$$egin{aligned} egin{aligned} igwedge b_j &= \top \ S_{out,i} & exec_{\chi_\ell}(au_i) + 1 \ igwedge b_j &= igwedge S_{i+1} \ igwedge b_j &= igwedge S_{i+1} \end{aligned}$$