$MATH\ 221$

For full credit please explain all of your answers. No calculators are allowed.

Problem 1. Let f(x) = 5x - 6.

- (a) Find $L = \lim_{x\to 1} f(x)$ without proving it.
- (b) Find a number $\delta > 0$ such that for all x with $0 < |x 1| < \delta$ we have |f(x) L| < 1.

Problem 2. Let

$$f(x) = \begin{cases} 2x & x \ge 0\\ x^2 - 2 & x < 0 \end{cases}$$

Find $\lim_{x\to 0^+} f(x)$ and $\lim_{x\to 0^-} f(x)$. Does $\lim_{x\to 0} f(x)$ exist, why or why not?