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```

1 Basic

1.1 install vscode [d41d8c]

1.2 default code [3cd57c]

```
#include <bits/stdc++.h>
#define all(x) (x).begin(), (x).end()
#define pii pair<int, int>
using namespace std;
using ll = long long;
const int mod = 1e9 + 7;

void solve() {
}

int main() {
   ios_base::sync_with_stdio(0);
   cin.tie(nullptr);
   int t = 1;
   cin >> t;
   while (t--) {
      solve();
   }
}
```

1.3 compare fuction [4bc3e0]

```
}:
struct cmp {
    vector < int > &v;
                  // 要在 template 的資結用外部變數
     cmp(vector<int>& vec) : v(vec) {}
bool operator() (int a, int b) const {
   return v[a] > v[b];
// main: cmp cmp1(vector);
// math. cmp cmp1(vector),
// priority_queue<int, vector<int>, cmp> pq(cmp1);
};
1.4 pbds [e28ae8]
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template<typename T>
using pbds_set = tree<T, null_type,</pre>
       less<T>, rb_tree_tag, tree_order_statistics_node_update>;
1.5 浮點數誤差 [a0d4e5]
struct EDouble {
     constexpr static double Eps = 1e-9;
constexpr EDouble() : x{} {}
constexpr EDouble(double v) : x{v} {}
     constexpr double val() const {
         return x:
     explicit constexpr operator double() const {
         return x;
     constexpr EDouble operator-() const {
         return EDouble(-x);
     constexpr EDouble &operator+=(const EDouble &rhs) & {
         x += rhs.x
         return *this:
     constexpr EDouble &operator -=(const EDouble &rhs) & {
         x -= rhs.x;
return *this;
     constexpr EDouble &operator*=(const EDouble &rhs) & {
         x *= rhs.x:
         return *this;
     constexpr EDouble &operator/=(const EDouble &rhs) & {
   assert(fabs(rhs.x) > Eps);
         x /= rhs.x;
         return *this;
           EDouble operator+(EDouble lhs, const EDouble &rhs) {
         lhs += rhs;
     friend constexpr
           EDouble operator - (EDouble lhs, const EDouble &rhs) {
         lhs -= rhs;
         return lhs:
           EDouble operator*(EDouble lhs, const EDouble &rhs) {
         lhs *= rhs;
         return lhs;
     friend constexor
           EDouble operator/(EDouble lhs, const EDouble &rhs) {
         lhs /= rhs;
return lhs;
     friend constexpr bool
           operator < (const EDouble &lhs, const EDouble &rhs) {</pre>
         return lhs.x - rhs.x < -Eps:
     friend constexpr bool
           operator > (const EDouble &lhs, const EDouble &rhs) {
         return lhs.x - rhs.x > Eps;
     friend constexpr bool
    operator==(const EDouble &lhs, const EDouble &rhs) {
         return fabs(lhs.x - rhs.x) < Eps;</pre>
     friend constexpr bool
           operator <= (const EDouble &lhs, const EDouble &rhs) {</pre>
         return lhs < rhs || lhs == rhs;</pre>
     friend constexpr bool
           operator >=(const EDouble &lhs, const EDouble &rhs) {
         return lhs > rhs || lhs == rhs;
           operator!=(const EDouble &lhs, const EDouble &rhs) {
         return !(lhs == rhs);
     friend istream & operator >> (istream &is, EDouble &a) {
```

2 Graph

2.1 DFS 跟 BFS [cdd1d5]

```
int main() {
       vector<vector<int>> adj(n + 1, vector<int>());
       // dfs_graph
vector<bool> vis(n + 1, 0);
auto dfs = [&](auto self, int u) -> void {
    if (vis[u]) return;
    vis[u] = true;
               for (auto v: adj[u]) {
    self(self, v);
              }
       dfs(dfs, 1);
       // bfs
vector < int > depth(n + 1, 1e9);
       queue <int> depth(u + 1, 1e9),
queue <int> q;
auto bfs = [&](auto self, int u) -> void {
   vis[u] = true;
   depth[u] = 0;
               q.push(u);
while (!q.empty()) {
                       int u = q.front(); q.pop();
                      for (auto v : adj[u]) {
    if (vis[v]) continue;
    vis[v] = true;
    depth[v] = depth[u] + 1;
                              q.push(v);
                      }
              }
       bfs(bfs, 1);
}
```

2.2 Prim [f00ec0]

2.3 BellmanFord [430ded]

```
if (i == n) t = v;
}

}
if (t == -1) { cout << "NO\n"; return; }
for (int i = 1; i < n; i++) t = par[t];
vector<int> ans {t};
int i = t;
do {
    i = par[i];
    ans.push_back(i);
} while (i != t);
reverse(ans.begin(), ans.end());
cout << "YES\n";
for (auto x : ans) cout << x + 1 << " ";</pre>
```

2.4 負權最大距離 [2148ca]

```
CSES High Score
void dfs(int u, vector<int> &vis, vector<vector<int>> &adj) {
      if (vis[u]) return;
      vis[u] = 1;
for (int v : adj[u]) {
           dfs(v, vis, adj);
     }
signed main() {
   int n, m; cin >> n >> m;
   vector<array<int, 3>> edges;
      vector<vector<int>> adj(n + 1);
      vector < int > dis(n + 1), vis(n + 1);
while (m--) {
           int u, v, w;
cin >> u >> v >> w;
edges.push_back({u, v, w});
           adj[u].push_back(v);
      }
fill(dis.begin(), dis.end(), -1e18);
      dis[1] = 0;
for (int i = 1; i <= n; i++) {
           for (auto [u, v, w] : edges) {
   if (dis[u] != -1e18 && dis[v] < dis[u] + w) {
      dis[v] = dis[u] + w;
}</pre>
                             i == n) {
dfs(v, vis, adj);
                       if (i
                       }
                 }
           }
      if (vis[n]) cout << -1;</pre>
      else cout << dis[n];</pre>
}
```

2.5 FloydWarshall [206b76]

```
const int inf = 1e18:
int main() {
       int n, m, q; cin >> n >> m;
vector <vector <int>> graph(n + 1, vector <int>(n + 1, inf));
vector <vector <int>> dis(n + 1, vector <int>(n + 1));
for (int i = 0; i < m; i++) {</pre>
             int u, v, w; cin >> u >> v >> w;
cin >> u >> v >> w;
graph[u][v] = min(graph[u][v], w);
              graph[v][u] = min(graph[v][u], w);
       for (int i = 0; i <= n; i++) {
             for(int j = 0; j <= n; j++) {
    dis[i][j] = graph[i][j];</pre>
       for (int i = 0; i <= n; i++) // 自己到自己是 0
             dis[i][i] = 0;
       for (int k = 1; k <= n; k++) {</pre>
             for (int i = 1; i <= n; i++) {
    for (int j = 1; j <= n; j++) {
        dis[i][j</pre>
                                  ] = min(dis[i][j], dis[i][k] + dis[k][j]);
            }
       for (int i = 0; i < q; i++) {</pre>
             int u, v; cin >> u >> v;
cout << (dis[u][v] >= inf ? -1 : dis[u][v]) << "\n";</pre>
}
```

2.6 <u>歐拉環與歐拉路</u> [0911ed]

```
adj[now].erase(nxt);
             dfs(nxt, road);
      road.push_back(now);
void solve() {
      cin >> n >> m;
in.assign(n + 1, 0);
adj.assign(n + 1, set<int>());
for (int i = 1; i <= m; i++) {
   int u, v; cin >> u >> v;
             adj[u].insert(v);
             in[v]++;
     }
in[1]++;
     in[1]++;
in[n]--;
for (int i = 1; i <= n; i++) {
    if(adj[i].size() != in[i]) {
        cout << "IMPOSSIBLE";
        caturn:</pre>
            }
      vector<int> road;
      dfs(1, road);
if (road.size() != m + 1) {
            cout << "IMPOSSIBLE";</pre>
             return:
       for(auto i : road) cout << i <<</pre>
2.7 SCC [5d3e16]
```

```
struct SCC {
     int n, cur, cnt;
vector<vector<int>> adj;
     vector <int> stk, dfn, low, bel;
SCC(int n_ = 0) {
   init(n_);
     void init(int n_) {
          n = n_;
adj.assign(n, {});
          dfn.assign(n, -1);
          low.resize(n);
          bel.assign(n, -1);
          stk.clear();
          cur = cnt = 0;
     void addEdge(int u, int v) {
          adj[u].push_back(v);
     void dfs(int x) {
          dfn[x] = low[x] = cur++;
          stk.push_back(x);
for (auto y : adj[x]) {
    if (dfn[y] == -1) {
                     dfs(y);
                     low[x] = min(low[x], low[y]);

se if (bel[y] == -1) {

low[x] = min(low[x], dfn[y]);
               }
          if (dfn[x] == low[x]) {
                int y;
do {
                     y = stk.back();
               bel[y] = cnt;
stk.pop_back();
while (y != x);
                cnt++;
          }
     vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
          return bel;
     struct Graph {
          int n;
          vector<pair<int, int>> edges;
          vector<int> siz;
          vector<int> cnte;
     Graph compress() {
          Graph g;
g.n = cnt;
          g.siz.resize(cnt);
          g.cnte.resize(cnt);
          g.edges.emplace_back(bel[i], bel[j]);
                     } else {
                          g.cnte[bel[i]]++;
               }
          return g;
```

```
}: }
```

2.8 VBCC [170604]

```
struct VBCC {
       int n, cur;
vector<vector<int>> adj;
       vector<vector<int>> adj;
vector<int> dfn, low, parent;
vector<bool> is_cut;
VBCC(int n_ = 0) {
   init(n_);
       void init(int n_) {
             n = n;
             adj.assign(n, {});
dfn.assign(n, -1);
low.resize(n);
              parent.assign(n, -1);
              is_cut.assign(n, false);
             cur = 0:
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       children++;
                           parent[v] = x;
                           dfs(v);
low[x] = min(low[x], low[v]);
                           if (parent[x] != -1 && low[v] >= dfn[x]) {
   is_cut[x] = true;
                    } else if (v != parent[x]) {
    low[x] = min(low[x], dfn[v]);
             if (parent[x] == -1 && children > 1) {
    is_cut[x] = true;
      }
void work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i);
        }
}</pre>
             }
      }
};
```

2.9 EBCC [49d862]

```
struct EBCC { // CF/contest/1986/pF
      int n, cur, cnt;
vector<vector<int>> adj;
      vector<int> stk, dfn, low, bel;
      vector<pair<int, int>> bridges; // 關鍵邊
      EBCC(int n_) {
            init(n_);
      void init(int n_) {
            n = n_;
adj.assign(n, {});
            dfn.assign(n, -1);
             low.resize(n);
            bel.assign(n, -1);
            stk.clear():
            bridges.clear();
            cur = cnt = 0;
      void addEdge(int u, int v) {
   adj[u].push_back(v);
            adj[v].push_back(u);
      void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
           dfn[x] = low[x] = cui++,
stk.push_back(x);
for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
        dfs(y, x);
        low[x] = min(low[x], low[y]);
        if (low[y] > dfn[x]) {
            bridges.emplace_back(x, y)
                               bridges.emplace_back(x, y);
                  } else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
            if (dfn[x] == low[x]) {
                   int y;
do {
                         y = stk.back();
                         bel[y] = cnt;
                         stk.pop_back();
                   } while (y != x);
```

```
cnt++:
          }
     vector < int > work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {</pre>
                     dfs(i, -1);
           return bel;
      struct Graph {
           int n;
           vector<pair<int, int>> edges;
           vector<int> siz; // BCC 內節點數
           vector<int> cnte; // BCC 內邊數
     Graph compress() {
          Graph g;
g.n = cnt;
           g.siz.resize(cnt);
           g.cnte.resize(cnt);
           for (int i = 0; i < n; i++) {
                g.siz[bel[i]]++;
                for (auto j : adj[i]) {
    if (bel[i] < bel[j]) {</pre>
                     g.edges.emplace_back(bel[i], bel[j]);
} else if (i < j) {</pre>
                          g.cnte[bel[i]]++;
               }
           return g;
     }
};
```

2.10 2-SAT [eeddc1]

```
/ CSES Giant Pizza
struct TwoSat {
     int n;
      vector<vector<int>> e;
     bool satisfiable() {
            vector<int
                  > id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
            vector<int> stk;
int now = 0, cnt = 0;
function<void(int)> tarjan = [&](int u) {
                  stk.push_back(u);
                 stk.push_back(u);
dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
        tarjan(v);
        low[u] = min(low[u], low[v]);
    } else if (id[v] == -1) { // in stk
        low[u] = min(low[u], dfn[v]);
}
                        }
                  if (dfn[u] == low[u]) {
                        int v;
do {
    v = stk.back();
                        stk.pop_back();
id[v] = cnt;
} while (v != u);
                        ++cnt:
                 }
            for (int i
            vector < bool > answer() { return ans; }
int main() {
      int m, n; cin >> m >> n;
TwoSat ts(n);
for (int i = 0; i < m; ++i) {</pre>
           int u, v; char x, y;
cin >> x >> u >> y >> v;
ts.addClause(u - 1, x == '+', v - 1, y == '+');
      if (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";</pre>
      else cout << "IMPOSSIBLE\n";</pre>
```

// 保證出度是 1 所以對 1 個點來說,從他出發只可能遇到一個環int n, q; int dp[200005][30]; // 倍 vector<vector<int>>> cycles; // 倍增表 vector<**int** > no, cycle_idx, vis; // Order & Can be in cycle, void set_out_of_cycle_no(int now, unordered_set<int> &done) { if (done.find(now)!= done.end()) return; set_out_of_cycle_no(dp[now][0], done); done.insert(now); // post order no[now] = no[dp[now][0]] - 1; int wiint_go_to(int u, int k) { // 回傳當 u 走 k 步時會到的地方 for (int i = 0; i <= 18; i++) { if (k & (1 << i)) { u = dp[u][i]; return u; void find cycle(int now) { unordered_set<int> appear; vector<int> v; bool flag = true; // 代表有環 while (appear.find(now) == appear.end()) { appear.insert(now); v.push_back(now); if (vis[now]) { flag = false; break; now = dp[now][0];for (auto i : v) vis[i] = true; if (!flag) return; // now 是環的起點,我們先找到他在 v 的哪裡 int z = find(v.begin(), v.end(), now) - v.begin(); vector<int> cycle(v.begin() + z, v.end()); cycles.push_back(cycle); int main() { cin >> n >> q; no.assign(n + 1, -1); cycle_idx.assign(n + 1, -1); vis.assign(n + 1, 0); for (int u = 1; u <= n; u++) cin >> dp[u][0]; for (int i = 1; i <= 18; i++) // 倍增表 for (int u = 1; u <= n; u++) dp[u][i] = dp[dp[u][i - 1]][i - 1]; for (int i = 1; i <= n; i++) {

if (!vis[i]) find_cycle(i);

int idx = 0:

unordered_set < int > done;

for (auto &i : cycles) {

vector<int> dis. v: vector<bool> vis;

queue < int > path;
void dfs(int x) { path.push(x); if (vis[x]) {
 step += dis[x];

step++;

dfs(v[x]);

int main() {
 int n; cin >> n;

vis[x] = true:

// count path_dis to rep

cin >> v[i];

step = 0;

cout << '\n';

int n; cin >> n;
v.assign(n + 1, 0);
dis.assign(n + 1, 0);
vis.assign(n + 1, false);
for (int i = 1; i <= n; i++) {</pre>

for (int i = 1; i <= n; i++) {

int is_outof_cycle = 1;

for (int i = 1; i <= n; i++) {
 cout << dis[i] << ' ';</pre>

2.12 Planet Queries II [872f72]

| // 在有向圖中,從 A 到 B 的最短距離

dfs(i);
while (!path.empty()) {
 if (path.front() == path.back()) {
 is out of cvcle = 0;
}

is_outof_cycle = 0;

dis[path.front()] = step; step -= is_outof_cycle;
path.pop();

int step;

2.11 Planets Cycles [71ac0e]

```
for (auto &j : i) {
    no[j] = c++;
    cycle_idx[j] = idx;
    done.insert(j);
          idx++:
     for (int i = 1; i <= n; i++) set_out_of_cycle_no(i, done);
for (int i = 1; i <= q; i++) {
   int u, v; cin >> u >> v;
          // 在同個環內
if (cycle_idx[u] == cycle_idx
[v] && cycle_idx[u] != -1 && cycle_idx[v] != -1) {
                int cyc_size = cycles[cycle_idx[u]].size();
               cout <<
                     (no[v] - no[u] + cyc_size) % cyc_size << "\n";</pre>
          // 都不再環內
          continue:
               if (wiint_go_to(u, no[v] - no[u]) == v) {
    cout << no[v] - no[u] << "\n";</pre>
               else cout << -1 << "\n";
          else if (cycle_idx[u]
                == -1 && cycle_idx[v] != -1) { // v 在環內,二分搜
               int l = -1, r = n;
               l <= n) { // 如果 n 步內可以到
int in_cycle_of_u = wiint_go_to(u, l);
int cycle_size = cycles[cycle_idx[v]].size();
               if (l <= n) {
                     cout << l + (no[v] - no[in_cycle_of_u
] + cycle_size) % cycle_size << "\n";
               else cout << -1 << "\n";
          }
          else { // u 在環內 b 不在,直接不可能 cout << -1 << "\n";
     }
}
```

3 Data Structure

3.1 BIT [d41d8c]

```
template <typename T>
struct Fenwick { // 全部以 0 based 使用
     int n;
     vector<T> a:
     Fenwick(int n_ = 0) {
          init(n_);
     void init(int n_) {
          a.assign(n, T{});
     void add(int x, const T &v) {
    for (int i = x + 1; i <= n; i += i & -i) {
        a[i - 1] = a[i - 1] + v;
    }
}</pre>
     T sum(int x) { // 左閉右開查詢
          T ans{};
for (int i = x; i > 0; i -= i & -i) {
    ans = ans + a[i - 1];
          return ans;
    T rangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
     int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
          int x = 0;
T cur{};
          for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n && cur + a[x + i - 1] <= k) {</pre>
                    x += i:
                     cur = cur + a[x - 1];
               }
          return x:
    }
template <class T>
struct TwoDFenwick { // 全部以 0 based 使用
    int nx, ny; // row, col 個數
vector < vector < T >> a;
```

```
TwoDFenwick(int nx_ = 0, int ny_ = 0) {
    init(nx_, ny_);
}

void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
}

void add(int x, int y, const T &v) {
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            a[i - 1][j - 1] = a[i - 1][j - 1] + v;
        }
}

T sum(int x, int y) { // 左閉右開查詢
    T ans{};
for (int i = x; i > 0; i -= i & -i) {
        for (int j = y; j > 0; j -= j & -j) {
            ans = ans + a[i - 1][j - 1];
        }
}
return ans;
}
T rangeSum
    (int lx, int ly, int rx, int ry) { // 左閉右開查詢
    return sum(
        rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
}
};
```

3.2 RangeBit [d41d8c]

```
template <typename T>
 struct rangeFenwick { // 全部以 0 based 使用
               int n;
vector<T> d, di;
               rangeFenwick(int n_ = 0) {
                             init(n );
                void init(int n_) {
                             d.assign(n, T{});
                             di.assign(n, T{});
               Joid add(int x, const T &v) {
   T vi = v * (x + 1);
   for (int i = x + 1; i <= n; i += i & -i) {
      d[i - 1] = d[i - 1] + v;
      di[i - 1] = di[i - 1] + v;
}</pre>
                           }
              void rangeAdd(int l, int r, const T &v) {
   add(l, v); add(r, -v);
               T sum(int x) { // 左閉右開查詢
                             T`ans{};
                             for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
                             return ans;
              }
              TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
               int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
                            x += i;
                                                                        cur = cur + val:
                                                          }
                                          }
                             return x;
             }
template <class T>
struct rangeTwoDFenwick { // 全部以 0 based 使用
              int nx, ny; // row, col 個數
vector<vector<T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
                             init(nx_, ny_);
              void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
                             dij.assign(nx, vector<T>(ny, T{}));
```

for (int j = y + 1; j <= ny; j += j & -j) {</pre>

```
d[i - 1][j - 1] = d[i - 1][j - 1] + v;
di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
dij[i - 1][j - 1] = dij[i - 1][j - 1] + vij;
               }
        void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
               add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
       T sum(int x, int y) { // 左閉右開查詢
               T ans{};
for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
                               ans = ans
                              \begin{array}{lll} & - & \text{ans} & + & \text{T(x * y + x + y + 1) * d[i - 1][j - 1];} \\ & + & \text{T(x * y + x + y + 1) * d[i - 1][j - 1];} \\ & \text{ans = ans } - & \text{T(y + 1) * d[i - 1][j - 1];} \\ & \text{ans = ans } + & \text{dij[i - 1][j - 1];} \end{array}
                      }
                return ans;
        .
T rangeSum
                (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                        (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
}:
3.3 DSU [d41d8c]
struct DSU {
        int n;
        vector < int > boss, siz;
        DSU() {}
```

```
DSU(int n_) {
   init(n_);
     void init(int n_) {
           n = n_{j}
           boss.resize(n);
           iota(boss.begin(), boss.end(), 0);
           siz.assign(n, 1);
     int find_boss(int x) {
           if (boss[x] == x) return x;
return boss[x] = find_boss(boss[x]);
     bool same(int x, int y) {
    return find_boss(x) == find_boss(y);
     bool merge(int x, int y) {
    x = find_boss(x);
    y = find_boss(y);
           if (x == y) {
    return false;
           if(siz[x] < siz[y]) swap(x, y);
siz[x] += siz[y];
boss[y] = x;</pre>
           return true;
     int size(int x) {
   return siz[find_boss(x)];
     }
};
struct DSU {
     int n:
     vector < int > boss, siz, stk;
     DSU() {}
DSU(int n_) {
           init(n_);
     void init(int n_) {
           n = n_;
           boss.resize(n);
           iota(boss.begin(), boss.end(), 0);
           siz.assign(n, 1);
           stk.clear();
     int find(int x) {
   return x == boss[x] ? x : find(boss[x]);
     bool same(int x, int y) {
    return find(x) == find(y);
     bool merge(int x, int y) {
    x = find(x);
           y = find(y);
           if (x == y) {
    return false;
           if (siz[x] < siz[y]) swap(x, y);</pre>
           siz[x] += siz[y];
boss[y] = x;
           n - -;
```

```
stk.push_back(y);
     void undo(int x) {
         while (stk.size() > x) {
              int y = stk.back();
              stk.pop_back();
              n++;
              siz[boss[y]] -= siz[y];
              boss[y] = y;
         }
     int size(int x) {
   return siz[find(x)];
};
```

3.4 線段樹 [d41d8c]

```
| template <class Info>
 struct Seg { // 左閉右開寫法
int n; vector xInfo > info;
Seg(): n(0) {}
Seg(int n_, Info v_ = Info()) {
init(n_, v_);
}
        template <class T>
Seg(vector<T> init_) {
              init(init_);
        void init(int n_, Info v_ = Info()) {
  init(vector(n_, v_));
        template <class T>
void init(vector<T> init_) {
              n = init_.size();
              info[p] = init_[l];
                            return:
                     int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                     pull(p);
              build(1, 0, n);
        (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
      info[p] = v;
}
        void pull
                    return;
               int m = (l + r) / 2;
              if (x < m) {
                     modify(2 * p, l, m, x, v);
              } else {
                    modify(2 * p + 1, m, r, x, v);
              pull(p);
        void modify(int p, const Info &i) {
              modify(1, 0, n, p, i);
        Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    return query(p *</pre>
              return query(p
                      2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
              (int ql, int qr) { return query(1, 0, n, ql, qr); }
        template < class F> // 尋找區間內,第一個符合條件的
              (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)
    return -1;
if (l >= x && r <= y && !pred(info[p]))
    return -1;
if (r = l -- 4)</pre>
        int findFirst
              if (r - l == 1)
              if (r - l == 1)
    return l;
int m = (l + r) / 2;
int res = findFirst(2 * p, l, m, x, y, pred);
if (res == -1)
    res = findFirst(2 * p + 1, m, r, x, y, pred);
              return res;
        template < class F> // 若要找 last, 先右子樹遞廻即可
int findFirst(int l, int r, F & pred) {
    return findFirst(1, 0, n, l, r, pred);
 };
// ---define structure and info plus---
 struct Info {
   int n = 1;
        int sum = 0;
```

```
return -1:
Info operator+(const Info &a, const Info &b) {
   return { a.n + b.n, a.sum + b.sum };
                                                                                                                if (l >= x && r <= y && !pred(info[p])) {</pre>
}
                                                                                                                      return -1:
3.5 懶標線段樹 [d41d8c]
                                                                                                                if (r - l == 1) {
                                                                                                                      return l;
template <class Info, class Tag>
struct LazySeg { // 左閉右開寫法
                                                                                                                int m = (l + r) / 2;
     int n;
                                                                                                                push(p);
                                                                                                                int res = findFirst(2 * p, l, m, x, y, pred);
      vector < Info > info:
     res = findFirst(2 * p + 1, m, r, x, y, pred);
                                                                                                          }
     template <class T>
LazySeg(vector<T> init_) {
   init(init_);
                                                                                                          template < class F> // 若要找 last, 先右子樹遞迴即可
int findFirst(int l, int r, F & pred) {
return findFirst(1, 0, n, l, r, pred);
      void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
                                                                                                    };
// ---define structure and info plus---
                                                                                                    struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add; void apply(const Tag& v) {
     template <class T>
void init (vector<T> init_) {
            n = init_.size();
                                                                                                                if (v.set_val) {
            info.assign(4 << __lg(n), Info());
tag.assign(4 << __lg(n), Tag());
function <void(</pre>
                                                                                                                     set_val = v.set_val;
add = v.add;
                  int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
   info[p] = init_[l];
                                                                                                                else {
                                                                                                                      add += v.add;
                                                                                                         }
                                                                                                    };
                  int m = (l + r) / 2;
                                                                                                    struct Info {
                 build(p * 2, l, m);
build(p * 2 + 1, m, r);
                                                                                                          int sum;
void apply(int l, int r, const Tag &v) {
   if (v.set_val) {
      sum = (r - l) * v.set_val;
      .
                 pull(p);
            build(1, 0, n);
                                                                                                                sum += (r - l) * v.add;
      void pull
      (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
                                                                                                          // Info& operator=(const Info &rhs) {
                                                                                                          //
//
// }
                                                                                                                   // 部分 assignment 使用
return *this;
            tag[p].apply(v);
     void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
                                                                                                    };
                                                                                                    Info operator+(const Info &a, const Info &b) {
   return { a.sum + b.sum };
                                                                                                    3.6 莫隊 [d41d8c]
            tag[p] = Tag();
                                                                                                    struct query {
                                                                                                   int l, r, id;
} typedef query;
void MO(int n, vector<query> &queries) {
  int block = sqrt(n);
}
      void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
}
                 return;
                                                                                                          function <bool(query, query)> cmp = [&](query a, query b) {
   int block_a = a.l / block;
   int block_b = b.l / block;
            int m = (l + r) / 2;
push(p, l, r);
if (x < m) {</pre>
                                                                                                                if (block_a != block_b) return block_a < block_b;
return a.r < b.r;</pre>
                  modify(2 * p, l, m, x, v);
                 modify(2 * p + 1, m, r, x, v);
                                                                                                          sort(queries.begin(), queries.end(), cmp);
                                                                                                    void compress(vector<int> &nums) {
            pull(p);
                                                                                                          vector < int > sorted = nums;
sort(sorted.begin(), sorted.end());
      void modify(int p, const Info &i) {
                                                                                                          sorted.erase
           modify(1, 0, n, p, i);
                                                                                                                 (unique(sorted.begin(), sorted.end()), sorted.end());
                                                                                                          for (int i = 0; i < nums.size(); i++) {
  nums[i] = lower_bound(sorted.begin
          (), sorted.end(), nums[i]) - sorted.begin() + 1;</pre>
      Info query(int p, int l, int r, int ql, int qr) {
   if (qr <= l || ql >= r) return Info();
   if (ql <= l && r <= qr) return info[p];</pre>
            int m = (l + r) / 2;
push(p, l, r);
            return query(p *
2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
                                                                                                    3.7 Treap [d41d8c]
      Info query
                                                                                                    struct Treap {
             (int ql, int qr) { return query(1, 0, n, ql, qr); }
                                                                                                          Treap *lc, *rc;
int pri, siz; bool rev_valid;
int val; int min;
     void range_apply
   (int p, int l, int r, int ql, int qr, const Tag &v) {
   if (qr <= l || ql >= r) return;
   if (ql <= l && r <= qr) {</pre>
                                                                                                          Treap(int val_) {
                                                                                                                min = val = val_;
pri = rand();
                  apply(p, l, r, v);
                 return;
                                                                                                                lc = rc = nullptr;
                                                                                                                siz = 1; rev_valid = 0;
           int m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
                                                                                                           void pull() { // update siz or other information
                                                                                                                siz = 1;
min = val;
            pull(p):
                                                                                                                for (auto c : {lc, rc}) {
                                                                                                                      if (!c) continue;
      void range_apply(int l, int r, const Tag &v) {
    range_apply(1, 0, n, l, r, v);
                                                                                                                      siz += c->siz:
                                                                                                                      min = std::min(min, c->min);
     }
                                                                                                                }
      template < class F> // 尋找區間內,第一個符合條件的
      int findFirst
                                                                                                          void push() {
            (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {</pre>
                                                                                                                if (rev_valid) {
```

swap(lc, rc);

```
if (lc) lc->rev_valid ^= 1;
if (rc) rc->rev_valid ^= 1;
           rev_valid = false;
     int find(int k) { // 找到 min 是 k 的位置 (1-based)
           push();
int ls = (lc ? lc->siz : 0) + 1;
if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
     }
int size(Treap *t) {
    return t ? t->siz : 0;
freap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
    a->push(); b->push();
    if (a->pri > b->pri) {
           a->rc = merge(a->rc, b);
           a->pull();
           return à;
     else {
    b->lc = merge(a, b->lc);
            b->pull();
           return b;
     }
pair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
     return {t, b};
     else {
            auto [a, b] = split(t->lc, k);
           t->lc = b;
            t->pull();
           return {a, t};
     }
void Print(Treap *t) {
     if (!t) return;
     t->push();
     Print(t->lc);
cout << t->val;
     Print(t->rc);
```

4 Flow

4.1 Dinic [287fe8]

```
template < class T>
struct Dinic {
      struct Edge {
            int to;
            T flow, cap; // 流量跟容量
                    s, t;
      T INF_FloW = numeric_limits <T>::max() / 2;
      vector<vector<int>> adj; // 此點對應的 edges 編號
      vector<Edge> edges; // 幫每個 edge 編號
     vector <tdge> euges, // m w ma eug
vector <int> dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
    n = n_; m = 0;
    dis.resize(n); ptr.resize(n);
}
            adj.assign(n, vector<int>{});
edges.clear();
      void add_edge(int u, int v, T cap) {
            // 偶數 id 是正向邊
            edges.push_back({ v, 0, cap });
edges.push_back({ u, 0, 0 });
adj[u].push_back(m++);
            adj[v].push_back(m++);
      bool bfs() {
            fill(dis.begin(), dis.end(), -1);
            dis[s] = 0; queue < int > q;
            q.push(s);
            while (!q.empty() && dis[t] == -1) {
                  int u = q.front(); q.pop();
for (int id : adj[u]) {
    Edge &e = edges[id];
                        if (e.flow == e.cap) continue;
if (dis[e.to] == -1) {
    dis[e.to] = dis[u] + 1;
                              q.push(e.to);
                       }
                  }
            return dis[t] != -1;
```

```
T dfs(int u, T flow) {
                                                       if (flow == 0) return 0;
if (u == t) return flow;
                                                         for (int
                                                                                 (int
    &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {
    Edge &e = edges[adj[u][cur]];
    if (dis[u] + 1 != dis[e.to]) continue;
    if (e.cap == e.flow) continue;
    T mn = dfs(e.to, min(flow, e.cap - e.flow));
    if (mn > 0) {
        e.flow += mn;
        e.flow | continue | cont
                                                                                                             edges[adj[u][cur] ^ 1].flow -= mn;
                                                                                                             return mn;
                                                                                 }
                                                        return 0; // 到不了終點就會 return 0
                             T work(int s_, int t_) {
    s = s_; t = t_; T flow = 0;
    while (bfs()) {
                                                                                  fill(ptr.begin(), ptr.end(), 0);
                                                                                  while (true) {
    T res = dfs(s, INF_Flow);
                                                                                                             if (res == 0) break;
flow += res;
                                                       return flow;
                             void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
};
```

4.2 Min Cut [44ae6c]

```
CSES Police Chase
int main(){
      int n, m; cin >> n >> m;
Dinic < int >> g(n);
for (int i = 0; i < m; i++) {
    int u, v, cap = 1;
    cin >> u >> v;

              u--; v--;
              g.add_edge(u, v, cap);
              g.add_edge(v, u, cap);
       int res = g.work(0, n - 1);
cout << res << "\n";
       if (res == 0) return;
       for (int id : g.adj[u]) {
    auto e = g.edges[id];
    if (e.cap - e.flow > 0) {
                                     self(self, e.to);
                     }
             }
     };
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
        auto e = g.edges[id];
    }
}</pre>
                      if (!vis[e.to]) {
    cout << i + 1 << " " << e.to + 1 << "\n";</pre>
              }
      }
```

4.3 Hangarian [350fc3]

```
struct Hangarian { // 0-based
       int n, m; // 最小路徑覆蓋,二分匹配
vector<vector<int>>> adj;
      vector <int> used, vis;
vector<pair<int, int>> match;
Hangarian(int n_ = 0, int m_ = 0) {
   init(n_, m_);
       void init(int n_ = 0, int m_ = 0) {
            n = n_; m = m_;
adj.assign(n + m, vector < int > ());
used.assign(n + m, -1);
            vis.assign(n + m, \theta);
       void addEdge(int u, int v) {
            adj[u].push_back(n + v);
            adj[n + v].push_back(u);
       vector<pair<int, int>> work() {
            match.clear();
            used.assign(n + m, -1
vis.assign(n + m, 0);
                                        -1):
            auto dfs = [&](auto self, int u) -> bool {
```

```
return true;
                  }
              }
           return false;
       for (int i = 0; i < n; i++) {
           fill(vis.begin(), vis.end(), 0);
           dfs(dfs, i);
       for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
               match.emplace_back(used[i], i - n);
       return match:
   }
};
```

4.4 MCMF [f667f8]

```
template < class Tf, class Tc>
struct MCMF {
      // 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就好
     int n, m, s, t;
If INF_FLOW = numeric_limits<If>::max() / 2;
It INF_COST = numeric_limits<It>::max() / 2;
      struct Edge {
           int to;
            Tf flow, cap; // 流量跟容量
            Tc cost:
      vector < vector < int >> adj;
     vector < Edge > edges; // 幫每個 edge 編號
vector < Tc > dis, pot; // johnson algorithm, using spfa
vector < int > rt; // 路徑恢復, 對應 id
     vector <book inq;

MCMF(int n_ = 0) { init(n_); }

void init(int n_ = 0) {</pre>
           n = n_;
m = 0;
            edges.clear();
            adj.assign(n, vector<int>{});
     void add_edge(int u, int v, Tf cap, Tc cost){
  edges.push_back({v, 0, cap, cost});
  edges.push_back({u, 0, 0, -cost});
  adj[u].push_back(m++);
            adj[v].push_back(m++);
     bool spfa() {
    dis.assign(n, INF_COST);
    rt.assign(n, -1); inq.assign(n, false);
            queue<int> q;
            quedictite q,
q.push(s), dis[s] = 0, inq[s] = true;
while (!q.empty()) {
                 q.push(v); inq[v] = true;
                              }
                       }
                 }
            return dis[t] != INF_COST;
     bool dijkstra() {
           dis.assign(n, INF_COST); rt.assign(n, -1);
priority_queue<pair<Tc, int>,
    vector<pair<Tc, int>>, greater<pair<Tc, int>>> pq;
dis[s] = 0; pq.emplace(dis[s], s);
           pq.emplace(ndis, v);
                        }
                 }
            return dis[t] != INF_COST;
     // 限定 flow, 最小化 cost
pair<Tf, Tc> work_flow(int s_, int t_, Tf need) {
    s = s_, t = t_; pot.assign(n, 0);
    Tf flow{}; Tc cost{}; bool fr = true;
            while ((fr ? spfa() : dijkstra())) {
```

```
for (int i = 0; i < n; i++) {
    dis[i] += pot[i] - pot[s];</pre>
                            If f = INF_FLOW;
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
                                     f = min
                                                (f, edges[rt[i]].cap - edges[rt[i]].flow);
                           }
f = min<Tf>(f, need);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
}
                            flow += f; need -= f;
cost += f * dis[t]; fr = false;
                            swap(dis, pot);
if (need == 0) break;
                   return make_pair(flow, cost);
         }
         // 限定 cost, 最大化 flow
pairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpairpair
                            Tf f = INF FLOW;
                            for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
                                     f = min
                                               (f, edges[rt[i]].cap - edges[rt[i]].flow);
                            f = min<Tf>(f, budget / dis[t]);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
                                     edges[rt[i] ^ 1].flow -= f;
                            flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
                            swap(dis, pot);
if (budget == 0 || f == 0) break;
                   return make_pair(flow, cost);
         void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
};
           String
```

5.1 KMP [cddfd9]

```
struct KMP {
      string sub;
      vector<int> failure;
      KMP(string sub_) {
    sub = sub_;
            failure.resize(sub.size(), -1);
            buildFailFunction();
       void buildFailFunction() {
    for (int i = 1; i < (int)sub.size(); i++) {
        int_now = failure[i - 1];
}</pre>
                 while (now != -1
                 && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
            }
      vector<int> match(string &s) {
            for (int i = 0, now = -1; i < (int)s.size(); i++) {
    // now is the compare sucessed length -1
    while (s[i] !=</pre>
                 match.push_back(i - now);
                       now = failure[now];
                 }
            return match;
      }
};
```

5.2 Z Function [8dd6ac]

```
|// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
        // 的最長公共前綴 (LCP) 的長度
vector<int> Z(string s) {
  int n = s.size();
                                                             vector<int> z(n);
                                                         vector vect
                                                                                                              if (i + z[i] > j + z[j]) {
```

```
National Chung Cheng University Salmon
                                                                                                              cur->is word = true:
                                                                                                        bool is_in_trie(string &s) {
      return z; // 最後一格不算
                                                                                                              trie_node *cur = root;
for (int i = 0; i < s.size(); i++) {</pre>
                                                                                                                    if (cur->
                                                                                                                   children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
5.3 Duval Algorithm [f9dcca]
// duval algorithm
// 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
                                                                                                              return true:
vector<string> duval(string s) {
    int i = 0, n = s.size();
                                                                                                        int search_i_start(string &s, int i, vector<int> &dp) {
                                                                                                              trie_node *cur = root;
int sz = s.size(), ans = 0;
for (int j = i; j < sz; j++) {</pre>
      vector<string> res;
     while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
      else k++;
}</pre>
                                                                                                                    (ans += dp[j + 1]) %= mod;
           while (i <= k) {
                 res.push_back(s.substr(i, j - k));
i += j - k;
                                                                                                       }
                                                                                                  };
int main() {
           }
                                                                                                        // 找到 sub 集合裡,可以重複用,組成 s 的組數 Trie trie;
      return res;
}
                                                                                                        string s; cin >> s;
int sz = s.size();
// 最小旋轉字串
string min_round(string s) {
                                                                                                        // dp 代表 i 開頭到最後的配對總數
     s += s;
      int i = 0, n = s.size();
                                                                                                        // 找到有結尾為 stop 的 dp[i] += dp[j + 1]
     int t = 0, n = s.stze();
int start = i;
while (i < n / 2) {
    start = i;
    int k = i, j = i + 1;
    while (s[k] <= s[j] && j < n) {
        if (s[k] < s[j]) k = i;
    }
}</pre>
                                                                                                        int n; cin >> n;
vector <int> dp(sz + 1, 0);
for (int i = 0; i < n; i++) {
    string sub; cin >> sub;
    trie.insert(sub);
                                                                                                        dp[sz] = 1;
for (int i = sz - 1; i >= 0; i--) {
    dp[i] = trie.search_i_start(s, i, dp);
            while (i <= k) {</pre>
                 i += j - k;
                                                                                                        cout << dp[0] << endl;</pre>
      return s.substr(start, n / 2);
                                                                                                  6
                                                                                                          Math
                                                                                                  6.1 質因數分解 [ee1622]
5.4 Manacher [9c9ca6]
// 找到對於每個位置的迴文半徑
                                                                                                     a^{(m-1)} = 1 \pmod{m}
                                                                                                  // a^(m-1) = 1 (moa m)

// a^(m-2) = 1/a (mod m)

// EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)

// Filter + DP; DP save min factor 'recur' factor decomposition

// FacNums = (x+1)(y+1)(z+1)...

// FacSum = (a^0+a^1...+a^x)(b^0+...+b^y)

// FacMul = N(x+1)(y+1)(z+1)/2
vector<int> manacher(string s) {
      string t = "#";
      for (auto c : s) {
           t += c;
t += '#';
      int n = t.size();
      vector<int> r(n);
                                                                                                  vector<int> is_prime;
                                                                                                  // 1 代表是質數, 非 1 不是
void init(int n) {
      for (int i = 0, j =
           0; i < n; i++) { // i 是中心, j 是最長回文字串中心 if (2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
                                                                                                        is_prime.assign(n + 1, 1);
for (int i = 2; i <= (int)sqrt(n) + 1; i++) {</pre>
                                                                                                              if (is_prime[i] == 1) {
    for (int j = i + i; j <= n; j += i) {
        is_prime[j] = i;
    }</pre>
            while (i - r[i] >=
                 0 && i + r[i] < n && t[i - r[i]] == t[i + r[i]]) {
r[i] += 1;
                                                                                                             }
           if (i + r[i] > j + r[j]) {
    j = i;
                                                                                                       }
                                                                                                  int main() {
    init(1000000);
                                                                                                       return r:
     // # a # b # a #
// 1 2 1 4 1 2 1
     // # a # b # b # a #
// 1 2 1 2 5 2 1 2 1
                                                                                                              mp[is_prime[q]]++;
                                                                                                              q /= is_prime[q];
      // 值 -1 代表原回文字串長度
      // (id - val + 1) / 2 可得原字串回文開頭
                                                                                                        if (q != 1) mp[q]++;
for (auto [a, b] : mp) {
    ans *= b + 1;
5.5 Trie [3b3aa0]
                                                                                                        cout << ans << "\n";
struct Trie {
      struct trie_node {
           bool is_word;
vector<trie_node *> children;
trie_node() {
   is_word = false;
   children.resize(26, NULL);
                                                                                                  6.2 模除計算 [9b1014]
```

trie_node *root = new trie_node();
void insert(string &s) {

trie_node *cur = root;
for (int i = 0; i < s.size(); i++) {
 int idx = s[i] - 'a';
 if (cur->children[idx] == NULL) {

cur = cur->children[idx];

cur->children[idx] = new trie_node();

```
using i64 = long long;
template < class T >
constexpr T power(T a, i64 b) {
      T res = 1;
for (; b; b /= 2, a *= a) {
    if (b % 2) {
                  res *= a;
            }
      return res;
}
constexpr i64 mul(i64 a, i64 b, i64 p) {
   i64 res = a * b - i64(1.L * a * b / p) * p;
```

```
res %= p;
if (res < 0) {
                                                                                             i64 MLong<0LL>::Mod = i64(1E18) + 9:
                                                                                            constexpr i64 P = 998244353;
using Z = MLong <P>;
// using Z = MLong <0LL>; // change Mod
           res += p;
template < i64 P>
                                                                                             struct Comb {
                                                                                                 ict Comb {
    i64 n;
    vector <Z> _fac;
    vector <Z> _invfac;
    vector <Z> _inv;
    Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
    Comb(i64 n) : Comb() { init(n); }
struct MLong {
     i64 x;
     constexpr MLong() : x{} {}
constexpr MLong(i64 x) : x{norm(x % getMod())} {}
     static i64 Mod;
constexpr static i64 getMod() {
   if (P > 0) {
                                                                                                  void init(i64 m) {
                                                                                                       m = min(m, Z::getMod() - 1);
if (m <= n) return;
_fac.resize(m + 1);</pre>
                `return P;
          } else {
                return Mod;
                                                                                                       _invfac.resize(m +
                                                                                                        _inv.resize(m + 1);
     constexpr static void setMod(i64 Mod_) {
    Mod = Mod_;
                                                                                                       for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;</pre>
     constexpr i64 norm(i64 x) const {
                                                                                                       for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
           if (x < 0) {
               x += getMod();
           if (x >= getMod()) {
                x -= getMod();
           }
                                                                                                       n = m;
           return x:
                                                                                                  Z fac(i64 m) {
                                                                                                       if (m > n) init(2 * m);
return _fac[m];
     constexpr i64 val() const {
          return x:
                                                                                                  J invfac(i64 m) {
   if (m > n) init(2 * m);
   return _invfac[m];
     explicit constexpr operator i64() const {
           return x;
     constexpr MLong operator-() const {
                                                                                                  Z inv(i64 m) {
   if (m > n) init(2 * m);
   return _inv[m];
          MLong res;
res.x = norm(getMod() - x);
                                                                                                  J binom(i64 n, i64 m) {
    if (n < m || m < 0) return 0;
    return fac(n) * invfac(m) * invfac(n - m);</pre>
     constexpr MLong inv() const {
   assert(x != 0);
           return power(*this, getMod() - 2);
                                                                                                  constexpr MLong &operator*=(MLong rhs) & {
           x = mul(x, rhs.x, getMod());
return *this;
     constexpr MLong &operator+=(MLong rhs) & {
                                                                                           } comb; // 注意宣告, 若要換模數需重新宣告
          x = norm(x + rhs.x);
return *this;
                                                                                            6.3 中國餘數定理 [d41d8c]
     constexpr MLong &operator -= (MLong rhs) & {
    x = norm(x - rhs.x);
    return *this;
                                                                                            ll exgcd(ll a, ll b, ll &x, ll &y) {
                                                                                                  if (!b) {
    x = 1, y = 0;
                                                                                                       return a;
     constexpr MLong &operator/=(MLong rhs) & {
    return *this *= rhs.inv();
                                                                                                  ll g = exgcd(b, a % b, y, x);
y -= a / b * x;
return g;
     friend constexpr MLong operator*(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res *= rhs;
           return res;
                                                                                             ĺl inv(ll x, ll m){
                                                                                                  ll`a, b;
     friend constexpr MLong operator+(MLong lhs, MLong rhs) {
                                                                                                  exgcd(x, m, a, b);
           MLong res = lhs;
                                                                                                  a %= m;
if (a < 0) a += m;
           res += rhs:
           return res;
                                                                                                  return a;
     friend constexpr MLong operator-(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res -= rhs;
                                                                                             // remain, mod
                                                                                            Il CRT(vector<pair<ll, ll>> &a){
                                                                                                  ll prod = 1;
for (auto x : a) {
    prod *= x.second;
           return res:
     friend constexpr MLong operator/(MLong lhs, MLong rhs) {
          MLong res = lhs;
res /= rhs;
                                                                                                  ĺl res = 0:
                                                                                                  for (auto x : a) {
   auto t = prod / x.second;
   res += x.first * t % prod * inv(t, x.second) % prod;
   if(res >= prod) res -= prod;
           return res;
            constexpr istream &operator>>(istream &is, MLong &a) {
           i64 v;
                                                                                                  return res;
           is >> v;
a = MLong(v);
           return is;
                                                                                            6.4 矩陣與快速幕 [08b5fe]
     friend constexpr
                                                                                             template < class T>
            ostream &operator<<(ostream &os, const MLong &a) {
                                                                                             struct Mat {
           return os << a.val();</pre>
                                                                                                  int m, n;
                                                                                                  constexpr static ll mod = 1e9 + 7;
     friend constexpr bool operator == (MLong lhs, MLong rhs) {
                                                                                                  vector < vector < T >> matrix;
           return lhs.val() == rhs.val();
                                                                                                  Mat(int n_ = 0) { init(n_, n_); }
Mat(int m_, int n_) { init(m_, n_); }
Mat(vector<vector<T>> matrix_) { init(matrix_); }
     friend constexpr bool operator!=(MLong lhs, MLong rhs) {
  return lhs.val() != rhs.val();
                                                                                                  void init(int m_, int n_) {
                                                                                                       m = m_; n = n_;
matrix.assign(m, vector<T>(n));
};
template<>
                                                                                                  void init(vector<vector<T>> &matrix_) {
```

```
m = matrix_.size();
n = matrix_[0].size();
          matrix = matrix_;
                                                 // 單位矩陣
     vector<vector<T>> unit(int n) {
          return res;
     constexpr Mat & operator *= (const Mat& rhs) & {
    assert(matrix[0].size() == rhs.matrix.size());
           int m = matrix.size()
                 , k = matrix[0].size(), n = rhs.matrix[0].size();
          l] * rhs.matrix[l][j] % mod)) %= mod;
               }
          matrix = ans.matrix;
return *this;
     constexpr Mat &operator^=(ll p) & {
   assert(m == n); assert(p >= 0);
   Mat ans(p-- == 0 ? unit(m) : matrix);
           while (p > 0) {
   if (p & 1) ans *= *this;
   *this *= *this;
               p >>= 1;
          matrix = ans.matrix;
return *this;
     friend Mat operator*(Mat lhs, const Mat &rhs) {
           return lhs;
     }
friend Mat operator^(Mat lhs, const ll p) {
          lhs ^= p;
return lhs;
};
// fn = fn-3 + fn-2 + fn-1
// 初始矩陣
// f4 f3 f2
// f3 f2 f1
// f2 f1 f0
                轉移式
                 1 1 0  f5 f4 f3
1 0 1 => f4 f3 f2
1 0 0  f3 f2 f1
```

6.5 樹論分塊 [06204a]

6.6 Mobius Theorem

- 數論分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在O(1)內計算f(r)-f(l)或已經預處理 出 f 的前缀和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n}\!\mu(d)\!=\!\begin{cases} 1 & \text{for } n\!=\!1\\ 0 & \text{for } n\!\neq\!0 \end{cases}$$

2. μ 是常數函數 1 的反元素 $\Rightarrow \mu*1=\epsilon$, $\epsilon(n)$ 只在n=1時為 1 ,其餘情況皆為 0 。

- φ歐拉函數: x 以下與 x 互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^{i}) \\ &= 1 + p^{0}(p-1) + p^{1}(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^{c} \\ &= id \end{split}$$

• 莫比烏斯反演公式

-
$$f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$$

- $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

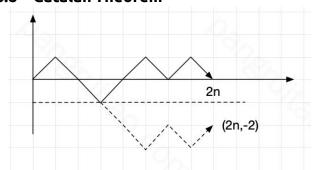
• 例子

$$\begin{split} &\sum_{i=aj=c}^b \sum_{j=1}^d [gcd(i,j)=k] \\ &\Rightarrow \sum_{i=1}^x \sum_{j=1}^y [gcd(i,j)=k] \\ &= \sum_{i=1}^x \sum_{j=1}^y \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^x \sum_{j=1}^y \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^\infty \mu(d) \sum_{i=1}^x \left[d \mid i \right] \sum_{j=1}^y \left[d \mid j \right] \, \mathrm{d} \, \mathrm{可整除} \, \mathrm{i} \, \mathrm{F} \hspace{-0.5em} \overset{\wedge}{>} \, 1 \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^\infty \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.7 **莫比烏斯反演** [d41d8c]

```
const int maxn = 2e5;
ll mobius_pref[maxn];
 void init() {
        mobius_pref[1] = 1;
vector<ll> wei
        (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
    }
                      continue; // 包含平方
               if (wei[i] == 0) {
                      wel[i] == 0, 1
wel[i] = 1;
for (ll j = 2; i * j < maxn; j++) {
    if (j % i == 0) wel[i * j] = -1;
    else if (wel[i * j] != -1) wel[i * j]++;</pre>
                      }
               mobius_pref[i]
                       = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
        }
 void solve() {
        auto cal = [&](ll x, ll y) -> int {
               for (int l = 1, r; l <= min(x, y); l = r + 1) {
    r = min(x / (x / l), y / (y / l));
    res += (mobius_pref[r] - mobius_pref[l])</pre>
                                 - 1]) * (x / l) * (y / l); // 代推出來的式子
               return res;
                (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k,
(c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n";
}
```

6.8 Catalan Theorem



1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$ 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有x 個,往下有y 個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.9 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- X/G:本質不同的方案的集合
- X^g : 對於某一種操作 g, 所有方案中,經過 g 這種翻轉後保持不變的方案的集合
- 集合取絕對值代表集合數

7 Search and Gready

7.1 二分搜 [d41d8c]

```
int main() {
    int l = 1, r = 10;
    // 1 to tar, find tar
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}</pre>
```

7.2 三分搜 [d41d8c]

```
| // 找極值問題,遞增遞減
| void solve() {
| int | = 0, r = 10, ans = 0; // ans 紀錄答案 |
| while (| <= r) {
| int | d = (r - l) / 3; // 差 |
| int | ml = l + d, mr = r - d; // mr 要用減的 |
| auto | cal = [&](int | m) -> int {
| int | x = 0; |
| return | x; // 計算答案 |
| ; int | ansl = | cal(|ml), ansr = | cal(|mr); if (| ansl | < | ansr) {
| | l = | ml + 1; |
| } else | r = | mr - 1; |
| }
```

8 Tree

8.1 LCA [9f95b1]

```
}
int lca(int a, int b) {
    if (depth[a] < depth[b]) swap(a, b);
    int pull = depth[a] - depth[b];
    for (int i = 0; i < 18; i++) {
        if (pull & (1 << i)) {
            a = par[a][i];
        }
    if (a == b) return a;
    for (int i = 17; i >= 0; i--) {
        if (par[a][i] != par[b][i]) {
            a = par[a][i], b = par[b][i];
        }
    }
    return par[a][0];
}
```

8.2 樹重心 [30b436]

```
struct centroid_decomposition {
       int n:
        vector<vector<int>> adj;
        vector<bool> vis;
       vector<int> siz;
       centroid_decomposition() {}
centroid_decomposition(int n_) { init(n_); }
       void init(int n_) {
             n = n_;
adj.assign(n, {});
vis.assign(n, false);
             siz.assign(n, 1);
        void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void get_siz(int dep, int x, int p = -1) {
             siz[x] = 1;
             stz[x] = 1;
for (int y : adj[x]) {
    if (y == p || vis[y]) continue;
    get_siz(dep + 1, y, x);
    siz[x] += siz[y];
       return get_cen(y, sz, x);
              return x:
       void work(int x = 0) {
    get_siz(0, x);
    int cen = get_cen(x, siz[x]);
    vis[cen] = true;
              // do something
              for (int y : adj[cen]) {
   if (vis[y]) continue;
   work(y);
1 };
```

8.3 樹壓平 [51199c]

```
點加值 = 所有子節點區間加值,求單點,使用 bit,做前綴差分
CSES 1138_Path Queries
   int n, q; cin >> n >> q;
vector <int> node_value(n + 1), euler_ordered_value(n);
for (int i = 1; i <= n; i++) {</pre>
        cin >> node_value[i];
   vector<vector<int>> tree(n + 1);
   for (int i = 1; i < n; i++) {
  int u, v; cin >> u >> v;
  tree[u].push_back(v);
        tree[v].push_back(u);
   vector<pair<int, int>> tree mapping(n + 1);
   int cnt = 0;
auto dfs = [&](auto self, int u, int par) -> void {
    euler_ordered_value[++cnt] = node_value[u];
        tree_mapping[u].first = cnt;
        for (auto v : tree[u]) {
   if (v == par) continue;
   self(self, v, u);
        tree_mapping[u].second = cnt;
   dfs(dfs,
   BIT bit(n);
for (int i = 1; i <= n; i++) {
        bit.modify(tree_mapping[i].first, node_value[i]);
        if (tree_mapping[i].first < n) { // root 就不用扣了</pre>
                    (tree_mapping[i].second + 1, -node_value[i]);
```

8.4 Heavy Light Decomposition [ad25b6]

```
struct HLD {
      int n, cur;
vector<int> siz, top, dep, parent, in, out, seq;
vector<vector<int>> adj;
      vector < vector < int >> adj;
HLD(int n = 0) { init(n ); }
void init(int n = 0) {
    n = n ; cur = 0;
    siz.resize(n); top.resize(n); dep.resize(n);
    parent.resize(n); in.resize(n); out.resize(n);
              seq.resize(n); adj.assign(n, {});
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void work(int root = 0) {
             top[root] = root;
dep[root] = 0;
parent[root] = -1;
              dfs1(root); dfs2(root);
       void dfs1(int u) {
             if (parent[u] != -1)
    adj[u].erase(find
                            (adj[u].begin(), adj[u].end(), parent[u]));
             for (auto &v : adj[u]) {
    parent[v] = u, dep[v] = dep[u] + 1;
                     dfs1(v);
                    siz[u] += siz[v];
if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
                    } // 讓 adj[u][0] 是重子節點
       void dfs2(int u) {
              in[u] = cur++;
             seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
    top[v] = v == adj[u][0] ? top[u] : v;
                    dfs2(v);
              out[u] = cur;
      fint lca(int u, int v) {
    while (top[u] != top[v]) {
        if (dep[top[u]] > dep[top[v]]) {
            u = parent[top[u]];
        } else {
                           v = parent[top[v]];
                    }
              return dep[u] < dep[v] ? u : v;</pre>
       int dist(int u, int v) {
              return dep[u] + dep[v] - 2 * dep[lca(u, v)];
      fint jump(int u, int k) {
    if (dep[u] < k) return -1;
    int d = dep[u] - k;
    while (dep[top[u]] > d)
                    u = parent[top[u]];
              return seq[in[u] - dep[u] + d];
      bool isAncester(int u, int v) {
             // 判斷 u 是否是 v 的祖先
return in[u] <= in[v] && in[v] < out[u];
      int rootedParent(int u, int v) {
    // 根據新根節點 u 計算 v 的父節點
             swap(u, v);
if (u == v) return u;
if (!isAncester(u, v)) return parent[u];
              auto it = upper_bound(adj
   [u].begin(), adj[u].end(), v, [&](int x, int y) {
   return in[x] < in[y];</pre>
```

```
return *it;
}
int rootedSize(int u, int v) {
    // 根據新根節點 u 計算子樹 v 的大小
    if (u == v) return n;
    if (!isAncester(v, u)) return siz[v];
    return n - siz[rootedParent(u, v)];
}
int rootedLca(int a, int b, int c) {
    // 根據新的根節點計算三個節點 a \ b 和 c 的最近公共祖先
    return lca(a, b) ^ lca(b, c) ^ lca(c, a);
}
};
```

8.5 Virtual Tree [622e69]

```
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
// 可以建立虚樹達成快速樹 DP
 // 例如這題是有權樹,跟 vertex 1 隔開的最小成本
// 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector <int>stk(maxn);
void insert(int u, vector <vector <int>> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
        vt[stk[top - 1]].push_back(stk[top]), top--;
    if (stk[top - 1] != l) {
        vt[l].push_back(stk[top]);
        stk[top] = l;
    } else vt[l].push back(stk[top--]);
        } else vt[l].push_back(stk[top--]);
stk[++top] = u;
 void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
        vt[u].clear();
 void solve(int n, int q) {
    vector g(n + 1, vector<pair<int, int>>());
        g[u].push_back({v, w});
g[v].push_back({u, w});
        build_lca(n, g);
        build(n, g);
for (int i = 0; i < q; i++) {
               int m; top = -1; cin >> m;
vector < int >> key(m);
               for (int j = 0; j < m; j++) {
    cin >> key[j];
                      iskey[key[j]] = 1;
               key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
               for (int x : key) insert(x, vt);
               while (top
                        > 0) vt[stk[top - 1]].push_back(stk[top]), --top;
               // DP
               auto dfs = [&](auto self, int u) -> void {
    for (auto v : vt[u]) {
        self(self, v);
    }
}
                             if (iskey[v]) {
                                    dp[u] += min_dis[v];
                                    // 砍掉 1 到 v 之間最短的路
                             else {
                                   dp[u] += min(dp[v], min_dis[v]);
                             iskey[v] = dp[v] = 0;
                      vt[u].clear();
               dfs(dfs, key[0]); // key[0] 一定是 root
cout << dp[key[0]] << "\n";
iskey[key[0]] = dp[key[0]] = 0;
 }
```

8.6 Dominator Tree [baa540]

```
struct Dominator_tree {
    int n, id;
    vector<vector<int>> adj, radj, bucket;
    vector<int>> sdom, dom, vis, rev, pa, rt, mn, res;
    Dominator_tree(int n_ = 0) { init(n_); }
    void init(int _n) {
        n = _n, id = 0;
        adj.assign(n, vector<int>());
        radj.assign(n, vector<int>());
        bucket.assign(n, vector<int>());
        sdom.resize(n); dom.assign(n, -1);
        vis.assign(n, -1); rev.resize(n);
        pa.resize(n); rt.resize(n);
        mn.resize(n); res.resize(n);
}
void add_edge(int u, int v) { adj[u].push_back(v); }
```

```
int query(int v, int x) {
   if (rt[v] == v) return x ? -1 : v;
   int p = query(rt[v], 1);
   if (p == -1) return x ? rt[v] : mn
                                                                             : mn[v]:
                 if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
                 return x ? p : mn[v];
         }
void dfs(int v) {
    vis[v] = id, rev[id] = v;
    rt[id] = mn[id] = sdom[id] = id, id++;
    for (int u : adj[v]) {
        if (vis[u] == -1) dfs(u), pa[vis[u]] = vis[v];
        radj[vis[u]].push_back(vis[v]);
}
         void build(int s) {
                sdom[i] = min(sdom[i], sdom[quer
if (i) bucket[sdom[i]].push_back(i);
for (int u : bucket[i]) {
   int p = query(u, 0);
   dom[u] = sdom[p] == i ? i : p;
                         if (i) rt[i] = pa[i];
                res.assign(n, -1);
for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];
for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre>
                 res[s] = s;
                 for (int i = 0; i < n; i++) dom[i] = res[i];</pre>
};
 9
           DP
```

9.1 LCS [5781cf]

```
int m, n; cin >> m >> n;
string s1, s2; cin >> s1 >> s2;
int L = 0;
vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0));
for (int i = 1; i <= m; i++) {
   for (int j = 1; j <= n; j++) {
     if (s1[i - 1] == s2[j - 1]</pre>
             dp[i][j] = dp[i - 1][j - 1] + 1;
             dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
    }
m--, n--, length--;
         if (dp[m - 1][n] > dp[m][n - 1]) m--;
         else n--:
cout << s << "\n":
```

9.2 LIS [66d09f]

```
int main() {
       int n; cin >> n;
       vector<int> v(n);
      vector <tnt> v(n);
for (int i = 0; i < n; i++) cin >> v[i];
int dp[n]; vector <int> stk;
stk.push_back(v[0]);
dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) {
    if (v[i] > stk.back()) {
                    stk.push_back(v[i]);
                     dp[i] = ++L;
              } else {
                     auto it
                              = lower_bound(stk.begin(), stk.end(), v[i]);
                     *it = v[i]; dp[i] = it - stk.begin() + 1;
             }
      vector<int> ans; cout << L << "\n";
for (int i = n - 1; i >= 0; i--) {
   if (dp[i] == L) {
                     ans.push_back(v[i]), L--;
       reverse(ans.begin(), ans.end());
for (auto i : ans) cout << i << " ";</pre>
```

9.3 Edit Distance [308023]

```
| int main() {
```

```
string s1, s2; cin >> s1 >> s2;
int n1 = s1.size(), n2 = s2.size();
// dp[i][j] 為 s1 的前 i 個字元, 跟 s2 的前 j 個字元vector (int > dp(n2 + 1);
cur[j] = dp[j - 1];
           // s1 新增等價於 s2 砍掉
            // dp[i][j] = min(s2 新增, 修改, s1 新增);
           cur[j]
                 min({cur[j - 1], dp[j - 1], dp[j]}) + 1;
       }
   swap(dp, cur);
cout << dp[n2] << "\n";
```

9.4 Bitmask [a626f9]

```
void hamiltonianPath(){
                     int n, m; cin >> n >> m;
vector adj(n, vector<int>());
                     for (int i = 0; i < m; i++) {
  int u, v; cin >> u >> v;
  adj[--v].push_back(--u);
                     // 以...為終點,走過...
                      vector dp(n, vector<int>(findBit(n)));
                   vector dp(n, vector<int>(findbit(n));
dp[0][1] = 1;
for (int mask = 1; mask < findBit(n); mask++) {
    if ((mask & 1) == 0) continue;
    for (int i = 0; i < n; i++) {
        if ((mask & findBit(i)) == 0) continue;
        if (i == n - 1 && mask != findBit(n) - 1) continue;
        int pre_mask = mask ^ findBit(i);
        for (int i = 0) difill |</pre>
                                                            for (int j : adj[i]) {
   if ((pre_mask & findBit(j)) == 0) continue;
                                                                               dp[i][mask
                                                                                                     ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
                                                          }
                     cout << dp[n - 1][findBit(n) - 1] << "\n";</pre>
 void elevatorRides() {
                    int n, x; cin >> n >> x; vector<int> a(n);
for (int i = 0; i < n; i++) cin >> a[i];
vector<array<int, 2>>> dp(findBit(n));
                   vector <array <int, 2>> dp(findBit(n));
dp[0][0] = 1; // 次數、已使用人數
for (int mask = 1; mask < findBit(n); mask++) {
    dp[mask][0] = dp[mask][1] = 2e9;
    for (int i = 0; i < n; i++) {
        if ((mask & findBit(i)) == 0) continue;
        int pre_mask = mask ^ findBit(i);
        if (dp[pre_mask][1] + a[i] <= x) {
            if (dp[pre_mask][0] < dp[mask][1] | dp[pre_mask][0] == dp[mask][1] | dp[pre_mask][1] == dp[mask][1] | dp[pre_mask][1] == dp[mask][1] | dp[pre_mask][1] == dp[mask][1] | dp[pre_mask][1] == dp[mask][1] | dp
                                                                                                  dp[mask][1] = a[i];
                                     }
                     cout << dp[findBit(n) - 1][0] << "\n";
3
```

9.5 Projects [0942aa]

```
int main() { // 排程有權重問題,輸出價值最多且時間最少
struct E {
        int from, to, w,
        bool operator <(const E &rhs) {
    return to == rhs.to ? w > rhs.w : to < rhs.to;</pre>
        int n; cin >> n; vector <E> a(n + 1);
for (int i = 1; i <= n; i++) {
   int u, v, w; cin >> u >> v >> w;
   a[i] = {u, v, w, i};
        vector<array<ll, 2>> dp(n + 1); // w, time
        vector<array<int, 2>> rec(n + 1); // 有沒選, 上個是誰
        vector<array<unt, 2>> rec(n + 1); // 月(文地 / 上間定能
sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
    auto it = --lower_bound(all(a), E({0, a[i].from}),
    [](E x, E y){ return x.to < y.to; });
    int id = it - a.begin(); dp[i] = dp[i - 1];
}</pre>
                ll nw = dr[id][0] + a[i].w;
ll nt = dp[id][1] + a[i].to - a[i].from;
if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
    dp[i] = {nw, nt}; rec[i] = {1, id};
```

```
}
}
vector<int> ans;
for (int i = n; i != 0;) {
    if (rec[i][0]) {
        ans.push_back(a[i].id);
        i = rec[i][1];
    } else i--;
}
```

9.6 Removal Game [7bb56b]

9.7 Codeforces Example [7d37ea]

```
CF 1932 pF
// 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
// 請問在線段不重複的情況下,最多獲得幾分 int main() {
    int n, m;
cin >> n >> m;
    // 記錄每點有幾個線段
     // 再一個紀錄,包含這個點的左界
     vector<int> l_side(n + 1, inf), cnt(n + 5, 0);
for (int i = 0; i < m; i++) {
   int l, r; cin >> l >> r;
          l_side[r] = min(l_side[r], l);
         cnt[l]++;
cnt[r + 1]--;
    for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
     for (int i = n; i >= 2; i--) {
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
     vector<int> dp(n + 1);
    dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
         dp[i] = cnt[i];
if (l_side[i] != inf) {
              dp[i] += dp[l_side[i] - 1];
         dp[i] = max(dp[i], dp[i - 1]);
    cout << dp[n] << "\n";
}
// CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
// 再加上 max(bi) - min(bi)
int main(){
    int n, k, ans = 0; cin >> n >> k;
     vector<pii> v(n + 1);
     for (int i = 1; i <= n; i++) {
  int a, b; cin >> a >> b;
  v[i] = {a, b};
          if (a <= k) ans = 1;
    sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
         return a.second < b.second;</pre>
     }); // 用 bi 來排,考慮第 i 個時可以先扣
     vector<vector<int>> dp(n + 1, vector<int>(n + 1, inf));
     // 考慮 v[i] 時, 選 j 個的 sum(ai) - min(bi)
    for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
               // min(不選, 選)
               if (dp[i
                       1][j - 1] + v[i].first + v[i].second <= k) {
                    // 假如可以選, 更新 ans 時再加回去 bi
                    ans = max(ans, j);
          dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
     cout << ans << endl:
}
```

9.8 CHT [5f5c25]

```
struct Line {
     ll m, b;
Line(ll m = 0, ll b = 0) : m(m), b(b) {}
     ll eval(ll x) {
    return m * x + b;
}:
struct CHT { // 用在查詢單調斜率也單調
  int n, lptr, rptr; vector<line> hull;
  CHT(int n_ = 0, Line init_ = Line()) {
    init(n_, init_);
     void init(int n_ = 0, Line init_ = Line()) {
    n = n_; hull.resize(n); reset(init_);
      void reset(Line init_ = Line()) {
    lptr = rptr = 0; hull[0] = init_;
      bool pop_front(Line &l1, Line &l2, ll x) {
          // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y
          // 代表查詢的當下,右線段的高度已經低於左線段了
return ll.eval(x) >= l2.eval(x);
     bool pop_back(Line &l1, Line &l2, Line &l3) {
          // 本題斜率遞減、上凸包
          // 因此只要 12 跟
          l3 的 X 交點 <= l1 跟 l3 的 X 交點, l2 就用不到了
return (l3.b - l2.b)
* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
     rptr--;
          hull[++rptr] = L;
     ll query(ll x) {
    while (rptr - lptr
                 > 0 && pop_front(hull[lptr], hull[lptr + 1], x))
                lptr++
          return hull[lptr].eval(x);
     }
};
```

9.9 LiChaoSegmentTree [a6e320]

```
constexpr ll Inf = 4e18;
// dp[i] = min(f[j] * s[i] + dp[j])
// y =
struct Line {
      Line(ll m = 0, ll b = Inf) : m(m), b(b) {}
      ll eval(ll x) const { return m * x + b; }
struct LiChaoSeg { // 取 max 再變換就好
      int n;
      vector < Line > info;
     LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
            info.assign(4 << __lg(n), Line());</pre>
      void update(Line line, int node, int l, int r) {
  int m = (l + r) / 2;
  bool left = line.eval(l) < info[node].eval(l);
  bool mid = line.eval(m) < info[node].eval(m);</pre>
           if (mid) swap(info[node], line); // 如果新線段比較好
           if (r - l == 1) return;
else if (left != mid) update(line, 2 * node, l, m);
            // 代表左半有交點
            else update(line, 2 * node + 1, m, r);
           // 代表如果有交點一定在右半
     void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
   if (r - l == 1) return info[node].eval(x);
   int m = (l + r) / 2;
   if (x < m) return</pre>
                  min(info[node].eval(x), query(x, 2 * node, l, m));
           else return min(
    info[node].eval(x), query(x, 2 * node + 1, m, r));
      ll query(int x) { return query(x, 1, 0, n); }
```

10 Geometry

10.1 Basic [d41d8c]

```
#include <bits/stdc++.h>
using namespace std;
using i64 = long long;

template < class T >
struct Point {
    T x;
    T y;
```

```
Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) \{ \}
     template < class U>
    operator Point<U>() {
   return Point<U>(U(x), U(y));
     Point & operator += (const Point &p) & {
         x += p.x;
y += p.y;
          return *this:
     Point & operator -= (const Point &p) & {
          x -= p.x;
          y -= p.y;
return *this;
     Point & operator *= (const T &v) & {
         x *= v;
y *= v;
return *this;
     Point & operator /= (const T & v) & {
         x /= v;
y /= v;
return *this;
    Point operator -() const {
    return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
         return a += b:
     friend Point operator (Point a, const Point &b) {
         return a -= b:
     friend Point operator*(Point a, const T &b) {
  return a *= b;
     friend Point operator/(Point a, const T &b) {
         return a /= b;
     friend Point operator*(const T &a, Point b) {
          return b *= a;
     friend bool operator==(const Point &a, const Point &b) {
          return a.x == b.x && a.y == b.y;
     friend istream &operator>>(istream &is, Point &p) {
          return is >> p.x >> p.y;
     friend ostream & operator < <(ostream & os, const Point & p) {
    return os << "(" << p.x << ", " << p.y << ")";</pre>
}:
template < class T>
struct Line {
     Point<T>
    Point<T> b;
Line(const Point<T> &a_ = Point<T>()
, const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
template < class T>
T dot(const Point<T> &a, const Point<T> &b) {
    return a.x * b.x + a.y * b.y;
template < class T>
T cross(const Point<T> &a, const Point<T> &b) {
    return a.x * b.y - a.y * b.x;
template < class T>
 square(const Point<T> &p) {
    return dot(p, p);
template < class T >
double length(const Point < T > &p) {
    return sqrt(square(p));
template < class T>
double length(const Line<T> &l) {
    return length(l.a - l.b);
template < class T>
Point < T > normalize(const Point < T > & p) {
    return p / length(p);
template < class T>
bool parallel(const Line<T> &l1, const Line<T> &l2) {
   return cross(l1.b - l1.a, l2.b - l2.a) == θ;
template < class T>
double distance(const Point<T> &a, const Point<T> &b) {
    return length(a - b);
```

```
template < class T>
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0) {
      return distance(p, l.a);
}</pre>
      if (dot(p - l.b, l.a - l.b) < 0) {
    return distance(p, l.b);</pre>
      return distancePL(p, l);
}
template < class T>
Point<T> rotate(const Point<T> &a) {
     return Point(-a.y, a.x);
template < class T>
int sgn(const Point<T> &a) {
    return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
template < class T>
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
     return cross(l.b - l.a, p - l.a) > 0;
template < class T>
Point < T
       > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
      return l1.a + (l1.b - l1.a) * (cross(l2.b - l2.a, l1.a - l2.a) / cross(l2.b - l2.a, l1.a - l1.b));
}
template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
     return cross(p - l.a, l.b - l.a) == 0 &&
    min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)
           && min
                  (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
      (const Point<T> &a, const vector<Point<T>> &p) {
int n = p.size();
for (int i = 0; i < n; i++) {</pre>
           if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {
                 return true:
     }
      int t = 0;
      for (int i = 0; i < n; i++) {
    auto u = p[i];
           auto v = p[(i + 1) \% n];
           if (u.x < a.x
                 && v.x >= a.x && pointOnLineLeft(a, Line(v, u))) {
           if (u.x >= a.x
                  && v.x < a.x && pointOnLineLeft(a, Line(u, v))) {
     }
     return t == 1;
}
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
template <ctass I>
tuple <int, Point <T>, Point <T>> segmentIntersection
  (const Line <T> &l1, const Line <T> &l2) {
  if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x)) {
    return {0, Point <T>(), Point <T>()};
}
      if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x)) {
   return {0, Point<T>(), Point<T>()};
      if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y)) {</pre>
           return {0, Point<T>(), Point<T>()};
      if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y)) {
           return {0, Point<T>(), Point<T>()};
      if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
           if (cross(l1.b - l1.a, l2.a - l1.a) !=
    return {0, Point<T>(), Point<T>()};
           } else {
                 auto maxx1 = max(l1.a.x, l1.b.x);
                 auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
auto miny1 = min(l1.a.y, l1.b.y);
                 auto maxx2 = max(l2.a.x, l2.b.x);
```

```
auto minx2 = min(l2.a.x, l2.b.x);
                                                                                                                  return false:
              auto minx2 = min(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.y, l2.b.y);
auto miny2 = min(l2.a.y, l2.b.y);
Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
                                                                                                   } else {
   if (pointOnLineLeft(u, l)) {
              if (!pointOnSegment(p1, l1)) {
                                                                                                             if (pointOnLineLeft(w, Line(l.b, l.a))
                   swap(p1.y, p2.y);
                                                                                                                  || pointOnLineLeft
                                                                                                                  (w, Line(u, v))) {
return false;
              if (p1 == p2) {
                   return {3, p1, p2};
                                                                                                        } else {
                   return {2, p1, p2};
                                                                                                                  || pointOnLineLeft
         }
                                                                                                                  (w, Line(u, v))) {
return false;
    }
    auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
                                                                                                             }
                                                                                                        }
                                                                                                   }
    auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
                                                                                              }
                                                                                         }
    template < class T>
    Point p = lineIntersection(l1, l2); if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
                                                                                vector<Point<T>> hp(vector<Line<T>> lines) {
                                                                                    sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
   auto d1 = l1.b - l1.a;
   auto d2 = l2.b - l2.a;
         return {1, p, p};
    } else {
         return {3, p, p};
                                                                                         if (sgn(d1) != sgn(d2)) {
    return sgn(d1) == 1;
template < class T>
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
                                                                                          return cross(d1, d2) > 0:
    if (get<0>(segmentIntersection(l1, l2)) != 0) {
                                                                                     });
         return 0.0;
                                                                                     deque<Line<T>> ls;
                                                                                     deque <Point <T>> ps;
for (auto l : lines) {
     return min({distancePS(l1.a, l2), distancePS(l1
          .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
                                                                                         if (ls.empty())
}
                                                                                               ls.push_back(l);
template < class T>
                                                                                               continue;
}
     int n = p.size();
                                                                                          while (!ps.empty() && !pointOnLineLeft(ps.back(), l)) {
    if (!pointInPolygon(l.a, p)) {
                                                                                              ps.pop_back();
ls.pop_back();
         return false;
     if (!pointInPolygon(l.b, p)) {
                                                                                          while (!ps.empty() && !pointOnLineLeft(ps[0], l)) {
         return false:
                                                                                              ps.pop_front();
ls.pop_front();
    for (int i = 0; i < n; i++) {
   auto u = p[i];
   auto v = p[(i + 1) % n];</pre>
         auto w = p[(i + 2) \% n];
auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
                                                                                         if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
                                                                                               if (dot
                                                                                                    (l.b - l.a, ls.back().b - ls.back().a) > 0) {
         if (t == 1) {
    return false;
                                                                                                   if (!pointOnLineLeft(ls.back().a, l)) {
                                                                                                        assert(ls.size() == 1);
         if (t == 0) {
              continue;
                                                                                                   continue;
         if (t == 2) {
              if (pointOnSegment(v, l) && v != l.a && v != l.b) {
                                                                                               return {};
                   if (cross(v - u, w - v) > 0) {
    return false;
                                                                                          ps.push_back(lineIntersection(ls.back(), l));
                                                                                          ls.push_back(l);
         } else {
              while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0])) {
    ps.pop_back();
                                                                                          ls.pop_back();
                        return false;
              } else if (p1 == v) {
   if (l.a == v) {
                                                                                     if (ls.size() <= 2) {</pre>
                        ps.push back(lineIntersection(ls[0], ls.back()));
                                 (w, Line(u, v))) {
return false;
                                                                                     return vector(ps.begin(), ps.end());
                                                                               using P = Point<i64>;
                            if (pointOnLineLeft(w, l)
                                 || pointOnLineLeft
                                                                                10.2 Convex Hull [01a63e]
                                 (w, Line(u, v))) {
return false;
                                                                                int main() {
                                                                                     int n; cin >> n;
vector <P> P(n), U, L;
for (int i = 0; i < n; i++) {</pre>
                   } else if (l.b == v) {
    if (pointOnLineLeft(u, Line(l.b, l.a))) {
        if (pointOnLineLeft(w, Line(l.b, l.a)))
                                                                                         cin >> P[i]:
                                  && pointOnLineLeft
                                                                                     sort(P.begin(), P
    .end(), [](const Point<i64> &a, const Point<i64> &b) {
    return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
                                 (w, Line(u, v))) {
return false;
                       } else {
   if (pointOnLineLeft(w, Line(l.b, l.a))
                                                                                     || pointOnLineLeft
                                       (w, Line(u, v))) {
                                                                                              L.pop_back();
```

constexpr double Eps = 1e-7;

return mx;

double mx = 0;
for (auto& p : a)

auto searchY = [&](double x) {

return (l + r) / 2;

if (ansl > ansr) l = ml;

else r = mr;

void solve(int n, vector<P> a, double maxR) {
 auto cal = [&](P center) {

mx = max(mx, distance(center, p));

double l = -maxR, r = maxR;
while (r - l > Eps) {
 double d = (r - l) / 3;
 double ml = l + d, mr = r - d;
 double ansl = cal({x, ml}), ansr = cal({x, mr});
 if (ansl > ansr) l = ml;

};
double l = -maxR, r = maxR;
while (r - l > Eps) {
 double d = (r - l) / 3;
 double ml = l + d, mr = r - d;
 double yl = searchY(ml), yr = searchY(mr);
 double ansl = cal({ml, yl}), ansr = cal({mr, yr});

if (accl > accs) l - ml

double ansX = (l + r) / 2, ansY = searchY(ansX);

```
while (U.size() >= 2 && cross(U.back()
                     - U[U.size() - 2], P[i] - U[U.size() - 2]) > 0LL){
                   U.pop_back();
             L.push_back(P[i]);
            U.push_back(P[i]);
      cout << L.size() + U.size() - 2 << "|n";
for (int i = 0; i < L.size() - 1; i++) {
    cout << L[i].x << " " << L[i].y << "|n";</pre>
      for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << "\n";</pre>
}
```

10.3 MinEuclideanDistance [469a8f]

```
T distanceSquare(const Point<T> &a, const Point<T> &b) {
    return square(a - b);
void solve() {
    int n; cin >> n;
constexpr i64 inf = 8e18;
    vector <Point < i64 >> a(n);
         i64 x, y;
cin >> x >> y;
         a[i] = Point < i64 > (x, y);
    struct sortY {
         bool operator()
             (const Point<i64> &a, const Point<i64> &b) const {
             return a.y < b.y;</pre>
        }
    struct sortXY {
         bool operator()
              (const Point<i64> &a, const Point<i64> &b) const {
             if (a.x == b.x) return a.y < b.y;
else return a.x < b.x;</pre>
        }
    sort(a.begin(), a.end(), sortXY());
    vector < Point < i64 >> t(n);
    auto devide = [&](auto &&self, int l, int r) -> i64 {
   if (l == r) return inf;
   int m = (l + r) / 2;
         i64 ans = min(self(self, l, m), self(self, m + 1, r));
         i64 \ midval = a[m].x;
         i64 p = 0;
for (int i = l; i <= r; i++) {
   if ((midval - a[i].x) * (midval - a[i].x) <= ans) {</pre>
                  t[p++] = a[i];
         ans = min(ans, distanceSquare(t[i], t[j]));
                  if ((t[i].y
                         t[j].y) * (t[i].y - t[j].y) > ans) break;
             }
         return ans;
    cout << devide(devide, 0, n - 1) << "\n";
```

10.4 LatticePoints [7750d6]

```
int main() {
     area += cross(polygon[i], polygon[(i + 1) % n]);
     area = abs(area);
     auto countBoundaryPoints
             = [](const vector<Point<i64>>& polygon) -> i64 {
           i64 res = 0;
           int n = polygon.size();
for (int i = 0; i < n; i++) {
    i64 dx = polygon[(i + 1) % n].x - polygon[i].x;
    i64 dy = polygon[(i + 1) % n].y - polygon[i].y;
    res += std::gcd(abs(dx), abs(dy));</pre>
           return res:
      i64 res = countBoundaryPoints(polygon);
     i64 ans = (area - res + 2) / 2;
cout << ans << " " << res << " \n";
```

10.5 MinRadiusCoverCircle [a9fa76]