1.4 Pbds

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Basic 1

4.5

1.1 Install VScode [d41d8c]

```
// 如何安裝 vscode
// 1. 下載 vscode & msys2
// 2. 在跳出的 terminal 中 / 或打開 ucrt64,打上
     "pacman -S --needed base-devel mingw-w64-x86_64-toolchain"
// 3. 環境變數加上 C:\\msys64\\ucrt64\\bin
// 4. 重開 vscode, 載 C/C++, 運行, 編譯器選擇 g++
// 5. 打開 settings -> compiler -> add compilerPath
     -> 在 "" 裡打上 C:\\msys64\\ucrt64\\bin\\g++.exe
```

1.2 Default Code [d41d8c]

```
#include <bits/stdc++.h>
#Include <olis/stdc++.n>
// #pragma GCC target("popcnt")
// C++ 20 vector grammer will not work
using namespace std;
using ll = long long;
void solve() {
}
int main() {
       ios_base::sync_with_stdio(false);
       cin.tie(nullptr);
      int t = 1;
cin >> t;
       while (t--) {
             solve();
```

1.3 Compare Fuction [d41d8c]

```
// 1. sort, 二分搜刻在函式內 lambda 就好
// 2. priority queue 小到大是 >, set 是 <
// 3. set 不能 = , multiset 必須 =
 // 4. 確保每個成員都要比到
// 5. pbds_multiset 不要用 lower_bound
|// 6. 如果要用 find, 插入 inf 後使用 upper_bound
|// 7. multiset 可以跟 set 一樣使用, 但請注意第 3、4 點
```

```
auto cmp = [](int i, int j) { return i > j; };
priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
vector<int> a {1, 2, 5, 4, 3}; // 小心不要改到 a auto cmp = [&a](int i, int j) { return a[i] > a[j]; }; priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
```

1.4 Pbds [d41d8c]

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < class T>
using pbds_set = tree<T, null_type,
    less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template<class T>
using pbds_multiset = tree<T, null_type, less_equal
    <T>, rb_tree_tag, tree_order_statistics_node_update>;
```

1.5 Double [f7a49d]

```
struct D {
     double x;
     constexpr static double eps = 1E-12;
D() : x{0.0} {}
D(double v) : x{v} {}
     double val() const { return x; }
explicit operator double() const { return x; }
D operator -() const {
           return D(-x);
     D & operator += (const D & rhs) & {
           x += rhs.x; return *this;
     D & operator -= (const D & rhs) & {
           x -= rhs.x; return *this;
     D & operator *= (const D & rhs) & {
           x *= rhs.x; return *this;
     D & operator /= (const D & rhs) & {
           assert(fabs(rhs.x) > eps);
x /= rhs.x; return *this;
      friend D operator+(D lhs, const D &rhs) {
           return lhs += rhs;
     friend D operator - (D lhs, const D &rhs) {
    return lhs -= rhs;
      friend D operator*(D lhs, const D &rhs) {
           return lhs *= rhs;
     friend D operator/(D lhs, const D &rhs) {
   return lhs /= rhs;
      friend bool operator < (const D &lhs, const D &rhs) {</pre>
           return lhs.x - rhs.x < -eps;</pre>
      friend bool operator > (const D &lhs, const D &rhs) {
           return lhs.x - rhs.x > eps;
      friend bool operator == (const D &lhs, const D &rhs) {
           return fabs(lhs.x - rhs.x) < eps;</pre>
      friend bool operator <= (const D &lhs, const D &rhs) {</pre>
           return lhs < rhs || lhs == rhs;
      friend bool operator >= (const D &lhs, const D &rhs) {
           return lhs > rhs || lhs == rhs;
     friend bool operator!=(const D &lhs, const D &rhs) {
           return !(lhs == rhs);
     friend istream &operator>>(istream &is, D &a) {
   double v; is >> v; a = D(v); return is;
     friend ostream &operator<<(ostream &os, const D &a) {
    return os << fixed << setprecision(10) << a.val()
    + (a.val() > 0 ? eps : a.val() < 0 ? -eps : 0);
} // eps should < precision</pre>
};
```

1.6 Int128 [9454fa]

```
using i128 = __int128_t; // 1.7E38
using 1128 = __int12o_t; // 1.72.
inline i128 read() {
   i128 sgn = 1, x = 0;
   char c = getchar();
   while (c < '0' || c > '9') {
      if (c == '-') sgn = -1;
      c = otchar();
}
                 c = getchar();
         while (c >= '0' && c <= '9') {
    x = x * 10 + c - '0';
                 c = getchar();
         return x * sgn;
inline void write(i128 x){
    if (x < 0) {</pre>
```

```
putchar('-');
    x = -x;
}
if (x > 9) write(x / 10);
putchar(x % 10 + '0');
}
```

1.7 Rng [401544]

```
mt19937_64 rng
          (chrono::steady_clock::now().time_since_epoch().count());
ll x = rng(); shuffle(a.begin(), a.end(), rng);
```

2 Graph

2.1 DFS And BFS [e2d856]

```
int main() {
       int n;
       vector < int >> adj(n);
       // dfs_graph
vector<bool> vis(n);
auto dfs = [&](auto self, int u) -> void {
            if (vis[u]) return;
vis[u] = true;
for (auto v: adj[u]) {
    self(self, v);
            }
       dfs(dfs, 0);
       vector<int> depth(n, 1e9);
       queue<int> q;
       auto bfs = [&](auto self, int s) -> void {
   vis[s] = true, depth[s] = 0;
             q.push(s);
             while (!q.empty()) {
                   int u = q.front(); q.pop();
for (auto v : adj[u]) {
                         if (vis[v]) continue;
vis[v] = true;
depth[v] = depth[u] + 1;
                         q.push(v);
                   }
             }
      bfs(bfs, 0);
}
```

2.2 Prim [3a3805]

2.3 BellmanFord [430ded]

```
} while (i != t);
reverse(ans.begin(), ans.end());
cout << "YES|n";
for (auto x : ans) cout << x + 1 << " ";</pre>
```

2.4 FloydWarshall [3f61a4]

2.5 Euler [4177dc]

```
/// 1. 無向圖是歐拉圖:
// 非零度頂點是連通的
// 頂點的度數都是偶數
// 2. 無向圖是半歐拉圖(有路沒有環):
// 非零度頂點是連通的
// 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
// 非零度頂點是強連通的
// 每個頂點的入度和出度相等
// 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
// 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
// 其他頂點的入度和出度相等
vector<int> ans;
auto dfs = [&](auto &&self, int u) -> void {
   while (g[u].size()) {
   int v = *g[u].begin();
      q[u].erase(v);
       self(self, v);
    ans.push back(u);
dfs(dfs, 0);
reverse(ans.begin(), ans.end());
```

2.6 DSU [749620]

```
struct DSU {
    int n;
    vector <int > boss, siz;
    DSU() {}
    DSU(int n_) { init(n_); }
    void init(int n_) {
        n = n_; boss.resize(n);
        iota(boss.begin(), boss.end(), 0);
        siz.assign(n, 1);
    }
    int find(int x) {
        if (boss[x] == x) return x;
        return boss[x] = find(boss[x]);
    }
    bool same(int x, int y) {
        return find(x) == find(y);
    }
    bool merge(int x, int y) {
        x = find(x); y = find(y);
        if (x == y) return false;
        if (siz[x] < siz[y]) swap(x, y);
        siz[x] += siz[y];
        boss[y] = x;
        n--;
        return true;
    }
    int size(int x) {
        return siz[find(x)];
    }
};</pre>
```

```
struct DSU {
      int n;
       vector<int> boss, siz, stk;
       DSU() {}
      DSU(int n_) { init(n_); }
       void init(int n_) {
    n = n_;
             boss.resize(n);
             iota(boss.begin(), boss.end(), 0);
siz.assign(n, 1);
             stk.clear();
      int find(int x) {
   return x == boss[x] ? x : find(boss[x]);
      bool same(int x, int y) {
    return find(x) == find(y);
      fool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);
    siz[x] += siz[y];
    boss[y] = x;</pre>
             stk.push_back(y);
             return true;
      void undo(int x) {
    while (stk.size() > x) {
        int y = stk.back();
    }
}
                    stk.pop_back();
                    n++
                    siz[boss[y]] -= siz[y];
                    boss[y] = y;
             }
       int size(int x) {
   return siz[find(x)];
      }
};
2.7 SCC [5d3e16]
```

```
struct SCC {
      int n, cur, cnt;
vector<vector<int>> adj;
vector<int>> stk, dfn, low, bel;
SCC(int n_ = 0) { init(n_); }
void init(int n_) {
            n = n_;
            adj.assign(n, {});
            dfn.assign(n, -1);
low.resize(n);
             bel.assign(n, -1);
             stk.clear();
             cur = cnt = 0;
      void addEdge(int u, int v) {
   adj[u].push_back(v);
      dfs(y);
low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
low[x] = min(low[x], dfn[y]);
                   }
            }
if (dfn[x] == low[x]) {
                   int y;
do {
                         y = stk.back();
                         bel[y] = cnt;
stk.pop_back();
                   } while (y != x);
                   cnt++;
            }
      vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
    }
}</pre>
             return bel;
      struct Graph { // 可能有重邊
            vector<pair<int, int>> edges;
             vector<int> siz:
             vector<int> cnté;
      Graph compress() {
            Graph g;
g.n = cnt;
            g.siz.resize(cnt);
g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {</pre>
                   g.siz[bel[i]]++;
```

```
for (auto j : adj[i]) {
    if (bel[i] != bel[j]) {
                         g.edges.emplace_back(bel[i], bel[j]);
                    } else {
                         g.cnte[bel[i]]++;
               }
           return q;
     }
};
```

2.8 VBCC [170604]

```
struct VBCC {
       int n, cur;
vector<vector<int>> adj;
       vector < vector < int > auj,
vector < int > dfn, low, parent;
vector < bool > is_cut;
VBCC(int n_ = 0) { init(n_); }
void init(int n_) {
               n = n_;
               adj.assign(n, {});
               dfn.assign(n, -1);
low.resize(n);
               parent.assign(n, -1);
               is_cut.assign(n, false);
               cur = 0:
        void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
        void dfs(int x) {
   int children = 0;
               dfn[x] = low[x] = cur++;
for (int v : adj[x]) {
    if (dfn[v] == -1) {
                            `children++;
                             parent[v] = x;
                              dfs(v):
                              low[x] = min(low[x], low[v]);
                             if (parent[x] != -1 && low[v] >= dfn[x]) {
    is_cut[x] = true;
                      } else if (v != parent[x]) {
    low[x] = min(low[x], dfn[v]);
               if (parent[x] == -1 && children > 1) {
                      is_cut[x] = true;
               }
       }
void work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i);
        }
}</pre>
               }
       }
};
```

2.9 EBCC [59d8ca]

```
struct EBCC { // CF/contest/1986/pF
       int n, cur, cnt;
vector<vector<int>> adj;
       vector <victor <int >> adj;
vector <int >> stk, dfn, low, bel;
vector <pair <int, int >> bridges; // 關鍵邊
EBCC(int n_ = 0) { init(n_); }
void init(int n_) {
              n = n:
              adj.assign(n, {});
              dfn.assign(n, -1);
              low.resize(n);
bel.assign(n, -1);
              stk.clear();
              bridges.clear();
              cur = cnt = 0;
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
              stk.push_back(x);
              for (auto y : adj[x]) {
   if (y == p) continue;
   if (dfn[y] == -1) {
                            dfs(y, x);
low[x] = min(low[x], low[y]);
if (low[y] > dfn[x]) {
                                   bridges.emplace_back(x, y);
                     } else if (bel[y] == -1) {
    low[x] = min(low[x], dfn[y]);
              if (dfn[x] == low[x]) {
                     int y;
```

```
y = stk.back();
                    bel[y] = cnt;
stk.pop_back();
while (y != x);
                     cnt++;
             }
       fvector<int> work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
        }
}</pre>
              return bel;
       struct Graph { // 不會有重邊
              int n;
              vector<pair<int, int>> edges;
              vector<int> siz; // BCC 內節點數
              vector<int> cnte; // BCC 內邊數
       Graph compress() {
              Graph g;
g.n = cnt;
              g.siz.resize(cnt);
g.cnte.resize(cnt);
              g.the.restze(cnt),
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;
    for (auto j : adj[i]) {
        if (bel[i] < bel[j]) {</pre>
                            g.edges.emplace_back(bel[i], bel[j]);
} else if (i < j) {</pre>
                                  g.cnte[bel[i]]++;
                            }
                    }
              return g;
      }
};
```

2.10 2-SAT [3f3604]

// CSES Giant Pizza

```
struct TwoSat {
      int n; vector<vector<int>> e;
vector<bool> ans;
      TwoSat(int n) : n(n), e(2 * n), ans(n) {}
void addClause(int u, bool f, int v, bool g) {
    e[2 * u + !f].push_back(2 * v + g);
    e[2 * v + !g].push_back(2 * u + f);
      void ifThen(int u, bool f, int v, bool g) {
            // 必取 A: not A -> A
e[2 * u + !f].push_back(2 * v + g);
      bool satisfiable() {
            vector<int
             > id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
vector<int> stk;
            int now = 0, cnt = 0;
function<void(int)> tarjan = [&](int u) {
                  stk.push_back(u);
dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
                               tarjan(v);
                        low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in stk
low[u] = min(low[u], dfn[v]);
                        }
                   if (dfn[u] == low[u]) {
                         int v;
                         do {
                               v = stk.back();
                               stk.pop_back();
                        id[v] = cnt;
} while (v != u);
                 }
            };
for (int i
            return true:
      vector < bool > answer() { return ans; }
int m, n; cin >> m >> n;
TwoSat ts(n);
for (int i = 0; i < m; ++i) {</pre>
            int u, v; char x, y;
cin >> x >> u >> y >> v;
ts.addClause(u - 1, x == '+', v - 1, y == '+');
      if (ts.satisfiable()) {
```

```
for (int i = 0; i < n; ++i) {
          cout << (ts.answer()[i] ? '+' : '-') << " ";
     }
} else cout << "IMPOSSIBLE\n";</pre>
```

2.11 Funtional Graph [85c464]

```
| constexpr int N = 2e5 + 5;
| int cht[N][31]; // 倍增表, 放外面不然 TLE
| struct FuntionalGraph {
             int n, cnt;
             vector<int> g, bel, id, len, in, top;
FuntionalGraph() : n(0) {}
FuntionalGraph(vector<int> g_) { init(g_); }
             void init(vector<int> g_) {
                   n = g_.size(); cnt = 0;

g = g_; bel.assign(n, -1);

id.resize(n); len.clear();

in.assign(n, 0); top.assign(n, -1);
                      build():
             void build() {
    for (int i = 0; i < n; i++) {
        cht[i][0] = g[i];
}</pre>
                                 in[g[i]]++;
                      for (int i = 1; i <= 30; i++)
                      for (int i = 1; i <= 30; i++)
    for (int u = 0; u < n; u++)
        cht[u][i] = cht[cht[u][i - 1]][i - 1];
for (int i = 0; i < n; i++)
    if (in[i] == 0) label(i);
for (int i = 0; i < n; i++)
    if (top[i] == -1) label(i);</pre>
             void label(int u) {
                      vector<int> p; int cur = u;
while (top[cur] == -1) {
                                 top[cur] = u;
                                p.push_back(cur);
cur = g[cur];
                      auto s = std::find(p.begin(), p.end(), cur);
vector <int> cyc(s, p.end());
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {
    bel[cyc[i]] = cnt;
    id[cyc[i]] = i;</pre>
                      cnt++; len.push_back(cyc.size());
for (int i = p.size() - 1; i > 0; i--)
   id[p[i - 1]] = id[p[i]] - 1;
            int jump(int u, int k) {
    for (int b = 0; k > 0; b++){
        if (k & 1) u = cht[u][b];
}
                                k >>= 1:
                       return u;
            }
  };
```

3 Data Structure

3.1 BIT [d41d8c]

```
template < typename T>

struct Fenwick { // 全部以 0 based 使用
    int n; vector < T> a;
    Fenwick(int n_ = 0) { init(n_); }
    void init(int n_ ) {
        n = n_;
        a.assign(n, T{});
    }

void add(int x, const T &v) {
        for (int i = x + 1; i <= n; i += i & -i) {
            a[i - 1] = a[i - 1] + v;
    }
}

T sum(int x) { // 左閉右開查詢
    T ans{};
    for (int i = x; i > 0; i -= i & -i) {
            ans = ans + a[i - 1];
    }
    return ans;
}

T rangeSum(int l, int r) { // 左閉右開查詢
    return sum(r) - sum(l);
}

int select(const T &k, int start = 0) {
    // 找到最小的 x, 使得 sum(x + 1) - sum(start) > k
    int x = 0; T cur = -sum(start);
    for (int i = 1 << __lg(n); i; i /= 2) {
        if (x + i <= n && cur + a[x + i - 1] <= k) {
            x += i;
            cur = cur + a[x - 1];
        }
}
return x;
```

```
template < class T>
struct TwoDFenwick { // 全部以 0 based 使用
                     int nx, ny; // row, col 個數
vector < vector < T >> a;
                       TwoDFenwick(int nx_ = 0, int ny_ = 0) {
                                           init(nx_, ny_);
                      void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
                       void add(int x, int y, const T &v) {
                                           for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        a[i - 1][j - 1] = a[i - 1][j - 1] + v;
}</pre>
                                          }
                     T sum(int x, int y) { // 左閉右開查詢
                                           Im(int x, the x, t
                                            return ans;
                    }
T rangeSum
                                              (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                                            return sum(
                                                                   (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
};
```

3.2 RangeBit [d41d8c]

```
template < class T>
struct rangeFenwick { // 全部以 0 based 使用
                 int n;
                 vector<T> d, di;
                 vector<i> u, ut,
rangeFenwick(int n_ = 0) { init(n_); }
void init(int n_) {
                              n = n_;
d.assign(n, T{});
di.assign(n, T{});
                Joid add(int x, const T &v) {
   T vi = v * (x + 1);
   for (int i = x + 1; i <= n; i += i & -i) {
        d[i - 1] = d[i - 1] + v;
        di[i - 1] = di[i - 1] + v;
}</pre>
                 void rangeAdd(int l, int r, const T &v) {
  add(l, v); add(r, -v);
                T sum(int x) { // 左閉右開查詢
                                 for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
                                  return ans:
               T rangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
                 int select(const T &k, int start = 0) {
                                 | 大利最小的 x, 使得 sum(x + 1) - sum(start) > k
| int x = 0; T cur = -sum(start);
| for (int i = 1 << __lg(n); i; i /= 2) {
| if (x + i <= n) {
| T val = T(
                                                                                      x + i + 1) * d[x + i - 1] - di[x + i - 1];
                                                                     if (cur + val <= k) {
    x += i;
    cur = cur + val;
                                                 }
                                  return x;
              }
template < class T>
struct rangeTwoDFenwick { // 全部以 0 based 使用
                int nx, ny; // row, col 個數
vector <vector <T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
                                  init(nx_, ny_);

}
void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T>(ny, T{}));

dj.assign(nx, vector<T);

dj.assign(nx, vecto
                                  dij.assign(nx, vector<T>(ny, T{}));
                 void add(int x, int y, const T &v) {
    T vi = v * (x + 1);
```

```
T vj = v * (y + 1);
T vij = v * (x + 1) * (y + 1);
for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        d[i - 1][j - 1] = d[i - 1][j - 1] + v;
        di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
        dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
        dij[i - 1][j - 1] = dij[i - 1][j - 1] + vij;
}</pre>
             }
        void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
              add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
              add(lx, ly, v);
        T sum(int x, int y) { // 左閉右開查詢
              T ans{}:
              for (int i = x; i > 0; i -= i & -i) {
                     for (int j = y; j > 0; j -= j & -j) {
                           ans = ans
                          return ans;
        T rangeSum
               (int lx, int ly, int rx, int ry) { // 左閉右開查詢
              return sum(
                     rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
       }
};
```

3.3 SegmentTree [d41d8c]

```
struct Seg { // 左閉右開寫法
int n; vector<Info> info;
      Seg() : n(0) {}
Seg(int n_, Info v_ = Info()) { init(n_, v_); }
       template < class T>
      Seg(vector<T> init_) { init(init_); }
void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
      template < class T>
      void init(vector<T> init_) {
             n = init_.size();
             info.assign(4 << __lg(n), Info());</pre>
             info.assign(4 << __lg(n), Info());
function <void(
   int, int, int)> build = [&](int p, int l, int r) {
   if (r - l == 1) {
      info[p] = init_[l];
}
                          return;
                   int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                   pull(p);
             build(1, 0, n);
      void pull(int p) {
   info[p] = info[p * 2] + info[p * 2 + 1];
      void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
      info[p] = v; return;
}
             int m = (l + r) / 2;
             if (x < m) modify(2 * p, l, m, x, v);
else modify(2 * p + 1, m, r, x, v);</pre>
             pull(p);
       void modify(int p, const Info &i) {
             modify(1, 0, n, p, i);
      info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];</pre>
             int m = (l + r) / 2;
return query(p *
    2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
      template < class F> // 尋找區間內,第一個符合條件的
       int findFirst
             (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)
                    return
             if (l >= x && r <= y && !pred(info[p]))</pre>
             return -1;
if (r - l == 1)
return l;
             int m = (l + r) / 2;
```

```
int res = findFirst(2 * p, l, m, x, y, pred);
    if (res == -1)
        res = findFirst(2 * p + 1, m, r, x, y, pred);
    return res;
}

template < class F > // 若要找 last * 先右子樹遞迴即可
int findFirst(int l, int r, F &&pred) {
    return findFirst(1, 0, n, l, r, pred);
};

// ---define structure and info plus---
struct Info {
    int n = 0;
    int sum = 0;
};
Info operator + (const Info &a, const Info &b) {
    return { a.n + b.n, a.sum + b.sum };
}
```

3.4 Lazy Segment Tree [d41d8c]

```
template < class Info, class Tag>
struct LazySeg { // 左閉右開寫法
      int n;
       vector < Info > info;
       vector < Tag > tag;
LazySeg() : n(0) {}
LazySeg(int n_, Info v_ = Info()) {
             init(n_, v_);
      template < class T >
LazySeg(vector < T > init_) {
             init(init_);
       void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
       template < class T>
       void init (vector<T> init_) {
             int( (vector=") tint(_) {
    n = init_.size();
    info.assign(4 << __lg(n), Info());
    tag.assign(4 << __lg(n), Tag());
    function <void(
        int, int, int)> build = [&](int p, int l, int r) {
        if (r - l == 1) {
            info[p] = init_[l];
            return.
                           return;
                     int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                     pull(p);
              build(1, 0, n);
       void pull
       (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
              tag[p].apply(v);
       void push(int p, int l, int r) {
              int m = (l + r) / 2;
if (r - l >= 1) {
    apply(p * 2, l, m, tag[p]);
    apply(p * 2 + 1, m, r, tag[p]);
}
              tag[p] = Tag();
       void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
}
                    return;
              int m = (l + r) / 2;
push(p, l, r);
if (x < m) {</pre>
                     modify(2 * p, l, m, x, v);
              } else {
                     modify(2 * p + 1, m, r, x, v);
              pull(p);
       void modify(int p, const Info &i) {
              modify(1, 0, n, p, i);
      Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    push(p, l, r);
}</pre>
              return query(p *
                     2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
       (int ql, int qr) { return query(1, 0, n, ql, qr); } void range_apply
              (int p, int l, int r, int ql, int qr, const Tag &v) {
if (qr <= l || ql >= r) return;
if (ql <= l && r <= qr) {</pre>
                     apply(p, l, r, v);
                     return;
```

```
int m = (l + r) / 2;
          push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
          pull(p);
     void range_apply(int l, int r, const Tag &v) {
  range_apply(1, 0, n, l, r, v);
                               // 尋找區間內,第一個符合條件的
     int findFirst
          (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {</pre>
               return -1;
          if (l >= x && r <= y && !pred(info[p])) {</pre>
               return -1:
          if (r - l == 1) {
               return l;
          int m = (l + r) / 2;
          push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
          if (res ==
               res = findFirst(2 * p + 1, m, r, x, y, pred);
          return res;
     template < class F> // 若要找 last, 先右子樹遞廻即可
int findFirst(int l, int r, F & & pred) {
return findFirst(1, 0, n, l, r, pred);
};
struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add;
     void apply(const Tag& v) {
          if (v.set_val) {
    set_val = v.set_val;
                add = v.add;
          else {
                add += v.add;
    }
};
struct Info {
     int sum;
     void apply(int l, int r, const Tag &v) {
          if (v.set_val) {
    sum = (r - l) * v.set_val;
          sum += (r - l) * v.add;
     // Info& operator=(const Info &rhs) {
             // 部分 assignment 使用
return *this;
    //
// }
Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
3.5 Persistent Segment Tree [d41d8c]
```

```
template < class Info >
struct PST {
      struct Node {
            Info info = Info();
            int lc = 0, rc = 0;
      vector < Node > nd:
      int n = 0; vector < int > rt;
PST() : n(0) {}
      PST(int n_, Info v_ = Info()) { init(n_, v_); }
template < class T >
      PST(vector <T> init_) { init(init_); }
void init(int n_, Info v_ = Info()) {
  init(vector < Info > (n_, v_));
       template < class T>
      void init(vector<T> init_) {
            n = init_.size();
            nd.clear(); rt.clear();
            nd.emplace_back(); // 讓 root 指向 1-based rt.push_back(build(0, n, init_));
      int build(int l, int r, vector<Info> &init_) {
  int id = nd.size();
            nd.emplace_back();
if (r - l == 1) {
    nd[id].info = init_[l];
                   return id;
            int m = (l + r) >> 1;
nd[id].lc = build(l, m, init_);
nd[id].rc = build(m, r, init_);
             pull(nd[id]);
            return id;
```

Treap *merge(Treap *a, Treap *b) {
 if (!a || !b) return a ? a : b;
 a->push(); b->push();

if (a->pri > b->pri) {

```
void pull(Node &t) {
    t.info = nd[t.lc].info + nd[t.rc].info;
                                                                                                                  a->rc = merge(a->rc, b);
                                                                                                                  a->pull();
                                                                                                                  return a;
     int copy(int t) { // copy 一個 node
   nd.push_back(nd[t]);
                                                                                                            else {
                                                                                                                  b->lc = merge(a, b->lc);
            return nd.size() - 1;
                                                                                                                  b->pull();
     int generate() { // 創立新的 node
   nd.emplace_back();
                                                                                                                  return b;
                                                                                                            }
            return nd.size()
                                                                                                      pair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
      int modify(int t, int l, int r, int x, const Info &v) {
            t = t ? copy(t) : generate();
if (r - l == 1) {
    nd[t].info = v;
                                                                                                            t->push();
                                                                                                            if (size(t->lc) < k) {
   auto [a, b] = split(t->rc, k - size(t->lc) - 1);
   t->rc = a;
                  return t;
            int m = (l + r) >> 1;
                                                                                                                  t->pull();
            if (x < m) {
                                                                                                                  return {t, b};
                  `nd[t].lc = modify(nd[t].lc, l, m, x, v);
                                                                                                                  auto [a, b] = split(t->lc, k);
t->lc = b;
                  nd[t].rc = modify(nd[t].rc, m, r, x, v);
                                                                                                                  t->pull();
            pull(nd[t]);
                                                                                                                  return {a, t};
            return t;
                                                                                                            }
      void modify(int ver, int pos, const Info &val) {
   if (int(rt.size()) <= ver) rt.resize(ver + 1);
   rt[ver] = modify(rt[ver], 0, n, pos, val);</pre>
                                                                                                      void Print(Treap *t) {
   if (!t) return;
                                                                                                            t->push();
                                                                                                            Print(t->lc);
     Info query(int t, int l, int r, int ql, int qr) {
   if (l >= qr || r <= ql) return Info();
   if (ql <= l && r <= qr) return nd[t].info;</pre>
                                                                                                            cout << t->val:
                                                                                                            Print(t->rc);
            int m = (l + r) >> 1;
            return query(nd[t].
                                                                                                      3.7 RMQ [d41d8c]
                  lc, l, m, ql, qr) + query(nd[t].rc, m, r, ql, qr);
     Info query(int ver, int ql, int qr) {
    return query(rt[ver], 0, n, ql, qr);
                                                                                                      template < class T, class Cmp = greater < T >>
                                                                                                      struct RMQ {
                                                                                                            const Cmp cmp = Cmp();
                                                                                                            static constexpr unsigned B = 64; using u64 = unsigned long long;
      void createVersion(int ori_ver) {
    rt.push_back(copy(rt[ori_ver]));
                                                                                                            int n:
      void reserve(int n, int q) {
   nd.reserve(n + q * (2 * __lg(n) + 1));
   rt.reserve(q + 1);
                                                                                                            vector < vector < T >> a;
                                                                                                            vector <T> pre, suf, ini;
vector <u64> stk;
                                                                                                            RMQ() {}
     void resize(int n) {
                                                                                                            RMQ(const vector<T> &v) { init(v); }
                                                                                                            void init(const vector<T> &v) {
  n = v.size();
  pre = suf = ini = v;
           rt.resize(n);
     }
struct Info {
                                                                                                                   stk.resize(n);
     int sum = 0;
                                                                                                                  if (!n) {
                                                                                                                        return;
Info operator+(const Info &a, const Info &b) {
                                                                                                                  const int M = (n - 1) / B + 1;
const int lg = __lg(M);
a.assign(lg + 1, vector<T>(M));
for (int i = 0; i < M; i++) {
    a[0][i] = v[i * B];
    for (int j = 1; j < B && i * B + j < n; j++) {
        a[0][i] = min(a[0][i], v[i * B + j], cmp);
}</pre>
     return { a.sum + b.sum };
3.6 Treap [d41d8c]
struct Treap {
     Treap *lc, *rc;
     int pri, siz; bool rev_valid;
int val; int min;
Treap(int val_) {
    min = val = val_;
                                                                                                                   for (int i = 1; i < n; i++) {
   if (i % B) {
      pre[i] = min(pre[i], pre[i - 1], cmp);
}</pre>
            pri = rand();
lc = rc = nullptr;
            siz = 1; rev_valid = 0;
      }
void pull() { // update siz or other information
                                                                                                                  for (int i = n - 2; i >= 0; i--) {
   if (i % B != B - 1) {
      suf[i] = min(suf[i], suf[i + 1], cmp);
   }
}
            siz = 1;
            min = val;
            for (auto c : {lc, rc}) {
    if (!c) continue;
                                                                                                                  siz += c->siz;
                  min = std::min(min, c->min);
           }
                                                                                                                                      ] = min(a[j][i], a[j][i + (1 << j)], cmp);
                                                                                                                        }
      void push() {
           if (rev_valid) {
   swap(lc, rc);
   if (lc) lc->rev_valid ^= 1;
   if (rc) rc->rev_valid ^= 1;
                                                                                                                  for (int i = 0; i < M; i++) {
    const int l = i * B;
    const int r = min(1U * n, l + B);</pre>
                                                                                                                         for (int j = l; j < r; j++) {
    while (s && cmp(v[j], v[__lg(s) + l])) {
       s ^= 1ULL << __lg(s);
    }
}</pre>
            rev_valid = false;
      int find(int k) { // 找到 min 是 k 的位置 (1-based)
           push();
int ls = (lc ? lc->siz : 0) + 1;
                                                                                                                               s |= 1ULL << (j - l);
                                                                                                                               stk[j] = s;
            if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
                                                                                                                  }
                                                                                                            }
int size(Treap *t) {
    return t ? t->siz : 0;
```

int k = __lg(r - l);
ans = min

 $({ans, a[k][l], a[k][r - (1 << k)]}, cmp);$

4 Flow

4.1 Dinic [aa12d4]

template < class T>

```
struct Dinic {
      struct Edge {
             int to;
             T flow, cap; // 流量跟容量
      int n, m, s, t;
const T INF_FloW = 1 << 30;
      vector<vector<int>> adj; // 此點對應的 edges 編號
      vector < Vector < Lnt>> ad]; // 此對到應的 vector < Edge> edges; // 幫每個 edge 編號 vector < int> dis, ptr; Dinic(int n_ = 0) { init(n_); } void init(int n_) { n = n_; m = 0; dis.resize(n); ptr.resize(n); adj.assign(n, vector < int>{});
             edges.clear();
      void add_edge(int u, int v, T cap) {
             // 偶數 id 是正向邊
             // 何數 ta 定比问您
edges.push_back({ v, 0, cap });
edges.push_back({ u, 0, 0 });
adj[u].push_back(m++);
adj[v].push_back(m++);
      bool bfs() {
             fill(dis.begin(), dis.end(), -1);
dis[s] = 0; queue<int> q;
             q.push(s);
             q.push(e.to);
                   }
             return dis[t] != -1;
      }
T dfs(int u, T flow) {
    if (flow == 0) return 0;
    '    ' -- t) return flow;
             for (int
                      &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {</pre>
                   tage &e = edges[adj[u][cur]];
if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;
T mn = dfs(e.to, min(flow, e.cap - e.flow));
                    if (mn > 0) {
    e.flow += mn;
                           edges[adj[u](cur] ^ 1].flow -= mn;
                   }
             }
             return 0; // 到不了終點就會 return 0
       T work(int s_, int t_) {
    s = s_; t = t_; T flow = 0;
```

```
while (bfs()) {
    fill(ptr.begin(), ptr.end(), 0);
    while (true) {
        T res = dfs(s, INF_FloW);
        if (res == 0) break;
        flow += res;
    }
}
return flow;
}
void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;
}
};</pre>
```

4.2 Min Cut [44ae6c]

```
// CSES Police Chase
int main(){
          int n, m; cin >> n >> m;
Dinic < int > g(n);
for (int i = 0; i < m; i++) {</pre>
                  int u, v, cap = 1;
cin >> u >> v;
                  u--; v--:
                  g.add_edge(u, v, cap);
g.add_edge(v, u, cap);
           int res = g.work(0, n - 1);
cout << res << "\n";
           if (res == 0) return;
           vector<int> vis(n);
           auto find = [&](auto self, int u) -> void {
   if (!vis[u]) {
                           vis[u] = 1;
                           for (int id : g.adj[u])
                                   auto e = g.edges[id];
if (e.cap - e.flow > 0) {
                                           self(self, e.to);
                          }
                  }
         };
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
        auto e = g.edges[id];
        if (!vis[e.to]) {
            cout << i + 1 << " " << e.to + 1 << " | n";
}</pre>
                  }
          }
  }
```

4.3 MCMF [77fc99]

```
template < class Tf, class Tc>
struct MCMF {
     struct Edge {
           int to;
           Tf flow, cap; // 流量跟容量
      // 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就好
     int n, m, s, t;
const Tf INF_FLOW = 1 << 30;
const Tc INF_COST = 1 << 30;</pre>
     vector<vector<int>> adj;
     vector<Edge> edges; // 幫每個 edge 編號
vector<Tc> dis, pot; // johnson algorithm, using spfa
     vector<int> rt; // 路徑恢復,對應 id
     vector <book inq;
MCMF(int n = 0) { init(n); }
void init(int n) {</pre>
           n = n_; m = 0;
edges.clear();
adj.assign(n, vector<int>{});
     void add_edge(int u, int v, Tf cap, Tc cost){
  edges.push_back({v, 0, cap, cost});
  edges.push_back({u, 0, 0, -cost});
           adj[u].push_back(m++);
adj[v].push_back(m++);
     bool spfa() {
           dis.assign(n, INF_COST);
rt.assign(n, -1); inq.assign(n, false);
           queue<int> q;
q.push(s), dis[s] = 0, inq[s] = true;
while (!q.empty()) {
                if (!inq[v]) {
```

```
q.push(v); inq[v] = true;
                         }
                  }
             return dis[t] != INF_COST;
      }
bool dijkstra() {
    dis.assign(n, INF_COST); rt.assign(n, -1);
    priority_queue<pair<Tc, int>,
        vector<pair<Tc, int>>, greater<pair<Tc, int>>> pq;
    dis[s] = 0; pq.emplace(dis[s], s);
    vebile (log empty()) {
            pq.emplace(ndis, v);
                  }
             return dis[t] != INF_COST;
      dis[i] += pot[i] - pot[s];
                   Tf f = INF_FLOW;
                   for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                (f, edges[rt[i]].cap - edges[rt[i]].flow);
                   f = min<Tf>(f, need);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
                   flow += f; need -= f;
cost += f * dis[t]; fr = false;
                   swap(dis, pot);
if (need == 0) break;
             return make_pair(flow, cost);
      }
      // 限定 cost, 最大化 flow
pair<ff, Tc> work_budget(int s_, int t_, Tc budget) {
    s = s_, t = t_; pot.assign(n, 0);
    Tf flow{}; Tc cost{}; bool fr = true;
    while ((fr ? spfa() : dijkstra())) {
        for (int i = 0; i < n; i++) {
            dis[i] += pot[i] - pot[s];
        }
                   Tf f = INF_FLOW;
                   for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                (f, edges[rt[i]].cap - edges[rt[i]].flow);
                   f = min<Tf>(f, budget / dis[t]);
                   for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
                   flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
                   swap(dis, pot);
if (budget == 0 || f == 0) break;
             return make_pair(flow, cost);
       void reset() {
             for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
}:
4.4 Hungarian [eea453]
```

```
struct Hungarian { // 0-based
        int n, m;
vector<vector<int>> adj;
        vector <int>> adj;
vector <int>> used, vis;
vector <pair <int, int>> match;
Hungarian(int n_ = 0, int m_ = 0) {
   init(n_, m_);
        void init(int n_, int m_) {
    n = n_; m = m_;
                 adj.assign(n + m, vector<int>());
used.assign(n + m, -1);
vis.assign(n + m, 0);
        void addEdge(int u, int v) {
   adj[u].push_back(n + v);
   adj[n + v].push_back(u);
```

```
bool dfs(int u)
              int sz = adj[u].size();
              for (int i = 0; i < sz; i++) {
   int v = adj[u][i];</pre>
                     if (vis[v] == 0) {
    vis[v] = 1;
                           if (used[v] == -1 || dfs(used[v])) {
    used[v] = u;
                    }
              return false;
        vector<pair<int, int>> work() {
              match.clear(); used.assign(n + m, -1);
vis.assign(n + m, 0);
for (int i = 0; i < n; i++) {
    fill(vis.begin(), vis.end(), 0); dfs(i);</pre>
              for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
                           match.push_back(make_pair(used[i], i - n));
              return match;
       }
};
```

4.5 Theorem [d41d8c]

```
// 有向無環圖:
// 最小不相交路徑覆蓋:
// 最小路徑數 = 頂點數 - 最大匹配數
// 最小相交路徑覆蓋:
// 先用
   Floyd 求傳遞封包,有連邊就建邊,然後再套最小不相交路徑覆蓋
// 二分圖:
// 最小點
   覆蓋: 選出一些點,讓所有邊至少有一個端點在點集中的最少數量
// 最小點覆蓋 = 最大匹配數
|// 還原解, flow 的作法是從源點開始 dfs, 只走 cap - flow > 0
// 的邊,最後挑選左邊還沒被跑過的點和右邊被跑過的點當作覆蓋的點
1// 最少邊覆蓋: 選出一些邊,讓所有點都覆蓋到的最少數量
// 最少邊覆蓋 = 點數 - 最大匹配數
// 最大獨立集: 選出一些點, 使這些點兩兩沒有邊連接的最大數量
// 最大獨立集 = 點數 - 最大匹配數
```

5 String

5.1 Hash [852711]

```
constexpr int B = 59;
vector<Z> Hash(string &s) {
    vector<Z> ans {0};
    for (auto c : s) {
          ans.push_back(ans.back() * B + (c - 'a' + 1));
     return ans;
void solve() {
    string s, sub;
cin >> s >> sub;
     auto a = Hash(s);
auto q = Hash(sub);
     cout << ans << "\n";
```

5.2 KMP [cddfd9]

```
struct KMP {
      string sub;
      vector < int > failure;
KMP(string sub_) {
    sub = sub_;
            failure.resize(sub.size(), -1);
            buildFailFunction();
      void buildFailFunction() {
    for (int i = 1; i < (int)sub.size(); i++) {
        int now = failure[i - 1];
}</pre>
                   while (now != -1
                          && sub[now + 1] != sub[i]) now = failure[now];
```

```
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
                                                                                             vector<int> manacher(string s) {
                                                                                                   string t = "#
                                                                                                   for (auto c : s) {
       vector < int > match(string &s) {
                                                                                                        t += c;
t += '#';
            vector<int> match;
            for (int i = 0, now = -1; i < (int)s.size(); i++) {
    // now is the compare sucessed length -1
    while (s[i] !=</pre>
                                                                                                   int n = t.size();
                                                                                                   vector<int> r(n);
                  sub[now + 1] && now != -1) now = failure[now];
// failure stores if comparison fail, move to where
if (s[i] == sub[now + 1]) now++;
if (now + 1 == (int)sub.size()) {
                                                                                                   for (int i = 0, j =
                                                                                                        0; i < n; i++) { // i 是中心, j 是最長回文字串中心 if (2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
                       match.push_back(i - now);
now = failure[now];
                                                                                                              0 && i + r[i] < n && t[i - r[i]] == t[i + r[i]]) { r[i] += 1;
            return match;
      }
                                                                                                         if (i + r[i] > j + r[j]) {
};
                                                                                                        }
 5.3 Z Function [764b31]
                                                                                                   return r;
// # a # b # a #
// 1 2 1 4 1 2 1
|// z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
 // 的最長公共前綴 (LCP) 的長度
                                                                                                   // # a # b # b # a #
// 1 2 1 2 5 2 1 2 1
 vector < int > Z(string s) {
   int n = s.size();
                                                                                                   // 值 -1 代表原回文字串長度
       vector \langle int \rangle z(n); z[0] = n;
       for (int i = 1, j = 1; i < n; i++) {
  z[i] = max(0, min(j + z[j] - i, z[i - j]));
  while (i + z[i] < n && s[z[i]] == s[i + z[i]])</pre>
                                                                                                   // (id - val + 1) / 2 可得原字串回文開頭
                  z[i]++;
                                                                                             5.6 SAM [d15619]
            if (i + z[i] > j + z[j]) j = i;
                                                                                             struct SAM {
       return z; // 最後一格不算
                                                                                                   static constexpr int ALPHABET_SIZE = 26;
                                                                                                   struct Node {
                                                                                                        int len;
 5.4 SA [f0d44f]
                                                                                                        int link;
                                                                                                        array<int, ALPHABET_SIZE> next;
                                                                                                        Node() : len{}, link{}, next{} {}
 struct SuffixArray {
      int n; string s;
vector<int> sa, rk, lc;
                                                                                                   vector < Node > t
                                                                                                   SAM() { init(); }
void init() {
       // n: 字串長度
      // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
                                                                                                        t.assign(2, Node()
t[0].next.fill(1);
t[0].len = -1;
                                                                                                                        Node());
       // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
       // lc: LCP
             數組,lc[i] 表示 sa[i] 和 sa[i+1] 的最長公共前綴長度
      SuffixArray(const string &s_) {
   s = s_; n = s.length();
   sa.resize(n);
                                                                                                   int newNode() {
                                                                                                        t.emplace_back();
                                                                                                        return t.size() - 1;
            lc.resize(n - 1);
                                                                                                   int extend(int p, int c) {
    if (t[p].next[c]) {
            rk.resize(n);
            iota(sa.begin(), sa.end(), 0);
            sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });
rk[sa[0]] = 0;</pre>
                                                                                                              int q = t[p].next[c];
                                                                                                              if (t[q].len == t[p].len + 1) {
                                                                                                                   return q;
                         i = 1; i < n; ++i)
                 rk[sa[i]]
                                                                                                              int r = newNode():
                                                                                                              tr = newhode();
t[r].len = t[p].len +
t[r].link = t[q].link;
t[r].next = t[q].next;
t[q].link = r;
                         = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
            vector<int> tmp, cnt(n);
            tmp.reserve(n);
while (rk[sa[n - 1]] < n - 1) {</pre>
                                                                                                              while (t[p].next[c] == q) {
                  tmp.clear();
for (int i = 0; i < k; ++i)
                                                                                                                   t[p].next[c] = r;
p = t[p].link;
                  tror (int i = 0; i < k; ++1)
    tmp.push_back(n - k + i);
for (auto i : sa)
    if (i >= k)
        tmp.push_back(i - k);
                                                                                                              return r;
                                                                                                         int cur = newNode();
                  fill(cnt.begin(), cnt.end(), 0);

for (int i = 0; i < n; ++i)
                                                                                                        t[cur].len = t[p].len + 1;
while (!t[p].next[c]) {
    t[p].next[c] = cur;
                 for (int i = 0; i < n; ++i)
    ++cnt[rk[i]];
for (int i = 1; i < n; ++i)
    cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; --i)
                                                                                                              p = t[p].link;
                                                                                                        t[cur].link = extend(p, c);
                       sa[--cnt[rk[tmp[i]]]] = tmp[i];
                                                                                                         return cur:
                 }
                                                                                             void solve() {
                                                                                                   string s; cin >> s;
int n = s.length();
                                                                                                   vector < int > pos(n + 1); // s[i - 1] 的後綴終點位置
                                                                                                   pos[0] = 1;
                                                                                                   SAM sam;
            for (int i = 0, j = 0; i < n; ++i) {
   if (rk[i] == 0) {</pre>
                                                                                                   for (int i = 0; i < n; i++) {
    pos[i + 1] = sam.extend(pos[i], s[i] - 'a');</pre>
                 j = 0;
} else {
                       for (j
                                -= j > 0; i + j < n && sa[rk[i] - 1] + j
                                                                                             5.7 Trie [31e4ff]
                              < n && s[i + j] == s[sa[rk[i] - 1] + j];)
                                                                                             constexpr int N = 1E7;
                       lc[rk[i] - 1] = j;
                                                                                             int tot
                 }
                                                                                             int trie[N][26], cnt[N];
            }
                                                                                             void reset() {
   tot = 0, fill_n(trie[0], 26, 0);
      }
 };
```

int newNode() {

return x;

int x = ++tot;
cnt[x] = 0, fill_n(trie[x], 26, 0);

5.5 Manacher [9c9ca6]

```
void add(string &s) {
     int p = 0;
for (auto c : s) {
   int &q = trie[p][c - 'a'];
           if (!q) q = newNode();
           p = q;
     cnt[p] += 1;
int find(string &s) {
     int p = 0;
for (auto c : s) {
   int q = trie[p][c - 'a'];
           if (!q) return 0;
     return cnt[p];
}
```

5.8 Duval [f9dcca]

```
// duval_algorithm
// 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
// 將字串分解成若十個非嚴格應減的非嚴格:
vector<string> duval(string s) {
    int i = 0, n = s.size();
    vector<string> res;
    while (i < n) {
        int k = i, j = i + 1;
        while (s[k] <= s[j] && j < n) {
            if (s[k] < s[j]) k = i;
            else k++;
            i++:
            i++:
                             j++;
                    while (i <= k) {</pre>
                             res.push_back(s.substr(i, j - k));
                             i += j - k;
                  }
          return res;
 // 最小旋轉字串
string min_round(string s) {
         s += s;
int i = 0, n = s.size();
int start = i;
while (i < n / 2) {
    start = i;
    int k = i, j = i + 1;
    while (s[k] <= s[j] && j < n) {
        if (s[k] < s[j]) k = i;
        else k++;
        i++</pre>
                             j++;
                    while (i <= k) {
    i += j - k;</pre>
          return s.substr(start. n / 2):
```

6 Math

6.1 Modulo [6b1e0e]

```
template < class T>
constexpr T power(T a, ll b) {
  T res {1};
  for (; b; b /= 2, a *= a)
        if (b % 2) res *= a;
       return res;
constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
      res %= p;
if (res < 0) res += p;
template < ll P >
struct MInt {
      ll x;
      constexpr MInt() : x {0} {}
constexpr MInt(ll x) : x {norm(x % getMod())} {}
       static ll Mod;
      constexpr static ll getMod() {
   if (P > 0) return P;
   else return Mod;
      constexpr static void setMod(ll Mod_) {
    Mod = Mod_;
      constexpr ll norm(ll x) const {
   if (x < 0) x += getMod();
   if (x >= getMod()) x -= getMod();
             return x;
       constexpr MInt operator-() const {
             MInt res;
res.x = norm(getMod() - x);
             return res;
```

```
constexpr MInt inv() const {
    return power(*this, getMod() - 2);
     constexpr MInt &operator*=(MInt rhs) & {
    if (getMod() < (1ULL << 31)) {</pre>
                x = x * rhs.x % int(getMod());
          } else {
               x = mul(x, rhs.x, getMod());
           return *this:
     constexpr MInt &operator+=(MInt rhs) & {
          x = norm(x + rhs.x);
return *this;
     constexpr MInt &operator -=(MInt rhs) & {
          x = norm(x - rhs.x);
return *this;
     constexpr MInt &operator/=(MInt rhs) & {
    return *this *= rhs.inv();
     friend constexpr MInt operator*(MInt lhs, MInt rhs) {
   MInt res = lhs; return res *= rhs;
     friend constexpr MInt operator+(MInt lhs, MInt rhs) {
   MInt res = lhs; return res += rhs;
     friend constexpr MInt operator - (MInt lhs, MInt rhs) {
   MInt res = lhs; return res -= rhs;
     friend constexpr MInt operator/(MInt lhs, MInt rhs) {
          MInt res = lhs; return res /= rhs;
             constexpr istream &operator>>(istream &is, MInt &a) {
          ll v; is >> v; a = MInt(v); return is;
             ostream & operator << (ostream &os, const MInt &a) \{
           return os << a.x:
     friend constexpr bool operator==(MInt lhs, MInt rhs) {
   return lhs.x == rhs.x;
     friend constexpr bool operator!=(MInt lhs, MInt rhs) {
   return lhs.x != rhs.x;
     friend constexpr bool operator<(MInt lhs, MInt rhs) {</pre>
           return lhs.x < rhs.x;</pre>
template<>
ll MInt<0>::Mod = 998244353;
constexpr int P = 1e9 + 7;
using Z = MInt<P>;
6.2 Combination [6aa734]
```

```
struct Comb {
          ll n; vector<Z> _fac, _invfac, _inv;
Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
Comb(ll n) : Comb() { init(n); }
          void init(ll m) {
    m = min(m, Z::getMod() - 1);
    if (m <= n) return;
    _fac.resize(m + 1);
}</pre>
                  _invfac.resize(m + 1);
                  _inv.resize(m + 1);
for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;
                  for (int i = _fac[m].inv();
for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
                  n = m;
          J fac(ll m) {
    if (m > n) init(2 * m);
    return _fac[m];
          Z invfac(ll m) {
   if (m > n) init(2 * m);
   return _invfac[m];
          Z inv(ll m) {
                  if (m > n) init(2 * m);
return _inv[m];
          J binom(ll n, ll m) {
   if (n < m || m < 0) return 0;
   return fac(n) * invfac(m) * invfac(n - m);</pre>
          Z lucas(ll n, ll m) { // Mod 要在 1E5 左右
                  if (m == 0) return 1;
return binom(n % Z::getMod(), m % Z::getMod())
* lucas(n / Z::getMod(), m / Z::getMod());
|} comb; // 注意宣告, 若要換模數需重新宣告
```

6.3 Sieve [8a3c1c]

```
| vector < int > prime , minp;

void sieve(int n) {

    minp.assign(n + 1, 1); // 1 代表是質數 , 非 1 不是

    minp[0] = minp[1] = -1;

    int m = int(sqrt(n)) + 1;

    for (int i = 2; i <= m; i++) {

        if (minp[i] == 1) {

            prime.push_back(i);

            for (int j = 2; i * j <= n; j++) {

                minp[i * j] = i;

            }

        }

    }

}

// a ^ (m-1) = 1 (Mod m)

// a ^ (m-2) = 1/a (Mod m)

// Exp2: cout << power(x, power(y, p, Mod - 1), Mod)

// Num = (x+1) * (y+1) * (z+1)...

// Sum = (a^0 + a^1+...+a^x) * (b^0 +...+b^y)

// Mul = N * (x+1) * (y+1) * (z+1) / 2
```

6.4 CRT [d41d8c]

6.5 Matrix [08b5fe]

```
template < class T>
struct Mat {
     int m, n;
      constexpr static ll mod = 1e9 + 7;
     Mat(vector<T>> matrix;
Mat(int n_ = 0) { init(n_, n_); }
Mat(int m_, int n_) { init(m_, n_); }
Mat(vector<vector<T>> matrix_) { init(matrix_); }
      void init(int m_, int n_) {
    m = m_; n = n_;
    matrix.assign(m, vector<T>(n));
      void init(vector<vector<T>> &matrix_) {
           m = matrix_.size();
n = matrix_[0].size();
            matrix = matrix_;
     vector<vector<T>> unit(int n) { // 單位矩
vector<vector<T>> res(n, vector<T>(n));
for (int i = 0; i < n; i++) {
res[i][i] = 1;
                                                         // 單位矩陣
      constexpr Mat &operator*=(const Mat& rhs) & {
   assert(matrix[0].size() == rhs.matrix.size());
            int m = matrix.size()
           }
                 }
           matrix = ans.matrix;
return *this;
      constexpr Mat &operator^=(ll p) & {
            assert(m == n); assert(p >= 0);
Mat ans(p-- == 0 ? unit(m) : matrix);
            while (p > 0) {
```

6.6 Integer Partition [595ed2]

6.7 Mobius Theorem

- 數論分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n} \mu(d) = \begin{cases} 1 & \text{for } n=1\\ 0 & \text{for } n\neq 0 \end{cases}$$

- 2. μ 是常數函數 1 的反元素 $\Rightarrow \mu*1=\epsilon$, $\epsilon(n)$ 只在n=1 時為 1 , 其餘情況皆為 0 。
- $-\phi$ 歐拉函數: x以下與x互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^{i}) \\ &= 1 + p^{0}(p-1) + p^{1}(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^{c} \\ &= id \end{split}$$

- 莫比烏斯反演公式
 - $f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$
 - $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

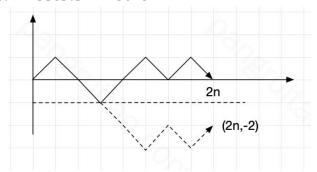
例子

$$\begin{split} &\sum_{i=aj=c}^{b} \sum_{j=1}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{\infty} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.8 Mobius Inverse [d41d8c]

```
const int maxn = 2e5:
ll mobius_pref[maxn];
void init() {
     mobius_pref[1] = 1;
vector<ll> wei
     (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
    }
                 continue; // 包含平方
           if (wei[i] == 0) {
    wei[i] = 1;
                 for (ll j = 2; i * j < maxn; j++) {
   if (j % i == 0) wei[i * j] = -1;
   else if (wei[i * j] != -1) wei[i * j]++;</pre>
                }
           mobius_pref[i]
                  = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
     }
void solve() {
     - 1]) * (x / l) * (y / l); // 代推出來的式子
           return res;
     cout << cal
            (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k, (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n";
}
```

6.9 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2)

假設往上有 x 個,往下有 y 個,會有:

$$\begin{cases} x + y = 2n \\ y - x = 2 \end{cases} \Rightarrow \begin{cases} x = n - 1 \\ y = n + 1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.10 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- X/G:本質不同的方案的集合 X^g :對於某一種操作 g,所有方案中,經過 g 這種翻轉後保持不變的方案 的集合
- 集合取絕對值代表集合數

Search and Gready

7.1 Binary Search [d41d8c]

```
int main() {
   int lo = 1, hi = 10;
   // 二分找上界
        // - // 1/ 1.2 r
while (lo < hi) {
  int x = (lo + hi + 1) / 2;
  if (check(x)) lo = x;
  else hi = x - 1;
        cout << lo;
        // 二分找下界
while (lo < hi) {
   int x = (lo + hi) / 2;
                if (check(m)) hi = x;
                else lo = x + 1;
        cout << lo;
}
```

7.2 Ternary Search [d41d8c]

```
int main() {
                 = 0, hi = 10;
      while (lo <= hi) {
    int xl = lo + (hi - lo) / 3;
    int xr = hi - (hi - lo) / 3;
}
            int ansl = check(xl), ansr = check(xr);
if (ansl < ansr) {</pre>
                   lo = xl + 1;
            } else {
   hi = xr - 1;
            // record ans and index
     }
```

Тгее 8

8.1 LCA [601e2d]

```
vector<vector<int>> par(maxn, vector<int>(18));
vector < int > depth(maxn + 1);
vector < int > dfn(maxn);
vector < int> dfn(maxn);
void build(int n, vector < vector < pair < int, int >>> & tree) {
    auto dfs = [&](auto self, int u, int pre) -> void {
        for (auto [v, w] : tree[u]) {
            if (v == pre) continue;
            par[v][0] = u; // 2 ^ 0
            depth[v] = depth[u] + 1;
            self(self, v, u);
}
                   }
         fdfs(dfs, 1, 0);
for (int i = 1; i <= 18; i++) {
    for (int j = 1; j <= n; j++) {
        par[j][i] = par[par[j][i - 1]][i - 1];
}</pre>
          }
int pull = depth[a] - depth[b];
for (int i = 0; i < 18; i++) {
   if (pull & (1 << i)) {</pre>
                             a = par[a][i];
                   }
           if (a == b) return a;
                   (int i = 17; i >= 0; i--) {
if (par[a][i] != par[b][i]) {
    a = par[a][i], b = par[b][i];
          return par[a][0];
```

8.2 Centroid Decomposition [ec760b]

```
#include <bits/stdc++.h>
using namespace std;
struct CenDecom {
     int n;
     vector<vector<int>> adj;
     vector<bool> vis;
     vector < int > siz;
CenDecom(int n_ = 0) { init(n_); }
void init(int n_) {
         n = n_;
```

```
adj.assign(n, {});
vis.assign(n, false);
               siz.assign(n, 1);
        void addEdge(int u, int v) {
               adj[u].push_back(v);
               adi[v].push_back(u);
        void get_siz(int x, int p = -1) {
              fet_stz(tht x, tht p = -1) {
    siz[x] = 1;
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        get_siz(y, x);
        siz[x] += siz[y];
}
       int get_cen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz) {
                             return get_cen(y, sz, x);
               return x:
        void get_ans(int x, int p) {
               // do something
for (int y : adj[x]) {
   if (y == p || vis[y]) continue;
                      get_ans(y, x);
        void work(int x = 0) {
              get_siz(0, x);
int cen = get_cen(x, siz[x]);
              vis[cen] = true;
for (int y : adj[cen]) {
   if (vis[y]) continue;
                      get_ans(y, cen);
              for (int y : adj[cen]) {
   if (vis[y]) continue;
                      work(y);
      }
};
```

8.3 Tree Flattening [5293b7]

```
點加值 = 所有子節點區間加值,求單點,使用 bit,做前綴差分
// CSES 1138_Path Queries
int main(){
      int n, q; cin >> n >> q;
vector <int> val(n + 1), dfnToVal(n);
for (int i = 1; i <= n; i++) {
    cin >> val[i];
       vector<vector<int>> tree(n + 1);
       for (int i = 1; i < n; i++) {
   int u, v; cin >> u >> v;
   tree[u].push_back(v);
              tree[v].push_back(u);
       vector<pair<int, int>> mp(n + 1); // dfn 區間
      int cnt = 0;
auto dfs = [&](auto self, int u, int par) -> void {
    dfnToVal[++cnt] = val[u];
             mp[u].first = cnt;
for (auto v : tree[u]) {
    if (v == par) continue;
    self(self, v, u);
             mp[u].second = cnt;
       dfs(dfs, 1, 0);
      BIT bit(n);
for (int i = 1; i <= n; i++) {
    bit.modify(mp[i].first, val[i]);
}</pre>
             if (mp[i].first < n) { // root 就不用扣了
  bit.modify(mp[i].second + 1, -val[i]);</pre>
       for (int i = 0; i < q; i++) {
             int op; cin >> op;
if (op == 1) {
                    int s, x; cin >> s >> x;
int add = x - dfnToVal[mp[s].first];
dfnToVal[mp[s].first] = x;
                    bit.modify(mp[s].first, add);
                    if (mp[s].first < n) { // root 就不用扣了
  bit.modify(mp[s].second + 1, -add);</pre>
                    }
                     int node; cin >> node;
                    cout << bit.query(mp[node].first) << "\n";</pre>
}
```

8.4 Heavy Light Decomposition [325476]

```
struct HLD {
      int n, cur;
vector < int > siz, top, dep, parent, in, out, seq;
       vector<vector<int>> adj;
       HLD(int n_ = 0) { init(n_); }
void init(int n_) {
             n = n_; cur = 0;
siz.resize(n); top.resize(n); dep.resize(n);
parent.resize(n); in.resize(n); out.resize(n);
              seq.resize(n); adj.assign(n, {});
             adj[u].push_back(v);
             adj[v].push_back(u);
       void work(int rt = 0) {
             top[rt] = rt;
dep[rt] = 0;
parent[rt] = -1;
             dfs1(rt); dfs2(rt);
       void dfs1(int u) {
    if (parent[u] != -1)
                    adj[u].erase(find
                            (adj[u].begin(), adj[u].end(), parent[u]));
             for (auto &v : adj[u]) {
    parent[v] = u, dep[v] = dep[u] + 1;
                    dfs1(v);
                    siz[u] += siz[v];
                    if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
                    } // 讓 adj[u][0] 是重子節點
       void dfs2(int u) {
             in[u] = cur++;
             seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
  top[v] = v == adj[u][0] ? top[u] : v;
                    dfs2(v);
             out[u] = cur;
       int lca(int u, int v) {
    while (top[u] != top[v]) {
        if (dep[top[u]] > dep[top[v]]) {
                          u = parent[top[u]];
                    } else {
                           v = parent[top[v]];
                   }
              return dep[u] < dep[v] ? u : v;
       int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
      int jump(int u, int k) {
    if (dep[u] < k) return -1;
    int d = dep[u] - k;
    while (dep[top[u]] > d)
        u = parent[top[u]];
    return seq[in[u] - dep[u] + d];
}
       bool isAncester(int u, int v) {
             return in[u] <= in[v] && in[v] < out[u];</pre>
       int rootedParent(int rt. int v) {
            rootedParent(int rt, int v) {
swap(rt, v);
if (rt == v) return rt;
if (!isAncester(rt, v)) return parent[rt];
auto it = upper_bound(adj[
    rt].begin(), adj[rt].end(), v, [&](int x, int y) {
    return in[x] < in[y];
}) - 1;
return *it;</pre>
      int rootedSize(int rt, int v) {
   if (rt == v) return n;
   if (!isAncester(v, rt)) return siz[v];
}
             return n - siz[rootedParent(rt, v)];
       int rootedLca(int a, int b, int rt) {
  return lca(a, b) ^ lca(b, rt) ^ lca(rt, a);
```

8.5 Link Cut Tree [d69ee0]

```
template < class Info, class Tag>
struct Node {
    Node *ch[2], *p;
    bool rev = false; int size = 1;
    Info info = Info(); Tag tag = Tag();
    Node() : ch{nullptr, nullptr}, p(nullptr) {}
    bool isrt() {
        return !p || (p->ch[0] != this && p->ch[1] != this);
    }
    void make_rev() {
        swap(ch[0], ch[1]);
}
```

```
rev ^= true;
     void apply(const Tag &v) {
  info.apply(size, v);
  tag.apply(v);
     void push() {
    if (rev) {
                if (ch[0]) ch[0]->make_rev();
if (ch[1]) ch[1]->make_rev();
rev = false;
           if (ch[0]) ch[0]->apply(tag);
if (ch[1]) ch[1]->apply(tag);
           tag = Tag();
     void pull() {
          int pos() {
           return p->ch[1] == this;
     void pushAll()
           if (!isrt())
                p->pushAll();
           push();
     void rotate() {
          Node *q = p;
int x = !pos();
q->ch[!x] = ch[x];
           if (ch[x]) ch[x] -> p = q;
           p = q->p;
if (!q->isrt()) q->p->ch[q->pos()] = this;
          ch[x] = q;
q->p = this;
           q->pull();
     void splay() {
    pushAll();
           while (!isrt()) {
                if (!p->isrt()) {
    if (pos() == p->pos()) {
                           p->rotate();
                      } else {
                           rotate();
                     }
                rotate();
           pull();
     void access() { // access 後自動 splay
           for (Node
    *i = this, *q = nullptr; i; q = i, i = i->p) {
                i->splay();
                i->ch[1] = i->pull();
           splay();
     void makeRoot() {
           access();
           make_rev();
     Node* findRoot() {
          access();
Node *t = this;
while (t->ch[0]) {
               t->push();
                t = t->ch[0];
           t->access();
           return t;
    }
template < class Info, class Tag>
bool connected(Node < Info, Tag> *x, Node < Info, Tag> *y) {
    return x -> findRoot() == y -> findRoot();
template < class Info, class Tag>
bool neighber(Node < Info, Tag> *x, Node < Info, Tag> *y) {
     x->makeRoot();
     y->access();
if (y->ch[0] != x || x->ch[1]) return false;
     return true:
remplate < class Info, class Tag >
void split(Node < Info, Tag > *rt, Node < Info, Tag > *y) {
     y->makeRoot();
     rt->access();
template < class Info, class Tag>
void link(Node < Info, Tag> *t, Node < Info, Tag> *p) {
     t->makeRoot();
     if (p->findRoot() != t) {
           t->p = p;
```

```
template < class Info, class Tag>
bool cut(Node < Info, Tag> *x, Node < Info, Tag> *y) {
      x->makeRoot():
      x->makenout(,,
y->access();
if (y->ch[0] != x || x->ch[1]) return false;
y->ch[0] = y->ch[0]->p = nullptr;
       x->pull();
       y->pull();
       return true;
remplate < class Info, class Tag>
void modify(Node < Info, Tag> *x, const Info &v) {
      x->access():
       x - sinfo = v;
template < class Info, class Tag>
void path_apply
      (Node<Info, Tag> *x, Node<Info, Tag> *y, const Tag &v) {
       assert(connected(x, y));
       split(x, y);
x->apply(v);
template < class Info, class Tag>
Info path_query(Node < Info, Tag> *x, Node < Info, Tag> *y) {
      assert(connected(x, y));
       split(x, y);
return x->info;
constexpr int Mod = 51061;
struct Tag {
    ll add = 0; ll mul = 1;
    void apply(const Tag& v) {
        mul = mul * v.mul % Mod;
        add = (add * v.mul % Mod + v.add) % Mod;
}
};
};
struct Info {
    ll val = 0; ll sum = 0;
    void apply(int size, const Tag &v) {
        val = (val * v.mul % Mod + v.add) % Mod;
        sum = (sum * v.mul % Mod + v.add * size % Mod) % Mod;
}
       void pull(const Info &l, const Info &r) {
             sum = (l.sum + r.sum + val) % Mod;
      }
};
using lct = Node<Info, Tag>;
8.6 Virtual Tree [622e69]
```

```
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
// 可以建立虚樹達成快速樹 DP
 // 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector <int>>stk(maxn);
 int top = -1; vector < int > stk(maxn);
void insert(int u, vector < vector < int >> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
        vt[stk[top - 1]].push_back(stk[top]), top--;
    if (stk[top - 1] != l) {
        vt[l].push_back(stk[top]);
        stk[top] = l;
    } else vt[l].push_back(stk[top--]);
    stk[++ton] = u;</pre>
          stk[++top] = u;
  void reset(int u, vector<vector<int>> &vt) {
          for (int i : vt[u]) reset(i, vt);
          vt[u].clear();
  void solve(int n, int q) {
  vector g(n + 1, vector<pair<int, int>>());
         vector vt(n + 1, vector<int>()); // dfs 完清除, 否則會退化
vector<ll> dp(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;
                  g[u].push_back(\{v, w\});
                 g[v].push_back({u, w});
          build_lca(n, g);
          build(n, g);
for (int i = 0; i < q; i++) {</pre>
                 int m; top = -1; cin >> m;
vector <int> key(m);
for (int j = 0; j < m; j++) {
    cin >> key[j];
    iskey[key[j]] = 1;
                 key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
                 auto dfs = [&](auto self, int u) -> void {
                         for (auto v : vt[u]) {
    self(self, v);
```

8.7 Dominator Tree [baa540]

```
struct Dominator_tree {
        vector <vector <int>> adj, radj, bucket;
vector <int>> sdom, dom, vis, rev, pa, rt, mn, res;
Dominator_tree(int n_ = 0) { init(n_); }
        void init(int _n) {
    n = _n, id = 0;
    adj.assign(n, vector<int>())
                radj.assign(n, vector<int>());
               bucket.assign(n, vector <int>());
sdom.resize(n); dom.assign(n, -1)
vis.assign(n, -1); rev.resize(n);
pa.resize(n); rt.resize(n);
mn.resize(n); res.resize(n);
        void add_edge(int u, int v) { adj[u].push_back(v); }
int query(int v, int x) {
   if (rt[v] == v) return x ? -1 : v;
                int p = query(rt[v], 1);
if (p == -1) return x ? rt[v] : mn[v];
if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
               rt[v] = p;
return x ? p : mn[v];
        radj[vis[u]].push_back(vis[v]);
               }
        void build(int s) {
               dfs(s);
               for (int i = id - 1; i >= 0; i--) {
    for (int u : radj[i])
        sdom[i] = min(sdom[i], sdom[query(u, 0)]);
                       if (i) bucket[sdom[i]].push_back(i);
                       for (int u : bucket[i]) {
   int p = query(u, 0);
   dom[u] = sdom[p] == i ? i : p;
                       if (i) rt[i] = pa[i];
               res.assign(n, -1);
for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];
for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre>
                res[s] = s;
                for (int i = 0; i < n; i++) dom[i] = res[i];</pre>
        }
};
```

9 DP

9.1 LCS [5781cf]

```
16
      cout << s << "\n":
9.2 LIS [66d09f]
int main() {
      int n; cin >> n;
vector <int> v(n);
for (int i = 0; i < n; i++) cin >> v[i];
      int dp[n]; vector<int> stk;
      true up[ii], vector<int> stk;
stk.push_back(v[0]);
dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) {
    if (v[i] > stk.back()) {
        stk.push_back(v[i]);
        dp[i] = ++L;
} else {
            } else {
                  auto it
                         = lower_bound(stk.begin(), stk.end(), v[i]);
                  *it = v[i]; dp[i] = it - stk.begin() + 1;
           }
      vector<int> ans; cout << L << "\n";
      for (int i = n - 1; i >= 0; i--) {
   if (dp[i] == L) {
                  ans.push_back(v[i]), L--;
            }
      reverse(ans.begin(), ans.end());
for (auto i : ans) cout << i << " ";</pre>
}
9.3 Edit Distance [308023]
int main() {
      string s1, s2; cin >> s1 >> s2;
      int n1 = s1.size(), n2 = s2.size();
      // dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元
       vector<int> dp(n2 + 1);
      for (int i = 1; i <= n1; i++) {
    vector<int> cur(n2 + 1); cur[0] = i;
            for (int j = 1; j <= n2; j++) {
    if (s1[i - 1] == s2[j - 1]) {
        cur[j] = dp[j - 1];
                        // s1 新增等價於 s2 砍掉
```

// dp[i][j] = min(s2 新增, 修改, s1 新增);

= min({cur[j - 1], dp[j - 1], dp[j]}) + 1;

9.4 Bitmask [a626f9]

}

swap(dp, cur);

cout << dp[n2] << "\n";

cur[j]

```
void hamiltonianPath(){
      int n, m; cin >> n >> m;
vector adj(n, vector < int > ());
for (int i = 0; i < m; i++) {</pre>
             int u, v; cin >> u >> v;
adj[--v].push_back(--u);
       // 以...為終點,走過...
       vector dp(n, vector<int>(findBit(n)));
      dp[0][1] = 1;
      for (int mask = 1; mask < findBit(n); mask++) {
    if ((mask & 1) == 0) continue;
    for (int i = 0; i < n; i++) {
        if ((mask & findBit(i)) == 0) continue;
        if (i == n - 1 && mask != findBit(n) - 1) continue;
    }
}</pre>
                     int pre_mask = mask ^ findBit(i);
                     for (int j : adj[i]) {
   if ((pre_mask & findBit(j)) == 0) continue;
                            dp[i][mask
                                    ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
                    }
             }
      cout << dp[n - 1][findBit(n) - 1] << "\n":
void elevatorRides() {
      int n, x; cin >> n >> x; vector<int> a(n);

for (int i = 0; i < n; i++) cin >> a[i];

vector<array<int, 2>> dp(findBit(n));

dp[0][0] = 1; // 次數、已使用人數

for (int mask = 1; mask < 1 (indBit(n); mask++) {
```

9.5 Projects [0942aa]

9.6 Removal Game [7bb56b]

9.7 Monotonic Queue [f4976d]

```
| // 應用: dp(i) = h(i) + max(A(j)), for l(i)≤j≤r(i)
| // A(j) 可能包含 dp(j), h(i) 可 O(1)
| void Bounded_Knapsack() {
| int n, k; // O(nk) |
| vector <int> w(n), v(n), num(n); deque <int> q;
| // 於是我們將同餘的數分在同一組
| // 每次取出連續 num[i] 格中最大值
| // g_x = max(_{{k=0}^num[i] (g'_{{x-k}} + v_i*k)) |
| // G_x = g'_{{x}} - v_i*x |
| // x ( x - k = v_i*(x - k) |
| // g_x = max(_{{k=0}^num[i] (G_{{x-k}} + v_i*x)) |
| vector <vector <li>vector vector vector vector vector vector <vector <li>vector vector vector
```

9.8 SOS [93cb19]

9.9 CHT [5f5c25]

```
|// 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \le r(i)
 // A(j), B(j) 可能包含 dp(j), 分別就是 m 跟 b
 struct Line {
     ll m,
     line(ll m = 0, ll b = 0) : m(m), b(b) {}
ll eval(ll x) {
    return m * x + b;
};
struct CHT { // 用在查詢單調斜率也單調
  int n, lptr, rptr; vector<Line> hull;
  CHT(int n_ = 0, Line init_ = Line()) {
         init(n_, init_);
     void init(int n_ = 0, Line init_ = Line()) {
    n = n_; hull.resize(n); reset(init_);
     void reset(Line init_ = Line()) {
    lptr = rptr = 0; hull[0] = init_;
     bool pop_front(Line &l1, Line &l2, ll x) {
         // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y
          // 代表查詢的當下,右線段的高度已經低於左線段了
return ll.eval(x) >= l2.eval(x);
     bool pop_back(Line &l1, Line &l2, Line &l3) {
         // 本題斜率遞減、上凸包
         // 因此只要 12 跟
         l3 的 X 交點 <= l1 跟 l3 的 X 交點, l2 就用不到了
return (l3.b - l2.b)
* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
     void insert(Line L) {
         hull[++rptr] = L;
     return hull[lptr].eval(x);
     }
};
```

9.10 DNC [61c639]

```
| // 應用: 切 k 段問題, 且滿足四邊形不等式
| // w(a,c) + w(b,d) ≤(≥) w(a,d) + w(b,c)
| // dp[k][j] = min(dp[k - 1][i] + cost[i][j])
| // cost: (i, j]
| constexpr int N = 3e3 + 5;
| constexpr ll inf = 4e18;
| ll dp[N][N]; // 1-based
| ll get_cost(int l, int r) {}
| void DNC(int k, int l, int r, int optl, int optr) {
| if (l > r) return;
| int m = (l + r) >> 1, opt = -1;
| dp[k][m] = inf;
| for (int i = max(k, optl); i <= min(m, optr); i++) {
| // 注意 i 的範圍 \ get_cost 與 dp 的邊界
| ll cur = dp[k - 1][i] + get_cost(i, m);
| if (cur < dp[k][m]) {
| dp[k][m] = cur, opt = i;
| }
| dp[k][m] = cur, opt = i;
```

9.11 LiChaoSegmentTree [f23ef4]

```
// 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \le r(i)
constexpr ll inf = 4e18;
struct Line {
    ll m, b;
     Line(ll m = 0, ll b = inf) : m(m), b(b) {}
     ll eval(ll x) const { return m * x + b; }
struct LiChaoSeg { // 取 max 再變換就好
     int n;
vector <Line > info;
     LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_) {
           n = n_{;}
           info.assign(4 << __lg(n), Line());</pre>
     void update(Line line, int node, int l, int r) {
  int m = (l + r) / 2;
  bool left = line.eval(l) < info[node].eval(l);
  bool mid = line.eval(m) < info[node].eval(m);</pre>
           if (mid) swap(info[node], line); // 如果新線段比較好
if (r - l == 1) return;
else if (left != mid) update(line, 2 * node, l, m);
           // 代表左半有交點
           else update(line, 2 * node + 1, m, r);
           // 代表如果有交點一定在右半
     void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
   if (r - l == 1) return info[node].eval(x);
           int m = (l + r) / 2;
           if (x < m) return
                 min(info[node].eval(x), query(x, 2 * node, l, m));
                 info[node].eval(x), query(x, 2 * node + 1, m, r));
     il query(int x) { return query(x, 1, 0, n); }
```

9.12 Codeforces Example [7d37ea]

```
|// CF 1932 nF
// 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
 // 請問在線段不重複的情況下,最多獲得幾分
 int main() {
     int n, m;
cin >> n >> m;
     // 記錄每點有幾個線段
     // 再一個紀錄,包含這個點的左界
     cnt[l]++
     for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
     for (int i = n; i >= 2; i--) {
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
     vector<int> dp(n + 1);
     dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
          dp[i] = cnt[i];
if (l_side[i] != inf) {
    dp[i] += dp[l_side[i] - 1];
          dp[i] = max(dp[i], dp[i - 1]);
     cout << dp[n] << "\n";
 }
 // CF 1935 pC
 // 給你每個事件的 a, b, 挑事件會把 a 全部加起來
 // 再加上 max(bi) - min(bi)
int main(){
    int n, k, ans = 0; cin >> n >> k;
     vector pii> v(n + 1);
for (int i = 1; i <= n; i++) {
   int a, b; cin >> a >> b;
          v[i] = {a, b};
```

10 Geometry

10.1 Basic [d41d8c]

```
template < class T>
struct Point {
     Point(const T &x_ = 0, const T &y_ = 0) : x(x_), y(y_) {} template < class U >
     operator Point<U>() {
         return Point < U > (U(x), U(y));
     Point &operator+=(const Point &p) & {
    x += p.x; y += p.y; return *this;
     Point &operator -= (const Point &p) & {
    x -= p.x; y -= p.y; return *this;
     Point & operator *= (const T & v) & {
    x *= v; y *= v; return *this;
     Point &operator/=(const T &v) & {
    x /= v; y /= v; return *this;
     Point operator - () const {
          return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
          return a += b;
     friend Point operator-(Point a, const Point &b) {
          return a -= b;
     friend Point operator*(Point a, const T &b) {
  return a *= b;
     friend Point operator/(Point a, const T &b) {
          return a /= b;
     friend Point operator*(const T &a, Point b) {
          return b *= a;
     friend bool operator == (const Point &a, const Point &b) {
          return a.x == b.x && a.y == b.y;
     friend istream & operator >> (istream & is. Point & p) {
          return is >> p.x >> p.y;
     friend ostream &operator << (ostream &os, const Point &p) {
   return os << "(" << p.x << ", " << p.y << ")";</pre>
};
template < class T>
struct Line {
     Point <T> a;
     Point<T> b;
Line(const Point<T> &a_ = Point<T>()
            , const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
T dot(const Point<T> &a, const Point<T> &b) {
     return a.x * b.x + a.y * b.y;
T cross(const Point<T> &a, const Point<T> &b) {
   return a.x * b.y - a.y * b.x;
template < class T>
T square(const Point < T > & p) {
    return dot(p, p);
template < class T>
double length(const Point < T> &p)
     return sqrt(double(square(p)));
template < class T>
double length(const Line<T> &l) {
    return length(l.a - l.b);
```

```
template < class T>
Point<T> normalize(const Point<T> &p) {
       return p / length(p);
template < class T >
bool parallel(const Line < T > &l1, const Line < T > &l2) {
    return cross(l1.b - l1.a, l2.b - l2.a) == 0;
template < class T>
double distance(const Point<T> &a, const Point<T> &b) {
       return length(a - b);
double distancePL(const Point<T> &p, const Line<T> &l) {
       return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)
      return distance(p, l.a);
   if (dot(p - l.b, l.a - l.b) < 0)
      return distance(p, l.b);
   return distance(p, l.b);</pre>
       return distancePL(p, 1);
template<class T>
Point<T> rotate(const Point<T> &a) {
    return Point(-a.y, a.x);
template < class T >
int sgn(const Point < T > & a) {
    return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
      return cross(l.b - l.a, p - l.a) > 0;
template < class T>
Point<T
       > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
return l1.a + (l1.b - l1.a) * (cross(l2.b -
                l2.a, l1.a - l2.a) / cross(l2.b - l2.a, l1.a - l1.b));
template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
       return cross(p - l.a, l.b - l.a) == 0 &&
min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)
                       (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
       (const Point<T> &a, const vector<Point<T>> &p) {
int n = p.size(), t = θ;
for (int i = θ; i < n; i++) {</pre>
               if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {
                      return true:
       for (int i = 0; i < n; i++) {
    auto u = p[i];</pre>
               auto v = p[(i + 1) \% n];
               if (u.x < a.
                      x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
               if (u.x >= a
                       .x && v.x < a.x && pointOnLineLeft(a, Line(u, v)))</pre>
       return t == 1:
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
(const Line<T> &l1, const Line<T> &l2) {
   if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
      return {0, Point<T>(), Point<T>()};
   if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
      return {0, Point<T>(), Point<T>()};
   if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y))
      return {0, Point<T>(), Point<T>()};
   if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y))
      return {0, Point<T>(), Point<T>()};
   if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
      if (cross(l1.b - l1.a, l2.a - l1.a) != 0) {
        return {0, Point<T>(), Point<T>()};
   }
   else {
              auto maxx1 = max(l1.a.x, l1.b.x);
auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
auto miny1 = min(l1.a.y, l1.b.y);
auto minx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
auto miny2 = min(l2.a.y, l2.b.y);
                      Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
if (!pointOnSegment(p1, l1))
                              swap(p1.y, p2.y);
```

```
if (p1 == p2) {
    return {3, p1, p2};
               } else {
                     return {2, p1, p2};
          }
     }
     auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
     Point p = lineIntersection(l1, l2);
     if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
          return {1, p, p};
     } else {
          return {3, p, p};
template < class T>
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
   if (get<0>(segmentIntersection(l1, l2)) != 0)
     return min({distancePS(l1.a, l2), distancePS(l1
    .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
bool segmentInPolygon
      (const Line<T> &l, const vector<Point<T>> &p) {
     int n = p.size();
     if (!pointInPolygon(l.a, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
for (int i = 0; i < n; i++) {
    auto u = p[i];
}</pre>
          auto v = p[(i + 1) % n];
auto w = p[(i + 2) % n];
          auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
if (t == 1) return false;
if (t == 0) continue;
           if (t == 2) {
                if (pointOnSegment(v, l) && v != l.a && v != l.b)
   if (cross(v - u, w - v) > 0)
       return false;
          || pointOnLineLeft(l.b, Line(v, u)))
               return false;
} else if (p1 == v) {
   if (l.a == v) {
                          if (pointOnLineLeft(u, l)) {
    if (pointOnLineLeft(w, l))
                                     && pointOnLineLeft(w, Line(u, v)))
                                     return false;
                          return false;
                          return false;
                          }
               }
          }
     return true:
vector <Point <T>> hp(vector <Line <T>> lines) {
    sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
        auto d1 = l1.b - l1.a;
        auto d2 = l2.b - l2.a;
        if (auto l2) }
          if (sgn(d1) != sgn(d2))
    return sgn(d1) == 1
          return cross(d1, d2) > 0;
     deque<Line<T>> ls;
     deque<Point<T>> ps;
for (auto l : lines) {
    if (ls.empty()) {
                ls.push_back(l);
```

```
while (!ps.empty() && !pointOnLineLeft(ps.back(), l))
         ps.pop_back(), ls.pop_back();
while (!ps.empty() && !pointOnLineLeft(ps[0], l))
ps.pop_front(), ls.pop_front();
          if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
               if (dot
                     (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                    if (!pointOnLineLeft(ls.back().a, l)) {
                         assert(ls.size() == 1);
                         ls[0] = l;
                    continue;
              return {}:
          ps.push_back(lineIntersection(ls.back(), l));
          ls.push_back(l);
    while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0]))
    ps.pop_back(), ls.pop_back();
if (ls.size() <= 2) return {};
ps.push_back(lineIntersection(ls[0], ls.back()));</pre>
     return vector(ps.begin(), ps.end());
using P = Point<ll>;
```

10.2 Convex Hull [b5758d]

```
int main() {
     int n; cin >> n;
vector <P> P(n), U, L;
for (int i = 0; i < n; i++) {</pre>
          cin >> P[i];
     sort(P.begin(),
          .end(), [](const Point<i64> &a, const Point<i64> &b) {
return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
     L.pop_back();
          while (U.size() >= 2 && cross(U.back() -
     U[U.size() - 2], P[i] - U[U.size() - 2]) >= 0LL){
               U.pop_back();
          if (L.
                empty() || !(L.back() == P[i])) L.push_back(P[i]);
          if (U.
                if (L.size() <= 2 && U.size() <= 2) {
          // No Hull
     cout << L.size() + U.size() - 2 << "|n";
for (int i = 0; i < L.size() - 1; i++) {
    cout << L[i].x << " " << L[i].y << "|n";</pre>
     for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << " | n";</pre>
}
```

10.3 MinEuclideanDistance [3020bc]

```
T distanceSquare(const Point<T> &a, const Point<T> &b) {
      return square(a - b);
void solve() {
   int n; cin >> n;
   constexpr ll inf = 8e18;
       vector < Point < ll >> a(n);
      for (int i = 0; i < n; i++) {
    ll x, y;
    cin >> x >> y;
             a[i] = Point < il>(x, y);
       struct sortY {
             bool operator
     ()(const Point<ll> &a, const Point<ll> &b) const {
                    return a.y < b.y;</pre>
            }
      struct sortXY {
                     ()(const Point<ll> &a, const Point<ll> &b) const {
                    if (a.x == b.x) return a.y < b.y;
else return a.x < b.x;</pre>
             }
       sort(a.begin(), a.end(), sortXY());
      sort(a.begin(), a.end(), sortXY());
vector < Point < ll >> t(n);
auto devide = [&](auto &&self, int l, int r) -> ll {
    if (l == r) return inf;
    int m = (l + r) / 2;
    ll ans = min(self(self, l, m), self(self, m + 1, r));
    ll midval = a[m].x;
    ll a = 0.
             for (int i = l; i <= r; i++) {</pre>
```

10.4 LatticePoints [00db9d]

10.5 MinCoverCircle [c9ca81]