起
                    // 不買或買
                    dp[i][j] = max(dp[i
                          ij[j], dp[i - 1][j - Price[i]] + Page[i]);
                    dp[i][j] = dp[i - 1][j];
         }
    cout << dp[n][bud] << "\n";
```

9.2 Bitmask [b18541]

```
void travel_exactly_once(){
      // [走過的路][終點]
      vector < vector < int >> dp(1 << 20, vector < int > (20, 0));
      vector < int > rev_adj[20];
int n, m; cin >> n >> m;
for(int i = 0; i < m; i++){</pre>
            int u, v; cin >> u >> v;
rev_adj[--v].push_back(--u);
      dp[1][0] = 1;
for (int road = 0; road < (1 << n); road++) {</pre>
            // 沒經過起點,不用走
if (road & 1 == 0) continue;
             // 有終點但沒全部走過
             if (road & (1
                      << (n - 1)) && road != ((1 << n) - 1)) continue;
             // DP,隨便選定一個當前路徑的終點
             for (int end = 0; end < n; end++) {</pre>
                   // 路徑沒包含假定的 end
if ((road & (1 << end)) == 0) continue;
                   // 去除終點,得到 pre_road
                   for (int pre_road 的終點
for (int pre_road_end : rev_adj[end]) {
    if ((road & (1 << pre_road_end))) {
                                dp[road
                                | ][end] += dp[pre_road][pre_road_end];
dp[road][end] %= mod;
                         }
                   }
            }
      cout << dp[(1 << n) - 1][n - 1];
void elevator_rides(){
      int n, k; cin >> n >> k;
vector <int > passenger(n);
      for (int i = 0; i < n; i++) cin >> passenger[i];
      vector<int
      > used(1 << n, 0);  // 最後載完人的電梯用了多少空間
vector <int > dp(1 << n, 1);  // bitset
for (int i = 1; i < 1 << n; i++) {
    used[i] = dp[i] = 2e9;
    for (int j = 0; j < n; j++) {
                   if (i & (1 << j)) { // 有 j
int pre = i ^ (1 << j);
                         // 最後的電梯遷能載 j
if (used[pre] + passenger[j] <= k) {
    // 電梯數先比,再來比用掉的空間
    if (dp
                                      [pre] < dp[i] || (dp[pre] == dp[i] &&
    used[pre] + passenger[j] < used[i])) {
    used[i] = used[pre] + passenger[j];
    dp[i] = dp[pre];</pre>
                                }
                         // 搭新的電梯
```

```
}
                }
          }
      cout << dp[(1 << n) - 1];
 int main(){
      travel_exactly_once();
elevator_rides();
 9.3 硬幣 [d41d8c]
void coin_combination_II(){
      // 有 n 種錢幣,求組合為 x 的組數,順序不可顛倒
      // 可顛倒的話只要一維,先 x 廻圈,再 coin[i] 去加
int n, x; cin >> n >> x;
vector<int> coin(n + 1);
      // dp[i][j] 為考慮前 i 個硬幣,組合為 i 的組數
       vector<vector<int>> dp(2, vector<int>(x + 1, 0));
      for (int i = 1; i <= n; i++) {
    for (int j = 0; j <= x; j++) {</pre>
                // 壓到 2 * n
                dp[i & 1][j] = dp[!(i & 1)][j];
                if (j >= coin[i]) {
                     (dp[i
                           & 1][j] += dp[i & 1][j - coin[i]]) %= mod;
                }
           }
      cout << dp[n & 1][x];
 void minimize_coins_nums(){
      // 有 n 種錢幣, 求組合為 x 的最小硬幣數
      vector < int > dp(x + 1, 0);
for (int i = 1; i <= x; i++) {</pre>
           dp[i] = 2e9;
           for(auto &j : coin){
   if(j <= i){</pre>
                     dp[i] = min(dp[i], dp[i - j] + 1);
           }
      cout << (dp[x] == 2e9 ? -1 : dp[x]);
      coin_combination_II();
minimize_coins_nums();
9.4 編輯距離 [4d4a6d]
 int main() {
      string s1, s2; cin >> s1 >> s2;
      int size1 = s1.size(), size2 = s2.size();
      // dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元
      vector<
    vector<int>> dp(size1 + 1, vector<int>(size2 + 1, 0));
s1 = "0" + s1, s2 = "0" + s2;
for (int i = 1; i <= size1; i++) dp[i][0] = i;
for (int i = 1; i <= size2; i++) dp[0][i] = i;
for (int i = 1; i <= size1; i++){
    for (int j = 1; j <= size2; j++) {
        if (s1[i] == s2[j]) {
            dp[i][j] = dp[i - 1][j - 1];
        }
}</pre>
                     // s1 新增等價於 s2 砍掉
                     // dp[i][j] = min(修改, s1 新增, s2 新增);
dp[i][j] = min({dp[i - 1][
j - 1], dp[i - 1][j], dp[i][j - 1]}) + 1;
          }
      cout << dp[size1][size2];</pre>
 9.5 LCS [087c0d]
 int main() {
      int m, n; cin >> m >> n;
      string s1, s2;
cin >> s1 >> s2;
      int L = 0;
      vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0));
```

for (int i = 1; i <= m; i++) {</pre>

for (int j = 1; j <= n; j++) {</pre>

for (auto i : dp[n])

```
cout << i << " " << "\n";
               if (s1[i - 1] == s2[j - 1]) {
   dp[i][j] = dp[i - 1][j - 1] + 1;
                                                                                              (int now = n; now > 0; now = par[now])
if (add[now] != -1)
                                                                                          ans.push_back(add[now]);
sort(all(ans));
               else {
                    dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
                                                                                          for (auto &i : ans) cout << i << " ";</pre>
                                                                                   }
         }
                                                                                    9.8 Removal Game [211de0]
     int length = dp[m][n];
    tout tength = dp[m][n];
cout << length << "|n";
string s(length, 'c');
// along to dp to trace back
while (m >= 1 && n >= 1) {
    if (s1[m - 1] == s2[n - 1]) {
        s[length - 1] = s1[m - 1]
    }
}
                                                                                   | // 兩個人比賽,每個人輪流取一個數字且只能是頭尾
                                                                                    // 問兩人都選得好,第一個人可取得的最大分數
                                                                                     int main() {
                                                                                          int n; cin >> n;
vector<vector<int>> dp(n + 1, vector<int>(n + 1));
               m--, n--, length--;
                                                                                          int pref = 0;
                                                                                          tht piel = 0;
vector < int > v(n + 1);
for (int i = 1; i <= n; i++) {
    cin >> v[i];
    pref += v[i];
}
          else {
    if (dp[m - 1][n] > dp[m][n - 1]) m--;
               else n--;
                                                                                          // dp[i][j] 是 i 到 j 區間選完,的最大分數差
for (int i = n; i > 0; i--) {
    for (int j = i; j <= n; j++) {
        if (i == j) {
     cout << s << "\n";
9.6 LIS [668131]
                                                                                                         dp[i][j] = v[i];
int main() {
     int n; cin >> n;
vector <int> v(n);
for (int i = 0; i < n; i++) {</pre>
                                                                                                         // 選左差距大,還是選右差距大
                                                                                                         dp[i][j] = max(
    v[i] - dp[i + 1][j], v[j] - dp[i][j - 1]);
          cin >> v[i];
                                                                                                    }
     int dp[n]; vector<int> mono;
     mono.push_back(v[0]);
                                                                                          // x + y = sum, dp[1][n] = x - y;
cout << (pref + dp[1][n]) / 2;
     dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) {
    if (v[i] > mono.back()) {
               mono.push_back(v[i]);
                                                                                     9.9 CF Example [7d37ea]
               dp[i] = ++L;
          else {
                                                                                   // CF 1932 pF
               // 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
                                                                                     // 請問在線段不重複的情況下,最多獲得幾分
               *it = v[i];
                                                                                     int main() {
               dp[i] = it - mono.begin() + 1;
                                                                                          int n, m;
cin >> n >> m;
          }
                                                                                          // 記錄每點有幾個線段
     vector<int> ans;
     // 再一個紀錄,包含這個點的左界
                                                                                          ans.push_back(v[i]);
                                                                                               cnt[l]++;
cnt[r + 1]--;
     reverse(ans.begin(), ans.end());
                                                                                          for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
     for (auto i : ans) {
    cout << i << " ";</pre>
                                                                                          for (int i = n; i >= 2; i--) {
                                                                                               l_side[i - 1] = min(l_side[i - 1], l_side[i]);
9.7 Projects [18998c]
                                                                                          vector<int> dp(n + 1);
  排程有權重問題,輸出價值最多且時間最少
                                                                                          dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
struct project {
   int from, end, gain, id;
                                                                                               dp[i] = cnt[i];
if (l_side[i] != inf) {
    dp[i] += dp[l_side[i] - 1];
int main() {
     int n; cin >> n;
     tut i; cti >> i;
vector roject> projects(n + 1);
for (int i = 1; i <= n; i++) {
    int f, e, g; cin >> f >> e >> g;
    projects[i] = {f, e, g, i};
                                                                                               dp[i] = max(dp[i], dp[i - 1]);
                                                                                          cout << dp[n] << "\n";
                                                                                    }
                                                                                    // CF 1935 pC
     sort(all(projects), [](project a, project b) {
   if (a.end == b.end) return a.gain < b.gain;</pre>
                                                                                    // 給你每個事件的 a, b, 挑事件會把 a 全部加起來
          return a.end < b.end;</pre>
                                                                                     // 再加上 max(bi) - min(bi)
                                                                                    int main(){
  int n, k, ans = 0; cin >> n >> k;
  vector <pii> v(n + 1);
  for (int i = 1; i <= n; i++) {
    int a, b; cin >> a >> b;
    v[i] = {a, b};
    if (a = k) and a = 1;
    if (a <= k) ans = 1;
          }) - projects.begin(); // 二分搜最接近 from 的 end dp[i] = dp[i - 1]; par[i] = i - 1;
                                                                                          sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
                                                                                          }); // 用 bi 來排,考慮第 i 個時可以先扣
          if (dp
                                                                                          for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
               // 如果報酬率一樣,比時間少的
               dp[i] = {dp
      [id][0] + 1, dp[id][1] + projects[i].gain, dp
      [id][2] + projects[i].end - projects[i].from};
                                                                                                    // min(不選,選)
if (dp[i
                                                                                                           - 1][j - 1] + v[i].first + v[i].second <= k) {
               add[i] = projects[i].id;
                                                                                                          // 假如可以選,更新 ans 時再加回去 bi
          }
                                                                                                         ans = max(ans, j);
```

```
dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
    cout << ans << endl:
9.10 Slope Trick [2ccb3a]
|// 設 dp[i][j] 為將陣列前
      i 個元素變為非嚴格遞增,並且所有 ai <= bj 所需要花的代價
#include <bits/stdc++.h>
using namespace std;
#define int long long
signed main() {
    int n; cin >> n;
vector <int> v(n);
    for (int i = 0;
cin >> v[i];
                  i < n; i++) {
        v[i] -= i;
    vector < int > discrete = v;
sort(discrete.begin(), discrete.end());
    int m = unique
    1], dp[0][j] + abs(v[i] - discrete[j - 1]));
        swap(dp[0], dp[1]);
    cout << *min_element(dp[0].begin(), dp[0].end());</pre>
}
|// 當 dp 是凸函數且答案是極值時,可以用 slope trick 優化
// 要注意的是
     如果兩個相鄰段的斜率差異大於 1,那麼這個關鍵點是要存兩次的
// 例如這題假設在 i-1 時 f{i-1}(x) 是一個 Slope Trick 函數,
// 我們額外定義一個函數 g_i(x)
     )表示將前 i 個元素變為非嚴格遞增,且 a_i = x 的最小花費。
  「則 g_i(x) = f{i-1}(x) + |x-a_i| , 我們可以觀察到
// f_i(x) = min(g_i(y))
     )), for y <= x ' 由於 /x-a_i/ 是一個 Slope Trickable 函數 '
// 因此
     g_i(x) 和 f_i(x) 都是 Slope Trickable 函數,因為 /x-a_i/,
// 分段點是 a_i,且因為斜率一定大於 1,要 push 2 次
// 因為 g_i(x) 最右邊函數的斜率是
      1,因此我們只需去除 g_i(x) 的最大斜率變化點得到 f_i(x)。
int main () {
    priority_queue < int > q;
    int n; cin >> n;
for (int i = 0; i < n; i++) {
   int x; cin >> x;
        q.push(x);
        a.push(x):
        ans += q.top() - x;
        q.pop();
    cout << ans;
```

10 Geometry 10.1 Cross Product [8113ac]

```
const double eps = 1e-8:
 struct point {
       double x, y;
       point operator * (int a){ return {a * x, a * y}; }
point operator + (point b){ return {x + b.x, y + b.y}; }
point operator - (point b){ return {x - b.x, y - b.y}; }
double operator * (point b){ return x * b.x + y * b.y; }
double operator ^ (point b){ return x * b.y - y * b.x; }
                 < (point b){ return x == b.x ? y < b.y : x < b.x; }</pre>
double abs(point a) { return sqrt(a * a); }
int sign
        (double a) { return fabs(a) < eps ? 0 : a > 0 ? 1 : -1; }
int ori(point
a, point b, point c) { return sign((b - a) ^ (c - a)); }
bool colinear(point a,
    point b, point c) { return sign((b - a) ^ (c - a)) == 0; }
bool between(point a, point b, point c){ // c between a and b
   if (!colinear(a, b, c)) return false;
   return sign((a - c) * (b - c)) <= 0;</pre>
bool intersect(point
       a, point b, point c, point d){ // line(a, b) line(c, d)
int abc = ori(a, b, c);
       int abd = ori(a, b, d);
       }
```

10.2 Convex Hull [e84f76]

```
vector<pii> P, L, U;
int cross(pii o, pii a, pii b){ // OA OB > O counterclock
  return (a.first - o.first) * (b.second
            o.second) - (a.second-o.second) * (b.first-o.first);
int Andrew_monotone_chain(int n){
    sort(P.begin(), P.end());
int l = 0, u = 0; // upper and lower hull
for (int i=0; i<n; ++i){</pre>
         while (l >= 2 && cross(L[l-2], L[l-1], P[i]) <= 0){
              L.pop_back();
          while (u >= 2 && cross(U[u-2], U[u-1], P[i]) >= 0){
              U.pop back();
         l++;
         u++:
         L.push_back(P[i]);
         U.push_back(P[i]);
    cout << l << ' ' << u << '\n';
    return l + u;
int main(){
    int n, x, y;
cin >> n;
for(int i = 0;i < n;i++){</pre>
         P.push_back({x, y});
     int ans = Andrew_monotone_chain(n) - 2;
    cout << ans << "\n";
    return 0:
```