Contents 6 Math 10 6.1 Mint **6.2** Combination 11 1 Basic 1.1 Default Code **CRT** 12 1.2 Compare Fuction 1.3 Pbds 1.4 Double **1.5 Int128** 1 1.6 Rng 2 Graph **6.13 Mobius Inverse** 13 **6.14 Catalan Theorem** 14 2.1 DFS And BFS 2.2 Prim 6.15 Burnside's Lemma 14 2.3 Bellman-Ford Search and Gready 2.4 Floyd-Warshall **7.1** Binary Search 14 **7.2** Ternary Search 14 2.5 Euler 2.6 DSU Тгее 2.7 SCC 8 8.1 Binary Lifting LCA 14 8.2 Centroid Decomposition . 14 2.8 VBCC 2.9 EBCC Heavy Light Decomposition 14 2.10 2-SAT 8.4 8.5 Link Cut Tree 15 2.11 Functional Graph 4 Virtual Tree 15 8.6 Dominator Tree 16 3 Data Structure DΡ 16 **3.1** Segment Tree 4 **9.1 LCS** 16 3.2 Persistent Segment Tree . 5 3.3 Static Kth-element 3.4 Dynamic Kth-element . . . 5 **3.5 Fenwick** 6 3.6 Range Fenwick 3.7 Treap **9.8 SOS** 17 3.8 RMQ **9.9 CHT** 18 3.9 Mo 9.12 Codeforces Example . . . 18 Flow Matching **4.1 Dinic** 7 **4.2** Min Cut 8 4.3 MCMF 10.3 Max Euclidean Distance . . 21 4.4 Hungarian **4.5** Theorem 8 5 String 10.7 Polygon Union Area 21 5.1 Hash 5.2 KMP 5.3 Z Function 5.4 Manacher 12 Else **12.1 Python** 24 **5.6 SA** 9 5.8 Palindrome Tree 10 12.4 Division . . 12.5 Division-Python 25 **5.9 Duval** 10

1 Basic

1.1 Default Code [d41d8c]

```
1.2 Compare Fuction [d41d8c]
|// 1. sort, 二分搜刻在函式內 lambda 就好
|// 2. priority queue 小到大是 >, set 是 <
|// 3. set 不能 = , multiset 必須 =
// 4. 確保每個成員都要比到
|// 5. pbds_multiset 不要用 lower_bound
|// 6. 如果要用 find, 插入 inf 後使用 upper_bound
// 7. multiset 可以跟 set 一樣使用,但請注意第 3、4 點 auto cmp = [](int i, int j) { return i > j; }; priority_queue<int, vector<int>, decltype(cmp)> pq(cmp);
  vector <int> a {1, 2, 5, 4, 3}; // 小心不要改到 a
auto cmp = [&a](int i, int j) { return a[i] > a[j]; };
priority_queue <int, vector <int>, decltype(cmp)> pq(cmp);
   1.3 Pbds [d41d8c]
  #include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
  using namespace __gnu_pbds;
template < class T>
   using pbds_set = tree<T, null_type,</pre>
   less<T>, rb_tree_tag, tree_order_statistics_node_update >;
template < class T >
  using pbds_multiset = tree<T, null_type, less_equal
    <T>, rb_tree_tag, tree_order_statistics_node_update>;
   1.4 Double [85f18f]
          double x;
         double x;
D(double x = 0.0) : x{x} {};
constexpr static double eps = 1E-12;
explicit operator double() const { return x; }
D operator () const { return D(-x); }
D &operator+=(D b) & { x += b.x; return *this; }
D &operator-=(D b) & { x *= b.x; return *this; }
D &operator/=(D b) & { x *= b.x; return *this; }
D &operator/=(D b) & { x *= b.x; return *this; }

                 assert(fabs(b.x) > eps);
x /= b.x; return *this;
          friend D operator+(D a, D b) { return a += b;
friend D operator-(D a, D b) { return a -= b;
friend D operator*(D a, D b) { return a *= b;
friend D operator/(D a, D b) { return a /= b;
          friend istream & operator >> (istream & is, D & a) {
                 double v; is >> v; a = D(v); return is
           friend ostream &operator << (ostream &os, const D &a) {</pre>
                 return os << fixed << setprecision
(9) << a.x + (a.x > 0 ? eps : a.x < 0 ? -eps : 0);
              // eps should < precision
          friend bool operator <(D lhs, D rhs) {
   return lhs.x - rhs.x < -eps;</pre>
          friend bool operator > (D lhs, D rhs) {
    return lhs.x - rhs.x > eps;
          friend bool operator == (D lhs, D rhs) {
    return fabs(lhs.x - rhs.x) < eps;</pre>
```

1.5 Int128 [85923a]

D abs(D a) { return a < 0 ? -a : a; }

```
using i128 = __int128_t; // 1.7E38
istream &operator >> (istream &is, i128 &a) {
    i128 sgn = 1; a = 0;
    string s; is >> s;
    for (auto c : s) {
        if (c == '-') {
            sgn = -1;
        } else {
            a = a * 10 + c - '0';
        }
    }
    a *= sgn;
    return is;
}
ostream &operator << (ostream &os, i128 a) {
    string res;
    if (a < 0) os << '-', a = -a;
    while (a) {
        res.push_back(a % 10 + '0');
        a /= 10;
    }
    reverse(res.begin(), res.end());
    os << res;
    return os;
}</pre>
```

1.6 Rng [401544]

```
mt19937_64 rng
          (chrono::steady_clock::now().time_since_epoch().count());
ll x = rng();
shuffle(a.begin(), a.end(), rng);
```

2 Graph

2.1 DFS And BFS [1f02d8]

```
void dfsBfs() {
     vector <vector <int>> adj(n);
// dfs_graph
vector <bool> vis(n);
      auto dfs = [&](auto self, int u) -> void {
   if (vis[u]) return;
           vis[u] = true;
for (auto v: adj[u]) {
    self(self, v);
           }
     dfs(dfs, 0);
      // bfs
     vector < int > dep(n, -1);
auto bfs = [&](auto self, int s) -> void {
          }
                }
          }
     bfs(bfs, 0);
}
```

2.2 Prim [cefbbf]

```
auto prim :
      [&](int n, vector<vector<pair<int, int>>> &adj) -> bool {
int sz = 0; ll ans = 0;
priority_queue<pair<int, int>,
    vector<pair<int, int>>, greater<pair<int, int>>> pq;
      pq.emplace(0, 0); // w, vertex
vector<bool>
vis(n);
     pq.emplace(w, v);
      if (sz == n) return true;
return false;
```

2.3 Bellman-Ford [430de2]

};

```
用 Bellman Ford 找負環
void bellmanFord() {
       int n, m; cin >> n >> m;
vector<array<int, 3>> e;
for (int i = 0; i < m; i++) {</pre>
                int u, v, w; cin >> u >> v >> w;
u--, v--; e.push_back({u, v, w});
       }
vector<ll> dis(n, inf), par(n);
int t = -1; dis[0] = 0;
for (int i = 1; i <= n; i++) {
    for (auto [u, v, w] : e) {
        if (dis[v] > dis[u] + w) {
            dis[v] = dis[u] + w;
            corrul = u;
}
                                  par[v] = u;
                                  if (i == n) t = v;
                        }
                }
       if (t == -1) { cout << "NO|n"; return; }
for (int i = 1; i < n; i++) t = par[t];
vector <int> ans {t};
        int i = t;
       do {
    i = par[i];
    rush_ba
       ans.push_back(i);
} while (i != t);
reverse(ans.begin(), ans.end());
                          "YES\n'
        for (auto x : ans) cout << x + 1 << " ";</pre>
```

2.4 Floyd-Warshall [db13dd]

```
const ll inf = 1E18;
void floydWarshall(int n, int m) {
  int n, m; cin >> n >> m;
  vector<vector<int>> dis(n, vector<int>(n, inf));
         for (int i = 0; i < m; i++) {
  int u, v, w; cin >> u >> v >> w;
  dis[u][v] = min(dis[u][v], w);
  dis[v][u] = min(dis[v][u], w);
```

```
] = min(dis[i][j], dis[i][k] + dis[k][j]);
}
2.5 Euler [4177dc]
// 1. 無向圖是歐拉圖:
// 非零度頂點是連通的
// 頂點的度數都是偶數
| // 2. 無向圖是半歐拉圖(有路沒有環):
| // 非零度頂點是連通的
// 恰有 2 個奇度頂點
// 3. 有向圖是歐拉圖:
// 非零度頂點是強連通的
// 每個頂點的入度和出度相等
// 4. 有向圖是半歐拉圖(有路沒有環):
// 非零度頂點是弱連通的
```

2.6 DSU [6bd5f4]

dfs(dfs, 0);

// 至多一個頂點的出度與入度之差為 1 // 至多一個頂點的入度與出度之差為 1

> while (g[u].size()) {
> int v = *g[u].begin(); g[u].erase(v);

self(self, v);

reverse(ans.begin(), ans.end());

ans.push back(u):

vector(int> ans;
auto dfs = [&](auto &&self, int u) -> void {

// 其他頂點的入度和出度相等

```
struct DSU {
       int n:
       vector <int> f, siz;
DSU(int n) : n(n), f(n), siz(n, 1) {
    iota(f.begin(), f.end(), 0);
       int find(int x) {
   if (f[x] == x) return x;
   return f[x] = find(f[x]);
       bool same(int x, int y) {
    return find(x) == find(y);
       bool merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return false;
    if (siz[x] < siz[y]) swap(x, y);</pre>
              siz[x] += siz[y];
              f[y] = x;
              return true;
       int size(int x) {
              return siz[find(x)];
      }
struct DSU {
       int n;
       vector <int> f, siz, stk;
DSU(int n) : n(n), f(n), siz(n, 1) {
    iota(f.begin(), f.end(), 0);
              stk.clear():
       int find(int x) {
    return x == f[x] ? x : find(f[x]);
       bool same(int x, int y) {
    return find(x) == find(y);
       bool merge(int x, int y)
             if (x == y); y = find(y);
if (x == y) return false;
if (siz[x] < siz[y]) swap(x, y);</pre>
              siz[x] += siz[y];
              f[y] = x;
              stk.push_back(y);
              return true;
       void undo(int x) {
              while (stk.size() > x) {
```

```
National Chung Cheng University Salmon
              int y = stk.back();
              stk.pop_back();
              "++;
siz[f[y]] -= siz[y];
f[y] = y;
     int size(int x) {
          return siz[find(x)];
    }
}:
2.7 SCC [3ac1cb]
struct SCC {
   int n, cur, cnt;
     vector<vector<int>> adj;
    stk.push_back(x);
         for (auto y : adj[x]) {
    if (dfn[y] == -1) {
                   `dfs(y);
              low[x] = min(low[x], low[y]);
} else if (bel[y] == -1) {
                   low[x] = min(low[x], dfn[y]);
              }
          if (dfn[x] == low[x]) {
              int y;
              do {
                   y = stk.back();
              bel[y] = cnt;
stk.pop_back();
while (y != x);
              cnt++;
         }
     vector < int > work() {
    for (int i = 0; i < n; i++)
        if (dfn[i] == -1) dfs(i);</pre>
          return bel;
     struct Graph {
          int n;
         vector<pair<int, int>> edges;
vector<int> siz, cnte;
     Graph compress() {
         Graph g;
g.n = cnt;
          g.siz.resize(cnt);
         g.edges.emplace_back(bel[i], bel[j]);
                        g.cnte[bel[i]]++;
                   }
              }
          return g;
    }
};
2.8 VBCC [95997d]
struct VBCC {
    void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
    stk.push_back(x);
          int ch = 0;
         for (auto y : adj[x]) {
    if (y == p) continue;
    if (dfn[y] == -1) {
                   dfs(y, x), ch++;
low[x] = min(low[x], low[y]);
if (low[y] >= dfn[x]) {
                        int v;
                        do {
```

v = stk.back(); bcc[v].push_back(cnt);

stk.pop_back();
} while (v != y);
bcc[x].push_back(cnt);

cnt++;

```
} else {
                           low[x] = min(low[x], dfn[y]);
              if (p == -1 && ch > 1) ap[x] = true;
       vector <bool> work() {
    for (int i = 0; i < n; i++)
        if (dfn[i] == -1) dfs(i, -1);</pre>
       struct Graph {
             vector<pair<int, int>> edges;
vector<int> bel, siz, cnte;
       Graph compress() {
             Graph g; // 壓完是一棵樹,但不一定每個 bel 都有節點 g.bel.resize(n); g.siz.resize(cnt);
              g.cnte.resize(cnt);
              for (int u = 0; u < n; u++) {
   if (ap[u]) {
      g.bel[u] = cnt++;
}</pre>
                           g.siz.emplace_back()
                          g.cnte.emplace_back();
for (auto v : bcc[u]) {
                                g.edges.emplace_back(g.bel[u], v);
                    } else if (bcc[u].size() == 1) {
   g.bel[u] = bcc[u][0];
                    g.siz[g.bel[u]]++;
             }
g.n = cnt;
for (int i = 0; i < n; i++)
    for (auto j : adj[i])
        if (g.bel[i] == g.bel[j] && i < j)
            g.cnte[g.bel[i]]++;</pre>
};
 2.9 EBCC [12a170]
 struct EBCC { // CF/contest/1986/pF
       int n, cur, cnt;
vector<vector<int>> adj;
       vector<int> stk, dfn, low, bel;
vector<pair<int, int>> bridges; // 關鍵邊
       low(n), dfn(n, -1), bel(n, -1) {}
       void dfs(int x, int p) {
    dfn[x] = low[x] = cur++;
              stk.push_back(x);
              for (auto y : adj[x]) {
   if (y == p) continue;
   if (dfn[y] == -1) {
                          dfs(y, x);
low[x] = min(low[x], low[y]);
if (low[y] > dfn[x]) {
                                 bridges.emplace_back(x, y);
                    } else if (bel[y] == -1) {
   low[x] = min(low[x], dfn[y]);
              if (dfn[x] == low[x]) {
                    int y;
do {
                          y = stk.back();
                          bel[y] = cnt;
                    stk.pop_back();
} while (y != x);
             }
       vector<int> work() { // not connected
    for (int i = 0; i < n; i++)
        if (dfn[i] == -1) dfs(i, -1);</pre>
             return bel;
       struct Graph {
              int n:
             vector<pair<int, int>> edges;
vector<int> siz, cnte;
       Graph compress() {
             Graph g;
g.n = cnt;
              g.siz.resize(cnt);
             g.cnte.resize(cnt);
for (int i = 0; i < n; i++) {
    g.siz[bel[i]]++;
    for (auto j : adj[i]) {</pre>
```

2.10 2-SAT [28688f]

```
struct TwoSat {
     int n; vector<vector<int>> e;
vector<bool> ans;
     TwoSat(int n) : n(n), e(2 * n), ans(n) {}
void addClause(int u, bool f, int v, bool g) {
    e[2 * u + !f].push_back(2 * v + g);
           e[2 * v + !g].push_back(2 * u + f);
      void ifThen(int u, bool f, int v, bool g) {
           // 必取 A: not A -> A
e[2 * u + !f].push_back(2 * v + g);
     bool satisfiable() {
           vector<int
                  > id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
           vector<int> stk;
int now = 0, cnt = 0;
function<void(int)> tarjan = [&](int u) {
                stk.push_back(u);
dfn[u] = low[u] = now++;
for (auto v : e[u]) {
    if (dfn[v] == -1) {
                       tarjan(v);
  low[u] = min(low[u], low[v]);
} else if (id[v] == -1) { // in stk
  low[u] = min(low[u], dfn[v]);
                       }
                 if (dfn[u] == low[u]) {
                       int v;
do {
                            v = stk.back();
                            stk.pop_back();
id[v] = cnt;
                       } while (v != u);
                       ++cnt:
                }
           for (int i
           return true:
     vector<bool> answer() { return ans; }
```

2.11 Functional Graph [c314e3]

```
}
int jump(int u, int k) {
    for (int b = 0; k > 0; b++) {
        if (k & 1) u = cht[u][b];
        k >>= 1;
    }
    return u;
}
```

3 Data Structure

3.1 Segment Tree [d41d8c]

```
template < class Info, class Tag = bool() > struct SegmentTree \{ \ // \ [l, \ r), \ uncomment \ /**/ \ to \ lazy \}
      int n;
      vector < Info > info;
      ,
vector<Tag> tag;
      template < class T>
      SegmentTree(const vector<T> &init) {
           n = init.size();
            info.assign(4 << __lg(n), Info());</pre>
            tag.assign(4 << __lg(n), Tag());
            function < void (
                  int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
                        info[p] = init[l];
                        return;
                  int m = (l + r) / 2;
build(2 * p, l, m);
build(2 * p + 1, m, r);
                 pull(p);
            build(1, 0, n);
      void pull(int p) {
    info[p] = info[2 * p] + info[2 * p + 1];
      ,
void apply(int p, int l, int r, const Tag &v) {
    info[p].apply(l, r, v);
    tag[p].apply(v);
      void push(int p, int l, int r) {
   int m = (l + r) / 2;
   if (r - l >= 1) {
      apply(2 * p, l, m, tag[p]);
      apply(2 * p + 1, m, r, tag[p]);
}
            tag[p] = Tag();
      void modify(int p, int l, int r, int x, const Info &v) {
    if (r - l == 1) {
        info[p] = v;
}
                  return;
            int m = (l + r) / 2;
            push(p, l, r);
            if (x < m) {
                  modify(2 * p, l, m, x, v);
            } else {
                  modify(2 * p + 1, m, r, x, v);
            pull(p);
      void modify(int p, const Info &i) {
            modify(1, 0, n, p, i);
      Info query(int p, int l, int r, int ql, int qr) {
   if (qr <= l || ql >= r) return Info();
   if (ql <= l && r <= qr) return info[p];</pre>
            int m = (l + r) / 2;
            push(p, l, r);
                  p, l, m, ql, qr) + query(2 * p + 1, m, r, ql, qr);
      Info query(int ql, int qr) {
            return query(1, 0, n, ql, qr);
      void rangeApply
            (int p, int l, int r, int ql, int qr, const Tag &v) {
if (qr <= l || ql >= r) return;
if (ql <= l && r <= qr) {
                  apply(p, l, r, v);
                  return;
            int m = (l + r) / 2;
push(p, l, r);
rangeApply(2 * p, l, m, ql, qr, v);
rangeApply(2 * p + 1, m, r, ql, qr, v);
```

```
pull(p):
      void rangeApply(int l, int r, const Tag &v) {
           rangeApply(1, 0, n, l, r, v);
      template < class F> // 尋找區間內,第一個符合條件的
      int findFirst
           (int p, int l, int r, int x, int y, F &&pred) {
if (l >= y || r <= x) return -1;
if (l >= x && r <= y && !pred(info[p])) return -1;
if (r - l == 1) return l;
int m = (l + r) / 2;</pre>
           push(p, l, r);
            int res = findFirst(2 * p, l, m, x, y, pred);
           if (res == -1)
    res = findFirst(2 * p + 1, m, r, x, y, pred);
           return res;
     template < class F> // 若要找 last, 先右子樹遞廻即可int findFirst(int l, int r, F & & pred) {
           return findFirst(1, 0, n, l, r, pred);
// 有些 Tag 不用 push 例如 sweepLine
struct Tag {
   int setVal = 0;
      int add = 0;
      void apply(const Tag &t) & {
           if (t.setVal) {
    setVal = t.setVal;
           add = t.add;
} else {
    add += t.add;
     }
struct Info {
    ll sum = 0;
    /*
     void apply(int l, int r, const Tag &t) & {
    if (t.setVal) {
        sum = (r - l) * t.setVal;
    }
           sum += (r - l) * t.add;
     }
*/
     // we/s assignment 使用
// Info &operator=(const Info &rhs) & {
// return *this;
// }
     // 部分 assignment 使用
     Info &operator=(const ll &rhs) & {
           sum = rhs;
return *this;
Info operator+(const Info &a, const Info &b) {
     Info c;
c.sum = a.sum + b.sum;
     return c;
}
```

3.2 Persistent Segment Tree [d41d8c]

```
template < class Info >
struct PST {
    struct Node {
           Info info = Info();
           int lc = 0, rc = 0;
     vector <Node > nd;
vector <int > rt;
template <class T >
     PST(const vector<T> &init) {
    n = init.size();
    nd.assign(1, Node());
           rt.clear();
           function<int(int, int)> build = [&](int l, int r) {
  int id = nd.size();
                 nd.emplace_back();
                 if (r - l == 1) {
   nd[id].info = init[l];
                      return id;
                 int m = (l + r) >> 1;
                nd[id].lc = build(l, m);
nd[id].rc = build(m, r);
pull(nd[id]);
                 return id;
           rt.push_back(build(0, n));
      void pull(Node &t) {
           t.info = nd[t.lc].info + nd[t.rc].info;
     int copy(int t) { // copy 一個 node
```

```
nd.push_back(nd[t]);
return nd.size() - 1
      }
      int generate() { // 創立新的 node nd.emplace_back();
            return nd.size() - 1;
      int modify(int t, int l, int r, int x, const Info &v) {
   t = t ? copy(t) : generate();
   if (r - l == 1) {
                 nd[t].info = v;
                 return t:
            int m = (l + r) / 2;
           if (x < m) {
    nd[t].lc = modify(nd[t].lc, l, m, x, v);</pre>
                 nd[t].rc = modify(nd[t].rc, m, r, x, v);
           pull(nd[t]);
      void modify(int ver, int p, const Info &i) {
   if (int(rt.size()) <= ver) rt.resize(ver + 1);</pre>
            rt[ver] = modify(rt[ver], 0, n, p, i);
      Info query(int t, int l, int r, int ql, int qr) {
    if (l >= qr || r <= ql) return Info();
    if (ql <= l && r <= qr) return nd[t].info;
    int m = (l + r) / 2;</pre>
            return query(nd[t].
                  lc, l, m, ql, qr) + query(nd[t].rc, m, r, ql, qr);
      Info query(int ver, int ql, int qr) {
            return query(rt[ver], 0, n, ql, qr);
      void createVersion(int ori_ver)
           rt.push_back(copy(rt[ori_ver]));
      void reserve(int n, int q) {
    nd.reserve(n + q * (2 * _
           nd.reserve(n + q * rt.reserve(q + 1);
                                              __lg(n) + 1));
      void resize(int n) { rt.resize(n); }
struct Info {
     ll sum = 0;
Info operator+(const Info &a, const Info &b) {
    return { a.sum + b.sum };
```

3.3 Static Kth-element [d41d8c]

```
template < class
struct StaticKth : PST<int> {
   int dct(T x) {
           return lower_bound(s.begin(), s.end(), x) - s.begin();
      vector<T> v, s; // array, sorted
map<T, int> cnt;
      StaticKth(const vector<T> &v_) {
            sort(s.begin(), s.end());
            s.resize(unique(s.begin(), s.end()) - s.begin());
           init(s.size());
for (int i = 0; i < v.size(); i++) {</pre>
                 createVersion(i);
                 int d = dct(v[i]);
modify(i + 1, d, ++cnt[d]);
      int work(int a, int b, int l, int r, int k) {
   if (r - l == 1) return l;
   int x = nd[nd[b].lc].info - nd[nd[a].lc].info;
           int m = (l + r) / 2;
if (x >= k) {
                 return work(nd[a].lc, nd[b].lc, l, m, k);
           } else {
                 return work(nd[a].rc, nd[b].rc, m, r, k - x);
      int work(int l, int r, int k) { // [l, r), k > 0
    return s[work(rt[l], rt[r], 0, n, k)];
};
```

3.4 Dynamic Kth-element [d41d8c]

```
′ Fenwick(rt-indexed) 包線段樹
template < class T>
struct DynamicKth : PST < int > {
      int dct(T x) {
           return lower_bound(s.begin(), s.end(), x) - s.begin();
      vector<T> v, s; // array, sorted
DynamicKth(const vector<T> &v_, const vector<T> &s_)
: PST<int>(vector<int>(s_.size(), 0)) {
           assert(is_sorted(s_.begin(), s_.end()));
v = v_, s = s_;
           rt.resize(v.size());
```

```
i = 0; i < v.size(); i++) add(i, dct(v[i]), 1);
      int modify(int t, int l, int r, int x, int v) {
    t = t ? t : generate();
    if (r - l == 1) {
        nd[t].info += v;
    }
}
                   return t;
             int m = (l + r) / 2;
             if (x < m) {
                    nd[t].lc = modify(nd[t].lc, l, m, x, v);
             } else {
   nd[t].rc = modify(nd[t].rc, m, r, x, v);
              pull(nd[t]);
              return t;
       void add(int p, int x, int val) {
    for (int i = p + 1; i <= rt.size(); i += i & -i)
        rt[i - 1] = modify(rt[i - 1], 0, s.size(), x, val);</pre>
       void modify(int p, int y) {
   add(p, dct(v[p]), -1);
   v[p] = y;
              add(p, dct(v[p]), 1);
             vector<int> &a, vector<int> &b, int l, int r, int k) {
if (r - l == 1) return l;
int m = (l + r) / 2;
              int res = 0;
             for (auto x : a) res -= nd[nd[x].lc].info;
for (auto x : b) res += nd[nd[x].lc].info;
if (res >= k) {
                    for (auto &x : a) x = nd[x].lc;
for (auto &x : b) x = nd[x].lc;
return work(a, b, l, m, k);
             } else {
                    for (auto &x : a) x = nd[x].rc;
for (auto &x : b) x = nd[x].rc;
                    return work(a, b, m, r, k - res);
       int work(int l, int r, int k) { // [l, r), k > 0
             vector < int > a, b;
for (int i = l; i > 0; i -= i & -i)
    a.push_back(rt[i - 1]);
             for (int i = r; i > 0; i -=
    b.push_back(rt[i - 1]);
             return s[work(a, b, 0, s.size(), k)];
};
```

3.5 Fenwick [d41d8c]

```
template < class T >
struct Fenwick {
       int n; vector<T> a;
Fenwick(int n) : n(n), a(n) {}
void add(int x, const T &v) {
              for (int i = x + 1; i <= n; i += i & -i)
a[i - 1] = a[i - 1] + v;
       T sum(int x) {
              T ans{};
               for (int i = x; i > 0; i -= i & -i)
    ans = ans + a[i - 1];
               return ans:
      T rangeSum(int l, int r) {
    return sum(r) - sum(l);
       int select(const T &k, int start = 0) {
               // 找到最小的 x, 使得 sum(x + 1) - sum(start) > k
               int x = 0; T cur = -sum(start);
for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n && cur + a[x + i - 1] <= k) {</pre>
                              cur = cur + a[x - 1];
                      }
               return x;
      }
template < class T>
struct TwoDFenwick {
      int nx, ny; // row, col 個數
vector-vector<T>> a;
TwoDFenwick(int nx, int ny): nx(nx), ny(ny) {
    a.assign(nx, vector<T>(ny, T{}));
       void add(int x, int y, const T &v) {
    for (int i = x + 1; i <= nx; i += i & -i)
        for (int j = y + 1; j <= ny; j += j & -j)
        a[i - 1][j - 1] = a[i - 1][j - 1] + v;</pre>
       T sum(int x, int y) {
              T ans{};
for (int i = x; i > 0; i -= i & -i)
    for (int j = y; j > 0; j -= j & -j)
        ans = ans + a[i - 1][j - 1];
```

3.6 Range Fenwick [d41d8c]

```
| template < class T>
 struct RangeFenwick { // 全部以 0 based 使用
         int n:
         vector<T> d, di;
        Vector<i> d, di;
RangeFenwick(int n) : n(n), d(n), di(n) {}
void add(int x, const T &v) {
    T vi = v * (x + 1);
    for (int i = x + 1; i <= n; i += i & -i) {
        d[i - 1] = d[i - 1] + v;
        di[i - 1] = di[i - 1] + v;
}</pre>
         void rangeAdd(int l, int r, const T &v) {
  add(l, v); add(r, -v);
         T sum(int x) { // 左閉右開查詢
               for (int i = x; i > 0; i -= i & -i) {
    ans = ans + T(x + 1) * d[i - 1];
    ans = ans - di[i - 1];
               return ans:
        TrangeSum(int l, int r) { // 左閉右開查詢 return sum(r) - sum(l);
         int select(const T &k, int start = 0) {
               // 找到最小的 x, 使得 sum(x + 1) - sum(start) > k
int x = 0; T cur = -sum(start);
for (int i = 1 << __lg(n); i; i /= 2) {
    if (x + i <= n) {
        T val = T(
                                     x + i + 1) * d[x + i - 1] - di[x + i - 1];
                             if (cur + val <= k) {
    x += i;</pre>
                                    cur = cur + val;
                             }
                      }
               return x;
       }
  template < class T>
 struct RangeTwoDFenwick { // 全部以 0 based 使用
        int nx, ny; // row, col 個數
vector<vector<T>> d, di, dj, dij;
RangeTwoDFenwick(int x, int y): nx(x), ny(y) {
    d.assign(nx, vector<T>(ny, T{}));
    di.assign(nx, vector<T>(ny, T{}));
    dj.assign(nx, vector<T>(ny, T{}));
               dij.assign(nx, vector<T>(ny, T{}));
         void add(int x, int y, const T &v) {
               T vi = v * (x + 1);

T vj = v * (y + 1);

T vj = v * (y + 1);

T vij = v * (x + 1) * (y + 1);

for (int i = x + 1; i <= nx; i += i & -i) {
                      for (int j = y + 1; j <= ny; j += j & -j) {
    d[i - 1][j - 1] = d[i - 1][j - 1] + v;
    di[i - 1][j - 1] = di[i - 1][j - 1] + vi;
    dj[i - 1][j - 1] = dj[i - 1][j - 1] + vj;
    dij[i - 1][j - 1] = dij[i - 1][j - 1] + vj;</pre>
              }
         void rangeAdd(int lx, int ly, int rx, int ry, const T &v) {
               add(rx, ry, v);
               add(lx, ry, -v);
add(rx, ly, -v);
add(lx, ly, v);
         T sum(int x, int y) { // 左閉右開查詢
               T ans{};
for (int i = x; i > 0; i -= i & -i) {
                       for (int j = y; j > 0; j -= j & -j) {
                             ans = ans
                             }
               return ans;
                (int lx, int ly, int rx, int ry) { // 左閉右開查詢
                       (x, y) - sum(x, y) - sum(x, y) + sum(x, y);
        }
};
```

3.7 Treap [d41d8c]

```
val += t.add;
sum += 1LL * siz * t.add;
template < class Info, class Tag = bool()>
struct Treap { // 0 -> initial root
  vector<Info> info;
                                                                                                           void pull(const Info &l, const Info &r) {
                                                                                                                 sum = val + l.sum + r.sum;
      // vector<Tag> tag;
     }
                                                                                                    };
                                                                                                    3.8 RMQ [d41d8c]
                                                                                                     template < class T, class F = less < T >>
struct RMQ { // [l, r)
                  siz[i] = 1, pri[i] = rand();
                                                                                                           int n;
     // void apply(int t, const Tag &v) {
// info[t].apply(siz[t], v);
// tag[t].apply(v);
// }
void push(int t) {
                                                                                                           F cmp = F();
vector<vector<T>> g;
                                                                                                           RMQ() {}
                                                                                                           RMQ(const vector<T> &a, F cmp = F()) : cmp(cmp) {
                                                                                                                 init(a):
            if (rev[t]) {
                 swap(ch[t][0], ch[t][1]);
if (ch[t][0]) rev[ch[t][0]] ^= 1;
if (ch[t][1]) rev[ch[t][1]] ^= 1;
                                                                                                           void init(const vector<T> &a) {
                                                                                                                 n = a.size();
int lg = __lg(n);
g.resize(lg + 1);
                  rev[t] = 0;
                                                                                                                // apply(ch[t][0], tag[t]);
// apply(ch[t][1], tag[t]);
// tag[t] = Tag();
      void pull(int t) {
    siz[t] = 1 + siz[ch[t][0]] + siz[ch[t][1]];
    info[t].pull(info[ch[t][0]], info[ch[t][1]]);
                                                                                                           formula | Toperator()(int l, int r) {
    assert(0 <= l && l < r && r <= n);
    int lg = __lg(r - l);
    return min(g[lg][l], g[lg][r - (1 << lg)], cmp);
}</pre>
     int merge(int a, int b) {
    if (!a || !b) return a ? a : b;
           push(a), push(b);
if (pri[a] > pri[b]) {
   ch[a][1] = merge(ch[a][1], b);
   pull(a); return a;
                                                                                                    };
                                                                                                     3.9 Mo [d41d8c]
                 ch[b][0] = merge(a, ch[b][0]);
pull(b); return b;
                                                                                                    struct Query { int id, l, r; };
void mo(vector<Query> &q) {
                                                                                                           int blk = sqrt(q.size());
     pair < int, int > split(int t, int k) {
                                                                                                           sort(q.begin
            if (!t) return {0, 0};
                                                                                                                 (), q.end(), [&](const Query &a, const Query &b) {
  int x = a.l / blk, y = b.l / blk;
  return x == y ? a.r < b.r : x < y;
            push(t);
            if (siz[ch[t][0]] >= k) {
    auto [a, b] = split(ch[t][0], k);
    ch[t][0] = b, pull(t);
                                                                                                    return {a, t};
            } else {
                  auto [a
                 , b] = split(ch[t][1], k - siz[ch[t][0]] - 1);
ch[t][1] = a, pull(t);
return {t, b};
                                                                                                           while (nl < l) delL(), nl++;
           }
     }
     template < class F> // 尋找區間內,第一個符合條件的int findFirst(int t, F & & pred) {
                                                                                                            Flow Matching
            if (!t) return 0;
                                                                                                     4.1 Dinic [d41d8c]
            push(t);
            if (!pred(info[t])) return 0;
int idx = findFirst(ch[t][0], pred);
if (!idx) idx
                                                                                                    template < class T>
struct Dinic {
                                                                                                           struct Edge {
                    = 1 + siz[ch[t][0]] + findFirst(ch[t][1], pred);
                                                                                                                 int to;
                                                                                                                 T f, cap; // 流量跟容量
     int getPos(int rt, int t) { // get t's index in array
  int res = siz[t] + 1;
                                                                                                           int n, m, s, t;
const T INF_FlOW = numeric_limits<T>::max();
            while (t != rt)
                 int p = par[t];
                                                                                                           vector < vector < int >> g;
                  if (ch[p][1] == t) res += siz[ch[p][0]] + 1;
                                                                                                           vector<Edge> e;
                                                                                                           vector < int > h, cur;
Dinic(int n) : n(n), m(0), g(n), h(n), cur(n) {}
void addEdge(int u, int v, T cap) {
    e.push_back({v, 0, cap});
    e.push_back({u, 0, 0});

                  t = p;
            return res;
      void getArray(int t, vector<Info> &a) {
                                                                                                                 g[u].push_back(m++);
g[v].push_back(m++);
            if (!t) return;
            push(t);
            getArray(ch[t][0], a);
a.push_back(info[t]);
                                                                                                           bool bfs() {
                                                                                                                 fill(h.begin(), h.end(), -1);
h[s] = 0; queue<int> q;
            getArray(ch[t][1], a);
                                                                                                                 q.push(s);
                                                                                                                 q.push(s);
while (!q.empty()) {
   int u = q.front(); q.pop();
   for (int id : g[u]) {
     auto [v, f, cap] = e[id];
     if (f == cap) continue;
     if (h[v] == -1) {
        h[v] = h[u] + 1;
        if (v == t) return true;
        a push(v):
struct Tag {
   int setVal; ll add;
      void apply(const Tag &t) {
           if (t.setVal) {
    setVal = t.setVal;
                  add = t.add;
           } else {
   add += t.add;
                                                                                                                                    q.push(v);
     }
                                                                                                                             }
                                                                                                                       }
struct Info {
      ll val, sum;
                                                                                                                 return false;
      void apply(int siz, const Tag &t) {
           if (t.setVal) {
   val = t.setVal;
                                                                                                           T dfs(int u, T flow) {
                                                                                                                 if (flow == 0) return 0;
if (u == t) return flow;
                  sum = 1LL * siz * t.setVal;
```

```
for (int &i = cur[u]; i < g[u].size(); i++) {
   int j = g[u][i];
   auto [v, f, cap] = e[j];
   if (h[u] + 1 != h[v]) continue;
   if (f == cap) continue;</pre>
                 return mn;
                 }
            return 0:
     while (true) {
  T res = dfs(s, INF_Flow);
  if (res == 0) break;
                 }
     void reuse(int n_) { // 走殘留網路, res += f
while (n < n_) {
    g.emplace_back();
    h.emplace_back();
                  cur.emplace_back();
                  n += 1:
           }
};
4.2 Min Cut [d41d8c]
```

```
void minCut(int n, int m, Dinic<int> d) {
       int ans = d.work(0, n - 1);
cout << ans << "\n";
vector <int> vis(n);
       auto dfs = [&](auto self, int u) -> void {
               if (!vis[u]) {
                     vis[u] = 1;
for (int id : d.g[u]) {
   auto [to, f, cap] = d.e[id];
   if (cap - f > 0) {
                                     self(self, to);
                      }
              }
       for (int i = 0; i < n; i++) {
   if (!vis[i]) continue;
   for (int id : d.g[i]) {
      if (id & 1) continue;
      auto e = d.e[id];
      if (id & 1) [</pre>
                      if (!vis[e.to]) {
                              cout << i + 1 << " " << e.to + 1 << "\n";
              }
}
```

4.3 MCMF [d41d8c]

```
template < class Tf, class Tc>
struct MCMF {
    struct _Edge {
        int to;
}
                 Tf f, cap; // 流量跟容量
                 Tc cost:
        int n, m, s, t;
const Tf INF_FLOW = numeric_limits<Tf>::max();
const Tc INF_COST = numeric_limits<Tc>::max();
        vector<_Edge> e;
         vector<vector<int>> g;
       vector < vector < int>> g;
vector < Tc> dis;
vector < Tc> dis;
vector < int> rt, inq;
MCMF(int n) : n(n), m(0), g(n) {}
void addEdge(int u, int v, Tf cap, Tc cost) {
    e.push_back({v, 0, cap, cost});
    e.push_back({u, 0, 0, -cost});
    g[u].push_back(m++);
                g[v].push_back(m++);
        bool spfa() {
                 dis.assign(n, INF_COST);
rt.assign(n, -1), inq.assign(n, 0);
queue<int> q; q.push(s);
                 dis[s] = 0;
                 while (!q.empty()) {
                         int u = q.front(); q.pop();
inq[u] = 0;
                          Inq[u] = 0;
for (int id : g[u]) {
    auto [v, f, cap, cost] = e[id];
    Tc ndis = dis[u] + cost;
    if (f < cap && dis[v] > ndis) {
                                           dis[v] = ndis, rt[v] = id;
```

```
if (!ina[v])
                                 q.push(v), inq[v] = 1;
                      }
                }
           return dis[t] != INF_COST;
     }
     // 限定 flow,最小化 cost
pair<Tf, Tc> workFlow(int s_, int t_, Tf need) {
           s = s_, t = t_;
           Tf flow{}; Tc co
while (spfa()) {
    Tf f = need;
                 for (int i = t; i != s; i = e[rt[i] ^ 1].to)
                f = min(f, e[rt[i]].cap - e[rt[i]].f);
for (int i = t; i != s; i = e[rt[i] ^ 1].to)
    e[rt[i]].f += f, e[rt[i] ^ 1].f -= f;
flow += f, need -= f;
cost += f * dis[t];
                 if (need == 0) break;
           return {flow. cost}:
     }
    return {flow, cost};
     void reset() {
    for (int i = 0; i < m; i++) e[i].f = 0;</pre>
};
```

4.4 Hungarian [d41d8c]

```
struct Hungarian { // 0-based, O(VE)
         int n, m;
vector<vector<int>> adj;
         vector <int>> adj;
vector <int>> used, vis;
vector <pair <int, int>> match;
Hungarian(int n, int m) : n(n), m(m) {
   adj.assign(n + m, {});
   used.assign(n + m, -1);
   vis.assign(n + m, 0);
}
         void addEdge(int u, int v) {
   adj[u].push_back(n + v);
   adj[n + v].push_back(u);
         bool dfs(int u)
                 int sz = adj[u].size();
for (int i = 0; i < sz; i++) {
   int v = adj[u][i];
   int v = adj[u][i];</pre>
                         if (vis[v] == 0) {
    vis[v] = 1;
                                 if (used[v] == -1 || dfs(used[v])) {
    used[v] = u;
                                 }
                        }
                 return false;
          vector<pair<int, int>> work() {
                 match.clear();
                 used.assign(n + m, -1);
                 vis.assign(n + m, 0);
for (int i = 0; i < n; i++) {
    fill(vis.begin(), vis.end(), 0);</pre>
                         dfs(i):
                 for (int i = n; i < n + m; i++)
    if (used[i] != -1)</pre>
                                 match.emplace_back(used[i], i - n);
                 return match;
};
```

4.5 Theorem [d41d8c]

// 有向無環圖:

```
// 最小不相交路徑覆蓋:
// 最小路徑數 = 頂點數 - 最大匹配數
1// 最小相交路徑覆蓋:
// 先用
   Floyd 求傳遞封包,有連邊就建邊,然後再套最小不相交路徑覆蓋
```

```
| // 二分圖:
| // 最小點
| 覆蓋: 選出一些點,讓所有邊至少有一個端點在點集中的最少數量
| // 最小點覆蓋 = 最大匹配數
| // 還原解,flow 的作法是從源點開始 dfs,只走 cap - flow > 0
| // 的邊,最後挑選左邊還沒被跑過的點和右邊被跑過的點當作覆蓋的點
| // 最少邊覆蓋: 選出一些邊,讓所有點都覆蓋到的最少數量
| // 最少邊覆蓋 = 點數 - 最大匹配數
| // 最大獨立集: 選出一些點,使這些點兩兩沒有邊連接的最大數量
| // 最大獨立集 = 點數 - 最大匹配數
```

5 String

5.1 Hash [234076]

```
const int D = 59;
vector <int> rollingHash(string &s) {
    vector <int> a {0};
    for (auto c : s)
        a.push_back(mul(a.back(), D) + (c - 'A' + 1));
    return a;
}
int qryHash(vector <int> &h, int l, int r) { // [l, r)
    return sub(h[r], mul(h[l], power(D, r - l)));
}
```

5.2 KMP [e3717b]

5.3 Z Function [5b63dc]

```
| // z[i] 表示 s 和 s[i, n - 1] (以 s[i] 開頭的後綴)
| // 的最長公共前綴 (LCP) 的長度
vector < int > Z(const string &s) {
    int n = s.size();
    vector < int > z(n);
    z[0] = n; // lcp(s, s), -1 or n
    for (int i = 1, j = 1; i < n; i++) {
        z[i] = max(0, min(j + z[j] - i, z[i - j]));
        while (i + z[i] < n && s[z[i]] == s[i + z[i]])
        z[i]++;
        if (i + z[i] > j + z[j]) j = i;
    }
    return z;
}
```

5.4 Manacher [1eb30d]

```
# a # b # a #
 // # a # b # b # a #
// 1 2 1 2 5 2 1 2 1
 // 值 -1 代表原回文字串長度
|// (id - val + 1) / 2 可得原字串回文開頭
        Trie [6c7186]
 const int N = 1E7; // 0 -> initial state
const int ALPHABET_SIZE = 26;
 int tot = 0:
 int trie[N][ALPHABET_SIZE], cnt[N];
 void reset() {
  tot = 0, fill_n(trie[0], ALPHABET_SIZE, 0);
 int newNode() {
      int x = ++tot;
cnt[x] = 0, fill_n(trie[x], ALPHABET_SIZE, 0);
 void add(const string &s) {
      int p = 0;
      for (auto c : s) {
           int &q = trie[p][c - 'a'];
           if (!q) q = newNode();
      cnt[p] += 1;
 int find(const string &s) {
      int p = 0;
for (auto c : s) {
           int q = trie[p][c - 'a'];
if (!q) return 0;
           p = q;
      return cnt[p];
 5.6 SA [b04578]
 struct SuffixArray {
      vector<int> sa, rk, lc;
      // n: 字串長度
      // sa: 後綴數組, sa[i] 表示第 i 小的後綴的起始位置
      // rk: 排名數組, rk[i] 表示從位置 i 開始的後綴的排名 // lc: LCP
            數組,lc[i] 表示 sa[i] 和 sa[i+1] 的最長公共前綴長度
      SuffixArray(const string &s) {
           n = s.length();
sa.resize(n);
lc.resize(n - 1);
            rk.resize(n);
            iota(sa.begin(), sa.end(), 0);
            sort(sa.begin(), sa.
           end(), [&](int a, int b) { return s[a] < s[b]; });
rk[sa[0]] = 0;
for (int i = 1; i < n; i++)
                 rk[sa[i]]
                         = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
           vector < int > tmp, cnt(n);
tmp.reserve(n);
while (rk[sa[n - 1]] < n - 1) {</pre>
                 tmp.clear();
                 for (int
                 i = 0; i < k; i++) tmp.push_back(n - k + i);
for (auto i : sa) if (i >= k) tmp.push_back(i - k);
                 swap(rk, tmp); rk[sa[0]] = 0;
                 for (int
                       (tnc)
i = 1; i < n; i++) rk[sa[i]] = rk[sa[i - 1]] +
(tmp[sa[i - 1]] < tmp[sa[i]] || sa[i - 1] + k
== n || tmp[sa[i - 1] + k] < tmp[sa[i] + k]);
            for (int i = 0, j = 0; i < n; i++) {
   if (rk[i] == 0) {</pre>
                 j = 0;
} else {
   for (j -=
                            \bigcit{\frac{1}{3}} & 0; i + j < n && sa[rk[i] - 1] + j < n \\ && s[i + j] == s[sa[rk[i] - 1] + j]; j++); \\ k[i] - 1] = j;
                      lc[rk[i]
                 }
           }
      }
 RMQ<int> rmq(sa.lc);
auto lcp = [&](int i, int j) { // [i, j]
    i = sa.rk[i], j = sa.rk[j];
```

if (i > j) swap(i, j);

```
struct PAM {
    // 0 -> even root, 1 -> odd root
    static constexpr int ALPHABET_SIZE = 26;
    // fail -> longest prefix(suffix) palindrome
    // number end at i = end at link[last[i]] + 1
      assert(i != j);
return rmq(i, j);
};
5.7 SAM [50a2d0]
                                                                                                                struct Node {
                                                                                                                      int len, fail, cnt;
array<int, ALPHABET_SIZE> next;
struct SAM {
   // 0 -> initial state
   static constexpr int ALPHABET_SIZE = 26;
                                                                                                                      Node() : len{}, fail{}, next{} {}
      // node -> strings with the same endpos set
// link -> longest suffix with different endpos set
// len -> state's longest suffix
// fpos -> first endpos
// strlen range -> [len(link) + 1, len]
                                                                                                                vector<int> s:
                                                                                                                vector < Node > t;
                                                                                                               PAM() {
    t.assign(2, Node());
    t[0].len = 0, t[0].fail = 1;
    t[1].len = -1;
      struct Node {
   int len, link = -1, fpos;
             array<int, ALPHABET_SIZE> next;
                                                                                                                int newNode() {
                                                                                                                      t.emplace_back();
       vector < Node > t:
                                                                                                                      return t.size() - 1;
       SAM() : t(1) { }
      int newNode()
                                                                                                                t.emplace_back();
return t.size() - 1;
                                                                                                                       return p;
      int extend(int p, int c) {
   int cur = newNode();
                                                                                                                int extend(int p, int c) {
   int i = s.size();
             t[cur].len = t[p].len + 1;
             t[cur].fpos = t[cur].len - 1;
while (p != -1 && !t[p].next[c]) {
    t[p].next[c] = cur;
                                                                                                                      s.push_back(c);
                                                                                                                      p = getFail(p, i);
if (!t[p].next[c]) {
    int r = newNode();
                   p = t[p].link;
                                                                                                                             int v = getFail(t[p].fail, i);
t[r].len = t[p].len + 2;
t[r].fail = t[v].next[c];
             if (p == -1) {
                   t[cur].link = 0;
            t[p].next[c] = r;
                   if (t[p].len + 1 == t[q].len) {
                                                                                                                      return p = t[p].next[c];
                          t[cur].link = q;
                                                                                                               }
                  };
                                                                                                         //
void solve() {
    string s; cin >> s;
    int n = s.length();
    vector <int> last(n + 1);
                         t[r] = t[q];
t[r].len = t[p].len + 1;
while (p != -1 && t[p].next[c] == q) {
    t[p].next[c] = r;
    - +[o] link;
                                                                                                                last[0] = 1;
                               p = t[p].link;
                                                                                                                PAM pam;

for (int i = 0; i < n; i++)

    last[i + 1] = pam.extend(last[i], s[i] - 'a');
                          t[q].link = t[cur].link = r;
                  }
                                                                                                                int sz = pam.t.size();
vector<int> cnt(sz);
for (int i = 1; i <= n; i++)</pre>
      }
                                                                                                                cnt[last[i]]++; // 去重 = 1
for (int i = sz - 1; i > 1; i--
void solve(int n, string s, ll k) { // Substring Order II
                                                                                                                      cnt[pam.t[i].fail] += cnt[i];
       vector < int > last(n + 1);
      SAM sam;
for (int i = 0; i < n; i++)
    last[i + 1] = sam.extend(last[i], s[i] - 'a');</pre>
                                                                                                         5.9 Duval [aed467]
      int sz = sam.t.size();
                                                                                                        // duval_algorithm
      // 將字串分解成若干個非嚴格遞減的非嚴格遞增字串
                                                                                                         vector<string> duval(string s) {
   int i = 0, n = s.size();
                                                                                                                vector<string> res;
                                                                                                                while (i < n) {
   int k = i, j = i + 1;
   while (s[k] <= s[j] && j < n) {
      if (s[k] < s[j]) k = i;
   }
}</pre>
                                                                                                                             else k++;
      }; dfs(dfs, 0);
      vector<ll> dp(sz, -1);
// for any path from root
    , how many substring's prefix is the the path string
auto rec = [&](auto self, int u) -> ll {
    if (dp[u] != -1) return dp[u];
    dp[u] = cnt[u]; // distinct: = 1
    for (int c = 0; c < SAM::ALPHABET_SIZE; c++) {
        int v = sam.t[u].next[c];
        if (v) dp[u] += self(self, v);</pre>
                                                                                                                      while (i <= k) {
    res.push_back(s.substr(i, j - k));</pre>
                                                                                                                return res;
                   if (v) dp[u] += self(self, v);
                                                                                                         // 最小旋轉字串
                                                                                                         string minRound(string s) {
             return dp[u];
                                                                                                               s += s;
int i = 0, n = s.size(), start = i;
      rec(rec, 0);
                                                                                                                while (i < n / 2) {
                                                                                                                     int p = 0; string ans;
while (k > 0) { // 1-based
   for (int c = 0; c < SAM::ALPHABET_SIZE; c++) {</pre>
                    int v = sam.t[p].next[c];
                                                                                                                             else k++:
                   if (v) {
   if (k > dp[v]) {
                         k -= dp[v];
} else {
                                                                                                                      while (i <= k) i += j - k;
                               ans.push_back('a' + c);
k -= cnt[v]; // distinct: --
p = v; break;
                                                                                                                return s.substr(start, n / 2);
                                                                                                        1
                         }
                                                                                                         6
                                                                                                                  Math
                   }
                                                                                                         6.1 Mint [5e2f37]
      } cout << ans << "\n";
```

ll mul(ll a, ll b, ll p) {
 ll res = a * b - ll(1.L * a * b / p) * p;

res %= p;

5.8 Palindrome Tree [e5a1ed]

```
if (res < 0) res += p:
      return res;
// 改 MLong: getMod() < (1ULL << 31),會爆用 mul
template < class T>
constexpr T power(T a, ll b) {
    T res {1};
    for (; b > 0; b >>= 1, a *= a)
        if (b & 1) res *= a;
    return res;
}
template<int P>
struct Mint {
// Dynamic Mint, not necessary
     static int Mod;
static int getMod() {
   return P > 0 ? P : Mod;
      static void setMod(int Mod_) {
           Mod = Mod_;
      ll x:
      Mint(ll x = 0) : x \{norm(x \% getMod())\} \{\}
     ll norm(ll x) const {
   if (x < 0) x += getMod();
   if (x >= getMod()) x -= getMod();
            return x;
                                                                                               |} comb; // 若要換模數需重新宣告
      explicit operator int() const { return x; }
     Mint operator -() const {
    return Mint(norm(getMod() - x));
      Mint inv() const {
    return power(*this, getMod() - 2);
      Mint & operator += (Mint rhs) & {
           x = norm(x + rhs.x);
return *this;
      Mint & operator -= (Mint rhs) & {
    x = norm(x - rhs.x);
            return *this;
     Mint & operator *= (Mint rhs) & {
    x = x * rhs.x % getMod();
    return *this;
      Mint & operator /= (Mint rhs) & {
           return *this *= rhs.inv();
      friend Mint operator+(Mint lhs, Mint rhs) {
           return lhs += rhs;
      friend Mint operator - (Mint lhs, Mint rhs) {
    return lhs -= rhs;
      friend Mint operator*(Mint lhs, Mint rhs) {
    return lhs *= rhs;
      friend Mint operator/(Mint lhs, Mint rhs) {
           return lhs /= rhs;
      friend istream &operator>>(istream &is, Mint &a) {
           ll v; is >> v; a = Mint(v); return is;
      friend ostream &operator<<(ostream &os, const Mint &a) {</pre>
           return os << a.x;
      /// following operators are not necessary
friend bool operator==(Mint lhs, Mint rhs) {
    return lhs.x == rhs.x;
      friend bool operator!=(Mint lhs, Mint rhs) {
            return lhs.x != rhs.x;
      friend bool operator<(Mint lhs, Mint rhs) {
    return lhs.x < rhs.x;</pre>
     }
template<>
int Mint<0>::Mod = 998244353;
constexpr int P = 1E9 + 7;
using Z = Mint<P>;
6.2 Combination [f12983]
// C(m, n) = C(m, n - 1) * (m - n + 1) / n
struct Comb {
     int n:
     tert ",
vector <Z> _fac, _invfac, _inv;
Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
Comb(int n) : Comb() { init(n); }
void init(int m) {
           m = min(m, Z::getMod() - 1);
if (m <= n) return;
_fac.resize(m + 1);</pre>
```

_invfac.resize(m + 1);

_inv.resize(m + 1); for (int i = n + 1; i <= m; i++) { _fac[i] = _fac[i - 1] * i;

} } // a ^ (m-1) = 1 (Mod m) // a ^ (m-2) = 1/a (Mod m) // Exp2: cout << power(x, power(y, p, Mod - 1), Mod) // Num = (x+1) * (y+1) * (z+1)... // Sum = (a^0 + a^1+...+ a^x) * (b^0 +...+ b^y) // Mul = N * (x+1) * (y+1) * (z+1) / 2 6.4 Miller Rabin Pollard Rho [394cfb] ll mul(ll a, ll b, ll p) { ll res = a * b - ll(1.L * a * b / p) * p; res %= p; if (res < 0) res += p; fll power(ll a, ll b, ll p) { ll res {1}; for (; b; b /= 2, a = mul(a, a, p)) if (b & 1) res = mul(res, a, p); return res: vector<ll > chk {2, 325, 9375, 28178, 450775, 9780504, 1795265022}; bool check(ll a, ll d, int s, ll n) { a = power(a, d, n); if (a <= 1) return 1; for (int i = 0; i < s; i++, a = mul(a, a, n)) { if (a == 1) return 0; if (a == n - 1) return 1; }</pre> bool isPrime(ll n) { if (n < 2) return 0; if (n % 2 == 0) return n == 2; ll d = n - 1, s = 0; while (d % 2 == 0) d /= 2, s++;</pre> for (ll i : chk) if (!check(i, d, s, n)) return 0; const vector<ll> small = {2, 3, 5, 7, 11, 13, 17, 19}; ll findFactor(ll n) { if (isPrime(n)) return 1; for (ll p : small) if (n % p == 0) return p; ll x, y = 2, d, t = 1; auto f = [&](ll a) {

return (mul(a, a, n) + t) % n;

for (int l = 2; ; l *= 2) {

x = y;

_invfac[m] = _fac[m].inv(); for (int i = m; i > n; i--) { _invfac[i - 1] = _invfac[i] * i; _inv[i] = _invfac[i] * _fac[i - 1];

J binom(int n, int m) {
 if (n < m || m < 0) return 0;
 return fac(n) * invfac(m) * invfac(n - m);</pre>

Z lucas(int n, int m) { // Mod 要在 1E5 左右

if (m == 0) return 1;
return binom(n % Z::getMod(), m % Z::getMod()) *
 lucas(n / Z::getMod(), m / Z::getMod());

If ac(int m) {
 if (m > n) init(2 * m);
 return _fac[m];

Z invfac(int m) {
 if (m > n) init(2 * m);
 return _invfac[m];

Z inv(int m) {
 if (m > n) init(2 * m);
 return _inv[m];

6.3 Sieve [37ae54]

vector < int > primes , minp;
void sieve(int n) {
 minp.assign(n + 1, 0);

// minp[i] == i, 質數

for (int i = 2; i <= n; i++) {
 if (minp[i] == 0) {
 minp[i] = i;
}</pre>

primes.push_back(i);

for (auto p : primes) {
 if (i * p > n) break;
 minp[i * p] = p;
 if (p == minp[i]) break;

primes.clear();

```
int m = min(l, 32);
for (int i = 0; i < l; i += m) {</pre>
                 \dot{d} = 1:
                 for (int j = 0; j < m; j++)
    y = f(y), d = mul(d, abs(x - y), n);</pre>
                 ll g = __gcd(d, n);
if (g == n) {
    l = 1, y = 2, ++t;
                       break;
                 if (g != 1) return g;
     }
map<ll, int> res;
void pollardRho(ll n) {
     if (n == 1) return;
if (isPrime(n)) {
           res[n]++;
           return;
     Il d = findFactor(n);
     pollardRho(n / d), pollardRho(d);
}
```

6.5 CRT [6b1b59]

```
ll exgcd(ll a, ll b, ll &x, ll &y) {
      if (!b) {
    x = 1, y = 0;
    return a;
       Il g = exgcd(b, a \% b, y, x);
      y -= a / b * x;
      return g;
}
ll inv(ll x, ll m) {
.
      ll a, b;
exgcd(x, m, a, b);
      a %= m;
if (a < 0) a += m;
// gcd(mod) = 1, res % mod_i = remain_i
// a: remain, mod
ll CRT(vector<pair<ll, ll>> &a) {
      for (auto [r, m] : a) s *= m;

for (auto [r, m] : a) s *= m;

for (auto [r, m] : a) {

    ll t = s / m;

    res += r * t % s * inv(t, m) % s;
             if (res >= s) res -= s;
       return res:
}
```

6.6 Matrix [2856cb]

```
int n = a.size(), k = a[0].size(), m = b[0].size();
      assert(k == b.size());
      vector<vector<T>> res(n, vector<T>(m));
      for (int i = 0; i < n; i++)
    for (int j = 0; j < m; j++)
        for (int l = 0; l < k; l++)</pre>
                      res[i][j] += a[i][l] * b[l][j];
     return res;
vector<vector<T>> unit(int n) {
    vector<vector<T>> res(n, vector<T>(n));
    for (int i = 0; i < n; i++) res[i][i] = 1;</pre>
template < class T>
vector<vector<T>>> power(vector<vector<T>>> a, ll b) {
     int n = a.size();
     int n = a.size();
assert(n == a[0].size());
auto res = unit<T>(n);
for (; b; b /= 2, a = a * a)
        if (b % 2) res = res * a;
     return res;
}
using Matrix = vector<vector<Z>>;
```

6.7 Mex [00904e]

```
template < class T>
T mex(vector<T> &v) {
      unordered_set<T> s;
      for (auto e : v) s.insert(e);
for (T i = 0; ; i++)
    if (s.find(i) == s.end()) return i;
```

6.8 Game Theorem

- sq 值為 0 代表先手必敗
- 當前 sq 值 = 可能的後繼狀態的 mex (例如拿一個或拿兩個, 就等於兩者的 sg值mex),若有互相依賴就兩個後繼狀態xor當作一組sg值(例如切開成 兩半,只算一次)

- 單組基礎 nim 的 sg 值為本身的原因: f(0) = 0, f(1) = mex(f(0)) = 1, f(2) = mex(f(0), f(1)) = 2...,都是自己 多組賽局可以把 sg 值 xor 起來,當成最後的 sg 值, nim 也是一樣,且由於
- xor 性質, 如果可以快速知道 sg(1)g(2)...g(n), 就可以用 xor 性質處理不連

續組合 **6.9 Fraction** [3f8970]

```
template < class T >
 struct Fraction {
      Tn,d;
      void reduce() {
   T g = gcd(abs(n), abs(d));
   n /= g, d /= g;
   if (d < 0) n = -n, d = -d;</pre>
      Fraction(T n_ = 0, T d_ = 1) : n(n_), d(d_) {    assert(d != 0);
           reduce();
      Fraction(const string &str) {
           istringstream ss(str);
           char slash:
            if (str.find('/') != -1) {
                ss >> n >> slash >> d;
           } else {
    ss >> n;
           Fraction(n. d):
      Fraction operator+=(Fraction rhs) & {
    n = n * rhs.d + rhs.n * d;
    d *= rhs.d;
           reduce();
return *this;
      Fraction operator -= (Fraction rhs) & {
    n = n * rhs.d - rhs.n * d;
    d *= rhs.d;
            reduce();
           return *this:
      Fraction operator*=(Fraction rhs) & {
           n *= rhs.n;
d *= rhs.d;
           reduce();
      Fraction operator/=(Fraction rhs) & {
           assert(rhs.n != 0);
           n *= rhs.d;
d *= rhs.n;
           reduce();
           return *this;
      friend Fraction operator+(Fraction lhs, Fraction rhs) {
           return lhs += rhs;
      friend Fraction operator - (Fraction lhs. Fraction rhs) {
           return lhs -= rhs;
      friend Fraction operator*(Fraction lhs, Fraction rhs) {
   return lhs *= rhs;
      friend Fraction operator/(Fraction lhs, Fraction rhs) {
   return lhs /= rhs;
      friend istream &operator>>(istream &is, Fraction &f) {
           string s;
           is >> s;
           f = Fraction(s);
           return is:
      friend
              ostream & operator << (ostream &os, const Fraction &f) {
           if (f.d == 1) {
                os << f.n;
           } else {
                os << f.n << "/" << f.d;
            return os:
      friend bool operator == (Fraction lhs, Fraction rhs) {
           return lhs.n * rhs.d == rhs.n * lhs.d;
      friend bool operator!=(Fraction lhs, Fraction rhs) {
  return lhs.n * rhs.d != rhs.n * lhs.d;
      friend bool operator < (Fraction lhs, Fraction rhs) {
  return lhs.n * rhs.d < rhs.n * lhs.d;</pre>
};
```

6.10 Gaussian Elimination [5d1aa7]

```
// 找反矩陣
      就開 2n,右邊放單位矩陣,做完檢查左半是不是單位,回傳右半
// 0 : no solution
// -1 : infinity solution
// 1 : one solution
template < class T>
```

```
tuple < T.
         int, vector<T>> gaussianElimination(vector<vector<T>> a) {
        T det = 1;
        bool zeroDet = false;
int n = a.size(), m = a[0].size(), rk = 0, sgn = 1;
        for (int c = 0; c < n; c++) {
   int p = -1;
   for (int r = rk; r < n; r++) {
      if (a[r][c] != 0) {</pre>
                                 p = r;
break;
                        }
                 if (p == -1) {
    zeroDet = true;
                 if (p != rk) swap(a[rk], a[p]), sgn *= -1;
                if (p != rk) swap(a[rk], a[p]), sgn *= -1;
det *= a[rk][c];
Tinv = 1 / a[rk][c];
for (int j = c; j < m; j++) a[rk][j] *= inv;
for (int r = 0; r < n; r++) {
    if (r == rk || a[r][c] == 0) continue;
    T fac = a[r][c];
    for (int j = c; j < m; j++)
        a[r][j] -= fac * a[rk][j];
}</pre>
        det = (zeroDet ? 0 : det * sgn);
for (int r = rk; r < n; r++)
    if (a[r][m - 1] != 0) return {det, 0, {}};
if (rk < n) return {det, -1, {}};
vector < T> ans(n);
         for (int i = 0; i < n; i++) ans[i] = a[i][m - 1];</pre>
         return {det, 1, ans};
template < class T>
tuple<int, vector
        int n = a.size(), m = a[0].size(), rk = 0;
vector<int> pos(m - 1, -1);
for (int c = 0; c < m - 1; c++) {
   int p = -1;
   for (int r = rk; r < n; r++) {
   if (a[1][1][1][-0][1]
}</pre>
                         if (a[r][c] != 0) {
                                 p = r;
break;
                         }
                 if (p == -1) continue;
if (p != rk) swap(a[rk], a[p]);
                for (int j = c; j < m; j++)
    a[r][j] -= fac * a[rk][j];</pre>
                 rk++;
         vector<T> sol(m - 1);
        vector<l> sol(m - 1);
vector<vector<T>> basis;
for (int r = rk; r < n; r++)
    if (a[r][m - 1] != 0)
        return {-1, sol, basis};
for (int c = 0; c < m - 1; c++)
    if (pos[c] != -1)
        sol[c] = a[pos[c]][m - 1];</pre>
        for (int c = 0; c < m - 1; c++)
  if (pos[c] == -1) {
    vector < T > v(m - 1);
                        return {rk, sol, basis};
template < class T>
using Matrix = vector < vector < T>>;
```

6.11 Integer Partition [83bc9d]

cout << ans << "\n";

6.12 Mobius Theorem

- 數論 分塊可以快速計算一些含有除法向下取整的和式,就是像 $\sum_{i=1}^n f(i)g(\left\lfloor \frac{n}{i} \right\rfloor)$ 的和式。當可以在 O(1) 內計算 f(r)-f(l) 或已經預處理 出 f 的前綴和時,數論分塊就可以在 $O(\sqrt{n})$ 的時間內計算上述和式的值。
- 迪利克雷捲積 $h(x) = \sum_{d|x} f(d) g(\frac{x}{d})$
- 積性函數
 - 莫比烏斯函數
 - 1. 定義

$$\sum_{d\mid n}\!\!\mu(d)\!=\!\begin{cases} 1 & \text{for } n\!=\!1\\ 0 & \text{for } n\!\neq\!0 \end{cases}$$

- 2. μ是常數函數1的反元素
- $\Rightarrow \mu * 1 = \epsilon$, $\epsilon(n)$ 只在n = 1時為 1 , 其餘情況皆為 0 。
- $-\phi$ 歐拉函數: x以下與x互質的數量

$$\begin{split} \phi*1 &= \sum_{d|n} \phi(\frac{n}{d}) \text{ 質因數分解} \\ &= \sum_{i=0}^{c} \phi(p^i) \\ &= 1 + p^0(p-1) + p^1(p-1) + \ldots + p^{c-1}(p-1) \\ &= p^c \\ &= id \end{split}$$

• 莫比烏斯反演公式

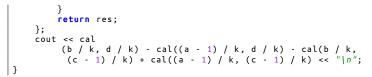
-
$$f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$$

- $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

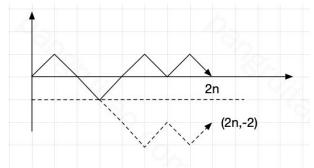
• 例子

$$\begin{split} &\sum_{i=a}^{b} \sum_{j=c}^{d} [gcd(i,j) = k] \\ &\Rightarrow \sum_{i=1}^{x} \sum_{j=1}^{y} [gcd(i,j) = k] \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \frac{y}{k} \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \epsilon(gcd(i,j)) \\ &= \sum_{i=1}^{x} \sum_{j=1}^{y} \frac{y}{k} \\ &= \sum_{d=1}^{x} \sum_{j=1}^{y} \frac{y}{k} \\ &= \sum_{d=1}^{x} \mu(d) \sum_{i=1}^{y} \frac{y}{k} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \\ &= \sum_{d=1}^{min(\left\lfloor \frac{x}{k} \right\rfloor, \left\lfloor \frac{y}{k} \right\rfloor)} \mu(d) \left\lfloor \frac{x}{kd} \right\rfloor \left\lfloor \frac{y}{kd} \right\rfloor \end{split}$$

6.13 Mobius Inverse [d41d8c]



6.14 Catalan Theorem



- 1. n 個往上n 個往下,先枚舉所有情況 $\frac{(2n)!}{n!n!} = C_n^{2n}$
- 2. 扣掉非法的,有多少種可能讓最後的點落在 (2n,-2) 假設往上有 x 個,往下有 y 個,會有:

$$\begin{cases} x + y = 2n \\ y - x = 2 \end{cases} \Rightarrow \begin{cases} x = n - 1 \\ y = n + 1 \end{cases}$$

所以只要扣掉 C_{n-1}^{2n} 即可

6.15 Burnside's Lemma

 $|X/G|\!=\!\frac{1}{|G|}\!\sum_{g\in G}\!|X^g|$

- G:各種翻轉操作所構成的置換群
- X/G: 本質不同的方案的集合
- X^g : 對於某一種操作 g, 所有方案中, 經過 g 這種翻轉後保持不變的方案的集合
- 集合取絕對值代表集合數

7 Search and Gready

7.1 Binary Search [d41d8c]

7.2 Ternary Search [d41d8c]

```
void ternarySearch() {
   int lo = 0, hi = 10;
   while (lo < hi) {
      int xl = lo + (hi - lo) / 3;
      int xr = hi - (hi - lo) / 3;
      int resl = calc(xl), resr = calc(xr);
      if (resl < resr) {
            lo = xl + 1;
      } else {
            hi = xr - 1;
      }
}</pre>
```

8 Tree

8.1 Binary Lifting LCA [a136c5]

```
const int N = 2E5;
const int Lg = __lg(N); // __lg(max(n, qi)), [0, Lg]
int up[N][Lg + 1];
vector<int> dep, dfn;
void build(int n, vector<vector<int>> &g, int rt = 0) {
    dep.assign(n, 0); dfn.assign(n, 0);
    int cur = 0;
    auto dfs = [&](auto self, int x, int p) -> void {
        dfn[x] = cur++;
        up[x][0] = p;
        for (int i = 1; i <= Lg; i++) {</pre>
```

8.2 Centroid Decomposition [2ecec4]

```
vector < bool > vis(n);
vector < int > siz(n), par(n, -1);
auto findSize = [&](auto self, int u, int p) -> int {
    siz[u] = 1;
    for (int v : g[u]) {
        if (v == p || vis[v]) continue;
            siz[u] += self(self, v, u);
    }
    return siz[u];
};
auto findCen = [&](auto self, int u, int p, int sz) -> int {
    for (int v : g[u]) {
        if (v == p || vis[v]) continue;
            if (siz[v] * 2 > sz) return self(self, v, u, sz);
    }
    return u;
};
auto buildCen = [&](auto self, int u, int p) -> void {
    findSize(findSize, u, p);
    int c = findCen(findCen, u, -1, siz[u]);
    vis[c] = true, par[c] = p;
    for (int v : g[c]) if (!vis[v]) self(self, v, c);
};
buildCen(buildCen, 0, -1);
```

8.3 Heavy Light Decomposition [9facc3]

```
int n, cur;
vector<int> siz, top, dep, parent, in, out, seq;
vector<vector<int>> adj;
HLD(int n) : n(n), cur(0) {
    siz.resize(n); top.resize(n); dep.resize(n);
    parent.resize(n); in.resize(n); out.resize(n);
    seq.resize(n); adj.assign(n, {});
void addEdge(int u. int v) {
      adj[u].push_back(v);
adj[v].push_back(u);
void work(int rt = 0) {
      top[rt] = rt;
dep[rt] = 0;
parent[rt] = -1;
      dfs1(rt); dfs2(rt);
(adj[u].begin(), adj[u].end(), parent[u]));
      for (auto &v : adj[u]) {
    parent[v] = u, dep[v] = dep[u] + 1;
             dfs1(v);
             if (siz[v] > siz[adj[u][0]]) {
    swap(v, adj[u][0]);
            } // 讓 adj[u][0] 是重子節點
      }
void dfs2(int u) {
      in[u] = cur++;
      seq[in[u]] = u; // dfn 對應的編號
for (auto v : adj[u]) {
   top[v] = v == adj[u][0] ? top[u] : v;
```

dfs2(v);

```
National Chung Cheng University Salmon
              out[u] = cur;
       int lca(int u, int v) {
    while (top[u] != top[v]) {
                     if (dep[top[u]] > dep[top[v]]) {
                     u = parent[top[u]];
} else {
                             v = parent[top[v]];
              return dep[u] < dep[v] ? u : v;</pre>
      int dist(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[lca(u, v)];
      int jump(int u, int k) {
    if (dep[u] < k) return -1;
    int d = dep[u] - k;
    while (dep[top[u]] > d)
        u = parent[top[u]];
    return seq[in[u] - dep[u] + d];
}
      bool isAncester(int u, int v) {
    return in[u] <= in[v] && in[v] < out[u];</pre>
      int rootedParent(int rt, int v) {
   if (rt == v) return rt;
   if (!isAncester(v, rt)) return parent[v];
   auto it = upper_bound(adj[v].begin(), adj[v].end(), rt,
        [&](int x, int y) {
        return in[x] < in[y];
     }) - 1;
}</pre>
              return *it;
       int rootedSize(int rt, int v) {
              if (rt == v) return n;
if (!isAncester(v, rt)) return siz[v];
return n - siz[rootedParent(rt, v)];
      int rootedLca(int rt, int a, int b) {
   return lca(rt, a) ^ lca(a, b) ^ lca(b, rt);
}:
8.4 Link Cut Tree [cf936b]
template < class Info, class Tag>
struct LinkCutTree { // 1-based
      struct Node {
            Info info = Info();
              Tag tag = Tag();
int siz = 0, ch[2], p = 0, rev = 0;
       vector<Node> nd;
```

```
LinkCutTree(int n) : nd(n + 1) {}
bool isrt(int t) {
     return
              nd[nd[t].p].ch[0] != t && nd[nd[t].p].ch[1] != t;
int pos(int t) { // t 是其 par 的左/右 return nd[nd[t].p].ch[1] == t;
void applyRev(int t) {
    swap(nd[t].ch[0], nd[t].ch[1]);
    nd[t].rev ^= 1;
}
void apply(int t, const Tag &v) {
   nd[t].info.apply(nd[t].siz, v);
   nd[t].tag.apply(v);
void push(int t) {
      if (nd[t].rev) {
           if (nd[t].ch[0]) applyRev(nd[t].ch[0]);
if (nd[t].ch[1]) applyRev(nd[t].ch[1]);
     if (nd[t].ch[0]) apply(nd[t].ch[0], nd[t].tag);
if (nd[t].ch[1]) apply(nd[t].ch[1], nd[t].tag);
      nd[t].tag = Tag();
void pull(int t) {
     .pull(nd[nd[t].ch[0]].info, nd[nd[t].ch[1]].info);
void pushAll(int t) {
      if (!isrt(t)) pushAll(nd[t].p);
      push(t);
void rotate(int x) { // x 與其 par 交換位置 int f = nd[x].p, r = pos(x); nd[f].ch[r] = nd[x].ch[!r];
      if (nd[x].ch[!r]) nd[nd[x].ch[!r]].p = f;
     ind[x].p = nd[f].p;
if (!isrt(f)) nd[nd[f].p].ch[pos(f)] = x;
nd[x].ch[!r] = f, nd[f].p = x;
pull(f), pull(x);
void splay(int x) {
     pushAĺl(x);
```

```
for (int f = nd[x].p; f = nd[x].p, !isrt(x); rotate(x))
if (!isrt(f)) rotate(pos(x) == pos(f) ? f : x);
       void access(int x) {
    for (int f = 0; x; f = x, x = nd[x].p)
                     splay(x), nd[x].ch[1] = f, pull(x);
       void makeRoot(int p) {
              access(p), splay(p), applyRev(p);
       int findRoot(int x) {
              access(x), splay(x);
while (nd[x].ch[0]) x = nd[x].ch[0];
splay(x); return x;
       void split(int x, int y) { // y 為根
   makeRoot(x), access(y), splay(y);
       void link(int rt, int p) {
    makeRoot(rt), nd[rt].p = p;
       void cut(int x, int y) {
    makeRoot(x), access(y), splay(y);
    nd[y].ch[0] = nd[nd[y].ch[0]].p = 0;
              pull(y);
       bool neighbor(int x, int y) {
              makeRoot(x), access(y);
if (nd[y].ch[0] != x || nd[x].ch[1]) return false;
              return true;
       bool connected(int x, int y) {
    return findRoot(x) == findRoot(y);
       void modify(int x, const Info &v) {
   access(x), nd[x].info = v;
       void pathApply(int x, int y, const Tag &v) {
  assert(connected(x, y));
              split(x, y), apply(y, v);
       Info pathQuery(int x, int y) {
   assert(connected(x, y));
   split(x, y); return nd[y].info;
};
const int Mod = 51061;
struct Tag {
    ll add = 0, mul = 1;
       void apply(const Tag &v) {
  mul = mul * v.mul % Mod;
  add = (add * v.mul % Mod + v.add) % Mod;
      }
};

};
struct Info {
    ll val = 0, sum = 0;
    void apply(int siz, const Tag &v) {
        val = (val * v.mul % Mod + v.add) % Mod;
        sum = (sum * v.mul % Mod + v.add * siz % Mod) % Mod;
}

       void pull(const Info &l, const Info &r) {
   sum = (l.sum + r.sum + val) % Mod;
};
8.5 Virtual Tree [c3a0b3]
```

```
| // 多次詢問給某些關鍵點, 虚樹可達成快速樹 DP (前處理每個點)
| // 例如這題是有權樹,給一些關鍵點,求跟 vertex 1 隔開的最小成本
 // 前處理 root 到所有點的最小邊權
 vector<int> stk;
 void insert(int key, vector<vector<int>>> &vt) {
    if (stk.empty()) {
        stk.push_back(key);
}
       int l = lca(stk.back(), key);
      if (l == stk.back())
           stk.push_back(key);
           return:
            stk.size() > 1 && dfn[stk[stk.size() - 2]] > dfn[l]) {
           vt[stk[stk.size() - 2]].push_back(stk.back());
            stk.pop_back();
      if (stk.size() < 2 || stk[stk.size() - 2] != l) {
   vt[l].push_back(stk.back());</pre>
           stk.back() = l;
      } else {
   vt[l].push_back(stk.back());
           stk.pop_back();
       stk.push back(kev):
 int work(vector<vector<int>> &vt) {
   while (stk.size() > 1) {
     vt[stk[stk.size() - 2]].push_back(stk.back());
}
           stk.pop_back();
       int rt = stk[0];
      stk.clear();
```

```
return rt:
void solve() {
     int n; cin >> n;
vector<vector<int>>> g(n);
      vector<vector<pair<int, int>>> wg(n);
      vector < vector < int >> vt(n);
      for (int i = 1; i < n; i++) {
           int u, v, w;
cin >> u >> v >> w;
           v , , g[u].push_back(v), g[v].push_back(u); wg[u].emplace_back(v, w), wg[v].emplace_back(u, w);
      build(n, g); // build LCA
     vector<int> dis(n, 1E9); // root 到各點的最小邊權
auto dfs_dis = [&](auto &&self, int x, int p) -> void {
           for (auto [y, w] : wg[x]) {
   if (y == p) continue;
   dis[y] = min(w, dis[x]);
                 self(self, y, x);
           }
      dfs_dis(dfs_dis, 0, -1);
      vector < bool > isKey(n);
      vector<ll> dp(n);
      int q; cin >> q;
while (q--) {
   int m; cin >> m;
            vector <int> key(m);
for (int i = 0; i < m; i++) {
    cin >> key[i];
                 key[i] -=
                 isKey[key[i]] = true;
           key.push_back(0); // 固定 0 為 root, 看題目需求
sort(key.begin(), key.end(), [&](int a, int b) {
    return dfn[a] < dfn[b];
            }); // 要 sort 再 insert
            for (auto x : key) insert(x, vt);
           work(vt);
auto dfs = [&](auto &&self, int x) -> void {
                 for (auto y : vt[x]) {
    self(self, y);
                       if (isKey[y]) { // ₫ dp[x] += dis[y];
                                              // 直接砍了
                       } else { // 不砍 or 砍
                             dp[x] += min < ll > (dp[y], dis[y]);
                           // 記得 reset
                       isKey[y] = dp[y] = 0;
                 vt[x].clear(); // 記得 reset
           dfs(dfs, 0);
cout << dp[0] << "\n";</pre>
            dp[0] = 0; // 最後 reset root
}
         Dominator Tree [0cbb87]
```

9 DP

9.1 LCS [9c3c7b]

```
string LCS(const string &a, const string &b) {
   int n = a.length(), m = b.length();
   vector<vector<int>> dp(n + 1, vector<int>(m + 1));
   for (int i = 1; i <= n; i++) {
      for (int j = 1; j <= m; j++) {
        if (a[i - 1] == b[j - 1]) {
           dp[i][j] = dp[i - 1][j - 1] + 1;
      } else {
           dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
      }
   }
  int l = dp[n][m];
   string ans(l, 0);
  while (n >= 1 && m >= 1) {
      if (a[n - 1] == b[m - 1]) {
           ans[l - 1] = a[n - 1];
           n--, m--, l--;
      } else {
           if (dp[n - 1][m] > dp[n][m - 1]) n--;
           else m--;
      }
  }
  return ans;
}
```

9.2 LIS [3018f4]

9.3 Edit Distance [b13609]

9.4 **Bitmask** [60bdb9]

```
void hamiltonianPath() {
      int n, m; cin >> n >> m;
vector<vector<int>> adj(n);
for (int i = 0; i < m; i++) {
    int u, v; cin >> u >> v;
             adj[--v].push_back(--u);
      // 以...為終點,走過...
vector dp(n, vector<int>(1 << n));
dp[0][1] = 1;
for (int mask = 1; mask < 1 << n; mask++) {
            (int mask = 1; mask < 1 << n; mask++) {
if ((mask & 1) == 0) continue;
for (int i = 0; i < n; i++) {
   if ((mask >> i & 1) == 0) continue;
   if (i == n - 1 && mask != (1 << n) - 1) continue;
   int pre = mask ^ (1 << i);
   for (int j : adj[i]) {
      if ((pre >> j & 1) == 0) continue;
      dofil[mask] - (dofil[mask] + dofil[pre]) % Montinue;
      dofil[mask] - (dofil[mask] + dofil[pre]) % Montinue;
}
                           dp[i][mask] = (dp[i][mask] + dp[j][pre]) % Mod;
             }
      cout << dp[n - 1][(1 << n) - 1] << "\n";
void elevatorRides() {
      int n, x; cin >> n >> x;
vector<int> a(n);
      for (int i = 0; i < n; i++) cin >> a[i];
vector <int> dp(1 << n), f(1 << n);
dp[0] = 1; // 次數、已使用人數
for (int mask = 1; mask < 1 << n; mask++) {
             dp[mask] = 2E9;
for (int i = 0; i < n; i++) {
    if ((mask >> i & 1) == 0) continue;
    int pre = mask ^ (1 << i);</pre>
                    f[mask] = a[i];
             }
      cout << dp[(1 << n) - 1] << "\n";
void minClique() { // 移掉一些邊,讓整張圖由最少團組成
      int n, m;
cin >> n >> m;
       vector < bitset < N >> g(n);
      for (int i = 0; i < m; i++) {
  int u, v; cin >> u >> v;
  u--; v--; g[u][v] = g[v][u] = 1;
       vector<int> dp(1 << n, inf);</pre>
      dp[0] = 1;
      for (int mask = 0; mask < 1 << n; mask++) { // 先正常 dp for (int i = 0; i < n; i++) {
                    if (mask & (1 << i)) {
   int pre = mask ^ (1 << i);
   if (dp[pre</pre>
                                   ] == 1 && (g[i] & bitset<N>(pre)) == pre)
                                  dp[mask] = 1; // i 有連到所有 pre
                    }
             }
```

9.5 Projects [8d16b1]

```
ll nt = dp[id][1] + a[i].to - a[i].from;
if (dp[i][0] < nw || dp[i][0] == nw && dp[i][1] > nt) {
            dp[i] = {nw, nt};
            rec[i] = {1, id};
        }
        vector < int > ans;
        for (int i = n; i != 0;) {
            if (rec[i][0]) {
                ans.push_back(a[i].id);
                i = rec[i][1];
        } else {
            i --;
        }
    }
}
```

9.6 Removal Game [c4b594]

9.7 Monotonic Queue [c9ba14]

```
| // 應用: dp(i) = h(i) + max(A(j)), for l(i) \le j \le r(i)
 // A(j) 可能包含 dp(j), h(i) 可 O(1) void boundedKnapsack() {
       int n, k; // O(nk)
vector<int> w(n), v(n), num(n);
       deque<int> q;
       // 於是我們將同餘的數分在同一組
       // 每次取出連續 num[i] 格中最大值
       // g_x = max([k=0]^num[i] (g'_{x-k} + v_i*k))
// G_x = g'_{x} - v_i*x
       // u_x = y _l^x - v_u^x /

// x 代 x-k => v_i*(x-k)

// g_x = max(_{{k-0}}^num[i] (G_{{x-k}} + v_i*x))

vector<vector<ll>> dp(2, vector<ll>(k + 1));

for (int i = 0; i < n; i++) {
             for (int r = 0; r < w[i]; r++) { // 餘數
                   q.clear(); // q 記錄在 x = i 時的 dp 有單調性
for (int x = 0; x * w[i] + r <= k; x++) {
    while (!q.empty() && q.front() < x - num[i])
                         q.pop_back();
                         q.push_back(x);
dp[1][x * w[i] + r] = dp[0][q.front()
     * w[i] + r] - q.front() * v[i] + x * v[i];
                   }
             swap(dp[0], dp[1]);
       cout << dp[0][k] << "\n";
```

9.8 SOS [6f70d0]

dp[k][m] = inf; for (int i = max(k, optl); i <= min(m, optr); i++) { // 注意 i 的範圍 \ get_cost 與 dp 的邊界 ll cur = dp[k - 1][i] + getCost(i, m); if (cur < dp[k][m])

dp[k][m] = cur, opt = i;

```
rec(k, l, m - 1, optl, opt);
rec(k, m + 1, r, opt, optr);
       for (int mask = 0; mask < 1 << m; mask++) {
    int sgn = __builtin_popcount(mask) & 1 ? -1 : 1;
    ans += sgn * (power(Z(2), dp[mask]) - 1);</pre>
                                                                                                          void DNC() {
                                                                                                                cout << ans << "\n";
                                                                                                                for (int i = 2; i <= k; i++)
  rec(i, 1, n, 1, n);
cout << dp[k][n] << "\n";</pre>
// x / y = x, 代表包含於 x 的 y 個數, 定義為 dp[x][0] // x & y = x, 代表包含 x 的 y 個數, 定義為 dp[x][1]
         != 0, 代表至少有一個位元都為 1 的 y 個數, = n - dp[~x][0]
                                                                                                         9.11 LiChao Segment Tree [2a9325]
 void solve() {
                                                                                                         int n; cin >> n;
vector <int> a(n);
       map <int, int> mp;
for (int i = 0; i < n; i++) {
    cin >> a[i];
                                                                                                         template < class T, class F = less < ll >>
                                                                                                         struct LiChaoSeg {
                                                                                                               mp[a[i]]++;
       int m = __lg(*max_element(a.begin(), a.end())) + 1;
       vector<array<ll, 2>> dp(1 << m);
for (int i = 0; i < n; i++) {
    dp[a[i]][0]++;</pre>
                                                                                                                      T m, b;
                                                                                                                      Line(T m = 0, T b = inf) : m(m), b(b) {}
T eval(T x) const { return m * x + b; }
             dp[a[i]][1]++;
       for (int i = 0; i < m; i++) {
    for (int mask = 0; mask < 1 << m; mask++) {
        if (mask >> i & 1) {
            int pre = mask ^ (1 << i);
            dp[mask][0] += dp[pre][0];
            dp[pre][1] += dp[mask][1];
}</pre>
                                                                                                                struct Node {
                                                                                                                      Line line;
ll l = -1, r = -1;
                                                                                                                ĺĺ n;
                                                                                                               }
       private:
                                                                                                                int newNode() {
                                                                                                                      nd.emplace_back();
 }
                                                                                                                      return nd.size() - 1;
9.9 CHT [ce439f]

}
void update(int p, ll l, ll r, Line line) {
    ll m = (l + r) / 2;
    bool left = cmp(line.eval(l), nd[p].line.eval(l));
    bool mid = cmp(line.eval(m), nd[p].line.eval(m));
    if (mid) swap(nd[p].line, line);
    if (r - l == 1) return;
    if (left != mid) {
        if (nd[p].l == -1) nd[p].l = newNode();
            update(nd[p].l, l, m, line);
    }
} else {

|\hspace{.06cm}|\hspace{.06cm}| 應用: dp(x) = C(x) + min/max(A(i) * x + B(i)), for i < x
struct Line { // x 盡量從 1 開始
      ll m, b;
Line(ll m = 0, ll b = 0) : m(m), b(b) {}
ll eval(ll x) { return m * x + b; }
struct CHT { // 斜率單調
int lptr = 0, rptr = 0;
                                                                                                                      } else {
    if (nd[p].r == -1) nd[p].r = newNode();
    update(nd[p].r, m, r, line);
       vector <Line > hull;
       CHT(Line init = Line()) { hull.push_back(init); } bool frontBad(Line &l1, Line &l2, ll x) {
    // 斜率遞減、查詢遞增,因此只要左直線的 Y >= 右直線的 Y
                                                                                                                void rangeUpdate
             // 代表查詢的當下, 右線段的高度已經低於左線段了
return l1.eval(x) >= l2.eval(x);
                                                                                                                      (int p, ll l, ll r, ll ql, ll qr, Line line) {
   if (r <= ql || l >= qr) return;
   if (ql <= l && r <= qr) return update(p, l, r, line);
   if (nd[p].l == -1) nd[p].l = newNode();
   if (nd[p].r == -1) nd[p].r = newNode();</pre>
       bool backBad(Line &l1, Line &l2, Line &l3) {
             // 斜率遞減、上凸包、取 min
                                                                                                                      rangeUpdate(nd[p].r, m, r, ql, qr, line);
rangeUpdate(nd[p].r, m, r, ql, qr, line);
             // 因此只要 12 跟
                     13 的 X 交點 <= 11 跟 13 的 X 交點, 12 就用不到了
             return (13.b - 12.b)

* (l1.m - l3.m) <= (l3.b - l1.b) * (l2.m - l3.m);
                                                                                                                .
T query(ll x, int p, ll l, ll r) {
       if (p == -1) return inf;
ll m = (l + r) / 2;
                                                                                                                      if (x < m) return min(
    nd[p].line.eval(x), query(x, nd[p].l, l, m), cmp);</pre>
             hull.pop_back(), rptr--;
hull.push_back(l), rptr++;
                                                                                                                      else return min(
                                                                                                                              nd[p].line.eval(x), query(x, nd[p].r, m, r), cmp);
       ll query(ll x) { // 查詢沒單調性需要二分搜
while (rptr - lptr
> 0 && frontBad(hull[lptr], hull[lptr + 1], x))
                                                                                                         };
                                                                                                         9.12 Codeforces Example [08fee8]
             return hull[lptr].eval(x);
                                                                                                        // CF 1932 pF
      }
                                                                                                         // 給你很多區間,你可以選一些點,重疊到的線段得到 1 分
};
                                                                                                         // 請問在線段不重複的情況下,最多獲得幾分
9.10 DNC [98abd5]
                                                                                                          void solve() {
                                                                                                               int n, m;
cin >> n >> m;
 // 應用: 切 k 段問題, 且滿足四邊形不等式
// 應用: 切 k 段問題,且滿足四邊形不等式
// w(a,c) + w(b,d) ≤(≥) w(a,d) + w(b,c)
// dp[k][j] = min(dp[k - 1][i] + cost[i][j])
// cost: (i, j]
constexpr int N = 3E3 + 5;
constexpr ll inf = 4E18;
ll dp[N][N]; // 1-based
ll getCost(int l, int r) {}
void rec(int k, int l, int r, int optl, int optr) {
    if (l > r) return;
    int m = (l + r) >> 1, opt = -1;
    dp[k][m] = inf;
                                                                                                                // 記錄每點有幾個線段
                                                                                                                // 再一個紀錄,包含這個點的左界
                                                                                                               // 冉一個紀錄,包含這個點的左界
vector<int> lside(n + 1, inf), cnt(n + 5, 0);
for (int i = 0; i < m; i++) {
    int l, r; cin >> l >> r;
    lside[r] = min(lside[r], l);
    cnt[l]++;
    cnt[r + 1]--;
```

for (int i = 2; i <= n; i++)
 cnt[i] += cnt[i - 1];
for (int i = n; i >= 2; i--)
 lside[i - 1] = min(lside[i - 1], lside[i]);
vector<int> dp(n + 1);
dp[n] = c.

for (int i = 1; i <= n; i++) {</pre>

dp[0] = 0;

```
dp[i] = cnt[i];
if (lside[i] != inf)
    dp[i] += dp[lside[i] - 1];
dp[i] = max(dp[i], dp[i - 1]);
     cout << dp[n] << "\n";
}
// CF 1935 pC
// 給你每個事件的 a, b, 挑事件會把 a 全部加起來
// 再加上 max(bi) - min(bi)
void solve() {
     int n, k, ans = 0; cin >> n >> k;
     vector<pair<int, int>> v(n + 1);
for (int i = 1; i <= n; i++) {</pre>
          int a, b; cin >> a >> b;
v[i] = {a, b};
if (a <= k) ans = 1;</pre>
     sort(v.begin() +
           1, v.end(), [](pair<int, int> &a, pair<int, int> &b) {
          return a.second < b.second;</pre>
     }); // 用 bi 來排,考慮第 i 個時可以先扣
     vector<vector<int>> dp(n + 1, vector<int>(n + 1, inf));
     // 考慮 v[i] 時, 選 j 個的 sum(ai) - min(bi)
    for (int i = 1; i <= n; i++) { // 滚動 dp
for (int j = n; j >= 2; j--) {
    dp[i][j] = min
        (dp[i - 1][j], dp[i - 1][j - 1] + v[i].first);
               // min(不選, 選)
if (dp[i
                      - 1][j - 1] + v[i].first + v[i].second <= k) {
                     // 假如可以選, 更新 ans 時再加回去 bi
                    ans = max(ans. i):
          dp[i][1] = min(dp[i - 1][1], v[i].first - v[i].second);
     cout << ans << "\n";
}
```

10 Geometry

10.1 Basic [d41d8c]

```
template < class Ta
struct Point {
     T x. v:
     . ^, y, Point(const T &x_ = \theta, const T &y_ = \theta) : x(x_), y(y_) {} template<class U> operator Point<U>() {
          return Point<U>(U(x), U(y));
     Point &operator+=(const Point &p) & {
    x += p.x; y += p.y; return *this;
     Point & operator -= (const Point &p) & {
          x -= p.x; y -= p.y; return *this;
     Point & operator *= (const T & v) & {
          x *= v; y *= v; return *this;
     Point & operator /= (const T & v) & {
          x /= v; y /= v; return *this;
     Point operator - () const {
          return Point(-x, -y);
     friend Point operator+(Point a, const Point &b) {
          return a += b;
     friend Point operator - (Point a, const Point &b) {
     friend Point operator*(Point a, const T &b) {
   return a *= b;
     friend Point operator/(Point a, const T &b) {
          return a /= b;
     friend Point operator*(const T &a, Point b) {
   return b *= a;
     friend bool operator == (const Point &a, const Point &b) {
   return a.x == b.x && a.y == b.y;
     friend istream &operator>>(istream &is, Point &p) {
          return is >> p.x >> p.y;
     friend ostream & operator < <(ostream &os, const Point &p) {
   return os << "(" << p.x << ", " << p.y << ")";</pre>
template < class T >
T dot(const Point < T > &a, const Point < T > &b) {
     return a.x * b.x + a.y * b.y;
template < class T>
  cross(const Point<T> &a, const Point<T> &b) {
  return a.x * b.y - a.y * b.x;
```

```
template < class T>
T square(const Point<T> &p) {
     return dot(p, p);
template < class T>
double length(const Point < T > & p) {
    return sqrt(double(square(p)));
template < class T>
Point<T> normalize(const Point<T> &p) {
     return p / length(p);
template < class T>
Point<T> rotate(const Point<T> &a) {
     return Point(-a.y, a.x);
template < class T>
int sgn(const Point<T> &a) {
    return a.y > 0 || (a.y == 0 && a.x > 0) ? 1 : -1;
template < class T>
struct Line {
   Point<T> ;
     Point<T> b;
     Line(const Point<T> &a_ = Point<T>()
           , const Point<T> &b_ = Point<T>()) : a(a_), b(b_) {}
double length(const Line<T> &l) {
    return length(l.a - l.b);
template < class T>
bool parallel(const Line<T> &l1, const Line<T> &l2) {
     return cross(l1.b - l1.a, l2.b - l2.a) == 0;
template < class T>
double distance(const Point<T> &a, const Point<T> &b) {
     return length(a - b);
double distancePL(const Point<T> &p, const Line<T> &l) {
    return abs(cross(l.a - l.b, l.a - p)) / length(l);
template < class T>
double distancePS(const Point<T> &p, const Line<T> &l) {
   if (dot(p - l.a, l.b - l.a) < 0)</pre>
     return distance(p, l.a);
if (dot(p - l.b, l.a - l.b) < 0)
return distance(p, l.b);
     return distancePL(p, 1);
template < class T>
bool pointOnLineLeft(const Point<T> &p, const Line<T> &l) {
     return cross(l.b - l.a, p - l.a) > 0;
template < class T>
Point<T
     template < class T>
bool pointOnSegment(const Point<T> &p, const Line<T> &l) {
   return cross(p - l.a, l.b - l.a) == 0 &&
            min(l.a.x, l.b.x) \ll p.x \ll p.x \ll max(l.a.x, l.b.x)
                (l.a.y, l.b.y) <= p.y && p.y <= max(l.a.y, l.b.y);
template < class T>
bool pointInPolygon
     (const Point<T> &a, const vector < Point <T>> &p) {
int n = p.size(), t = 0;
for (int i = 0; i < n; i++)</pre>
          if (pointOnSegment(a, Line(p[i], p[(i + 1) % n])))
               return true;
     for (int i = 0; i < n; i++) {
   auto u = p[i];
   auto v = p[(i + 1) % n];
   if (u.x < a.</pre>
                x && v.x >= a.x && pointOnLineLeft(a, Line(v, u)))
               t ^= 1;
          if (u.x >= a
                .x && v.x < a.x && pointOnLineLeft(a, Line(u, v)))</pre>
               t ^= 1:
     return t == 1;
// 0 : strictly outside
// 1 : on boundary
// 2 : strictly inside
template < class T>
int pointInConvexPolygon
      (const Point<T> &a, const vector<Point<T>> &p) {
     int n = p.size();
if (n == 0) {
          return
     } else if (n <= 2) {</pre>
          return pointOnSegment(a, Line(p[0], p.back()));
```

```
if (pointOnSegment(a, Line(p[0], p[1])) || pointOnSegment(a, Line(p[0], p[n - 1]))) {
      int lo = 1, hi = n - 2;
      while (lo < hi) {
   int x = (lo + hi + 1) / 2;
   if (pointOnLineLeft(a, Line(p[0], p[x]))) {
      lo = x;
}</pre>
             } else {
   hi = x - 1;
      if (pointOnLineLeft(a, Line(p[lo], p[lo + 1]))) {
             return 2;
             return pointOnSegment(a, Line(p[lo], p[lo + 1]));
      }
template < class T>
bool lineIntersectsPolygon
       (const Line<T> &l, const vector<Point<T>> &p) {
      int n = p.size();
      for (int i = 0; i < n; i++) {
   Line<T> seg(p[i], p[(i + 1) % n]);
             if (cross(b - a
    , seg.a - a) == 0 || cross(b - a, seg.b - a) == 0)
                              true;
             if (cross(b
                      - a, seg.a - a) > 0 ^ cross(b - a, seg.b - a) > 0)
                   return true;
      return false:
// 0 : not intersect
// 1 : strictly intersect
// 2 : overlap
// 3 : intersect at endpoint
template < class T>
tuple<int, Point<T>, Point<T>> segmentIntersection
    (const Line<T> &l1, const Line<T> &l2) {
     (const Line<T> &11, const Line<T> &12) {
   if (max(l1.a.x, l1.b.x) < min(l2.a.x, l2.b.x))
      return {0, Point<T>(), Point<T>()};
   if (min(l1.a.x, l1.b.x) > max(l2.a.x, l2.b.x))
      return {0, Point<T>(), Point<T>()};
   if (max(l1.a.y, l1.b.y) < min(l2.a.y, l2.b.y))
      return {0, Point<T>(), Point<T>()};
   if (min(l1.a.y, l1.b.y) > max(l2.a.y, l2.b.y))
      return {0, Point<T>(), Point<T>()};
   if (cross(l1.b - l1.a, l2.b - l2.a) == 0) {
      if (cross(l1.b - l1.a, l2.a - l1.a) != 0) {
            return {0, Point<T>()}. Point<T>());
   }
}
                   return {0, Point<T>(), Point<T>()};
             } else {
                   auto maxx1 = max(l1.a.x, l1.b.x);
                   swap(p1.y, p2.y);
if (p1 == p2) {
    return {3, p1, p2};
                   } else {
                          return {2, p1, p2};
                   }
            }
      auto cp1 = cross(l2.a - l1.a, l2.b - l1.a);
auto cp2 = cross(l2.a - l1.b, l2.b - l1.b);
      auto cp3 = cross(l1.a - l2.a, l1.b - l2.a);

auto cp4 = cross(l1.a - l2.b, l1.b - l2.b);

if ((cp1 > 0 && cp2 > 0) || (cp1 < 0 && cp2
       < 0) || (cp3 > 0 && cp4 > 0) || (cp3 < 0 && cp4 < 0))
  return {0, Point<T>(), Point<T>()};
Point p = lineIntersection(l1, l2);
      if (cp1 != 0 && cp2 != 0 && cp3 != 0 && cp4 != 0) {
             return {1, p, p};
      } else {
    return {3, p, p};
double distanceSS(const Line<T> &l1, const Line<T> &l2) {
   if (get<0>(segmentIntersection(l1, l2)) != 0)
      return 0.0;
      return min({distancePS(l1.a, l2), distancePS(l1
    .b, l2), distancePS(l2.a, l1), distancePS(l2.b, l1)});
bool segmentInPolygon
     (const Line<T> &l, const vector<Point<T>> &p) {
       int n = p.size();
      if (!pointInPolygon(l.a, p)) return false;
```

```
if (!pointInPolygon(l.b, p)) return false;
for (int i = 0; i < n; i++) {
    auto u = p[i];
          auto v = p[(i + 1) % n];
auto w = p[(i + 2) % n];
          auto [t, p1, p2] = segmentIntersection(l, Line(u, v));
if (t == 1) return false;
if (t == 0) continue;
                if (pointOnSegment(v, l) && v != l.a && v != l.b)
    if (cross(v - u, w - v) > 0)
        return false;
          || pointOnLineLeft(l.b, Line(v, u)))
               return false;
} else if (p1 == v) {
   if (l.a == v) {
                           if (pointOnLineLeft(u, l)) {
    if (pointOnLineLeft(w, l)
        && pointOnLineLeft(w, Line(u, v)))
                                      return false;
                          } else +
                                if (pointOnLineLeft(w, l)
                                      || pointOnLineLeft(w, Line(u, v)))
                                      return false:
                     } else if (l.b == v) {
   if (pointOnLineLeft(u, Line(l.b, l.a))) {
      if (pointOnLineLeft(w, Line(l.b, l.a)))
                                      && pointOnLineLeft(w, Line(u, v)))
                                      return false:
                          || pointOnLineLeft(w, Line(u, v)))
                                      return false:
                     } else {
                                if (pointOnLineLeft(w, l)
                                      || pointOnLineLeft(w, Line(u, v)))
                                      return false:
                          }
                     }
               }
          }
     return true;
template < class T>
vector<Point<T>> convexHull(vector<Point<T>> a) {
     sort(a.begin()
          , a.end(), [](const Point<T> &l, const Point<T> &r) {
return l.x == r.x ? l.y < r.y : l.x < r.x;</pre>
     a.resize(unique(a.begin(), a.end()) - a.begin()):
     if (a.size() <= 1) return a;
vector<Point<T>> h(a.size() + 1);
     int s = 0, t = 0;
for (int i = 0; i < 2; i++, s = --t) {
          h[t++] = p;
          reverse(a.begin(), a.end());
     return {h.begin(), h.begin() + t};
vector<Point<T>> hp(vector<Line<T>> lines) {
     sort(lines.begin(), lines.end(), [&](auto l1, auto l2) {
    auto d1 = l1.b - l1.a;
    auto d2 = l2.b - l2.a;
    if (sgn(d1) != sgn(d2))
        return sgn(d1) == 1;
    }
}
          return cross(d1, d2) > 0;
     deque<Line<T>> ls;
     deque<Point<T>> ps;
for (auto l : lines) {
          if (ls.empty()) {
    ls.push_back(l);
                continue:
           while (!ps.empty() && !pointOnLineLeft(ps.back(), l))
          ps.pop_back(), ls.pop_back();
while (!ps.empty() && !pointOnLineLeft(ps[0], l))
    ps.pop_front(), ls.pop_front();
if (cross(l.b - l.a, ls.back().b - ls.back().a) == 0) {
                if (dot
                      (l.b - l.a, ls.back().b - ls.back().a) > 0) {
                     if (!pointOnLineLeft(ls.back().a, l)) {
                           assert(ls.size() == 1);
                           ls[0] = l;
                     continue;
```

```
}
    return {};
}
ps.push_back(lineIntersection(ls.back(), l));
ls.push_back(l);
}
while (!ps.empty() && !pointOnLineLeft(ps.back(), ls[0]))
    ps.pop_back(), ls.pop_back();
if (ls.size() <= 2) return {};
ps.push_back(lineIntersection(ls[0], ls.back()));
return vector(ps.begin(), ps.end());
}
using P = Point<ll>;
```

10.2 Min Euclidean Distance [8badbf]

```
void minEuclideanDistance() {
       int n; cin >> n;
const ll inf = 8E18;
       vector < Point < ll >> a(n);
       for (int i = 0; i < n; i++) {
     ll x, y;</pre>
              cin >> x >> y;
a[i] = Point<ll>(x, y);
       struct sortY {
              bool operator
                      ()(const Point<ll> &a, const Point<ll> &b) const {
                     return a.y < b.y;</pre>
              }
       struct sortXY {
              bool operator
   ()(const Point<ll> &a, const Point<ll> &b) const {
   return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
              }
       sort(a.begin(), a.end(), sortXY());
vector<Point<ll>> t(n);
       auto devide = [&](auto &&self, int l, int r) -> ll {
   if (l == r) return inf;
   int m = (l + r) / 2;
              ll ans = min(self(self, l, m), self(self, m + 1, r));
ll midval = a[m].x;
             ll midvat - o...
ll p = 0;
for (int i = l; i <= r; i++)
   if ((midval - a[i].x) * (midval - a[i].x) <= ans)
        t[p++] = a[i];
        ' --in()   t.begin() + p, sortY());</pre>
              sort(t.begin(), t.begin() + p, sortY());
for (int i = 0; i < p; i++) {
    for (int j = i + 1; j < p; j++) {
        ans = min(ans, square(t[i] - t[j]));
}</pre>
                            if ((t[i].y -
                                      t[j].y) * (t[i].y - t[j].y) > ans) break;
                     }
              return ans;
       cout << devide(devide, 0, n - 1) << "\n";</pre>
}
```

10.3 Max Euclidean Distance [4aa1f0]

10.4 Lattice Points [d50756]

```
for (int i = 0; i < n; i++) {
            ll dx = polygon[(i + 1) % n].x - polygon[i].x;
            ll dy = polygon[(i + 1) % n].y - polygon[i].y;
            res += __gcd(abs(dx), abs(dy));
      }
    return res;
};
ll res = countBoundaryPoints(polygon);
ll ans = (area - res + 2) / 2;
cout << ans << " " << res << "\n";</pre>
```

10.5 Min Circle Cover [9380bf]

10.6 Min Rectangle Cover [ede9f3]

10.7 Polygon Union Area [a86535]

```
template < class T >
double polygonUnion(vector < vector < Point < T >>> ps) {
   int n = ps.size();
   for (auto &v : ps) v.push_back(v[0]);
   double res = 0;
   auto seg = [&](const Point < T > &o, const Point <
```

11 Polynomial

11.1 FFT [e258ad]

```
const double PI = acos(-1.0);
using cd = complex < double >;
vector<int> rev;
void fft(vector<cd> &a, bool inv) {
        int n = a.size();
if (int(rev.size()) != n) {
                 int k = __builtin_ctz(n) - 1;
                 rev.resize(n);
for (int i = 0; i < n; i++)
    rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;
        for (int i = 0; i < n; i++)</pre>
        if (rev[i] < i) swap(a[i], a[rev[i]]);
for (int k = 1; k < n; k *= 2) {
    double ang = (inv ? -1 : 1) * PI / k;
    cd wn(cos(ang), sin(ang));
    for (int i = 0; i < n; i += 2 * k) {</pre>
                         cd w(1);
for (int j = 0; j < k; j++, w = w * wn) {
                                 cd u = a[i + j];
cd v = a[i + j + k] * w;
a[i + j] = u + v;
                                  a[i + j + k] = u - v;
                }
        if (inv) for (auto &x : a) x /= n;
template < class T>
vector < T> Multiple(const vector < T> &a, const vector < T> &b) {
  vector < Color fa(a.begin(), a.end()), fb(b.begin(), b.end());
  int n = 1, tot = a.size() + b.size() - 1;
  while (n < tot) n *= 2;
  fa.resize(n), fb.resize(n);
  fft(fa, false), fft(fb, false);
  for (int i = 0; i < n; i++)
      fa[i] = fa[i] * fb[i];
  fft(fa. true);</pre>
        fft(fa, true);
vector<T> res(tot);
         for (int i = 0; i < tot; i++)
    res[i] = fa[i].real(); // use llround if need</pre>
         return res;
```

11.2 NTT [6caf78]

```
template < int V, int P>
Mint < P > CInv = Mint < P > (V).inv();
vector<int> rev;
template < int P>
vector<Mint<P>> roots{0, 1};
template < int P>
Mint<P> findPrimitiveRoot() {
           Mint < P > i = 2
           int k = __builtin_ctz(P - 1);
while (true) {
                      if (power(i, (P - 1) / 2) != 1) break;
           return power(i, (P - 1) >> k);
template < int P>
Mint<P> primitiveRoot = findPrimitiveRoot<P>();
template<>
Mint<998244353> primitiveRoot<998244353> {31};
template<int P>
void dft(vector<Mint<P>> &a) {
           int n = a.size();
           if (int(rev.size()) != n) {
   int k = __builtin_ctz(n) - 1;
   rev.resize(n);
   for (int i = 0; i < n; i++)
        rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;
}</pre>
           while ((1 << k) < n) {
    auto e = power(primitiveRoot</pre>
                                 }
           for (int k = 1; k < n; k *= 2) {
    for (int i = 0; i < n; i += 2 * k) {
        for (int j = 0; j < k; j++) {
            Mint < P > u = a[i + j];
            Mint < P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * roots < P > [k + j];
            P > v = a[i + j + k] * ro
                                            a[i + j] = u + v;
a[i + j + k] = u - v;
                                }
                     }
          }
}
template < int P>
void idft(vector<Mint<P>> &a) {
           int n = a.size();
            reverse(a.begin() + 1, a.end());
           dft(a);
Mint<P> inv = (1 - P) / n;
for (int i = 0; i < n; i++) a[i] *= inv;</pre>
template < int P = 998244353>
struct Poly : public vector<Mint<P>> {
   using Value = Mint<P>;
   Poly() : vector<Value>() {}
           explicit Poly(int n) : vector<Value>(n) {}
explicit Poly(const vector<Value> &a) : vector<Value>(a) {}
           Poly(const
           initializer_list<Value> &a) : vector<Value>(a) {}
template<class InputIt, class = _RequireInputIter<InputIt>>
explicit Poly(InputIt
           first, InputIt last) : vector<Value>(first, last) {}
template < class F>
           Poly shift(int k) const {
                      if (k >= 0) {
    auto b = *this;
                                  b.insert(b.begin(), k, 0);
                      return b;
} else if (this->size() <= -k) {
                                return Poly();
                                 return Poly(this->begin() + (-k), this->end());
           Poly trunc(int k) const {
    Poly f = *this;
                       f.resize(k);
                      return f;
```

```
friend Poly operator+(const Poly &a, const Poly &b) {
   Poly res(max(a.size(), b.size()));
   for (int i = 0; i < a.size(); i++)
      res[i] += a[i];
   for (int i = 0; i < b.size(); i++)</pre>
                 res[i] += b[i];
         return res;
friend Poly operator - (const Poly &a, const Poly &b) {
   Poly res(max(a.size(), b.size()));
   for (int i = 0; i < a.size(); i++)
        res[i] += a[i];</pre>
         for (int i = 0; i < b.size(); i++)
  res[i] -= b[i];</pre>
         return res:
friend Poly operator - (const Poly &a) {
  vector < Value > res(a.size());
  for (int i = 0; i < int(res.size()); i++)
    res[i] = -a[i];</pre>
         return Poly(res);
friend Poly operator*(Poly a, Poly b) {
   if (a.size() == 0 || b.size() == 0)
      return Poly();
        return Poly();
if (a.size() < b.size()) swap(a, b);
int n = 1, tot = a.size() + b.size() - 1;
while (n < tot) n *= 2;
if (((P - 1) & (n - 1)) != 0 || b.size() < 128) {
   Poly c(a.size() + b.size() - 1);
   for (int i = 0; i < a.size(); i++)
        for (int j = 0; j < b.size(); j++)
        c[i + j] += a[i] * b[j];
return c:
                 return c:
        f
a.resize(n), b.resize(n);
dft(a), dft(b);
for (int i = 0; i < n; i++)
    a[i] *= b[i];
idft(a);</pre>
         a.resize(tot):
 friend Poly operator*(Value a, Poly b) {
        b[i] *= a;
return b;
friend Poly operator*(Poly a, Value b) {
    for (int i = 0; i < int(a.size()); i++)
        a[i] *= b;</pre>
friend Poly operator/(Poly a, Value b) {
   for (int i = 0; i < int(a.size()); i++)</pre>
               a[i] /= b;
         return a;
Poly & operator += (Poly b) {
    return (*this) = (*this) + b;
Poly &operator -= (Poly b) {
    return (*this) = (*this) - b;
 Poly & operator *= (Poly b) {
    return (*this) = (*this) * b;
 Poly &operator*=(Value b) {
    return (*this) = (*this) * b;
 Poly & operator /= (Value b) {
         return (*this) = (*this) / b;
 Poly deriv() const {
        fet() ( this -> empty()) return Poly();
Poly res(this -> size() - 1);
for (int i = 0; i < this -> size() - 1; i++)
    res[i] = (i + 1) * (*this)[i + 1];
         return res;
 Poly integr() const {
         Poly res(this->size() + 1);

for (int i = 0; i < this->size(); i++)

res[i + 1] = (*this)[i] / (i + 1);
x = (x * (Poly{2} - trunc(k) * x)).trunc(k);
         return x.trunc(m);
Poly log(int m) const {
    return (deriv() * inv(m)).integr().trunc(m);
Poly exp(int m) const {
    Poly x{1};
    int k = 1;
         while (k < m) {
```

```
k *= 2;
x = (x * (Poly{1} - x.log(k) + trunc(k))).trunc(k);
           return x.trunc(m):
     Poly pow(int k, int m) const {
          int i = 0;
while (i < this->size() && (*this)[i] == 0) i++;
if (i == this->size() || 1LL * i * k >= m)
    return Poly(m);
          return Poly(m);

Value v = (*this)[i];

auto f = shift(-i) * v.inv();

return (f.log(m - i *

k) * k).exp(m - i * k).shift(i * k) * power(v, k);
     Poly sqrt(int m) const {
          Poly x{1};
int k = 1;
           while (k < m) {
    k *= 2;
               x = (x +
                        (trunc(k) * x.inv(k)).trunc(k)) * CInv<2, P>;
          return x.trunc(m):
     Poly mulT(Poly b) const {
   if (b.size() == 0) return Poly();
   int n = b.size();
          reverse(b.begin(), b.end());
return ((*this) * b).shift(-(n - 1));
      vector<Value> eval(vector<Value> x) const {
          if (this->size() == 0)
   return vector<Value>(x.size(), 0);
           const int n = max(x.size(), this->size());
           vector < Poly > q(4 * n);
           vector < Value > ans(x.size());
           x.resize(n);
           function < void (
                int, int, int)> build = [&](int p, int l, int r) {
if (r - l == 1) {
                     q[p] = Poly(1, -x[l]);
                alpj = 'vey'z', 'k'e's',

else {
  int m = (l + r) / 2;
  build(2 * p, l, m);
  build(2 * p + 1, m, r);
  q[p] = q[2 * p] * q[2 * p + 1];
}
               }
          } else {
                     work(1, 0, n, mulT(q[1].inv(n)));
           return ans;
     }
}:
Poly<P> berlekampMassey(const Poly<P> &s) {
   Poly<P> c, oldC;
template < int P = 998244353>
     c.resize(i + 1);
f = i;
          } else {
                auto d = oldC;
                d *= -1:
                d.insert(d.begin(), 1);
                for (int j = 1; j <= d.size(); j++)
    df1 += d[j - 1] * s[f + 1 - j];
assert(df1 != 0);</pre>
                auto coef = delta / df1;
d *= coef;
                Poly<P> zeros(i - f - 1);
                zeros.insert(zeros.end(), d.begin(), d.end());
                d = zeros;
auto temp = c;
c += d;
if (i - temp.size() > f - oldC.size()) {
                     oldC = temp;
          }
     c *= -1:
```

12 Else

12.1 Python [fa7d62]

```
from decimal import * # 無誤差浮點數
from fractions import * # 分數
from random import *
from math import *
  set decimal prec if it could overflow in precision
     (Context(prec=10, Emax=MAX_EMAX, rounding=ROUND_FLOOR))
# read and print
x = int(input())
a, b, c = list(map(Fraction, input().split()))
arr = list(map(Decimal, input().split()))
print(x)
print(a, b, c)
print(*arr)
# set
S = set(); S.add((a, b)); S.remove((a, b))
if not (a, b) in S:
D = dict(); D[(a, b)] = 1; del D[(a, b)]
for (a, b) in D.items():
# random
arr = [randint(l, r) for i in range(size)]
choice([8, 6, 4, 1]) # random pick one
shuffle(arr)
```

12.2 **Bigint** [70f2dd]

```
struct Bigint { // not support hex division
private:
      using u128 = __uint128_t;
static const int digit = 9; // hex: 7
static const int base = 10; // hex: 16
static const int B = power(ll(base), digit);
Bigint(vector<int> x, int sgn) : x(x), sgn(sgn) {}
       template < class U>
       vector<int> norm(vector<U> a) {
               if (a.empty()) return {0};
              if (a.empty()) return {0};
for (int i = 0; i < a.size(); i++) {
    U c = a[i];
    a[i] = c % B;
    c /= B;
    if (c) {
        if (i == a.size() - 1) a.push_back(c);
        else a[i + 1] += c;
}</pre>
               while (a.size() > 1 && a.back() == 0) a.pop_back();
               return {a.begin(), a.end()};
       void resign() {
              sgn = x.back() == 0 ? 1 : sgn;
       vector<int> Add(vector<int> a. vector<int> b) {
               int n = max(a.size(), b.size());
              a.resize(n), b.resize(n);
for (int i = 0; i < n; i++) a[i] += b[i];
return norm(a);</pre>
       vector < int > Minus(vector < int > a, vector < int > b) {
   int n = max(a.size(), b.size());
               a.resize(n), b.resize(n);
               for (int i = 0; i < n; i++) {
    a[i] -= b[i];
    if (a[i] < 0) a[i] += B, a[i + 1]--;</pre>
               return norm(a):
       int toInt(char c) const {
   if (isdigit(c)) return c - '0';
   else return c - 'A' + 10;
       char toChar(int c) const {
    if (c < 10) return c + '0
    else return c - 10 + 'A';</pre>
```

```
public:
     int sgn = 1;
     .eccor <int> x; // 反著存
Bigint() : x {0}, sgn(1) {}
Bigint(ll a) {
    *thic - ^*
            *this = Bigint(std::to_string(a));
     Bigint(string s)
           if (s.empty()) {
   *this = Bigint();
           fif (s[0] == '-') s.erase(s.begin()), sgn = -1;
int add = 0, cnt = 0, b = 1;
while (s.size()) {
                 if (cnt == digit) {
                       x.push_back(add), add = cnt = 0;
                 add += toInt(s.back()) * b;
cnt++, b *= base;
                 s.pop_back();
           if (add) x.push_back(add);
           x = norm(x);
     int size() const { return x.size(); }
Bigint abs() const { return Bigint(x, 1); }
string to_string() const {
           string res;
for (int i = 0; i < x.size(); i++) {</pre>
                 string add;
                 int v = x[i];
for (int j = 0; j < digit; j++)
    add += toChar(v % base), v /= base;</pre>
                 res += add:
           while (res.size() > 1 && res.back() == '0')
           res.pop_back();
if (sgn == -1) res += '-';
           reverse(res.begin(), res.end());
     Bigint operator -() const { return Bigint(x, -sgn); }
Bigint &operator+=(const Bigint &rhs) & {
    if (sgn != rhs.sgn) return *this -= (-rhs);
    x = Add(x, rhs.x), resign();
     Bigint & operator -= (const Bigint &rhs) & {
           if (sgn != rhs.sgn) return *this += -rhs;
if (abs() < rhs.abs()) return *this = -(rhs - *this);</pre>
           x = Minus(x, rhs.x), resign();
return *this;
     friend Bigint operator+(Bigint lhs, Bigint rhs) {
  return lhs += rhs;
     friend Bigint operator - (Bigint lhs, Bigint rhs) {
           return lhs -= rhs;
      friend istream &operator>>(istream &is, Bigint &a) {
           string v; is >> v; a = Bigint(v); return is;
      friend ostream &operator<<(ostream &os, const Bigint &a) {</pre>
           os << a.to_string();
           return os;
     friend bool operator <(const Bigint &a, const Bigint &b) {
   if (a.sgn != b.sgn) return a.sgn < b.sgn;
   if (a.x.size() != b.x.size()) {</pre>
                 return a.x.size() < b.x.size();</pre>
           if (a.x[i] != b.x[i]) return a.x[i] < b.x[i];</pre>
           return 0;
     friend bool operator > (const Bigint &a, const Bigint &b) {
   if (a.sgn != b.sgn) return a.sgn > b.sgn;
   if (a.x.size() != b.x.size()) {
                 return a.x.size() > b.x.size();
           } else {
                 for (int i = a.x.size() - 1; i >= 0; i--)
    if (a.x[i] != b.x[i]) return a.x[i] > b.x[i];
           return 0;
     friend bool operator==(const Bigint &a, const Bigint &b) {
   return a.sgn == b.sgn && a.x == b.x;
     friend bool operator!=(const Bigint &a, const Bigint &b) {
           return a.sgn != b.sgn || a.x != b.x;
     friend bool operator>=(const Bigint &a, const Bigint &b) {
           return a == b || a > b;
      friend bool operator <= (const Bigint &a, const Bigint &b) {</pre>
           return a == b || a < b;
```

12.3 Multiple [fc8c31]

```
Reauire:
// Mint, NTT ~constructor and * operator
const int P1 = 1045430273;
const int P2 = 1051721729;
const int P3 = 1053818881;
const int r12 = Mint<P2>(Mint<P1>::getMod()).inv().x;
const int r13 = Mint<P3>(Mint<P1::getMod()).inv().x;
const int r23 = Mint<P3>(Mint<P2>::getMod()).inv().x;
const int r1323 = Mint<P3>(ll(r13) * r23).x;
const ll w1 = Mint<P1>::getMod();
const ll w2 = w1 * Mint<P2>::getMod();
   Garner's Algorithm
int n = a.size(), m = b.size();
     Poly < P1 > x = Poly < P1
     >(a.begin(), a.end()) * Poly<P1>(b.begin(), b.end());
Poly<P2> y = Poly<P2
           >(a.begin(), a.end()) * Poly<P2>(b.begin(), b.end());
     Poly <P3> z = Poly <P3
           >(a.begin(), a.end()) * Poly<P3>(b.begin(), b.end());
     vector<T> res(x.size());
for (int i = 0; i < x.size(); i++) {
    ll p = x[i].x;</pre>
           ll q = (y[i].x + P2 - p) * r12 % P2;
          ([z[i] + P3 - p) * r1323 + (P3 - q) * r23).x % P3; res[i] = (T(r) * w2 + q * w1 + p);
     return res:
private:
     vector<int> Multiple(vector<int> a. vector<int> b) {
          return norm(arbitraryMult < u128 > (a, b));
     vector<int> smallMul(vector<int> a, int v) {
   vector<ll> res(a.begin(), a.end());
   for (auto &x : res) x *= v;
           return norm(res);
public:
     Bigint &operator*=(const Bigint &rhs) & {
          sgn *= rhs.sgn, resign();
return *this;
     friend Bigint operator*(Bigint lhs, Bigint rhs) {
  return lhs *= rhs;
     }
```

12.4 Division [7e7c85]

```
vector < int > smallDiv(vector < int > a, int v) {
           ll add = 0;
for (int i = a.size() - 1; i >= 0; i--) {
   add = add * B + a[i];
   int q = add / v;
   a[i] = q, add %= v;
           return norm(a);
     Bigint &operator <<=(int n) & {
           if (!x.empty()) {
    vector<int> add(n, 0);
                 x.insert(x.begin(), add.begin(), add.end());
           return *this:
     Bigint &operator>>=(int n) & {
           x = vector
                  <int>(x.begin() + min(n, int(x.size())), x.end());
           return *this;
     friend Bigint operator<<(Bigint lhs, int n) {</pre>
           return lhs <<= n;</pre>
     friend Bigint operator>>(Bigint lhs, int n) {
           return lhs >>= n;
public:
     Bigint &operator/=(const Bigint &rhs) & {
           Bigint a = abs(), b = rhs.abs();

sgn *= rhs.sgn;

if (a < b) return *this = Bigint();

if (b.size() == 1) {
                x = smallDiv(x, rhs.x[0]);
                 Bigint inv = 1LL * B * B / b.x.back();
                 Bigint pre = 0, res = 0;
int d = a.size() + 1 - b.size();
                 int cur = 2, bcur = 1;
while (inv != pre || bcur < b.size()) {
    bcur = min(bcur << 1, b.size());
    res.x = {b.x.end() - bcur, b.x.end()};</pre>
                       pre = inv;
                       inv *= ((Bigint
                             (2)
                                  <- (cur + bcur - 1)) - inv * res);
                       cur = min(cur << 1, d);</pre>
```

```
inv.x = {inv.x.end() - cur, inv.x.end()};
}
inv.x = {inv.x.end() - d, inv.x.end()};
res = a * inv;
res >>= a.size();
Bigint mul = res * b;
while (mul + b <= a) res += 1, mul += b;
x = norm(res.x);
}
return *this;
}
Bigint & operator*=(const Bigint & rhs) & {
return *this = *this - (*this / rhs) * rhs;
}
friend Bigint operator*(Bigint lhs, Bigint rhs) {
return lhs /= rhs;
}
friend Bigint operator*(Bigint lhs, Bigint rhs) {
return lhs %= rhs;
}</pre>
```

12.5 Division-Python [110bd8]