# Chapter 25: Electric Charges and Forces

Coulomb's Law:  $\overrightarrow{F} = \frac{|q_1||q_2|}{4\pi\epsilon_0 r^2} \hat{r}$ 

Superposition:  $\overrightarrow{F}_{Total} = \overrightarrow{F}_{12} + \overrightarrow{F}_{13} + \dots$ 

Force on charge in an E-Field:  $\overrightarrow{F}_{\text{ong}} = q\overrightarrow{E}$ 

E-Field at (x,y,z):  $\vec{E}(x,y,z) = \frac{\vec{F}_{onq} at(x,y,z)}{a}$ 

E-Field - point charge:  $\overrightarrow{E} = \frac{q}{4\pi\epsilon_0 r^2} \hat{r}$ 

# Chapter 26: The Electric Field

Electric dipole moment:  $\vec{p} = q\vec{d}$ 

E-Field - Electric dipole (on axis):  $\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{2\vec{p}}{r^3}$ 

E-Field - Electric dipole (bisecting plane):  $\vec{E} = -\frac{1}{4\pi\epsilon_0} \frac{\vec{p}}{r^3}$ 

Linear charge density:  $\lambda = \frac{Q}{L}$ 

Surface charge density:  $\eta = \frac{Q}{4}$ 

E-Field - charged ring (on axis):  $\vec{E}_{ring} = \frac{zQ}{4\pi\epsilon_0(z^2+R^2)^{3/2}}$ 

E-Field - above a plane of charge:  $\frac{\overrightarrow{L}}{E} = \frac{\eta}{2\epsilon_0}$ 

E-Field - below a plane of charge:  $\overrightarrow{E} = \frac{-\eta}{2\epsilon_0}$ 

E-Field - Outside a Sphere of charge:  $\overrightarrow{E}_{sphere} = \frac{|Q|}{4\pi\epsilon_0 r^2} \hat{r}$ 

E-Field - Capacitor (+ to -):  $\vec{E}_{capacitor} = \frac{\eta}{\epsilon_0}$ 

Motion in a uniform field:  $\vec{a} = \frac{q\vec{E}}{m}$ 

Torque on a dipole:  $\vec{\tau} = \vec{p} \times \vec{E}$ 

# Prefixes $\mu$ nano n

 $10^{-15}$  femto f

pico

## Constants

 $10^{-6}$ 

 $10^{-9}$ 

 $10^{-12}$ 

$$\epsilon_0 = 8.854 \times 10^{-12} \ \frac{\mathrm{C}^2}{\mathrm{Nm}^2}$$

$$e = 1.6 \times 10^{-19} \text{ C}$$

$$m_e = 9.109 \times 10^{-31} \text{ kg}$$

$$k = \frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2}$$

$$m_p = 1.673 \times 10^{-27} kg$$

## Units

Force:  $1 N = 1 kg \frac{m}{s^2}$ 

Energy (Joules): 1 J = 1 Nm

Energy (eV)  $1 eV = 1.6 \times 10^{-19} J$ 

Electric Field:  $1 \frac{N}{C} = 1 \frac{V}{m}$ 

Electric Potential  $1 V = 1 \frac{J}{C}$ 

Charge: 1 C = (1 A)(1 s)

Current:  $1 A = 1 \frac{C}{a}$ 

# Chapter 26: Gauss's Law

Electric Flux (constant E-field):  $\Phi_E = \overrightarrow{E} \cdot \overrightarrow{A}$ 

Electric Flux:  $\Phi_E = \int \vec{E} \cdot d\vec{A}$ 

Gauss's Law:  $\epsilon_0 \Phi_E = q_{enc}$ 

Gauss's Law:  $\epsilon_0 \oint \vec{E} \cdot d\vec{A} = q_{enc}$ 

# Chapter 28: The Electric Potential

Work from a constant force:  $W = \overrightarrow{F} \cdot \Delta \overrightarrow{r}$ 

Potential Energy and work:  $\Delta U = -W$ 

Work (general) :  $W = \int_{i}^{f} \overrightarrow{F} \cdot d\overrightarrow{s}$ 

Pot. Energy - uniform E-field:  $U_{elec} = U_0 + qEs$ 

Pot. Energy - 2 point charges:  $U_{elec} = k \frac{q_1 q_2}{r}$ 

Pot. Energy - Multiple point charges:  $U_{elec} = \sum_{i < j} k \frac{q_i q_j}{r}$ 

Potential Energy - dipole:  $U = -\vec{p} \cdot \vec{E}$ 

Potential Difference:  $\Delta V = V_f - V_i$ 

 $\Delta V = \frac{\Delta U}{q}$ 

 $\Delta V = -\frac{W}{q}$ 

Potential - capacitor: V = Es

Potential - point charge:  $V = \frac{q}{4\pi\epsilon_0 r}$ 

Potential - many point charges:  $V = \sum_i \frac{q_i}{4\pi\epsilon_0 r_i}$ 

Potential - dipole:  $V = \frac{p cos \theta}{4 \pi \epsilon_0 r^2}$ 

Potential - charge distr:  $V = \frac{1}{4\pi\epsilon_0} \int \frac{dq}{r}$ 

Potential - ring of charge (on axis):  $V_{ring} = \frac{1}{4\pi\epsilon_0} \frac{Q}{\sqrt{R^2 + z^2}}$ 

Potential - charged disk (on axis):  $V_{disk} = \frac{Q}{2\pi\epsilon_0 R^2} (\sqrt{z^2 + R^2} - z)$