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```

1 Basic

1.1 Install VScode [d41d8c]

1.2 Default Code [d41d8c]

```
#include <bits/stdc++.h>
// #pragma GCC target("popent")
// C++ 20 vector grammer will not work
using namespace std;
using ll = long long;

void solve() {
}

int main() {
   ios_base::sync_with_stdio(false);
   cin.tie(nullptr);
   int t = 1;
   cin >> t;
   while (t--) {
      solve();
   }
}
```

1.3 Compare Fuction [d41d8c]

```
| // 1. sort, 二分搜刻在函式內 lambda 就好 | // 2. priority queue 小到大是 >, set 是 < | // 3. set 不能 = , multiset 必須 = | // 4. 確保每個成員都要比到 | // 5. pbds_multiset 不要用 lower_bound | // 6. 如果要用 find, 插入 inf 後使用 upper_bound | // 7. multiset 可以跟 set 一樣使用, 但請注意第 3 \ 4 點 auto cmp = [](int i, int j) { return i > j; }; priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
```

```
vector <int> a {1, 2, 5, 4, 3}; // 小心不要改到 a
auto cmp = [&a](int i, int j) { return a[i] > a[j]; };
priority_queue <int, vector <int>, decltype(cmp)> pq(cmp);
```

1.4 Pbds [d41d8c]

1.5 Double [b44e11]

```
double x;
constexpr static double eps = 1e-12;
Constexpr static double eps = 1e-12;
D() : x{0.0} {}
D(double v) : x{v} {}
double val() const { return x; }
explicit operator double() const { return x; }
  operator -() const {
  return D(-x);
D & operator += (const D & rhs) & {
      x += rhs.x; return *this;
D & operator -= (const D & rhs) & {
      x -= rhs.x; return *this;
D & operator *= (const D & rhs) & {
      x *= rhs.x; return *this;
D & operator /= (const D & rhs) & {
    assert(fabs(rhs.x) > eps);
    x /= rhs.x; return *this;
friend D operator+(D lhs, const D &rhs) {
     return lhs += rhs;
friend D operator - (D lhs, const D &rhs) {
     return lhs -= rhs;
friend D operator*(D lhs, const D &rhs) {
     return lhs *= rhs;
friend D operator/(D lhs, const D &rhs) {
     return lhs /= rhs;
friend bool operator < (const D &lhs, const D &rhs) {</pre>
     return lhs.x - rhs.x < -eps;</pre>
friend bool operator>(const D &lhs, const D &rhs) {
   return lhs.x - rhs.x > eps;
friend bool operator==(const D &lhs, const D &rhs) {
   return fabs(lhs.x - rhs.x) < eps;</pre>
friend bool operator <= (const D &lhs, const D &rhs) {
   return lhs < rhs || lhs == rhs;</pre>
return lhs > rhs || lhs == rhs;
friend bool operator!=(const D &lhs, const D &rhs) {
   return !(lhs == rhs);
friend istream &operator>>(istream &is, D &a) {
      double v; is >> v; a = D(v); return is;
friend ostream & operator << (ostream & os, const D & a) {
    return os << fixed << setprecision(10) << a.val()
    + (a.val() > 0 ? eps : a.val() < 0 ? -eps : 0);</pre>
} // eps should < precision
```

1.6 Rng [3ff504]

};

```
mt19937_64 rng
     (chrono::steady_clock::now().time_since_epoch().count());
ll x = rng();
```

2 Graph

2.1 DFS And BFS [e2d856]

```
int main() {
    int n;
    vector<vector<int>> adj(n);
    // dfs_graph
    vector<bool> vis(n);
    auto dfs = [&](auto self, int u) -> void {
        if (vis[u]) return;
        vis[u] = true;
        for (auto v: adj[u]) {
            self(self, v);
        }
}
```

```
dfs(dfs, 0);
// bfs
vector < int > depth(n. 1e9):
queue<int> q;
auto bfs = [%](auto self, int s) -> void {
   vis[s] = true, depth[s] = 0;
   q.push(s);
         q.pusn(s);
while (!q.empty()) {
   int u = q.front(); q.pop();
   for (auto v : adj[u]) {
      if (vis[v]) continue;
      vis[v] = true;
      depth[v] = depth[u] + 1;
      conth(v);
                           q.push(v);
                  }
         }
bfs(bfs, 0);
```

2.2 Prim [3a3805]

```
auto prim =
     [&](int n, vector<vector<pair<int, int>>> &adj) -> bool {
   int node_sz = 0;
        node_sz++;
        for (auto v : adj[u]) {
   if (!vis[v.first]) {
      pq.emplace(v.second, v.first);
}
       }
    if (node_sz == n) return true;
    return false;
};
```

2.3 BellmanFord [430ded]

```
// 用 Bellman Ford 找負環
int main() {
     int n, m; cin >> n >> m;
vector<array<int, 3>> e;
for (int i = 0; i < m; i++) {</pre>
           int u, v, w; cin >> u >> v >> w;
u--, v--; e.push_back({u, v, w});
      vector<ll> dis(n, inf), par(n);
     par[v] = u;
if (i == n) t = v;
                }
           }
     if (t == -1) { cout << "NO|n"; return; }
for (int i = 1; i < n; i++) t = par[t];
vector <int> ans {t};
     int i = t;
do {
           i = par[i];
     ans.push_back(i);
} while (i != t);
      reverse(ans.begin(), ans.end());
      cout << "YES\n";
      for (auto x : ans) cout << x + 1 << " ";
```

2.4 FloydWarshall [3f61a4]

```
constexpr ll inf = 1e18;
  void FloydWarshall(int n, int m) {
         int n, m; cin >> n >> m;
vector<vector<int>> dis(n, vector<int>(n, inf));
         for (int i = 0; i < m; i++) {
  int u, v, w; cin >> u >> v >> w;
  dis[u][v] = min(dis[u][v], w);
  dis[v][u] = min(dis[v][u], w);
         for (int i = 0; i < n; i++) dis[i][i] = 0;
for (int k = 0; k < n; k++) {
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            dis[i][j</pre>
                                          ] = min(dis[i][j], dis[i][k] + dis[k][j]);
                        }
                 }
| const int N = 500; // Floyd 封包
```

```
}
```

2.5 Euler [4177dc]

```
| // 1. 無向圖是歐拉圖:
// 非零度頂點是連通的
// 頂點的度數都是偶數
| // 2. 無向圖是半歐拉圖(有路沒有環):
// 非零度頂點是連通的
// 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
// 非零度頂點是強連通的
// 每個頂點的入度和出度相等
| // 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
// 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
// 其他頂點的入度和出度相等
g[u].erase(v);
self(self, v);
   ans.push_back(u);
dfs(dfs, 0);
reverse(ans.begin(), ans.end());
```

2.6 SCC [5d3e16]

```
struct SCC {
      int n, cur, cnt;
vector<vector<int>> adj;
vector<int>> stk, dfn, low, bel;
SCC(int n_ = 0) { init(n_); }
void init(int n_) {
             n = n:
             adj.assign(n, {});
             dfn.assign(n, -1);
             low.resize(n);
             bel.assign(n, -1);
             stk.clear();
             cur = cnt = 0;
       void addEdge(int u, int v) {
             adj[u].push_back(v);
       void dfs(int x) {
    dfn[x] = low[x] = cur++;
             stk.push_back(x);
for (auto y : adj[x]) {
    if (dfn[y] == -1) {
                          dfs(y);
                   low[x] = min(low[x], low[y]);

else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
             if (dfn[x] == low[x]) {
                    int y;
do {
                          y = stk.back();
                          bel[y] = cnt;
                          stk.pop_back();
                    } while (y != x);
                    cnt++;
             }
       vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
             return bel;
       struct Graph {
             int n;
vector<pair<int, int>> edges;
             vector<int> cnte;
       Graph compress() {
             Graph g;
             g.n = cnt;
             g.siz.resize(cnt);
             g.cnte.resize(cnt);
             for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;
    for (auto j : adj[i]) {
        if (bel[i] != bel[j]) {
    }
}</pre>
```

```
dfn.assign(n, -1);
     low.resize(n);
     parent.assign(n, -1);
is_cut.assign(n, false);
      cur = 0;
void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
void dfs(int x) {
     int children = 0;

dfn[x] = low[x] = cur++;

for (int v : adj[x]) {

   if (dfn[v] == -1) {
                children++;
parent[v] = x;
                 low[x] = min(low[x], low[v]);
                 if (parent[x] != -1 && low[v] >= dfn[x]) {
                      is_cut[x] = true;
           } else if (v != parent[x]) {
                 low[x] = min(low[x], dfn[v]);
      if (parent[x] == -1 && children > 1) {
    is_cut[x] = true;
     }
```

2.8 EBCC [59d8ca]

}

};

```
struct EBCC { // CF/contest/1986/pF
   int n, cur, cnt;
     vector < int >> adj;
     vector<int> stk, dfn, low, bel;
    vector<pair<int, int>> bridges; // 關鍵邊
EBCC(int n_ = 0) { init(n_); }
void init(int n_) {
         n = n_;
         adj.assign(n, {});
         dfn.assign(n, -1);
low.resize(n);
          bel.assign(n, -1);
          stk.clear();
          bridges.clear();
          cur = cnt = 0;
    void addEdge(int u, int v) {
         adj[u].push_back(v);
adj[v].push_back(u);
     void dfs(int x, int p) {
         dfn[x] = low[x] = cur++;
         dfs(y, x);
low[x] = min(low[x], low[y]);
if (low[y] > dfn[x]) {
                        bridges.emplace_back(x, y);
              } else if (bel[y] == -1) {
                   low[x] = min(low[x], dfn[y]);
          if (dfn[x] == low[x]) {
              int y;
do {
                   y = stk.back();
```

```
bel[y] = cnt;
                         stk.pop_back();
                   } while (y != x);
                   cnt++:
            }
       fvector <int> work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
        }
}</pre>
             return bel;
       struct Graph {
             int n;
             vector<pair<int, int>> edges;
             vector<int> siz; // BCC 內節點數
             vector<int> cnte; // BCC 內邊數
       Graph compress() {
             Graph g;
g.n = cnt;
             g.siz.resize(cnt);
             g.cnte.resize(cnt);
                                        g.siz[bel[i]]++;
                   for (auto j : adj[i]) {
    if (bel[i] < bel[j]) {</pre>
                         g.edges.emplace_back(bel[i], bel[j]);
} else if (i < j) {
   g.cnte[bel[i]]++;</pre>
                   }
             return g;
       }
};
 2.9 2-SAT [eeddc1]
 // CSES Giant Pizza
 struct TwoSat {
       int n; vector<vector<int>> e;
       vector<bool> ans;
       vector < bool > ans;
TwoSat(int n) : n(n), e(2 * n), ans(n) {}
void addClause(int u, bool f, int v, bool g) {
    e[2 * u + !f].push_back(2 * v + g);
    e[2 * v + !g].push_back(2 * u + f);
       bool satisfiable() {
             int now = 0, cnt = 0;
function < void(int) > tarjan = [&](int u) {
                   stk.push_back(u);
dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
                               tarjan(v);
                         low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in stk
low[u] = min(low[u], dfn[v]);
                   if (dfn[u] == low[u]) {
                          int v;
                         do {
    v = stk.back();
                         stk.pop_back();
id[v] = cnt;
} while (v != u);
                          ++cnt:
                  }
             for (int i
             return true:
       vector<bool> answer() { return ans; }
 };
int main() {
       int m, n; cin >> m >> n;
TwoSat ts(n);
for (int i = 0; i < m; ++i) {</pre>
             int u, v; char x, y;
cin >> x >> u >> y >> v;
ts.addClause(u - 1, x == '+', v - 1, y == '+');
       if (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";</pre>
```

else cout << "IMPOSSIBLE\n";</pre>

2.10 Funtional Graph [85c464]

```
constexpr int N = 2e5 + 5;
int cht[N][31]; // 倍增表, 放外面不然 TLE
struct FuntionalGraph {
        int n, cnt;
vector <int> g, bel, id, len, in, top;
FuntionalGraph() : n(0) {}
FuntionalGraph(vector <int> g_) { init(g_); }
         void init(vector<int> g_) { init(g_
void init(vector<int> g_) {
    n = g_.size(); cnt = 0;
    g = g_; bel.assign(n, -1);
    id.resize(n); len.clear();
    in.assign(n, 0); top.assign(n, -1);
}
                  build();
         in[g[i]]++;
                  for (int i = 1; i <= 30; i++)
    for (int u = 0; u < n; u++)
        cht[u][i] = cht[cht[u][i - 1]][i - 1];
for (int i = 0; i < n; i++)
    if (in[i] == 0) label(i);
for (int i = 0; i < n; i++)
    if (too[i] == 1) label(i);</pre>
                           if (top[i] == -1) label(i);

}
void label(int u) {
    vector int > p; int cur = u;
    while (top[cur] == -1) {
        top[cur] = u;
    }
}

                          p.push_back(cur);
                           cur = g[cur];
                  auto s = std::find(p.begin(), p.end(), cur);
                 vector < int> cyc(s, p.end());
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {
    bel[cyc[i]] = cnt;
}</pre>
                           id[cyc[i]] = i;
                  cnt++; len.push_back(cyc.size());
                  for (int i = p.size() - 1; i > 0; i--)
   id[p[i - 1]] = id[p[i]] - 1;
         int jump(int u, int k) {
    for (int b = 0; k > 0; b++){
        if (k & 1) u = cht[u][b];
}
                  return u;
};
```

3 Data Structure

3.1 BIT [d41d8c]

```
template < typename T >
struct Fenwick { // 全部以 0 based 使用
int n; vector<T> a;
Fenwick(int n_ = 0) { init(n_); }
     void init(int n_) {
    n = n_;
           a.assign(n, T{});
     void add(int x, const T &v) {
   for (int i = x + 1; i <= n; i += i & -i) {
      a[i - 1] = a[i - 1] + v;
}</pre>
     T sum(int x) { // 左閉右開查詢
           T`ans{};
           for (int i = x; i > 0; i -= i & -i) {
    ans = ans + a[i - 1];
           return ans;
     T rangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
     int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
           int x = 0;
           T cur{};

for (int i = 1 << __lg(n); i; i /= 2) {

   if (x + i <= n && cur + a[x + i - 1] <= k) {
                      x += i;
                      cur = cur + a[x - 1];
                }
           return x;
     }
template < class T>
struct TwoDFenwick { // 全部以 0 based 使用
     int nx, ny; // row, col 個數
vector < vector < T >> a;
     TwoDFenwick(int nx_ = 0, int ny_ = 0) {
```

```
init(nx_, ny_);
                 void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
                void add(int x, int y, const T &v) {
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            a[i - 1][j - 1] = a[i - 1][j - 1] + v;
        }
}</pre>
                            }
                }
                 T sum(int x, int y) { // 左閉右開查詢
                            return ans;
               }
T rangeSum
                                (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                              return sum(
                                              (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
               }
 };
   3.2 RangeBit [d41d8c]
template < class T >
   struct rangeFenwick { // 全部以 0 based 使用
                 int n;
                 vector<T> d, di;
rangeFenwick(int n_ = 0) { init(n_); }
void init(int n_) {
                              d.assign(n, T{});
                              di.assign(n, T{});
                Joid add(int x, const T &v) {
   T vi = v * (x + 1);
   for (int i = x + 1; i <= n; i += i & -i) {
        d[i - 1] = d[i - 1] + v;
        di[i - 1] = di[i - 1] + v;
}</pre>
                 void rangeAdd(int l, int r, const T &v) {
   add(l, v); add(r, -v);
                 T sum(int x) { // 左閉右開查詢
                             for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
                              return ans:
                }
                TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
                 int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
                           }
                              return x:
              }
   template < class T>
   struct rangeTwoDFenwick { // 全部以 0 based 使用
                int nx, ny; // row, col 個數
vector<vector<T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
                              init(nx_, ny_);
                void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
                              dij.assign(nx, vector<T>(ny, T{}));
                 void add(int x, int y, const T &v) {
                            d add(int x, int y, const T &v) {
T vi = v * (x + 1);
T vj = v * (y + 1);
T vij = v * (x + 1) * (y + 1);
for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        d[i - 1][j - 1] = d[i - 1][j - 1] + v;
        di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
        dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;</pre>
```

```
dij[i - 1][j - 1] = dij[i - 1][j - 1] + vij;
                      }
                                                                                                                                                                                           3.4 Segment [d41d8c]
           void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
                      add(rx, ry, v);
                                                                                                                                                                                           template < class Info>
                                                                                                                                                                                                       int Seg { // 左閉右開寫法
int n; vector<Info> info;
Seg(): n(0) {}
Seg(int n ***
                      add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
                                                                                                                                                                                            struct Seg {
                                                                                                                                                                                                       Seg(int n_, Info v_ = Info()) { init(n_, v_); }
          T sum(int x, int y) { // 左閉右開查詢
                                                                                                                                                                                                       template < class T>
Seg(vector < T > init_) { init(init_);
                      T ans{};
for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
                                                                                                                                                                                                       void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
                                            ans = ans
                                              + T(x * y + x + y + 1) * d[i - 1][j - 1];  ans = ans - T(y + 1) * d[i - 1][j - 1];  ans = ans - T(x + 1) * d[i - 1][j - 1]; 
                                                                                                                                                                                                       template < class T>
                                                                                                                                                                                                       void init(vector<T> init_) {
                                                                                                                                                                                                                  info.assign(4 << __lg(n), Info());
function <void(
    int, int, int)> build = [&](int p, int l, int r) {
    if (r - l == 1) {
        informal | in
                                                                                                                                                                                                                  n = init_.size();
                                             ans = ans + dij[i - 1][j - 1];
                                 }
                      return ans;
                                                                                                                                                                                                                                         info[p] = init_[l];
           Ť rangeSum
                                                                                                                                                                                                                                         return;
                       (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                                                                                                                                                                                                                             int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                                  (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
                                                                                                                                                                                                                             pull(p);
3.3 DSU [d41d8c]
                                                                                                                                                                                                                  build(1, 0, n);
                                                                                                                                                                                                       void pull(int p) {
    info[p] = info[p * 2] + info[p * 2 + 1];
struct DSU {
           int n;
           vector < int > boss, siz;
                                                                                                                                                                                                       void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
      info[p] = v; return;
}
           DSU() {}
           DSU(int n_) { init(n_); }
           void init(int n_) {
    n = n_; boss.resize(n);
                                                                                                                                                                                                                  int m = (l + r) / 2;
if (x < m) modify(2 * p, l, m, x, v);
else modify(2 * p + 1, m, r, x, v);</pre>
                      iota(boss.begin(), boss.end(), \theta);
                      siz.assign(n, 1);
          int find(int x) {
   if (boss[x] == x) return x;
                                                                                                                                                                                                                   pull(p);
                      return boss[x] = find(boss[x]);
                                                                                                                                                                                                       void modify(int p, const Info &i) {
                                                                                                                                                                                                                  modify(1, 0, n, p, i);
          bool same(int x, int y) {
    return find(x) == find(y);
                                                                                                                                                                                                       Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];</pre>
          bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);
    siz[x] += siz[y];
    if (siz[x] < siz[y]);
    if (siz[x] < siz[x] < siz[y]);
    if (siz[x] < siz[x] < 
                                                                                                                                                                                                                  int m = (l + r) / 2;
                                                                                                                                                                                                                  return query(p
                                                                                                                                                                                                                               2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
                      boss[y] = x;
                                                                                                                                                                                                       Info query(int ql, int qr) {
                                                                                                                                                                                                                  return query(1, 0, n, ql, qr);
                      return true;
                                                                                                                                                                                                        template < class F> // 尋找區間內,第一個符合條件的
          int size(int x) {
    return siz[find(x)];
                                                                                                                                                                                                       int findFirst
                                                                                                                                                                                                                  (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)
    return -1;
if (l >= x && r <= y && !pred(info[p]))</pre>
};
struct DSU {
                                                                                                                                                                                                                              return -1;
                                                                                                                                                                                                                  if (r - l == 1)
          vector<int> boss, siz, stk;
                                                                                                                                                                                                                  return l;
int m = (l + r) /
          DSU() {}
DSU(int n_) { init(n_); }
void init(int n_) {
                                                                                                                                                                                                                  int res = findFirst(2 * p, l, m, x, y, pred);
                                                                                                                                                                                                                  if (res == -1)
                     n = n_;
boss.resize(n);
                                                                                                                                                                                                                              res = findFirst(2 * p + 1, m, r, x, y, pred);
                      iota(boss.begin(), boss.end(), 0);
                      siz.assign(n, 1);
                                                                                                                                                                                                       template < class F> // 若要找 last, 先右子樹遞迴即可
int findFirst(int l, int r, F & & pred) {
    return findFirst(1, 0, n, l, r, pred);
                      stk.clear();
          int find(int x) {
    return x == boss[x] ? x : find(boss[x]);
                                                                                                                                                                                           // ---define structure and info plus---
          bool same(int x, int y) {
    return find(x) == find(y);
                                                                                                                                                                                           struct Info {
          bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);</pre>
                                                                                                                                                                                                       int sum = 0;
                                                                                                                                                                                           Info operator+(const Info &a, const Info &b) {
                                                                                                                                                                                                       return { a.n + b.n, a.sum + b.sum };
                                                                                                                                                                                           }
                      siz[x] += siz[y];
                      boss[y] = x;
                                                                                                                                                                                           3.5 Lazy Segment [d41d8c]
                      stk.push_back(y);
                                                                                                                                                                                          template < class Info, class Tag>
                      return true:
                                                                                                                                                                                            struct LazySeg { // 左閉右開寫法
           void undo(int x) {
    while (stk.size() > x) {
        int y = stk.back();
    }
}
                                                                                                                                                                                                       int n;
                                                                                                                                                                                                       vector<Info> info;
                                                                                                                                                                                                        vector<Tag> tag;
                                 stk.pop_back();
                                                                                                                                                                                                       LazySeg() : n(0) {}
                                                                                                                                                                                                       LazySeg(int n_, Info v_ = Info()) {
  init(n_, v_);
                                 n++
                                 siz[boss[y]] -= siz[y];
                                 boss[y] = y;
                     }
                                                                                                                                                                                                       template < class T>
                                                                                                                                                                                                       LazySeg(vector<T> init_) {
           int size(int x) {
   return siz[find(x)];
                                                                                                                                                                                                                  init(init_);
```

```
void init(int n_, Info v_ = Info()) {
  init(vector(n_, v_));
                                                                                                        }
                                                                                                  };
// ---define structure and info plus---
                                                                                                  struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add; void apply(const Tag& v) { if (v.set_val) {
template < class T>
void init (vector<T> init_) {
      n = init_.size();
      info.assign(4 << __lg(n), Info());
tag.assign(4 << __lg(n), Tag());</pre>
                                                                                                                     set_val = v.set_val;
add = v.add;
       function < void(</pre>
             int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
                                                                                                               else {
                   info[p] = init_[l];
                                                                                                                      add += v.add:
                   return;
                                                                                                               }
                                                                                                        }
             int m = (l + r) / 2;
                                                                                                  build(p * 2, l, m);
build(p * 2 + 1, m, r);
                                                                                                        int sum;
void apply(int l, int r, const Tag &v) {
   if (v.set_val) {
      sum = (r - l) * v.set_val;
      .
            pull(p);
      build(1, 0, n);
                                                                                                               sum += (r - l) * v.add;
(int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
                                                                                                         // Info& operator=(const Info &rhs) {
                                                                                                                   // 部分 assignment 使用 return *this;
                                                                                                        //
//
// }
      tag[p].apply(v);
void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
                                                                                                  Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
                                                                                                  3.6 Treap [d41d8c]
      tag[p] = Tag();
void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
}
                                                                                                  struct Treap {
                                                                                                         Treap t
Treap *lc, *rc;
int pri, siz; bool rev_valid;
int val; int min;
Treap(int val_) {
   min = val = val_;
   pri = val_;
}
      fint m = (l + r) / 2;
push(p, l, r);
if (x < m) {
    modify(2 * p, l, m, x, v);
}</pre>
                                                                                                               pri = rand();
lc = rc = nullptr;
                                                                                                               siz = 1; rev_valid = 0;
                                                                                                         void pull() { // update siz or other information
            modify(2 * p + 1, m, r, x, v);
                                                                                                               siz = 1;
min = val;
      pull(p);
                                                                                                               for (auto c : {lc, rc}) {
    if (!c) continue;
void modify(int p, const Info &i) {
    modify(1, 0, n, p, i);
                                                                                                                      siz += c->siz;
                                                                                                                      min = std::min(min, c->min);
Info query(int p, int l, int r, int ql, int qr) {
   if (qr <= l || ql >= r) return Info();
   if (ql <= l && r <= qr) return info[p];</pre>
                                                                                                               }
                                                                                                         void push() {
    if (rev_valid) {
        swap(lc, rc);
        if (lc) lc->rev_valid ^= 1;
        if (rc) rc->rev_valid ^= 1;
      int m = (l + r) / 2;
push(p, l, r);
return query(p *
             2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
                                                                                                                rev_valid = false;
Info query
       (int ql, int qr) { return query(1, 0, n, ql, qr); }
int find(int k) { // 找到 min 是 k 的位置 (1-based)
                                                                                                               push();
int ls = (lc ? lc->siz : 0) + 1;
                                                                                                               if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
            apply(p, l, r, v);
            return;
                                                                                                        }
     int m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
pull(p);
                                                                                                  int size(Treap *t) {
    return t ? t->siz : 0;
                                                                                                  Treap *merge(Treap *a, Treap *b) {
   if (!a || !b) return a ? a : b;
   a->push(); b->push();
void range_apply(int l, int r, const Tag &v) {
                                                                                                         if (a->pri > b->pri) {
    a->rc = merge(a->rc, b);
      range_apply(1, 0, n, l, r, v);
                                                                                                               a->pull();
template < class F> // 尋找區間內,第一個符合條件的
                                                                                                               return a;
int findFirst
      (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
    return -1;</pre>
                                                                                                         else {
                                                                                                               b->lc = merge(a, b->lc);
b->pull();
                                                                                                               return b;
      if (l >= x && r <= y && !pred(info[p])) {</pre>
                                                                                                        }
            return -1:
                                                                                                  pair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
      if (r - l == 1) {
            return l;
      int m = (l + r) / 2;
                                                                                                         t->push();
                                                                                                         if (size(t->lc) < k) {
    auto [a, b] = split(t->rc, k - size(t->lc) - 1);
    t->rc = a;
      push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
      if (res == -1)
            res = findFirst(2 * p + 1, m, r, x, y, pred);
                                                                                                               t->pull();
                                                                                                               return {t, b};
      return res;
}
template < class F> // 若要找 last,先右子樹遞迴即可
int findFirst(int l, int r, F & pred) {
    return findFirst(1, 0, n, l, r, pred);
                                                                                                               auto [a, b] = split(t->lc, k);
t->lc = b;
                                                                                                               t->pull();
                                                                                                               return {a, t};
```

if (mn > 0) {
 e.flow += mn;

T work(int s_, int t_) {
 s = s_; t = t_; T flow = 0;

} }

edges[adj[u](cur] ^ 1].flow -= mn;

return 0; // 到不了終點就會 return 0

```
while (bfs()) {
   fill(ptr.begin(), ptr.end(), 0);
           }
                                                                                                                                                                                                                  while (true) {
   T res = dfs(s, INF_Flow);
   if (res == 0) break;
void Print(Treap *t) {
           if (!t) return;
t->push();
           Print(t->lc);
                                                                                                                                                                                                                            flow += res;
           cout << t->val;
Print(t->rc);
                                                                                                                                                                                                                 }
                                                                                                                                                                                                       return flow;
                                                                                                                                                                                            void reset() {
   for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
3.7 Mo [d41d8c]
struct query {
   int l, r, id;
} typedef query;
void MO(int n, vector<query> &queries) {
   int block = sqrt(n);
}
                                                                                                                                                                                 }:
                                                                                                                                                                                 4.2 Min Cut [44ae6c]
           function <body>
function <br/>
functio
                                                                                                                                                                              // CSES Police Chase
int main(){
                                                                                                                                                                                            int n, m; cin >> n >> m;
Dinic < int > g(n);
for (int i = 0; i < m; i++) {</pre>
                      return a.r < b.r;
                                                                                                                                                                                                      int u, v, cap = 1;
cin >> u >> v;
           sort(queries.begin(), queries.end(), cmp);
                                                                                                                                                                                                      u--; v--:
void compress(vector<int> &nums) {
                                                                                                                                                                                                      g.add_edge(u, v, cap);
g.add_edge(v, u, cap);
           vector < int > sorted = nums;
sort(sorted.begin(), sorted.end());
           sorted.erase
                                                                                                                                                                                            int res = g.work(0, n - 1);
cout << res << "\n";
           if (res == 0) return;
                                                                                                                                                                                            vector<int> vis(n);
                                                                                                                                                                                            auto find = [&](auto self, int u) -> void {
   if (!vis[u]) {
                                                                                                                                                                                                                  vis[u] = 1;
4 Flow
                                                                                                                                                                                                                  for (int id : g.adj[u])
                                                                                                                                                                                                                            auto e = g.edges[id];
if (e.cap - e.flow > 0) {
4.1 Dinic [aa12d4]
                                                                                                                                                                                                                                      self(self, e.to);
template < class T>
                                                                                                                                                                                                                 }
struct Dinic {
           struct Edge {
                                                                                                                                                                                                      }
                     int to;
                                                                                                                                                                                           };
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
        auto e = g.edges[id];
        if (!vis[e.to]) {
            cout << i + 1 << " " << e.to + 1 << " | n";
}</pre>
                     T flow, cap; // 流量跟容量
           int n, m, s, t;
const T INF_FloW = 1 << 30;
           vector<vector<int>>> adj; // 此點對應的 edges 編號
          vector < Vector < Lnt>> ad]; // 此對到應的 vector < Edge> edges; // 幫每個 edge 編號 vector < int> dis, ptr; Dinic(int n_ = 0) { init(n_); } void init(int n_) { n = n_; m = 0; dis.resize(n); ptr.resize(n); adj.assign(n, vector < int>{});
                                                                                                                                                                                                      }
                                                                                                                                                                                           }
                                                                                                                                                                                 }
                      edges.clear();
                                                                                                                                                                                  4.3 MCMF [77fc99]
           void add_edge(int u, int v, T cap) {
                                                                                                                                                                                  template < class Tf, class Tc>
                      // 偶數 id 是正向邊
                     // 何數 ta 定比问您
edges.push_back({ v, 0, cap });
edges.push_back({ u, 0, 0 });
adj[u].push_back(m++);
adj[v].push_back(m++);
                                                                                                                                                                                  struct MCMF {
                                                                                                                                                                                            struct Edge {
                                                                                                                                                                                                      int to;
                                                                                                                                                                                                      Tf flow, cap; // 流量跟容量
           bool bfs() {
                      fill(dis.begin(), dis.end(), -1);
dis[s] = 0; queue<int> q;
                                                                                                                                                                                             // 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就好
                                                                                                                                                                                            int n, m, s, t;
const Tf INF_FLOW = 1 << 30;
const Tc INF_COST = 1 << 30;</pre>
                      q.push(s);
                     vector<vector<int>> adj;
                                                                                                                                                                                            vector<Edge> edges; // 幫每個 edge 編號
vector<Tc> dis, pot; // johnson algorithm, using spfa
vector<int> rt; // 路徑恢復,對應 id
                                                                                                                                                                                            vector <book inq;
MCMF(int n = 0) { init(n); }
void init(int n) {</pre>
                                                      q.push(e.to);
                                                                                                                                                                                                      n = n_; m = 0;
edges.clear();
adj.assign(n, vector<int>{});
                                }
                      return dis[t] != -1;
           }
T dfs(int u, T flow) {
    if (flow == 0) return 0;
    '    ' -- t) return flow;
                                                                                                                                                                                            void add_edge(int u, int v, Tf cap, Tc cost){
  edges.push_back({v, 0, cap, cost});
  edges.push_back({u, 0, 0, -cost});
                                                                                                                                                                                                      adj[u].push_back(m++);
adj[v].push_back(m++);
                      for (int
                                    &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {</pre>
                                tage &e = edges[adj[u][cur]];
if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;
T mn = dfs(e.to, min(flow, e.cap - e.flow));
```

bool spfa() {

dis.assign(n, INF_COST);
rt.assign(n, -1); inq.assign(n, false); queue<int> q; q.push(s), dis[s] = 0, inq[s] = true; while (!q.empty()) {

if (!inq[v]) {

```
q.push(v); inq[v] = true;
                         }
                  }
             return dis[t] != INF_COST;
      }
bool dijkstra() {
    dis.assign(n, INF_COST); rt.assign(n, -1);
    priority_queue<pair<Tc, int>,
        vector<pair<Tc, int>>, greater<pair<Tc, int>>> pq;
    dis[s] = 0; pq.emplace(dis[s], s);
    vebile (log empty()) {
            pq.emplace(ndis, v);
                  }
             return dis[t] != INF_COST;
      dis[i] += pot[i] - pot[s];
                   Tf f = INF_FLOW;
                   for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                (f, edges[rt[i]].cap - edges[rt[i]].flow);
                  f = min<Tf>(f, need);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
                   flow += f; need -= f;
cost += f * dis[t]; fr = false;
                   swap(dis, pot);
if (need == 0) break;
             return make_pair(flow, cost);
      }
      // 限定 cost, 最大化 flow
pair<ff, Tc> work_budget(int s_, int t_, Tc budget) {
    s = s_, t = t_; pot.assign(n, 0);
    Tf flow{}; Tc cost{}; bool fr = true;
    while ((fr ? spfa() : dijkstra())) {
        for (int i = 0; i < n; i++) {
            dis[i] += pot[i] - pot[s];
        }
                   Tf f = INF_FLOW;
                   for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                (f, edges[rt[i]].cap - edges[rt[i]].flow);
                   f = min<Tf>(f, budget / dis[t]);
                   for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
                   flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
                   swap(dis, pot);
if (budget == 0 || f == 0) break;
             return make_pair(flow, cost);
       void reset() {
             for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
}:
4.4 Hangarian [dfa1c4]
```

```
struct Hangarian { // 0-based
        int n, m;
vector<vector<int>> adj;
        vector <int>> adj;
vector <int>> used, vis;
vector <pair <int, int>> match;
Hangarian(int n_ = 0, int m_ = 0) {
   init(n_, m_);
        void init(int n_, int m_) {
    n = n_; m = m_;
                 adj.assign(n + m, vector<int>());
used.assign(n + m, -1);
vis.assign(n + m, 0);
        void addEdge(int u, int v) {
   adj[u].push_back(n + v);
   adj[n + v].push_back(u);
```

```
bool dfs(int u)
              int sz = adj[u].size();
              for (int i = 0; i < sz; i++) {
   int v = adj[u][i];</pre>
                     if (vis[v] == 0) {
    vis[v] = 1;
                           if (used[v] == -1 || dfs(used[v])) {
    used[v] = u;
                    }
              return false;
        vector<pair<int, int>> work() {
              match.clear(); used.assign(n + m, -1);
vis.assign(n + m, 0);
for (int i = 0; i < n; i++) {
    fill(vis.begin(), vis.end(), 0); dfs(i);</pre>
              for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
                           match.push_back(make_pair(used[i], i - n));
              return match;
       }
};
```

4.5 Theorem [d41d8c]

```
1// 有向無環圖:
// 最小不相交路徑覆蓋:
// 最小路徑數 = 頂點數 - 最大匹配數
| // 最小相交路徑覆蓋:
// 先用
   Floyd 求傳遞封包,有連邊就建邊,然後再套最小不相交路徑覆蓋
// 二分圖:
// 最小點覆蓋 = 最大匹配數
// 選出一些點,讓所有邊至少有一個端點在點集中的最少數量
// 最少邊覆蓋: 選出一些邊,讓所有點都覆蓋到的最少數量
// 最少邊覆蓋 = 點數 - 最大匹配數
// 最大獨立集: 選出一些點, 使這些點兩兩沒有邊連接的最大數量
// 最大獨立集 = 點數 - 最大匹配數
```

5 String

5.1 Hash [852711]

```
constexpr int B = 59;
vector<Z> Hash(string &s) {
      vector < Z > ans {0};
for (auto c : s) {
            ans.push_back(ans.back() * B + (c - 'a' + 1));
      return ans;
void solve() {
      string s, sub;
cin >> s >> sub;
auto a = Hash(s);
      auto q = Hash(sub);
       auto find = q.back();
      int ans = 0;
int l = 1, r = sub.size(), len = sub.size();
while (r <= s.size()) {
    if (a[r] - a[l - 1] * power(Z(B), len) == find) {
                  ans++;
            l++, r++;
      cout << ans << "\n";
```

5.2 KMP [cddfd9]

```
struct KMP {
    string sub;
vector<int> failure;
    KMP(string sub_) {
        sub = sub_;
failure.resize(sub.size(), -1);
        buildFailFunction();
    while (now != -1
             && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
        }
    vector<int> match(string &s) {
        vector<int> match;
```

if (cp > lcp){
 lcp = cp;
 p = i;

}

```
for (int i = 0, now = -1; i < (int)s.size(); i++) {
   // now is the compare sucessed length -1</pre>
                                                                                                                                                                     if (lcp) {
                           while (s[i] !=
                                                                                                                                                                              return s.substr(p, lcp);
                                 sub[now + 1] && now != -1) now = failure[now];
failure stores if comparison fail, move to where
                                                                                                                                                                    } else {
                                                                                                                                                                             return "-1";
                           if (s[i] == sub[now + 1]) now++;
if (now + 1 == (int)sub.size()) {
   match.push_back(i - now);
                                                                                                                                                          }
                                                                                                                                                 };
                                    now = failure[now];
                                                                                                                                                   5.5 Manacher [9c9ca6]
                           }
                                                                                                                                                   // 找到對於每個位置的迴文半徑
                  return match:
        }
                                                                                                                                                   vector<int> manacher(string s) {
}:
                                                                                                                                                            string t = "#";
                                                                                                                                                            for (auto c : s) {
5.3 Z Function [764b31]
                                                                                                                                                                    t += c;
t += '#';
// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
// 的最長公共前綴 (LCP) 的長度
vector<int> Z(string s) {
  int n = s.size();
                                                                                                                                                            int n = t.size();
                                                                                                                                                            vector<int> r(n);
                                                                                                                                                            for (int i = 0, j =
         vector <int> z(n); z[0] = n;
for (int i = 1, j = 1; i < n; i++) {
    z[i] = max(0, min(j + z[j] - i, z[i - j]));</pre>
                                                                                                                                                                    0; i < n; i++) { // i 是中心, j 是最長回文字串中心 if (2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
                  while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]])
                                                                                                                                                                      Jet it is a second of the second of the
                           z[i]++:
                  if (i + z[i] > j + z[j]) j = i;
                                                                                                                                                                              r[i] += 1;
         return z; // 最後一格不算
                                                                                                                                                                    if (i + r[i] > j + r[j]) {
    j = i;
}
5.4 SA [d40e3e]
                                                                                                                                                                    }
                                                                                                                                                            return r;

// # a # b # a #

// 1 2 1 4 1 2 1

// # a # b # b # a #

// 1 2 1 2 5 2 1 2 1
struct SuffixArray {
         int n; string s;
vector<int> sa, rk, lc;
         // n: 字串長度
         // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
                                                                                                                                                            // 值 -1 代表原回文字串長度
         // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
         // lc: LCP
                                                                                                                                                            // (id - val + 1) / 2 可得原字串回文開頭
         數組,lc[i] 表示 sa[i] 和 sa[i + 1] 的最長公共前綴長度
SuffixArray(const string &s_) {
   s = s_; n = s.length();
                                                                                                                                                   5.6 SAM [d15619]
                  sa.resize(n);
                                                                                                                                                   struct SAM {
                  lc.resize(n - 1);
                                                                                                                                                            static constexpr int ALPHABET_SIZE = 26;
struct Node {
                  rk.resize(n);
                   iota(sa.begin(), sa.end(), 0);
                 rotalsa.begin(), sa.en(), 0),
sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });
rk[sa[0]] = 0;
for (int i = 1; i < n; ++i)</pre>
                                                                                                                                                                    int link;
                                                                                                                                                                     array<int, ALPHABET_SIZE> next;
                                                                                                                                                                     Node(): len{}, link{}, next{}{}
                           rk[sa[i]]
                                       = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
                                                                                                                                                            vector < Node > t
                                                                                                                                                            SAM() { init(); }
                                                                                                                                                             void init() {
                  vector < int > tmp, cnt(n);
                                                                                                                                                                    t.assign(2, Node()
t[0].next.fill(1);
                  tmp.reserve(n);
while (rk[sa[n - 1]] < n - 1) {</pre>
                                                                                                                                                                                               Node());
                                                                                                                                                                    t[0].len = -1;
                           tmp.clear();
for (int i = 0; i < k; ++i)
    tmp.push_back(n - k + i);</pre>
                                                                                                                                                            int newNode() {
                                                                                                                                                                     t.emplace_back();
                           for (auto i : sa)
    if (i >= k)
        tmp.push_back(i - k);
                                                                                                                                                                     return t.size() - 1;
                           tmp.pusn_pack(i - k);
fill(cnt.begin(), cnt.end(), 0);
for (int i = 0; i < n; ++i)
    ++cnt[rk[i]];
for (int i = 1; i < n; ++i)
    cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; --i)
                                                                                                                                                            int extend(int p, int c) {
    if (t[p].next[c]) {
                                                                                                                                                                              int q = t[p].next[c];
if (t[q].len == t[p].len + 1) {
                                                                                                                                                                                      return q;
                                                                                                                                                                              int r = newNode();
                                    sa[--cnt[rk[tmp[i]]]] = tmp[i];
                                                                                                                                                                             thr - hewhold (),

t[r].len = t[p].len + 1;

t[r].link = t[q].link;

t[r].next = t[q].next;

t[q].link = r;
                          while (t[p].next[c] == q) {
                                                                                                                                                                                      t[p].next[c] = r;
p = t[p].link;
                  for (int i = 0, j = 0; i < n; ++i) {
   if (rk[i] == 0) {</pre>
                                                                                                                                                                              return r:
                                                                                                                                                                     int cur = newNode();
                                   j = 0;
                                                                                                                                                                    t[cur].len = t[p].len + 1;
while (!t[p].next[c]) {
    t[p].next[c] = cur;
                           } else {
                                    for (j
                                                -= j > 0; i + j < n && sa[rk[i] - 1] + j
                                                                                                                                                                              p = t[p].link;
                                              < n && s[i + j] == s[sa[rk[i] - 1] + j]; )
                                                                                                                                                                     t[cur].link = extend(p, c);
                                   lc[rk[i] - 1] = j;
                                                                                                                                                                     return cur;
                          }
                                                                                                                                                          }
                 }
         string getLCP() {
   int cp = 0, k, lcp = 0, p;
   for (int i = 0; i < n; i++) {
      if (!rk[i]) continue;</pre>
                                                                                                                                                   void solve() {
                                                                                                                                                            string s; cin >> s;

int n = s.length();
                                                                                                                                                            vector<int> pos(n + 1); // s[i - 1] 的後綴終點位置
                           k = sa[rk[i] - 1];
                                                                                                                                                            pos[0] = 1;
                           if (cp) cp--;
while (s[i + cp] == s[k + cp]) cp++;
                                                                                                                                                             SAM sam;
                                                                                                                                                            for (int i = 0; i < n; i++) {
   pos[i + 1] = sam.extend(pos[i], s[i] - 'a');</pre>
```

}

5.7 Trie [3b3aa0]

```
struct Trie {
             struct trie_node {
   bool is_word;
                             vector < trie_node *> children;
                             trie_node() {
   is_word = false;
                                           children.resize(26, NULL);
               trie_node *root = <mark>new</mark> trie_node();
             void insert(string &s) {
    trie_node *cur = root;
    for (int i = 0; i < s.size(); i++) {
        int idx = s[i] - 'a';
        record in the string in the string
                                           if (cur->children[idx] == NULL) {
    cur->children[idx] = new trie_node();
                                           cur = cur->children[idx];
                             cur->is_word = true;
             bool is_in_trie(string &s) {
    trie_node *cur = root;
    for (int i = 0; i < s.size(); i++) {</pre>
                                           if (cur->
                                           children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
                             return true:
             ->children[s[j] - 'a'] == nullptr) return ans;
cur = cur->children[s[j] - 'a'];
                                           if (cur->is_word)
     (ans += dp[j + 1]) %= mod;
                             return ans;
             }
};
int main() {
             // 找到 sub 集合裡,可以重複用,組成 s 的組數 Trie trie;
             string s; cin >> s;
int sz = s.size();
              // dp 代表 i 開頭到最後的配對總數
              // 找到有結尾為 stop 的 dp[i] += dp[j + 1] int n; cin >> n;
             vector <int> op(sz + 1, 0);
for (int i = 0; i < n; i++) {
    string sub; cin >> sub;
    trie.insert(sub);
             dp[sz] = 1;
for (int i = sz - 1; i >= 0; i--) {
                            dp[i] = trie.search_i_start(s, i, dp);
             cout << dp[0] << endl;
5.8 Duval [f9dcca]
```

```
// duval algorithm
// 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
vector<string> duval(string s) {
   int i = 0, n = s.size();
       vector<string> res;
      while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
      else k++;
}</pre>
              while (i <= k) {
    res.push_back(s.substr(i, j - k));
    i += j - k;</pre>
              }
       return res;
// 最小旋轉字串
string min_round(string s) {
      s += s;
int i = 0, n = s.size();
      int start = i;
while (i < n / 2) {</pre>
              start = i;
             start = 1;
int k = i, j = i + 1;
while (s[k] <= s[j] && j < n) {
   if (s[k] < s[j]) k = i;
   else k++;</pre>
                    j++;
              while (i <= k) {
    i += j - k;
```

```
}
return s.substr(start, n / 2);
```

6 Math

}

6.1 Prime [02092d]

```
| vector < int > prime, minp;

void sieve(int n) {

    minp.assign(n + 1, 1); // 1 代表是質數,非 1 不是

    minp[0] = minp[1] = -1;

    int m = int(sqrt(n)) + 1;

    for (int i = 2; i <= m; i++) {

        if (minp[i] == 1) {

            prime.push_back(i);

            for (int j = i + i; j <= n; j += i) {

                 minp[j] = i;

            }

        }

    }

    // a^(m-1) = 1 (mod m)

    // a^(m-2) = 1/a (mod m)

    // EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)

    // FacNums = (x+1)(y+1)(z+1)...

    // FacSum = (a^0+a^1...+a^x)(b^0+...+b^y)

    // FacMul = N(x+1)(y+1)(z+1)/2
```

```
6.2 Modulo [a1aab8]
template < class T>
constexpr T power(T a, ll b) {
  T res {1};
  for (; b; b /= 2, a *= a)
      if (b % 2) res *= a;
      return res;
constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
      res %= p;
if (res < 0) res += p;
      return res;
template < ll P >
struct MInt {
      ll x;
      constexpr MInt() : x {0} {}
constexpr MInt(ll x) : x {norm(x % getMod())} {}
      constexpr wint((( x) : x {norm
static ll Mod;
constexpr static ll getMod() {
   if (P > 0) return P;
   else return Mod;
      constexpr static void setMod(ll Mod_) {
    Mod = Mod_;
      constexpr ll norm(ll x) const {
   if (x < 0) x += getMod();
   if (x >= getMod()) x -= getMod();
            return x:
      constexpr ll val() const { return x; }
constexpr MInt operator-() const {
            MInt res;
            res.x = norm(getMod() - x);
            return res;
      constexpr MInt inv() const {
   return power(*this, getMod() - 2);
      constexpr MInt &operator*=(MInt rhs) & {
            if (getMod() < (1ULL << 31))</pre>
            x = x * rhs.x % int(getMod());
} else {
                 x = mul(x, rhs.x, getMod());
            return *this:
      constexpr MInt &operator+=(MInt rhs) & {
            x = norm(x + rhs.x);
return *this;
      constexpr MInt & operator -= (MInt rhs) & {
    x = norm(x - rhs.x);
            return *this;
      constexpr MInt &operator/=(MInt rhs) & {
    return *this *= rhs.inv();
      friend constexpr MInt operator*(MInt lhs, MInt rhs) {
   MInt res = lhs; return res *= rhs;
      friend constexpr MInt operator+(MInt lhs, MInt rhs) {
   MInt res = lhs; return res += rhs;
      friend constexpr MInt operator-(MInt lhs, MInt rhs) {
            MInt res = lhs; return res -= rhs;
      friend constexpr MInt operator/(MInt lhs, MInt rhs) {
```

```
MInt res = lhs: return res /= rhs:
     friend constexpr
             std::istream &operator>>(std::istream &is, MInt &a) {
           ll v; is >> v; a = MInt(v); return is;
     friend constexpr std::
    ostream &operator<<(std::ostream &os, const MInt &a) {</pre>
           return os << a.val();</pre>
     friend constexpr bool operator==(MInt lhs, MInt rhs) {
   return lhs.val() == rhs.val();
     friend constexpr bool operator!=(MInt lhs, MInt rhs) {
   return lhs.val() != rhs.val();
     friend constexpr bool operator<(MInt lhs, MInt rhs) {
   return lhs.val() < rhs.val();</pre>
template<>
ll MInt<0>::Mod = 998244353;
constexpr int P = 1e9 + 7;
using Z = MInt<P>;
```

6.3 Combination [878efe]

```
struct Comb {
        ll n; vector<Z> _fac, _invfac, _inv;
Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
Comb(ll n) : Comb() { init(n); }
         void init(ll m) {
              m = min(m, Z::getMod() - 1);
if (m <= n) return;
_fac.resize(m + 1);</pre>
               _invfac.resize(m + 1);
               _inv.resize(m + 1);
for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;
               for (int i = _fac[m].inv();
for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
}
         Z fac(ll m) {
               if (m > n) init(2 * m);
               return _fac[m];
        If Invfac(ll m) {
   if (m > n) init(2 * m);
   return _invfac[m];
        Z inv(ll m) {
   if (m > n) init(2 * m);
   return _inv[m];
        }
Z binom(ll n, ll m) {
    if (n < m || m < 0) return 0;
    return fac(n) * invfac(m) * invfac(n - m);
}</pre>
        |} comb; // 注意宣告, 若要換模數需重新宣告
```

6.4 CRT [d41d8c]

```
ll exgcd(ll a, ll b, ll &x, ll &y) {
      if (!b) {
    x = 1, y = 0;
    return a;
      ll g = exgcd(b, a % b, y, x);
      y -= a / b * x;
      return g;
ĺl inv(ll x, ll m){
      ll a, b;
      exgcd(x, m, a, b);
      a %= m;
if (a < 0) a += m;
      return a:
// remain, mod
ll CRT(vector<pair<ll, ll>> &a){
    ll prod = 1;
    for (auto x : a) {
        prod *= x.second;
}
      ll res = 0;
      for (auto x : a) {
    auto t = prod / x.second;
    res += x.first * t % prod * inv(t, x.second) % prod;
            if(res >= prod) res -= prod;
      return res;
}
```

6.5 Matrix [08b5fe]

```
template < class T>
struct Mat {
      int m, n;
constexpr static ll mod = 1e9 + 7;
vector<vector<T>> matrix;
Mat(int n_ = 0) { init(n_, n_); }
Mat(int m_, int n_) { init(m_, n_); }
Mat(vector<vector<T>> matrix_) { init(matrix_); }
void init(int m_, int n_) {
    m = m_; n = n_;
    matrix_assign(m__vector_T__(^>); }

             matrix.assign(m, vector<T>(n));
       void init(vector<vector<T>> &matrix_) {
            m = matrix_.size();
n = matrix_[0].size();
             matrix = matrix_;
       vector<vector<T>> unit(int n) {
             vector<vector<l>> res(n, vector<l>(n));
for (int i = 0; i < n; i++) {
    res[i][i] = 1;</pre>
             return res:
       constexpr Mat &operator*=(const Mat& rhs) & {
             assert(matrix[0].size() == rhs.matrix.size());
int m = matrix.size()
                     , k = matrix[0].size(), n = rhs.matrix[0].size();
            l] * rhs.matrix[l][j] % mod)) %= mod;
                   }
             matrix = ans.matrix;
return *this;
       constexpr Mat &operator^=(ll p) & {
   assert(m == n);   assert(p >= 0);
   Mat ans(p-- == 0 ? unit(m) : matrix);
             while (p > 0) {
   if (p & 1) ans *= *this;
   *this *= *this;
                   p >>= 1;
             matrix = ans.matrix;
             return *this;
       friend Mat operator*(Mat lhs, const Mat &rhs) {
             lhs *= rhs:
             return lhs;
       friend Mat operator^(Mat lhs, const ll p) {
             lhs ^= p;
};
// fn = fn-3 + fn-2 + fn-1
// 初始矩陣 轉移式
// f4 f3 f2 f1 1 0 f5 f4 f3
// f3 f2 f1 1 0 1 => f4 f3 f2
// f2 f1 f0 1 0 0 f3 f2 f1
```

6.6 Integer Partition [595ed2]

```
// CSES_Sum_of_Divisors
// C25_3um_0__DtvtSu/s
const int mod = 1e9 + 7;
const int inv_2 = 500000004;
// n / 1 * 1 + n / 2 * 2 + n / 3 * 3 + ... + n / n * n
int main() {
       ll ans = 0;
      ll n; cin >> n;
for (ll l = 1, r; l <= n; l = r + 1) {
    r = n / (n / l);</pre>
             ll val = n / l; // n / l 到 n / r 一樣的值ll sum = (((l + r) % mod) *
                    ((r - l + 1) % mod)) % mod * inv_2; // l 加到 r
             val %= mod; sum %= mod;
ans += val * sum;
             ans %= mod:
       cout << ans << "\n";
}
```

6.7 Mobius Theorem

- 數論分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^{n} f(i)g(\lfloor \frac{n}{i} \rfloor)$ 的和式。當可以在O(1)內計算f(r) - f(l)或已經預處理
- 出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。 • 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
- 莫比烏斯函數
 - 1. 定義

$$\sum_{d|n} \mu(d) = \begin{cases} 1 & \text{for } n=1\\ 0 & \text{for } n \neq 0 \end{cases}$$

- 2. μ 是常數函數 1 的反元素 $\Rightarrow \mu*1=\epsilon$, $\epsilon(n)$ 只在n=1時為 1,其餘情況皆為 0。
- $-\phi$ 歐拉函數: x 以下與 x 互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^{i}) \\ &= 1 + p^{0}(p-1) + p^{1}(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^{c} \\ &= id \end{split}$$

• 莫比烏斯反演公式

-
$$f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$$

- $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

例子

$$\begin{split} &\sum_{i=a}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \frac{\left\lfloor \frac{y}{k} \right\rfloor}{\left\lfloor \frac{y}{k} \right\rfloor} \\ &= \sum_{d=1}^{\infty} \mu(d) \left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor) \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

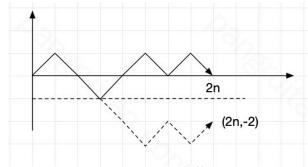
6.8 Mobius Inverse [d41d8c]

const int maxn = 2e5;

```
ll mobius_pref[maxn];
void init() {
      mobius_pref[1] = 1;
      vector<ll> wei
      (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
}
                  continue; // 包含平方
            if (wei[i] == 0) {
                  wet[i] == 0) {
wei[i] = 1;
for (ll j = 2; i * j < maxn; j++) {
    if (j % i == 0) wei[i * j] = -1;
    else if (wei[i * j] != -1) wei[i * j]++;</pre>
                  }
            mobius pref[i]
                   = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
     }
void solve() {
      ll a, b, c, d, k; cin >> a >> b >> c >> d >> k;

auto cal = [&](ll x, ll y) -> int {
            cout << cal
             (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k, (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n"
}
```

6.9 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有x 個,往下有y 個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.10 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- · X/G:本質不同的方案的集合
- X^g : 對於某一種操作 g,所有方案中,經過 g 這種翻轉後保持不變的方案的集合
- 集合取絕對值代表集合數

7 Search and Gready

7.1 Binary Search [d41d8c]

```
int main() {
    int l = 1, r = 10;
    // 1 to tar, find tar
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}</pre>
```

7.2 Ternary Search [d41d8c]

8 Тгее

8.1 LCA [601e2d]

```
}
}
int lca(int a, int b) {
    if (depth[a] < depth[b]) swap(a, b);
    int pull = depth[a] - depth[b];
    for (int i = 0; i < 18; i++) {
        if (pull & (1 << i)) {
            a = par[a][i];
        }
}
if (a == b) return a;
for (int i = 17; i >= 0; i--) {
        if (par[a][i] != par[b][i]) {
            a = par[a][i], b = par[b][i];
        }
}
return par[a][0];
}
```

8.2 Centroid Decomposition [ec760b]

```
#include <bits/stdc++.h>
using namespace std;
struct CenDecom {
      int n;
vector<vector<int>> adj;
       vector < bool > vis;
       vector <int> siz;
CenDecom(int n_ = 0) { init(n_); }
void init(int n_) {
             n = n_;
adj.assign(n, {});
vis.assign(n, false);
siz.assign(n, 1);
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void get_siz(int x, int p = -1) {
              siz[x] += siz[y];
       int get_cen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz) {
                            return get_cen(y, sz, x);
              return x;
       void get_ans(int x, int p) {
              fyct_discipled x, the p, \
// do something
for (int y : adj[x]) {
    if (y == p || vis[y]) continue;
    get_ans(y, x);
}
       void work(int x = 0) {
              get_siz(0, x);
int cen = get_cen(x, siz[x]);
              vis[cen] = true;
for (int y : adj[cen]) {
    if (vis[y]) continue;
                     get_ans(y, cen);
              for (int y : adj[cen]) {
   if (vis[y]) continue;
                     work(y);
      }
};
```

8.3 Tree Flattening [5293b7]

```
|// 父節
| 點加值 = 所有子節點區間加值,求單點,使用 bit,做前級差分

// CSES 1138_Path Queries
int main(){
    int n, q; cin >> n >> q;
    vector<int> val(n + 1), dfnToVal(n);
    for (int i = 1; i <= n; i++) {
        cin >> val[i];
    }
    vector<vector<int>> tree(n + 1);
    for (int i = 1; i < n; i++) {
        int u, v; cin >> u >> v;
        tree[u].push_back(v);
        tree[v].push_back(u);
    }

    vector<pair<int, int>> mp(n + 1); // dfn 區間
    int cnt = 0;
    auto dfs = [&](auto self, int u, int par) -> void {
        dfnToVal[++cnt] = val[u];
        mp[u].first = cnt;
        for (auto v : tree[u]) {
```

```
if (v == par) continue;
    self(self, v, u);
}
mp[u].second = cnt;
};
dfs(dfs, 1, 0);
BIT bit(n);
for (int i = 1; i <= n; i++) {
    bit.modify(mp[i].first, val[i]);
    if (mp[i].first < n) { // root 就不用扣了
        bit.modify(mp[i].second + 1, -val[i]);
}

for (int i = 0; i < q; i++) {
    int op; cin >> op;
    if (op == 1) {
        int s, x; cin >> s >> x;
        int add = x - dfnToVal[mp[s].first];
        dfnToVal[mp[s].first] = x;
        bit.modify(mp[s].first, add);
        if (mp[s].first < n) { // root 就不用扣了
            bit.modify(mp[s].second + 1, -add);
        }
}
else {
    int node; cin >> node;
    cout << bit.query(mp[node].first) << "\n";
}
}
```

8.4 Heavy Light Decomposition [bfd902]

```
struct HLD {
       int n, cur;
vector < int > siz, top, dep, parent, in, out, seq;
       vector < int >> adj;
       vector < tht> adj;
HLD(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
    n = n_; cur = 0;
    siz.resize(n); top.resize(n); dep.resize(n);
    parent.resize(n); in.resize(n); out.resize(n);
    seq.resize(n); adj.assign(n, {});
}
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void work(int rt = 0) {
              top[rt] = rt;
dep[rt] = 0;
              parent[rt] =
              dfs1(rt); dfs2(rt);
       void dfs1(int u) {
              if (parent[u] != -1)
                      adj[u].erase(find
                              (adj[u].begin(), adj[u].end(), parent[u]));
              for (auto &v : adj[u]) {
                     parent[v] = u, dep[v] = dep[u] + 1;
                     dfs1(v);
siz[u] += siz[v];
if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
                     } // 讓 adj[u][0] 是重子節點
             }
       void dfs2(int u) {
              in[u] = cur++;
              seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
   top[v] = v == adj[u][0] ? top[u] : v;
              out[u] = cur;
       int lca(int u, int v) {
    while (top[u] != top[v]) {
        if (dep[top[u]] > dep[top[v]]) {
            u = parent[top[u]];
        } else {
                            v = parent[top[v]];
              return dep[u] < dep[v] ? u : v;</pre>
       int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
       int jump(int u, int k) {
   if (dep[u] < k) return -1;
   int d = dep[u] - k;
   while (dep[top[u]] > d)
              u = parent[top[u]];
return seq[in[u] - dep[u] + d];
       bool isAncester(int u, int v) {
    return in[u] <= in[v] && in[v] < out[u];</pre>
```

int rootedParent(int rt, int v) {

```
8.5 Link Cut Tree [29ae0d]
#include <bits/stdc++.h>
using ll = long long;
constexpr int Mod = 51061;
struct Tag {
    ll add = 0;
     ll mul = 1;
     void apply(const Tag& v) {
    mul = mul * v.mul % Mod;
    add = (add * v.mul % Mod + v.add) % Mod;
};
struct Info {
     ll val = 1;
ll sum = 1;
     void apply(int size, const Tag &v) {
   val = (val * v.mul % Mod + v.add) % Mod;
   sum = (sum * v.mul % Mod + v.add * size % Mod) % Mod;
};
struct Node {
     Node *ch[2], *p;
     int rev = 0;
     int size = 1;
void make_rev() {
           swap(ch[0], ch[1]);
     Node() : ch {nullptr, nullptr}, p(nullptr) {}
     Info info = Info();
Tag tag = Tag();
     void apply(const Tag &v) {
   info.apply(size, v);
           tag.apply(v);
     void push_tag() {
          if (rev) {
   if (ch[0]) ch[0]->make_rev();
   if (ch[1]) ch[1]->make_rev();
           if (ch[0]) {
                ch[0]->apply(tag);
           if (ch[1]) {
    ch[1]->apply(tag);
           tag = Tag();
     void pull_info() {
          }
bool isroot(Node *t) {
             == nullptr \mid | (t->p->ch[0] != t && t->p->ch[1] != t);
int pos(Node *t) { // 回傳 1 代表是右子節點 return t->p->ch[1] == t;
void rotate(Node *t) {
     Node *q = t->p;

int x = !pos(t);

q->ch[!x] = t->ch[x];
     if (t->ch[x]) {
           t - ch[x] - p = q;
     t->p = q->p;
if (!isroot(q)) {
           q->p->ch[pos(q)] = t;
     t - ch[x] = q;
```

```
a -> p = t:
     q->pull_info();
}
void splay(Node *t) { // 單點修改前必須呼叫
     // 把 t 旋轉到目前 splay 的根while (!isroot(t)) {
          Node *p = t->p;
p->push_tag();
t->push_tag();
           rotate(t);
     t->push_tag();
t->pull_info();
void access(Node *t) {
     // 把從根到 t 的所有點都放在一條實鏈裡,使根
     // 到 t 成為一條實路徑,並且在同一棵 splay 裡 for (Node *i = t, *q = nullptr; i; q = i, i = i->p) {    splay(i);
           i->ch[1] = q;
     splay(t);
void makeRoot(Node *t) { // 使 t 點成為其所在樹的根
     access(t);
     swap(t->ch[0], t->ch[1]);
t->rev ^= 1;
Node* findRoot(Node *t) { // 找到 t 的 root
     splay(t);
     t->push tag();
     while (\bar{t} - > ch[0]) {
           t = t - sch[0]
           t->push_tag();
     splay(t);
     return t;
void link(Node *t, Node *p) {
     makeRoot(t);
if (findRoot(p) != t) {
           makeRoot(p);
          t->p = p;
p->pull_info();
}
bool cut(Node *x, Node *y) { // 不存在邊,回傳 false
     makeRoot(x);
     access(y);
if (y->ch[0] != x || x->ch[1]) return false;
     y->ch[0]->p = nullptr;
     y->ch[0] = nullptr;
y->pull_info();
      return true;
void split(Node
     *x, Node *y) { // 以 y 做根, 區間修改用, apply 在 y 上 makeRoot(x);
     access(y);
     splay(y);
}
bool isconnected(Node *x, Node *y) { // 查詢有沒有連通
     makeRoot(x);
     access(v);
     return findRoot(x) == findRoot(y);
}
int main() {
    int n; cin >> n;
    vector <Node *> nodes(n);
     vector < Node ^> nodes(n);
int q; cin >> q;
for (int i = 0; i < n; i++) {
    nodes[i] = new Node();
    nodes[i] -> info.val = nodes[i] -> info.sum = 1LL;
     for (int i = 0; i < n - 1; i++) {
  int u, v; cin >> u >> v;
  u--; v--;
           link(nodes[u], nodes[v]);
      for (int i = 0; i < q; i++) {
           char op; cin >> op;
if (op == '+') {
                 int u, v; cin >> u >> v;
                u--; v--;
split(nodes[u], nodes[v]);
                 Tag tag;
                cin >> tag.add;
tag.add % Mod;
nodes[v]->apply(tag);
           else if (op == '-') {
                int u1, v1; cin >> u1 >> v1;
int u2, v2; cin >> u2 >> v2;
u1--; v1--; u2--; v2--;
cut(nodes[u1], nodes[v1]);
link(nodes[u2], nodes[v2]);
           else if (op == '*') {
```

```
National Chung Cheng University Salmon
                 int u, v; cin >> u >> v;
u--: v--:
                 split(nodes[u], nodes[v]);
                 Tag tag;
cin >> tag.mul;
                 tag.mul % Mod;
                 nodes[v]->apply(tag);
                 int u, v; cin >> u >> v;
                 split(nodes[u], nodes[v]);
                 cout << nodes[v]->info.sum << "\n";</pre>
            }
      return 0;
 }
 8.6 Virtual Tree [622e69]
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
// 可以建立虚樹達成快速樹 DP
 ...
// 例如這題是有權樹,跟 vertex 1 隔開的最小成本
 int top = -1; vector < int > stk(maxn);
 int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
   if (top == -1) return stk[++top] = u, void();
   int l = lca(stk[top], u);
   if (l == stk[top]) return stk[++top] = u, void();
   while (dfn[l] < dfn[stk[top - 1]])</pre>
      vt[stk[top - 1]].push_back(stk[top]), top--;
if (stk[top - 1] != l) {
            vt[l].push_back(stk[top]);
```

stk[top] = l; } else vt[l].push_back(stk[top--]); stk[++top] = u;

void reset(int u, vector<vector<int>> &vt) { for (int i : vt[u]) reset(i, vt); vt[u].clear(); void solve(int n, int q) { vector g(n + 1, vector<pair<int, int>>()); vector vt(n + 1, vector vector vt(n + 1, vector <int>()); // dfs 完清除, 否則會退化 vector <ll> dp(n + 1), iskey(n + 1); for (int i = 0; i < n - 1; i++) { int u, v, w; cin >> u >> v >> w; g[u].push_back({v, w}); $g[v].push_back({u, w});$ build_lca(n, g); for (int j = 0; j < m; j++) { cin >> key[j]; iskey[key[j]] = 1; key.push_back(1); // 看題目,需要才放 sort(all(key), [%](int a, int b) { return dfn[a] < dfn[b]; for (int x : key) insert(x, vt); while (top > 0) vt[stk[top - 1]].push_back(stk[top]), --top; // DP auto dfs = [&](auto self, int u) -> void { for (auto v : vt[u]) { self(self, v); if (iskey[v]) { dp[u] += min_dis[v]; // 砍掉 1 到 v 之間最短的路 dp[u] += min(dp[v], min_dis[v]); iskey[v] = dp[v] = 0;vt[u].clear();

8.7 Dominator Tree [baa540]

}

```
struct Dominator_tree {
    int n, id;
    vector<vector<int>> adj, radj, bucket;
    vector<int>> sdom, dom, vis, rev, pa, rt, mn, res;
    Dominator_tree(int n_ = 0) { init(n_); }
    void init(int _n) {
        n = _n, id = 0;
        adj.assign(n, vector<int>());
        radj.assign(n, vector<int>());
        bucket.assign(n, vector<int>());
        sdom.resize(n); dom.assign(n, -1);
        vis.assign(n, -1); rev.resize(n);
```

dfs(dfs, key[θ]); // key[θ] 一定是 root cout << dp[key[θ]] << "\n"; iskey[key[θ]] = dp[key[θ]] = θ ;

```
pa.resize(n); rt.resize(n);
mn.resize(n); res.resize(n);
        void add_edge(int u, int v) { adj[u].push_back(v); }
int query(int v, int x) {
   if (rt[v] == v) return x ? -1 : v;
              int p = query(rt[v], 1);
if (p == -1) return x ? rt[v] : mn[v];
if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
              rt[v] = p;
return x ? p : mn[v];
        void dfs(int v) {
    vis[v] = id, rev[id] = v;
    rt[id] = mn[id] = sdom[id] = id, id++;
               for (int u : adj[v]) {
   if (vis[u] == -1) dfs(u), pa[vis[u]] = vis[v];
   radj[vis[u]].push_back(vis[v]);
        void build(int s) {
               dfs(s);
              for (int i = id - 1; i >= 0; i--) {
    for (int u : radj[i])
        sdom[i] = min(sdom[i], sdom[query(u, 0)]);
                      if (i) bucket[sdom[i]].push_back(i);
                      for (int u : bucket[i]) {
   int p = query(u, 0);
   dom[u] = sdom[p] == i ? i : p;
                      if (i) rt[i] = pa[i];
              res.assign(n, -1);
for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];</pre>
               for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre>
              res[s] = s;
for (int i = 0; i < n; i++) dom[i] = res[i];
       }
};
```

9 DP

9.1 LCS [5781cf]

```
int main() {
   int m, n; cin >> m >> n;
   string s1, s2; cin >> s1 >> s2;
   int L = 0;
   vector <vector <int>>> dp(m + 1, vector <int>(n + 1, 0));
   for (int i = 1; i <= m; i++) {
      for (int j = 1; j <= n; j++) {
        if (s1[i - 1] == s2[j - 1])
            dp[i][j] = dp[i - 1][j - 1] + 1;
      else
            dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
   }
}
int length = dp[m][n]; cout << length << "\n";
string s(length, 'c'); // backtracking
while (m >= 1 && n >= 1) {
      if (s1[m - 1] == s2[n - 1]) {
        s[length - 1] = s1[m - 1];
        m--, n--, length--;
   }
else {
      if (dp[m - 1][n] > dp[m][n - 1]) m--;
        else n--;
   }
}
cout << s << "\n";
}</pre>
```

9.2 LIS [66d09f]

9.3 Edit Distance [308023]

9.4 Bitmask [a626f9]

```
void hamiltonianPath(){
   int n, m; cin >> n >> m;
vector adj(n, vector<int>());
   for (int i = 0; i < m; i++) {
   int u, v; cin >> u >> v;
   adj[--v].push_back(--u);
   ·// 以...為終點,走過...
   vector dp(n, vector<int>(findBit(n)));
   if ((pre_mask & findBit(j)) == 0) continue;
              dp[i][mask
                   ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
          }
       }
   cout << dp[n - 1][findBit(n) - 1] << "\n";
void elevatorRides() {
   int n, x; cin >> n >> x; vector <int > a(n);
for (int i = 0; i < n; i++) cin >> a[i];
   }
   cout << dp[findBit(n) - 1][0] << "\n";
}
```

9.5 Projects [0942aa]

```
int main() { // 排程有權重問題,輸出價值最多且時間最少
struct E {
    int from, to, w, id;
    bool operator <(const E &rhs) {
        return to == rhs.to ? w > rhs.w : to < rhs.to;
};
int n; cin >> n; vector <E> a(n + 1);
for (int i = 1; i <= n; i++) {
        int u, v, w; cin >> u >> v >> w;
        a[i] = {u, v, w, i};
}
vector <array < ll, 2>> dp(n + 1); // w, time
vector <array < ll, 2>> dp(n + 1); // 有沒選, 上個是誰
sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
        auto it = --lower_bound(all(a), E({0, a[i].from}),
        [](E x, E y){ return x.to < y.to; });
        int id = it - a.begin(); dp[i] = dp[i - 1];
        ll nw = dp[id][0] + a[i].w;</pre>
```

```
ll nt = dp[id][1] + a[i].to - a[i].from;
    if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
        dp[i] = {nw, nt}; rec[i] = {1, id};
    }
}
vector < int > ans;
for (int i = n; i != 0;) {
    if (rec[i][0]) {
        ans.push_back(a[i].id);
        i = rec[i][1];
    } else i--;
}
```

9.6 Removal Game [7bb56b]

9.7 Monotonic Queue [f4976d]

9.8 SOS [93cb19]

```
| // 使用情況: 跟 bit 與(被)包含有關,且 x 在 1e6 左右
| // 題目: 一數組,問有多少所有數 & 起來為 0 的集合數
| // dp[x]代表包含 x 的 y 個數(比x大且bit 1全包含 x 的有幾個)
| // 答案應該包含在 dp[0]内,但是有重複元素,所以考慮容斥
| // => ans = |sum _{i=0}^{n} (-1)^{pop_count(i)} 2^{dp[i]-1}
| // => 全部為0的個數 - 至少一個為1的個數 + 至少兩個為1的個數 void solve() {
    int n; cin >> n; Z ans = 0;
    vector<int> a(n);
    for (int i = 0; i < n; i++)
        cin >> a[i];
    int m = __lg(*max_element(a.begin(), a.end())) + 1;
    // 定義 dp[mask] 為 mask 被包含於 a[i] 的 a[i] 個數 vector<Z> dp(1 << m);
    for (int i = 0; i < n; i++)
        dp[a[i]] += 1;
    for (int i = 0; i < m; i++)
        if (mask >> i & 1) {
            int pre = mask ^ (1 << i);
            dp[pre] += dp[mask];
        }
    for (int mask = 0; mask < 1 << m; mask++) {
        int sgn = __builtin_popcount(mask) & 1 ? -1 : 1;
        ans += sgn * (power(Z(2), dp[mask].val()) - 1);
    }
    cout << ans << "\n";
```

9.9 CHT [5f5c25]

```
// 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \le r(i)
// A(j), B(j) 可能包含 dp(j), 分別就是 m 跟 b
struct Line {
    ll m, b;
ll m, b;
Line(ll m = 0, ll b = 0) : m(m), b(b) {}
ll eval(ll x) {
    return m * x + b;
};
struct CHT { // 用在查詢單調斜率也單調
  int n, lptr, rptr; vector<Line> hull;
  CHT(int n_ = 0, Line init_ = Line()) {
     init(n_, init_);
}
     void init(int n_ = 0, Line init_ = Line()) {
    n = n_; hull.resize(n); reset(init_);
     void reset(Line init_ = Line()) {
    lptr = rptr = 0; hull[0] = init_;
     bool pop_front(Line &l1, Line &l2, ll x) {
         // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y
          // 代表查詢的當下,右線段的高度已經低於左線段了
          return l1.eval(x) >= l2.eval(x);
    bool pop_back(Line &l1, Line &l2, Line &l3) {
         // 本題斜率遞減、上凸包
          // 因此只要 12 跟
         l3 的 X 交點 <= l1 跟 l3 的 X 交點, l2 就用不到了
return (l3.b - l2.b)
* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
    void insert(Line L) {
          while (rptr - lptr
                > 0 && pop_back(hull[rptr - 1], hull[rptr], L))
          hull[++rptr] = L;
    };
```

9.10 DNC [61c639]

```
| // 應用: 切 k 段問題, 且滿足四邊形不等式
| // w(a,c) + w(b,d) ≤(≥) w(a,d) + w(b,c)
| // dp[k][j] = min(dp[k - 1][i] + cost[i][j])
| // cost: (i, j]
| constexpr int N = 3e3 + 5;
| constexpr ll inf = 4e18;
| ll dp[N][N]; // 1-based
| ll get_cost(int l, int r) {}
| void DNC(int k, int l, int r, int optl, int optr) {
| if (l > r) return;
| int m = (l + r) >> 1, opt = -1;
| dp[k][m] = inf;
| for (int i = max(k, optl); i <= min(m, optr); i++) {
| // 注意 i 的範園 yet_cost 與 dp 的邊界
| ll cur = dp[k - 1][i] + get_cost(i, m);
| if (cur < dp[k][m]) {
| dp[k][m] = cur, opt = i;
| }
| DNC(k, l, m - 1, optl, opt);
| DNC(k, m + 1, r, opt, optr);
| }
| int main() {
| // first build cost...
| for (int i = 1; i <= n; i++) {
| // init dp[1][i] }
| for (int i = 2; i <= k; i++) {
| DNC(i, 1, n, 1, n);
| }
| cout << dp[k][n] << "\n";
| }
```

9.11 LiChaoSegmentTree [846572]

```
}

void update(Line line, int node, int l, int r) {
    int m = (l + r) / 2;
    bool left = line.eval(l) < info[node].eval(l);
    bool mid = line.eval(m) < info[node].eval(m);
    if (mid) swap(info[node], line); // 如果新線段比較好
    if (r - l == 1) return;
    else if (left != mid) update(line, 2 * node, l, m);
    // 代表左半有交點
    else update(line, 2 * node + 1, m, r);
    // 代表如果有交點一定在右半
}

void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
    if (r - l == 1) return info[node].eval(x);
    int m = (l + r) / 2;
    if (x < m) return
        min(info[node].eval(x), query(x, 2 * node, l, m));
    else return min(
        info[node].eval(x), query(x, 2 * node + 1, m, r));
}
ll query(int x) { return query(x, 1, 0, n); }
}
</pre>
```

9.12 Codeforces Example [7d37ea]

```
// CF 1932 pF
// 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
// 請問在線段不重複的情況下,最多獲得幾分 int main() {
      int n, m;
cin >> n >> m;
      // 記錄每點有幾個線段
      // 再一個紀錄,包含這個點的左界
      cnt[l]++;
          cnt[r + 1]--;
      for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
      for (int i = n; i >= 2; i--) {
           l_side[i - 1] = min(l_side[i - 1], l_side[i]);
      vector<int> dp(n + 1):
      dp[0] = 0;
      for (int i = 1; i <= n; i++) {
   dp[i] = cnt[i];
   if (l_side[i] != inf) {</pre>
               dp[i] += dp[l_side[i] - 1];
          dp[i] = max(dp[i], dp[i - 1]);
      cout << dp[n] << "\n";
}
// CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
 // 再加上 max(bi) - min(bi)
int main(){
  int n, k, ans = 0; cin >> n >> k;
  vector<pii> v(n + 1);
  for (int i = 1; i <= n; i++) {
    int a, b; cin >> a >> b;
    v[i] = {a, b};
    if (a <= k) ans = 1;
}</pre>
     sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
      }); // 用 bi 來排,考慮第 i 個時可以先扣
      vector<vector<int>> dp(n + 1, vector<int>(n + 1, inf));
      // 考慮 v[i] 時, 選 j 個的 sum(ai) - min(bi)
     for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
                  min(不選,選)
               if (dp[i
                     -1][j - 1] + v[i].first + v[i].second <= k) {
                    // 假如可以選, 更新 ans 時再加回去 bi
                    ans = max(ans, j);
          dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
      cout << ans << endl;
```

10 Geometry

10.1 Basic [d41d8c]

```
template < class T>
struct Point {
    T x, y;
    Point(const T &x_ = 0, const T &y_ = 0) : x(x_), y(y_) {}
```

```
template < class U>
     operator Point<U>()
          return Point<U>(U(x), U(y));
     Point &operator+=(const Point &p) & {
          x += p.x; y += p.y; return *this;
     Point & operator -= (const Point &p) & {
          x -= p.x; y -= p.y; return *this;
     Point &operator*=(const T &v) & {
          x *= v; y *= v; return *this;
     Point & operator /= (const T & v) & {
          x /= v; y /= v; return *this;
     Point operator - () const {
          return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
          return a += b:
     friend Point operator - (Point a, const Point &b) {
          return a -= b:
     friend Point operator*(Point a, const T &b) {
          return a *= b:
     friend Point operator/(Point a, const T &b) {
          return a /= b;
     friend Point operator*(const T &a, Point b) {
          return b *= a;
     friend bool operator==(const Point &a, const Point &b) {
          return a.x == b.x && a.y == b.y;
     friend istream &operator>>(istream &is, Point &p) {
          return is >> p.x >> p.y;
     friend ostream &operator<<(ostream &os, const Point &p) {</pre>
          return os << "(" << p.x << ", " << p.y << ")";
template < class T>
struct Line {
     Point <T> a;
     Point<T> b;
     Line(const Point<T> &a_ = Point<T>()
          , const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
template < class T>
T dot(const Point<T> &a, const Point<T> &b) {
    return a.x * b.x + a.y * b.y;
template < class T >
T cross(const Point < T > & a, const Point < T > & b) {
    return a.x * b.y - a.y * b.x;
template < class T >
T square(const Point < T > &p) {
     return dot(p, p);
template < class T>
double length(const Point<T> &p)
    return sqrt(double(square(p)));
double length(const Line<T> &l) {
     return length(l.a - l.b);
template < class T>
Point < T> normalize(const Point < T> &p) {
    return p / length(p);
template < class T>
bool parallel(const Line<T> &l1, const Line<T> &l2) {
   return cross(l1.b - l1.a, l2.b - l2.a) == 0;
template < class T>
double distance(const Point<T> &a, const Point<T> &b) {
    return length(a - b);
template < class T>
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)
      return distance(p, l.a);
   if (dot(p - l.b, l.a - l.b) < 0)
      return distance(p, l.b);
   return distance(p, l);
}</pre>
template < class T>
Point<T> rotate(const Point<T> &a) {
     return Point(-a.y, a.x);
template < class T>
int sgn(const Point<T> &a) {
     return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
```

```
template < class T>
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
      return cross(l.b - l.a. p - l.a) > 0:
template < class T>
Point < T
        > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
       return ll.a + (ll.b - ll.a) * (cross(l2.b - l2.a, l1.a - l2.a) / cross(l2.b - l2.a, l1.a - l1.b));
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
    return cross(p - l.a, l.b - l.a) == 0 &&
        min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)
                     (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
        (const Point<T> &a, const vector<Point<T>> &p) {
       int n = p.size(), t = 0;
for (int i = 0; i < n; i++) {
    if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {</pre>
       for (int i = 0; i < n; i++) {
    auto u = p[i];</pre>
              auto v = p[(i + 1) % n];
             if (u.x < a.
                     x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
                    t ^= 1;
             if (u.x >= a
                     .x && v.x < a.x && pointOnLineLeft(a, Line(u, v)))</pre>
                    t ^= 1;
       return t == 1;
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
tuple < int , Point < T > , Point < T > > segmentIntersection
      le<int, Point<T>, Point<T>> segmentIntersecti
(const Line<T> &l1, const Line<T> &l2) {
    if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.)
        return {0, Point<T>(), Point<T>());
    if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.)
        return {0, Point<T>(), Point<T>());
    if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.)
        return {0, Point<T>(), Point<T>());
    if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.)
        return {0, Point<T>(), Point<T>());
    if (cons(l1.b. - l1.a, l2.b. - l2.a) == 0) {
        if (cross(l1.b. - l1.a, l2.a. - l1.a) != 0)
                                                                      12.b.x))
                                                                       ĺ2.b.x))
                                                                       .
(2.b.y))
             if (cross(l1.b - l1.a, l2.a - l1.a) !=
    return {0, Point<T>(), Point<T>()};
                                                                               0) {
             } else {
                    auto maxx1 = max(l1.a.x, l1.b.x);
auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
                    auto miny1 = min(l1.a.y, l1.b.y);
auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
                    auto maxy2 = max(l2.a.y, l2.b.y);
auto miny2 = min(l2.a.y, l2.b.y);
                    Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
                    if (!pointOnSegment(p1, l1))
                    swap(p1.y, p2.y);
if (p1 == p2) {
                           return {3, p1, p2};
                    } else {
                           return {2, p1, p2};
             }
       auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
       auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
      return {1, p, p};
      } else {
             return {3, p, p};
template < class T:
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
   if (get<0>(segmentIntersection(l1, l2)) != 0)
       template < class Ta
bool segmentInPolygon
        (const Line<T> &l, const vector<Point<T>> &p) {
       int n = p.size();
```

int n; cin >> n;

vector <P> P(n), U, L;

```
if (!pointInPolygon(l.a, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
for (int i = 0; i < n; i++) {
    auto u = p[i];</pre>
                                                                                                         for (int i = 0: i < n: i++) {</pre>
                                                                                                               cin >> P[i];
                                                                                                         sort(P.begin(), P
            auto v = p[(i + 1) \% n];
                                                                                                                 .end(), [](const Point<i64> &a, const Point<i64> &b) {
            auto v = PL(t + 1) % n];
auto w = p[(i + 2) % n];
auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
if (t == 1) return false;
if (t == 0) continue;
                                                                                                               return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
                                                                                                         for (int i = 0; i < n; i++) {
    while (L.size() >= 2 && cross(L.back() -
        L[L.size() - 2], P[i] - L[L.size() - 2]) <= 0LL) {</pre>
            if (t == 2) {
                  if (pointOnSegment(v, l) && v != l.a && v != l.b)
    if (cross(v - u, w - v) > 0)
        return false;
                                                                                                                     L.pop_back();
                                                                                                               while (U.size() >= 2 && cross(U.back() -
    U[U.size() - 2], P[i] - U[U.size() - 2]) >= 0LL){
           U.pop_back();
                                                                                                               if (L.
                              || pointOnLineLeft(l.b, Line(v, u)))
                                                                                                                      empty() || !(L.back() == P[i])) L.push_back(P[i]);
                              return false;
                 } else if (p1 == v) {
    if (l.a == v) {
        if (pointOnLineLeft(u, l)) {
            if (pointOnLineLeft(w, l)) }
}
                                                                                                               if (U.
                                                                                                                      empty() || !(U.back() == P[i])) U.push_back(P[i]);
                                                                                                          if (L.size() <= 2 && U.size() <= 2) {
                                          && pointOnLineLeft(w, Line(u, v)))
                                                                                                               // No Hull
                                          return false:
                                                                                                         cout << L.size() + U.size() - 2 << "\n";
                                    for (int i = 0; i < L.size() - 1; i++) {
  cout << L[i].x << " " << L[i].y << " | n";</pre>
                                                                                                         for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << " | n";</pre>
                        && pointOnLineLeft(w, Line(u, v)))
                                                                                                   10.3
                                                                                                               MinEuclidean Distance [3020bc]
                                          return false:
                                    if (pointOnLineLeft(w, Line(l.b, l.a))
    || pointOnLineLeft(w, Line(u, v)))
    return false;
                                                                                                   template < class T>
                                                                                                   T distanceSquare(const Point<T> &a, const Point<T> &b) {
    return square(a - b);
                       void solve() {
                                                                                                         int n; cin >> n;
constexpr ll inf = 8e18;
                                                                                                         vector < Point < ll >> a(n);
for (int i = 0; i < n; i++) {
    ll x, y;</pre>
                                    if (pointOnLineLeft(w, l)
    || pointOnLineLeft(w, Line(u, v)))
    return false;
                                                                                                               a[i] = Point < ll>(x, y);
                             }
                                                                                                          struct sortY {
                       }
                                                                                                               bool operator
                 }
                                                                                                                      ()(const Point<ll> &a, const Point<ll> &b) const {
           }
                                                                                                                     return a.y < b.y;</pre>
                                                                                                              }
      return true:
                                                                                                         }:
                                                                                                          struct sortXY {
remplate < class T>
vector < Point < T>> hp(vector < Line < T>> lines) {
                                                                                                               bool operator
                                                                                                                     ()(const Point<ll> &a, const Point<ll> &b) const {
if (a.x == b.x) return a.y < b.y;</pre>
     sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
   auto d1 = l1.b - l1.a;
   auto d2 = l2.b - l2.a;
                                                                                                                     else return a.x < b.x;</pre>
                                                                                                              }
            if (sgn(d1) != sgn(d2))
                  return sgn(d1) == 1;
                                                                                                         sort(a.begin(), a.end(), sortXY());
                                                                                                         solt(a.begin(), a.enu(), soltx*());
vector<Point<ll>> t(n);
auto devide = [&](auto &&self, int l, int r) -> ll {
    if (l == r) return inf;
    int m = (l + r) / 2;
    ll ans = min(self(self, l, m), self(self, m + 1, r));
    ll midval = a[m].x;
}
            return cross(d1, d2) > 0;
      }):
      deque<Line<T>> ls;
      deque<Point<T>> ps;
for (auto l : lines) {
    if (ls.empty()) {
                                                                                                               ll p = 0;
for (int i = l; i <= r; i++) {
    if ((midval - a[i].x) * (midval - a[i].x) <= ans) {</pre>
                  ls.push_back(l);
                  continue:
            while (!ps.empty() && !pointOnLineLeft(ps.back(), l))
                                                                                                                           t[p++] = a[i];
            \begin{array}{lll} & ps.pop\_back(), & ls.pop\_back(); \\ & \textbf{while} & (!ps.empty() & \& \; !pointOnLineLeft(ps[\theta], \; l)) \end{array}
            ps.pop_front(), ls.pop_front();
if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
                                                                                                               sort(t.begin(), t.begin() + p, sortY());
                                                                                                               for (int i = 0; i < p; i++){
   for (int j = i + 1; j < p; j++) {
      ans = min(ans, distanceSquare(t[i], t[j]));</pre>
                  if (dot
                         (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                           (!pointOnLineLeft(ls.back().a, l)) {
                                                                                                                                    t[j].y) * (t[i].y - t[j].y) > ans) break;
                              assert(ls.size() == 1);
                                                                                                                     }
                        continue:
                                                                                                               return ans;
                                                                                                         cout << devide(devide, 0, n - 1) << "\n";</pre>
            ps.push_back(lineIntersection(ls.back(), l));
            ls.push_back(l);
                                                                                                   10.4 LatticePoints [00db9d]
     while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0]))
    ps.pop_back(), ls.pop_back();
if (ls.size() <= 2) return {};
ps.push_back(lineIntersection(ls[0], ls.back()));
return vector(ps.begin(), ps.end());</pre>
                                                                                                 int main() {
                                                                                                          // Polygun 內整數點數
                                                                                                         int n; cin >> n;
vector <Point <ll>> polygon(n);
for (int i = 0; i < n; i++) cin >> polygon[i];
                                                                                                         for (int i = 0; i < n; i++) {
    area += cross(polygon[i], polygon[(i + 1) % n]);</pre>
using P = Point<ll>:
10.2 Convex Hull [b5758d]
                                                                                                         area = abs(area);
                                                                                                         auto countBoundaryPoints
int main() {
```

= [](const vector<Point<ll>>& polygon) -> ll {

ll res = 0;

10.5 MinCoverCircle [c9ca81]