

# Problem 7

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5:35 PM

$$\bar{X}_{Yes} = 10 \quad \text{companies} = "Yes"$$

$$\bar{X}_{No} = 0 \quad \text{companies} = "No"$$

$$\hat{\sigma}_{Yes}^2 = 36 \quad \text{for Yes and No}$$

80% issued dividends

$X$  = normal distribution

predict Yes based on  $X=4$

$$\pi_{Yes} = .80 \quad \text{since } 80\%$$

use LDA since  $\sigma_1 = \sigma_2$  and normal  
use density function 4.16 into 4.15 to get  
4.17, Take the log for 4.18, like  
we did in problem 2 and problem 3.

$$f_k(x) = \frac{1}{\sqrt{2(10)(36)}} e^{\left(-\frac{1}{2(36)}(4-10)^2\right)}$$

$$f_k(x) = \frac{1}{\sqrt{72(36)}} e^{\frac{-(x-10)^2}{3(36)}}$$

$$f_{Yes}(4) = \frac{e^{-1/2}}{\sqrt{72(36)}}$$

$$Pr(Y=Yes | X=4) = \frac{\pi_{Yes} f_{Yes}}{\sum_{i=1}^K \pi_i f_i(4)}$$

$$= \frac{\pi_{Yes} f_{Yes}}{\pi_{No} f_{No}(4) + \pi_{Yes} f_{Yes}}$$

$$f_{No} = \frac{1}{\sqrt{2\pi(36)}} e^{\frac{-(x-0)^2}{2(36)}} = \frac{e^{-2/9}}{\sqrt{72\pi}}$$

$$= .752 \quad \text{when you plug it all in.}$$

★ so 75.2 chance to return a dividend