

THE IMPACT OF RACIAL BIAS OF STOP AND FRISK TACTIC  
IN THE NEW YORK POLICE DEPARTMENT

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# I. BACKGROUND

## A. INTRODUCTION

Recently there has been a lot of press around racism in America, particularly racism in the form of excessive force used by police. Cases of police using excessive force are all over the news and protests such as #BlackLivesMatter have come up in response.

One controversial policing tactic is the “Stop and Frisk” tactic, where police can stop and investigate pedestrians. Law enforcement argues that this tactic is effective at preventing crime by getting guns and contraband off the street, particularly in high-risk neighborhoods. However, many civil liberties advocates argue this practice is racially biased and many of these stops were not based on reasonable suspicion as defined by the law<sup>1</sup>, even though it is constitutionally required by the fourth amendment.

## B. EXISTING RESEARCH

There are numerous studies that have addressed how the “Stop and Frisk” tactic justifies violence<sup>2</sup>. While these studies are informative on data, methodology, and factor, none of these studies examined whether the use of force is significantly different for individuals of different race.

With our paper, we hope to add to the existing body of knowledge on the topic of stop and frisk, which already covers issues including: stop and frisk usage on minority precincts, racial difference in the total number of people stopped, and the focus of stop and frisk in impoverished neighborhoods.<sup>3,4</sup>

# II. STRATEGY

## A. RESEARCH QUESTIONS

The NYPD has been practicing “Stop and Frisk” for over ten years. They have made public data collected during these investigations.<sup>5</sup> Racial disparities from analyzing this data set are heavily documented, but is also unsurprising since the tactic is used in poorer, riskier neighborhoods, which have a lot more underrepresented minorities to begin with. Instead of looking at this disparity, our project intends to use this data to address the following research questions:

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<sup>1</sup> “Stop and Frisk Data”. NYCLU - <http://www.nyclu.org/content/stop-and-frisk-data>

<sup>2</sup> Simmons, Kami Chavis. “The Legacy of Stop and Frisk: Addressing the vestiges of a violent police culture”. 2014

<sup>3</sup> Goel, Rao, & Shroff. “Precinct or Prejudice”. 2015

<sup>4</sup> Coviello and Persico “An Economic Analysis of Black-White Disparities”. 2013.

<sup>5</sup> “The Stop, Question and Frisk Data”. nyc.gov -

[http://www.nyc.gov/html/nypd/html/analysis\\_and\\_planning/stop\\_question\\_and\\_frisk\\_report.shtml](http://www.nyc.gov/html/nypd/html/analysis_and_planning/stop_question_and_frisk_report.shtml)

1. Do NYPD police officers use more/less force and make more/fewer arrests for any particular race?
2. Are police more likely to make stops near the end of the month versus the rest of the month, which may suggest pressure to meet a number or informal quota?

## B. DATASET

Our data set uses the NYPD stop and frisk database. This database offers a complete collection of police reports filed after stopping people and dates back from 2003. The data is very large and has a wide array of columns. We have combined certain binary variables of interest to accurately represent the information in which we are interested. The following derived columns were made from the data set:

A 'Force Used' column is generated from other columns indicating use of force by law enforcement officers. If any force was used for a given observation, this column is set to true for that observation, otherwise it is set to false. Following are the types of force provided by the NYPD:

- pf\_hands - Hands
- pf\_wall - Suspect against wall
- pf\_grnd - Suspect on Ground
- pf\_drwep - Weapon Drawn
- pf\_ptwep - Weapon Pointed
- pf\_baton - Baton
- pf\_hcuff - Handcuffs
- pf\_pepsp - Pepper Spray
- pf\_other - Other

A 'Had Weapon' column was created. This variable indicates whether the suspect had any kind of weapon. If any of the following indicator columns are set to true for a given observation, this column is set to true, otherwise it is set to false:

- pistol - Pistol
- riflshot - Rifle / Shotgun
- asltweap - Assault Weapon
- knifcuti - Knife or cutting instrument
- machgun - Machine Gun
- othrweap - Other Weapons

Race is an important categorical variable we use in the data set. Each category is converted to a binary variable:

Code	Race	Code	Race
A	Asian / Pacific Islander	Q	White - Hispanic

<b>B</b>	Black	<b>W</b>	White
<b>I</b>	American Indian / Alaskan native	<b>U / X*</b>	Unknown
<b>P</b>	Black - Hispanic	<b>Z</b>	Other

\* The codebook states Unknown race as X, but there is no data with X, just U.

Date data was adjusted to test our hypothesis of whether the last week of the month had more stops. We created a new column that extracted the day of the month from the date. Using the 22nd of the month as a cutoff, we created an indicator variable for the end of the month. Days after the 22nd are “end of the month,” and days before are not “end of the month.”

### III. HYPOTHESIS TESTING

#### Question 1: Is there a difference between the amount of force used between races?

Previous studies show individuals of different races are not equally likely to be stopped. We account for this bias in our experimental design by comparing the **odds** of force being used on individuals stopped. The binary response variable (“Force Used”) naturally led us to consider logistic regression to examine the relationship between race and force used. Our test setup is as follows:

Let  $O_x := \text{odds of force used to force not used for race } x$

$$H_0: \forall i, j \text{ where } i, j \in \text{races}, O_i = O_j$$

$$H_A: \exists i, j \text{ where } i, j \in \text{races}, O_i \neq O_j$$

Using R, we constructed a logistic regression model with the dependent variable of the derived field ‘force used’, and each race category converted to binary indicator variables. We ended up with the following fit equation:

$$F := \text{Force Used}$$

$$F = -1.5615 + 0.3008 R_b + 0.0693 R_I + 0.4727 R_P + 0.3978 R_Q - 0.0696 R_W + 0.2615 R_Z$$

(The intercept represents  $R_A$ , Asian. See Section II.B “Data Sets” for the race code legend. See Appendix for details on the removal of unknown race.)

Test for significant difference between White and Black Hispanic:

All predictor variables were found to be statistically significant. Our findings suggest a significant difference between the amount of force used for different races. The percent chance of force used during a given stop is as follows:

Asian / P.I.	Black	American Indian	Black Hisp.	White Hisp.	White	Other
17.344%	22.085%	18.360%	25.185%	23.799%	16.368%	21.418%

Looking at the confidence intervals, we see that there exists a significant difference. Particularly, you can see how the confidence bands for whites and/or asians do not overlap with those of blacks or hispanics. The confidence bands are displayed below:

```

                                0.312 %    99.688 %
(Intercept) 17.02384    17.66844
raceB       21.31178    22.87897
raceI       17.07308    19.71985
raceP       24.27503    26.11806
raceQ       22.97356    24.64554
raceW       15.71329    17.04538
raceZ       20.50025    22.36450
* Data in Percentages
** Confidence interval is Bonferroni Corrected

```

The confidence band significance was further verified using a t-test of linear combinations, which yield significant p-values under Bonferroni corrections.<sup>6</sup> Thus, we reject the null hypothesis that force used is the same for all races. Further investigation into these results are discussed in the conclusion and analysis.

## Question 2: Are there more or less arrests for any particular race?

The following test is very similar to the previous one. Instead of ‘force used’ as the response variable, we use ‘arrest made.’

Let  $O_x := \text{odds of an arrest being made vs. not being made for race } x$

$H_0: \forall i, j \text{ where } i, j \in \text{races and } O_i = O_j$

$H_A: \exists i, j \text{ where } i, j \in \text{races and } O_i \neq O_j$

A logistic regression model was constructed for data between 2008 and 2014. We look at how likely a stop leads to an arrest depending on race. This provides the following model:

$$Odds_{Arrests} = -2.639 - 0.062R_b - 0.250R_I + 0.068R_P - 0.0227R_Q - 0.006R_W - 0.282R_Z$$

---

<sup>6</sup> An example of this methodology can be found in the appendix, “t-test for Linear Combinations of Races”.

Asian / P.I.	Black	American Indian	Black Hisp.	White Hisp.	White	Other
6.665%	6.288%	5.266%	7.103%	6.525%	6.630%	5.111%

We find some cases of non-overlapping confidence intervals. People classified as ‘Other’ seem particularly low in their arrest rates when stopped. Moreover, ‘American Indians’ have a confidence band that does not overlap with Whites, Hispanics, or Asians. Following are the confidence bands:

```

0.312 % 99.688 %
(Intercept) 6.455600 6.880267
raceB       5.891559 6.709396
raceI       4.581102 6.047683
raceP       6.620174 7.617773
raceQ       6.108983 6.969116
raceW       6.189148 7.101550
raceZ       4.690094 5.567876
* Data in Percentages
** Confidence interval is Bonferroni Corrected

```

As in the previous analysis, we confirmed the significance further using linear combination t-tests.<sup>7</sup> We reject the null hypothesis that different races are arrested at the same rate when stopped.

### Question 3: Are police more likely to make more stops near the end of the month versus the rest of the month?

To address this question, we created an indicator variable for “end of month”, which is true when it’s the end of the month, and false when it’s not the end of the month. “end of month” is false for the first  $\frac{3}{4}$  of the month, and true for the last  $\frac{1}{4}$  of the month. Since the end of the month was about  $\frac{1}{4}$  of the month and the rest of the month was about  $\frac{3}{4}$  of the month, we multiply the average for the end of the month by 3 to balance counts.

The test statistic of the mean and the setup of comparison made this a good fit for a two sample t-test comparison with the following setup.

Let  $\mu_x := \text{mean stops in time category } x$

$$H_0 : \mu_{\text{not last week of month}} - 3 * \mu_{\text{last week of month}} = 0$$

$$H_A : \mu_{\text{not last week of month}} - 3 * \mu_{\text{last week of month}} \neq 0$$

We performed a Welch two-sample t-test, and found no difference in the mean number of stops at the beginning of the month and at the end of the month ( $t = 0.0288$ ,  $p = 0.977$ ). We performed this

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<sup>7</sup> An example of this methodology can be found in the appendix, “t-test for Linear Combinations of Races”.

test because: (1) We have random, independent samples of individuals stops in different boroughs; (2) We are comparing a dependent continuous variable, number of stops, to an independent categorical variable (stops~month) (3) We have enough observations in each category for the Central Limit Theorem to hold; (4) and the variances of each category are different.

#### **Welch Two Sample t-test**

```
data: test.month$BegMonth and test.month$EndMonth
t = 0.028884, df = 93.923, p-value = 0.977
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 -3848.652  3962.277
sample estimates:
mean of x mean of y
 20984.35  20927.54
```

## **IV. CONCLUSIONS AND BIAS ANALYSIS**

### **A. Potential Bias**

#### **Analyzing race for force used and arrests**

Our statistical analysis found a statistically significant difference between the races analyzed. Black and Black Hispanics had a notably larger chance that force would be used on them if they were stopped. Before producing conclusions, we investigate whether there were other factors that may have biased this.

One thing we investigated was whether any particular race was more likely to have a weapon. Such correlations may indicate force used due to finding weapons. Having a weapon was indeed a significant predictor of force being used. Moreover, the data suggested that those with weapons were over twice as likely to have force used on them.<sup>8</sup> This begs the question, maybe races with more force used against them were more likely to be found with a weapon.

Our data found that there was a significant difference in the likelihood of any particular race having a weapon. We found that whites had a significantly higher probability than any other race to carry a weapon when they were stopped. If we were to follow our initial supposition that those with weapons were more likely to have force used upon them, then this data would have suggested that whites stopped should have more force used against them than the other group. Surprisingly, we instead found that they are one of the least likely to have force used against them.<sup>9</sup>

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<sup>8</sup> Data can be found in the appendix under “Analysis of Weapons Found with Race”

<sup>9</sup> *ibid.*



This potential bias source also applies for the arrests made analysis. However, even though we find statistically significant treatment for the 'Other' and 'American Indian' race, they don't stand out in any way with regards to arrests made.

## B. Conclusion

Our analysis set out to find statistical trends in the NYPD Stop and Frisk data set that would give us better insight to the following questions:

1. Do NYPD police officers use more/less force and make more/fewer arrests for any particular race?
2. Are police more likely to make stops near the end of the month versus the rest of the month?

We believe this offers an important contribution as it could allow for a better understanding of the fairness of NYPD practices.

It is important to note that our findings are based on an existing data set of police reports and is by nature, an observational study. Thus, no causal conclusions can be made from the data, only correlational. Moreover, there are so many social, economic, and other factors that contribute to the data that our models, even backed with strong statistical significance, should be accepted as insight to further investigation, not conclusive evidence of any trends.

## Uneven use of force between races

Our statistical analysis of Force used for each race shows that, in the data set, those identified in the reports as Black and Hispanic are significantly more likely to have force used against them when stopped than those identified as 'White' and 'Asian'.

What makes this data more interesting is that although having a weapon is associated with a much larger probability of force being used, only the 'White' group were statistically more likely to have a weapon in the 2008 - 2014 data reviewed.

The fact that although whites are significantly more likely to have a weapon than blacks or hispanics but significantly less likely to have force used against them offers evidence that there may be bias in how police officers judge whether the use of force is needed.

Our data also looked at arrests and found that reports of those identified as 'American Indians' and 'Other' in the reports were statistically less likely to be associated with an arrest being made. Although, this is interesting, it is not clear what potential reasons may be associated with this. However, it is important to note, though, that they are the two least represented racial groups in the data in terms of number of reports between 2008 - 2014.

### There is no evidence of more stops at the end of the month

We aggregated the data and compared the number of stops made in the last week of the month versus the rest of the month. This was with the intent to see if police were responding to any pressures like a 'monthly stop quota'.

Our t-test did not reject the null hypothesis. We found no difference in the mean number of number of stops at the beginning of the month and at the end of the month ( $t = 0.0288$ ,  $p = 0.977$ ). Thus, we found no evidence that there was a significant different between the odds of police making a stop at the beginning of the month versus the rest of the month.

## IV. APPENDIX

We did all the calculations using “R Studio”:

### A. Excluding Unknown Race entries for race related questions

Looking at question one, we plotted the original data and found the following regression:

$F := \text{Force Used}$

$$F = -1.5615 + 0.3008 R_b + 0.0693 R_I + 0.4727 R_P + 0.3978 R_Q - 0.0011 R_U - 0.0696 R_W + 0.2615 R_Z$$

(See section II.c “Data Sets” for the race code legend. The intercept represents  $R_A$  (Asian) )

Call:

```
glm(formula = FORCE_USED ~ race, family = binomial(), data = fulltable)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-0.7618	-0.7065	-0.7065	-0.5979	1.9025

Coefficients:

	Estimate	Std. Error	z value	Pr(> z )
(Intercept)	-1.561457	0.008222	-189.909	< 2e-16 ***
raceB	0.300761	0.008432	35.670	< 2e-16 ***
raceI	0.069280	0.024063	2.879	0.00399 **
raceP	0.472706	0.009665	48.911	< 2e-16 ***
raceQ	0.397751	0.008637	46.052	< 2e-16 ***
raceU	-0.001128	0.019577	-0.058	0.95404
raceW	-0.069610	0.009570	-7.273	3.5e-13 ***
raceZ	0.261523	0.012032	21.735	< 2e-16 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 3345680 on 3179027 degrees of freedom  
Residual deviance: 3335214 on 3179020 degrees of freedom  
AIC: 3335230

Number of Fisher Scoring iterations: 4

The regression summary also found that all the statistics were statistically significant except for the unknown race category.

From 2008 - 2014, Unknown race stops accounted for only 1% of the massive dataset and the data does not serve to help us understand our question nor would excluding them bias the race data.

	race	N
1:	B	1665022
2:	Q	788476
3:	P	205679
4:	W	304519
5:	Z	76988
6:	A	103184
7:	I	13045
8:	U	22115

Thus, we opted to refit the data without these confusing points. Refitting the data, the new equation ends up being exactly the same as the old but without the Unknown race predictor and all the coefficients are significant:

$$F = -1.5615 + 0.3008 R_b + 0.0693 R_I + 0.4727 R_P + 0.3978 R_Q - 0.0696 R_W + 0.2615 R_Z$$

Call:

```
glm(formula = FORCE_USED ~ race, family = binomial(), data = table)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-0.7618	-0.7065	-0.7065	-0.5979	1.9025

Coefficients:

	Estimate	Std. Error	z value	Pr(> z )
(Intercept)	-1.561457	0.008222	-189.909	< 2e-16 ***
raceB	0.300761	0.008432	35.670	< 2e-16 ***
raceI	0.069280	0.024063	2.879	0.00399 **
raceP	0.472706	0.009665	48.911	< 2e-16 ***
raceQ	0.397751	0.008637	46.052	< 2e-16 ***
raceW	-0.069610	0.009570	-7.273	3.5e-13 ***
raceZ	0.261523	0.012032	21.735	< 2e-16 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 3324995 on 3156912 degrees of freedom  
 Residual deviance: 3314822 on 3156906 degrees of freedom  
 AIC: 3314836

Number of Fisher Scoring iterations: 4

## B. Beginning vs End of Month Data

The table below depicts the number of stops per month/year (for question 3)

year	month	BegMonth	EndMonth	year	month	BegMonth	EndMonth
1: 2010	1	24926	29696	25: 2012	1	31810	37021
2: 2010	2	24010	22456	26: 2012	2	34715	31197
3: 2010	3	23795	24679	27: 2012	3	35323	33536
4: 2010	4	27494	33258	28: 2012	4	28504	26996
5: 2010	5	31292	29813	29: 2012	5	24350	21842
6: 2010	6	24354	23876	30: 2012	6	17075	15041
7: 2010	7	24179	21471	31: 2012	7	14448	18581
8: 2010	8	21497	24270	32: 2012	8	18045	18194
9: 2010	9	22486	23247	33: 2012	9	17796	18817
10: 2010	10	26009	29329	34: 2012	10	19238	17100
11: 2010	11	26018	23929	35: 2012	11	10884	14447
12: 2010	12	22508	16693	36: 2012	12	15648	12303
13: 2011	1	26436	32089	37: 2013	1	17441	19835
14: 2011	2	32829	28080	38: 2013	2	17965	16882
15: 2011	3	31159	32679	39: 2013	3	16728	10882
16: 2011	4	31926	30132	40: 2013	4	10063	10900
17: 2011	5	30462	29710	41: 2013	5	10348	10823
18: 2011	6	27638	29091	42: 2013	6	8595	7690
19: 2011	7	27284	25889	43: 2013	7	5559	5494
20: 2011	8	23456	25903	44: 2013	8	4001	2289
21: 2011	9	22883	28121	45: 2013	9	1759	2083
22: 2011	10	27660	31461	46: 2013	10	2132	2239
23: 2011	11	32596	25493	47: 2013	11	2197	2086
24: 2011	12	27713	25034	48: 2013	12	2015	1845

## Regression Frisked ~ Race

The coefficients for the logistic regression of being frisked after being stopped:

Coefficients:

	Estimate	Std. Error	z value	Pr(> z )
(Intercept)	0.0794159	0.2253893	0.352	0.72458
binaryendmonth	-0.0217576	0.0037518	-5.799	6.66e-09 ***
raceB	0.5203530	0.0096064	54.167	< 2e-16 ***
raceI	0.0136102	0.0270490	0.503	0.61485
raceP	0.5052509	0.0119013	42.454	< 2e-16 ***
raceQ	0.4538757	0.0098554	46.053	< 2e-16 ***
raceU	0.0707770	0.0221869	3.190	0.00142 **
raceZ	0.2642137	0.0168533	15.677	< 2e-16 ***
sexZ	-0.2708425	0.0163157	-16.600	< 2e-16 ***
month	0.0078648	0.0005926	13.271	< 2e-16 ***
cityBRONX	0.1553748	0.2251750	0.690	0.49018
cityBROOKLYN	-0.3948219	0.2251604	-1.754	0.07951 .
cityQUEENS	0.0206330	0.2251715	0.092	0.92699
citySTATEN IS	-0.5382043	0.2253487	-2.388	0.01693 *
citySTATEN ISLAND	-0.0870866	0.2389788	-0.364	0.71555

## C. Analysis of Weapons Found vs Race

### Force ~ Weapon

```
Call:
glm(formula = FORCE_USED ~ HAD_WEAPON, family = binomial(), data = table)

Deviance Residuals:
    Min       1Q   Median       3Q      Max
-1.1825  -0.6977  -0.6977  -0.6977   1.7505

Coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept)  -1.288756   0.001376  -936.3  <2e-16 ***
HAD_WEAPONTRUE  1.300612   0.009994   130.1  <2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

    Null deviance: 3324995  on 3156912  degrees of freedom
Residual deviance: 3309043  on 3156911  degrees of freedom
AIC: 3309047

Number of Fisher Scoring iterations: 4

> conf<-confint.lm(fit.forcetoweapon)
> conf[2,] = conf[2,] + conf[1,] # add intercept
> conf.probs<- exp(conf) / (exp(conf) + 1) * 100
> conf.probs
              2.5 %    97.5 %
(Intercept)   21.56069 21.65208
HAD_WEAPONTRUE 49.73926 50.85346
```

### Weapon ~ Race

We used a logistical regression to see the likelihood of weapons being found in a stop with race as the predictors.

```
> # Weapon vs Race
> fit.weapon<-glm(HAD_WEAPON~race, data=table, family=binomial())
> summary(fit.weapon)

Call:
glm(formula = HAD_WEAPON ~ race, family = binomial(), data = table)

Deviance Residuals:
    Min       1Q   Median       3Q      Max
-0.1991  -0.1677  -0.1522  -0.1522   3.0813

Coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept)  -4.51589   0.03010 -150.043  < 2e-16 ***
raceB         0.06275   0.03096   2.027   0.0427 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```

raceI      -0.20648    0.09838   -2.099    0.0358 *
raceP       0.22782    0.03563    6.393 1.62e-10 ***
raceQ       0.25810    0.03159    8.170 3.08e-16 ***
raceW       0.60438    0.03281   18.420 < 2e-16 ***
raceZ      -0.22251    0.04915   -4.527 5.98e-06 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 436130  on 3156912  degrees of freedom
Residual deviance: 434684  on 3156906  degrees of freedom
AIC: 434698

Number of Fisher Scoring iterations: 7

> getProbs(fit.weapon)
(Intercept)      raceB      raceI      raceP      raceQ      raceW      raceZ
0.010815630 0.011507956 0.008815638 0.013545379 0.013956037 0.019617824 0.008676677
> conf<-confint.lm(fit.weapon, level=(1-0.05/8) )
> intercept<-conf[1,1:2]
> conf[2:7,1] <- conf[2:7,1] + intercept[1]
> conf[2:7,2] <- conf[2:7,2] + intercept[2]
> conf.probs<- exp(conf) / (exp(conf) + 1) * 100
> conf.probs
      0.312 % 99.688 %
(Intercept) 0.9969695 1.173249
raceB       0.9755693 1.357064
raceI       0.6220436 1.247998
raceP       1.1342368 1.616928
raceQ       1.1815371 1.647807
raceW       1.6568907 2.321454
raceZ       0.6998071 1.075356

```

## t-test for Linear Combinations of Races

The following setup shows the t-test for the null hypothesis “force used is the same for all races.”

$$H_0 : \beta_P - \beta_W = 0$$

$$H_A : \beta_P - \beta_W \neq 0$$

Simultaneous Tests for General Linear Hypotheses

Fit: glm(formula = FORCE\_USED ~ race, family = binomial(), data = fulltable)

Linear Hypotheses:

```

              Estimate Std. Error z value Pr(>|z|)
raceP - raceW == 0 0.542315   0.007056   76.86  <2e-16 ***
---

```

```

Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Adjusted p values reported -- single-step method)

```

Our null hypothesis was as follows:  $H_0 : \forall i, j \in \text{races}, \beta_i = \beta_j$ . Since we found a significant difference above, we can reject the null hypothesis.