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```

1 Basic

1.1 install vscode [d41d8c]

1.2 default code [3cd57c]

```
#include <bits/stdc++.h>
#define all(x) (x).begin(), (x).end()
#define pii pair<int, int>
using namespace std;
using ll = long long;
const int mod = 1e9 + 7;

void solve() {
}

int main() {
   ios_base::sync_with_stdio(0);
   cin.tie(nullptr);
   int t = 1;
   cin >> t;
   while (t--) {
      solve();
   }
}
```

1.3 compare fuction [4bc3e0]

```
};
struct cmp {
    vector < int > &v;
                  // 要在 template 的資結用外部變數
     cmp(vector<int>& vec) : v(vec) {}
bool operator() (int a, int b) const {
   return v[a] > v[b];
// mutil: cmp cmp1(vector);
// priority_queue<int, vector<int>, cmp> pq(cmp1);
};
1.4 pbds [e28ae8]
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template<typename T>
using pbds_set = tree<T, null_type,</pre>
       less<T>, rb_tree_tag, tree_order_statistics_node_update>;
1.5 浮點數誤差 [a0d4e5]
struct EDouble {
     constexpr static double Eps = 1e-9;
constexpr EDouble() : x{} {}
constexpr EDouble(double v) : x{v} {}
     constexpr double val() const {
         return x:
     explicit constexpr operator double() const {
         return x;
     constexpr EDouble operator-() const {
         return EDouble(-x);
     constexpr EDouble &operator+=(const EDouble &rhs) & {
         x += rhs.x
          return *this:
     constexpr EDouble &operator -=(const EDouble &rhs) & {
         x -= rhs.x;
return *this;
     constexpr EDouble &operator*=(const EDouble &rhs) & {
         x *= rhs.x:
         return *this;
     constexpr EDouble &operator/=(const EDouble &rhs) & {
   assert(fabs(rhs.x) > Eps);
         x /= rhs.x;
          return *this;
           EDouble operator+(EDouble lhs, const EDouble &rhs) {
          lhs += rhs;
     friend constexpr
           EDouble operator - (EDouble lhs, const EDouble &rhs) {
         lhs -= rhs;
         return lhs:
           EDouble operator*(EDouble lhs, const EDouble &rhs) {
          lhs *= rhs;
          return lhs;
     friend constexor
           EDouble operator/(EDouble lhs, const EDouble &rhs) {
         lhs /= rhs;
return lhs;
     friend constexpr bool
           operator < (const EDouble &lhs, const EDouble &rhs) {</pre>
          return lhs.x - rhs.x < -Eps:
     friend constexpr bool
           operator > (const EDouble &lhs, const EDouble &rhs) {
          return lhs.x - rhs.x > Eps;
     friend constexpr bool
    operator==(const EDouble &lhs, const EDouble &rhs) {
          return fabs(lhs.x - rhs.x) < Eps;</pre>
     friend constexpr bool
            operator <= (const EDouble &lhs, const EDouble &rhs) {</pre>
          return lhs < rhs || lhs == rhs;</pre>
     friend constexpr bool
           operator >=(const EDouble &lhs, const EDouble &rhs) {
          return lhs > rhs || lhs == rhs;
            operator!=(const EDouble &lhs, const EDouble &rhs) {
          return !(lhs == rhs);
     friend istream & operator >> (istream &is, EDouble &a) {
```

2 Graph

2.1 DFS 跟 BFS [cdd1d5]

```
int main() {
       vector<vector<int>> adj(n + 1, vector<int>());
       // dfs_graph
vector<bool> vis(n + 1, 0);
auto dfs = [&](auto self, int u) -> void {
    if (vis[u]) return;
    vis[u] = true;
               for (auto v: adj[u]) {
    self(self, v);
              }
       dfs(dfs, 1);
       // bfs
vector < int > depth(n + 1, 1e9);
       queue <int> depth(u + 1, 1e9),
queue <int> q;
auto bfs = [&](auto self, int u) -> void {
    vis[u] = true;
    depth[u] = 0;
               q.push(u);
while (!q.empty()) {
                       int u = q.front(); q.pop();
                      for (auto v : adj[u]) {
    if (vis[v]) continue;
    vis[v] = true;
    depth[v] = depth[u] + 1;
                              q.push(v);
                      }
               }
       bfs(bfs, 1);
}
```

2.2 Prim [f00ec0]

2.3 BellmanFord [430ded]

```
if (i == n) t = v;
}

}
if (t == -1) { cout << "NO\n"; return; }
for (int i = 1; i < n; i++) t = par[t];
vector<int> ans {t};
int i = t;
do {
    i = par[i];
    ans.push_back(i);
} while (i != t);
reverse(ans.begin(), ans.end());
cout << "YES\n";
for (auto x : ans) cout << x + 1 << " ";</pre>
```

2.4 負權最大距離 [2148ca]

```
CSES High Score
void dfs(int u, vector<int> &vis, vector<vector<int>> &adj) {
      if (vis[u]) return;
      vis[u] = 1;
for (int v : adj[u]) {
           dfs(v, vis, adj);
     }
signed main() {
   int n, m; cin >> n >> m;
   vector<array<int, 3>> edges;
      vector<vector<int>> adj(n + 1);
      vector < int > dis(n + 1), vis(n + 1);
while (m--) {
           int u, v, w;
cin >> u >> v >> w;
edges.push_back({u, v, w});
           adj[u].push_back(v);
      }
fill(dis.begin(), dis.end(), -1e18);
      dis[1] = 0;
for (int i = 1; i <= n; i++) {
           for (auto [u, v, w] : edges) {
   if (dis[u] != -1e18 && dis[v] < dis[u] + w) {
      dis[v] = dis[u] + w;
}</pre>
                             i == n) {
dfs(v, vis, adj);
                       if (i
                       }
                 }
           }
      if (vis[n]) cout << -1;</pre>
      else cout << dis[n];</pre>
}
```

2.5 FloydWarshall [206b76]

```
const int inf = 1e18:
int main() {
       int n, m, q; cin >> n >> m;
vector <vector <int>> graph(n + 1, vector <int>(n + 1, inf));
vector <vector <int>> dis(n + 1, vector <int>(n + 1));
for (int i = 0; i < m; i++) {</pre>
             int u, v, w; cin >> u >> v >> w;
cin >> u >> v >> w;
graph[u][v] = min(graph[u][v], w);
              graph[v][u] = min(graph[v][u], w);
       for (int i = 0; i <= n; i++) {
             for(int j = 0; j <= n; j++) {
    dis[i][j] = graph[i][j];</pre>
       for (int i = 0; i <= n; i++) // 自己到自己是 0
             dis[i][i] = 0;
       for (int k = 1; k <= n; k++) {</pre>
             for (int i = 1; i <= n; i++) {
    for (int j = 1; j <= n; j++) {
        dis[i][j</pre>
                                  ] = min(dis[i][j], dis[i][k] + dis[k][j]);
            }
       for (int i = 0; i < q; i++) {</pre>
             int u, v; cin >> u >> v;
cout << (dis[u][v] >= inf ? -1 : dis[u][v]) << "\n";</pre>
}
```

2.6 <u>歐拉環與歐拉路</u> [0911ed]

```
adj[now].erase(nxt);
             dfs(nxt, road);
      road.push_back(now);
void solve() {
      cin >> n >> m;
in.assign(n + 1, 0);
adj.assign(n + 1, set<int>());
for (int i = 1; i <= m; i++) {
   int u, v; cin >> u >> v;
             adj[u].insert(v);
             in[v]++;
     }
in[1]++;
     in[1]++;
in[n]--;
for (int i = 1; i <= n; i++) {
    if(adj[i].size() != in[i]) {
        cout << "IMPOSSIBLE";
        caturn:</pre>
            }
      vector<int> road;
      dfs(1, road);
if (road.size() != m + 1) {
            cout << "IMPOSSIBLE";</pre>
             return:
       for(auto i : road) cout << i <<</pre>
2.7 SCC [5d3e16]
```

```
struct SCC {
     int n, cur, cnt;
vector<vector<int>> adj;
      vector <int> stk, dfn, low, bel;
SCC(int n_ = 0) {
   init(n_);
      void init(int n_) {
           n = n_;
adj.assign(n, {});
            dfn.assign(n, -1);
            low.resize(n);
            bel.assign(n, -1);
            stk.clear();
            cur = cnt = 0;
      void addEdge(int u, int v) {
            adj[u].push_back(v);
      void dfs(int x) {
            dfn[x] = low[x] = cur++;
            stk.push_back(x);
for (auto y : adj[x]) {
    if (dfn[y] == -1) {
                        dfs(y);
                        low[x] = min(low[x], low[y]);
se if (bel[y] == -1) {
low[x] = min(low[x], dfn[y]);
                  }
            if (dfn[x] == low[x]) {
                  int y;
do {
                        y = stk.back();
                  bel[y] = cnt;
stk.pop_back();
while (y != x);
                  cnt++;
           }
      vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
            return bel;
      struct Graph {
            int n;
            vector<pair<int, int>> edges;
            vector<int> siz;
            vector<int> cnte;
      Graph compress() {
           Graph g;
g.n = cnt;
            g.siz.resize(cnt);
            g.cnte.resize(cnt);
            g.the.restze(ctn),
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;
    for (auto j : adj[i]) {
        if (bel[i] != bel[j]) {
    }
}</pre>
                              g.edges.emplace_back(bel[i], bel[j]);
                        } else {
                              g.cnte[bel[i]]++;
                  }
            return g;
```

```
}: }
```

2.8 VBCC [170604]

```
struct VBCC {
       int n, cur;
vector<vector<int>> adj;
       vector<vector<int>> adj;
vector<int> dfn, low, parent;
vector<bool> is_cut;
VBCC(int n_ = 0) {
   init(n_);
       void init(int n_) {
             n = n;
             adj.assign(n, {});
dfn.assign(n, -1);
low.resize(n);
              parent.assign(n, -1);
              is_cut.assign(n, false);
             cur = 0:
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       children++;
                           parent[v] = x;
                           dfs(v);
low[x] = min(low[x], low[v]);
                           if (parent[x] != -1 && low[v] >= dfn[x]) {
    is_cut[x] = true;
                    } else if (v != parent[x]) {
    low[x] = min(low[x], dfn[v]);
             if (parent[x] == -1 && children > 1) {
    is_cut[x] = true;
      }
void work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i);
        }
}</pre>
             }
      }
};
```

2.9 EBCC [49d862]

```
struct EBCC { // CF/contest/1986/pF
      int n, cur, cnt;
vector<vector<int>> adj;
      vector<int> stk, dfn, low, bel;
      vector<pair<int, int>> bridges; // 關鍵邊
      EBCC(int n_) {
            init(n_);
      void init(int n_) {
            n = n_;
adj.assign(n, {});
            dfn.assign(n, -1);
             low.resize(n);
            bel.assign(n, -1);
            stk.clear():
            bridges.clear();
            cur = cnt = 0;
      void addEdge(int u, int v) {
   adj[u].push_back(v);
            adj[v].push_back(u);
      void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
           dfn[x] = low[x] = cui++,
stk.push_back(x);
for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
        dfs(y, x);
        low[x] = min(low[x], low[y]);
        if (low[y] > dfn[x]) {
            bridges.emplace_back(x, y)
                               bridges.emplace_back(x, y);
                  } else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
            if (dfn[x] == low[x]) {
                   int y;
do {
                         y = stk.back();
                         bel[y] = cnt;
                         stk.pop_back();
                   } while (y != x);
```

```
cnt++:
          }
     vector < int > work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {</pre>
                     dfs(i, -1);
           return bel;
      struct Graph {
           int n;
           vector<pair<int, int>> edges;
           vector<int> siz; // BCC 內節點數
           vector<int> cnte; // BCC 內邊數
     Graph compress() {
          Graph g;
g.n = cnt;
           g.siz.resize(cnt);
           g.cnte.resize(cnt);
           for (int i = 0; i < n; i++) {
                g.siz[bel[i]]++;
                for (auto j : adj[i]) {
    if (bel[i] < bel[j]) {</pre>
                     g.edges.emplace_back(bel[i], bel[j]);
} else if (i < j) {</pre>
                          g.cnte[bel[i]]++;
               }
           return g;
     }
};
```

2.10 2-SAT [eeddc1]

```
/ CSES Giant Pizza
struct TwoSat {
     int n;
      vector<vector<int>> e;
     bool satisfiable() {
            vector<int
                  > id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
            vector<int> stk;
int now = 0, cnt = 0;
function<void(int)> tarjan = [&](int u) {
                  stk.push_back(u);
                 stk.push_back(u);
dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
        tarjan(v);
        low[u] = min(low[u], low[v]);
    } else if (id[v] == -1) { // in stk
        low[u] = min(low[u], dfn[v]);
}
                        }
                  if (dfn[u] == low[u]) {
                        int v;
do {
    v = stk.back();
                        stk.pop_back();
id[v] = cnt;
} while (v != u);
                        ++cnt:
                 }
            for (int i
            vector < bool > answer() { return ans; }
int main() {
      int m, n; cin >> m >> n;
TwoSat ts(n);
for (int i = 0; i < m; ++i) {</pre>
           int u, v; char x, y;
cin >> x >> u >> y >> v;
ts.addClause(u - 1, x == '+', v - 1, y == '+');
      if (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";</pre>
      else cout << "IMPOSSIBLE\n";</pre>
```

// 保證出度是 1 所以對 1 個點來說,從他出發只可能遇到一個環 int n, q; int dp[200005][30]; // 倍 vector<vector<int>>> cycles; // 倍增表 vector<**int** > no, cycle_idx, vis; // Order & Can be in cycle, void set_out_of_cycle_no(int now, unordered_set<int> &done) { if (done.find(now)!= done.end()) return; set_out_of_cycle_no(dp[now][0], done); done.insert(now); // post order no[now] = no[dp[now][0]] - 1; int wiint_go_to(int u, int k) { // 回傳當 u 走 k 步時會到的地方 for (int i = 0; i <= 18; i++) { if (k & (1 << i)) { u = dp[u][i]; return u; void find cycle(int now) { unordered_set<int> appear; vector<int> v; bool flag = true; // 代表有環 while (appear.find(now) == appear.end()) { appear.insert(now); v.push_back(now); if (vis[now]) { flag = false; break; now = dp[now][0];for (auto i : v) vis[i] = true; if (!flag) return; // now 是環的起點,我們先找到他在 v 的哪裡 int z = find(v.begin(), v.end(), now) - v.begin(); vector<int> cycle(v.begin() + z, v.end()); cycles.push_back(cycle); int main() { cin >> n >> q; no.assign(n + 1, -1); cycle_idx.assign(n + 1, -1); vis.assign(n + 1, 0); for (int u = 1; u <= n; u++) cin >> dp[u][0]; for (int i = 1; i <= 18; i++) // 倍增表 for (int u = 1; u <= n; u++) dp[u][i] = dp[dp[u][i - 1]][i - 1]; for (int i = 1; i <= n; i++) {

if (!vis[i]) find_cycle(i);

int idx = 0:

unordered_set < int > done;

for (auto &i : cycles) {

vector<int> dis. v: vector<bool> vis;

queue < int > path;
void dfs(int x) { path.push(x); if (vis[x]) {
 step += dis[x];

step++;

dfs(v[x]);

int main() {
 int n; cin >> n;

vis[x] = true:

// count path_dis to rep

cin >> v[i];

step = 0;

cout << '\n';

int n; cin >> n;
v.assign(n + 1, 0);
dis.assign(n + 1, 0);
vis.assign(n + 1, false);
for (int i = 1; i <= n; i++) {</pre>

for (int i = 1; i <= n; i++) {

int is_outof_cycle = 1;

for (int i = 1; i <= n; i++) {
 cout << dis[i] << ' ';</pre>

2.12 Planet Queries II [872f72]

| // 在有向圖中,從 A 到 B 的最短距離

dfs(i);
while (!path.empty()) {
 if (path.front() == path.back()) {
 is out of cvcle = 0;
}

is_outof_cycle = 0;

dis[path.front()] = step; step -= is_outof_cycle;
path.pop();

int step;

2.11 Planets Cycles [71ac0e]

```
for (auto &j : i) {
    no[j] = c++;
    cycle_idx[j] = idx;
    done.insert(j);
          idx++:
     for (int i = 1; i <= n; i++) set_out_of_cycle_no(i, done);
for (int i = 1; i <= q; i++) {
   int u, v; cin >> u >> v;
          // 在同個環內
if (cycle_idx[u] == cycle_idx
[v] && cycle_idx[u] != -1 && cycle_idx[v] != -1) {
                int cyc_size = cycles[cycle_idx[u]].size();
               cout <<
                     (no[v] - no[u] + cyc_size) % cyc_size << "\n";</pre>
          // 都不再環內
          continue:
               if (wiint_go_to(u, no[v] - no[u]) == v) {
    cout << no[v] - no[u] << "\n";</pre>
               else cout << -1 << "\n";
          else if (cycle_idx[u]
                == -1 && cycle_idx[v] != -1) { // v 在環內,二分搜
               int l = -1, r = n;
               l <= n) { // 如果 n 步內可以到
int in_cycle_of_u = wiint_go_to(u, l);
int cycle_size = cycles[cycle_idx[v]].size();
               if (l <= n) {
                     cout << l + (no[v] - no[in_cycle_of_u
] + cycle_size) % cycle_size << "\n";
               else cout << -1 << "\n";
          }
          else { // u 在環內 b 不在,直接不可能 cout << -1 << "\n";
     }
}
```

3 Data Structure

3.1 BIT [d41d8c]

```
template <typename T>
struct Fenwick { // 全部以 0 based 使用
     int n;
     vector<T> a:
     Fenwick(int n_ = 0) {
          init(n_);
     void init(int n_) {
          a.assign(n, T{});
     void add(int x, const T &v) {
    for (int i = x + 1; i <= n; i += i & -i) {
        a[i - 1] = a[i - 1] + v;
    }
}</pre>
     T sum(int x) { // 左閉右開查詢
          T ans{};
for (int i = x; i > 0; i -= i & -i) {
    ans = ans + a[i - 1];
          return ans;
    T rangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
     int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
          int x = 0;
T cur{};
          for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n && cur + a[x + i - 1] <= k) {</pre>
                    x += i:
                     cur = cur + a[x - 1];
               }
          return x:
    }
template <class T>
struct TwoDFenwick { // 全部以 0 based 使用
    int nx, ny; // row, col 個數
vector < vector < T >> a;
```

```
TwoDFenwick(int nx_ = 0, int ny_ = 0) {
    init(nx_, ny_);
}

void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
}

void add(int x, int y, const T &v) {
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            a[i - 1][j - 1] = a[i - 1][j - 1] + v;
        }
}

T sum(int x, int y) { // 左閉右開查詢
    T ans{};
for (int i = x; i > 0; i -= i & -i) {
        for (int j = y; j > 0; j -= j & -j) {
            ans = ans + a[i - 1][j - 1];
        }
}
return ans;
}
T rangeSum
    (int lx, int ly, int rx, int ry) { // 左閉右開查詢
    return sum(
        rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
}
};
```

3.2 RangeBit [d41d8c]

```
template <typename T>
 struct rangeFenwick { // 全部以 0 based 使用
               int n;
vector<T> d, di;
               rangeFenwick(int n_ = 0) {
                             init(n );
                void init(int n_) {
                             d.assign(n, T{});
                             di.assign(n, T{});
               Joid add(int x, const T &v) {
   T vi = v * (x + 1);
   for (int i = x + 1; i <= n; i += i & -i) {
      d[i - 1] = d[i - 1] + v;
      di[i - 1] = di[i - 1] + v;
}</pre>
                           }
              void rangeAdd(int l, int r, const T &v) {
   add(l, v); add(r, -v);
               T sum(int x) { // 左閉右開查詢
                             T`ans{};
                             for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
                             return ans;
              }
              TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
               int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
                            x += i;
                                                                        cur = cur + val:
                                                          }
                                          }
                             return x;
             }
template <class T>
struct rangeTwoDFenwick { // 全部以 0 based 使用
              int nx, ny; // row, col 個數
vector<vector<T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
                             init(nx_, ny_);
              void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
                             dij.assign(nx, vector<T>(ny, T{}));
```

for (int j = y + 1; j <= ny; j += j & -j) {</pre>

```
d[i - 1][j - 1] = d[i - 1][j - 1] + v;
di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
dij[i - 1][j - 1] = dij[i - 1][j - 1] + vij;
             }
      void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
             add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
      T sum(int x, int y) { // 左閉右開查詢
             T ans{};
for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
                          ans = ans
                          \begin{array}{c} -... \\ + \ T(x \ * \ y + x + y + 1) \ * \ d[i \ - \ 1][j \ - \ 1]; \\ \text{ans = ans - } T(y + 1) \ * \ di[i \ - \ 1][j \ - \ 1]; \\ \text{ans = ans - } T(x + 1) \ * \ dj[i \ - \ 1][j \ - \ 1]; \\ \text{ans = ans + } dij[i \ - \ 1][j \ - \ 1]; \end{array}
                   }
             return ans;
       .
T rangeSum
              (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                    (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
}:
3.3 DSU [d41d8c]
struct DSU {
      int n;
       vector < int > boss, siz;
      DSU() {}
      DSU(int n_) {
   init(n_);
       void init(int n_) {
             n = n_{j}
             boss.resize(n);
             iota(boss.begin(), boss.end(), 0);
             siz.assign(n, 1);
      int find_boss(int x) {
             if (boss[x] == x) return x;
return boss[x] = find_boss(boss[x]);
      bool same(int x, int y) {
    return find_boss(x) == find_boss(y);
      bool merge(int x, int y) {
    x = find_boss(x);
    y = find_boss(y);
             if (x == y) {
    return false;
             if(siz[x] < siz[y]) swap(x, y);
siz[x] += siz[y];
boss[y] = x;</pre>
             return true;
       int size(int x) {
   return siz[find_boss(x)];
      }
};
struct DSU {
       int n:
      vector<int> boss, siz, stk;
      DSU() {}
DSU(int n_) {
             init(n_);
      void init(int n_) {
             n = n_;
             boss.resize(n);
             iota(boss.begin(), boss.end(), 0);
             siz.assign(n, 1);
             stk.clear();
      int find(int x) {
   return x == boss[x] ? x : find(boss[x]);
      bool same(int x, int y) {
    return find(x) == find(y);
      bool merge(int x, int y) {
    x = find(x);
             y = find(y);
             if (x == y) {
    return false;
             if (siz[x] < siz[y]) swap(x, y);</pre>
             siz[x] += siz[y];
boss[y] = x;
```

n - -;

```
stk.push_back(y);
     void undo(int x) {
         while (stk.size() > x) {
              int y = stk.back();
              stk.pop_back();
              n++;
              siz[boss[y]] -= siz[y];
              boss[y] = y;
         }
     int size(int x) {
   return siz[find(x)];
};
```

3.4 線段樹 [d41d8c]

```
| template <class Info>
 struct Seg { // 左閉右開寫法
       int n:
      vector <Info> info;
Seg() : n(0) {}
Seg(int n_, Info v_ = Info()) {
   init(n_, v_);
       template <class T>
       Seg(vector < T > init_) {
   init(init_);
       void init(int n_, Info v_ = Info()) {
  init(vector(n_, v_));
       template <class T>
void init(vector<T> init_) {
            n = init_.size();
            n = lnlt_.stze();
info.assign(4 << __lg(n), Info());
function <void(
    int, int, int)> build = [&](int p, int l, int r) {
    if (r - l == 1) {
        info[p] = init_[l];
        reference.
                       return;
                  int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                  pull(p);
            build(1, 0, n);
      void pull
    (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
       void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
    }
}
                  return;
            int m = (l + r) / 2;
if (x < m) {
                  modify(2 * p, l, m, x, v);
            } else {
                  modify(2 * p + 1, m, r, x, v);
            pull(p);
       void modify(int p, const Info &i) {
            modify(1, 0, n, p, i);
      2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
       (int ql, int qr) { return query(1, 0, n, ql, qr); } template < class F> // 尋找區間內,第一個符合條件的
       int findFirst
            (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
    return -1;</pre>
            if (l >= x && r <= y && !pred(info[p])) {</pre>
                  return -1:
            if (r - l == 1) {
                  return l;
            int m = (l + r) / 2;
int res = findFirst(2 * p, l, m, x, y, pred);
            if (res == -1)
                  res = findFirst(2 * p + 1, m, r, x, y, pred);
            return res;
      }
      template < class F> // 若要找 last, 先右子樹遞迴即可int findFirst(int l, int r, F &&pred) {
            return findFirst(1, 0, n, l, r, pred);
```

void range_apply(int l, int r, const Tag &v) {

range_apply(1, 0, n, l, r, v);

```
// ---define structure and info plus---
                                                                                                              template < class F> // 尋找區間內,第一個符合條件的
struct Info {
                                                                                                               int findFirst
                                                                                                                    (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
    return -1;</pre>
      int n = 1:
      int sum = 0;
Info operator+(const Info &a, const Info &b) {
    return { a.n + b.n, a.sum + b.sum };
                                                                                                                     if (l >= x && r <= y && !pred(info[p])) {</pre>
                                                                                                                           return -1:
3.5 懶標線段樹 [d41d8c]
                                                                                                                     if (r - l == 1) {
                                                                                                                           return l;
template <class Info, class Tag>
struct LazySeg { // 左閉右開寫法
                                                                                                                     int m = (l + r) / 2;
                                                                                                                    push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
      int n;
      vector < Info > info:
      vector <Tag> tag;
LazySeg() : n(0) {}
                                                                                                                     if (res ==
                                                                                                                          res = findFirst(2 * p + 1, m, r, x, y, pred);
      LazySeg(int n_, Info v_ = Info()) {
  init(n_, v_);
                                                                                                                     return res:
      template <class T>
LazySeg(vector<T> init_) {
                                                                                                              template <class F> // 若要找 last, 先右子樹遞迴即可int findFirst(int l, int r, F &&pred) {
           init(init_);
                                                                                                                    return findFirst(1, 0, n, l, r, pred);
      void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
                                                                                                        };
// ---define structure and info plus---
                                                                                                        struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add; void apply(const Tag& v) {
      template <class T>
void init (vector<T> init_) {
            n = init_.size();
info.assign(4 << __lg(n), Info());
tag.assign(4 << __lg(n), Tag());</pre>
                                                                                                                    if (v.set_val) {
                                                                                                                           set_val = v.set_val;
                                                                                                                          add = v.add:
            else {
                                                                                                                           add += v.add;
                                                                                                             }
                  int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                                                                                                        struct Info {
                                                                                                              void apply(int l, int r, const Tag &v) {
    if (v.set_val) {
        sum = (r - l) * v.set_val;
    }
}
                  pull(p);
             build(1, 0, n);
                                                                                                                     sum += (r - l) * v.add;
      void pull
      void aprly (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
   tag[p].apply(v);
                                                                                                              // Info& operator=(const Info &rhs) {
                                                                                                                        // 部分 assignment 使用 return *this;
                                                                                                              //
//
// }
      void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
                                                                                                        Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
                                                                                                        }
                                                                                                        3.6 莫隊 [d41d8c]
            tag[p] = Tag();
                                                                                                        struct query {
                                                                                                       struct query {
    int l, r, id;
} typedef query;
void MO(int n, vector<query> &queries) {
    int block = sqrt(n);
    function <bool(query, query)> cmp = [&](query a, query b) {
        int block_a = a.l / block;
        int block_b = b.l / block;
        if (block_a != block_b) return block_a < block_b;
        return a.r < b.r;
};</pre>
      void modify(int p, int l, int r, int x, const Info &v) {
            if (r - l == 1) {
    info[p] = v;
                  return;
            int m = (l + r) / 2;
push(p, l, r);
if (x < m) {</pre>
                  modify(2 * p, l, m, x, v);
            } else
                  modify(2 * p + 1, m, r, x, v);
                                                                                                              sort(queries.begin(), queries.end(), cmp);
                                                                                                        void compress(vector<int> &nums) {
            pull(p);
                                                                                                              vector < int > sorted = nums;
sort(sorted.begin(), sorted.end());
      void modify(int p, const Info &i) {
                                                                                                              sorted.erase
            modify(1, 0, n, p, i);
                                                                                                                      (unique(sorted.begin(), sorted.end()), sorted.end());
      Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    push(p, l, r);
    return query(r *</pre>
                                                                                                              for (int i = 0; i < nums.size(); i++) {
    nums[i] = lower_bound(sorted.begin</pre>
                                                                                                                            (), sorted.end(), nums[i]) - sorted.begin() + 1;
             return query(p *
2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
                                                                                                        3.7 Treap [d41d8c]
                                                                                                        struct Treap {
   Treap *lc, *rc;
      Ínfo query
             (int ql, int qr) { return query(1, 0, n, ql, qr); }
                                                                                                              int pri, siz; bool rev_valid;
int val; int min;
Treap(int val_) {
    min = val = val_;
      void range_apply
             (int p, int l, int r, int ql, int qr, const Tag &v) {
if (qr <= l || ql >= r) return;
if (ql <= l && r <= qr) {</pre>
                                                                                                                    pri = rand();
lc = rc = nullptr;
                  apply(p, l, r, v);
                  return:
                                                                                                                     siz = 1; rev_valid = 0;
            int m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
                                                                                                              void pull() { // update siz or other information
                                                                                                                    siz = 1;
min = val;
            pull(p);
                                                                                                                    for (auto c : {lc, rc}) {
   if (!c) continue;
```

siz += c->siz;

min = std::min(min, c->min);

```
void push() {
              if (rev_valid) {
   swap(lc, rc);
   if (lc) lc->rev_valid ^= 1;
   if (rc) rc->rev_valid ^= 1;
              rev_valid = false;
       int find(int k) { // 找到 min 是 k 的位置 (1-based)
              push();
int ls = (lc ? lc->siz : 0) + 1;
              if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
int size(Treap *t) {
    return t ? t->siz : 0;
Treap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
    a->push(); b->push();
    if (a->pri > b->pri) {
        a->rc = merge(a->rc, b);
}
              a->pull();
              return a;
       else {
              b->lc = merge(a, b->lc);
b->pull();
              return b;
pair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
       t->push();
       if (size(t->lc) < k) {
    auto [a, b] = split(t->rc, k - size(t->lc) - 1);
    t->rc = a;
              t->pull();
              return {t, b};
              auto [a, b] = split(t->lc, k);
t->lc = b;
              t->pull();
              return {a, t};
      }
void Print(Treap *t) {
       if (!t) return;
t->push();
       Print(t->lc);
       cout << t->val;
Print(t->rc);
```

4 Flow

4.1 Dinic [287fe8]

```
template < class T>
struct Dinic {
    struct Edge {
         int to;
          T flow, cap; // 流量跟容量
     int n, m, s, t;

T INF_Flow = numeric_limits<T>:::max() / 2;
     vector < vector < int >> adj; // 此點對應的 edges 編號
     vector<Edge> edges; // 幫每個 edge 編號
     vector <int> dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
    n = n_; m = 0;
    dis.resize(n); ptr.resize(n);
    adj.assign(n, vector <int>{});
edges clear();
           edges.clear();
     void add_edge(int u, int v, T cap) {
           // 偶數 id 是正向邊
          edges.push_back({ v, 0, cap });
edges.push_back({ u, 0, 0 });
           adj[u].push_back(m++);
          adj[v].push_back(m++);
     bool bfs() {
          fill(dis.begin(), dis.end(), -1);
dis[s] = 0; queue<int> q;
           q.push(s);
          if (e.flow == e.cap) continue;
if (dis[e.to] == -1) {
                           dis[e.to] = dis[u] + 1;
```

```
q.push(e.to);
                   }
              return dis[t] != -1;
       T dfs(int u, T flow) {
   if (flow == 0) return 0;
   if (u == t) return flow;
             for (int
                   &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {
Edge &e = edges[adj[u][cur]];
if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;</pre>
                    T mn = dfs(e.to, min(flow, e.cap - e.flow));
                    if (mn > 0) {
    e.flow += mn;
                          edges[adj[u][cur] ^ 1].flow -= mn;
                   }
             }
             return 0; // 到不了終點就會 return 0
        T work(int s_, int t_) {
             s = s_; t = t_; T flow = 0;
while (bfs()) {
    fill(ptr.begin(), ptr.end(), 0);
                    while (true) {
    T res = dfs(s, INF_Flow);
                          if (res == 0) break;
                          flow += res;
                   }
             return flow;
       void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
       }
};
```

4.2 Min Cut [44ae6c]

```
// CSES Police Chase
  int main(){
          int n, m; cin >> n >> m;
Dinic < int > g(n);
for (int i = 0; i < m; i++) {</pre>
                 int u, v, cap = 1;
cin >> u >> v;
                 g.add_edge(u, v, cap);
                 g.add_edge(v, u, cap);
         int res = g.work(0, n - 1);
cout << res << "\n";
if (res == 0) return;
         vector <int> vis(n);
auto find = [&](auto self, int u) -> void {
   if (!vis[u]) {
                         vis[u] = 1;
                          for (int id : g.adj[u])
                                 auto e = g.edges[id];
if (e.cap - e.flow > 0) {
    self(self, e.to);
                         }
                }
          find(find, 0);
         frind(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
        auto e = g.edges[id];
}</pre>
                         if (!vis[e.to]) {
    cout << i + 1 << " " << e.to + 1 << " | n";
                         }
                 }
         }
1
```

4.3 Hangarian [350fc3]

```
| struct Hangarian { // 0-based
           int n, m; // 最小路徑覆蓋,二分匹配
vector<vector<int>>> adj;
          vector <int>> adj;
vector <int> used, vis;
vector <pair <int, int>> match;
Hangarian(int n_ = 0, int m_ = 0) {
    init(n_, m_);
           void init(int n_ = 0, int m_ = 0) {
    n = n_; m = m_;
                   adj.assign(n + m, vector<int>());
used.assign(n + m, -1);
vis.assign(n + m, 0);
           void addEdge(int u, int v) {
   adj[u].push_back(n + v);
   adj[n + v].push_back(u);
```

```
vector<pair<int, int>> work() {
            match.clear();
used.assign(n + m, -1);
            vis.assign(n + m, 0);
auto dfs = [&](auto self, int u) -> bool {
                  for (int v : adj[u]) {
    if (vis[v] == 0) {
        vis[v] = 1;
        if (used[v] == -1 || self(self, used[v])) {
                                     used[v] = u;
                                     return true:
                               }
                        }
                  return false:
            for (int i = 0; i < n; i++) {
    fill(vis.begin(), vis.end(), 0);
}</pre>
                   dfs(dfs, i);
             for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
                         match.emplace_back(used[i], i - n);
             return match;
      }
};
```

MCMF [f667f8]

```
template < class Tf, class Tc>
struct MCMF {
    // 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就好
    int n, m, s, t;
If INF_FLOW = numeric_limits<Tf>::max() / 2;
It INF_COST = numeric_limits<Tc>::max() / 2;
    struct Edge {
         int to;
         Tf flow, cap; // 流量跟容量
         Tc cost;
    vector < vector < int >> adj;
    vector<Edge> edges; // 幫每個 edge 編號
vector<Tc> dis, pot; // johnson algorithm, using spfa
    vector <int> rt; // 路徑恢復,對應 id
    vector <bool> inq;
MCMF(int n_ = 0) { init(n_); }
    void init(int n_ = 0) {
         n = n_;
         m = 0;
         edges.clear();
adj.assign(n, vector<int>{});
    void add_edge(int u, int v, Tf cap, Tc cost){
   edges.push_back({v, 0, cap, cost});
   edges.push_back({u, 0, 0, -cost});
         adj[u].push_back(m++);
         adj[v].push_back(m++);
    bool spfa() {
    dis.assign(n, INF_COST);
    rt.assign(n, -1); inq.assign(n, false);
        q.push(v); inq[v] = true;
                       }
                  }
             }
         return dis[t] != INF_COST;
   dis[v] = ndis; rt[v] = id;
                       pq.emplace(ndis, v);
                  }
         return dis[t] != INF_COST;
```

```
// 限定 flow, 最小化 cost
pair<Tf, Tc> work_flow(<mark>int</mark> s_, int t_, Tf need) {
             s = s_, t = t_; pot.assign(n, 0);
Tf flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {</pre>
                          dis[i] += pot[i] - pot[s];
                    Tf f = INF_FLOW;
                    for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                  (f, edges[rt[i]].cap - edges[rt[i]].flow);
                   edges[rt[i]].flow += f;
edges[rt[i] ^ 1].flow -= f;
                    flow += f; need -= f;
cost += f * dis[t]; fr = false;
                    swap(dis, pot);
if (need == 0) break;
             return make pair(flow. cost):
       ,
// 限定 cost,最大化 flow
pair<Tf, Tc> work_budget(<mark>int</mark> s_, <mark>int</mark> t_, Tc budget) {
             s = s_, t = t_; pot.assign(n, 0);
If flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] += pot[i] - pot[s];
}</pre>
                    (f, edges[rt[i]].cap - edges[rt[i]].flow);
                   }
f = min<Tf>(f, budget / dis[t]);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
}
                    flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
                    swap(dis, pot);
if (budget == 0 || f == 0) break;
             return make_pair(flow, cost);
       void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
};
         String
```

5

5.1 KMP [cddfd9]

```
string sub;
vector<int> failure;
            KMP(string sub_) {
                     sub = sub_;
failure.resize(sub.size(), -1);
                     buildFailFunction();
           void buildFailFunction() {
    for (int i = 1; i < (int)sub.size(); i++) {
        int now = failure[i - 1];
}</pre>
                               while (now != -1
    && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
                    }
            vector<<mark>int</mark>> match(string &s) {
                     vector <int> match;
for (int i = 0, now = -1; i < (int)s.size(); i++) {
    // now is the compare sucessed length -1</pre>
                              // now is the compare sucessed tength -1
while (s[i] !=
    sub[now + 1] && now != -1) now = failure[now];
// failure stores if comparison fail, move to where
if (s[i] == sub[now + 1]) now++;
if (now + 1 == (int)sub.size()) {
    match.push_back(i - now);
    now = failure[now];
}
                               }
                     return match;
| };
```

5.2 Z Function [8dd6ac]

```
|// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
// 的最長公共前綴 (LCP) 的長度
vector<int> Z(string s) {
    int n = s.size();
    vector<int> z(n);
    z[0] = n;
    for (int i = 1, j = 1; i < n; i++) {</pre>
```

```
z[i] = max(0, min(j + z[j] - i, z[i - j]));
while (i + z[i] < n && s[z[i]] == s[i + z[i]]) {
                z[i]++;
           if (i + z[i] > j + z[j]) {
                j = i;
      return z; // 最後一格不算
}
```

5.3 Duval Algorithm [f9dcca]

```
|// duval_algorithm
 // 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
 vector<string> duval(string s) {
       int i = 0, n = s.size();
vector<string> res;
       while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
      else k++;
}</pre>
                   j++;
             while (i <= k) {</pre>
                   res.push_back(s.substr(i, j - k));
                   i += j - k;
             }
       return res:
 // 最小旋轉字串
 string min_round(string s) {
       s += s;
int i = 0, n = s.size();
       int start = i;
       while (i < n / 2) {
    start = i;
    int k = i, j = i + 1;
    while (s[k] <= s[j] && j < n) {
        if (s[k] < s[j]) k = i;
        else k+++</pre>
                   else k++;
                   j++;
             while (i <= k) {
                   i += j - k;
       return s.substr(start, n / 2);
}
```

5.4 Manacher [9c9ca6]

```
// 找到對於每個位置的迴文半徑
vector < int > manacher(string s) {
    string t = "#";
     for (auto c : s) {
          t += c;
t += '#';
     int n = t.size();
    vector < int > r(n);
for (int i = 0, j =
            0; i < n; i++) { // i 是中心, j 是最長回文字串中心 f(2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
          if (2
          while (i - r[i] >=
               0 && i + r[i] < n && t[i - r[i]] == t[i + r[i]]) { r[i] += 1;
          if (i + r[i] > j + r[j]) {
               j = i;
          }
     return r;
// # a # b # a #
// 1 2 1 4 1 2 1
     // # a # b # b # a #
     // 1 2 1 2 5 2 1 2 1
     // 值 -1 代表原回文字串長度
    // (id - val + 1) / 2 可得原字串回文開頭
```

5.5 Trie [3b3aa0]

```
struct Trie {
     struct trie_node {
            bool is_word;
           vector<trie_node *> children;
trie_node() {
   is_word = false;
                 children.resize(26, NULL);
           }
      trie_node *root = new trie_node();
     void insert(string &s) {
    trie_node *cur = root;
    for (int i = 0; i < s.size(); i++) {</pre>
                 int idx = s[i] - 'a';
```

```
if (cur->children[idx] == NULL) {
   cur->children[idx] = new trie_node();
                   cur = cur->children[idx]:
            cur->is_word = true;
      bool is_in_trie(string &s) {
            trie_node *cur = root;
for (int i = 0; i < s.size(); i++) {
                   if (cur->
                   children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
      int search_i_start(string &s, int i, vector<int> &dp) {
    trie_node *cur = root;
    int sz = s.size(), ans = 0;
    for (int j = i; j < sz; j++) {
        if (cur</pre>
                  ->children[s[j] - 'a'] == nullptr) return ans;
cur = cur->children[s[j] - 'a'];
if (cur->is_word)
    (ans += dp[j + 1]) %= mod;
            return ans;
     }
int main() {
      // 找到 sub 集合裡,可以重複用,組成 s 的組數 Trie trie; string s; cin >> s; int sz = s.size();
      // dp 代表 i 開頭到最後的配對總數
      ,,
// 找到有結尾為 stop 的 dp[i] += dp[j + 1]
      int n; cin >> n;
      vector < int > dp(sz + 1, 0);
for (int i = 0; i < n; i++) {
    string sub; cin >> sub;
            trie.insert(sub);
      dp[sz] = 1;
for (int i = sz - 1; i >= 0; i--) {
            dp[i] = trie.search_i_start(s, i, dp);
      cout << dp[0] << endl;
```

Math 6

6.1 質因數分解 [ee1622]

```
// FacMul = N(x+1)(y+1)(z+1)/2
vector<int> is_prime;
// 1 代表是質數,非 1 不是
void init(int n) {
    is_prime.assign(n + 1, 1);
    is_prime[j] = i;
        }
    }
int main() {
    init(1000000);
    ll ans = 1;
    ll ans = 1;
ll q; cin >> q;
map<ll, ll> mp;
while (is_prime[q] != 1) {
    mp[is_prime[q]]++;
    q /= is_prime[q];
}
    if (q != 1) mp[q]++;
for (auto [a, b] : mp) {
    ans *= b + 1;
    cout << ans << "\n";
```

6.2 模除計算 [9b1014]

```
using i64 = long long;
template < class T>
constexpr T power(T a, i64 b) {
  T res = 1;
  for (; b; b /= 2, a *= a) {
    if (b % 2) {
      res *= a;
  }
}
         }
```

```
return res:
constexpr i64 mul(i64 a, i64 b, i64 p) {
   i64 res = a * b - i64(1.L * a * b / p) * p;
     res %= p;
     if (res < 0) {
    res += p;
     return res;
template < i64 P>
struct MLong {
    i64 x;
     constexpr MLong() : x{} {}
constexpr MLong(i64 x) : x{norm(x % getMod())} {}
     static i64 Mod;
     constexpr static i64 getMod() {
   if (P > 0) {
               return P:
          } else {
               return Mod;
          }
     constexpr static void setMod(i64 Mod_) {
   Mod = Mod_;
     constexpr i64 norm(i64 x) const {
          if (x < 0) {
              x += getMod();
          if (x >= getMod()) {
    x -= getMod();
          return x;
     constexpr i64 val() const {
          return x;
     explicit constexpr operator i64() const {
     constexpr MLong operator-() const {
          MLong res;
          res.x = norm(getMod() - x);
          return res;
     constexpr MLong inv() const {
          assert(x != 0);
return power(*this, getMod() - 2);
     constexpr MLong &operator*=(MLong rhs) & {
    x = mul(x, rhs.x, getMod());
    return *this;
     constexpr MLong &operator+=(MLong rhs) & {
    x = norm(x + rhs.x);
    return *this;
     constexpr MLong &operator -= (MLong rhs) & {
          x = norm(x - rhs.x);
          return *this:
     constexpr MLong &operator/=(MLong rhs) & {
    return *this *= rhs.inv();
     friend constexpr MLong operator*(MLong lhs, MLong rhs) {
          MLong res = lhs;
          res *= rhs:
          return res;
     friend constexpr MLong operator+(MLong lhs, MLong rhs) {
   MLong res = lhs;
          return res:
     friend constexpr MLong operator - (MLong lhs, MLong rhs) {
          MLong res = lhs;
res -= rhs;
          return res;
     friend constexpr MLong operator/(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res /= rhs;
          return res;
            constexpr istream &operator>>(istream &is, MLong &a) {
          i64 v;
is >> v;
          a = MLong(v);
          return is:
            ostream & operator << (ostream &os, const MLong &a) {
          return os << a.val();</pre>
     friend constexpr bool operator==(MLong lhs, MLong rhs) {
    return lhs.val() == rhs.val();
     friend constexpr bool operator!=(MLong lhs, MLong rhs) {
```

```
return lhs.val() != rhs.val():
      }
 };
 template<>
 i64 MLong<0LL>::Mod = i64(1E18) + 9;
 constexpr i64 P = 998244353;
using Z = MLong <P>;
// using Z = MLong <0LL>; // change Mod
 struct Comb {
       i64 n;
      vector <Z> _fac;
vector <Z> _invfac;
vector <Z> _inv;
Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
Comb(i64 n) : Comb() { init(n); }
       void init(i64 m) {
            m = min(m, Z::getMod() - 1);
if (m <= n) return;</pre>
            _fac.resize(m + 1);
_invfac.resize(m +
            _inv.resize(m + 1);
            for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;</pre>
            for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
       Z fac(i64 m) {
   if (m > n) init(2 * m);
       Z invfac(i64 m) {
            if (m > n) init(2 * m);
            return _invfac[m];
       Z inv(i64 m) {
            if (m > n) init(2 * m);
return _inv[m];
       J binom(i64 n, i64 m) {
   if (n < m || m < 0) return 0;
   return fac(n) * invfac(m) * invfac(n - m);</pre>
       |} comb; // 注意宣告, 若要換模數需重新宣告
 6.3 中國餘數定理 [d41d8c]
 ll exgcd(ll a, ll b, ll &x, ll &y) {
       if (!b) {
            x = 1, y = 0;
            return a;
       ll g = exgcd(b, a \% b, y, x);
         -= a / b * x;
       return g;
 ĺl inv(ll x, ll m){
       ll a, b;
exgcd(x, m, a, b);
       a %= m;
       if (a < 0) a += m;
       return a:
 // remain, mod
ll CRT(vector<pair<ll, ll>> &a){
       ll prod = 1;
       for (auto x : a) {
    prod *= x.second;
       ĺl res = 0;
       for (auto x : a) {
   auto t = prod / x.second;
   res += x.first * t % prod * inv(t, x.second) % prod;
            if(res >= prod) res -= prod;
       return res;
 }
 6.4 矩陣與快速幂 [08b5fe]
  template < class T>
 struct Mat {
       int m, n;
       constexpr static ll mod = 1e9 + 7;
      Mat(int n_ = 0) { init(n_, n_); }
Mat(int m_, int n_) { init(m_, n_); }
Mat(vector<vector<T>> matrix_) { init(matrix_); }
```

```
void init(int m_, int n_) {
    m = m_; n = n_;

           matrix.assign(m, vector<T>(n));
     void init(vector<vector<T>> &matrix_) {
          m = matrix_.size();
n = matrix_[0].size();
           matrix = matrix_;
     vector<vector<T>> unit(int n) { // 單位矩陣
           vector < vector < T >> res(n, vector < T >(n));
for (int i = 0; i < n; i++) {
    res[i][i] = 1;</pre>
           return res:
     constexpr Mat &operator*=(const Mat& rhs) & {
           assert(matrix[0].size() == rhs.matrix.size());
int m = matrix.size()
                 , k = matrix[0].size(), n = rhs.matrix[0].size();
          l] * rhs.matrix[l][j] % mod)) %= mod;
                }
           matrix = ans.matrix;
           return *this;
     constexpr Mat &operator^=(ll p) & {
           assert(m == n); assert(p >= 0);
Mat ans(p-- == 0 ? unit(m) : matrix);
          wat ans(p - == 0 / unit(n) :
while (p > 0) {
   if (p & 1) ans *= *this;
     *this *= *this;
   p >>= 1;
           matrix = ans.matrix;
return *this:
     friend Mat operator*(Mat lhs, const Mat &rhs) {
    lhs *= rhs;
           return lhs;
     friend Mat operator^(Mat lhs, const ll p) {
           lhs ^= p;
};
// fn = fn-3 + fn-2 + fn-1
// 初始矩陣 轉移式
// f4 f3 f2 1 1 0
// f3 f2 f1 1 0 1 =
                 轉移以
1 1 0 f5 f4 J3
1 0 1 => f4 f3 f2
1 0 0 f3 f2 f1
```

6.5 樹論分塊 [06204a]

6.6 Mobius Theorem

- 數論 分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理 出 f 的前缀和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n}\!\mu(d)\!=\!\begin{cases} 1 & \text{for } n\!=\!1\\ 0 & \text{for } n\!\neq\!0 \end{cases}$$

2. μ 是常數函數 1 的反元素 $\Rightarrow \mu*1=\epsilon$, $\epsilon(n)$ 只在n=1時為 1, 其餘情況皆為 0。

φ歐拉函數: x 以下與 x 互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^i) \\ &= 1 + p^0(p-1) + p^1(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^c \\ &= id \end{split}$$

• 莫比烏斯反演公式

-
$$f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$$

- $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

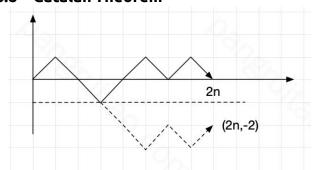
• 例子

$$\begin{split} &\sum_{i=a}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{i=1}^{\infty} \mu(d) \sum_{i=1}^{\left \lfloor \frac{x}{k} \right \rfloor} \left \lfloor \frac{y}{k} \right \rfloor \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left \lfloor \frac{x}{k} \right \rfloor} [d \mid i] \sum_{j=1}^{y} [d \mid j] \ \mathrm{d} \ \mathrm{PSER} \ \mathrm{i} \ \mathrm{FRA} \ \mathrm{1} \\ &= \sum_{d=1}^{\min(\left \lfloor \frac{x}{k} \right \rfloor, \left \lfloor \frac{y}{k} \right \rfloor)} \mu(d) \left \lfloor \frac{x}{kd} \right \rfloor \left \lfloor \frac{y}{kd} \right \rfloor \end{split}$$

6.7 莫比烏斯反演 [d41d8c]

```
const int maxn = 2e5;
ll mobius_pref[maxn];
 void init() {
        mobius_pref[1] = 1;
vector<ll> wei
        (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
    }
                      continue; // 包含平方
               if (wei[i] == 0) {
                      wel[i] == 0, 1
wel[i] = 1;
for (ll j = 2; i * j < maxn; j++) {
    if (j % i == 0) wel[i * j] = -1;
    else if (wel[i * j] != -1) wel[i * j]++;</pre>
                      }
               mobius_pref[i]
                       = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
       }
 void solve() {
        auto cal = [&](ll x, ll y) -> int {
              for (int l = 1, r; l <= min(x, y); l = r + 1) {
    r = min(x / (x / l), y / (y / l));
    res += (mobius_pref[r] - mobius_pref[l]</pre>
                                - 1]) * (x / l) * (y / l); // 代推出來的式子
               return res;
                (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k, (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n";
}
```

6.8 Catalan Theorem



1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$ 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有x 個,往下有y 個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.9 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- X/G:本質不同的方案的集合
- X'^g : 對於某一種操作 g, 所有方案中, 經過 g 這種翻轉後保持不變的方案的集合
- 集合取絕對值代表集合數

7 Search and Gready

7.1 二分搜 [d41d8c]

```
int main() {
    int l = 1, r = 10;
    // 1 to tar, find tar
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}</pre>
```

7.2 三分搜 [d41d8c]

```
| // 找極值問題,遞增遞減
| void solve() {
| int | = 0, r = 10, ans = 0; // ans 紀錄答案 |
| while (| <= r) {
| int | d = (r - l) / 3; // 差 |
| int | ml = l + d, mr = r - d; // mr 要用減的 |
| auto | cal = [&](int | m) -> int {
| int | x = 0; |
| return | x; // 計算答案 |
| ; int | ansl = | cal(|ml), ansr = | cal(|mr); if (| ansl | < | ansr) {
| l = | ml + 1; |
| else | r = | mr - 1; |
| }
```

8 Tree

8.1 LCA [9f95b1]

```
}
int lca(int a, int b) {
    if (depth[a] < depth[b]) swap(a, b);
    int pull = depth[a] - depth[b];
    for (int i = 0; i < 18; i++) {
        if (pull & (1 << i)) {
            a = par[a][i];
        }
    if (a == b) return a;
    for (int i = 17; i >= 0; i--) {
        if (par[a][i] != par[b][i]) {
            a = par[a][i], b = par[b][i];
        }
    }
    return par[a][0];
}
```

8.2 樹重心 [30b436]

```
struct centroid_decomposition {
       int n:
        vector<vector<int>> adj;
        vector<bool> vis;
       vector<int> siz;
       centroid_decomposition() {}
centroid_decomposition(int n_) { init(n_); }
       void init(int n_) {
             n = n_;
adj.assign(n, {});
vis.assign(n, false);
             siz.assign(n, 1);
        void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void get_siz(int dep, int x, int p = -1) {
             siz[x] = 1;
             stz[x] = 1;
for (int y : adj[x]) {
    if (y == p || vis[y]) continue;
    get_siz(dep + 1, y, x);
    siz[x] += siz[y];
       return get_cen(y, sz, x);
              return x:
       void work(int x = 0) {
    get_siz(0, x);
    int cen = get_cen(x, siz[x]);
    vis[cen] = true;
              // do something
              for (int y : adj[cen]) {
   if (vis[y]) continue;
   work(y);
1 };
```

8.3 樹壓平 [51199c]

```
點加值 = 所有子節點區間加值,求單點,使用 bit,做前綴差分
CSES 1138_Path Queries
   int n, q; cin >> n >> q;
vector <int> node_value(n + 1), euler_ordered_value(n);
for (int i = 1; i <= n; i++) {</pre>
        cin >> node_value[i];
   vector<vector<int>> tree(n + 1);
   for (int i = 1; i < n; i++) {
  int u, v; cin >> u >> v;
  tree[u].push_back(v);
        tree[v].push_back(u);
   vector<pair<int, int>> tree mapping(n + 1);
   int cnt = 0;
auto dfs = [&](auto self, int u, int par) -> void {
    euler_ordered_value[++cnt] = node_value[u];
        tree_mapping[u].first = cnt;
        for (auto v : tree[u]) {
   if (v == par) continue;
   self(self, v, u);
        tree_mapping[u].second = cnt;
   dfs(dfs,
   BIT bit(n);
for (int i = 1; i <= n; i++) {
        bit.modify(tree_mapping[i].first, node_value[i]);
        if (tree_mapping[i].first < n) { // root 就不用扣了</pre>
                    (tree_mapping[i].second + 1, -node_value[i]);
```

8.4 Heavy Light Decomposition [6791f6]

```
struct HLD {
     vector<int> siz, top, dep, parent, in, out, seq;
     vector<vector<int>> adj;
     int cur;
    HLD() {}
HLD(int n) {
          init(n);
     void init(int n) {
          this ->n = n:
          siz.resize(n);
          top.resize(n);
          dep.resize(n);
parent.resize(n);
          .
in.resize(n);
          out.resize(n);
          seq.resize(n);
          adj.assign(n, {});
     void addEdge(int u, int v) {
          adj[u].push_back(v);
          adj[v].push_back(u);
     void work(int root = 0) {
          top[root] = root;
dep[root] = 0;
          parent[root] = -1;
          dfs1(root);
          dfs2(root):
     void dfs1(int u) {
          if (parent[u] != -1) {
    adj[u].erase(find
                     (adj[u].begin(), adj[u].end(), parent[u]));
          siz[u] = 1;
          for (auto &v : adj[u]) {
    parent[v] = u;
    dep[v] = dep[u] + 1;
               dfs1(v);
               siz[u] += siz[v];
if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
              } // 讓 adj[u][0] 是重子節點
         }
     void dfs2(int u) {
          in[u] = cur++;
          seq[in[u]] = u; // dfn 對應的編號
          dfs2(v):
          out[u] = cur;
     int lca(int u, int v) {
          while (top[u] != top[v]) {
    if (dep[top[u]] > dep[top[v]]) {
        u = parent[top[u]];
}
               } else {
                    v = parent[top[v]];
          return dep[u] < dep[v] ? u : v;</pre>
    int dist(int u, int v) {
   return dep[u] + dep[v] - 2 * dep[lca(u, v)];
     int jump(int u, int k) {
    if (dep[u] < k) {
        return -1;</pre>
          int d = dep[u] - k;
```

```
while (dep[top[u]] > d) {
    u = parent[top[u]];
          return seq[in[u] - dep[u] + d];
     bool isAncester(int u, int v) {
          // 判斷 u 是否是 v 的祖先
          return in[u] <= in[v] && in[v] < out[u];</pre>
      int rootedParent(int u, int v) {
          // 根據新根節點 u 計算 v 的父節點
          swap(u, v);
          if (u == v) {
               return u;
          if (!isAncester(u, v)) {
               return parent[u];
          auto it = upper_bound(adj
    [u].begin(), adj[u].end(), v, [&](int x, int y) {
    return in[x] < in[y];</pre>
          }) - 1;
return *it;
      int rootedSize(int u, int v) {
          // 根據新根節點 u 計算子樹 v 的大小
          if (u == v) {
          if (!isAncester(v, u)) {
              return siz[v];
          return n - siz[rootedParent(u, v)];
      int rootedLca(int a, int b, int c) {
          // 根據新的根節點計算三個節點 a、b 和 c 的最近公共祖先 return lca(a, b) ^ lca(b, c) ^ lca(c, a);
     }
};
```

8.5 Virtual Tree [622e69]

```
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
// 可以建立虚樹達成快速樹 DP
 // 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector <int>stk(maxn);
 int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
        vt[stk[top - 1]].push_back(stk[top]), top--;
    if (stk[top - 1] != l) {
        vt[l] sush back(stk[top]);
        vt[l] sush back(stk[top]);
        vt[l] sush back(stk[top]);
}</pre>
                vt[l].push_back(stk[top]);
                 stk[top] = l;
         } else vt[l].push_back(stk[top--]);
         stk[++top] = u;
  void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
         vt[u].clear();
  void solve(int n, int q) {
         vector g(n + 1, vector<pair<int, int>>());
         vector vt(n + 1, vector vector vt(n + 1, vector <int>()); // dfs 完清除, 否則會退化
vector <ll> dp(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;

                g[u].push_back({v, w});
                 g[v].push_back({u, w});
         build_lca(n, g);
         build(n, g);
for (int i = 0; i < q; i++) {
   int m; top = -1; cin >> m;
                 vector<int> key(m);
                for (int j = 0; j < m; j++) {
    cin >> key[j];
                         iskey[key[j]] = 1;
                key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
                 for (int x : key) insert(x, vt);
                while (top
                           > 0) vt[stk[top - 1]].push_back(stk[top]), --top;
                 // DP
                auto dfs = [&](auto self, int u) -> void {
    for (auto v : vt[u]) {
        self(self, v);
        if (iskey[v]) {
            dp[u] += min_dis[v];
        }
                                       // 砍掉 1 到 v 之間最短的路
                                       dp[u] += min(dp[v], min_dis[v]);
                                iskey[v] = dp[v] = 0;
```

```
vt[u].clear():
          dfs(dfs, key[0]); // key[0] 一定是 root cout << dp[key[0]] << "\n";
          iskey[key[0]] = dp[key[0]] = 0;
}
```

8.6 Dominator Tree [baa540]

```
struct Dominator_tree {
       int n, id;
       vector <vector <int>> adj, radj, bucket;
vector <int>> sdom, dom, vis, rev, pa, rt, mn, res;
Dominator_tree(int n_ = 0) { init(n_); }
        void init(int _n) {
    n = _n, id = 0;
    adj.assign(n, vector<int>());
    radj.assign(n, vector<int>());
               bucket.assign(n, vector<int>());
sdom.resize(n); dom.assign(n, -1)
vis.assign(n, -1); rev.resize(n);
pa.resize(n); rt.resize(n);
                mn.resize(n); res.resize(n);
       void add_edge(int u, int v) { adj[u].push_back(v); }
int query(int v, int x) {
    if (rt[v] == v) return x ? -1 : v;
    int p = query(rt[v], 1);
    if (p == -1) return x ? rt[v] : mn[v];
    if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
    rt[v] = p.
               rt[v] = p;
return x ? p : mn[v];
       }
        void build(int s) {
               dfs(s);
                for (int i = id - 1; i >= 0; i--) {
                       (Int i = tu - 1, color
for (int u : radj[i])
    sdom[i] = min(sdom[i], sdom[query(u, 0)]);
                       if (i) bucket[sdom[i]].push_back(i);
for (int u : bucket[i]) {
                               int p = query(u, 0);
dom[u] = sdom[p] == i ? i : p;
                       if (i) rt[i] = pa[i];
                res.assign(n, -1);
                for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];
for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre>
                for (int i = 0; i < n; i++) dom[i] = res[i];</pre>
};
```

9 DP

9.1 LCS [5781cf]

```
int main() {
         int m, n; cin >> m >> n;
         string s1, s2; cin >> s1 >> s2;
int L = 0;
        tnt L = 0,
vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0));
for (int i = 1; i <= m; i++) {
    for (int j = 1; j <= n; j++) {
        if (s1[i - 1] == s2[j - 1])
            dp[i][j] = dp[i - 1][j - 1] + 1;
}</pre>
                                    dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
       fint length = dp[m][n]; cout << length << "\n";
string s(length, 'c'); // backtracking
while (m >= 1 && n >= 1) {
    if (s1[m - 1] == s2[n - 1]) {
        s[length - 1] = s1[m - 1];
        m--, n--, length--;
}
                 else {
    if (dp[m - 1][n] > dp[m][n - 1]) m--;
         cout << s << "\n";
```

9.2 LIS [66d09f]

```
int main() {
     int n; cin >> n;
vector <int> v(n);
     for (int i = 0; i < n; i++) cin >> v[i];
```

```
int dp[n]: vector<int> stk:
        stk.push_back(v[0]);
        dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) {
    if (v[i] > stk.back()) {
                     stk.push_back(v[i]);
                     dp[i] = ++L;
              } else {
                    auto it
                              = lower_bound(stk.begin(), stk.end(), v[i]);
                     *it = v[i]; dp[i] = it - stk.begin() + 1;
             }
        vector < int > ans; cout << L << " | n";
for (int i = n - 1; i >= 0; i--) {
    if (dp[i] == L) {
                     ans.push_back(v[i]), L--;
        for (auto i : ans) cout << i <<</pre>
 9.3 Edit Distance [308023]
 int main() {
        string s1, s2; cin >> s1 >> s2;
int n1 = s1.size(), n2 = s2.size();
        // dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元
        vector<int> dp(n2 + 1);
        vector<int> dp(n2 + 1);
iota(dp.begin(), dp.end(), 0);
for (int i = 1; i <= n1; i++) {
    vector<int> cur(n2 + 1); cur[0] = i;
    for (int j = 1; j <= n2; j++) {
        if (s1[i - 1] == s2[j - 1]) {
            cur[j] = dp[j - 1];
        lelse {</pre>
                     } else {
                          // s1 新增等價於 s2 砍掉
                            // dp[i][j] = min(s2 新增, 修改, s1 新增);
                           cur[j]
                                    -
= min({cur[j - 1], dp[j - 1], dp[j]}) + 1;
                    }
              swap(dp, cur);
        cout << dp[n2] << "\n";
 9.4 Bitmask [a626f9]
 void hamiltonianPath(){
       int n, m; cin >> n >> m;
vector adj(n, vector <int >());
for (int i = 0; i < m; i++) {
   int u, v; cin >> u >> v;
              adj[--v].push_back(--u);
        // 以...為終點,走過...
        vector dp(n, vector<int>(findBit(n)));
dp[0][1] = 1;
       ap[0][1] = 1;
for (int mask = 1; mask < findBit(n); mask++) {
    if ((mask & 1) == 0) continue;
    for (int i = 0; i < n; i++) {
        if ((mask & findBit(i)) == 0) continue;
        if (i == n - 1 && mask != findBit(n) - 1) continue;
        int pre_mask = mask ^ findBit(i);
        for (int i : adi[i]) {</pre>
                     for (int j : adj[i]) {
   if ((pre_mask & findBit(j)) == 0) continue;
                           dp[i][mask
                                   ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
             }
        cout << dp[n - 1][findBit(n) - 1] << "\n";
 void elevatorRides() {
        int n, x; cin >> n >> x; vector<int> a(n);
for (int i = 0; i < n; i++) cin >> a[i];
vector<array<int, 2>> dp(findBit(n));
       } else if (dp[pre_mask
                           | (dp[pre_mask]
|][0] + 1 < dp[mask][0] || dp[pre_mask][0]
| + 1 == dp[mask][0] && a[i] < dp[mask][1]) {
| dp[mask][0] = dp[pre_mask][0] + 1;
| dp[mask][1] = a[i];
              }
        cout << dp[findBit(n) - 1][0] << "\n";
1
```

9.5 Projects [0942aa]

9.6 Removal Game [7bb56b]

9.7 CF Example [7d37ea]

```
// 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
// 請問在線段不重複的情況下,最多獲得幾分 int main() {
     int n, m;
     cin >> n >> m;
     // 記錄每點有幾個線段
      // 再一個紀錄,包含這個點的左界
     cnt[l]++;
cnt[r + 1]--;
     for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
     for (int i = n; i >= 2; i--) {
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
      vector<int> dp(n + 1);
     dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
           dp[i] = cnt[i];
if (l_side[i] != inf) {
    dp[i] += dp[l_side[i] - 1];
           dp[i] = max(dp[i], dp[i - 1]);
     cout << dp[n] << "\n";
// CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
// 再加上 max(bi) - min(bi)

int main(){
    int n, k, ans = 0; cin >> n >> k;
    vector<pii> v(n + 1);
    for (int i = 1; i <= n; i++) {
        int a, b; cin >> a >> b;
        v[i] = {a, b};
        if (a = k) > a >> b;
           if (a <= k) ans = 1;
```

9.8 斜率優化 [a6e320]

```
constexpr ll Inf =
// dp[i] = min(f[j] * s[i] + dp[j])
// y = m
// y =
struct Line {
     ll m, b;
ll m, b;
Line(ll m = 0, ll b = Inf) : m(m), b(b) {}
ll eval(ll x) const { return m * x + b; }
struct LiChaoSeg { // 取 max 再變換就好
      vector<Line> info;
      LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
           info.assign(4 << __lg(n), Line());</pre>
      void update(Line line, int node, int l, int r) {
   int m = (l + r) / 2;
   bool left = line.eval(l) < info[node].eval(l);</pre>
           bool mid = line.eval(m) < info[node].eval(m);</pre>
           if (mid) swap(info[node], line); // 如果新線段比較好
           if (r - l == 1) return;
else if (left != mid) update(line, 2 * node, l, m);
           // 代表左半有交點
           else update(line, 2 * node + 1, m, r);
           // 代表如果有交點一定在右半
     yoid add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
    if (r - l == 1) return info[node].eval(x);
    int m = (l + r) / 2;
           if (x < m) return
                  min(info[node].eval(x), query(x, 2 * node, l, m));
                  info[node].eval(x), query(x, 2 * node + 1, m, r));
      ill query(int x) { return query(x, 1, 0, n); }
```

10 Geometry

10.1 Basic [d41d8c]

```
#include <bits/stdc++.h>
using namespace std;
using i64 = long long;
template < class T>
struct Point {
     T x;
     Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) \{ \}
     template < class U>
     operator Point<U>()
         return Point<U>(U(x), U(y));
     Point & operator += (const Point &p) & {
         x += p.x;
y += p.y;
return *this;
     Point & operator -= (const Point &p) & {
         x \leftarrow p.x;
          return *this:
     Point & operator *= (const T &v) & {
         x *= v;
y *= v;
return *this;
     Point & operator /= (const T &v) & {
         x /= v:
         y /= v;
          return *this;
```

```
Point operator - () const {
          return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
     friend Point operator - (Point a, const Point &b) {
          return a -= b;
     friend Point operator*(Point a, const T &b) {
    return a *= b;
     friend Point operator/(Point a, const T &b) {
          return a /= b;
     friend Point operator*(const T &a, Point b) {
   return b *= a;
     friend bool operator == (const Point &a, const Point &b) {
          return a.x == b.x && a.y == b.y;
     friend istream & operator >> (istream &is, Point &p) {
          return is >> p.x >> p.v:
     friend ostream & operator < < (ostream & os, const Point & p) {
   return os << "(" << p.x << ", " << p.y << ")";</pre>
template < class T>
struct Line {
    Point<T>
     Point < T > b;
     Line(const Point<T> &a_ = Point<T>()
          , const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
template < class T>
T dot(const Point<T> &a, const Point<T> &b) {
   return a.x * b.x + a.y * b.y;
template < class T>
T cross(const Point<T> &a, const Point<T> &b) {
     return a.x * b.y - a.y * b.x;
}
template < class T>
T square(const Point < T > &p) {
    return dot(p, p);
template < class T>
double length(const Point<T> &p) {
    return sqrt(square(p));
template < class T>
double length(const Line<T> &l) {
    return length(l.a - l.b);
template < class T>
Point<T> normalize(const Point<T> &p) {
    return p / length(p);
bool parallel(const Line<T> &l1, const Line<T> &l2) {
   return cross(l1.b - l1.a, l2.b - l2.a) == θ;
template < class T>
double distance(const Point<T> &a, const Point<T> &b) {
    return length(a - b);
}
template < class T >
double distancePL(const Point<T> &p, const Line<T> &l) {
   return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0) {
     return distance(p, l.a);</pre>
     if (dot(p - l.b, l.a - l.b) < 0) {
    return distance(p, l.b);</pre>
     return distancePL(p, l);
Point<T> rotate(const Point<T> &a) {
    return Point(-a.y, a.x);
template < class T>
int sgn(const Point<T> &a) {
     return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
```

```
template < class T>
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
    return cross(l.b - l.a, p - l.a) > 0;
template < class T >
Point < T
       template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
    return cross(p - l.a, l.b - l.a) == 0 &&
        min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)</pre>
                     (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
     (const Point<T> &a, const vector<Point<T>> &p) {
       int n = p.size();
for (int i = 0; i < n; i++) {
    if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {</pre>
                    return true;
       }
       int t = 0;
for (int i = 0; i < n; i++) {</pre>
             auto u = p[i];
              auto v = p[(i + 1) % n];
              if (u.x < a.x
                     && v.x >= a.x && pointOnLineLeft(a, Line(v, u))) {
             if (u.x >= a.x
                      && v.x < a.x && pointOnLineLeft(a, Line(u, v))) {
                    t ^= 1;
             }
      }
       return t == 1;
}
// 0 : not intersect
tuple < int , Point < T > , Point < T >> segmentIntersection
       (const Line<T> &l1, const Line<T> &l2) {
if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.
    return {0, Point<T>(), Point<T>()};
       if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x)) {
    return {0, Point<T>(), Point<T>()};
       if (max(l1.a.y, l1.b.y) < min(l2.a.y, l
    return {0, Point<T>(), Point<T>()};
       if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y)) {
    return {0, Point<T>(), Point<T>()};
       if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
    if (cross(l1.b - l1.a, l2.a - l1.a) != 0) {
        return {0, Point<T>(), Point<T>()};
             } else {
                    auto maxx1 = max(l1.a.x, l1.b.x);
auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
                    auto miny1 = min(l1.a.y, l1.b.y);
auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
                    auto maxy2 = max(l2.a.y, l2.b.y);
auto miny2 = min(l2.a.y, l2.b.y);
Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
if (!pointOnSegment(p1, l1)) {
                          swap(p1.y, p2.y);
                    if (p1 == p2) {
                          return {3, p1, p2};
                    } else {
                          return {2, p1, p2};
             }
       auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
```

```
Point p = lineIntersection(l1, l2); if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
         return {1, p, p};
    } else {
    return {3, p, p};
    }
}
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
   if (get<0>(segmentIntersection(l1, l2)) != 0) {
         return 0.0:
    return min({distancePS(l1.a, l2), distancePS(l1
    .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
template < class T>
bool segmentInPolygon
     (const Line<T> &l, const vector<Point<T>> &p) {
    int n = p.size();
    if (!pointInPolygon(l.a, p)) {
         return false;
    if (!pointInPolygon(l.b, p)) {
         return false;
    for (int i = 0; i < n; i++) {
    auto u = p[i];</pre>
         auto v = p[(i + 1) % n];
auto w = p[(i + 2) % n];
auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
         if (t == 1) {
    return false;
         if (t == 0) {
             continue;
         if (t == 2) {
             if (pointOnSegment(v, l) && v != l.a && v != l.b) {
   if (cross(v - u, w - v) > 0) {
      return false;
}
                  }
         || pointOnLineLeft(l.b, Line(v, u))) {
             if (pointOnLineleft(w, l)
                                && pointOnLineLeft
                                (w, Line(u, v))) {
return false;
                           }
                      } else {
    if (pointOnLineLeft(w, l)
                                || pointOnLineLeft
                                (w, Line(u, v))) {
return false;
                 return false;
                       } else {
                           if (pointOnLineLeft(w, Line(l.b, l.a))
                                || pointOnLineLeft
                                (w, Line(u, v))) {
return false;
                           }
                      }
                  } else {
                      (w, Line(u, v))) {
return false;
                      (w, Line(u, v))) {
return false;
                           }
                      }
                 }
             }
        }
    return true:
template < class T >
```

```
vector<Point<T>> hp(vector<Line<T>> lines) {
    auto d1 = l1.b - l1.a;
auto d2 = l2.b - l2.a;
        if (sgn(d1) != sgn(d2)) {
    return sgn(d1) == 1;
        return cross(d1, d2) > 0;
    }):
    deque<Line<T>> ls;
    deque < Point < T >> ps;
    for (auto l : lines) {
        if (ls.empty()) {
             ls.push_back(l);
             continue:
        while (!ps.empty() && !pointOnLineLeft(ps.back(), l)) {
             ps.pop_back();
             ls.pop_back();
        while (!ps.empty() && !pointOnLineLeft(ps[0], l)) {
             ps.pop_front();
ls.pop_front();
        if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
             if (dot
                  (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                 if (!pointOnLineLeft(ls.back().a, l)) {
                      assert(ls.size() == 1);
                      ls[0] = l;
                 continue;
             return {}:
        ps.push_back(lineIntersection(ls.back(), l));
ls.push_back(l);
    while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0])) {
        ps.pop_back()
        ls.pop_back();
    if (ls.size() <= 2) {</pre>
         return {};
    ps.push_back(lineIntersection(ls[0], ls.back()));
    return vector(ps.begin(), ps.end());
using P = Point<i64>;
10.2 Convex Hull [01a63e]
int main() {
```

```
int n; cin >> n;
vector<P> P(n), U, L;
for (int i = 0; i < n; i++) {
for (int i = 0;
    cin >> P[i];
sort(P.begin(), P
      .end(), [](const Point<i64> &a, const Point<i64> &b) {
return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
for (int i = 0; i < n; i++) {
    while (L.size() >= 2 && cross(L.back() -
        L[L.size() - 2], P[i] - L[L.size() - 2]) < 0LL) {</pre>
             L.pop_back();
       while (U.size() >= 2 && cross(U.back()
               - U[U.size() - 2], P[i] - U[U.size() - 2]) > 0LL){
             U.pop back();
       L.push_back(P[i]);
      U.push_back(P[i]);
cout << L.size() + U.size() - 2 << "|n";
for (int i = 0; i < L.size() - 1; i++) {
    cout << L[i].x << " " << L[i].y << "|n";</pre>
for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << " | n";</pre>
}
```

10.3 MinEuclideanDistance [469a8f]

```
template < class T>
 distanceSquare(const Point<T> &a, const Point<T> &b) {
    return square(a - b);
void solve() {
   int n; cin >> n;
```

```
constexpr i64 inf = 8e18;
vector<Point<i64>> a(n);
for (int i = 0; i < n; i++) {</pre>
      i64 x, y;
cin >> x >> y;
      a[i] = Point < i64 > (x, y);
struct sortY {
      bool operator()
            (const Point<i64> &a, const Point<i64> &b) const {
            return a.y < b.y;</pre>
      }
struct sortXY {
      bool operator()
            (const Point<i64> &a, const Point<i64> &b) const {
if (a.x == b.x) return a.y < b.y;
else return a.x < b.x;</pre>
     }
};
sort(a.begin(), a.end(), sortXY());
vector<Point<i64>> t(n);
auto devide = [&](auto &&self, int l, int r) -> i64 {
   if (l == r) return inf;
   int m = (l + r) / 2;
      i64 ans = min(self(self, l, m), self(self, m + 1, r));
      i64 midval = a[m].x;
     i64 midva( - \( \) ...,
i64 p = 0;
for (int i = l; i <= r; i++) {
   if ((midval - a[i].x) * (midval - a[i].x) <= ans) {
        t[p++] = a[i];
   }</pre>
      sort(t.begin(), t.begin() + p, sortY());
for (int i = 0; i < p; i++){</pre>
            for (int j = i + 1; j < p; j++) {
    ans = min(ans, distanceSquare(t[i], t[j]));
    if ((t[i].y -</pre>
                            t[j].y) * (t[i].y - t[j].y) > ans) break;
            }
      return ans;
cout << devide(devide, 0, n - 1) << "\n";</pre>
```

10.4 LatticePoints [7750d6]