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Basic 1

1.1 Install VScode [d41d8c]

```
|// 如何安裝 vscode
 // 1. 下載 vscode & msys2
// 2. 在跳出的 terminal 中 / 或打開 ucrt64,打上
"pacman -S --needed base-devel mingw-w64-x86_64-toolchain"
// 3. 環境變數加上 C:\\msys64\\ucrt64\\bin
// 4. 重開 vscode, 載 C/C++, 運行, 編譯器選擇 g++
 // 5. 打開 settings -> compiler -> add compilerPath
        -> 在 "" 裡打上 C:\\msys64\\ucrt64\\bin\\g++.exe
```

1.2 Default Code [d41d8c]

```
#include <bits/stdc++.h>
// #pragma GCC target("popcnt")
  / C++ 20 vector grammer will not work
using namespace std;
using ll = long long;
void solve() {
}
int main() {
     ios_base::sync_with_stdio(false);
     cin.tie(nullptr);
     int t = 1;
cin >> t;
while (t--) {
         solve();
}
```

1.3 Compare Fuction [d41d8c]

```
|// 1. sort, 二分搜刻在函式內 lambda 就好
// 2. priority queue 小到大是 >, set 是 <
// 3. set 不能 = , multiset 必須 =
// 4. 確保每個成員都要比到
// 5. pbds_multiset 不要用 lower_bound
// 6. 如果要用 find, 插入 inf 後使用 upper_bound
// 7. multiset 可以跟 set 一樣使用, 但請注意第 3、4 點
```

```
auto cmp = [](int i, int j) { return i > j; };
priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
vector<int> a {1, 2, 5, 4, 3}; // 小心不要改到 a auto cmp = [&a](int i, int j) { return a[i] > a[j]; }; priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
```

1.4 Pbds [d41d8c]

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < class T>
using pbds_set = tree<T, null_type,
    less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template<class T>
```

1.5 Double [b44e11]

```
struct D {
   double x;
      counte x;
constexpr static double eps = 1e-12;
D() : x{0.0} {}
D(double v) : x{v} {}
double val() const { return x; }
explicit operator double() const { return x; }
D operator -() const {
    return D(-x);
       D &operator+=(const D &rhs) & {
               x += rhs.x; return *this;
       D &operator -= (const D &rhs) & {
    x -= rhs.x; return *this;
       D & operator *= (const D & rhs) & {
              x *= rhs.x; return *this;
       D & operator/=(const D &rhs) & {
    assert(fabs(rhs.x) > eps);
    x /= rhs.x; return *this;
       friend D operator+(D lhs, const D &rhs) {
    return lhs += rhs;
       friend D operator - (D lhs, const D &rhs) {
    return lhs -= rhs;
       friend D operator*(D lhs, const D &rhs) {
   return lhs *= rhs;
       friend D operator/(D lhs, const D &rhs) {
   return lhs /= rhs;
       friend bool operator <(const D &lhs, const D &rhs) {
   return lhs.x - rhs.x < -eps;</pre>
       friend bool operator>(const D &lhs, const D &rhs) {
   return lhs.x - rhs.x > eps;
        friend bool operator==(const D &lhs, const D &rhs) {
              return fabs(lhs.x - rhs.x) < eps;</pre>
       friend bool operator <= (const D &lhs, const D &rhs) {
  return lhs < rhs || lhs == rhs;</pre>
       riend bool operator >= (const D &lhs, const D &rhs) {
  return lhs > rhs || lhs == rhs;
       friend bool operator!=(const D &lhs, const D &rhs) {
  return !(lhs == rhs);
       friend istream &operator>>(istream &is, D &a) {
   double v; is >> v; a = D(v); return is;
      friend ostream & operator << (ostream & os, const D & a) {
    return os << fixed << setprecision(10) << a.val()
    + (a.val() > 0 ? eps : a.val() < 0 ? -eps : 0);
} // eps should < precision</pre>
```

1.6 Rng [401544]

};

```
mt19937_64 rng
     (chrono::steady_clock::now().time_since_epoch().count());
ll x = rng(); shuffle(a.begin(), a.end(), rng);
```

2 Graph

2.1 DFS And BFS [e2d856]

```
int main() {
  int n:
  vector<vector<int>> adj(n);
  vis[u] = true;
```

```
for (auto v: adj[u]) {
    self(self, v);
       }
dfs(dfs, 0);
vector<int> depth(n, 1e9);
queue < int > q;
auto bfs = [&](auto self, int s) -> void {
   vis[s] = true, depth[s] = 0;
       while (!q.empty()) {
              int u = q.front(); q.pop();
for (auto v : adj[u]) {
   if (vis[v]) continue;
                    vis[v] = true;
depth[v] = depth[u] + 1;
q.push(v);
              }
      }
bfs(bfs, 0);
```

2.2 Prim [3a3805]

```
auto prim =
                           [&](int n, vector<vector<pair<int, int>>> &adj) -> bool {
int node_sz = 0;
                         priority_queue
prio
                          while (!pq.empty()) {
   auto [u, w] = pq.top(); pq.pop();
   if (vis[u]) continue;
                                                  vis[u] = true;
                                                  node_sz++;
for (auto v : adj[u]) {
                                                                         if (!vis[v.first])
                                                                                                   pg.emplace(v.second, v.first);
                                                  }
                           if (node_sz == n) return true;
};
```

2.3 BellmanFord [430ded]

```
/ 用 Bellman Ford 找負環
int main() {
   int n, m; cin >> n >> m;
                                    for (int i = 0; i < m; i++) {
   int u, v, w; cin >> u >> v >> w;
   u--, v--; e.push_back({u, v, w});
                                    for (auto [u, v, w] : e) {
    dis[v] = dis[u] + w;
    dis[v] = dis[v] + w;
    dis[v] = d
                                                                                                                                                 par[v] = u;
if (i == n) t = v;
                                                                        }
                                    if (t == -1) { cout << "NO|n"; return; }
for (int i = 1; i < n; i++) t = par[t];
vector <int> ans {t};
                                       int i = t;
                                       do {
                                                                         i = par[i];
                                     ans.push_back(i);
} while (i != t);
                                     reverse(ans.begin(), ans.end());

cout << "YES\n";

for (auto x : ans) cout << x + 1 << " ";
```

2.4 FloydWarshall [3f61a4]

```
nstexpr ll inf = 1e18;
void FloydWarshall(int n, int m) {
   int n, m; cin >> n >> m;
       tht n, m; ctn >> m;
vector < int >> dis(n, vector < int >(n, inf));
for (int i = 0; i < m; i++) {
   int u, v, w; cin >> u >> v >> w;
   dis[u][v] = min(dis[u][v], w);
               dis[v][u] = min(dis[v][u], w);
       for (int i = 0; i < n; i++) dis[i][i] = 0;</pre>
               (int k = 0; k < n; k++) {
for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
        dis[i][j</pre>
                                        ] = min(dis[i][j], dis[i][k] + dis[k][j]);
                       }
               }
```

```
const int N = 500; // Floyd 封包
void Floyd(int n, vector<bitset<N>> &dp) {
      for (int k = 0; k < n; k++)
    for (int i = 0; i < n; i++)
        if (dp[i][k])</pre>
                       dp[i] |= dp[k];
}
```

2.5 Euler [4177dc]

```
// 1. 無向圖是歐拉圖:
// 非零度頂點是連通的
// 頂點的度數都是偶數
// 2. 無向圖是半歐拉圖(有路沒有環):
// 非零度頂點是連通的
// 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
// 非零度頂點是強連通的
// 每個頂點的入度和出度相等
// 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
| // 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
// 其他頂點的入度和出度相等
 vector<int> ans;
auto dfs = [&](auto &&self, int u) -> void {
    while (g[u].size()) {
   int v = *g[u].begin();
       g[u].erase(v);
       self(self, v);
    ans.push_back(u);
dfs(dfs, 0);
reverse(ans.begin(), ans.end());
```

2.6 DSU [749620]

```
struct DSU {
      vector < int > boss, siz;
      DSU() {}
DSU(int n_) { init(n_); }
      void init(int n_) {
    n = n_; boss.resize(n);
             iota(boss.begin(), boss.end(), 0);
            siz.assign(n, 1);
      int find(int x) {
   if (boss[x] == x) return x;
   return boss[x] = find(boss[x]);
      bool same(int x, int y) {
    return find(x) == find(y);
       bool merge(int x, int y) {
            x = find(x); y = find(y);
if (x == y) return false;
if (siz[x] < siz[y]) swap(x, y);
             siz[x] += siz[y];
            boss[y] = x;
             return true;
      int size(int x)
             return siz[find(x)];
};
struct DSU {
      int n;
      vector<int> boss, siz, stk;
      DSU() {}
      DSU(jnt n_) { init(n_); }
void init(int n_) {
            n = n_;
             boss.resize(n);
            iota(boss.begin(), boss.end(), 0);
siz.assign(n, 1);
             stk.clear();
      int find(int x) {
   return x == boss[x] ? x : find(boss[x]);
      bool same(int x, int y) {
    return find(x) == find(y);
      bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (stz[x] < stz[y]) swap(x, y);
    if [stz]</pre>
             siz[x] += siz[y];
boss[y] = x;
```

```
stk.push_back(y);
              return true;
       void undo(int x) {
              while (stk.size() > x) {
                    int y = stk.back();
                     stk.pop_back();
                     siz[boss[y]] -= siz[y];
                     boss[y] = y;
              }
       int size(int x) {
    return siz[find(x)];
};
2.7 SCC [5d3e16]
struct SCC {
       int n, cur, cnt;
vector < vector < int >> adj;
vector < int >> stk, dfn, low, bel;
SCC(int n = 0) { init(n_); }
       void init(int n_) {
             n = n_;
adj.assign(n, {});
              dfn.assign(n, -1);
low.resize(n);
              bel.assign(n, -1);
              stk.clear();
cur = cnt = 0;
       void addEdge(int u, int v) {
   adj[u].push_back(v);
       void dfs(int x) {
    dfn[x] = low[x] = cur++;
              stk.push_back(x);
              for (auto y : adj[x]) {
    if (dfn[y] == -1) {
                    dfs(y);
  dfs(y);
  low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
  low[x] = min(low[x], dfn[y]);
                     }
              if (dfn[x] == low[x]) {
                     int y;
do {
                            y = stk.back();
                    bel[y] = cnt;
stk.pop_back();
} while (y != x);
                     cnt++;
             }
       vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
              return bel;
       struct Graph {
              int n;
              vector<pair<int, int>> edges;
              vector < int > siz;
vector < int > cnte;
       Graph compress() {
              Graph g;
g.n = cnt;
              g.siz.resize(cnt);
              g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {</pre>
                    g.siz[bel[i]]++;
for (auto j : adj[i]) {
    if (bel[i] != bel[j]) {
        g.edges.emplace_back(bel[i], bel[j]);
    } else {
                                  g.cnte[bel[i]]++;
                    }
              return q;
};
2.8 VBCC [170604]
struct VBCC {
       int n, cur;
vector<vector<int>> adj;
       vector<int> dfn, low, parent;
       vector <tnt> din, tow, parent,
vector <bool>
    is_cut;
VBCC(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_;
    adj.assign(n, {});

dfaccion(n_ 1);
              dfn.assign(n, -1);
low.resize(n);
```

parent.assign(n, -1);

is_cut.assign(n, false); void addEdge(int u, int v) { adj[u].push_back(v); adj[v].push_back(u); void dfs(int x) { int children dfn[x] = low[x] = cur++; for (int v : adj[x]) { if (dfn[v] == -1) { children++; parent[v] = x; dfs(v); low[x] = min(low[x], low[v]); if (parent[x] != -1 && low[v] >= dfn[x]) { } else if (v != parent[x]) { low[x] = min(low[x], dfn[v]); if (parent[x] == -1 && children > 1) { is_cut[x] = true; } } }; 2.9 EBCC [59d8ca] struct EBCC { // CF/contest/1986/pF int n, cur, cnt; vector<vector<int>> adj; vector<int> stk, dfn, low, bel; vector<pair<int, int>> bridges; // 關鍵邊 EBCC(int n_ = 0) { init(n_); } void init(int n_) { n = n_; adj.assign(n, {}); dfn.assign(n, -1); low.resize(n); bel.assign(n, -1); stk.clear(); bridges.clear(); cur = cnt = 0; void addEdge(int u, int v) { adj[u].push_back(v); adj[v].push_back(u); void dfs(int x, int p) { dfn[x] = low[x] = cur++; stk.push_back(x); for (auto y : adj[x]) { if (y == p) continue; if (dfn[y] == -1) { dfs(y, x); low[x] = min(low[x], low[y]); if (low[y] > dfn[x]) { bridges.emplace_back(x, y); } else if (bel[y] == -1) { low[x] = min(low[x], dfn[y]); if (dfn[x] == low[x]) { int y; do { y = stk.back(); bel[y] = cnt; stk.pop_back(); while (y != x); cnt++; } vector < int > work() { // not connected for (int i = 0; i < n; i++) { if (dfn[i] == -1) {</pre> dfs(i, -1); } return bel; struct Graph { vector<pair<int, int>> edges; vector<int> siz; // BCC 內節點數 vector<int> cnte; // BCC 內邊數 Graph compress() { Graph g; g.n = cnt;

g.siz.resize(cnt);

```
g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;
    for (auto j : adj[i]) {
        if (bel[i] < bel[j]) {
            g.edges.emplace_back(bel[i], bel[j]);
        } else if (i < j) {
            g.cnte[bel[i]]++;
        }
    }
}
return g;
}
</pre>
```

2.10 2-SAT [eeddc1]

```
// CSES Giant Pizza
struct TwoSat {
     int n; vector<vector<int>> e;
      TwoSat(int n) : n(n), e(2 * n), ans(n) {}
void addClause(int u, bool f, int v, bool g) {
    e[2 * u + !f].push_back(2 * v + g);
    e[2 * v + !g].push_back(2 * u + f);
      bool satisfiable() {
             vector<int
                    > id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
             vector<int> stk;
             int now = 0, cnt = 0;
function < void(int) > tarjan = [&](int u) {
                   stk.push_back(u);

dfn[u] = low[u] = now++;

for (auto v : e[u]) {
                         if (dfn[v] == -1) {
                         tarjan(v);
  low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in st
  low[u] = min(low[u], dfn[v]);
                         }
                   if (dfn[u] == low[u]) {
                         int v;
do {
                                v = stk.back();
                               stk.pop_back();
id[v] = cnt;
                         } while (v != u);
                          ++cnt:
                  }
            vector<bool> answer() { return ans; }
int main() {
      int m, n; cin >> m >> n;
TwoSat ts(n);
      for (int i = 0; i < m; ++i) {
   int u, v; char x, y;
   cin >> x >> u >> y >> v;
   ts.addClause(u - 1, x == '+', v - 1, y == '+');
      if (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";</pre>
      else cout << "IMPOSSIBLE\n";</pre>
3
```

2.11 Funtional Graph [85c464]

```
constexpr int N = 2e5 + 5;
int cht[N][31]; // 倍增表, 放外面不然 TLE
struct FuntionalGraph {
   int n, cnt;
   vector int > g, bel, id, len, in, top;
   FuntionalGraph(): n(0) {}
   FuntionalGraph(vector int > g_) { init(g_); }
   void init(vector int > g_) { init(g_); }
   in = g_. size(); cnt = 0;
        g = g_; bel.assign(n, -1);
        id.resize(n); len.clear();
        in.assign(n, 0); top.assign(n, -1);
        build();
   }
   void build() {
        for (int i = 0; i < n; i++) {
            cht[i][0] = g[i];
            in[g[i]]++;
        }
        for (int i = 1; i <= 30; i++)
            for (int u = 0; u < n; u++)
            cht[u][i] = cht[cht[u][i - 1]][i - 1];
        cht[u][i] = cht[cht[u][i - 1]][i - 1];
        chtild in the context of the contex
```

```
for (int i = 0; i < n; i++)
   if (in[i] == 0) label(i);
for (int i = 0; i < n; i++)
   if (top[i] == -1) label(i);</pre>
         void label(int u) {
                vector<int> p; int cur = u;
while (top[cur] == -1) {
                        top[cur] = u;
                        p.push_back(cur);
                        cur = g[cur];
                 auto s = std::find(p.begin(), p.end(), cur);
                auto s = std::tind(p.begin(), p.end(), cur);
vector <int> cyc(s, p.end());
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {
    bel[cyc[i]] = cnt;
    id[cyc[i]] = i;
}</pre>
                 cnt++; len.push_back(cyc.size());
                for (int i = p.size() - 1; i > 0; i--)
   id[p[i - 1]] = id[p[i]] - 1;
         int jump(int u, int k) {
    for (int b = 0; k > 0; b++){
                       if (k & 1) u = cht[u][b];
                        k >>= 1;
                 return u;
        }
}:
```

3 Data Structure

3.1 BIT [d41d8c]

```
| template < typename T>
 struct Fenwick { // 全部以 0 based 使用
int n; vector<T> a;
Fenwick(int n_ = 0) { init(n_); }
        void init(int n_) {
              n = n;
              a.assign(n, T{});
        void add(int x, const T &v) {
   for (int i = x + 1; i <= n; i += i & -i) {
      a[i - 1] = a[i - 1] + v;
}</pre>
        T sum(int x) { // 左閉右開查詢
               T ans{};
              for (int i = x; i > 0; i -= i & -i) {
    ans = ans + a[i - 1];
        TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
         int select(const T &k, int start = 0) {
              int x = 0; T cur = -sum(start) > k
int x = 0; T cur = -sum(start);
for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n && cur + a[x + i - 1] <= k) {
                            x += i;
                            cur = cur + a[x - 1];
                     }
               return x;
       }
 template < class T>
 struct TwoDFenwick { // 全部以 0 based 使用
        int nx, ny; // row, col 個數 vector<vector<T>> a;
        TwoDFenwick(int nx_{=} = 0, int ny_{=} = 0) {
              init(nx_, ny_);
        void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
        for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        a[i - 1][j - 1] = a[i - 1][j - 1] + v;
    }
}</pre>
              }
       }
        T sum(int x, int y) { // 左閉右開查詢
              Im(int x, che ,,
T ans{};
for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans + a[i - 1][j - 1];
}
              return ans;
        T rangeSum
               (int lx, int ly, int rx, int ry) { // 左閉右開查詢
```

3.2 RangeBit [d41d8c]

```
template < class T>
struct rangeFenwick { // 全部以 0 based 使用
             int n;
vector<T> d, di;
               rangeFenwick(int n_ = 0) { init(n_); }
              void init(int n_) {
    n = n_;
                             d.assign(n, T{});
                            di.assign(n, T{});
             void add(int x, const T &v) {
   T vi = v * (x + 1);
   for (int i = x + 1; i <= n; i += i & -i) {
      d[i - 1] = d[i - 1] + v;
      di[i - 1] = di[i - 1] + v;
}</pre>
                            }
               void rangeAdd(int l, int r, const T &v) {
                            add(l, v); add(r, -v);
             T sum(int x) { // 左閉右開查詢
                            T ans{};
                            for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
                            return ans;
             TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
               int select(const T &k, int start = 0) {
                            | 找到最小的 x, 使得 sum(x + 1) - sum(start) > k
| int x = 0; T cur = -sum(start);
| for (int i = 1 << __lg(n); i; i /= 2) {
| if (x + i <= n) {
                                                         x += i;
                                                                        cur = cur + val;
                                                         }
                                          }
                             return x:
            }
template < class T>
struct rangeTwoDFenwick { // 全部以 0 based 使用
             int nx, ny; // row, col 個數
vector <vector <T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
                            init(nx_, ny_);
              void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector (Ty(ny, T{}));
    ...
    ...
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                            di.assign(nx, vector<T>(ny, T{}));
dj.assign(nx, vector<T>(ny, T{}));
dij.assign(nx, vector<T>(ny, T{}));
             }
void add(int x, int y, const T &v) {
    T vi = v * (x + 1);
    T vj = v * (y + 1);
    T vij = v * (x + 1) * (y + 1);
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            d[i - 1][j - 1] = d[i - 1][j - 1] + v;
            di[i - 1][j - 1] = dj[i - 1][j - 1] + vi;
            dj[i - 1][i - 1] = dj[i - 1][j - 1] + vj;
            dij[i - 1][i - 1] = dj[i - 1][j - 1] + vj;
            dij[i - 1][i - 1] = dj[i - 1][i - 1] + vj</pre>
                                                          dij[i - 1][j - 1] = dij[i -
                                                                                                                                                                1][i -
                                                                                                                                                                                         1] + vij;
                                          }
                           }
               void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
                            add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
              T sum(int x, int y) { // 左閉右開查詢
                             T`ans{};
                            for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans
                                                          + T(x * y + x + y + 1) * d[i - 1][j - 1]; \\ ans = ans - T(y + 1) * di[i - 1][j - 1]; \\ ans = ans - T(x + 1) * dj[i - 1][j - 1]; \\
                                                           ans = ans + dij[i - 1][j
                                          }
                             return ans;
```

3.3 SegmentTree [d41d8c]

```
| template < class Info >
 Seg(int n_, Info v_ = Info()) { init(n_, v_); }
       template <class T >
Seg(vector < T > init_) { init(init_); }
void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
}
        template < class T>
        void init(vector<T> init_) {
             n = init_.size();
info.assign(4 << __lg(n), Info());</pre>
              function <void(
   int, int, int)> build = [&](int p, int l, int r) {
   if (r - l == 1) {
                          info[p] = init_[l];
                          return:
                    int m = (l + r) / 2;
                   build(p * 2, l, m);
build(p * 2 + 1, m, r);
                   pull(p);
             build(1, 0, n);
        void pull(int p) {
    info[p] = info[p * 2] + info[p * 2 + 1];
        void modify(int p, int l, int r, int x, const Info &v) {
             if (r - l == 1) {
    info[p] = v; return;
             int m = (l + r) / 2;
if (x < m) modify(2 * p, l, m, x, v);
else modify(2 * p + 1, m, r, x, v);</pre>
             pull(p);
        void modify(int p, const Info &i) {
             modify(1, 0, n, p, i);
       Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    return query(p *</pre>
             return query(p
                    2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
       Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
        template < class F > // 尋找區間內,第一個符合條件的
        int findFirst
             (int p, int l, int r, int x, int y, F &&pred) {
  if (l >= y || r <= x)
     return -1;
  if (l >= x && r <= y && !pred(info[p]))
     return -1;
}</pre>
             if (r - l == 1)
             return l;
int m = (l + r) / 2;
int res = findFirst(2 * p, l, m, x, y, pred);
             if (res == -1)
    res = findFirst(2 * p + 1, m, r, x, y, pred);
              return res:
       template < class F> // 若要找 last,先右子樹遞迴即可
int findFirst(int l, int r, F & & pred) {
    return findFirst(1, 0, n, l, r, pred);
     ---define structure and info plus---
 struct Info {
        int sum = 0:
 Info operator+(const Info &a, const Info &b) {
        return { a.n + b.n, a.sum + b.sum };
```

3.4 Lazy Segment Tree [d41d8c]

```
| template < class Info, class Tag >
| struct LazySeg { // 左閉右開寫法
    int n;
    vector < Info > info;
    vector < Tag > tag;
    LazySeg() : n(0) {}
    LazySeg(int n_, Info v_ = Info()) {
        init(n_, v_);
    }
```

```
template < class T>
LazySeg(vector < T> init_) {
            init(init_);
 void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
 template < class T>
            void init (vector<T> init_) {
            info.assign(4 << __lg(n), Info());
tag.assign(4 << __lg(n), Tag());
function <void(
   int, int, int)> build = [&](int p, int l, int r) {
   if (r - l == 1) {
                                     info[p] = init_[l];
                                     return;
                         int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                         pull(p);
            build(1, 0, n);
 void pull
(int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
}
             tag[p].apply(v);
 void push(int p, int l, int r) {
            int m = (l + r) / 2;
if (r - l >= 1) {
    apply(p * 2, l, m, tag[p]);
    apply(p * 2 + 1, m, r, tag[p]);
}
             tag[p] = Tag();
void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
    }
}
                         return;
             int m = (l + r) / 2;
            push(p, l, r);
if (x < m) {</pre>
                         modify(2 * p, l, m, x, v);
             } else {
                         modify(2 * p + 1, m, r, x, v);
            pull(p);
void modify(int p, const Info &i) {
    modify(1, 0, n, p, i);
info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    push(p, l, r);
}</pre>
            return query(p *
2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
               (int ql, int qr) { return query(1, 0, n, ql, qr); }
(Int qt, the qt, the qt, the const and 
            }
int m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
void range_apply(int l, int r, const Tag &v) {
   range_apply(1, 0, n, l, r, v);
 template < class F> // 尋找區間內,第一個符合條件的
 int findFirst
            (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
    return -1;</pre>
             if (l >= x && r <= y && !pred(info[p])) {</pre>
                        return -1;
            if (r - l == 1) {
                         return l;
             int m = (l + r) / 2;
            push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
             if (res == -1)
                         res = findFirst(2 * p + 1, m, r, x, y, pred);
             return res;
```

```
template < class F> // 若要找 last, 先右子樹遞廻即可
int findFirst(int l, int r, F &&pred) {
    return findFirst(1, 0, n, l, r, pred);
}:
struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add; void apply(const Tag& v) { if (v.set_val) { set_val = v.set_val;
                  add = v.add;
            }
else {
                  add += v.add;
     }
};
struct Info {
      int sum;
      void apply(int l, int r, const Tag &v) {
            if (v.set_val) {
    sum = (r - l) * v.set_val;
            sum += (r - l) * v.add;
      // Info& operator=(const Info &rhs) {
               // 部分 assignment 使用 return *this;
     //
//
// }
Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
}
3.5 Persistent Segment Tree [d41d8c]
```

```
template < class Info >
struct PST {
    struct Node {
            Info info = Info();
int lc = 0, rc = 0;
       vector<Node> nd;
      int n = 0; vector<int> rt;
PST() : n(0) {}
      PST(int n_, Info v_ = Info()) { init(n_, v_); }
      template <class T>
PST(vector <T> init_) { init(init_); }
void init(int n_, Info v_ = Info()) {
   init(vector < Info > (n_, v_));
}
      template < class T >
      void init(vector<T> init_) {
            n = init_.size();
nd.clear(); rt.clear();
            nd.emplace_back(); // 讓 root 指向 1-based rt.push_back(build(0, n, init_));
      int build(int l, int r, const vector<Info> &init_) {
  int id = nd.size();
             nd.emplace_back();
            if (r - l == 1) {
   nd[id].info = init_[l];
   return id;
            int m = (l + r) >> 1;
nd[id].lc = build(l, m, init_);
nd[id].rc = build(m, r, init_);
            pull(nd[id]);
             return id:
      void pull(Node &t) {
   t.info = nd[t.lc].info + nd[t.rc].info;
      int copy(int t) {
   nd.push_back(nd[t]);
   return nd.size() - 1;
      int modify(int t, int p, const Info &v, int l, int r) {
            int nt = copy(t);
if (r - l == 1) {
                  nd[nt].info = v;
                   return nt:
             int m = (l + r) >> 1;
            if (p < m) {
    nd[nt].lc = modify(nd[t].lc, p, v, l, m);</pre>
                  nd[nt].rc = modify(nd[t].rc, p, v, m, r);
            pull(nd[nt]);
            return nt;
      void modify(int ver, int pos, const Info& val) {
            rt[ver] = modify(rt[ver], pos, val, 0, n);
      Info query(int t, int ql, int qr, int l, int r) {
    if (l >= qr || r <= ql) return Info();
    if (ql <= l && r <= qr) return nd[t].info;
    int m = (l + r) >> 1;
             return query(nd[t].
```

lc, ql, qr, l, m) + query(nd[t].rc, ql, qr, m, r);

```
const Cmp cmp = Cmp();
                                                                                                                  static constexpr unsigned B = 64; using u64 = unsigned long long;
       Info query(int ver, int ql, int qr) {
             return query(rt[ver], ql, qr, 0, n);
                                                                                                                  int n:
                                                                                                                  vector<vector<T>> a;
       void createVersion(int ori_ver)
                                                                                                                  vector <T> pre, suf, ini;
vector <u64> stk;
             rt.push_back(copy(rt[ori_ver]));
      void reserve(int n, int q) {
   nd.reserve(n + q * (2 * __lg(n) + 1));
   rt.reserve(q + 1);
                                                                                                                  RMQ() {}
RMQ(const vector<T> &v) { init(v); }
                                                                                                                  void init(const vector<T> &v) {
                                                                                                                       n = v.size();
pre = suf = ini = v;
      }
struct Info {
   int sum = 0;
                                                                                                                         stk.resize(n);
                                                                                                                        if (!n) {
Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
                                                                                                                        const int M = (n - 1) / B + 1;
const int lg = __lg(M);
a.assign(lg + 1, vector<T>(M));
for (int i = 0; i < M; i++) {
    a[0][i] = v[i * B];
    for (int j = 1; j < B && i * B + j < n; j++) {
        a[0][i] = min(a[0][i], v[i * B + j], cmp);
}</pre>
3.6 Treap [d41d8c]
Treap(int val_) {
    min = val = val_;
    pri = rand();
                                                                                                                        for (int i = 1; i < n; i++) {
   if (i % B) {
      pre[i] = min(pre[i], pre[i - 1], cmp);
}</pre>
             lc = rc = nullptr;
             siz = 1; rev_valid = 0;
                                                                                                                        for (int i = n - 2; i >= 0; i--) {
   if (i % B != B - 1) {
      suf[i] = min(suf[i], suf[i + 1], cmp);
}
       void pull() { // update siz or other information
             siz = 1;
min = val;
             for (auto c : {lc, rc}) {
    if (!c) continue;
    siz += c->siz;
                                                                                                                        for (int j = 0; j < lg; j++) {
   for (int i = 0; i + (2 << j) <= M; i++) {
     a[j + 1][i</pre>
                   min = std::min(min, c->min);
             }
                                                                                                                                            ] = min(a[j][i], a[j][i + (1 << j)], cmp);
       void push() {
                                                                                                                         for (int i = 0; i < M; i++) {
    const int l = i * B;
    const int r = min(1U * n, l + B);</pre>
             if (rev_valid) {
                   swap(lc, rc);
if (lc) lc->rev_valid ^= 1;
if (rc) rc->rev_valid ^= 1;
                                                                                                                               u64 s = 0;
                                                                                                                               for (int j = l; j < r; j++) {
   while (s && cmp(v[j], v[__lg(s) + l])) {
      s ^= 1ULL << __lg(s);</pre>
             rev_valid = false;
      int find(int k) { // 找到 min 是 k 的位置 (1-based)
                                                                                                                                     s |= 1ULL << (j - l);
             push();
             int ls = (lc ? lc->siz : 0) + 1;

if (val == k) return ls;

if (lc && lc->min == k) return lc->find(k);

else return rc->find(k) + ls;
                                                                                                                                     stk[j] = s;
                                                                                                                              }
                                                                                                                        }
                                                                                                                  T operator()(int l, int r) {
    if (l / B != (r - 1) / B) {
        T ans = min(suf[l], pre[r - 1], cmp);
        l = l / B + 1;
      }
int size(Treap *t) {
    return t ? t->siz : 0;
                                                                                                                               r = r / B;
if (l < r) {
int k = _
Treap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
    a->push(); b->push();
                                                                                                                                     int k = __lg(r - l);
ans = min
       if (a->pri > b->pri) {
                                                                                                                                            ({ans, a[k][l], a[k][r - (1 << k)]}, cmp);
             a->rc = merge(a->rc, b);
a->pull();
                                                                                                                               return ans;
                                                                                                                        } else {
   int x = B * (l / B);
             return a;
                                                                                                                               return ini
      else {
    b->lc = merge(a, b->lc);
                                                                                                                                     [__builtin_ctzll(stk[r - 1] >> (l - x)) + l];
             b->pull();
                                                                                                                        }
                                                                                                                 }
             return b:
                                                                                                           };
      }
                                                                                                           3.8 Mo [d41d8c]
pair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first *, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
                                                                                                           struct query {
                                                                                                           int l, r, id;
} typedef query;
      t->push():
                                                                                                           } typedef query;
void MO(int n, vector<query> &queries) {
   int block = sqrt(n);
   function <bool(query, query)> cmp = [&](query a, query b) {
     int block_a = a.l / block;
     int block_b = b.l / block;
     if (block_a != block_b) return block_a < block_b;
     return a.r < b.r;
}</pre>
       if (size(t->lc) < k) {
             auto [a, b] = split(t->rc, k - size(t->lc) - 1);
             t->rc = a;
             t->pull();
             return {t, b};
      else {
             auto [a, b] = split(t->lc, k);
             t->lc = b;
t->pull();
                                                                                                                  sort(queries.begin(), queries.end(), cmp);
             return {a, t};
                                                                                                            void compress(vector<int> &nums) {
      }
                                                                                                                  vector<int> sorted = nums;
                                                                                                                  sort(sorted.begin(), sorted.end());
void Print(Treap *t) {
                                                                                                                  sorted.erase
      if (!t) return;
                                                                                                                          (unique(sorted.begin(), sorted.end()), sorted.end());
      t->push();
                                                                                                                  for (int i = 0; i < nums.size(); i++) {
    nums[i] = lower_bound(sorted.begin</pre>
      Print(t->lc);
cout << t->val;
                                                                                                                                (), sorted.end(), nums[i]) - sorted.begin() + 1;
      Print(t->rc);
                                                                                                                  }
                                                                                                           }
3.7 RMQ [d41d8c]
                                                                                                            4 Flow
```

template < class T, class Cmp = greater < T >> struct RMQ {

4.1 Dinic [aa12d4]

```
template < class T>
struct Dinic {
      struct Edge {
           int to:
            T flow, cap; // 流量跟容量
      int n, m, s, t;

const T INF_FlOW = 1 << 30;
      vector<vector<int>> adj; // 此點對應的 edges 編號
      vector<Edge> edges; // 幫每個 edge 編號
      vector < tage > eages; // 帛好间 e
vector < int > dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_; m = 0;
}
             dis.resize(n); ptr.resize(n);
adj.assign(n, vector < int > { } );
edges.clear();
      void add_edge(int u, int v, T cap) {
// 偶數 id 是正向邊
             edges.push_back({ v, 0, cap });
edges.push_back({ u, 0, 0 });
adj[u].push_back(m++);
             adj[v].push_back(m++);
      bool bfs() {
             fill(dis.begin(), dis.end(), -1);
dis[s] = 0; queue<int> q;
             q.push(s);
             while (!q.empty() && dis[t] == -1) {
                   int u = q.front(); q.pop();
for (int id : adj[u]) {
    Edge &e = edges[id];
                          if (e.flow == e.cap) continue;
if (dis[e.to] == -1) {
    dis[e.to] = dis[u] + 1;
                                q.push(e.to);
                         }
                  }
             return dis[t] != -1;
      T dfs(int u, T flow) {
             if (flow == 0) return 0;
if (u == t) return flow;
             for (int
                   &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {
Edge &e = edges[adj[u][cur]];
if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;</pre>
                   T mn = dfs(e.to, min(flow, e.cap - e.flow));
if (mn > 0) {
    e.flow += mn;
                          edges[adj[u][cur] ^ 1].flow -= mn;
                          return mn;
                   }
             return 0; // 到不了終點就會 return 0
      riti(ptr.begin(), ptr.end(),
while (true) {
   T res = dfs(s, INF_Flow);
   if (res == 0) break;
   flow += res;
                  }
             return flow;
      void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
};
4.2 Min Cut [44ae6c]
```

```
// CSES Police Chase
int main(){
       int n, m; cin >> n >> m;
Dinic < int >> g(n);
for (int i = 0; i < m; i++) {</pre>
              int u, v, cap = 1;
cin >> u >> v;
u--; v--;
               g.add_edge(u, v, cap);
              g.add_edge(v, u, cap);
       int res = g.work(0, n - 1);
cout << res << "\n";
if (res == 0) return;</pre>
       vector <int> vis(n);
auto find = [&](auto self, int u) -> void {
   if (!vis[u]) {
                      vis[u] =
                      for (int id : g.adj[u]) {
    auto e = g.edges[id];
    if (e.cap - e.flow > 0) {
                                     self(self, e.to);
```

```
}
                             }
             }
 find(find, 0);
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
        auto e = g.edges[id];
        if (!vis[e.to]) {
            cout << i + 1 << " " << e.to + 1 << "\n";
        }
}</pre>
               }
}
```

```
}
 4.3 MCMF [77fc99]
 template < class Tf, class Tc>
 struct MCMF {
      struct Edge {
   int to;
           Tf flow, cap; // 流量跟容量
           Tc cost:
      // 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就好
      int n, m, s, t;

const Tf INF_FLOW = 1 << 30;

const Tc INF_COST = 1 << 30;

vector<vector<int>> adj;
      vector<Edge> edges; // 幫每個 edge 編號
vector<Tc> dis, pot; // johnson algorithm, using spfa
vector<int> rt; // 路徑恢復,對應 id
      vector<int> rt; // 脐徑內復; 
vector<bool> inq;
MCMF(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_; m = 0;
            edges.clear();
           adj.assign(n, vector<int>{});
      void add_edge(int u, int v, Tf cap, Tc cost){
  edges.push_back({v, 0, cap, cost});
  edges.push_back({u, 0, 0, -cost});
  adj[u].push_back(m++);
            adj[v].push_back(m++);
      bool spfa() {
           dis.assign(n, INF_COST);
rt.assign(n, -1); inq.assign(n, false);
            queue < int > q;
           q.push(v); inq[v] = true;
                      }
                }
           return dis[t] != INF_COST;
      bool dijkstra() {
           pq.emplace(ndis, v);
                 }
            return dis[t] != INF_COST;
      .
// 限定 flow,最小化 cost
pair<Tf, Tc> work_flow(int s_, int t_, Tf need) {
           s = s_, t = t_; pot.assign(n, 0);
Tf flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {</pre>
                      dis[i] += pot[i] - pot[s];
                 Tf f = INF_FLOW;
                 for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
                      f = min
                            (f, edges[rt[i]].cap - edges[rt[i]].flow);
```

```
National Chung Cheng University Salmon
                   f = min<Tf>(f, need);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
                   flow += f; need -= f;
cost += f * dis[t]; fr = false;
                   swap(dis, pot);
if (need == 0) break;
            return make_pair(flow, cost);
      // 限定 cost, 最大化 flow
      pair<Tf, Tc> work_budget(int s_, int t_, Tc budget) {
            s = s_, t = t_; pot.assign(n, 0);
Tf flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] += pot[i] - pot[s];
}</pre>
                   If f = INF_FLOW;
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                (f, edges[rt[i]].cap - edges[rt[i]].flow);
                   f = min<Tf>(f, budget / dis[t]);
                   for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
   edges[rt[i]].flow += f;
   edges[rt[i] ^ 1].flow -= f;
                   flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
                   swap(dis, pot);
                   if (budget == 0 || f == 0) break;
            return make_pair(flow, cost);
      void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
4.4 Hungarian [eea453]
struct Hungarian { // 0-based
      int n, m;
      vector<vector<int>> adj;
      vector <int> used, vis;
vector <pair <int, int>> match;
Hungarian(int n = 0, int m = 0) {
             init(n_, m_);
      void init(int n_, int m_) {
    n = n_; m = m_;
    adj.assign(n + m, vector<int>());
             used.assign(n + \dot{m}, -1);
             vis.assign(n + m, 0);
      void addEdge(int u, int v) {
   adj[u].push_back(n + v);
             adj[n + v].push_back(u);
      bool dfs(int u)
            int sz = adj[u].size();
for (int i = 0; i < sz; i++) {
   int v = adj[u][i];</pre>
```


4.5 Theorem [d41d8c]

```
|// 有向無環圖:
|// 最小不相交路徑覆蓋:
|// 最小路徑數 = 頂點數 - 最大匹配數
|// 最小相交路徑覆蓋:
|// 先用
| Floyd 求傳遞封包,有連邊就建邊,然後再套最小不相交路徑覆蓋
```

```
// 二分圖:
// 最小點
        覆蓋: 選出一些點,讓所有邊至少有一個端點在點集中的最少數量
// 最小點覆蓋 = 最大匹配數
// 還原解,flow 的作法是從源點開始 dfs,只走 cap - flow > 0
// 的邊,最後挑選左邊還沒被跑過的點和右邊被跑過的點當作覆蓋的點
// 最少邊覆蓋: 選出一些邊,讓所有點都覆蓋到的最少數量
// 最少邊覆蓋 = 點數 - 最大匹配數
// 最大獨立集: 選出一些點,使這些點兩兩沒有邊連接的最大數量
// 最大獨立集 = 點數 - 最大匹配數
```

5 String

5.1 Hash [852711]

```
constexpr int B = 59;
vector<Z> Hash(string &s) {
    vector<Z> ans {0};
    for (auto c : s) {
        ans.push_back(ans.back() * B + (c - 'a' + 1));
    }
    return ans;
}
void solve() {
    string s, sub;
    cin >> s >> sub;
    auto a = Hash(s);
    auto q = Hash(sub);
    auto find = q.back();
    int ans = 0;
    int l = 1, r = sub.size(), len = sub.size();
    while (r <= s.size()) {
        if (a[r] - a[l - 1] * power(Z(B), len) == find) {
            ans++;
        }
        l++, r++;
    }
    cout << ans << "|n";
}</pre>
```

5.2 KMP [cddfd9]

```
struct KMP {
         string sub;
         vector<int> failure;
         KMP(string sub_) {
                sub = sub_;
failure.resize(sub.size(), -1);
                buildFailFunction();
        void buildFailFunction() {
    for (int i = 1; i < (int)sub.size(); i++) {
        int now = failure[i - 1];
}</pre>
                        while (now != -1
                        && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
         vector<<mark>int</mark>> match(string &s) {
               vector <int> match;
for (int i = 0, now = -1; i < (int)s.size(); i++) {
    // now is the compare sucessed length -1
    while (s[i] !=</pre>
                                sub[now + 1] && now != -1) now = failure[now];
                       sub[now + 1] & now := -1) now = latture[now];
// failure stores if comparison fail, move to where
if (s[i] == sub[now + 1]) now++;
if (now + 1 == (int)sub.size()) {
   match.push_back(i - now);
                               now = failure[now];
                       }
                return match;
        }
};
```

5.3 Z Function [764b31]

```
|// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)

// 的最長公共前綴 (LCP) 的長度

vector < int > Z(string s) {
    int n = s.size();
    vector < int > z(n); z[0] = n;
    for (int i = 1, j = 1; i < n; i++) {
        z[i] = max(0, min(j + z[j] - i, z[i - j]));
        while (i + z[i] < n && s[z[i]] == s[i + z[i]])
        z[i]++;
        if (i + z[i] > j + z[j]) j = i;
    }

    return z; // 最後一格不算
}
```

5.4 SA [d40e3e]

```
struct SuffixArray {
   int n; string s;
```

```
vector<int> sa. rk. lc:
              // n: 字串長度
              // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
               // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
              // lc: LCP
                              數組,lc[i] 表示 sa[i] 和 sa[i + 1] 的最長公共前綴長度
              SuffixArray(const string &s_) {
   s = s_; n = s.length();
   sa.resize(n);
                            lc.resize(n - 1);
                            rk.resize(n);
                            iota(sa.begin(), sa.end(), 0);
                           sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });</pre>
                            rk[sa[0]] = 0;
for (int i = 1; i < n; ++i)
                                         rk[sa[i]]
                                                           = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
                            int k = 1;
                            vector<int> tmp, cnt(n);
                           tmp.reserve(n);
while (rk[sa[n - 1]] < n - 1) {</pre>
                                         tmp.clear();
for (int i = 0; i < k; ++i)
    tmp.push_back(n - k + i);
for (auto i : sa)
    if (i >= k)
                                         tmp.push_back(i - k);
fill(cnt.begin(), cnt.end(), 0);
for (int i = 0; i < n; ++i)</pre>
                                        for (tht t = 0; t < n; ++t)
    ++cnt[rk[i]];
for (int i = 1; i < n; ++i)
    cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; --i)
                                                      sa[--cnt[rk[tmp[i]]]] = tmp[i];
                                       for (int i = 0, j = 0; i < n; ++i) {
   if (rk[i] == 0) {
        j = 0;
        reconstruction | j = 0;
        reconstr
                                         } else {
                                                       for (j
                                                                           -= j > 0; i + j < n && sa[rk[i] - 1] + j
                                                                       < n && s[i + j] == s[sa[rk[i] - 1] + j]; )
                                                      lc[rk[i] - 1] = j;
                           }
               string getLCP() {
                           ing getted, {
  int cp = 0, k, lcp = 0, p;
  for (int i = 0; i < n; i++) {
    if (!rk[i]) continue;</pre>
                                        k = sa[rk[i] - 1];
if (cp) cp--;
while (s[i + cp] == s[k + cp]) cp++;
                                          if (cp`> lcp){
                                                       lcp = cp;
                                                    p = i;
                                        }
                           if (lcp) {
    return s.substr(p, lcp);
                           } else {
                                       return "-1";
};
```

Manacher [9c9ca6]

```
// 找到對於每個位置的迴文半徑
vector<int> manacher(string s) {
    string t = "#";
    for (auto c : s) {
        t += c;
t += '#';
    int n = t.size();
    vector < int > r(n);
for (int i = 0, j =
        0; i < n; i++) { // i 是中心, j 是最長回文字串中心 if (2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
        r[i] += 1;
         if (i + r[i] > j + r[j]) {
        }
    return r;
// # a # b # a #
```

```
// # a # b # b # a #
// 1 2 1 2 5 2 1 2 1
// 值 -1 代表原回文字串長度
// (id - val + 1) / 2 可得原字串回文開頭
```

5.6 SAM [d15619]

```
struct SAM {
      static constexpr int ALPHABET_SIZE = 26;
      struct Node {
            int len;
int link:
            array<int, ALPHABET_SIZE> next;
            Node() : len{}, link{}, next{} {}
      vector < Node > t;
      vector (Node)

SAM() { init(); }

void init() {
    t.assign(2, Node());
    t[0] next.fill(1);

            t[0].len = -1;
      int newNode() {
            t.emplace_back();
            return t.size() - 1;
      int extend(int p, int c) {
    if (t[p].next[c]) {
        int q = t[p].next[c];
        if (t[q].len == t[p].len + 1) {
                   int r = newNode();
                  t[r].len = t[p].len + 1;
t[r].link = t[q].link;
t[r].next = t[q].next;
                   t[q].link = r;
                   while (t[p].next[c] == q) {
    t[p].next[c] = r;
    p = t[p].link;
                  return r:
            int cur = newNode();
            t[cur].len = t[p].len + 1;
while (!t[p].next[c]) {
                 t[p].next[c] =
                  p = t[p].link;
            t[cur].link = extend(p, c);
            return cur;
      }
void solve() {
      string s; cin >> s;

int n = s.length();
      vector < int > pos(n + 1); // s[i - 1] 的後綴終點位置
      pos[0] = 1;
      SAM sam;
      for (int i = 0; i < n; i++) {
    pos[i + 1] = sam.extend(pos[i], s[i] - 'a');</pre>
}
```

5.7 Trie [3b3aa0]

```
struct Trie {
      struct trie_node {
           bool is_word;
           vector<trie_node *> children;
trie_node() {
   is_word = false;
   children.resize(26, NULL);
}
          }
      trie_node *root = new trie_node();
      void insert(string &s) {
    trie_node *cur = root;
           for (int i = 0; i < s.size(); i++) {
   int idx = s[i] - 'a';</pre>
                 if (cur->children[idx] == NULL) {
                      cur->children[idx] = new trie_node();
                 cur = cur->children[idx];
           cur->is_word = true;
      bool is_in_trie(string &s) {
           trie_node *cur = root;
for (int i = 0; i < s.size(); i++) {
                 if (cur->
                 children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
           return true;
      int search_i_start(string &s, int i, vector<int> &dp) {
    trie_node *cur = root;
           int sz = s.size(), ans = 0;
```

```
for (int j = i; j < sz; j++) {</pre>
               ->children[s[j] - 'a'] == nullptr) return ans;
cur = cur->children[s[j] - 'a'];
               if (cur->is_word)
                    (ans += dp[j + 1]) \% = mod;
          return ans;
    }
int main() {
    // 找到 sub 集合裡,可以重複用,組成 s 的組數 Trie trie;
     string s; cin >> s;
     int sz = s.size();
     // dp 代表 i 開頭到最後的配對總數
     // 找到有結尾為 stop 的 dp[i] += dp[j + 1]
     int n; cin >> n;
     vector <int> dp(sz + 1, 0);
for (int i = 0; i < n; i++) {
    string sub; cin >> sub;
          trie.insert(sub);
    dp[sz] = 1;
for (int i = sz - 1; i >= 0; i--) {
    dp[i] = trie.search_i_start(s, i, dp);
     cout << dp[0] << endl;
3
5.8 Duval [f9dcca]
```

```
// duval_algorithm
// 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
int i = 0, n = s.size();
vector<string> res;
   j++;
        while (i <= k) {</pre>
            res.push_back(s.substr(i, j - k));
           i += j - k;
       }
    return res;
// 最小旋轉字串
string min_round(string s) {
   int i = 0, n = s.size();
int start = i;
while (i < n / 2) {</pre>
       else k++;
           i++:
       while (i <= k) {
    i += j - k;</pre>
    return s.substr(start, n / 2);
```

6 Math

6.1 Modulo [56b9fb]

```
constexpr ll norm(ll x) const {
           if (x < 0) x += getMod();
if (x >= getMod()) x -= getMod();
            return x:
      constexpr ll val() const { return x; }
constexpr MInt operator-() const {
           MInt res;
            res.x = norm(getMod() - x);
            return res;
      constexpr MInt inv() const {
   return power(*this, getMod() - 2);
      constexpr MInt &operator*=(MInt rhs) & {
           if (getMod() < (1ULL << 31)) {
    x = x * rhs.x % int(getMod());
} else {</pre>
                x = mul(x, rhs.x, getMod());
           return *this;
      constexpr MInt &operator+=(MInt rhs) & {
           x = norm(x + rhs.x);
return *this;
      constexpr MInt &operator -= (MInt rhs) & {
    x = norm(x - rhs.x);
            return *this;
      constexpr MInt &operator/=(MInt rhs) & {
    return *this *= rhs.inv();
      friend constexpr MInt operator*(MInt lhs, MInt rhs) {
   MInt res = lhs; return res *= rhs;
      friend constexpr MInt operator+(MInt lhs, MInt rhs) {
   MInt res = lhs; return res += rhs;
      friend constexpr MInt operator-(MInt lhs, MInt rhs) {
            MInt res = lhs; return res -= rhs;
      friend constexpr MInt operator/(MInt lhs, MInt rhs) {
   MInt res = lhs; return res /= rhs;
           constexpr istream &operator>>(istream &is, MInt &a) {
ll v; is >> v; a = MInt(v); return is;
      friend constexpr
ostream &operator << (ostream &os, const MInt &a) {
            return os << a.val();</pre>
      friend constexpr bool operator==(MInt lhs, MInt rhs) {
  return lhs.val() == rhs.val();
      friend constexpr bool operator!=(MInt lhs, MInt rhs) {
   return lhs.val() != rhs.val();
      friend constexpr bool operator<(MInt lhs, MInt rhs) {
   return lhs.val() < rhs.val();</pre>
     }
};
template<>
ll MInt<0>::Mod = 998244353;
constexpr int P = 1e9 + 7;
using Z = MInt<P>;
```

6.2 Combination [878efe]

6.4 CRT [d41d8c]

```
Ill exgcd(ll a, ll b, ll &x, ll &y) {
    if (!b) {
        x = 1, y = 0;
        return a;
    }
    ll g = exgcd(b, a % b, y, x);
    y -= a / b * x;
    return g;
}
ll inv(ll x, ll m) {
    ll a, b;
    exgcd(x, m, a, b);
    a %= m;
    if (a < 0) a += m;
    return a;
}
// remain, mod
ll CRT(vector<pair<ll, ll>> &a) {
    ll prod = 1;
    for (auto x : a) {
        prod *= x.second;
    }
    ll res = 0;
    for (auto x : a) {
        auto t = prod / x.second;
        res += x.first * t % prod * inv(t, x.second) % prod;
    if(res >= prod) res -= prod;
}
return res;
}
```

6.5 Matrix [08b5fe]

6.6 Integer Partition [595ed2]

6.7 Mobius Theorem

- 數論分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n} \mu(d) = \begin{cases} 1 & \text{for } n=1\\ 0 & \text{for } n\neq 0 \end{cases}$$

- 2. μ 是常數函數 1 的反元素 $\Rightarrow \mu*1=\epsilon$, $\epsilon(n)$ 只在n=1時為 1 , 其餘情況皆為 0 。
- $-\phi$ 歐拉函數: x以下與x互質的數量

$$\phi*1 = \sum_{d|n} \phi(\frac{n}{d})$$
 質因數分解
$$= \sum_{i=0}^{c} \phi(p^{i})$$

$$= 1 + p^{0}(p-1) + p^{1}(p-1) + \dots + p^{c-1}(p-1)$$

$$= p^{c}$$

$$= id$$

- 莫比烏斯反演公式
 - $f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$
 - $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

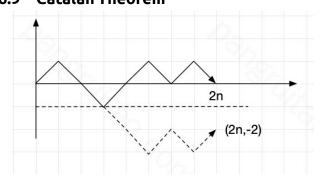
例子

$$\begin{split} &\sum_{i=aj=c}^{b} \sum_{j=1}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{i=1}^{x} \sum_{j=1}^{x} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{\infty} \sum_{j=1}^{x} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.8 Mobius Inverse [d41d8c]

```
const int maxn = 2e5:
 ll mobius_pref[maxn];
 void init() {
                     mobius_pref[1] = 1;
vector<ll> wei
                      (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
    }
                                                                  continue; // 包含平方
                                            if (wei[i] == 0) {
    wei[i] = 1;
                                                                  }
                                           mobius_pref[i]
                                                                      = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
void solve() {
                   a solve() {
    ll a, b, c, d, k; cin >> a >> b >> c >> d >> k;
    auto cal = [&](ll x, ll y) -> int {
        int res = 0;
        for (int l = 1, r; l <= min(x, y); l = r + 1) {
            r = min(x / (x / l), y / (y / l));
            res += (mobius_pref[r] - mobius_pref[l] - mobius_p
                                                                                               - 1]) * (x / l) * (y / l); // 代推出來的式子
                                            return res;
                     cout << cal
                                               (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k, (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n";
}
```

6.9 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2)

假設往上有 x 個,往下有 y 個,會有:

$$\begin{cases} x + y = 2n \\ y - x = 2 \end{cases} \Rightarrow \begin{cases} x = n - 1 \\ y = n + 1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.10 Burnside's Lemma

 $|X/G|\!=\!\frac{1}{|G|}\sum_{g\in G}\!|X^g|$

- · G:各種翻轉操作所構成的置換群
- X/G:本質不同的方案的集合 X^g :對於某一種操作 g,所有方案中,經過 g 這種翻轉後保持不變的方案 的集合
- 集合取絕對值代表集合數

Search and Gready

7.1 Binary Search [d41d8c]

```
int main() {
        int l = 1, r = 10;
// 1 to tar, find tar
while (l <= r) {</pre>
                int m = (l + r) / 2;
                if (check(m)) l = m + 1;
else r = m - 1;
        cout << r;
        // tar to end
while (l <= r) {
    int m = (l + r) / 2;
    if (check(m)) r = m - 1;
    else l = m + 1;
        cout << l:
}
```

7.2 Ternary Search [d41d8c]

```
// 找極值問題,遞增遞減
void solve() {
     int l = 0, r = 10, ans = 0; // ans 紀錄答案 while (l <= r) {
          int d = (r - l) / 3; // 差
          int ml = l + d, mr = r - d; // mr 要用減的
auto cal = [&](int m) -> int {
               int x = 0;
               return x; // 計算答案
          int ansl = cal(ml), ansr = cal(mr);
if (ansl < ansr) {
    l = ml + 1;</pre>
          } else {
    r = mr - 1;
          }
     }
```

8 Tree

8.1 LCA [601e2d]

```
vector < vector < int >> par(maxn, vector < int > (18));
  vector < int > depth(maxn + 1);
vector < int > dfn(maxn);
 vector < int> dfn(maxn);
void build(int n, vector < vector < pair < int, int >>> & tree) {
    auto dfs = [&](auto self, int u, int pre) -> void {
        for (auto [v, w] : tree[u]) {
            if (v == pre) continue;
            par[v][0] = u; // 2 ^ 0
            depth[v] = depth[u] + 1;
            self(self, v, u);
}
                      }
            }
int lca(int a, int b) {
   if (depth[a] < depth[b]) swap(a, b);
   int pull = depth[a] - depth[b];
   for (int i = 0; i < 18; i++) {
      if (pull & (1 << i)) {
            a = par[a][i];
      }
}</pre>
            for (int i = 17; i >= 0; i--) {
   if (par[a][i] != par[b][i]) {
      a = par[a][i], b = par[b][i];
}
             return par[a][0];
```

8.2 Centroid Decomposition [ec760b]

```
#include <bits/stdc++.h>
using namespace std;
struct CenDecom {
     int n:
     vector<vector<int>> adj;
     vector < bool > vis;
```

```
vector < int > siz;
CenDecom(int n_ = 0) { init(n_); }
         void init(int n_) {
                  n = n_;
adj.assign(n, {});
vis.assign(n, false);
                   siz.assign(n, 1);
         void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
         void get_siz(int x, int p = -1) {
    siz[x] = 1;
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        get_siz(y, x);
        siz[x] += siz[y];
}
         int get_cen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz) {
            return get_cen(y, sz, x);
        }
}
                           }
                   return x;
         void get_ans(int x, int p) {
                   // do something
                   for (int y : adj[x]) {
    if (y == p || vis[y]) continue;
    get_ans(y, x);
         void work(int x = 0) {
    get_siz(0, x);
                  get_stz(0, x);
int cen = get_cen(x, siz[x]);
vis[cen] = true;
for (int y : adj[cen]) {
    if (vis[y]) continue;
                           get_ans(y, cen);
                   for (int y : adj[cen]) {
                           if (vis[y]) continue;
work(y);
};
```

8.3 Tree Flattening [5293b7]

```
|// 父節
         點加值 = 所有子節點區間加值,求單點,使用 bit,做前綴差分
  // CSES 1138_Path Queries
 int main(){
        int n, q; cin >> n >> q;
vector <int> val(n + 1), dfnToVal(n);
for (int i = 1; i <= n; i++) {</pre>
              cin >> val[i];
        vector<vector<int>> tree(n + 1);
        for (int i = 1; i < n; i++) {
   int u, v; cin >> u >> v;
               tree[u].push_back(v);
               tree[v].push_back(u);
        vector<pair<int, int>> mp(n + 1); // dfn 區間
        auto dfs = [&](auto self, int u, int par) -> void {
    dfnToVal[++cnt] = val[u];
    mp[u].first = cnt;
               for (auto v : tree[u]) {
   if (v == par) continue;
   self(self, v, u);
              mp[u].second = cnt;
        dfs(dfs, 1, 0);
        BIT bit(n);

for (int i = 1; i <= n; i++) {
              bit.modify(mp[i].first, val[i]);
              if (mp[i].first < n) { // root 就不用扣了
  bit.modify(mp[i].second + 1, -val[i]);</pre>
        for (int i = 0; i < q; i++) {
               int op; cin >> op;
              int op; cin >> op;
if (op == 1) {
   int s, x; cin >> s >> x;
   int add = x - dfnToVal[mp[s].first];
   dfnToVal[mp[s].first] = x;
   bit.modify(mp[s].first, add);
   if (mp[s].first < n) { // root 就不用扣了
        bit.modify(mp[s].second + 1, -add);
   }
}</pre>
               else {
                     int node; cin >> node;
                     cout << bit.query(mp[node].first) << "\n";</pre>
```

```
}
```

8.4 Heavy Light Decomposition [325476]

```
int n, cur;
vector<int> siz, top, dep, parent, in, out, seq;
vector<vector<int>> adj;
      HLD(int n_ = 0) { init(n_); }
       void init(int n_) {
            n = n_; cur = 0;
siz.resize(n); top.resize(n); dep.resize(n);
            parent.resize(n); in.resize(n); out.resize(n); seq.resize(n); adj.assign(n, {});
       void addEdge(int u, int v) {
            adj[u].push_back(v);
adj[v].push_back(u);
       void work(int rt = 0) {
            top[rt] = rt;
dep[rt] = 0;
parent[rt] = -1;
            dfs1(rt); dfs2(rt);
      void dfs1(int u) {
   if (parent[u] != -1)
       adj[u].erase(find
                          (adj[u].begin(), adj[u].end(), parent[u]));
             siz[u] = 1;
            for (auto &v : adj[u]) {
    parent[v] = u, dep[v] = dep[u] + 1;
                   dfs1(v);
                   siz[u] += siz[v];
                   if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
                  } // 讓 adj[u][0] 是重子節點
            }
      void dfs2(int u) {
            in[u] = cur++;
            seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
   top[v] = v == adj[u][0] ? top[u] : v;
                   dfs2(v):
             out[u] = cur;
      u = parent[top[u]];
} else {
                         v = parent[top[v]];
                  }
            return dep[u] < dep[v] ? u : v;</pre>
      int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
      int jump(int u, int k) {
   if (dep[u] < k) return -1;
   int d = dep[u] - k;
   while (dep[top[u]] > d)
        u = parent[top[u]];
             return seq[in[u] - dep[u] + d];
      bool isAncester(int u, int v) {
    return in[u] <= in[v] && in[v] < out[u];</pre>
      int rootedParent(int rt. int v) {
            if (rt == v) return rt;
if (!isAncester(rt, v)) return parent[rt];
auto it = upper_bound(adj[
                  rt].begin(), adj[rt].end(), v, [&](int x, int y) {
    return in[x] < in[y];
            }) - 1;
return *it;
      int rootedSize(int rt, int v) {
            if (rt == v) return n;
if (!isAncester(v, rt)) return siz[v];
return n - siz[rootedParent(rt, v)];
      int rootedLca(int a, int b, int rt) {
  return lca(a, b) ^ lca(b, rt) ^ lca(rt, a);
      }
};
```

8.5 Link Cut Tree [d69ee0]

```
template < class Info, class Tag >
struct Node {
   Node *ch[2], *p;
   bool rev = false; int size = 1;
   Info info = Info(); Tag tag = Tag();
   Node() : ch{nullptr, nullptr}, p(nullptr) {}
   bool isrt() {
```

```
return !p || (p->ch[0] != this && p->ch[1] != this);
     void make_rev() +
          swap(ch[0], ch[1]);
rev ^= true;
     void apply(const Tag &v) {
   info.apply(size, v);
           tag.apply(v);
     void push() {
          if (rev)
               if (ch[0]) ch[0]->make_rev();
if (ch[1]) ch[1]->make_rev();
rev = false;
          if (ch[0]) ch[0]->apply(tag);
if (ch[1]) ch[1]->apply(tag);
     int pos() {
          return p->ch[1] == this;
     void pushAll() {
          if (!isrt())
               p->pushAll();
          push();
     void rotate() {
          Node *q = p;
int x = !pos();
          q \rightarrow ch[!x] = ch[x];
          if (ch[x]) ch[x] -> p = q;
           if (!q->isrt()) q->p->ch[q->pos()] = this;
          ch[x] = q;
q->p = this;
          q->pull();
     void splay() {
          pushAll();
           while (!isrt()) {
    if (!p->isrt()) {
        if (pos() == p->pos()) {
                          p->rotate();
                     } else {
   rotate();
                     }
               rotate();
          pull();
     }
     void access() { // access 後自動 splay
           for (Node
                  *i = this, *q = nullptr; i; q = i, i = i->p) {
               i->splay();
i->ch[1] = q;
i->pull();
           splay();
     void makeRoot() {
           access()
          make_rev();
     Node* findRoot() {
          access();
Node *t = this;
          while (t->ch[0]) {
    t->push();
    t = t->ch[0];
          t->access();
          return t;
    }
template < class Info, class Tag>
bool connected(Node < Info, Tag> *x, Node < Info, Tag> *y) {
    return x -> findRoot() == y -> findRoot();
template < class Info, class Tag>
bool neighber(Node<Info, Tag> *x, Node<Info, Tag> *y) {
     x->makeRoot();
     y->access();
if (y->ch[0] != x || x->ch[1]) return false;
     return true;
remplate < class Info, class Tag >
void split(Node < Info, Tag > *rt, Node < Info, Tag > *y) {
     y->makeRoot();
     rt->access();
remplate < class Info, class Tag>
void link(Node < Info, Tag> *t, Node < Info, Tag> *p) {
```

```
t->makeRoot():
      if (p->findRoot() != t) {
            t->p = p;
     }
template < class Info, class Tag>
bool cut(Node < Info, Tag> *x, Node < Info, Tag> *y) {
     x->makeRoot();
     y->access();
if (y->ch[0] != x || x->ch[1]) return false;
y->ch[0] = y->ch[0]->p = nullptr;
      x->pull();
      y->pull();
      return true:
remplate < class Info, class Tag>
void modify(Node < Info, Tag> *x, const Info &v) {
     x->access();
template < class Info. class Tag>
void path_apply
    (Node<Info, Tag> *x, Node<Info, Tag> *y, const Tag &v) {
      assert(connected(x, y));
      split(x, y);
     x->apply(v);
template < class Info, class Tag >
Info path_query(Node < Info, Tag > *x, Node < Info, Tag > *y) {
    assert(connected(x, y));
      split(x, y);
return x->info;
}
constexpr int Mod = 51061;
struct Tag {
    ll add = 0; ll mul = 1;
      void apply(const Tag& v) {
  mul = mul * v.mul % Mod;
  add = (add * v.mul % Mod + v.add) % Mod;
     }
struct Info {
    ll val = 0; ll sum = 0;
      void apply(int size, const Tag &v) {
           val = (val * v.mul % Mod + v.add) % Mod;
sum = (sum * v.mul % Mod + v.add * size % Mod) % Mod;
      void pull(const Info &l, const Info &r) {
           sum = (l.sum + r.sum + val) % Mod:
using lct = Node<Info, Tag>;
```

8.6 Virtual Tree [622e69]

```
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
// 可以建立虚樹達成快速樹 DP
    // 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector <int>>stk(maxn);
    int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
        vt[stk[top - 1]].push_back(stk[top]), top--;
    if (stk[top - 1] != l) {
        vt[l] such back(stk[top]);
        vt[l] such back(stk[top]);
        vt[l] such back(stk[top]);</pre>
                                                 vt[l].push_back(stk[top]);
                                                  stk[top] = l;
                            } else vt[l].push_back(stk[top--]);
                            stk[++top] = u;
      void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
    vt[u].clear();
       void solve(int n, int q) {
                          vector g(n + 1, vector<pair<int, int>>());
vector vt(n + 1, vector<int>()); // dfs 完清除,否則會退化
vector<ll> dp(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
    int u, v, w; cin >> u >> v >> w;
    int and a service of the s
                                                 g[u].push_back({v, w});
g[v].push_back({u, w});
                         }
build_lca(n, g);
build(n, g);
for (int i = 0; i < q; i++) {
   int m; top = -1; cin >> m;
   vector < int > key(m);
   for (int j = 0; j < m; j++) {
      cin >> key[j];
      iskey[key[j]] = 1;
}
                                                 key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
                                                   for (int x : key) insert(x, vt);
                                                  while (top
                                                                                > 0) vt[stk[top - 1]].push_back(stk[top]), --top;
```

```
// DP
auto dfs = [&](auto self, int u) -> void {
    for (auto v : vt[u]) {
        self(self, v);
        if (iskey[v]) {
            dp[u] += min_dis[v];
            // 砍掉 1 到 v 之間最短的路
    }
    else {
            dp[u] += min(dp[v], min_dis[v]);
        }
        iskey[v] = dp[v] = 0;
    }
    vt[u].clear();
};
dfs(dfs, key[0]); // key[0] 一定是 root
    cout << dp[key[0]] << "\n";
    iskey[key[0]] = dp[key[0]] = 0;
}
```

8.7 Dominator Tree [baa540]

```
struct Dominator_tree {
         int n, id;
vector<vector<int>> adj, radj, bucket;
vector<int> sdom, dom, vis, rev, pa, rt, mn, res;
Dominator_tree(int n_ = 0) { init(n_); }
         Dominator_free(int n_ = 0) { init(n_)
void init(int _n) {
    n = _n, id = 0;
    adj.assign(n, vector<int>());
    radj.assign(n, vector<int>());
    bucket.assign(n, vector<int>());
    sdom.resize(n); dom.assign(n, -1)
    vis.assign(n, -1); rev.resize(n);
    pa.resize(n); rt.resize(n);
    mn.resize(n); res.resize(n);
}
         void add_edge(int u, int v) { adj[u].push_back(v); }
int query(int v, int x) {
   if (rt[v] == v) return x ? -1 : v;
                   int p = query(rt[v], 1);
if (p == -1) return x ? rt[v] : mn[v];
                   if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
                   rt[v] = p;
return x ? p : mn[v];
          void dfs(int v) {
   vis[v] = id, rev[id] = v;
   rt[id] = mn[id] = sdom[id] = id, id++;
                   for (int u : adj[v]) {
   if (vis[u] == -1) dfs(u), pa[vis[u]] = vis[v];
   radj[vis[u]].push_back(vis[v]);
          void build(int s) {
                   dfs(s);
                   for (int i = id - 1; i >= 0; i--) {
    for (int u : radj[i])
        sdom[i] = min(sdom[i], sdom[query(u, 0)]);
                            if (i) bucket[sdom[i]].push_back(i);
for (int u : bucket[i]) {
   int p = query(u, 0);
                                     dom[u] = sdom[p] == i ? i : p;
                            if (i) rt[i] = pa[i];
                  fer.assign(n, -1);
for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];
for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre>
                   for (int i = 0; i < n; i++) dom[i] = res[i];</pre>
         }
};
```

9 DP

9.1 LCS [5781cf]

```
int main() {
    int m, n; cin >> m >> n;
    string s1, s2; cin >> s1 >> s2;
    int L = 0;
    vector < vector < int >> dp(m + 1, vector < int >(n + 1, 0));
    for (int i = 1; i <= m; i++) {
        if (s1[i - 1] == s2[j - 1])
            dp[i][j] = dp[i - 1][j - 1] + 1;
        else
            dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
    }
}
int length = dp[m][n]; cout << length << "\n";
    string s(length, 'c'); // backtracking
white (m >= 1 && n >= 1) {
        if (s1[m - 1] == s2[n - 1]) {
            s[length - 1] = s1[m - 1];
            m--, n--, length--;
        }
        else {
```

```
if (dp[m - 1][n] > dp[m][n - 1]) m--;
            }
      cout << s << "\n";
9.2 LIS [66d09f]
int main() {
      int n; cin >> n;
vector <int> v(n);
for (int i = 0; i < n; i++) cin >> v[i];
int dp[n]; vector <int> stk;
      dp[i] = ++L;
             } else {
                   auto it
                                lower_bound(stk.begin(), stk.end(), v[i]);
                    *it = v[i]; dp[i] = it - stk.begin() + 1;
      vector < int > ans; cout << L << "|n";
for (int i = n - 1; i >= 0; i--) {
    if (dp[i] == L) {
                    ans.push_back(v[i]), L--;
      reverse(ans.begin(), ans.end());
for (auto i : ans) cout << i << " ";</pre>
9.3 Edit Distance [308023]
int main() {
      string s1, s2; cin >> s1 >> s2;
int n1 = s1.size(), n2 = s2.size();
       // dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元
      cur[j] = dp[j - 1];
                    } else {
                         // s1 新增等價於 s2 砍掉
                           // dp[i][j] = min(s2 新增, 修改, s1 新增);
                          cur[j]
                                   = min({cur[j - 1], dp[j - 1], dp[j]}) + 1;
                   }
             swap(dp, cur);
      cout << dp[n2] << "\n";
9.4 Bitmask [a626f9]
void hamiltonianPath(){
      int n, m; cin >> n >> m;
vector adj(n, vector <int >());
for (int i = 0; i < m; i++) {
    int u, v; cin >> u >> v;
    adj[--v].push_back(--u);
}
      }
// 以...為終點,走過...
vector dp(n, vector<int>(findBit(n)));
dp[0][1] = 1;
for (int mask = 1; mask < findBit(n); mask++) {
    if ((mask & 1) == 0) continue;
    for (int i = 0; i < n; i++) {
        if ((mask & findBit(i)) == 0) continue;
        if (i == n - 1 && mask != findBit(n) - 1) continue;
        int pre_mask = mask ^ findBit(i);
        for (int j : adj[i]) {
                    for (int j : adj[i]) {
   if ((pre_mask & findBit(j)) == 0) continue;
   dp[i][mask
                                   ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
                   }
             }
      cout << dp[n - 1][findBit(n) - 1] << "\n";</pre>
void elevatorRides() {
      int n, x; cin >> n >> x; vector<int> a(n);
for (int i = 0; i < n; i++) cin >> a[i];
vector<array<int, 2>> dp(findBit(n));
dp[0][0] = 1; // 次數、已使用人數
for (int mask = 1; mask < findBit(n); mask++) {
```

&& $dp[pre_mask][1] + a[i] < dp[mask][1]) {$

swap(dp[0], dp[1]);

```
dp[mask][0] = dp[pre_mask][0];
dp[mask][1] = dp[pre_mask][1] + a[i];
                                                                                                         cout << dp[0][k] << "\n";
                  9.8 SOS [93cb19]
                                                                                                 | // 使用情況: 跟 bit 與(被)包含有關, 且 x 在 1e6 左右
                                                                                                 |// 題目:一數組,問有多少所有數 & 起來為 Ø 的集合數
                                                                                                 |// dp[x]代表包含 x 的 y 個數(比x大且bit 1全包含 x 的有幾個)
                                                                                                  // 答案應該包含在 dp[0]内,但是有重複元素,所以考慮容斥
// => ans = \sum _{i=0}^{n} (-1)^{pop_count(i)} 2^{dp[i]-1}
// => 全部為θ的個數 - 至少一個為1的個數 + 至少兩個為1的個數
            }
       cout << dp[findBit(n) - 1][0] << "\n";
}
                                                                                                   void solve() {
                                                                                                        int n; cin >> n; Z ans = 0;
vector<int> a(n);
 9.5 Projects [0942aa]
                                                                                                         for (int i = 0; i < n; i++)
 int main() { // 排程有權重問題,輸出價值最多且時間最少
                                                                                                              cin >> a[i];
                                                                                                        cin >> a[i];
int m = __lg(*max_element(a.begin(), a.end())) + 1;
// 定義 dp[mask] 為 mask 被包含於 a[i] 的 a[i] 個數
vector <Z> dp(1 << m);
for (int i = 0; i < n; i++)
    dp[a[i]] += 1;
for (int i = 0; i < m; i++)
    for (int mask = 0; mask < 1 << m; mask++)
        if (mask >> i & 1) {
            int pre = mask ^ (1 << i);
            dp[pre] += dp[mask];
        }
 struct E {
       int from, to, w, id;
       bool operator < (const E &rhs) {</pre>
             return to == rhs.to ? w > rhs.w : to < rhs.to;
      int n; cin >> n; vector <E> a(n + 1);
for (int i = 1; i <= n; i++) {
   int u, v, w; cin >> u >> v >> w;
   a[i] = {u, v, w, i};
       vector<array<ll, 2>> dp(n + 1); // w, time
      vector darray <int, 2>> rec(n + 1); // 有沒選, 上個是誰
sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
    auto it = --lower_bound(all(a), E({0, a[i].from}),
                                                                                                         for (int mask = 0; mask < 1 << m; mask++) {
   int sgn = __builtin_popcount(mask) & 1 ? -1 : 1;
   ans += sgn * (power(Z(2), dp[mask].val()) - 1);</pre>
            cout << ans << "\n";
                                                                                                  9.9 CHT [5f5c25]
                   dp[i] = {nw, nt}; rec[i] = {1, id};
                                                                                                 |// 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \le r(i)
                                                                                                  A(j), B(j) 可能包含 dp(j), 分別就是 m 跟 b struct Line {
      }
vector < int > ans;
for (int i = n; i != 0;) {
    if (rec[i][0]) {
        ans.push_back(a[i].id);
        i = confil[1];
}
                                                                                                         ll m,
                                                                                                         Line(ll m = 0, ll b = 0) : m(m), b(b) {}
ll eval(ll x) {
    return m * x + b;
                   i = rec[i][1];
            } else i--:
                                                                                                  1:
      }
                                                                                                  struct CHT { // 用在查詢單調斜率也單調
  int n, lptr, rptr; vector<Line> hull;
  CHT(int n_ = 0, Line init_ = Line()) {
}
 9.6 Removal Game [7bb56b]
                                                                                                              init(n_, init_);
| // 兩個人比賽,每個人輪流取一個數字且只能是頭尾
                                                                                                         void init(int n_ = 0, Line init_ = Line()) {
    n = n_; hull.resize(n); reset(init_);
 // 問兩人都選得好,第一出手的人可取得的最大分數
 int main() {
      int n; cin >> n;
vector<ll> a(n);
for (int i = 0; i < n; i++) cin >> a[i];
                                                                                                         void reset(Line init_ = Line()) {
   lptr = rptr = 0; hull[0] = init_;
       vector dp(n, vector<ll>(n)); // i 到 j 區間的最大 diff
                                                                                                         // 代表查詢的當下,右線段的高度已經低於左線段了
                                                                                                               return l1.eval(x) >= l2.eval(x);
                         max(a[i] - dp[i + 1][j], a[j] - dp[i][j - 1]);
                                                                                                         bool pop_back(Line &l1, Line &l2, Line &l3) {
                                                                                                              // 本題斜率遞減、上凸包
       \frac{1}{x + y} = sum; // x - y = dp[0][n - 1]
                                                                                                              // 因此只要 12 跟
       cout << (accumulate
              (a.begin(), a.end(), 0LL) + dp[0][n - 1]) / 2 << "\n";
                                                                                                              l3 的 X 交點 <= l1 跟 l3 的 X 交點, l2 就用不到了
return (l3.b - l2.b)
* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
}
          Monotonic Queue [f4976d]
                                                                                                         void insert(Line L) {
 // 應用: dp(i) = h(i) + max(A(j)), for l(i) \le j \le r(i)
                                                                                                              // A(j) 可能包含 dp(j), h(i) 可 O(1)
void Bounded_Knapsack() {
                                                                                                              hull[++rptr] = L;
      int n, k; // O(①k)
vector < int > w(n), v(n), num(n); deque < int > q;
// 於是我們將同餘的數分在同一組
                                                                                                        // 每次取出連續 num[i] 格中最大值
      // 每次取出煙纜 num[i] 格甲最大值
// g_x = max(_{k=0}^num[i] (g'_{x-k} + v_i*k))
// G_x = g'_{x} - v_i*x
// x 代 x-k => v_i*(x-k)
// g_x = max(_{k=0}^num[i] (G_{x-k} + v_i*x))
vector<vector<ll>> dp(2, vector<ll>(k + 1));
for (int i = 0; i < n; i++) {
                                                                                                              return hull[lptr].eval(x);
                                                                                                        }
                                                                                                 };
                                                                                                  9.10 DNC [61c639]
             for (int r = 0; r < w[i]; r++) { // 餘數
                  q.clear(); // q 記錄在 x = i 時的 dp 有單調性
for (int x = 0; x * w[i] + r <= k; x++) {
    while (!q.empty() && q.front() < x - num[i])
                                                                                                  // 應用: 切 k 段問題, 且滿足四邊形不等式
                                                                                                  // 應用: 切 k 段問題,且滿足四邊形不等式
// w(a,c) + w(b,d) ≤(z) w(a,d) + w(b,c)
// dp[k][j] = min(dp[k - 1][i] + cost[i][j])
// cost: (i, j]
constexpr int N = 3e3 + 5;
constexpr ll inf = 4e18;
ll dp[N][N]; // 1-based
ll get_cost(int l, int r) {}
void DNC(int k, int l, int r, int optl, int optr) {
    if (l > r) return;
    int m = (l + r) >> 1, opt = -1;
    dp[k][m] = inf;
    for (int i = max(k, optl); i <= min(m, optr); i++) {
        // 注意 i 的範圍 > aet cost 與 dp 的邊界
    }
                        q.pop_back();
                        q.push_back(x);
dp[1][x * w[i] + r] = dp[0][q.front()
    * w[i] + r] - q.front() * v[i] + x * v[i];
                  }
```

// 注意 i 的範圍、 *get_cost* 與 *dp* 的邊界 ll cur = dp[k - 1][i] + get_cost(i, m);

9.11 LiChaoSegmentTree [f23ef4]

```
// 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \leq r(i)
constexpr il inf = 4e18;
struct Line {
    ll m, b;
      Line(ll m = 0, ll b = inf) : m(m), b(b) {}
      ll eval(ll x) const { return m * x + b; }
struct LiChaoSeg { // 取 max 再變換就好
     int n;
vector < Line > info;
LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_) {
            info.assign(4 << __lg(n), Line());</pre>
     void update(Line line, int node, int l, int r) {
   int m = (l + r) / 2;
   bool left = line.eval(l) < info[node].eval(l);
   bool mid = line.eval(m) < info[node].eval(m);</pre>
            if (mid) swap(info[node], line); // 如果新線段比較好
           if (r - l == 1) return;
else if (left != mid) update(line, 2 * node, l, m);
            // 代表左半有交點
            else update(line, 2 * node + 1, m, r);
            // 代表如果有交點一定在右半
     void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
   if (r - l == 1) return info[node].eval(x);
   int m = (l + r) / 2;
           if (x < m) return
    min(info[node].eval(x), query(x, 2 * node, l, m));</pre>
                  info[node].eval(x), query(x, 2 * node + 1, m, r));
      il query(int x) { return query(x, 1, 0, n); }
```

9.12 Codeforces Example [7d37ea]

```
| // CF 1932 pF
// 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
// 請問在線段不重複的情況下,最多獲得幾分
int main() {
    int n, m;
cin >> n >> m;
     // 記錄每點有幾個線段
     // 再一個紀錄,包含這個點的左界
    cnt[l]++;
         cnt[r + 1]--;
    for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
     for (int i = n; i >= 2; i--) {
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
     vector<int> dp(n + 1);
    dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
         dp[i] = cnt[i];
if (l_side[i] != inf) {
    dp[i] += dp[l_side[i] - 1];
         dp[i] = max(dp[i], dp[i - 1]);
     cout << dp[n] << "\n";
}
// CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
// 再加上 max(bi) - min(bi)
int main(){
   int n, k, ans = 0; cin >> n >> k;
    vector < pii > v(n + 1);
```

10 Geometry

10.1 Basic [d41d8c]

```
template < class T >
struct Point {
     Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) {}
     template < class U>
     operator Point<U>() {
         return Point <U >(U(x), U(y));
     Point &operator+=(const Point &p) & {
    x += p.x; y += p.y; return *this;
     Point &operator -= (const Point &p) & {
    x -= p.x; y -= p.y; return *this;
     Point &operator*=(const T &v) & {
    x *= v; y *= v; return *this;
     Point & operator /= (const T & v) & {
         x /= v; y /= v; return *this;
     Point operator - () const {
          return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
          return a += b;
     friend Point operator - (Point a, const Point &b) {
          return a -= b;
     friend Point operator*(Point a, const T &b) {
          return a *= b;
     friend Point operator/(Point a, const T &b) {
          return a /= b;
     friend Point operator*(const T &a, Point b) {
   return b *= a;
     friend bool operator == (const Point &a, const Point &b) {
          return a.x == b.x && a.y == b.y;
     friend istream &operator>>(istream &is, Point &p) {
          return is >> p.x >> p.y;
     friend ostream & operator << (ostream & os, const Point & p) {
    return os << "(" << p.x << ", " << p.y << ")";</pre>
};
template < class T>
struct Line {
     Point <T>
     Point<T> b;
Line(const Point<T> &a_ = Point<T>()
           , const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
template < class T>
T dot(const Point<T> &a, const Point<T> &b) {
     return a.x * b.x + a.y * b.y;
T cross(const Point<T> &a, const Point<T> &b) {
   return a.x * b.y - a.y * b.x;
template < class T >
T square(const Point < T > &p) {
   return dot(p, p);
template < class T>
double length(const Point<T> &p)
    return sqrt(double(square(p)));
```

```
template < class T>
double length(const Line<T> &l) {
      return length(l.a - l.b);
Point<T> normalize(const Point<T> &p) {
      return p / length(p);
template < class T >
bool parallel(const Line < T > &l1, const Line < T > &l2) {
    return cross(l1.b - l1.a, l2.b - l2.a) == 0;
template < class T>
double distance(const Point<T> &a, const Point<T> &b) {
      return length(a - b);
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)
      return distance(p, l.a);
   if (dot(p - l.b, l.a - l.b) < 0)
      return distance(p, l.b);
}</pre>
      return distancePL(p, l);
 template<class T>
Point<T> rotate(const Point<T> &a) {
      return Point(-a.y, a.x);
Jemplate < class T >
int sgn(const Point < T > & a) {
    return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
template < class T>
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
      return cross(l.b - l.a, p - l.a) > 0;
template < class T>
Point < T
       > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
return l1.a + (l1.b - l1.a) * (cross(l2.b - l2.a, l1.a - l2.a) / cross(l2.b - l2.a, l1.a - l1.b));
template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
      return cross(p - l.a, l.b - l.a) == 0 &&
min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)
             && min
                     (l.a.y, l.b.y) \ll p.y \ll max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
      (const Point<T> &a, const vector<Point<T>> &p) {
int n = p.size(), t = θ;
for (int i = θ; i < n; i++) {</pre>
             if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {
                   return true:
      for (int i = 0; i < n; i++) {
    auto u = p[i];</pre>
             auto v = p[(i + 1) \% n];
             if (u.x < a.
                    x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
t ^= 1;
             return t == 1:
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
          intersect at endpoint
template < class T>
(const Line<T> &l1, const Line<T> &l2) {
   if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
      return {0, Point<T>(), Point<T>()};
   if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
      return {0, Point<T>(), Point<T>()};
   if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y))
      return {0, Point<T>(), Point<T>()};
   if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y))
      return {0, Point<T>(), Point<T>()};
   if (cross(l1.b - l1.a, l2.a - l1.a) != 0) {
      return {0, Point<T>(), Point<T>());
   }
}
                   return {0, Point<T>(), Point<T>()};
             auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
auto miny1 = min(l1.a.y, l1.b.y);
auto maxy2 = max(l2.a.x, l2.b.x);
                    auto minx2 = min(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.y, l2.b.y);
auto miny2 = min(l2.a.y, l2.b.y);
                    Point<T> p1(max(minx1, minx2), max(miny1, miny2));
```

```
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
if (!pointOnSegment(p1, l1))
               swap(p1.y, p2.y);
if (p1 == p2) {
    return {3, p1, p2};
                } else {
                     return {2, p1, p2};
         }
    }
    auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);

auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);

auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);

auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);

if ((cp1 > 0 && cp2 > 0) || (cp1 < 0 && cp2
     return {1, p, p};
     } else {
          return {3, p, p};
template < class T>
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
     if (get<0>(segmentIntersection(l1, l2)) != 0)
          return 0.0;
     return min({distancePS(l1.a, l2), distancePS(l1
           .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
bool segmentInPolygon
      (const Line<T> &l, const vector<Point<T>> &p) {
     int n = p.size();
     if (!pointInPolygon(l.a, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
for (int i = 0; i < n; i++) {
    auto u = p[i];
}</pre>
          auto v = p[(i + 1) % n];
auto w = p[(i + 2) % n];
          auto w = pl(t + 2) % n];
auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
if (t == 1) return false;
if (t == 0) continue;
if (t == 2) {
                if (pointOnSegment(v, l) && v != l.a && v != l.b)
   if (cross(v - u, w - v) > 0)
       return false;
                if (p1 != u && p1 != v) {
                     if (pointOnLineLeft(l.a, Line(v, u))
                          || pointOnLineLeft(ĺ.b, Line(v, u)))
               return false;
} else if (p1 == v) {
   if (l.a == v) {
                          if (pointOnLineLeft(u, l)) {
    if (pointOnLineLeft(w, l)
        && pointOnLineLeft(w, Line(u, v)))
                                     return false;
                          } else {
    if (pointOnLineLeft(w, l)
                                     || pointOnLineLeft(w, Line(u, v)))
                                     return false;
                    return false;
                          || pointOnLineLeft(w, Line(u, v)))
                                     return false;
                    || pointOnLineLeft(w, Line(u, v)))
                                     return false:
                          }
                    }
               }
         }
     return true;
vector<Point<T>> hp(vector<Line<T>> lines) {
     sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
   auto d1 = l1.b - l1.a;
   auto d2 = l2.b - l2.a;
}
          if (sgn(d1) != sgn(d2))
    return sgn(d1) == 1
         return cross(d1, d2) > 0;
     deque<Line<T>> ls;
     deque<Point<T>> ps;
     for (auto l : lines) {
```

```
if (ls.empty()) {
    ls.push_back(l);
               continue;
          while (!ps.empty() && !pointOnLineLeft(ps.back(), l))
          ps.pop_back(), ls.pop_back();
while (!ps.empty() && !pointOnLineLeft(ps[0], l))
    ps.pop_front(), ls.pop_front();
if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
               if (dot
                      (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                     if (!pointOnLineLeft(ls.back().a, l)) {
                          assert(ls.size() == 1);
                          ls[0] = l;
                     continue;
               return {};
          ps.push_back(lineIntersection(ls.back(), l));
          ls.push_back(l);
     while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0]))
     ps.pop_back(), ls.pop_back();
if (ls.size() <= 2) return {};</pre>
     ps.push_back(lineIntersection(ls[0], ls.back()));
     return vector(ps.begin(), ps.end());
using P = Point<ll>;
```

10.2 Convex Hull [b5758d]

```
int main() {
     int n; cin >> n;
vector<P> P(n), U, L;
for (int i = 0; i < n; i++) {</pre>
            cin >> P[i];
      sort(P.begin(), P
             .end(), [](const Point<i64> &a, const Point<i64> &b) {
            return a.x == b.x ? a.y < b.y : a.x < b.x;
      for (int i = 0; i < n; i++) {
    while (L.size() >= 2 && cross(L.back() -
        L[L.size() - 2], P[i] - L[L.size() - 2]) <= 0LL) {</pre>
                  L.pop_back();
            while (U.size() >= 2 && cross(U.back() -
     U[U.size() - 2], P[i] - U[U.size() - 2]) >= 0LL){
                  U.pop_back();
            if (L.
                   empty() || !(L.back() == P[i])) L.push_back(P[i]);
            if (U.
                   empty() || !(U.back() == P[i])) U.push_back(P[i]);
     if (L.size() <= 2 && U.size() <= 2) {
    // No Hull
     cout << L.size() + U.size() - 2 << "|n";
for (int i = 0; i < L.size() - 1; i++) {
    cout << L[i].x << " " << L[i].y << "|n";</pre>
      for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << "\n";</pre>
```

10.3 MinEuclidean Distance [3020bc]

```
T distanceSquare(const Point<T> &a, const Point<T> &b) {
     return square(a - b);
void solve() {
     int n; cin >> n;
constexpr ll inf = 8e18;
vector<Point<ll>> a(n);
     for (int i = 0; i < n; i++) {
    ll x, y;
    cin >> x >> y;
    a[i] = Point<ll>(x, y);
      struct sortY {
                  ()(const Point<ll> &a, const Point<ll> &b) const {
                 return a.y < b.y;</pre>
          }
     struct sortXY {
           bool operator
                  ()(const Point<ll> &a, const Point<ll> &b) const {
                 if (a.x == b.x) return a.y < b.y;
else return a.x < b.x;</pre>
           }
     sort(a.begin(), a.end(), sortXY());
vector<Point<ll>>> t(n);
     auto devide = [&](auto &&self, int l, int r) -> ll {
   if (l == r) return inf;
   int m = (l + r) / 2;
           ll ans = min(self(self, l, m), self(self, m + 1, r));
```

```
ll midval = a[m].x;
           ll midvai - oi...
ll p = 0;
for (int i = l; i <= r; i++) {
   if ((midval - a[i].x) * (midval - a[i].x) <= ans) {
      t[p++] = a[i];
}</pre>
           for (int j = i + 1; j < p; j++) {
    ans = min(ans, distanceSquare(t[i], t[j]));
}</pre>
                       if ((t[i].y
                                t[j].y) * (t[i].y - t[j].y) > ans) break;
                 }
            return ans;
      1:
      cout << devide(devide, 0, n - 1) << "\n";
}
10.4 LatticePoints [00db9d]
```

```
int main() {
      // Polygun 內整數點數
      int n; cin >> n;
vector<Point<ll>> polygon(n);
      for (int i = 0; i < n; i++) cin >> polygon[i]; ll area = 0;
       for (int i = 0; i < n; i++) {</pre>
            area += cross(polygon[i], polygon[(i + 1) % n]);
      area = abs(area):
      auto countBoundaryPoints
              = [](const vector<Point<ll>>& polygon) -> ll {
            ll res = 0;
            int n = polygon.size();
            for (int i = 0; i < n; i++) {
    ll dx = polygon[(i + 1) % n].x - polygon[i].x;
    ll dy = polygon[(i + 1) % n].y - polygon[i].y;</pre>
                 res += std::gcd(abs(dx), abs(dy));
            return res:
      };
ll res = countBoundaryPoints(polygon);
      ll ans = (area - res + 2) / 2;
cout << ans << " " << res << " | n ";
```

10.5 MinCoverCircle [c9ca81]

```
template < class T>
pair < T, Point < T >> MinCircular (vector < Point < T >> &a) {
      random_shuffle(a.begin(), a.end());
      int n = a.size();
      Point<T> c = a[0]; T r = 0;
for (int i = 1; i < n; i++) {
   if (T(length(c - a[i]) - r) > 0.0) {
              p + rotate(a[j] - a[i])), Line
  (q, q + rotate(a[k] - a[j])));
r = length(c - a[i]);
                                }
                           }
                     }
                }
          }
      return make_pair(r, c);
}
```