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1 Basic

1.1 Install VScode [d41d8c]

1.2 Default Code [d41d8c]

```
#include <bits/stdc++.h>
// #pragma GCC target("popcnt")
// C++ 20 vector grammer will not work
#define all(x) (x).begin(), (x).end()
using namespace std;
using ll = long long;

void solve() {
}
int main() {
   ios_base::sync_with_stdio(false);
   cin.tie(nullptr);
   int t = 1;
   cin >> t;
   while (t--) {
      solve();
   }
}
```

1.3 Compare Fuction [d41d8c]

```
// 如果有自定義比較結構就比照以上
};
struct cmp {
                    // 要在 template 的資結用外部變數
     vector<int> &v;
     cmp(vector<int>& vec) : v(vec) {}
bool operator() (int a, int b) const {
   return v[a] > v[b];
// mutil: cmp cmp1(vector);
// priority_queue<int, vector<int>, cmp> pq(cmp1);
};
1.4 Pbds [d41d8c]
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < typename T>
using pbds_set = tree<T, null_type,</pre>
        less<T>, rb_tree_tag, tree_order_statistics_node_update>;
template < typename T>
using pbds_multiset = tree<T, null_type, less_equal</pre>
      <T>, rb_tree_tag, tree_order_statistics_node_update>;
1.5 Double [b44e11]
struct D {
     double x;
     constexpr static double eps = 1e-12;
     constexpr static double eps = 1e-12;
D() : x{0.0} {}
D(double v) : x{v} {}
double val() const { return x; }
explicit operator double() const { return x; }
D operator-() const {
          return D(-x);
     D & operator += (const D & rhs) & {
          x += rhs.x; return *this;
     D & operator -= (const D & rhs) & {
          x -= rhs.x; return *this;
     D & operator *= (const D & rhs) & {
          x *= rhs.x; return *this;
     D & operator/=(const D &rhs) & {
    assert(fabs(rhs.x) > eps);
    x /= rhs.x; return *this;
      friend D operator+(D lhs, const D &rhs) {
          return lhs += rhs;
      friend D operator - (D lhs, const D &rhs) {
          return lhs -= rhs;
      friend D operator*(D lhs, const D &rhs) {
          return lhs *= rhs;
      friend D operator/(D lhs, const D &rhs) {
          return lhs /= rhs;
     friend bool operator<(const D &lhs, const D &rhs) {
   return lhs.x - rhs.x < -eps;</pre>
     friend bool operator > (const D &lhs, const D &rhs) {
   return lhs.x - rhs.x > eps;
      friend bool operator == (const D &lhs, const D &rhs) {
          return fabs(lhs.x - rhs.x) < eps;</pre>
     friend bool operator <= (const D &lhs, const D &rhs) {
   return lhs < rhs || lhs == rhs;</pre>
      friend bool operator>=(const D &lhs, const D &rhs) {
          return lhs > rhs || lhs == rhs;
      friend bool operator!=(const D &lhs, const D &rhs) {
          return !(lhs == rhs);
      friend istream &operator>>(istream &is, D &a) {
           double v; is >> v; a = D(v); return is;
      friend ostream &operator<<(ostream &os, const D &a) {</pre>
     return os << fixed << setprecision(10) << a.val() + (a.val() > 0 ? eps : a.val() < 0 ? -eps : 0); } // eps should < precision
```

2 Graph

};

2.1 DFS And BFS [e2d856]

```
int main() {
    int n;
    vector < vector < int >> adj(n);
    // dfs_graph
    vector < bool > vis(n);
    auto dfs = [&](auto self, int u) -> void {
        if (vis[u]) return;
        vis[u] = true;
        for (auto v: adj[u]) {
```

```
self(self. v):
       }
};
dfs(dfs, 0);
// bfs
vector < int > depth(n, 1e9);
queue<int> q;
auto bfs = [&](auto self, int s) -> void {
    vis[s] = true, depth[s] = 0;
       q.push(s);
       while (!q.empty()) {
    int u = q.front(); q.pop();
               tit d = q.:\text{ont}(y, q.pop(),
for (auto v : adj[u]) {
    if (vis[v]) continue;
    vis[v] = true;
    depth[v] = depth[u] + 1;
                      q.push(v);
               }
      }
bfs(bfs, 0);
```

2.2 Prim [3a3805]

```
auto prim
       [&](int n, vector<vector<pair<int, int>>> &adj) -> bool {
     int node_sz = 0;
     priority_queue<pair<int, int>,
            vector<pair<int, int>>, greater<pair<int, int>>> pq;
     pq.emplace(0, 0); // w, vertex
vector<bool> vis(n);
     while (!pq.empty()) {
   auto [u, w] = pq.top(); pq.pop();
   if (vis[u]) continue;
          vis[u] = true;
          node_sz++;
          for (auto v : adj[u]) {
    if (!vis[v.first]) {
                    pq.emplace(v.second, v.first);
         }
    }
if (node_sz == n) return true;
return false;
```

2.3 BellmanFord [430ded]

```
// 用 Bellman Ford 找負環
int main() {
                             main() {
int n, m; cin >> n >> m;
vector array < int, 3>> e;
for (int i = 0; i < m; i++) {
   int u, v, w; cin >> u >> v >> w;
   u--, v--; e.push_back({u, v, w});
}
                             for (auto [u, v, w] : e) {
    for (auto [u, v, w] : e) {
        if (dis[v] > dis[u] + w) {
            dis[v] = u;
            par[v] = u;
            if (dis[v] > dis[v] + w;
            par[v] = u;
            if (i - o) + - v;
            if (i - o) + - v;
           if (i - o) + - v;
            if (i - o) + - v;

                                                                                                                                 if (i == n) t = v;
                                                                                           }
                                                             }
                              if (t == -1) { cout << "NO|n"; return; }
for (int i = 1; i < n; i++) t = par[t];
vector <int> ans {t};
                                int i = t:
                                do {
                                                                i = par[i];
                              ans.push_back(i);
} while (i != t);
                                 reverse(ans.begin(), ans.end());
                                 cout << "YES\n";
                                 for (auto x : ans) cout << x + 1 << " ";
```

2.4 FloydWarshall [3f61a4]

```
constexpr ll inf = 1e18;
 void FloydWarshall(int n, int m) {
  int n, m; cin >> n >> m;
  vector<vector<int>> dis(n, vector<int>(n, inf));
         for (int i = 0; i < m; i++) {
  int u, v, w; cin >> u >> v >> w;
  dis[u][v] = min(dis[u][v], w);
  dis[v][u] = min(dis[v][u], w);
        for (int i = 0; i < n; i++) dis[i][i] = 0;
for (int k = 0; k < n; k++) {</pre>
                 for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
        dis[i][j</pre>
                                           ] = min(dis[i][j], dis[i][k] + dis[k][j]);
                         }
                 }
        }
}
```

```
for (int i = 0; i < n; i++)
    if (dp[i][k])</pre>
            dp[i] |= dp[k];
}
```

2.5 Euler [4177dc]

```
|// 1. 無向圖是歐拉圖:
// 非零度頂點是連通的
// 頂點的度數都是偶數
// 2. 無向圖是半歐拉圖(有路沒有環):
| // 非零度頂點是連通的
// 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
// 非零度頂點是強連通的
// 每個頂點的入度和出度相等
| // 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
| // 至多一個頂點的出度與入度之差為 1
// 至多一個頂點的入度與出度之差為 1
 // 其他頂點的入度和出度相等
vector < int > ans;
auto dfs = [&](auto &&self, int u) -> void {
    while (g[u].size()) {
   int v = *g[u].begin();
       g[u].erase(v);
       self(self, v);
    ans.push back(u);
 dfs(dfs, 0);
reverse(ans.begin(), ans.end());
```

2.6 SCC [5d3e16]

```
struct SCC {
      int n, cur, cnt;
vector<vector<int>>> adj;
      vector<int> stk, dfn, low, bel;
SCC(int n_ = 0) { init(n_); }
void init(int n_) {
           n = n_;
adj.assign(n, {});
            low.resize(n);
           bel.assign(n,
            stk.clear();
            cur = cnt =
      void addEdge(int u, int v) {
           adj[u].push_back(v);
      void dfs(int x) {
    dfn[x] = low[x] = cur++;
            stk.push_back(x);
           for (auto y : adj[x]) {
   if (dfn[y] == -1) {
                       dfs(y);
                 low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
                 }
            if (dfn[x] == low[x]) {
                  int y;
                  do {
                       v = stk.back();
                       bel[y] = cnt;
                       stk.pop_back();
                 } while (y != x);
           }
      vector < int > work() {
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) dfs(i);
}</pre>
            return bel;
      struct Graph {
            int n:
           vector<pair<int, int>> edges;
            vector<int> siz:
            vector<int> cnte;
      Graph compress() {
           Graph g;
g.n = cnt;
           g.siz.resize(cnt);
           g.cnte.resize(cnt);

for (int i = 0; i < n; i++) {
                 g.siz[bel[i]]++;
```

```
for (auto j : adj[i]) {
    if (bel[i] != bel[j]) {
        g.edges.emplace_back(bel[i], bel[j]);
    } else {
        g.cnte[bel[i]]++;
    }
    }
    return g;
}
```

2.7 VBCC [170604]

```
struct VBCC {
     int n, cur;
     vector < int >> adj;
     vector <int> dfn, low, parent;
vector <bool> is_cut;
     VBCC(int n_ = 0) { init(n_); }
void init(int n_) {
           n = n_;
           adj.assign(n, {});
           dfn.assign(n, -1);
low.resize(n);
           parent.assign(n, -1);
           is_cut.assign(n, false);
           cur = 0:
     void addEdge(int u, int v) {
   adj[u].push_back(v);
           adj[v].push_back(u);
     void dfs(int x) {
   int children = 0;
           dfn[x] = low[x] = cur++;
           for (int v : adj[x]) {
   if (dfn[v] == -1) {
                      children++;
                      parent[v] = x;
                      dfs(v);
                      low[x] = min(low[x], low[v]);
                      if (parent[x] != -1 && low[v] >= dfn[x]) {
    is_cut[x] = true;
                } else if (v != parent[x]) {
    low[x] = min(low[x], dfn[v]);
           if (parent[x] == -1 && children > 1) {
                is_cut[x] = true;
           }
     void work() {
           for (int i = 0; i < n; i++) {
    if (dfn[i] == -1) {
        dfs(i);
}</pre>
          }
     }
```

2.8 EBCC [59d8ca]

```
struct EBCC { // CF/contest/1986/pF
      int n, cur, cnt;
vector<vector<int>> adj;
      vector<int> stk, dfn, low, bel;
      vector<pair<int, int>> bridges; // 關鍵邊
EBCC(int n_ = 0) { init(n_); }
void init(int n_) {
            n = n_;
adj.assign(n, {});
            dfn.assign(n, -1);
            low.resize(n);
            bel.assign(n, -1);
            stk.clear();
            bridges.clear();
            cur = cnt = 0:
      void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
     void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
    stk.push_back(x);
            for (auto y : adj[x]) {
   if (y == p) continue;
   if (dfn[y] == -1) {
                        dfs(y, x);
low[x] = min(low[x], low[y]);
if (low[y] > dfn[x]) {
                              bridges.emplace_back(x, y);
                  } else if (bel[y] ==
                                                    -1) {
                        low[x] = min(low[x], dfn[y]);
            if (dfn[x] == low[x]) {
                  int y;
```

```
do {
                               y = stk.back();
                               bel[y] = cnt;
                       stk.pop_back();
} while (y != x);
                       cnt++;
               }
        fvector<int> work() { // not connected
    for (int i = 0; i < n; i++) {
        if (dfn[i] == -1) {
            dfs(i, -1);
        }
}</pre>
                return bel;
        struct Graph {
                int n;
               vector<pair<int, int>> edges;
               vector<int> siz; // BCC 內節點數
               vector<int> cnte; // BCC 內邊數
        Graph compress() {
               Graph g;
g.n = cnt;
               g.siz.resize(cnt);
                g.cnte.resize(cnt);
               g.tite:TestZe(cit),
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;
    for (auto j : adj[i]) {
        if (bel[i] < bel[j]) {
            g.edges.emplace_back(bel[i], bel[j]);
        } else if (i < j) {
            cata[bel[i]]++;
        }
}</pre>
                                      g.cnte[bel[i]]++;
                       }
                return a:
       }
};
```

```
2.9 2-SAT [eeddc1]
// CSES Giant Pizza
struct TwoSat {
      int n; vector<vector<int>> e;
vector<bool>
    ans;
TwoSat(int n) : n(n), e(2 * n), ans(n) {}
void addClause(int u, bool f, int v, bool g) {
        e[2 * u + !f].push_back(2 * v + g);
        e[2 * v + !g].push_back(2 * u + f);
}
       bool satisfiable() {
             vector < int > id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
             vector <int> stk;
int now = 0, cnt = 0;
function <void(int)> tarjan = [&](int u) {
                    stk.push_back(u);
                    dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
                          tarjan(v);
  low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in s
  low[u] = min(low[u], dfn[v]);
                    if (dfn[u] == low[u]) {
                           int v;
                          stk.pop_back();
id[v] = cnt;
                           } while (v != u);
                           ++cnt;
                   }
             for (int i
             return true;
       vector<bool> answer() { return ans; }
int main() {
       int m, n; cin >> m >> n;
TwoSat ts(n);
      for (int i = 0; i < m; ++i) {
   int u, v; char x, y;
   cin >> x >> u >> y >> v;
   ts.addClause(u - 1, x == '+', v - 1, y == '+');
       fif (ts.satisfiable()) {
    for (int i = 0; i < n; ++i) {
        cout << (ts.answer()[i] ? '+' : '-') << " ";</pre>
       else cout << "IMPOSSIBLE\n";</pre>
```

2.10 Funtional Graph [85c464]

| }

```
constexpr int N = 2e5 + 5;
int cht[N][31]; // 倍增表,放外面不然 TLE struct FuntionalGraph {
        int n, cnt;
vector <int> g, bel, id, len, in, top;
FuntionalGraph() : n(0) {}
FuntionalGraph(vector <int> g_) { init(g_); }
         void init(vector < int > g_) {
    n = g_.size(); cnt = 0;
                  g = g_; bel.assign(n, -1);
id.resize(n); len.clear();
                  in.assign(n, 0); top.assign(n, -1);
                  build();

}
void build() {
    for (int i = 0; i < n; i++) {
        cht[i][0] = g[i];
        cht[i][0] = g[i];
}
</pre>
                          in[g[i]]++;
                 for (int i = 1; i <= 30; i++)
    for (int u = 0; u < n; u++)
        cht[u][i] = cht[cht[u][i - 1]][i - 1];
for (int i = 0; i < n; i++)
    if (in[i] == 0) label(i);
for (int i = 0; i < n; i++)
    if (top[i] == -1) label(i);</pre>
         void label(int u) {
    vector<int> p; int cur = u;
    while (top[cur] == -1) {
        top[cur] = u;
    }
}
                          p.push_back(cur);
                           cur = g[cur];
                  auto s = std::find(p.begin(), p.end(), cur);
                 vector < int> cyc(s, p.end());
p.erase(s, p.end()); p.push_back(cur);
for (int i = 0; i < (int)cyc.size(); i++) {
    bel[cyc[i]] = cnt;</pre>
                          id[cyc[i]] = i;
                  cnt++; len.push_back(cyc.size());
                  for (int i = p.size() - 1; i > 0; i--)
id[p[i - 1]] = id[p[i]] - 1;
         int jump(int u, int k) {
    for (int b = 0; k > 0; b++){
        if (k & 1) u = cht[u][b];
}
                          k >>= 1;
};
```

Data Structure

3.1 BIT [d41d8c]

template <tvpename T>

```
struct Fenwick { // 全部以 0 based 使用
int n; vector<T> a;
Fenwick(int n_ = 0) { init(n_); }
void init(int n_) {
         n = n_;
a.assign(n, T{});
     void add(int x, const T &v) {
   for (int i = x + 1; i <= n; i += i & -i) {
      a[i - 1] = a[i - 1] + v;
}</pre>
     T sum(int x) { // 左閉右開查詢
          T ans{};
          for (int i = x; i > 0; i -= i & -i) {
              ans = ans + a[i - 1];
          return ans;
     TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
     int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
          int x = 0;
          T cur{};
          for (int i = 1 << __lg(n); i; i /= 2) {
               if (x + i <= n && cur + a[x + i - 1] <= k) {
    x += i;
                    cur = cur + a[x - 1];
               }
          return x;
    }
template <class T>
struct TwoDFenwick { // 全部以 0 based 使用
    int nx, ny; // row, col 個數
```

```
vector < T >> a;
TwoDFenwick(int nx_ = 0, int ny_ = 0) {
             init(nx_, ny_);
        void init(int nx_, int ny_) {
             nx = nx_; ny = ny_;
a.assign(nx, vector<T>(ny, T{}));
        void add(int x, int y, const T &v) {
             for (int i = x + 1; i <= nx; i += i & -i) {
    for (int j = y + 1; j <= ny; j += j & -j) {
        a[i - 1][j - 1] = a[i - 1][j - 1] + v;
             }
       }
       T sum(int x, int y) { // 左閉右開查詢 T ans{}};
             for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans + a[i - 1][j - 1];
    }
}
              return ans;
       T rangeSum
               (int lx, int ly, int rx, int ry) { // 左閉右開查詢
              return sum(
                     (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
};
 3.2 RangeBit [d41d8c]
template <typename T>
 struct rangeFenwick { // 全部以 0 based 使用
       int n:
       vector<T> d, di;
       rangeFenwick(int n_ = 0) { init(n_); }
       void init(int n_) {
             n = n;
              d.assign(n, T{})
             di.assign(n, T{});
       Joid add(int x, const T &v) {
   T vi = v * (x + 1);
   for (int i = x + 1; i <= n; i += i & -i) {
      d[i - 1] = d[i - 1] + v;
      di[i - 1] = di[i - 1] + vi;
}</pre>
             }
       void rangeAdd(int l, int r, const T &v) {
   add(l, v); add(r, -v);
       T sum(int x) { // 左閉右開查詢
             T ans{};
              for (int i = x; i > 0; i -= i & -i) {
                   ans = ans + T(x + 1) * d[i - 1];
ans = ans - di[i - 1];
             return ans;
       T rangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
       int select(const T &k) { // 找到最小的 x, 使得 sum(x) > k
             int x = 0;
            x + i + 1) * d[x + i - 1] - di[x + i - 1];
if (cur + val <= k) {
    x += i;</pre>
                                cur = cur + val;
                  }
             return x;
      }
 template <class T>
 struct rangeTwoDFenwick { // 全部以 0 based 使用
       int nx, ny; // row, col 個數
vector<vector<T>> d, di, dj, dij;
       rangeTwoDFenwick(int nx_ = 0, int ny_ = 0) {
             init(nx , ny );
       void init(int nx_, int ny_) {
    nx = nx_; ny = ny_;
    d.assign(nx, vector<T>(ny, T{}));
             di.assign(nx, vector<T>(ny, T{}));
dj.assign(nx, vector<T>(ny, T{}));
dij.assign(nx, vector<T>(ny, T{}));
       }
void add(int x, int y, const T &v) {
    T vi = v * (x + 1);
    T vj = v * (y + 1);
    T vij = v * (x + 1) * (y + 1);
    for (int i = x + 1; i <= nx; i += i & -i) {
        for (int j = y + 1; j <= ny; j += j & -j) {
            d[i - 1][j - 1] = d[i - 1][j - 1] + v;
    }
}</pre>
```

```
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                    }
          }
     void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
          add(rx, ry, v);
add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
     T sum(int x, int y) { // 左閉右開查詢
          T ans{};
          for (int i = x; i > 0; i -= i & -i) {
    for (int j = y; j > 0; j -= j & -j) {
        ans = ans
                    ans = ans  + T(x * y + x + y + 1) * d[i - 1][j - 1];  ans = ans - T(y + 1) * di[i - 1][j - 1];  ans = ans - T(x + 1) * dj[i - 1][j - 1];  ans = ans + dij[i - 1][j - 1]; 
               }
          return ans;
    }
T rangeSum
           (int lx, int ly, int rx, int ry) { // 左閉右開查詢
          return sum(
                (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
    }
}:
3.3 DSU [d41d8c]
struct DSU {
     int n;
     vector < int > boss, siz;
     DSU() {}
     DSU(int n_) { init(n_); }
     void init(int n_) {
          n = n_;
          boss.resize(n);
iota(boss.begin(), boss.end(), 0);
          siz.assign(n, 1);
```

```
int find(int x) {
   if (boss[x] == x) return x;
   return boss[x] = find(boss[x]);
     bool same(int x, int y) {
    return find(x) == find(y);
     bool merge(int x, int y) {
          x = find(x);
y = find(y);
           if (x == y)
                return false;
           if(siz[x] < siz[y]) swap(x, y);
siz[x] += siz[y];
boss[y] = x;</pre>
           n - -;
           return true;
     int size(int x) {
   return siz[find(x)];
     }
};
struct DSU {
     vector < int > boss, siz, stk;
     DSU() {}
DSU(int n_) { init(n_); }
     void init(int n_) {
          n = n_;
boss.resize(n);
           iota(boss.begin(), boss.end(), 0);
           siz.assign(n, 1);
           stk.clear():
     int find(int x) {
   return x == boss[x] ? x : find(boss[x]);
     bool same(int x, int y) {
   return find(x) == find(y);
     bool merge(int x, int y) {
          x = find(x);
y = find(y);
           if(x == y)
                return false;
           if (siz[x] < siz[y]) swap(x, y);</pre>
           siz[x] += siz[y];
boss[y] = x;
           stk.push_back(y);
           return true;
     void undo(int x) {
```

while (stk.size() > x) {

```
int y = stk.back();
    stk.pop_back();
    n++;
    siz[boss[y]] -= siz[y];
    boss[y] = y;
    }
int size(int x) {
    return siz[find(x)];
}
```

3.4 Segment [d41d8c]

```
template <class Info>
struct Seg { // 左閉右開寫法
  int n; vector <Info > info;
  Seg() : n(0) {}
  Seg(int n_, Info v_ = Info()) { init(n_, v_); }
  template <class T>
      Seg(vector<T> init_) { init(init_); }
void init(int n_, Info v_ = Info()) {
  init(vector(n_, v_));
      template <class T>
      void init(vector<T> init_) {
           n = init_.size();
            info[p] = init_[l];
                 int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                 pull(p);
           build(1, 0, n);
      void pull(int p) {
    info[p] = info[p * 2] + info[p * 2 + 1];
      void modify(int p, int l, int r, int x, const Info &v) {
   if (r - l == 1) {
                 info[p] = v; return;
           int m = (l + r) / 2;
if (x < m) modify(2 * p, l, m, x, v);
else modify(2 * p + 1, m, r, x, v);</pre>
           pull(p);
      void modify(int p, const Info &i) {
    modify(1, 0, n, p, i);
      Info query(int ql, int qr) {
    return query(1, 0, n, ql, qr);
      template < class F>
                               // 尋找區間內,第一個符合條件的
      int findFirst
           (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x)</pre>
           return -1;
if (l >= x && r <= y && !pred(info[p]))
                 return -1;
                 return l;
           int m = (l + r) / 2;
int res = findFirst(2 * p, l, m, x, y, pred);
            if (res == -1)
                 res = findFirst(2 * p + 1, m, r, x, y, pred);
           return res;
      template < class F> // 若要找 last,先右子樹遞迴即可int findFirst(int l, int r, F & pred) {
    return findFirst(1, 0, n, l, r, pred);
 // ---define structure and info plus---
 struct Info {
      int n = 0;
      int sum = 0;
 Info operator+(const Info &a, const Info &b) {
      return { a.n + b.n, a.sum + b.sum };
}
```

3.5 Lazy Segment [d41d8c]

```
| template <class Info, class Tag>
| struct LazySeg { // 左閉右開寫法
| int n;
| vector<Info> info;
```

```
vector <Tag> tag;
LazySeg() : n(0) {}
LazySeg(int n_, Info v_ = Info()) {
      init(n_, v_);
                                                                                                            }
template <class T>
LazySeg(vector<T> init_) {
   init(init_);
void init(int n_, Info v_ = Info()) {
   init(vector(n_, v_));
femplate <class T>
void init (vector<T> init_) {
    n = init_.size();
    info.assign(4 << __lg(n), Info());
    tag.assign(4 << __lg(n), Tag());
    function <void(</pre>
       function <void(
   int, int, int)> build = [&](int p, int l, int r) {
   if (r - l == 1) {
      info[p] = init_[l];
}
                                                                                                                   else {
                                                                                                            }
                                                                                                      };
             int m = (l + r) / 2;
build(p * 2, l, m);
build(p * 2 + 1, m, r);
                                                                                                      struct Info {
                                                                                                             int sum;
             pull(p);
       build(1, 0, n);
void pull
        (int p) { info[p] = info[p * 2] + info[p * 2 + 1]; }
void apply(int p, int l, int r, const Tag &v) {
  info[p].apply(l, r, v);
  tag[p].apply(v);
                                                                                                            //
//
// }
void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(p * 2, l, m, tag[p]);
      apply(p * 2 + 1, m, r, tag[p]);
}
                                                                                                      }
       tag[p] = Tag();
                                                                                                      struct Treap {
void modify(int p, int l, int r, int x, const Info &v) {
       if (r - l == 1) {
    info[p] = v;
            return;
       int m = (l + r) / 2;
push(p, l, r);
if (x < m) {</pre>
             modify(2 * p, l, m, x, v);
             modify(2 * p + 1, m, r, x, v);
       pull(p);
void modify(int p, const Info &i) {
       modify(1, 0, n, p, i);
info query(int p, int l, int r, int ql, int qr) {
    if (qr <= l || ql >= r) return Info();
    if (ql <= l && r <= qr) return info[p];</pre>
       int m = (l + r) / 2;
push(p, l, r);
       return query(p *
2, l, m, ql, qr) + query(p * 2 + 1, m, r, ql, qr);
Info query
       (int ql, int qr) { return query(1, 0, n, ql, qr); }
void range_apply
                                                                                                                   push();
       (int p, int l, int r, int ql, int qr, const Tag &v) {
if (qr <= l || ql >= r) return;
if (ql <= l && r <= qr) {</pre>
             apply(p, l, r, v);
             return:
                                                                                                            }
      int m = (l + r) / 2;
push(p, l, r);
range_apply(p * 2, l, m, ql, qr, v);
range_apply(p * 2 + 1, m, r, ql, qr, v);
       pull(p);
void range_apply(int l, int r, const Tag &v) {
   range_apply(1, 0, n, l, r, v);
template < class F> // 尋找區間內,第一個符合條件的
int findFirst
       (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) {</pre>
             return 1:
                                                                                                            }
       if (l >= x && r <= y && !pred(info[p])) {</pre>
             return -1;
       if (r - l == 1) {
             return l;
                                                                                                             t->push();
       int m = (l + r) / 2;
       push(p);
       int res = findFirst(2 * p, l, m, x, y, pred);
```

```
if (res == -1) {
                res = findFirst(2 * p + 1, m, r, x, y, pred);
           return res:
     template < class F> // 若要找 last , 先右子樹遞廻即可
int findFirst(int l, int r, F & pred) {
return findFirst(1, 0, n, l, r, pred);
};
// ---define structure and info plus---
struct Tag { // 有些 Tag 不用 push 例如 sweepLine int set_val; int add;
     void apply(const Tag& v) {
   if (v.set_val) {
                set_val = v.set_val;
                add = v.add;
                add += v.add;
     void apply(int l, int r, const Tag &v) {
    if (v.set_val) {
        sum = (r - l) * v.set_val;
    }
}
           sum += (r - l) * v.add;
     // Info& operator=(const Info &rhs) {
             // 部分 assignment 使用 return *this;
Info operator+(const Info &a, const Info &b) {
     return { a.sum + b.sum };
3.6 Treap [d41d8c]
```

```
Treap *lc, *rc;
int pri, siz; bool rev_valid;
int val; int min;
       Treap(int val_) {
    min = val = val_;
    pri = rand();
             lc = rc = nullptr;
             siz = 1; rev_valid = 0;
       void pull() { // update siz or other information
             siz = 1;
min = val;
             for (auto c : {lc, rc}) {
    if (!c) continue;
                   siz += c->siz;
                   min = std::min(min, c->min);
       void push() {
   if (rev_valid) {
                    swap(lc, rc);
if (lc) lc->rev_valid ^= 1;
if (rc) rc->rev_valid ^= 1;
             rev_valid = false;
       int find(int k) { // 找到 min 是 k 的位置 (1-based)
             int ls = (lc ? lc->siz : 0) + 1;
             if (val == k) return ls;
if (lc && lc->min == k) return lc->find(k);
else return rc->find(k) + ls;
int size(Treap *t) {
    return t ? t->siz : 0;
Treap *merge(Treap *a, Treap *b) {
      p ^mer ye(||eap = a, ||reap = b, |
if (|a || !b) return a ? a : b;
a->push(); b->push();
if (a->pri > b->pri) {
    a->rc = merge(a->rc, b);
}
             a->pull();
             return à;
      else {
    b->lc = merge(a, b->lc);
             b->pull();
pair<Treap*, Treap*> split(Treap *t, int k) {
    // 分割前 k 個在 first, 剩下的在 second
    if (t == nullptr) return {nullptr, nullptr};
       if (size(t->lc) < k) {
             auto [a, b] = split(t->rc, k - size(t->lc) - 1);
t->rc = a;
```

```
t->pull();
    return {t, b};
}
else {
    auto [a, b] = split(t->lc, k);
    t->lc = b;
    t->pull();
    return {a, t};
}

void Print(Treap *t) {
    if (!t) return;
    t->push();
    Print(t->lc);
    cout << t->val;
    Print(t->rc);
}

3.7 MO [d41d8c]

struct query {
    int l. r. id;
```

4 Flow

4.1 Dinic [aa12d4]

```
template < class T>
struct Dinic {
       struct Edge {
   int to;
                T flow, cap; // 流量跟容量
       int n, m, s, t;
const T INF_FlOW = 1 << 30;
vector<vector<int>> adj; // 此點對應的 edges 編號
        vector<Edge> edges; // 幫每個 edge 編號
       vector < tage> edges; // 吊時间 edg.
vector < int> dis, ptr;
Dinic(int n_ = 0) { init(n_); }
void init(int n_) {
    n = n_; m = 0;
    dis.resize(n); ptr.resize(n);
    adj.assign(n, vector < int>{});
    edges.clear();
       yoid add_edge(int u, int v, T cap) {
    // 偶數 id 是正向邊
    edges.push_back({ v, 0, cap });
    edges.push_back({ u, 0, 0 });
                adj[u].push_back(m++);
adj[v].push_back(m++);
        bool bfs() {
                fill(dis.begin(), dis.end(), -1);
dis[s] = 0; queue<int> q;
                q.push(s);
                 while (!q.empty() && dis[t] == -1) {
                        int u = q.front(); q.pop();
for (int id : adj[u]) {
    Edge &e = edges[id];
                                 if (e.flow == e.cap) continue;
if (dis[e.to] == -1) {
                                          dis[e.to] = dis[u] + 1;
                                          q.push(e.to);
                                }
                        }
                 return dis[t] != -1;
       J dfs(int u, T flow) {
   if (flow == 0) return 0;
   if (u == t) return flow;
                 for (int
                        &cur = ptr[u]; cur < (int)adj[u].size(); cur++) {
Edge & e = edges[adj[u][cur]];
if (dis[u] + 1 != dis[e.to]) continue;
if (e.cap == e.flow) continue;
T mn = dfs(e.to, min(flow, e.cap - e.flow));</pre>
                         if (mn > 0) {
                                 e.flow += mn:
```

4.2 Min Cut [44ae6c]

```
|// CSES Police Chase
  int main(){
           int n, m; cin >> n >> m;
Dinic<int> g(n);
for (int i = 0; i < m; i++) {
   int u, v, cap = 1;</pre>
                     cin >> u >> v;
                     u--; v--;
                     g.add_edge(u, v, cap);
                     g.add_edge(v, u, cap);
            int res = g.work(0, n - 1);
cout << res << "\n";
            if (res == 0) return;
            vector<int> vis(n);
           vector < int > vis(n);
auto find = [&](auto self, int u) -> void {
    if (!vis[u]) {
        vis[u] = 1;
        for (int id : g.adj[u]) {
            auto e = g.edges[id];
            if (e.cap - e.flow > 0) {
                  self(self, e.to);
            }
}
                              }
                    }
          };
find(find, 0);
for (int i = 0; i < n; i++) {
    if (!vis[i]) continue;
    for (int id : g.adj[i]) {
        if (id & 1) continue;
        auto e = g.edges[id];
        if (!vis[e.to]) {</pre>
                               if (!vis[e.to]) {
                                        cout << i + 1 << " " << e.to + 1 << "\n";
                    }
          }
```

4.3 MCMF [77fc99]

```
template < class Tf. class Tc>
struct MCMF {
      struct Edge {
            int to;
            Tf flow, cap; // 流量跟容量
            Tc cost:
     // 可以只用 spfa 或 dijkstra, 把跟 pot 有關的拿掉就好
int n, m, s, t;
const Tf INF_FLOW = 1 << 30;
const Tc INF_COST = 1 << 30;
vector<vector<int>>> adj;
      vector<Edge> edges; // 幫每個 edge 編號
vector<Tc> dis, pot; // johnson algorithm, using spfa
      vector<int> rt; // 路徑恢復, 對應 id
      vector<bool> inq;
      MCMF(int n_ = 0) { init(n_); }
      void init(int n_) {
    n = n_; m = 0;
    edges.clear();
            adj.assign(n, vector<int>{});
      void add_edge(int u, int v, Tf cap, Tc cost){
  edges.push_back({v, 0, cap, cost});
  edges.push_back({u, 0, 0, -cost});
  adj[u].push_back(m++);
            adj[v].push_back(m++);
      bool spfa() {
            dis.assign(n, INF_COST);
rt.assign(n, -1); inq.assign(n, false);
            queue<int> q;
q.push(s), dis[s] = 0, inq[s] = true;
            while (!q.empty()) {
```

```
int u = q.front(); q.pop();
inq[u] = false;
for (int id : adj[u]) {
    auto [v, flow, cap, cost] = edges[id];
    Tc ndis = dis[u] + cost + pot[u] - pot[v];
    if (flow < cap && dis[v] > ndis) {
        dis[v] = ndis; rt[v] = id;
        if (!inq[v]) {
            q.push(v); inq[v] = true;
        }
}
                                              }
                                    }
                           }
                  return dis[t] != INF_COST;
         vector<pair<Tc, int>>, greater<pair<Tc, int>>>
dis[s] = 0; pq.emplace(dis[s], s);
while (!pq.empty()) {
    auto [d, u] = pq.top(); pq.pop();
    if (dis[u] < d) continue;
    for (int id : adj[u]) {
        auto [v, flow, cap, cost] = edges[id];
        Tc ndis = dis[u] + cost + pot[u] - pot[v];
        if (flow < cap && dis[v] > ndis) {
            dis[v] = ndis; rt[v] = id;
            pa emplace(ddis v):
                                              pq.emplace(ndis, v);
                                     }
                           }
                   return dis[t] != INF_COST;
         }
        // 限定 flow, 最小化 cost
pair<ff, Tc> work_flow(int s_, int t_, Tf need) {
    s = s_, t = t_; pot.assign(n, 0);
    Tf flow{}; Tc cost{}; bool fr = true;
    while ((fr ? spfa() : dijkstra())) {
        for (int i = 0; i < n; i++) {
            dis[i] += pot[i] - pot[s];
        }
                            If f = INF_FLOW;
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                              (f, edges[rt[i]].cap - edges[rt[i]].flow);
                            f = min<Tf>(f, need);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
                            flow += f; need -= f;
cost += f * dis[t]; fr = false;
                            swap(dis, pot);
if (need == 0) break;
                   return make pair(flow, cost);
          // 限定 cost, 最大化 flow
         pair < Tf, Tc > work_budget(int s_, int t_, Tc budget) {
                  s = s_, t = t_; pot.assign(n, 0);
If flow{}; Tc cost{}; bool fr = true;
while ((fr ? spfa() : dijkstra())) {
    for (int i = 0; i < n; i++) {
        dis[i] += pot[i] - pot[s];
}</pre>
                            Tf f = INF_FLOW;
                            for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    f = min
                                               (f, edges[rt[i]].cap - edges[rt[i]].flow);
                            f = min<Tf>(f, budget / dis[t]);
for (int i = t; i != s; i = edges[rt[i] ^ 1].to) {
    edges[rt[i]].flow += f;
    edges[rt[i] ^ 1].flow -= f;
}
                            flow += f; budget -= f * dis[t];
cost += f * dis[t]; fr = false;
                            swap(dis, pot);
if (budget == 0 || f == 0) break;
                   return make pair(flow. cost):
          void reset() {
    for (int i = 0; i < m; i++) edges[i].flow = 0;</pre>
         }
};
4.4 Hangarian [cc6b11]
```

```
struct Hangarian { // 0-based
     int n, m; // 最小路徑覆蓋, 二分匹配
     vector < vector < int >> adj;
     vector < int > used, vis;
vector < pair < int, int >> match;
Hangarian(int n = 0, int m = 0) {
          init(n_, m_);
     void init(int n_, int m_) {
          n = n_; m = m_;
```

```
adj.assign(n + m, vector<int>());
         used.assign(n + m,
        vis.assign(n + m, 0);
     void addEdge(int u, int v) {
        adj[u].push_back(n + v)
        adj[n + v].push_back(u);
     vector<pair<int, int>> work() {
        match.clear();
        vis[v] = 1;
                    if (used[v] == -1 || self(self, used[v])) {
                        used[v] = u;
                }
             return false;
         for (int i = 0; i < n; i++) {
             fill(vis.begin(), vis.end(), 0);
            dfs(dfs, i);
         for (int i = n; i < n + m; i++) {
   if (used[i] != -1) {</pre>
                match.emplace_back(used[i], i - n);
        return match:
    }
};
```

4.5 Theorem [d41d8c]

```
// 有向無環圖:
| // 最小不相交路徑覆蓋:
// 最小路徑數 = 頂點數 - 最大匹配數
// 最小相交路徑覆蓋:
// 先用
   Floyd 求傳遞封包,有連邊就建邊,然後再套最小不相交路徑覆蓋
|
|// 二分圖:
|// 最小點覆蓋 = 最大匹配數
// 選出一些點,讓所有邊至少有一個端點在點集中的最少數量
// 最少邊覆蓋: 選出一些邊,讓所有點都覆蓋到的最少數量
// 最少邊覆蓋 = 點數 - 最大匹配數
1// 最大獨立集: 選出一些點, 使這些點兩兩沒有邊連接的最大數量
| // 最大獨立集 = 點數 - 最大匹配數
```

String 5

5.1 Hash [852711]

```
constexpr int B = 59;
vector<Z> Hash(string &s) {
     vector<Z> ans {0};
     for (auto c : s) {
          ans.push_back(ans.back() * B + (c - 'a' + 1));
     return ans;
void solve() {
     string s, sub;
cin >> s >> sub;
     auto a = Hash(s);
     auto q = Hash(sub);
auto find = q.back();
      int ans = 0;
     int l = 1, r = sub.size(), len = sub.size();
while (r <= s.size()) {
    if (a[r] - a[l - 1] * power(Z(B), len) == find) {</pre>
          ĺ++, r++;
     cout << ans << "\n";
```

5.2 KMP [cddfd9]

```
struct KMP {
      string sub;
      vector<int> failure;
      KMP(string sub_) {
  sub = sub_;
  failure.resize(sub.size(), -1);
            buildFailFunction();
      void buildFailFunction() {
    for (int i = 1; i < (int)sub.size(); i++) {</pre>
```

}

string getLCP() {
 int cp = 0, k, lcp = 0, p;
 for (int i = 0; i < n; i++) {</pre>

```
int now = failure[i - 1]:
                                                                                                                   if (!rk[i]) continue:
                  while (now != -1
    && sub[now + 1] != sub[i]) now = failure[now];
if (sub[now + 1] == sub[i]) failure[i] = now + 1;
                                                                                                                   k = sa[rk[i] - 1];
                                                                                                                   if (cp) cp--;
while (s[i + cp] == s[k + cp]) cp++;
if (cp > lcp){
            }
                                                                                                                        lcp = cp;
p = i;
       vector < int > match(string &s) {
            vector<int> match;
                                                                                                                  }
            for (int i = 0, now = -1; i < (int)s.size(); i++) {
   // now is the compare sucessed length -1
   while (s[i] !=</pre>
                                                                                                             if (lcp) {
                                                                                                                   return s.substr(p, lcp);
                  sub[now + 1] && now != -1) now = failure[now];
// failure stores if comparison fail, move to where
if (s[i] == sub[now + 1]) now++;
if (now + 1 == (int)sub.size()) {
                                                                                                             } else {
                                                                                                                   return "-1":
                                                                                                       }
                        match.push_back(i - now);
                                                                                                };
                        now = failure[now];
                                                                                                 5.5 Manacher [9c9ca6]
             return match;
                                                                                                 // 找到對於每個位置的迴文半徑
      }
                                                                                                 vector<int> manacher(string s) {
1:
                                                                                                       string t =
                                                                                                       for (auto c : s) {
 5.3 Z Function [764b31]
                                                                                                            t += c;
t += '#';
| // z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
 // 的最長公共前綴 (LCP) 的長度
                                                                                                       int n = t.size():
 vector<int> Z(string s) {
                                                                                                       vector<int> r(n);
       int n = s.size();
                                                                                                       for (int i = \hat{0}, j = \hat{0}
      int n = s.stze();
vector <int> z(n); z[0] = n;
for (int i = 1, j = 1; i < n; i++) {
    z[i] = max(0, min(j + z[j] - i, z[i - j]));
    while (i + z[i] < n && s[z[i]] == s[i + z[i]])</pre>
                                                                                                             0; i < n; i++) { // i 是中心, j 是最長回文字串中心 if (2 * j - i >= 0 && j + r[j] > i) { r[i] = min(r[2 * j - i], j + r[j] - i);
                  z[i]++;
            if (i + z[i] > j + z[j]) j = i;
                                                                                                                  0 && i + r[i] < n && t[i - r[i]] == t[i + r[i]]) {
r[i] += 1;
      return z; // 最後一格不算
}
                                                                                                             if (i + r[i] > j + r[j]) {
 5.4 SA [d40e3e]
                                                                                                             }
 struct SuffixArray {
                                                                                                       return r;

// # a # b # a #

// 1 2 1 4 1 2 1

// # a # b # b # a #

// 1 2 1 2 5 2 1 2 1
      int n; string s;
vector<int> sa, rk, lc;
       // n: 字串長度
      // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
                                                                                                       // 值 -1 代表原回文字串長度
       // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名
       // lc: LCP
                                                                                                       // (id - val + 1) / 2 可得原字串回文開頭
       數組, lc[i] 表示 sa[i] 和 sa[i + 1] 的最長公共前綴長度
SuffixArray(const string &s_) {
                                                                                                 5.6 SAM [d15619]
            s = s_; n = s.length();
sa.resize(n);
             lc.resize(n - 1);
                                                                                                 struct SAM {
                                                                                                       static constexpr int ALPHABET_SIZE = 26;
struct Node {
             rk.resize(n);
             iota(sa.begin(), sa.end(), 0);
            rtota(sa.begin(), sa.en(), 0),
sort(sa.begin(), sa.
    end(), [&](int a, int b) { return s[a] < s[b]; });
rk[sa[0]] = 0;
for (int i = 1; i < n; ++i)
    rk[sa[i]]</pre>
                                                                                                             int len;
                                                                                                             int link;
                                                                                                             array<int, ALPHABET_SIZE> next;
Node() : len{}, link{}, next{} {}
                           = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
                                                                                                       vector < Node > t;
             int k = 1:
                                                                                                       SAM() { init(); }
void init() {
             vector<int> tmp, cnt(n);
            tmp.reserve(n);
while (rk[sa[n - 1]] < n - 1) {</pre>
                                                                                                             t.assign(2, Node());
t[0].next.fill(1);
t[0].len = -1;
                  int newNode() {
    t.emplace_back();
    return t.size() -
                  for (auto i : sa)
    if (i >= k)
                              tmp.push_back(i - k);
                  fill(cnt.begin(), cnt.end(), 0);
for (int i = 0; i < n; ++i)
                                                                                                       int extend(int p, int c) {
                                                                                                             if (t[p].next[c]) {
                  ror (int i = 0; i < n; ++i)
    ++cnt[rk[i]];
for (int i = 1; i < n; ++i)
    cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; --i)
    sa[--cnt[rk[tmp[i]]]] = tmp[i];
                                                                                                                   int q = t[p].next[c];
if (t[q].len == t[p].len + 1) {
                                                                                                                        return q;
                                                                                                                   int r = newNode();
                                                                                                                   t[r].len = t[p].len + 1;
t[r].link = t[q].link;
                  swap(rk, tmp);
                                                                                                                   t[r].next = t[q].next;
                                                                                                                   t[q].link = r;
while (t[p].next[c] == q) {
                                                                                                                        t[p].next[c] = r;
p = t[p].link;
             for (int i = 0, j = 0; i < n; ++i) {
    if (rk[i] == 0) {</pre>
                                                                                                                   return r;
                                                                                                             int cur = newNode():
                        i = 0:
                                                                                                             t[cur].len = t[p].len + 1;
while (!t[p].next[c]) {
                  } else {
                        for (j
                               -= j > 0; i + j < n && sa[rk[i] - 1] + j
< n && s[i + j] == s[sa[rk[i] - 1] + j]; )
                                                                                                                  t[p].next[c] = cur;
p = t[p].link;
                        lc[rk[i] - 1] = j;
                                                                                                             t[cur].link = extend(p, c);
                  }
                                                                                                             return cur;
```

};

void solve() {
 string s; cin >> s;

int n = s.length();

```
vector < int > pos(n + 1); // s[i - 1] 的後綴終點位置
     pos[0] = 1;
    for (int i = 0; i < n; i++) {
   pos[i + 1] = sam.extend(pos[i], s[i] - 'a');</pre>
}
5.7 Trie [3b3aa0]
struct Trie {
    struct trie node {
```

```
bool is_word;
          vector<trie_node *> children;
          trie_node() {
    is_word = false;
              children.resize(26, NULL);
         }
     trie_node *root = new trie_node();
    void insert(string &s) {
    trie_node *cur = root;
         for (int i = 0; i < s.size(); i++) {</pre>
              int idx = s[i] - 'a';
if (cur->children[idx] == NULL) {
                   cur->children[idx] = new trie_node();
              cur = cur->children[idx]:
          cur->is_word = true;
    bool is_in_trie(string &s) {
         trie_node *cur = root;
for (int i = 0; i < s.size(); i++) {
    if (cur->
              children[s[i] - 'a'] == nullptr) return false;
cur = cur->children[s[i] - 'a'];
         return true;
    }
int search_i_start(string &s, int i, vector<int> &dp) {
    trie_node *cur = root;
         int sz = s.size(), ans = 0;
for (int j = i; j < sz; j++) {
    if (cur
               ->children[s[j] - 'a'] == nullptr) return ans;
cur = cur->children[s[j] - 'a'];
              if (cur->is_word)
     (ans += dp[j + 1]) %= mod;
          return ans;
    }
int main() {
    // 找到 sub 集合裡,可以重複用,組成 s 的組數 Trie trie;
    string s; cin >> s;
int sz = s.size();
     // dp 代表 i 開頭到最後的配對總數
     // 找到有結尾為 stop 的 dp[i] += dp[j + 1]
    dp[sz] = 1;
    for (int i = sz - 1; i >= 0; i--) {
          dp[i] = trie.search_i_start(s, i, dp);
```

5.8 Duval [f9dcca]

cout << dp[0] << endl;

```
// duval_algorithm
// 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
// 將子甲分解放右十個非嚴格應減的非嚴格:
vector<string> duval(string s) {
   int i = 0, n = s.size();
   vector<string> res;
   while (i < n) {
      int k = i, j = i + 1;
      while (s[k] <= s[j] && j < n) {
        if (s[k] < s[j]) k = i;
        else
                      else k++;
               while (i <= k) {</pre>
                       res.push_back(s.substr(i, j - k));
                      i += j - k;
               }
       return res;
// 最小旋轉字串
string min_round(string s) {
      int i = 0, n = s.size();
int start = i;
while (i < n / 2) {</pre>
              start = i;
```

```
int k = i, j = i + 1;
while (s[k] <= s[j] && j < n) {
   if (s[k] < s[j]) k = i;</pre>
               else k++:
       while (i <= k) {
    i += j - k;</pre>
return s.substr(start. n / 2):
```

Math 6

6.1 Prime [4e0864]

```
// a^(m-1) = 1 (mod m)

// a^(m-2) = 1/a (mod m)

// EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)

// Filter + DP; DP save min factor 'recur' factor decomposition

// FacNums = (x+1)(y+1)(z+1)...

// FacSum = (a^0+a^1...+a^x)(b^0+...+b^y)

// FacMul = N(x+1)(y+1)(z+1)/2
vector<int> is_prime;
// 1 代表是質數,非 1 不是
void init(int n) {
       is_prime.assign(n + 1,
       }
int main() {
        init(1000000);
       ll ans = 1, q; cin >> q;
map<ll, ll> mp;
while (is_prime[q] != 1) {
             mp[is_prime[q]]++;
              q /= is_prime[q];
        if (q != 1) mp[q]++;
       for (auto [a, b] : mp) ans *= b + 1;
cout << ans << "\n";</pre>
```

6.2 Modulo [a1aab8]

```
template < class T>
constexpr T power(T a, ll b) {
   T res {1};
      for (; b; b /= 2, a *= a)

if (b % 2) res *= a;
constexpr ll mul(ll a, ll b, ll p) {
    ll res = a * b - ll(1.L * a * b / p) * p;
      res %= p;
if (res < 0) res += p;
template < ll P >
struct MInt {
      ll x;
      constexpr MInt() : x {0} {}
constexpr MInt(ll x) : x {norm(x % getMod())} {}
static ll Mod;
      constexpr static ll getMod() {
   if (P > 0) return P;
   else return Mod;
      constexpr static void setMod(ll Mod_) {
    Mod = Mod_;
      constexpr ll norm(ll x) const {
           if (x < 0) x += getMod();
if (x >= getMod()) x -= getMod();
            return x;
      constexpr ll val() const { return x; }
      constexpr MInt operator-() const {
           MInt res;
res.x = norm(getMod() - x);
return res;
      constexpr MInt inv() const {
   return power(*this, getMod() - 2);
      constexpr MInt &operator*=(MInt rhs) & {
  if (getMod() < (1ULL << 31)) {</pre>
                 x = x * rhs.x % int(getMod());
           } else {
    x = mul(x, rhs.x, getMod());
            return *this:
      constexpr MInt &operator+=(MInt rhs) & {
           x = norm(x + rhs.x);
```

```
return *this:
      constexpr MInt &operator -= (MInt rhs) & {
           x = norm(x - rhs.x);
return *this;
     constexpr MInt &operator/=(MInt rhs) & {
    return *this *= rhs.inv();
     friend constexpr MInt operator*(MInt lhs, MInt rhs) {
   MInt res = lhs; return res *= rhs;
     friend constexpr MInt operator+(MInt lhs, MInt rhs) {
   MInt res = lhs; return res += rhs;
      friend constexpr MInt operator - (MInt lhs, MInt rhs) {
   MInt res = lhs; return res -= rhs;
      friend constexpr MInt operator/(MInt lhs, MInt rhs) {
   MInt res = lhs; return res /= rhs;
      friend constexpr
             std::istream &operator>>(std::istream &is, MInt &a) {
           ll v; is >> v; a = MInt(v); return is;
           ostream &operator <<(std::ostream &os, const MInt &a) {
return os << a.val();</pre>
     friend constexpr bool operator==(MInt lhs, MInt rhs) {
   return lhs.val() == rhs.val();
     friend constexpr bool operator!=(MInt lhs, MInt rhs) {
   return lhs.val() != rhs.val();
      friend constexpr bool operator<(MInt lhs, MInt rhs) {
  return lhs.val() < rhs.val();</pre>
     }
template<>
ll MInt<0>::Mod = 998244353;
constexpr int P = 1e9 + 7;
using Z = MInt<P>;
```

6.3 Combination [878efe]

6.4 CRT [d41d8c]

```
ll exgcd(ll a, ll b, ll &x, ll &y) {
    if (!b) {
        x = 1, y = 0;
        return a;
    }
    ll g = exgcd(b, a % b, y, x);
    y -= a / b * x;
    return g;
}
ll inv(ll x, ll m){
    ll a, b;
    exgcd(x, m, a, b);
```

```
a %= m;
   if (a < 0) a += m;
    return a;
}
// remain, mod
ll CRT(vector pair < ll, ll >> &a) {
        ll prod = 1;
        for (auto x : a) {
            prod *= x.second;
        }
        ll res = 0;
        for (auto x : a) {
            auto t = prod / x.second;
            res += x.first * t % prod * inv(t, x.second) % prod;
        if(res >= prod) res -= prod;
    }
    return res;
}
```

6.5 Matrix [08b5fe]

```
template < class T>
struct Mat {
     int m, n;
    constexpr static ll mod = 1e9 + 7;
vector<vector<T>> matrix;
Mat(int n_ = 0) { init(n_, n_); }
Mat(int m_, int n_) { init(m_, n_); }
Mat(vector<vector<T>> matrix_) { init(matrix_); }
     void init(int m_, int n_) {
    m = m_; n = n_;
         matrix.assign(m, vector<T>(n));
     void init(vector<vector<T>> &matrix_) {
        m = matrix_.size();
n = matrix_[0].size();
         matrix = matrix_;
    return res:
     constexpr Mat & operator*=(const Mat& rhs) & {
         assert(matrix[0].size() == rhs.matrix.size());
int m = matrix.size()
              , k = matrix[0].size(), n = rhs.matrix[0].size();
         Mat ans(m, n);
        }
             }
         matrix = ans.matrix;
         return *this;
     constexpr Mat &operator^=(ll p) & {
        matrix = ans.matrix;
return *this;
     friend Mat operator*(Mat lhs, const Mat &rhs) {
         lhs *= rhs;
     friend Mat operator^(Mat lhs, const ll p) {
         lhs ^= p;
return lhs;
    }
};
// fn = fn-3 + fn-2 + fn-1
```

6.6 Integer Partition [595ed2]

```
val %= mod; sum %= mod;
ans += val * sum;
ans %= mod;
}
cout << ans << "\n";
}
```

6.7 Mobius Theorem

- 數論分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1)內計算 f(r)-f(l) 或已經預處理 出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d)g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n}\!\!\mu(d)\!=\!\begin{cases} 1 & \text{for } n\!=\!1\\ 0 & \text{for } n\!\neq\!0 \end{cases}$$

- 2. μ 是常數函數1的反元素
- $\rightarrow \mu * 1 = \epsilon \cdot \epsilon(n)$ 只在n = 1時為 1,其餘情況皆為 0。
- $-\phi$ 歐拉函數: x以下與x互質的數量

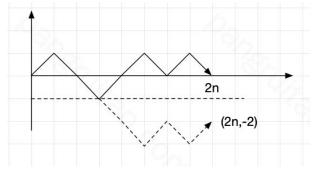
$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^i) \\ &= 1 + p^0(p-1) + p^1(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^c \\ &= id \end{split}$$

- 莫比烏斯反演公式
 - $f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$
 - $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$
- 例子

$$\begin{split} &\sum_{i=aj=c}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \sum_{d|gcd(i,j)} \mu(d) \\ &= \sum_{d=1}^{\infty} \mu(d) \sum_{i=1}^{\left\lfloor \frac{x}{k} \right\rfloor} \left\lfloor \frac{y}{k} \right\rfloor \left\lfloor \frac{y}{k} \right\rfloor \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.8 Mobius Inverse [d41d8c]

6.9 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{1!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2)

假設往上有x個,往下有y個,會有:

$$\begin{cases} x + y = 2n \\ y - x = 2 \end{cases} \Rightarrow \begin{cases} x = n - 1 \\ y = n + 1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.10 Burnside's Lemma

$$|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$$

- G:各種翻轉操作所構成的置換群
- · X/G:本質不同的方案的集合
- X^g : 對於某一種操作 g, 所有方案中, 經過 g 這種翻轉後保持不變的方案的集合
- 集合取絕對值代表集合數

7 Search and Gready

7.1 Binary Search [d41d8c]

```
int main() {
    int l = 1, r = 10;
    // 1 to tar, find tar
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while (l <= r) {
        int m = (l + r) / 2;
        if (check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}</pre>
```

7.2 Ternary Search [d41d8c]

8 Tree

8.1 LCA [601e2d]

8.2 Centroid Decomposition [4a66fb]

```
struct CenDecom {
      int n:
       vector<vector<int>> adj;
       vector < bool > vis;
vector < int > siz;
       CenDecom() {}
CenDecom(int n_) { init(n_); }
       void init(int n_) {
             n = n;
             adj.assign(n, {});
vis.assign(n, false);
siz.assign(n, 1);
       void addEdge(int u, int v) {
   adj[u].push_back(v);
   adj[v].push_back(u);
      if (y == p || vis[y]) continue;
get_siz(dep + 1, y, x);
siz[x] += siz[y];
       int get_cen(int x, int sz, int p = -1) {
    for (int y : adj[x]) {
        if (y == p || vis[y]) continue;
        if (siz[y] * 2 > sz) {
                           return get_cen(y, sz, x);
                    }
              return x;
       void work(int x = 0) {
             get_siz(0, x);
int cen = get_cen(x, siz[x]);
vis[cen] = true;
              // do something
              for (int y : adj[cen]) {
    if (vis[y]) continue;
                    work(y);
};
```

8.3 Tree Flattening [5293b7]

```
int cnt = 0;
auto dfs = [&](auto self, int u, int par) -> void {
    dfnToVal[++cnt] = val[u];
    mp[u].first = cnt;
    for (auto v : tree[u]) {
        if (v == par) continue;
        self(self, v, u);
}
             mp[u].second = cnt;
      dfs(dfs, 1, 0);
       BIT bit(n);
      for (int i = 1; i <= n; i++) {
    bit.modify(mp[i].first, val[i]);
    if (mp[i].first < n) { // root 就不用扣了
                    bit.modify(mp[i].second + 1, -val[i]);
       for (int i = 0; i < q; i++) {
    int op; cin >> op;
             if (op == 1) {
                    int s, x; cin >> s >> x;
int add = x - dfnToVal[mp[s].first];
dfnToVal[mp[s].first] = x;
                    bit.modify(mp[s].first, add);
                    if (mp[s].first < n) { // root 就不用扣了
                           bit.modify(mp[s].second + 1, -add);
              else {
                    int node: cin >> node:
                    cout << bit.query(mp[node].first) << "\n";</pre>
      }
}
```

8.4 Heavy Light Decomposition [ad25b6]

```
int n, cur;
vector<int> siz, top, dep, parent, in, out, seq;
vector<vector<int> adj;
vector < vector < int> > auj;
HLD(int n = 0) { init(n); }
void init(int n = 0) {
    n = n_; cur = 0;
    siz.resize(n); top.resize(n); dep.resize(n);
    parent.resize(n); in.resize(n); out.resize(n);
    resize(n); dep.resize(n); out.resize(n);
      seq.resize(n); adj.assign(n, {});
void addEdge(int u, int v) {
     adj[u].push_back(v);
adj[v].push_back(u);
void work(int root = 0) {
     top[root] = root;
dep[root] = 0;
parent[root] = -1;
      dfs1(root); dfs2(root);
void dfs1(int u) {
     if (parent[u] != -1)
          adj[u].erase(find
                  (adj[u].begin(), adj[u].end(), parent[u]));
      siz[u] = 1;
     for (auto &v : adj[u]) {
    parent[v] = u, dep[v] = dep[u] + 1;
            dfs1(v);
           siz[u] += siz[v];
if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
           } // 讓 adj[u][0] 是重子節點
     }
void dfs2(int u) {
     in[u] = cur++;
     seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
   top[v] = v == adj[u][0] ? top[u] : v;
           dfs2(v):
      out[u] = cur;
int lca(int u, int v) {
      while (top[u] != top[v]) {
           if (dep[top[u]] > dep[top[v]]) {
                 u = parent[top[u]];
           } else {
                 v = parent[top[v]];
      return dep[u] < dep[v] ? u : v;</pre>
int dist(int u, int v) {
      return dep[u] + dep[v] - 2 * dep[lca(u, v)];
return seq[in[u] - dep[u] + d];
```

```
}
bool isAncester(int u, int v) {
    // 判斷 u 是否是 v 的祖先
    return in[u] <= in[v] && in[v] < out[u];
}
int rootedParent(int u, int v) {
    // 根據新根節點 u 計算 v 的父節點
    swap(u, v);
    if (u == v) return u;
    if (!isAncester(u, v)) return parent[u];
    auto it = upper_bound(adj
        [u].begin(), adj[u].end(), v, [&](int x, int y) {
        return in[x] < in[y];
    }) - 1;
    return *it;
}
int rootedSize(int u, int v) {
    // 根據新根節點 u 計算子樹 v 的大小
    if (u == v) return n;
    if (!isAncester(v, u)) return siz[v];
    return n - siz[rootedParent(u, v)];
}
int rootedLca(int a, int b, int c) {
    // 根據新的根節點計算三個節點 a \ b 和 c 的最近公共祖先
    return lca(a, b) ^ lca(b, c) ^ lca(c, a);
}
};
```

8.5 Link Cut Tree [29ae0d]

```
#include <bits/stdc++.h>
using ll = long long;
constexpr int Mod = 51061;
struct Tag {
     ll add = 0;
     ll mul = 1;
     void apply(const Tag& v) {
  mul = mul * v.mul % Mod;
  add = (add * v.mul % Mod + v.add) % Mod;
};
struct Info {
     ll val = 1;
ll sum = 1;
     void apply(int size, const Tag &v) {
   val = (val * v.mul % Mod + v.add) % Mod;
   sum = (sum * v.mul % Mod + v.add * size % Mod) % Mod;
     }
};
struct Node {
   Node *ch[2], *p;
     int rev = 0;
     int size = 1;
     void make rev() {
          swap(ch[0], ch[1]);
          rev ^= 1;
     Node() : ch {nullptr, nullptr}, p(nullptr) {}
     Info info = Info();
Tag tag = Tag();
     void apply(const Tag &v) {
   info.apply(size, v);
           tag.apply(v);
     void push_tag() {
           if (rev) {
   if (ch[0]) ch[0]->make_rev();
   if (ch[1]) ch[1]->make_rev();
           if (ch[0]) {
                ch[0]->apply(tag);
          if (ch[1]) {
    ch[1]->apply(tag);
          tag = Tag();
     void pull_info() {
          };
bool isroot(Node *t) {
     return t->p
             == nullptr \mid | (t->p->ch[0] != t && t->p->ch[1] != t);
int pos(Node *t) { // 回傳 1 代表是右子節點
     return t->p->ch[1] == t;
void rotate(Node *t) {
     Node *q = t -> p;
```

```
int x = !pos(t);
     q->ch[!x] = t->ch[x];
if (t->ch[x]) {
          t->ch[x]->p = q;
     t->p = q->p;
     if (!isroot(q)) {
          q->p->ch[pos(q)] = t;
     t - ch[x] = q;
     a->p =
     q->pull_info();
void splay(Node *t) { // 單點修改前必須呼叫
     // 把 t 旋轉到目前 splay 的根while (!isroot(t)) {
          Node *p = t->p;
p->push_tag();
t->push_tag();
          rotate(t);
     t->push_tag();
     t->pull_info();
void access(Node *t) {
     // 把從根到 t 的所有點都放在一條實鏈裡,使根
     // 到 t 成為一條實路徑,並且在同一棵 splay 裡
for (Node *i = t, *q = nullptr; i; q = i, i = i->p) {
          splay(i);
          i->ch[1] = q;
     splay(t);
}
void makeRoot(Node *t) { // 使 t 點成為其所在樹的根
     access(t);
     swap(t->ch[0], t->ch[1]);
t->rev ^= 1;
Node* findRoot(Node *t) { // 找到 t 的 root
     access(t);
     splay(t);
     t->push_tag();
while (t->ch[0]) {
    t = t->ch[0];
          t->push_tag();
     splay(t);
     return t;
void link(Node *t, Node *p) {
     makeRoot(t);
if (findRoot(p) != t) {
          makeRoot(p);
          t->p = p;
p->pull_info();
     }
}
bool cut(Node *x, Node *y) { // 不存在邊,回傳 false
     makeRoot(x);
     access(y);
     if (y->ch[0] != x || x->ch[1]) return false;
     y->ch[0]->p = nullptr;
y->ch[0] = nullptr;
y->pull_info();
     return true;
void split(Node
       *x, Node *y) { // 以 y 做根, 區間修改用, apply 在 y 上
     makeRoot(x);
     access(y);
     splay(y);
bool isconnected(Node *x, Node *y) { // 查詢有沒有連通
     makeRoot(x);
     access(v);
     return findRoot(x) == findRoot(y);
}
int main() {
     int n; cin >> n;
vector<Node *> nodes(n);
     vector < Node ^> nodes(n);
int q; cin >> q;
for (int i = 0; i < n; i++) {
    nodes[i] = new Node();
    nodes[i] -> info.val = nodes[i] -> info.sum = 1LL;
     for (int i = 0; i < n - 1; i++) {
   int u, v; cin >> u >> v;
          link(nodes[u], nodes[v]);
     for (int i = 0; i < q; i++) {
          char op; cin >> op;
if (op == '+') {
               int u, v; cin >> u >> v;
               split(nodes[u], nodes[v]);
               Tag tag;
cin >> tag.add;
tag.add % Mod;
```

int n, id;

```
vector<vector<int>> adj, radj, bucket;
vector<int> sdom, dom, vis, rev, pa, rt, mn, res;
Dominator_tree(int n_ = 0) { init(n_); }
                      nodes[v]->apply(tag);
               else if (op == '-') {
                                                                                                                              void init(int _n) {
    n = _n, id = 0;
    adj.assign(n, vector <int >());
}
                      int u1, v1; cin >> u1 >> v1;
int u2, v2; cin >> u2 >> v2;
                      u1--; v1--; u2--; v2--
                                                                                                                                     radj.assign(n, vector <int>());
bucket.assign(n, vector <int>());
sdom.resize(n); dom.assign(n, -1)
vis.assign(n, -1); rev.resize(n);
pa.resize(n); rt.resize(n);
mn.resize(n); res.resize(n);
                      cut(nodes[u1], nodes[v1]);
link(nodes[u2], nodes[v2]);
              else if (op == '*') {
   int u, v; cin >> u >> v;
   u--; v--;
                      split(nodes[u], nodes[v]);
                                                                                                                               void add_edge(int u, int v) { adj[u].push_back(v); }
int query(int v, int x) {
   if (rt[v] == v) return x ? -1 : v;
                      Tag tag;
cin >> tag.mul;
tag.mul % Mod;
                                                                                                                                      int p = query(rt[v], 1);
if (p == -1) return x ? rt[v] : mn[v];
if (sdom[mn[v]] > sdom[mn[rt[v]]]) mn[v] = mn[rt[v]];
                      nodes[v]->apply(tag);
              else {
   int u, v; cin >> u >> v;
                                                                                                                                      rt[v] = p;
return x ? p : mn[v];
                      split(nodes[u], nodes[v]);
cout << nodes[v]->info.sum << "\n";</pre>
                                                                                                                               void dfs(int v) {
    vis[v] = id, rev[id] = v;
    rt[id] = mn[id] = sdom[id] = id, id++;
              }
                                                                                                                                      for (int u : adj[v]) {
   if (vis[u] == -1) dfs(u), pa[vis[u]] = vis[v];
   radj[vis[u]].push_back(vis[v]);
       return 0;
}
8.6 Virtual Tree [622e69]
                                                                                                                               void build(int s) {
// 當存在關鍵點且除了關鍵點的根關鍵點的 LCA 都沒用處
                                                                                                                                      dfs(s);
                                                                                                                                      for (int i = id - 1; i >= 0; i--) {
    for (int u : radj[i])
        sdom[i] = min(sdom[i], sdom[query(u, 0)]);
// 可以建立虚樹達成快速樹 DP
// 例如這題是有權樹,跟 vertex 1 隔開的最小成本
int top = -1; vector <int>stk(maxn);
int top = -1; vector<int>stk(maxn);
void insert(int u, vector<vector<int>> &vt) {
    if (top == -1) return stk[++top] = u, void();
    int l = lca(stk[top], u);
    if (l == stk[top]) return stk[++top] = u, void();
    while (dfn[l] < dfn[stk[top - 1]])
        vt[stk[top - 1]].push_back(stk[top]), top--;
    if (stk[top - 1] != l) {</pre>
                                                                                                                                             if (i) bucket[sdom[i]].push_back(i);
                                                                                                                                             for (int u : bucket[i]) {
   int p = query(u, 0);
   dom[u] = sdom[p] == i ? i : p;
                                                                                                                                             if (i) rt[i] = pa[i];
                                                                                                                                      res.assign(n, -1);
for (int i = 1; i < id; i++)
    if (dom[i] != sdom[i]) dom[i] = dom[dom[i]];</pre>
       tr (stk[top - 1] != t) {
   vt[l].push_back(stk[top]);
   stk[top] = l;
} else vt[l].push_back(stk[top--]);
stk[++top] = u;
                                                                                                                                      for (int i = 1; i < id; i++) res[rev[i]] = rev[dom[i]];</pre>
                                                                                                                                      res[s] = s:
                                                                                                                                      for (int i = 0; i < n; i++) dom[i] = res[i];</pre>
void reset(int u, vector<vector<int>> &vt) {
    for (int i : vt[u]) reset(i, vt);
                                                                                                                       };
       vt[u].clear();
                                                                                                                       9
                                                                                                                                 DP
void solve(int n, int q) {
    vector g(n + 1, vector<pair<int, int>>());
       vector vt(n + 1, vector vector vt(n + 1, vector vector vt(n + 1), iskey(n + 1);
for (int i = 0; i < n - 1; i++) {
   int u, v, w; cin >> u >> v >> w;
   g[u].push_back({v, w});
   [u].push_back({v, w});
                                                                                                                       9.1 LCS [5781cf]
                                                                                                                        int main() {
                                                                                                                               int m, n; cin >> m >> n;
string s1, s2; cin >> s1 >> s2;
               g[v].push_back({u, w});
                                                                                                                              build_lca(n, g);
       build_ica(in, g),
build(n, g);
for (int i = 0; i < q; i++) {
   int m; top = -1; cin >> m;
   vector<int> key(m);
   for (int j = 0; j < m; j++) {
      cin >> key[j];
      int puffbaufill = 1;
                                                                                                                                                    dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
                                                                                                                                      }
                      iskey[key[j]] = 1;
                                                                                                                              int length = dp[m][n]; cout << length << "\n";
string s(length, 'c'); // backtracking
while (m >= 1 && n >= 1) {
    if (s1[m - 1] == s2[n - 1]) {
        s[length - 1] = s1[m - 1];
        m--, n--, length--;
}
              key.push_back(1); // 看題目,需要才放
sort(all(key), [&](int a, int b) {
    return dfn[a] < dfn[b];
               for (int x : key) insert(x, vt);
              else {
    if (dp[m - 1][n] > dp[m][n - 1]) m--;
               // DP
               auto dfs = [&](auto self, int u) -> void {
                                                                                                                                      }
                     for (auto v : vt[u]) {
    self(self, v);
                                                                                                                               cout << s << "\n";
                             if (iskey[v]) {
    dp[u] += min_dis[v];
                                    // 砍掉 1 到 v 之間最短的路
                                                                                                                       9.2 LIS [66d09f]
                                                                                                                       int main() {
    int n; cin >> n;
    vector<int> v(n);
    for (int i = 0; i < n; i++) cin >> v[i];
    int dp[n]; vector<int> stk;
                                    dp[u] += min(dp[v], min_dis[v]);
                             iskey[v] = dp[v] = 0;
                      vt[u].clear();
                                                                                                                               stk.push_back(v[0]);
              };
                                                                                                                               dp[0] = 1; int L = 1;
for (int i = 1; i < n; i++) {
    if (v[i] > stk.back()) {
              dfs(dfs, key[0]); // key[0] 一定是 root
cout << dp[key[0]] << "\n";
                                                                                                                                           stk.push_back(v[i]);
dp[i] = ++L;
               iskey[key[0]] = dp[key[0]] = 0;
                                                                                                                                      } else {
8.7 Dominator Tree [baa540]
                                                                                                                                                       = lower_bound(stk.begin(), stk.end(), v[i]);
                                                                                                                                             *it = v[i]; dp[i] = it - stk.begin() + 1;
struct Dominator_tree {
```

int n; cin >> n; vector <E > a(n + 1);
for (int i = 1; i <= n; i++) {</pre> int u, v, w; cin >> u >> v >> w;

```
vector < int > ans; cout << L << "\n";
for (int i = n - 1; i >= 0; i - -) {
    if (dp[i] == L) {
                                                                                                                        a[i] = \{u, v, w, i\};
                                                                                                                  vector<array<ll, 2>> dp(n + 1); // w, time
                   ans.push_back(v[i]), L--;
                                                                                                                  vector<array<int, 2>> rec(n + 1); // 有沒選, 上個是誰
                                                                                                                  vector<array<unt, 2>> rec(n + 1); // 有沒幾, 上個定誰
sort(a.begin(), a.end());
for (int i = 1; i <= n; i++) {
    auto it = --lower_bound(all(a), E({0, a[i].from}),
    [](E x, E y){ return x.to < y.to; });
    int id = it - a.begin(); dp[i] = dp[i - 1];
    ll nw = dp[id][0] + a[i].w;
    ll nt = dp[id][1] + a[i].to - a[i].from;
    if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
        dp[i] = {nw, nt}; rec[i] = {1, id};
    }
}
      reverse(ans.begin(), ans.end());
for (auto i : ans) cout << i << " ";</pre>
9.3 Edit Distance [308023]
int main() {
      string s1, s2; cin >> s1 >> s2;
int n1 = s1.size(), n2 = s2.size();
       // dp[i][j] 為 s1 的前 i 個字元,跟 s2 的前 j 個字元
vector <\int > dp(n2 + 1);
                                                                                                                  vector <int> dp(n2 + 1);
iota(dp.begin(), dp.end(), 0);
for (int i = 1; i <= n1; i++) {
    vector <int> cur(n2 + 1); cur[0] = i;
    for (int j = 1; j <= n2; j++) {
        if (s1[i - 1] == s2[j - 1]) {
            cur[j] = dp[j - 1];
        }
}</pre>
                                                                                                                               ans.push_back(a[i].id);
                                                                                                                               i = rec[i][1];
                                                                                                                        } else i--;
                                                                                                                  }
                   } else {
                                                                                                           9.6 Removal Game [7bb56b]
                          // s1 新增等價於 s2 砍掉
                          // dp[i][j] = min(s2 新增, 修改, s1 新增);
                                                                                                          | // 兩個人比賽,每個人輪流取一個數字且只能是頭尾
                          cur[j]
                                                                                                           int main() {
    int n; cin >> n;
    vector<ll> a(n);
    for (int i = 0; i < n; i++) cin >> a[i];
                                  = min({cur[j - 1], dp[j - 1], dp[j]}) + 1;
                   }
             swap(dp, cur);
                                                                                                                  vector dp(n, vector<ll>(n)); // i 到 j 區間的最大 diff
for (int i = n - 1; i >= 0; i--) {
    dp[i][i] = a[i];
    for (int j = i + 1; j < n; j++)
        dp[i][j] =
      cout << dp[n2] << "\n";
9.4 Bitmask [a626f9]
void hamiltonianPath(){
                                                                                                                                       max(a[i] - dp[i + 1][j], a[j] - dp[i][j - 1]);
      int n, m; cin >> n >> m;
vector adj(n, vector <int >());
for (int i = 0; i < m; i++) {
   int u, v; cin >> u >> v;
   adj[--v].push_back(--u);
}
                                                                                                                  \frac{1}{x} + y = \frac{sum}{x} / x - y = \frac{dp[0][n - 1]}{sum}
cout << (accumulate
                                                                                                                          (a.begin(), a.end(), 0LL) + dp[0][n - 1]) / 2 << "\n";
      // 以...為終點,走過...
vector dp(n, vector<int>(findBit(n)));
dp[0][1] = 1;
                                                                                                           9.7 CHT [5f5c25]
                                                                                                           struct Line {
                                                                                                                  ll m, b;
ll m, b;
Line(ll m = 0, ll b = 0) : m(m), b(b) {}
ll eval(ll x) {
    return m * x + b;
       for (int mask = 1; mask < findBit(n); mask++) {</pre>
             for (int i = 0; i < n; i++) {
   if ((mask & findBit(i)) == 0) continue;
   if (i == n - 1 && mask != findBit(n) - 1) continue;
   int pre_mask = mask ^ findBit(i);</pre>
                                                                                                           }:
                   for (int j : adj[i]) {
   if ((pre_mask & findBit(j)) == 0) continue;
   dp[i][mask
                                                                                                           struct CHT { // 用在查詢單調斜率也單調
                                                                                                                  int n, lptr, rptr; vector<Line> hull;
CHT(int n_ = 0, Line init_ = Line()) {
   init(n_, init_);
                                  ] = (dp[i][mask] + dp[j][pre_mask]) % Mod;
                   }
            }
                                                                                                                  void init(int n_ = 0, Line init_ = Line()) {
   n = n_; hull.resize(n); reset(init_);
      cout << dp[n - 1][findBit(n) - 1] << "\n";</pre>
                                                                                                                  void reset(Line init_ = Line()) {
    lptr = rptr = 0; hull[0] = init_;
     void elevatorRides() {
                                                                                                                  bool pop_front(Line &l1, Line &l2, ll x) {
                                                                                                                        bool pop_back(Line &l1, Line &l2, Line &l3) {
                                                                                                                        // 本題斜率遞減、上凸包
                                                                                                                        // 因此只要 12 跟
                                                                                                                        l3 的 X 交點 <= l1 跟 l3 的 X 交點, l2 就用不到了
return (l3.b - l2.b)
* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
                                                                                                                   void insert(Line L) {
                                                                                                                        } else if (dp[pre_mask
    ][0] + 1 < dp[mask][0] || dp[pre_mask][0]
    + 1 == dp[mask][0] && a[i] < dp[mask][1]) {
    dp[mask][0] = dp[pre_mask][0] + 1;
    dp[mask][1] = a[i];</pre>
                                                                                                                                rptr - -
                                                                                                                        hull[++rptr] = L;
                                                                                                                  }
            }
      cout << dp[findBit(n) - 1][0] << "\n";</pre>
                                                                                                           };
9.5 Projects [0942aa]
                                                                                                            9.8 DNC [61c639]
int main() { // 排程有權重問題,輸出價值最多且時間最少
                                                                                                           constexpr int N = 3e3 + 5;
constexpr ll inf = 4e18;
// dp[k][j] = min(dp[k - 1][i] + cost[i][j])
// cost: (i, j]
ll dp[N][N]; // 1-based
ll get_cost(int l, int r) {}
void DNC(int k, int l, int r, int optl, int optr) {
    if (l > r) return;
struct E {
   int from, to, w, id;
   bool operator < (const E &rhs) {</pre>
             return to == rhs.to ? w > rhs.w : to < rhs.to;</pre>
```

9.9 LiChaoSegmentTree [a6e320]

```
constexpr ll Inf = 4e18;
// dp[i] = min(f[j] * s[i] + dp[j])
// y = m x + b
// y = struct Line {
     ll m, b;
li m, b;
Line(ll m = 0, ll b = Inf) : m(m), b(b) {}
ll eval(ll x) const { return m * x + b; }
struct LiChaoSeg { // 取 max 再變換就好
     int n;
vector < Line > info;
LiChaoSeg(int n_ = 0) { init(n_); }
      void init(int n_ = 0) {
            n = n_;
            info.assign(4 << __lg(n), Line());</pre>
     void update(Line line, int node, int l, int r) {
  int m = (l + r) / 2;
  bool left = line.eval(l) < info[node].eval(l);</pre>
            bool mid = line.eval(m) < info[node].eval(m);</pre>
            if (mid) swap(info[node], line); // 如果新線段比較好
            if (r - l == 1) return;
else if (left != mid) update(line, 2 * node, l, m);
            // 代表左半有交點
            else update(line, 2 * node + 1, m, r);
// 代表如果有交點一定在右半
     void add_line(Line line) { update(line, 1, 0, n); }
ll query(int x, int node, int l, int r) {
   if (r - l == 1) return info[node].eval(x);
   int m = (l + r) / 2;
            if (x < m) return</pre>
                  min(info[node].eval(x), query(x, 2 * node, l, m));
            else return min(
  info[node].eval(x), query(x, 2 * node + 1, m, r));
     il query(int x) { return query(x, 1, 0, n); }
```

9.10 Codeforces Example [7d37ea]

```
// CF 1932 pF
// 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
// 請問在線段不重複的情況下,最多獲得幾分
int main() {
   int n, m;
cin >> n >> m;
   // 記錄每點有幾個線段
    // 再一個紀錄,包含這個點的左界
    cnt[l]++;
       cnt[r + 1]--;
    for (int i = 2; i <= n; i++) {
       cnt[i] += cnt[i - 1];
   for (int i = n; i >= 2; i--) {
    l_side[i - 1] = min(l_side[i - 1], l_side[i]);
   vector<int> dp(n + 1);
   dp[i] += dp[l_side[i] - 1];
       dp[i] = max(dp[i], dp[i - 1]);
    cout << dp[n] << "\n";</pre>
// CF 1935 pC
```

```
| // 給你每個事件的 a, b, 挑事件會把 a 全部加起來
| // 再加上 max(bi) - min(bi)
int main(){
    int n, k, ans = 0; cin >> n >> k;
    vector<pii> v(n + 1);
    for (int i = 1; i <= n; i++) {
        int a, b; cin >> a >> b;
        v[i] = {a, b};
        if (a <= k) ans = 1;
    }
    sort(v.begin() + 1, v.end(), [](pii &a, pii &b) {
        return a.second < b.second;
    }); // 用 bi 來排,考慮第 i 個時可以先扣
    vector<vector vector vecto
```

10 Geometry

10.1 Basic [d41d8c]

```
struct Point {
     T x, y;
Point(const T &x_ = 0, const T &y_ = 0) : x(x_), y(y_) {}
template < class U>
     operator Point<U>() {
         return Point < U > (U(x), U(y));
     Point &operator+=(const Point &p) & {
    x += p.x; y += p.y; return *this;
     Point & operator -= (const Point &p) & {
         x -= p.x; y -= p.y; return *this;
     Point & operator *= (const T & v) & {
    x *= v; y *= v; return *this;
     Point & operator /= (const T & v) & {
          x /= v; y /= v; return *this;
          return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
          return a += b;
     friend Point operator - (Point a, const Point &b) {
          return a -= b;
     friend Point operator*(Point a, const T &b) {
   return a *= b;
     friend Point operator/(Point a, const T &b) {
          return a /= b;
     friend Point operator*(const T &a, Point b) {
   return b *= a;
     friend bool operator==(const Point &a, const Point &b) {
          return a.x == b.x && a.y == b.y;
     friend istream &operator>>(istream &is, Point &p) {
          return is >> p.x >> p.y;
     friend ostream & operator < <(ostream & os, const Point & p) {
    return os << "(" << p.x << ", " << p.y << ")";</pre>
template < class T>
struct Line {
     Point<T>
     Point<T> b;

Line(const Point<T> &a_ = Point<T>()

, const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
template < class T>
T dot(const Point<T> &a, const Point<T> &b) {
     return a.x * b.x + a.y * b.y;
template < class T>
T cross(const Point<T> &a, const Point<T> &b) {
   return a.x * b.y - a.y * b.x;
T square(const Point<T> &p) {
```

```
return dot(p. p):
template < class Ta
double length(const Point<T> &p) {
    return sqrt(double(square(p)));
template < class T>
double length(const Line<T> &l) {
       return length(l.a - l.b);
template < class T>
Point<T> normalize(const Point<T> &p) {
       return p / length(p);
bool parallel(const Line<T> &l1, const Line<T> &l2) {
   return cross(l1.b - l1.a, l2.b - l2.a) == θ;
double distance(const Point<T> &a, const Point<T> &b) {
       return length(a - b);
template < class Ta
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
template <ctass 1>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)
      return distance(p, l.a);
   if (dot(p - l.b, l.a - l.b) < 0)
      return distance(p, l.b);
      return distance(p, l.b);</pre>
       return distancePL(p, l);
template < class T>
Point<T> rotate(const Point<T> &a) {
        return Point(-a.y, a.x);
template < class T>
int sgn(const Point < T > &a) {
       return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
template < class T>
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
   return cross(l.b - l.a, p - l.a) > 0;
template < class T>
Point < T
        template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
       return cross(p - l.a, l.b - l.a) == 0 &&
    min(l.a.x, l.b.x) <= p.x && p.x <= max(l.a.x, l.b.x)
               && min
                       (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
     (const Point<T> &a, const vector<Point<T>> &p) {
       int n = p.size(), t = 0;
for (int i = 0; i < n; i++) {</pre>
               if (pointOnSegment(a, Line(p[i], p[(i + 1) % n]))) {
                      return true;
       for (int i = 0; i < n; i++) {
   auto u = p[i];
   auto v = p[(i + 1) % n];</pre>
               if (u.x < a.
                      x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
t ^= 1;
               if (u.x >= a
                     .x && v.x < a.x && pointOnLineLeft(a, Line(u, v)))
t ^= 1;</pre>
       return t == 1;
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
template < class T>
tuple < int, Point < T>, Point < T>> segmentIntersection
  (const Line < T> & l1, const Line < T> & l2) {
    if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
        return {0, Point < T>(), Point < T>()};
    if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
        return {0, Point < T>(), Point < T>()};
    if (max(l1.a.x, l1.b.x) > min(l2.a.x, l2.b.x))
        return {0, Point < T>(), Point < T>()};
}
       return {0, Point<T>(), Point<T>()};

if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y))
    return {0, Point<T>(), Point<T>()};

if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y))
    return {0, Point<T>(), Point<T>()};

if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
    if (cross(l1.b - l1.a, l2.a - l1.a) != 0) {
        return {0, Point<T>()}
    }
                      return {0, Point<T>(), Point<T>()};
                     auto maxx1 = max(l1.a.x, l1.b.x);
auto minx1 = min(l1.a.x, l1.b.x);
auto maxy1 = max(l1.a.y, l1.b.y);
```

```
auto miny1 = min(l1.a.y, l1.b.y);
auto maxx2 = max(l2.a.x, l2.b.x);
auto minx2 = min(l2.a.x, l2.b.x);
                 auto maxy2 = max(l2.a.y, l2.b.y);
auto maxy2 = min(l2.a.y, l2.b.y);
Point<T> p1(max(minx1, minx2), max(miny1, miny2));
Point<T> p2(min(maxx1, maxx2), min(maxy1, maxy2));
if (!pointOnSegment(p1, l1))
                 swap(p1.y, p2.y);
if (p1 == p2) {
    return {3, p1, p2};
                 } else {
                      return {2, p1, p2};
          }
     return {0, Point<T>(), Point<T>()};
Point p = lineIntersection(l1, l2);
if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
           return {1, p, p};
     } else {
           return {3, p, p};
template < class T>
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
     if (get<0>(segmentIntersection(l1, l2)) != 0)
           return 0.0:
     return min({distancePS(l1.a, l2), distancePS(l1
           .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
template < class T>
bool segmentInPolygon
       (const Line<T> &l, const vector<Point<T>> &p) {
      int n = p.size();
     int n = p.size();
if (!pointInPolygon(l.a, p)) return false;
if (!pointInPolygon(l.b, p)) return false;
for (int i = 0; i < n; i++) {
    auto u = p[i];
}</pre>
           auto v = p[(i + 1) % n];
auto v = p[(i + 2) % n];
auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
if (t == 1) return false;
if (t == 0) continue;
           if (t == 2) {
                 if (pointOnSegment(v, l) && v != l.a && v != l.b)
                       if (cross(v - u, w - v) > 0)
    return false;
                 if (p1 != u && p1 != v) {
    if (pointOnLineLeft(l.a, Line(v, u))
                             || pointOnLineLeft(l.b, Line(v, u)))
                return false;
} else if (p1 == v) {
    if (l.a == v) {
                             if (pointOnLineLeft(u, l)) {
   if (pointOnLineLeft(w, l)
        && pointOnLineLeft(w, Line(u, v)))
                                        return false;
                            } else if (l.b == v) {
                            if (pointOnLineLeft(u, Line(l.b, l.a))) {
   if (pointOnLineLeft(w, Line(l.b, l.a))
        && pointOnLineLeft(w, Line(u, v)))
                                        return false;
                            return false;
                            }
                      }
                }
          }
     return true;
template < class T>
vector<Point<T>> hp(vector<Line<T>> lines) {
     sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
   auto d1 = l1.b - l1.a;
   auto d2 = l2.b - l2.a;
           if (sgn(d1) != sgn(d2))
```

```
return san(d1) == 1
            return cross(d1, d2) > 0;
      deaue < Line < T >> ls:
      deque < Point < T >> ps;
      for (auto l : lines) {
            if (ls.empty()) {
    ls.push_back(l);
            while (!ps.empty() && !pointOnLineLeft(ps.back(), l))
    ps.pop_back(), ls.pop_back();
while (!ps.empty() && !pointOnLineLeft(ps[0], l))
    ps.pop_front(), ls.pop_front();
if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
                  if (dot
                        (l.b - l.a, ls.back().b - ls.back().a) > 0) {
if (!pointOnLineLeft(ls.back().a, l)) {
                               assert(ls.size() == 1);
                              ls[0] = l;
                        continue;
                  return {}:
            ps.push_back(lineIntersection(ls.back(), l));
            ls.push_back(l);
      while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0]))
      ps.pop_back(), ls.pop_back();
if (ls.size() <= 2) return {};</pre>
      ps.push_back(lineIntersection(ls[0], ls.back()));
      return vector(ps.begin(), ps.end());
}
using P = Point<ll>;
```

10.2 Convex Hull [b5758d]

```
int main() {
     int n; cin >> n;
     vector <P> P(n), U, L;
for (int i = 0; i < n; i++) {
           cin >> P[i];
     sort(P.begin()
           .end(), [](const Point<i64> &a, const Point<i64> &b) {
return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
     for (int i = 0; i < n; i++) {
    while (L.size() >= 2 && cross(L.back() -
        L[L.size() - 2], P[i] - L[L.size() - 2]) <= 0LL) {</pre>
                 L.pop_back();
           U.pop_back();
           if (L.
                  empty() || !(L.back() == P[i])) L.push_back(P[i]);
           if (U.
                  empty() || !(U.back() == P[i])) U.push_back(P[i]);
     if (L.size() <= 2 && U.size() <= 2) {
           // No Hull
     cout << L.size() + U.size() - 2 << "|n";
for (int i = 0; i < L.size() - 1; i++) {
    cout << L[i].x << " " << L[i].y << "|n";</pre>
     for (int i = U.size() - 1; i > 0; i--) {
   cout << U[i].x << " " << U[i].y << "\n";</pre>
```

10.3 MinEuclidean Distance [3020bc]

```
template < class T>
T distanceSquare(const Point<T> &a, const Point<T> &b) {
    return square(a - b);
void solve() {
    int n; cin >> n;
constexpr ll inf = 8e18;
vector<Point<ll>> a(n);
     for (int i = 0; i < n; i++) {
         il x, y;
cin >> x >> y;
a[i] = Point<ll>(x, y);
     struct sortY {
               ()(const Point<ll> &a, const Point<ll> &b) const {
               return a.y < b.y;</pre>
         }
     struct sortXY {
          bool operator
                ()(const Point<ll> &a, const Point<ll> &b) const {
               if (a.x == b.x) return a.y < b.y;
else return a.x < b.x;</pre>
         }
    };
```

```
sort(a.begin(), a.end(), sortXY());
vector<Point<ll>> t(n);
auto devide = [&](auto &&self, int l, int r) -> ll {
   if (l == r) return inf;
   int m = (l + r) / 2;
    ll ans = min(self(self, l, m), self(self, m + 1, r));
    ll midval = a[m].x;
    sort(t.begin(), t.begin() + p, sortY());
for (int i = 0; i < p; i++){
    for (int j = i + 1; j < p; j++) {</pre>
              ans = min(ans, distanceSquare(t[i], t[j]));
              if ((t[i].y
                      t[j].y) * (t[i].y - t[j].y) > ans) break;
         }
cout << devide(devide. 0. n - 1) << "\n":
```

10.4 LatticePoints [00db9d]

```
int main() {
       // Polygun 內整數點數
       int n; cin >> n;
vector<Point<ll>> polygon(n);
       for (int i = 0; i < n; i++) cin >> polygon[i];
       ll area = 0:
       for (int i = 0; i < n; i++) {
    area += cross(polygon[i], polygon[(i + 1) % n]);</pre>
       area = abs(area);
       auto countBoundaryPoints
               = [](const vector<Point<ll>>& polygon) -> ll {
            ll res = 0;
             int n = polygon.size();
            for (int i = 0; i < n; i++) {
    ll dx = polygon[(i + 1) % n].x - polygon[i].x;
    ll dy = polygon[(i + 1) % n].y - polygon[i].y;</pre>
                  res += std::gcd(abs(dx), abs(dy));
            return res;
       Il res = countBoundaryPoints(polygon);
       ll ans = (area - res + 2) / 2;
cout << ans << " " << res << " \n";</pre>
```

10.5 MinCoverCircle [c9ca81]

```
template < class T >
pair < T , Point < T >> MinCircular (vector < Point < T >> &a) {
     random_shuffle(a.begin(), a.end());
int n = a.size();
     for (int i = 1; i < n; i++) {
   if (T(length(c - a[i]) - r) > 0.0) {
               p + rotate(a[j] - a[i])), Line
  (q, q + rotate(a[k] - a[j])));
r = length(c - a[i]);
                               }
                          }
                     }
               }
          }
     return make_pair(r, c);
}
```