

# Mobile Robots Lab

## Localization using magnets

### Presentation

## Beware

- The robot is pretty much a toy.
- The sensor is extremely rudimentary.
- The problem is not a toy. It's actually a bit challenging and, should you have to solve it from scratch, it would take you some time.
- Much easier variants have been and are still used in the industry.

# The robot

# The robot and the sensor

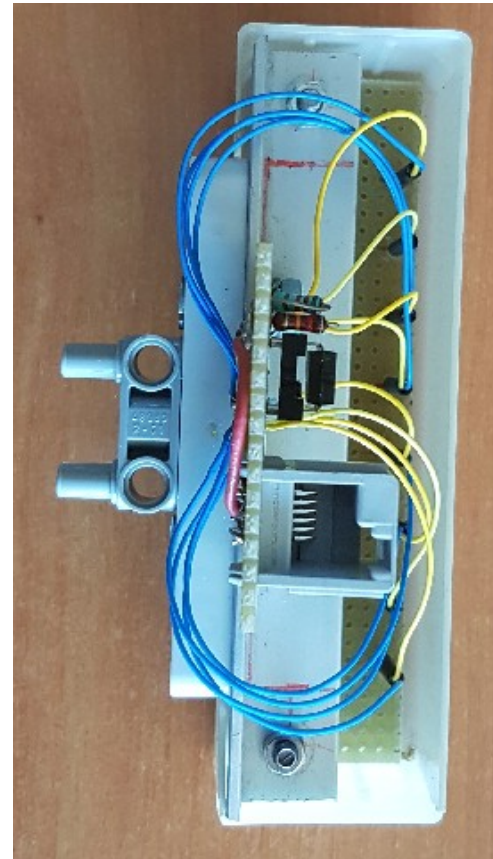
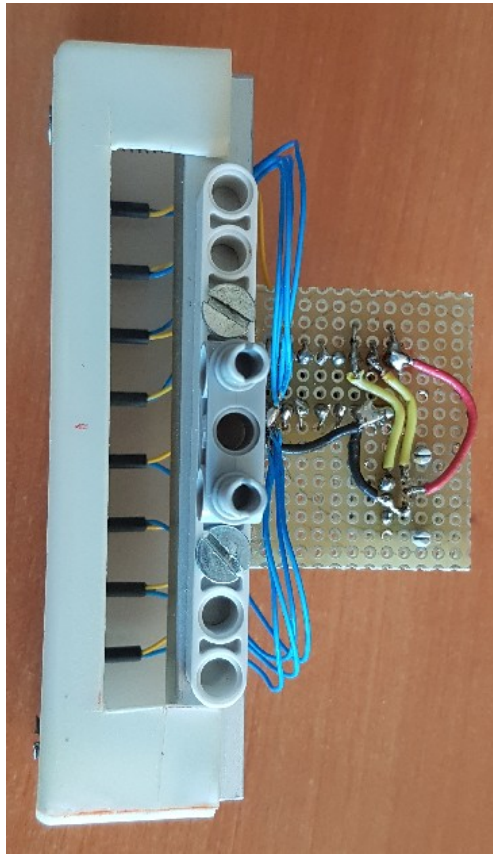


# Robot characteristics

- Encoders:
  - 360 dots per wheel revolution.
  - “Dumbed down” to 45 dots per revolution to make the problem a bit more challenging.
- Recording frequency:
  - 20 Hz.
  - We will work at 5 Hz.

# The sensor and magnet setup

# The magnet detector



# The reed switch

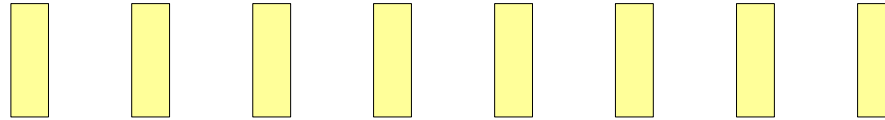


A normally open reed switch.

In a sufficiently intense magnetic field, the switch closes.

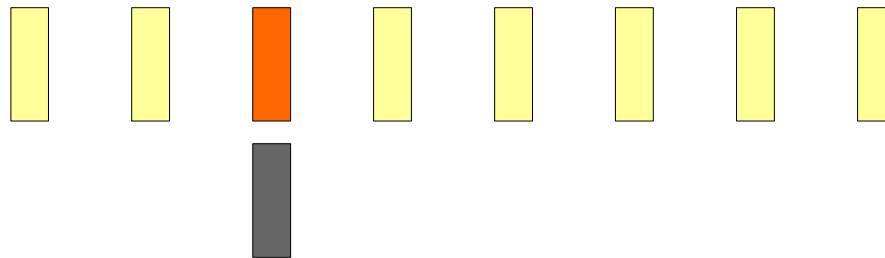


# The magnet sensor



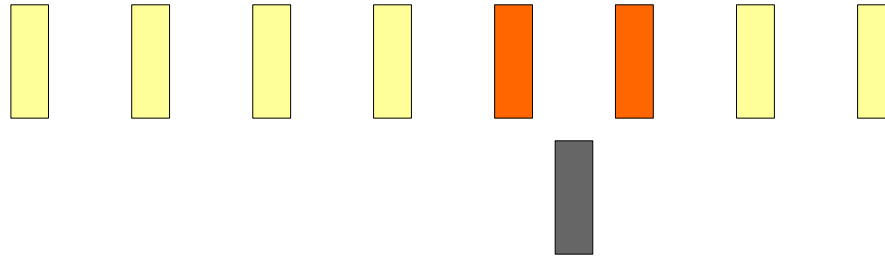
No magnet in the vicinity of the reed switches: all are open

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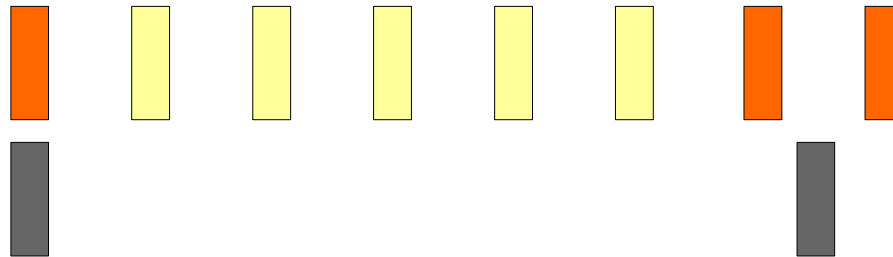
A magnet is right under reed switch 3, which is closed.

# The magnet sensor



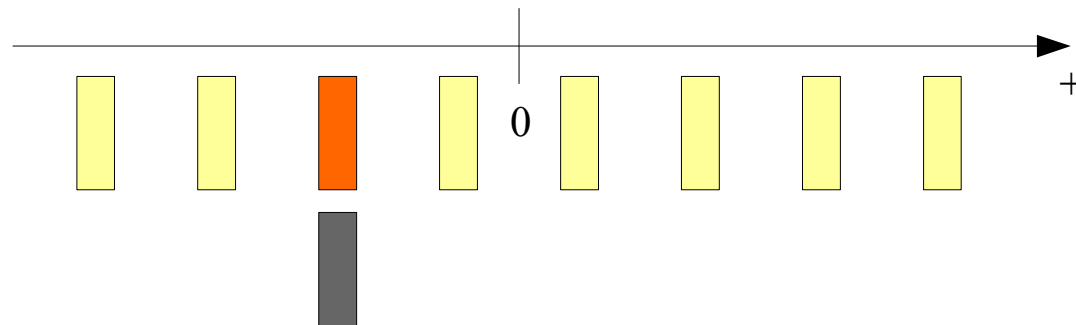
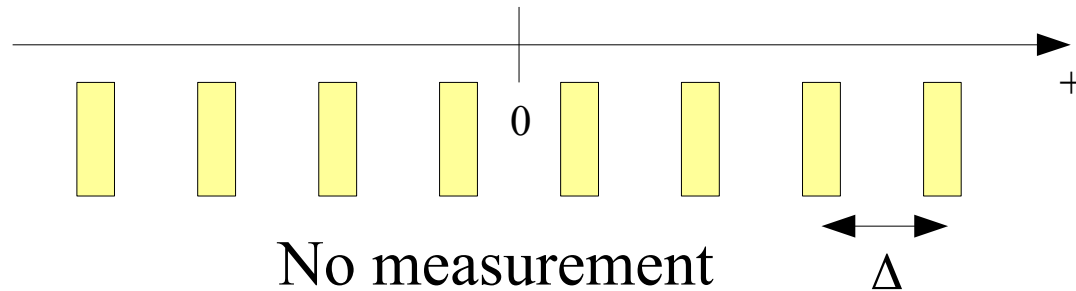
A magnet is right under switches 5 and 6, which are closed.

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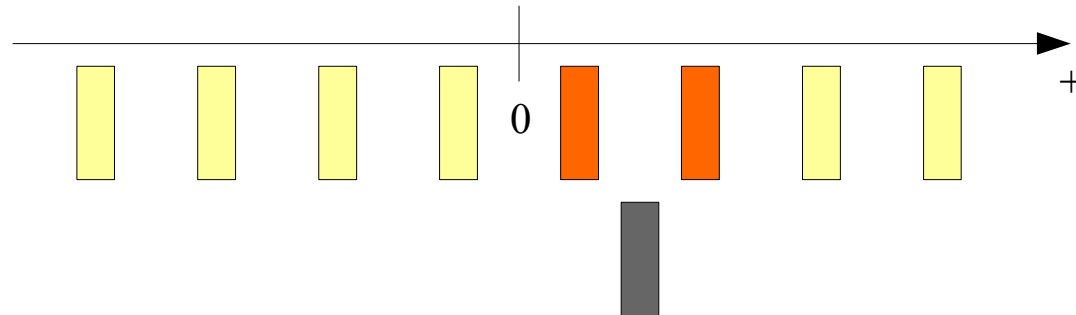
A magnet is right under switch 1, another under 7 and 8

# The magnet sensor measurements

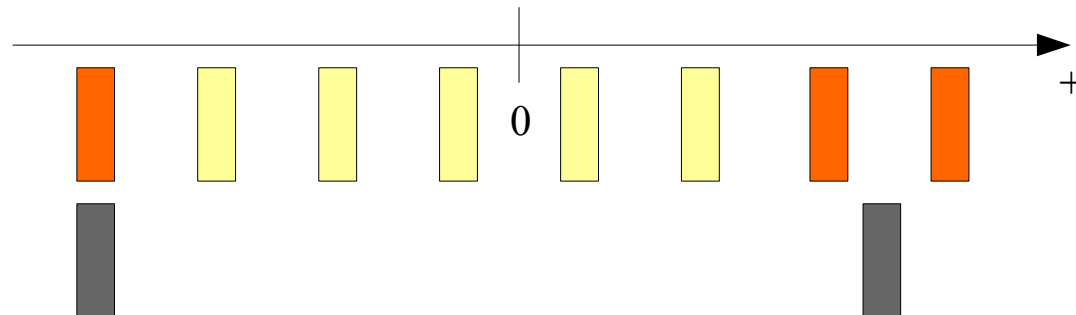


The resolution  $\Delta$  is 10 mm

# The magnet sensor measurements

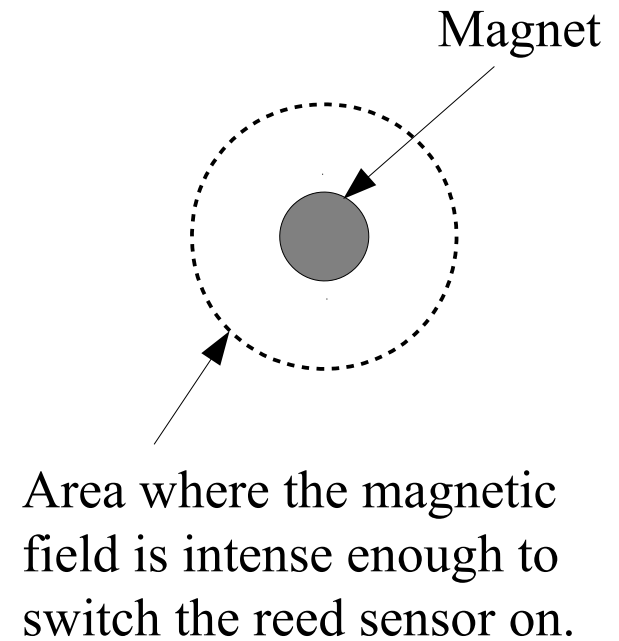
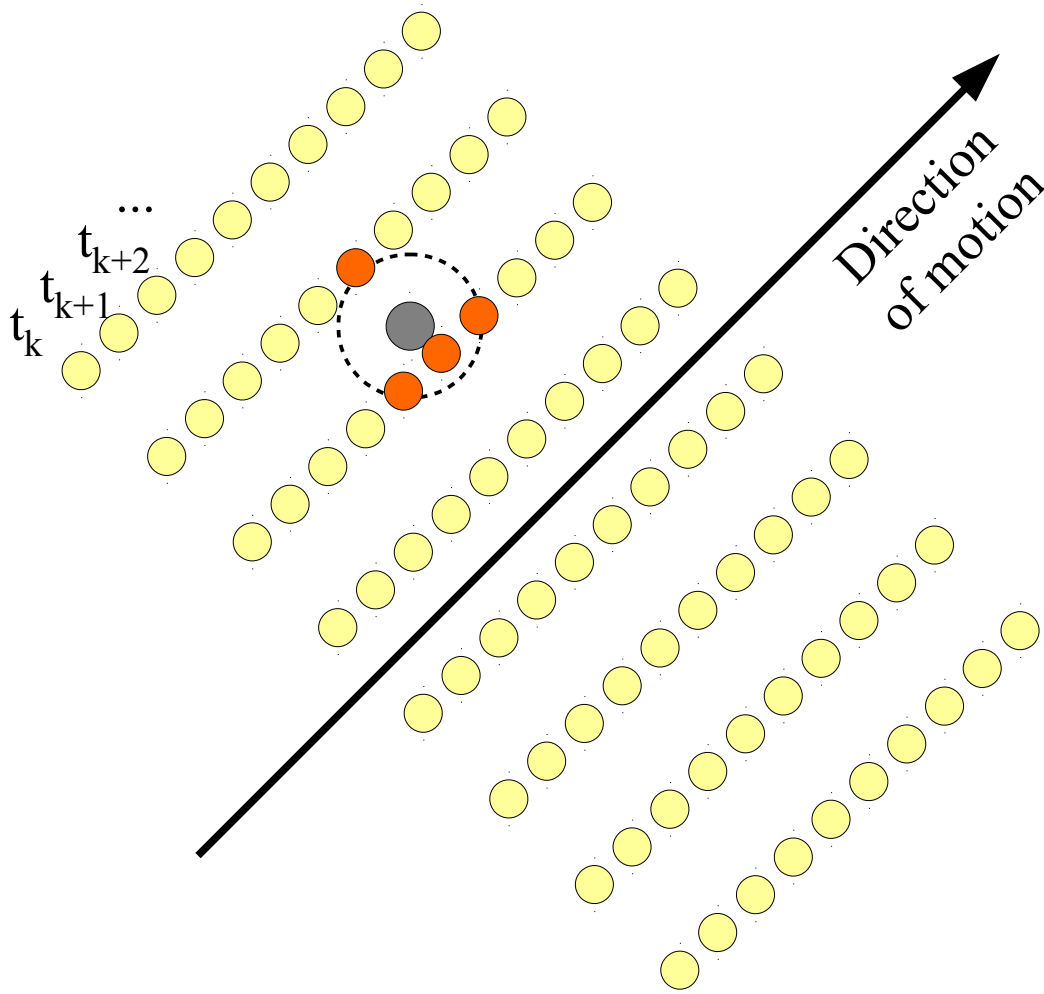


Measurement is  $+\Delta$

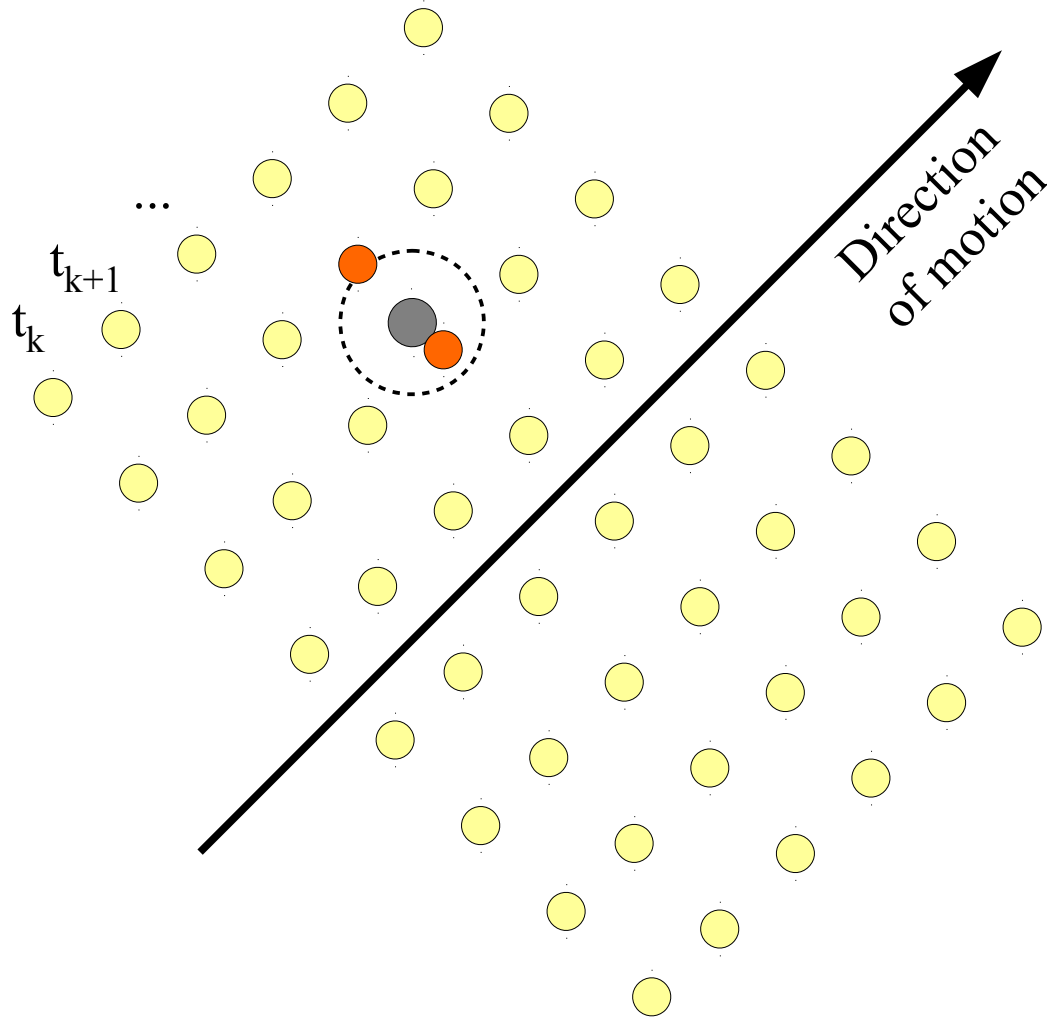


Two measurements:  $-3.5\Delta$  and  $+3\Delta$

# Sensor passing over a magnet



# Sensor passing over a magnet (lower sampling rate)

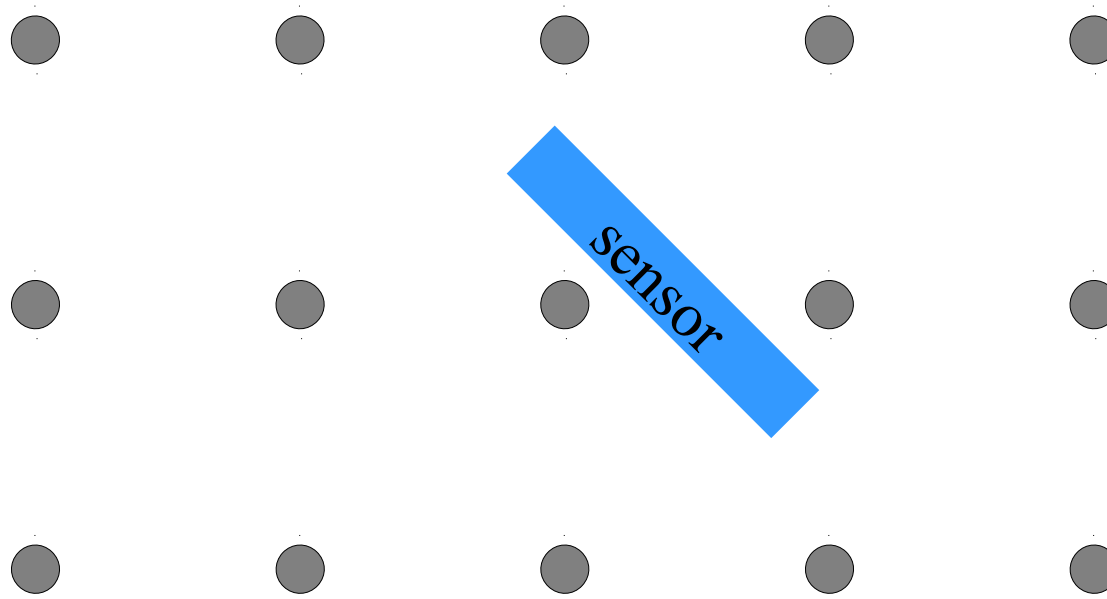


# About the magnet sensor

- The system design parameters are:
  - Magnet field intensity.
  - Inter-magnet distance
  - Reed switch sensitivity.
  - Reed switch number/spacing and sensor length.
- The sensor has been designed in such a way that:
  - When passing over a magnet, either one or two reed switches are activated.
  - When the robot moves, the sensor “cannot avoid crossing magnets”

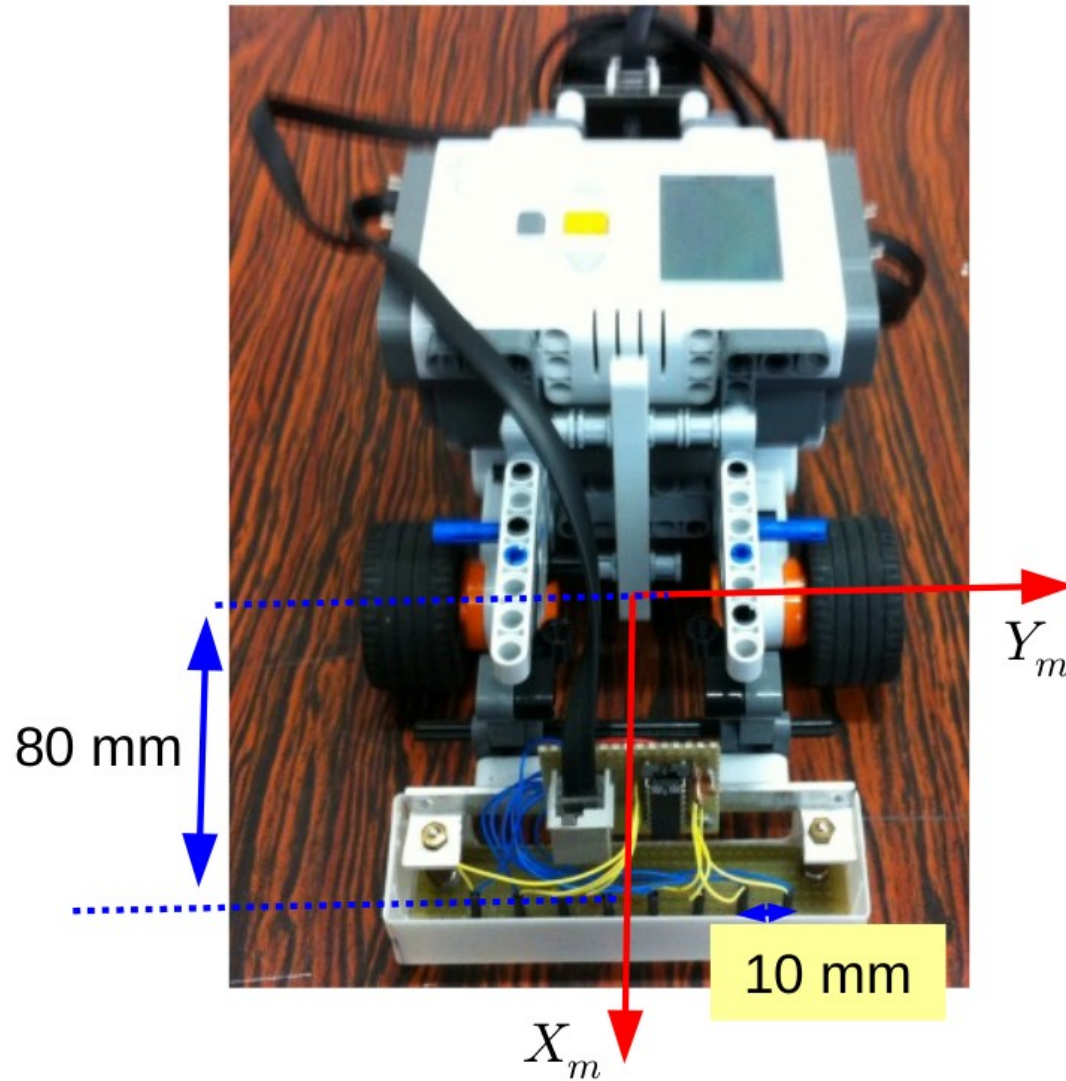
# System characteristics

- 8 reed switches.
- 10 mm interval between reed switches
- 55 mm interval between magnets, arranged in a regular square pattern.





# Robot and sensor

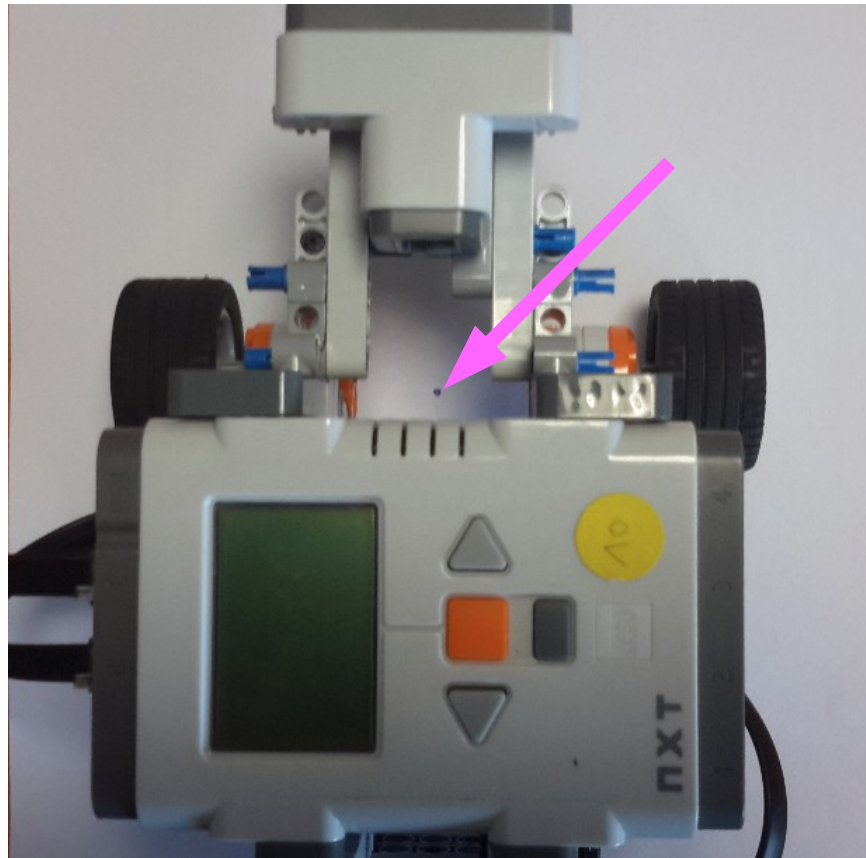


# Information about the setup

- It is available in the file “RobotAndSensorDefinition.m”
  - Robot characteristics
  - Sensor characteristics
  - Magnet array
  - Frequency
- In the initial phases (determination of measurement noise variance), you can change the frequency to 20 Hz, but when you tune/run/test your Kalman filter, the frequency must be reset to 5 Hz.

# Initial positioning of the robot

# Initial positioning of the robot



The center point of the fixed wheel axle is put above a dot painted at (0,0).

# Variant of Kalman filter equations

# Variant of Kalman filter equations

- The program uses a slight variant of the Kalman filter equations, where the input  $u$  is assumed to be disturbed by noise:

$$X_{k+1} = f(X_k, U_k^*) + \alpha_k$$

$$U_k^* = U_k + \beta_k \quad \text{The measured input is affected by an additive noise}$$

$$P_{k+1} = A_k P_k A_k^T + B_k Q_\beta B_k^T + Q_\alpha$$

The error propagation equation is the only change.

$$A_k = \frac{\partial f}{\partial X} \quad B_k = \frac{\partial f}{\partial U}$$

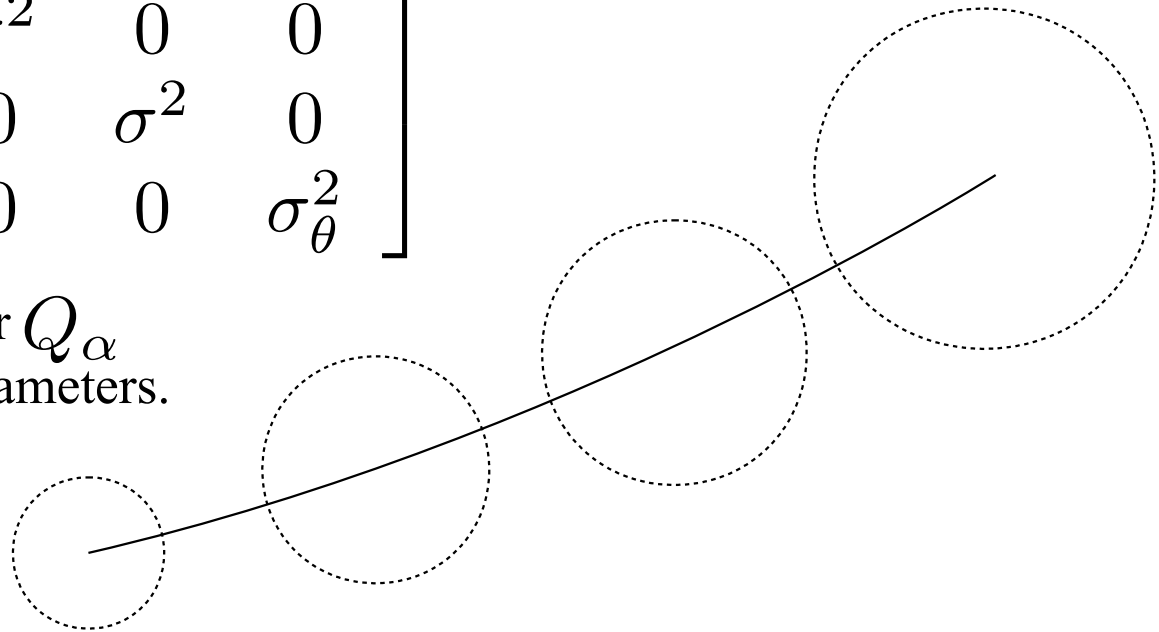
See paragraph 5.2 of the “book” form of the localization class material for the equations.

# Evolution of uncertainty (standard form of the equations)

$$P_{k+1} = A_k P_k A_k^T + Q_\alpha$$

$$Q_\alpha = \begin{bmatrix} \sigma^2 & 0 & 0 \\ 0 & \sigma^2 & 0 \\ 0 & 0 & \sigma_\theta^2 \end{bmatrix}$$

A logical for for  $Q_\alpha$   
Two tuning parameters.



Assuming the initial uncertainty is the same in x and y, the uncertainty ellipse

in the x-y plane starts as a circle and remains a circle during successive odometry phases (no update phase).

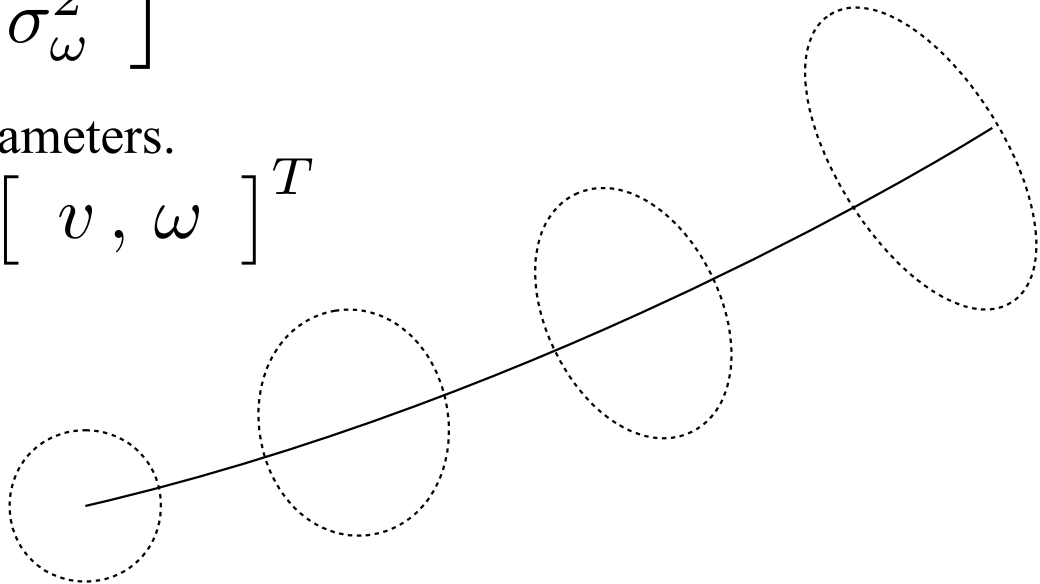
# Evolution of uncertainty (form with noisy input)

$$P_{k+1} = A_k P_k A_k^T + B_k Q_\beta B_k^T \quad (Q_\alpha \text{ has been set to zero})$$

$$Q_\beta = \begin{bmatrix} \sigma_v^2 & 0 \\ 0 & \sigma_\omega^2 \end{bmatrix}$$

Still two tuning parameters.

Remember:  $u = \begin{bmatrix} v, \omega \end{bmatrix}^T$



Now the uncertainty ellipse orients with the motion of the robot. The result is closer to the way errors actually evolve during odometry.



## The input noise in the lab

$$\begin{cases} v = (r_r \dot{q}_r + r_l \dot{q}_l) / 2 \\ \omega = (r_r \dot{q}_r - r_l \dot{q}_l) / e \end{cases}$$

There is a linear relation between  $v$ ,  $w$  and the rotation speed of the wheels.

So  $Q_\beta$  can be written as a function of the covariance matrix of errors on  $\dot{q}_r$  and  $\dot{q}_l$ .

$$Q_\beta = K Q_{\dot{q}} K^T \quad \text{with} \quad K = \begin{bmatrix} r_r/2 & r_l/2 \\ r_r/e & -r_l/e \end{bmatrix}$$

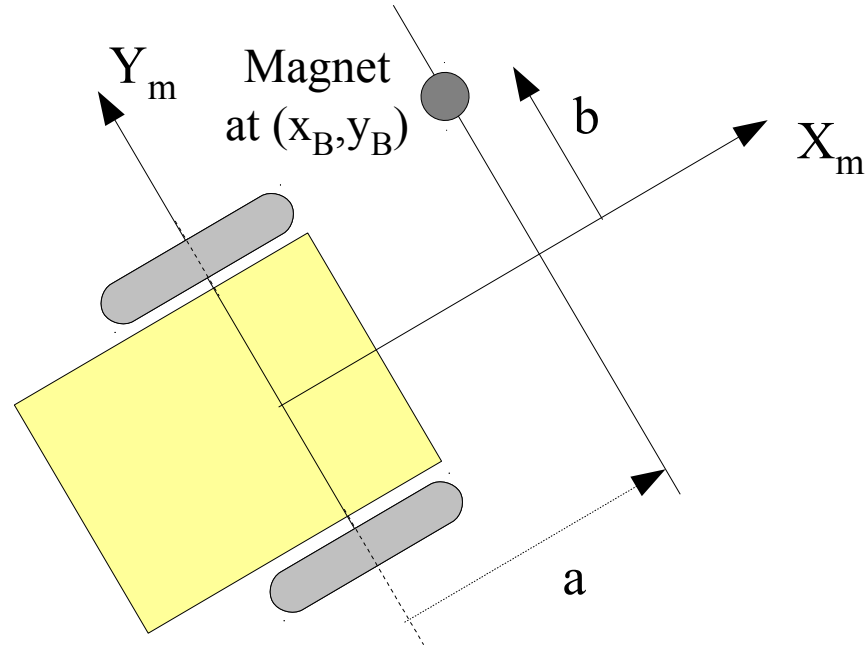
A reasonable form for  $Q_{\dot{q}}$ :

$$Q_{\dot{q}} = \begin{bmatrix} \sigma_{\dot{q}}^2 & 0 \\ 0 & \sigma_{\dot{q}}^2 \end{bmatrix}$$

Now the number of tuning parameters for the input noise is 1.

# Measurement equation

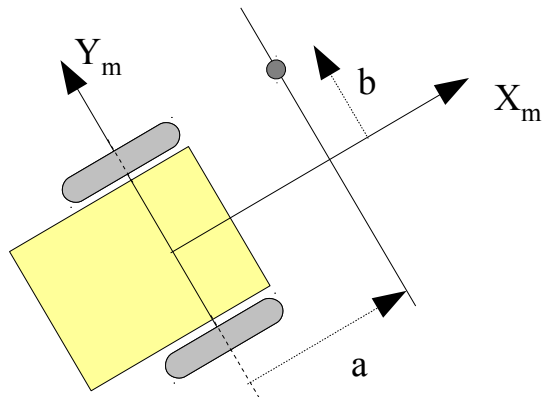
# The robot detecting a magnet



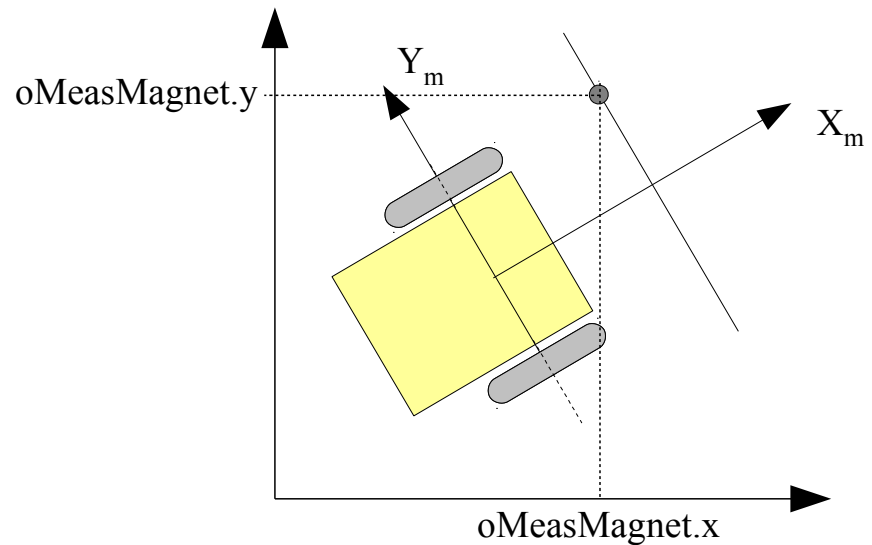
- Express in plain English what the sensor measures.
- Write the measurement equation

## Which magnet to use?

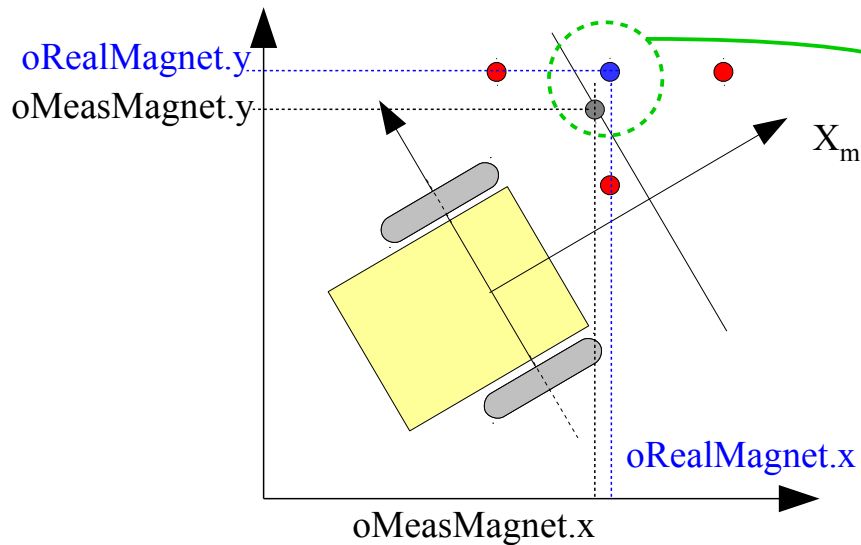
- Practical problem: the magnets are not signed beacons.
- The next slides explain how the problem is solved.
- It uses the same notations as in the program, so you can understand the code.
- Come back to these explanations if you need to.



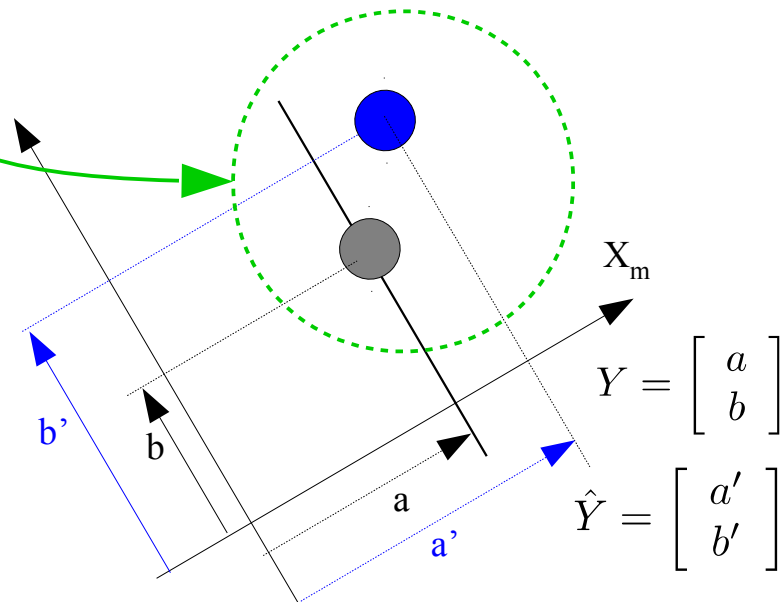
Step 1: measurement vector  $Y$



Step 2: oMeasMagnet: coordinates of the measurement point in absolute frame



Step 3: No magnet coordinates exactly match, but one of them is closest: it's the candidate magnet. The algorithm assumes it's the correct one, and it will fail if not.



Step 4: The expected measurement is the coordinates of the real magnet in the robot frame

# Project history

- Project initiator and principle of the system: G. Garcia
- Sensor prototype: J. Rousseau
- Characterization of the sensor and implementation of a sequential algorithm as described in the class:  
H. Chame & M. Gaudenzi de Faria.
- First Kalman filter implementation:  
F. Chichosz & M. Samuel.
- Version in this lab: G. Garcia

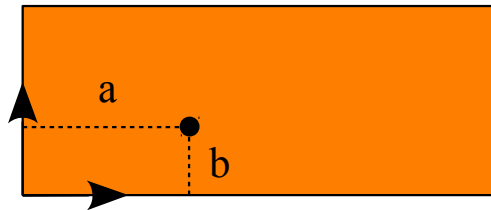
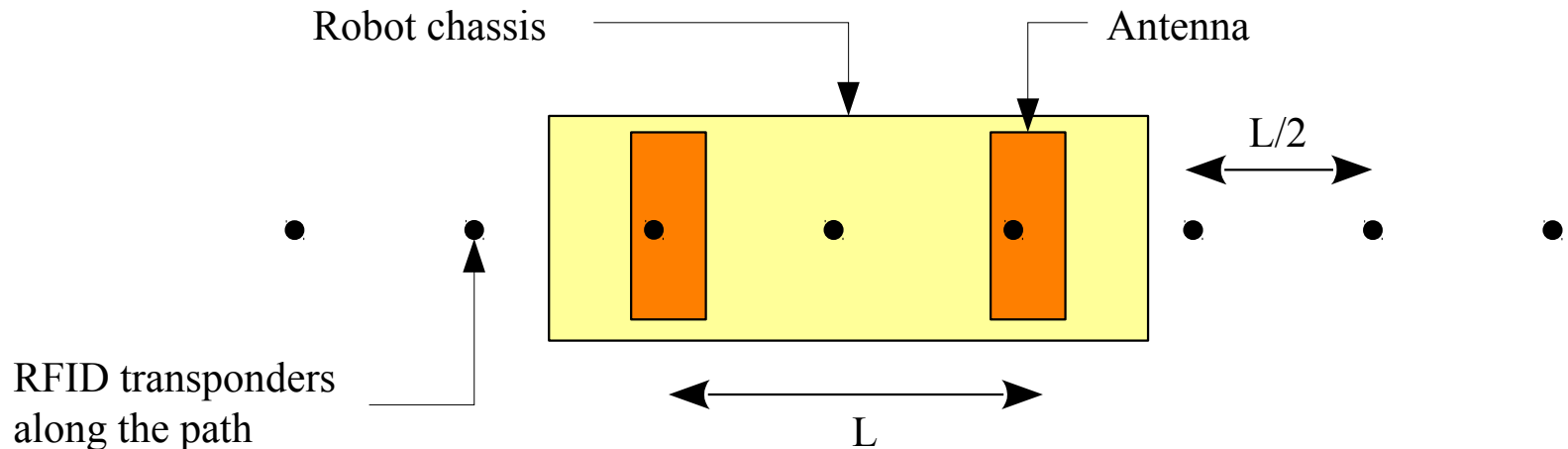
# Industrial example

# Container transport in ports





# RFID tags and antenna solution



The antenna measures the position of the RFID transponder in the antenna frame

From the positions of the transponders relative to the two antennas and the known positions of the antennas relative to the vehicle, and the positions of the transponders in the absolute reference frame, the position of the vehicle is calculated. Between two detections, odometry is used.

# Vehicle and antennas



# RFID tags and antenna solution

- The transponders are signed beacons. When the antenna passes over the transponder, it emits its position.
- The algorithm is very easy to implement.
- The locations of the transponders define the possible paths. It's not very flexible.
- Two different vehicles can use the same transponders if the distance between their antennas agree.
- The system is costly: 10 to 20 k€ per antenna. 30 to 50 € per transponder, including setup, which includes measurement of the transponder position by surveying and programming of the coordinates in the transponder memory.
- With the methods developed in this lab, you can dramatically enhance the flexibility and considerably reduce the cost of the solution. With the results of the VASCO project, we got rid of the whole system using SLAM.

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