

$$\frac{\pi}{2} = \sum_{k=0}^{\infty} \frac{2^k k!^2}{(2k+1)!}$$

$$\text{Let } D_m = \sum_{k=0}^m \frac{2^k k!^2}{(2k+1)!}$$

$$D_{m+1} = D_m + T_{m+1}$$

Where

$$T_k = \frac{2^k (k!)^2}{(2k+1)!}$$

1)  $T_{k+1}$  in terms of  $T_k$

$$\begin{aligned} T_{k+1} &= \frac{2^{k+1} (k+1)!^2}{(2k+3)!} \\ &= \frac{2 \cdot 2^k \cdot (k+1)^2 \cdot (k!)^2}{(2k+3) \cdot (2k+2) \cdot (2k+1)!} \\ &= \frac{2 \cdot (k+1)^2}{(2k+3) \cdot (2k+2)} \cdot T_k \\ &= \frac{k+1}{2k+3} \cdot T_k \end{aligned}$$

2) Optimizing FLOPS

$$\text{Let } x = k+1, y = 2k+3$$

for each iteration:

$$T_{k+1} = \frac{x}{y} \cdot T_k$$

$$x = x + 1$$

$$y = y + 2$$

$$S_{k+1} = S_k + T_{k+1}$$

5 FLOPS