$$S_i^{\chi_\ell}$$
  $b_i := op$   $S_{i+1}^{\chi_\ell}$   $S_i^{\chi_\ell}$   $S_i^{\chi_{\ell+1}}$