

Team notebook

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October 17, 2023

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1 Attention

```
// Construct VScode
// 1. install vscode & msys2, check desktop path of vscode
// 2. open mingw64, not ucrt64, "pacman -S --needed
    base-devel mingw-w64-x86_64-toolchain"
// 3. add C:\\msys64\\mingw64\\bin to environment path
// 4. (re)open vscode, install C/C++, run, choose g++
// 5. open settings -> compiler -> add compilerPath
    "C:\\msys64\\mingw64\\bin\\g++.exe"

// Make Codebook
// notebook-generator ./ --author "Salmon" --initials
    Salmon --columns 3 --output "CodeBook.pdf" --size 8

// Init
#include <bits/stdc++.h>
using namespace std;
#define all(x) (x).begin(), (x).end()
#define endl "\n"
#define lrep(i, st, n) for(int i = st; i < n; i++)
#define rep(i, st, n) for(int i = st; i <= n; i++)
#define sz size()
#define pb(x) push_back(x)
#define ppb pop_back()
```

```
#define IO ios_base::sync_with_stdio(0); cin.tie(nullptr);
#define init(x, k) memset(x, k, sizeof(x));
#define vec_init(x, k) x.assign(x.size(), k);
#define lc 2*now
#define rc 2*now+1
#define mid (L+R)/2
typedef long long int ll;
typedef pair<int, int> pii;
typedef vector<int> vi;
typedef vector<pii> vii;
typedef pair<ll, ll> pll;
typedef vector<ll> vl;
typedef vector<pll> vll;
typedef struct {
    int from; int to;
    ll weight;
} edge;
typedef struct {
    ll sum;
} Node;
const ll llinf = 1e18;
const int inf = 1e9;
const int MOD = 1e9+7;
const int maxn = 2e5+5;

void solve(){
}

int main(){
    IO;
    int t = 1;
    cin >> t;
    while(t--){
        solve();
    }
}
```

2 DP

2.1 Bag

```
int dp[1005][100005];
vector<int> Page(1005, 0);
vector<int> Price(1005, 0);
int main(){
```

```

int n, bud;
cin >> n >> bud;
for(int i = 1; i <= n; i++){
    int tmp; cin >> tmp;
    Price[i] = tmp;
}
for(int i = 1; i <= n; i++){
    int tmp; cin >> tmp;
    Page[i] = tmp;
}
memset(dp, 0, sizeof(dp));
for(int i = 1; i <= n; i++){
    for(int j = 1; j <= bud; j++){
        if(j >= Price[i]){
            dp[i][j] = max(dp[i-1][j],
                           dp[i-1][j-Price[i]]+Page[i]);
        }
        else {
            dp[i][j] = dp[i-1][j];
        }
    }
}
cout << dp[n][bud] << endl;
}

```

2.2 Bitmask DP

```

// Bit_Mask_DP, Travel Exactly Once
int dp[(1 << 20) - 1][20];
vector<int> rev_adj[20];
int n, m;
const int mod = 1e9 + 7;
void solve(){
    cin >> n >> m;
    rep(i, 1, m){
        int u, v; cin >> u >> v;
        rev_adj[--v].push_back(--u);
    }
    dp[1][0] = 1;
    lrep(road, 1 << 1, 1 << n){
        // Not include 1
        if(road & 1 == 0) continue;
        // include n but not all walked
        if(road & (1 << (n - 1)) && road != ((1 << n) - 1))
            continue;
        // DP
        for (int end = 0; end < n; end++) {
            // Not include end
            if ((road & (1 << end)) == 0)
                continue;
            // exclude end point is last road
            int pre_road = road - (1 << end);
            for (int pre_road_end : rev_adj[end])
                // pre_road_end is prev's end
                if ((road & (1 <<
                    pre_road_end))) {
                    dp[road][end] +=
                        dp[pre_road][pre_road_end];
                }
            }
        }
    }
}

```

```

dp[road][end] %= mod;
    }
}
cout << dp[(1 << n) - 1][n - 1];
// elevator rides
for(int i = 1; i < 1 << n; i++){
    used[i] = dp[i] = inf;
    for(int j = 0; j < n; j++){
        if(i & (1 << j)){ // j
            int last = i ^ (1 << j);
            if(used[last] + s[j] <= x){
                if(dp[last] < dp[i] || dp[last] ==
                    dp[i] && used[last] + s[j] < used[i]){
                    used[i] = used[last] + s[j];
                    dp[i] = dp[last];
                }
            }
            else {
                if(dp[last] + 1 < dp[i] || dp[last] +
                    1 == dp[i] && s[j] < used[i]){
                    used[i] = s[j];
                    dp[i] = dp[last] + 1;
                }
            }
        }
    }
}
// cout << dp[(1 << n) - 1];
}

```

2.3 Coin

```

// combine
// arrange: nested loop exchange
ll dp[2][1000001];
void solve(){
    int n, x; cin >> n >> x;
    vector<int> coin(n + 1);
    rep(i, 1, n){
        cin >> coin[i];
    }
    init(dp[0], 0);
    dp[0][0] = 1;
    rep(i, 1, n){
        rep(j, 0, x){
            dp[i & 1][j] = dp[(i & 1) ^ 1][j];
            if(j >= coin[i]){
                (dp[i & 1][j] += dp[(i & 1) ^ 1][j - coin[i]]) %=
                    MOD;
            }
        }
    }
    cout << dp[n & 1][x];
}
// Minimize coins nums
void solve(){
    int n, x; cin >> n >> x;
}

```

```

vector<int> coin(n);
lrep(i, 0, n){
    cin >> coin[i];
}
ll dp[x+1]; // init(dp, 0);
dp[0] = 0;
rep(i, 1, x){
    dp[i] = llinf;
    for(auto &j : coin){
        if(j <= i){
            dp[i] = min(dp[i], dp[i - j] + 1);
        }
    }
}
cout << (dp[x] == llinf ? -1 : dp[x]);
}

```

2.4 Edit Distance

```

ll dp[maxn][maxn];
void solve(){
    init(dp, 0);
    string s1, s2; cin >> s1 >> s2;
    int size1 = s1.sz, size2 = s2.sz;
    s1 = "0" + s1, s2 = "0" + s2;
    rep(i, 1, size2) dp[0][i] = i; // s2 = {}, s1 = ...;
    rep(i, 1, size1) dp[i][0] = i; // s1 = {}, s2 = ...;
    rep(i, 1, size1){
        rep(j, 1, size2){
            if(s1[i] == s2[j]){
                dp[i][j] = dp[i-1][j-1];
            }
            else {
                dp[i][j] = min(min(dp[i-1][j-1],
                    dp[i-1][j]), dp[i][j-1]) + 1;
                // modify // s1 del / s2 add
                // s1 add s2 del
            }
        }
    }
    cout << dp[size1][size2];
}

```

2.5 Print LCS

```

void solve(){
    int m, n; cin >> m >> n;
    string s1, s2;
    cin >> s1 >> s2;
    s1.insert(s1.begin(), '1');
    s2.insert(s2.begin(), '1');
    int L = 0;
    int dp[m+1][n+1]; init(dp, 0);
    rep(i, 1, m){
        rep(j, 1, n){
            if(s1[i] == s2[j]){

```

```

        dp[i][j] = dp[i-1][j-1] + 1;
    }
    else {
        dp[i][j] = max(dp[i-1][j], dp[i][j-1]);
    }
}
}
int length = dp[m][n];
cout << length << "\n";
vector<char> s(length);
// along to dp to trace back
while(m >= 1 && n >= 1){
    if(s1[m] == s2[n]){
        s[length - 1] = s1[m];
        m--;
        n--;
        length--;
    }
    else {
        if(dp[m-1][n] > dp[m][n-1]){
            m--;
        }
        else n--;
    }
}
for(auto c : s){
    cout << c;
}
}
}

```

2.6 Print LIS

```

// Rec Sequence LIS
void solve(){
    int n; cin >> n;
    vector<int> v(n);
    lrep(i, 0, n){
        cin >> v[i];
    }
    int dp[n]; vector<int> mono;
    mono.push_back(v[0]);
    dp[0] = 1; int L = 1;
    lrep(i, 1, n){
        if(v[i] > mono.back()){
            mono.push_back(v[i]);
            dp[i] = ++L;
        }
        else {
            auto it = lower_bound(all(mono), v[i]);
            *it = v[i];
            dp[i] = it - mono.begin() + 1;
        }
    }
    vector<int> ans;
    cout << L << endl;
    for(int i = n - 1; i >= 0; i--){
        if(dp[i] == L){
            ans.push_back(v[i]);
            L--;
        }
    }
}

```

```

    }
}
reverse(all(ans));
for(auto i : ans){
    cout << i << " ";
}
}

```

2.7 Removal Game

```

ll dp[5005][5005];
void solve(){
    int n; cin >> n;
    ll pref = 0;
    vector<ll> v(n+1);
    rep(i, 1, n){
        cin >> v[i];
        pref += v[i];
    }
    // dp[i][j] = max_diff(i to j);
    for(int i = n; i > 0; i--){
        for(int j = 1; j <= n; j++){
            if(i > j) continue;
            else if(i == j){
                dp[i][j] = v[i];
            }
            else {
                dp[i][j] = max(v[i] - dp[i+1][j], v[j] - dp[i][j-1]); // i+1, j-1, care dp's order
            }
        }
    }
    // x + y = sum, dp[1][n] = x - y;
    cout << (pref + dp[1][n]) / 2;
}

```

3 Flow

3.1 Dinic

```

#include <bits/stdc++.h>
using namespace std;
bool vis[505];
int lev[505], n, m, ans;
typedef struct {
    int to, w, rev_ind;
} edge;
vector<edge> adj[505];
bool label_level(){ // Tag the depth if can't reach end =>
    return false;
}
memset(lev, -1, sizeof(lev));
lev[1] = 0;
queue<int> q; q.push(1);
while(!q.empty()){

```

```

    int u = q.front(); q.pop();
    for(auto i : adj[u]){
        if(i.w > 0 && lev[i.to] == -1){
            q.push(i.to);
            lev[i.to] = lev[u] + 1;
        }
    }
}
return (lev[n] == -1 ? false : true);
}
int dfs(int u, int flow){
    if(u == n) return flow;
    for(auto &i : adj[u]){
        if(lev[i.to] == lev[u] + 1 && !vis[i.to] && i.w > 0){
            vis[i.to] = true;
            int ret = dfs(i.to, min(flow, i.w));
            if(ret > 0){
                i.w -= ret;
                adj[i.to][i.rev_ind].w += ret;
                return ret;
            }
        }
    }
    return 0; // if can't reach end => return 0
}
void dinic(){
    while(label_level()){
        while(1){
            init(vis, 0);
            int tmp = dfs(1, inf);
            if(tmp == 0) break;
            ans += tmp;
        }
    }
}
void build(){
    rep(i, 1, m){
        int u, v, w; cin >> u >> v >> w;
        adj[u].push_back({v, w, (int)adj[v].sz}); // inverse flow's index
        adj[v].push_back({u, 0, (int)adj[u].sz-1}); // have pushed on need to -1
    }
}
// Police Chaseneed to open adj to Augment && ori to determine what pb give
// Dinicdfs2then use reach as u if the edge pb has given && w == 0 && v is not in reach is the ans
void dfs2(int now, unordered_set<int> &reach){
    if(!vis[now]){
        vis[now] = 1;
        reach.insert(now);
        for(auto i : adj[now]){
            if(i.w > 0){
                dfs2(i.to, reach);
            }
        }
    }
}
// two two pair // School Dance
// Dinicthen w == 0 edge, which pb has given is the ans

```

```
// Distinct Route
// edge set valid varif we need to argument pos roadthe
// reverse edge set true valid
// if we need argument the argumented edgeboth set
// falselast, from v dfs ans times
bool get_road(int now, vector<int> &ans, vector<bool>
&vis){
    if(now == 1) return true;
    for(auto &v : adj[now]){
        if(v.arg_valid && !vis[v.to]){
            ans.push_back(v.to);
            vis[v.to] = true;
            bool flag = get_road(v.to, ans, vis);
            if(flag){
                v.arg_valid = false;
                return true;
            }
        }
        ans.pop_back();
    }
    return false;
}
```

3.2 MCMF

```
#include <bits/stdc++.h>
using namespace std;
// Ceiled MinCostMaxFlowif not, use dinic
typedef struct {
    int from, to, w, cost;
} edge;
int n, m, parcel;
vector<edge> adj; // set num to each edge
vector<int> p[505]; // p[u] has edge's num
int now_edge = 0;
void add_edge(int u, int v, int w, int cost){
    adj.push_back({u, v, w, cost});
    p[u].push_back(now_edge);
    now_edge++;
    adj.push_back({v, u, 0, -cost}); // argumenting path
    use -
    p[v].push_back(now_edge);
    now_edge++;
}
ll Bellman_Ford(){
    vector<ll> dis(n+1, inf); dis[1] = 0;
    vector<int> par(m);
    vector<int> flow_rec(n+1, 0); flow_rec[1] = 1e9;
    lrep(i, 1, n){
        bool flag = 1;
        int size = adj.sz;
        lrep(i, 0, size){
            auto &[from, to, w, cost] = adj[i];
            if(w > 0 && dis[to] > dis[from] + cost){
                flag = 0;
                dis[to] = dis[from] + cost;
                par[to] = i; // record num
                flow_rec[to] = min(flow_rec[from], w);
            }
        }
    }
    if(flag) break;
}
int mn_flow = flow_rec[n];
int v = n;
while(v != 1){
    int u = adj[par[v]].from;
    adj[par[v]].w -= mn_flow;
    adj[par[v] ^ 1].w += mn_flow;
    v = u;
}
mn_flow = min(mn_flow, parcel);
parcel -= mn_flow;
return mn_flow * dis[n];
}
void solve(){
    cin >> n >> m >> parcel;
    ll ans = 0;
    rep(i, 1, m){
        int u, v, w, cost; cin >> u >> v >> w >> cost;
        add_edge(u, v, w, cost);
    }
    while(parcel > 0){
        int tmp = Bellman_Ford();
        if(tmp == 0) break;
        ans += tmp;
    }
    cout << (parcel > 0 ? -1 : ans);
}
```

4 Geometry

4.1 Convex Hull

```
vector<pii> P, L, U;
ll cross(pii o, pii a, pii b){ // OA OB >0 counterclock
    return (a.first - o.first) * (b.second - o.second) -
        (a.second - o.second) * (b.first - o.first);
}
ll Andrew_monotone_chain(ll n){
    sort(P.begin(), P.end());
    ll l = 0, u = 0; // upper and lower hull
    for (ll i=0; i<n; ++i){
        while (l >= 2 && cross(L[l-2], L[l-1], P[i]) <= 0){
            l--;
            L.pop_back();
        }
        while (u >= 2 && cross(U[u-2], U[u-1], P[i]) >= 0){
            u--;
            U.pop_back();
        }
        l++;
        u++;
        L.push_back(P[i]);
        U.push_back(P[i]);
    }
}
```

```
cout << l << ' ' << u << '\n';
return l + u;
}
int main(){
    ll n,x,y;
    cin >> n;
    for(ll i = 0; i < n; i++){
        cin >> x >> y;
        P.push_back({x,y});
    }
    ll ans = Andrew_monotone_chain(n) - 2;
    cout << ans << "\n";
    return 0;
}
```

4.2 Cross Product

```
const double EPS = 1e-9;
struct point{
    double x, y;
    point operator * (ll a){return {a * x, a * y};}
    point operator + (point b){return {x + b.x, y + b.y};}
    point operator - (point b){return {x - b.x, y - b.y};}
    double operator * (point b){return x * b.x + y * b.y;}
    double operator ^ (point b){return x * b.y - y * b.x;}
    bool operator < (point b){return x == b.x ? y < b.y : x
        < b.x;}
};
// len
double abs(point a){return sqrt(a.x * a.x + a.y * a.y);}
int sign(double a){
    if(abs(a) < EPS)
        return 0;
    else
        return (a > 0 ? 1 : -1);
}
//cross product
int ori(point a,point b,point c){
    return sign((b - a) ^ (c - a));
}
bool colinear(point a,point b,point c){
    return sign((b - a) ^ (c - a)) == 0;
}
bool between(point a,point b,point c){ // c between a and b
    if(!colinear(a,b,c))
        return false;
    return sign((a - c) * (b - c)) <= 0;
}
bool intersect(point a,point b,point c,point d){ //
    line(a,b) line(c,d)
    int abc = ori(a,b,c);
    int abd = ori(a,b,d);
    int cda = ori(c,d,a);
    int cdb = ori(c,d,b);
    if(abc == 0 || abd == 0)
        return between(a,b,c) || between(a,b,d) ||
            between(c,d,a) || between(c,d,b);
    return abc * abd <= 0 && cda * cdb <= 0;
}
```

```
int main(){
    int n;
    cin >> n;
    point p[1010];
    cin >> p[0].x >> p[0].y;
    ll ans = 0;
    for(int i = 1; i < n; i++){
        cin >> p[i].x >> p[i].y;
        ans += (p[i] ^ p[i - 1]);
    }
    ans += (p[0] ^ p[n - 1]);
    cout << abs(ans) << '\n';

    return 0;
}
```

5 Graph

5.1 2-SAT

```
// +(-) u or +(-) v
const int maxn = 1e5 + 5;
vector<int> adj[2 * maxn], rev_adj[2 * maxn];
vector<int> order;
int cat[2 * maxn];
int k = 1;
bool vis[2 * maxn];
void dfs(int now){
    if (!vis[now]){
        vis[now] = 1;
        for (auto v : adj[now]){
            dfs(v);
        }
        order.push_back(now);
    }
}
void rev_dfs(int now){
    if (!vis[now]){
        cat[now] = k;
        vis[now] = 1;
        for (auto v : rev_adj[now]){
            rev_dfs(v);
        }
    }
}
void solve(){
    int n, m;
    cin >> m >> n;
    rep(i, 1, m){
        int u, v;
        char a, b;
        cin >> a >> u >> b >> v;
        if (a == '-' ){
            u = 2 * n - u + 1; // reverse
        }
        if (b == '-' ){
            v = 2 * n - v + 1; // reverse
        }
    }
}
```

```
adj[2 * n - u + 1].push_back(v); // from -u to v;
// if -u, then v
adj[2 * n - v + 1].push_back(u); // from -v to u;
// if -v, then u
rev_adj[v].push_back(2 * n - u + 1);
rev_adj[u].push_back(2 * n - v + 1);
}
rep(i, 1, 2 * n){
    if (!vis[i]){
        dfs(i);
    }
}
memset(vis, 0, sizeof(vis));
reverse(all(order));
for (auto i : order){
    if (!vis[i]){
        rev_dfs(i);
        k++;
    }
}
}
char ans[2 * n + 1];
rep(i, 1, n){
    if (cat[i] == cat[2 * n - i + 1]){
        cout << "IMPOSSIBLE";
        return;
    }
    if (cat[i] > cat[2 * n - i + 1]){
        ans[i] = '+';
    }
    else ans[i] = '-';
}
rep(i, 1, n){
    cout << ans[i] << " ";
}
}
```

5.2 Coin Collector And Topo DP

```
// Find All SCC and Build a DAG then Topo DP
const int maxn = 1e5 + 5;
vector<int> v, adj[maxn], rev_adj[maxn], DAG[maxn];
int order[maxn], coin[maxn], in[maxn];
int n, m, k = 0;
bool vis[maxn];
void dfs(int now){
    if (!vis[now]){
        vis[now] = 1;
        for (auto i : adj[now]){
            dfs(i);
        }
        v.push_back(now);
    }
}
void rev_dfs(int now){
    if (!vis[now]){
        vis[now] = 1;
        order[now] = k;
        for (auto i : rev_adj[now]){
            rev_dfs(i);
        }
    }
}
```

```

    }
}
}
void solve(){
    cin >> n >> m;
    rep(i, 1, n){
        cin >> coin[i];
    }
    rep(i, 1, m){
        int u, v; cin >> u >> v;
        adj[u].push_back(v);
        rev_adj[v].push_back(u);
    }
    rep(i, 1, n){
        if (!vis[i]){
            dfs(i);
        }
    }
    reverse(all(v));
    init(vis, 0);
    for (auto i : v){
        if (!vis[i]){
            k++;
            rev_dfs(i);
        }
    }
    // Categorized SCC
    ll sum_coin[k + 1], dp_coin[k + 1];
    init(sum_coin, 0); init(dp_coin, 0);
    ll ans = -inf;
    rep(i, 1, n){
        sum_coin[order[i]] += coin[i]; // Now team(k) += coin;
        for (auto j : adj[i]){
            if (order[i] != order[j]){
                DAG[order[i]].push_back(order[j]);
                in[order[j]]++;
            }
        }
    }
    // Topo DP
    queue<int> q;
    rep(i, 1, k){
        if (in[i] == 0){
            q.push(i);
        }
    }
    while (!q.empty()){
        int now = q.front(); q.pop();
        dp_coin[now] += sum_coin[now];
        ans = max(ans, dp_coin[now]);
        for (auto v : DAG[now]){
            in[v]--;
            dp_coin[v] = max(dp_coin[v], dp_coin[now]);
            if (in[v] == 0) q.push(v);
        }
    }
    cout << ans;
}
```

5.3 DFS and BFS

```

11 N = 1e6;
vi adj[N];
bool vis[N];
void DFS(11 s){
    if(vis[s]) return;
    vis[s] = true;
    for(auto u: adj[s]){
        DFS(u);
    }
}
queue<11> q;
11 dis[N];
void BFS(11 x){
    vis[x] = true;
    dis[x] = 0;
    q.push(x);
    while(!q.empty()){
        11 now = q.front();q.pop();
        for(auto nxt : adj[now]){
            if(vis[nxt]) continue;
            vis[nxt] = true;
            dis[nxt] = dis[now] + 1;
            q.push(nxt);
        }
    }
}

```

5.4 DSU

```

// After each day, print the number of components
// and the size of the largest component
const int maxn = 2e5+5;
int ans, mx_sz = 1;
int boss[maxn];
int set_sz[maxn];
int find_boss(int x){
    if(boss[x] == x) return x;
    return boss[x] = find_boss(boss[x]);
}
void dsu(int x, int y){
    int boss_x = find_boss(x);
    int boss_y = find_boss(y);
    if(boss_x != boss_y){
        ans--;
        if(set_sz[boss_x] < set_sz[boss_y]){
            swap(boss_x, boss_y);
        }
        boss[boss_y] = boss_x;
        set_sz[boss_x] += set_sz[boss_y];
        mx_sz = max(mx_sz, set_sz[boss_x]);
    }
    cout << ans << " " << mx_sz << endl;
}
void solve(){
    int n, q; cin >> n >> q;
    ans = n;

```

```

rep(i, 1, n){
    boss[i] = i;
    set_sz[i] = 1;
}
rep(i, 1, q){
    int x, y;
    cin >> x >> y;
    dsu(x, y);
}
}

```

5.5 EulerRoad

```

// Undirected : check adj[i].sz == odd =>
// IMPOSSIBLE
// Directed : minimize to 1 -> 2 so check in_degree ==
// out_degree
int n, m;
set<int> adj[maxn]; // rev_adj[maxn];
int in[maxn];
void dfs(int now, vector<int> &road){
    while(!adj[now].empty()){
        int nxt = *adj[now].begin();
        adj[now].erase(nxt);
        dfs(nxt, road);
    }
    road.push_back(now);
}
void solve(){
    cin >> n >> m;
    init(in, 0);
    rep(i, 1, m){
        int u, v; cin >> u >> v;
        adj[u].insert(v);
        in[v]++;
    }
    in[1]++;
    in[n]--;
    rep(i, 1, n){
        if(adj[i].size() != in[i]){
            cout << "IMPOSSIBLE";
            return;
        }
    }
    vector<int> road;
    dfs(1, road);
    if(road.size() != m+1){
        cout << "IMPOSSIBLE";
        return;
    }
    reverse(all(road));
    for(auto i : road) cout << i << " ";
}

```

5.6 FloydWarshall

```

const int maxn = 505;
11 graph[maxn][maxn];
11 dis[maxn][maxn];
11 n, m, q; 11 a, b, c;
const 11 INF = 1e18;
int main(){
    cin >> n >> m >> q;
    for(int i = 0; i <= n; i++) {
        for(int j = 0; j <= n; j++) {
            graph[i][j] = INF;
        }
    }
    for(int i = 0; i < m; i++){
        cin >> a >> b >> c;
        graph[a][b] = min(graph[a][b], c);
        graph[b][a] = min(graph[b][a], c);
    }
    for(int i = 0; i <= n; i++) {
        for(int j = 0; j <= n; j++) {
            dis[i][j] = graph[i][j];
        }
    }
    for(int i = 0; i <= n; i++) // self to self is 0
        dis[i][i] = 0;

    for(int k = 1; k <= n; k++){
        for(int i = 1; i <= n; i++){
            for(int j = 1; j <= n; j++){
                dis[i][j] = min(dis[i][j], dis[i][k] +
                                dis[k][j]);
            }
        }
    }
    for(int i = 0; i < q; i++){
        cin >> a >> b;
        cout << (dis[a][b] >= INF ? -1 : dis[a][b]) << "\n";
    }
}

```

5.7 MaxDistance

```

// Max_DisUse TopoUse queue
// If 1 can't reach n still may be relaxedShould dis[n] < 0
// Only Directed Graph
void print_ans(int n, vector<int> &par){
    deque<int> ans;
    int now = n;
    while(now != 1){
        ans.push_front(now);
        now = par[now];
    }
    ans.push_front(1);
    cout << ans.size() << endl;
    for(auto i : ans){
        cout << i << " ";
    }
}
void solve(){

```

```

int n, m;
cin >> n >> m;
vector<int> dis(n+1, -inf); dis[1] = 0;
vi graph[n+1];
vector<bool> vis(n+1, 0);
vector<int> par(n+1);
vector<int> in(n+1, 0);
queue<int> q;
rep(i, 1, m){
    int u, v; cin >> u >> v;
    graph[u].push_back(v);
    in[v]++;
}
rep(i, 1, n){
    if(in[i] == 0) q.push(i);
}
while(!q.empty()){
    int u = q.front(); q.pop();
    for(auto nxt : graph[u]){
        if(dis[nxt] < dis[u] + 1){
            dis[nxt] = dis[u] + 1;
            par[nxt] = u;
        }
        in[nxt]--; if(in[nxt] == 0) q.push(nxt);
    }
    vis[u] = 1;
}
if(dis[n] < 0){
    cout << "IMPOSSIBLE";
}
else print_ans(n, par);
}

```

5.8 NegCyc Using BellmanFord

```

typedef struct{
    int from; int to;
    ll weight;
} edge;
const ll inf = 1LL << 62;
// NegCyc_Finding_Road
vector<edge> graph;
int main(){
    int src = 0;
    int n, m; cin >> n >> m;
    vector<int> par(n+1), dis(n+1);
    rep(i, 0, m){
        int a, b, w; cin >> a >> b >> w;
        graph.push_back({a, b, w});
    }
    rep(i, 0, n+1) {
        dis[i] = 1e9 + 5;
    }
    dis[1] = 0;
    rep(i, 0, n + 1){
        src = 0;
        for(auto [a, b, w] : graph){
            if(dis[b] > dis[a] + w){
                dis[b] = dis[a] + w;
            }
        }
    }
}

```

```

        par[b] = a;
        src = b;
    }
}
}
if(src){
    vector<int> ans;
    cout << "YES" << endl;
    rep(i, 0, n + 1) src = par[src];
    ans.push_back(src);
    for(int i = par[src]; i != src; i = par[i]){
        ans.push_back(i);
    }
    ans.push_back(src);
    reverse(all(ans));
    for (auto i : ans){
        cout << i << " ";
    }
}
else {
    cout << "NO" << endl;
}
}
}

```

5.9 NegWeights Max Distance

```

const int maxn = 2505;
int m, n;
vector<edge> graph;
vll adj[maxn];
vll rev_adj[maxn];
ll dis[maxn];
bool vis[maxn] = {0};
bool nvis[maxn] = {0};
void dfs(int par, int now){
    if (vis[now] == 1) return;
    vis[now] = 1;
    for (auto [i, w] : adj[now]){
        if (i != par){
            dfs(now, i);
        }
    }
}
void rev_dfs(int par, int now){
    if (nvis[now] == 1) return;
    nvis[now] = 1;
    for (auto i : rev_adj[now]){
        if (i != par){
            rev_dfs(now, i);
        }
    }
}
void solve(){
    cin >> n >> m;
    rep(i, 1, m){
        int u, v, w;
        cin >> u >> v >> w;
        graph.push_back({u, v, w});
        adj[u].push_back({v, w});
    }
}

```

```

        rev_adj[v].push_back(u);
    }
    rep(i, 1, n) dis[i] = minf;
    dis[1] = 0;
    rep(i, 1, n){
        for (auto [u, v, w] : graph){
            if (dis[u] + w > dis[v]){
                dis[v] = dis[u] + w;
            }
        }
    }
    dfs(0, 1);
    rev_dfs(0, n);
    for (auto [u, v, w] : graph){
        if (dis[u] + w > dis[v] && nvis[u] && nvis[v] &&
            vis[u] && vis[v]){
            cout << -1;
            return;
        }
    }
    cout << dis[n];
}

```

5.10 Planet Queries II

```

// now on a and want to reach b, the min steps, directed
int n, q;
int dp[30][maxn];
vector<vector<int>> cycles;
int no[maxn]; // OrderCan be in cycle or out
int cycle_idx[maxn];
bool vis[maxn];
void set_out_of_cycle_no(int now, unordered_set<int>
    &done){
    if (done.find(now) != done.end())
        return;
    set_out_of_cycle_no(dp[0][now], done);
    done.insert(now);
    no[now] = no[dp[0][now]] - 1;
}
int will_go_to(int u, int k){ // return the node when walk
    k
    rep(i, 0, 18){
        if (k & (1 << i)){
            u = dp[i][u];
        }
    }
    return u;
}
void find_cycle(int now){
    unordered_set<int> appear;
    vector<int> vec;
    bool flag = true;
    while (appear.find(now) == appear.end()){
        appear.insert(now);
        vec.push_back(now);
        if (vis[now]){ // Didn't Find Cycle
            flag = false;
            break;
        }
    }
}

```

```

    }
    now = dp[0][now];
}
for (auto i : vec) vis[i] = true;
if (!flag) return;
int z = find(vec.begin(), vec.end(), now) -
    vec.begin(); // start pushing from last now
int m = vec.size();
vector<int> cycle;
for (int i = z; i < m; i++){
    cycle.push_back(vec[i]);
}
cycles.push_back(cycle);
}
void solve(){
    cin >> n >> q;
    rep(u, 1, n){
        cin >> dp[0][u];
    }
    rep(i, 1, 18){ // Make Chart
        rep(u, 1, n){
            dp[i][u] = dp[i - 1][dp[i - 1][u]];
        }
    }
    rep(i, 1, n){
        if (!vis[i]) find_cycle(i);
    }
    ll idx = 0;
    memset(no, -1, sizeof(no));
    memset(cycle_idx, -1, sizeof(cycle_idx));
    unordered_set<int> done;
    for (auto &i : cycles){
        ll c = 0;
        for (auto &j : i){
            no[j] = c++;
            cycle_idx[j] = idx;
            done.insert(j);
        }
        idx++;
    }
    rep(i, 1, n) set_out_of_cycle_no(i, done);
    rep(i, 1, q){
        int u, v; cin >> u >> v;
        // Same Cycle
        if (cycle_idx[u] == cycle_idx[v] && cycle_idx[u] !=
            -1 && cycle_idx[v] != -1){
            int cyc_size = cycles[cycle_idx[u]].size();
            cout << (no[v] - no[u] + cyc_size) % cyc_size
                << endl;
        }
        else if (cycle_idx[u] == -1 && cycle_idx[v] == -1){
            // Both are not in a Cycle
            if (no[u] > no[v]){
                cout << -1 << endl;
                continue;
            }
            ll jump = no[v] - no[u];
            if (will_go_to(u, jump) == v){
                cout << jump << endl;
            }
            else cout << -1 << endl;
        }
    }
}

```

```

    else if (cycle_idx[u] == -1 && cycle_idx[v] != -1){
        // v is in cycleSmaller Binary Search
        int l = -1, r = n;
        while (l <= r){
            int m = (l + r) / 2;
            if (cycle_idx[will_go_to(u, m)] ==
                cycle_idx[v]){
                r = m - 1;
            }
            else
                l = m + 1;
        }
        if (l != -1 && l <= n){
            int in_cycle_of_u = will_go_to(u, l);
            int cycle_size = cycles[cycle_idx[v]].size();
            cout << l + (no[v] - no[in_cycle_of_u] +
                cycle_size) % cycle_size << endl;
        }
        else cout << -1 << endl;
    }
    else { // u is death in the cyclecan't reach
        cout << -1 << endl;
    }
}
}
}

```

5.11 Planets Cycles

```

vi dis, v;
vector<bool> vis;
ll step;
queue<ll> path;
void dfs(ll x){
    path.push(x);
    if (vis[x]){
        step += dis[x];
        return;
    }
    vis[x] = true;
    step++;
    dfs(v[x]);
}
// count pathdis to rep
int main(){
    v.assign(n + 1, 0);
    dis.assign(n + 1, 0);
    vis.assign(n + 1, false);
    for (int i = 1; i <= n; i++){
        cin >> v[i];
    }
    for (int i = 1; i <= n; i++){
        step = 0;
        int is_outof_cycle = 1;
        dfs(i);
        while (!path.empty()){
            if (path.front() == path.back()){
                is_outof_cycle = 0;
            }
        }
        dis[path.front()] = step;
    }
}

```

```

        step -= is_outof_cycle;
        path.pop();
    }
}
for (int i = 1; i <= n; i++){
    cout << dis[i] << ' ';
}
cout << '\n';
}

```

5.12 PosCycle Finding

```

const int maxn = 1e5+5;
vector<int> graph[maxn];
int color[maxn], parent[maxn];
bool vis[maxn];
int n, m;
void print_ans(int ori){
    int now = parent[ori];
    deque<int> ans;
    ans.push_front(ori);
    while(now != ori){
        ans.push_front(now);
        now = parent[now];
    }
    ans.push_front(ori);
    cout << ans.size() << endl;
    for(auto i : ans){
        cout << i << " ";
    }
    exit(0);
}
void dfs(int now){
    color[now] = 1;
    vis[now] = 1;
    for(auto nxt : graph[now]){
        parent[nxt] = now;
        if(color[nxt] == 1){
            print_ans(nxt);
        }
        else if(color[nxt] == 0){
            dfs(nxt);
        }
    }
    color[now] = 2;
}
void solve(){
    cin >> n >> m;
    rep(i, 1, m){
        int u, v; cin >> u >> v;
        graph[u].push_back(v);
    }
    rep(i, 1, n){
        if(!vis[i])
            dfs(i);
    }
    cout << "IMPOSSIBLE";
}

```


5.13 Prim

```
int n, m;
ll ans = 0;
vii adj[maxn];
bool Prim(){
    int node_sz = 0;
    priority_queue<pii, vii, greater<pii>> pq;
    pq.push({0, 1});
    bool vis[maxn]; init(vis, false);
    while(!pq.empty()){
        auto [cost, u] = pq.top(); pq.pop();
        if(vis[u]) continue;
        vis[u] = true;
        ans += cost;
        node_sz++;
        for(auto [v, cost] : adj[u]){
            if(!vis[v])
                pq.push({cost, v});
        }
    }
    if(node_sz == n) return true;
    return false;
}
void solve(){
    cin >> n >> m;
    rep(i, 1, m){
        int u, v, cost; cin >> u >> v >> cost;
        adj[u].push_back({v, cost});
        adj[v].push_back({u, cost});
    }
    if(Prim()) cout << ans;
    else cout << "IMPOSSIBLE";
}
```

5.14 State Dijkstra

```
// Flight Discount
int n, m;
vll graph[maxn];
ll dis[maxn][2]; // 0 for not used
void dijkstra(){
    priority_queue<vector<ll>, vector<vector<ll>>,
        greater<vector<ll>>> pq; // 0 for w, 1 for u, 2
        for discount
    rep(i, 1, n){
        dis[i][0] = dis[i][1] = inf;
    }
    dis[1][0] = dis[1][1] = 0;
    pq.push({0, 1, 0});
    while(!pq.empty()){
        auto nxt = pq.top(); pq.pop();
        ll dist = nxt[0], u = nxt[1]; bool us = nxt[2];
        if(dis[u][us] < dist) continue; //
        if(us){
            for(auto [v, w] : graph[u]){
                if(dis[u][1] + w < dis[v][1]){
                    dis[v][1] = dis[u][1] + w;

```

```
                pq.push({dis[v][1], v, 1});
            }
        }
        else {
            for(auto [v, w] : graph[u]){
                if(dis[u][0] + w < dis[v][0]){
                    dis[v][0] = dis[u][0] + w;
                    pq.push({dis[v][0], v, 0});
                }
                if(dis[u][0] + w / 2 < dis[v][1]){
                    dis[v][1] = dis[u][0] + w / 2;
                    pq.push({dis[v][1], v, 1});
                }
            }
        }
    }
    cout << min(dis[n][0], dis[n][1]);
}
void solve(){
    cin >> n >> m;
    rep(i, 1, m){
        int u, v, w;
        cin >> u >> v >> w;
        graph[u].push_back({v, w});
    }
    dijkstra();
}
```

5.15 Vis Dijkstra

```
void solve(){
    int n, m, noon, night;
    cin >> n >> m >> noon >> night;
    ll dis[n + 1];
    vll graph[n + 1];
    bool vis[n + 1];
    rep(i, 1, m){
        int u, v, w; cin >> u >> v >> w;
        graph[u].push_back({v, w});
        graph[v].push_back({u, w});
    }
    priority_queue<vector<ll>, vector<vector<ll>>,
        greater<vector<ll>>> pq;
    // noon is -
    rep(i, 1, n){
        dis[i] = inf; vis[i] = 0;
    }
    pq.push({0, -noon, 1});
    dis[1] = 0;
    while(!pq.empty()){
        vl now = pq.top(); pq.pop();
        ll now_noon = -now[1], u = now[2];
        if(vis[u]) continue;
        for(auto [nxt, w] : graph[u]){
            if(noon < w) continue; // never pass
            ll tmp = dis[u] + (now_noon >= w ? w : now_noon
                + night + w);
            if(tmp < dis[nxt]){

```

```
                dis[nxt] = tmp;
                pq.push({dis[nxt], -(now_noon >= w ?
                    now_noon - w : noon - w), nxt});
            }
        }
        vis[u] = true;
    }
    if(dis[n] == inf) cout << -1 << endl;
    else cout << dis[n] << endl;
}
// Investigation
for(auto [v, w] : graph[u]){
    if(dis[u] + w < dis[v]){
        dis[v] = dis[u] + w;
        pq.push({dis[v], v});
        min_price_nums[v] = min_price_nums[u];
        max_dis_min_price[v] = max_dis_min_price[u] + 1;
        min_dis_min_price[v] = min_dis_min_price[u] + 1;
    }
    else if(dis[u] + w == dis[v]){
        min_price_nums[v] = (min_price_nums[u] +
            min_price_nums[v]) % mod;
        max_dis_min_price[v] = max(max_dis_min_price[u] +
            1, max_dis_min_price[v]);
        min_dis_min_price[v] = min(min_dis_min_price[u] +
            1, min_dis_min_price[v]);
    }
}
}
```

6 Math

6.1 Prime

```
// a^(m-1) 1 (mod m)
// a^(m-2) 1/a (mod m)
// EXP2: cout << fast_exp(x, fast_exp(y, p, MOD - 1), MOD)
// Filter + DP; DP save min factorrecurfactor
// decomposition
// FacNums = (x+1)(y+1)(z+1)...
// FacSum = (a^0+a^1+...+a^x)(b^0+...+b^y)
// FacMul = N(x+1)(y+1)(z+1)/2
ll fast_exp(ll x, ll p, ll mod){
    ll ans = 1;
    while(p > 0){
        if(p & 1) ans = (ans * x) % mod;
        x = x * x % mod;
        p >>= 1;
    }
    return ans;
}
ll quick_mul(ll a, ll b){
    ll ans = 0;
    a %= MOD;
    while(b > 0){
        if(b & 1){
            ans = (ans + a) % MOD;
        }
        a = (a << 1) % MOD;
    }
}
```

```

    b >>= 1;
}
return ans;
}

```

7 Queries

7.1 Binary Search

```

#include <bits/stdc++.h>
using namespace std;
int main(){
    int l = 1, r = 10;
    // 1 to tar, find tar
    while(l <= r){
        int m = (l + r) / 2;
        if(check(m)) l = m + 1;
        else r = m - 1;
    }
    cout << r;
    // tar to end
    while(l <= r){
        int m = (l + r) / 2;
        if(check(m)) r = m - 1;
        else l = m + 1;
    }
    cout << l;
}

```

7.2 BIT

```

typedef struct {
    int set_val, add, sum, val;
} node;
node tree[100];
int n, q, nums[100], _1D_BIT[100], _2D_BIT[100][100];

// 1D-BIT
void modify(int x, int mod){
    for(; x <= n; x += (x&-x)){
        _1D_BIT[x] += mod;
    }
}

ll query(int x){
    ll ans = 0;
    for(; x; x -= (x&-x)){
        ans += _1D_BIT[x];
    }
    return ans;
}

// 2D-BIT // Forest Queries (Area)
void modify(int x, int y, int mod){
    for(; x <= n; x += (x&-x)){
        for(int tmp = y; tmp <= n; tmp += (tmp&-tmp)){
            _2D_BIT[x][tmp] += mod;
        }
    }
}

```

```

    }
}

ll query(int x, int y){
    ll ans = 0;
    for(; x; x -= (x&-x)){
        for(int tmp = y; tmp; tmp -= (tmp&-tmp)){
            ans += _2D_BIT[x][tmp];
        }
    }
    return ans;
}

```

7.3 Mo

```

typedef struct {
    int l, r, ind;
} query;
query queries[100];
int n, block, nums[100];
bool cmp(query a, query b){
    int block_a = a.l / block;
    int block_b = b.l / block;
    if(block_a != block_b) return block_a < block_b;
    return a.r < b.r;
}

void Mo(){
    // sort
    int cl = 1, cr = 0;
    for(auto i : queries){
        while(cl < i.l){ // remove
            while(cr > i.r){ // remove
                while(cl > i.l){ // add
                    while(cr < i.r){ // add

```

7.4 Segment

```

typedef struct {
    int set_val, add, sum, val;
} node;
int n, q; node tree[4*maxn]; int nums[maxn];
#define lc 2*now
#define rc 2*now+1
#define mid (L+R)/2 // LR is now range, lr is target range
// Pull
void pull(int now){ // update now with 2 children
    // use lcrc to undate now
    // tree[now].sum = tree[lc].sum + tree[rc].sum;
    // tree[now].prefix = max(tree[lc].sum+tree[rc].prefix,
    // tree[lc].prefix);
    // tree[now].suffix = max(tree[lc].suffix+tree[rc].sum,
    // tree[rc].suffix);
    // tree[now].middle_max = max(max(tree[lc].middle_max,
    // tree[rc].middle_max),
    // tree[lc].suffix+tree[rc].prefix);
    // tree[now].middle_max = max(max(tree[now].middle_max,
    // tree[now].prefix), tree[now].suffix);
}

// Lazy
void push(int now, int child){
    if(tree[now].set_val){
        tree[child].set_val = 1;
        tree[child].val = tree[now].val;
        tree[child].add = tree[now].add;
    }
    else {
        tree[child].add += tree[now].add;
    }
}

void apply_tag(int now, int L, int R){
    if(tree[now].set_val)
        tree[now].sum = (R-L+1)*tree[now].val;
    tree[now].sum += (R-L+1)*tree[now].add;
    if(L != R){ // can go lower
        push(now, lc);
        push(now, rc);
    }
    tree[now].add = tree[now].set_val = 0; // Reset
}

// Build
void build(int L, int R, int now){
    if(L == R){
        // init tree[now];
        return;
    }
    int M = mid;
    build(L, M, lc);
    build(M+1, R, rc);
    pull(now);
}

// modify
void modify(int l, int r, int L, int R, int now){
    if(R < l || r < L || L > n) // invalid range
        return;
    if(l <= L && R <= r){
        // modify tree[now];

```

```

        // tree[now].add += add; // modify_add
        // tree[now].set_val = 1; // modify_mod
        // tree[now].val = mod;
        // tree[now].add = 0; // Set is more prior
        return;
    }
    int M = mid;
    apply_tag(now, L, R);
    modify(l, r, L, M, lc);
    modify(l, r, M+1, R, rc);
    apply_tag(lc, L, M); // need
    apply_tag(rc, M+1, R); // need
    pull(now); // update now with 2 children
}
// query
ll query(int l, int r, int L, int R, int now){
    int M = mid;
    if(R < l || r < L || L > n){
        return 0;
    }
    // apply_tag(now, L, R); // Lazy to uncomment
    if(l <= L && R <= r){
        return tree[now].sum;
    }
    return query(l, r, L, M, lc) + query(l, r, M+1, R, rc);
    // if(l <= L && R <= r) return tree[now].val;
    // if(r <= M) return query(l, r, L, M, lc);
    // else if(l > M) return query(l, r, M+1, R, rc);
    // return query(l, r, L, M, lc) & query(l, r, M+1, R, rc);
}
// pizza_queries
// Left(s < t): dis_l = (pizza[s] - s) + t;
// Right(t < s): dis_r = (pizza[s] + s) - t;

// List Removals
// Use seg_tree to maintain how many nums have been
// selected in the range
// Use binary_Search to find "mod" nums have been selected
// before ans
// if ans - mod == posnums[ans] is the answer and we modify
// tree[pos]

// polynomial queries
// Lazy_segset under and distance

```

7.5 Treap

```

struct Treap {
    Treap *l, *r;
    int pri, subsize; char val; bool rev_valid;
    Treap(int _val){
        val = _val;
        pri = rand();
        l = r = nullptr;
        subsize = 1; rev_valid = 0;
    }
    void pull(){ // update subsize or other information

```

```

        subsize = 1;
        for(auto i: {l,r}){
            if(i) subsize += i->subsize;
        }
    }
};
int size(Treap *treap) {
    if (treap == NULL) return 0;
    return treap->subsize;
}
// lazy
void push(Treap *t){
    if(!t) return;
    if(t->rev_valid){
        swap(t->l, t->r);
        if(t->l) t->l->rev_valid ^= 1;
        if(t->r) t->r->rev_valid ^= 1;
    }
    t->rev_valid = false;
}
Treap *merge(Treap *a, Treap *b){
    if(!a || !b) return a ? a : b;
    // push(a); push(b); // lazy
    if(a->pri > b->pri){
        a->r = merge(a->r, b);
        a->pull();
        return a;
    }
    else {
        b->l = merge(a, b->l);
        b->pull();
        return b;
    }
}
pair<Treap*, Treap*> split(Treap *root, int k) { // find
    1~k
    if (root == nullptr) return {nullptr, nullptr};
    // push(root); // lazy
    if (size(root->l) < k) {
        auto [a, b] = split(root->r, k -
            size(root->l) - 1);
        root->r = a;
        root->pull();
        return {root, b};
    }
    else {
        auto [a, b] = split(root->l, k);
        root->l = b;
        root->pull();
        return {a, root};
    }
}
void Print(Treap *t){
    if(t){
        // push(t); // lazy
        Print(t->l);
        cout << t->val;
        Print(t->r);
    }
}
void substring_rev(){

```

```

int n, m; cin >> n >> m;
Treap *root = nullptr;
string str; cin >> str;
for(auto c : str){
    root = merge(root, new Treap(c));
}
rep(i, 1, m){
    int x, y; cin >> x >> y;
    auto [a, b] = split(root, x-1); // a: 1~x-1, b: x~n
    auto [c, d] = split(b, y-x+1); // Use b to split
    // c->rev_valid ^= true;
    // push(c);
    b = merge(a, d); // Notice the order
    root = merge(b, c);
}
Print(root);
}

```

8 Sorting and Searching

8.1 Concert Ticket

```

// Better than Binary Search
#include <bits/stdc++.h>
using namespace std;
int main(){
    ios::sync_with_stdio(0);
    cin.tie(nullptr);
    int n, m; cin >> n >> m;
    multiset<int> tik;
    for(int i = 0; i < n; i++){
        int tmp; cin >> tmp;
        tik.insert(tmp);
    }
    while(m--){
        int x; cin >> x;
        auto it = tik.upper_bound(x);
        if(it == tik.begin()){
            cout << -1 << " ";
            continue;
        }
        it--;
        cout << *it << " ";
        tik.erase(it);
    }
}

```

8.2 Restaurant Customers

```

#include <bits/stdc++.h>
using namespace std;
int main(){
    vector<pair<int, int>> times;
    int n; cin >> n;
    for(int i = 0; i < n; i++){

```

```

    int u, v; cin >> u >> v;
    times.push_back({u, 1});
    times.push_back({v, -1});
}
sort(times.begin(), times.end());
int now_people = 0, ans = 0;
for(auto [t, x] : times){
    ans = max(ans, (now_people + x));
}
cout << ans;
}

```

9 Tree

9.1 LCA

```

#include <bits/stdc++.h> // LCA from 1
using namespace std;
const int maxn = 2e5+5;
int boss[maxn];
int height[maxn];
int arr[18][maxn];
vector<int> tree[maxn];
void Calculate_H(int now_node){
    for(auto nxt_node : tree[now_node]){
        height[nxt_node] = height[now_node] + 1;
        Calculate_H(nxt_node);
    }
}
int Find_Ancestor(int k, int h){
    for(int i = 0; i <= 17; i++){
        if(h & (1 << i)) k = arr[i][k];
    }
    return k;
}
int main(){
    memset(arr, 0, sizeof(arr));
    int n, q; cin >> n >> q;
    boss[1] = 1;
    for(int i = 2; i <= n; i++){
        int tmp; cin >> tmp; // tmp to i
        boss[i] = tmp;
        tree[tmp].push_back(i);
    }
    Calculate_H(1);
    for(int i = 2; i <= n; i++){
        arr[0][i] = boss[i];
    }
    for(int i = 1; i <= 17; i++){ // make chart
        for(int j = 1; j <= n; j++){
            arr[i][j] = arr[i-1][arr[i-1][j]];
        }
    }
    while(q--){
        int a, b; cin >> a >> b;
        if(height[a] < height[b]) swap(a, b);
        a = Find_Ancestor(a, height[a] - height[b]); //
        same depth from 1
    }
}

```

```

if(a == b){ // same point
    cout << a << "\n";
    continue;
}
for(int i = 17; i >= 0; i--){
    if(arr[i][a] != arr[i][b]){ // if a, b up 2 ^ i
        not the same point
        a = arr[i][a];
        b = arr[i][b];
    }
}
cout << arr[0][a] << "\n"; // more one
}
}

```

9.2 Subordinates DP

```

#include <bits/stdc++.h>
using namespace std;
const int maxn = 2e5+5;
vector<int> tree[maxn];
int sub[maxn];
void dfs(int now){
    for(auto nxt : tree[now]){
        dfs(nxt);
        sub[now] += sub[nxt] + 1;
    }
}
int main(){
    memset(sub, 0, sizeof(sub));
    int n; cin >> n;
    for(int i = 2; i <= n; i++){
        int b; cin >> b;
        tree[b].push_back(i);
    }
    dfs(1);
    for(int i = 1; i <= n; i++){
        cout << sub[i] << " ";
    }
}

```

9.3 Tree Centroid

```

#include <bits/stdc++.h>
using namespace std;
const int maxn = 2e5+5;
vector<int> tree[maxn];
int cen = 0, n;
int dfs(int par, int now){
    bool flag = 1;
    int size = 0;
    for(auto nxt : tree[now]){
        if(par != nxt){
            int subsize = dfs(now, nxt);
            if(subsize > n / 2) flag = false;
            size += subsize;
        }
    }
}

```

```

    }
}
if(n - 1 - size > n / 2) flag = false;
if(flag) cen = now;
return size + 1;
}
int main(){
    cin >> n;
    for(int i = 1; i < n; i++){
        int u, v; cin >> u >> v;
        tree[u].push_back(v);
        tree[v].push_back(u);
    }
    for(int i = 1; i <= n; i++){
        for(auto nxt : tree[i])
            dfs(i, nxt);
        if(cen) break;
    }
}
}

```

9.4 Tree Sum Distances

```

#include <bits/stdc++.h>
using namespace std;
const int maxn = 2e5+5;
vector<int> tree[maxn];
vector<int> subtree(maxn, 1);
long long ans[maxn];
int n;
void dfs(int par, int now, int depth){
    ans[1] += depth;
    for(auto nxt : tree[now]){
        if(par != nxt){
            dfs(now, nxt, depth + 1);
            subtree[now] += subtree[nxt];
        }
    }
}
void find_ans(int par, int now){
    // each sub's dis make - 1 non subnode + 1
    for(auto nxt : tree[now]){
        if(par != nxt){
            ans[nxt] = ans[now] + (n - subtree[nxt]) -
                subtree[nxt];
            find_ans(now, nxt);
        }
    }
}
int main(){
    cin >> n;
    for(int i = 1; i < n; i++){
        int u, v; cin >> u >> v;
        tree[u].push_back(v);
        tree[v].push_back(u);
    }
    dfs(0, 1, 0);
    find_ans(0, 1);
    for(int i = 1; i <= n; i++){
        cout << ans[i] << " ";
    }
}

```

```
    }
}
```

9.5 Unweighted Tree Distances

```
#include <bits/stdc++.h>
using namespace std;
const int maxn = 2e5+5;
int dep1[maxn], dep2[maxn];
vector<int> tree[maxn];
int start, maxdep = 1, End;
void dfs1(int par, int now){
    for(auto nxt : tree[now]){
        if(par != nxt){
            dep1[nxt] = dep1[now] + 1;
            if(dep1[nxt] > maxdep){
                maxdep = dep1[nxt];
                start = nxt;
            }
            dfs1(now, nxt);
        }
    }
}
void find_depth1(int par, int now){
    for(auto nxt : tree[now]){
        if(par != nxt){
            dep1[nxt] = dep1[now] + 1;
            if(dep1[nxt] > maxdep){
                maxdep = dep1[nxt];
                End = nxt;
            }
        }
    }
    find_depth1(now, nxt);
}
```

```
    }
}
}
void find_depth2(int par, int now){
    for(auto nxt : tree[now]){
        if(par != nxt){
            dep2[nxt] = dep2[now] + 1;
            find_depth2(now, nxt);
        }
    }
}
int main(){
    int n; cin >> n;
    for(int i = 1; i < n; i++){
        int u, v; cin >> u >> v;
        tree[u].push_back(v);
        tree[v].push_back(u);
    }
    dep1[1] = 1;
    dfs1(0, 1);
    dep1[start] = 1;
    maxdep = 1;
    find_depth1(start, start);
    dep2[End] = 1;
    find_depth2(End, End);
    for(int i = 1; i <= n; i++){
        cout << max(dep1[i], dep2[i]) - 1 << " ";
    }
}
```

9.6 Weighted Tree Distance

```
#include <bits/stdc++.h> //
using namespace std;
const int maxn = 1e5+5;
using ll = long long int;
vector<pair<int, int>> tree[maxn];
ll dp[maxn];
ll ans = 0;
void DP(int now, int par){
    ll mx1 = 0; ll mx2 = 0;
    for(auto [nxt, w] : tree[now]){
        if(nxt == par) continue;
        DP(nxt, now);
        if(mx1 < w + dp[nxt]){ // mx2 = mx1mx1 = new mx
            mx2 = mx1; mx1 = w + dp[nxt];
        }
        else if(mx2 < w + dp[nxt]){ // mx2 = new
            mx2 = w + dp[nxt];
        }
    }
    dp[now] = mx1;
    ans = max(ans, mx1 + mx2);
}
int main(){
    int n; cin >> n;
    memset(dp, 0, sizeof(dp));
    for(int i = 1; i < n; i++){
        int u, v, w; cin >> u >> v >> w;
        tree[u].push_back({v, w});
        tree[v].push_back({u, w});
    }
    DP(1, 0);
    cout << (ans < 0 ? 0 : ans);
}
```