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1.1 Default Code [d41d8c]

```
#include <bits/stdc++.h>
using namespace std;
using ll = long long;
void solve() {
int main() {
    ios_base::sync_with_stdio(false);
    cin.tie(nullptr);
    int t = 1;
    cin >> t;
    while (t--) {
        solve();
    return 0;
3
```

1.2 Compare Fuction [d41d8c]

```
// 1. sort, 二分搜刻在函式內 lambda 就好
// 2. priority queue 小到大是 >, set 是 <
// 3. set 不能 = , multiset 必須 =
// 4. 確保每個成員都要比到
// 5. pbds_multiset 不要用 lower_bound
// 6. 如果要用 find, 插入 inf 後使用 upper_bound
// 7. multiset 可以跟 set 一樣使用, 但請注意第 3、4 點
auto cmp = [](int i, int j) { return i > j; };
priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
vector<int> a {1, 2, 5, 4, 3}; // 小心不要改到 a
auto cmp = [&a](int i, int j) { return a[i] > a[j]; };
priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
```

1.3 Pbds [d41d8c]

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < class T>
using pbds_set = tree<T, null_type,
    less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template < class T>
1.4 Double [a94c1c]
     double x;
constexpr D() : x{0} {}
constexpr D(double x) : x{x} {}
constexpr static double eps = 1E-12;
      explicit operator double() const { return x; }
constexpr D operator-() const {
           return D(-x);
      constexpr D &operator*=(D rhs) & {
           x *= rhs.x; return *this;
      constexpr D &operator+=(D rhs) & {
           x += rhs.x; return *this;
      constexpr D &operator -=(D rhs) & {
    x -= rhs.x; return *this;
      constexpr D & operator/=(D rhs) & {
   assert(fabs(rhs.x) > eps);
   x /= rhs.x; return *this;
      friend constexpr D operator*(D lhs, D rhs) {
           return lhs *= rhs;
      friend constexpr D operator+(D lhs, D rhs) {
           return lhs += rhs;
      friend constexpr D operator - (D lhs, D rhs) {
    return lhs -= rhs;
      friend constexpr D operator/(D lhs, D rhs) {
    return lhs /= rhs;
      friend istream &operator>>(istream &is, D &a) {
   double v; is >> v; a = D(v); return is;
      } // eps should < precision
friend constexpr bool operator <(D lhs, D rhs) {
   return lhs.x - rhs.x < -eps;</pre>
      friend constexpr bool operator>(D lhs, D rhs) {
           return lhs.x - rhs.x > eps:
      friend constexpr bool operator==(D lhs, D rhs) {
    return fabs(lhs.x - rhs.x) < eps;</pre>
      friend constexpr bool operator <= (D lhs, D rhs) {
    return lhs < rhs || lhs == rhs;</pre>
      friend constexpr bool operator>=(D lhs, D rhs) {
   return lhs > rhs || lhs == rhs;
      friend constexpr bool operator!=(D lhs, D rhs) {
   return !(lhs == rhs);
};
1.5 Int128 [85923a]
     i128 sgn = 1; a = 0;
string s; is >> s;
for (auto c : s) {
   if (c == '-') {
                sgn = -1;
           } else {
                 a = a * 10 + c - '0';
```

```
using i128 = __int128_t; // 1.7F38
istream &operator>>(istream &is, i128 &a) {
          }
     a *= sgn;
     return is;
ostream &operator<<(ostream &os. i128 a) {
     string res;
if (a < 0) os << '-', a = -a;
while (a) {
          res.push_back(a % 10 + '0');
          a /= 10;
     reverse(res.begin(), res.end());
     os << res; return os;
```

1.6 Rng [401544]

2 Graph

2.1 DFS And BFS [e2d856]

```
int main() {
       vector < int >> adj(n);
       // dfs_graph
vector<bool> vis(n);
       auto dfs = [&](auto self, int u) -> void {
  if (vis[u]) return;
  vis[u] = true;
             for (auto v: adj[u]) {
    self(self, v);
             }
       dfs(dfs, 0);
       // bfs
       vector < int > depth(n, 1e9);
       queue < int > q;
auto bfs = [&](auto self, int s) -> void {
   vis[s] = true, depth[s] = 0;
              q.push(s);
             while (!q.empty()) {
   int u = q.front(); q.pop();
   for (auto v : adj[u]) {
                           if (vis[v]) continue;
vis[v] = true;
depth[v] = depth[u] + 1;
                           q.push(v);
                    }
             }
      };
bfs(bfs, 0);
```

2.2 Prim [3a3805]

2.3 Bellman-Ford [430ded]

2.4 Floyd-Warshall [3f61a4]

2.5 **Euler** [4177dc]

```
// 1. 無向圖是歐拉圖:
| // 非零度頂點是連通的
// 頂點的度數都是偶數
| // 2. 無向圖是半歐拉圖(有路沒有環):
// 非零度頂點是連通的
// 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
// 非零度頂點是強連通的
// 每個頂點的入度和出度相等
// 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
// 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
// 其他頂點的入度和出度相等
vector<int> ans;
auto dfs = [&](auto &&self, int u) -> void {
   while (g[u].size()) {
   int v = *g[u].begin();
       g[u].erase(v);
       self(self, v);
    ans.push_back(u);
dfs(dfs, 0);
reverse(ans.begin(), ans.end());
```

2.6 DSU [749620]

```
struct DSU {
       vector<int> boss, siz;
      DSU() {}
DSU(int n_) { init(n_); }
       void init(int n_) {
    n = n_; boss.resize(n);
             iota(boss.begin(), boss.end(), 0);
             siz.assign(n, 1);
      int find(int x) {
   if (boss[x] == x) return x;
   return boss[x] = find(boss[x]);
       bool same(int x, int y) {
    return find(x) == find(y);
      bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);</pre>
                            siz[y];
             boss[y] = x;
       int size(int x) {
    return siz[find(x)];
      }
};
struct DSU {
       vector<int> boss. siz. stk:
       DSU() {}
```

DSU(int n_) { init(n_); }

```
void init(int n_) {
             n = n_;
              boss.resize(n);
             iota(boss.begin(), boss.end(), 0);
siz.assign(n, 1);
              stk.clear();
      int find(int x) {
   return x == boss[x] ? x : find(boss[x]);
      bool same(int x, int y) {
    return find(x) == find(y);
      bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);
    siz[x] += siz[y];
    boss[y] = x;
}</pre>
             n - -;
             stk.push_back(y);
       void undo(int x) {
   while (stk.size() > x) {
                   int y = stk.back();
                    stk.pop_back();
                     siz[boss[y]] -= siz[y];
                    boss[y] = y;
             }
      int size(int x) {
    return siz[find(x)];
};
```

2.7 SCC [5d3e16]

```
struct SCC {
     int n, cur, cnt;
     vector < int >> adj;
     vector <int> stk, dfn, low, bel;
SCC(int n_ = 0) { init(n_); }
void init(int n_) {
          n = n_;
adj.assign(n, {});
          dfn.assign(n, -1);
low.resize(n);
          bel.assign(n, -1);
stk.clear();
           cur = cnt = 0;
     void addEdge(int u, int v) {
          adj[u].push_back(v);
     void dfs(int x) {
    dfn[x] = low[x] = cur++;
           stk.push_back(x);
           for (auto y : adj[x]) {
   if (dfn[y] == -1) {
                     dfs(y);
                low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
                     low[x] = min(low[x], dfn[y]);
                }
           if (dfn[x] == low[x]) {
                int y;
                do {
                     y = stk.back();
                bel[y] = cnt;
stk.pop_back();
while (y != x);
          }
     vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
           return bel;
     struct Graph {
          vector<pair<int, int>> edges;
           vector<int> siz;
           vector<int> cnte;
     Graph compress() {
          Graph g;
g.n = cnt;
g.siz.resize(cnt);
           g.cnte.resize(cnt);
          g.edges.emplace_back(bel[i], bel[j]);
                     } else {
                          g.cnte[bel[i]]++;
```

```
}
         return g;
    }
};
```

2.8 VBCC [ee1554]

```
struct VBCC {
                int n, cur, cnt;
vector<vector<int>> adj;
vector<vector<int>> bcc;
                vector<int> stk, dfn, low;
                vector < bool > ap;
VBCC(int n_ = 0) { init(n_); }
void init(int n_) {
                             n = n_;
adj.assign(n, {});
bcc.assign(n, {});
                               dfn.assign(n, -1);
                               low.resize(n);
                               ap.assign(n, false);
stk.clear();
                              cur = cnt = 0:
                void addEdge(int u, int v) {
                             adj[u].push_back(v);
adj[v].push_back(u);
                void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
    stk.push_back(x);
                               int child = 0;
                              for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
        dfs(y, x), child++;
        low[x] = min(low[x], low[y]);
        continue;
        low[x] = min(low[x], low[y]);
        continue;
        low[x] = min(low[x], low[y]);
        continue;
        low[x] = min(low[x], low[y]);
        low[x] = min(low[x], low[x], low[y]);
        low[x] = min(low[x], low[x], low[x], low[x]);
        low[x] = min(low[x], low[x], lo
                                                             if (low[y] >= dfn[x]) {
                                                                           int v;
do {
    v = stk.back();
                                                                                           bcc[v].push_back(cnt);
                                                                            stk.pop_back();
} while (v != y);
                                                                             bcc[x].push_back(cnt);
                                                                           cnt++:
                                                            if (low[y] >= dfn[x] && p != -1) {
    ap[x] = true;
                                                            }
                                             } else {
                                                            low[x] = min(low[x], dfn[y]);
                                             }
                               if (p == -1 && child > 1) {
    ap[x] = true;
               fvector < bool > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
            }
}</pre>
                                             }
                               return ap;
                struct Graph {
                               int n;
                              vector<pair<int, int>> edges;
vector<int> bel;
vector<int> siz; // BCC 內節點數
                               vector<int> cnte; // BCC 內邊數
                Graph compress() {
                             Graph g; // 壓完是一棵樹,但不一定每個 bel 都有節點 g.bel.resize(n);
                               g.siz.resize(cnt)
                              g.cnte.resize(cnt);
for (int u = 0; u < n; u++) {
    if (ap[u]) {
        g.bel[u] = cnt++;
    }
}</pre>
                                                            g.siz.emplace_back();
g.cnte.emplace_back();
                                                             for (auto v : bcc[u]) {
                                                                           g.edges.emplace_back(g.bel[u], v);
                                             } else if (bcc[u].size() == 1) {
   g.bel[u] = bcc[u][0];
                                             g.siz[g.bel[u]]++;

}
g.n = cnt;
for (int i = 0; i < n; i++) {
    for (auto j : adj[i]) {
        if (g.bel[i] == g.bel[j] && i < j) {
            g.cnte[g.bel[i]]++;
        }
}
</pre>
                                             }
                               return g;
```

2.9 EBCC [59d8ca]

| };

```
struct EBCC { // CF/contest/1986/pF
  int n, cur, cnt;
  vector<vector<int>> adj;
       vector<int> stk, dfn, low, bel;
      adj.assign(n, {});
              dfn.assign(n, -1);
              low.resize(n);
              bel.assign(n, -1);
             stk.clear();
bridges.clear();
cur = cnt = 0;
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
      void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
              stk.push_back(x);
             for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
                          dfs(y, x);
low[x] = min(low[x], low[y]);
if (low[y] > dfn[x]) {
                                 bridges.emplace_back(x, y);
                   } else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
              if (dfn[x] == low[x]) {
                    int y;
                   bel[y] = cnt;
stk.pop_back();
                    } while (y != x);
                    cnt++;
             }
      vector < int > work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
        }
}</pre>
                   }
              return bel;
       struct Graph {
             vector<pair<int, int>> edges;
              vector<int> siz; // BCC 內節點數
              vector<int> cnte; // BCC 內邊數
       Graph compress() {
             Graph g;
g.n = cnt;
              g.siz.resize(cnt);
             g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;</pre>
                    g.stz[bet[t]]++;
for (auto j : adj[i]) {
    if (bel[i] < bel[j]) {
        g.edges.emplace_back(bel[i], bel[j]);
    } else if (i < j) {
        g.cnte[bel[i]]++;
}</pre>
                          }
                   }
              return g;
      }
};
```

2.10 2-SAT [28688f]

2.11 Funtional Graph [e8fd64]

```
constexpr int N = 2E5 + 5;
constexpr int N = 2tb + 5;
int cht[N][31]; // 倍增表, 放外面不然 TLE
struct FuntionalGraph {
  int n, cnt;
  vector<int> g, bel, id, len, in, top;
  FuntionalGraph(): n(0) {}
  FuntionalGraph(vector<int> g_) { init(g_); }
  vaid init(vector<int> a_) {
          build();
          for (int i = 0; i < n; i++) {
    cht[i][0] = g[i];
    in[g[i]]++;</pre>
                   for (int i = 1; i <= 30; i++)
    for (int u = 0; u < n; u++)
        cht[u][i] = cht[cht[u][i - 1]][i - 1];
for (int i = 0; i < n; i++)
        if (in[i] == 0) label(i);</pre>
                   for (int i = 0; i < n; i++)
    if (top[i] == -1) label(i);</pre>
           void label(int u) {
                   vector <int > p; int cur = u;
while (top[cur] == -1) {
   top[cur] = u;
                             p.push_back(cur);
                             cur = g[cur];
                    auto s = find(p.begin(), p.end(), cur);
                   vector s = rind(p.begin(), p.end());
vector sint> cyc(s, p.end());
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {
    bel[cyc[i]] = cnt;
    id[cyc[i]] = i;</pre>
                    if (!cyc.empty())
                   ++cnt, len.push_back(cyc.size());

for (int i = p.size() - 1; i > 0; i--)

id[p[i - 1]] = id[p[i]] - 1;
          int jump(int u, int k) {
    for (int b = 0; k > 0; b++){
        if (k & 1) u = cht[u][b];
}
                            k >>= 1:
                   return u;
         }
};
```

3 Data Structure

3.1 BIT [d41d8c]

```
template < typename T>
struct Fenwick { // 全部以 0 based 使用
int n; vector < T> a;
Fenwick(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_;
    a.assign(n, T{});
}
```

```
void add(int x, const T &v) {
   for (int i = x + 1; i <= n; i += i & -i) {
      a[i - 1] = a[i - 1] + v;
}</pre>
      T sum(int x) { // 左閉右開查詢
            T ans{};
            for (int i = x; i > 0; i -= i & -i) {
    ans = ans + a[i - 1];
      T rangeSum(int l, int r) { // 左閉右開查詢
            return sum(r) - sum(l);
      int select(const T &k, int start = 0) {
           `x += i;
                      cur = cur + a[x - 1];
                 }
            }
            return x;
     }
};
template < class T>
struct TwoDFenwick { // 全部以 0 based 使用
     int nx, ny; // row, col 個數 vector < vector < T >> a;
      TwoDFenwick(int nx_ = 0, int ny_ = 0) {
            init(nx_, ny_);
      void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
      void add(int x, int y, const T &v) {
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            a[i - 1][j - 1] = a[i - 1][j - 1] + v;
        }
}</pre>
           }
     }
      T sum(int x, int y) { // 左閉右開查詢
           Im(int x, c..., );
T ans{};
for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans + a[i - 1][j - 1];
}
            return ans;
     }
T rangeSum
            (int lx, int ly, int rx, int ry) { // 左閉右開查詢
            return sum(
                  (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
}:
```

3.2 RangeBit [d41d8c]

```
T \text{ val} = T(
                           x + i + 1) * d[x + i - 1] - di[x + i - 1];
if (cur + val <= k) {
x += i;
                                  cur = cur + val:
                    }
              return x;
     }
template < class T>
struct rangeTwoDFenwick { // 全部以 0 based 使用
       int nx, ny; // row, col 個數
vector<vector<T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
             init(nx_, ny_);
       void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
              dj.assign(nx, vector<T>(ny, T{}));
             dij.assign(nx, vector<T>(ny, T{}));
       T vi = v * (x + 1);
T vj = v * (y + 1);
             T vj = v * (y + 1);
T vij = v * (x + 1) * (y + 1);
for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        d[i - 1][j - 1] = d[i - 1][j - 1] + v;
        di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
        dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
        dij[i - 1][j - 1] = dij[i - 1][j - 1] + vj;
}</pre>
                    }
             }
       void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
             add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
             add(lx, ly, v);
       T sum(int x, int y) { // 左閉右開查詢
              T ans{}:
              for (int i = x; i > 0; i -= i & -i) {
                     for (int j = y; j > 0; j -= j & -j) {
                           ans = ans
                            + T(x * y + x + y + 1) * d[i - 1][j - 1];  ans = ans - T(y + 1) * d[i - 1][j - 1];  ans = ans - T(x + 1) * d[i - 1][j - 1]; 
                           ans = ans + dij[i - 1][j - 1];
                    }
             return ans;
       T rangeSum
               (int lx, int ly, int rx, int ry) { // 左閉右開查詢
              return sum(
                     (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
      }
};
```

3.3 Segment Tree [d41d8c]

```
if (x < m) {
    modify(2 * p, l, m, x, v);</pre>
             } else {
                   modify(2 * p + 1, m, r, x, v);
            pull(p);
      void modify(int p, const Info &i) {
            modify(1, 0, n, p, i);
      info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    return query(p *</pre>
             return query(p
                   2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
      template < class F> // 尋找區間內,第一個符合條件的
      int findFirst
            (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)
    return -1;
if (l >= x && r <= y && !pred(info[p]))</pre>
            return -1;

if (r - l == 1)

return l;

int m = (l + r) / 2;
             int res = findFirst(2 * p, l, m, x, y, pred);
            if (res == -1)
    res = findFirst(2 * p + 1, m, r, x, y, pred);
      template < class F> // 若要找 last,先右子樹遞迴即可
int findFirst(int l, int r, F & pred) {
    return findFirst(1, 0, n, l, r, pred);
};
struct Info {
      int n = 1;
      int sum = 0;
Info operator+(const Info &a, const Info &b) {
    return { a.n + b.n, a.sum + b.sum };
3.4 Lazy Segment Tree [d41d8c]
```

```
template < class Info, class Tag>
struct LazySeg { // 左閉右開寫法
       int n;
       vector < Info > info;
       vector < Tag > tag;
LazySeg() : n(0) {}
LazySeg(int n_, Info v_ = Info()) {
              init(n_, v_);
       template < class T>
       LazySeg(vector<T> init_) {
              init(init_);
       void init(int n_, Info v_ = Info()) {
    init(vector(n_, v_));
       template < class T>
       void init (vector<T> init_) {
             int( (vector=r) tint(_) {
    n = init_.size();
    info.assign(4 << __lg(n), Info());
    tag.assign(4 << __lg(n), Tag());
    function <void(
        int, int, int)> build = [&](int p, int l, int r) {
        if (r - l == 1) {
            info[p] = init_[l];
            return.
                            return;
                     int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                     pull(p);
              build(1, 0, n);
       void pull(int p) {
   info[p] = info[p * 2] + info[p * 2 + 1];
       void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
   tag[p].apply(v);
      void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
              tag[p] = Tag();
       void modify(int p, int l, int r, int x, const Info &v) {
              if (r - l == 1) {
```

```
info[p] = v;
            int m = (l + r) / 2;
            push(p, l, r);
            if (x < m) {
                  modify(2 * p, l, m, x, v);
            } else {
                  modify(2 * p + 1, m, r, x, v);
            pull(p);
      void modify(int p, const Info &i) {
    modify(1, 0, n, p, i);
      Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;</pre>
            push(p, l, r);
            return query(p
                   2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
      void range_apply
    (int p, int l, int r, int ql, int qr, const Tag &v) {
    if (qr <= l || ql >= r) return;
    if (ql <= l && r <= qr) {</pre>
                  apply(p, l, r, v);
                  return;
           fint m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
pull(p);
      void range_apply(int l, int r, const Tag &v) {
    range_apply(1, 0, n, l, r, v);
      template < class F> // 尋找區間內,第一個符合條件的
      int findFirst
            (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
    return -1;</pre>
            if (l >= x && r <= y && !pred(info[p])) {</pre>
                  return -1;
            if (r - l == 1) {
                  return l;
            int m = (l + r) / 2;
            push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
            if (res ==
                  res = findFirst(2 * p + 1, m, r, x, y, pred);
            return res;
      template < class F> // 若要找 last, 先右子樹遞迴即可
int findFirst(int l, int r, F & & pred) {
    return findFirst(1, 0, n, l, r, pred);
};
struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add; void apply(const Tag& v) {
            if (v.set_val) {
                 set_val = v.set_val;
add = v.add;
            else {
                  add += v.add;
     }
};
struct Info {
      int sum;
void apply(int l, int r, const Tag &v) {
           if (v.set_val) {
    sum = (r - l) * v.set_val;
            sum += (r - l) * v.add;
      // Info &operator=(const Info &rhs) {
               // 部分 assignment 使用
return *this;
     //
// }
Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
3.5 Persistent Segment Tree [d41d8c]
```

```
template < class Info >
struct PST {
    struct Node {
```

```
Info info = Info();
                                                                                                                        void pull() { // update siz or other information
              int lc = 0, rc = `
                                                                                                                              min = val;
                                                                                                                              for (auto c : {lc, rc}) {
    if (!c) continue;
       vector < Node > nd:
       int n = 0; vector<int> rt;
       PST() : n(0) {}
                                                                                                                                      siz += c->siz;
      PST(int n_, Info v_ = Info()) { init(n_, v_); }
template < class T >
                                                                                                                                     min = std::min(min, c->min);
                                                                                                                              }
       PST(vector<T> init_) { init(init_); }
void init(int n_, Info v_ = Info()) {
   init(vector<Info>(n_, v_));
                                                                                                                       }
void push() {
    if (rev_valid) {
        swap(lc, rc);
        if (lc) lc->rev_valid ^= 1;
        if (rc) rc->rev_valid ^= 1;
}
      femplate < class T >
void init(vector < T > init_) {
    n = init_.size();
    nd.clear(); rt.clear();
                                                                                                                               rev_valid = false;
             nd.emplace_back(); // 讓 root 指向 1-based rt.push_back(build(0, n, init_));
                                                                                                                        int find(int k) { // 找到 min 是 k 的位置 (1-based)
                                                                                                                              push();
int ls = (lc ? lc->siz : 0) + 1;
       int build(int l, int r, vector<Info> &init_) {
                                                                                                                              if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
              int id = nd.size();
             nd.emplace_back();
if (r - l == 1) {
    nd[id].info = init_[l];
                                                                                                                       }
                    return id;
                                                                                                                int size(Treap *t) {
    return t ? t->siz : 0;
             int m = (l + r) >> 1;
nd[id].lc = build(l, m, init_);
nd[id].rc = build(m, r, init_);
pull(nd[id]);
                                                                                                                 Treap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
    a->push(); b->push();
    if (a->pri > b->pri) {
        a -> c = merge(a->rc, b);
        a -> c = merge(a -> c, b);
    }
}
       void pull(Node &t) {
             t.info = nd[t.lc].info + nd[t.rc].info;
                                                                                                                              a->pull();
                                                                                                                              return a:
       int copy(int t) { // copy 一個 node
  nd.push_back(nd[t]);
                                                                                                                        else {
                                                                                                                              b->lc = merge(a, b->lc);
b->pull();
              return nd.size() - 1;
                                                                                                                              return b;
      int generate() { // 創立新的 node
    nd.emplace_back();
                                                                                                                       }
              return nd.size() - 1;
                                                                                                                pair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
       int modify(int t, int l, int r, int x, const Info &v) {
   t = t ? copy(t) : generate();
   if (r - l == 1) {
                                                                                                                        t->push();
                                                                                                                        if (size(t->lc) < k) {
   auto [a, b] = split(t->rc, k - size(t->lc) - 1);
   t->rc = a;
                    nd[t].info = v;
                                                                                                                              t->pull();
              int m = (l + r) >> 1;
                                                                                                                              return {t, b};
              if (x < m) {
                    nd[t].lc = modify(nd[t].lc, l, m, x, v);
                                                                                                                        else {
                                                                                                                              auto [a, b] = split(t->lc, k);
t->lc = b;
                    nd[t].rc = modify(nd[t].rc, m, r, x, v);
                                                                                                                               t->pull();
             pull(nd[t]);
                                                                                                                              return {a, t};
              return t;
                                                                                                                       }
       void modify(int ver, int pos, const Info &val) {
   if (int(rt.size()) <= ver) rt.resize(ver + 1);</pre>
                                                                                                                 void Print(Treap *t) {
                                                                                                                        if (!t) return:
              rt[ver] = modify(rt[ver], 0, n, pos, val);
                                                                                                                        t->push();
      Info query(int t, int l, int r, int ql, int qr) {
    if (l >= qr || r <= ql) return Info();
    if (ql <= l && r <= qr) return nd[t].info;
    int m = (l + r) >> 1;
                                                                                                                        Print(t->lc);
                                                                                                                        cout << t->val;
                                                                                                                        Print(t->rc);
              return query(nd[t].
                                                                                                                3.7 RMQ [d41d8c]
                     lc, l, m, ql, qr) + query(nd[t].rc, m, r, ql, qr);
      Info query(int ver, int ql, int qr) {
    return query(rt[ver], 0, n, ql, qr);
                                                                                                                 template < class T, class Cmp = less < T >>
                                                                                                                 struct RMQ {
                                                                                                                        const Cmp cmp = Cmp();
                                                                                                                        static constexpr unsigned B = 64; using u64 = unsigned long long;
      void createVersion(int ori ver)
             rt.push_back(copy(rt[ori_ver]));
                                                                                                                        vector<vector<T>> a;
      void reserve(int n, int q) {
   nd.reserve(n + q * (2 * __lg(n) + 1));
   rt.reserve(q + 1);
                                                                                                                        vector < T > pre, suf, ini;
vector < u64 > stk;
                                                                                                                        RMQ() {}
RMQ(const vector<T> &v) { init(v); }
void init(const vector<T> &v) {
       void resize(int n) {
             rt.resize(n);
                                                                                                                              n = v.size();
pre = suf = ini = v;
      }
                                                                                                                               stk.resize(n);
struct Info {
   int sum = 0;
                                                                                                                              if (!n) {
                                                                                                                                     return:
Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
                                                                                                                               const int M = (n - 1) / B + 1;
                                                                                                                              const int W = (N - 1) / B + 1;
const int Ug = __lg(M);
a.assign(lg + 1, vector<T>(M));
for (int i = 0; i < M; i++) {
    a[0][i] = v[i * B];
    for (int j = 1; j < B && i * B + j < n; j++) {
        a[0][i] = min(a[0][i], v[i * B + j], cmp);
}</pre>
3.6 Treap [d41d8c]
struct Treap {
      ict Treap {
   Treap *lc, *rc;
   int pri, siz; bool rev_valid;
   int val; int min;
   Treap(int val_) {
      min = val = val_;
      pri = rand();
      le = re = rand();
      le = re = rand();
}
                                                                                                                               for (int i = 1; i < n; i++) {
    if (i % B) {</pre>
                                                                                                                                            pre[i] = min(pre[i], pre[i - 1], cmp);
              lc = rc = nullptr;
              siz = 1; rev_valid = 0;
```

for (int i = n - 2; i >= 0; i--) {

```
if (i % B != B - 1)
                      suf[i] = min(suf[i], suf[i + 1], cmp);
           for (int j = 0; j < lg; j++) {
    for (int i = 0; i + (2 << j) <= M; i++) {
        a[j + 1][i
        ] = min(a[j][i], a[j][i + (1 << j)], cmp);</pre>
           for (int i = 0; i < M; i++) {
    const int l = i * B;
    const int r = min(1U * n, l + B);</pre>
                tent :
u64 s = 0;
for (int j = l; j < r; j++) {
    while (s && cmp(v[j], v[__lg(s) + l])) {
        s ^= 1ULL << __lg(s);
}</pre>
                      s |= 1ULL << (j - l);
                      stk[j] = s;
                }
           }
     int k = __lg(r - l);
ans = min
                            ({ans, a[k][l], a[k][r - (1 << k)]}, cmp);
                return ans;
           } else {
                int x = B * (l / B);
                return ini
                       [__builtin_ctzll(stk[r - 1] >> (l - x)) + l];
           }
     }
};
```

3.8 Mo [d41d8c]

4 Flow Matching

4.1 Dinic [d41d8c]

```
while (!q.empty() && dis[t] == -1) {
                                                                    int u = q.front(); q.pop();
for (int id : adj[u]) {
    Edge &e = edges[id];
    if( for it is it
                                                                                           if (e.flow == e.cap) continue;
                                                                                          if (dis[e.to] == -1)
                                                                                                             dis[e.to] == -1) {
  dis[e.to] = dis[u] + 1;
  q.push(e.to);
                                                                  }
                                                return dis[t] != -1;
                          T dfs(int u, T flow) {
                                               if (flow == 0) return 0;
                                              if (u == 0) return 0,
if (u == t) return flow;
for (int &cur = ptr[u]; cur < adj[u].size(); cur++) {
    Edge &e = edges[adj[u][cur]];
    if (dis[u] + 1 != dis[e.to]) continue;
    if (e.cap == e.flow) continue;
    The = dfs(a to min(flow e.cap = e.flow));</pre>
                                                                     T mn = dfs(e.to, min(flow, e.cap - e.flow));
                                                                      if (mn > 0) {
                                                                                         e.flow += mn:
                                                                                         edges[adj[u](cur] ^ 1].flow -= mn;
                                                                  }
                                              }
                                               return 0; // 到不了終點就會 return 0
                          T work(int s_, int t_) {
    s = s_; t = t_; T flow = 0;
    while (bfs()) {
        fill(ptr.begin(), ptr.end(), 0);
    }
}
                                                                     while (true) {
   T res = dfs(s, INF_Flow);
   if (res == 0) break;
                                                                                          flow += res;
                                                                  }
                                               return flow;
                         void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
};
```

4.2 Min Cut [d41d8c]

```
// CSES Police Chase
int main(){
        int n, m; cin >> n >> m;
Dinic < int >> g(n);
for (int i = 0; i < m; i++) {
    int u, v, cap = 1;
    cin >> u >> v;
              g.add_edge(u, v, cap);
g.add_edge(v, u, cap);
        int res = g.work(0, n - 1);
cout << res << "\n";
if (res == 0) return;</pre>
        vector < int > vis(n);
auto find = [&](auto self, int u) -> void {
              if (!vis[u]) {
                     vis[u] = 1;
for (int id : g.adj[u])
                            auto e = g.edges[id];
if (e.cap - e.flow > 0) {
    self(self, e.to);
                     }
              }
       auto e = g.edges[id];
                      if (!vis[e.to]) {
                            cout << i + 1 << " " << e.to + 1 << " \n";
                     }
              }
       }
}
```

4.3 MCMF [d41d8c]

```
template < class Tf, class Tc > struct MCMF {
    struct Edge {
        int to;
        Tf flow, cap; // 流量跟容量
        Tc cost;
    };
    int n, m, s, t;
    const Tf INF_FLOW = 1 << 30;
    const Tc INF_COST = 1 << 30;
    vector < vector < int >> adj;
    vector < Edge > edges; // 幫每個 edge 編號
```

```
vector<Tc> dis, pot; // johnson algorithm, using spfa vector<int> rt; // 路徑恢復, 對應 id vector<bool> ing;
MCMF(int n_ = 0) { init(n_); }
void init(int n_)
       n = n_; m = 0;
edges.clear();
        adj.assign(n, {});
void add_edge(int u, int v, Tf cap, Tc cost){
  edges.push_back({v, 0, cap, cost});
  edges.push_back({u, 0, 0, -cost});
  adj[u].push_back(m++);
  adj[v].push_back(m++);
bool spfa() {
        dis.assign(n, INF_COST);
rt.assign(n, -1); inq.assign(n, false);
        aueue < int > a:
        q.push(s), dis[s] = 0, inq[s] = true;
        while (!q.empty()) {
   int u = q.front(); q.pop();
   inq[u] = false;
               q.push(v); inq[v] = true;
                       }
               }
        return dis[t] != INF_COST;
bool dijkstra() {
        dis.assign(n, INF_COST); rt.assign(n, -1);
priority_queue<pair<Tc, int>,
    vector<pair<Tc, int>>, greater<pair<Tc, int>>> pq;
       vector<pair<Tc, int>>, greater<pair<Tc, int>>;
dis[s] = 0; pq.emplace(dis[s], s);
while (!pq.empty()) {
    auto [d, u] = pq.top(); pq.pop();
    if (dis[u] < d) continue;
    for (int id : adj[u]) {
        auto [v, flow, cap, cost] = edges[id];
        Tc ndis = dis[u] + cost + pot[u] - pot[v];
        if (flow < cap && dis[v] > ndis) {
            dis[v] = ndis; rt[v] = id;
            contact(dis; v);
        }
}
                               pq.emplace(ndis, v);
              }
        return dis[t] != INF_COST;
}
// 限定 flow,最小化 cost
pair<Tf, Tc> work_flow(int s_, int t_, Tf need) {
       s = s_, t = t_; pot.assign(n, 0);
If flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {</pre>
                       dis[i] += pot[i] - pot[s];
                for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                (f, edges[rt[i]].cap - edges[rt[i]].flow);
               f = min < Tf > (f, need);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
}
               flow += f; need -= f;
cost += f * dis[t]; fr = false;
               swap(dis, pot);
if (need == 0) break;
        return {flow, cost};
·// 限定 cost, 最大化 flow
pair<Tf, Tc> work_budget(int s_, int t_, Tc budget) {
       s = s_, t = t_; pot.assign(n, 0);
If flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {</pre>
                       dis[i] += pot[i] - pot[s];
                for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                 (f, edges[rt[i]].cap - edges[rt[i]].flow);
               }
f = min<Tf>(f, budget / dis[t]);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
}
               flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
```

```
swap(dis, pot);
if (budget == 0 || f == 0) break;
          return {flow. cost}:
      void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
 };
 4.4 Hungarian [d41d8c]
 struct Hungarian { // 0-based, 0(VE)
      int n, m;
vector<vector<int>> adi:
      vector < int > used, vis;
      vector<pair<int, int>> match;
Hungarian(int n_ = 0, int m_ = 0) {
           init(n_, m_);
      void init(int n_, int m_) {
          n = n_; m = m_;
adj.assign(n + m, {});
used.assign(n + m, -1)
vis.assign(n + m, 0);
      void addEdge(int u, int v) {
          adj[u].push_back(n + v);
adj[n + v].push_back(u);
      fbool dfs(int u) {
  int sz = adj[u].size();
  for (int i = 0; i < sz; i++) {
    int v = adj[u][i];
    int v = adj[u][i];
}</pre>
               if (vis[v] == 0) {
    vis[v] = 1;
                    if (used[v] == -1 || dfs(used[v])) {
                         used[v] = u;
return true;
               }
           return false;
     }
vector<pair<int, int>> work() {
    match.clear(); used.assign(n + m, -1);
    vis.assign(n + m, 0);
    for (int i = 0; i < n; i++) {
        fill(vis.begin(), vis.end(), 0); dfs(i);
        .</pre>
           for (int i = n; i < n + m; i++) {
    if (used[i] != -1) {</pre>
                    match.emplace_back(used[i], i - n);
           return match;
1 }:
 4.5
        Theorem [d41d8c]
| // 有向無環圖:
// 最小不相交路徑覆蓋:
 // 最小路徑數 = 頂點數 - 最大匹配數
| // 最小相交路徑覆蓋:
// 先用
      Floyd 求傳遞封包,有連邊就建邊,然後再套最小不相交路徑覆蓋
 // 二分圖:
// 最小點
      覆蓋:選出一些點,讓所有邊至少有一個端點在點集中的最少數量
 // 最小點覆蓋 = 最大匹配數
 // 還原解, flow 的作法是從源點開始 dfs, 只走 cap - flow > 0
 // 的邊,最後挑選左邊還沒被跑過的點和右邊被跑過的點當作覆蓋的點
 // 最少邊覆蓋: 選出一些邊,讓所有點都覆蓋到的最少數量
 // 最少邊覆蓋 = 點數 - 最大匹配數
 // 最大獨立集: 選出一些點, 使這些點兩兩沒有邊連接的最大數量
// 最大獨立集 = 點數 - 最大匹配數
 5
        String
 5.1 Hash [852711]
 constexpr int B = 59;
vector<Z> Hash(string &s) {
      vector < Z > ans {0};
for (auto c : s) {
          ans.push_back(ans.back() * B + (c - 'a' + 1));
```

return ans:

void solve() {
 string s, sub;

```
5.5 Trie [31e4ff]
      cin >> s >> sub:
      auto a = Hash(s);
      auto q = Hash(sub);
                                                                                    constexpr int N = 1E7;
                                                                                    int tot = 0;
int trie[N][26], cnt[N];
      auto find = q.back();
      int ans = 0;
      int l = 1, r = sub.size(), len = sub.size();
                                                                                   void reset() {
   tot = 0, fill_n(trie[0], 26, 0);
     while (r <= s.size()) {
   if (a[r] - a[l - 1] * power(Z(B), len) == find) {</pre>
                                                                                    int newNode() {
                                                                                         int x = ++tot;
cnt[x] = 0, fill_n(trie[x], 26, 0);
           l++. r++:
     cout << ans << "\n";
                                                                                    void add(string &s) {
                                                                                         int p = 0;
for (auto c : s) {
 5.2 KMP [3a8e3d]
 struct KMP {
                                                                                              int &q = trie[p][c - 'a'];
                                                                                              if (!q) q = newNode();
     string sub;
     vector<int> fail;
      // fail 存匹配失敗時,移去哪,也就是最長共同前後綴長度
                                                                                         cnt[p] += 1:
     KMP() {}
KMP(const string &sub_) {
                                                                                    int find(string &s) {
          build(sub_);
                                                                                         int p = 0;
for (auto c : s) {
   int q = trie[p][c - 'a'];
     vector <int> build(const string &sub_) {
    sub = sub_, fail.resize(sub.size(), -1);
    for (int i = 1; i < sub.size(); i++) {
        int now = fail[i - 1];
        while (now != -1 && sub[now + 1] != sub[i]) {</pre>
                                                                                              if (!q) return 0;
                                                                                              p = q;
                                                                                         return cnt[p];
                    now = fail[now];
                if (sub[now + 1] == sub[i]) {
    fail[i] = now + 1;
                                                                                    5.6 SA [b58946]
               }
                                                                                    struct SuffixArray {
                                                                                         int n; string s;
           return fail:
                                                                                         vector < int > sa, rk, lc;
                                                                                         // n: 字串長度
      vector<int> match(string &s) {
           vector < int > match;
                                                                                         // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
           for (int i = 0, now = -1; i < s.size(); i++) {</pre>
                                                                                         // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
                // now 是成功匹配的長度 -1
                                                                                         // lc: LCP
                數組,lc[i] 表示 sa[i] 和 sa[i+1] 的最長公共前綴長度
                                                                                         SuffixArray(const string &s_) {
    s = s_; n = s.length();
                                                                                              sa.resize(n);
                    match.push_back(i - now);
now = fail[now];
                                                                                              lc.resize(n - 1);
                                                                                              rk.resize(n):
                                                                                              iota(sa.begin(), sa.end(), 0);
                                                                                              sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });
rk[sa[0]] = 0;</pre>
           return match;
                                                                                              for (int i = 1; i < n; i++)</pre>
5.3 Z Function [764b31]
                                                                                                  rk[sa[i]]
                                                                                                          = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
|// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
 // 的最長公共前綴 (LCP) 的長度
                                                                                              vector<int> tmp, cnt(n);
                                                                                              tmp.reserve(n);
while (rk[sa[n - 1]] < n - 1) {</pre>
 vector<int> Z(string s) {
     int n = s.size();
     tht n = S.stze(),
vector <int> z(n); z[0] = n;
for (int i = 1, j = 1; i < n; i++) {
    z[i] = max(0, min(j + z[j] - i, z[i - j]));
    while (i + z[i] < n && s[z[i]] == s[i + z[i]])</pre>
                                                                                                   tmp.clear();
for (int i = 0; i < k; i++)</pre>
                                                                                                   if (i + z[i] > j + z[j]) j = i;
                                                                                                   tmp.pusn_back(i - k);
fill(cnt.begin(), cnt.end(), 0);
for (int i = 0; i < n; i++)
    ++cnt[rk[i]];
for (int i = 1; i < n; i++)
    cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; i--)
      return z; // 最後一格不算
}
5.4 Manacher [9c9ca6]
 // 找到對於每個位置的迴文半徑
                                                                                                        sa[--cnt[rk[tmp[i]]]] = tmp[i];
                                                                                                   vector<int> manacher(string s) {
      string t = "#";
      for (auto c : s) {
    t += c;
    t += '#';
      int n = t.size():
      vector<int> r(n);
      for (int i = 0, j =
                                                                                              for (int i = 0, j = 0; i < n; i++) {
    if (rk[i] == 0) {
        j = 0;
    }
}</pre>
           0; i < n; i++) { // i 是中心, j 是最長回文字串中心 if (2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
                                                                                                   } else {
                                                                                                        for (j -=
           j > 0; i + j < n && sa[rk[i] - 1] + j < n
                                                                                                       && s[i + j] == s[sa[rk[i] - 1] + j]; j++);
lc[rk[i] - 1] = j;
                r[i] += 1;
           if (i + r[i] > j + r[j]) {
    j = i;
                                                                                        }
                                                                                   };
     return r;
// # a # b # a #
// 1 2 1 4 1 2 1
// # a # b # b # a #
// 1 2 1 2 5 2 1 2 1
                                                                                    5.7 SAM [b09888]
                                                                                   struct SAM {
   // 1 -> initial state
                                                                                         static constexpr int ALPHABET_SIZE = 26;
      // 值 -1 代表原回文字串長度
                                                                                         struct Node {
      // (id - val + 1) / 2 可得原字串回文開頭
                                                                                              int len:
                                                                                              int link;
                                                                                              array<int, ALPHABET_SIZE> next;
```

```
Node() : len{}, link{}, next{} {}
       vector<Node> t;
      SAM() {
   init();
      void init() {
    t.assign(2, Node());
    t[0].next.fill(1);
             t[0].len = -1;
       int newNode() {
             t.emplace_back();
return t.size() - 1;
      int extend(int p, int c) {
    if (t[p].next[c]) {
        int q = t[p].next[c];
    }
}
                   if (t[q].len == t[p].len + 1) {
                         return q;
                    int r = newNode();
                   t[r].len = t[p].len + 1;
t[r].link = t[q].link;
t[r].next = t[q].next;
                   t[q].link = r;
                   while (t[p].next[c] == q) {
    t[p].next[c] = r;
                         p = t[p].link;
                   return r:
            int cur = newNode();
t[cur].len = t[p].len + 1;
while (!t[p].next[c]) {
    t[p].next[c] = cur;
    t[r].line.
                   p = t[p].link;
             t[cur].link = extend(p, c);
             return cur;
     }
void solve() {
    string s; cin >> s;
    int n = s.length();
       vector<int> last(n + 1); // s[i - 1] 的後綴終點位置
       last[0] = 1;
      SAM sam;

for (int i = 0; i < n; i++) {

    last[i + 1] = sam.extend(last[i], s[i] - 'a');
       int sz = sam.t.size();
      vector < int > cnt(sz);
for (int i = 1; i <= n; i++) {</pre>
            cnt[last[i]]++; // 去重 = 1
      vector < vector < int >> order(sz);
for (int i = 1; i < sz; i++) {</pre>
             order[sam.t[i].len].push_back(i);
       for (int i = sz - 1: i > 0: i--) {
             for (int u : order[i]) {
    if (sam.t[u].link != -1) {
        cnt[sam.t[u].link] += cnt[u];
    }
}
             }
      vector<ll> dp(sz, -1);
      auto dfs = [&](auto self, int u) -> void {
            dp[u] = cnt[u];
for (int c = 0; c < SAM::ALPHABET_SIZE; c++) {
   int v = sam.t[u].next[c];</pre>
                   if (v) {
   if (dp[v] == -1) self(self, v);
   dp[u] += dp[v];
            }
      dfs(dfs, 1);
}
```

5.8 Palindrome Tree [f10e9d]

```
struct PAM {
    // 0 -> even root, 1 -> odd root
    static constexpr int ALPHABET_SIZE = 26;
    struct Node {
        int len;
        int fail;
        array<int, ALPHABET_SIZE> next;
        Node() : len{}, fail{}, next{} {}
};
    vector<int> s;
    vector<Node> t;
PAM() {
        init();
}
void init() {
        t.assign(2, Node());
        s.clear();
        t[0].len = 0;
        t[1].len = -1;
```

```
t[0].fail = 1:
       int newNode() {
             t.emplace_back();
return t.size() - 1;
       int extend(int p, int c) {
   int n = s.size();
              s.push_back(c);
             while (s[n - t[p].len - 1] != c) {
   p = t[p].fail;
              if (!t[p].next[c])
                     int r = newNode();
                    int r = newwoe(,,
t[r].len = t[p].len + 2;
int cur = t[p].fail;
while (s[n - t[cur].len - 1] != c) {
    cur = t[cur].fail;
}
                     t[r].fail = t[cur].next[c];
                    t[p].next[c] = r;
              p = t[p].next[c];
              return p;
      }
f;
void solve() {
    string s; cin >> s;
    int n = s.length();
    vector<int> last(n + 1);
       last[0] = 1:
       Fam pam;
for (int i = 0; i < n; i++) {
    last[i + 1] = pam.extend(last[i], s[i] - 'a');</pre>
       int sz = pam.t.size();
       vector < int > cnt(sz);
for (int i = 1; i <= n; i++) {</pre>
             cnt[last[i]]++; // 去重 = 1
             (int i = sz - 1; i > 1; i--) {
cnt[pam.t[i].fail] += cnt[i];
```

5.9 Duval [f9dcca]

```
// duval_algorithm
     // 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
      vector<string> duval(string s) {
   int i = 0, n = s.size();
   vector<string> res;
                                while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
}</pre>
                                                                                     else k++;
                                                                                  j++;
                                                           while (i <= k) {</pre>
                                                                                  res.push_back(s.substr(i, j - k));
                                                                                     i += i - k:
                                 return res:
     }
        // 最小旋轉字串
      string min_round(string s) {
                                 s += s;
int i = 0, n = s.size();
int start = i;
                                 while (i < n / 2) {</pre>
                                                        te ( < n / 2) {
    start = i;
    int k = i, j = i + 1;
    while (s[k] <= s[j] && j < n) {
        if (s[k] < s[j]) k = i;
        if (s[k] < s[j]) k =
                                                                                    else k++;
                                                         while (i <= k) {
    i += j - k;</pre>
                                 return s.substr(start, n / 2);
    }
```

6 Math

6.1 Modulo [a55187]

```
template < class T >
constexpr T power(T a, ll b) {
    T res {1};
    for (; b; b /= 2, a *= a)
        if (b % 2) res *= a;
    return res;
}
constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
    res %= p;
    if (res < 0) res += p;</pre>
```

```
return res:
template < ll P >
struct MInt {
     ll x;
     constexpr MInt() : x {0} {}
constexpr MInt(ll x) : x {norm(x % getMod())} {}
static ll Mod;
     constexpr static ll getMod() {
    return P > 0 ? P : Mod;
     constexpr static void setMod(ll Mod_) {
    Mod = Mod_;
     constexpr ll norm(ll x) const {
          if (x < 0) x += getMod();
if (x >= getMod()) x -= getMod();
          return x;
     constexpr MInt operator-() const {
          return MInt(norm(getMod() - x));
     constexpr MInt inv() const {
   return power(*this, getMod() - 2);
     constexpr MInt &operator*=(MInt rhs) & {
          if (getMod() < (1ULL << 31)) {
    x = x * rhs.x % int(getMod());</pre>
           } else {
              x = mul(x, rhs.x, getMod());
     constexpr MInt &operator+=(MInt rhs) & {
    x = norm(x + rhs.x);
           return *this;
     constexpr MInt &operator -= (MInt rhs) & {
          x = norm(x - rhs.x);
return *this;
     constexpr MInt &operator/=(MInt rhs) & {
   return *this *= rhs.inv();
     friend constexpr MInt operator*(MInt lhs, MInt rhs) {
          return lhs *= rhs;
     friend constexpr MInt operator+(MInt lhs, MInt rhs) {
          return lhs += rhs;
     friend constexpr MInt operator-(MInt lhs, MInt rhs) {
          return lhs -= rhs;
     friend constexpr MInt operator/(MInt lhs, MInt rhs) {
          return lhs /= rhs;
     friend istream &operator>>(istream &is, MInt &a) {
    ll v; is >> v; a = MInt(v); return is;
     friend ostream &operator<<(ostream &os, const MInt &a) {</pre>
          return os << a.x:
     friend constexpr bool operator==(MInt lhs, MInt rhs) {
   return lhs.x == rhs.x;
     friend constexpr bool operator!=(MInt lhs, MInt rhs) {
   return lhs.x != rhs.x;
     friend constexpr bool operator<(MInt lhs, MInt rhs) {
   return lhs.x < rhs.x;</pre>
template <>
ll MInt < 0 > :: Mod = 998244353;
constexpr ll P = 1E9 + 7;
using Z = MInt<P>;
6.2 Combination [6aa734]
```

```
struct Comb {
         lct comb {
ll n; vector < Z > _fac , _invfac , _inv;
Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
Comb(ll n) : Comb() { init(n); }
void init(ll m) {
                   int((t m) {
    m = min(m, Z::getMod() - 1);
    if (m <= n) return;
    _fac.resize(m + 1);
    _invfac.resize(m + 1);
}</pre>
                   __inv.resize(m + 1);
for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;
                   for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
}
         Z fac(ll m) {
                    if (m > n) init(2 * m);
                    return _fac[m];
```

```
Z invfac(ll m) {
    if (m > n) init(2 * m);
               return _invfac[m];
        If I inv(ll m) {
    if (m > n) init(2 * m);
    return _inv[m];
        J binom(ll n, ll m) {
   if (n < m || m < 0) return 0;
   return fac(n) * invfac(m) * invfac(n - m);</pre>
        Z lucas(ll n, ll m) { // Mod 要在 1E5 左右
              if (m == 0) return 1;
return binom(n % Z::getMod(), m % Z::getMod())
* lucas(n / Z::getMod(), m / Z::getMod());
        }
|} comb; // 注意宣告, 若要換模數需重新宣告
```

6.3 Sieve [37ae54]

```
vector<int> primes, minp;
void sieve(int n) {
    minp.assign(n + 1, 0);
          primes.clear();
          // minp[i] == i, 質數
          for (int i = 2; i <= n; i++) {
   if (minp[i] == 0) {
      minp[i] = i;
}</pre>
                             primes.push_back(i);
                   for (auto p : primes) {
    if (i * p > n) break;
    minp[i * p] = p;
    if (p == minp[i]) break;
         }
}
// a ^ (m-1) = 1 (Mod m)
// a ^ (m-2) = 1/a (Mod m)
// Exp2: cout << power(x, power(y, p, Mod - 1), Mod)
// Num = (x+1) * (y+1) * (z+1)...
// Sum = (a^0 + a^1+...+ a^x) * (b^0 +...+ b^y)
// Mul = N * (x+1) * (y+1) * (z+1) / 2
```

6.4 MillerRabinPollardRho [b9e5be]

```
constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
        res %= p;
if (res < 0) res += p;
        return res;
template < class T>
constexpr T power(T a, ll b, ll p) {
    T res {1};
        for (; b; b /= 2, a = mul(a, a, p))
    if (b % 2) res = mul(res, a, p);
vector<ll
vector<ll
> chk {2, 325, 9375, 28178, 450775, 9780504, 1795265022};
bool check(ll a, ll d, int s, ll n) {
    a = power(a, d, n);
    if (a <= 1) return 1;
    for (int i = 0; i < s; ++i, a = mul(a, a, n)) {
        if (a == 1) return 0;
        if (a == n - 1) return 1;
    }
}</pre>
        return 0:
bool IsPrime(ll n) {
       if (n < 2) return 0;
if (n % 2 == 0) return n == 2;
ll d = n - 1, s = 0;
while (d % 2 == 0) d >>= 1, ++s;
for (ll i : chk) if (!check(i, d, s, n)) return 0;
        return 1:
const vector<ll> small = {2, 3, 5, 7, 11, 13, 17, 19};
ll FindFactor(ll n) {
    if (IsPrime(n)) return 1;
       for (ll p : small) if (n % p == 0) return p;
ll x, y = 2, d, t = 1;
auto f = [&](ll a) {
               return (mul(a, a, n) + t) % n;
        for (int l = 2; ; l <<= 1) {
               for (int j = 0; j < m; ++j) {
    y = f(y), d = mul(d, abs(x - y), n);</pre>
                       ll g = gcd(d, n);
                       if (g == n) {
    l = 1, y = 2, ++t;
    break;
```

```
if (g != 1) return g;
    }
map<ll. int> res:
void PollardRho(ll n) {
    if (n == 1) return;
if (IsPrime(n)) return ++res[n], void(0);
    ll d = FindFactor(n);
    PollardRho(n / d), PollardRho(d);
```

6.5 CRT [d41d8c]

```
ll exgcd(ll a, ll b, ll &x, ll &y) {
     if (!b) {
    x = 1, y = 0;
    return a;
     ll g = exgcd(b, a % b, y, x);
     y -= a / b * x;
     return g;
ll inv(ll x, ll m){
     ll a, b;
     exgcd(x, m, a, b);
     a \%= m;
if (a < 0) a += m;
     return a;
// remain, mod
ll CRT(vector<pair<ll, ll>> &a){
  remain, mod
     ll prod = 1;
for (auto x : a) {
         prod *= x.second;
     illres = 0;
     for (auto x : a) {
          auto t = prod / x.second;
res += x.first * t % prod * inv(t, x.second) % prod;
if(res >= prod) res -= prod;
     return res:
}
```

6.6 Matrix [bec759]

```
template < class T>
struct Matrix {
     int n, m;
vector<vector<T>> mat;
      constexpr Matrix(int n_, int m_) { init(n_, m_); }
      constexpr Matrix(vector<vector<T>> mat_) { init(mat_); }
      constexpr void init(int n_, int m_) {
    n = n_; m = m_;

            mat.assign(n, vector<T>(m));
      constexpr void init(vector<vector<T>> mat_) {
           n = mat_.size();
m = mat_[0].size();
            mat = mat_;
      constexpr Matrix & operator *= (const Matrix & rhs) & {
   assert(mat[0].size() == rhs.mat.size());
                   .size(), k = mat[0].size(), m = rhs.mat[0].size();
           .slze(), k - mast_j.

Matrix res(n, m);

for (int i = 0; i < n; i++) {
    for (int j = 0; j < m; j++) {
        for (int l = 0; l < k; l++) {
            res.mat[i][j] += mat[i][l] * rhs.mat[l][j];
        }
                 }
            mat = res.mat;
            return *this;
      friend constexpr
            Matrix operator*(Matrix lhs, const Matrix &rhs) {
return lhs *= rhs;
template < class T>
constexpr Matrix<T> unit(int n) {
     Matrix<T> res(n, n);
for (int i = 0; i < n; i++) {
    res.mat[i][i] = 1;</pre>
      return res:
template < class T>
constexpr Matrix<T> power(Matrix<T> a, ll b) {
     assert(a.n == a.m);
Matrix<T> res = unit<T>(a.n);
for (; b; b /= 2, a *= a)
if (b % 2) res *= a;
      return res;
```

```
template < class T>
int mex(vector<T> &v) {
    unordered_set <T> s;
    for (auto e : v) s.insert(e);
for (T i = 0; ; i++) {
         if (s.find(i) == s.end()) return i;
```

6.8 Game Theorem

- · sg 值為 0 代表先手必敗
- 當前 sg 值 = 可能的後繼狀態的 mex (例如拿一個或拿兩個, 就等於兩者的 sg值mex),若有互相依賴就兩個後繼狀態xor當作一組sg值(例如切開成 兩半,只算一次)
- 單組基礎 nim 的 sg 值為本身的原因: f(0) = 0, f(1) = mex(f(0)) =
- 1,f(2)=mex(f(0),f(1))=2...,都是自己 多組賽局可以把 sg 值 xor 起來,當成最後的 sg 值,nim 也是一樣,且由於 xor 性質, 如果可以快速知道 sg(1)g(2)...g(n), 就可以用 xor 性質處理不連

6.9 Integer Partition [595ed2]

```
// CSES_Sum_of_Divisors
const int mod = 1e9 + 7;
const int inv_2 = 500000004;
// n / 1 * 1 + n / 2 * 2 + n / 3 * 3 + ... + n / n * n
     ll ans = 0;
     ll n; cin >> n;

for (ll l = 1, r; l <= n; l = r + 1) {

    r = n / (n / l);
         ((r - l + 1) % mod)) % mod * inv_2; // l 加到 r
         val %= mod; sum %= mod;
ans += val * sum;
         ans %= mod;
     cout << ans << "\n";
```

6.10 Mobius Theorem

- 數論分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left|\frac{n}{i}\right|)$ 的和式。當可以在O(1)內計算f(r)-f(l)或已經預處理 出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n} \mu(d) = \begin{cases} 1 & \text{for } n=1\\ 0 & \text{for } n\neq 0 \end{cases}$$

- 2. μ是常數函數1的反元素 $\Rightarrow \mu * 1 = \epsilon$, $\epsilon(n)$ 只在n = 1 時為 1 , 其餘情況皆為 0 。
- $-\phi$ 歐拉函數: x以下與x互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^i) \\ &= 1 + p^0(p-1) + p^1(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^c \\ &= id \end{split}$$

• 莫比烏斯反演公式

```
- f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})
- f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)
```

6.7 Mex [4e24ed]

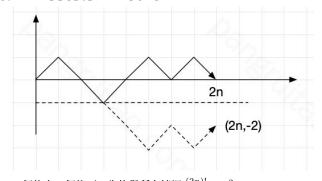
例子

$$\begin{split} &\sum_{i=a}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{y}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.11 Mobius Inverse [d41d8c]

```
const int maxn = 2e5:
ll mobius_pref[maxn];
void init() {
                    mobius_pref[1] = 1;
vector<ll> wei
                     (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
                                                                 continue; // 包含平方
                                           if (wei[i] == 0) {
    wei[i] = 1;
                                                                 }
                                          mobius_pref[i]
                                                                     = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
                    }
void solve() {
                  a solve() {
    ll a, b, c, d, k; cin >> a >> b >> c >> d >> k;
    auto cal = [&](ll x, ll y) -> int {
        int res = 0;
        for (int l = 1, r; l <= min(x, y); l = r + 1) {
            r = min(x / (x / l), y / (y / l));
            res += (mobius_pref[r] - mobius_pref[l] - mobius_p
                                                                                             - 1]) * (x / l) * (y / l); // 代推出來的式子
                                           return res;
                    cout << cal
                                              (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k, (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n";
```

6.12 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2)

假設往上有 x 個,往下有 y 個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.13 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- · G:各種翻轉操作所構成的置換群
- X/G: 本質不同的方案的集合 X/G: 對於某一種操作 g, 所有方案中, 經過 g 這種翻轉後保持不變的方案 的集合
- 集合取絕對值代表集合數

Search and Gready

Binary Search [d41d8c]

```
int main() {
          二分找上界
     while (lo < hi) {
   int x = (lo + hi + 1) / 2;
   if (check(x)) lo = x;</pre>
           else hi = x - 1;
      cout << lo; // 保證有解
     while (lo <= hi) {
   int x = (lo + hi) / 2;
   if (check(x)) lo = x + 1;
}</pre>
           else hi = x - 1;
      cout << hi; // 範圍外代表無解
         二分找下界
      cout << lo; // 保證有解
      while (lo <= hi) {
   int x = (lo + hi) / 2;</pre>
           if (check(m)) hi = x - 1;
           else lo = x + 1;
      cout << lo; // 範圍外代表無解
```

7.2 Ternary Search [d41d8c]

```
int main() {
     int lo = 0, hi = 10;
     while (lo <= hi) {</pre>
          int xl = lo + (hi - lo) / 3;
int xr = hi - (hi - lo) / 3;
          int ansl = check(xl), ansr = check(xr);
if (ansl < ansr) {</pre>
                 lo = xl + 1;
          } else {
    hi = xr - 1;
           // record ans and index
     }
```

Tree 8

8.1 LCA [f45014]

```
vector<vector<int>> par;
vector<int> dep;
void build(int n, vector<vector<int>> &tree, int u = 0) {
       par.assign(n, vector<int>(B + 1, -1));
dep.assign(n, 0);
auto dfs = [&](auto self, int x, int p) -> void {
              for (auto y : tree[x]) {
    if (y == p) continue;
    par[y][0] = x; // 2 ^ 0
    dep[y] = dep[x] + 1;
    self(self, y, x);
}
             }
       par[u][0] = u; dfs(dfs, 0, -1);
       for (int i = 1; i <= B; i++) {
    for (int j = 0; j < n; j++) {
        par[j][i] = par[par[j][i - 1]][i - 1];</pre>
      }
a = par[a][i];
       for (int i = B; i >= 0; i--) {
   if (par[a][i] != par[b][i]) {
      a = par[a][i], b = par[b][i];
}
       }
```

```
return par[a][0];
}
int jump(int x, int k) {
    for (int i = B; i >= 0; i--) {
        if (k >> i & 1) {
            x = par[x][i];
        }
    return x;
}
```

8.2 Centroid Decomposition [ec760b]

```
#include <bits/stdc++.h>
using namespace std;
struct CenDecom {
        vector<vector<int>> adi:
        vector < bool > vis;
        vector < int > siz;
CenDecom(int n_ = 0) { init(n_); }
        void init(int n_) {
                n = n_{;}
                adj.assign(n, {});
vis.assign(n, false);
siz.assign(n, 1);
        void addEdge(int u, int v) {
  adj[u].push_back(v);
  adj[v].push_back(u);
       }
void get_siz(int x, int p = -1) {
    siz[x] = 1;
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        get_siz(y, x);
        siz[x] += siz[y];
}
                }
        int get_cen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz) {
                                 return get_cen(y, sz, x);
                        }
                return x;
        void get_ans(int x, int p) {
                    do something
                for (int y : adj[x]) {
   if (y == p || vis[y]) continue;
   get_ans(y, x);
        void work(int x = 0) {
                get_siz(0, x);
                int cen = get_cen(x, siz[x]);
vis[cen] = true;
for (int y : adj[cen]) {
    if (vis[y]) continue;
    get_ans(y, cen);
}
                for (int y : adj[cen]) {
   if (vis[y]) continue;
                        work(y);
       }
};
```

8.3 Heavy Light Decomposition [41d99e]

```
struct HLD {
      vector<int> siz, top, dep, parent, in, out, seq;
     vector <int> st2, top, dep, parent, th, out, seq;
vector <vector <int>> adj;
HLD(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_; cur = 0;
    siz.resize(n); top.resize(n); dep.resize(n);
    parent.resize(n); in.resize(n); out.resize(n);
    sec.resize(n); dep.resize(n);
            seq.resize(n); adj.assign(n, {});
      void addEdge(int u, int v) {
            adj[u].push_back(v);
            adj[v].push_back(u);
      void work(int rt = 0) {
            top[rt] = rt;
dep[rt] = 0;
            parent[rt]
            dfs1(rt); dfs2(rt);
      void dfs1(int u) {
            if (parent[u] != -1)
                  for (auto &v : adj[u]) {
   parent[v] = u, dep[v] = dep[u] + 1;
   dfs1(v);
                  siz[u] += siz[v];
```

```
if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
                     } // 讓 adj[u][0] 是重子節點
       void dfs2(int u) {
              in[u] = cur++;
              seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
   top[v] = v == adj[u][0] ? top[u] : v;
                      dfs2(v):
              out[u] = cur;
       int lca(int u, int v) {
    while (top[u] != top[v]) {
        if (dep[top[u]] > dep[top[v]]) {
                     u = parent[top[u]];
} else {
                             v = parent[top[v]];
                     }
              return dep[u] < dep[v] ? u : v;</pre>
       int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
       bool isAncester(int u, int v) {
    return in[u] <= in[v] && in[v] < out[u];</pre>
       int rootedParent(int rt. int v) {
              rootedParent(int rt, int v) {
swap(rt, v);
if (rt == v) return rt;
if (!isAncester(rt, v)) return parent[rt];
auto it = upper_bound(adj[
    rt].begin(), adj[rt].end(), v, [&](int x, int y) {
    return in[x] < in[y];
}</pre>
              }) - 1;
return *it;
       int rootedSize(int rt, int v) {
   if (rt == v) return n;
   if (!isAncester(v, rt)) return siz[v];
   return n - siz[rootedParent(rt, v)];
       int rootedLca(int rt, int a, int b) {
  return lca(rt, a) ^ lca(a, b) ^ lca(b, rt);
};
```

8.4 Link Cut Tree [0e9031]

```
template < class Info, class Tag>
struct LinkCutTree { // 1-based
    struct Node {
    Info info = Info();
         Tag tag = Tag();
bool rev = false;
int size = 0;
         int ch[2], p = 0;
     vector < Node > nd:
     LinkCutTree(int n = 0) { init(n); }
     void init(int n) {
        nd.clear();
         nd.emplace_back();
         resize(n);
     void resize(int n) {
         nd.resize(n + 1);
    void make_rev(int t) {
    swap(nd[t].ch[0], nd[t].ch[1]);
    nd[t].rev ^= true;
     void apply(int t, const Tag &v) {
   nd[t].info.apply(nd[t].size, v);
   nd[t].tag.apply(v);
    nd[t].rev = false;
         if (nd[t].ch[0]) apply(nd[t].ch[0], nd[t].tag);
if (nd[t].ch[1]) apply(nd[t].ch[1], nd[t].tag);
nd[t].tag = Tag();
     void pull(int t) {
```

```
nd[t].size
                  1 + nd[nd[t].ch[0]].size + nd[nd[t].ch[1]].size;
           nd[t].info
                 .pull(nd[nd[t].ch[0]].info, nd[nd[t].ch[1]].info);
     int pos(int t) {
    return nd[nd[t].p].ch[1] == t;
      void pushAll(int t) {
          if (!isrt(t)) {
   pushAll(nd[t].p);
          push(t);
      void rotate(int t) {
          int q = nd[t].p;
int x = !pos(t);
nd[q].ch[!x] = nd[t].ch[x];
if (nd[t].ch[x]) nd[nd[t].ch[x]].p = q;
nd[t].p = nd[q].p;
          if (!isrt(q)) nd[nd[q].p].ch[pos(q)] = t;
nd[t].ch[x] = q;
          nd[q].p = t;
pull(q);
      void splay(int t) {
          if (pos(t) == pos(nd[t].p)) {
    rotate(nd[t].p);
                    } else {
                         rotate(t):
                    }
               rotate(t);
          pull(t);
     }
     void access(int t) { // access 後自動 splay
    for (int i = t, q = 0; i; q = i, i = nd[i].p) {
               splay(i);
               nd[i].ch[1] = q;
               pull(i);
           splay(t);
      void makeRoot(int t) {
           access(t);
          make_rev(t);
      int findRoot(int t) {
           access(t);
          int x = t;
while (nd[x].ch[0]) {
               push(x);
               x = nd[x].ch[0];
           access(x);
           return x:
     bool connected(int x, int y) {
    return findRoot(x) == findRoot(y);
     bool neighber(int x, int y) {
           makeRoot(x);
           access(y);
           if (nd[y].ch[0] != x || nd[x].ch[1]) return false;
          return true;
      void split(int rt, int y) {
          makeRoot(y);
access(rt);
      void link(int x, int y) {
          makeRoot(x);
           if (findRoot(y) != x) {
               nd[x].p = y;
     void cut(int x, int y) {
    makeRoot(x);
           access(y);
           nd[y].ch[0] = nd[nd[y].ch[0]].p = 0;
          pull(x);
           pull(y);
      void modify(int x, const Info &v) {
           access(x);
          nd[x].info = v;
     void path_apply(int x, int y, const Tag &v) {
   assert(connected(x, y));
          split(x, y);
           apply(x, v);
      Info path_query(int x, int y) {
           assert(connected(x, y));
           split(x, y);
           return nd[x].info;
     }
};
```

```
constexpr int Mod = 51061;
struct Tag {
    ll add = 0; ll mul = 1;
    void apply(const Tag &v) {
        mul = mul * v.mul % Mod;
        add = (add * v.mul % Mod + v.add) % Mod;
    }
};
struct Info {
    ll val = 0; ll sum = 0;
    void apply(int size, const Tag &v) {
        val = (val * v.mul % Mod + v.add) % Mod;
        sum = (sum * v.mul % Mod + v.add * size % Mod) % Mod;
    }
    void pull(const Info &l, const Info &r) {
        sum = (l.sum + r.sum + val) % Mod;
    }
};
```

8.5 Virtual Tree [622e69]

```
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
// 可以建立虚樹達成快速樹 DP
   // 可以建立區樹達成快速樹 DP
// 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
        vt[stk[top - 1]].push_back(stk[top]), top--;
    if (stk[top - 1] != l) {
        vt[l].push back(stk[ton]):
                    tr (stk[top - 1] := t) {
   vt[l].push_back(stk[top]);
   stk[top] = l;
} else vt[l].push_back(stk[top--]);
stk[++top] = u;
    void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
    vt[u].clear();
    void solve(int n, int q) {
   vector g(n + 1, vector<pair<int, int>>());
                    vector vt(n + 1, vector vtatt, clitz, clitz
                                    g[u].push_back({v, w});
                                    g[v].push_back({u, w});
                     build_lca(n, g);
                   for (int j = 0; j < m; j++) {
    cin >> key[j];
                                                     iskey[key[j]] = 1;
                                    key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
                                     for (int x : key) insert(x, vt);
                                   // DP
                                     auto dfs = [&](auto self, int u) -> void {
                                                   for (auto v : vt[u]) {
    self(self, v);
                                                                      if (iskey[v]) {
                                                                                     dp[u] += min_dis[v];
                                                                                      // 砍掉 1 到 v 之間最短的路
                                                                                     dp[u] += min(dp[v], min_dis[v]);
                                                                      iskey[v] = dp[v] = 0;
                                                    vt[u].clear();
                                    dfs(dfs, key[0]); // key[0] 一定是 root
cout << dp[key[0]] << "\n";
iskey[key[0]] = dp[key[0]] = 0;
```

8.6 Dominator Tree [0b03d9]

```
// dom

存起點到達此點的必經的上個節點(起點 = 自己),無法到達 = -1

struct Dominator_tree {
    int n, id;
    vector<vector<int>> adj, radj, bucket;
    vector<int>> sdom, dom, vis, rev, pa, rt, mn, res;
    Dominator_tree(int n_ = 0) { init(n_); }
    void init(int n_) {
        n = n_, id = 0;
        adj.assign(n, {});
        radj.assign(n, {});
```

```
bucket.assign(n, {});
sdom.resize(n), dom.assign(n, -1);
vis.assign(n, -1), rev.resize(n);
pa.resize(n), rt.resize(n);
mn.resize(n), res.resize(n);
                                                                                                                                   ans.push_back(v[i]), L--;
                                                                                                                      reverse(ans.begin(), ans.end());
for (auto i : ans) cout << i << " ";
      void add_edge(int u, int v) { adj[u].push_back(v); }
int query(int v, int x) {
   if (rt[v] == v) return x ? -1 : v;
                                                                                                               9.3 Edit Distance [308023]
             int p = query(rt[v], 1);
if (p == -1) return x ? rt[v]
                                                                                                               int main() {
                                                                                                                      string s1, s2; cin >> s1 >> s2;
int n1 = s1.size(), n2 = s2.size();
// dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元
                                                                : mn[v];
              if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
             rt[v] = p;
return x ? p : mn[v];
                                                                                                                      vector<int> dp(n2 + 1);
                                                                                                                     vector <int> dp(n2 + 1);
iota(dp.begin(), dp.end(), 0);
for (int i = 1; i <= n1; i++) {
    vector <int> cur(n2 + 1); cur[0] = i;
    for (int j = 1; j <= n2; j++) {
        if (s1[i - 1] == s2[j - 1]) {
            cur[j] = dp[j - 1];
        }
        lete {</pre>
      radj[vis[u]].push_back(vis[v]);
                                                                                                                                   } else {
                                                                                                                                          // s1 新增等價於 s2 砍掉
                                                                                                                                          // dp[i][j] = min(s2 新增, 修改, s1 新增);
       vector < int > build(int s) {
                                                                                                                                          cur[j]
              dfs(s);
                                                                                                                                                    min({cur[j - 1], dp[j - 1], dp[j]}) + 1;
              for (int i = id - 1; i >= 0; i--) {
    for (int u : radj[i])
        sdom[i] = min(sdom[i], sdom[query(u, 0)]);
                                                                                                                                   }
                                                                                                                             swap(dp, cur);
                    if (i) bucket[sdom[i]].push_back(i);
                    for (int u : bucket[i]) {
   int p = query(u, 0);
   dom[u] = sdom[p] == i ? i : p;
                                                                                                                      cout << dp[n2] << "\n";
                                                                                                               9.4 Bitmask [a626f9]
                    if (i) rt[i] = pa[i];
             for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i])
        dom[i] = dom[dom[i]];
for (int i = 1; i < id; i++)
        res[rev[i]] = rev[dom[i]];
</pre>
                                                                                                               void hamiltonianPath(){
                                                                                                                      int n, m; cin >> n >> m;
vector adj(n, vector < int >());
for (int i = 0; i < m; i++) {
    int u, v; cin >> u >> v;
                                                                                                                            adj[--v].push_back(--u);
              res[s] = s;
                                                                                                                      // 以...為終點,走過...
vector dp(n, vector<<mark>int</mark>>(findBit(n)));
dp[0][1] = 1;
             for (int i = 0; i < n; i++)
    dom[i] = res[i];</pre>
                                                                                                                      dp[0][1] = 1,
for (int mask = 1; mask < findBit(n); mask++) {
    if ((mask & 1) == 0) continue;
    for (int i = 0; i < n; i++) {
        if ((mask & findBit(i)) == 0) continue;
        if (i == n - 1 && mask != findBit(n) - 1) continue;
        int pre_mask = mask ^ findBit(i);
        for (int i = adi[i]) {</pre>
};
9
      DP
9.1 LCS [5781cf]
                                                                                                                                   for (int j : adj[i]) {
    if ((pre_mask & findBit(j)) == 0) continue;
    dp[i][mask
int main() {
       int m, n; cin >> m >> n;
                                                                                                                                                  ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
       string s1, s2; cin >> s1 >> s2;
                                                                                                                                   }
       int L = 0;
                                                                                                                            }
       vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0));
       vector < vector < int >> dp(m + 1, vector < int >< (n -
for (int i = 1; i <= m; i++) {
    for (int j = 1; j <= n; j++) {
        if (s1[i - 1] == s2[j - 1])
            dp[i][j] = dp[i - 1][j - 1] + 1;
}</pre>
                                                                                                                      cout << dp[n - 1][findBit(n) - 1] << "\n";
                                                                                                                     void elevatorRides() {
                           dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
             }
      int length = dp[m][n];    cout << length << "\n";
string s(length, 'c'); // backtracking
while (m >= 1 && n >= 1) {
             if (s1[m - 1] == s2[n - 1]) {
    s[length - 1] = s1[m - 1]
    m--, n--, length--;
             else {
   if (dp[m - 1][n] > dp[m][n - 1]) m--;
             }
                                                                                                                                  cout << s << "\n";
9.2 LIS [66d09f]
int main() {
   int n; cin >> n;
                                                                                                                            }
       vector<int> v(n);
                                                                                                                      cout << dp[findBit(n) - 1][0] << "\n";
       for (int i = 0; i < n; i++) cin >> v[i];
int dp[n]; vector < int >> stk;
       stk.push_back(v[0]);
                                                                                                               9.5 Projects [0942aa]
      dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) {
   if (v[i] > stk.back()) {
                                                                                                               int main() { // 排程有權重問題,輸出價值最多且時間最少
             stk.push_back(v[i]);
    dp[i] = ++L;
} else {
                                                                                                               struct E {
   int from, to, w, id;
                                                                                                                      bool operator < (const E &rhs) {</pre>
                                                                                                                            return to == rhs.to ? w > rhs.w : to < rhs.to;</pre>
                    = lower_bound(stk.begin(), stk.end(), v[i]);
*it = v[i]; dp[i] = it - stk.begin() + 1;
                                                                                                                      int n; cin >> n; vector < E > a(n + 1);
                                                                                                                      int u, v, w; cin >> u >> v >> w;
a[i] = {u, v, w, i};
             }
      vector <int> ans; cout << L << "\n";
for (int i = n - 1; i >= θ; i--) {
   if (dp[i] == L) {
```

vector<array<ll, 2>> dp(n + 1); // w, time

```
National Chung Cheng University Salmon
       vector<array<int, 2>> rec(n + 1); // 有沒選, 上個是誰
       vector < array < int, 2 >> rec(n + 1); // 有沒選, 上個是誰
sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
    auto it = --lower_bound(all(a), E({0, a[i].from}),
    [](E x, E y){ return x.to < y.to; });
    int id = it - a.begin(); dp[i] = dp[i - 1];
    ll nw = dp[id][0] + a[i].w;
    ll nt = dp[id][1] + a[i].to - a[i].from;
    if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
        dp[i] = {nw, nt}; rec[i] = {1, id};
    }
}
                                                                                                                         cout << ans << "\n":
                                                                                                                  9.9 CHT [5f5c25]
       vector < int > ans;
for (int i = n; i != 0;) {
    if (rec[i][0]) {
                                                                                                                         ll m.
                    ans.push_back(a[i].id);
                     i = rec[i][1];
                                                                                                                         }
              } else i--;
                                                                                                                  };
}
9.6 Removal Game [7bb56b]
                                                                                                                                init(n_, init_);
// 兩個人比賽,每個人輪流取一個數字且只能是頭尾
vector <ll> a(n);
for (int i = 0; i < n; i++) cin >> a[i];
       vector dp(n, vector<ll>(n)); // i 到 j 區間的最大 diff
for (int i = n - 1; i >= 0; i--) {
    dp[i][i] = a[i];
    for (int j = i + 1; j < n; j++)
        dp[i][j] =
                             max(a[i] - dp[i + 1][j], a[j] - dp[i][j - 1]);
       \frac{1}{x} + y = sum; // x - y = dp[0][n - 1]
                                                                                                                                // 因此只要 12 跟
       cout << (accumulate</pre>
               (a.begin(), a.end(), 0LL) + dp[0][n - 1]) / 2 << "\n";
            Monotonic Queue [f4976d]
                                                                                                                         void insert(Line L) {
// 應用: dp(i) = h(i) + max(A(j)), for l(i) \le j \le r(i)
// Mc/li 可能包含 dp(j), h(i) 可 0(1)

void Bounded_Knapsack() {
   int n, k; // O(nk)
   vector < int > w(n), v(n), num(n); deque < int > q;
                                                                                                                                hull[++rptr] = L;
       // 於是我們將同餘的數分在同一組
       // 於定我们將阿爾的數分任何 離

// 每次取出連續 num[i] 格中最大值

// g_x = max(_{k=0}^nnum[i] (g'_{x-k} + v_i*k))

// G_x = g'_{x} - v_i*x

// x 代 x-k => v_i*(x-k)

// g_x = max(_{k=0}^nnum[i] (G_{x-k} + v_i*x))

vector < vector < ll>> dp(2, vector < ll>(k + 1));

for (int i = 0; i < n; i++) {
                                                                                                                                       lptr+
                                                                                                                        }
                                                                                                                 };
                                                                                                                  9.10 DNC [61c639]
              for (int r = 0; r < w[i]; r++) { // 餘數
                     q.clear(); // q 記錄在 x = i 時的 dp 有單調性
for (int x = 0; x * w[i] + r <= k; x++) {
    while (!q.empty() && q.front() < x - num[i])
                           q.pop_front(); // 維護遞減
ll nxt = dp[0][x * w[i] + r] - x * v[i];
while (!q.empty() && dp[0][q.back
() * w[i] + r] - q.back() * v[i] < nxt)
                                  q.pop_back();
                           }
              swap(dp[0], dp[1]);
       cout << dp[0][k] << "\n";
```

9.8 SOS [93cb19]

}

```
for (int mask = 0; mask < 1 << m; mask++) {
   int sgn = __builtin_popcount(mask) & 1 ? -1 : 1;
   ans += sgn * (power(Z(2), dp[mask].val()) - 1);</pre>
| // 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \le r(i)
 // A(j), B(j) 可能包含 dp(j), 分別就是 m 跟 b
       line(ll m = 0, ll b = 0) : m(m), b(b) {}
ll eval(ll x) {
    return m * x + b;
 struct CHT { // 用在查詢單調斜率也單調
  int n, lptr, rptr; vector<Line> hull;
  CHT(int n_ = 0, Line init_ = Line()) {
       void init(int n_ = 0, Line init_ = Line()) {
             n = n_; hull.resize(n); reset(init_);
       void reset(Line init_ = Line()) {
    lptr = rptr = 0; hull[0] = init_;
       bool pop_front(Line &l1, Line &l2, ll x) {
            // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y
// 代表查詢的當下,右線段的高度已經低於左線段了
             return l1.eval(x) >= l2.eval(x);
       bool pop_back(Line &l1, Line &l2, Line &l3) {
             // 本題斜率遞減、上凸包
             l3 的 X 交點 <= l1 跟 l3 的 X 交點, l2 就用不到了
return (l3.b - l2.b)
* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
            while (rptr - lptr
> 0 && pop_back(hull[rptr - 1], hull[rptr], L))
       return huli[lptr].eval(x);
 // 應用: 切 k 段問題, 且滿足四邊形不等式
 // 應用: 切 k 段問題, 且滿足四邊形不等式
// w(a,c) + w(b,d) ≤(≥) w(a,d) + w(b,c)
// dp[k][j] = min(dp[k - 1][i] + cost[i][j])
// cost: (i, j]
constexpr int N = 3e3 + 5;
constexpr ll inf = 4e18;
ll dp[N][N]; // 1-based
ll get_cost(int l, int r) {}
 void DNC(int k, int l, int r, int optl, int optr) {
       if (l > r) return;
int m = (l + r) >> 1, opt = -1;
       dp[k][m] = inf;
for (int i = max(k, optl); i <= min(m, optr); i++) {</pre>
             // 注意 i 的範圍、 get_cost 與 dp 的邊界
ll cur = dp[k - 1][i] + get_cost(i, m);
if (cur < dp[k][m]) {
                   dp[k][m] = cur, opt = i;
             }
       DNC(k, l, m - 1, optl, opt);
       DNC(k, m + 1, r, opt, optr);
 int main() {
       // first build cost...

for (int i = 1; i <= n; i++) {
    // init dp[1][i]
       for (int i = 2; i <= k; i++) {
    DNC(i, 1, n, 1, n);</pre>
       cout << dp[k][n] << "\n";
```

9.11 LiChao Segment Tree [f23ef4]

```
// 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j ≤ r(i)
// y = c + m x + b

constexpr ll inf = 4e18;
struct Line {
    ll m, b;
    Line(ll m = 0, ll b = inf) : m(m), b(b) {}
    ll eval(ll x) const { return m * x + b; }
};
```

```
struct LiChaoSeg { // 取 max 再變換就好
     int n;
     vector<Line> info;
     LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_) {
          info.assign(4 << __lg(n), Line());</pre>
     void update(Line line, int node, int l, int r) {
          int m = (l + r) / 2;
bool left = line.eval(l) < info[node].eval(l);
bool mid = line.eval(m) < info[node].eval(m);</pre>
          if (mid) swap(info[node], line); // 如果新線段比較好
          if (r - l == 1) return;
else if (left != mid) update(line, 2 * node, l, m);
          // 代表左半有交點
          else update(line, 2 * node + 1, m, r);
          // 代表如果有交點一定在右半
     void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
          if (r - l == 1) return info[node].eval(x);
int m = (l + r) / 2;
          if (x < m) return
                min(info[node].eval(x), query(x, 2 * node, l, m));
          else return min(
                info[node].eval(x), query(x, 2 * node + 1, m, r));
     il query(int x) { return query(x, 1, 0, n); }
};
```

9.12 Codeforces Example [7d37ea]

```
| // CF 1932 pF
// 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
// 請問在線段不重複的情況下,最多獲得幾分
int main() {
     int n, m;
cin >> n >> m;
     // 記錄每點有幾個線段
     // 再一個紀錄,包含這個點的左界
     cnt[l]++;
         cnt[r + 1]--;
     for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
     vector<int> dp(n + 1);
     dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
         dp[i] = cnt[i];
if (l_side[i] != inf) {
    dp[i] += dp[l_side[i] - 1];
         dp[i] = max(dp[i], dp[i - 1]);
     cout << dp[n] << "\n";
}
// CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
// 再加上 max(bi) - min(bi)
int main(){
     int n, k, ans = 0; cin >> n >> k;
     vector vector color pi v(n + 1);
for (int i = 1; i <= n; i++) {
   int a, b; cin >> a >> b;
   v[i] = {a, b};
   if (a <= k) ans = 1;
</pre>
     sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
         // 用 bi 來排,考慮第 i 個時可以先扣
     for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
              // min(不選, 選)
              if (dp[i
                     1][j - 1] + v[i].first + v[i].second <= k) {
                  // 假如可以選, 更新 ans 時再加回去 bi
                  ans = max(ans, j);
         dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
     cout << ans << endl;
```

10 Geometry

10.1 Basic [d41d8c]

```
template < class T>
struct Point {
     Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) \{ \}
    template < class U > operator Point < U > () {
         return Point<U>(U(x), U(y));
     Point &operator+=(const Point &p) & {
         x += p.x; y += p.y; return *this;
     Point & operator -= (const Point &p) & {
         x -= p.x; y -= p.y; return *this;
     Point &operator*=(const T &v) & {
    x *= v; y *= v; return *this;
     Point & operator /= (const T & v) & {
         x /= v; y /= v; return *this;
     Point operator -() const {
    return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
     friend Point operator - (Point a, const Point &b) {
     friend Point operator*(Point a, const T &b) {
         return a *= b;
     friend Point operator/(Point a, const T &b) {
         return a /= b;
     friend Point operator*(const T &a, Point b) {
   return b *= a;
     friend bool operator==(const Point &a, const Point &b) {
         return a.x == b.x && a.y == b.y;
     friend istream &operator>>(istream &is, Point &p) {
         return is >> p.x >> p.y;
     friend ostream &operator<<(ostream &os, const Point &p) {</pre>
         return os << "(" << p.x << ",
                                               ' << p.y << ")";
template < class T>
T dot(const Point<T> &a, const Point<T> &b) {
    return a.x * b.x + a.y * b.y;
template < class T>
T cross(const Point<T> &a, const Point<T> &b) {
   return a.x * b.y - a.y * b.x;
template < class T>
T square(const Point<T> &p) {
     return dot(p, p);
template < class T>
double length(const Point < T > & p) {
    return sqrt(double(square(p)));
template < class T>
Point<T> normalize(const Point<T> &p) {
    return p / length(p);
template < class T>
Point<T> rotate(const Point<T> &a) {
     return Point(-a.y, a.x);
template < class T>
int sgn(const Point<T> &a) {
    return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
template < class T>
struct Line {
   Point<T> a;
    Line(const Point<T> &a_ = Point<T>()
, const Point<T> &b_ = Point<T>() : a(a_), b(b_) {}
double length(const Line<T> &l) {
    return length(l.a - l.b);
template < class T>
bool parallel(const Line<T> &l1, const Line<T> &l2) {
    return cross(l1.b - l1.a, l2.b - l2.a) == 0;
template < class T>
double distance(const Point<T> &a, const Point<T> &b) {
    return length(a - b);
template < class T>
double distancePL(const Point<T> &p, const Line<T> &l) {
```

```
return abs(cross(l.a - l.b. l.a - p)) / length(l):
template < class T:
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)</pre>
             return distance(p, l.a);
      if (dot(p - l.b, l.a - l.b) < 0)
    return distance(p, l.b);</pre>
       return distancePL(p, 1);
template < class T>
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
      return cross(l.b - l.a, p - l.a) > 0;
template < class T>
Point<T
      template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
      return cross(p - l.a, l.b - l.a) == 0 &&
min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)
                    (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
      (const Point<T> &a, const vector<Point<T>> &p) {
int n = p.size(), t = 0;
for (int i = 0; i < n; i++) {
   if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {</pre>
                   return true:
      for (int i = 0; i < n; i++) {
    auto u = p[i];</pre>
             auto v = p[(i + 1) % n];
if (u.x < a.</pre>
                    x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
             if (u.x >= a
                     .x && v.x < a.x && pointOnLineLeft(a, Line(u, v)))
      return t == 1;
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
    return {0, Point<T>(), Point<T>()};
if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
    return {0, Point<T>(), Point<T>()};
if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
      .
[2.b.y])
                                                                     ĺ2.b.y))
                   return {0, Point<T>(), Point<T>()};
            | else {
    auto maxx1 = max(l1.a.x, l1.b.x);
    auto minx1 = min(l1.a.x, l1.b.x);
    auto maxy1 = max(l1.a.y, l1.b.y);
    auto miny1 = min(l1.a.y, l1.b.y);
    auto miny1 = min(l1.a.y, l1.b.y);
                   auto miny1 = min(l1.a.y, l1.b.y);
auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.y, l2.b.y);
auto miny2 = min(l2.a.y, l2.b.y);
auto miny2 = min(l2.a.y, l2.b.y);
Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
if (!pointOnSegment(p1, l1))
                   swap(p1.y, p2.y);
if (p1 == p2) {
    return {3, p1, p2};
                          return {2, p1, p2};
            }
      auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
       if ((cp1 > 0 && cp2 > 0) || (cp1 < 0 && cp2
        < 0) || (cp3 > 0 && cp4 > 0) || (cp3 < 0 && cp4 < 0))
  return {0, Point<T>(), Point<T>()};
Point p = lineIntersection(l1, l2);
       if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
             return {1, p, p};
      } else {
             return {3, p, p};
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
```

```
if (get<0>(segmentIntersection(l1, l2)) != 0)
      return 0.0;
return min({distancePS(l1.a, l2), distancePS(l1
    .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
bool segmentInPolygon
       (const Line<T> &l, const vector<Point<T>> &p) {
      int n = p.size();
     if (!pointInPolygon(l.a, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
for (int i = 0; i < n; i++) {</pre>
      for (int i = 0; i < auto u = p[i];
           auto v = p[(i + 1) % n];
auto w = p[(i + 2) % n];
           auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
if (t == 1) return false;
if (t == 0) continue;
            if (t == 2) {
                 if (pointOnSegment(v, l) && v != l.a && v != l.b)
    if (cross(v - u, w - v) > 0)
        return false;
           || pointOnLineLeft(l.b, Line(v, u)))
                return false;
} else if (p1 == v) {
    if (l.a == v) {
        if (pointOnLineLeft(u, l)) {
            if (pointOnLineLeft(w, l)) }
                                         && pointOnLineLeft(w, Line(u, v)))
                                         return false:
                            || pointOnLineLeft(w, Line(u, v)))
                                         return false:
                       } else if (l.b == v) {
   if (pointOnLineLeft(u, Line(l.b, l.a))) {
      if (pointOnLineLeft(w, Line(l.b, l.a)))
      && pointOnLineLeft(w, Line(u, v)))
                                         return false;
                             } else {
                                   if (pointOnLineLeft(w, Line(l.b, l.a))
                                         || pointOnLineLeft(w, Line(u, v)))
                                         return false:
                       return false;
                            || pointOnLineLeft(w, Line(u, v)))
                                         return false:
                             }
                       }
                }
           }
      return true:
vector<Point<T>> hp(vector<Line<T>> lines) {
     sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
   auto d1 = l1.b - l1.a;
   auto d2 = l2.b - l2.a;
}
           if (sgn(d1) != sgn(d2))
return sgn(d1) == 1;
           return cross(d1, d2) > 0;
      deaue < Line < T >> ls:
      deque < Point < T >> ps;
for (auto l : lines) {
    if (ls.empty()) {
                 ls.push_back(l);
           while (!ps.empty() && !pointOnLineLeft(ps.back(), l))
           ps.pop_back(), ls.pop_back();
while (!ps.empty() && !pointOnLineLeft(ps[0], l))
    ps.pop_front(), ls.pop_front();
if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
                 if (dot
                       (1.b - l.a, ls.back().b - ls.back().a) > 0) {
if (!pointOnLineLeft(ls.back().a, l)) {
                             assert(ls.size() == 1);
                       continue;
                 return {};
            ps.push_back(lineIntersection(ls.back(), l));
            ls.push_back(l);
      while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0]))
    ps.pop_back(), ls.pop_back();
if (ls.size() <= 2) return {};</pre>
      ps.push_back(lineIntersection(ls[0], ls.back()));
```

```
National Chung Cheng University Salmon
     return vector(ps.begin(), ps.end());
using P = Point<ll>;
10.2 Convex Hull [f99ef6]
template < class T>
vector < Point < T>> convexHull(vector < Point < T>> a) {
    sort(a.begin()
         , a.end(), [](const Point<T> &l, const Point<T> &r) {
return l.x == r.x ? l.y < r.y : l.x < r.x;</pre>
    }):
     a.resize(unique(a.begin(), a.end()) - a.begin());
    if (a.size() <= 1) return a;
vector < Point < T >> hull;
    for(int i = 0; i < 2; i++){
   int t = hull.size();</pre>
         for (Point<T> p : a) {
   while (hull.size)
                    - t >= 2 && cross(hull.back() - hull[hull.size
() - 2], p - hull[hull.size() - 2]) <= 0) {
                   hull.pop_back
                        (); // 要不要有等於要看點有沒有在邊上
              hull.push_back(p);
         hull.pop_back();
         reverse(a.begin(), a.end());
    return hull:
10.3 Min Euclidean Distance [d7fdcf]
void solve() {
    int n; cin >> n;
     constexpr ll inf = 8e18;
     vector < Point < ll >> a(n);
    for (int i = 0; i < n; i++) {
    ll x, y;
    cin >> x >> y;
    a[i] = Point<ll>(x, y);
     struct sortY {
         bool operator
     ()(const Point<ll> &a, const Point<ll> &b) const {
              return a.y < b.y;</pre>
    struct sortXY {
               ()(const Point<ll> &a, const Point<ll> &b) const {
              if (a.x == b.x) return a.y < b.y;
else return a.x < b.x;</pre>
         }
     sort(a.begin(), a.end(), sortXY());
     vector < Point < ll >> t(n);
    vector return < in);
auto devide = [&](auto &&self, int l, int r) -> ll {
    if (l == r) return inf;
    int m = (l + r) / 2;
    ll ans = min(self(self, l, m), self(self, m + 1, r));
}
         ll midval = a[m].x;
         if ((t[i].y
                          t[j].y) * (t[i].y - t[j].y) > ans) break;
              }
         return ans;
    cout << devide(devide, 0, n - 1) << "\n";
10.4 Max Euclidean Distance [0a8bec]
tuple<T, int, int> mxdisPair(vector<Point<T>> a) {
   auto get = [&](const Point<T> &p, const Line<T> &l) -> T {
      return abs(cross(l.a - l.b, l.a - p));
}
    Tres = 0; int n = a.size(), x, y, id = 2;
     a.push_back(a.front());
    if (n <= 2) {
         return {square(a[0] - a[1]), 0, 1};
```

if (res < square(a[i] - a[id])) {
 res = square(a[i] - a[id]);</pre>

x = i, y = id;

```
21
             if (res < square(a[i + 1] - a[id])) {
    res = square(a[i + 1] - a[id]);</pre>
                  x = i + 1, y = id;
      return {res, x, y};
10.5 Lattice Points [00db9d]
int main() {
      // Area 求法與 Polygun 內整數點數
      int n; cin >> n;
vector<Point<ll>> polygon(n);
      for (int i = 0; i < n; i++) cin >> polygon[i];
       ll area = 0;
      for (int i = 0; i < n; i++) {</pre>
            area += cross(polygon[i], polygon[(i + 1) % n]);
      area = abs(area);
      auto countBoundaryPoints
               = [](const vector<Point<ll>>& polygon) -> ll {
             ll res = 0;
             int n = polygon.size();
            for (int i = 0; i < n; i++) {
    ll dx = polygon[(i + 1) % n].x - polygon[i].x;
    ll dy = polygon[(i + 1) % n].y - polygon[i].y;
    res += std::gcd(abs(dx), abs(dy));</pre>
      ll ans = (area - res + 2) / 2;
cout << ans << " " << res << "\n";
}
10.6 Min Circle Cover [02619b]
template < class T>
pair<T, Point<T>> minCircle(vector<Point<T>> &a) {
   random_shuffle(a.begin(), a.end());
      int n = a.size();
      funt n = a.stze();
Point<T> c = a[0]; T r = 0;
for (int i = 1; i < n; i++) {
    if (T(length(c - a[i]) - r) > 0.0) {
        c = a[i], r = 0;
    }
}
                  c = lineIntersection(Line(p,
    p + rotate(a[j] - a[i])), line
    (q, q + rotate(a[k] - a[j])));
r = length(c - a[i]);
                                     }
                              }
                        }
            }
      return {r, c};
10.7 Min Rectangle Cover [b80323]
template < class T>
remplate <ctass 1>
pair <T, vector <Point <T>>> minRectangle(vector <Point <T>> a) {
   if (a.size() <= 2) return {0, {}};
   auto get = [&](const Point <T> &p, const Line <T> &l) -> T {
      return abs(cross(l.a - l.b, l.a - p).x);
}
      int n = a.size(), j = 2, l = 1, r = 1;
      a.push_back(a.front());
      D th, tw, area = numeric_limits < double >::infinity();
      for (int i = 0; i < n; i++) {
    while (get(a[j], Line(a[i], a[i + 1])
        ) <= get(a[(j + 1) % n], Line(a[i], a[i + 1]))) {</pre>
                   j = (j + 1) \% n;
             while (dot(a[i + 1] - a[i], a[r] - a[i])
     <= dot(a[i + 1] - a[i], a[(r + 1) % n] - a[i])) {</pre>
                   r = (r + 1) \% n;
            if (i == 0) l = j;
while (dot(a[i + 1] - a[i], a[l] - a[i])
>= dot(a[i + 1] - a[i], a[(l + 1) % n] - a[i])) {
```

l = (l + 1) % n;

ans.clear

D th = get(a[j], Line(a[i], a[i + 1]));

b tw = dot(a[i] - a[i + 1],
 a[l] - a[i]) + dot(a[i + 1] - a[i], a[r] - a[i]);
if (th * tw / square(a[i + 1] - a[i]) < area) {</pre>

(), area = th * tw / square(a[i + 1] - a[i]);

11 Polynomial

11.1 FFT [2e8718]

```
const double PI = acos(-1.0);
struct Complex {
       double x. v:
        Complex (double x_ = 0, double y_ = 0) : x(x_), y(y_) {}
Complex operator+(const Complex &b) const {
    return Complex(x + b.x, y + b.y);
       Complex operator - (const Complex &b) const {
    return Complex(x - b.x, y - b.y);
        Complex operator*(const Complex &b) const {
  return Complex(x * b.x - y * b.y, x * b.y + y * b.x);
       }
vector<int> rev;
void fft(vector<Complex> &a, bool inv) {
        int n = a.size();
        if (int(rev.size()) != n) {
                int k = __builtin_ctz(n) - 1;
rev.resize(n);
                for (int i = 0; i < n; i++) {
    rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;
        for (int i = 0; i < n; i++) {
    if (rev[i] < i) {
        swap(a[i], a[rev[i]]);
    }
}</pre>
       for (int k = 1; k < n; k *= 2) {
    double ang = (inv ? -1 : 1) * PI / k;
    Complex wn(cos(ang), sin(ang));
    for (int i = 0; i < n; i += 2 * k) {
        Complex w(1);
        for (int j = 0; j < k; j++, w = w * wn) {
            Complex u = a[i + j];
            Complex v = a[i + j + k] * w;
            afi + il = u + v:</pre>
                                 a[i + j] = u + v;
a[i + j + k] = u - v;
                }
        if (inv) {
                for (auto &x : a) {
                        x.x /= n;
x.y /= n;
       }
template < class T>
vector<T> mulT(const vector<T> &a, const vector<T> &b) {
       vector<Complex
                 > fa(a.begin(), a.end()), fb(b.begin(), b.end());
       > ra(a.begin(), a.end()), rb(b.begint)
int n = 2 << __lg(a.size() + b.size());
fa.resize(n), fb.resize(n);
fft(fa, false), fft(fb, false);
for (int i = 0; i < n; i++) {
    fa[i] = fa[i] * fb[i];
}</pre>
        fft(fa, true);
       rit(la, true);
vector <T> res(n);
for (int i = 0; i < n; i++) {
    if constexpr (!is_same_v < T, double >) {
        res[i] = round(fa[i].x);
}
                } else {
    res[i] = fa[i].x;
       return res;
```

11.2 NTT [1c9189]

```
template < int V, ll P>
constexpr MInt < P> CInv = MInt < P> (V).inv();

vector < ll> rev;
template < ll P>
vector < MInt < P>> roots {0, 1};

template < int P>
```

```
constexpr MInt<P> findPrimitiveRoot() {
              MInt<P> i =
              int k = __builtin_ctz(P - 1);
while (true) {
    if (power(i, (P - 1) / 2) != 1) {
                                         break;
              return power(i, (P - 1) >> k);
 template < ll P >
 constexpr MInt<P> primitiveRoot = findPrimitiveRoot<P>();
 constexpr MInt<998244353> primitiveRoot<998244353> {31};
 template < ll P >
rev.resize(n);

for (int i = 0; i < n; i++) {

    rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;
              for (int i = 0; i < n; i++) {
    if (rev[i] < i) {</pre>
                                        swap(a[i], a[rev[i]]);
              if (roots<P>.size() < n) {
   int k = __builtin_ctz(roots<P>.size());
   roots<P>.resize(n);
                           k++:
                           }
              for (int k = 1; k < n; k *= 2) {
    for (int i = 0; i < n; i += 2 * k) {
        for (int j = 0; j < k; j++) {
            MInt<P> u = a[i + j];
            MInt<P> v = a[i + j + k] * roots<P>[k + j];
            a[i + j] = u + v;
            a[i + j + k] = u - v;
            a[i + j + k] = u - v;
            aline for a finite form of the form o
                                        }
                         }
             }
}
 template < ll P >
 constexpr void idft(vector<MInt<P>> &a) {
   int n = a.size();
               reverse(a.begin() + 1, a.end());
             feverse(a.begtin() + 1, a.enu(
dft(a);
MIntrP> inv = (1 - P) / n;
for (int i = 0; i < n; i++) {
    a[i] *= inv;
}</pre>
}
Poly(const vector<Value> &a) : vector<Value>(a) {}
              constexpr Poly(const
    initializer_list<Value> &a) : vector<Value>(a) {}
template<class InputIt, class = _RequireInputIter<InputIt>>
explicit constexpr Poly(InputIt
    first, InputIt last) : vector<Value>(first, last) {}
template<class F>
              explicit constexpr Poly(int n, F f) : vector<Value>(n) {
    for (int i = 0; i < n; i++) {
        (*this)[i] = f(i);
    }
}</pre>
              constexpr Poly shift(int k) const {
   if (k >= 0) {
      auto b = *this;
      b.insert(b.begin(), k, 0);
}
                                         return b;
                           } else if (this->size() <= -k) {</pre>
                                        return Poly();
                                        return Poly(this->begin() + (-k), this->end());
              constexpr Poly trunc(int k) const {
  Poly f = *this;
  f.resize(k);
                           return f;
```

```
constexpr
    friend Poly operator+(const Poly &a, const Poly &b) {
       Poly res(max(a.size(), b.size()));

for (int i = 0; i < a.size(); i++) {

    res[i] += a[i];
       for (int i = 0; i < b.size(); i++) {
    res[i] += b[i];</pre>
       return res;
constexpr
       friend Poly operator - (const Poly &a, const Poly &b) {
Poly res(max(a.size(), b.size()));
for (int i = 0; i < a.size(); i++) {</pre>
              res[i] += a[i];
       for (int i = 0; i < b.size(); i++) {</pre>
              res[i] -= b[i];
       return res:
constexpr friend Poly operator - (const Poly &a) {
   vector < Value > res(a.size());
   for (int i = 0; i < int(res.size()); i++) {</pre>
              res[i] = -a[i];
       return Poly(res);
constexpr friend Poly operator*(Poly a, Poly b) {
  if (a.size() == 0 || b.size() == 0) {
    return Poly();
      }
if (a.size() < b.size()) swap(a, b);
int n = 1, tot = a.size() + b.size() - 1;
while (n < tot) n *= 2;
if (((P - 1) & (n - 1)) != 0 || b.size() < 128) {
    Poly c(a.size() + b.size() - 1);
    for (int i = 0; i < a.size(); i++) {
        c[i + j] += a[i] * b[j];
}</pre>
              return c:
       a.resize(n), b.resize(n);
dft(a), dft(b);
for (int i = 0; i < n; ++i) {
              à[i] *= b[i];
       idft(a);
       a.resize(tot);
       return a;
constexpr friend Poly operator*(Value a, Poly b) {
       for (int i = 0; i < int(b.size()); i++) {
  b[i] *= a;</pre>
       return b;
constexpr friend Poly operator*(Poly a, Value b) {
       for (int i = 0; i < int(a.size()); i++) {
    a[i] *= b;
}</pre>
constexpr friend Poly operator/(Poly a, Value b) {
   for (int i = 0; i < int(a.size()); i++) {
      a[i] /= b;
}</pre>
       return a;
constexpr Poly &operator+=(Poly b) {
   return (*this) = (*this) + b;
constexpr Poly &operator -=(Poly b) {
      return (*this) = (*this) - b;
constexpr Poly &operator*=(Poly b) {
   return (*this) = (*this) * b;
constexpr Poly &operator*=(Value b) {
      return (*this) = (*this) * b;
constexpr Poly &operator/=(Value b) {
   return (*this) = (*this) / b;
constexpr Poly deriv() const {
       if (this->empty()) return Poly();
Poly res(this->size() - 1);
for (int i = 0; i < this->size() - 1; ++i) {
              res[i] = (i + 1) * (*this)[i + 1];
       return res;
constexpr Poly integr() const {
   Poly res(this->size() + 1);
   for (int i = 0; i < this->size(); ++i) {
      res[i + 1] = (*this)[i] / (i + 1);
   }
}
       return res;
```

```
constexpr Poly inv(int m) const {
   Poly x{(*this)[0].inv()};
            int k = 1;
while (k < m) {
 k *= 2;
                  x = (x * (Poly{2} - trunc(k) * x)).trunc(k);
            return x.trunc(m);
      constexpr Poly log(int m) const {
   return (deriv() * inv(m)).integr().trunc(m);
      constexpr Poly exp(int m) const {
            Poly x{1};
int k = 1;
            while (k < m) {
   k *= 2;
   x = (x * (Poly{1} - x.log(k) + trunc(k))).trunc(k);</pre>
            return x.trunc(m);
      constexpr Poly pow(int k, int m) const {
            int i = 0;
            while (i < this->size() && (*this)[i] == 0) {
            if (i == this->size() || 1LL * i * k >= m) {
                  return Poly(m);
            Value v = (*this)[i];
auto f = shift(-i) * v.inv();
return (f.log(m - i *
                   k) * k).exp(m - i * k).shift(i * k) * power(v, k);
      constexpr Poly sqrt(int m) const {
           Poly x{1};

int k = 1;

while (k < m) {

    k *= 2;
                  x = (x +
                           (trunc(k) * x.inv(k)).trunc(k)) * CInv<2, P>;
            return x.trunc(m);
      constexpr Poly mulT(Poly b) const {
            if (b.size() == 0) return Poly();
int n = b.size();
reverse(b.begin(), b.end());
return ((*this) * b).shift(-(n - 1));
      constexpr vector<Value> eval(vector<Value> x) const {
   if (this->size() == 0) {
      return vector<Value>(x.size(), 0);
}
            const int n = max(x.size(), this->size());
            vector<Poly> q(4 * n);
            vector < Value > ans(x.size());
            x.resize(n);
            function < void (
                  int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
                        q[p] = Poly{1, -x[l]};
                 qlpj - - - ,;
} else {
   int m = (l + r) / 2;
   build(2 * p, l, m);
   build(2 * p + 1, m, r);
   q[p] = q[2 * p] * q[2 * p + 1];
                 }
            };
build(1, 0, n);
function < void(int, int, int, const Poly &) >
    work = [&](int p, int l, int r, const Poly &num) {
    if (r - l == 1) {
        if (l < int(ans.size())) {
            ans[l] = num[0];
        }
};</pre>
                  m, num.mulT(q[2 * p + 1]).resize(m - l)); work(2 * p + 1,
                                m, r, num.mulT(q[2 * p]).resize(r - m));
                 }
            work(1, 0, n, mulT(q[1].inv(n)));
            return ans;
     }
};
template < ll P = 998244353>
Poly<P> berlekampMassey(const Poly<P> &s) {
      Poly<P> c, oldC;
      int f = -1;
for (int i = 0; i < s.size(); i++) {</pre>
            auto delta = s[i];
for (int j = 1; j <= c.size(); j++) {
    delta -= c[j - 1] * s[i - j];</pre>
            if (delta == 0) continue;
if (f == -1) {
                  c.resize(i + 1);
```

```
} else {
    auto d = oldC;
    d *= -1;
                   d.insert(d.begin(), 1);
                   Mint df1 = 0;
for (int j = 1; j <= d.size(); j++) {
    df1 += d[j - 1] * s[f + 1 - j];
}</pre>
                   assert(df1 != 0);
auto coef = delta / df1;
d *= coef;
                   Poly<P> zeros(i - f - 1);
                   zeros.insert(zeros.end(), d.begin(), d.end());
                   d = zeros;
auto temp = c;
                  c += d;
if (i - temp.size() > f - oldC.size()) {
    oldC = temp;
    f = i;
                  }
            }
      c *= -1;
      c.insert(c.begin(), 1);
template < ll P = 998244353>
MInt < P > linear Recurrence (Poly < P > p , Poly < P > q , ll n) {
     fauto newp = p * newq;
newq = q * newq;
for (int i = 0; i < m; i++) {
    p[i] = newp[i * 2 + n % 2];</pre>
            for (int i = 0; i <= m; i++) {
    q[i] = newq[i * 2];</pre>
            n /= 2;
      return p[0] / q[0];
```

12 Else

12.1 Python [44ab0e]

```
from decimal import * # 無誤差浮點數
from fractions import * # 分數
from random import *
from math import *
# set decimal prec if it could overflow in precision
setcontext(Context(prec=10, rounding=ROUND_FLOOR))
# read and print
x = int(input())
a, b, c = map(Fraction, input().split())
arr = map(Decimal, input().split())
print(x)
print(a, b, c)
print(*arr)
# set
S = set(); S.add((a, b)); S.remove((a, b))
if not (a, b) in S:
# dict
D = dict(); D[(a, b)] = 1; del D[(a, b)]

for (a, b) in D.items():
# random
arr = [randint(l, r) for i in range(size)] choice([8, 6, 4, 1]) # random pick one shuffle(arr)
```