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```

1 Basic

1.1 install vscode [d41d8c]

1.2 default code [767e68]

```
#include <bits/stdc++.h>
#pragma GCC optimize("03")
// #pragma GCC target("popent")
// C++ 20 vector grammer will not work
#define all(x) (x).begin(), (x).end()
using namespace std;
using ll = long long;

void solve() {
}

int main() {
    ios_base::sync_with_stdio(false);
    cin.tie(nullptr);
    int t = 1;
    cin >> t;
    while (t--) {
        solve();
    }
}
```

1.3 compare fuction [4bc3e0]

```
struct cmp {
    vector < int > &v;
                  // 要在 template 的資結用外部變數
     cmp(vector<int>& vec) : v(vec) {}
bool operator() (int a, int b) const {
   return v[a] > v[b];
// main: cmp cmp1(vector);
// main. cmp cmp1(vector),
// priority_queue<int, vector<int>, cmp> pq(cmp1);
};
1.4 pbds [e28ae8]
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template<typename T>
using pbds_set = tree<T, null_type,</pre>
       less<T>, rb_tree_tag, tree_order_statistics_node_update>;
1.5 浮點數誤差 [a0d4e5]
struct EDouble {
     constexpr static double Eps = 1e-9;
constexpr EDouble() : x{} {}
constexpr EDouble(double v) : x{v} {}
     constexpr double val() const {
         return x:
     explicit constexpr operator double() const {
         return x;
     constexpr EDouble operator-() const {
         return EDouble(-x);
     constexpr EDouble &operator+=(const EDouble &rhs) & {
         x += rhs.x
          return *this:
     constexpr EDouble &operator -=(const EDouble &rhs) & {
         x -= rhs.x;
return *this;
     constexpr EDouble &operator*=(const EDouble &rhs) & {
         x *= rhs.x:
         return *this;
     constexpr EDouble &operator/=(const EDouble &rhs) & {
   assert(fabs(rhs.x) > Eps);
         x /= rhs.x;
          return *this;
           EDouble operator+(EDouble lhs, const EDouble &rhs) {
          lhs += rhs;
     friend constexpr
           EDouble operator - (EDouble lhs, const EDouble &rhs) {
         lhs -= rhs;
         return lhs:
           EDouble operator*(EDouble lhs, const EDouble &rhs) {
          lhs *= rhs;
          return lhs;
     friend constexor
           EDouble operator/(EDouble lhs, const EDouble &rhs) {
         lhs /= rhs;
return lhs;
     friend constexpr bool
           operator < (const EDouble &lhs, const EDouble &rhs) {</pre>
          return lhs.x - rhs.x < -Eps:
     friend constexpr bool
           operator > (const EDouble &lhs, const EDouble &rhs) {
          return lhs.x - rhs.x > Eps;
     friend constexpr bool
    operator==(const EDouble &lhs, const EDouble &rhs) {
          return fabs(lhs.x - rhs.x) < Eps;</pre>
     friend constexpr bool
            operator <= (const EDouble &lhs, const EDouble &rhs) {</pre>
          return lhs < rhs || lhs == rhs;</pre>
     friend constexpr bool
           operator >=(const EDouble &lhs, const EDouble &rhs) {
          return lhs > rhs || lhs == rhs;
            operator!=(const EDouble &lhs, const EDouble &rhs) {
          return !(lhs == rhs);
     friend istream & operator >> (istream &is, EDouble &a) {
```

2 Graph

2.1 DFS 跟 BFS [cdd1d5]

2.2 Prim [f00ec0]

2.3 BellmanFord [430ded]

```
if (i == n) t = v;
}

}
if (t == -1) { cout << "NO\n"; return; }
for (int i = 1; i < n; i++) t = par[t];
vector<int> ans {t};
int i = t;
do {
    i = par[i];
    ans.push_back(i);
} while (i != t);
reverse(ans.begin(), ans.end());
cout << "YES\n";
for (auto x : ans) cout << x + 1 << " ";</pre>
```

2.4 FloydWarshall [206b76]

```
| const int inf = 1e18;
| int main() {
| int n, m, q; cin >> n >> m >> q;
| vector < vector < int >> graph(n + 1, vector < int >(n + 1, inf));
| vector < vector < int >> dis(n + 1, vector < int >(n + 1));
| for (int i = 0; i < m; i++) {
| int u, v, w; cin >> u >> v >> w;
| cin >> u >> v >> w;
| graph[u][v] = min(graph[u][v], w);
| graph[v][u] = min(graph[v][u], w);
| }
| for (int i = 0; i <= n; i++) {
| dis[i][j] = graph[i][j];
| }
| }
| for (int i = 0; i <= n; i++) // 自己到自己是 0 |
| dis[i][i] = 0;
| for (int k = 1; k <= n; k++) {
| for (int i = 1; i <= n; i++) {
| dis[i][j] | j <= n; j++) {
| cint u, v; cin >> u >> v; cout << (dis[u][v] >= inf ? -1 : dis[u][v]) << "\n";
| }
| }
```

2.5 歐拉環與歐拉路 [0911ed]

```
1// 無向圖、尤拉環: 檢查每個點的出度為偶數
// 有向圖、
        尤拉路:可以看成 1 走到 n,所以檢查所有點的出度等於入度
 int n, m;
const int maxn = 1e5 + 5;
 vector<set<int>> adj;
 vector<int> in;
 void dfs(int now, vector<int> &road) {
      while (!adj[now].empty()) {
    int nxt = *adj[now].begin();
            adj[now].erase(nxt);
            dfs(nxt, road);
      road.push_back(now);
 void solve() {
      cin >> n >> m;
      in >> m;
in.assign(n + 1, 0);
adj.assign(n + 1, set<int>());
for (int i = 1; i <= m; i++) {
   int u, v; cin >> u >> v;
   adj[u].insert(v);
}
            in[v]++;
      in[1]++;
      in[i]..,
in[n]..;
for (int i = 1; i <= n; i++) {
    if(adj[i].size() != in[i]) {
        cout << "IMPOSSIBLE";
}</pre>
           }
      vector<int> road;
      dfs(1, road);
      if (road.size() != m + 1) {
    cout << "IMPOSSIBLE";</pre>
            return:
      for(auto i : road) cout << i <<</pre>
```

2.6 SCC [5d3e16]

```
struct SCC {
  int n, cur, cnt;
  vector<vector<int>> adj;
```

```
vector<int> stk, dfn, low, bel;
SCC(int n_ = 0) {
           init(n_);
      void init(int n_) {
           n = n_;
adj.assign(n, {});
            dfn.assign(n, -1);
            low.resize(n);
           bel.assign(n, -1);
           stk.clear();
cur = cnt = 0;
      void addEdge(int u, int v) {
   adj[u].push_back(v);
      void dfs(int x) {
    dfn[x] = low[x] = cur++;
            stk.push_back(x);
           for (auto y : adj[x]) {
   if (dfn[y] == -1) {
      dfs(y);
                 low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
            if (dfn[x] == low[x]) {
                  int y;
                 do {
                       v = stk.back():
                       bel[y] = cnt;
                       stk.pop_back();
                 } while (y != x);
           }
      vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
    }
}</pre>
            return bel;
      struct Graph {
            int n;
            vector<pair<int, int>> edges;
           vector < int > siz;
vector < int > cnte;
      Graph compress() {
           Graph g;
g.n = cnt;
            g.siz.resize(cnt);
            g.cnte.resize(cnt);
            for (int i = 0; i < n; i++) {
                 g.siz[bel[i]]++;
                 for (auto j : adj[i]) {
    if (bel[i] != bel[j]) {
                             g.edges.emplace_back(bel[i], bel[j]);
                       } else {
                             g.cnte[bel[i]]++;
                 }
            return g;
     }
}:
```

2.7 VBCC [170604]

```
struct VBCC {
      int n, cur;
vector<vector<int>> adj;
      vector<int> dfn, low, parent;
      vector < bool > is_cut;
VBCC(int n_ = 0) {
    init(n_);
      void init(int n_) {
            n = n_;
adj.assign(n, {});
dfn.assign(n, -1);
low.resize(n);
            parent.assign(n, -1);
             is_cut.assign(n, false);
            cur = 0;
      void addEdge(int u, int v) {
    adj[u].push_back(v);
            adj[v].push_back(u);
      void dfs(int x) {
   int children = 0;
   dfn[x] = low[x] = cur++;
            for (int v : adj[x]) {
    if (dfn[v] == -1) {
        children++;
    }
                         parent[v] = x;
                         dfs(v);
low[x] = min(low[x], low[v]);
                         if (parent[x] != -1 && low[v] >= dfn[x]) {
```

```
2.8 EBCC [49d862]
 struct EBCC { // CF/contest/1986/pF
        int n, cur, cnt;
        vector<vector<int>> adj;
        vector<int> stk, dfn, low, bel;
vector<pair<int, int>> bridges; // 關鍵邊
        EBCC(int n_) {
   init(n_);
        void init(int n_) {
               n = n_{;}
               adj.assign(n, {});
               dfn.assign(n,
low.resize(n);
               bel.assign(n,
               stk.clear();
               bridges.clear();
               cur = cnt = 0;
        void addEdge(int u, int v) {
               adj[u].push_back(v);
               adj[v].push_back(u);
        void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
               stk.push_back(x);
              stk.push_back(x);
for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
        dfs(y, x);
        low[x] = min(low[x], low[y]);
        if (low[y] > dfn[x]) {
            bridges.emplace_back(x, y);
        }
}
                     } else if (bel[y] == -1) {
    low[x] = min(low[x], dfn[y]);
               if (dfn[x] == low[x]) {
                      int y;
do {
                             y = stk.back();
                             bel[y] = cnt;
                             stk.pop_back();
                      } while (y != x);
                      cnt++;
              }
        fvector<int> work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
        }
}</pre>
                     }
               return bel;
        struct Graph {
               vector<pair<int, int>> edges;
               vector<int> siz; // BCC 內節點數
               vector<int> cnte; // BCC 內邊數
        Graph compress() {
              Graph g;
g.n = cnt;
               g.siz.resize(cnt);
              g.stz.restze(cnt);
g.cnte.restze(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;
    for (auto j : adj[i]) {
        if (bel[i] < bel[j]) {
            g.edges.emplace_back(bel[i], bel[j]);
        } else if (i < j) {</pre>
                                   g.cnte[bel[i]]++;
                     }
               return g;
        }
};
```

2.9 2-SAT [eeddc1]

```
// CSES Giant Pizza
struct TwoSat {
   int n;
      vector < int >> e;
      vector < bool > ans;
      vector < bool > ans;
TwoSat(int n) : n(n), e(2 * n), ans(n) {}
void addClause(int u, bool f, int v, bool g) {
        e[2 * u + !f].push_back(2 * v + g);
        e[2 * v + !g].push_back(2 * u + f);
      bool satisfiable() {
            vector<int
                   > id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
            vector<int> stk;
            int now = 0, cnt = 0;
function < void(int) > tarjan = [&](int u) {
                 stk.push_back(u);
dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
                              tarjan(v);
                        low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in stk
low[u] = min(low[u], dfn[v]);
                        }
                  if (dfn[u] == low[u]) {
                        int v;
do {
                              v = stk.back();
                             stk.pop_back();
id[v] = cnt;
                        } while (v != u);
                        ++cnt;
                 }
            for (int i
            vector < bool > answer() { return ans; }
int main() {
      int m, n; cin >> m >> n;
TwoSat ts(n);
for (int i = 0; i < m; ++i) {</pre>
            int u, v; char x, y;
cin >> x >> u >> y >> v;
ts.addClause(u - 1, x == '+', v - 1, y == '+');
      cout << (ts.answer()[i] ? '+' : '-') << " ";
      else cout << "IMPOSSIBLE\n";</pre>
}
```

2.10 Funtional Graph [85c464]

```
constexpr int N = 2e5 + 5;
int cht[N][31]; // 倍增表, 放外面不然 TLE struct FuntionalGraph {
       int n, cnt;
vector <int> g, bel, id, len, in, top;
FuntionalGraph() : n(0) {}
FuntionalGraph(vector <int> g_) { init(g_); }
        void init(vector < int > g_) {
    n = g_.size(); cnt = 0;
                g = g_; bel.assign(n, -1);
id.resize(n); len.clear();
in.assign(n, 0); top.assign(n, -1);
                build();
       }
void build() {
    for (int i = 0; i < n; i++) {
        cht[i][0] = g[i];
        in[g[i]]++;</pre>
                for (int i = 1; i <= 30; i++)
    for (int u = 0; u < n; u++)
        cht[u][i] = cht[cht[u][i - 1]][i - 1];
for (int i = 0; i < n; i++)
    if (in[i] == 0) label(i);
for (int i = 0; i < n; i++)
    if (ton[i] == 1) label(i);</pre>
                        if (top[i] == -1) label(i);
        void label(int u) {
                vector<int> p; int cur = u;
while (top[cur] == -1) {
   top[cur] = u;
                        p.push_back(cur);
                         cur = g[cur];
                auto s = std::find(p.begin(), p.end(), cur);
                vector<int> cyc(s, p.end());
```

```
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {
    bel[cyc[i]] = cnt;</pre>
                        id[cyc[i]] = i;
                 cnt++; len.push_back(cyc.size());
                for (int i = p.size() - 1; i > 0; i--)
   id[p[i - 1]] = id[p[i]] - 1;
         int jump(int u, int k) {
    for (int b = 0; k > 0; b++){
        if (k & 1) u = cht[u][b];
}
                        k >>= 1;
                 return u:
        }
1 };
```

3 Data Structure

3.1 BIT [d41d8c]

```
template <typename T>
struct Fenwick { // 全部以 0 based 使用
      vector<T> a;
      Fenwick(int n_ = 0) {
          init(n_);
      void init(int n_) {
           a.assign(n, T{});
      void add(int x, const T &v) {
           for (int i = x + 1; i <= n; i += i & -i) {
   a[i - 1] = a[i - 1] + v;</pre>
      T sum(int x) { // 左閉右開查詢
           for (int i = x; i > 0; i -= i & -i) {
    ans = ans + a[i - 1];
           return ans;
     T rangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
      int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
          }
           return x;
    }
template <class T>
struct TwoDFenwick { // 全部以 0 based 使用
     int nx, ny; // row, col 個數 vector<vector<T>> a;
      TwoDFenwick(int nx_ = 0, int ny_ = 0) {
           init(nx_, ny_);
      void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
     void add(int x, int y, const T &v) {
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            a[i - 1][j - 1] = a[i - 1][j - 1] + v;
        }
}</pre>
          }
     }
      T sum(int x, int y) { // 左閉右開查詢
          Jm(tit ^, ----,
T ans{};
for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans + a[i - 1][j - 1];
}
           return ans;
      T rangeSum
           (int lx, int ly, int rx, int ry) { // 左閉右開查詢
           return sum(
                 (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
     }
};
```

3.2 RangeBit [d41d8c]

```
| template <typename T>
struct rangeFenwick { // 全部以 0 based 使用
    vector<T> d. di:
```

rangeFenwick(int n_ = 0) {

```
vector<int> boss, siz;
                init(n_);
                                                                                                                           DSU() {}
         void init(int n_) {
                                                                                                                           DSU(int n ) {
                                                                                                                                  init(n_);
               n = n_;
                d.assign(n, T{});
                                                                                                                           void init(int n_) {
                di.assign(n, T{});
                                                                                                                                  n = n_;
boss.resize(n);
         Joid add(int x, const T &v) {
   T vi = v * (x + 1);
   for (int i = x + 1; i <= n; i += i & -i) {
        d[i - 1] = d[i - 1] + v;
        di[i - 1] = di[i - 1] + v;
}</pre>
                                                                                                                                  iota(boss.begin(), boss.end(), 0);
                                                                                                                                  siz.assign(n, 1);
                                                                                                                           int find_boss(int x) {
   if (boss[x] == x) return x;
   return boss[x] = find_boss(boss[x]);
         void rangeAdd(int l, int r, const T &v) {
   add(l, v); add(r, -v);
                                                                                                                           bool same(int x, int y) {
    return find_boss(x) == find_boss(y);
        }
         T sum(int x) { // 左閉右開查詢
                                                                                                                           bool merge(int x, int y) {
    x = find_boss(x);
    y = find_boss(y);
                T ans{};
                for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
                                                                                                                                  if (x == y) {
    return false;
                return ans;
                                                                                                                                  if(siz[x] < siz[y]) swap(x, y);</pre>
                                                                                                                                  siz[x] += siz[y];
boss[y] = x;
        TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
                                                                                                                                  return true:
        int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
               int x = 0;
T cur{};
for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n) {</pre>
                                                                                                                           int size(int x)
                                                                                                                                  return siz[find_boss(x)];
                                                                                                                           }
                                                                                                                    }:
                             T val = T(
    x + i + 1) * d[x + i - 1] - di[x + i - 1];
                                                                                                                    struct DSU {
                              if (cur + val <= k) {
                                                                                                                           int n;
                                    x += i;
                                                                                                                           vector < int > boss, siz, stk;
                                    cur = cur + val;
                                                                                                                           DSU() {}
                                                                                                                           DSU(int n ) {
                      }
                                                                                                                                  init(n_);
               return x;
                                                                                                                           void init(int n_) {
        }
                                                                                                                                  n = n_;
                                                                                                                                  boss.resize(n);
  template <class T>
                                                                                                                                  iota(boss.begin(), boss.end(), 0);
siz.assign(n, 1);
  struct rangeTwoDFenwick { // 全部以 0 based 使用
        int nx, ny; // row, col 個數
vector <vector <T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
                                                                                                                                  stk.clear();
                                                                                                                           int find(int x) {
                                                                                                                                  return x == boss[x] ? x : find(boss[x]);
                init(nx_, ny_);
        }
void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
}
                                                                                                                           bool same(int x, int y) {
    return find(x) == find(y);
                                                                                                                           bool merge(int x, int y) {
    x = find(x);
    y = find(y);
}
                                                                                                                                  if (x == y) {
    return false;

}
void add(int x, int y, const T &v) {
    T vi = v * (x + 1);
    T vj = v * (y + 1);
    T vij = v * (x + 1) * (y + 1);
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            d[i - 1][j - 1] = d[i - 1][j - 1] + v;
            di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
            dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
            dij[i - 1][j - 1] = dij[i - 1][j - 1] + vij;
            dij[i - 1][j - 1] = dij[i - 1][j - 1] + vij;
            reconstructions.
}
</pre>
                                                                                                                                  if (siz[x] < siz[y]) swap(x, y);
siz[x] += siz[y];
boss[y] = x;</pre>
                                                                                                                                  stk.push_back(y);
return true;
                                                                                                                           void undo(int x) {
   while (stk.size() > x) {
                      }
               }
                                                                                                                                        int y = stk.back();
                                                                                                                                         stk.pop_back();
         void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
                                                                                                                                         siz[boss[y]] -= siz[y];
                add(rx, ry, v);
               add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
                                                                                                                                        boss[y] = y;
                                                                                                                                 }
                                                                                                                           int size(int x) {
    return siz[find(x)];
         T sum(int x, int y) { // 左閉右開查詢
                T ans{};
               for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans
                                                                                                                    3.4 線段樹 [d41d8c]
                             ans = ans  + T(x * y + x + y + 1) * d[i - 1][j - 1];  ans = ans - T(y + 1) * di[i - 1][j - 1];  ans = ans - T(x + 1) * dj[i - 1][j - 1];  ans = ans + dij[i - 1][j - 1]; 
                                                                                                                    template <class Info>
                                                                                                                    }
                return ans;
        }
T rangeSum
                                                                                                                           template <class T>
Seg(vector<T> init_) {
                (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                                                                                                                                  init(init_);
                       rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
                                                                                                                           void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
       }
 };
 3.3 DSU [d41d8c]
                                                                                                                           template <class T>
                                                                                                                           void init(vector<T> init_) {
| struct DSU {
                                                                                                                                 n = init_.size();
```

int n:

```
info.assign(4 << __lg(n), Info());</pre>
            function <void(
   int, int, int)> build = [&](int p, int l, int r) {
   if (r - l == 1) {
                         info[p] = init_[l];
                         return;
                  int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                  pull(p);
            build(1, 0, n);
      (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
            if (r - l == 1)
   info[p] = v;
                  return;
            int m = (l + r) / 2;
            if (x < m) {
                  modify(2 * p, l, m, x, v);
            } else {
                  modify(2 * p + 1, m, r, x, v);
            pull(p);
      void modify(int p, const Info &i) {
            modify(1, 0, n, p, i);
      info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];</pre>
            int m = (l + r) / 2;
return query(p *
    2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
      Info query
      (int ql, int qr) { return query(1, 0, n, ql, qr); }
template < class F> // 尋找區間內,第一個符合條件的
      int findFirst
            (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)</pre>
                  return 1:
            if (l >= x && r <= y && !pred(info[p]))</pre>
            return -1;
if (r - l == 1)
            return l;
int m = (l + r) / 2;
int res = findFirst(2 * p, l, m, x, y, pred);
if (res == -1)
                  res = findFirst(2 * p + 1, m, r, x, y, pred);
            return res;
      template < class F> // 若要找 last, 先右子樹遞廻即可int findFirst(int l, int r, F &&pred) {
    return findFirst(1, 0, n, l, r, pred);
  / ---define structure and info plus---
struct Info {
     int n = 1;
      int sum = 0;
Info operator+(const Info &a, const Info &b) {
    return { a.n + b.n, a.sum + b.sum };
```

3.5 懶標線段樹 [d41d8c]

template <class Info. class Tag>

```
build(p * 2 + 1, m, r);
                    pull(p);
              build(1, 0, n);
        void pull
       (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
              tag[p].apply(v);
       foid push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
              tag[p] = Tag();
       void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
      info[p] = v;
}
                     return;
              int m = (l + r) / 2;
              push(p, l, r);
if (x < m) {
    modify(2 * p, l, m, x, v);</pre>
              } else {
                    modify(2 * p + 1, m, r, x, v);
              pull(p);
       void modify(int p, const Info &i) {
    modify(1, 0, n, p, i);
       Info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];
    int m = (l + r) / 2;
    push(p, l, r);
    return query(p *</pre>
                      2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
               (int ql, int qr) { return query(1, 0, n, ql, qr); }
       void range_apply
   (int p, int l, int r, int ql, int qr, const Tag &v) {
              if (qr <= l || ql >= r) return;
if (ql <= l && r <= qr) {
    apply(p, l, r, v);</pre>
              int m = (l + r) / 2;
              push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
              pull(p);
       void range_apply(int l, int r, const Tag &v) {
    range_apply(1, 0, n, l, r, v);
       template < class F >
                                        // 尋找區間內,第一個符合條件的
       int findFirst
              (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
   return -1;</pre>
              if (l >= x && r <= y && !pred(info[p])) {</pre>
                    return -1;
              }
if (r - l == 1) {
                    return l;
              int m = (l + r) / 2;
              push(p);
int res = findFirst(2 * p, l, m, x, y, pred);
              if (res == -1)
                    res = findFirst(2 * p + 1, m, r, x, y, pred);
              return res:
       template <class F> // 若要找 last,先右子樹遞迴即可
int findFirst(int l, int r, F &&pred) {
    return findFirst(1, 0, n, l, r, pred);
};
// ---define structure and info plus---
| struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add; | void apply(const Tag& v) { | if (v.set_val) { | set_val = v.set_val; | add = v.add; | }
              else {
                     add += v.add;
       }
struct Info {
```

3.6 **莫隊** [d41d8c]

3.7 Treap [d41d8c]

```
struct Treap {
      ict Treap {
   Treap *lc, *rc;
   int pri, siz; bool rev_valid;
   int val; int min;
   Treap(int val_) {
      min = val = val_;
      pri = rand();
      lc = rc = nullptr;
      cir = 1: rev_valid = 0;
               siz = 1; rev_valid = 0;
       void pull() { // update siz or other information
              siz = 1;
min = val;
              for (auto c : {lc, rc}) {
    if (!c) continue;
                     siz += c->siz;
                     min = std::min(min, c->min);
              }
       void push() {
   if (rev_valid) {
                     swap(lc, rc);
if (lc) lc->rev_valid ^= 1;
if (rc) rc->rev_valid ^= 1;
               rev_valid = false;
       int find(int k) { // 找到 min 是 k 的位置 (1-based)
              push();
int ls = (lc ? lc->siz : 0) + 1;
              if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
int size(Treap *t) {
    return t ? t->siz : 0;
Treap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
       a->push(); b->push();
if (a->pri > b->pri) {
    a->rc = merge(a->rc, b);
               a->pull();
               return a;
       else {
              b->lc = merge(a, b->lc);
              b->pull();
              return b;
pair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
       if (size(t->lc) < k) {
```

```
auto [a, b] = split(t->rc, k - size(t->lc) - 1);
    t->rc = a;
    t->pull();
    return {t, b};
}
else {
    auto [a, b] = split(t->lc, k);
    t->lc = b;
    t->pull();
    return {a, t};
}

void Print(Treap *t) {
    if (!t) return;
    t->push();
    Print(t->lc);
    cout << t->val;
    Print(t->rc);
}
```

4 Flow

4.1 Dinic [287fe8]

```
template < class T>
 struct Dinic {
    struct Edge {
            int to;
            T flow, cap; // 流量跟容量
       int n, m, s, t;
T INF_FlOW = numeric_limits<T>::max() / 2;
       vector<vector<int>> adj; // 此點對應的 edges 編號
      void add_edge(int u, int v, T cap) {
            // 偶數 id 是正向邊
            edges.push_back({ v, 0, cap });
edges.push_back({ u, 0, 0 });
            adj[u].push_back(m++);
adj[v].push_back(m++);
      bool bfs() {
    fill(dis.begin(), dis.end(), -1);
    dis[s] = 0; queue<int> q;
            q.push(s);
            dis[e.to] = dis[u] + 1;
q.push(e.to);
                 }
            return dis[t] != -1;
       T dfs(int u, T flow) {
   if (flow == 0) return 0;
   if (u == t) return flow;
            for (int
                  &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {
Edge & e = edges[adj[u][cur]];
if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;
T mn = dfs(e.to, min(flow, e.cap - e.flow));</pre>
                  if (mn > 0) {
    e.flow += mn;
                       edges[adj[u][cur] ^ 1].flow -= mn;
                  }
            return 0; // 到不了終點就會 return 0
       T work(int s_, int t_) {
    s = s_; t = t_; T flow = 0;
    while (bfs()) {
                  fill(ptr.begin(), ptr.end(), 0);
                  while (true) {
    T res = dfs(s, INF_Flow);
                        if (res == 0) break;
                       flow += res;
                 }
            return flow;
      void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
       }
};
```

4.2 Min Cut [44ae6c]

```
' CSES Police Chase
int main(){
       int n, m; cin >> n >> m;
Dinic < int >> g(n);
for (int i = 0; i < m; i++) {
    int u, v, cap = 1;
    cin >> u >> v;
                 u--; v--;
                 g.add_edge(u, v, cap);
                 g.add_edge(v, u, cap);
         int res = g.work(0, n - 1);
        cout << res << "\n";
if (res == 0) return;
        vector <int> vis(n);
auto find = [&](auto self, int u) -> void {
   if (!vis[u]) {
                          vis[u]
                         vts[u] = 1;
for (int id : g.adj[u]) {
    auto e = g.edges[id];
    if (e.cap - e.flow > 0) {
        self(self, e.to);
    }
}
                         }
                }
        };
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
    }
        re = - q edges[id];</pre>
                          auto e = g.edges[id];
                          if (!vis[e.to]) {
    cout << i + 1 << " " << e.to + 1 << " \n";
                 }
      }
```

4.3 Hangarian [350fc3]

```
struct Hangarian { // 0-based int n, m; // 最小路徑覆蓋,二分匹配 vector<vector<int>> adj;
         vector<int> used, vis;
        vector <pair <int, int >> match;
Hangarian(int n_ = 0, int m_ = 0) {
   init(n_, m_);
        void init(int n_ = 0, int m_ = 0) {
    n = n_; m = m_;
    adj.assign(n + m, vector<int>());
    used.assign(n + m, -1);
    vis.assign(n + m, 0);
         void addEdge(int u, int v) {
   adj[u].push_back(n + v);
   adj[n + v].push_back(u);
        vector<pair<int, int>> work() {
   match.clear();
   used.assign(n + m, -1);
                 vis.assign(n + m, 0);
auto dfs = [&](auto self, int u) -> bool {
                         for (int v : adj[u]) {
    if (vis[v] == 0) {
       vis[v] = 1;
    }
}
                                          vis[v] = 1;
if (used[v] = -1 || self(self, used[v])) {
    used[v] = u;
                                                  return true:
                                         }
                                }
                         return false;
                 for (int i = 0; i < n; i++) {
   fill(vis.begin(), vis.end(), 0);
   dfs(dfs, i);</pre>
                 for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
                                 match.emplace_back(used[i], i - n);
                 return match;
}:
```

4.4 MCMF [f667f8]

```
template < class Tf, class Tc>
struct MCMF {

// 可以只用 spfa 或 dijkstra,把跟 pot 有關的拿掉就好
int n, m, s, t;

Tf INF_FLOW = numeric_limits < Tf>::max() / 2;

Tc INF_COST = numeric_limits < Tc>::max() / 2;

struct Edge {

int to;

If flow, cap; // 流量跟容量
```

```
Tc cost:
vector<vector<int>> adj;
vector < vector < int> aaa];
vector < Edge > edges; // 幫每個 edge 編號
vector < Tc > dis, pot; // johnson algorithm, using spfa
vector < int> rt; // 路徑恢復, 對應 id
vector < bool > inq;
MCMF(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
       n = n_;
       m = 0;
       edges.clear();
       adj.assign(n, vector<int>{});
void add_edge(int u, int v, Tf cap, Tc cost){
  edges.push_back({v, 0, cap, cost});
  edges.push_back({u, 0, 0, -cost});
  adj[u].push_back(m++);
       adj[v].push_back(m++);
bool spfa() {
       dis.assign(n, INF_COST);
rt.assign(n, -1); inq.assign(n, false);
       queue < int > q;
q.push(s), dis[s] = 0, inq[s] = true;
        while (!q.empty()) {
             if (!inq[v]) {
    q.push(v); inq[v] = true;
                     }
             }
       return dis[t] != INF_COST;
bool dijkstra() {
      }
       return dis[t] != INF_COST;
// 限定 flow, 最小化 cost
pair x Tf, Tc > work_flow(int s_, int t_, Tf need) {
    s = s_, t = t_; pot.assign(n, 0);
    Tf flow{}; Tc cost{}; bool fr = true;
    while ((fr ? spfa() : dijkstra())) {
        for (int i = 0; i < n; i++) {
            dis[i] += pot[i] - pot[s];
        }
}</pre>
              Tf f = INF_FLOW;
              for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
                     f = min
                            (f, edges[rt[i]].cap - edges[rt[i]].flow);
             flow += f; need -= f;
cost += f * dis[t]; fr = false;
swap(dis, pot);
if (need == 0) break;
       return make_pair(flow, cost);
}
// 限定 cost, 最大化 flow
pair<Tf, Tc> work_budget(int s_, int t_, Tc budget) {
    s = s_, t = t_; pot.assign(n, 0);
    Tf flow{}; Tc cost{}; bool fr = true;
    while ((fr ? spfa() : dijkstra())) {
        for (int i = 0; i < n; i++) {
            dis[i] += pot[i] - pot[s];
        }
              Tf f = INF_FLOW;
              for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
                     f = min
                             (f, edges[rt[i]].cap - edges[rt[i]].flow);
              f = min<Tf>(f, budget / dis[t]);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
```

5 String

5.1 KMP [cddfd9]

```
struct KMP {
       string sub;
       vector<int> failure;
       KMP(string sub_) {
   sub = sub_;
             failure.resize(sub.size(), -1);
             buildFailFunction();
       void buildFailFunction() {
    for (int i = 1; i < (int)sub.size(); i++) {
        int now = failure[i - 1];
}</pre>
                    while (now != -1
                   && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
             }
      vector<int> match(string &s) {
             vector<int> match;
             for (int i = 0, now = -1; i < (int)s.size(); i++) {
    // now is the compare sucessed length -1
    while (s[i] !=</pre>
                            sub[now + 1] \&\& now != -1) now = failure[now];
                   // failure stores if comparison fail, move to where
if (s[i] == sub[now + 1]) now++;
if (now + 1 == (int)sub.size()) {
                          match.push_back(i - now);
now = failure[now];
                   }
             return match:
};
```

5.2 Z Function [8dd6ac]

```
| // z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
|// 的最長公共前綴 (LCP) 的長度
vector <int > Z(string s) {
    int n = s.size();
    vector <int > z(n);
    z[0] = n;
    for (int i = 1, j = 1; i < n; i++) {
        z[i] = max(0, min(j + z[j] - i, z[i - j]));
        while (i + z[i] < n && s[z[i]] == s[i + z[i]]) {
        z[i]++;
        }
        if (i + z[i] > j + z[j]) {
              j = i;
        }
    }
    return z; // 最後一格不算
```

5.3 SA [32e429]

```
struct SuffixArray {
    int n; vector<int> sa, rk, lc;
    // n: 字串長度
    // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
     // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
    // lc: LCP
    數組, lc[i] 表示 sa[i] 和 sa[i+1] 的最長公共前綴長度
SuffixArray(const string &s) {
         n = s.length();
         sa.resize(n);
lc.resize(n - 1);
          rk.resize(n);
         iota(sa.begin(), sa.end(), 0);
         rota(sa.begin(), sa.ein(), 0),
sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });
rk[sa[0]] = 0;
for (int i = 1; i < n; ++i)</pre>
              rk[sa[i]]
                      = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
         int k = 1;
vector < int > tmp, cnt(n);
          tmp.reserve(n);
          while (rk[sa[n - 1]] < n - 1) {
              tmp.clear();
for (int i = 0; i < k; ++i)</pre>
                   tmp.push_back(n - k + i);
```

```
for (auto i : sa)
    if (i >= k)
                            tmp.push_back(i - k);
                 fill(cnt.begin(), cnt.end(), 0);
for (int i = 0; i < n; ++i)
                       ++cnt[rk[i]];
                 for (int i = 1; i < n; ++i)
   cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; --i)
                      sa[--cnt[rk[tmp[i]]]] = tmp[i];
                 swap(rk, tmp);
                 rk[sa[0]] = 0;
                 for (int i = 0, j = 0; i < n; ++i) {
   if (rk[i] == 0) {</pre>
                 j = 0;
} else {
                      for (j
                            -= j > 0; i + j < n && sa[rk[i] - 1] + j
< n && s[i + j] == s[sa[rk[i] - 1] + j]; )
                      lc[rk[i] - 1] = j;
                 }
           }
      }
1:
```

5.4 Duval Algorithm [f9dcca]

```
// duval_algorithm
 // 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
 vector<string> duval(string s) {
  int i = 0, n = s.size();
  vector<string> res;
       while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
}</pre>
                   else k++;
             while (i <= k) {</pre>
                  res.push_back(s.substr(i, j - k));
i += j - k;
       return res:
 }
 // 最小旋轉字串
 string min_round(string s) {
       s += s;
int i = 0, n = s.size();
       int start = i;
       while (i < n / 2) {
            start = i;
             int k = i, j = i + 1;
while (s[k] <= s[j] && j < n) {
   if (s[k] < s[j]) k = i;</pre>
                   else k++;
             while (i <= k) {
                  i += j - k;
       return s.substr(start, n / 2);
 }
```

5.5 Manacher [9c9ca6]

```
| // 1 2 1 2 5 2 1 2 1
| // 值 -1 代表原回文字串長度
| // (id - val + 1) / 2 可得原字串回文開頭
|}
```

5.6 Trie [3b3aa0]

```
struct Trie {
     struct trie_node {
   bool is_word;
           vector < trie_node *> children;
trie_node() {
   is_word = false;
   children.resize(26, NULL);
      trie_node *root = new trie_node();
            insert(string &s) {
           trie_node *cur = root;
for (int i = 0; i < s.size(); i++) {
   int idx = s[i] - 'a';
                 if (cur->children[idx] == NULL) {
    cur->children[idx] = new trie_node();
                 cur = cur->children[idx];
            cur->is_word = true;
     bool is_in_trie(string &s) {
    trie_node *cur = root;
            for (int i = 0; i < s.size(); i++) {</pre>
                 if (cur->
                 children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
            return true:
      int search_i_start(string &s, int i, vector<int> &dp) {
           trie_node *cur = root;
int sz = s.size(), ans = 0;
for (int j = i; j < sz; j++) {</pre>
                 (ans += dp[j + 1]) %= mod;
            return ans;
     }
};
int main() {
      // 找到 sub 集合裡,可以重複用,組成 s 的組數
      Trie trie;
      string s; cin >> s;
     int sz = s.size();
// dp 代表 i 開頭到最後的配對總數
     // 找到有結尾為 stop 的 dp[i] += dp[j + 1]
int n; cin >> n;
vector <int> dp(sz + 1, 0);
for (int i = 0; i < n; i++) {
    string sub; cin >> sub;
            trie.insert(sub);
     dp[sz] = 1;
for (int i = sz - 1; i >= 0; i--) {
    dp[i] = trie.search_i_start(s, i, dp);
     cout << dp[0] << endl;
```

6 Math

6.1 質因數分解 [ee1622]

```
mp[is_prime[q]]++;
    q /= is_prime[q];
}
if (q != 1) mp[q]++;
for (auto [a, b] : mp) {
    ans *= b + 1;
}
cout << ans << "\n";
}</pre>
```

```
6.2 模除計算 [9b1014]
using i64 = long long;
template < class T>
constexpr T power(T a, i64 b) {
     T res = 1;
for (; b; b /= 2, a *= a) {
    if (b % 2) {
              res *= a;
         }
     return res;
}
constexpr i64 mul(i64 a, i64 b, i64 p) {
   i64 res = a * b - i64(1.L * a * b / p) * p;
   res %= p;
   if (res < 0) {</pre>
          res += p;
     return res:
template < i64 P>
struct MLong {
     i64 x;
     constexpr MLong() : x{} {}
constexpr MLong(i64 x) : x{norm(x % getMod())} {}
     static i64 Mod;
     constexpr static i64 getMod() {
   if (P > 0) {
              return P;
          } else {
              return Mod;
     constexpr static void setMod(i64 Mod ) {
     constexpr i64 norm(i64 x) const {
          if (x < 0) {
              x += getMod();
          if (x >= getMod()) {
              x -= getMod();
          return x;
     constexpr i64 val() const {
          return x:
     explicit constexpr operator i64() const {
          return x:
     constexpr MLong operator-() const {
          MLong res;
res.x = norm(getMod() - x);
          return res;
     constexpr MLong inv() const {
   assert(x != 0);
          return power(*this, getMod() - 2);
     constexpr MLong &operator*=(MLong rhs) & {
          x = mul(x, rhs.x, getMod());
return *this;
     constexpr MLong &operator+=(MLong rhs) & {
          x = norm(x + rhs.x);
          return *this;
     constexpr MLong &operator -= (MLong rhs) & {
         x = norm(x - rhs.x);
return *this;
     constexpr MLong &operator/=(MLong rhs) & {
    return *this *= rhs.inv();
     friend constexpr MLong operator*(MLong lhs, MLong rhs) {
   MLong res = lhs;
   res *= rhs;
          return res
     friend constexpr MLong operator+(MLong lhs, MLong rhs) {
          MLong res = lhs;
          res += rhs;
          return res;
     friend constexpr MLong operator - (MLong lhs, MLong rhs) {
          MLong res = lhs;
```

return res;

```
friend constexpr MLong operator/(MLong lhs, MLong rhs) {
             MLong res = lhs;
res /= rhs;
             return res;
       friend
              constexpr istream &operator>>(istream &is, MLong &a) {
             is >> v;
a = MLong(v);
             return is;
       friend constexpr
               ostream & operator < < (ostream &os, const MLong &a) {
             return os << a.val();</pre>
       friend constexpr bool operator==(MLong lhs, MLong rhs) {
    return lhs.val() == rhs.val();
       friend constexpr bool operator!=(MLong lhs, MLong rhs) {
   return lhs.val() != rhs.val();
 };
 i64 MLong < 0LL >:: Mod = i64(1E18) + 9;
 constexpr i64 P = 998244353;
using Z = MLong<P>;
// using Z = MLong<0LL>; // change Mod
 struct Comb {
       i64 n;
       to4 i;
vector <Z> _fac;
vector <Z> _invfac;
vector <Z> _inv;
Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
Comb(i64 n) : Comb() { init(n); }
       void init(i64 m) {
            int(to4 m) {
    m = min(m, Z::getMod() - 1);
    if (m <= n) return;
    _fac.resize(m + 1);
    _invfac.resize(m + 1);</pre>
             _inv.resize(m + 1);
             for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;</pre>
             for (int i = m; i > n; i--) {
    _invfac[i - 1] = _invfac[i] * i;
    _inv[i] = _invfac[i] * _fac[i - 1];
}
             n = m;
      }
Z fac(i64 m) {
    if (m > n) init(2 * m);
    return _fac[m];
       If Z invfac(i64 m) {
    if (m > n) init(2 * m);
    return _invfac[m];
       Z inv(i64 m) {
    if (m > n) init(2 * m);
    return _inv[m];
       return fac(n) * invfac(m) * invfac(n - m);
       Z Lucas(Z m, Z n)
             |} comb; // 注意宣告, 若要換模數需重新宣告
```

6.3 中國餘數定理 [d41d8c]

```
ll exgcd(ll a, ll b, ll &x, ll &y) {
    if (!b) {
        x = 1, y = 0;
        return a;
    }

    ll g = exgcd(b, a % b, y, x);
    y -= a / b * x;
    return g;
}

ll inv(ll x, ll m){
    ll a, b;
    exgcd(x, m, a, b);
    a %= m;
    if (a < 0) a += m;
    return a;
}
// remain, mod
ll CRT(vector < pair < ll, ll >> &a) {
    ll prod = 1;
    for (auto x : a) {
```

```
prod *= x.second;
}
ll res = 0;
for (auto x : a) {
    auto t = prod / x.second;
    res += x.first * t % prod * inv(t, x.second) % prod;
    if(res >= prod) res -= prod;
}
return res;
```

6.4 矩陣與快速幂 [08b5fe]

```
template < class T >
struct Mat {
       int m, n;
       constexpr static ll mod = 1e9 + 7;
      Mat(vector<T>> matrix;
Mat(int n_ = 0) { init(n_, n_); }
Mat(int m_, int n_) { init(m_, n_); }
Mat(vector<vector<T>> matrix_) { init(matrix_); }
       void init(int m_, int n_) {
    m = m_; n = n_;
    matrix.assign(m, vector<T>(n));
       void init(vector<vector<T>> &matrix_) {
             m = matrix_.size();
n = matrix_[0].size();
             matrix = matrix_;
      vector<vector<T>> unit(int n) { // 單位矩|
vector<vector<T>> res(n, vector<T>(n));
for (int i = 0; i < n; i++) {
res[i][i] = 1;
                                                            // 單位矩陣
       constexpr Mat & operator *=(const Mat& rhs) & {
    assert(matrix[0].size() == rhs.matrix.size());
             int m = matrix.size()
            matrix = ans.matrix:
             return *this;
       constexpr Mat &operator^=(ll p) & {
   assert(m == n);   assert(p >= 0);
   Mat ans(p-- == 0 ? unit(m) : matrix);
             while (p > 0) {
   if (p & 1) ans *= *this;
   *this *= *this;
                   p >>= 1;
             matrix = ans.matrix;
return *this;
       friend Mat operator*(Mat lhs, const Mat &rhs) {
             return lhs:
       friend Mat operator^(Mat lhs, const ll p) {
             lhs ^= p;
return lhs;
};
// fn = fn-3 + fn-2 + fn-1
軸 较量
// 初始矩陣 轉移式
// f4 f3 f2 1 1 0 f5 f4 f3
// f3 f2 f1 1 0 1 => f4 f3 f2
// f2 f1 f0 1 0 0 f3 f2 f1
```

6.5 樹論分塊 [06204a]

Mobius Theorem 6.6

- 數論分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在O(1)內計算f(r)-f(l)或已經預處理 出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d|n} \mu(d) = \begin{cases} 1 & \text{for } n = 1 \\ 0 & \text{for } n \neq 0 \end{cases}$$

2. μ是常數函數1的反元素

 $\Rightarrow \mu*1=\epsilon, \epsilon(n)$ 只在n=1 時為 1 ,其餘情況皆為 0 \circ $-\phi$ 歐拉函數: x 以下與 x 互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^{i}) \\ &= 1 + p^{0}(p-1) + p^{1}(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^{c} \\ &= id \end{split}$$

• 莫比烏斯反演公式

-
$$f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$$

- $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

例子

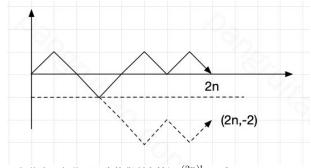
$$\begin{split} &\sum_{i=a}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \sum_{d \mid gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

莫比烏斯反演 [d41d8c]

const int maxn = 2e5;

```
ll mobius_pref[maxn];
void init() {
        mobius_pref[1] = 1;
vector<ll> wei
        (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
    }
                         continue; // 包含平方
                 if (wei[i] == 0) {
                         wet[i] == 0; {
wet[i] = 1;
for (ll j = 2; i * j < maxn; j++) {
    if (j % i == 0) wet[i * j] = -1;
    else if (wet[i * j] != -1) wet[i * j]++;</pre>
                         }
                 mobius_pref[i]
                           = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
       }
void solve() {
       is solve() {
    ll a, b, c, d, k; cin >> a >> b >> c >> d >> k;
    auto cal = [&](ll x, ll y) -> int {
        int res = 0;
        for (int l = 1, r; l <= min(x, y); l = r + 1) {
            r = min(x / (x / l), y / (y / l));
            res += (mobius_pref[r] - mobius_pref[l]</pre>
                                      - 1]) * (x / l) * (y / l); // 代推出來的式子
                 return res:
```

Catalan Theorem 6.8



1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$

2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2)假設往上有x個,往下有y個,會有:

$$\begin{cases} x + y = 2n \\ y - x = 2 \end{cases} \Rightarrow \begin{cases} x = n - 1 \\ y = n + 1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.9 Burnside's Lemma

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

- G:各種翻轉操作所構成的置換群
- · X/G:本質不同的方案的集合
- X^g :對於某一種操作g,所有方案中,經過g這種翻轉後保持不變的方案 的集合
- 集合取絕對值代表集合數

Search and Gready

7.1 二分搜 [d41d8c]

```
int main() {
   int l = 1, r = 10;
   // 1 to tar, find tar
   while (l <= r) {
      int m = (l + r) / 2;
}</pre>
              if (check(m)) l = m + 1;
              else r = m - 1;
       cout << r;
        // tar to end
       while (l <= r) {
   int m = (l + r) / 2;
              if (check(m)) r = m - 1;
else l = m + 1;
       cout << l;
```

7.2 三分搜 [d41d8c]

```
// 找極值問題,遞增遞減
void solve() {
    int l = 0, r = 10, ans = 0; // ans 紀錄答案 while (l <= r) {
         int d = (r - l) / 3; // 差
         int ml = l + d, mr = r - d; // mr 要用減的
auto cal = [&](int m) -> int {
             int x = 0;
                           // 計算答案
              return x;
         int ansl = cal(ml), ansr = cal(mr);
         if (ansl < ansr) {
    l = ml + 1;
         else r = mr - 1;
    }
```

8 Tree

8.1 LCA [9f95b1]

```
vector < vector < int >> par(maxn, vector < int > (18));
 vector < int > depth(maxn + 1);
vector < int > dfn(maxn);
vector < int > dfn(maxn);
void build_lca(int n, vector < vector < pair < int , int >>> & tree) {
    auto dfs = [&](auto self, int u, int pre) -> void {
        for (auto [v, w] : tree[u]) {
            if (v == pre) continue;
            par[v][0] = u; // 2 ^ 0
            depth[v] = depth[u] + 1;
            self(self, v, u);
}
                          }
```

```
};
dfs(dfs, 1, 0);
for (int i = 1; i <= 18; i++) {
    for (int j = 1; j <= n; j++) {
        par[j][i] = par[par[j][i - 1]][i - 1];
    }
}
int lca(int a, int b) {
    if (depth[a] < depth[b]) swap(a, b);
    int pull = depth[a] - depth[b];
    for (int i = 0; i < 18; i++) {
        if (pull & (1 << i)) {
            a = par[a][i];
        }
}
if (a == b) return a;
for (int i = 17; i >= 0; i--) {
        if (par[a][i] != par[b][i]) {
            a = par[a][i], b = par[b][i];
        }
}
return par[a][0];
}
```

8.2 樹重心 [30b436]

```
struct centroid_decomposition {
      vector<vector<int>> adi:
      vector<bool> vis;
      vector<int> siz;
      centroid_decomposition() {}
centroid_decomposition(int n_) { init(n_); }
      void init(int n_) {
           n = n_;
adj.assign(n, {});
vis.assign(n, false);
siz.assign(n, 1);
      void addEdge(int u. int v) {
            adj[u].push_back(v);
adj[v].push_back(u);
      void get_siz(int dep, int x, int p = -1) {
           | get_stz(int dep, see ),
siz[x] = 1;
for (int y : adj[x]) {
    if (y == p || vis[y]) continue;
      get_siz(dep + 1, y, x);
    siz[x] += siz[y];
      return get_cen(y, sz, x);
            return x;
      void work(int x = 0) {
            get_siz(0, x);
int cen = get_cen(x, siz[x]);
vis[cen] = true;
            // do something
for (int y : adj[cen]) {
   if (vis[y]) continue;
                  work(y);
};
```

8.3 樹壓平 [51199c]

8.4 Heavy Light Decomposition [ad25b6]

```
int n, cur;
vector<int> siz, top, dep, parent, in, out, seq;
vector <vector <int>> adj;
HLD(int n_ = 0) { init(n_); }
void init(int n_ = 0) {
    n = n_; cur = 0;
    siz.resize(n); top.resize(n); dep.resize(n);
    percept resize(n); in resize(n); out resize(n)
     parent.resize(n); in.resize(n); out.resize(n);
     seq.resize(n); adj.assign(n, {});
void addEdge(int u, int v) {
   adj[u].push_back(v);
     adj[v].push_back(u);
void work(int root = 0) {
     top[root] = root;
dep[root] = 0;
     parent[root] =
     dfs1(root); dfs2(root);
void dfs1(int u) {
     if (parent[u] != -1)
           adj[u].erase(find
                 (adj[u].begin(), adj[u].end(), parent[u]));
     for (auto &v : adj[u]) {
   parent[v] = u, dep[v] = dep[u] + 1;
           dfs1(v);
           siz[u] += siz[v];
           if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
          } // 讓 adj[u][0] 是重子節點
    }
void dfs2(int u) {
     in[u] = cur++;
     seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
           top[v] = v = adj[u][0] ? top[u] : v;
           dfs2(v);
     out[u] = cur;
u = parent[top[u]];
} else {
                v = parent[top[v]];
          }
     return dep[u] < dep[v] ? u : v;</pre>
int dist(int u. int v) {
     return dep[u] + dep[v] - 2 * dep[lca(u, v)];
int jump(int u, int k) {
    if (dep[u] < k) return -1;
    int d = dep[u] - k;
    while (dep[top[u]] > d)
        u = parent[top[u]];
    return seq[in[u] - dep[u] + d];
bool isAncester(int u. int v) {
     // 判斷 u 是否是 v 的祖先
return in[u] <= in[v] && in[v] < out[u];
int rootedParent(int u, int v) {
     // 根據新根節點 u 計算 v 的父節點
```

swap(u, v);

```
if (u == v) return u;
    if (!isAncester(u, v)) return parent[u];
    auto it = upper_bound(adj
        [u].begin(), adj[u].end(), v, [&](int x, int y) {
        return in[x] < in[y];
    }) - 1;
    return *it;
}
int rootedSize(int u, int v) {
        // 根據新根節點 u 計算子樹 v 的大小
        if (u == v) return n;
        if (!isAncester(v, u)) return siz[v];
        return n - siz[rootedParent(u, v)];
}
int rootedLca(int a, int b, int c) {
        // 根據新的根節點計算三個節點 a \ b 和 c 的最近公共祖先
        return lca(a, b) ^ lca(b, c) ^ lca(c, a);
}

8.5 Link Cut Tree [c26f51]

#include <bits/stdc++.h>
```

```
using namespace std;
using i64 = long long;
constexpr i64 Mod = 51061;
struct Tag {
    i64 add = 0;
     i64 \text{ mul} = 1;
    void apply(const Tag& v) {
   mul = mul * v.mul % Mod;
   add = (add * v.mul % Mod + v.add) % Mod;
struct Info {
    i64 val = 1;
i64 sum = 1;
    void apply(int size, const Tag &v) {
   val = (val * v.mul % Mod + v.add) % Mod;
   sum = (sum * v.mul % Mod + v.add * size % Mod) % Mod;
    }
};
struct Node {
     Node *ch[2], *p;
     int rev = 0;
int size = 1;
     void make_rev() {
         swap(ch[0], ch[1]);
         rev ^= 1;
     Node() : ch {nullptr, nullptr}, p(nullptr) {}
     Info info = Info();
    Tag tag = Tag();
    void apply(const Tag &v) {
          info.apply(size, v);
          tag.apply(v);
    if (ch[1]) ch[1]->make_rev();
              rev = 0;
          if (ch[0]) {
              ch[0]->apply(tag);
          if (ch[1]) {
              ch[1]->apply(tag);
          tag = Tag();
     void pull_info() {
         };
bool isroot(Node *t) {
           == nullptr || (t->p->ch[0] != t && t->p->ch[1] != t);
int pos(Node *t) { // 回傳 1 代表是右子節點 return t->p->ch[1] == t;
void rotate(Node *t) {
    Node *q = t->p;
int x = !pos(t);
     q->ch[!x] = t->ch[x];
if (t->ch[x]) {
    t->ch[x]->p = q;
     t->p = q->p;
     if (!isroot(a)) {
         q->p->ch[pos(q)] = t;
```

```
t - ch[x] = q;
     q->p =
     q->pull_info();
}
void splay(Node *t) { // 單點修改前必須呼叫
     // 把 t 旋轉到目前 splay 的根while (!isroot(t)) {
    Node *p = t->p;
    p->push_tag();
    t->push_tag();
          rotate(t):
     t->push_tag();
     t->pull_info();
void access(Node *t) {
     // 把從根到 t 的所有點都放在一條實鏈裡, 使根
     // 到 t 成為一條實路徑,並且在同一棵 splay 裡 for (Node *i = t, *q = nullptr; i; q = i, i = i->p) {
          splay(i);
          i->ch[1] = q;
     splay(t);
}
void makeRoot(Node *t) { // 使 t 點成為其所在樹的根
     access(t);
swap(t->ch[0], t->ch[1]);
t->rev ^= 1;
Node* findRoot(Node *t) { // 找到 t 的 root
     access(t);
     splay(t);
     t->push_tag();
     while (t->ch[0]) {
    t = t->ch[0];
          t->push_tag();
     splay(t);
     return t;
void link(Node *t, Node *p) {
     makeRoot(t);
     if (findRoot(p) != t) {
          makeRoot(p);
          t->p = p;
p->pull_info();
     }
}
bool cut(Node *x, Node *y) { // 不存在邊,回傳 false
     makeRoot(x);
     access(v);
     if (y->ch[0] != x || x->ch[1]) return false;
y->ch[0]->p = nullptr;
y->ch[0] = nullptr;
     y->pull_info();
     return true;
void split(Node
       *x, Node *y) { // 以 y 做根, 區間修改用, apply 在 y 上
     makeRoot(x);
     access(y);
     splay(y);
bool isconnected(Node *x, Node *y) { // 查詢有沒有連通
     makeRoot(x);
     return findRoot(x) == findRoot(y);
}
int main() {
     int n; cin >> n;
vector <Node *> nodes(n);
     for (int i = 0; i < n; i++) {
    nodes[i] = new Node();
    nodes[i]->info.val = nodes[i]->info.sum = 1LL;
     for (int i = 0; i < n - 1; i++) {
          int u, v; cin >> u >> v;
          link(nodes[u], nodes[v]):
     for (int i = 0; i < q; i++) {
          char op; cin >> op;
if (op == '+') {
                int u, v; cin >> u >> v;
                split(nodes[u], nodes[v]);
               Tag tag;
cin >> tag.add;
tag.add % Mod;
                nodes[v]->apply(tag);
          else if (op == '-') {
   int u1, v1; cin >> u1 >> v1;
   int u2, v2; cin >> u2 >> v2;
   u1--; v1--; u2--; v2--;
   cut(nodes[u1], nodes[v1]);
                link(nodes[u2], nodes[v2]);
```

```
else if (op == '*') {
                                                                                                                         vis.assign(n, -1); rev.resize(n);
pa.resize(n); rt.resize(n);
mn.resize(n); res.resize(n);
                    int u, v; cin >> u >> v;
                    u--: v--
                     split(nodes[u], nodes[v]);
                     Tag tag;
                                                                                                                    void add_edge(int u, int v) { adj[u].push_back(v); }
                                                                                                                   cin >> tag.mul;
tag.mul % Mod;
nodes[v]->apply(tag);
              else {
                    int u, v; cin >> u >> v;
                                                                                                                         rt[v] = p;
return x ? p : mn[v];
                    split(nodes[u], nodes[v]);
cout << nodes[v]->info.sum << "\n";</pre>
                                                                                                                   void dfs(int v) {
    vis[v] = id, rev[id] = v;
    rt[id] = mn[id] = sdom[id] = id, id++;
    vis[v] = vis[v] f
       }
                                                                                                                          for (int u : adj[v]) {
   if (vis[u] == -1) dfs(u), pa[vis[u]] = vis[v];
       return 0;
}
                                                                                                                                radj[vis[u]].push_back(vis[v]);
 8.6 Virtual Tree [622e69]
                                                                                                                    void build(int s) {
                                                                                                                         dfs(s);
for (int i = id - 1; i >= 0; i--) {
    for (int u : radj[i])
| // 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
 // 可以建立虚樹達成快速樹 DP
 // 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector <int>stk(maxn);
                                                                                                                                sdom[i] = min(sdom[i], sdom[query(u, 0)]);
if (i) bucket[sdom[i]].push_back(i);
for (int u : bucket[i]) {
 int p = query(u, 0);
dom[u] = sdom[p] == i ? i : p;
                                                                                                                                if (i) rt[i] = pa[i];
                                                                                                                         res.assign(n, -1);

for (int i = 1; i < id; i++)
       vt[l].push_back(stk[top]);
stk[top] = l;
} else vt[l].push_back(stk[top--]);
                                                                                                                         if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];
for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre>
        stk[++top] = u;
                                                                                                                          res[s] = s;
                                                                                                                          for (int i = 0; i < n; i++) dom[i] = res[i];</pre>
 void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
                                                                                                                   }
                                                                                                            };
       vt[u].clear();
                                                                                                             9
                                                                                                                     DP
 void solve(int n, int q) {
       vector g(n + 1, vector<pair<int, int>>());
                                                                                                             9.1 LCS [5781cf]
        vector vt(n + 1, vector<int>()); // dfs 完清除, 否則會退化
       vector<ll> dp(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;
                                                                                                             int main() {
                                                                                                                   int m, n; cin >> m >> n;
string s1, s2; cin >> s1 >> s2;
int L = 0;
              g[u].push_back({v, w});
g[v].push_back({u, w});
                                                                                                                   tnt L = 0,
vector < vector < int >> dp(m + 1, vector < int > (n + 1, 0));
for (int i = 1; i <= m; i++) {
    for (int j = 1; j <= n; j++) {
        if (s1[i - 1] == s2[j - 1])
            dp[i][j] = dp[i - 1][j - 1] + 1;
}</pre>
        build_lca(n, g);
       build(n, g);
for (int i = 0; i < q; i++) {</pre>
              int m; top = -1; cin >> m;
vector <int> key(m);
for (int j = 0; j < m; j++) {
    cin >> key[j];
                                                                                                                                else
                                                                                                                                       dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
                                                                                                                   int length = dp[m][n]; cout << length << "\n";
string s(length, 'c'); // backtracking
while (m >= 1 && n >= 1) {
    if (s1[m - 1] == s2[n - 1]) {
        s[length - 1] = s1[m - 1];
        m--, n--, length--;
}
                    iskey[key[j]] = 1;
              key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
              });
for (int x : key) insert(x, vt);
              while (top
> 0) vt[stk[top - 1]].push_back(stk[top]), --top;
                                                                                                                          else {
    if (dp[m - 1][n] > dp[m][n - 1]) m--;
              auto dfs = [&](auto self, int u) -> void {
                    for (auto v : vt[u]) {
    self(self, v);
                                                                                                                   cout << s << "\n";
                           if (iskey[v]) {
    dp[u] += min_dis[v];
                                                                                                             9.2 LIS [66d09f]
                                 // 砍掉 1 到 v 之間最短的路
                                                                                                             int main() {
                           delse {
   dp[u] += min(dp[v], min_dis[v]);
                                                                                                                   int n; cin >> n;
vector <int> v(n);
for (int i = 0; i < n; i++) cin >> v[i];
int dp[n]; vector <int> stk;
                           }
iskey[v] = dp[v] = 0;
                                                                                                                   stk.push_back(v[0]);
                    vt[u].clear();
                                                                                                                   dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) {
    if (v[i] > stk.back()) {
        stk.push_back(v[i]);
        dp[i] = ++L;
}
              dfs(dfs, key[0]); // key[0] 一定是 root cout << dp[key[0]] << "\n";
              iskey[key[0]] = dp[key[0]] = 0;
                                                                                                                         } else {
                                                                                                                                auto it
                                                                                                                                          = lower_bound(stk.begin(), stk.end(), v[i]);
 8.7 Dominator Tree [baa540]
                                                                                                                                *it = v[i]; dp[i] = it - stk.begin() + 1;
                                                                                                                         }
 struct Dominator_tree {
                                                                                                                   vector < int > ans; cout << L << "|n";
for (int i = n - 1; i >= 0; i--) {
    if (dp[i] == L) {
        int n. id:
        vector<vector<int>> adj, radj, bucket;
       vector < vector < int> > adj, radj, bucket;
vector < int> sdom, dom, vis, rev, pa, rt, mn, res;
Dominator_tree(int n_ = 0) { init(n_); }
void init(int _n) {
    n = _n, id = 0;
    adj.assign(n, vector < int>());
    radj.assign(n, vector < int>());
    bucket.assign(n, vector < int>());
    sdom.resize(n); dom.assign(n, -1);
                                                                                                                                ans.push_back(v[i]), L--;
```

for (auto i : ans) cout << i <<</pre>

9.3 Edit Distance [308023]

9.4 Bitmask [a626f9]

```
void hamiltonianPath(){
      int n, m; cin >> n >> m;
vector adj(n, vector<int>());
      for (int i = 0; i < m; i++) {
  int u, v; cin >> u >> v;
  adj[--v].push_back(--u);
      ·
// 以...為終點,走過...
      vector dp(n, vector<int>(findBit(n)));
     vector dp(n, vector<int>(((())))
dp[0][1] = 1;
for (int mask = 1; mask < findBit(n); mask++) {
    if ((mask & 1) == 0) continue;
    for (int i = 0; i < n; i++) {
        if ((mask & findBit(i)) == 0) continue;
        if (i == n - 1 && mask != findBit(n) - 1) continue;
        int pre_mask = mask ^ findBit(i);
        for (int i : adj[i]) {</pre>
                  for (int j : adj[i]) {
   if ((pre_mask & findBit(j)) == 0) continue;
                        dp[i][mask
                                ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
            }
      cout << dp[n - 1][findBit(n) - 1] << "\n";
void elevatorRides() {
      int n, x; cin >> n >> x; vector<int> a(n);
for (int i = 0; i < n; i++) cin >> a[i];
      vector<array<int, 2>> dp(findBit(n));
     }
      cout << dp[findBit(n) - 1][0] << "\n";
}
```

9.5 Projects [0942aa]

```
int main() { // 排程有權重問題,輸出價值最多且時間最少
struct E {
    int from, to, w, id;
    bool operator <(const E &rhs) {
        return to == rhs.to ? w > rhs.w : to < rhs.to;
};
int n; cin >> n; vector <E> a(n + 1);
for (int i = 1; i <= n; i++) {
        int u, v, w; cin >> u >> v >> w;
        a[i] = {u, v, w, i};
}
vector <array < ll, 2>> dp(n + 1); // w, time
vector <array < int, 2>> rec(n + 1); // 有沒選, 上個是誰
sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
        auto it = --lower_bound(all(a), E({0, a[i].from}),
        [](E x, E y){ return x.to < y.to; });
        int id = it - a.begin(); dp[i] = dp[i - 1];
        ll nw = dp[id][0] + a[i].w;</pre>
```

```
16
          ll nt = dp[id][1] + a[i].to - a[i].from;
if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
     dp[i] = {nw, nt}; rec[i] = {1, id};
      }
      vector < int > ans;
for (int i = n; i != 0;) {
    if (rec[i][0]) {
               ans.push_back(a[i].id);
               i = rec[i][1];
          } else i--:
     }
}
 9.6 Removal Game [7bb56b]
1// 兩個人比賽,每個人輪流取一個數字且只能是頭尾
 // 問兩人都選得好,第一出手的人可取得的最大分數
 int main() {
      int n; cin >> n;
vector<ll> a(n);
      for (int i = 0; i < n; i++) cin >> a[i];
      vector dp(n, vector<ll>(n)); // i 到 j 區間的最大 diff
for (int i = n - 1; i >= 0; i--) {
    dp[i][i] = a[i];
    for (int j = i + 1; j < n; j++)
               dp[i][j] =
                     max(a[i] - dp[i + 1][j], a[j] - dp[i][j - 1]);
      ^{\prime}// x + y = sum; // x - y = dp[0][n - 1] cout << (accumulate
            (a.begin(), a.end(), 0LL) + dp[0][n - 1]) / 2 << "\n";
}
9.7 Codeforces Example [7d37ea]
| // 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
 // 請問在線段不重複的情況下,最多獲得幾分 int main() {
      int n, m;
cin >> n >> m;
      // 記錄每點有幾個線段
      // 再一個紀錄,包含這個點的左界
      cnt[l]++;
          cnt[r + 1]--:
      for (int i = 2; i <= n; i++) {
          cnt[i] += cnt[i - 1];
      for (int i = n; i >= 2; i--) {
           l_side[i - 1] = min(l_side[i - 1], l_side[i]);
      vector<int> dp(n + 1);
      dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
          dp[i] = cnt[i];
if (l_side[i] != inf) {
               dp[i] += dp[l_side[i] - 1];
          dp[i] = max(dp[i], dp[i - 1]);
      cout << dp[n] << "\n":
 // CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
 // 再加上 max(bi) - min(bi)
 int main(){
   int n, k, ans = 0; cin >> n >> k;
   vector<pii> v(n + 1);
      for (int i = 1; i <= n; i++) {
  int a, b; cin >> a >> b;
  v[i] = {a, b};
  if (a <= k) ans = 1;</pre>
      sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
    return a.second < b.second;</pre>
      }); // 用 bi 來排,考慮第 i 個時可以先扣
      vector<vector<int>> dp(n + 1, vector<int>(n + 1, inf));
      // 考慮 v[i] 時, 選 j 個的 sum(ai) - min(bi)
     for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
               // min(不選, 選)
if (dp[i
                     - 1][j - 1] + v[i].first + v[i].second <= k) {
                     // 假如可以選,更新 ans 時再加回去 bi
```

ans = max(ans, j);

cout << ans << endl:

dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);

9.8 CHT [5f5c25]

```
struct Line {
    ll m, b;
    Line(ll m = 0, ll b = 0) : m(m), b(b) {}
    ll eval(ll x) {
        return m * x + b;
    }
}
}:
struct CHT { // 用在查詢單調斜率也單調
  int n, lptr, rptr; vector<Line> hull;
  CHT(int n_ = 0, Line init_ = Line()) {
         init(n_, init_);
     void init(int n_ = 0, Line init_ = Line()) {
    n = n_; hull.resize(n); reset(init_);
     void reset(Line init_ = Line()) {
    lptr = rptr = 0; hull[0] = init_;
     bool pop_front(Line &l1, Line &l2, ll x) {
         // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y
         // 代表查詢的當下,右線段的高度已經低於左線段了
return ll.eval(x) >= l2.eval(x);
     bool pop_back(Line &l1, Line &l2, Line &l3) {
         // 本題斜率遞減、上凸包
         // 因此只要 12 跟
         l3 的 X 交點 <= l1 跟 l3 的 X 交點, l2 就用不到了
return (l3.b - l2.b)
* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
    hull[++rptr] = L;
    };
```

9.9 DNC [61c639]

9.10 LiChaoSegmentTree [a6e320]

```
| constexpr ll Inf = 4e18;

|// dp[i] = min(f[j] * s[i] + dp[j])

|// y = m x + b

| struct Line {

| ll m, b;

| Line(ll m = 0, ll b = Inf) : m(m), b(b) {}

| ll eval(ll x) const { return m * x + b; }

};

| struct LiChaoSeg { // 取 max 再變換就好

| int n;

| vector<Line> info;

| LiChaoSeg(int n_ = 0) { init(n_); }

| void init(int n_ = 0) {

| n = n_;

| info.assign(4 << __lg(n), Line());

| }

| void update(Line line, int node, int l, int r) {

| int m = (l + r) / 2;

| bool left = line.eval(l) < info[node].eval(l);
```

```
| bool mid = line.eval(m) < info[node].eval(m);
| if (mid) swap(info[node], line); // 如果新線段比較好
| if (r - l == 1) return;
| else if (left != mid) update(line, 2 * node, l, m);
| // 代表左半有交點
| else update(line, 2 * node + 1, m, r);
| // 代表如果有交點一定在右半
| void add_line(Line line) { update(line, 1, 0, n); }
| ll query(int x, int node, int l, int r) {
| if (r - l == 1) return info[node].eval(x);
| int m = (l + r) / 2;
| if (x < m) return
| min(info[node].eval(x), query(x, 2 * node, l, m));
| else return min(
| info[node].eval(x), query(x, 2 * node + 1, m, r));
| }
| ll query(int x) { return query(x, 1, 0, n); }
| ;
```

10 Geometry

10.1 Basic [d41d8c]

```
template < class T>
struct Point {
     Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) \{ \}
     template < class U >
operator Point < U > () {
         return Point<U>(U(x), U(y));
     Point & operator += (const Point &p) & {
         x += p.x;
y += p.y;
return *this;
     Point &operator -= (const Point &p) & {
         x -= p.x;
y -= p.y;
return *this;
     Point & operator *= (const T &v) & {
         x *= v;
y *= v;
return *this;
     Point & operator /= (const T &v) & {
         x /= v;
y /= v;
          return *this;
     Point operator -() const {
    return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
     friend Point operator - (Point a, const Point &b) {
          return a -= b;
     friend Point operator*(Point a, const T &b) {
  return a *= b;
     friend Point operator/(Point a, const T &b) {
          return a /= b;
     friend Point operator*(const T &a, Point b) {
          return b *= a;
     friend bool operator==(const Point &a, const Point &b) {
         return a.x == b.x && a.y == b.y;
     friend istream & operator >> (istream &is, Point &p) {
         return is >> p.x >> p.y;
     friend ostream & operator < < (ostream & os, const Point & p) {
   return os << "(" << p.x << ", " << p.y << ")";</pre>
};
template < class T>
struct Line {
    Point<T> a;
     Point<T> b;
     }:
template < class T>
T dot(const Point<T> &a, const Point<T> &b) {
    return a.x * b.x + a.y * b.y;
template < class T>
T cross(const Point<T> &a, const Point<T> &b) {
   return a.x * b.y - a.y * b.x;
```

```
template < class T>
T square(const Point < T > &p) {
     return dot(p, p);
template < class T>
double length(const Point < T > & p) {
    return sqrt(square(p));
template < class T>
double length(const Line<T> &l) {
    return length(l.a - l.b);
template < class T>
Point<T> normalize(const Point<T> &p) {
    return p / length(p);
template < class T>
bool parallel(const Line<T> &l1, const Line<T> &l2) {
   return cross(l1.b - l1.a, l2.b - l2.a) == θ;
template < class T>
double distance(const Point<T> &a, const Point<T> &b) {
    return length(a - b);
template < class T>
double distancePL(const Point<T> &p, const Line<T> &l) {
   return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0) {
     return distance(p, l.a);</pre>
     if (dot(p - l.b, l.a - l.b) < 0) {
          return distance(p, l.b);
     return distancePL(p. l):
template < class T>
Point<T> rotate(const Point<T> &a) {
    return Point(-a.y, a.x);
int sgn(const Point<T> &a) {
    return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
template < class T>
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
     return cross(l.b - l.a, p - l.a) > 0;
template < class T>
Point < T
      > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
     return l1.a + (l1.b - l1.a) * (cross(l2.b - l2.a, l1.a - l1.b));
template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
   return cross(p - l.a, l.b - l.a) == 0 &&
        min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)
                (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
     (const Point<T> &a, const vector<Point<T>> &p) {
     int n = p.size();
for (int i = 0; i < n; i++) {</pre>
          if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {
               return true:
    }
    int t = 0;
for (int i = 0; i < n; i++) {</pre>
          auto u = p[i];
auto v = p[(i + 1) % n];
          if (u.x < a.x
               && v.x >= a.x && pointOnLineLeft(a, Line(v, u))) {
               t ^= 1:
                 && v.x < a.x && pointOnLineLeft(a, Line(u, v))) {
               t ^= 1;
    }
     return t == 1;
```

```
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
tuple<int, Point<T>, Point<T>> segmentIntersection
  (const Line<T> &l1, const Line<T> &l2) {
  if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x)) {
    return {0, Point<T>(), Point<T>()};
}
      if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x)) {
    return {0, Point<T>(), Point<T>()};
       if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y)) {</pre>
            return {0, Point<T>(), Point<T>()};
      if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y)) {
    return {0, Point<T>(), Point<T>()};
      if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
    if (cross(l1.b - l1.a, l2.a - l1.a) != 0) {
        return {0, Point<T>(), Point<T>()};
}
            } else {
                   auto maxx1 = max(l1.a.x, l1.b.x);
                   auto minx1 = min(l1.a.x, l1.b.x);
                   auto maxy1 = max(l1.a.y, l1.b.y);
auto miny1 = min(l1.a.y, l1.b.y);
auto maxx2 = max(l2.a.x, l2.b.x);
                   auto minx2 = min(l2.a.x, l2.b.x);
auto maxy2 = max(l2.a.y, l2.b.y);
auto miny2 = min(l2.a.y, l2.b.y);
                   Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
if (!pointOnSegment(p1, l1)) {
                         swap(p1.y, p2.y);
                   if (p1 == p2) {
                         return {3, p1, p2};
                  } else {
                         return {2, p1, p2};
            }
       auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
      auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);
auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);
      if ((cp1 > 0 && cp2 > 0) || (cp1 < 0 && cp2 < 0) || (cp3 > 0 && cp4 > 0) || (cp3 < 0 && cp4 < 0)) {
             return {0, Point<T>(), Point<T>()};
      Point p = lineIntersection(l1, l2);
      if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
            return {1, p, p};
      } else {
            return {3, p, p};
}
template < class T>
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
   if (get<0>(segmentIntersection(l1, l2)) != 0) {
             return 0.0:
      return min({distancePS(l1.a, l2), distancePS(l1
              .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
}
 template<class T>
bool segmentInPolygon
       (const Line<T> &l, const vector<Point<T>> &p) {
       int n = p.size();
      if (!pointInPolygon(l.a, p)) {
            return false:
      if (!pointInPolygon(l.b, p)) {
            return false:
      for (int i = 0; i < n; i++) {
    auto u = p[i];
    auto v = p[(i + 1) % n];
    auto w = p[(i + 2) % n];</pre>
            auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
            if (t == 1) {
                  return false;
             if (t == 0) {
                   continue;
             if (t == 2) {
                   if (pointOnSegment(v, l) && v != l.a && v != l.b) {
   if (cross(v - u, w - v) > 0) {
      return false;
            if (pointOnLineLeft(l.a, Line(v, u))
```

```
|| pointOnLineLeft(l.b, Line(v, u))) {
                       return false:
             } else if (p1 == v) {
   if (l.a == v) {
                       if (pointOnLineLeft(u, l)) {
   if (pointOnLineLeft(w, l)
        && pointOnLineLeft
                                 (w, Line(u, v))) {
return false;
                            if (pointOnLineLeft(w, l)
                                 || pointOnLineLeft
                                      (w, Line(u, v))) {
                                 return false;
                            }
                  } else if (l.b == v) {
   if (pointOnLineLeft(u, Line(l.b, l.a))) {
                            if (pointOnLineLeft(w, Line(l.b, l.a))
    && pointOnLineLeft
                                 (w, Line(u, v))) {
return false;
                       } else {
                            (w, Line(u, v))) {
return false;
                  } else {
    if (pointOnLineLeft(u, l)) {
                            if (pointOnLineleft(w, Line(l.b, l.a))
                                 || pointOnLineLeft
                                 (w, Line(u, v))) {
return false;
                       } else {
   if (pointOnLineLeft(w, l)
                                 || pointOnLineLeft
                                 (w, Line(u, v))) {
return false;
                            }
                       }
                  }
             }
         }
    return true:
template < class T>
vector<Point<T>> hp(vector<Line<T>> lines) {
    sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
   auto d1 = l1.b - l1.a;
   auto d2 = l2.b - l2.a;
         if (sgn(d1) != sgn(d2)) {
              return sgn(d1) == 1;
         return cross(d1, d2) > 0:
    deque<Line<T>> ls:
    deque<Point<T>> ps;
        (auto l : lines) {
         if (ls.empty()) {
              ls.push_back(l);
              continue;
         }
         while (!ps.empty() && !pointOnLineLeft(ps.back(), l)) {
              ps.pop_back();
              ls.pop back();
         while (!ps.empty() && !pointOnLineLeft(ps[\theta], l)) { ps.pop_front();
              ls.pop_front();
         if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
                   (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                   if (!pointOnLineLeft(ls.back().a, l)) {
                        assert(ls.size() == 1);
                       ls[0] = l;
                   continue;
              return {};
         ps.push_back(lineIntersection(ls.back(), l));
    }
    while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0])) {
```

```
ps.pop_back();
    ls.pop_back();
}
if (ls.size() <= 2) {
    return {};
}
ps.push_back(lineIntersection(ls[0], ls.back()));
return vector(ps.begin(), ps.end());
}
using P = Point<ll>;
10.2 Convex Hull [b5758d]
int main() {
    int n; cin >> n;
    vector ch P(s)
```

```
vector<P> P(n), U, L;
for (int i = 0; i < n; i++) {
    cin >> P[i];
sort(P.begin(), P
      .end(), [](const Point<i64> &a, const Point<i64> &b) {
     return a.x == b.x ? a.y < b.y : a.x < b.x;
while (U.size() >= 2 && cross(U.back() -
    U[U.size() - 2], P[i] - U[U.size() - 2]) >= 0LL){
         U.pop_back();
     if (L.
          empty() || !(L.back() == P[i])) L.push_back(P[i]);
    if (U.
          empty() || !(U.back() == P[i])) U.push_back(P[i]);
if (L.size() <= 2 && U.size() <= 2) {
    // No Hull
cout << L.size() + U.size() - 2 << "\n'
for (int i = 0; i < L.size() - 1; i++) {
   cout << L[i].x << " " << L[i].y << "\n";</pre>
for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << " | n";</pre>
```

10.3 MinEuclideanDistance [469a8f]

```
template < class T>
T distanceSquare(const Point<T> &a, const Point<T> &b) {
    return square(a - b);
void solve() {
    int n; cin >> n;
    constexpr i64 inf = 8e18;
     vector<Point<i64>> a(n);
     for (int i = 0; i < n; i++) {</pre>
         i64 x, y;
cin >> x >> y;
         a[i] = Point < i64 > (x, y);
    struct sortY {
               (const Point<i64> &a, const Point<i64> &b) const {
              return a.y < b.y;</pre>
         }
    struct sortXY {
         bool operator()
               (const Point<i64> &a, const Point<i64> &b) const {
              if (a.x == b.x) return a.y < b.y;
else return a.x < b.x;</pre>
    sort(a.begin(), a.end(), sortXY());
vector<Point<i64>> t(n);
    auto devide = [&](auto &&self, int l, int r) -> i64 {
   if (l == r) return inf;
   int m = (l + r) / 2;
         i64 ans = min(self(self, l, m), self(self, m + 1, r));
         i64 midval = a[m].x;
         sort(t.begin(), t.begin() + p, sortY());
for (int i = 0; i < p; i++){</pre>
              for (int j = i + 1; j < p; j++) {
    ans = min(ans, distanceSquare(t[i], t[j]));</pre>
                   if ((t[i].y
                          t[j].y) * (t[i].y - t[j].y) > ans) break;
              }
         return ans;
```

```
cout << devide(devide, 0, n - 1) << "\n";
```

10.4 LatticePoints [7750d6]

10.5 MinRadiusCoverCircle [a9fa76]

```
constexpr double Eps = 1e-7;
void solve(int n, vector<P> a, double maxR) {
    auto cal = [&](P center) {
        double mx = 0;
        for (auto& p : a)
            mx = max(mx, distance(center, p));
        return mx;
};
auto searchY = [&](double x) {
        double l = -maxR, r = maxR;
        while (r - l > Eps) {
            double d = (r - l) / 3;
            double ml = l + d, mr = r - d;
            double ansl = cal({x, ml}), ansr = cal({x, mr});
            if (ansl > ansr) l = ml;
            else r = mr;
        }
        return (l + r) / 2;
};
double d = (r - l) / 3;
        double d = (r - l) / 3;
        double ml = l + d, mr = r - d;
        double ml = l + d, mr = r - d;
        double ansl = cal({ml, yl}), ansr = cal({mr, yr});
        if (ansl > ansr) l = ml;
        else r = mr;
}
double ansX = (l + r) / 2, ansY = searchY(ansX);
}
```