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1 Basic

1.1 install vscode [d41d8c]

```
// 如何安裝 vscode
// 1. 下載 vscode & msys2
// 2. 在跳出的 terminal 中 / 或打開 ucrt64，打上
    "pacman -S --needed base-devel mingw-w64-x86_64-toolchain"
// 3. 環境變數加上 C:\\msys64\\ucrt64\\bin
// 4. 重開 vscode, 載 C/C++, 運行, 編譯器選擇 g++
// 5. 打開 settings -> compiler -> add compilerPath
    -> 在 "" 裡打上 C:\\msys64\\ucrt64\\bin\\g++.exe
```

1.2 default code [bee7dd]

```cpp
#include <bits/stdc++.h>
#define all(x) (x).begin(), (x).end()
#define pii pair<int, int>
#define endl "\n"
#define int long long
using namespace std;

const int llinf = 4e18;
const int inf = 2e9;
const int mod = 1e9 + 7;
const int maxn = 2e5 + 5;

void solve() {

}

signed main() {
    ios_base::sync_with_stdio(0);
    cin.tie(nullptr);
    int t = 1;
    cin >> t;
    while (t--) {
        solve();
    }
}
```

1.3 compare fuction [4bc3e0]

```cpp
struct cmp {    // 在有 template 的資結使用
    bool operator()(const int &a, const int &b) const {
        return a < b;
    }
    // sort, bound 不用 struct
    // priority queue 小到大是 > , set 是 <
    // set 不能 = , multiset 要 =
    // 每個元素都要比到，不然會不見
    // pbds_multiset 的 upper_bound 跟 lower_bound
          功能相反, 如果要 find, 插入 inf 後使用 upper_bound
    // 內建 multiset
          可以跟 set 一樣正常使用, 自定義比較結構就比照以上
};

struct cmp {
    vector<int> &v;
    cmp(vector<int>& vec) : v(vec) {}
    bool operator() (int a, int b) const {
        // 根據外
             部向量來比較元素的優先級，記得不要改到比較 vector
        return v[a] > v[b];
    }
// main: cmp cmp1(vector);
// priority_queue<int, vector<int>, cmp> pq(cmp1);
};
```

1.4 pbds [e28ae8]

```cpp
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template<typename T>
using pbds_set = tree<T, null_type,
      less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template<typename T>
using pbds_multiset = tree<T, null_type, less_equal
     <T>, rb_tree_tag, tree_order_statistics_node_update>;
```

2 Graph

2.1 DFS 跟 BFS [aa5b45]

```cpp
int main() {
    int n;
    vector<vector<int>> adj(n + 1, vector<int>());
    // dfs_graph
    vector<bool> vis(n + 1, 0);
    auto dfs = [&](auto self, int u) -> void {
        if (vis[u]) return;
        vis[u] = true;
        for (auto v: adj[u]) {
            self(self, v);
        }
    };
    dfs(dfs, 1);
    // bfs
    vector<int> deep(n + 1, 1e9);
    queue<int> q;
    auto bfs = [&](auto self, int u) -> void {
        vis[u] = true;
        deep[u] = 0;
        q.push(u);
        while (!q.empty()) {
            int now = q.front(); q.pop();
            for (auto nxt : adj[now]) {
                if (vis[nxt]) continue;
                vis[nxt] = true;
                deep[nxt] = deep[now] + 1;
                q.push(nxt);
            }
        }
    };
    bfs(bfs, 1);
}
```

2.2 最短距離算法 - Dijkstra [4e0023]

```cpp
// Flight Discount
int main() {
    int n, m; cin >> n >> m;
    vector<vector<pair<
         int, int>>> adj(n + 1, vector<pair<int, int>>(n + 1));
    vector<vector<int>>
          dis(n + 1, vector<int>(2, 2e9));    // 0 for not used
    for (int i = 1; i <= m; i++) {
        int u, v, w;
        cin >> u >> v >> w;
        adj[u].push_back({v, w});
    }
    priority_queue
         <array<int, 3>, vector<array<int, 3>>, greater<array
         <int, 3>>> pq;  // 0 for w, 1 for u, 2 for discount
    dis[1][0] = dis[1][1] = 0;
    pq.push({0, 1, 0});
    while (!pq.empty()) {
        auto [dist, u, us] = pq.top(); pq.pop();
        if (dis[u][us] < dist) continue;
        if (us) {
            for (auto [v, w] : adj[u]) {
                if (dis[u][1] + w < dis[v][1]) {
                    dis[v][1] = dis[u][1] + w;
                    pq.push({dis[v][1], v, 1});
                }
            }
        }
        else {
            for (auto [v, w] : adj[u]) {
                if (dis[u][0] + w < dis[v][0]) {
                    dis[v][0] = dis[u][0] + w;
                    pq.push({dis[v][0], v, 0});
                }
                if (dis[u][0] + w / 2 < dis[v][1]) {
                    dis[v][1] = dis[u][0] + w / 2;
```

```
                    pq.push({dis[v][1], v, 1});
                }
            }
        }
    }
    cout << min(dis[n][0], dis[n][1]);
}
```

2.3 最小生成樹 - Prim [e54eda]

```
int n, m, ans = 0;
const int maxn = 2e5 + 5;
vector<pair<int, int>> adj[maxn];
bool Prim() {
    int node_sz = 0;
    priority_queue<pii, vector<pii>, greater<pii>> pq;
    pq.push({0, 1});
    bool vis[maxn] = {false};
    while (!pq.empty()) {
        auto [cost, u] = pq.top(); pq.pop();
        if (vis[u]) continue;
        vis[u] = true;
        ans += cost;
        node_sz++;
        for(auto [v, cost] : adj[u]) {
            if (!vis[v])
                pq.push({cost, v});
        }
    }
    if (node_sz == n) return true;
    return false;
}
void solve() {
    cin >> n >> m;
    for(int i = 1; i <= m; i++) {
        int u, v, cost; cin >> u >> v >> cost;
        adj[u].push_back({v, cost});
        adj[v].push_back({u, cost});
    }
    if (Prim()) cout << ans;
    else cout << "IMPOSSIBLE";
}
```

2.4 正權找環 [0e0fdf]

```
const int maxn = 1e5+5;
vector<int> graph[maxn];
int color[maxn], parent[maxn];
bool vis[maxn];
int n, m;
void print_ans(int ori) {
    int now = parent[ori];
    deque<int> ans;
    ans.push_front(ori);
    while (now != ori) {
        ans.push_front(now);
        now = parent[now];
    }
    ans.push_front(ori);
    cout << ans.size() << endl;
    for (auto i : ans) {
        cout << i << " ";
    }
    exit(0);
}
void dfs(int now) {
    color[now] = 1;
    vis[now] = 1;
    for (auto nxt : graph[now]) {
        parent[nxt] = now;
        if (color[nxt] == 1) {
            print_ans(nxt);
        }
        else if (color[nxt] == 0) {
            dfs(nxt);
        }
    }
    color[now] = 2;
}
void solve() {
    cin >> n >> m;
    for (int i = 1; i <= m; i++) {
        int u, v; cin >> u >> v;
        graph[u].push_back(v);
    }
    for (int i = 1; i <= n; i++) {
        if (!vis[i])
            dfs(i);
    }
    cout << "IMPOSSIBLE";
}
```

2.5 負權找負環 [02f480]

```
// 用 Bellman Ford 找負環
vector<array<int, 3>> graph;    // u, v, w
int main() {
    int src = 0;
    int n, m;    cin >> n >> m;
    vector<int> par(n + 1), dis(n + 1, 1e9);
    for (int i = 0; i < m; i++) {
        int a, b, w; cin >> a >> b >> w;
        graph.push_back({a, b, w});
    }
    dis[1] = 0;
    for (int i = 0; i <= n; i++) {
        src = 0;
        for (auto [u, v, w] : graph) {
            if (dis[v] > dis[u] + w) {
                dis[v] = dis[u] + w;
                par[v] = u;
                src = v;
            }
        }
    }
    if (src) {  // 到第 n + 1 次還在鬆弛
        vector<int> ans;
        cout << "YES" << endl;
        for (int
              i = 0; i <= n; i++) src = par[src]; // 找那個負環
        ans.push_back(src);
        for (int
             i = par[src]; i != src; i = par[i]) {  // 輸出負環
            ans.push_back(i);
        }
        ans.push_back(src);
        reverse(ans.begin(), ans.end());
        for (auto i : ans) {
            cout << i << " ";
        }
    }
    else {
        cout << "NO" << "\n";
    }
}
```

2.6 正權最大距離 [9f10c8]

```
// 只能用在 DAG，用拓樸按順序鬆弛
// 如果 1 不能到達 n，n 也有
     可能被鬆弛，所以要看的是 dis[n] < 0，不能只看有沒有 = -1e9
void print_ans(int n, vector<int> &par) {
    deque<int> ans;
    int now = n;
    while(now != 1) {
        ans.push_front(now);
        now = par[now];
    }
    ans.push_front(1);
    cout << ans.size() << endl;
    for(auto i : ans) {
        cout << i << " ";
    }
}
void solve() {
    int n, m;
    cin >> n >> m;
    vector<int> dis(n + 1, -1e9); dis[1] = 0;
    vector<vector<int>> graph(n + 1, vector<int>());
    vector<bool> vis(n + 1, 0);
    vector<int> par(n + 1);
    vector<int> in(n + 1, 0);
    queue<int> q;
    for (int i = 1; i <= m; i++) {
        int u, v; cin >> u >> v;
        graph[u].push_back(v);
        in[v]++;
    }
    for (int i = 1; i <= n; i++) {
        if(in[i] == 0) q.push(i);
    }
    while (!q.empty()) {
        int u = q.front(); q.pop();
        for (auto nxt : graph[u]) {
            if (dis[nxt] < dis[u] + 1) {  // 鬆弛
                dis[nxt] = dis[u] + 1;
                par[nxt] = u;
            }
            in[nxt]--;
            if (in[nxt] == 0) q.push(nxt);
        }
        vis[u] = 1;
    }
    if (dis[n] < 0) {
        cout << "IMPOSSIBLE";
    }
    else print_ans(n, par);
}
```

2.7 負權最大距離 [f979d8]

```
// CSES High Score
void dfs(int u, vector<int> &vis, vector<vector<int>> &adj) {
    if (vis[u]) return;
    vis[u] = 1;
    for (int v : adj[u]) {
        dfs(v, vis, adj);
    }
}
void bellman_ford
     (int n, int s, vector<int> &vis, vector<int> &dis
     , vector<array<int, 3>> edge, vector<vector<int>> &adj) {
```

```
    fill(dis.begin(), dis.end(), -1e18);
    dis[s] = 0;
    for (int i = 1; i <= n; i++) {
        for (auto [u, v, w] : edge) {
            if (dis[u] != -1e18 && dis[v] < dis[u] + w) {
                dis[v] = dis[u] + w;
                if (i == n) {
                    dfs(v, vis, adj);
                }
            }
        }
    }
}
signed main() {
    int n, m; cin >> n >> m;
    vector<array<int, 3>> edge;
    vector<vector<int>> adj(n + 1);
    vector<int> dis(n + 1), vis(n + 1);
    while (m--) {
        int u, v, w;
        cin >> u >> v >> w;
        edge.push_back({u, v, w});
        adj[u].push_back(v);
    }
    bellman_ford(n, 1, vis, dis, edge, adj);
    if (vis[n]) cout << -1;
    else cout << dis[n];
}
```

2.8 FloydWarshall [206b76]

```
const int inf = 1e18;
int main() {
    int n, m, q; cin >> n >> m >> q;
    vector<vector<int>> graph(n + 1, vector<int>(n + 1, inf));
    vector<vector<int>> dis(n + 1, vector<int>(n + 1));
    for (int i = 0; i < m; i++) {
        int u, v, w; cin >> u >> v >> w;
        cin >> u >> v >> w;
        graph[u][v] = min(graph[u][v], w);
        graph[v][u] = min(graph[v][u], w);
    }
    for (int i = 0; i <= n; i++) {
        for(int j = 0; j <= n; j++) {
            dis[i][j] = graph[i][j];
        }
    }
    for (int i = 0; i <= n; i++) // 自己到自己是 0
        dis[i][i] = 0;

    for (int k = 1; k <= n; k++) {
        for (int i = 1; i <= n; i++) {
            for (int j = 1; j <= n; j++) {
                dis[i][j
                    ] = min(dis[i][j], dis[i][k] + dis[k][j]);
            }
        }
    }
    for (int i = 0; i < q; i++) {
        int u, v; cin >> u >> v;
        cout << (dis[u][v] >= inf ? -1 : dis[u][v]) << "\n";
    }
}
```

2.9 歐拉環與歐拉路 [0911ed]

```
// 無向圖、尤拉環：檢查每個點的出度為偶數
// 有向圖、
    尤拉路：可以看成 1 走到 n，所以檢查所有點的出度等於入度
int n, m;
const int maxn = 1e5 + 5;
vector<set<int>> adj;
vector<int> in;
void dfs(int now, vector<int> &road) {
    while (!adj[now].empty()) {
        int nxt = *adj[now].begin();
        adj[now].erase(nxt);
        dfs(nxt, road);
    }
    road.push_back(now);
}
void solve() {
    cin >> n >> m;
    in.assign(n + 1, 0);
    adj.assign(n + 1, set<int>());
    for (int i = 1; i <= m; i++) {
        int u, v; cin >> u >> v;
        adj[u].insert(v);
        in[v]++;
    }
    in[1]++;
    in[n]--;
    for (int i = 1; i <= n; i++) {
        if(adj[i].size() != in[i]) {
            cout << "IMPOSSIBLE";
            return;
        }
    }
    vector<int> road;
    dfs(1, road);
    if (road.size() != m + 1) {
        cout << "IMPOSSIBLE";
        return;
    }
    reverse(road.begin(), road.end());
    for(auto i : road) cout << i << " ";
}
```

2.10 SCC 結合拓樸 DP [8036c2]

```
// 找到所有 SCC 然後結合原圖重建一個 DAG，然後拓樸 DP
void dfs(int u, vector<int
    > &vis, vector<int> &kosaraju, vector<vector<int>> &adj) {
    if (!vis[u]) {
        vis[u] = 1;
        for (auto v : adj[u]) {
            dfs(v, vis, kosaraju, adj);
        }
        kosaraju.push_back(u);  // finish time 小到大排列
    }
}
void rev_dfs(int u, vector<int> &vis, vector<
    int> &order, vector<vector<int>> &rev_adj, int &scc_num) {
    if (!vis[u]) {
        vis[u] = 1;
        order[u] = scc_num;
        for (auto v : rev_adj[u]) {
            rev_dfs(v, vis, order, rev_adj, scc_num);
        }
    }
}
signed main() {
    int n, m, scc_num = 0;
    cin >> n >> m;
    vector<int> coin(n + 1), order(n + 1), vis(n + 1, 0);
    vector<vector<int>> adj(n + 1), rev_adj(n + 1);
    vector<int> kosaraju;
    for (int i = 1; i <= n; i++) {
        cin >> coin[i];
    }
    for (int i = 1; i <= m; i++) {
        int u, v; cin >> u >> v;
        adj[u].push_back(v);
        rev_adj[v].push_back(u);
    }
    for (int i = 1; i <= n; i++) {
        if (!vis[i]) {
            dfs(i, vis, kosaraju, adj);
        }
    }
    reverse(kosaraju.begin(), kosaraju
        .end());  // 轉過來，從 finish time 大的開始做 dfs
    vis.assign(n + 1, 0);
    for (auto &u : kosaraju) {
        if (!vis[u]) {
            scc_num++;
            rev_dfs(u, vis, order, rev_adj, scc_num);
        }
    }
    // 重新建 DAG，根據原圖，如果不再同個 SCC，對 order 加邊
    vector<vector<int>> DAG(scc_num + 1, vector<int>());
    vector<int> in_degree(scc_num + 1, 0);
    vector<int
        > sum_coin(scc_num + 1, 0), dp_coin(scc_num + 1, 0);
    set<pair<int, int>> st;
    int ans = -1e9;
    for (int i = 1; i <= n; i++) {
        sum_coin[order[i]] += coin[i];
        for (auto j : adj[i]) {
            // 如果不是在同一個 SCC 且 order 邊還沒加過
            if (order[i] != order[j] &&
                  st.find({order[i], order[j]}) == st.end()) {
                DAG[order[i]].push_back(order[j]);
                in_degree[order[j]]++;
                st.insert({order[i], order[j]});
            }
        }
    }
    // 對 DAG 拓蹼 DP
    queue<int> q;
    for (int i = 1; i <= scc_num; i++) {
        if (in_degree[i] == 0) {
            q.push(i);
        }
    }
    while (!q.empty()) {
        int now = q.front(); q.pop();
        dp_coin[now] += sum_coin[now];
        ans = max(ans, dp_coin[now]);
        for (auto v : DAG[now]) {
            in_degree[v]--;
            dp_coin[v] = max(dp_coin[v], dp_coin[now]);
            if (in_degree[v] == 0) q.push(v);
        }
    }
    cout << ans;
}
```

2.11 Tarjan [86b533]

```
vector<vector<int>> g;
vector<int> id(n + 1, -1), dfn(n + 1, -1), low(n + 1, -1);
```

```
vector<int> stk;
int now = 0, cnt = 0;
function<void(int)> tarjan = [&](int u) {
    stk.push_back(u);
    dfn[u] = low[u] = now++;
    for (auto v : g[u]) {
        if (dfn[v] == -1) {
            tarjan(v);
            low[u] = min(low[u], low[v]);
        } else if (id[v] == -1) {
            low[u] = min(low[u], dfn[v]);
        }
    }
    if (dfn[u] == low[u]) {
        int v;
        do {
            v = stk.back();
            stk.pop_back();
            id[v] = cnt;
        } while (v != u);
        ++cnt;
    }
};
for (int i = 0; i < 2 * n; ++i) if (dfn[i] == -1) tarjan(i);
for (auto i : id) cout << i << " ";
```

2.12 2-SAT [800826]

```
// +(-) u or +(-) v
const int maxn = 1e5 + 5;
vector<int> adj[2 * maxn], rev_adj[2 * maxn];
vector<int> order;
int cat[2 * maxn];
int k = 1;
bool vis[2 * maxn];
void dfs(int now) {
    if (!vis[now]) {
        vis[now] = 1;
        for (auto v : adj[now]) {
            dfs(v);
        }
        order.push_back(now);
    }
}
void rev_dfs(int now) {
    if (!vis[now]) {
        cat[now] = k;
        vis[now] = 1;
        for (auto v : rev_adj[now]) {
            rev_dfs(v);
        }
    }
}
int main() {
    int n, m;
    cin >> m >> n;
    for (int i = 1; i <= m; i++) {
        int u, v;
        char a, b;
        cin >> a >> u >> b >> v;
        if (a == '-') {
            u = 2 * n - u + 1; // reverse
        }
        if (b == '-') {
            v = 2 * n - v + 1; // reverse
        }
        adj[2 * n - u + 1].
            push_back(v); // from -u to v;  // if -u, then v
        adj[2 * n - v + 1].
            push_back(u); // from -v to u;  // if -v, then u
        rev_adj[v].push_back(2 * n - u + 1);
        rev_adj[u].push_back(2 * n - v + 1);
    }
    for (int i = 1; i <= 2 * n; i++) {
        if (!vis[i]) {
            dfs(i);
        }
    }
    memset(vis, 0, sizeof(vis));
    reverse(order.begin(), order.end());
    for (auto i : order) {
        if (!vis[i]) {
            rev_dfs(i);
            k++;
        }
    }
    char ans[2 * n + 1];
    for (int i = 1; i <= n; i++) {
        if (cat[i] == cat[2 * n - i + 1]) {
            cout << "IMPOSSIBLE";
            return;
        }
        if (cat[i] > cat[2 * n - i + 1]) {
            ans[i] = '+';
        }
        else ans[i] = '-';
    }
    for (int i = 1; i <= n; i++) {
        cout << ans[i] << " ";
    }
}
```

2.13 Planets Cycles [71ac0e]

```
vector<int> dis, v;
vector<bool> vis;
int step;
queue<int> path;
void dfs(int x) {
    path.push(x);
    if (vis[x]) {
        step += dis[x];
        return;
    }
    vis[x] = true;
    step++;
    dfs(v[x]);
}
// count path_dis to rep
int main() {
    int n; cin >> n;
    v.assign(n + 1, 0);
    dis.assign(n + 1, 0);
    vis.assign(n + 1, false);
    for (int i = 1; i <= n; i++) {
        cin >> v[i];
    }
    for (int i = 1; i <= n; i++) {
        step = 0;
        int is_outof_cycle = 1;
        dfs(i);
        while (!path.empty()) {
            if (path.front() == path.back()) {
                is_outof_cycle = 0;
            }
            dis[path.front()] = step;
            step -= is_outof_cycle;
            path.pop();
        }
    }
    for (int i = 1; i <= n; i++) {
        cout << dis[i] << ' ';
    }
    cout << '\n';
}
```

2.14 Planet Queries II [872f72]

```
// 在有向圖中，從 A 到 B 的最短距離
// 保證出度是 1 所以對 1 個點來說，從他出發只可能遇到一個環
int n, q;
int dp[200005][30];   // 倍增表
vector<vector<int>> cycles;
vector<int
     > no, cycle_idx, vis; // Order & Can be in cycle, or out
void set_out_of_cycle_no(int now, unordered_set<int> &done) {
    // 把不在環內的也編號，v 是 u 的編號 -1
    if (done.find(now) != done.end()) return;
    set_out_of_cycle_no(dp[now][0], done);
    done.insert(now);   // post order
    no[now] = no[dp[now][0]] - 1;
}
int wiint_go_to(int u, int k) { // 回傳當 u 走 k 步時會到的地方
    for (int i = 0; i <= 18; i++) {
        if (k & (1 << i)) {
            u = dp[u][i];
        }
    }
    return u;
}
void find_cycle(int now) {
    unordered_set<int> appear;
    vector<int> v;
    bool flag = true;   // 代表有環
    while (appear.find(now) == appear.end()) {
        appear.insert(now);
        v.push_back(now);
        if (vis[now]) {
            flag = false;
            break;
        }
        now = dp[now][0];
    }
    for (auto i : v)  vis[i] = true;
    if (!flag)  return;
    // now 是環的起點，我們先找到他在 v 的哪裡
    int z = find(v.begin(), v.end(), now) - v.begin();
    vector<int> cycle(v.begin() + z, v.end());
    cycles.push_back(cycle);
}
int main() {
    cin >> n >> q;
    no.assign(n + 1, -1);
    cycle_idx.assign(n + 1, -1);
    vis.assign(n + 1, 0);
    for (int u = 1; u <= n; u++) cin >> dp[u][0];
    for (int i = 1; i <= 18; i++) // 倍增表
        for (int u = 1; u <= n; u++)
            dp[u][i] = dp[dp[u][i - 1]][i - 1];
    for (int i = 1; i <= n; i++) {
        if (!vis[i]) find_cycle(i);
    }
    int idx = 0;
```

```
    unordered_set<int> done;
    for (auto &i : cycles) {
        int c = 0;
        for (auto &j : i) {
            no[j] = c++;
            cycle_idx[j] = idx;
            done.insert(j);
        }
        idx++;
    }
    for (int i = 1; i <= n; i++) set_out_of_cycle_no(i, done);
    for (int i = 1; i <= q; i++) {
        int u, v; cin >> u >> v;
        // 在同個環內
        if (cycle_idx[u] == cycle_idx
             [v] && cycle_idx[u] != -1 && cycle_idx[v] != -1) {
            int cyc_size = cycles[cycle_idx[u]].size();
            cout <<
                 (no[v] - no[u] + cyc_size) % cyc_size << "\n";
        }
        // 都不再環內
        else if (cycle_idx[u] == -1 &&
              cycle_idx[v] == -1) { // Both are not in a Cycle
            if (no[u] > no[v]) {
                cout << -1 << "\n";
                continue;
            }
            if (wiint_go_to(u, no[v] - no[u]) == v) {
                cout << no[v] - no[u] << "\n";
            }
            else cout << -1 << "\n";
        }
        else if (cycle_idx[u]
             == -1 && cycle_idx[v] != -1) { // v 在環內，二分搜
            int l = -1, r = n;
            while (l <= r) {
                int m = (l + r) / 2;
                if (cycle_idx[wiint_go_to
                     (u, m)] == cycle_idx[v]) r = m - 1;
                else l = m + 1;
            }
            if (l <= n) {   // 如果 n 步內可以到
                int in_cycle_of_u = wiint_go_to(u, l);
                int cycle_size = cycles[cycle_idx[v]].size();
                cout << l + (no[v] - no[in_cycle_of_u
                     ] + cycle_size) % cycle_size << "\n";
            }
            else cout << -1 << "\n";
        }
        else { // u 在環內 b 不在，直接不可能
            cout << -1 << "\n";
        }
    }
}
```

3 Data Structure

3.1 BIT [d41d8c]

```
struct BIT {    // BIT 都是 1-based 的查詢
    int n;
    vector<int> bit;
    BIT(int n) {    // 有幾個數
        this->n = n;
        bit.resize(n + 1, 0);
    }
    BIT(vector<int> &init) {    // 必須是 1-based
        this->n = init.size() - 1;
        bit.resize(n + 1, 0);
        for (int i = 1; i <= n; i++) {
            modify(i, init[i]);
        }
    }
    void modify(int i, int val) {
        for (; i <= n; i += i & -i) {
            bit[i] += val;
        }
    }
    int query(int r) {
        int ans = 0;
        for (; r; r -= r & -r) ans += bit[r];
        return ans;
    }
    int query(int l, int r) {
        return query(r) - query(l - 1);
    }
};
struct TwoDimensionBIT {
    int nx, ny;
    vector<vector<int>> bit;
    TwoDimensionBIT(int x, int y) {
        nx = x; ny = y;
        bit.resize(x + 1, vector<int>(y + 1, 0));
    }
    void modify(int x, int y, int mod) {
        for (; x <= nx; x += x & -x) {
            for (int tmp = y; tmp <= ny; tmp += tmp & -tmp) {
                bit[x][tmp] += mod;
            }
        }
    }
    int query(int r1, int r2) {
        int ans = 0;
        for (; r1; r1 -= r1 & -r1) {
            for (int tmp = r2; tmp; tmp -= tmp & -tmp) {
                ans += bit[r1][tmp];
            }
        }
        return ans;
    }
};
```

3.2 DSU [d41d8c]

```
struct DSU {
    vector<int> boss, siz;
    DSU(int n) {    // 1 based
        boss.resize(n + 1);
        iota(boss.begin(), boss.end(), 0);
        siz.assign(n + 1, 1);
    }
    int find_boss(int x) {
        if(boss[x] == x) return x;
        return boss[x] = find_boss(boss[x]);
    }
    bool same(int x, int y) {
        return find_boss(x) == find_boss(y);
    }
    bool merge(int x, int y) {
        x = find_boss(x);
        y = find_boss(y);
        if (x == y) {
            return false;
        }
        if(siz[x] < siz[y]) swap(x, y);
        siz[x] += siz[y];
        boss[y] = x;
        return true;
    }
    int size(int x) {
        return siz[find_boss(x)];
    }
};
```

3.3 Increasing Array Queries [d41d8c]

```
const int maxn = 2e5+5;
int n, q;
int nums
    [maxn], prefix[maxn], ans[maxn], BIT[maxn], contrib[maxn];
vector<pair<int, int>> queries[maxn];
void update(int pos, int val) {
    for (; pos <= n; pos += pos & -pos) BIT[pos] += val;
}
int query(int a, int b) {
    int ans = 0;
    for (; b; b -= b&-b) ans += BIT[b];
    for (a--; a; a -= a&-a) ans -= BIT[a];
    return ans;
}
void solve() {
    cin >> n >> q;
    for (int i = 1; i <= n; i++) {
        cin >> nums[i];
        prefix[i] = prefix[i-1] + nums[i];
    }
    nums[n + 1] = 1e9;
    prefix[n + 1] = 2e18;
    for (int i = 1; i <= q; i++) {
        int a, b; cin >> a >> b;
        queries[a].push_back({b, i});
    }
    deque<int> mono; mono.push_front(n+1);
    for (int i = n; i
         > 0; i--) { // question from start at n to start at 1
        while (nums[i] >= nums[mono.front()]) {
            update(mono.front(), -contrib[mono
                 .front()]);   // mono.front's contrib become 0
            mono.pop_front();
        }
        contrib[i] = (mono.front() - 1 - i) *
              nums[i] - (prefix[mono.front() - 1] - prefix[i]);
        update(i, contrib[i]);
        mono.push_front(i);
        for (auto j : queries
             [i]) {  // pos is the index in mono <= end's
            int pos = upper_bound(mono.begin
                 (), mono.end(), j.first) - mono.begin() - 1;
            ans[j.second] = (pos ? query(i, mono
                 [pos - 1]) : 0)   // smainter than y's mono
                              // mono to y caculate directly
                          + (j.first
                               - mono[pos]) * nums[mono[pos]]
                          - (prefix
                               [j.first] - prefix[mono[pos]]);
        }
    }
    for (int i = 1; i <= q; i++) {
        cout << ans[i] << endl;
    }
}
```

3.4 線段樹 [d41d8c]

```
template <class Node>
struct Seg {
    int n;
    vector<Node> tree;
    Seg (vector<Node> init_) {
        n = init_.size() - 1;
        tree.resize(4 * n);
        function <void(int
             , int, int)> build = [&](int now, int l, int r) {
            if (l == r) {
                tree[now] = init_[l];
                return;
            }
            int m = (l + r) / 2;
            build(now << 1, l, m);
            build((now << 1) + 1, m + 1, r);
            pull(now);
        };
        build(1, 1, n);
    }
    Node query(int l, int r, int ql, int qr, int now) {
        int m = (l + r) >> 1;
        if (qr < l || ql > r) {
            return Node();
        }
        if (ql <= l && r <= qr) {
            return tree[now];
        }
        return query(l, m, ql, qr, now
              << 1) + query(m + 1, r, ql, qr, (now << 1) + 1);
    }
    Node query(int l, int r) { return query(1, n, l, r, 1); }
    void pull(int now) {
        tree[now] = tree[now << 1] + tree[(now << 1) + 1];
    }
    void modify(int l, int r, int idx, int now, int add) {
        if (l == r) {
// ------------------------------
     how to modify ?----------------------------------
            tree[now].sum = add;
//

     ------------------------------------------------------------

            return;
        }
        int m = (l + r) >> 1;
        if (idx <= m) {
            modify(l, m, idx, now << 1, add);
        }
        else {
            modify(m + 1, r, idx, (now << 1) + 1, add);
        }
        pull(now);
    }
    void modify
         (int idx, int add) { modify(1, n, idx, 1, add); }
};
// ------------------------
     define structure and info plus------------------------
struct Node {
    int sum;
    Node () {
        sum = 0;
    }
};
Node operator + (const Node &a, const Node &b) {
    Node c;
    c.sum = a.sum + b.sum;
    return c;
    // use lc、rc to undate now
    // tree[now].sum = tree[lc].sum + tree[rc].sum;
    // tree[now].prefix
          = max(tree[lc].sum+tree[rc].prefix, tree[lc].prefix);
    // tree[now].suffix
          = max(tree[lc].suffix+tree[rc].sum, tree[rc].suffix);
    // tree[now].middle_max = max(max(tree[lc].middle_max, tree
         [rc].middle_max), tree[lc].suffix+tree[rc].prefix);
    // tree[now].middle_max = max(max(tree[
         now].middle_max, tree[now].prefix), tree[now].suffix);
}
//

     ------------------------------------------------------------


// pizza_queries
// 左邊的店(s < t): dis_l = (pizza[s] - s) + t;
// 右邊的店(t < s): dis_r = (pizza[s] + s) - t;
// 實作: 建左查詢線段樹跟右查詢線段樹，用最小值pull
// 答案是 min(left_query(1, s) + t, right_query(s, end) + t);

// List Removals
// 維護區間內有幾個數字被選過
// 用二
     分搜找右區間最小位，使得 ans - query == 1~ans 被選過的數量
```

3.5 懶標線段樹 [d41d8c]

```
template <class Node, class Lazy>
struct LazySeg {
    int n;
    vector<Node> tree;
    vector<Lazy> lazy;
    template <typename T>
    LazySeg (vector<T> init_) {  // 必須是 1-based
        n = init_.size() - 1;
        tree.resize(4 * n);
        lazy.resize(4 * n);
        function <void(int
             , int, int)> build = [&](int now, int l, int r) {
            if (l == r) {
                tree[now] = init_[l];
                return;
            }
            int m = (l + r) / 2;
            build(now << 1, l, m);
            build((now << 1) + 1, m + 1, r);
            pull(now);
        };
        build(1, 1, n);
    }
    Node query(int l, int r, int ql, int qr, int now) {
        int m = (l + r) >> 1;
        if (qr < l || ql > r) {
// ------------------------
     out of range, return what------------------------------
            return Node();
//

     ------------------------------------------------------------

        }
        push(now, l, r);
        if (ql <= l && r <= qr) {
            return tree[now];
        }
        return query(l, m, ql, qr, now
              << 1) + query(m + 1, r, ql, qr, (now << 1) + 1);
    }
    Node query(int l, int r) { return query(1, n, l, r, 1); }
    void pull(int now) {
        tree[now] = tree[now << 1] + tree[(now << 1) + 1];
    }
    void modify_add
         (int l, int r, int ql, int qr, int now, int add) {
        int m = (l + r) >> 1;
        if (qr < l || ql > r) {
            return;
        }
        if (ql <= l && r <= qr) {
// ------------------------------
     how to modify ?----------------------------------
            lazy[now].add += add;
//

     ------------------------------------------------------------

            return;
        }
        push(now, l, r);
        modify_add(l, m, ql, qr, now << 1, add);
        modify_add(m + 1, r, ql, qr, (now << 1) + 1, add);
        push(now << 1, l, m);
        push((now << 1) + 1, m + 1, r);
        pull(now);
    }
    void modify_add(int
         l, int r, int add) { modify_add(1, n, l, r, 1, add); }
    void modify_set
         (int l, int r, int ql, int qr, int now, int val) {
        int m = (l + r) >> 1;
        if (qr < l || ql > r) {
            return;
        }
        if (ql <= l && r <= qr) {
// ------------------------------
     how to modify ?----------------------------------
            lazy[now].set_val = val;
            lazy[now].add = 0;
//

     ------------------------------------------------------------

            return;
        }
        push(now, l, r);
        modify_set(l, m, ql, qr, now << 1, val);
        modify_set(m + 1, r, ql, qr, (now << 1) + 1, val);
        push(now << 1, l, m);
        push((now << 1) + 1, m + 1, r);
        pull(now);
    }
    void modify_set(int
         l, int r, int val) { modify_set(1, n, l, r, 1, val); }
    void push(int now, int l, int r) {
        apply(now, l, r);
// ------------------------
     how to push down ?-------------------------------------
        if (l != r) {
            if (lazy[now].set_val) {
```

```
                lazy[now << 1].set_val = lazy[now].set_val;
                lazy[(now
                      << 1) + 1].set_val = lazy[now].set_val;
                lazy[now << 1].add = lazy[now].add;
                lazy[(now << 1) + 1].add = lazy[now].add;
            }
            else {
                lazy[now << 1].add += lazy[now].add;
                lazy[(now << 1) + 1].add += lazy[now].add;
            }
        }
//

     ------------------------------------------------------------


        lazy[now] = Lazy();
    }
    void apply(int now, int l, int r) {
        if (lazy[now].set_val) {
            tree[now].sum = (r - l + 1) * lazy[now].set_val;
        }
        tree[now].sum += (r - l + 1) * lazy[now].add;
    }
};
// ------------------------
    define structure and info plus------------------------
struct Node {
    int sum;
};
struct Lazy {
    int set_val; int add;
};
Node operator+(const Node &a, const Node &b) {
    return {{a.sum + b.sum}};
}
//

     ------------------------------------------------------------


// polynomial queries
// 設置梯形的底跟加了幾次，apply_tag時底為
    l的合，d為加給次，所以sum += (底*2 + 次*區間) * 區間 / 2;
```

3.6 莫隊 [d41d8c]

```
struct query {
    int l, r, id;
} typedef query;
void MO(int n, vector<query> &queries) {
    int block = sqrt(n);
    function <bool(query, query)> cmp = [&](query a, query b) {
        int block_a = a.l / block;
        int block_b = b.l / block;
        if (block_a != block_b) return block_a < block_b;
        return a.r < b.r;
    };
    sort(queries.begin(), queries.end(), cmp);
}
void compress(vector<int> &nums) {
    vector<int> sorted = nums;
    sort(sorted.begin(), sorted.end());
    sorted.erase
         (unique(sorted.begin(), sorted.end()), sorted.end());
    for (int i = 0; i < nums.size(); i++) {
        nums[i] = lower_bound(sorted.begin
             (), sorted.end(), nums[i]) - sorted.begin() + 1;
    }
}
```

3.7 Treap [d41d8c]

```
struct Treap {
    Treap *l, *r;
    int pri, subsize; char val; bool rev_valid;
    Treap(int val) {
        this->val = val;
        pri = rand();
        l = r = nullptr;
        subsize = 1; rev_valid = 0;
    }
    void pull() {    // update subsize or other information
        subsize = 1;
        for(auto i : {l, r}) {
            if (i) subsize += i->subsize;
        }
    }
};
int size(Treap *treap) {
    if (treap == NULL) return 0;
    return treap->subsize;
}
// lazy
void push(Treap *t) {
    if (!t) return;
    if (t->rev_valid) {
        swap(t->l, t->r);
        if (t->l) t->l->rev_valid ^= 1;
        if (t->r) t->r->rev_valid ^= 1;
    }
    t->rev_valid = false;
}
Treap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
    // push(a); push(b);    // lazy
    if (a->pri > b->pri) {
        a->r = merge
             (a->r, b);  // a->r = new, inorder, make sense
        a->pull();
        return a;
    }
    else {
        b->l = merge
             (a, b->l);  // new->l = a, inorder, make sense
        b->pull();
        return b;
    }

}
pair<Treap*, Treap*> split(Treap *root, int k) {    // find 1~k
    if (root == nullptr) return {nullptr, nullptr};
    // push(root); // lazy
    if (size(root->l) < k) {
        auto [a, b] = split(root->r, k - size(root->l) - 1);
        root->r = a;
        root->pull();
        return {root, b};
    }
    else {
        auto [a, b] = split(root->l, k);
        root->l = b;
        root->pull();
        return {a, root};
    }
}
void Print(Treap *t) {
    if (t) {
        // push(t);    // lazy
        Print(t->l);
        cout << t->val;
        Print(t->r);
    }
}
void substring_rev() {
    int n, m; cin >> n >> m;
    Treap *root = nullptr;
    string str; cin >> str;
    for(auto c : str) {
        root = merge(root, new Treap(c));
    }
    for(int i = 1; i <= m; i++) {
        int x, y; cin >> x >> y;
        auto [a, b] = split(root, x-1); // a: 1~x-1, b: x~n
        auto [c, d] = split(b, y-x+1);  // Use b to split
        // c->rev_valid ^= true;
        // push(c);
        b = merge(a, d);    // Notice the order
        root = merge(b, c);
    }
    Print(root);
}
```

4 Flow

4.1 Dinic [db7233]

```
vector<bool> vis;
vector<int> lev;
int n, m, ans;
struct edge {
    int to, w, rev_ind;
};
vector<edge> adj[505];
bool label_level
     () { // Tag the depth, if can't reach end => return false
    lev.assign(505, -1);
    lev[1] = 0;
    queue<int> q;   q.push(1);
    while (!q.empty()) {
        int u = q.front(); q.pop();
        for (auto i : adj[u]) {
            if (i.w > 0 && lev[i.to] == -1) {
                q.push(i.to);
                lev[i.to] = lev[u] + 1;
            }
        }
    }
    return (lev[n] == -1 ? false : true);
}
int dfs(int u, int flow) {
    if(u == n) return flow;
    for (auto &i : adj[u]) {
        if (lev[i.to] == lev[u] + 1 && !vis[i.to] && i.w > 0) {
            vis[i.to] = true;
            int ret = dfs(i.to, min(flow, i.w));
            if (ret > 0) {
                i.w -= ret;
                adj[i.to][i.rev_ind].w += ret;
                return ret;
            }
        }
    }
    return 0;   // if can't reach end => return 0
```

```
}
void dinic(){
    while (label_level()) {
        while (1) {
            vis.assign(505, 0);
            int tmp = dfs(1, inf);
            if(tmp == 0) break;
            ans += tmp;
        }
    }
}
void build() {
    for(int i = 1; i <= m; i++) {
        int u, v, w; cin >> u >> v >> w;
        adj[u].push_back({
             v, w, (int)adj[v].sz});   // inverse flow's index
        adj[v].push_back({u, 0, (int
             )adj[u].sz - 1}); // have pushed one, need to -1
    }
}
// Police Chase, need
     to open adj to Augment && ori to determine what pb give
// Dinic、dfs2, then use reach as u, if the edge
     pb has given && w == 0 && v is not in reach, is the ans
void dfs2(int now, unordered_set<int> &reach) {
    if(!vis[now]){
        vis[now] = 1;
        reach.insert(now);
        for(auto i : adj[now]){
            if(i.w > 0){
                dfs2(i.to, reach);
            }
        }
    }
}
// two two pair // School Dance
// Dinic, then w == 0's edge, which pb has given is the ans

// Distinct Route
// edge set valid var, if we need
     to argument pos road, the reverse edge set true valid;
// if we need argument the argumented
     edge' both set false. Last, from v dfs ans times
bool get_road(int now, vector<int> &ans, vector<bool> &vis) {
    if(now == 1) return true;
    for(auto &v : adj[now]){
        if(v.arg_valid && !vis[v.to]) {
            ans.push_back(v.to);
            vis[v.to] = true;
            bool flag = get_road(v.to, ans, vis);
            if(flag){
                v.arg_valid = false;
                return true;
            }
            ans.pop_back();
        }
    }
    return false;
}
```

4.2 MCMF [7f63db]

```
// Ceiled MinCostMaxFlow' if not, use dinic
typedef struct {
    int from, to, w, cost;
} edge;
int n, m, parcel;
vector<edge> adj;   // set num to each edge
vector<int> p[505]; // p[u] has edge's num
int now_edge = 0;
void add_edge(int u, int v, int w, int cost){
    adj.push_back({u, v, w, cost});
    p[u].push_back(now_edge);
    now_edge++;
    adj.push_back
        ({v, u, 0, -cost});    // argumenting path use -
    p[v].push_back(now_edge);
    now_edge++;
}
int Bellman_Ford(){
    vector<int> dis(n+1, inf); dis[1] = 0;
    vector<int> par(m);
    vector<int> flow_rec(n + 1, 0); flow_rec[1] = 1e9;
    for(int i = 1; i < n; i++){
        bool flag = 1;
        int size = adj.sz;
        for(int i = 0; i < size; i++){
            auto &[from, to, w, cost] = adj[i];
            if(w > 0 && dis[to] > dis[from] + cost){
                flag = 0;
                dis[to] = dis[from] + cost;
                par[to] = i;   // record num
                flow_rec[to] = min(flow_rec[from], w);
            }
        }
        if(flag) break;
    }
    if(dis[n] == 1e9) return 0;
    int mn_flow = flow_rec[n];
    int v = n;
    while(v != 1){
        int u = adj[par[v]].from;
        adj[par[v]].w -= mn_flow;
        adj[par[v] ^ 1].w += mn_flow;
        v = u;
    }
    mn_flow = min(mn_flow, parcel);
    parcel -= mn_flow;
    return mn_flow * dis[n];
}
void solve(){
    cin >> n >> m >> parcel;
    int ans = 0;
    for(int i = 1; i <= m; i++){
        int u, v, w, cost; cin >> u >> v >> w >> cost;
        add_edge(u, v, w, cost);
    }
    while(parcel > 0){
        int tmp = Bellman_Ford();
        if(tmp == 0) break;
        ans += tmp;
    }
    cout << (parcel > 0 ? -1 : ans);
}
```

5 String

5.1 KMP [132b98]

```
struct KMP {
    string sub;
    vector<int> failure;
    KMP(string &sub) {
        this->sub = sub;
        failure.resize(sub.size(), -1);
        buildFailFunction();
    }
    void buildFailFunction() {
        for(int i = 1; i < sub.size(); i++) {
            int now = failure[i - 1];
            while(now != -1
                  && sub[now + 1] != sub[i]) now = failure[now];
            if (sub[now + 1] == sub[i]) failure[i] = now + 1;
        }
    }
    vector<int> KMPmatching(string &s) {
        vector<int> match;
        for(int i = 0, now = -1; i < s.size(); i++) {
            // now is the compare sucessed length -1
            while (s[i] !=
                   sub[now + 1] && now != -1) now = failure[now];
            // f stores if comparison fail, move to where
            if (s[i] == sub[now + 1]) now++;
            if (now + 1 == sub.size()) {
                match.push_back(i - now);
                now = failure[now];
            }
        }
        return match;
    }
};
int main() {
    string s = "xxtxxtxtx";
    string sub = "tx";
    KMP kmp(sub);
    vector<int> ans = kmp.KMPmatching(s);
    for(auto &i : ans) cout << i << " ";
}
```

5.2 Manacher [9c9ca6]

```
// 找到對於每個位置的迴文半徑
vector<int> manacher(string s) {
    string t = "#";
    for (auto c : s) {
        t += c;
        t += '#';
    }
    int n = t.size();
    vector<int> r(n);
    for (int i = 0, j =
          0; i < n; i++) {    // i 是中心, j 是最長回文字串中心
        if (2 * j - i >= 0 && j + r[j] > i) {
            r[i] = min(r[2 * j - i], j + r[j] - i);
        }
        while (i - r[i] >=
             0 && i + r[i] < n && t[i - r[i]] == t[i + r[i]]) {
            r[i] += 1;
        }
        if (i + r[i] > j + r[j]) {
            j = i;
        }
    }
    return r;
    // # a # b # a #
    // 1 2 1 4 1 2 1
    // index 為奇數代表中心點在字元上(即回文字串長度是奇數)
}
```

5.3 Trie [3b3aa0]

```
struct Trie {
    struct trie_node {
```

```
        bool is_word;
        vector<trie_node *> children;
        trie_node() {
            is_word = false;
            children.resize(26, NULL);
        }
    };
    trie_node *root = new trie_node();
    void insert(string &s) {
        trie_node *cur = root;
        for (int i = 0; i < s.size(); i++) {
            int idx = s[i] - 'a';
            if (cur->children[idx] == NULL) {
                cur->children[idx] = new trie_node();
            }
            cur = cur->children[idx];
        }
        cur->is_word = true;
    }
    bool is_in_trie(string &s) {
        trie_node *cur = root;
        for (int i = 0; i < s.size(); i++) {
            if (cur->
                children[s[i] - 'a'] == nullptr) return false;
            cur = cur->children[s[i] - 'a'];
        }
        return true;
    }
    int search_i_start(string &s, int i, vector<int> &dp) {
        trie_node *cur = root;
        int sz = s.size(), ans = 0;
        for (int j = i; j < sz; j++) {
            if (cur
                ->children[s[j] - 'a'] == nullptr) return ans;
            cur = cur->children[s[j] - 'a'];
            if (cur->is_word)
                (ans += dp[j + 1]) %= mod;
        }
        return ans;
    }
};
int main() {
    // 找到 sub 集合裡，可以重複用，組成 s 的組數
    Trie trie;
    string s; cin >> s;
    int sz = s.size();
    // dp 代表 i 開頭到最後的配對總數
    // 找到有結尾為 stop 的 dp[i] += dp[j + 1]
    int n; cin >> n;
    vector<int> dp(sz + 1, 0);
    for (int i = 0; i < n; i++) {
        string sub; cin >> sub;
        trie.insert(sub);
    }
    dp[sz] = 1;
    for (int i = sz - 1; i >= 0; i--) {
        dp[i] = trie.search_i_start(s, i, dp);
    }
    cout << dp[0] << endl;
}
```

6 Math

6.1 質因數分解 [91ef59]

```
// a^(m-1) = 1 (mod m)
// a^(m-2) = 1/a (mod m)
// EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)
// Filter + DP; DP save min factor ' recur ' factor decomposition
// FacNums = (x+1)(y+1)(z+1)...
// FacSum = (a^0+a^1...+a^x)(b^0+...+b^y)
// FacMul = N(x+1)(y+1)(z+1)/2
int main() {
    vector<int> is_prime(2e6 + 1, 1);
    // 1 代表是質數，非 1 不是
    for (int i = 2; i <= 1000; i++) {
        if (is_prime[i] == 1) {
            for (int j = i + i; j <= 1000000; j += i) {
                is_prime[j] = i;
            }
        }
    }
    int ans = 1;
    int q; cin >> q;
    map<int, int> mp;
    while (is_prime[q] != 1) {
        mp[is_prime[q]]++;
        q /= is_prime[q];
    }
    if (q != 1) mp[q]++;
    for (auto [a, b] : mp) {
        ans *= b + 1;
    }
    cout << ans << "\n";
}
```

6.2 矩陣快速冪 [d41d8c]

```
const int mod = 1e9 + 7;
struct Mat {
    int n;
    vector<vector<int>> matrix;
    Mat(int n) {
        this->n = n;
        matrix.resize(n);
        for (int i = 0; i < n; i++) {
            matrix[i].resize(n);
        }
    }
    Mat(vector<vector<int>> matrix) {
        this->n = matrix.size();
        this->matrix = matrix;
    }
    Mat unit(int n) {   // 單位矩陣
        Mat res(n);
        for (int i = 0; i < n; i++) {
            res.matrix[i][i] = 1;
        }
        return res;
    }
    void mul(Mat b) {
        Mat ans(n);
        for (int i = 0; i < n; i++) {
            for (int j = 0; j < n; j++) {
                for (int k = 0; k < n; k++) {
                    (ans.matrix[i][j] += (matrix[
                        i][k] * b.matrix[k][j] % mod)) %= mod;
                }
            }
        }
        matrix = ans.matrix;
    }
    void pow(int p) {
        Mat x = *this;
        *this = unit(n);
        while (p > 0) {
            if (p & 1) {
                mul(x);
            }
            x.mul(x);
            p >>= 1;
        }
    }
};
signed main() {
    int n, ans; cin >> n;
    if (n <= 4) {
        vector<int> v = {0, 1, 1, 2, 4};
        ans = v[n];
    }
    else {
        Mat mat({{4, 2, 1}, {2, 1, 1}, {1, 1, 0}});
        Mat x(3);
        x.matrix = {{1, 1, 0}, {1, 0, 1}, {1, 0, 0}};
        x.pow(n - 4);
        mat.mul(x);
        ans = mat.matrix[0][0];
    }
    cout << ans << "\n";
}
// 初始矩陣   轉移式
// f4 f3 f2   1 1 0    f5 f4 f3
// f3 f2 f1   1 0 1 => f4 f3 f2
// f2 f1 f0   1 0 0    f3 f2 f1
```

6.3 盧卡斯定理 [fdcf53]

```
struct nCr {
    int mod;
    nCr(int mod) : mod(mod) {};
    int inverse(int num) {
        if (num == 1) return 1;
        return (mod
            - ((mod / num) * inverse(mod % num)) % mod) % mod;
    }
    int fast_exp(int x, int p) {
        int ans = 1;
        while (p > 0) {
            if (p & 1) ans = (ans * x) % mod;
            x = x * x % mod;
            p >>= 1;
        }
        return ans;
    }
    vector<int> fac;
    void BuildLucas(int n) {
        fac.resize(n + 1);
        fac[0] = 1;
        for(int i = 1; i <= n; i++) {
            fac[i] = fac[i - 1] * i % mod;
        }
    }
    int C(int m, int n) {
        return m < n ? 0 : fac[m] *
            inverse(fac[n]) % mod * inverse(fac[m - n]) % mod;
    }
    int Lucas(int m, int n) {
        return n == 0 ? 1 % mod : Lucas
            (m / mod, n / mod) * C(m % mod, n % mod) % mod;
    }
};
```

6.4 樹論分塊 [99629d]

```cpp
// CSES_Sum_of_Divisors
const int mod = 1e9 + 7;
const int inv_2 = 500000004;
// n / 1 * 1 + n / 2 * 2 + n / 3 * 3 + ... + n / n * n
signed main() {
    ios::sync_with_stdio(false);
    cin.tie(nullptr);

    int ans = 0;
    int n; cin >> n;
    for (int l = 1, r; l <= n; l = r + 1) {
        r = n / (n / l);
        int val = n / l;    // n / l 到 n / r 一樣的值
        int sum = (((l + r) % mod) *
             ((r - l + 1) % mod)) % mod * inv_2;    // l 加到 r
        val %= mod; sum %= mod;
        ans += val * sum;
        ans %= mod;
    }
    cout << ans << "\n";
}
```

6.5 Theorem

- 數論分塊可以快速計算一些含有除法向下取整的和式，就是像 $\sum_{i=1}^{n} f(i)g(\lfloor \frac{n}{i} \rfloor)$ 的和式。當可以在 $O(1)$ 內計算 $f(r)-f(l)$ 或已經預處理出 f 的前綴和時，數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x)=\sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
  - 莫比烏斯函數
    1. 定義
    $$\sum_{d|n}\mu(d)=\begin{cases}1 & \text{for } n=1\\ 0 & \text{for } n\neq 0\end{cases}$$
    2. μ 是常數函數 1 的反元素
    $\Rightarrow \mu * 1=\epsilon$，$\epsilon(n)$只在$n=1$時為 1，其餘情況皆為 0。
  - ϕ 歐拉函數: x 以下與 x 互質的數量

$$\begin{aligned}\phi * 1 &= \sum_{d|n}\phi(\frac{n}{d}) \text{ 質因數分解}\\ &= \sum_{i=0}^{c}\phi(p^i)\\ &= 1+p^0(p-1)+p^1(p-1)+...+p^{c-1}(p-1)\\ &= p^c\\ &= id\end{aligned}$$

- 莫比烏斯反演公式
  - $f(n)=\sum_{d|n} g(d) \Leftrightarrow g(n)=\sum_{d|n}\mu(d)f(\frac{n}{d})$
  - $f(n)=\sum_{n|d} g(d) \Leftrightarrow g(n)=\sum_{n|d}\mu(\frac{d}{n})f(d)$
- 例子

$$\begin{aligned}&\sum_{i=a}^{b}\sum_{j=c}^{d}[gcd(i,j)=k]\\ &\Rightarrow \sum_{i=1}^{x}\sum_{j=1}^{y}[gcd(i,j)=k]\\ &= \sum_{i=1}^{\lfloor \frac{x}{k} \rfloor}\sum_{j=1}^{\lfloor \frac{y}{k} \rfloor}\epsilon(gcd(i,j))\\ &= \sum_{i=1}^{\lfloor \frac{x}{k} \rfloor}\sum_{j=1}^{\lfloor \frac{y}{k} \rfloor}\sum_{d|gcd(i,j)}\mu(d)\\ &= \sum_{d=1}^{\infty}\mu(d)\sum_{i=1}^{\lfloor \frac{x}{k} \rfloor}[d|i]\sum_{j=1}^{\lfloor \frac{y}{k} \rfloor}[d|j] \text{ d 可整除 i 時為 1}\\ &= \sum_{d=1}^{min(\lfloor \frac{x}{k} \rfloor, \lfloor \frac{y}{k} \rfloor)}\mu(d)\lfloor \frac{x}{kd} \rfloor\lfloor \frac{y}{kd} \rfloor\end{aligned}$$

6.6 莫比烏斯反演 [d41d8c]

```cpp
const int maxn = 2e5;
int mobius_pref[maxn];
void init() {
    mobius_pref[1] = 1;
    vector<int> wei
        (maxn);  // wei = 0 代表是質數，-1 代表可被平方數整除
    for (int i = 2; i < maxn; i++) {
        if (wei[i] == -1) {
            mobius_pref[i] = mobius_pref[i - 1];
            continue; // 包含平方
        }
        if (wei[i] == 0) {
            wei[i] = 1;
            for (int j = 2; i * j < maxn; j++) {
                if (j % i == 0) wei[i * j] = -1;
                else if (wei[i * j] != -1) wei[i * j]++;
            }
        }
        mobius_pref[i]
            = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
    }
}
void solve() {
    int a, b, c, d, k; cin >> a >> b >> c >> d >> k;
    auto cal = [&](int x, int y) -> int {
        int res = 0;
        for (int l = 1, r; l <= min(x, y); l = r + 1) {
            r = min(x / (x / l), y / (y / l));
            res += (mobius_pref[r] - mobius_pref[l
                - 1]) * (x / l) * (y / l);  // 代推出來的式子
        }
        return res;
    };
    cout << cal
        (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k,
         (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n";
}
```

7 Search and Gready

7.1 二分搜 [d41d8c]

```cpp
int main() {
    int l = 1, r = 10;
    // 1 to tar, find tar
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}
```

7.2 三分搜 [d41d8c]

```cpp
// 找極值問題，遞增遞減
void solve() {
    int l = 0, r = 10, ans = 0; // ans 紀錄答案
    while (l <= r) {
        int d = (r - l) / 3;    // 差
        int ml = l + d, mr = r - d; // mr 要用減的
        auto cal = [&](int m) -> int {
            int x = 0;
            return x;   // 計算答案
        };
        int ansl = cal(ml), ansr = cal(mr);
        if (ansl < ansr) {
            l = ml + 1;
        }
        else r = mr - 1;
    }
}
```

8 Tree

8.1 LCA [2be9ca]

```cpp
int main() {
    int n, q; cin >> n >> q;
    vector<vector<int>> tree(n + 1);
    for (int i = 1; i < n; i++) {
        int u, v; cin >> u >> v;
        tree[u].push_back(v);
        tree[v].push_back(u);
    }
    vector<vector<int>> par(n + 1, vector<int>(18));
    vector<int> depth(n + 1);
    auto dfs = [&](auto self, int u, int pre) -> void {
        for (auto v : tree[u]) {
            if (v == pre) continue;
            par[v][0] = u;  // 2 ^ 0
            depth[v] = depth[u] + 1;
            self(self, v, u);
        }
    };
    dfs(dfs, 1, 0);
    for (int i = 1; i < 18; i++) {
        for (int j = 1; j <= n; j++) {
            par[j][i] = par[par[j][i - 1]][i - 1];
        }
```

```
    }
    auto lca = [&](int a, int b) -> int {
        if (depth[a] < depth[b]) swap(a, b);
        int pull = depth[a] - depth[b];
        for (int i = 0; i < 18; i++) {
            if (pull & (1 << i)) {
                a = par[a][i];
            }
        }
        if (a == b) return a;
        for (int i = 17; i >= 0; i--) {
            if (par[a][i] != par[b][i]) {
                a = par[a][i], b = par[b][i];
            }
        }
        return par[a][0];
    };
}
```

8.2 樹 DFS [7b2c0c]

```
const int maxn = 2e5+5;
vector<int> depth;
void dfs(vector<vector<int>> &tree, int u, int pre) {
    for(auto v : tree[u]){
        if(v == pre)
        depth[v] = depth[u] + 1;
        dfs(tree, v, u);
    }
}
```

8.3 樹重心 [833d90]

```
const int maxn = 2e5+5;
vector<int> tree[maxn];
int cen = 0, n;
int dfs(int par, int now) {
    bool flag = 1;
    int size = 0;
    for (auto nxt : tree[now]) {
        if (par != nxt) {
            int subsize = dfs(now, nxt);
            if (subsize > n / 2) flag = false;
            size += subsize;
        }
    }
    if (n - 1 - size > n / 2) flag = false;
    if (flag) cen = now;
    return size + 1;
}
int main() {
    cin >> n;
    for (int i = 1; i < n; i++) {
        int u, v; cin >> u >> v;
        tree[u].push_back(v);
        tree[v].push_back(u);
    }
    for (int i = 1; i <= n; i++) {
        for (auto nxt : tree[i])
            dfs(i, nxt);
        if (cen) break;
    }
}
```

8.4 節點距離總和 [52870c]

```
const int maxn = 2e5+5;
vector<int> tree[maxn];
vector<int> subtree(maxn, 1);
long long ans[maxn];
int n;
void dfs(int par, int now, int depth) {
    ans[1] += depth;
    for (auto nxt : tree[now]) {
        if (par != nxt) {
            dfs(now, nxt, depth + 1);
            subtree[now] += subtree[nxt];
        }
    }
}
void find_ans(int par, int now) {
// each sub's dis make - 1, non subnode + 1
    for (auto nxt : tree[now]) {
        if (par != nxt) {
            ans[nxt] =
                  ans[now] + (n - subtree[nxt]) - subtree[nxt];
            find_ans(now, nxt);
        }
    }
}
int main() {
    cin >> n;
    for (int i = 1; i < n; i++) {
        int u, v; cin >> u >> v;
        tree[u].push_back(v);
        tree[v].push_back(u);
    }
    dfs(0, 1, 0);
    find_ans(0, 1);
    for (int i = 1; i <= n; i++) {
        cout << ans[i] << " ";
    }
}
```

8.5 有權樹直徑 [ca20c3]

```
// weighted tree centroid
const int maxn = 1e5+5;
vector<pair<int, int>> tree[maxn];
ll dp[maxn];
ll ans = 0;
void DP(int now, int par){
    ll mx1 = 0; ll mx2 = 0;
    for(auto [nxt, w] : tree[now]){
        if(nxt == par) continue;
        DP(nxt, now);
        if(mx1 < w + dp[nxt]){ // mx2 = mx1, mx1 = new mx
            mx2 = mx1; mx1 = w + dp[nxt];
        }
        else if(mx2 < w + dp[nxt]){ // mx2 = new
            mx2 = w + dp[nxt];
        }
    }
    dp[now] = mx1;
    ans = max(ans, mx1 + mx2);
}
int main(){
    int n; cin >> n;
    memset(dp, 0, sizeof(dp));
    for(int i = 1; i < n; i++){
        int u, v, w; cin >> u >> v >> w;
        tree[u].push_back({v, w});
        tree[v].push_back({u, w});
    }
    DP(1, 0);
    cout << (ans < 0 ? 0 : ans);
}
```

8.6 樹壓平 [83ba92]

```
// 父節
    點加值 = 所有子節點區間加值，求單點，使用 bit，做前綴差分
// CSES 1138_Path Queries
struct BIT {    // BIT 都是 1-based 的查詢
    int n;
    vector<int> bit;
    BIT(int n) {    // 有幾個數
        this->n = n;
        bit.resize(n + 1, 0);
    }
    BIT(vector<int> &init) {    // 必須是 1-based
        this->n = init.size() - 1;
        bit.resize(n + 1, 0);
        for (int i = 1; i <= n; i++) {
            modify(i, init[i]);
        }
    }
    void modify(int i, int val) {
        for (; i <= n; i += i & -i) {
            bit[i] += val;
        }
    }
    int query(int r) {
        int ans = 0;
        for (; r; r -= r & -r) ans += bit[r];
        return ans;
    }
    int query(int l, int r) {
        return query(r) - query(l - 1);
    }
};
void solve(){
    int n, q; cin >> n >> q;
    vector<int> node_value(n + 1), euler_ordered_value(n);
    for (int i = 1; i <= n; i++) {
        cin >> node_value[i];
    }
    vector<vector<int>> tree(n + 1);
    for (int i = 1; i < n; i++) {
        int u, v; cin >> u >> v;
        tree[u].push_back(v);
        tree[v].push_back(u);
    }
    vector<pair<int, int>> tree_mapping(n + 1);
    int cnt = 0;
    auto dfs = [&](auto self, int u, int par) -> void {
        euler_ordered_value[++cnt] = node_value[u];
        tree_mapping[u].first = cnt;
        for (auto v : tree[u]) {
            if (v == par) continue;
            self(self, v, u);
        }
        tree_mapping[u].second = cnt;
    };
    dfs(dfs, 1, 0);
    BIT bit(n);
    for (int i = 1; i <= n; i++) {
        bit.modify(tree_mapping[i].first, node_value[i]);
        if (tree_mapping[i].first < n) {
            bit.modify
                 (tree_mapping[i].second + 1, -node_value[i]);
        }
    }
    for (int i = 0; i < q; i++) {
        int op; cin >> op;
```

```
        if (op == 1) {
            int s, x; cin >> s >> x;
            int add = x
                  - euler_ordered_value[tree_mapping[s].first];
            euler_ordered_value[tree_mapping[s].first] = x;
            bit.modify(tree_mapping[s].first, add);
            if (tree_mapping[s].first < n) {
                bit.modify(tree_mapping[s].second + 1, -add);
            }
        }
        else {
            int node; cin >> node;
            cout <<
                  bit.query(tree_mapping[node].first) << "\n";
        }
    }
}
```

9 DP

9.1 背包問題 [6d6b63]

```
// 考慮前 i 個，預算有 j 塊錢的最多 page
int main(){
    int n, bud;
    cin >> n >> bud;
    vector<vector<int>> dp(n + 1, vector<int>(bud + 1));
    vector<int> Page(n + 1, 0);
    vector<int> Price(n + 1, 0);

    for(int i = 1; i <= n; i++){
        cin >> Price[i];
    }
    for(int i = 1; i <= n; i++){
        cin >> Page[i];
    }
    for (int i = 1; i <= n; i++) {
        for (int j = 1; j <= bud; j++) {
            if (j >= Price[i]) {  // 買得起
                // 不買或買
                dp[i][j] = max(dp[i -
                     1][j], dp[i - 1][j - Price[i]] + Page[i]);
            }
            else {
                dp[i][j] = dp[i - 1][j];
            }
        }
    }
    cout << dp[n][bud] << "\n";
}
```

9.2 Bitmask DP [b18541]

```
void travel_exactly_once(){
    // [走過的路][終點]
    vector<vector<int>> dp(1 << 20, vector<int> (20, 0));
    vector<int> rev_adj[20];
    int n, m; cin >> n >> m;
    for(int i = 0; i < m; i++){
        int u, v; cin >> u >> v;
        rev_adj[--v].push_back(--u);
    }
    dp[1][0] = 1;
    for (int road = 0; road < (1 << n); road++) {
        // 沒經過起點，不用走
        if (road & 1 == 0) continue;
        // 有終點但沒全部走過
        if (road & (1
              << (n - 1)) && road != ((1 << n) - 1)) continue;
        // DP，隨便選定一個當前路徑的終點
        for (int end = 0; end < n; end++) {
            // 路徑沒包含假定的 end
            if ((road & (1 << end)) == 0) continue;
            // 去除終點，得到 pre_road
            int pre_road = road - (1 << end);
            // 從 rev_adj 找 pre_road 的終點
            for (int pre_road_end : rev_adj[end]) {
                if ((road & (1 << pre_road_end))) {
                    dp[road
                         ][end] += dp[pre_road][pre_road_end];
                    dp[road][end] %= mod;
                }
            }
        }
    }
    cout << dp[(1 << n) - 1][n - 1];
}
void elevator_rides(){
    int n, k; cin >> n >> k;
    vector<int> passenger(n);
    for (int i = 0; i < n; i++) cin >> passenger[i];
    vector<int
         > used(1 << n, 0);     // 最後載完人的電梯用了多少空間
    vector<int> dp(1 << n, 1);  // bitset
    for (int i = 1; i < 1 << n; i++) {
        used[i] = dp[i] = 2e9;
        for (int j = 0; j < n; j++) {
            if (i & (1 << j)) {  // 有 j
                int pre = i ^ (1 << j);
                // 最後的電梯還能載 j
                if (used[pre] + passenger[j] <= k) {
                    // 電梯數先比，再來比用掉的空間
                    if (dp
                         [pre] < dp[i] || (dp[pre] == dp[i] &&
                         used[pre] + passenger[j] < used[i])) {
                        used[i] = used[pre] + passenger[j];
                        dp[i] = dp[pre];
                    }
                }
                // 搭新的電梯
                else {
                    if (dp[pre] + 1 < dp[i] || (dp[pre] + 1
                         == dp[i] && passenger[j] < used[i])) {
                        used[i] = passenger[j];
                        dp[i] = dp[pre] + 1;
                    }
                }
            }
        }
    }
    cout << dp[(1 << n) - 1];
}
int main(){
    travel_exactly_once();
    elevator_rides();
}
```

9.3 硬幣 [d41d8c]

```
void coin_combination_II(){
    // 有 n 種錢幣，求組合為 x 的組數，順序不可顛倒
    // 可顛倒的話只要一維，先 x 迴圈，再 coin[i] 去加
    int n, x; cin >> n >> x;
    vector<int> coin(n + 1);
    // dp[i][j] 為考慮前 i 個硬幣，組合為 i 的組數
    vector<vector<int>> dp(2, vector<int>(x + 1, 0));
    dp[0][0] = 1;
    for (int i = 1; i <= n; i++) cin >> coin[i];
    for (int i = 1; i <= n; i++){
        for (int j = 0; j <= x; j++) {
            // 壓到 2 * n
            dp[i & 1][j] = dp[!(i & 1)][j];
            if (j >= coin[i]) {
                (dp[i
                     & 1][j] += dp[i & 1][j - coin[i]]) %= mod;
            }
        }
    }
    cout << dp[n & 1][x];
}
void minimize_coins_nums(){
    // 有 n 種錢幣，求組合為 x 的最小硬幣數
    int n, x; cin >> n >> x;
    vector<int> coin(n);
    for (int i = 0; i < n; i++) cin >> coin[i];
    // dp[i] 是組合為 i 的最小硬幣數
    vector<int> dp(x + 1, 0);
    for (int i = 1; i <= x; i++) {
        dp[i] = 2e9;
        for(auto &j : coin){
            if(j <= i){
                dp[i] = min(dp[i], dp[i - j] + 1);
            }
        }
    }
    cout << (dp[x] == 2e9 ? -1 : dp[x]);
}
int main(){
    coin_combination_II();
    minimize_coins_nums();
}
```

9.4 編輯距離 [4d4a6d]

```
int main() {
    string s1, s2; cin >> s1 >> s2;
    int size1 = s1.size(), size2 = s2.size();
    // dp[i][j] 為 s1 的前 i 個字元，跟 s2 的前 j 個字元
    vector<
         vector<int>> dp(size1 + 1, vector<int>(size2 + 1, 0));
    s1 = "0" + s1, s2 = "0" + s2;
    for (int i = 1; i <= size1; i++) dp[i][0] = i;
    for (int i = 1; i <= size2; i++) dp[0][i] = i;
    for (int i = 1; i <= size1; i++){
        for (int j = 1; j <= size2; j++) {
            if (s1[i] == s2[j]) {
                dp[i][j] = dp[i - 1][j - 1];
            }
            else {
                // s1 新增等價於 s2 砍掉
                // dp[i][j] = min(修改, s1 新增, s2 新增);
                dp[i][j] = min({dp[i - 1][
                     j - 1], dp[i - 1][j], dp[i][j - 1]}) + 1;
            }
        }
    }
    cout << dp[size1][size2];
}
```

9.5 LCS [087c0d]

```
int main() {
    int m, n; cin >> m >> n;
    string s1, s2;
    cin >> s1 >> s2;
    int L = 0;
    vector<vector<int>> dp(m + 1, vector<int>(n + 1, 0));

    for (int i = 1; i <= m; i++) {
        for (int j = 1; j <= n; j++) {
            if (s1[i - 1] == s2[j - 1]) {
                dp[i][j] = dp[i - 1][j - 1] + 1;
            }
            else {
                dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
            }
        }
    }
    int length = dp[m][n];
    cout << length << "\n";
    string s(length, 'c');
    // along to dp to trace back
    while (m >= 1 && n >= 1) {
        if (s1[m - 1] == s2[n - 1]) {
            s[length - 1] = s1[m - 1];
            m--, n--, length--;
        }
        else {
            if (dp[m - 1][n] > dp[m][n - 1]) m--;
            else n--;
        }
    }
    cout << s << "\n";
}
```

9.6 LIS [668131]

```
int main() {
    int n; cin >> n;
    vector<int> v(n);
    for (int i = 0; i < n; i++) {
        cin >> v[i];
    }
    int dp[n]; vector<int> mono;
    mono.push_back(v[0]);
    dp[0] = 1;  int L = 1;
    for (int i = 1; i < n; i++) {
        if (v[i] > mono.back()) {
            mono.push_back(v[i]);
            dp[i] = ++L;
        }
        else {
            auto it
                = lower_bound(mono.begin(), mono.end(), v[i]);
            *it = v[i];
            dp[i] = it - mono.begin() + 1;
        }
    }
    vector<int> ans;
    cout << L << "\n";
    for (int i = n - 1; i >= 0; i--) {
        if (dp[i] == L) {
            ans.push_back(v[i]);
            L--;
        }
    }
    reverse(ans.begin(), ans.end());
    for (auto i : ans) {
        cout << i << " ";
    }
}
```

9.7 Projects [479ba0]

```
struct project {
    int from, end, gain, id;
};
int main() {
    int n; cin >> n;
    vector<project> projects(n + 1);
    for (int i = 1; i <= n; i++) {
        cin >> projects
            [i].from >> projects[i].end >> projects[i].gain;
        projects[i].id = i;
    }
    sort(all(projects), [](project a, project b) {
        if (a.end == b.end) return a.gain < b.gain;
        return a.end < b.end;
    });
    vector<array
        <int, 3>> dp(n + 1, {0, 0, 0}); // nums, gain, time
    vector<int> par(n + 1, 0), ans, add(n + 1, -1);
    for (int i = 1; i <= n; i++) {
        int idx = --upper_bound(projects.begin(), projects.
            begin() + i, project({0, projects[i].from, 0, 0}),
            [](const project &a, const project &b) -> bool {
                return a.end < b.end;
            }) - projects
                .begin();   // 二分搜最接近 from 的 end
        dp[i] = dp[i - 1];
        par[i] = i - 1;
        if (dp[i][1] < dp[idx][1] + projects[i].gain ||
        (dp[i][1]
            == dp[idx][1] + projects[i].gain && dp[i][2] > dp
            [idx][2] + projects[i].end - projects[i].from)) {
            dp[i] = {dp[idx
                ][0] + 1, dp[idx][1] + projects[i].gain, dp[
                idx][2] + projects[i].end - projects[i].from};
            par[i] = idx;
            add[i] = projects[i].id;
        }
    }
    cout << dp
        [n][0] << " " << dp[n][1] << " " << dp[n][2] << "\n";
    for (int now = n; now > 0; now = par[now]) {
        if (add[now] != -1)
            ans.push_back(add[now]);
    }
    sort(all(ans));
    for (auto &i : ans) cout << i << " ";
}
```

9.8 Removal Game [211de0]

```
// 兩個人比賽，每個人輪流取一個數字且只能是頭尾
// 問兩人都選得好，第一個人可取得的最大分數
int main() {
    int n; cin >> n;
    vector<vector<int>> dp(n + 1, vector<int>(n + 1));
    int pref = 0;
    vector<int> v(n + 1);
    for (int i = 1; i <= n; i++) {
        cin >> v[i];
        pref += v[i];
    }
    // dp[i][j] 是 i 到 j 區間選完，的最大分數差
    for (int i = n; i > 0; i--) {
        for (int j = i; j <= n; j++) {
            if (i == j) {
                dp[i][j] = v[i];
            }
            else {
                // 選左差距大，還是選右差距大
                dp[i][j] = max(
                    v[i] - dp[i + 1][j], v[j] - dp[i][j - 1]);
            }
        }
    }
    // x + y = sum, dp[1][n] = x - y;
    cout << (pref + dp[1][n]) / 2;
}
```

9.9 Max overlap [07fccd]

```
// CF 1932 pF
// 給你很多區間，你可以選一些點，重疊到的線段得到 1 分
// 請問在線段不重複的情況下，最多獲得幾分
int main() {
    int n, m;
    cin >> n >> m;
    // 記錄每點有幾個線段
    // 再一個紀錄，包含這個點的左界
    vector<int> l_side(n + 1, inf), cnt(n + 5, 0);
    for (int i = 0; i < m; i++) {
        int l, r; cin >> l >> r;
        l_side[r] = min(l_side[r], l);
        cnt[l]++;
        cnt[r + 1]--;
    }
    for (int i = 2; i <= n; i++) {
        cnt[i] += cnt[i - 1];
    }
    for (int i = n; i >= 2; i--) {
        l_side[i - 1] = min(l_side[i - 1], l_side[i]);
    }
    vector<int> dp(n + 1);
    dp[0] = 0;
    for (int i = 1; i <= n; i++) {
        dp[i] = cnt[i];
        if (l_side[i] != inf) {
            dp[i] += dp[l_side[i] - 1];
        }
        dp[i] = max(dp[i], dp[i - 1]);
    }
    cout << dp[n] << "\n";
}
```

10 Geometry

10.1 Cross Product [8113ac]

```
const double eps = 1e-8;
struct point {
    double x, y;
    point operator * (int a){ return {a * x, a * y}; }
    point operator + (point b){ return {x + b.x, y + b.y}; }
    point operator - (point b){ return {x - b.x, y - b.y}; }
    double operator * (point b){ return x * b.x + y * b.y; }
    double operator ^ (point b){ return x * b.y - y * b.x; }
    bool operator
        < (point b){ return x == b.x ? y < b.y : x < b.x; }
```

```
};
double abs(point a) { return sqrt(a * a); }
int sign
     (double a) { return fabs(a) < eps ? 0 : a > 0 ? 1 : -1; }
int ori(point
      a, point b, point c) { return sign((b - a) ^ (c - a)); }
bool colinear(point a,
     point b, point c) { return sign((b - a) ^ (c - a)) == 0; }
bool between(point a, point b, point c){ // c between a and b
    if (!colinear(a, b, c)) return false;
    return sign((a - c) * (b - c)) <= 0;
}
bool intersect(point
      a, point b, point c, point d){ // line(a, b) line(c, d)
    int abc = ori(a, b, c);
    int abd = ori(a, b, d);
    int cda = ori(c, d, a);
    int cdb = ori(c, d, b);
    if(abc == 0 || abd == 0)
        return between(a, b, c) || between
             (a, b, d) || between(c, d, a) || between(c, d, b);
    return abc * abd <= 0 && cda * cdb <= 0;
}
```

10.2 Convex Hull [e84f76]

```
vector<pii> P, L, U;
int cross(pii o, pii a, pii b){ // OA OB > 0 counterclock
    return (a.first - o.first) * (b.second
         - o.second) - (a.second-o.second) * (b.first-o.first);
}
int Andrew_monotone_chain(int n){
    sort(P.begin(), P.end());
    int l = 0, u = 0;   // upper and lower hull
    for (int i=0; i<n; ++i){
        while (l >= 2 && cross(L[l-2], L[l-1], P[i]) <= 0){
            l--;
            L.pop_back();
        }
        while (u >= 2 && cross(U[u-2], U[u-1], P[i]) >= 0){
            u--;
            U.pop_back();
        }
        l++;
        u++;
        L.push_back(P[i]);
        U.push_back(P[i]);
    }
    cout << l << ' ' <<  u << '\n';
    return l + u;
}
int main(){
    int n, x, y;
    cin >> n;
    for(int i = 0;i < n;i++){
        cin >> x >> y;
        P.push_back({x, y});
    }
    int ans = Andrew_monotone_chain(n) - 2;
    cout << ans << "\n";
    return 0;
}
```