

**Measurement of the Chiral-Odd Generalized
Parton Distribution Functions through
Non-Parametric Analysis of the Deeply Virtual
Neutral Pion Electroproduction Cross Section at
the Thomas Jefferson National Accelerator Facility
at 10.6 GeV**

by

Robert Johnston

Submitted to the Department of Physics
in partial fulfillment of the requirements for the degree of

Interdisciplinary PhD in Physics and Statistics

at the

MASSACHUSETTS INSTITUTE OF TECHNOLOGY

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Abstract

Deeply virtual exclusive reactions provide unique channels to study both transverse and longitudinal properties of the nucleon simultaneously, allowing for a 3D image of nucleon substructure. This presentation will discuss work towards extracting an absolute cross section for one such exclusive process, deeply virtual neutral pion production, using 10.6 GeV electron scattering data off a proton target from the CLAS12 experiment in Jefferson Lab Hall B . This measurement is important as exclusive meson production has unique access to the chiral odd GPDs, and is also a background for other exclusive processes such as DVCS, making the determination of this cross section crucial for other exclusive analyses.

Thesis Supervisor: Richard Milner
Title: Professor

Acknowledgments

I'd like to take this chance to acknowledge

absolutely nobody



Lupe Fiasco, for inspiration, Nick Cambi for perspiration, and Inky Johnson for motivation.

joe jack Cathy Karen Dow (mit general services) Ernie Kelsey Tami Messina Rice Miskimen Joe (service guy from UMass) All JLab hockey guys Elton Smith JLab the tech guy from JLab that was fat and crazy Thesis Peter Charles axel Fabian jlab people Fridericke Jentoft Jan, ross, frank taylor for thesis

TO DO - Get a slide for Richard (best plot) - Need to include error bars (and bigger data points) on plot vs. T graph - compare chi square of clas12 and clas 6 data points - - Compare to other hall results (A, C) Need to figure out discrepancy between my epsilon calculation and that of Pi0GKVegas.cpp DONE People to email: Maurizio Maxieme Dufrene Kemal Tenzign

Remove low acceptance bins and rerun

Email Simonetta on easy as Pi!

figure out rosenbluth separation a la igor for statistical analysiss need to reine code for grabbing nearest GK model fit because doing averaging doesn't seem to be a good idea

Official Repo: <https://github.com/robertej19/clas12DVPiP> Local working dir: /mnt/c/Users/rober/Dropbox/Bobby/Linux/work/CLAS12/mit-clas12-analysis/theana/paragon/anal Local data dir: /mnt/d/GLOBUS/CLAS12 Simulation submission portal:

For Fall DNP:

More notes for Thesis: GK model link:

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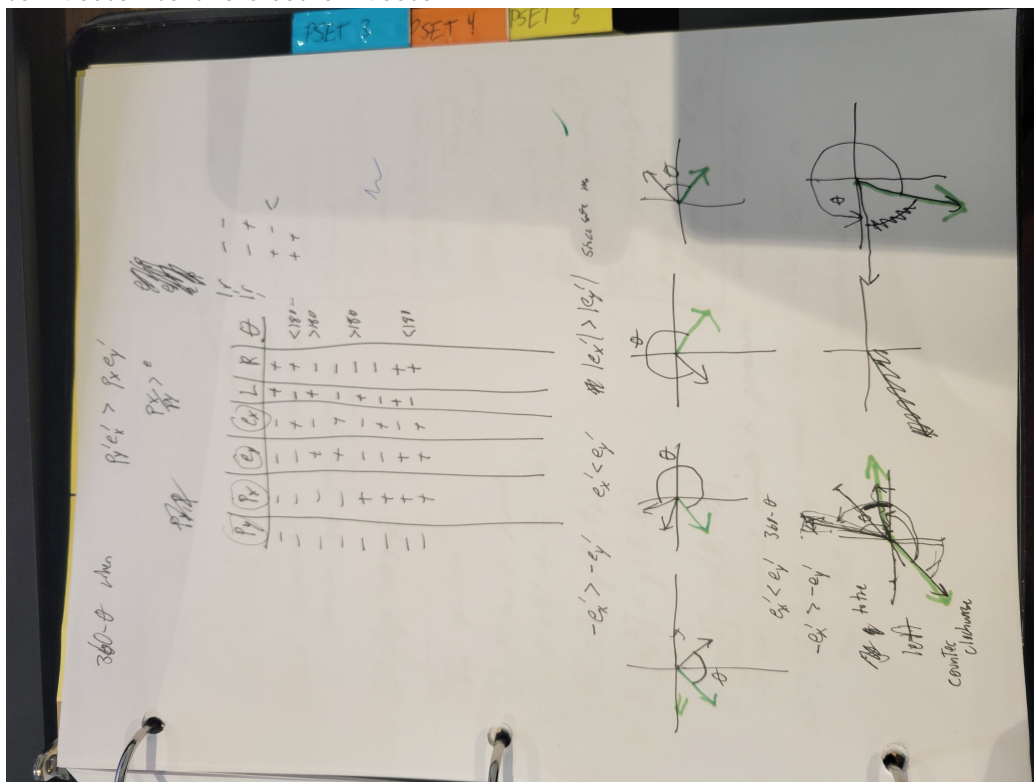
A.1 Armadillos	23
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Chapter 1

On the Trento angle convention

if $\text{dot}(\mathbf{p}_e \text{ cross } \mathbf{p}_e', \mathbf{p}_p')$ is greater than 0, then do $360 - \phi = \phi$. If we expand the above out, we get: $-\mathbf{p}_p'x \cdot \mathbf{e}_z \cdot \mathbf{e}_y' + \mathbf{p}_y \cdot \mathbf{e}_z \cdot \mathbf{e}_x'$ is greater than zero which we can reduce to $-\mathbf{p}_p'x \cdot \mathbf{e}_y' + \mathbf{p}_y \cdot \mathbf{e}_x'$ is greater than zero

By inspecting table below, we can see what this really amounts to, is the trento convention saying that we take the angle by measuring counterclockwise from the proton vector to the electron vector.



Chapter 2

Introduction

I'd like to take this chance to acknowledge

The universe is immense and it seems to be homogeneous, in a large scale, everywhere we look at.



absolutely nobody

Lorem ipsum dolor sit amet, consectetur adipiscing elit. Aliquam quis sollicitudin metus. Quisque quam ex, tincidunt et porttitor quis, tincidunt faucibus quam. Nulla facilisi. Nam a libero posuere, mattis leo ac, ultrices est. Nullam auctor lacus eu metus venenatis, gravida consectetur felis laoreet. Nam non ante felis. Maecenas id

dignissim turpis, eget pulvinar nisl. Cras nec mauris feugiat, aliquam elit ac, blandit ex [1].

Nunc vehicula velit nibh, ut facilisis magna blandit semper. Fusce varius odio in velit mattis porttitor. Vivamus aliquam vulputate quam, non auctor augue ornare ut. Vivamus ac pretium sapien, sed gravida elit. Etiam facilisis risus libero, sed vulputate velit lobortis sed. Aliquam erat volutpat. Sed est orci, dignissim nec varius et, auctor non purus [3, 4]. Morbi feugiat gravida ipsum. Sed maximus nibh eget feugiat tempor. Pellentesque nec urna varius, volutpat dolor at, mattis leo. Vivamus elit eros, pretium sed magna nec, faucibus egestas enim. Vivamus ipsum ex, condimentum eu felis ac, tempus feugiat metus discussed in section 2.2.

2.1 Section sample 1

Ut hendrerit risus egestas, sollicitudin mauris sit amet, fermentum ipsum. Donec vulputate enim in justo pellentesque rhoncus. Nunc a dui condimentum, egestas ipsum eu, fermentum enim. Duis condimentum iaculis luctus. Nam sodales pellentesque luctus. Aenean tristique ante mattis tellus tincidunt, vitae mattis nunc tristique. Ut nec mattis ante, eu sodales ex.

Praesent pulvinar risus in diam mollis tincidunt. Nam aliquam lacus sed eleifend mattis. Ut at blandit ex, eget molestie massa. Morbi fermentum sit amet mauris ut placerat. Ut in eros pretium, congue felis sit amet, gravida justo. Suspendisse purus leo, posuere sed odio vel, mollis tempus nisi. Aenean est tortor, tincidunt et rhoncus ut, fermentum semper leo [2]. Integer id viverra metus, a blandit neque. In in enim eu ipsum euismod hendrerit.

Cras et pellentesque sapien. Maecenas vitae sollicitudin sapien. Sed elementum feugiat ligula, eu maximus nunc porttitor in. Etiam porttitor nisi ante, vel fermentum arcu pulvinar et. Sed bibendum diam nisl, vitae dapibus elit convallis congue. Ut vehicula lectus et enim consectetur cursus. Praesent non viverra augue, id bibendum risus. Maecenas lorem massa, dignissim ac purus in, tincidunt sodales nisi. Praesent condimentum tempus mauris. Etiam vitae sem maximus, auctor orci at, rhoncus

diam. Donec pretium sodales sodales. Donec sodales ultrices metus ac pharetra. Mauris non ullamcorper urna. Mauris ac faucibus tortor, eu lobortis leo are described in detail in section 2.2.

2.2 Section sample 2

Phasellus sed elit vehicula, gravida odio in, vulputate quam. Quisque in elit enim. Vivamus finibus justo elit, sed semper turpis aliquam porttitor. Nulla posuere bibendum nunc sit amet consequat. Vivamus commodo lorem sed metus fermentum rhoncus. Etiam porta sodales purus, vel aliquet lacus facilisis et. Etiam ornare velit non dui auctor fermentum. In elit augue, fringilla at lacinia at, facilisis sit amet lectus. Sed et hendrerit ex. Morbi tristique felis a augue egestas commodo. Nulla porttitor ut urna nec dignissim. Fusce ac pharetra risus, id rhoncus ligula. Pellentesque euismod viverra sem, vel porttitor libero blandit quis. Phasellus orci augue, mattis nec dolor ut, cursus mattis quam. Sed tincidunt eu metus sed pulvinar. Ut a nulla at leo semper accumsan efficitur eget leo.

Sed vel lectus ut dui tempor molestie. Suspendisse blandit sapien posuere quam tempor lobortis. Duis sollicitudin tincidunt dui, at aliquam lorem dictum sit amet. Aenean congue nibh lectus, ut faucibus turpis facilisis quis. Ut aliquet magna at placerat ultricies. Mauris convallis, risus efficitur gravida dapibus, lacus lorem malesuada ligula, eget porta diam felis non turpis. Nulla sed sem finibus, vehicula quam at, vulputate tellus¹

Quisque elit enim, molestie ac metus ut, condimentum convallis nibh:

2.2.1 Subsection sample

In tempus ex nibh, non eleifend risus iaculis ac. Vestibulum ante ipsum primis in faucibus orci luctus et ultrices posuere cubilia Curae; Nullam in nisi eu arcu laoreet sollicitudin. Mauris consectetur venenatis arcu id finibus. Aenean pellentesque consectetur erat lacinia vulputate. Praesent tempus tempus lorem at dignissim. Proin

¹Here is a sample footnote referencing figures B-1 and B-2.

at odio vitae tortor sollicitudin pretium. Quisque ac purus eu sem rutrum bibendum.

Pellentesque ac leo eget lorem vulputate mattis eu a nisl. Duis elit erat, consectetur vulputate ullamcorper a, finibus quis turpis. Vivamus tincidunt dui id purus bibendum malesuada. Fusce accumsan, ipsum quis feugiat sodales, enim est aliquet leo, ut ornare justo mauris quis ex. Sed eros magna, suscipit et blandit non, pretium id felis. Praesent a vehicula tortor. Donec blandit dolor a ipsum sodales, eget aliquet nisl fermentum.

2.2.2 Subsection with list

Ut sollicitudin, lectus eget posuere porttitor, risus dui facilisis risus, a pharetra lacus elit vel eros. Proin fermentum accumsan mauris, quis posuere nisi pharetra scelerisque.

1. Item 1.
2. Item 2.
3. Item 3.

Cras nec ullamcorper mauris. Aliquam erat volutpat. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Suspendisse sed dui ac mi auctor scelerisque. Etiam at semper nisi. Cras nec dolor ac purus feugiat auctor. Nunc eget pulvinar massa.

2.3 Section sample 3

Quisque sed ultrices leo. Donec vestibulum auctor nibh, at faucibus libero mollis in. Quisque massa lorem, feugiat a lectus in, lobortis volutpat lectus. Donec accumsan dui erat, eu tempor tortor facilisis sed. Nulla ullamcorper augue et sapien dapibus, quis bibendum velit porta. Nullam mattis vehicula tortor porttitor porta. Interdum et malesuada fames ac ante ipsum primis in faucibus. Praesent suscipit, lorem vel viverra rhoncus, turpis orci dignissim dui, bibendum pulvinar justo sem vel lorem.

Nam porttitor mollis tristique. Aliquam rhoncus magna quis nisl varius mattis. Sed rhoncus, diam in gravida iaculis, mauris tellus imperdiet turpis, at porttitor est leo vel velit. Praesent faucibus ornare sodales. Sed eu lorem purus.

2.3.1 Another subsection sample

Nullam rhoncus posuere lacus, id volutpat nisi pulvinar viverra. Quisque quis ultricies ante. Duis sollicitudin sapien nec consequat vehicula. Vestibulum convallis erat in arcu aliquam eleifend. Nunc scelerisque lorem non luctus sodales. Curabitur eleifend odio et sagittis semper. Praesent sodales, diam nec vulputate iaculis, neque leo consectetur nunc, a luctus lacus purus et dui. Sed sit amet tortor ullamcorper, malesuada libero quis, imperdiet tortor. Cras tempor blandit massa, sit amet molestie sapien tincidunt quis. Nullam hendrerit venenatis massa, sed lacinia ligula tincidunt vitae.

Nam efficitur et lacus sed eleifend. Aenean quis ipsum eget leo ultrices ornare. Nullam rhoncus ante odio, at dignissim neque posuere eu. Pellentesque sodales tortor est, nec egestas sapien mollis quis. In lectus sapien, pellentesque congue erat consequat, hendrerit aliquet elit. Pellentesque eleifend purus ac diam bibendum, ac auctor ipsum posuere. Cras suscipit leo nec velit fermentum, id varius erat eleifend. Proin sagittis purus id ante lacinia, et congue eros tincidunt. Pellentesque at cursus tellus. Quisque id semper nunc. Quisque viverra a ex at ullamcorper. Morbi mollis erat at ex viverra fringilla. Proin ante dolor, dignissim sodales nisl ac, finibus egestas urna.

Nulla porta urna at pulvinar consectetur. Pellentesque suscipit, neque vitae ultricies rutrum, eros tellus iaculis dui, nec pulvinar justo nibh eu urna. Ut euismod massa nisi, et bibendum risus placerat quis. Integer pretium nulla id risus lobortis laoreet. Aenean quis quam fringilla, elementum odio non, lacinia purus. Vestibulum dui sapien, mollis sit amet massa vel, egestas faucibus velit. Phasellus non justo ut ante vestibulum dictum. Nam in nibh et libero malesuada aliquet. Donec in ex in magna luctus volutpat.

Sed quis dapibus libero. Curabitur id finibus nulla, sed semper felis. Proin dapibus nulla interdum, bibendum tortor et, blandit sapien. Etiam pretium tristique tortor

non lacinia. Aliquam dapibus turpis lorem, sit amet porta ex dignissim vitae. In neque felis, sagittis sed ullamcorper lacinia, lobortis ut turpis. Nam quis aliquet justo. Nam eros mi, aliquam vel massa ac, ornare dignissim erat. This is done by using some combination of

$$\begin{aligned} a_i &= a_j + a_k \\ a_i &= 2a_j + a_k \\ a_i &= 4a_j + a_k \\ a_i &= 8a_j + a_k \\ a_i &= a_j - a_k \\ a_i &= a_j \ll m\text{shift} \end{aligned}$$

instead of the multiplication. For example, you could use:

$$\begin{aligned} r &= 4s + s \\ r &= r + r \end{aligned}$$

Or by xx:

$$\begin{aligned} t &= 2s + s \\ r &= 2t + s \\ r &= 8r + t \end{aligned}$$

Cras pharetra ligula nec lectus bibendum, euismod mattis purus cursus. Nullam ut mi molestie purus ultricies lacinia. Phasellus sed orci ac lacus convallis vestibulum. Quisque id nulla ut ipsum finibus vehicula. Curabitur scelerisque erat lobortis, dapibus purus eget, faucibus sapien. Nam enim leo, faucibus id ante sed, fringilla luctus eros. Morbi vulputate, purus at commodo aliquet, turpis dolor sollicitudin libero, id vehicula risus dui sit amet nulla. Sed auctor efficitur urna. Praesent sagittis tellus ac velit vestibulum dignissim. Vivamus justo enim, pellentesque eu posuere id, mattis

vitae felis. Aliquam id tincidunt diam. Class aptent taciti sociosqu ad litora torquent per conubia nostra, per inceptos himenaeos. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas.

Appendix A

Tables

Table A.1: Armadillos

Armadillos	are
our	friends

Appendix B

Figures

Figure B-1: Armadillo slaying lawyer.

Figure B-2: Armadillo eradicating national debt.

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