

$$L = \frac{1}{2} m \dot{q}_1^2 - \frac{1}{2} k q_1^2 + \frac{1}{2} S q_1 \ddot{q}_1 + \frac{1}{2} S c q_1 \dot{q}_1^2 - \frac{1}{2} S S (q_1 + q_2) (\ddot{q}_1 + \ddot{q}_2)$$

↓ find velocity & acceleration.

The reaction force is  $F = M \ddot{x}_G - M \bar{g}$   
 $F = 2m \ddot{x}_G - 2m \bar{g}$

$$\bar{g} = [g \sin \theta \quad -g \cos \theta]$$

FUNCTION IMPACT

$A_1 \quad J_R = \text{function IMPACT.}$

$$\begin{bmatrix} A_1 & -J_{R2}^T \\ J_{R2} & 0_{2 \times 2} \end{bmatrix} \begin{bmatrix} \dot{x}_1^+ \\ \dot{y}_1^+ \\ \dot{q}_1^+ \\ \dot{q}_2^+ \\ J_{R2} x \\ I_{R2} y \end{bmatrix} = \begin{bmatrix} A_1 \\ 0_{2 \times 2} \end{bmatrix} \begin{bmatrix} \dot{x}_1^- \\ \dot{y}_1^- \\ \dot{q}_1^- \\ \dot{q}_2^- \\ J_{R2} x \\ I_{R2} y \end{bmatrix}$$

$\Delta$  of velocity definition, etc.

$$\delta = \delta u + \delta u_2 = \frac{1}{2} [\dot{x} \dot{y} \dot{q}_1 \dot{q}_2] [A] \begin{bmatrix} l \\ \dot{q}_1 \\ \dot{q}_2 \end{bmatrix}$$

Known  $H_0$  position  $(X, Y)$

$$\dot{x}_j = J_{Rj} \dot{q}_j$$

$$X = l \sin q_1$$

$$Y = l \cos q_1$$

now  $X$  and  $Y$  are known

$$G_1 = \begin{bmatrix} X - l \sin q_1 \\ Y - l \cos q_1 \end{bmatrix} \quad \dot{G}_1 = \begin{bmatrix} \dot{X} - l \cos q_1 \dot{q}_1 \\ \dot{Y} + l \sin q_1 \dot{q}_1 \end{bmatrix}$$

$$G_2 = \begin{bmatrix} X - l \sin(q_1 + q_2) \\ Y + l \cos(q_1 + q_2) \end{bmatrix} \quad \dot{G}_2 = \begin{bmatrix} \dot{X} - l \cos(q_1 + q_2) (\dot{q}_1 + \dot{q}_2) \\ \dot{Y} + l \sin(q_1 + q_2) (\dot{q}_1 + \dot{q}_2) \end{bmatrix}$$

$$\omega_1 = \dot{q}_1 \quad \omega_2 = (\dot{q}_1 + \dot{q}_2)$$

$$\delta_1 = \frac{1}{2} m \begin{bmatrix} \dot{x} - l \cos q_1 \dot{q}_1 & \dot{y} + l \sin q_1 \dot{q}_1 \end{bmatrix} \begin{bmatrix} \dot{x} - l \cos q_1 \dot{q}_1 \\ \dot{y} + l \sin q_1 \dot{q}_1 \end{bmatrix} + \frac{1}{2} m \begin{bmatrix} \dot{x} - l \cos(q_1 + q_2) (\dot{q}_1 + \dot{q}_2) \\ \dot{y} + l \sin(q_1 + q_2) (\dot{q}_1 + \dot{q}_2) \end{bmatrix} \begin{bmatrix} \dot{x} - l \cos(q_1 + q_2) (\dot{q}_1 + \dot{q}_2) \\ \dot{y} + l \sin(q_1 + q_2) (\dot{q}_1 + \dot{q}_2) \end{bmatrix}$$

~~$$\frac{1}{2} m \begin{bmatrix} \dot{x} - l \cos q_1 \dot{q}_1 \\ \dot{y} + l \sin q_1 \dot{q}_1 \end{bmatrix} \begin{bmatrix} \dot{x} - l \cos q_1 \dot{q}_1 \\ \dot{y} + l \sin q_1 \dot{q}_1 \end{bmatrix}$$~~

$$= \frac{1}{2} m \left[ \dot{x}^2 - 2\dot{x} l \cos q_1 \dot{q}_1 + l^2 \dot{q}_1^2 \cos^2 q_1 + \dot{y}^2 + 2\dot{y} l \sin q_1 \dot{q}_1 + l^2 \dot{q}_1^2 \sin^2 q_1 \right]$$

$$= \frac{1}{2} m \left[ \dot{x}^2 + \dot{y}^2 + 2 l \dot{q}_1 (-\dot{x} \cos q_1 + \dot{y} \sin q_1) + l^2 \dot{q}_1^2 \right]$$

$$\mathcal{L}_2 = m \frac{1}{2} \left[ \dot{x}^2 - S C(q_1 + q_2) (\dot{q}_1 + \dot{q}_2) \dot{y} - S S(q_1 + q_2) (\dot{q}_1 + \dot{q}_2) \right] \left[ \dot{x} - S C(q_1 + q_2) (\dot{q}_1 + \dot{q}_2) \right. \\ \left. \dot{y} - S S(q_1 + q_2) (\dot{q}_1 + \dot{q}_2) \right] \\ = \frac{1}{2} m \left[ \dot{x}^2 - 2 S C(q_1 + q_2) (\dot{q}_1 + \dot{q}_2) \dot{x} + S^2 C^2(q_1 + q_2) (\dot{q}_1 + \dot{q}_2)^2 \right. \\ \left. + \dot{y}^2 - 2 S S(q_1 + q_2) (\dot{q}_1 + \dot{q}_2) \dot{y} + S^2 S^2(q_1 + q_2) (\dot{q}_1 + \dot{q}_2)^2 \right] + \frac{1}{2} I (\dot{q}_1 + \dot{q}_2)^2$$

$$= \frac{1}{2} m \left[ \dot{x}^2 + \dot{y}^2 - 2 S (\dot{q}_1 + \dot{q}_2) (\dot{x} C(q_1 + q_2) + \dot{y} S(q_1 + q_2)) + S (\dot{q}_1 + \dot{q}_2)^2 \right] + \frac{1}{2} I (\dot{q}_1 + \dot{q}_2)^2$$

from this, we can extrapolate mapping from the A matrix to  $\mathcal{B}_{TOT} = \mathcal{B}_1 + \mathcal{B}_2$  carefully

$$\begin{bmatrix} \ddot{x} \\ \ddot{y} \\ \ddot{q}_1 \\ \ddot{q}_2 \end{bmatrix} \begin{bmatrix} 2m & 0 & m S C q_1 - m S C(q_1 + q_2) & -m S C(q_1 + q_2) \\ 0 & 2m & m S S q_1 - S S S(q_1 + q_2) & -m S S(q_1 + q_2) \\ m S C(q_1) - m S C(q_1 + q_2) & m S S(q_1) - m S S(q_1 + q_2) & +2m S^2 + 2I & m S^2 + I \\ -m S C(q_1 + q_2) & -m S S(q_1 + q_2) & m S^2 + I & m S^2 + I \end{bmatrix}$$

$$2m a_y \quad \frac{1}{2} m \dot{x}^2 + \frac{1}{2} m \dot{y}^2$$

A found.

It is also only found

$$\ddot{x} = J_R \ddot{q}_e \quad J_R = \begin{bmatrix} 1 & 0 & -l c q_1 & -l c(q_1 + q_2) \\ 0 & 1 & -l s q_1 & -l s(q_1 + q_2) \end{bmatrix}$$