Contents

```
6 Math
  Basic
                                    6.1 Prime . . . . . . . . . . . . . . . .
  1.1 Install VScode . . . . . . .
                                    1.4 Pbds . . . . . . . . . . . .
  6.6 Integer Partition . . . . . 12
                                    6.7 Mobius Theorem . . . . . 12
                                    6.8 Mobius Inverse . . . . . 12
6.9 Catalan Theorem . . . . 12
2 Graph
     DFS And BFS . . . . . . . .
  2.1
                                    6.10 Burnside's Lemma . . . . . 13
  7 Search and Gready 13 7.1 Binary Search . . . . . 13 7.2 Ternary Search . . . . . 13
  2.4 FloydWarshall . . . . . . .
  2.5 Euler . . . . . . . . . . . . . .
  2.6 DSU . . . . . . . . . . . .
  8 Тгее
                                                               13
                                    2.9 EBCC . . . . . . . . . . .
  2.10 2-SAT . .
                                    8.3 Tree Flattening . . . . . 13
8.4 Heavy Light Decomposition 14
  2.11 Funtional Graph . . . . . .
                                    8.5 Link Cut Tree . . . . . . . 14 8.6 Virtual Tree . . . . . . . 15
3 Data Structure
                                    8.7 Dominator Tree . . . . . 15
  3.2 RangeBit . . . . . . . . . .
      Segment . . . . . . . . . . . .
                                    DΡ
      Lazy Segment . . . . . .
                                    9.1 LCS . . . . . . . . . . . . . 16
  3.5
     Treap . . . . . . . . . . . . . . . .
                                    3.6 RMQ . . . . . . . . . . . .
  3.7
      Mo . . . . . . . . . . . . .
  Flow
                                    9.6 Removal Game . . . . . . 16 9.7 Monotonic Queue . . . . 17
  4.2 Min Cut . . . . . . . . . .
  9.8 SOS . . . . . . . . . . . . 17
                                    5.1 Hash . . . . . . . . . . . .
  10 Geometry
                                    10.1 Basic .
  10.4 LatticePoints . . . . . . 20
10.5 MinCoverCircle . . . . . 20
```

5.8 Duval 10

1 Basic

1.1 Install VScode [d41d8c]

1.2 Default Code [d41d8c]

```
#include <bits/stdc++.h>
// #pragma GCC target("popcnt")
// C++ 20 vector grammer will not work
using namespace std;
using ll = long long;

void solve() {
}

int main() {
    ios_base::sync_with_stdio(false);
    cin.tie(nullptr);
    int t = 1;
    cin >> t;
    while (t--) {
        solve();
    }
}
```

1.3 Compare Fuction [d41d8c]

```
|// 1. sort, 二分搜刻在函式內 lambda 就好
|// 2. priority queue 小到大是 >, set 是 <
|// 3. set 不能 = , multiset 必須 =
|// 4. 確保每個成員都要比到
|// 5. pbds_multiset 不要用 lower_bound
|// 6. 如果要用 find, 插入 inf 後使用 upper_bound
|// 7. multiset 可以跟 set 一樣使用, 但請注意第 3 \ 4 點
auto cmp = [](int i, int j) { return i > j; };
priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
```

```
vector<int> a {1, 2, 5, 4, 3}; // 小心不要改到 a auto cmp = [&a](int i, int j) { return a[i] > a[j]; }; priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
```

1.4 Pbds [d41d8c]

1.5 Double [b44e11]

```
double x;
constexpr static double eps = 1e-12;
D() : x{0.0} {}
D(double v) : x{v} {}
double val() const { return x; }
explicit operator double() const { return x; }
  operator -() const {
    return D(-x);
D & operator += (const D & rhs) & {
    x += rhs.x; return *this;
D & operator -= (const D & rhs) & {
    x -= rhs.x; return *this;
D & operator *= (const D & rhs) & {
    x *= rhs.x; return *this;
D & operator /= (const D & rhs) & {
    assert(fabs(rhs.x) > eps);
x /= rhs.x; return *this;
friend D operator+(D lhs, const D &rhs) {
    return lhs += rhs;
friend D operator - (D lhs, const D &rhs) {
    return lhs -= rhs;
friend D operator*(D lhs, const D &rhs) {
    return lhs *= rhs;
friend D operator/(D lhs, const D &rhs) {
    return lhs /= rhs;
friend bool operator <(const D &lhs, const D &rhs) {
   return lhs.x - rhs.x < -eps;</pre>
friend bool operator > (const D &lhs, const D &rhs) {
    return lhs.x - rhs.x > eps;
friend bool operator==(const D &lhs, const D &rhs) {
    return fabs(lhs.x - rhs.x) < eps;
friend bool operator <= (const D &lhs, const D &rhs) {
   return lhs < rhs || lhs == rhs;</pre>
friend bool operator>=(const D &lhs, const D &rhs) {
   return lhs > rhs || lhs == rhs;
friend bool operator!=(const D &lhs, const D &rhs) {
   return !(lhs == rhs);
friend istream &operator>>(istream &is, D &a) {
    double v; is >> v; a = D(v); return is;
} // eps should < precision
```

1.6 Rng [401544]

```
mt19937_64 rng
          (chrono::steady_clock::now().time_since_epoch().count());
ll x = rng(); shuffle(a.begin(), a.end(), rng);
```

2 Graph

};

2.1 DFS And BFS [e2d856]

```
int main() {
   int n;
   vector<vector<int>>> adj(n);
   // dfs_graph
   vector<bool> vis(n);
   auto dfs = [&](auto self, int u) -> void {
      if (vis[u]) return;
      vis[u] = true;
      for (auto v: adj[u]) {
            self(self, v);
      }
}
```

```
}
    dfs(dfs, 0);
    // bfs
vector < int > depth(n, 1e9);
    queue < int > q;
auto bfs = [&](auto self, int s) -> void {
    vis[s] = true, depth[s] = 0;
         q.push(s);
         q.push(v);
              }
         }
    bfs(bfs, 0);
}
```

2.2 Prim [3a3805]

```
auto prim =
                                    [&](int n, vector<vector<pair<int, int>>> &adj) -> bool {
                          int node_sz = 0;
                        priority_queue
                                                auto [u, w] = pq.top(); pq.pop();
if (vis[u]) continue;
vis[u] = true;
                                                node_sz++;
for (auto v : adj[u]) {
    if (!vis[v.first]) {
                                                                                            pq.emplace(v.second, v.first);
                                               }
                          if (node_sz == n) return true;
                         return false:
};
```

2.3 BellmanFord [430ded]

```
'用 Bellman Ford 找負環
// 用 Bellmur
int main() {
        int n, m; cin >> n >> m;
       vector < array < int , 3>> e;
for (int i = 0; i < m; i++) {</pre>
               int u, v, w; cin >> u >> v >> w;
u--, v--; e.push_back({u, v, w});
       vector < ll> dis(n, ini), per("),
int t = -1; dis[0] = 0;
for (int i = 1; i <= n; i++) {
    for (auto [u, v, w] : e) {
        if (dis[v] > dis[u] + w) {
            dis[v] = dis[u] + w;
            reconstructions.
        vector<ll> dis(n, inf), par(n);
                               par[v] = u;
if (i == n) t = v;
                      }
              }
       if (t == -1) { cout << "NO\n"; return; }
for (int i = 1; i < n; i++) t = par[t];
vector <int> ans {t};
        int i = t;
       do {
    i = par[i];
               ans.push_back(i);
       } while (i != t);
reverse(ans.begin(), ans.end());
        cout << "YES\n";
        for (auto x : ans) cout << x + 1 << " ";</pre>
```

2.4 FloydWarshall [3f61a4]

```
constexpr ll inf = 1e18:
void FloydWarshall(int n, int m) {
    int n, m; cin >> n >> m;
vector <vector <int>> or m;
for (int i = 0; i < m; i++) {
   int u, v, w; cin >> u >> v >> w;
   dis[u][v] = min(dis[u][v], w);
   dis[v][u] = min(dis[v][u], w);
}
    }
    }
```

```
const int N = 500; // Floyd 封包
void Floyd(int n, vector bitset <N>> &dp) {
    for (int k = 0; k < n; k++)
        for (int i = 0; i < n; i++)
        if (dp[i][k])</pre>
                                                    dp[i] |= dp[k];
}
```

2.5 Euler [4177dc]

```
/// 1. 無向圖是歐拉圖:
// 非零度頂點是連通的
// 頂點的度數都是偶數
// 2. 無向圖是半歐拉圖(有路沒有環):
// 非零度頂點是連通的
// 恰有 2 個奇度頂點
| // 3. 有向圖是歐拉圖:
| // 非零度頂點是強連通的
| // 每個頂點的入度和出度相等
// 4. 有向圖是半歐拉圖(有路沒有環):
| // 非零度頂點是弱連通的
// 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
 // 其他頂點的入度和出度相等
 vector<int> ans;
 auto dfs = [&](auto &&self, int u) -> void {
    while (g[u].size()) {
   int v = *g[u].begin();
       g[u].erase(v);
        self(self, v);
    ans.push_back(u);
dfs(dfs, 0);
reverse(ans.begin(), ans.end());
```

2.6 DSU [749620]

```
struct DSU {
      int n;
      vector<int> boss, siz;
      DSU() {}
      DSU(int n_) { init(n_); }
      void init(int n_) {
    n = n_; boss.resize(n);
             iota(boss.begin(), boss.end(), 0);
            siz.assign(n, 1);
      int find(int x) {
   if (boss[x] == x) return x;
   return boss[x] = find(boss[x]);
      bool same(int x, int y) {
    return find(x) == find(y);
      bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);</pre>
            siz[x] += siz[y];
boss[y] = x;
             return true;
      int size(int x) {
   return siz[find(x)];
};
struct DSU {
      int n;
       vector<int> boss, siz, stk;
      DSU() {}
      DSU(int n_) { init(n_); }
       void init(int n_) {
            n = n_;
             boss.resize(n);
             iota(boss.begin(), boss.end(), 0);
             siz.assign(n, 1);
            stk.clear();
      int find(int x) {
   return x == boss[x] ? x : find(boss[x]);
      bool same(int x, int y) {
   return find(x) == find(y);
       bool merge(int x, int y)
            t merge(tnt x, tnt y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);
    siz[x] += siz[y];</pre>
             boss[y] = x;
             stk.push_back(y);
             return true;
```

```
void undo(int x) {
             while (stk.size() > x) {
   int y = stk.back();
   stk.pop_back();
                   siz[boss[y]] -= siz[y];
boss[y] = y;
      int size(int x) {
   return siz[find(x)];
};
2.7 SCC [5d3e16]
struct SCC {
   int n, cur, cnt;
      vector < int >> adj;
      vector <int> stk, dfn, low, bel;
SCC(int n_ = 0) { init(n_); }
void init(int n_) {
            n = n_;
adj.assign(n, {});
             dfn.assign(n, -1);
             low.resize(n);
             bel.assign(n, -1);
             stk.clear();
             cur = cnt = 0;
      void addEdge(int u, int v) {
   adj[u].push_back(v);
      void dfs(int x) {
    dfn[x] = low[x] = cur++;
             stk.push_back(x);
             for (auto y : adj[x]) {
    if (dfn[y] == -1) {
                         dfs(y);
                   low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
                   }
             if (dfn[x] == low[x]) {
                   int y;
do {
                         y = stk.back();
                         bel[y] = cnt;
                   stk.pop_back();
} while (y != x);
            }
      vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
             return bel;
       struct Graph {
             int n;
             vector<pair<int, int>> edges;
             vector<int> siz;
             vector<int> cnte;
      };
Graph compress() {
            Graph g;
g.n = cnt;
             g.siz.resize(cnt);
             g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;
}</pre>
                   for (auto j : adj[i]) {
    if (bel[i] != bel[j]) {
                         g.edges.emplace_back(bel[i], bel[j]);
} else {
                               g.cnte[bel[i]]++;
                         }
                   }
             return g;
     }
};
2.8 VBCC [170604]
struct VBCC {
      int n. cur:
       vector<vector<int>> adj;
      vector <int> dfn, low, parent;
vector <bool>
vector <bool>
is_cut;
VBCC(int n_ = 0) { init(n_); }
void init(int n_) {
            n = n_;
adj.assign(n, {});
```

cur = 0;

if (dfn[x] == low[x]) { int y; do { v = stk.back(): bel[y] = cnt; stk.pop_back(); } while (y != x); cnt++; } return bel; struct Graph { int n: Graph compress() { dfn.assign(n, -1); low.resize(n); Graph g; g.n = cnt; g.siz.resize(cnt); parent.assign(n. -1): is_cut.assign(n, false); g.cnte.resize(cnt);

```
void addEdge(int u, int v) {
                  adj[u].push_back(v);
adj[v].push_back(u);
         for int x) {
    int children = 0;
    dfn[x] = low[x] = cur++;
    for (int v : adj[x]) {
        if (dfn[v] == -1) {
            children++;
        }
}
                                   children++;
                                   parent[v] = x;
                                   dfs(v);
low[x] = min(low[x], low[v]);
                                   if (parent[x] != -1 && low[v] >= dfn[x]) {
    is_cut[x] = true;
}
                          } else if (v != parent[x]) {
   low[x] = min(low[x], dfn[v]);
                          }
                  if (parent[x] == -1 && children > 1) {
    is_cut[x] = true;
         }
void work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i);
        }
}</pre>
                  }
        }
}:
2.9 EBCC [59d8ca]
struct EBCC { // CF/contest/1986/pF
   int n, cur, cnt;
         vector<vector<int>> adj;
         vector<vector<tht>> adj;
vector<int> stk, dfn, low, bel;
vector<pair<int, int>> bridges; // 關鍵邊
EBCC(int n_ = 0) { init(n_); }
void init(int n_) {
                 n = n_;
adj.assign(n, {});
dfn.assign(n, -1);
                  low.resize(n);
                  bel.assign(n, -1);
stk.clear();
                  bridges.clear();
                  cur = cnt = 0;
          void addEdge(int u, int v) {
                  adj[u].push_back(v);
adj[v].push_back(u);
         void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
    stk.push_back(x);
                  stk.push_back(x);
for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
        dfs(y, x);
        low[x] = min(low[x], low[y]);
        if (low[y] > dfn[x]) {
            bridges.emplace_back(x, y);
    }
}
                          } else if (bel[y] == -1) {
    low[x] = min(low[x], dfn[y]);
         fvector<int> work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
        }
}</pre>
                  vector<pair<int, int>> edges;
vector<int> siz; // BCC 內節點數
                  vector<int> cnte; // BCC 內邊數
```

for (int i = 0; i < n; i++) {

```
g.siz[bel[i]]++;
    for (auto j : adj[i]) {
        if (bel[i] < bel[j]) {
            g.edges.emplace_back(bel[i], bel[j]);
        } else if (i < j) {
            g.cnte[bel[i]]++;
        }
    }
    return g;
}</pre>
```

2.10 2-SAT [eeddc1]

```
/ CSES Giant Pizza
struct TwoSat {
       int n; vector<vector<int>> e;
vector<bool> ans;
       vector volus airs,
TwoSat(int n): n(n), e(2 * n), ans(n) {}
void addClause(int u, bool f, int v, bool g) {
    e[2 * u + !f].push_back(2 * v + g);
    e[2 * v + !g].push_back(2 * u + f);
       bool satisfiable() {
              vector<int
                     > id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
              vector<int> stk;
              int now = 0, cnt = 0;
function<void(int)> tarjan = [&](int u) {
                    stk.push_back(u);

dfn[u] = low[u] = now++;

for (auto v : e[u]) {

    if (dfn[v] == -1) {
                                   tarjan(v);
                            low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in stk
low[u] = min(low[u], dfn[v]);
                     if (dfn[u] == low[u]) {
                            int v;
                            do {
                                   v = stk.back();
                                  stk.pop_back();
id[v] = cnt;
                           } while (v != u);
                            ++cnt:
                    }
              for (int i
              return true:
       vector < bool > answer() { return ans; }
fint main() {
   int m, n; cin >> m >> n;
   TwoSat ts(n);
   for (int i = 0; i < m; ++i) {
      int u, v; char x, y;
      cin >> x >> u >> y >> v;
      ts.addClause(u - 1, x == '+', v - 1, y == '+');
}
       if (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";</pre>
       else cout << "IMPOSSIBLE\n";</pre>
```

2.11 Funtional Graph [85c464]

```
| constexpr int N = 2e5 + 5;
| int cht[N][31]; // 倍增表, 放外面不然 TLE
| struct FuntionalGraph {
| int n, cnt;
| vector < int > g, bel, id, len, in, top;
| FuntionalGraph() : n(0) {}
| FuntionalGraph(vector < int > g_) { | init(g_); }
| void init(vector < int > g_) { | n = g_. size(); cnt = 0; | g = g_; bel.assign(n, -1); | id.resize(n); | len.clear(); | in.assign(n, 0); top.assign(n, -1); | build(); | }
| void build() { | for (int i = 0; i < n; i++) { | cht[i][0] = g[i]; | in[g[i]]++; | } | for (int i = 1; i <= 30; i++) | for (int u = 0; u < n; u++) | cht[u][i] = cht[cht[u][i - 1]][i - 1]; | for (int i = 0; i < n; i++) | if (in[i] == 0) | label(i); | | |
```

3 Data Structure

3.1 BIT [d41d8c]

```
template < typename T>
struct Fenwick { // 全部以 0 based 使用
  int n; vector<T> a;
  Fenwick(int n_ = 0) { init(n_); }
       void init(int n_) {
             a.assign(n, T{});
       void add(int x, const T &v) {
             for (int i = x + 1; i <= n; i += i & -i) {
   a[i - 1] = a[i - 1] + v;</pre>
       }
       T sum(int x) { // 左閉右開查詢
             T ans{};
for (int i = x; i > 0; i -= i & -i) {
    ans = ans + a[i - 1];
             return ans:
       TrangeSum(int l, int r) { // 左閉右開查詢return sum(r) - sum(l);
      int select(const T &k, int start = 0) {
    // 找到最小的 x, 使得 sum(x + 1) - sum(start) > k
    int x = 0; T cur = -sum(start);
    for (int i = 1 << __lg(n); i; i /= 2) {
        if (x + i <= n && cur + a[x + i - 1] <= k) {
                           x += i:
                           cur = cur + a[x - 1];
             }
             return x;
     }
template < class T>
struct TwoDFenwick { // 全部以 0 based 使用
      int nx, ny; // row, col 個數
vector<vector<T>> a;
      TwoDFenwick(int nx_ = 0, int ny_ = 0) {
  init(nx_, ny_);
      void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    a.assign(nx, vector<T>(ny, T{}));
      for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        a[i - 1][j - 1] = a[i - 1][j - 1] + v;
    }
}</pre>
            }
      T sum(int x, int y) { // 左閉右開查詢
    T ans{};
    for (int i = x; i > 0; i -= i & -i) {
                    for (int j = y; j > 0; j -= j & -j) {
    ans = ans + a[i - 1][j - 1];
             return ans;
              (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                     (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
```

3.2 RangeBit [d41d8c]

```
template < class T>
struct rangeFenwick { // 全部以 0 based 使用
            int n;
            vector <T> d, di;
rangeFenwick(int n_ = 0) { init(n_); }
             void init(int n_) {
                       n = n_;
d.assign(n, T{});
                        di.assign(n, T{});
            Joid add(int x, const T &v) {
   T vi = v * (x + 1);
   for (int i = x + 1; i <= n; i += i & -i) {
        d[i - 1] = d[i - 1] + v;
        di[i - 1] = di[i - 1] + v;
}</pre>
                        }
             void rangeAdd(int l, int r, const T &v) {
                        add(l, v); add(r, -v);
           T sum(int x) { // 左閉右開查詢 T ans{};
                        for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
                         return ans;
           TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
             int select(const T &k, int start = 0) {
                        T val = T(
    x + i + 1) * d[x + i - 1] - di[x + i - 1];
if (cur + val <= k) {
    x += i;
}</pre>
                                                             cur = cur + val;
                                                }
                                    }
                         return x;
           }
template < class T>
struct rangeTwoDFenwick { // 全部以 0 based 使用
            int nx, ny; // row, col 個數
vector <vector <T>> d, di, dj, dij;
rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
                        init(nx_, ny_);
            void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
                        di.assign(nx, vector<T>(ny, T{}));
dj.assign(nx, vector<T>(ny, T{}));
                         dij.assign(nx, vector<T>(ny, T{}));

}
void add(int x, int y, const T &v) {
    T vi = v * (x + 1);
    T vj = v * (y + 1);
    T vij = v * (y + 1);
    T vij = v * (x + 1) * (y + 1);
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            d[i - 1][j - 1] = d[i - 1][j - 1] + v;
            di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
            dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
            dii[i - 1][i - 1] = diif[i - 1][i - 1] + vy;
            diif[i - 1][i - 1] = diif[i - 1][i - 1] + vy;
            diif[i - 1][i - 1] = diif[i - 1][i - 1] + vy;
            diif[i - 1][i - 1] = diif[i - 1][i - 1] + vy;
            diif[i - 1][i - 1] = diif[i - 1][i - 1] + vy;
            diif[i - 1][i - 1][i - 1][i - 1][i - 1][i - 1][i - 1]
            diif[i - 1][i 
                                                 dij[i - 1][j - 1] = dij[i -
                                                                                                                                       1][j -
                                                                                                                                                             1] + vij;
                                    }
                       }
             void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
                        add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
            T sum(int x, int y) { // 左閉右開查詢
                        for (int j = y; j > 0; j -= j & -j) {
    ans = ans
                                                  + T(x * y + x + y + 1) * d[i - 1][j - 1]; \\ ans = ans - T(y + 1) * di[i - 1][j - 1]; \\ ans = ans - T(x + 1) * dj[i - 1][j - 1]; \\
                                                 ans = ans + dij[i - 1][j - 1];
                                    }
                        return ans;
            T rangeSum
                          (int lx, int ly, int rx, int ry) { // 左閉右開查詢
```

```
return sum(
             rx, ry) - sum(lx, ry) - sum(rx, ly) + sum(lx, ly);
    }
};
```

3.3 Segment [d41d8c]

```
template < class Info>
 struct Seg { // 左閉右開寫法
int n; vector<Info> info;
       Seg() : n(0) {}
Seg(int n_, Info v_ = Info()) { init(n_, v_); }
template < class T >
       Seg(vector<T> init_) { init(init_); }
void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
       template < class T>
       void init(vector<T> init_) {
             n = init_.size();
             info.assign(4 << __lg(n), Info());
function <void(
    int, int, int)> build = [&](int p, int l, int r) {
    if (r - l == 1) {
        info.all = int []].
                          info[p] = init_[l];
                          return:
                   int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                   pull(p);
             build(1, 0, n);
       void pull(int p) {
    info[p] = info[p * 2] + info[p * 2 + 1];
       void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
      info[p] = v; return;
}
              int m = (l + r) /
             int m = (l + r) / 2;
if (x < m) modify(2 * p, l, m, x, v);
else modify(2 * p + 1, m, r, x, v);</pre>
             pull(p);
        void modify(int p, const Info &i) {
             modify(1, 0, n, p, i);
       Info query(int p, int l, int r, int ql, int qr) {
             if (qr <= l || ql >= r) return Info();
if (ql <= l && r <= qr) return info[p];</pre>
             return query(p *
    2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
       Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
       template < class F> // 尋找區間內,第一個符合條件的
        int findFirst
             (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)</pre>
                    return
             if (l >= x && r <= y && !pred(info[p]))</pre>
             return -1;
if (r - l == 1)
             return l;
int m = (l + r) / 2;
int res = findFirst(2 * p, l, m, x, y, pred);
             if (res == -1)

res = findFirst(2 * p + 1, m, r, x, y, pred);
             return res;
       template < class F> // 若要找 last,先右子樹遞迴即可
int findFirst(int l, int r, F & pred) {
    return findFirst(1, 0, n, l, r, pred);
 };
// ---define structure and info plus---
 struct Info {
   int n = 0;
       int sum = 0;
 };
Info operator+(const Info &a, const Info &b) {
       return { a.n + b.n, a.sum + b.sum };
```

3.4 Lazy Segment [d41d8c]

```
template < class Info, class Tag>
 struct LazySeg { // 左閉右開寫法
      int n:
      vector<Info> info;
      vector <Tag> tag;
LazySeg() : n(0) {}
LazySeg(int n_, Info v_ = Info()) {
          init(n_, v_);
      LazySeg(vector<T> init_) {
```

```
int findFirst(int l, int r, F &&pred) {
    return findFirst(1, 0, n, l, r, pred);
      init(init):
void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
                                                                                              };
// ---define structure and info plus---
                                                                                              struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add; void apply(const Tag& v) { if (v.set_val) { set_val = v.set_val; add = v.set_val; add = v.set_val;
void init (vector<T> init_) {
    n = init_.size();
    info.assign(4 << __lg(n), Info());
    tag.assign(4 << __lg(n), Tag());
    function valid(</pre>
      function <void(
   int, int, int)> build = [&](int p, int l, int r) {
   if (r - l == 1) {
      info[p] = init_[l];
}
                                                                                                                add = v.add;
                                                                                                          }
else {
                                                                                                                add += v.add;
                 return;
                                                                                                   }
            int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                                                                                              };
                                                                                              struct Info {
                                                                                                    int sum;
            pull(p);
                                                                                                    void apply(int l, int r, const Tag &v) {
                                                                                                          if (v.set_val) {
    sum = (r - l) * v.set_val;
      build(1, 0, n);
void pull
                                                                                                          sum += (r - l) * v.add;
(int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
   info[p].apply(l, r, v);
   to[r].apply(l, r, v);
                                                                                                    // Info& operator=(const Info &rhs) {
                                                                                                             // 部分 assignment 使用 return *this;
                                                                                                   //
//
// }
      tag[p].apply(v);
void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
                                                                                              Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
                                                                                              }
                                                                                              3.5 Treap [d41d8c]
      tag[p] = Tag();
void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
}
                                                                                              struct Treap {
                                                                                                    Treap *lc, *rc;
int pri, siz; bool rev_valid;
int val; int min;
           return:
                                                                                                    Treap(int val_) {
    min = val = val_;
      int m = (l + r) / 2;
push(p, l, r);
if (x < m) {</pre>
                                                                                                          pri = rand();
lc = rc = nullptr;
siz = 1; rev_valid = 0;
            modify(2 * p, l, m, x, v);
           modify(2 * p + 1, m, r, x, v);
                                                                                                     void pull() { // update siz or other information
                                                                                                          siz = 1;
min = val;
      pull(p);
                                                                                                          for (auto c : {lc, rc}) {
void modify(int p, const Info &i) {
                                                                                                                if (!c) continue;
                                                                                                                siz += c->siz:
      modify(1, 0, n, p, i);
                                                                                                                min = std::min(min, c->min);
                                                                                                          }
Info query(int p, int l, int r, int ql, int qr) {
      if (qr <= l || ql >= r) return Info();
if (ql <= l && r <= qr) return info[p];
int m = (l + r) / 2;</pre>
                                                                                                    void push() {
                                                                                                          if (rev_valid) {
                                                                                                                swap(lc, rc);
if (lc) lc->rev_valid ^= 1;
if (rc) rc->rev_valid ^= 1;
      push(p, l, r);
      return query(p *
2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
                                                                                                          rev_valid = false;
       (int ql, int qr) { return query(1, 0, n, ql, qr); }
int find(int k) { // 找到 min 是 k 的位置 (1-based)
                                                                                                          push();
                                                                                                          int ls = (lc ? lc->siz : 0) + 1;
if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
            apply(p, l, r, v);
           return:
                                                                                                    }
      int m = (l + r) / 2;
      push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
                                                                                              int size(Treap *t) {
    return t ? t->siz : 0;
                                                                                              Treap *merge(Treap *a, Treap *b) {
    if (!a || !b) return a ? a : b;
    a->push(); b->push();
    if (a->pri > b->pri) {
        a ->rc = merge(a->rc, b);
    }
}
void range_apply(int l, int r, const Tag &v) {
      range_apply(1, 0, n, l, r, v);
                                                                                                          a->pull();
template < class F> // 尋找區間內,第一個符合條件的
int findFirst
                                                                                                          return a;
      (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {
    return -1;</pre>
                                                                                                    else {
   b->lc = merge(a, b->lc);
                                                                                                          b->pull();
      if (l >= x && r <= y && !pred(info[p])) {</pre>
                                                                                                    }
            return -1;
      if (r - l == 1) {
                                                                                              pair<Treap*, Treap*> split(Treap *t, int k) {
                                                                                                    // 分割前 k 個在 first, 剩下的在 second if (t == nullptr) return {nullptr, nullptr};
            return l;
      int m = (l + r) / 2;
                                                                                                    t->push();
      push(p);
                                                                                                    if (size(t->lc) < k) {
      int res = findFirst(2 * p, l, m, x, y, pred);
if (res == -1) {
                                                                                                          auto [a, b] = split(t->rc, k - size(t->lc) - 1);
                                                                                                          t - > rc = a;
            res = findFirst(2 * p + 1, m, r, x, y, pred);
                                                                                                          t->pull();
                                                                                                          return {t, b};
      return res;
                                                                                                    else {
template < class F> // 若要找 last, 先右子樹遞迴即可
                                                                                                          auto [a, b] = split(t->lc, k);
```

t->lc = b;

```
t->pull();
    return {a, t};
}

void Print(Treap *t) {
    if (!t) return;
    t->push();
    Print(t->lc);
    cout << t->val;
    Print(t->rc);
}

3.6 RMQ [d41d8c]

template < class T, class
struct RMQ {
    const Cmp cmp = Cm;
    static constexpr u
    using u64 = unsignuint n;</pre>
```

```
template < class T, class Cmp = greater < T >>
struct RMQ {
     const Cmp cmp = Cmp();
     static constexpr unsigned B = 64;
using u64 = unsigned long long;
     vector<vector<T>> a;
vector<T> pre, suf, ini;
vector<u64> stk;
     RMQ() {}
     RMQ(const vector<T> &v) { init(v); }
void init(const vector<T> &v) {
          n = v.size();
pre = suf = ini = v;
           stk.resize(n);
           if (!n) {
                return;
          for (int j = 1; j < B && i * B + j < n; j++) {
    a[0][i] = min(a[0][i], v[i * B + j], cmp);</pre>
           for (int i = 1; i < n; i++) {
   if (i % B) {
      pre[i] = min(pre[i], pre[i - 1], cmp);
}</pre>
                }
           for (int i = n - 2; i >= 0; i--) {
   if (i % B != B - 1) {
                      suf[i] = min(suf[i], suf[i + 1], cmp);
                }
           for (int j = 0; j < lg; j++) {
    for (int i = 0; i + (2 << j) <= M; i++) {
        a[j + 1][i
        ] = min(a[j][i], a[j][i + (1 << j)], cmp);
        .</pre>
                }
           for (int i = 0; i < M; i++) {
   const int l = i * B;
   const int r = min(1U * n, l + B);</pre>
                s |= 1ULL << (j - l);
                      stk[j] = s;
                }
          }
    ({ans, a[k][l], a[k][r - (1 << k)]}, cmp);
                return ans;
          } else {
   int x = B * (l / B);
                return ini
                      [__builtin_ctzll(stk[r - 1] >> (l - x)) + l];
           }
```

3.7 Mo [d41d8c]

```
struct query {
   int l, r, id;
} typedef query;
void MO(int n, vector<query> &queries) {
   int block = sqrt(n);
   function <bool(query, query)> cmp = [&](query a, query b) {
     int block_a = a.l / block;
     int block_b = b.l / block;
     if (block_a != block_b) return block_a < block_b;
     return a.r < b.r;
};</pre>
```

4 Flow

4.1 Dinic [aa12d4]

```
template < class T >
struct Dinic {
      struct Edge {
   int to;
            T flow, cap; // 流量跟容量
      int n, m, s, t;
const T INF_FlOW = 1 << 30;
      vector<vector<int>> adj; // 此點對應的 edges 編號
       vector<Edge> edges; // 幫每個 edge 編號
      vector < Ldge > edges; // 常時間 edg
vector < int > dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_; m = 0;
    dis.resize(n); ptr.resize(n);
    adj.assign(n, vector < int > { } });
    edges.clear();
      void add_edge(int u, int v, T cap) {
            // 偶數 id 是正向邊
edges.push_back({ v, 0, cap });
edges.push_back({ u, 0, 0 });
            adj[u].push_back(m++);
            adj[v].push_back(m++);
      bool bfs() {
    fill(dis.begin(), dis.end(), -1);
    dis[s] = 0; queue<int> q;
            q.push(s);
            while (!q.empty() && dis[t] == -1) {
   int u = q.front(); q.pop();
   for (int id : adj[u]) {
      Edge &e = edges[id];
      if (6]
                         if (e.flow == e.cap) continue;
if (dis[e.to] == -1) {
    dis[e.to] = dis[u] + 1;
                               q.push(e.to);
                         }
                  }
            return dis[t] != -1;
      T dfs(int u, T flow) {
   if (flow == 0) return 0;
            if (u == t) return flow;
            for (int
                  edges[adj[u][cur] ^ 1].flow -= mn;
                         return mn;
                  }
            }
             return 0; // 到不了終點就會 return 0
       T work(int s_, int t_) {
            s = s_; t = t_; T flow = 0;
while (bfs()) {
                   fill(ptr.begin(), ptr.end(), 0);
                   while (true) {
   T res = dfs(s, INF_Flow);
   if (res == 0) break;
                         flow += res;
                  }
            return flow;
      void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
};
```

4.2 Min Cut [44ae6c]

```
// CSES Police Chase
int main(){
   int n, m; cin >> n >> m;
   Dinic <int >> g(n);
   for (int i = 0; i < m; i++) {
     int u, v, cap = 1;</pre>
```

```
cin >> u >> v:
                 g.add_edge(u, v, cap);
                 g.add_edge(v, u, cap);
         int res = g.work(0, n - 1);
cout << res << "\n";
        cout << res << "\n";
if (res == 0) return;</pre>
        vector <int> vis(n);
auto find = [&](auto self, int u) -> void {
   if (!vis[u]) {
                         vis[u] = 1;
                         for (int id : g.adj[u]) {
                                 auto e = g.edges[id];
if (e.cap - e.flow > 0) {
                                          self(self, e.to);
                        }
                }

};
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
        auto e = g.edges[id];
        if (!vis[e.to]) {
            cout << i + 1 << " " << e.to + 1 << " \n";
    }
}
</pre>
        }
}
```

4.3 MCMF [77fc99]

```
template < class Tf, class Tc>
struct MCMF {
     struct Edge {
           int to;
           Tf flow, cap; // 流量跟容量
     // 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就好
int n, m, s, t;
const Tf INF_FLOW = 1 << 30;
const Tc INF_COST = 1 << 30;
     vector < vector < int >> adj;
     vector<Edge> edges; // 幫每個 edge 編號
vector<Tc> dis, pot; // johnson algorithm, using spfa
vector<int> rt; // 路徑恢復, 對應 id
     vector < bool > inq;
MCMF(int n = 0) { init(n); }
     void init(int n_) {
          n = n_; m = 0;
edges.clear();
           adj.assign(n, vector<int>{});
     void add_edge(int u, int v, Tf cap, Tc cost){
  edges.push_back({v, 0, cap, cost});
  edges.push_back({u, 0, 0, -cost});
  adj[u].push_back(m++);
  adj[v].push_back(m++);
     }
                }
           return dis[t] != INF_COST;
     bool dijkstra() {
          dis.assign(n, INF_COST); rt.assign(n, -1);
priority_queue<pair<Tc, int>,
    vector<pair<Tc, int>>, greater<pair<Tc, int>>> pq;
dis[s] = 0; pq.emplace(dis[s], s);
          pq.emplace(ndis, v);
```

```
}
                 return dis[t] != INF_COST;
        }
        }
// 限定 flow, 最小化 cost
pair<Tf, Tc> work_flow(int s_, int t_, Tf need) {
    s = s_, t = t_; pot.assign(n, 0);
    Tf flow{}; Tc cost{}; bool fr = true;
    while ((fr ? spfa() : dijkstra())) {
        for (int i = 0; i < n; i++) {
            dis[i] += pot[i] - pot[s];
        }
                        ff = INF_FLOW;
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
                                         (f, edges[rt[i]].cap - edges[rt[i]].flow);
                        f = min<Tf>(f, need);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
}
                        flow += f; need -= f;
cost += f * dis[t]; fr = false;
                        swap(dis, pot);
if (need == 0) break;
                return make_pair(flow, cost);
        }
        // 限定 cost, 最大化 flow
pair
pair
// 限定 cost, 最大化 flow
pair
s = s_, t = t_; pot.assign(n, 0);
If flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] += pot[i] - pot[s];
}
</pre>
                        If f = INF_FLOW;
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
                                f = min
                                         (f, edges[rt[i]].cap - edges[rt[i]].flow);
                        f = min<Tf>(f, budget / dis[t]);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
                                edges[rt[i] ^ 1].flow
                        flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
                        swap(dis, pot);
if (budget == 0 || f == 0) break;
                return make_pair(flow, cost);
                for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
        }
};
 4.4 Hangarian [dfa1c4]
```

```
struct Hangarian { // 0-based
        int n, m;
vector<vector<int>> adj;
       vector <int> used, vis;
vector <pair <int, int>> match;
Hangarian(int n = 0, int m = 0) {
                init(n_, m_);
       void init(int n_, int m_) {
    n = n_; m = m_;
    adj.assign(n + m, vector < int > ());
    used.assign(n + m, -1);
}
               vis.assign(n + m, 0);
       void addEdge(int u, int v) {
   adj[u].push_back(n + v);
   adj[n + v].push_back(u);
        bool dfs(int u) {
               int sz = adj[u].size();
for (int i = 0; i < sz; i++) {
   int v = adj[u][i];
   if (vis[v] == 0) {</pre>
                               vis[v] = 1;
                               if (used[v] == -1 || dfs(used[v])) {
    used[v] = u;
                               }
                       }
                return false;
        vector<pair<<mark>int, int</mark>>> work() {
               match.clear(); used.assign(n + m, -1);
vis.assign(n + m, 0);
for (int i = 0; i < n; i++) {
    fill(vis.begin(), vis.end(), 0); dfs(i);</pre>
                for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
                               match.push_back(make_pair(used[i], i - n));
```

vector $\langle int \rangle$ z(n); z[0] = n;

```
for (int i = 1, j = 1; i < n; i++) {
   z[i] = max(0, min(j + z[j] - i, z[i - j]));
   while (i + z[i] < n && s[z[i]] == s[i + z[i]])</pre>
           return match;
     }
                                                                                                  z[i]++:
                                                                                              if (i + z[i] > j + z[j]) j = i;
 4.5 Theorem [d41d8c]
                                                                                         return z; // 最後一格不算
                                                                                   }
| // 有向無環圖:
                                                                                    5.4 SA [d40e3e]
 // 最小不相交路徑覆蓋:
 // 最小路徑數 = 頂點數 - 最大匹配數
                                                                                   struct SuffixArray {
                                                                                         int n; string s;
 // 最小相交路徑覆蓋:
                                                                                         vector<int> sa, rk, lc;
// 先用
                                                                                         // n: 字串長度
       Floyd 求傳遞封包,有連邊就建邊,然後再套最小不相交路徑覆蓋
                                                                                         // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
                                                                                         // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名 // lc: LCP
 // 二分圖:
                                                                                              數組,lc[i] 表示 sa[i] 和 sa[i+1] 的最長公共前綴長度
 // 最小點覆蓋 = 最大匹配數
                                                                                         SuffixArray(const string &s_) {
    s = s_; n = s.length();
 // 選出一些點,讓所有邊至少有一個端點在點集中的最少數量
                                                                                              sa.resize(n);
 // 最少邊覆蓋: 選出一些邊,讓所有點都覆蓋到的最少數量
                                                                                              lc.resize(n - 1);
                                                                                              rk.resize(n);
// 最少邊覆蓋 = 點數 - 最大匹配數
                                                                                              iota(sa.begin(), sa.end(), 0);
                                                                                              sort(sa.begin(), sa.enu(), 0);
sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });
rk[sa[0]] = 0;
for (int i = 1; i < n; ++i)</pre>
 // 最大獨立集: 選出一些點, 使這些點兩兩沒有邊連接的最大數量
// 最大獨立集 = 點數 - 最大匹配數
       String
                                                                                                  rk[sa[i]]
                                                                                                          = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
 5.1 Hash [852711]
                                                                                              vector < int > tmp, cnt(n);
                                                                                              tmp.reserve(n);
 constexpr int B = 59;
vector<Z> Hash(string &s) {
                                                                                              while (rk[sa[n - 1]] < n - 1) {
                                                                                                  tmp.clear();
for (int i = 0; i < k; ++i)</pre>
      vector<Z> ans {0};
      for (auto c : s)
                                                                                                        tmp.push_back(n - k + i);
           ans.push_back(ans.back() * B + (c - 'a' + 1));
                                                                                                   for (auto i : sa)
   if (i >= k)
        tmp.push_back(i - k);
      return ans;
                                                                                                   void solve() {
     string s, sub;
cin >> s >> sub;
auto a = Hash(s);
                                                                                                   for (int i = 1; i < n; ++i)</pre>
                                                                                                   cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; --i)
      auto q = Hash(sub);
      auto find = q.back();
int ans = θ;
int l = 1, r = sub.size(), len = sub.size();
                                                                                                        sa[--cnt[rk[tmp[i]]]] = tmp[i];
                                                                                                  while (r <= s.size()) {
   if (a[r] - a[l - 1] * power(Z(B), len) == find) {</pre>
               ans++;
           l++, r++;
      cout << ans << "\n";
                                                                                              for (int i = 0, j = 0; i < n; ++i) {
   if (rk[i] == 0) {</pre>
                                                                                                       j = 0;
 5.2 KMP [cddfd9]
                                                                                                   } else {
                                                                                                        for (j
 struct KMP {
                                                                                                              `-= j > 0; i + j < n && sa[rk[i] - 1] + j
< n && s[i + j] == s[sa[rk[i] - 1] + j]; )
      string sub;
      vector < int > failure;
KMP(string sub_) {
                                                                                                             ++j;
                                                                                                        lc[rk[i] - 1] = j;
           sub = sub_;
                                                                                                  }
           failure.resize(sub.size(), -1);
buildFailFunction();
                                                                                             }
                                                                                         string getLCP() {
      void buildFailFunction() {
    for (int i = 1; i < (int)sub.size(); i++) {
        int_now = failure[i - 1];
}</pre>
                                                                                             ing getLCP() {
  int cp = 0, k, lcp = 0, p;
  for (int i = 0; i < n; i++) {
    if (!rk[i]) continue;
    k = sa[rk[i] - 1];
</pre>
                while (now != -1
    && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
                                                                                                   if (cp) cp--;
                                                                                                   while (s[i + cp] == s[k + cp]) cp++;
           }
                                                                                                   if (cp > lcp){
                                                                                                        lcp = cp;
      vector<int> match(string &s) {
                                                                                                        p = i;
           vector<int> match;
for (int i = 0, now = -1; i < (int)s.size(); i++) {
    // now is the compare sucessed length -1</pre>
                                                                                                  }
                                                                                              if (lcp) {
                while (s[i] !=
                                                                                                   return s.substr(p, lcp);
                sub[now + 1] && now != -1) now = failure[now];
// failure stores if comparison fail, move to where
if (s[i] == sub[now + 1]) now++;
                                                                                              } else {
                                                                                                  return "-1";
                if (now + 1 == (int)sub.size()) {
                                                                                       }
                     match.push_back(i - now);
now = failure[now];
                }
                                                                                    5.5 Manacher [9c9ca6]
           return match:
                                                                                       找到對於每個位置的迴文半徑
                                                                                   vector < int > manacher(string s) {
    string t = "#";
};
                                                                                         for (auto c : s) {
 5.3 Z Function [764b31]
                                                                                             t += c;
t += '#';
 // z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
 // 的最長公共前綴 (LCP) 的長度
vector<int> Z(string s) {
  int n = s.size();
                                                                                         int n = t.size();
                                                                                         vector<int> r(n);
                                                                                         for (int i = 0, j =
```

0; i < n; i++) {

// i 是中心, j 是最長回文字串中心

```
if (2 * j - i >= 0 && j + r[j] > i) {
    r[i] = min(r[2 * j - i], j + r[j] - i);
    r[i] += 1;
    if (i + r[i] > j + r[j]) {
    }
return r;
// # a # b # a #
// 1 2 1 4 1 2 1
// # a # b # b # a #
// 1 2 1 2 5 2 1 2 1
// 值 -1 代表原回文字串長度
// (id - val + 1) / 2 可得原字串回文開頭
```

5.6 SAM [d15619]

```
struct SAM {
      static constexpr int ALPHABET_SIZE = 26;
struct Node {
            int len;
int link;
            array<int, ALPHABET_SIZE> next;
            Node() : len{}, link{}, next{} {}
      vector < Node > t;
      SAM() { init(); }
void init() {
            t.assign(2, Node());
t[0].next.fill(1);
            t[0].len = -1;
      int newNode() {
            t.emplace_back();
return t.size() - 1;
      int extend(int p, int c) {
   if (t[p].next[c]) {
                  int q = t[p].next[c];
if (t[q].len == t[p].len + 1) {
                        return q;
                   int r = newNode();
                  thr = hewhold(),

t[r].len = t[p].len + 1;

t[r].link = t[q].link;

t[r].next = t[q].next;

t[q].link = r;
                  while (t[p].next[c] == q) {
                       t[p].next[c] = r;
p = t[p].link;
                  return r:
            int cur = newNode();
            t[cur].len = t[p].len + 1;
while (!t[p].next[c]) {
    t[p].next[c] = cur;
                  p = t[p].link;
            t[cur].link = extend(p, c);
            return cur;
     }
void solve() {
    string s; cin >> s;
    int n = s.length();
      vector < int > pos(n + 1); // s[i - 1] 的後綴終點位置
     pos[0] = 1;
      SAM sam;
     for (int i = θ; i < n; i++) {
    pos[i + 1] = sam.extend(pos[i], s[i] - 'a');</pre>
```

5.7 Trie [3b3aa0]

```
struct Trie {
         struct trie_node {
                 bool is_word;
                 vector<trie_node *> children;
trie_node() {
    is_word = false;
                          children.resize(26, NULL);
                }
        f;
trie_node *root = new trie_node();
void insert(string &s) {
   trie_node *cur = root;
   for (int i = 0; i < s.size(); i++) {
      int idx = s[i] - 'a';
      if (cur->children[idx] == NULL) {
         cur->children[idx] = new trie_node();
}
                          cur = cur->children[idx]:
                  cur->is_word = true;
```

```
bool is_in_trie(string &s) {
                                              trie_node *cur = root;

for (int i = 0; i < s.size(); i++) {

    if (cur->
                                                                    children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
                         int search_i_start(string &s, int i, vector<int> &dp) {
    trie_node *cur = root;
    int sz = s.size(), ans = 0;
    for (int j = i; j < sz; j++) {
        if (sure in the first interest in the first in the first in the first in the first in the
                                                                     if (cur
                                                                   ->children[s[j] - 'a'] == nullptr) return ans;
cur = cur->children[s[j] - 'a'];
if (cur->is_word)
    (ans += dp[j + 1]) %= mod;
                                              return ans:
                      }
    int main() {
                         // 找到 sub 集合裡,可以重複用,組成 s 的組數 Trie trie; string s; cin >> s; int sz = s.size();
                          // dp 代表 i 開頭到最後的配對總數
                           .,
// 找到有結尾為 stop 的 dp[i] += dp[j + 1]
                           int n; cin >> n;
                          vector < int > dp(sz + 1, 0);
for (int i = 0; i < n; i++) {
    string sub; cin >> sub;
                                               trie.insert(sub);
                          dp[sz] = 1;
                          for (int i = sz - 1; i >= 0; i--) {
    dp[i] = trie.search_i_start(s, i, dp);
                          cout << dp[0] << endl;
1 }
```

5.8 Duval [f9dcca]

```
// duval algorithm
    // 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
vector<string> duval(string s) {
                              int i = 0, n = s.size();
vector<string> res;
while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i;
      if section | if (s[k] < s[j]) k = i
                                                                                     else k++;
                                                                                  j++;
                                                           while (i <= k) {
                                                                                     res.push_back(s.substr(i, j - k));
                                                                                    i += i - k:
                                                        }
                                return res:
    }
     // 最小旋轉字串
     string min_round(string s) {
                                int i = 0, n = s.size();
                                int start = i;
while (i < n / 2) {</pre>
                                                        else k++;
                                                         while (i <= k) {
    i += j - k;</pre>
                                return s.substr(start, n / 2);
```

Math 6

6.1 Prime [02092d]

```
vector < int > prime, minp;
void sieve(int n) {
       minp.assign(n + 1, 1); // 1 代表是質數,非 1 不是minp[0] = minp[1] = -1;
int m = int(sqrt(n)) + 1;
       for (int i = 2; i <= m; i++) {
    if (minp[i] == 1) {</pre>
                    prime.push_back(i);
                     for (int j = i + i; j <= n; j += i) {
    minp[j] = i;</pre>
             }
```

ll MInt<0>::Mod = 998244353:

```
constexpr int P = 1e9 + 7;
using Z = MInt<P>;
     }
// a^(m-1) = 1 (mod m)
// a^(m-2) = 1/a (mod m)
// EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)
                                                                                                  6.3 Combination [878efe]
// FacNums = (x+1)(y+1)(z+1)...

// FacSum = (a^0+a^1...+a^x)(b^0+...+b^y)

// FacMul = N(x+1)(y+1)(z+1)/2
                                                                                                 6.2 Modulo [56b9fb]
                                                                                                             if (m <= n) return;
_fac.resize(m + 1);</pre>
template < class T >
constexpr T power(T a, ll b) {
  T res {1};
  for (; b; b /= 2, a *= a)
        if (b % 2) res *= a;
}
                                                                                                              _invfac.resize(m +
                                                                                                              _inv.resize(m + 1);
for (int i = n + 1; i <= m; i++) {
    _fac[i] = _fac[i - 1] * i;
      return res;
Constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
    res %= p;
    if (res < 0) res += p;</pre>
                                                                                                              _invfac[m] = _fac[m].inv();

for (int i = m; i > n; i--) {

   _invfac[i - 1] = _invfac[i] * i;
                                                                                                                    _inv[i] = _invfac[i] * _fac[i - 1];
      return res;
                                                                                                              n = m:
template < ll P >
                                                                                                        Z fac(ll m) {
   if (m > n) init(2 * m);
   return _fac[m];
struct MInt {
    ll x;
      constexpr MInt() : x {0} {}
constexpr MInt(ll x) : x {norm(x % getMod())} {}
static ll Mod;
                                                                                                        Z invfac(ll m) {
   if (m > n) init(2 * m);
   return _invfac[m];
      constexpr static ll getMod() {
   if (P > 0) return P;
   else return Mod;
                                                                                                        Z inv(ll m) {
   if (m > n) init(2 * m);
   return _inv[m];
     constexpr static void setMod(ll Mod_) {
    Mod = Mod_;
                                                                                                        Z binom(ll n, ll m) {
   if (n < m || m < 0) return 0;
   return fac(n) * invfac(m) * invfac(n - m);</pre>
      constexpr ll norm(ll x) const {
           if (x < 0) x += getMod();
if (x >= getMod()) x -= getMod();
                                                                                                        constexpr ll val() const { return x; }
constexpr MInt operator-() const {
            MInt res;
            res.x = norm(getMod() - x);
                                                                                                |} comb; // 注意宣告, 若要換模數需重新宣告
            return res;
                                                                                                  6.4 CRT [d41d8c]
      constexpr MInt inv() const {
   return power(*this, getMod() - 2);
                                                                                                  ll exgcd(ll a, ll b, ll &x, ll &y) {
                                                                                                        if (!b) {
    x = 1, y = 0;
      constexpr MInt &operator*=(MInt rhs) & {
           if (getMod() < (1ULL << 31)) {
    x = x * rhs.x % int(getMod());</pre>
                                                                                                              return a:
                                                                                                        ll g = exgcd(b, a % b, y, x);
                 x = mul(x, rhs.x, getMod());
                                                                                                        return q;
                                                                                                  Il inv(ll x, ll m){
      constexpr MInt &operator+=(MInt rhs) & {
    x = norm(x + rhs.x);
                                                                                                        ll a, b;
                                                                                                        exgcd(x, m, a, b);
            return *this;
                                                                                                        a %= m;
if (a < 0) a += m;
      constexpr MInt &operator -= (MInt rhs) & {
            x = norm(x - rhs.x);
return *this;
                                                                                                  // remain, mod
ll CRT(vector<pair<ll, ll>> &a){
    ll prod = 1;
    for (auto x : a) {
        prod *= x.second;
}
      constexpr MInt &operator/=(MInt rhs) & {
            return *this *= rhs.inv();
      friend constexpr MInt operator*(MInt lhs, MInt rhs) {
            MInt res = lhs; return res *= rhs;
                                                                                                        for (auto x : a) {
   auto t = prod / x.second;
   res += x.first * t % prod * inv(t, x.second) % prod;
   if(res >= prod) res -= prod;
      friend constexpr MInt operator+(MInt lhs, MInt rhs) {
            MInt res = lhs; return res += rhs;
      friend constexpr MInt operator - (MInt lhs, MInt rhs) {
   MInt res = lhs; return res -= rhs;
                                                                                                        return res;
      friend constexpr MInt operator/(MInt lhs, MInt rhs) {
   MInt res = lhs; return res /= rhs;
                                                                                                  6.5 Matrix [08b5fe]
                                                                                                  template < class T>
              constexpr istream &operator>>(istream &is, MInt &a) {
                                                                                                  struct Mat {
            ll v; is >> v; a = MInt(v); return is;
                                                                                                        int m, n;
                                                                                                        constexpr static ll mod = 1e9 + 7;
vector<vector<T>> matrix;
Mat(int n_ = 0) { init(n_, n_); }
Mat(int m_, int n_) { init(m_, n_); }
Mat(vector<vector<T>> matrix_) { init(matrix_); }
      friend constexpr
              ostream & operator << (ostream & os, const MInt &a) {
            return os << a.val();</pre>
      friend constexpr bool operator==(MInt lhs, MInt rhs) {
                                                                                                        void init(int m_, int n_) {
    m = m_; n = n_;
    matrix.assign(m, vector<T>(n));
            return lhs.val() == rhs.val();
      friend constexpr bool operator!=(MInt lhs, MInt rhs) {
           return lhs.val() != rhs.val();
                                                                                                        void init(vector<vector<T>> &matrix_) {
                                                                                                             m = matrix_.size();
n = matrix_[0].size();
      friend constexpr bool operator<(MInt lhs, MInt rhs) {</pre>
           return lhs.val() < rhs.val();</pre>
                                                                                                              matrix = matrix_;
```

vector<vector<T>> unit(int n) {

vector<vector<T>> res(n, vector<T>(n));

```
for (int i = 0; i < n; i++) {
    res[i][i] = 1;</pre>
         return res:
     constexpr Mat &operator*=(const Mat& rhs) & {
         assert(matrix[0].size() == rhs.matrix.size());
int m = matrix.size()
              , k = matrix[0].size(), n = rhs.matrix[0].size();
         l] * rhs.matrix[l][j] % mod)) %= mod;
             }
         matrix = ans.matrix;
return *this;
     constexpr Mat &operator^=(ll p) & {
         assert(m == n); assert(p >= 0);
Mat ans(p-- == 0 ? unit(m) : matrix);
         while (p > 0) {
             if (p & 1) ans *= *this;
*this *= *this;
p >>= 1;
         matrix = ans.matrix;
return *this;
     friend Mat operator*(Mat lhs, const Mat &rhs) {
         lhs *= rhs;
         return lhs;
     friend Mat operator^(Mat lhs, const ll p) {
         lhs ^= p;
return lhs;
};
// fn = fn-3 + fn-2 + fn-1
```

6.6 Integer Partition [595ed2]

6.7 Mobius Theorem

- 數論 分塊 可以 快速 計算 一些 含有 除法 向下 取整的 和 式,就 是 像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理 出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n}\!\!\mu(d)\!=\!\begin{cases} 1 & \text{for } n\!=\!1\\ 0 & \text{for } n\!\neq\!0 \end{cases}$$

2. μ是常數函數1的反元素

 $\Rightarrow \mu * 1 = \epsilon$, $\epsilon(n)$ 只在n = 1時為 1 , 其餘情況皆為 0 。

 $-\phi$ 歐拉函數: x以下與x互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^{i}) \\ &= 1 + p^{0}(p-1) + p^{1}(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^{c} \\ &= id \end{split}$$

• 莫比烏斯反演公式

-
$$f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$$

- $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

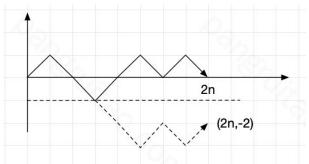
例子

$$\begin{split} &\sum_{i=a}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \sum_{d \mid gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \sum_{j=1}^{y} \sum_{d \mid gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left \lfloor \frac{x}{k} \right \rfloor} \left \lfloor \frac{y}{k} \right \rfloor \\ &= \sum_{d=1}^{min(\left \lfloor \frac{x}{k} \right \rfloor, \left \lfloor \frac{y}{k} \right \rfloor)} \mu(d) \left \lfloor \frac{x}{kd} \right \rfloor \left \lfloor \frac{y}{kd} \right \rfloor \end{split}$$

6.8 Mobius Inverse [d41d8c]

```
const int maxn = 2e5:
ll mobius_pref[maxn];
void init() {
      mobius_pref[1] = 1;
vector<ll> wei
      (maxn); // wei = 0 代表是質數, -1 代表可被平方數整除
for (ll i = 2; i < maxn; i++) {
    if (wei[i] == -1) {
        mobius_pref[i] = mobius_pref[i - 1];
    }
                   continue; // 包含平方
            wei[i] == 0/;
wei[i] = 1;
for (ll j = 2; i * j < maxn; j++) {
    if (j % i == 0) wei[i * j] = -1;
    else if (wei[i * j] != -1) wei[i * j]++;</pre>
                  }
            mobius_pref[i]
                    = mobius_pref[i - 1] + (wei[i] % 2 == 0 ? 1 : -1);
     }
void solve() {
      auto cal = [&](ll x, ll y) -> int {
            int res = 0;
            for (int l = 1, r; l <= min(x, y); l = r + 1) {
    r = min(x / (x / l), y / (y / l));
    res += (mobius_pref[r] - mobius_pref[l])</pre>
                            - 1]) * (x / l) * (y / l); // 代推出來的式子
            return res;
      };
      cout << cal
             (b / k, d / k) - cal((a - 1) / k, d / k) - cal(b / k, (c - 1) / k) + cal((a - 1) / k, (c - 1) / k) << "\n";
```

6.9 Catalan Theorem



1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$ 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有x 個,往下有y 個,會有:

$$\begin{cases} x + y = 2n \\ y - x = 2 \end{cases} \Rightarrow \begin{cases} x = n - 1 \\ y = n + 1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.10 Burnside's Lemma

 $|X/G|\!=\!\frac{1}{|G|}\!\sum_{g\in G}\!|X^g|$

- · G:各種翻轉操作所構成的置換群
- X/G:本質不同的方案的集合 X^g :對於某一種操作 g,所有方案中,經過 g 這種翻轉後保持不變的方案
- 集合取絕對值代表集合數

Search and Gready

7.1 Binary Search [d41d8c]

```
int main() {
          int l = 1, r = 10;
// 1 to tar, find tar
while (l <= r) {
    int m = (l + r) / 2;
    int m = (l + r) / 2;</pre>
                     if (check(m)) l = m + 1;
else r = m - 1;
          cout << r;
          // tar to end
while (l <= r) {
   int m = (l + r) / 2;
   if (check(m)) r = m - 1;
   else l = m + 1;
           cout << 1:
}
```

7.2 Ternary Search [d41d8c]

```
找極值問題,遞增遞減
void solve() {
    int l = 0, r = 10, ans = 0; // ans 紀錄答案 while (l <= r) {
          int d = (r - l) / 3; // 差
          int ml = l + d, mr = r - d; // mr 要用減的
auto cal = [&](int m) -> int {
              int x = 0;
               return x; // 計算答案
          int ansl = cal(ml), ansr = cal(mr);
if (ansl < ansr) {
    l = ml + 1;</pre>
          } else {
    r = mr - 1;
          }
    }
```

8 Тгее

8.1 LCA [601e2d]

```
vector < vector < int >> par(maxn, vector < int >(18));
vector < int > depth(maxn + 1);
vector < int > dfn(maxn);
vector < int > dfn(maxn);
void build(int n, vector < vector < pair < int, int >>> & tree) {
    auto dfs = [&](auto self, int u, int pre) -> void {
        for (auto [v, w] : tree[u]) {
            if (v == pre) continue;
            par[v][0] = u; // 2 ^ 0
            depth[v] = depth[u] + 1;
            self(self, v, u);
}
                }
        }
`a = par[a][i];
         for (int i = 17; i >= 0; i--) {
   if (par[a][i] != par[b][i]) {
        a = par[a][i], b = par[b][i];
}
         return par[a][0];
```

8.2 Centroid Decomposition [ec760b]

```
#include <bits/stdc++.h>
using namespace std;
struct CenDecom {
    int n:
     vector<vector<int>> adj;
    vector<bool> vis;
```

```
vector < int > siz;
CenDecom(int n_ = 0) { init(n_); }
        void init(int n_) {
              n = n_;
adj.assign(n, {});
              vis.assign(n, false);
              siz.assign(n, 1);
        void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
       void get_siz(int x, int p = -1) {
    siz[x] = 1;
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        get_siz(y, x);
        siz[x] += siz[y];
}
       return get_cen(y, sz, x);
              return x;
        void get_ans(int x, int p) {
              // do something
for (int y : adj[x]) {
    if (y == p || vis[y]) continue;
    get_ans(y, x);
        void work(int x = 0) {
    get_siz(0, x);
              int cen = get_cen(x, siz[x]);
              vis[cen] = true;
for (int y : adj[cen]) {
   if (vis[y]) continue;
                     get_ans(y, cen);
              for (int y : adj[cen]) {
                     if (vis[y]) continue;
                     work(y);
1 };
```

8.3 Tree Flattening [5293b7]

```
點加值 = 所有子節點區間加值,求單點,使用 bit,做前綴差分
// CSES 1138_Path Queries int main(){
      int n, q; cin >> n >> q;
vector <int> val(n + 1), dfnToVal(n);
for (int i = 1; i <= n; i++) {</pre>
            cin >> val[i];
      vector<vector<int>> tree(n + 1);
      for (int i = 1; i < n; i++) {
    int u, v; cin >> u >> v;
            tree[u].push_back(v);
tree[v].push_back(u);
      vector<pair<int, int>> mp(n + 1); // dfn 區間
      int cnt = 0;
auto dfs = [&](auto self, int u, int par) -> void {
    dfnToVal[++cnt] = val[u];
    mp[u].first = cnt;
}
            for (auto v : tree[u]) {
   if (v == par) continue;
   self(self, v, u);
            mp[u].second = cnt;
      dfs(dfs, 1, 0);
      | SIT bit(n);
| for (int i = 1; i <= n; i++) {
| bit.modify(mp[i].first, val[i]);
| if (mp[i].first < n) { // root 就不用扣了
                   bit.modify(mp[i].second + 1, -val[i]);
       for (int i = 0; i < q; i++) {
             int op; cin >> op;
            if (op == 1) {
   int s, x; cin >> s >> x;
   int add = x - dfnToVal[mp[s].first];
   dfnToVal[mp[s].first] = x;
                   bit.modify(mp[s].first, add);
                   if (mp[s].first < n) { // root 就不用扣了
bit.modify(mp[s].second + 1, -add);
             else {
                   int node; cin >> node;
                   cout << bit.query(mp[node].first) << "\n";</pre>
```

```
}
8.4
           Heavy Light Decomposition [325476]
       int n, cur;
vector <int> siz, top, dep, parent, in, out, seq;
vector <vector <int>> adj;
       HLD(int n_ = 0) { init(n_); }
       void init(int n_) {
             n = n(\( \text{int n} \) \
n = n_; \( \text{cur} = 0; \);
siz.resize(n); \( \text{top.resize(n)}; \) \( \text{dep.resize(n)}; \)
parent.resize(n); \( \text{in.resize(n)}; \) \( \text{out.resize(n)}; \)
seq.resize(n); \( \text{adj.assign(n, \{\})}; \)
       void addEdge(int u, int v) {
              adj[u].push_back(v);
adj[v].push_back(u);
       void work(int rt = 0) {
             top[rt] = rt;
dep[rt] = 0;
parent[rt] = -1;
dfs1(rt); dfs2(rt);
       void dfs1(int u) {
   if (parent[u] != -1)
       adj[u].erase(find
                            (adj[u].begin(), adj[u].end(), parent[u]));
              for (auto &v : adj[u]) {
    parent[v] = u, dep[v] = dep[u] + 1;
                    | dfs1(v);
| siz[u] += siz[v];
| if (siz[v] > siz[ad][u][0]]) {
| swap(v, ad][u][0]);
                    } // 讓 adj[u][0] 是重子節點
             }
       void dfs2(int u) {
              in[u] = cur++;
              seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
  top[v] = v == adj[u][0] ? top[u] : v;
                    dfs2(v);
              out[u] = cur;
       u = parent[top[u]];
} else {
                           v = parent[top[v]];
                    }
              return dep[u] < dep[v] ? u : v;</pre>
       int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
       int jump(int u, int k) {
   if (dep[u] < k) return -1;
   int d = dep[u] - k;
   while (dep[top[u]] > d)
        u = parent[top[u]];
}
              return seq[in[u] - dep[u] + d];
       bool isAncester(int u, int v) {
    return in[u] <= in[v] && in[v] < out[u];</pre>
       int rootedParent(int rt. int v) {
             if (rt == v) return rt;
if (!isAncester(rt, v)) return parent[rt];
auto it = upper_bound(adj[
             rt].begin(), adj[rt].end(), v, [&](int x, int y) {
    return in[x] < in[y];
}) - 1;
return *it;
       int rootedSize(int rt, int v) {
              if (rt == v) return n;
if (!isAncester(v, rt)) return siz[v];
return n - siz[rootedParent(rt, v)];
       int rootedLca(int a, int b, int rt) {
  return lca(a, b) ^ lca(b, rt) ^ lca(rt, a);
      }
};
8.5 Link Cut Tree [29ae0d]
#include <bits/stdc++.h>
```

```
using namespace std;
using ll = long long;
constexpr int Mod = 51061;
struct Tag {
    ll add = 0;
```

```
ll mul = 1:
     void apply(const Tag& v) {
    mul = mul * v.mul % Mod;
    add = (add * v.mul % Mod + v.add) % Mod;
struct Info {
    ll val = 1;
    ll sum = 1;
     void apply(int size, const Tag &v) {
   val = (val * v.mul % Mod + v.add) % Mod;
   sum = (sum * v.mul % Mod + v.add * size % Mod) % Mod;
};
struct Node {
     Node *ch[2], *p;
int rev = 0;
int size = 1;
     void make rev() {
          swap(ch[0], ch[1]);
rev ^= 1;
     Node() : ch {nullptr, nullptr}, p(nullptr) {}
     Info info = Info();
Tag tag = Tag();
     void apply(const Tag &v) {
   info.apply(size, v);
          tag.apply(v);
     rev = 0;
          if (ch[0]) {
                ch[0]->apply(tag);
          if (ch[1]) {
    ch[1]->apply(tag);
          tag = Tag();
     void pull_info() {
          };
bool isroot(Node *t) {
     return t->p
             == nullptr || (t->p->ch[0] != t && t->p->ch[1] != t);
int pos(Node *t) { // 回傳 1 代表是右子節點 return t->p->ch[1] == t;
void rotate(Node *t) {
     Node *q = t->p;
int x = !pos(t);
     q->ch[!x] = t->ch[x];
if (t->ch[x]) {
          t \rightarrow ch[x] \rightarrow p = q;
     t - p = q - p;
     if (!isroot(q)) {
          q \rightarrow p \rightarrow ch[pos(q)] = t;
     t - ch[x] = q;
     q->p = t;
q->pull_info();
void splay(Node *t) { // 單點修改前必須呼叫
     // 把 t 旋轉到目前 splay 的根while (!isroot(t)) {
          Node *p = t \rightarrow p;
          p->push_tag();
t->push_tag();
          rotate(t);
     t->push_tag();
t->pull_info();
void access(Node *t) {
     // 把從根到 t 的所有點都放在一條實鏈裡,使根
     // 到 t 成為一條實路徑,並且在同一棵 splay 裡 for (Node *i = t, *q = nullptr; i; q = i, i = i->p) {    splay(i);
          i->ch[1] = q;
     splay(t);
}
void makeRoot(Node *t) { // 使 t 點成為其所在樹的根
     access(t);
     swap(t->ch[0], t->ch[1]);
t->rev ^= 1;
```

```
Node* findRoot(Node *t) { // 找到 t 的 root
      access(t);
       splay(t);
      t->push_tag();
while (t->ch[0]) {
    t = t->ch[0];
            t->push_tag();
       splay(t);
 }
void link(Node *t, Node *p) {
       makeRoot(t);
if (findRoot(p) != t) {
            makeRoot(p);
            t->p = p;
p->pull_info();
      }
 bool cut(Node *x, Node *y) { // 不存在邊,回傳 false
      makeRoot(x);
       access(y);
      if (y->ch[0] != x || x->ch[1]) return false;
y->ch[0]->p = nullptr;
y->ch[0] = nullptr;
y->pull_info();
       return true:
 void split(Node
        *x, Node *y) { // 以 y 做根, 區間修改用, apply 在 y 上
       makeRoot(x);
       access(y);
       splay(y);
 bool isconnected(Node *x, Node *y) { // 查詢有沒有連通
      makeRoot(x);
      access(y);
return findRoot(x) == findRoot(y);
int main() {
    int n; cin >> n;
    vector <Node *> nodes(n);
    int q; cin >> q;
    for (int i = 0; i < n; i++) {
        nodes[i] = new Node();
        nodes[i]->info.val = nodes[i]->info.sum = 1LL;
}
       for (int i = 0; i < n - 1; i++) {
            int u, v; cin >> u >> v;
u--; v--;
             link(nodes[u], nodes[v]);
       for (int i = 0; i < q; i++) {
            char op; cin >> op;
if (op == '+') {
  int u, v; cin >> u >> v;
  u--; v--;
                  split(nodes[u], nodes[v]);
                  Tag tag;
cin >> tag.add;
                   tag.add % Mod;
                  nodes[v]->apply(tag);
             else if (op == '-') {
                  int u1, v1; cin >> u1 >> v1;
int u2, v2; cin >> u2 >> v2;
u1--; v1--; u2--; v2--;
cut(nodes[u1], nodes[v1]);
                  link(nodes[u2], nodes[v2]);
            else if (op == '*') {
   int u, v; cin >> u >> v;
   u--; v--;
                  split(nodes[u], nodes[v]);
                  Tag tag;
cin >> tag.mul;
tag.mul % Mod;
                  nodes[v]->apply(tag);
                  int u, v; cin >> u >> v;
                  split(nodes[u], nodes[v]);
                  cout << nodes[v]->info.sum << "\n";</pre>
            }
      }
       return 0;
}
```

8.6 Virtual Tree [622e69]

```
1// 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
 // 可以建立虚樹達成快速樹 DP
 // 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
   if (top == -1) return stk[++top] = u, void();
   int l = lca(stk[top], u);
```

```
if (l == stk[top]) return stk[++top] = u, void();
while (dfn[l] < dfn[stk[top - 1]])
    vt[stk[top - 1]].push_back(stk[top]), top--;
if (stk[top - 1] != l) {
    vt[l].push_back(stk[top]);
    stk[top] = l;
} else vt[l] sush back(stk[top.-]);</pre>
       } else vt[l].push_back(stk[top--]);
stk[++top] = u;
void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
       vt[u].clear();
void solve(int n, int q) {
   vector g(n + 1, vector<pair<int, int>>());
       vector v((n + 1, vector <patr < int > ()); // dfs 完清除, 否則會退化 vector <ll> dp(n + 1), iskey(n + 1); for (int i = 0; i < n - 1; i++) {
    int u, v, w; cin >> u >> v >> w;
             g[u].push_back({v, w});
             g[v].push_back({u, w});
       build_lca(n, g);
      for (int j = 0; j < m; j++) {
  cin >> key[j];
  iskey[key[j]] = 1;
             key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
                   return dfn[a] < dfn[b];</pre>
             });
for (int x : key) insert(x, vt);
              while (top
                       > 0) vt[stk[top - 1]].push_back(stk[top]), --top;
              auto dfs = [&](auto self, int u) -> void {
                    for (auto v : vt[u]) {
    self(self, v);
                           if (iskey[v]) {
                                 dp[u] += min_dis[v];
                                  // 砍掉 1 到 v 之間最短的路
                                 dp[u] += min(dp[v], min_dis[v]);
                           iskey[v] = dp[v] = 0;
                    vt[u].clear();
             };
             dfs(dfs, key[0]); // key[0] 一定是 root
cout << dp[key[0]] << "\n";
iskey[key[0]] = dp[key[0]] = 0;
}
```

8.7 Dominator Tree [baa540]

```
struct Dominator_tree {
            int n, id;
vector < vector < int >> adj, radj, bucket;
vector < int >> sdom, dom, vis, rev, pa, rt, mn, res;
Dominator_tree(int n_ = 0) { init(n_); }
void init(int _n) {
    n = _n, id = 0;
    adj.assign(n, vector < int >());
    radj.assign(n, vector < int >());
    bucket.assign(n, vector < int >());
    sdom.resize(n); dom.assign(n, -1);
    vis.assign(n, -1); rev.resize(n);
    pa.resize(n); rt.resize(n);
    mn.resize(n); res.resize(n);
}
            }
void add_edge(int u, int v) { adj[u].push_back(v); }
int query(int v, int x) {
    if (rt[v] == v) return x ? -1 : v;
    int p = query(rt[v], 1);
    if (p == -1) return x ? rt[v] : mn[v];
    if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
    rt[v] = n:
                          rt[v] = p;
                          return x ? p : mn[v];
            }
void dfs(int v) {
    vis[v] = id, rev[id] = v;
    rt[id] = mn[id] = sdom[id] = id, id++;
    for (int u : adj[v]) {
        if (vis[u] == -1) dfs(u), pa[vis[u]] = vis[v];
        radj[vis[u]].push_back(vis[v]);
}
              void build(int s) {
                         dfs(s);
for (int i = id - 1; i >= 0; i--) {
                                       for (int u : radj[i])
    sdom[i] = min(sdom[i], sdom[query(u, 0)]);
                                       if (i) bucket[sdom[i]].push_back(i);
for (int u : bucket[i]) {
                                                   int p = query(u, 0);
```

9 DP

9.1 LCS [5781cf]

9.2 LIS [66d09f]

```
int main() {
       int n; cin >> n;
       vector < int > v(n);
for (int i = 0; i < n; i++) cin >> v[i];
int dp[n]; vector < int > stk;
       stk.push_back(v[0]);
       stk.pusn_back(v[v]);
dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) {
    if (v[i] > stk.back()) {
        stk.push_back(v[i]);
        dp[i] = ++L;
}
             } else {
                    auto it
                             = lower_bound(stk.begin(), stk.end(), v[i]);
                    *it = v[i]; dp[i] = it - stk.begin() + 1;
             }
        vector<<mark>int</mark>> ans; cout << L << "\n";
       for (int i = n - 1; i >= 0; i--) {
   if (dp[i] == L) {
                    ans.push_back(v[i]), L--;
        }
reverse(ans.begin(), ans.end());
---> cout << i << " ";
       for (auto i : ans) cout << i <<
1
```

9.3 Edit Distance [308023]

9.4 Bitmask [a626f9]

```
void hamiltonianPath(){
         int n, m; cin >> n >> m;
vector adj(n, vector < int >());
for (int i = 0; i < m; i++) {
    int u, v; cin >> u >> v;
    adj[--v].push_back(--u);
         // 以...為終點,走過...
        if ((pre_mask & findBit(j)) == 0) continue;
                                   dp[i][mask
                                            }
         cout << dp[n - 1][findBit(n) - 1] << "\n";
}
void elevatorRides() {
    int n, x; cin >> n >> x; vector<int> a(n);
    for (int i = 0; i < n; i++) cin >> a[i];
    vector<array<int, 2>> dp(findBit(n));
    dp[0][0] = 1; // 次數、已使用人數
    for (int mask = 1; mask < findBit(n); mask++) {
        dp[mask][0] = dp[mask][1] = 2e9;
        for (int i = 0; i < n; i++) {
            if ((mask & findBit(i)) == 0) continue;
                 int pre_mask = mask < findBit(i);
                  if (dp[pre_mask][1] + a[i] <= x) {
                  if (dp[pre_mask][0] < dp[mask]
                                  } else if (dp[pre_mask
    ][0] + 1 < dp[mask][0] || dp[pre_mask][0]
    + 1 == dp[mask][0] && a[i] < dp[mask][1]) {
    dp[mask][0] = dp[pre_mask][0] + 1;</pre>
                                   dp[mask][1] = a[i];
                         }
                 }
         cout << dp[findBit(n) - 1][0] << "\n";
}
```

9.5 Projects [0942aa]

9.6 Removal Game [7bb56b]

```
| // 兩個人比賽,每個人輪流取一個數字且只能是頭尾
| // 間兩人都選得好,第一出手的人可取得的最大分數
    int main() {
        int n; cin >> n;
        vector<ll> a(n);
        for (int i = 0; i < n; i++) cin >> a[i];
        vector dp(n, vector<ll>(n)); // i 到 j 區間的最大 diff
        for (int i = n - 1; i >= 0; i--) {
              dp[i][i] = a[i];
```

bool pop_front(Line &l1, Line &l2, ll x) {

// 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y

```
for (int j = i + 1; j < n; j++)
    dp[i][j] =</pre>
                                                                                                                   // 代表查詢的當下,右線段的高度已經低於左線段了
                                                                                                                    return l1.eval(x) >= l2.eval(x);
                           max(a[i] - dp[i + 1][j], a[j] - dp[i][j - 1]);
                                                                                                             bool pop_back(Line &l1, Line &l2, Line &l3) {
       \frac{1}{x + y} = sum; // x - y = dp[0][n - 1]
                                                                                                                   // 本題斜率遞減、上凸包
       cout << (accumulate</pre>
                                                                                                                   // 因此只要 12 跟
              (a.begin(), a.end(), 0LL) + dp[0][n - 1]) / 2 << "\n";
                                                                                                                   l3 的 X 交點 <= l1 跟 l3 的 X 交點, l2 就用不到了return (l3.b - l2.b)
* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
 9.7 Monotonic Queue [f4976d]
                                                                                                             void insert(Line L) {
|// 應用: dp(i) = h(i) + max(A(j)), for l(i) \le j \le r(i)
                                                                                                                   while (rptr - lptr
 // A(j) 可能包含 dp(j), h(i) 可 O(1)
void Bounded_Knapsack() {
                                                                                                                           > 0 && pop_back(hull[rptr - 1], hull[rptr], L))
                                                                                                                         rptr - -;
      int n, k; // O([k)
vector<int> w(n), v(n), num(n); deque<int> q;
                                                                                                                   hull[++rptr] = L;
                                                                                                             ll query(ll x) {
       // 於是我們將同餘的數分在同一組
       // 於定我们將阿爾的數分任何 離

// 每次取出連續 num[i] 格中最大值

// g_x = max(_{k=0}^nnum[i] (g'_{x-k} + v_i*k))

// G_x = g'_{x} - v_i*x

// x 代 x-k => v_i*(x-k)

// g_x = max(_{k=0}^nnum[i] (G_{x-k} + v_i*x))

vector < vector < ll>> dp(2, vector < ll>(k + 1));

for (int i = 0; i < n; i++) {
                                                                                                                   while (rptr
                                                                                                                                      - lptr
                                                                                                                            > 0 && pop_front(hull[lptr], hull[lptr + 1], x))
                                                                                                                         lptr++
                                                                                                                   return hull[lptr].eval(x);
                                                                                                             }
                                                                                                      1:
                                                                                                       9.10 DNC [61c639]
             for (int r = 0; r < w[i]; r++) { // 餘數
                   q.clear(); // q 記錄在 x = i 時的 dp 有單調性
for (int x = 0; x * w[i] + r <= k; x++) {
    while (!q.empty() && q.front() < x - num[i])
                                                                                                      // 應用: 切 k 段問題,且滿足四邊形不等式
// w(a,c) + w(b,d) ≤(≥) w(a,d) + w(b,c)
// dp[k][j] = min(dp[k - 1][i] + cost[i][j])
                         // uplnj[j] - min(upln 3];

// cost: (i, j]

constexpr int N = 3e3 + 5;

constexpr ll inf = 4e18;

ll dp[N][N]; // 1-based

ll get_cost(int l, int r) {}
                                                                                                       void DNC(int k, int l, int r, int optl, int optr) {
    if (l > r) return;
    int m = (l + r) >> 1, opt = -1;
    dp[k][m] = inf;
    for (int i = max(k, optl); i <= min(m, optr); i++) {</pre>
                   }
                                                                                                                   // 注意 i 的範圍、 get_cost 與 dp 的邊界
ll cur = dp[k - 1][i] + get_cost(i, m);
if (cur < dp[k][m]) {
             swap(dp[0], dp[1]);
       cout << dp[0][k] << "\n";
                                                                                                                         dp[k][m] = cur, opt = i;
 9.8 SOS [93cb19]
                                                                                                             DNC(k, l, m - 1, optl, opt);
DNC(k, m + 1, r, opt, optr);
| // 使用情況: 跟 bit 與(被)包含有關, 且 x 在 1e6 左右
// 題目:一數組, 問有多少所有數 & 起來為 0 的集合數
                                                                                                       // dp[x]代表包含 x 的 y 個數(比x大且bit 1全包含 x 的有幾個)
 // 答案應該包含在 dp[0]内,但是有重複元素,所以考慮容斥
// => ans = \sum _{i=0}^{n} (-1)^{pop_count(i)} 2^{dp[i]-1}
// => 全部為0的個數 - 至少一個為1的個數 + 至少兩個為1的個數
                                                                                                             for (int i = 2; i <= k; i++) {
    DNC(i, 1, n, 1, n);</pre>
 void solve() {
       int n; cin >> n; Z ans = 0;
vector <int> a(n);
for (int i = 0; i < n; i++)
    cin >> a[i];
                                                                                                             cout << dp[k][n] << "\n";
       int m = __lg(*max_element(a.begin(), a.end())) + 1;
                                                                                                       9.11 LiChaoSegmentTree [f23ef4]
       // 定義 dp[mask] 為 mask 被包含於 a[i] 的 a[i] 個數
       // Lax Up/Mask ns mask ns
vector <Z > dp(1 << m);
for (int i = 0; i < n; i++)
    dp[a[i]] += 1;
for (int i = 0; i < m; i++)</pre>
                                                                                                       // 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \le r(i)
                                                                                                       constexpr ll inf = 4e18;
             for (int mask = 0; mask < 1 << m; mask++)
   if (mask >> i & 1) {
      int pre = mask ^ (1 << i);
      dp[pre] += dp[mask];</pre>
                                                                                                      struct Line {
    ll m, b;
    Line(ll m = 0, ll b = inf) : m(m), b(b) {}
    ll eval(ll x) const { return m * x + b; }
                                                                                                      };
       for (int mask = 0; mask < 1 << m; mask++) {
   int sgn = __builtin_popcount(mask) & 1 ? -1 : 1;
   ans += sgn * (power(Z(2), dp[mask].val()) - 1);</pre>
                                                                                                       struct LiChaoSeg { // 取 max 再變換就好
                                                                                                             int n:
                                                                                                             vector<Line> info;
                                                                                                             LiChaoSeg(int n_ = 0) { init(n_); }
void init(int n_) {
       cout << ans << "\n";
                                                                                                                   info.assign(4 << __lg(n), Line());</pre>
 9.9 CHT [5f5c25]
                                                                                                             void update(Line line, int node, int l, int r) {
   int m = (l + r) / 2;
|// 應用: dp(i) = h(i) + min/max(A(j)X(i) + B(j)), for j \le r(i)
 // A(j), B(j) 可能包含 dp(j), 分別就是 m 跟 b struct Line {
                                                                                                                   bool left = line.eval(l) < info[node].eval(l);
bool mid = line.eval(m) < info[node].eval(m);</pre>
                                                                                                                   if (mid) swap(info[node], line); // 如果新線段比較好
       ll m, b;
       Line(ll m = 0, ll b = 0) : m(m), b(b) {}
ll eval(ll x) {
    return m * x + b;
                                                                                                                   if (r - l == 1) return;
else if (left != mid) update(line, 2 * node, l, m);
                                                                                                                   // 代表左半有交點
                                                                                                                   else update(line, 2 * node + 1, m, r);
 };
                                                                                                                   // 代表如果有交點一定在右半
 struct CHT { // 用在查詢單調斜率也單調
   int n, lptr, rptr; vector Line > hull;
   CHT(int n = 0, Line init = Line()) {
                                                                                                             void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
    if (r - l == 1) return info[node].eval(x);
    int m = (l + r) / 2;
    if (x < m) return
        min(info[node].eval(x), query(x, 2 * node, l, m));
}</pre>
             init(n_, init_);
       void init(int n_ = 0, Line init_ = Line()) {
             n = n_; hull.resize(n); reset(init_);
       void reset(Line init_ = Line()) {
    lptr = rptr = 0; hull[0] = init_;
                                                                                                                          info[node].eval(x), query(x, 2 * node + 1, m, r));
```

Il query(int x) { return query(x, 1, 0, n); }

9.12 Codeforces Example [7d37ea]

```
// 給你很多區間, 你可以選一些點, 重疊到的線段得到 1 分
// 請問在線段不重複的情況下,最多獲得幾分 int main() {
    int n, m;
cin >> n >> m;
    // 記錄每點有幾個線段
    // 再一個紀錄,包含這個點的左界
    cnt[l]++;
         cnt[r + 1]--;
    for (int i = 2; i <= n; i++) {
    cnt[i] += cnt[i - 1];</pre>
    for (int i = n; i >= 2; i--) {
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
    vector<int> dp(n + 1);
    dp[0] = 0;
for (int i = 1; i <= n; i++) {</pre>
         dp[i] = cnt[i];
if (l_side[i] != inf)
             dp[i] += dp[l_side[i] - 1];
         dp[i] = max(dp[i], dp[i - 1]);
    cout << dp[n] << "\n";
// CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
// 再加上 max(bi) - min(bi)
int main(){
   int n, k,
               ans = 0; cin >> n >> k;
    full i, k, ans = 0; ctn >> n >>
vector cpii> v(n + 1);
for (int i = 1; i <= n; i++) {
   int a, b; cin >> a >> b;
   v[i] = {a, b};
         if (a <= k) ans = 1;
    sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
         return a.second < b.second;
    }); // 用 bi 來排,考慮第 i 個時可以先扣
    vector<vector<int>> dp(n + 1, vector<int>(n + 1, inf));
    // 考慮 v[i] 時, 選 j 個的 sum(ai) - min(bi)
    for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
    (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
              // min(不選, 選)
              if (dp[i
                     1][j - 1] + v[i].first + v[i].second <= k) {
                  // 假如可以選, 更新 ans 時再加回去 bi
                  ans = max(ans, j);
         dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
    cout << ans << endl;
```

10 Geometry

10.1 Basic [d41d8c]

template < class T>

```
struct Point {
     T x, v;
     Point(const T &x_ = 0, const T &y_ = 0) : x(x_{-}), y(y_{-}) {}
     template < class U>
     operator Point<U>() {
          return Point<U>(U(x), U(y));
    Point &operator+=(const Point &p) & {
    x += p.x; y += p.y; return *this;
    Point &operator -= (const Point &p) & {
    x -= p.x; y -= p.y; return *this;
    Point & operator *= (const T & v) & {
    x *= v; y *= v; return *this;
    Point &operator/=(const T &v) & {
    x /= v; y /= v; return *this;
     Point operator - () const {
          return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
          return a += b;
     friend Point operator-(Point a, const Point &b) {
          return a -= b;
```

```
friend Point operator*(Point a, const T &b) {
           return a *= b;
      friend Point operator/(Point a, const T &b) {
           return a /= b;
      friend Point operator*(const T &a, Point b) {
   return b *= a;
      friend bool operator == (const Point &a. const Point &b) {
           return a.x == b.x && a.y == b.y;
      friend istream & operator >> (istream & is. Point & p) {
           return is >> p.x >> p.y;
      friend ostream &operator << (ostream &os, const Point &p) {
    return os << "(" << p.x << ", " << p.y << ")";</pre>
};
template < class T>
struct Line {
     Point<T>
      Point < T > b;
      Line(const Point<T> &a_ = Point<T>()
            , const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
template < class T>
T dot(const Point<T> &a, const Point<T> &b) {
      return a.x * b.x + a.y * b.y;
T cross(const Point<T> &a, const Point<T> &b) {
   return a.x * b.y - a.y * b.x;
template < class T >
T square(const Point < T > &p) {
   return dot(p, p);
template < class T>
double length(const Point<T> &p)
    return sqrt(double(square(p)));
template < class T>
double length(const Line<T> &l) {
      return length(l.a - l.b);
template < class T>
Point < T > normalize(const Point < T > &p) {
     return p / length(p);
bool parallel(const Line<T> &l1, const Line<T> &l2) {
   return cross(l1.b - l1.a, l2.b - l2.a) == 0;
template < class T >
double distance(const Point < T > & a, const Point < T > & b) {
    return length(a - b);
template < class T>
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)</pre>
     return distance(p, l.a);
if (dot(p - l.b, l.a - l.b) < 0)
return distance(p, l.b);
return distancePL(p, l);
template < class T>
Point<T> rotate(const Point<T> &a) {
    return Point(-a.y, a.x);
int sgn(const Point<T> &a) {
    return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
template < class T>
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
     return cross(l.b - l.a, p - l.a) > 0;
template < class T>
      > lineIntersection(const Line<T> &l1, const Line<T> &l2) {
return l1.a + (l1.b - l1.a) * (cross(l2.b - l2.a, l1.a - l2.a) / cross(l2.b - l2.a, l1.a - l1.b));
template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
     return cross(p - l.a, l.b - l.a) == 0 &&
min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)
                  (l.a.y, l.b.y) \ll p.y \ll max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
      (const Point<T> &a, const vector < Point < T>> &p) {
int n = p.size(), t = θ;
for (int i = θ; i < n; i++) {</pre>
           if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {
```

```
return true:
      for (int i = 0; i < n; i++) {
    auto u = p[i];</pre>
             auto v = p[(i + 1) \% n];
             if (u.x < a.
                   x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
t ^= 1;
             if (u.x >= a
    .x && v.x < a.x && pointOnLineLeft(a, Line(u, v)))</pre>
       return t == 1:
// 0 : not intersect
// 1 : strictly
// 2 : overlap
    1 : strictly intersect
// 3 : intersect at endpoint
template < class T>
tuple<int, Point<T>, Point<T>> segmentIntersection
   (const Line<T> &l1, const Line<T> &l2) {
      if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
    return {0, Point<T>(), Point<T>()};
if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
    return {0, Point<T>(), Point<T>()};
      if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.)
    return {0, Point<T>(), Point<T>()};
if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.)
    return {0, Point<T>(), Point<T>()};
if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
    if (cross(l1.b - l1.a, l2.a - l1.a) != vactors {0, Point<T>(), Point<T>(), Point<T>()
                                                                       ĺ2.b.y))
                                                                        ĺ2.b.y))
                    return {0, Point<T>(), Point<T>()};
             } else {
                    auto maxx1 = max(l1.a.x, l1.b.x);
                   swap(p1.y, p2.y);
if (p1 == p2) {
    return {3, p1, p2};
                    } else {
                           return {2, p1, p2};
             }
      auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);

auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);

auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);

auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);

if ((cp1 > 0 && cp2 > 0) || (cp1 < 0 && cp2
      < 0) || (cp3 > 0 && cp4 > 0) || (cp3 < 0 && cp4 < 0))
return {0, Point<T>(), Point<T>()};
Point p = lineIntersection(l1, l2);
       if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
             return {1, p, p};
      } else {
             return {3, p, p};
template < class T>
double distanceSS(const Line<T> &l1, const Line<T:
    if (get<0>(segmentIntersection(l1, l2)) != 0)
        return 0.0;
                                                              const Line<T> &l2) {
       return min({distancePS(l1.a, l2), distancePS(l1
               .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
bool segmentInPolygon
        (const Line<T> &l, const vector<Point<T>> &p) {
       int n = p.size();
      if (!pointInPolygon(l.a, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
for (int i = 0; i < n; i++) {
    auto u = p[i];
    auto v = p[(i + 1) % n];
    auto w = p[(i + 2) % n];</pre>
             if (pointOnSegment(v, l) && v != l.a && v != l.b)
    if (cross(v - u, w - v) > 0)
        return false;
             || pointOnLineLeft(l.b, Line(v, u)))
                    return false;
} else if (p1 == v) {
   if (l.a == v) {
                                  if (pointOnLineLeft(u, l)) {
    if (pointOnLineLeft(w, l))
                                                && pointOnLineLeft(w, Line(u, v)))
                                                return false;
```

```
if (pointOnLineLeft(w, l)
                                 || pointOnLineLeft(w, Line(u, v)))
                                 return false:
                  return false;
                       } else {
    if (pointOnLineLeft(w, l)
                                 |
|| pointOnLineLeft(w, Line(u, v)))
                                 return false:
                  }
             }
        }
    return true:
vector<Point<T>> hp(vector<Line<T>> lines) {
    sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
   auto d1 = l1.b - l1.a;
   auto d2 = l2.b - l2.a;
   if (sgn(d1) != sgn(d2))
        return sgn(d1) == 1;
   }
}
         return cross(d1, d2) > 0;
    deaue < Line < T >> ls:
     deque<Point<T>> ps;
    for (auto l : lines) {
    if (ls.empty()) {
              ls.push_back(l);
              continue;
         while (!ps.empty() && !pointOnLineLeft(ps.back(), l))
         ps.pop_back(), ls.pop_back();
while (!ps.empty() && !pointOnLineLeft(ps[0], l))
    ps.pop_front(), ls.pop_front();
if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
              if (dot
                    (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                   if (!pointOnLineLeft(ls.back().a, l)) {
                        assert(ls.size() == 1);
                        ls[0] = l;
                  continue;
              return {}:
         ps.push_back(lineIntersection(ls.back(), l));
ls.push_back(l);
    while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0]))
    ps.pop_back(), ls.pop_back();
if (ls.size() <= 2) return {};</pre>
    ps.push_back(lineIntersection(ls[0], ls.back()));
    return vector(ps.begin(), ps.end());
using P = Point<ll>;
10.2 Convex Hull [b5758d]
```

```
int main() {
     int n; cin >> n;
vector <P> P(n), U, L;
for (int i = 0; i < n; i++) {
    cin >> P[i];
            .end(), [](const Point<i64> &a, const Point<i64> &b) {
return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
     for (int i = 0; i < n; i++) {
   while (L.size() >= 2 && cross(L.back() -
        L[L.size() - 2], P[i] - L[L.size() - 2]) <= 0LL) {</pre>
                 L.pop_back();
            while (U.size() >= 2 && cross(U.back()
                 U[U.size() - 2], P[i] - U[U.size() - 2]) >= 0LL){
U.pop_back();
                  empty() || !(L.back() == P[i])) L.push_back(P[i]);
                   empty() || !(U.back() == P[i])) U.push_back(P[i]);
     if (L.size() <= 2 && U.size() <= 2) {
           // No Hull
```

}

}

return make pair(r, c);

}

}

p + rotate(a[j] - a[i])), Line
 (q, q + rotate(a[k] - a[j])));
r = length(c - a[i]);

```
cout << L.size() + U.size() - 2 << "\n";
for (int i = 0; i < L.size() - 1; i++) {
    cout << L[i].x << " " << L[i].y << "\n";</pre>
       for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << " | n";</pre>
10.3 MinEuclideanDistance [3020bc]
T distanceSquare(const Point<T> &a, const Point<T> &b) {
      return square(a - b);
void solve() {
      int n; cin >> n;
constexpr ll inf = 8e18;
vector<Point<ll>> a(n);
      for (int i = 0; i < n; i++) {
    ll x, y;
    cin >> x >> y;
            a[i] = Point < ll > (x, y);
       struct sortY {
            ()(const Point<ll> &a, const Point<ll> &b) const {
                   return a.y < b.y;</pre>
            }
       struct sortXY {
            bool operator
                    ()(const Point<ll> &a, const Point<ll> &b) const {
                   if (a.x == b.x) return a.y < b.y;
else return a.x < b.x;</pre>
            }
      sort(a.begin(), a.end(), sortXY());
vector<Point<ll>> t(n);
      auto devide = [&](auto &&self, int l, int r) -> ll {
   if (l == r) return inf;
   int m = (l + r) / 2;
            ll ans = min(self(self, l, m), self(self, m + 1, r));
ll midval = a[m].x;
            ll midvat - c...,
ll p = 0;
for (int i = l; i <= r; i++) {
   if ((midval - a[i].x) * (midval - a[i].x) <= ans) {
      t[p++] = a[i];
   }</pre>
            if ((t[i].y
                                  t[j].y) * (t[i].y - t[j].y) > ans) break;
                  }
      cout << devide(devide, 0, n - 1) << "\n";</pre>
10.4 LatticePoints [00db9d]
int main() {
      // Polygun 內整數點數
      int n; cin >> n;
vector <Point <ll>> polygon(n);
for (int i = 0; i < n; i++) cin >> polygon[i];
      for (int i = 0; i < n; i++) {
    area += cross(polygon[i], polygon[(i + 1) % n]);</pre>
       area = abs(area);
      auto countBoundaryPoints
               = [](const vector<Point<ll>>& polygon) -> ll {
            ll res = 0;
            int n = polygon.size();
for (int i = 0; i < n; i++) {
    ll dx = polygon[(i + 1) % n].x - polygon[i].x;
    ll dy = polygon[(i + 1) % n].y - polygon[i].y;
}</pre>
                   res += std::gcd(abs(dx), abs(dy));
             return res;
      };
ll res = countBoundaryPoints(polygon);
      ll ans = (area - res + 2) / 2;
cout << ans << " " << res << " | n ";
10.5 MinCoverCircle [c9ca81]
pair<T, Point<T>> MinCircular(vector<Point<T>> &a) {
   random_shuffle(a.begin(), a.end());
   int n = a.size();
      int n = a.stze();
Point<T> c = a[0]; T r = 0;
for (int i = 1; i < n; i++) {
    if (T(length(c - a[i]) - r) > 0.0) {
       c = a[i], r = 0;
       for (int j = 0; j < i; j++) {</pre>
```