

```
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Scientific Programming: The Use of Loops

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Environmental Systems Engineering, teaching seminar at SUNY ESF









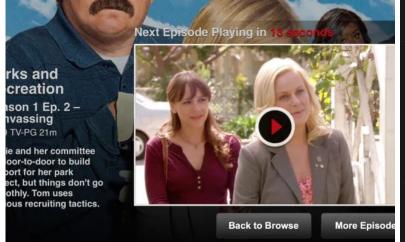
Expectations Control Flow Water Quality Loops **Shortcomings**

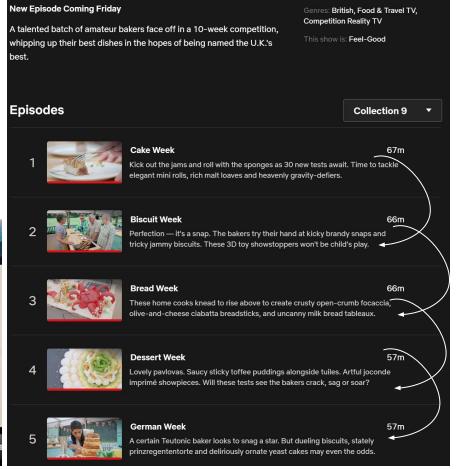
Daily life loops?

Daily life loops?

Netflix's 'post-play' feature:

 play every episode of that season after another

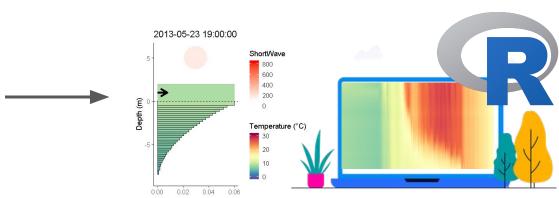


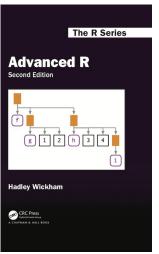


Expectations on today's topic

- important concept of control flow in scientific programming
- example code is in R (Advanced R, https://adv-r.hadley.nz/)
- review of the use of loops
- application for water quality modeling
- material: https://github.com/robertladwig/1DDiffusionExample

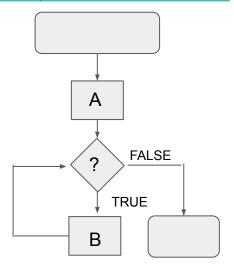






The Control Flow concept

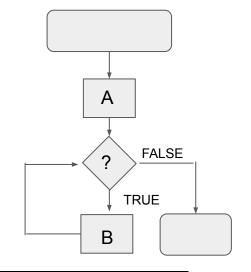
- control flow: order in which statements and calls are executed
- can have pathways and options



The Control Flow concept

- **control flow**: order in which statements and calls are executed
- can have pathways and options
- (mostly) **choices** or **loops**
 - choices are if statements or switch()





```
> if(b > a) {
     c = b - a
}
> print(c)
[1] 1
```

```
> lecture <- switch("Topic",
"Teacher" = "Robert Ladwig",
"Topic" = "Use of Loops")
> print(lecture)
[1] "Use of Loops"
```

The Control Flow concept

- **control flow**: order in which statements and calls are executed
- can have pathways and options
- (mostly) choices or loops
 - choices are if statements or switch
- today's topic: loops

```
> if(b > a) {
     c = b - a
}
> print(c)
[1] 1
```

```
A FALSE
TRUE
B
```

```
> lecture <- switch("Topic",
"Teacher" = "Robert Ladwig",
"Topic" = "Use of Loops")
> print(lecture)
[1] "Use of Loops"
```



- sequence of statements
- carried out iteratively and several times

$$\sum_{i=1}^{n=5} i = ?$$



- sequence of statements
- carried out iteratively and several times

$$\sum_{i=1}^{n=5} i = 1 + 2 + 3 + 4 + 5 = 15$$

Shortcomings



- for **or** while

```
for (item in vector) {
  perform action
```

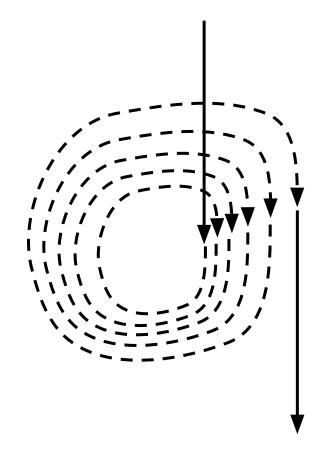
```
while (condition) {
  perform action
```



for or while



$$\sum_{i=1}^{n=5} i$$

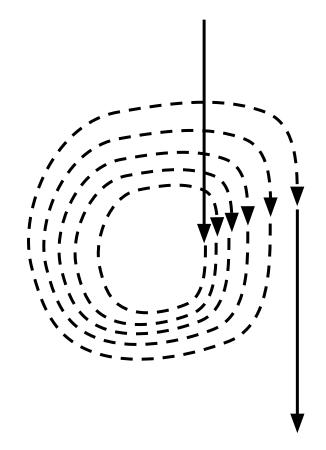




$$> i = 1$$
 $> n = 5$
 $> x = 0$



$$\sum_{i=1}^{n=5} i$$

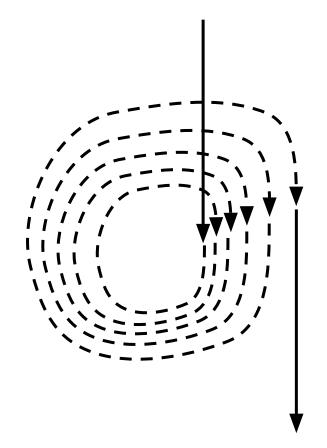




```
> i = 1
> n = 5
> x = 0
> for (item in i:n) {
    x < -x + item
```

Water Quality

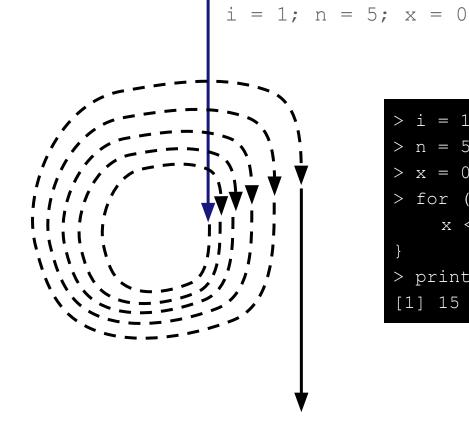
$$\sum_{i=1}^{n=5} i$$





```
> i = 1
> n = 5
> x = 0
> for (item in i:n) {
    x < -x + item
> print(x)
[1] 15
```

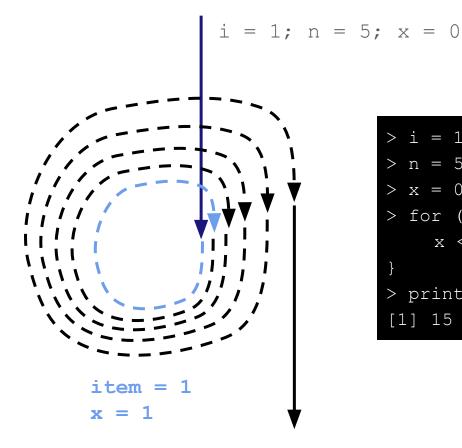
$$\sum_{i=1}^{n=5} i$$





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> i = 1
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    x < -x + item
> print(x)
[1] 15
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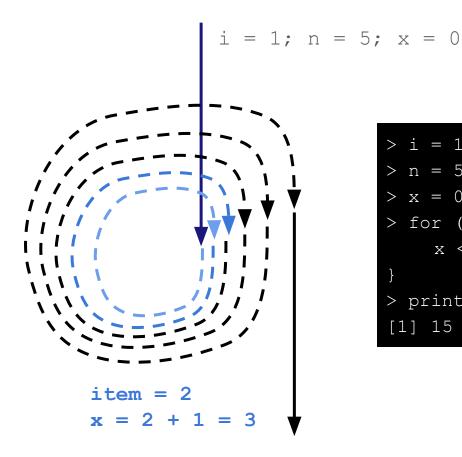
$$\sum_{i=1}^{n=5} i$$





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> i = 1
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    x < -x + item
> print(x)
[1] 15
```

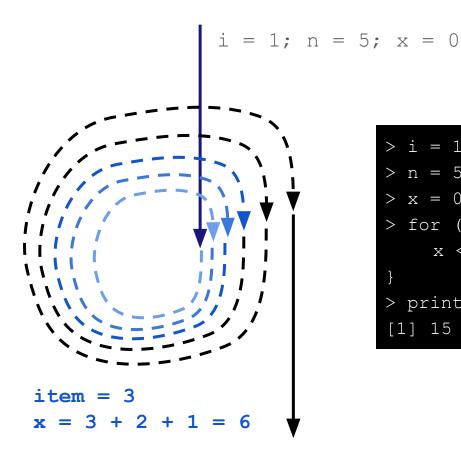
$$\sum_{i=1}^{n=5} i$$





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> i = 1
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> x = 0
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    x < -x + item
> print(x)
[1] 15
```

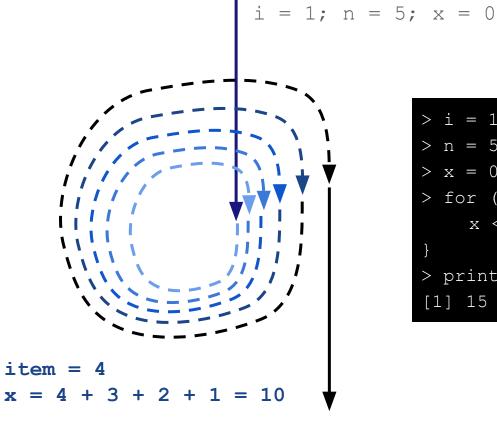
$$\sum_{i=1}^{n=5} i$$





```
> i = 1
> n = 5
> x = 0
> for (item in i:n) {
    x < -x + item
> print(x)
[1] 15
```

$$\sum_{i=1}^{n=5} i$$





```
> i = 1
> n = 5
> x = 0
> for (item in i:n) {
    x < -x + item
> print(x)
[1] 15
```

i = 1; n = 5; x = 0

Loops

- for-loop

$$\sum_{i=1}^{n=5}$$

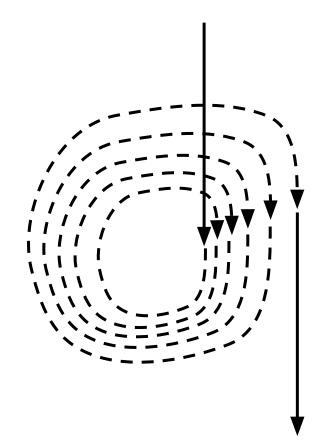
```
item = 5; item == n
```

x = 5 + 4 + 3 + 2 + 1 = 15



```
> i = 1
> n = 5
> x = 0
> for (item in i:n) {
    x < -x + item
> print(x)
[1] 15
```

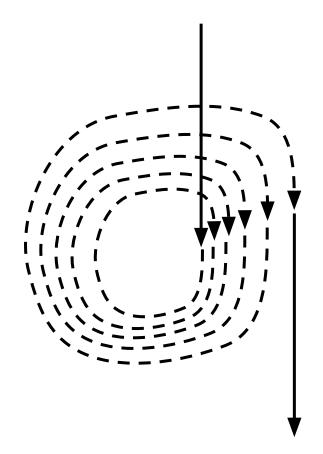
$$\sum_{i=1}^{n=5} i$$





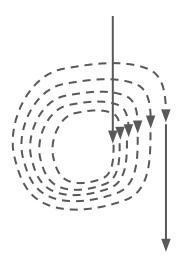
```
> numbers = [1, 2, 3, 4, 5]
> x = 0
> for item in numbers:
      x += item
> x
```

$$\sum_{i=1}^{n=5} i$$



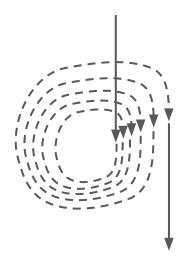


```
> int sum=0, number=5;
> for(int
i=1;i<=number;i++)</pre>
       sum = sum + i;
```

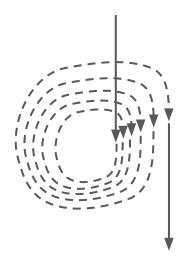




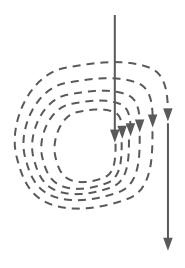
```
> vector <- c(1, 2, 3)
> for (item in vector) {
      vector <- c(vector, item * 2)</pre>
> vector
```



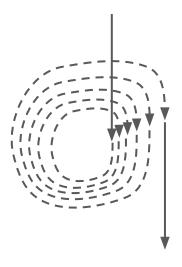
```
> vector <- c(1, 2, 3)
> for (item in vector) {
      vector <- c(vector, item * 2)</pre>
> vector
                 item = 1
                 vector <-c(c(1, 2, 3), 1 * 2)
```



```
> vector <- c(1, 2, 3)
> for (item in vector) {
       vector <- c(vector, item * 2)</pre>
> vector
              item = 2
              vector \leftarrow c(c(1, 2, 3, 2), 2 * 2)
```



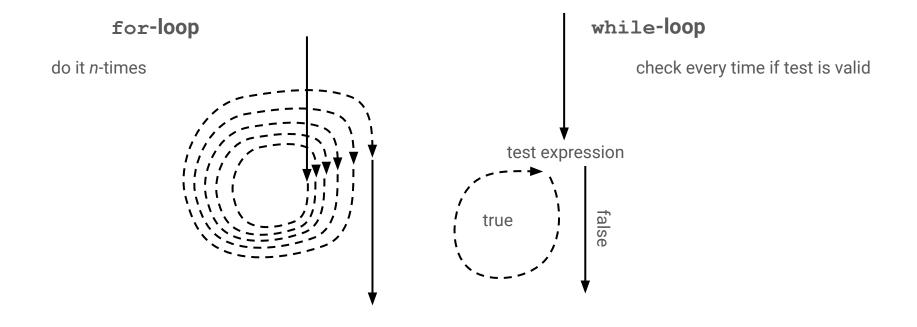
```
> vector <- c(1, 2, 3)
> for (item in vector) {
       vector <- c(vector, item * 2)</pre>
> vector
           item = 3
           vector \leftarrow c(c(1, 2, 3, 2, 4), 3 * 2)
```





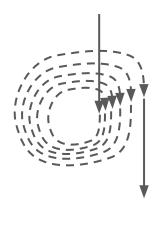
```
> vector <- c(1, 2, 3)
> for (item in vector) {
      vector <- c(vector, item * 2)</pre>
> vector
[1] 1 2 3 2 4 6
```





_oops

while-loop



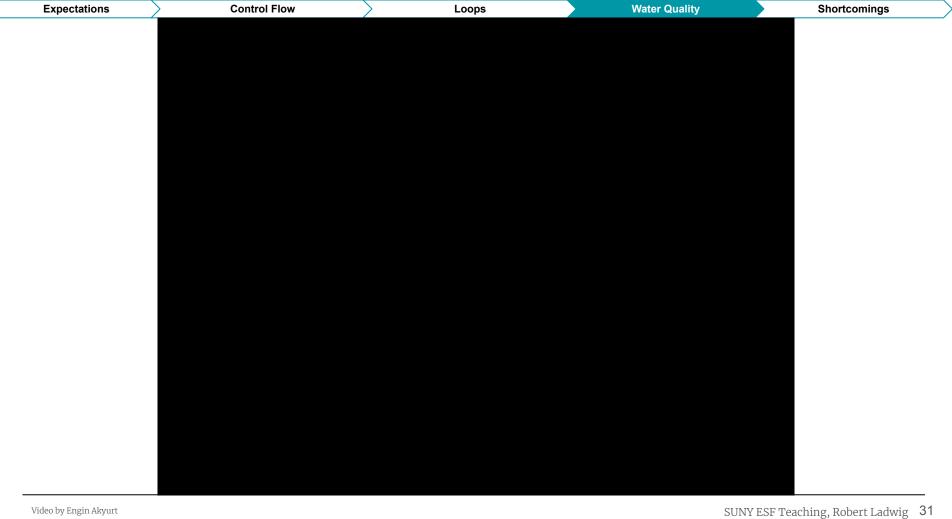
```
> i = 1
> n = 5
> x = 0
> for (item in i:n) {
    x < -x + item
> print(x)
[1] 15
```

```
> item = 1
> n = 5
> x = 0
> while(item <= n) {</pre>
     x < -x + item
     item = item + 1
> print(x)
[1] 15
                             test expression
                          true
```

Combining loops and choices

- the power of control flow statements: finding prime numbers
- natural numbers >1 and divisible by only one and the number itself
- %%: modulo operator, gives remainder of division

```
primeNum <- c()</pre>
for (item in 2:1000) {
     prime <- TRUE
     i = 2
     while(i < item) {</pre>
          if(item %% i == 0){
               prime <- FALSE</pre>
           i <- i + 1
         (prime) {
          primeNum <- c(primeNum,</pre>
     item)
```



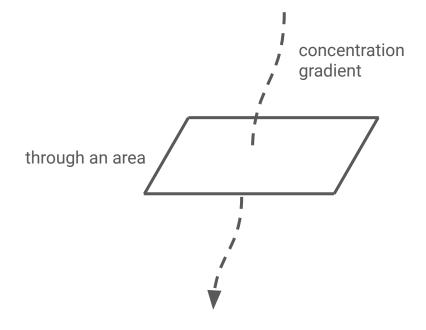
Applying loops for water quality modeling

- in aquatic systems, **diffusion** is one of the main transport processes
 - molecular diffusion: random Brownian motion
 - turbulent diffusion: large scale motion by eddies
- motion by a diffusion coefficient and a (velocity/concentration) gradient
- let's model the diffusion of a (passive) nutrient in a lake
 - passive: no reaction/transformation



Applying loops for water quality modeling

- code a model over time and space
- transport of a concentration over time





Shortcomings

Water Quality

code a model over time and space

diffusion coefficient

$$rac{dC}{dt} = K rac{d^2C}{dz^2}$$

change of concentration over time

second-order derivative of the concentration over the vertical axis z



Applying loops for water quality modeling

- code a model over time and space
- check the units!

area over time

$$rac{dC}{dt} = K rac{d^2C}{dz^2}$$

mass over volume and time

mass over volume and area

$$\frac{g}{m^3s} = \frac{m^2}{s} \frac{g}{m^3m^2}$$



Applying loops for water quality modeling

Control Flow

- luckily, we can discretize this using a **Central Difference** Scheme
- use of Taylor expansion (series expansion of a function)

$$f(x) = f(a) + rac{f'(a)}{1!}(x-a) + rac{f''(a)}{2!}(x-a)^2 + rac{f'''(a)}{3!}(x-a)^3 + O(a^4)$$

centered differencing in space, forward differencing in time



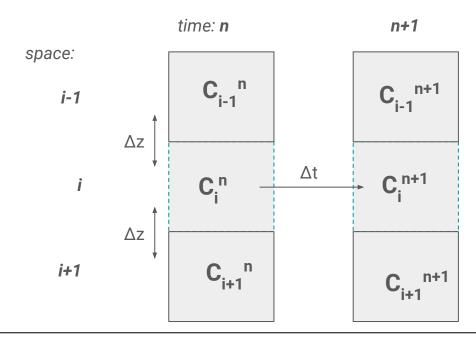
FTCS (forward in time, centered in space)

$$C_i^{n+1} = C_i^n + K \Delta t rac{C_{i+1}^n - 2C_i^n + C_{i-1}^n}{\Delta z^2}$$

FTCS (forward in time, centered in space)

Control Flow

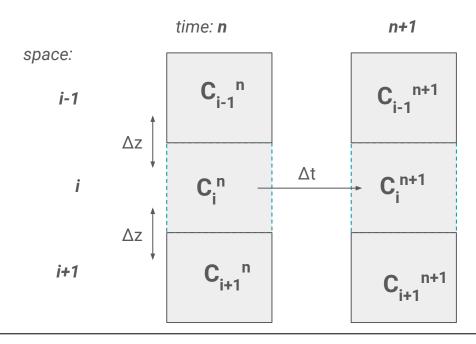
$$C_{i}^{n+1} = C_{i}^{n} + K \Delta t rac{C_{i+1}^{n} - 2C_{i}^{n} + C_{i-1}^{n}}{\Delta z^{2}}$$



FTCS (forward in time, centered in space)

the power of loops!

$$C_i^{n+1} = C_i^n + K \Delta t rac{C_{i+1}^n - 2C_i^n + C_{i-1}^n}{\Delta z^2}$$

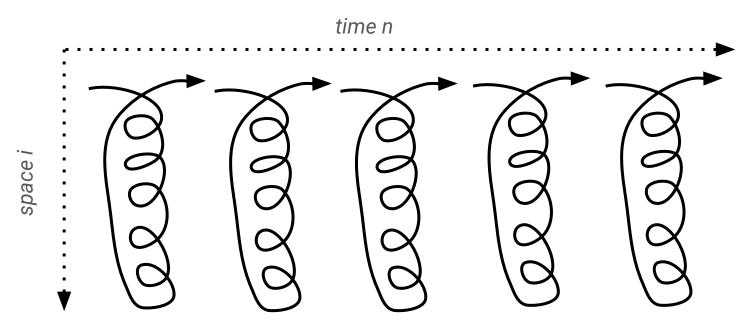


Beware! this is an explicit scheme, therefore its numerical stability depends on the time step size

$$\frac{u\Delta t}{\Delta x} \leq 1$$

FTCS (forward in time, centered in space)

$$C_{i}^{n+1} = C_{i}^{n} + K \Delta t rac{C_{i+1}^{n} - 2C_{i}^{n} + C_{i-1}^{n}}{\Delta z^{2}}$$



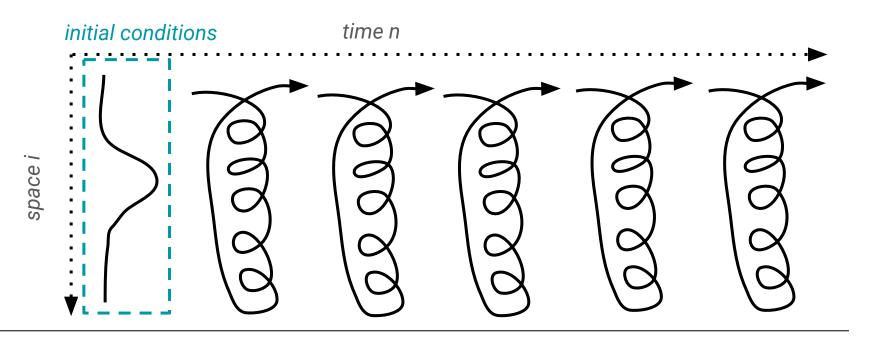
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FTCS (forward in time, centered in space)

$$C_{i}^{n+1} = C_{i}^{n} + K \Delta t rac{C_{i+1}^{n} - 2C_{i}^{n} + C_{i-1}^{n}}{\Delta z^{2}}$$



$$C_i^{n+1} = C_i^n + K\Delta t rac{C_{i+1} - 2C_i + C_{i-1}}{\Delta z^2}$$

i is space index, *n* is time index

```
> time = 100
> space = 100
> conc <- matrix(0, nrow = space, ncol = time)</pre>
# our results in a matrix: 100 seconds times 100 m over the depth
> K = 0.5 # diffusion coefficient, unit: m2/s
> dx = 1 \# our spatial step, unit: m
> dt = 1 # our time step, unit: s
> conc[, 1] = dnorm(seq(1,100,1), mean = 50, sd = 0.1) * 100
# initial conc. is defined vertically through a normal distribution, unit: -
> for (n in 2:ncol(conc)){ # time index
                          for (i in 2:(nrow(conc)-1)){ # space index
                                  [conc[i, n] = conc[i, n-1] + K * dt / dx**2 * (conc[i+1, n-1] - 2 * conc[i, n-1] + conc[i, n-1
                      conc[i-1, n-1]) # our FTCS schema
```

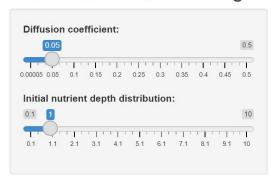
$$C_i^{n+1} = C_i^n + K\Delta t rac{C_{i+1} - 2C_i + C_{i-1}}{\Delta z^2}$$

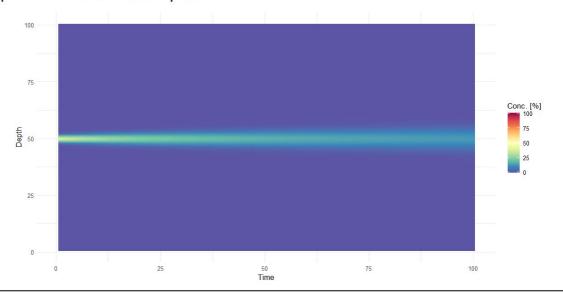
i is space index, *n* is time index

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> for (n in 2:ncol(conc)){ # time index
                          for (i in 2:(nrow(conc)-1)){ # space index
                                  [conc[i, n] = conc[i, n-1] + K * dt / dx**2 * (conc[i+1, n-1] - 2 * conc[i, n-1] + C * 
                      conc[i-1, n-1]) # our FTCS schema
```

- test our loop model: shorturl.at/asx56
- play around with the diffusion coefficient and initial concentration distribution

Our diffusion model using loops over time and space





loops are often not recommended for programming! **memory inefficient** → reallocates output every time

```
> vector <- c(1, 2, 3)
> for (item in vector) {
      vector <- c(vector,</pre>
x * 2)
```

- loops are often not recommended for programming!
 - **memory inefficient** → reallocates output every time
 - **slow** → vectorized alternatives are faster

```
> vector <- c(1, 2, 3)
> for (item in vector) {
      vector <- c(vector,</pre>
x * 2)
```

```
> i = 1
> n = 5
> x = 0
> for (item in i:n) {
    x < -x + item
```

or

```
> x = sum(seq(i,n))
```

- loops are often not recommended for programming!
 - **memory inefficient** → reallocates output every time
 - (2) $slow \rightarrow vectorized$ alternatives are faster
 - (3)endless loops → can easily happen with while-loops

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> vector <- c(1, 2, 3)
> for (item in vector) {
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or

```
> x = sum(seq(i,n))
```

- loops are often not recommended for programming!
 - **memory inefficient** → reallocates output every time
 - (2)**slow** → vectorized alternatives are faster
 - (3)endless loops → can easily happen with while-loops
- **but**: if speed is not always the main issue, loops can be easier to understand + easy to implement ideas
- and: need loops for recursive relationships, e.g., when temporal processes depend on previous ones

```
> vector <- c(1, 2, 3)
> for (item in vector) {
      vector <- c(vector,</pre>
x * 2)
```

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> i = 1
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> x = 0
> for (item in i:n) {
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or

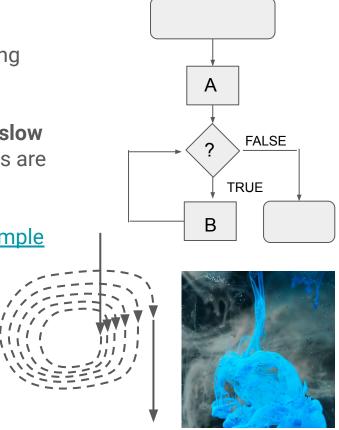
```
> x = sum(seq(i,n))
```

Summing up

- **control flow** in essential for scientific programming
- loops in R are either for or while
- loops can be used to model a dynamic system
- potential shortcomings: memory-inefficient and slow
- useful to test ideas & organize workflows → loops are a 'universal' concept
- material:

https://github.com/robertladwig/1DDiffusionExample

for (item in vector) { perform action

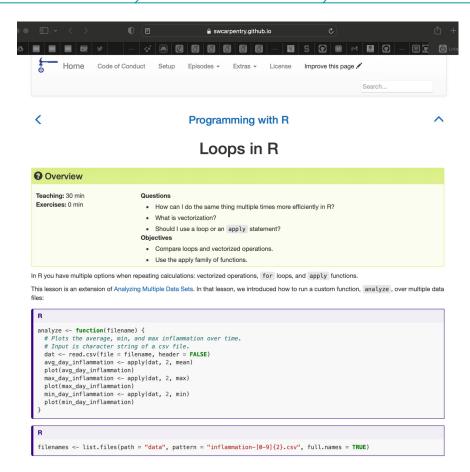


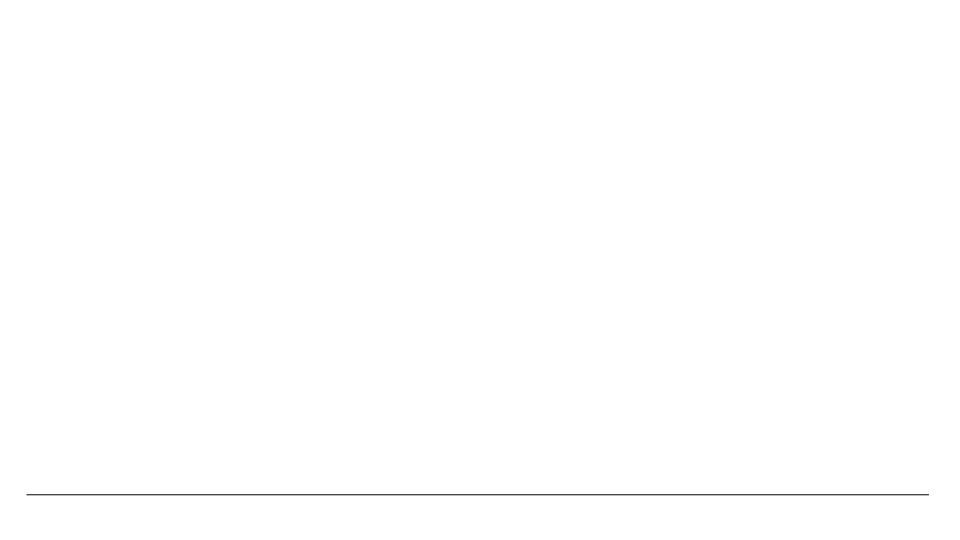
Expectations Control Flow Water Quality Shortcomings Loops

Assignments

software carpentry:

https://swcarpentry.github.io/r-novi ce-inflammation/15-supp-loops-in-d epth/





- applying Taylor expansion: $rac{dC}{dt} = K rac{d^2C}{dz^2}$

forwards:
$$C_{i+1}=C_i+\Delta z rac{\partial C}{\partial z}+rac{\Delta z^2}{2!}rac{\partial^2 C}{\partial z^2}+rac{\Delta z^3}{3!}rac{\partial^3 C}{\partial z^3}+O(\Delta z^4)$$

- $C_{i-1} = C_i \Delta z rac{\partial C}{\partial z} + rac{\Delta z^2}{2!} rac{\partial^2 C}{\partial z^2} rac{\Delta z^3}{2!} rac{\partial^3 C}{\partial z^3} + O(\Delta z^4)$ backwards:
- sum them up to get: $C_{i+1}+C_{i-1}=2C_i+\Delta z^2rac{\partial^2 C}{\partial z^2}+O(\Delta z^4)$
- and re-arrange:

$$rac{\partial^2 C}{\partial z^2} = rac{C_{i+1} - 2C_i + C_{i-1}}{\Delta z^2} + O(\Delta z^4)$$

applying Taylor expansion: $rac{dC}{dt} = K rac{d^2C}{d au^2}$

i is space index, *n* is time index

$$rac{dC}{dt} = K rac{C_{i+1} - 2C_i + C_{i-1}}{\Delta z^2}$$

forward differencing in time:

$$rac{dC}{dt} = rac{C_i^{n+1} - C_i^n}{\Delta t}$$

$$C_i^{n+1} = C_i^n + K\Delta t rac{C_{i+1} - 2C_i + C_{i-1}}{\Delta z^2}$$

FCTS (forward in time, central in space)