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```

1 Basic

1.1 Install VScode [d41d8c]

```
|// 如何安裝 vscode
|// 1. 下載 vscode & msys2
|// 2. 在跳出的 terminal 中 / 或打開 ucrt64 , 打上
    "pacman -S --needed base-devel mingw-w64-x86_64-toolchain"
|// 3. 環境變數加上 C:\\msys64\\ucrt64\\bin
|// 4. 重開 vscode, 載 C/C++, 運行, 編譯器選擇 g++
|// 5. 打開 settings -> compiler -> add compilerPath
    -> 在 "" 裡打上 C:\\msys64\\ucrt64\\bin\\g++.exe
```

1.2 Default Code [d41d8c]

```
#include <bits/stdc++.h>
#pragma GCC optimize("03")
// #pragma GCC target("popcnt")
// C++ 20 vector grammer will not work
#define all(x) (x).begin(), (x).end()
using namespace std;
using ll = long long;

void solve() {
}
int main() {
   ios_base::sync_with_stdio(false);
   cin.tie(nullptr);
   int t = 1;
   cin >> t;
   while (t--) {
      solve();
   }
}
```

1.3 Compare Fuction [d41d8c]

```
// 如果有自定義比較結構就比照以上
};
struct cmp { // 要在 template 的資
  vector <int> &v;
  cmp(vector <int>& vec) : v(vec) {}
                   // 要在 template 的資結用外部變數
     bool operator() (int a, int b) const {
   return v[a] > v[b];
// s
// main: cmp cmp1(vector);
// priority_queue<int, vector<int>, cmp> pq(cmp1);
};
1.4 Pbds [d41d8c]
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < typename T >
using pbds_set = tree<T, null_type,
    less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template < typename T>
1.5 Edouble [d41d8c]
struct EDouble {
     double x;
     constexpr static double Eps = 1e-9;
     constexpr EDouble(): x{} {}
constexpr EDouble(double v): x{v} {}
constexpr double val() const {
          return x;
     explicit constexpr operator double() const {
          return x;
     constexpr EDouble operator-() const {
          return EDouble(-x);
     constexpr EDouble &operator+=(const EDouble &rhs) & {
          x += rhs.x;
return *this;
     constexpr EDouble &operator -= (const EDouble &rhs) & {
          x -= rhs.x;
          return *this;
     constexpr EDouble &operator*=(const EDouble &rhs) & {
    x *= rhs.x;
          return *this:
     constexpr EDouble &operator/=(const EDouble &rhs) & {
          assert(fabs(rhs.x) > Eps);
          x /= rhs.x;
return *this;
     friend constexpr
            EDouble operator+(EDouble lhs, const EDouble &rhs) {
          return lhs
            EDouble operator - (EDouble lhs, const EDouble &rhs) {
          lhs -= rhs;
return lhs;
     friend constexpr
           EDouble operator*(EDouble lhs, const EDouble &rhs) {
          return lhs:
     friend constexpr
            EDouble operator/(EDouble lhs, const EDouble &rhs) {
          lhs /= rhs;
return lhs;
     friend constexpr bool
            operator < (const EDouble &lhs, const EDouble &rhs) {</pre>
          return lhs.x - rhs.x < -Eps;</pre>
     friend constexpr bool
            operator > (const EDouble &lhs, const EDouble &rhs) {
          return lhs.x - rhs.x > Eps;
     friend constexpr bool
    operator == (const EDouble &lhs, const EDouble &rhs) {
          return fabs(lhs.x - rhs.x) < Eps;</pre>
     friend constexpr bool
    operator<=(const EDouble &lhs, const EDouble &rhs) {</pre>
          return lhs < rhs || lhs == rhs;
     friend constexpr bool
          operator >= (const EDouble &lhs, const EDouble &rhs) {
return lhs > rhs || lhs == rhs;
     friend constexpr bool
            operator!=(const EDouble &lhs, const EDouble &rhs) {
          return !(lhs == rhs);
```

```
friend istream &operator>>(istream &is, EDouble &a) {
       double v; is >> v;
       a = EDouble(v);
       return is:
   } // Eps should < precision
namespace std {
   template<>
   class numeric_limits < EDouble > {
   public:
       static constexpr EDouble max() noexcept {
          return EDouble(numeric_limits < double >:: max());
       static constexpr EDouble min() noexcept {
          return EDouble(numeric_limits < double >:: min());
   };
using E = EDouble;
```

2 Graph

2.1 DFS And BFS [cdd1d5]

```
int main() {
      int n:
      vector<vector<int>> adj(n + 1, vector<int>());
      // dfs_graph
      vector <bool>
vector <bool>
auto dfs = [&](auto self, int u) -> void {
            if (vis[u]) return;
            vis[u] = true;
for (auto v: adj[u]) {
                  self(self, v);
            }
      dfs(dfs, 1);
      // bfs
vector<int> depth(n + 1, 1e9);
      vector <tnt> depth(n + 1, 1e9);
queue <int> q;
auto bfs = [8](auto self, int u) -> void {
    vis[u] = true;
    depth[u] = 0;
             q.push(u);
             while (!q.empty()) {
                  int u = q.front(); q.pop();
for (auto v : adj[u]) {
                         if (vis[v]) continue;
vis[v] = true;
depth[v] = depth[u] + 1;
                         q.push(v);
                  }
            }
      bfs(bfs, 1);
}
```

2.2 Prim [f00ec0]

2.3 BellmanFord [430ded]

```
par[v] = u;
    if (i == n) t = v;
}

}
if (t == -1) { cout << "NO|n"; return; }
for (int i = 1; i < n; i++) t = par[t];
vector<int> ans {t};
int i = t;
do {
    i = par[i];
    ans.push_back(i);
} while (i != t);
reverse(ans.begin(), ans.end());
cout << "YES|n";
for (auto x : ans) cout << x + 1 << " ";</pre>
```

2.4 FloydWarshall [206b76]

2.5 Euler [4177dc]

```
| // 1. 無向圖是歐拉圖:
// 非零度頂點是連通的
// 頂點的度數都是偶數
// 2. 無向圖是半歐拉圖(有路沒有環):
// 非零度頂點是連通的
// 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
// 非零度頂點是強連通的
// 每個頂點的入度和出度相等
// 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
// 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
// 其他頂點的入度和出度相等
vector<int> ans;
 auto dfs = [&](auto &&self, int u) -> void {
    while (g[u].size()) {
   int v = *g[u].begin();
       g[u].erase(v);
       self(self, v);
   ans.push back(u);
dfs(dfs, 0);
reverse(ans.begin(), ans.end());
```

2.6 SCC [5d3e16]

```
struct SCC {
    int n, cur, cnt;
    vector<vector<int>> adj;
    vector<int>> stk, dfn, low, bel;
    SCC(int n_ = 0) {
        init(n_);
    }
    void init(int n_) {
        n = n_;
        adj.assign(n, {});
        dfn.assign(n, -1);
        low.resize(n);
        bel.assign(n, -1);
```

```
stk.clear();
            cur = cnt = 0;
      void addEdge(int u, int v) {
            adj[u].push_back(v);
      void dfs(int x) {
    dfn[x] = low[x] = cur++;
            stk.push_back(x);
            for (auto y : adj[x]) {
   if (dfn[y] == -1) {
                        dfs(y);
                  low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
                  }
            if (dfn[x] == low[x]) {
                   int y;
                  do {
                        y = stk.back();
bel[y] = cnt;
                        stk.pop_back();
                  } while (y != x);
            }
      fvector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
            return bel;
      struct Graph {
            vector<pair<int, int>> edges;
            vector < int > siz;
vector < int > cnte;
      Graph compress() {
            Graph g;
g.n = cnt;
            g.siz.resize(cnt);
            g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
                  g.siz[bel[i]]++;
                  for (auto j : adj[i]) {
    if (bel[i] != bel[j]) {
                              g.edges.emplace_back(bel[i], bel[j]);
                        } else {
   g.cnte[bel[i]]++;
                  }
            return g;
      }
};
```

2.7 VBCC [170604]

```
struct VBCC {
     int n, cur;
     vector<vector<int>> adi:
     vector<int> dfn, low, parent;
     vector < bool > is_cut;
VBCC(int n_ = 0) {
    init(n_);
     void init(int n_) {
          n = n_;
adj.assign(n, {});
          dfn.assign(n, -1);
          low.resize(n):
          parent.assign(n, -1);
          is_cut.assign(n, false);
          cur = 0;
     void addEdge(int u, int v) {
    adj[u].push_back(v);
          adj[v].push_back(u);
     void dfs(int x) {
          int children = 0;
dfn[x] = low[x] = cur++;
          for (int v : adj[x]) {
   if (dfn[v] == -1) {
                     children++;
parent[v] = x;
                     dfs(v);
                     low[x] = min(low[x], low[v]);
                     if (parent[x] != -1 && low[v] >= dfn[x]) {
    is_cut[x] = true;
               } else if (v != parent[x]) {
                     low[x] = min(low[x], dfn[v]);
          if (parent[x] == -1 && children > 1) {
    is_cut[x] = true;
     }
```

```
void work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i);
        }
    }
}</pre>
```

2.8 EBCC [49d862]

```
struct EBCC { // CF/contest/1986/pF
  int n, cur, cnt;
  vector<vector<int>> adj;
       vector<int> stk, dfn, low, bel;
       vector<pair<int, int>> bridges; // 關鍵邊
       EBCC(int n_) {
            init(n_);
       void init(int n_) {
             n = n_;
adj.assign(n, {});
             dfn.assign(n, -1);
              low.resize(n);
             bel.assign(n, -1);
             stk.clear():
             bridges.clear();
             cur = cnt = 0;
       void addEdge(int u, int v) {
             adj[u].push_back(v);
             adj[v].push_back(u);
       void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
             stk.push_back(x);
              for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
                          dfs(y, x);
                          low[x] = min(low[x], low[y]);
if (low[y] > dfn[x]) {
    bridges.emplace_back(x, y);
                    } else if (bel[y] == -1) {
    low[x] = min(low[x], dfn[y]);
             if (dfn[x] == low[x]) {
                    int y;
do {
                          v = stk.back();
                          bel[y] = cnt;
                    stk.pop_back();
} while (y != x);
                    cnt++;
      fvector<int> work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
        }
}</pre>
             return bel:
       struct Graph {
             int n;
vector<pair<int, int>> edges;
             vector<int> siz; // BCC 內節點數
             vector<int> cnte; // BCC 內邊數
       Graph compress() {
             Graph g;
g.n = cnt;
             g.siz.resize(cnt);
             g.cnte.resize(cnt);
             g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;
    for (auto j : adj[i]) {
        if (bel[i] < bel[j]) {
            g.edges.emplace_back(bel[i], bel[j]);
        } else if (i < j) {
            g.cnte[bel[i]]++;
        }
}</pre>
                          }
                    }
              return g;
      }
```

2.9 2-SAT [eeddc1]

```
// CSES Giant Pizza
struct TwoSat {
  int n;
  vector<vector<int>> e;
  vector<bool> ans;
  TwoSat(int n) : n(n), e(2 * n), ans(n) {}
  void addClause(int u, bool f, int v, bool g) {
    e[2 * u + !f].push_back(2 * v + g);
}
```

```
e[2 * v + !q].push back(2 * u + f):
     bool satisfiable() {
          vector<int
                > id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
           vector<int> stk;
           int now = 0, cnt = 0;
function < void(int) > tarjan = [&](int u) {
               stk.push_back(u);
dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
                     tr (drn[v] == -1) {
    tarjan(v);
    low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in stk
    low[u] = min(low[u], dfn[v]);
                if (dfn[u] == low[u]) {
                     int v;
do {
    v = stk.back();
                          stk.pop_back();
                          id[v] = cnt;
                     } while (v != u);
                      ++cnt;
               }
           for (int i
          vector < bool > answer() { return ans; }
int main() {
     int m, n; cin >> m >> n;
TwoSat ts(n);
for (int i = 0; i < m; ++i) {</pre>
          int u, v; char x, y;
cin >> x >> u >> y >> v;
ts.addClause(u - 1, x == '+', v - 1, y == '+');
     else cout << "IMPOSSIBLE\n";</pre>
}
```

2.10 Funtional Graph [85c464]

```
constexpr int N = 2e5 + 5;
int cht[N][31]; // 倍增表, 放外面不然 TLE
struct FuntionalGraph {
      g = g_; bel.assign(n, -1);
id.resize(n); len.clear();
in.assign(n, 0); top.assign(n, -1);
              build();
      }
void build() {
    for (int i = 0; i < n; i++) {
        cht[i][0] = g[i];
        in[g[i]]++;</pre>
              for (int i = 1; i <= 30; i++)
    for (int u = 0; u < n; u++)
        cht[u][i] = cht[cht[u][i - 1]][i - 1];
for (int i = 0; i < n; i++)
    if (in[i] == 0) label(i);
for (int i = 0; i < n; i++)
    if (top[i] == -1) label(i);</pre>
       void label(int u) {
              vector<int> p; int cur = u;
while (top[cur] == -1) {
   top[cur] = u;
                      p.push_back(cur);
                      cur = g[cur];
               auto s = std::find(p.begin(), p.end(), cur);
              vector < int> cyc(s, p.end());
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {
    bel[cyc[i]] = cnt;
}</pre>
                      id[cyc[i]] = i;
               cnt++; len.push_back(cyc.size());
              for (int i = p.size() - 1; i > 0; i--)
   id[p[i - 1]] = id[p[i]] - 1;
       int jump(int u, int k) {
```

```
for (int b = 0; k > 0; b++){
    if (k & 1) u = cht[u][b];
    k >>= 1;
}
return u;
}
```

3 Data Structure

3.1 BIT [d41d8c]

```
template <typename T>
 struct Fenwick { // 全部以 0 based 使用
      vector < T > a;
Fenwick(int n_ = 0) {
            init(n_);
       void init(int n_) {
            a.assign(n, T{});
       void add(int x, const T &v) {
            for (int i = x + 1; i <= n; i += i & -i) {
   a[i - 1] = a[i - 1] + v;</pre>
       T sum(int x) { // 左閉右開查詢
            for (int i = x; i > 0; i -= i & -i) {
    ans = ans + a[i - 1];
            return ans;
      }
      T rangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
       int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
            T cur{};
for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n && cur + a[x + i - 1] <= k) {</pre>
                       x += i;
                       cur = cur + a[x - 1];
                }
            return x;
      }
 template <class T>
 struct TwoDFenwick { // 全部以 0 based 使用
      int nx, ny; // row, col 個數 vector<vector<T>> a;
       TwoDFenwick(int nx_ = 0, int ny_ = 0) {
            init(nx_, ny_);
       void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
      for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        a[i - 1][j - 1] = a[i - 1][j - 1] + v;
    }
}</pre>
      }
       T sum(int x, int y) { // 左閉右開查詢
            for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans + a[i - 1][j - 1];
}
            return ans;
       ,
T rangeSum
             (int lx, int ly, int rx, int ry) { // 左閉右開查詢
            return sum(
                  rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
     }
};
```

3.2 RangeBit [d41d8c]

```
| template <typename T>
| struct rangeFenwick { // 全部以 0 based 使用 int n; vector <T> d, di; rangeFenwick(int n_ = 0) { init(n_); }
| void init(int n_) { n = n_; d.assign(n, T{}); di.assign(n, T{}); }
| void add(int x, const T &v) { T vi = v * (x + 1); }
```

iota(boss.begin(), boss.end(), 0);

```
for (int i = x + 1; i <= n; i += i & -i) {
    d[i - 1] = d[i - 1] + v;
    di[i - 1] = di[i - 1] + vi;
}</pre>
                                                                                                                            siz.assign(n, 1);
                                                                                                                     int find_boss(int x) {
   if (boss[x] == x) return x;
   return boss[x] = find_boss(boss[x]);
             }
      void rangeAdd(int l, int r, const T &v) {
   add(l, v); add(r, -v);
                                                                                                                     bool same(int x, int y) {
    return find_boss(x) == find_boss(y);
      T sum(int x) { // 左閉右開查詢
                                                                                                                     bool merge(int x, int y) {
    x = find_boss(x);
    y = find_boss(y);
             T ans{};
             for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
                                                                                                                            if (x == y) {
    return false;
             return ans;
                                                                                                                            if(siz[x] < siz[y]) swap(x, y);
siz[x] += siz[y];</pre>
      T rangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
                                                                                                                            boss[y] = x;
                                                                                                                            return true;
      int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
            T cur{};
for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n) {</pre>
                                                                                                                     int size(int x) {
   return siz[find_boss(x)];
                                                                                                                     }
                                                                                                              }:
                          struct DSU {
   int n;
                                 x += i;
                                                                                                                      vector < int > boss, siz, stk;
                                 cur = cur + val:
                                                                                                                     DSU() {}
DSU(int n_) {
                          }
                   }
                                                                                                                            init(n_);
             return x:
                                                                                                                      void init(int n_) {
     }
                                                                                                                            n = n_;
                                                                                                                            boss.resize(n);
template <class T>
                                                                                                                            iota(boss.begin(), boss.end(), 0);
siz.assign(n, 1);
struct rangeTwoDFenwick { // 全部以 0 based 使用
      int nx, ny; // row, col 個數
vector <vector <T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
init(xy_ = xy_ = 0)
                                                                                                                            stk.clear();
                                                                                                                     int find(int x) {
   return x == boss[x] ? x : find(boss[x]);
             init(nx_, ny_);
      void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));

                                                                                                                     bool same(int x, int y) {
   return find(x) == find(y);
                                                                                                                     bool merge(int x, int y) {
    x = find(x);
    y = find(y);
             dij.assign(nx, vector<T>(ny, T{}));
                                                                                                                            if (x == y) {
    return false;

}
void add(int x, int y, const T &v) {
    T vi = v * (x + 1);
    T vj = v * (y + 1);
    T vij = v * (x + 1) * (y + 1);
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            d[i - 1][j - 1] = d[i - 1][j - 1] + v;
            di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
            dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
            dij[i - 1][j - 1] = dij[i - 1][j - 1] + vj;
            dij[i - 1][j - 1] = dij[i - 1][j - 1] + vij;
            reconstructions.
}
</pre>
                                                                                                                            if (siz[x] < siz[y]) swap(x, y);
siz[x] += siz[y];</pre>
                                                                                                                            boss[y] = x;
                                                                                                                            stk.push_back(y);
return true;
                                                                                                                     void undo(int x) {
                                                                                                                            while (stk.size() > x) {
    int y = stk.back();
                   }
                                                                                                                                   stk.pop_back();
      void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
            add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
                                                                                                                                   siz[boss[y]] -= siz[y];
                                                                                                                                  boss[y] = y;
                                                                                                                            }
                                                                                                                     int size(int x) {
   return siz[find(x)];
      T sum(int x, int y) { // 左閉右開查詢
            };
                                                                                                              3.4 Segment [d41d8c]
                                                                                                             template <class Info>
                                                                                                                     int n; vector<Info> info;
Seg(): n(0) {}
Seg(int n_, Info v_ = Info()) {
    init(n_, v_);
  }
                                                                                                              struct Seg {
                          ans = ans + dij[i - 1][j
                   }
             return ans;
      }
T rangeSum
                                                                                                                      template <class T>
                                                                                                                     Seg(vector<T> init_) {
              (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                                                                                                                            init(init_);
             return sum(
                    (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
                                                                                                                     void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
3.3 DSU [d41d8c]
                                                                                                                     template <class T>
                                                                                                                      void init(vector<T> init_) {
struct DSU {
                                                                                                                            n = init_.size();
                                                                                                                            info.assign(4 << __lg(n), Info());
function <void(</pre>
      int n:
      vector < int > boss, siz;
      DSU() {}
DSU(int n_) {
   init(n_);
                                                                                                                                   int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
   info[p] = init_[l];
      void init(int n_) {
                                                                                                                                  int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
             n = n_;
boss.resize(n);
```

tag[p].apply(v);

```
void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
                 pull(p):
            build(1, 0, n);
     (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
                                                                                                             tag[p] = Tag();
                                                                                                       void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
}
                 info[p] = v;
                 return;
            int m = (l + r) / 2;
                                                                                                                   return:
           if (x < m) {
    modify(2 * p, l, m, x, v);
                                                                                                             int m = (l + r) / 2;
                                                                                                             push(p, l, r);
                 modify(2 * p + 1, m, r, x, v);
                                                                                                             if (x < m) {
                                                                                                                  modify(2 * p, l, m, x, v);
           pull(p);
                                                                                                             } else {
                                                                                                                  modify(2 * p + 1, m, r, x, v);
      void modify(int p, const Info &i) {
                                                                                                             pull(p);
           modify(1, 0, n, p, i);
     info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];</pre>
                                                                                                       void modify(int p, const Info &i) {
                                                                                                             modify(1, 0, n, p, i);
           int m = (l + r) / 2;
return query(p *
                                                                                                       Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];</pre>
                  2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
                                                                                                             int m = (l + r) / 2;
      Info query
                                                                                                             push(p, l, r);
      (int ql, int qr) { return query(1, 0, n, ql, qr); }
template < class F> // 尋找區間內,第一個符合條件的
                                                                                                             return query(p *
2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      int findFirst
                                                                                                       Info query
    (int ql, int qr) { return query(1, 0, n, ql, qr); }
             (int p, int l, int r, int x, int y, F &&pred) {
           if (l >= y || r <= x)
                                                                                                       void range_apply
  (int p, int l, int r, int ql, int qr, const Tag &v) {
  if (qr <= l || ql >= r) return;
  if (ql <= l && r <= qr) {</pre>
                 return 1:
            if (l >= x && r <= y && !pred(info[p]))</pre>
           return -1;
if (r - l == 1)
                                                                                                                   apply(p, l, r, v);
                 return l;
           int m = (l + r) / 2;
int res = findFirst(2 * p, l, m, x, y, pred);
if (res == -1)
                                                                                                                  return:
                                                                                                             int m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
                 res = findFirst(2 * p + 1, m, r, x, y, pred);
            return res;
                                                                                                             range_apply(p * 2 + 1, m, r, ql, qr, v);
     template < class F> // 若要找 last <sup>*</sup> 先右子樹遞廻即可
int findFirst(int l, int r, F & & pred) {
    return findFirst(1, 0, n, l, r, pred);
                                                                                                             pull(p):
                                                                                                       void range_apply(int l, int r, const Tag &v) {
                                                                                                             range_apply(1, 0, n, l, r, v);
                                                                                                       template < class F> // 尋找區間內,第一個符合條件的
// ---define structure and info plus---
                                                                                                       int findFirst
struct Info {
                                                                                                             (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
   return -1;</pre>
     int n = 0;
int sum = 0;
Info operator+(const Info &a, const Info &b) {
    return { a.n + b.n, a.sum + b.sum };
                                                                                                             if (l >= x && r <= y && !pred(info[p])) {</pre>
                                                                                                                   return -1;
3.5 Lazy Segment [d41d8c]
                                                                                                             if (r - l == 1) {
                                                                                                                   return l:
template <class Info, class Tag>
struct LazySeg { // 左閉右開寫法
                                                                                                             int m = (l + r) / 2;
                                                                                                             push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
      int n;
      vector < Info > info:
     vector <Inio tino;
vector <Tag> tag;
LazySeg() : n(0) {}
LazySeg(int n_, Info v_ = Info()) {
   init(n_, v_);
}
                                                                                                                  res = findFirst(2 * p + 1, m, r, x, y, pred);
     template <class T>
LazySeg(vector<T> init_) {
                                                                                                       template < class F> // 若要找 last, 先右子樹遞迴即可int findFirst(int l, int r, F & & pred) {
            init(init_);
                                                                                                            return findFirst(1, 0, n, l, r, pred);
      void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
}
                                                                                                 // ---define structure and info plus---
                                                                                                 struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add; void apply(const Tag& v) {
      template <class T>
     void init (vector<T> init_) {
    n = init_.size();
}
                                                                                                             if (v.set_val) {
    set_val = v.set_val;
    add = v.add;
            info.assign(4 << __lg(n), Info());
tag.assign(4 << __lg(n), Tag());
function <void(</pre>
                 int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
   info[p] = init_[l];
                                                                                                             else {
                                                                                                                   add += v.add;
                      return;
                                                                                                      }
                                                                                                 };
                 int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                                                                                                 struct Info {
                                                                                                       int sum;
void apply(int l, int r, const Tag &v) {
                 pull(p):
                                                                                                             if (v.set_val) {
    sum = (r - l) * v.set_val;
            build(1, 0, n);
                                                                                                             sum += (r - l) * v.add;
      void pull
            (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
                                                                                                       // Info& operator=(const Info &rhs) {
      void apply(inf p, inf l, inf r, const Tag &v) {
  info[p].apply(l, r, v);
```

// 部分 assignment 使用 return *this;

sort(sorted.begin(), sorted.end());

```
sorted.erase
                                                                                                           Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
}
3.6 Treap [d41d8c]
                                                                                                    }
struct Treap {
      Treap *lc, *rc;
int pri, siz; bool rev_valid;
int val; int min;
                     *гс;
                                                                                                     4 Flow
                                                                                                     4.1 Dinic [287fe8]
      Treap(int val_) {
    min = val = val_;
    pri = rand();
                                                                                                     template < class T >
                                                                                                     struct Dinic {
            lc = rc = nullptr:
                                                                                                          struct Edge {
            siz = 1; rev_valid = 0;
                                                                                                                 int to;
                                                                                                                 T flow, cap; // 流量跟容量
      void pull() { // update siz or other information
            siz = 1;
min = val;
                                                                                                           int n, m, s, t;
T INF_FlOW = numeric_limits<T>::max() / 2;
            for (auto c : {lc, rc}) {
    if (!c) continue;
                                                                                                           vector<vector<int>> adj; // 此點對應的 edges 編號
                                                                                                           vector<Edge> edges; // 幫每個 edge 編號
                  siz += c->siz;
min = std::min(min, c->min);
                                                                                                           vector < Edge > edges; // 吊時間 edg
vector < int > dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
    n = n_; m = 0;
    dis.resize(n); ptr.resize(n);
      void push() {
   if (rev_valid) {
                  swap(lc, rc);
if (lc) lc->rev_valid ^= 1;
if (rc) rc->rev_valid ^= 1;
                                                                                                                 adj.assign(n, vector<int>{});
                                                                                                                 edges.clear();
                                                                                                            void add_edge(int u, int v, T cap) {
            rev_valid = false;
                                                                                                                 // 偶數 id 是正向邊
                                                                                                                 edges.push_back({ v, 0, cap });
edges.push_back({ u, 0, 0 });
adj[u].push_back(m++);
      int find(int k) { // 找到 min 是 k 的位置 (1-based)
            push();
             int ls = (lc ? lc->siz : 0) + 1;
                                                                                                                 adj[v].push_back(m++);
            if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
                                                                                                           bool bfs() {
                                                                                                                 fill(dis.begin(), dis.end(), -1);
dis[s] = 0; queue<int> q;
            else return rc->find(k) + ls;
     }
                                                                                                                 q.push(s);
int size(Treap *t) {
    return t ? t->siz : 0;
                                                                                                                  while (!q.empty() && dis[t] == -1) {
                                                                                                                       int u = q.front(); q.pop();
for (int id : adj[u]) {
    Edge &e = edges[id];
Treap *merge(Treap *a, Treap *b) {
      if (!a || !b) return a ? a : b;
a->push(); b->push();
if (a->pri > b->pri) {
                                                                                                                             if (e.flow == e.cap) continue;
if (dis[e.to] == -1) {
    dis[e.to] = dis[u] + 1;
                                                                                                                                    q.push(e.to);
            a->rc = merge(a->rc, b);
            a->pull();
            return a;
                                                                                                                       }
      else {
    b->lc = merge(a, b->lc);
                                                                                                                  return dis[t] != -1;
            b->pull();
                                                                                                            T dfs(int u, T flow) {
                                                                                                                 if (flow == 0) return 0;
if (u == t) return flow;
      }
                                                                                                                 for (int
                                                                                                                       &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {
Edge &e = edges[adj[u][cur]];
if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;
T mn = dfs(e.to, min(flow, e.cap - e.flow));
if (max = 20) [</pre>
pair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
      t->push();
if (size(t->lc) < k)
                                                                                                                        if (mn > 0) {
            auto [a, b] = split(t->rc, k - size(t->lc) - 1);
            t->rc = a;
                                                                                                                             e.flow += mn;
            t->pull();
                                                                                                                              edges[adj[u][cur] ^ 1].flow -= mn;
                                                                                                                             return mn;
            return {t, b};
                                                                                                                       }
      else {
            auto [a, b] = split(t->lc, k);
                                                                                                                 return 0; // 到不了終點就會 return 0
            t->lc = b;
t->pull();
                                                                                                           T work(int s_, int t_) {
    s = s_; t = t_; T flow = 0;
    while (bfs()) {
            return {a, t};
                                                                                                                       fill(ptr.begin(), ptr.end(), 0);
void Print(Treap *t) {
                                                                                                                       while (true) {
   T res = dfs(s, INF_Flow);
   if (res == 0) break;
   flow += res;
      if (!t) return;
      t->push();
      Print(t->lc);
cout << t->val;
                                                                                                                       }
      Print(t->rc);
}
                                                                                                                 return flow:
3.7 Mo [d41d8c]
                                                                                                                 for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
struct query {
   int l, r, id;
} typedef query;
void MO(int n, vector<query> &queries) {
   int block = sqrt(n);
   firstice = sheal(query = query)> cmp = [
                                                                                                     };
                                                                                                     4.2 Min Cut [44ae6c]
                                                                                                   // CSES Police Chase
int main(){
  int n, m; cin >> n >> m;
  Dinic<int> g(n);
  for (int i = 0; i < m; i++) {
    int u, v, cap = 1;
    cin >> u >> v;
}
      function <bool(query, query)> cmp = [&](query a, query b) {
   int block_a = a.l / block;
   int block_b = b.l / block;
            if (block_a != block_b) return block_a < block_b;
return a.r < b.r;</pre>
      sort(queries.begin(), queries.end(), cmp);
                                                                                                                 u--: v--:
void compress(vector<int> &nums) {
                                                                                                                 q.add edge(u, v, cap);
      vector<int> sorted = nums;
                                                                                                                 g.add_edge(v, u, cap);
```

```
int res = g.work(0, n - 1);
cout << res << "\n";
if (res == 0) return;

vector <int> vis(n);
auto find = [&](auto self, int u) -> void {
    if (!vis[u]) {
        vis[u] = 1;
        for (int id : g.adj[u]) {
            auto e = g.edges[id];
            if (e.cap - e.flow > 0) {
                self(self, e.to);
            }
        }
     }
};
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
        auto e = g.edges[id];
        if (!vis[e.to]) {
            cout << i + 1 << " " << e.to + 1 << " \n";
        }
     }
}
</pre>
```

4.3 Hangarian [350fc3]

```
struct Hangarian { // 0-based
      int n, m; // 最小路徑覆蓋,二分匹配
vector<vector<int>>> adj;
      vector <int>> adj;
vector <int>> used, vis;
vector <pair <int, int>> match;
Hangarian(int n_ = 0, int m_ = 0) {
   init(n_, m_);
      void init(int n_ = 0, int m_ = 0) {
    n = n_; m = m_;
    adj.assign(n + m, vector<int>());
    used.assign(n + m, -1);
    vis.assign(n + m, 0);
      void addEdge(int u, int v) {
   adj[u].push_back(n + v);
   adj[n + v].push_back(u);
      vector<pair<int, int>> work() {
    match.clear();
             vis[v] = 1;
                                 if (used[v] == -1 || self(self, used[v])) {
                                        used[v] = u;
                                        return true:
                          }
                    return false;
             for (int i = 0; i < n; i++) {
    fill(vis.begin(), vis.end(), 0);</pre>
                    dfs(dfs, i);
             for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
                           match.emplace_back(used[i], i - n);
             return match;
}:
```

4.4 MCMF [f667f8]

```
template < class Tf, class Tc>
struct MCMF {

    // 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就好
    int n, m, s, t;

    If INF_FLOW = numeric_limits < Tf>::max() / 2;

    Tc INF_COST = numeric_limits < Tc>::max() / 2;

    struct Edge {
        int to;

        If flow, cap; // 流量跟容量
        Tc cost;

    };

    vector < vector < int >> adj;

    vector < Edge > edges; // 幫每個 edge 編號
    vector < Tc > dis, pot; // johnson algorithm, using spfa

    vector < int > rt; // 路徑恢復, 對應 id
    vector < bool > inq;

    MCMF(int n_ = 0) {
        n = n_;
        m = 0;
        edges.clear();
```

```
adj.assign(n, vector<int>{});
void add_edge(int u, int v, Tf cap, Tc cost){
   edges.push_back({v, 0, cap, cost});
   edges.push_back({u, 0, 0, -cost});
       adj[u].push_back(m++);
       adj[v].push_back(m++);
bool spfa() {
       dis.assign(n, INF_COST);
rt.assign(n, -1); inq.assign(n, false);
       question q,
q.push(s), dis[s] = 0, inq[s] = true;
while (!q.empty()) {
   int u = q.front(); q.pop();
              q.push(v); inq[v] = true;
                      }
              }
       return dis[t] != INF_COST;
bool dijkstra() {
    dis.assign(n, INF_COST); rt.assign(n, -1);
    priority_queue<pair<Tc, int>,
        vector<pair<Tc, int>>> pq;
    dis[s] = 0; pq.emplace(dis[s], s);
    while (!pq.empty()) {
        vector(); respectively.
              auto [d, u] = pq.top(); pq.pop();
if (dis[u] < d) continue;
for (int id : adj[u]) {
    auto [v, flow, cap, cost] = edges[id];
    Tc ndis = dis[u] + cost + pot[u] - pot[v];
    if (flow < cap && dis[v] > ndis) {
        dis[v] = ndis; rt[v] = id;
        cap = captace(edis[v]);
}
                              pq.emplace(ndis, v);
       return dis[t] != INF_COST;
// 限定 flow,最小化 cost
pair<Tf, Tc> work_flow(int s_,
                                                         int t_, Tf need) {
       s = s_, t = t_; pot.assign(n, 0);
If flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] + potfil cost[]</pre>
                      dis[i] += pot[i] - pot[s];
               Tf f = INF_FLOW;
               for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                               (f, edges[rt[i]].cap - edges[rt[i]].flow);
               f = min<Tf>(f, need);
               for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
               flow += f; need -= f;
cost += f * dis[t]; fr = false;
               swap(dis, pot);
if (need == 0) break;
       return make_pair(flow, cost);
// 限定 cost,最大化 flow
pair<Tf, Tc> work_budget(int s_, int t_, Tc budget) {
       s = s_, t = t_; pot.assign(n, 0);
If flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] += pot[i] - pot[s];
}</pre>
               ff f = INF_FLOW;
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
                               (f, edges[rt[i]].cap - edges[rt[i]].flow);
               f = min<Tf>(f, budget / dis[t]);
               for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
   edges[rt[i]].flow += f;
   edges[rt[i] ^ 1].flow -= f;
               flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
               swap(dis, pot);
if (budget == 0 || f == 0) break;
       return make_pair(flow, cost);
void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
```

5

String 5.1 Hash [83f793]

```
constexpr i64 b = 233;
vector < Z > Hash(string s) {
       vector < Z > ans {0};
for (auto c : s) {
              ans.push_back(ans.back() * b + (c - 'a' + 1));
}
int main() { // KMP 詢問
       string s, sub;
cin >> s >> sub;
       auto a = Hash(s);
auto q = Hash(sub);
auto find = q.back();
       int ans = 0;
int l = 1, r = sub.size(), length = sub.size();
while (r <= s.size()) {
    if (a[r] - a[l - 1] * power(Z(b), length) == find)</pre>
                     ans++;
              l++, r++;
        cout << ans << "\n";
}
```

5.2 KMP [cddfd9]

```
struct KMP {
        string sub;
        vector<int> failure;
        KMP(string sub_) {
               sub = sub_;
failure.resize(sub.size(), -1);
               buildFailFunction():

}
void buildFailFunction() {
    for (int i = 1; i < (int)sub.size(); i++) {
        int now = failure[i - 1];
}
</pre>
                      while (now != -1
                      && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
               }
        vector < int > match(string &s) {
               for (int i = 0, now = -1; i < (int)s.size(); i++) {
    // now is the compare sucessed length -1
    while (s[i] !=</pre>
                              sub[now + 1] && now != -1) now = failure[now];
                      sub[now + 1] aa now := -1) now = ratture[now];
// failure stores if comparison fail, move to where
if (s[i] == sub[now + 1]) now++;
if (now + 1 == (int)sub.size()) {
   match.push_back(i - now);
                             now = failure[now];
                      }
               return match;
       }
};
```

Z Function [8dd6ac]

```
// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
// 的最長公共前綴 (LCP) 的長度
vector<int> Z(string s) {
    int n = s.size();
      vector<int> z(n);
      Vector value
z[0] = n;
for (int i = 1, j = 1; i < n; i++) {
    z[i] = max(0, min(j + z[j] - i, z[i - j]));
    while (i + z[i] < n && s[z[i]] == s[i + z[i]]) {</pre>
              if (i + z[i] > j + z[j]) {
    j = i;
       return z; // 最後一格不算
}
```

5.4 SA [d40e3e]

```
struct SuffixArray {
   int n; string s;
vector<int> sa, rk, lc;
    // n: 字串長度
    // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
    // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
    // lc: LCP
         數組,lc[i] 表示 sa[i] 和 sa[i+1] 的最長公共前綴長度
    SuffixArray(const string &s_) {
   s = s_; n = s.length();
   sa.resize(n);
        lc.resize(n - 1);
```

```
rk.resize(n):
         iota(sa.begin(), sa.end(), 0);
         sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });
rk[sa[0]] = 0;</pre>
         for (int i = 1; i < n; ++i)</pre>
             rk[sa[i]]
                    = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
         vector<int> tmp, cnt(n);
         tmp.reserve(n);
while (rk[sa[n - 1]] < n - 1) {</pre>
              tmp.clear();
for (int i = 0; i < k; ++i)
    tmp.push_back(n - k + i);</pre>
              for (auto i : sa)
if (i >= k)
                       tmp.push_back(i - k);
              fill(cnt.begin(), cnt.end(), 0);

for (int i = 0; i < n; ++i)
              sa[--cnt[rk[tmp[i]]]] = tmp[i];
              swap(rk, tmp);
             for (int i = 0, j = 0; i < n; ++i) {
   if (rk[i] == 0) {</pre>
                  j = 0;
              } else {
                  for (j
                         -= j > 0; i + j < n && sa[rk[i] - 1] + j
                        < n && s[i + j] == s[sa[rk[i] - 1] + j];)
                  lc[rk[i] - 1] = j;
              }
         }
     k = sa[rk[i] - 1];
              if (cp) cp--;
while (s[i + cp] == s[k + cp]) cp++;
              if (cp > lcp){
    lcp = cp;
                  p = i;
              }
         if (lcp) {
              return s.substr(p, lcp);
         } else {
              return "-1":
    }
}:
```

5.5 Duval Algorithm [f9dcca]

```
// duval_algorithm
 // 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
 vector<string> duval(string s) {
   int i = 0, n = s.size();
        vector<string> res;
       while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
}</pre>
                    else k++;
              while (i <= k) {
                    res.push_back(s.substr(i, j - k));
i += j - k;
       return res;
 }
 // 最小旋轉字串
 string min_round(string s) {
       int i = 0, n = s.size();
int start = i;
       while (i < n / 2) {
    start = i;</pre>
             start = 1;
int k = i, j = i + 1;
while (s[k] <= s[j] && j < n) {
   if (s[k] < s[j]) k = i;
   else k++;</pre>
              while (i <= k) {</pre>
                    i += j - k;
```

cout << dp[0] << endl;

```
6
                                                                                                        Math
      return s.substr(start, n / 2);
                                                                                                6.1 Prime [ee1622]
}
5.6 Manacher [9c9ca6]
                                                                                                   (a^{(m-1)} = 1 \pmod{m})
                                                                                                // a^(m-1) = 1 (Mod M)
// a^(m-2) = 1/a (Mod M)
// EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)
// Filter + DP; DP save min factor 'recur' factor decomposition
// FacNums = (x+1)(y+1)(z+1)...
// 找到對於每個位置的迴文半徑
vector<int> manacher(string s) {
      string t = "#";
      for (auto c : s) {
    t += c;
    t += '#';
                                                                                                // FacSum = (a^0+a^1...+a^x)(b^0+...+b^y)
// FacMul = N(x+1)(y+1)(z+1)/2
                                                                                                 vector<int> is_prime;
      int n = t.size();
                                                                                                 // 1 代表是質數,非 1 不是
void init(int n) {
      vector<int> r(n);
      for (int i = 0, j =
                                                                                                      is_prime.assign(n + 1, 1);
for (int i = 2; i <= (int)sqrt(n) + 1; i++) {</pre>
            0; i < n; i++) { // i 是中心, j 是最長回文字串中心 if (2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
                                                                                                            if (is_prime[i] == 1) {
   for (int j = i + i; j <= n; j += i) {
      is_prime[j] = i;
   }</pre>
            while (i - r[i] >=
     0 && i + r[i] < n && t[i - r[i]] == t[i + r[i]]) {
    r[i] += 1;</pre>
                                                                                                            }
                                                                                                      }
            if (i + r[i] > j + r[j]) {
    j = i;
                                                                                                 int main() {
    init(1000000);
                                                                                                       ll ans = 1;
                                                                                                       ll q; cin >> q;
      return r;
                                                                                                      map < ll, ll > mp;
while (is_prime[q] != 1) {
    mp[is_prime[q]]++;
    q /= is_prime[q];
}
      // # a # b # a #

// 1 2 1 4 1 2 1

// # a # b # b # a #

// 1 2 1 2 5 2 1 2 1
      // 值 -1 代表原回文字串長度
                                                                                                       if (q != 1) mp[q]++;
      // (id - val + 1) / 2 可得原字串回文開頭
                                                                                                      for (auto [a, b] : mp) {
    ans *= b + 1;
}
5.7 Trie [3b3aa0]
                                                                                                       cout << ans << "\n";
                                                                                                }
struct Trie {
      struct trie_node {
   bool is_word;
                                                                                                6.2 Modulo [29fd05]
            vector<free role *> children;
trie_node() {
   is_word = false;
                                                                                                 template < class T>
                                                                                                 constexpr T power(T a, ll b) {
                                                                                                      T res = 1;
                 children.resize(26, NULL);
                                                                                                       for (; b; b /= 2, a *= a) {
    if (b % 2) {
        res *= a;
}
      trie_node *root = new trie_node();
                                                                                                            }
      void insert(string &s) {
           trie_node *cur = root;
for (int i = 0; i < s.size(); i++) {
   int idx = s[i] - 'a';
                                                                                                       return res;
                 int idx = s[i] - 'a';
if (cur->children[idx] == NULL) {
    cur->children[idx] = new trie_node();
                                                                                                 constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
                                                                                                       res %= p;
if (res < 0) {
    res += p;
                 cur = cur->children[idx];
            cur->is_word = true;
                                                                                                       return res:
      bool is_in_trie(string &s) {
    trie_node *cur = root;
    for (int i = 0; i < s.size(); i++) {</pre>
                                                                                                 template < ll P >
                                                                                                 struct MLong {
                                                                                                       ll x:
                 if (cur->
                                                                                                       constexpr MLong() : x{} {}
                                                                                                      children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
            return true:
      }
int search_i_start(string &s, int i, vector<int> &dp) {
                                                                                                                  return P;
                                                                                                            } else {
            trie_node *cur = root;
int sz = s.size(), ans = 0;
for (int j = i; j < sz; j++) {</pre>
                                                                                                                  return Mod;
                 if (cur
                                                                                                       constexpr static void setMod(ll Mod_) {
                  ->children[s[j] - 'a'] == nullptr) return ans;
cur = cur->children[s[j] - 'a'];
                                                                                                            Mod = Mod_;
                  if (cur->is_word)
                                                                                                       constexpr ll norm(ll x) const {
                       (ans += dp[j'+1]) %= mod;
                                                                                                            if (x < 0) {
                                                                                                                 x += getMod();
            return ans;
     }
                                                                                                            if (x >= getMod()) {
};
int main() {
                                                                                                                  x -= getMod();
      // 找到 sub 集合裡,可以重複用,組成 s 的組數
                                                                                                            return x:
      Trie trie;
      string s; cin >> s;
int sz = s.size();
                                                                                                       constexpr ll val() const {
                                                                                                            return x;
      // dp 代表 i 開頭到最後的配對總數
      // 找到有結尾為 stop 的 dp[i] += dp[j + 1]
int n; cin >> n;
vector <int> dp(sz + 1, 0);
                                                                                                       explicit constexpr operator ll() const {
                                                                                                            return x;
      for (int i = 0; i < n; i++) {
    string sub; cin >> sub;
    trie.insert(sub);
                                                                                                       constexpr MLong operator -() const {
                                                                                                            MLong res;
res.x = norm(getMod() - x);
                                                                                                            return res;
      dp[sz] = 1;
for (int i = sz - 1; i >= 0; i--) {
    dp[i] = trie.search_i_start(s, i, dp);
                                                                                                      constexpr MLong inv() const {
   assert(x != 0);
```

return power(*this, getMod() - 2);

constexpr MLong &operator*=(MLong rhs) & {
 x = mul(x, rhs.x, getMod());

```
return *this:
     constexpr MLong &operator+=(MLong rhs) & {
          x = norm(x + rhs.x);
return *this;
     constexpr MLong &operator -= (MLong rhs) & {
    x = norm(x - rhs.x);
          return *this;
     constexpr MLong &operator/=(MLong rhs) & {
    return *this *= rhs.inv();
     friend constexpr MLong operator*(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res *= rhs;
          return res;
     friend constexpr MLong operator+(MLong lhs, MLong rhs) {
   MLong res = lhs;
          res += rhs:
     friend constexpr MLong operator - (MLong lhs, MLong rhs) {
    MLong res = lhs;
          res -= rhs;
          return res;
     friend constexpr MLong operator/(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res /= rhs;
          return res;
           constexpr istream &operator>>(istream &is. MLong &a) {
          ll v;
is >> v;
a = MLong(v);
          return is;
     friend constexpr
            ostream &operator << (ostream &os, const MLong &a) {
          return os << a.val();</pre>
     friend constexpr bool operator == (MLong lhs, MLong rhs) {
          return lhs.val() == rhs.val();
     friend constexpr bool operator!=(MLong lhs, MLong rhs) {
          return lhs.val() != rhs.val();
    }
template<>
ll MLong<0LL>::Mod = ll(1E9) + 7;
constexpr ll P = 998244353;
using Z = MLong < P >;
```

6.3 Combination [878efe]

6.4 CRT [d41d8c]

```
ll exgcd(ll a, ll b, ll &x, ll &y) {
     if (!b) {
    x = 1, y = 0;
           return a:
     ll g = exgcd(b, a % b, y, x);
y -= a / b * x;
ĺl inv(ll x, ll m){
     ll`a, b;
     exgcd(x, m, a, b);
     a %= m;
if (a < 0) a += m;
     return a;
// remain, mod
Il CRT(vector<pair<ll, ll>> &a){
     ll prod = 1;
for (auto x : a) {
          prod *= x.second;
     ĺl res = 0:
     for (auto x : a) {
   auto t = prod / x.second;
   res += x.first * t % prod * inv(t, x.second) % prod;
   if(res >= prod) res -= prod;
     return res;
```

6.5 Matrix [08b5fe]

```
template < class T >
 struct Mat {
      int m, n;
      constexpr static ll mod = 1e9 + 7;
      constexpr statt tt mod = 1e9 + 7;
vector < vector < T >> matrix;
Mat(int n_ = 0) { init(n_, n_); }
Mat(int m_, int n_) { init(m_, n_); }
Mat(vector < vector < T >> matrix_) { init(matrix_); }
      void init(int m_, int n_) {
    m = m_; n = n_;
    matrix.assign(m, vector<T>(n));
      void init(vector<vector<T>> &matrix_) {
            m = matrix_.size();
n = matrix_[0].size();
            matrix = matrix_;
      return res;
      constexpr Mat & operator*=(const Mat& rhs) & {
   assert(matrix[0].size() == rhs.matrix.size());
            int m = matrix.size()
    , k = matrix[0].size(), n = rhs.matrix[0].size();
Mat ans(m, n);
            }
                 }
            matrix = ans.matrix;
            return *this;
      constexpr Mat &operator^=(ll p) & {
   assert(m == n); assert(p >= 0);
   Mat ans(p-- == 0 ? unit(m) : matrix);
            while (p > 0) {
   if (p & 1) ans *= *this;
   *this *= *this;
                  p >>= 1;
            matrix = ans.matrix;
            return *this;
       friend Mat operator*(Mat lhs, const Mat &rhs) {
            return lhs:
      friend Mat operator^(Mat lhs, const ll p) {
            lhs ^= p;
return lhs;
| // 初始矩陣
| // f4 f3 f2
| // f3 f2 f1
| // f2 f1 f0
                    轉移式
                    1 1 0  f5 f4 f3
1 0 1 => f4 f3 f2
1 0 0  f3 f2 f1
```

6.6 Integer Partition [595ed2]

6.7 Mobius Theorem

- 數論分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n}\!\!\mu(d)\!=\!\begin{cases} 1 & \text{for } n\!=\!1\\ 0 & \text{for } n\!\neq\!0 \end{cases}$$

- 2. μ 是常數函數1的反元素
- $\Rightarrow \mu * 1 = \epsilon$, $\epsilon(n)$ 只在n = 1時為 1 , 其餘情況皆為 0 。
- $-\phi$ 歐拉函數: x以下與x互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^{i}) \\ &= 1 + p^{0}(p-1) + p^{1}(p-1) + \dots + p^{c-1}(p-1) \\ &= p^{c} \\ &= id \end{split}$$

• 莫比烏斯反演公式

-
$$f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$$

- $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

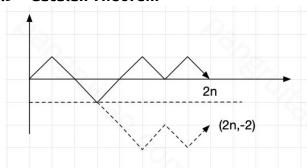
例子

$$\begin{split} &\sum_{i=aj=c}^{b} \sum_{j=1}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.8 Mobius Inverse [d41d8c]

```
| const int maxn = 2e5;
| ll mobius_pref[maxn];
| void init() {
| mobius_pref[1] = 1;
| vector < ll> wei | 0 代表是質數, -1 代表可被平方數整除
| for (ll i = 2; i < maxn; i++) {
| if (wei[i] == -1) {
| mobius_pref[i] = mobius_pref[i - 1];
| continue; // 包含平方
| }
```

6.9 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有x個,往下有y個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.10 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- X/G:本質不同的方案的集合
- X^g : 對於某一種操作 g,所有方案中,經過 g 這種翻轉後保持不變的方案 的集合
- 集合取絕對值代表集合數

7 Search and Gready

7.1 Binary Search [d41d8c]

```
int main() {
    int l = 1, r = 10;
    // 1 to tar, find tar
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}</pre>
```

7.2 Ternary Search [d41d8c]

```
l = ml + 1;
}
else r = mr - 1;
}
```

8 Tree

8.1 LCA [9f95b1]

```
vector < vector < int >> par (maxn, vector < int > (18));
vector < int > depth (maxn) + 1);
vector < int > dfn (maxn);
void build_lca(int n, vector < vector < pair < int, int >>> & tree) {
    auto dfs = [&](auto self, int u, int pre) -> void {
        for (auto [v, w] : tree[u]) {
            if (v == pre) continue;
                par[v][0] = u; // 2 ^ 0
                 depth[v] = depth[u] + 1;
                      self(self, v, u);
        }
    };
    dfs(dfs, 1, 0);
    for (int i = 1; i <= 18; i++) {
            for (int j = 1; j <= n; j++) {
                     par[j][i] = par[par[j][i - 1]][i - 1];
        }
    }
}
int lca(int a, int b) {
    if (depth[a] < depth[b]) swap(a, b);
    int pull = depth[a] - depth[b];
    for (int i = 0; i < 18; i++) {
            if (pull & (1 << i)) {
                      a = par[a][i];
                 }
            if (a == b) return a;
            for (int i = 17; i >= 0; i--) {
                     if (par[a][i] != par[b][i]) {
                      a = par[a][i], b = par[b][i];
                 }
            return par[a][0];
}
```

8.2 Centroid Decomposition [30b436]

```
struct centroid_decomposition {
     int n;
     vector < vector < int >> adj;
     vector <bool> vis;
vector <int> siz;
     centroid_decomposition() {}
centroid_decomposition(int n_) { init(n_); }
      void init(int n_) {
           adj.assign(n, {});
vis.assign(n, false);
            siz.assign(n, 1);
     void addEdge(int u, int v) {
    adj[u].push_back(v);
            adj[v].push_back(u);
      void get_siz(int dep, int x, int p = -1) {
           siz[x] += siz[y];
     int get_cen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz) {
                       return get_cen(y, sz, x);
            return x;
      void work(int x = 0) {
           get_siz(0, x);
int cen = get_cen(x, siz[x]);
vis[cen] = true;
            // do something
for (int y : adj[cen]) {
   if (vis[y]) continue;
                 work(y);
           }
     }
```

8.3 Tree Flattening [51199c]

```
cin >> node_value[i];
vector<vector<int>> tree(n + 1);
for (int i = 1; i < n; i++) {
   int u, v; cin >> u >> v;
   tree[u].push_back(v);
     tree[v].push_back(u);
vector<pair<int, int>> tree_mapping(n + 1);
int cnt = 0;
auto dfs = [&](auto self, int u, int par) -> void {
    euler_ordered_value[++cnt] = node_value[u];
    tree_mapping[u].first = cnt;
     for (auto v : tree[u]) {
   if (v == par) continue;
          self(self, v, u);
     tree_mapping[u].second = cnt;
dfs(dfs,
for (int i = 1; i <= n; i++) {
bit.modify(tree_mapping[i].first, node_value[i]);
     if (tree_mapping[i].first < n) { // root 就不用扣了</pre>
          bit.modify
                (tree_mapping[i].second + 1, -node_value[i]);
for (int i = 0; i < q; i++) {
  int op; cin >> op;
  if (op == 1) {
          int s, x; cin >> s >> x;
int add = x
                euler ordered value[tree mapping[s].first];
           euler_ordered_value[tree_mapping[s].first] = x;
          bit.modify(tree_mapping[s].first, add);
          if (tree_mapping[s].first < n) { // root 就不用扣了</pre>
               bit.modify(tree_mapping[s].second + 1, -add);
     else {
   int node; cin >> node;
          cout <<
                 bit.query(tree_mapping[node].first) << "\n";</pre>
     }
}
```

8.4 Heavy Light Decomposition [ad25b6]

```
int n, cur;
vector<int> siz, top, dep, parent, in, out, seq;
vector < vector < int >> adj;
HLD(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
    n = n_; cur = 0;
      siz.resize(n); top.resize(n); dep.resize(n);
     parent.resize(n); in.resize(n); out.resize(n);
seq.resize(n); adj.assign(n, {});
void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
void work(int root = 0) {
    top[root] = root;
    dep[root] = 0;
      parent[root] =
      dfs1(root); dfs2(root);
void dfs1(int u) {
   if (parent[u] != -1)
      adj[u].erase(find
                  (adj[u].begin(), adj[u].end(), parent[u]));
      siz[u] = 1;
      for (auto &v : adj[u]) {
    parent[v] = u, dep[v] = dep[u] + 1;
            dfs1(v);
siz[u] += siz[v];
if (siz[v] > siz[adj[u][0]]) {
                 swap(v, adj[u][0]);
           } // 讓 adj[u][0] 是重子節點
     }
void dfs2(int u) {
     in[u] = cur++;
     seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
   top[v] = v == adj[u][0] ? top[u] : v;
   dfs2(v);
     out[u] = cur;
} else {
```

```
v = parent[top[v]];
           return dep[u] < dep[v] ? u : v;</pre>
     int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
     int jump(int u, int k) {
   if (dep[u] < k) return -1;
   int d = dep[u] - k;
   while (dep[top[u]] > d)
               u = parent[top[u]];
           return seq[in[u] - dep[u] + d];
     bool isAncester(int u, int v) {
           // 判斷 u 是否是 v 的祖先
           return in[u] <= in[v] && in[v] < out[u];</pre>
     int rootedParent(int u, int v) {
    // 根據新根節點 u 計算 v 的父節點
          return *it;
     int rootedSize(int u, int v) {
           // 根據新根節點 u 計算子樹 v 的大小
if (u == v) return n;
if (!isAncester(v, u)) return siz[v];
           return n - siz[rootedParent(u, v)];
     int rootedLca(int a, int b, int c) {
    // 根據新的根節點計算三個節點 a \ b 和 c 的最近公共祖先
    return lca(a, b) ^ lca(b, c) ^ lca(c, a);
};
```

8.5 Link Cut Tree [c26f51]

```
#include <bits/stdc++.h>
using namespace std;
using i64 = long long;
constexpr i64 Mod = 51061;
struct Tag {
     i64 add = 0;
i64 mul = 1;
      void apply(const Tag& v) {
           mul = mul * v.mul % Mod;
add = (add * v.mul % Mod + v.add) % Mod;
     }
struct Info {
     i64 val = 1;
i64 sum = 1;
      void apply(int size, const Tag &v) {
   val = (val * v.mul % Mod + v.add) % Mod;
   sum = (sum * v.mul % Mod + v.add * size % Mod) % Mod;
     }
};
struct Node {
     Node *ch[2], *p;
int rev = 0;
int size = 1;
      void make_rev() {
    swap(ch[0], ch[1]);
    rev ^= 1;
     Node() : ch {nullptr, nullptr}, p(nullptr) {}
     Info info = Info();
Tag tag = Tag();
      void apply(const Tag &v) {
            info.apply(size, v);
            tag.apply(v);
     void push_tag() {
   if (rev) {
                  if (ch[0]) ch[0]->make_rev();
if (ch[1]) ch[1]->make_rev();
                  rev = 0:
            if (ch[0]) {
                 ch[0]->apply(tag);
            if (ch[1]) {
                  ch[1]->apply(tag);
            tag = Tag();
      void pull_info() {
            size = (ch[0]
                   ch[0]->size : 0) + (ch[1] ? ch[1]->size : 0) + 1;
```

```
info.sum = ((ch[0] ? ch[0]->info.sum : 0) + (ch[1] ? ch[1]->info.sum : 0) + info.val) % Mod;
    }
};
bool isroot(Node *t) {
    int pos(Node *t) { // 回傳 1 代表是右子節點 return t->p->ch[1] == t;
void rotate(Node *t) {
    Node *q = t->p;
int x = !pos(t);
     q - ch[!x] = t - ch[x];
     if (t->ch[x]) {
         t \rightarrow ch[x] \rightarrow p = q;
     t - p = q - p;
     if (!isroot(q)) {
         q \rightarrow p \rightarrow ch[pos(q)] = t;
     t - ch[x] = q;
    q->p = t;
q->pull_info();
void splay(Node *t) { // 單點修改前必須呼叫
     // 把 t 旋轉到目前 splay 的根while (!isroot(t)) {
         Node *p = \hat{t} - \hat{p};
         p->push_tag();
         t->push_tag();
         rotate(t);
    t->push_tag();
t->pull_info();
void access(Node *t) {
     // 把從根到 t 的所有點都放在一條實鏈裡,使根
     // 到 t 成為一條實路徑,並且在同一棵 splay 裡
     for (Node *i = t, *q = nullptr; i; q = i, i = i->p) {
         splay(i);
i->ch[1] = q;
     splay(t);
}
void makeRoot(Node *t) { // 使 t 點成為其所在樹的根
     access(t);
    swap(t->ch[0], t->ch[1]);
t->rev ^= 1;
}
Node* findRoot(Node *t) { // 找到 t 的 root
    access(t):
     splay(t);
     t->push_tag();
while (t->ch[0]) {
    t = t->ch[0];
         t->push_tag();
     splay(t);
void link(Node *t, Node *p) {
     makeRoot(t);
     if (findRoot(p) != t) {
         makeRoot(p);
         t - p = p;
         p->pull_info();
    }
}
bool cut(Node *x, Node *y) { // 不存在邊,回傳 false
    makeRoot(x);
     access(y);
    if (y->ch[0] != x || x->ch[1]) return false;
y->ch[0]->p = nullptr;
y->ch[0] = nullptr;
     y->pull_info();
     return true;
void split(Node
      *x, Node *y) { // 以 y 做根, 區間修改用, apply 在 y 上
     makeRoot(x);
     access(v);
     splay(y);
}
bool isconnected(Node *x, Node *y) { // 查詢有沒有連通
     makeRoot(x);
     access(y);
return findRoot(x) == findRoot(y);
}
int main() {
  int n; cin >> n;
  vector<Node *> nodes(n);
     int q; cin >> q;
for (int i = 0; i < n; i++) {
    nodes[i] = new Node();</pre>
         nodes[i]->info.val = nodes[i]->info.sum = 1LL;
```

```
for (int i = 0; i < n - 1; i++) {
   int u, v; cin >> u >> v;
             link(nodes[u], nodes[v]);
       for (int i = 0; i < q; i++) {
             char op; cin >> op;
if (op == '+') {
                    int u, v; cin >> u >> v;
                   u - -:
                   split(nodes[u], nodes[v]);
                   Tag tag;
                   cin >> tag.add;
tag.add % Mod;
                   nodes[v]->apply(tag);
             else if (op == '-') {
    int u1, v1; cin >> u1 >> v1;
    int u2, v2; cin >> u2 >> v2;
                   u1--; v1--; u2--; v2--;
cut(nodes[u1], nodes[v1]);
link(nodes[u2], nodes[v2]);
             else if (op == '*') {
   int u, v; cin >> u >> v;
                   split(nodes[u], nodes[v]);
Tag tag;
cin >> tag.mul;
                   tag.mut,
tag.mul % Mod;
nodes[v]->apply(tag);
             else {
    int u, v; cin >> u >> v;
                   split(nodes[u], nodes[v]);
                   cout << nodes[v]->info.sum << "\n";</pre>
             3
      }
      return 0:
}
```

8.6 Virtual Tree [622e69]

```
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
 // 可以建立虚樹達成快速樹 DP
 // 例如這題是有權樹,跟 vertex 1 隔開的最小成本
 int top = -1; vector <int>>stk(maxn); void insert(int u, vector <vector <int>>stk(maxn); void insert(int u, vector <vector <int>> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
    vt[stk[top - 1]] push back(stk[top]) top...
        vt[stk[top - 1]].push_back(stk[top]), top--;
if (stk[top - 1] != l) {
               vt[l].push_back(stk[top]);
stk[top] = l;
        } else vt[l].push_back(stk[top--]);
        stk[++top] = u;
 void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
    vt[u].clear();
 void solve(int n, int q) {
   vector g(n + 1, vector<pair<int, int>>());
        vector g(n + 1, vector<patr<int, int>>());
vector vt(n + 1, vector<int>>()); // dfs 完清除, 否則會退化
vector<ll>> dp(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;
   g[u].push_back({v, w});
   g[v].push_back({u, w});
}
         build_lca(n, g);
        for (int j = 0; j < m; j++) {
    cin >> key[j];
                       iskey[key[j]] = 1;
                key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
}):
                for (int x : key) insert(x, vt);
while (top
                         > 0) vt[stk[top - 1]].push_back(stk[top]), --top;
                auto dfs = [&](auto self, int u) -> void {
    for (auto v : vt[u]) {
        self(self, v);
}
                               if (iskey[v]) {
                                      dp[u] += min_dis[v];
                                      // 砍掉 1 到 v 之間最短的路
                               else {
                                      dp[u] += min(dp[v], min_dis[v]);
```

```
iskey[v] = dp[v] = 0;
                     vt[u].clear();
              }:
              dfs(dfs, key[0]); // key[0] 一定是 root
cout << dp[key[0]] << "\n";
iskey[key[0]] = dp[key[0]] = 0;
}
```

Dominator Tree [baa540] 8.7

```
struct Dominator_tree {

void add_edge(int u, int v) { adj[u].push_back(v); }
int query(int v, int x) {
    if (rt[v] == v) return x ? -1 : v;
    int p = query(rt[v], 1);
    if (p == -1) return x ? rt[v] : mn[v];
    if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
    rt[v] = n.

               rt[v] = p;
return x ? p : mn[v];
        void dfs(int v) {
  vis[v] = id, rev[id] = v;
  rt[id] = mn[id] = sdom[id] = id, id++;
                for (int u : adj[v]) {
    if (vis[u] == -1) dfs(u), pa[vis[u]] = vis[v];
    radj[vis[u]].push_back(vis[v]);
               }
        void build(int s) {
               if (i) bucket[sdom[i]].push_back(i);
for (int u : bucket[i]) {
   int p = query(u, 0);
   dom[u] = sdom[p] == i ? i : p;
                       if (i) rt[i] = pa[i];
               res.assign(n, -1);
for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];
for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];
res.[s] = s.</pre>
                res[s] = s:
                      (<mark>int</mark> i = 0; i < n; i++) dom[i] = res[i];
       }
};
```

DP 9

9.1 LCS [5781cf]

```
int main() {
       int m, n; cin >> m >> n;
       string s1, s2; cin >> s1 >> s2;
int L = 0:
       vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0));
       for (int i = 1; i <= m; i++) {
    for (int j = 1; j <= n; j++) {
        if (s1[i - 1] == s2[j - 1])
            dp[i][j] = dp[i - 1][j - 1] + 1;
}</pre>
                            dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
              }
       int length = dp[m][n]; cout << length << "\n";
string s(length, 'c'); // backtracking
while (m >= 1 && n >= 1) {
   if (s1[m - 1] == s2[n - 1]) {
      s[length - 1] = s1[m - 1];
}
                     m--, n--, length--;
              else {
    if (dp[m - 1][n] > dp[m][n - 1]) m--;
              }
       cout << s << "\n";
9.2 LIS [66d09f]
```

```
int main() {
     int n; cin >> n;
```

}

```
vector <int> v(n);
for (int i = 0; i < n; i++) cin >> v[i];
int dp[n]; vector <int> stk;
                                                                                                             cout << dp[findBit(n) - 1][0] << "\n";
      stk.push_back(v[0]);
dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) {
    if (v[i] > stk.back()) {
        stk.push_back(v[i]);
        dp[i] = .....
                                                                                                       9.5 Projects [0942aa]
                                                                                                       int main() { // 排程有權重問題,輸出價值最多且時間最少
                                                                                                       struct E
                  dp[i] = ++L;
                                                                                                             int from, to, w, id;
            } else {
                                                                                                             bool operator < (const E &rhs) {</pre>
                  auto it
                                                                                                                   return to == rhs.to ? w > rhs.w : to < rhs.to;</pre>
                           = lower_bound(stk.begin(), stk.end(), v[i]);
                   *it = v[i]; dp[i] = it - stk.begin() + 1;
                                                                                                              int n; cin >> n; vector<E> a(n + 1);
                                                                                                             for (int i = 1; i <= n; i++) {
   int u, v, w; cin >> u >> v >> w;
   a[i] = {u, v, w, i};
            }
      vector < int > ans; cout << L << " | n";
for (int i = n - 1; i >= 0; i--) {
    if (dp[i] == L) {
                                                                                                             vector<array<ll, 2 >> dp(n + 1); // w, time
                  ans.push_back(v[i]), L--;
                                                                                                             vector(array(int, 2)> rec(n + 1); // 有沒選,上個是誰
sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
    auto it = --lower_bound(all(a), E({0, a[i].from}),
      reverse(ans.begin(), ans.end());
for (auto i : ans) cout << i << " ";</pre>
                                                                                                                   auto it = --lower_bound(all(a), E({0, a[i].from}),
[](E x, E y){ return x.to < y.to; });
int id = it - a.begin(); dp[i] = dp[i - 1];
ll nw = dp[id][0] + a[i].w;
ll nt = dp[id][1] + a[i].to - a[i].from;
if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
    dp[i] = {nw, nt}; rec[i] = {1, id};
}
9.3 Edit Distance [308023]
int main() {
      string s1, s2; cin >> s1 >> s2;
      int n1 = s1.size(), n2 = s2.size();
      // dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元
                                                                                                             vector < int > ans;
for (int i = n; i != 0;) {
    if (rec[i][0]) {
      vector < int > dp(n2 + 1);
      vector <int> op(n2 + 1);
iota(dp.begin(), dp.end(), 0);
for (int i = 1; i <= n1; i++) {
   vector <int> cur(n2 + 1); cur[0] = i;
   for (int j = 1; j <= n2; j++) {
      if (s1[i - 1] == s2[j - 1]) {
        cur[j] = dp[j - 1];
      } else {</pre>
                                                                                                                         ans.push_back(a[i].id);
i = rec[i][1];
                                                                                                                   } else i--;
                                                                                                             }
                  } else {
                                                                                                       9.6 Removal Game [7bb56b]
                        // s1 新增等價於 s2 砍掉
                         // dp[i][j] = min(s2 新增, 修改, s1 新增);
                                                                                                     | // 兩個人比賽,每個人輪流取一個數字且只能是頭尾
                         cur[j]
                                                                                                       // 問兩人都選得好,第一出手的人可取得的最大分數int main() {
    int n; cin >> n;
                                 = min({cur[j - 1], dp[j - 1], dp[j]}) + 1;
                  }
                                                                                                             vector <ll> a(n);
for (int i = 0; i < n; i++) cin >> a[i];
            swap(dp, cur);
                                                                                                             vector dp(n, vector<ll>(n)); // i 到 j 區間的最大 diff
for (int i = n - 1; i >= 0; i--) {
    dp[i][i] = a[i];
    for (int j = i + 1; j < n; j++)
        dp[i][j] =
      cout << dp[n2] << "\n";
9.4 Bitmask [a626f9]
void hamiltonianPath(){
                                                                                                                                 max(a[i] - dp[i + 1][j], a[j] - dp[i][j - 1]);
      int n, m; cin >> n >> m;
vector adj(n, vector <int >());
for (int i = 0; i < m; i++) {
    int u, v; cin >> u >> v;

                                                                                                             // x + y = sum; // x - y = dp[0][n - 1] cout << (accumulate
                                                                                                                     (a.begin(), a.end(), 0LL) + dp[0][n - 1]) / 2 << "\n";
            adj[--v].push_back(--u);
                                                                                                       9.7 CHT [5f5c25]
      // 以...為終點,走過...
vector dp(n, vector<<mark>int</mark>>(findBit(n)));
      dp[0][1] = 1;
                                                                                                       struct Line {
      for (int mask = 1; mask < findBit(n); mask++) {
   if ((mask & 1) == 0) continue;</pre>
                                                                                                             ll m, b;
Line(ll m = 0, ll b = 0) : m(m), b(b) {}
ll eval(ll x) {
    return m * x + b;
            if ((mask & 1) -- 0) continue;
for (int i = 0; i < n; i++) {
   if ((mask & findBit(i)) == 0) continue;
   if (i == n - 1 && mask != findBit(n) - 1) continue;
   int pre_mask = mask ^ findBit(i);</pre>
                                                                                                       };
                   for (int j : adj[i]) {
   if ((pre_mask & findBit(j)) == 0) continue;
   dp[i][mask
                                                                                                       struct CHT { // 用在查詢單調斜率也單調
                                                                                                             int n, lptr, rptr; vector<line> hull;
CHT(int n_ = 0, Line init_ = Line()) {
   init(n_, init_);
                                 ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
                  }
            }
                                                                                                             void init(int n_ = 0, Line init_ = Line()) {
    n = n_; hull.resize(n); reset(init_);
      cout << dp[n - 1][findBit(n) - 1] << "\n";
                                                                                                             void reset(Line init_ = Line()) {
    lptr = rptr = 0; hull[0] = init_;
void elevatorRides() {
      int n, x; cin >> n >> x; vector<int> a(n);

for (int i = 0; i < n; i++) cin >> a[i];

vector<array<int, 2>> dp(findBit(n));

dp[0][0] = 1; // 次數、已使用人數

for (int mask = 1; mask < findBit(n); mask++) {
                                                                                                             bool pop_front(Line &l1, Line &l2, ll x) {
                                                                                                                   // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y
                                                                                                                    // 代表查詢的當下,右線段的高度已經低於左線段了
            return l1.eval(x) >= l2.eval(x);
                                                                                                             bool pop_back(Line &l1, Line &l2, Line &l3) {
                                                                                                                   // 本題斜率遞減、上凸包
                                                                                                                   // 因此只要 12 跟
                                                                                                                   l3 的 X 交點 <= l1 跟 l3 的 X 交點, l2 就用不到了
return (l3.b - l2.b)
* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
                                                                                                              void insert(Line L) {
                                                                                                                   rptr - -;
```

hull[++rptr] = L; Il query(ll x) {
 while (rptr - lptr

> 0 && pop_front(hull[lptr], hull[lptr + 1], x))

```
return hull[[lptr].eval(x);
};
 9.8 DNC [61c639]
 constexpr int N = 3e3 + 5;
constexpr ll inf = 4e18;
 // dp[k][j] = min(dp[k - 1][i] + cost[i][j])
 // dp[k][] - min(dp[k - 1][i] + Cost[i][]])
// cost: (i, j]
ll dp[N][N]; // 1-based
ll get_cost(int l, int r) {}
void DNC(int k, int l, int r, int optl, int optr) {
    if (l > r) return;
    int m = (l + r) >> 1, opt = -1;
    def[k][] - inf;
       dp[k][m] = inf;
for (int i = max(k, optl); i <= min(m, optr); i++) {</pre>
             // 注意 i 的範圍、 get_cost 與 dp 的邊界
ll cur = dp[k - 1][i] + get_cost(i, m);
if (cur < dp[k][m]) {
                   dp[k][m] = cur, opt = i;
      DNC(k, l, m - 1, optl, opt);
DNC(k, m + 1, r, opt, optr);
for (int i = 2; i <= k; i++) {
    DNC(i, 1, n, 1, n);</pre>
       cout << dp[k][n] << "\n";
 9.9 LiChaoSegmentTree [a6e320]
 constexpr ll Inf = 4e18;
// dp[i] = min(f[j] * s[i] + dp[j])
// y = m x + h
 // y = struct Line {
      ll m, b;
li m, b;
Line(ll m = 0, ll b = Inf) : m(m), b(b) {}
ll eval(ll x) const { return m * x + b; }
 struct LiChaoSeg { // 取 max 再變換就好
       int n;
       vector < Line > info;
       LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
             n = n_{\dot{}};
             info.assign(4 << __lg(n), Line());</pre>
       void update(Line line, int node, int l, int r) {
  int m = (l + r) / 2;
  bool left = line.eval(l) < info[node].eval(l);
  bool mid = line.eval(m) < info[node].eval(m);</pre>
             if (mid) swap(info[node], line); // 如果新線段比較好
if (r - l == 1) return;
else if (left != mid) update(line, 2 * node, l, m);
             // 代表左半有交點
             else update(line, 2 * node + 1, m, r);
// 代表如果有交點一定在右半
       void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
   if (r - l == 1) return info[node].eval(x);
   int m = (l + r) / 2;
             if (x < m) return</pre>
                    min(info[node].eval(x), query(x, 2 * node, l, m));
             else return min(
   info[node].eval(x), query(x, 2 * node + 1, m, r));
       il query(int x) { return query(x, 1, 0, n); }
 9.10 Codeforces Example [7d37ea]
|// CF 1932 pF
 // 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
 // 請問在線段不重複的情況下,最多獲得幾分
 int main() {
       int n, m;
cin >> n >> m;
       // 記錄每點有幾個線段
       // 再一個紀錄,包含這個點的左界
       cnt[l]++;
cnt[r + 1]--;
       for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
```

for (int i = n; i >= 2; i--) {

```
l_side[i - 1] = min(l_side[i - 1], l_side[i]);
     vector<int> dp(n + 1);
     dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
           dp[i] = cnt[i];
if (l_side[i] != inf) {
    dp[i] += dp[l_side[i] - 1];
           dp[i] = max(dp[i], dp[i - 1]);
     cout << dp[n] << "\n";
}
// CF 1935 DC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
// 再加上 max(bi) - min(bi)
int main(){
      int n, k, ans = 0; cin >> n >> k;
     vector<pii> v(n + 1);
for (int i = 1; i <= n; i++) {
           int a, b; cin >> a >> b; v[i] = {a, b};
           if (a <= k) ans = 1;
     sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
     }); // 用 bi 來排,考慮第 i 個時可以先扣 vector <vector <int>> dp(n + 1, vector <int>(n + 1, inf)); // 考慮 v[i] 時,選 j 個的 sum(ai) - min(bi)
     for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
                 // min(不選,選)
if (dp[i
                         1][j - 1] + v[i].first + v[i].second <= k) {
                      // 假如可以選,更新 ans 時再加回去 bi
                      ans = max(ans, j);
           dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
     cout << ans << endl:
```

10 Geometry

10.1 Basic [d41d8c]

```
template < class T>
struct Point {
     Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) {}
     template < class U>
     operator Point<U>() {
         return Point <U > (U(x), U(y));
     Point & operator += (const Point &p) & {
         x += p.x;
         y += p.y;
return *this;
     Point & operator -= (const Point &p) & {
         x -= p.x;
         y -= p.y;
return *this;
     Point & operator *= (const T & v) & {
         y *= v;
          return *this;
     Point & operator /= (const T & v) & {
         x /= v;
y /= v;
return *this;
     Point operator -() const {
    return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
   return a += b;
     friend Point operator - (Point a, const Point &b) {
         return a -= b;
     friend Point operator*(Point a, const T &b) {
   return a *= b;
     friend Point operator/(Point a, const T &b) {
         return a /= b;
     friend Point operator*(const T &a, Point b) {
   return b *= a;
     friend bool operator == (const Point &a, const Point &b) {
         return a.x == b.x && a.y == b.y;
```

```
friend istream &operator>>(istream &is, Point &p) {
          return is >> p.x >> p.y;
     friend ostream &operator<<(ostream &os, const Point &p) {</pre>
          return os << "(" << p.x << ", " << p.y << ")";
};
template < class T>
struct Line {
     Point <T>
     Point<T> b;
Line(const Point<T> &a_
                                  = Point<T>()
           , const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
template < class T>
 dot(const Point<T> &a, const Point<T> &b) {
  return a.x * b.x + a.y * b.y;
template < class T>
T cross(const Point<T> &a, const Point<T> &b) {
  return a.x * b.y - a.y * b.x;
template < class T>
  square(const Point<T> &p) {
     return dot(p, p);
template < class T >
double length(const Point < T > &p) {
     return sqrt(square(p));
template < class T>
double length(const Line<T> &l) {
     return length(l.a - l.b);
template < class T>
Point < T > normalize(const Point < T > & p) {
    return p / length(p);
template < class T>
bool parallel(const Line<T> &l1, const Line<T> &l2) {
   return cross(l1.b - l1.a, l2.b - l2.a) == θ;
template < class T>
double distance(const Point<T> &a, const Point<T> &b) {
     return length(a - b);
template < class T>
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0) {
      return distance(p, l.a);
}</pre>
     if (dot(p - l.b, l.a - l.b) < 0) {
          return distance(p, l.b);
     return distancePL(p, l);
template < class T>
Point<T> rotate(const Point<T> &a) {
    return Point(-a.y, a.x);
}
template < class T>
int sgn(const Point < T > &a) {
     return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
template < class T>
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
     return cross(l.b - l.a, p - l.a) > 0;
template < class T>
Point < T
      > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
     return l1.a + (l1.b - l1.a) * (cross(l2.b - l2.a, l1.a - l2.a) / cross(l2.b - l2.a, l1.a - l1.b));
template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
     return cross(p - l.a, l.b - l.a) == 0 &&
    min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)
          && min
                (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
```

```
template < class T>
bool pointInPolygon
       (const Point<T> &a. const vector<Point<T>> &p) {
      int n = p.size();
for (int i = 0; i < n; i++) {
           if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {
                 return true;
     }
      int t = 0;
      for (int i = 0; i < n; i++) {
   auto u = p[i];
   auto v = p[(i + 1) % n];</pre>
           if (u.x < a.x
                 && v.x >= a.x && pointOnLineLeft(a, Line(v, u))) {
           if (u.x >= a.x
                  && v.x < a.x && pointOnLineLeft(a, Line(u, v))) {
     }
     return t == 1;
}
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
tuple<int, Point<T>, Point<T>> segmentIntersection
    (const Line<T> &l1, const Line<T> &l2) {
      if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x)) {</pre>
           return {0, Point<T>(), Point<T>()};
      if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x)) {
    return {0, Point<T>(), Point<T>()};
      if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y)) {</pre>
           return {0, Point<T>(), Point<T>()};
      if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y)) {
           return {0, Point<T>(), Point<T>()};
      if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
    if (cross(l1.b - l1.a, l2.a - l1.a) != (
        return {0, Point<T>(), Point<T>()};
                                                                 0) {
           } else {
                 auto maxx1 = max(l1.a.x, l1.b.x);
                 auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
auto miny1 = min(l1.a.y, l1.b.y);
                 auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.y, l2.b.y);
                 auto miny2 = min(l2.a.y, l2.b.y);
                 Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
if (!pointOnSegment(p1, l1)) {
                      swap(p1.y, p2.y);
                 if (p1 == p2) {
                      return {3, p1, p2};
                } else {
                      return {2, p1, p2};
          }
     auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
     Point p = lineIntersection(l1, l2);
if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
    return {1, p, p};
           return {3, p, p};
     }
template < class T>
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
      if (get<0>(segmentIntersection(l1, l2)) != 0) {
           return 0.0:
      return min({distancePS(l1.a, l2), distancePS(l1
            .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
template < class T>
bool segmentInPolygon
       (const Line<T> &l, const vector<Point<T>> &p) {
      int n = p.size();
```

```
if (!pointInPolygon(l.a, p)) {
          return false:
     if (!pointInPolygon(l.b, p)) {
          return false;
     for (int i = 0; i < n; i++) {
    auto u = p[i];</pre>
          auto v = p[(i + 1) % n];
auto w = p[(i + 2) % n];
          auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
          if (t == 1) {
    return false;
          if (t == 0) {
                continue;
          if (t == 2) {
                if (pointOnSegment(v, l) && v != l.a && v != l.b) {
   if (cross(v - u, w - v) > 0) {
      return false;
                     }
          } else {
               if (p1 != u && p1 != v) {
   if (pointOnLineLeft(l.a, Line(v, u))
                          || pointOnLineLeft(l.b, Line(v, u))) {
                          return false;
               } else if (p1 == v) {
   if (l.a == v) {
                          if (pointOnLineLeft(u, l)) {
    if (pointOnLineLeft(w, l))
                                     && pointOnLineLeft
                                     (w, Line(u, v))) {
return false;
                               }
                          } else {
                               (w, Line(u, v))) {
return false;
                               }
                     } else if (l.b == v) {
   if (pointOnLineLeft(u, Line(l.b, l.a))) {
      if (pointOnLineLeft(w, Line(l.b, l.a)))
                                     && pointOnLineLeft
                                     (w, Line(u, v))) {
return false;
                          } else {
    if (pointOnLineLeft(w, Line(l.b, l.a))
                                     || pointOnLineLeft
                                     (w, Line(u, v))) {
return false;
                               }
                     } else {
    if (pointOnLineLeft(u, l)) {
                                if (pointOnLineLeft(w, Line(l.b, l.a))
                                     || pointOnLineLeft
                                     (w, Line(u, v))) {
return false;
                          } else {
    if (pointOnLineLeft(w, l)
                                     || pointOnLineLeft
                                     (w, Line(u, v))) {
return false;
                          }
                    }
               }
          }
     return true;
vector<Point<T>> hp(vector<Line<T>> lines) {
     sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
   auto d1 = l1.b - l1.a;
          auto d2 = l2.b - l2.a;
          if (sqn(d1) != sqn(d2)) {
               return sgn(d1) == 1;
          return cross(d1, d2) > 0;
     deque<Line<T>> ls;
     deque<Point<T>> ps;
for (auto l : lines) {
    if (ls.empty()) {
                ls.push_back(l);
          }
          while (!ps.empty() && !pointOnLineLeft(ps.back(), l)) {
```

```
ps.pop_back();
ls.pop_back();
        }
         while (!ps.empty() && !pointOnLineLeft(ps[0], l)) {
             ps.pop_front();
             ls.pop_front();
        if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
             if (dot
                  (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                 if (!pointOnLineLeft(ls.back().a, l)) {
                      assert(ls.size() == 1);
                 continue;
             return {};
        }
         ps.push_back(lineIntersection(ls.back(), l));
         ls.push_back(l);
    while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0])) {
    ps.pop_back();
         ls.pop_back();
    if (ls.size() <= 2) {</pre>
    ps.push_back(lineIntersection(ls[0], ls.back()));
    return vector(ps.begin(), ps.end());
using P = Point<ll>;
```

10.2 Convex Hull [b5758d]

```
int main() {
     int n; cin >> n;
     vector <P> P(n), U, L;
for (int i = 0; i < n; i++) {
         cin >> P[i];
     sort(P.begin(), P
           .end(), [](const Point<i64> &a, const Point<i64> &b) {
          return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
     L.pop_back();
         while (U.size() >= 2 && cross(U.back() -
    U[U.size() - 2], P[i] - U[U.size() - 2]) >= 0LL){
              U.pop_back();
         if (L.
               empty() || !(L.back() == P[i])) L.push_back(P[i]);
         if (U.
               empty() || !(U.back() == P[i])) U.push_back(P[i]);
     if (L.size() <= 2 && U.size() <= 2) {
    // No Hull</pre>
     cout << L.size() + U.size() - 2 << "\n";
     for (int i = 0; i < L.size() - 1; i++) {
   cout << L[i].x << " " << L[i].y << "\n";</pre>
     for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << "\n";</pre>
}
```

10.3 MinEuclideanDistance [469a8f]

```
T distanceSquare(const Point<T> &a, const Point<T> &b) {
     return square(a - b);
void solve() {
    int n; cin >> n;
constexpr i64 inf = 8e18;
     vector<Point<i64>> a(n);
     for (int i = 0; i < n; i++) {</pre>
         i64 x, y;
cin >> x >> y;
         a[i] = Point < i64 > (x, y);
     struct sortY {
         bool operator()
              (const Point<i64> &a, const Point<i64> &b) const {
return a.y < b.y;</pre>
         }
     struct sortXY {
         bool operator()
               (const Point<i64> &a, const Point<i64> &b) const {
```

10.4 LatticePoints [7750d6]

10.5 MinRadiusCoverCircle [a9fa76]