$$S_{wh,i}^{\chi_\ell}$$
  $S_{wh,i*}^{\chi_\ell}$   $S_{i+1}^{\chi_\ell}$   $S_{i+1}^{\chi_\ell}$   $S_{i+1}^{\chi_\ell}$