

# Data Privacy

## CMSC 463/663

L06 – k-anonymity,  $\ell$ -diversity, t-closeness



# Previously on...

- Access Control to represent user preferences
- Policies and mechanisms
- AC models:
  - DAC, MAC, RBAC, ABAC
- Challenges: scalability, inference problem, semantics...

**Google Is Hobbling Popular Ad Blocker uBlock Origin on Chrome**

Google is migrating Chrome browser extensions to a new specification that limits the functionality of ad blockers.

By Thomas Maxwell Published March 3, 2025 | Comments (16)



*In the news!*

BEST OF CES 2025 AWARDS

# The Need to Share Data

- For research purposes
  - E.g., social, medical, technological, etc.
- Mandated by laws and regulations
  - E.g., census
- For security/business decision making
  - E.g., network flow data for Internet-scale alert correlation
- For system testing before deployment
- ...
- **Publishing data may result in privacy violations**

# When Things go Wrong

AOL Search Data

## The Netflix Prize



dannypealed.com



- Anonymizing datasets (e.g., removing user identifiers) **does not preserve privacy!**
- De-anonymization attacks
  - E.g., use background knowledge (IMDB for Netflix prize)

*How to publish data to satisfy privacy while providing utility?*

# Classification of Attributes

- **Key attributes**
  - Name, address, phone number - uniquely identifying!
  - Always removed before release
- **Quasi-identifiers**
  - (5-digit ZIP code, birth date, gender) uniquely identify 87% of the population in the U.S.
  - Can be used for linking anonymized dataset with other datasets
- **Sensitive attributes**
  - Medical records, salaries, etc.
  - These attributes is what the researchers need, so they are always released directly

Key Attribute	Quasi-identifier			Sensitive attribute
Name	Age	Sex	Zipcode	Disease
Alice	29	Female	47677	Ovarian Cancer
Beth	22	Female	47602	Ovarian Cancer
Andre	27	Male	47678	Prostate Cancer
Dan	43	Male	47905	Heart Disease
Ellen	52	Female	47909	Heart Disease
Eric	47	Male	47906	Heart Disease

# *k*-Anonymity: Intuition

- Each **record is indistinguishable from at least  $k-1$  other records** when only quasi-identifiers are considered
  - *Example: you try to identify a man in the released table, but the only information you have is his birth date and gender. There are  $k$  men in the table with the same birth date and gender.*
- The  $k$  records form an **equivalence class**



# Achieving $k$ -Anonymity

- Main methods:
  - **Generalization**: Replace with less-specific values
  - **Suppression**: Remove outliers
- Many other methods in the literature...

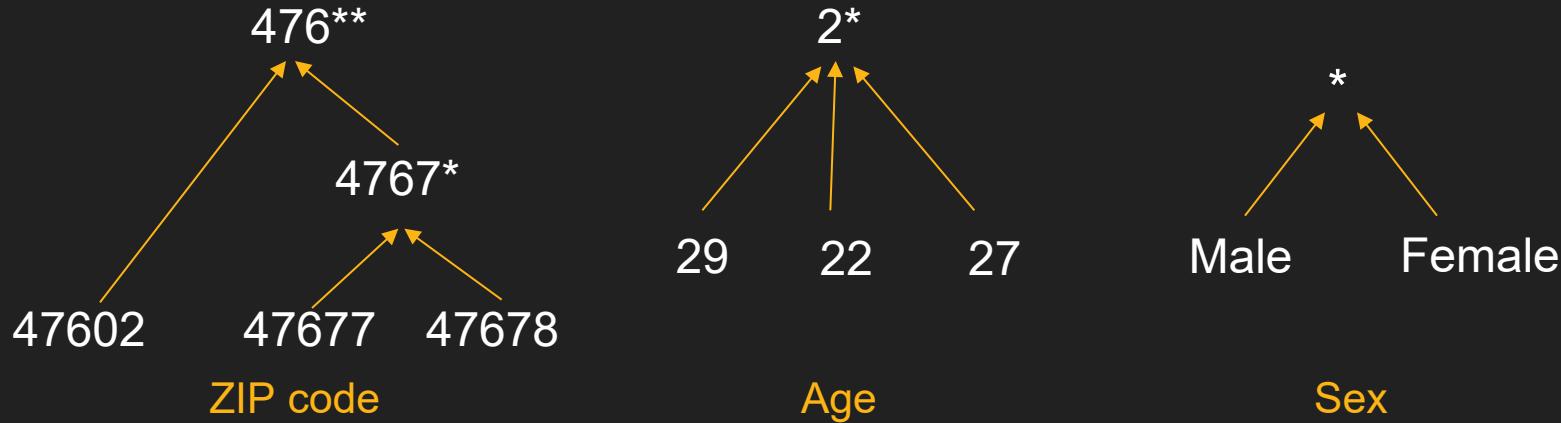
**Generalization**

Age	Sex	Zipcode	Disease
2*	*	476**	Ovarian Cancer
2*	*	476**	Ovarian Cancer
2*	*	476**	Prostate Cancer
[43,52]	*	4790*	Heart Disease
[43,52]	*	4790*	Heart Disease
[43,52]	*	4790*	Heart Disease

**Suppression (cell-level)**

# Generalization Hierarchies

- **Generalization Hierarchies:** Data owner defines how values can be generalized
- **Table Generalization:** A table generalization is created by generalizing all values in a column to a specific level of generalization



# *k*-Minimal Generalizations

- There are many *k*-anonymizations – which one to pick?
  - Intuition: The one that does not generalize the data more than needed (decrease in utility of the published dataset!)
- **K-minimal generalization:** A *k*-anonymized table that is not a generalization of another *k*-anonymized table

Race	ZIP
E <sub>0</sub>	Z <sub>0</sub>
Black	02138
Black	02139
Black	02141
Black	02142
White	02138
White	02139
White	02141
White	02142

**PT**

Race	ZIP
E <sub>1</sub>	Z <sub>0</sub>
Person	02138
Person	02139
Person	02141
Person	02142
Person	02138
Person	02139
Person	02141
Person	02142

**GT<sub>[1,0]</sub>**

Race	ZIP
E <sub>1</sub>	Z <sub>1</sub>
Person	0213*
Person	0213*
Person	0214*
Person	0214*
Person	0213*
Person	0213*
Person	0214*
Person	0214*

**GT<sub>[1,1]</sub>**

Race	ZIP
E <sub>0</sub>	Z <sub>2</sub>
Black	021**
White	021**
White	021**
White	021**

**GT<sub>[0,2]</sub>**

Race	ZIP
E <sub>0</sub>	Z <sub>1</sub>
Black	0213*
Black	0213*
Black	0214*
Black	0214*
White	0213*
White	0213*
White	0214*
White	0214*

**GT<sub>[0,1]</sub>**

Figure 4 Examples of generalized tables for PT

#	Zip	Age	Nationality	Condition
1	13053	< 40	*	Heart Disease
2	13053	< 40	*	Viral Infection
3	13067	< 40	*	Heart Disease
4	13067	< 40	*	Cancer

2-minimal  
Generalizations

#	Zip	Age	Nationality	Condition
1	130**	< 30	American	Heart Disease
2	130**	< 30	American	Viral Infection
3	130**	3*	Asian	Heart Disease
4	130**	3*	Asian	Cancer

#	Zip	Age	Nationality	Condition
1	130**	< 40	*	Heart Disease
2	130**	< 40	*	Viral Infection
3	130**	< 40	*	Heart Disease
4	130**	< 40	*	Cancer

NOT a  
2-minimal  
Generalization

# Example $k$ -anonymization

Age	Sex	Zipcode	Disease
2*	*	476**	Ovarian Cancer
2*	*	476**	Ovarian Cancer
2*	*	476**	Prostate Cancer
[43,52]	*	4790*	Heart Disease
[43,52]	*	4790*	Heart Disease
[43,52]	*	4790*	Heart Disease

- **3-Anonymous** table

**Problems?**

- The adversary knows Alice's QI values (47677, 29, F)
- The adversary does not know which one of the first 3 records corresponds to Alice

# Attacks on $k$ -Anonymity

- $k$ -anonymity does not provide privacy if:
  - Sensitive values **lack diversity**
  - The attacker has **background knowledge**

## Background Knowledge Attack

Andre → sex at birth was male

<Andre, 27>



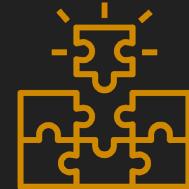
Age	Sex	Zipcode	Disease
2*	*	476**	Ovarian Cancer
2*	*	476**	Ovarian Cancer
2*	*	476**	Prostate Cancer
[43,52]	*	4790*	Heart Disease
[43,52]	*	4790*	Heart Disease
[43,52]	*	4790*	Heart Disease

## Homogeneity Attack

<Ellen, 52, 47909>

# Other Attacks

- **Complementary Release Attack**
  - Different releases of the same private table can be linked together to compromise k-anonymity
- **Unsorted Matching Attack**
  - Records appear in the same order in the released table as in the original table
- ...



# Group Activity

- Releasing  $k$ -anonymous reviews for professors by students

Name	Age	Nationality	Class	Level	Grade	Prof.	Review
Alice	21	U.S. citizen	CMSC331	Junior	B	Smith	4
Beth	20	U.S. citizen	CMSC334	Junior	F	Miller	1
Andre	22	U.S. citizen	CMSC331	Senior	A	Smith	2
Dan	21	U.S. citizen	CMSC491	Senior	C	Anderson	4
Ellen	20	U.S. citizen	CMSC203	Sophomore	F	Miller	5
Eric	19	U.S. citizen	CMSC101	Sophomore	A	Williams	4

*Privacy?*

*Utility?*

# $\ell$ -Diversity

- Recall →  $k$ -anonymity,  $k$  records form an **equivalence class**
- $\ell$ -diversity is a stronger definition of privacy
- Principle
  - Each equivalence class contains at least  $\ell$  **well-represented** sensitive values
- Instantiations
  - Distinct  $\ell$ -diversity
    - Each equivalence class contains distinct  $\ell$  sensitive values
    - ...

	Zip	Age	Nationality	Condition
1	130**	< 30	*	Heart Disease
2	130**	< 30	*	Heart Disease
3	130**	< 30	*	Viral Infection
4	130**	< 30	*	Viral Infection
5	1485*	$\geq 40$	*	Cancer
6	1485*	$\geq 40$	*	Heart Disease
7	1485*	$\geq 40$	*	Viral Infection
8	1485*	$\geq 40$	*	Viral Infection
9	130**	3*	*	Cancer
10	130**	3*	*	Cancer
11	130**	3*	*	Cancer
12	130**	3*	*	Cancer

4-anonymous table

	Zip	Age	Nationality	Condition
1	1305*	$\leq 40$	*	Heart Disease
4	1305*	$\leq 40$	*	Viral Infection
9	1305*	$\leq 40$	*	Cancer
10	1305*	$\leq 40$	*	Cancer
5	1485*	$> 40$	*	Cancer
6	1485*	$> 40$	*	Heart Disease
7	1485*	$> 40$	*	Viral Infection
8	1485*	$> 40$	*	Viral Infection
2	1306*	$\leq 40$	*	Heart Disease
3	1306*	$\leq 40$	*	Viral Infection
11	1306*	$\leq 40$	*	Cancer
12	1306*	$\leq 40$	*	Cancer

4-anonymous and 3-diverse table

What's Bob's (31yo/American/13053) disease?

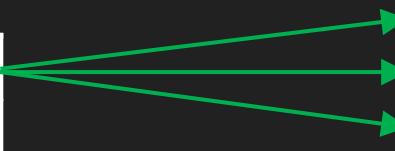
What's Umeko's (21yo/Japanese/13068) disease?  
 \*BK: Japanese are less prone to heart disease

# Limitations of $\ell$ -Diversity

## Similarity attack



Bob	
<b>Zip</b>	<b>Age</b>
47678	27



Zip	Age	Salary	Condition
476**	2*	20K	Gastric Ulcer
476**	2*	30K	Gastritis
476**	2*	40K	Stomach Cancer
4790*	≥40	50K	Gastritis
4790*	≥40	100K	Flu
4790*	≥40	70K	Bronchitis
476**	3*	60K	Bronchitis
476**	3*	80K	Pneumonia
476**	3*	90K	Stomach Cancer
476**	2*	20K	Gastric Ulcer
476**	2*	30K	Gastritis
476**	2*	40K	Stomach Cancer

## Conclusion

1. Bob's salary is in [20k,40k], which is relatively low
2. **Bob has some stomach-related disease**

**$\ell$ -diversity does not consider semantics of sensitive values!**

# Limitations of $\ell$ -Diversity

- Skewness Attack
- Example: sensitive attribute is HIV+ (1%) or HIV- (99%)



- *Before  $\ell$ -diversity:*

probability of Bob being HIV+ = 1%

Bob	
<b>Zip</b>	<b>Age</b>
47678	27

- *After 2-diverse table*

probability of Bob being HIV+ = 50%!

	Zip	Age	Condition
1	476**	< 30	HIV+
2	476**	< 30	HIV+
3	476**	< 30	HIV-
4	476**	< 30	HIV-

2-diverse table

**$\ell$ -diversity does not consider overall distribution of sensitive values!**

# *t*-Closeness

- Principle:
  - Distribution of sensitive attribute value in each equi-class should be “close” to that of the overall dataset (distance  $\leq t$ )

*Can we always do this?*

*How would it affect utility?*

Race	Zip	Condition	
Caucas	787XX	Flu	
Caucas	787XX	Shingles	
Caucas	787XX	Acne	
Caucas	787XX	Flu	
Caucas	787XX	Acne	
Caucas	787XX	Flu	
Asian/AfrAm	78XXX	Flu	
Asian/AfrAm	78XXX	Flu	
Asian/AfrAm	78XXX	Acne	
Asian/AfrAm	78XXX	Shingles	
Asian/AfrAm	78XXX	Acne	
Asian/AfrAm	78XXX	Flu	

# Combining Everything

Race	Zip	HIV status	Condition
Caucas	787XX	HIV+	Flu
Asian/AfrAm	787XX	HIV-	Flu
Asian/AfrAm	787XX	HIV+	Shingles
Caucas	787XX	HIV-	Acne
Caucas	787XX	HIV-	Shingles
Caucas	787XX	HIV-	Acne



*Bob is Caucasian and I've heard he was admitted to a hospital with flu...*

***This goes against the rules!  
“flu” is not a quasi-identifier***

Imagine a table which is:

- k-anonymous,
- l-diverse,
- and t-close table

***Perfect privacy?***

***Yes... and this is yet another problem with k-anonymity***

# $k$ -Anonymity $\neq$ Privacy

- **Syntactic**
  - Focuses on data transformation, not on what can be learned from the anonymized dataset
  - “ **$k$ -anonymous**” dataset can leak sensitive information  
**Background knowledge exists!**
- **“Quasi-identifier” fallacy**
  - Assumes a priori that attacker will not know certain information about his target
- **Relies on locality**
  - Destroys utility of many real-world datasets