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Basic

1.1 Default Code [d41d8c]

```
#include <hits/stdc++.h>
using namespace std;
using ll = long long;
void solve() {
}
int main() {
    ios_base::sync_with_stdio(false);
cin.tie(nullptr);
    int t = 1;
    cin >> t;
while (t--) {
         solve();
    return 0:
```

1.2 Compare Fuction [d41d8c]

```
|// 1. sort, 二分搜刻在函式內 lambda 就好
 // 2. priority queue 小到大是 >, set 是 <
 // 3. set 不能 = , multiset 必須 =
 // 4. 確保每個成員都要比到
 // 5. pbds_multiset 不要用 lower_bound
 // 6. 如果要用 find, 插入 inf 後使用 upper_bound
// 7. multiset 可以跟 set 一樣使用, 但請注意第 3、4 點
 auto cmp = [](int i, int j) { return i > j; };
priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
 vector<int> a {1, 2, 5, 4, 3}; // 小心不要改到 a auto cmp = [&a](int i, int j) { return a[i] > a[j]; }; priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
```

1.3 Pbds [d41d8c]

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < class T>
```

```
using pbds_set = tree<T, null_type,</pre>
less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template < class T>
using pbds_multiset = tree<T, null_type, less_equal
    <T>, rb_tree_tag, tree_order_statistics_node_update>;
```

1.4 Double [f7a49d]

```
struct D {
     double x;
     constexpr static double eps = 1E-12;
     constexpr static double eps = 1t-12;
D(): x{0.0} {}
D(double v): x{v} {}
double val() const { return x; }
explicit operator double() const { return x; }
D operator-() const {
   return D(-x);
     D & operator += (const D & rhs) & {
           x += rhs.x; return *this;
     D &operator -= (const D &rhs) & {
           x -= rhs.x; return *this;
     D & operator *= (const D & rhs) & {
           x *= rhs.x; return *this;
     D & operator /= (const D & rhs) & {
           assert(fabs(rhs.x) > eps);
x /= rhs.x; return *this;
      friend D operator+(D lhs, const D &rhs) {
           return lhs += rhs;
      friend D operator - (D lhs, const D &rhs) {
           return lhs -= rhs;
      friend D operator*(D lhs, const D &rhs) {
           return lhs *= rhs;
      friend D operator/(D lhs, const D &rhs) {
           return lhs /= rhs;
     friend bool operator <(const D &lhs, const D &rhs) {
   return lhs.x - rhs.x < -eps;</pre>
      friend bool operator > (const D &lhs. const D &rhs) {
           return lhs.x - rhs.x > eps;
     friend bool operator==(const D &lhs, const D &rhs) {
   return fabs(lhs.x - rhs.x) < eps;</pre>
     friend bool operator<=(const D &lhs, const D &rhs) {
   return lhs < rhs || lhs == rhs;</pre>
     friend bool operator>=(const D &lhs, const D &rhs) {
  return lhs > rhs || lhs == rhs;
     friend bool operator!=(const D &lhs, const D &rhs) {
  return !(lhs == rhs);
      friend istream &operator>>(istream &is, D &a) {
           double v; is >> v; a = D(v); return is;
      friend ostream &operator << (ostream &os, const D &a)</pre>
           return os << fixed << setprecision(10) << a.val() + (a.val() > 0 ? eps : a.val() < 0 ? -eps : θ);
     } // eps should < precision
```

1.5 Int128 [9454fa]

};

```
using i128 = __int128_t; // 1.7E38
inline i128 read() {
    i128 sgn = 1, x = 0;
     char c = getchar();
while (c < '0' || c > '9') {
   if (c == '-') sgn = -1;
           c = getchar();
     while (c >= '0' && c <= '9') {
    x = x * 10 + c - '0';
           c = getchar();
     return x * san:
inline void write(i128 x){
     if (x < 0) {
           putchár('-');
           x = -x;
     if (x > 9) write(x / 10);
putchar(x % 10 + '0');
```

1.6 Rng [401544]

```
(chrono::steady_clock::now().time_since_epoch().count());
ll x = rng(); shuffle(a.begin(), a.end(), rng);
```

2 Graph

2.1 DFS And BFS [e2d856]

```
int main() {
       vector < int >> adj(n);
       // dfs_graph
vector<bool> vis(n);
        auto dfs = [&](auto self, int u) -> void {
   if (vis[u]) return;
               vis[u] = true;
for (auto v: adj[u]) {
    self(self, v);
              }
       dfs(dfs, 0);
        // bfs
        vector<int> depth(n, 1e9);
       queue <int> q;
auto bfs = [&](auto self, int s) -> void {
    vis[s] = true, depth[s] = 0;
               q.push(s);
              while (!q.empty()) {
   int u = q.front(); q.pop();
   for (auto v : adj[u]) {
      if (vis[v]) continue;
      vis[v] = true;
      depth[v] = depth[u] + 1;
                             q.push(v);
                      }
              }
       bfs(bfs, 0);
```

2.2 Prim [3a3805]

2.3 Bellman-Ford [430ded]

```
// 用 Bellman Ford 找負環
int main() {
    int n, m; cin >> n >> m;
    vector <array int, 3>> e;
    for (int i = 0; i < m; i++) {
        int u, v, w; cin >> u >> v >> w;
        u --, v --; e.push_back({u, v, w});
}

vector <ll> dis(n, inf), par(n);
int t = -1; dis[0] = 0;
for (int i = 1; i <= n; i++) {
        for (auto [u, v, w] : e) {
            if (dis[v] > dis[u] + w) {
                dis[v] = dis[u] + w;
                par[v] = u;
                if (i == n) t = v;
            }
      }

if (t == -1) { cout << "NO\n"; return; }
for (int i = 1; i < n; i++) t = par[t];
vector <int> ans {t};
int i = t;
do {
        i = par[i];
        ans.push_back(i);
} while (i != t);
reverse(ans.begin(), ans.end());
cout << "YES\n";
for (auto x : ans) cout << x + 1 << " ";
}</pre>
```

2.4 Floyd-Warshall [3f61a4]

```
constexpr ll inf = 1e18;
void FloydWarshall(int n, int m) {
   int n, m; cin >> n >> m;
   vector < vector < int >> dis(n, vector < int >(n, inf));
   for (int i = 0; i < m; i++) {
      int u, v, w; cin >> u >> v >> w;
}
```

```
dis[u][v] = min(dis[u][v], w);
dis[v][u] = min(dis[v][u], w);
      for (int i = 0; i < n; i++) dis[i][i] = 0;
for (int k = 0; k < n; k++) {
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            dis[i][j</pre>
                           ] = min(dis[i][j], dis[i][k] + dis[k][j]);
           }
      }
 }
 dp[i] |= dp[k];
 2.5 Euler [4177dc]
|// 1. 無向圖是歐拉圖:
// 非零度頂點是連通的
 // 頂點的度數都是偶數
| // 2. 無向圖是半歐拉圖(有路沒有環):
// 非零度頂點是連通的
 // 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
// 非零度頂點是強連通的
 // 每個頂點的入度和出度相等
// 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
// 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
 // 其他頂點的入度和出度相等
 vector <int> ans;
auto dfs = [&](auto &&self, int u) -> void {
      while (g[u].size()) {
   int v = *g[u].begin();
           g[u].erase(v);
           self(self, v);
      ans.push_back(u);
 dfs(dfs, 0);
 reverse(ans.begin(), ans.end());
 2.6 DSU [749620]
 struct DSU {
      int n:
      vector<int> boss, siz;
      DSU() {}
      DSU(int n_) { init(n_); }
void init(int n_) {
           n = n_; boss.resize(n);
           iota(boss.begin(), boss.end(), 0);
siz.assign(n, 1);
      int find(int x) {
   if (boss[x] == x) return x;
   return boss[x] = find(boss[x]);
      bool same(int x, int y) {
    return find(x) == find(y);
      bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);
    if (x == y) return false;</pre>
```

siz[x] += siz[y]; boss[y] = x;

return siz[find(x)];

vector < int > boss, siz, stk;
DSU() {}
DSU(int n_) { init(n_); }

iota(boss.begin(), boss.end(), 0);

return true;

int size(int x) {

void init(int n_) {
 n = n_;

int find(int x) {

boss.resize(n);

siz.assign(n, 1);
stk.clear():

}

struct DSU {

};

```
return x == boss[x] ? x : find(boss[x]);
       bool same(int x, int y) {
   return find(x) == find(y);
       bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);
    if (siz[x] < siz[y])</pre>
              siz[x] += siz[y];
              boss[y] = x;
              stk.push_back(y);
              return true:
       void undo(int x) {
    while (stk.size() > x) {
        int y = stk.back();
}
                     stk.pop_back();
                     n++:
                     siz[boss[y]] -= siz[y];
boss[y] = y;
              }
       int size(int x) {
              return siz[find(x)];
      }
};
```

```
2.7 SCC [5d3e16]
struct SCC {
    adj.assign(n, {});
          dfn.assign(n, -1);
low.resize(n);
          bel.assign(n, -1);
          stk.clear();
          cur = cnt = 0;
     void addEdge(int u, int v) {
         adj[u].push_back(v);
     void dfs(int x) {
    dfn[x] = low[x] = cur++;
          stk.push_back(x);
for (auto y : adj[x]) {
    if (dfn[y] == -1) {
                    dfs(y);
                    low[x]' = min(low[x], low[y]);
               } else if (bel[y] == -1) {
    low[x] = min(low[x], dfn[y]);
          if (dfn[x] == low[x]) {
               int y;
do {
                    y = stk.back();
                    bel[y] = cnt;
                    stk.pop_back();
              } while (y != x);
               cnt++;
         }
     return bel:
     struct Graph { // 可能有重邊
          vector<pair<int, int>> edges;
          vector<int> siz;
          vector<int> cnte;
    };
Graph compress() {
         Graph g;
g.n = cnt;
          g.siz.resize(cnt);
          g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;</pre>
               for (auto j : adj[i]) {
   if (bel[i] != bel[j]) {
       g.edges.emplace_back(bel[i], bel[j]);
   } else {
                        g.cnte[bel[i]]++;
              }
          return g;
    }
}:
```

```
struct VBCC {
       int n, cur;
vector<vector<int>> adj;
       vector <int> > adj;
vector <int> dfn, low, parent;
vector <bool> is_cut;
VBCC(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_;
    adj accide(s)
              adj.assign(n, {});
              dfn.assign(n, -1);
              low.resize(n):
             parent.assign(n, -1);
is_cut.assign(n, false);
             cur = 0:
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void dfs(int x) {
             int children = 0;
              dfn[x] = low[x] = cur++;
             for (int v : adj[x]) {
    if (dfn[v] == -1) {
        children++;
                          parent[v] = x;
                          dfs(v);
low[x] = min(low[x], low[v]);
                          if (parent[x] != -1 && low[v] >= dfn[x]) {
                                 is_cut[x] = true;
                    } else if (v != parent[x]) {
   low[x] = min(low[x], dfn[v]);
             if (parent[x] == -1 && children > 1) {
    is_cut[x] = true;
             }
       }
       }
};
```

2.9 EBCC [59d8ca]

```
struct EBCC { // CF/contest/1986/pF
                       int n, cur, cnt;
vector<vector<int>> adj;
vector<vector<int>> bridges;
vector<pair<int, int>> bridges; // 關鍵邊
EBCC(int n_ = 0) { init(n_); }
void init(int n_) {
                                               n = n_;
                                                adj.assign(n, {});
dfn.assign(n, -1);
                                                 low.resize(n);
                                                bel.assign(n,
                                                 stk.clear();
                                                 bridges.clear();
                                                cur = cnt = 0;
                         void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
                         void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
                                                   stk.push_back(x);
                                                stk.push_back(x);
for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
        dfs(y, x);
        low[x] = min(low[x], low[y]);
        if (low[y] > dfn[x]) {
            bridges.emplace_back(x, y);
        lenter that the provided in the provi
                                                                         } else if (bel[y] == -1) {
    low[x] = min(low[x], dfn[y]);
                                                   if (dfn[x] == low[x]) {
                                                                          int y;
do {
                                                                                                  y = stk.back();
                                                                                                  bel[y] = cnt;
                                                                                                  stk.pop_back();
                                                                         } while (y != x);
                                              }
                         fvector<int> work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
        }
}</pre>
                                                }
```

2.8 VBCC [170604]

```
return bel:
     struct Graph { // 不會有重邊
           int n;
           vector<pair<int, int>> edges;
           vector<int> siz; // BCC 內節點數
           vector<int> cnte; // BCC 內邊數
     Graph compress() {
          Graph g;
g.n = cnt;
           g.siz.resize(cnt);
           g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {</pre>
                g.siz[bel[i]]++;
                for (auto j : adj[i]) {
    if (bel[i] < bel[j]) {</pre>
                     g.edges.emplace_back(bel[i], bel[j]);
} else if (i < j) {
   g.cnte[bel[i]]++;</pre>
               }
           return g;
     }
};
```

2.10 2-SAT [3f3604]

```
// CSES Giant Pizza
struct TwoSat {
      int n; vector<vector<int>> e;
      vector<bool> ans;
     TwoSat(int n) : n(n), e(2 * n), ans(n) {}
void addClause(int u, bool f, int v, bool g) {
    e[2 * u + !f].push_back(2 * v + g);
    e[2 * v + !g].push_back(2 * u + f);
}
      void ifThen(int u, bool f, int v, bool g) {
            // 必取 A: not A -> A
            e[2 * u + !f].push_back(2 * v + g);
     bool satisfiable() {
            vector<int
                  > id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
            vector<int> stk;
int now = 0, cnt = 0;
function<void(int)> tarjan = [&](int u) {
                 stk.push_back(u);
dfn[u] = low[u] = now++;
for (auto v : e[u]) {
   if (dfn[v] == -1) {
                              tarjan(v);
                        low[u] = min(low[u], low[v]);

} else if (id[v] == -1) { // in stk
low[u] = min(low[u], dfn[v]);
                  if (dfn[u] == low[u]) {
                        int v;
                        do {
    v = stk.back();
                             stk.pop_back();
id[v] = cnt;
                        } while (v != u);
                        ++cnt:
                }
            for (int i
            return true:
      vector < bool > answer() { return ans; }
int main() {
   int m, n; cin >> m >> n;
   TwoSat ts(n);
   for (int i = 0; i < m; ++i) {</pre>
           int u, v; char x, y;
cin >> x >> u >> y >> v;
ts.addClause(u - 1, x == '+', v - 1, y == '+');
      if (ts.satisfiable()) {
            for (int i = 0; i < n; ++i) {
   cout << (ts.answer()[i] ? '+' : '-') << " ";</pre>
     else cout << "IMPOSSIBLE\n";</pre>
```

2.11 Funtional Graph [e8fd64]

```
constexpr int N = 2E5 + 5;
int cht[N][31]; // 倍增表, 放外面不然 TLE
struct FuntionalGraph {
    int n, cnt;
    vector < int > g, bel, id, len, in, top;
```

```
FuntionalGraph() : n(0) {}
FuntionalGraph(vector<int> g_) { init(g_); }
        void init(vector<int> g_) {
               n = g_.size(); cnt = 0;
g = g_; bel.assign(n, -
                id.resize(n); len.clear();
in.assign(n, 0); top.assign(n, -1);
                build();
        void build() {
    for (int i = 0; i < n; i++) {
        cht[i][0] = g[i];
}</pre>
                         in[g[i]]++;
                 for (int i = 1; i <= 30; i++)
                for (int i = 1; i <= 30; i++)
    for (int u = 0; u < n; u++)
        cht[u][i] = cht[cht[u][i - 1]][i - 1];
for (int i = 0; i < n; i++)
    if (in[i] == 0) label(i);
for (int i = 0; i < n; i++)
    if (top[i] == -1) label(i);</pre>
        void label(int u) {
                vector<int> p; int cur = u;
while (top[cur] == -1) {
                        top[cur] = u;
                         p.push_back(cur);
                         cur = q[cur];
                auto s = find(p.begin(), p.end(), cur);
vector<int> cyc(s, p.end());
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {
    bel[cyc[i]] = cnt;
    id[cyc[i]] = i;</pre>
                int jump(int u, int k) {
   for (int b = 0; k > 0; b++){
      if (k & 1) u = cht[u][b];
                 return u:
};
```

3 Data Structure

3.1 BIT [d41d8c]

```
template < typename T>
struct Fenwick { // 全部以 θ based 使用
int n; vector<T> a;
Fenwick(int n_ = θ) { init(n_); }
     void init(int n_) {
          n = n;
          a.assign(n, T{});
     void add(int x, const T &v) {
   for (int i = x + 1; i <= n; i += i & -i) {
      a[i - 1] = a[i - 1] + v;
}</pre>
     T sum(int x) { // 左閉右開查詢
          T ans{};
          for (int i = x; i > 0; i -= i & -i) {
    ans = ans + a[i - 1];
     TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
      int select(const T &k, int start = 0) {
          cur = cur + a[x - 1];
               }
          return x;
    }
template < class T>
struct TwoDFenwick { // 全部以 0 based 使用
     int nx, ny; // row, col 個數 vector<vector<T>> a;
     TwoDFenwick(int nx_ = 0, int ny_ = 0) {
          init(nx_, ny_);
     void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
     void add(int x, int y, const T &v) {
```

```
for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        a[i - 1][j - 1] = a[i - 1][j - 1] + v;
    }
}

T sum(int x, int y) { // 左閉右開查詢
    T ans{};
    for (int i = x; i > 0; i -= i & -i) {
        for (int j = y; j > 0; j -= j & -j) {
            ans = ans + a[i - 1][j - 1];
        }
    return ans;
}

T rangeSum
    (int lx, int ly, int rx, int ry) { // 左閉右開查詢
    return sum(
        rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
}

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```

3.2 RangeBit [d41d8c]

```
template < class T>
struct rangeFenwick { // 全部以 0 based 使用
                   int n;
                     vector<T> d, di;
                     rangeFenwick(int n_ = 0) { init(n_); }
                     void init(int n_) {
                                         n = n_{\dot{}};
                                         d.assign(n, T{});
                                         di.assign(n, T{});
                    void add(int x, const T &v) {
   T vi = v * (x + 1);
   for (int i = x + 1; i <= n; i += i & -i) {</pre>
                                                            d[i - 1] = d[i - 1] + v;
di[i - 1] = di[i - 1] + vi;
                                        }
                    void rangeAdd(int l, int r, const T &v) {
                                         add(l, v); add(r, -v);
                    T sum(int x) { // 左閉右開查詢
                                         T`ans{};
                                         for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
                                         return ans;
                   TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
                     int select(const T &k, int start = 0) {
                                        T \text{ val} = T(
                                                                                  x + i + 1) * d[x + i - 1] - di[x + i - 1];

if (cur + val <= k) {

x += i;
                                                                                                       cur = cur + val:
                                                            }
                                         return x;
                 }
template < class T>
struct rangeTwoDFenwick { // 全部以 0 based 使用
                  int nx, ny; // row, col 個數
vector <vector <T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
init(x)
                                         init(nx , ny );
                  void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
                                         dij.assign(nx, vector<T>(ny, T{}));
                   }
void add(int x, int y, const T &v) {
    T vi = v * (x + 1);
    T vj = v * (y + 1);
    T vij = v * (y + 1);
    T vij = v * (x + 1) * (y + 1);
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            d[i - 1][j - 1] = d[i - 1][j - 1] + v;
            di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
            dj[i - 1][j - 1] = di[i - 1][j - 1] + vj;
            dif[i - 1][i - 1] = dii[i - 1][i - 1] + vi;
            dii[i - 1][i - 1] = dii[i - 1][i - 1] + vi;
            dii[i - 1][i - 1] = dii[i - 1][i - 1] + vi;
            dii[i - 1][i - 1] = dii[i - 1][i - 1] + vi;
            dii[i - 1][i - 1] = dii[i - 1][i - 1] + vi;
            dii[i - 1][i 
                                                                                  dij[i - 1][j - 1] = dij[i - 1][j - 1] + vij;
                                                           }
                                        }
                     void rangeAdd(int lx. int lv. int rx. int rv. const T &v) {
                                         add(rx, ry, v);
add(lx, ry, -v);
```

3.3 Segment Tree [d41d8c]

int sum = 0;

```
| template < class Info >
 struct Seg { // 左閉右開寫法
int n; vector<Info> info;
        Seg(): n(0) {}
Seg(int n_, Info v_ = Info()) { init(n_, v_); }
        template < class T>
        void init(int n_, Info v_ = Info()) {
  init(vector(n_, v_));

        template < class T >
        void init(vector<T> init_) {
             n = init_.size();
info.assign(4 << __lg(n), Info());</pre>
              function < void(
                    int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
                           info[p] = init_[l];
                           return
                    int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                    pull(p);
              build(1, 0, n);
        void pull(int p) {
    info[p] = info[p * 2] + info[p * 2 + 1];
        void modify(int p, int l, int r, int x, const Info &v) {
                    (r - l == 1) {
  info[p] = v; return;
              int m = (l + r) / 2;
if (x < m) modify(2 * p, l, m, x, v);
else modify(2 * p + 1, m, r, x, v);
publ(a);</pre>
              pull(p);
        void modify(int p, const Info &i) {
              modify(1, 0, n, p, i);
       Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    return query(p *</pre>
              return query(p
                      2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
       Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
        template < class F > // 尋找區間內,第一個符合條件的
        int findFirst
             (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)
    return -1;
if (l >= x && r <= y && !pred(info[p]))
    return -1;</pre>
              if (r - l == 1)
              return l;
int m = (l + r) / 2;
int res = findFirst(2 * p, l, m, x, y, pred);
              if (res == -1)
    res = findFirst(2 * p + 1, m, r, x, y, pred);
              return res;
       template < class F> // 若要找 last,先右子樹遞迴即可
int findFirst(int l, int r, F & & pred) {
    return findFirst(1, 0, n, l, r, pred);
       }
 };
 struct Info {
        int n = 0;
```

```
Info operator+(const Info &a, const Info &b) {
   return { a.n + b.n, a.sum + b.sum };
}
3.4 Lazy Segment Tree [d41d8c]
template < class Info, class Tag>
struct LazySeg { // 左閉右開寫法
      int n;
       vector < Info > info:
      vector<inio cinc,
vector<Tag> tag;
LazySeg() : n(0) {}
LazySeg(int n_, Info v_ = Info()) {
   init(n_, v_);
   .
      template < class T>
LazySeg(vector < T> init_) {
   init(init_);
       void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
                                                                                                                  };
       template < class T>
       void init (vector<T> init_) {
             n = init_.size();
              info.assign(4 << __lg(n), Info());
tag.assign(4 << __lg(n), Tag());
function <void(</pre>
                    int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
   info[p] = init_[l];
                                                                                                                        }
                                                                                                                  };
                     int m = (l + r) / 2;
                    build(p * 2, l, m);
build(p * 2 + 1, m, r);
                    pull(p);
             build(1, 0, n);
       void pull
       (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
  info[p].apply(l, r, v);
              tag[p].apply(v);
      void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
             tag[p] = Tag();
       void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
}
                    return;
             fint m = (l + r) / 2;
push(p, l, r);
if (x < m) {
    modify(2 * p, l, m, x, v);
}</pre>
                    modify(2 * p + 1, m, r, x, v);
             pull(p);
       void modify(int p, const Info &i) {
             modify(1, 0, n, p, i);
       Info query(int p, int l, int r, int ql, int qr) {
   if (qr <= l || ql >= r) return Info();
   if (ql <= l && r <= qr) return info[p];</pre>
             int m = (l + r) / 2;
push(p, l, r);
             return query(p *
2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      Info query
    (int ql, int qr) { return query(1, 0, n, ql, qr); }
      void range_apply
   (int p, int l, int r, int ql, int qr, const Tag &v) {
   if (qr <= l || ql >= r) return;
   if (ql <= l && r <= qr) {</pre>
                    apply(p, l, r, v);
                    return;
             int m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
pull(p);
                                                                                                                         }
       void range_apply(int l, int r, const Tag &v) {
    range_apply(1, 0, n, l, r, v);
       template < class F> // 尋找區間內,第一個符合條件的
```

int findFirst

(int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {</pre>

```
return -1:
           if (l >= x && r <= y && !pred(info[p])) {</pre>
                 return -1:
           if (r - l == 1) {
                 return l;
           int m = (l + r) / 2;
           push(p);
           int res = findFirst(2 * p, l, m, x, y, pred);
                 res = findFirst(2 * p + 1, m, r, x, y, pred);
      template < class F> // 若要找 last, 先右子樹遞迴即可
int findFirst(int l, int r, F & pred) {
return findFirst(1, 0, n, l, r, pred);
struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add;
     void apply(const Tag& v) {
   if (v.set_val) {
      set_val = v.set_val;
}
                add = v.add;
                 add += v.add;
struct Info {
      int sum;
      void apply(int l, int r, const Tag &v) {
    if (v.set_val) {
        sum = (r - l) * v.set_val;
}
           sum += (r - l) * v.add;
      // Info& operator=(const Info &rhs) {
              // 部分 assignment 使用 return *this;
     //
//
// }
Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
3.5 Persistent Segment Tree [d41d8c]
```

```
template < class Info >
struct PST {
      struct Node {
            Info info = Info();
            int lc = 0, rc = 0;
      vector < Node > nd;
     vector<Node> nd;
int n = 0; vector<int> rt;
PST() : n(0) {}
PST(int n_, Info v_ = Info()) { init(n_, v_); }
template<class T>
PST(vector<T> init_) { init(init_); }
void init(int n_, Info v_ = Info()) {
   init(vector<Info>(n_, v_));
}
      void init(vector<T> init_) {
    n = init_.size();
    nd.clear(); rt.clear();
            nd.emplace_back(); // 讓 root 指向 1-based rt.push_back(build(0, n, init_));
      int build(int l. int r. vector<Info> &init ) {
            int id = nd.size();
             nd.emplace_back();
            if (r - l == 1) {
   nd[id].info = init_[l];
   return id;
            int m = (l + r) >>
            nd[id].lc = build(l, m, init_);
            nd[id].rc = build(m, r, init_);
pull(nd[id]);
            return id;
      void pull(Node &t) {
   t.info = nd[t.lc].info + nd[t.rc].info;
      int copy(int t) { // copy 一個 node
  nd.push_back(nd[t]);
            return nd.size() - 1;
      int generate() { // 創立新的 node
    nd.emplace_back();
             return nd.size()
      int modify(int t, int l, int r, int x, const Info &v) {
            t = t ? copy(t) : generate();
if (r - l == 1) {
```

```
nd[t].info = v:
            int m = (l + r) >> 1;
if (x < m) {
                 nd[t].lc = modify(nd[t].lc, l, m, x, v);
                 nd[t].rc = modify(nd[t].rc, m, r, x, v);
            pull(nd[t]);
            return t:
      void modify(int ver, int pos, const Info &val) {
   if (int(rt.size()) <= ver) rt.resize(ver + 1);
   rt[ver] = modify(rt[ver], 0, n, pos, val);</pre>
     Info query(int t, int l, int r, int ql, int qr) {
   if (l >= qr || r <= ql) return Info();
   if (ql <= l && r <= qr) return nd[t].info;</pre>
            int m = (l + r) >> 1;
            return query(nd[t].
                   lc, l, m, ql, qr) + query(nd[t].rc, m, r, ql, qr);
     Info query(int ver, int ql, int qr) {
    return query(rt[ver], 0, n, ql, qr);
     void createVersion(int ori_ver) {
   rt.push_back(copy(rt[ori_ver]));
     void reserve(int n, int q) {
   nd.reserve(n + q * (2 * __lg(n) + 1));
   rt.reserve(q + 1);
      void resize(int n) {
            rt.resize(n):
     }
struct Info {
      int sum = 0;
Info operator+(const Info &a, const Info &b) {
     return { a.sum + b.sum };
3.6 Treap [d41d8c]
struct Treap {
     Treap {
Treap *lc, *rc;
int pri, siz; bool rev_valid;
int val; int min;
Treap(int val_) {
           min = val = val_;
pri = rand();
            lc = rc = nullptr;
            siz = 1; rev_valid = 0;
      void pull() { // update siz or other information
           siz = 1;
min = val;
            for (auto c : {lc, rc}) {
    if (!c) continue;
                  siz += c->siz;
                  min = std::min(min, c->min);
           }
      void push() {
            if (rev_valid) {
                  swap(lc, rc);
if (lc) lc->rev_valid ^= 1;
if (rc) rc->rev_valid ^= 1;
            rev_valid = false;
     int find(int k) { // 找到 min 是 k 的位置 (1-based)
            push();
            int ls = (lc ? lc->siz : 0) + 1;
            if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
     }
int size(Treap *t) {
    return t ? t->siz : 0;
Treap *merge(Treap *a, Treap *b) {
     if (!a || !b) return a ? a : b;
a->push(); b->push();
if (a->rc = merge(a->rc, b);
a->pull();
            return a;
      b->lc = merge(a, b->lc);
            b->pull();
     }
pair<Treap*, Treap*> split(Treap *t, int k) {
     // 分割前 k 個在 first, 剩下的在 second if (t == nullptr) return {nullptr, nullptr};
```

t->push();

```
if (size(t->lc) < k) {
   auto [a, b] = split(t->rc, k - size(t->lc) - 1);
   t->rc = a;
            t->pull();
            return {t, b};
       else {
            auto [a, b] = split(t->lc, k);
t->lc = b;
           t->lc = b;
t->pull();
            return {a, t};
      }
 void Print(Treap *t) {
      if (!t) return;
       t->push();
      Print(t->lc);
cout << t->val;
      Print(t->rc);
 3.7 RMO [d41d8c]
 template < class T, class Cmp = greater < T >>
 struct RMQ {
    const Cmp cmp = Cmp();
       static constexpr unsigned B = 64;
       using u64 = unsigned long long;
       int n;
       vector<vector<T>> a;
       vector<T> pre, suf, ini;
vector<u64> stk;
       RMQ() {}
       RMQ(const vector<T> &v) { init(v); }
       void init(const vector<T> &v) {
    n = v.size();
            pre = suf = ini = v;
            stk.resize(n);
            if (!n) {
                 return:
            for (int j = 1; j < B && i * B + j < n; j++) {
    a[0][i] = min(a[0][i], v[i * B + j], cmp);</pre>
            for (int i = 1; i < n; i++) {
   if (i % B) {
      pre[i] = min(pre[i], pre[i - 1], cmp);
}</pre>
            for (int i = n - 2; i >= 0; i--) {
   if (i % B != B - 1) {
      suf[i] = min(suf[i], suf[i + 1], cmp);
}
            for (int j = 0; j < lg; j++) {
    for (int i = 0; i + (2 << j) <= M; i++) {</pre>
                     a[j + 1][i
] = min(a[j][i], a[j][i + (1 << j)], cmp);
                 }
            for (int i = 0; i < M; i++) {
    const int l = i * B;
    const int r = min(1U * n, l + B);</pre>
                 u64 s = 0;
                 for (int j = l; j < r; j++) {
    while (s && cmp(v[j], v[__lg(s) + l])) {
       s ^= 1ULL << __lg(s);
    }
}</pre>
                       s |= 1ULL << (j - l);
                       stk[j] = s;
                 }
           }
      ({ans, a[k][l], a[k][r - (1 << k)]}, cmp);
                 return ans;
           } else {
   int x = B * (l / B);
                       [__builtin_ctzll(stk[r - 1] >> (l - x)) + l];
            }
      }
}:
 3.8 Mo [d41d8c]
struct query {
```

int l, r, id;

```
function <book = sqrt(n);
function <book = sqrt(n);
function <book = definition = sqrt(n);
int block_a = a.l / block;
int block_b = b.l / block;
if (block_a != block_b) return block_a < block_b;
return a.r < b.r;</pre>
      sort(queries.begin(), queries.end(), cmp);
void compress(vector<int> &nums) {
      vector < int > sorted = nums;
sort(sorted.begin(), sorted.end());
       sorted.erase
      (unique(sorted.begin(), sorted.end());
for (int i = 0; i < nums.size(); i++) {
   nums[i] = lower_bound(sorted.begin</pre>
                     (), sorted.end(), nums[i]) - sorted.begin() + 1;
}
```

4 Flow Matching

4.1 Dinic [d41d8c]

```
template < class T>
 struct Dinic {
       struct Edge {
             int to;
             T flow, cap; // 流量跟容量
       int n, m, s, t;

const T INF_FlOW = 1 << 30;

vector<vector<int>> adj; // 此點對應的 edges 編號
       vector<Edge> edges; // 幫每個 edge 編號
       vector <int> dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_) {
             n = n_; m = 0;
dis.resize(n); ptr.resize(n);
adj.assign(n, vector<int>{});
              edges.clear();
       void add_edge(int u, int v, T cap) {
              // 偶數 id 是正向邊
              edges.push_back({ v, 0, cap });
edges.push_back({ u, 0, 0 });
              adj[u].push_back(m++);
              adj[v].push_back(m++);
       bool bfs() {
              fill(dis.begin(), dis.end(), -1);
              dis[s] = 0; queue < int > q;
              q.push(s);
             q.push(s),
while (!q.empty() && dis[t] == -1) {
   int u = q.front(); q.pop();
   for (int id : adj[u]) {
      Edge &e = edges[id];
      if (s]
                           if (e.flow == e.cap) continue;
if (dis[e.to] == -1) {
    dis[e.to] = dis[u] + 1;
                                 q.push(e.to);
                    }
              return dis[t] != -1;
       &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {</pre>
                    acu = ptr[u]; cu < (tht/adj[u].stze(); cu
Edge &e = edges[adj[u][cur]];
if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;
T mn = dfs(e.to, min(flow, e.cap - e.flow));</pre>
                    if (mn > 0) {
    e.flow += mn;
                           edges[adj[u][cur] ^ 1].flow -= mn;
                    }
              }
              return 0; // 到不了終點就會 return 0
       f
    work(int s_, int t_) {
        s = s_; t = t_; T flow = 0;
        while (bfs()) {
            fill(ptr.begin(), ptr.end(), 0);
        }
}
                    while (true) {
   T res = dfs(s, INF_Flow);
   if (res == 0) break;
                           flow += res;
                    }
              return flow;
       void reset() {
              for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
1:
```

4.2 Min Cut [d41d8c]

```
// CSES Police Chase
int main(){
       int n, m; cin >> n >> m;
Dinic<int> g(n);
for (int i = 0; i < m; i++) {
   int u, v, cap = 1;
   cin >> u >> v;
             u--; v--;
             g.add_edge(u, v, cap);
             g.add_edge(v, u, cap);
       int res = g.work(0, n - 1);
cout << res << "\n";
       if (res == 0) return;
       vector < int > vis(n);
auto find = [&](auto self, int u) -> void {
             if (!vis[u]) {
                    vis[u] = 1;
for (int id : g.adj[u])
                            auto e = g.edges[id];
                           if (e.cap - e.flow > 0) {
    self(self, e.to);
                    }
             }
       find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;</pre>
              for (int id : g.adj[i]) {
    if (id & 1) continue;
    auto e = g.edges[id];
                     if (!vis[e.to]) {
                           cout << i + 1 << " " << e.to + 1 << "\n";
                    }
             }
      }
}
```

4.3 MCMF [d41d8c]

```
template < class Tf, class Tc>
struct MCMF {
     struct Edge {
   int to;
          Tf flow, cap; // 流量跟容量
          Tc cost;
      // 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就好
     vector<Edge> edges; // 幫每個 edge 編號
vector<Tc> dis, pot; // johnson algorithm, using spfa
     vector<int> rt; // 路徑恢復, 對應 id
     vector < int > rt; // 所程恢复 * s
vector < bool > inq;
MCMF(int n_ = 0) { init(n_); }
void init(int n_) {
n = n_; m = 0;
           edges.clear();
          adj.assign(n, vector<int>{});
     void add_edge(int u, int v, Tf cap, Tc cost){
   edges.push_back({v, 0, cap, cost});
   edges.push_back({u, 0, 0, -cost});
   adj[u].push_back(m++);
   adj[v].push_back(m++);
     bool spfa() {
          dis.assign(n, INF_COST);
rt.assign(n, -1); inq.assign(n, false);
          aueue<int> q;
          q.push(v); inq[v] = true;
                     }
          return dis[t] != INF_COST;
     dis[s] = 0; pq.emplace(dis[s], s);
while (!pq.empty()) {
    auto [d, u] = pq.top(); pq.pop();
    if (dis[u] < d) continue;</pre>
```

```
for (int id : adj[u]) {
                              (int id : ad][u]) {
  auto [v, flow, cap, cost] = edges[id];
  Tc ndis = dis[u] + cost + pot[u] - pot[v];
  if (flow < cap && dis[v] > ndis) {
     dis[v] = ndis; rt[v] = id;
}
                                      pq.emplace(ndis, v);
               return dis[t] != INF_COST;
       }
       // 限定 flow,最小化 cost
pair<Tf, Tc> work_flow(int s_, int t_, Tf need) {
               s = s_, t = t_; pot.assign(n, 0);
If flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] += pot[i] - pot[s];
}</pre>
                       If f = INF_FLOW;
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                       (f, edges[rt[i]].cap - edges[rt[i]].flow);
                      f = min<Tf>(f, need);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
                       flow += f; need -= f;
cost += f * dis[t]; fr = false;
                       swap(dis, pot);
                       if (need == 0) break;
               return make pair(flow, cost);
       // 限定 cost, 最大化 flow
pair<Tf, Tc> work_budget(int s_, int t_, Tc budget) {
               s = s_, t = t_; pot.assign(n, 0);
If flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] += pot[i] - pot[s];
}</pre>
                       Tf f = INF_FLOW;
                       for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                       (f, edges[rt[i]].cap - edges[rt[i]].flow);
                       f = min<Tf>(f, budget / dis[t]);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
                       flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
                       swap(dis, pot);
if (budget == 0 || f == 0) break;
               return make_pair(flow, cost);
       void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
       }
};
```

4.4 Hungarian [d41d8c]

```
struct Hungarian { // 0-based
     vector < vector < int >> adj;
     vector < int > used, vis;
vector < pair < int , int >> match;
     Hungarian(int n_{-} = 0, int m_{-} = 0) {
           init(n_, m_);
     void init(int n_, int m_) {
          n = n_; m = m_;
adj.assign(n + m, vector < int > ());
used.assign(n + m, -1);
           vis.assign(n + m, 0);
     void addEdge(int u, int v) {
           adj[u].push_back(n + v);
           adj[n + v].push_back(u);
     bool dfs(int u) {
           int sz = adj[u].size();
for (int i = 0; i < sz; i++) {
   int v = adj[u][i];</pre>
                if (vis[v] == 0) {
  vis[v] = 1;
  if (used[v] == -1 || dfs(used[v])) {
                           used[v] = u;
                           return true;
                     }
                }
           return false:
     vector<pair<int, int>> work() {
```

```
match.clear(); used.assign(n + m, -1);
             vis.assign(n + m, 0);

for (int i = 0; i < n; i++) {

    fill(vis.begin(), vis.end(), 0); dfs(i);
             for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
                        match.push_back(make_pair(used[i], i - n));
             return match:
      }
};
```

4.5 Theorem [d41d8c]

```
// 有向無環圖:
// 最小不相交路徑覆蓋:
// 最小路徑數 = 頂點數 - 最大匹配數
1// 最小相交路徑覆蓋:
| // 先用
   Floyd 求傳遞封包,有連邊就建邊,然後再套最小不相交路徑覆蓋
// 二分圖:
// 最小點
   覆蓋: 選出一些點,讓所有邊至少有一個端點在點集中的最少數量
// 最小點覆蓋 = 最大匹配數
// 還原解, flow 的作法是從源點開始 dfs, 只走 cap - flow > 0
// 的邊,最後挑選左邊還沒被跑過的點和右邊被跑過的點當作覆蓋的點
// 最少邊覆蓋: 選出一些邊,讓所有點都覆蓋到的最少數量
// 最少邊覆蓋 = 點數 - 最大匹配數
1// 最大獨立集: 選出一些點, 使這些點兩兩沒有邊連接的最大數量
// 最大獨立集 = 點數 - 最大匹配數
```

String

5.1 Hash [852711]

```
constexpr int B = 59;
vector<Z> Hash(string &s) {
      vector<Z> ans {0};
for (auto c : s) {
             ans.push_back(ans.back() * B + (c - 'a' + 1));
       return ans;
void solve() {
      string s, sub;
cin >> s >> sub;
auto a = Hash(s);
       auto q = Hash(sub)
       auto find = q.back();
int ans = 0;
       int l = 1, r = sub.size(), len = sub.size();
while (r <= s.size()) {
    if (a[r] - a[l - 1] * power(Z(B), len) == find) {</pre>
                   ans++;
             l++. r++:
       cout << ans << "\n";
}
```

5.2 KMP [cddfd9]

```
struct KMP {
      string sub;
vector<int> failure;
      KMP(string sub_) {
             sub = sub_;
failure.resize(sub.size(), -1);
             buildFailFunction();
      void buildFailFunction() {
   for (int i = 1; i < (int)sub.size(); i++) {
      int now = failure[i - 1];
}</pre>
                   while (now != -1
     && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
            }
       vector<<mark>int</mark>> match(string &s) {
             vector < int > match;
for (int i = 0, now = -1; i < (int)s.size(); i++) {</pre>
                        now is the compare sucessed length
                    while (s[i] !=
                    sub[now + 1] && now != -1) now = failure[now];

// failure stores if comparison fail, move to where
                   if (s[i] == sub[now + 1]) now++;
if (now + 1 == (int)sub.size()) {
                          match.push_back(i - now);
now = failure[now];
                   }
```

```
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           return match;
};
 5.3 Z Function [764b31]
| // z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
 // 的最長公共前綴 (LCP) 的長度
 vector<int> Z(string s) {
      int n = s.size();
     int n = S.stze(),
vector <int> z(n); z[0] = n;
for (int i = 1, j = 1; i < n; i++) {
    z[i] = max(0, min(j + z[j] - i, z[i - j]));
    while (i + z[i] < n && s[z[i]] == s[i + z[i]])
    -rs1-...</pre>
               z[i]++;
           if (i + z[i] > j + z[j]) j = i;
     return z; // 最後一格不算
5.4 Manacher [9c9ca6]
 // 找到對於每個位置的迴文半徑
 vector < int > manacher(string s) {
      string t = "#";
      for (auto c : s) {
    t += c;
    t += '#';
      int n = t.size();
     vector < int > r(n);
for (int i = 0, j =
           0; i < n; i++) { // i 是中心, j 是最長回文字串中心 if (2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
           while (i - r[i] >=
     0 && i + r[i] < n && t[i - r[i]] == t[i + r[i]]) {
    r[i] += 1;</pre>
           if (i + r[i] > j + r[j]) {
    j = i;
          }
      return r;
     // # a # b # a #
// 1 2 1 4 1 2 1
     // # a # b # b # a #
// 1 2 1 2 5 2 1 2 1
      // 值 -1 代表原回文字串長度
      // (id - val + 1) / 2 可得原字串回文開頭
5.5 Trie [31e4ff]
 constexpr int N = 1E7;
 int trie[N][26], cnt[N];
void reset() {
   tot = 0, fill_n(trie[0], 26, 0);
 int newNode() {
     int x = ++tot;
cnt[x] = 0, fill_n(trie[x], 26, 0);
      return x;
 void add(string &s) {
     int p = 0;
for (auto c : s) {
           int &q = trie[p][c - 'a'];
           if (!q) q = newNode();
           p = q;
     cnt[p] += 1;
 int find(string &s) {
      for (auto c : s) {
    int q = trie[p][c - 'a'];
           if (!q) return 0;
           p = q;
      return cnt[p];
}
 5.6 SA [b58946]
 struct SuffixArray {
     int n; string s;
vector<int> sa, rk, lc;
      // n: 字串長度
      // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
      // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
      // lc: LCP
            數組,lc[i] 表示 sa[i] 和 sa[i+1] 的最長公共前綴長度
      SuffixArray(const string &s_) {
   s = s_; n = s.length();
   sa.resize(n);
```

lc.resize(n - 1);

```
rk.resize(n):
             iota(sa.begin(), sa.end(), 0);
             sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });
rk[sa[0]] = 0;</pre>
             for (int i = 1; i < n; i++)</pre>
                  rk[sa[i]]
                           = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
             vector < int > tmp, cnt(n);
             tmp.reserve(n);
while (rk[sa[n - 1]] < n - 1) {</pre>
                  tmp.clear();
for (int i = 0; i < k; i++)
    tmp.push_back(n - k + i);</pre>
                   for (auto i : sa)
if (i >= k)
                              tmp.push_back(i - k);
                   fill(cnt.begin(), cnt.end(), 0);

for (int i = 0; i < n; i++)
                  for (int i = 0; i < n; i++)
     ++cnt[rk[i]];
for (int i = 1; i < n; i++)
     cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; i--)
                         sa[--cnt[rk[tmp[i]]]] = tmp[i];
                   swap(rk, tmp);
                  for (int i = 0, j = 0; i < n; i++) {
   if (rk[i] == 0) {</pre>
                         j = 0;
                   } else {
                         for (j -=
                         j > 0; i + j < n && sa[rk[i] - 1] + j < n
    && s[i + j] == s[sa[rk[i] - 1] + j]; j++);
lc[rk[i] - 1] = j;</pre>
            }
      }
};
 5.7 SAM [d15619]
 struct SAM { // 0 is initial state,
                                                      1-based
       static constexpr int ALPHABET_SIZE = 26;
       struct Node {
             int len;
             int link;
             arrav<int. ALPHABET SIZE> next:
             Node() : len{}, link{}, next{} {}
        vector<Node> t;
       SAM() {
   init();
       void init() {
    t.assign(2, Node());
    t[0].next.fill(1);
    restant
             t[0].len = -1;
       int newNode() {
             t.emplace_back();
return t.size() - 1;
       int extend(int p, int c) {
    if (t[p].next[c]) {
        int q = t[p].next[c];
    }
}
                   if (t[q].len == t[p].len + 1) {
                         return q:
                   int r = newNode();
                  t[r].len = t[p].len + 1;
t[r].link = t[q].link;
t[r].next = t[q].next;
t[q].link = r;
                   while (t[p].next[c] == q) {
    t[p].next[c] = r;
                         p = t[p].link;
                   return r;
             int cur = newNode();
t[cur].len = t[p].len + 1;
while (!t[p].next[c]) {
                  t[p].next[c] = cur;
                   p = t[p].link;
             t[cur].link = extend(p, c);
             return cur;
      }
 void solve() {
       string s; cin >> s;

int n = s.length();
       vector < int > pos(n + 1); // s[i - 1] 的後綴終點位置
```

pos[0] = 1;

SAM sam:

```
for (int i = 0; i < n; i++) {
   pos[i + 1] = sam.extend(pos[i], s[i] - 'a');</pre>
}
```

5.8 Palindrome Tree [bb3923]

```
struct PAM {
     static constexpr int ALPHABET_SIZE = 26;
     struct Node {
          int len;
int fail;
          int cnt;
          array<int, ALPHABET_SIZE> next;
Node() : len{}, fail{}, next{} {}
     };
// 0 -> even root, 1 -> odd root
     vector < Node > t;
PAM(const vector < int > &s) { init(s); }
     int newNode() {
          t.emplace_back();
          return t.size() - 1;
     void init(const vector<int> &s) {
          t.assign(2, Node());
t[0].len = 0;
          t[1].len = -1;
t[0].fail = 1;
          if (!t[p].next[s[i]])
                    int idx = newNode();
t[idx].len = t[p].len + 2;
                    int now = t[p].fail;
while (s[i - t[now].len - 1] != s[i]) {
    now = t[now].fail;
                    t[idx].fail = t[now].next[s[i]];
t[p].next[s[i]] = idx;
               p = t[p].next[s[i]];
               t[p].cnt++;
     void build_cnt() {
    for (int i = t.size() - 1; i > 1; i--) {
               t[t[i].fail].cnt += t[i].cnt;
```

5.9 Duval [f9dcca]

```
// duval_algorithm
// 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
vector<string> duval(string s) {
     int i = 0, n = s.size();
vector<string> res;
     while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
      else k++;</pre>
               j++;
          while (i <= k) {
               res.push_back(s.substr(i, j - k));
               i += j - k;
         }
     return res:
// 最小旋轉字串
string min_round(string s) {
     s += s;
int i = 0, n = s.size();
     int start = i;
     while (i < n / 2) {</pre>
         else k++;
          while (i <= k) {
    i += j - k;</pre>
     return s.substr(start, n / 2);
}
```

Math 6

6.1 Modulo [80b974]

```
template < class T>
constexpr T power(T a, ll b) {
```

```
res {1};
      for (; b; b /= 2, a *= a)

if (b % 2) res *= a;
      return res:
constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
    res %= p;
    if (res < 0) res += p;</pre>
      return res;
template < ll P>
struct MInt {
    ll x;
      constexpr MInt() : x {0} {}
constexpr MInt(ll x) : x {norm(x % getMod())} {}
static ll Mod;
      constexpr static ll getMod() {
  if (P > 0) return P;
  else return Mod;
      constexpr static void setMod(ll Mod_) {
           Mod = Mod_;
      constexpr ll norm(ll x) const {
           if (x < 0) x += getMod();
if (x >= getMod()) x -= getMod();
           return x;
      constexpr MInt operator-() const {
           MInt res:
           res.x = norm(getMod() - x);
           return res;
      constexpr MInt inv() const {
           return power(*this, getMod() - 2);
      constexpr MInt &operator*=(MInt rhs) & {
           if (getMod() < (1ULL << 31))
                x = x * rhs.x % int(getMod());
           } else {
               x = mul(x, rhs.x, getMod());
           return *this:
      constexpr MInt &operator+=(MInt rhs) & {
           x = norm(x + rhs.x);
           return *this;
      constexpr MInt &operator -= (MInt rhs) & {
    x = norm(x - rhs.x);
           return *this;
      constexpr MInt &operator/=(MInt rhs) & {
  return *this *= rhs.inv();
      friend constexpr MInt operator*(MInt lhs, MInt rhs) {
   MInt res = lhs; return res *= rhs;
      friend constexpr MInt operator+(MInt lhs, MInt rhs) {
           MInt res = lhs; return res += rhs;
      friend constexpr MInt operator - (MInt lhs, MInt rhs) {
    MInt res = lhs; return res -= rhs;
      friend constexpr MInt operator/(MInt lhs, MInt rhs) {
   MInt res = lhs; return res /= rhs;
           constexpr istream &operator>>(istream &is, MInt &a) {
ll v; is >> v; a = MInt(v); return is;
      friend constexor
             ostream & operator << (ostream &os. const MInt &a) {
           return os << a.x;
      friend constexpr bool operator==(MInt lhs, MInt rhs) {
   return lhs.x == rhs.x;
      friend constexpr bool operator!=(MInt lhs, MInt rhs) {
   return lhs.x != rhs.x;
      friend constexpr bool operator <(MInt lhs, MInt rhs) {
   return lhs.x < rhs.x;</pre>
template<>
ll MInt<0>::Mod = 998244353;
constexpr ll P = 1E9 + 7;
using Z = MInt<P>;
```

6.2 Combination [6aa734]

```
_invfac.resize(m + 1);
```

```
_inv.resize(m + 1);
    for (int i = n + 1; i <= m; i++) {
        _fac[i] = _fac[i - 1] * i;
    }
    _invfac[m] = _fac[m].inv();
    for (int i = m; i > n; i--) {
        _invfac[i - 1] = _invfac[i] * i;
        _inv[i] = _invfac[i] * _fac[i - 1];
    }
    n = m;
}

Z fac(ll m) {
    if (m > n) init(2 * m);
    return _fac[m];
}
Z invfac(ll m) {
    if (m > n) init(2 * m);
    return _invfac[m];
}
Z inv(ll m) {
    if (m > n) init(2 * m);
    return _inv[m];
}
Z inv(ll m) {
    if (m > n) init(2 * m);
    return _inv[m];
}
Z binom(ll n, ll m) {
    if (n < m || m < 0) return 0;
    return fac(n) * invfac(m) * invfac(n - m);
}
Z lucas(ll n, ll m) { // Mod 要在 1E5 左右
    if (m == 0) return 1;
    return binom(n % Z::getMod(), m % Z::getMod())
    * lucas(n / Z::getMod(), m / Z::getMod());
}
} comb; // 注意宣告,若要換模數需重新宣告
```

6.3 Sieve [8a3c1c]

```
| vector < int > prime, minp;
void sieve(int n) {
    minp.assign(n + 1, 1); // 1 代表是質數,非 1 不是
    minp[0] = minp[1] = -1;
    int m = int(sqrt(n)) + 1;
    for (int i = 2; i <= m; i++) {
        if (minp[i] == 1) {
            prime.push_back(i);
            for (int j = 2; i * j <= n; j++) {
                minp[i * j] = i;
            }
        }
    }
}

// a ^ (m-1) = 1 (Mod m)
// a ^ (m-2) = 1/a (Mod m)
// Exp2: cout << power(x, power(y, p, Mod - 1), Mod)
// Num = (x+1) * (y+1) * (z+1)...
// Sum = (a^0 + a^1+...+a^xx) * (b^0 + ...+b^y)
// Mul = N * (x+1) * (y+1) * (z+1) / 2
```

6.4 CRT [d41d8c]

```
ll exgcd(ll a, ll b, ll &x, ll &y) {
    if (!b) {
        x = 1, y = 0;
        return a;
    }
    ll g = exgcd(b, a % b, y, x);
    y -= a / b * x;
    return g;
}
ll inv(ll x, ll m){
    ll a, b;
    exgcd(x, m, a, b);
    a %= m;
    if (a < 0) a += m;
    return a;
}
// remain, mod
ll CRT(vector<pair<ll, ll>> &a){
    ll prod = 1;
    for (auto x : a) {
        prod *= x.second;
    }
    ll res = 0;
    for (auto x : a) {
        auto t = prod / x.second;
        res += x.first * t % prod * inv(t, x.second) % prod;
    if(res >= prod) res -= prod;
}
return res;
}
```

6.5 Matrix [bec759]

6.6 Integer Partition [595ed2]

6.7 Mobius Theorem

- 數論 分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理 出 \mathbf{f} 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n}\!\!\mu(d)\!=\!\begin{cases} 1 & \text{for } n\!=\!1\\ 0 & \text{for } n\!\neq\!0 \end{cases}$$

2. μ是常數函數1的反元素

 $\Rightarrow \mu * 1 = \epsilon$, $\epsilon(n)$ 只在n = 1時為 1 , 其餘情況皆為 0 。

- φ歐拉函數: x 以下與 x 互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^i) \\ &= 1 + p^0(p-1) + p^1(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^c \\ &= id \end{split}$$

- 莫比烏斯反演公式
 - $f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$
 - $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

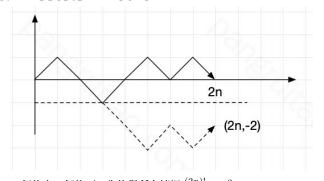
例子

$$\begin{split} &\sum_{i=a}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{x} [d|i] \sum_{j=1}^{y} [d|j] \text{ d 可整除 i 時為 1} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.8 Mobius Inverse [d41d8c]

```
const int maxn = 2e5:
 ll mobius_pref[maxn];
 void init() {
                     mobius_pref[1] = 1;
vector<ll> wei
                      (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
    }
                                                                  continue; // 包含平方
                                            if (wei[i] == 0) {
    wei[i] = 1;
                                                                  }
                                           mobius_pref[i]
                                                                      = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
                     }
void solve() {
                   a solve() {
    ll a, b, c, d, k; cin >> a >> b >> c >> d >> k;
    auto cal = [&](ll x, ll y) -> int {
        int res = 0;
        for (int l = 1, r; l <= min(x, y); l = r + 1) {
            r = min(x / (x / l), y / (y / l));
            res += (mobius_pref[r] - mobius_pref[l] - mobius_p
                                                                                               - 1]) * (x / l) * (y / l); // 代推出來的式子
                                            return res;
                     cout << cal
                                               (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k, (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n";
}
```

6.9 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2)

假設往上有 x 個,往下有 y 個,會有:

$$\begin{cases} x+y=2n \\ y-x=2 \end{cases} \Rightarrow \begin{cases} x=n-1 \\ y=n+1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.10 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- · G:各種翻轉操作所構成的置換群
- X/G: 本質不同的方案的集合 X/G: 對於某一種操作 g, 所有方案中, 經過 g 這種翻轉後保持不變的方案 的集合
- 集合取絕對值代表集合數

Search and Gready

Binary Search [d41d8c]

```
int main() {
          二分找上界
     while (lo < hi) {
   int x = (lo + hi + 1) / 2;
   if (check(x)) lo = x;</pre>
           else hi = x - 1;
      cout << lo; // 保證有解
     while (lo <= hi) {
   int x = (lo + hi) / 2;
   if (check(x)) lo = x + 1;
}</pre>
           else hi = x - 1;
      cout << hi; // 範圍外代表無解
         二分找下界
      cout << lo; // 保證有解
      while (lo <= hi) {
   int x = (lo + hi) / 2;</pre>
           if (check(m)) hi = x - 1;
           else lo = x + 1;
      cout << lo; // 範圍外代表無解
}
```

7.2 Ternary Search [d41d8c]

```
int main() {
     int lo = 0, hi = 10;
     while (lo <= hi) {</pre>
          int xl = lo + (hi - lo) / 3;
int xr = hi - (hi - lo) / 3;
          int ansl = check(xl), ansr = check(xr);
if (ansl < ansr) {</pre>
                 lo = xl + 1;
          } else {
    hi = xr - 1;
           // record ans and index
     }
```

Tree 8

8.1 LCA [f45014]

```
vector<vector<int>> par;
vector<int> dep;
void build(int n, vector<vector<int>> &tree, int u = 0) {
       par.assign(n, vector<int>(B + 1, -1));
dep.assign(n, 0);
auto dfs = [&](auto self, int x, int p) -> void {
              for (auto y : tree[x]) {
    if (y == p) continue;
    par[y][0] = x; // 2 ^ 0
    dep[y] = dep[x] + 1;
    self(self, y, x);
}
             }
       par[u][0] = u; dfs(dfs, 0, -1);
       for (int i = 1; i <= B; i++) {
    for (int j = 0; j < n; j++) {
        par[j][i] = par[par[j][i - 1]][i - 1];</pre>
      }
a = par[a][i];
       for (int i = B; i >= 0; i--) {
   if (par[a][i] != par[b][i]) {
      a = par[a][i], b = par[b][i];
}
       }
```

```
return par[a][0];
}
int jump(int x, int k) {
    for (int i = B; i >= 0; i--) {
        if (k >> i & 1) {
            x = par[x][i];
        }
    return x;
}
```

8.2 Centroid Decomposition [ec760b]

```
#include <bits/stdc++.h>
 using namespace std;
struct CenDecom {
          int n;
           vector < int >> adj;
          vector <book control
vector <book control
vector <book control
vector <int> siz;

CenDecom(int n_ = 0) { init(n_); }
void init(int n_) {
                   n = n_;
adj.assign(n, {});
vis.assign(n, false);
siz.assign(n, 1);
          void addEdge(int u, int v) {
   adj[u].push_back(v);
                    adj[v].push_back(u);
           void get_siz(int x, int p = -1) {
                    siz[x] = 1;
for (int y : adj[x]) {
   if (y == p || vis[y]) continue;
    get_siz(y, x);
   siz[x] += siz[y];
          int get_cen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz) {
            return get_cen(y, sz, x);
        }
}
                    return x;
           void get_ans(int x, int p) {
                    fget_ans(tht x, tht p) {
    // do something
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        get_ans(y, x);
}
          void work(int x = 0) {
   get_siz(0, x);
   int cen = get_cen(x, siz[x]);
   vis[cen] = true;
   for (int y : adj[cen]) {
        if (vis[y]) continue;
        cet_ass(x, cen);
   }
}
                              get_ans(y, cen);
                    for (int y : adj[cen]) {
                              if (vis[y]) continue;
                              work(y);
};
```

8.3 Tree Flattening [5293b7]

8.4 Heavy Light Decomposition [325476]

```
vector<int> siz, top, dep, parent, in, out, seq;
vector < vector < int >> adj;
HLD(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_; cur = 0;
      siz.resize(n); top.resize(n); dep.resize(n);
parent.resize(n); in.resize(n); out.resize(n);
seq.resize(n); adj.assign(n, {});
void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
void work(int rt = 0) {
      top[rt] = rt;
dep[rt] = 0;
parent[rt] = -1;
dfs1(rt); dfs2(rt);
void dfs1(int u) {
   if (parent[u] != -1)
      adj[u].erase(find
                     (adj[u].begin(), adj[u].end(), parent[u]));
      siz[u] = \dot{1};
       for (auto &v : adj[u]) {
             parent[v] = u, dep[v] = dep[u] + 1;
             dfs1(v);
siz[u] += siz[v];
             if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
             } // 讓 adj[u][0] 是重子節點
      }
void dfs2(int u) {
      in[u] = cur++;
      seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
   top[v] = v == adj[u][0] ? top[u] : v;
      out[u] = cur;
int lca(int u, int v) {
    while (top[u] != top[v]) {
        if (dep[top[u]] > dep[top[v]]) {
                    u = parent[top[u]];
             } else {
                    v = parent[top[v]];
      return dep[u] < dep[v] ? u : v;</pre>
int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
int jump(int u, int k) {
   if (dep[u] < k) return -1;
   int d = dep[u] - k;</pre>
       while (dep[top[u]] > d)
      u = parent[top[u]];
return seq[in[u] - dep[u] + d];
bool isAncester(int u, int v) {
    return in[u] <= in[v] && in[v] < out[u];</pre>
int rootedParent(int rt, int v) {
      swap(rt, v);
if (rt == v) return rt;
if (!isAncester(rt, v)) return parent[rt];
      auto it = upper_bound(adj[
    rt].begin(), adj[rt].end(), v, [&](int x, int y) {
    return in[x] < in[y];</pre>
      }) - 1;
return *it;
int rootedSize(int rt, int v) {
```

```
if (rt == v) return n;
if (!isAncester(v, rt)) return siz[v];
            return n - siz[rootedParent(rt, v)];
      int rootedLca(int a, int b, int rt) {
    return lca(a, b) ^ lca(b, rt) ^ lca(rt, a);
};
```

8.5 Link Cut Tree [d69ee0]

```
template < class Info, class Tag>
 struct Node {
     Node *ch[2], *p;
bool rev = false; int size = 1;
     Info info = Info(); Tag tag = Tag();
     Node() : ch{nullptr, nullptr}, p(nullptr) {}
     bool isrt() {
          return !p || (p->ch[0] != this && p->ch[1] != this);
     void make_rev() {
    swap(ch[0], ch[1]);
          rev ^= true;
     void apply(const Tag &v) {
          info.apply(size, v);
          tag.apply(v);
     void push() {
          if (rev)
               if (ch[0]) ch[0]->make_rev();
if (ch[1]) ch[1]->make_rev();
rev = false;
          if (ch[0]) ch[0]->apply(tag);
          if (ch[1]) ch[1]->apply(tag);
          tag = Tag();
     void pull() {
          int pos() {
          return p->ch[1] == this;
     void pushAll() {
   if (!isrt())
              p->pushAll();
          push();
     void rotate() {
          Node *q = p;
int x = !pos();
          q->ch[!x] = ch[x];
if (ch[x]) ch[x]->p = q;
          if (!q->isrt()) q->p->ch[q->pos()] = this;
          ch[x] = q;
q->p = this;
          q->pull();
     void splay() {
          pushAll();
          while (!isrt()) {
    if (!p->isrt()) {
        if (pos() == p->pos()) {
                    p->rotate();
} else {
                         rotate();
                    }
               rotate();
          pull();
     void access() { // access 後自動 splay
          for (Node
                 *i = this, *q = nullptr; i; q = i, i = i->p) {
               i->splay();
i->ch[1] = q;
               i->pull();
          splay();
     void makeRoot() {
          access();
          make_rev();
     Node* findRoot() {
          access();
Node *t = this;
while (t->ch[0]) {
    t->push();
    t = t->ch[0];
          t->access();
          return t:
};
```

```
template < class Info, class Tag>
bool connected(Node < Info, Tag> *x, Node < Info, Tag> *y) {
    return x -> findRoot() == y -> findRoot();
 template < class Info, class Tag>
 bool neighber(Node<Info, Tag> *x, Node<Info, Tag> *y) {
      x->makeRoot();
      y->access();
if (y->ch[0] != x || x->ch[1]) return false;
       return true:
 template < class Info, class Tag>
void split(Node < Info, Tag> *rt, Node < Info, Tag> *y) {
    y->makeRoot();
       rt->access():
 template < class Info, class Tag>
void link(Node < Info, Tag> *t, Node < Info, Tag> *p) {
       t->makeRoot();
       if (p->findRoot() != t) {
            t \rightarrow p = p;
 template < class Info, class Tag>
bool cut(Node < Info, Tag> *x, Node < Info, Tag> *y) {
      x->makeRoot();
      y->access();
if (y->ch[0] != x || x->ch[1]) return false;
y->ch[0] = y->ch[0]->p = nullptr;
       x->pull();
      v->pull():
 remplate < class Info, class Tag>
void modify(Node < Info, Tag> *x, const Info &v) {
     x->access();
      x - sinfo = v:
 template < class Info, class Tag>
 void path_apply
       (Node<Info, Tag> *x, Node<Info, Tag> *y, const Tag &v) {
       assert(connected(x, y));
      split(x, y);
x->apply(v);
 Info path_query(Node<Info, Tag> *x, Node<Info, Tag> *y) {
    assert(connected(x, y));
      split(x, y);
return x->info;
 }
 constexpr int Mod = 51061;
struct Tag {
    ll add = 0; ll mul = 1;
       void apply(const Tag& v) {
    mul = mul * v.mul % Mod;
    add = (add * v.mul % Mod + v.add) % Mod;
      }
};
       void pull(const Info &l, const Info &r) {
   sum = (l.sum + r.sum + val) % Mod;
 using lct = Node<Info, Tag>;
 8.6 Virtual Tree [622e69]
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
// 可以建立虚樹達成快速樹 DP
 // 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector <int>stk(maxn);
```

```
vt[l].push_back(stk[top]);
stk[top] = l;
} else vt[l].push_back(stk[top--]);
      stk[++top] = u;
void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
    vt[u].clear();
void solve(int n, int q) {
      vector g(n + 1, vector<pair<int, int>>());
      vector vt(n + 1, vector vector vt(n + 1, vector <int>()); // dfs 完清除, 否則會退化
vector <ll> dp(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;

            g[u].push_back({v, w});
            g[v].push_back({u, w});
```

```
build_lca(n, g);
build(n, g);
for (int i = 0; i < q; i++) {
   int m; top = -1; cin >> m;
     vector <int > key(m);
for (int j = 0; j < m; j++) {
    cin >> key[j];
           iskey[key[j]] = 1;
     }
     key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
     for (int x : key) insert(x, vt);
     // DP
     auto dfs = [&](auto self, int u) -> void {
    for (auto v : vt[u]) {
        self(self, v);
}
                if (iskey[v]) {
    dp[u] += min_dis[v];
                      // 砍掉 1 到 v 之間最短的路
                     dp[u] += min(dp[v], min_dis[v]);
                iskey[v] = dp[v] = 0;
           vt[u].clear();
     dfs(dfs, key[0]); // key[0] 一定是 root cout << dp[key[0]] << "\n";
     iskey[key[0]] = dp[key[0]] = 0;
```

8.7 Dominator Tree [baa540]

```
struct Dominator_tree {
       int n, id;
vector<vector<int>> adj, radj, bucket;
vector<int> sdom, dom, vis, rev, pa, rt, mn, res;
Dominator_tree(int n_ = 0) { init(n_); }
       void init(int _n) {
    n = _n, id = 0;
    adj.assign(n, vector<int>());
    radj.assign(n, vector<int>());
    bucket.assign(n, vector<int>());
    sdom.resize(n); dom.assign(n, -1);
    vis.assign(n, -1); cov.resize(n);
               vis.assign(n, -1); rev.resize(n);
pa.resize(n); rt.resize(n);
                mn.resize(n); res.resize(n);
       void add_edge(int u, int v) { adj[u].push_back(v); }
int query(int v, int x) {
   if (rt[v] == v) return x ? -1 : v;
               int p = query(rt[v], 1);
if (p == -1) return x ? rt[v] : mn[v];
if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
               rt[v] = p;
return x ? p : mn[v];
        radj[vis[u]].push_back(vis[v]);
        void build(int s) {
               sdom[u] = min(sdom[i], sdom[quer]
if (i) bucket[sdom[i]].push_back(i);
for (int u : bucket[i]) {
   int p = query(u, 0);
   dom[u] = sdom[p] == i ? i : p;
                       if (i) rt[i] = pa[i];
               res.assign(n, -1);
for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];
for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre>
                for (int i = 0; i < n; i++) dom[i] = res[i];</pre>
};
```

9 DP

9.1 LCS [5781cf]

```
int main() {
   int m, n; cin >> m >> n;
   string s1, s2; cin >> s1 >> s2;
   int L = 0;
```

```
vector < vector < int >> dp(m + 1, vector < int >(n + 1, 0));
for (int i = 1; i <= m; i++) {
    for (int j = 1; j <= n; j++) {
        if (s1[i - 1] == s2[j - 1])
            dp[i][j] = dp[i - 1][j] - 1] + 1;
    else
            dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
    }
}
int length = dp[m][n]; cout << length << "\n";
string s(length, 'c'); // backtracking
while (m >= 1 && n >= 1) {
    if (s1[m - 1] == s2[n - 1]) {
        s[length - 1] = s1[m - 1];
        m--, n--, length--;
    }
else {
        if (dp[m - 1][n] > dp[m][n - 1]) m--;
        else n--;
    }
}
cout << s << "\n";
}</pre>
```

9.2 LIS [66d09f]

9.3 Edit Distance [308023]

9.4 Bitmask [a626f9]

```
National Chung Cheng University Salmon
      cout << dp[n - 1][findBit(n) - 1] << "\n";
     void elevatorRides() {
                                                                                                }
                                                                                           swap(dp[0], dp[1]);
                                                                                      cout << dp[0][k] << "\n";
               9.8 SOS [93cb19]
          }
     cout << dp[findBit(n) - 1][0] << "\n";
                                                                                  void solve() {
                                                                                      int n; cin >> n; Z ans = 0;
vector <int > a(n);
 9.5 Projects [0942aa]
                                                                                      for (int i = 0; i < n; i++)
    cin >> a[i];
 int main() { // 排程有權重問題,輸出價值最多且時間最少
     int from, to, w, id;
bool operator<(const E &rhs) {</pre>
                                                                                      vector < Z > dp(1 << m);
for (int i = 0; i < n; i++)
          return to == rhs.to ? w > rhs.w : to < rhs.to;
      int n; cin >> n; vector<E> a(n + 1);
for (int i = 1; i <= n; i++) {
   int u, v, w; cin >> u >> v >> w;
           a[i] = \{u, v, w, i\};
      vector<array<ll, 2>> dp(n + 1); // w, time
      vector<array<int, 2>> rec(n + 1); // 有沒選, 上個是誰
      sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
    auto it = --lower_bound(all(a), E({0, a[i].from}),</pre>
          auto tt = --lower_bound(at(a), E({0, a[t].from})),
[](E x, E y){ return x.to < y.to; });
int id = it - a.begin(); dp[i] = dp[i - 1];
ll nw = dp[id][0] + a[i].w;
ll nt = dp[id][1] + a[i].to - a[i].from;
if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
    dp[i] = {nw, nt}; rec[i] = {1, id};
}
                                                                                      cout << ans << "\n":
                                                                                 9.9 CHT [5f5c25]
                                                                                 struct Line {
                                                                                      ll m, b;
     ans.push_back(a[i].id);
               i = rec[i][1];
                                                                                 };
          } else i--;
     }
}
                                                                                           init(n_, init_);
 9.6 Removal Game [7bb56b]
                                                                                      void init(int n
| // 兩個人比賽,每個人輪流取一個數字且只能是頭尾
int n; cin >> n; vector<ll> a(n);
      for (int i = 0; i < n; i++) cin >> a[i];
      vector dp(n, vector<ll>(n)); // i 到 j 區間的最大 diff
for (int i = n - 1; i >= 0; i--) {
    dp[i][i] = a[i];
          for (int j = i + 1; j < n; j++)
    dp[i][j] =</pre>
                     max(a[i] - dp[i + 1][j], a[j] - dp[i][j - 1]);
                                                                                           // 本題斜率遞減、上凸包
                                                                                           // 因此只要 12 跟
      \frac{1}{x} + y = sum; // x - y = dp[0][n - 1]
      cout << (accumulate
           (a.begin(), a.end(), 0LL) + dp[0][n - 1]) / 2 << "\n";
```

9.7 Monotonic Queue [f4976d]

```
| // 應用: dp(i) = h(i) + max(A(j)), for l(i)≤j≤r(i)
| // A(j) 可能包含 dp(j), h(i) 可 O(1)
void Bounded_Knapsack() {
    int n, k; // O(nk)
    vector <int> w(n), v(n), num(n); deque <int> q;
| // 於是我們將同餘的數分在同一組
| // 每次取出連續 num[i] 格中最大值
| // g_x = max(-{k=0}^num[i] (g'_{x-k} + v_i*k))
| // G_x = g'_{x} - v_i*x
| // x 代 x · k => v_i*(x · k)
| // g_x = max(-{k=0}^num[i] (G_{x-k} + v_i*x))
```

```
vector<vector<ll>> dp(2, vector<ll>(k + 1));
for (int i = 0; i < n; i++) {
          for (int r = 0; r < w[i]; r++) { // 餘數
               q.clear(); // q 記錄在 x = i 時的 dp 有單調性
for (int x = 0; x * w[i] + r <= k; x++) {
    while (!q.empty() && q.front() < x - num[i])
                   q.pop_back();
                   | // 使用情況: 跟 bit 與(被)包含有關, 且 x 在 1e6 左右
| // 題目: 一數組, 問有多少所有數 & 起來為 Ø 的集合數
| // dp[x]代表包含 x 的 y 個數(比x大且bit 1全包含 x 的有幾個)
 // 答案應該包含在 dp[0]内,但是有重複元素,所以考慮容斥
// => ans = \sum _{i=0}^{n} (-1)^{pop_count(i)} 2^{dp[i]-1}
// => 全部為0的個數 - 至少一個為1的個數 + 至少兩個為1的個數
      int m = __lg(*max_element(a.begin(), a.end())) + 1;
      // 定義 dp[mask] 為 mask 被包含於 a[i] 的 a[i] 個數
      dp[pre] += dp[mask];
      for (int mask = 0; mask < 1 << m; mask++) {
   int sgn = __builtin_popcount(mask) & 1 ? -1 : 1
   ans += sgn * (power(Z(2), dp[mask].val()) - 1);</pre>
| / / 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \le r(i)
 // A(j), B(j) 可能包含 dp(j), 分別就是 m 跟 b
      Line(ll m = 0, ll b = 0) : m(m), b(b) {}
ll eval(ll x) {
    return m * x + b;
  struct CHT { // 用在查詢單調斜率也單調
      int n, lptr, rptr; vector<Line> hull;
CHT(int n_ = 0, Line init_ = Line()) {
                         = 0, Line init_ = Line()) {
          n = n_; hull.resize(n); reset(init_);
      void reset(Line init_ = Line()) {
   lptr = rptr = 0; hull[0] = init_;
      bool pop_front(Line &l1, Line &l2, ll x) {
          // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y
           // 代表查詢的當下,右線段的高度已經低於左線段了
           return l1.eval(x) >= l2.eval(x);
      bool pop back(Line &l1, Line &l2, Line &l3) {
                 l3 的 X 交點 <= l1 跟 l3 的 X 交點,l2 就用不到了
          return (l3.b - l2.b)
  * (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);</pre>
      void insert(Line L) {
           while (rptr - lptr
                > 0 && pop_back(hull[rptr - 1], hull[rptr], L))
          hull[++rptr] = L;
      while (rptr - lptr
> 0 && pop_front(hull[lptr], hull[lptr + 1], x))
```

return hull[lptr].eval(x);

};

9.10 DNC [61c639]

9.11 LiChao Segment Tree [f23ef4]

```
// m = dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for <math>j \le r(i)
constexpr ll inf = 4e18;
struct Line {
    ll m, b;
    Line(ll m = 0, ll b = inf) : m(m), b(b) {}
      ll eval(ll x) const { return m * x + b; }
struct LiChaoSeg { // 取 max 再變換就好
     int n;
vector <Line > info;
      LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_) {
           n = n_{j}
            info.assign(4 << __lg(n), Line());</pre>
     void update(Line line, int node, int l, int r) {
   int m = (l + r) / 2;
   bool left = line.eval(l) < info[node].eval(l);
   bool mid = line.eval(m) < info[node].eval(m);</pre>
           if (mid) swap(info[node], line); // 如果新線段比較好if (r - l == 1) return; else if (left != mid) update(line, 2 * node, l, m);
            // 代表左半有交點
            else update(line, 2 * node + 1, m, r);
            // 代表如果有交點一定在右半
     void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
   if (r - l == 1) return info[node].eval(x);
            int m = (l + r) / 2;
           if (x < m) return</pre>
                  min(info[node].eval(x), query(x, 2 * node, l, m));
                  info[node].eval(x), query(x, 2 * node + 1, m, r));
     il query(int x) { return query(x, 1, 0, n); }
```

9.12 Codeforces Example [7d37ea]

```
| // CF 1932 pF
| // 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
| // 請問在線段不重複的情況下,最多獲得幾分
int main() {
    int n, m;
    cin >> n >> m;
| // 記錄每點有幾個線段
| // 再一個紀錄,包含這個點的左界
    vector<int> l_side(n + 1, inf), cnt(n + 5, 0);
    for (int i = 0; i < m; i++) {
        int l, r; cin >> l >> r;
        l_side[r] = min(l_side[r], l);
        cnt[l]++;
        cnt[r + 1]--;
}
for (int i = 2; i <= n; i++) {
        cnt[i] += cnt[i - 1];
}
for (int i = n; i >= 2; i--) {
        l_side[i - 1] = min(l_side[i - 1], l_side[i]);
}
vector<int> dp(n + 1);
```

```
dp[0] = 0;
for (int i = 1; i <= n; i++) {
    dp[i] = cnt[i];
    if (l_side[i] != inf) {
        dp[i] += dp[l_side[i] - 1];
    }
}</pre>
            dp[i] = max(dp[i], dp[i - 1]);
      cout << dp[n] << "\n";
}
// CF 1935 DC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
// 再加上 max(bi) - min(bi)
int main(){
      int n, k, ans = 0; cin >> n >> k;
vector <pii> v(n + 1);
for (int i = 1; i <= n; i++) {</pre>
            int a, b; cin >> a >> b;
            v[i] = {a, b};
if (a <= k) ans = 1;
      sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
      for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
                  // min(不選, 選)
                  if (dp[i
                        - 1][j - 1] + v[i].first + v[i].second <= k) {
// 假如可以選,更新 ans 時再加回去 bi
                        ans = max(ans, j);
            dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
      cout << ans << endl;
```

10 Geometry 10.1 Basic [d41d8c]

```
template < class T >
struct Point {
     Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) \{ \}
     template < class U>
     operator Point<U>() {
          return Point < U > (U(x), U(y));
     Point &operator+=(const Point &p) & {
    x += p.x; y += p.y; return *this;
     Point &operator -= (const Point &p) & {
    x -= p.x; y -= p.y; return *this;
     Point &operator*=(const T &v) & {
    x *= v; y *= v; return *this;
     Point &operator/=(const T &v) & {
    x /= v; y /= v; return *this;
     Point operator -() const {
    return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
   return a += b;
     friend Point operator - (Point a, const Point &b) {
          return a -= b;
     friend Point operator*(Point a, const T &b) {
   return a *= b;
     friend Point operator/(Point a, const T &b) {
          return a /= b;
     friend Point operator*(const T &a, Point b) {
          return b *= a;
     friend bool operator==(const Point &a, const Point &b) {
           return a.x == b.x && a.y == b.y;
     friend istream & operator >> (istream & is. Point &p) {
           return is >> p.x >> p.y;
     friend ostream &operator << (ostream &os, const Point &p) {
   return os << "(" << p.x << ", " << p.y << ")";</pre>
     }
template < class T>
struct Line {
     Point<T> a;
     Point <T > b;
     Line(const Point<T> &a_ = Point<T>()
```

, const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}

```
template < class T>
template < class T>
T cross(const Point < T > &a, const Point < T > &b) {
    return a.x * b.y - a.y * b.x;
template < class T>
T square(const Point < T > &p) {
      return dot(p, p);
template < class T>
double length(const Point<T> &p) {
     return sqrt(double(square(p)));
template < class T >
double length(const Line < T > &l) {
     return length(l.a - l.b);
template < class T>
Point<T> normalize(const Point<T> &p) {
     return p / length(p);
bool parallel(const Line<T> &11, const Line<T> &12) {
    return cross(l1.b - l1.a, l2.b - l2.a) == θ;
template < class T >
double distance(const Point < T > &a, const Point < T > &b) {
     return length(a - b);
template < class Ta
double distancePL(const Point<T> &p, const Line<T> &l) {
     return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)
    return distance(p, l.a);</pre>
     if (dot(p - l.b, l.a - l.b) < 0)
  return distance(p, l.b);
return distancePL(p, l);</pre>
template < class T>
Point<T> rotate(const Point<T> &a) {
    return Point(-a.y, a.x);
template < class T >
int sgn(const Point < T > & a) {
   return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
     return cross(l.b - l.a, p - l.a) > 0;
template < class T>
template<class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
   return cross(p - l.a, l.b - l.a) == 0 &&
        min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)</pre>
                  (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
     pointInFolygon
(const Point<T> &a, const vector<Point<T>> &p) {
  int n = p.size(), t = 0;
  for (int i = 0; i < n; i++) {
    if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {</pre>
                 return true:
     }
for (int i = 0; i < n; i++) {
    auto u = p[i];
    r(z + 4) & n];</pre>
           auto v = p[(i + 1) % n];
if (u.x < a.</pre>
                 x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
           if (u.x >= a
                  .x && v.x < a.x && pointOnLineLeft(a, Line(u, v)))</pre>
     return t == 1:
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
 // 3 : intersect at endpoint
template < class T>
if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
    return {0, Point<T>(), Point<T>()};
if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
           return {0, Point<T>(), Point<T>()};
```

```
if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y))
    return {0, Point<T>(), Point<T>()};
if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y))
    return {0, Point<T>(), Point<T>()};
if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
             if (cross(l1.b - l1.a, l2.a - l1.a) !=
    return {0, Point<T>(), Point<T>()};
                                                                                0) {
             } else {
                     auto maxx1 = max(l1.a.x, l1.b.x);
                    auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
auto miny1 = min(l1.a.y, l1.b.y);
                    auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.y, l2.b.y);
                     auto miny2 = min(l2.a.y, l2.b.y);
                    Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
if (!pointOnSegment(p1, l1))
                    swap(p1.y, p2.y);
if (p1 == p2) {
    return {3, p1, p2};
                    } else {
    return {2, p1, p2};
             }
       }
       auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
       Point p = lineIntersection(l1, l2);
       if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
              return {1, p, p};
       } else {
             return {3, p, p};
template < class T>
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
   if (get<0>(segmentIntersection(l1, l2)) != 0)
              return 0.0;
       return min({distancePS(l1.a, l2), distancePS(l1
    .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
template < class T>
bool segmentInPolygon
        (const Line<T> &l, const vector<Point<T>> &p) {
       int n = p.size();
      int n = p.size();
if (!pointInPolygon(l.a, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
for (int i = 0; i < n; i++) {
    auto u = p[i];
    auto v = p[(i + 1) % n];
    auto w = p[(i + 2) % n];
    auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
    if (t == 1) return false;
    if (t == 0) continue;
    if (t == 0) f</pre>
              if (t == 2) {
                     if (pointOnSegment(v, l) && v != l.a && v != l.b)
   if (cross(v - u, w - v) > 0)
      return false;
             || pointOnLineLeft(l.b, Line(v, u)))
                    return false;
} else if (p1 == v) {
    if (l.a == v) {
        if (pointOnLineLeft(u, l)) {
            if (pointOnLineLeft(w, l)) }
                                                && pointOnLineLeft(w, Line(u, v)))
                                                return false;
                                  } else if (l.b == v) {
                                  if (pointOnLineLeft(u, Line(l.b, l.a))) {
   if (pointOnLineLeft(w, Line(l.b, l.a))
   && pointOnLineLeft(w, Line(u, v)))
                                                return false:
                                         if (pointOnLineLeft(w, Line(l.b, l.a))
                                                || pointOnLineLeft(w, Line(u, v)))
                                                return false:
                           return false;
                                 }
                           }
```

```
}
     return true:
vector<Point<T>> hp(vector<Line<T>> lines) {
     sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
   auto d1 = l1.b - l1.a;
   auto d2 = l2.b - l2.a;
           if (sgn(d1) != sgn(d2))
return sgn(d1) == 1
           return cross(d1, d2) > 0;
     deque < Line < T >> ls:
     deque<Point<T>> ps;
for (auto l : lines) {
    if (ls.empty()) {
                ls.push_back(l);
                continue:
           while (!ps.empty() && !pointOnLineLeft(ps.back(), l))
    ps.pop_back(), ls.pop_back();
while (!ps.empty() && !pointOnLineLeft(ps[0], l))
                ps.pop_front(), ls.pop_front();
           if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
                if (dot
                       (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                      if (!pointOnLineLeft(ls.back().a, l)) {
                           assert(ls.size() == 1);
                           ls[0] = l;
                      continue;
                return {}:
           ps.push_back(lineIntersection(ls.back(), l));
ls.push_back(l);
     while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0]))
    ps.pop_back(), ls.pop_back();
if (ls.size() <= 2) return {};</pre>
     ps.push\_back(lineIntersection(ls[\theta], ls.back()));\\
     return vector(ps.begin(), ps.end());
using P = Point<ll>;
10.2 Convex Hull [b5758d]
int main() {
```

```
int n; cin >> n;
vector <P> P(n), U, L;
for (int i = 0; i < n; i++) {
    cin >> P[i];
       sort(P.begin()
             .end(), [](const Point<i64> &a, const Point<i64> &b) {
return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
      for (int i = 0; i < n; i++) {
    while (L.size() >= 2 && cross(L.back() -
        L[L.size() - 2], P[i] - L[L.size() - 2]) <= 0LL) {</pre>
                   L.pop_back();
             while (U.size() >= 2 && cross(U.back()
                     U[U.size() - 2], P[i] - U[U.size() - 2]) >= 0LL){
                   U.pop_back();
             if (L.
                    empty() || !(L.back() == P[i])) L.push_back(P[i]);
             if (U.
                    empty() || !(U.back() == P[i])) U.push_back(P[i]);
      if (L.size() <= 2 && U.size() <= 2) {
             // No Hull
      cout << L.size() + U.size() - 2 << "|n";
for (int i = 0; i < L.size() - 1; i++) {
    cout << L[i].x << " " << L[i].y << "|n";</pre>
      for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << "\n";</pre>
      }
}
```

10.3 Minimum Euclidean Distance [3020bc]

```
template < class T>
T distanceSquare(const Point < T > &a, const Point < T > &b) {
    return square(a - b);
}
void solve() {
    int n; cin >> n;
    constexpr ll inf = 8e18;
    vector < Point < ll >> a(n);
    for (int i = 0; i < n; i++) {
        ll x, y;
        cin >> x >> y;
        a[i] = Point < ll > (x, y);
}
struct sortY {
    bool operator
        ()(const Point < ll > &a, const Point < ll > &b) const {
```

```
return a.y < b.y;</pre>
     }
struct sortXY {
     bool operator
            ()(const Point<ll> &a, const Point<ll> &b) const {
          if (a.x == b.x) return a.y < b.y;
else return a.x < b.x;</pre>
    }
};
sort(a.begin(), a.end(), sortXY());
vector < Point < ll >> t(n);
auto devide = [&](auto &&self, int l, int r) -> ll {
    if (l == r) return inf;
    int m = (l + r) / 2;
}
     ll ans = min(self(self, l, m), self(self, m + 1, r));
     ll midval = a[m].x;
     ll p = 0;
for (int i = l; i <= r; i++) {
    if ((midval - a[i].x) * (midval - a[i].x) <= ans) {</pre>
                t[p++] = a[i];
     t[j].y) * (t[i].y - t[j].y) > ans) break;
          }
     return ans;
cout << devide(devide, 0, n - 1) << "\n";</pre>
```

10.4 Lattice Points [00db9d]

```
int main() {
      // Polygun 內整數點數
      int n; cin >> n;
vector<Point<ll>> polygon(n);
      for (int i = 0; i < n; i++) cin >> polygon[i];
      ll area = 0:
      for (int i = 0; i < n; i++) {</pre>
           area += cross(polygon[i], polygon[(i + 1) % n]);
      area = abs(area);
      auto countBoundaryPoints
             = [](const vector<Point<ll>>& polygon) -> ll {
           ll res = 0;
            int n = polygon.size();
           for (int i = 0; i < n; i++) {
    ll dx = polygon[(i + 1) % n].x - polygon[i].x;
    ll dy = polygon[(i + 1) % n].y - polygon[i].y;</pre>
                 res += std::gcd(abs(dx), abs(dy));
           return res;
      ll res = countBoundaryPoints(polygon);
      ll ans = (area - res + 2) / 2;
cout << ans << " " << res << " | n";</pre>
```

10.5 Minimum Cover Circle [c9ca81]