

Visualizing Data: NCAA Big East Football

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Spectral Rankability

Algorithm 1 Spectral Rankability of Graph Data Γ .

function $[r] = \text{specR}(\Gamma)$:

$n \leftarrow$ the number of vertices in Γ

$d \leftarrow$ the out-degree of the vertices in Γ

$L \leftarrow$ graph Laplacian of Γ

$e \leftarrow$ eigenvalues of L

$s = \{n - 1, n - 2, \dots, 0\}$

$r = \frac{\mathcal{H}(d,s) + \mathcal{H}(e,s)}{2(n-1)}$, where \mathcal{H} denotes the Hausdorff distance

return

Connectivity Rankability

Algorithm 2 Connectivity Rankability of Graph Data Γ .

function $[r] = \text{connR}(\Gamma)$:

$n \leftarrow$ the number of vertices in Γ

$L \leftarrow$ graph Laplacian of Γ

$\alpha = \min_{x \in S} x^T L x$, where $S = \{x \in \mathbb{R}^n : x \perp e, \|x\| = 1\}$

$\beta = \max_{x \in S} x^T L x$, where $S = \{x \in \mathbb{R}^n : x \perp e, \|x\| = 1\}$

$\tilde{\alpha} \leftarrow$ related quantity for perfect dominance graph

$\tilde{\beta} \leftarrow$ related quantity for perfect dominance graph

$r = \frac{|\alpha - \tilde{\alpha}| + |\beta - \tilde{\beta}|}{2n}$

return

Snapshot of Results

| Year | specR | connR | Year | specR | connR |
|------|-------|-------|------|-------|-------|
| 1995 | 0.143 | 0.043 | 2004 | 0.339 | 0.168 |
| 1996 | 0.143 | 0.043 | 2005 | 0.162 | 0.013 |
| 1997 | 0.185 | 0.069 | 2006 | 0.195 | 0.100 |
| 1998 | 0.183 | 0.062 | 2007 | 0.316 | 0.169 |
| 1999 | 0.143 | 0.058 | 2008 | 0.195 | 0.099 |
| 2000 | 0.143 | 0.002 | 2009 | 0.143 | 0.049 |
| 2001 | 0.143 | 0.001 | 2010 | 0.292 | 0.166 |
| 2002 | 0.143 | 0.005 | 2011 | 0.286 | 0.149 |
| 2003 | 0.143 | 0.049 | 2012 | 0.286 | 0.163 |

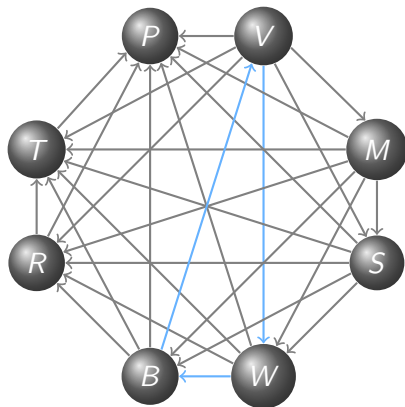


Most Rankable



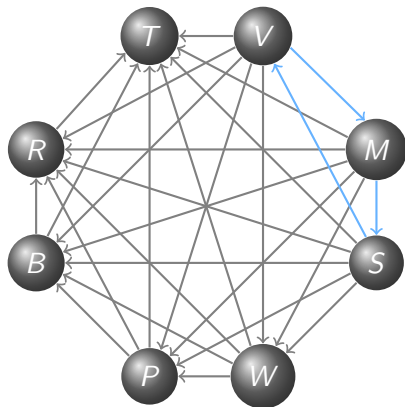
Least Rankable

Year 1995



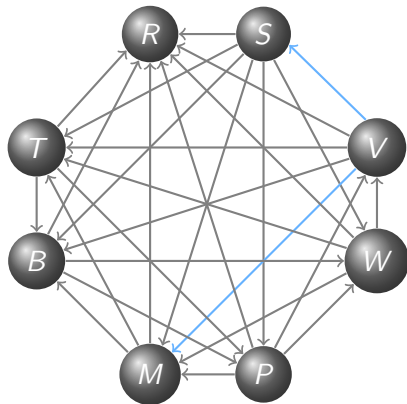
Cycle of length 3

Year 1996



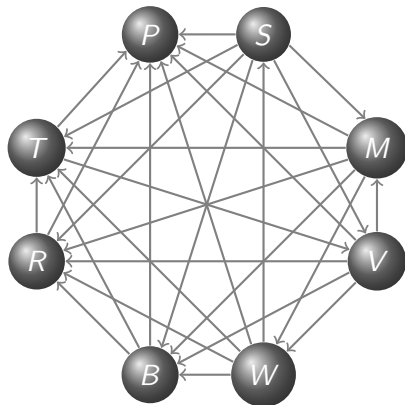
Cycle of length 3

Year 1997



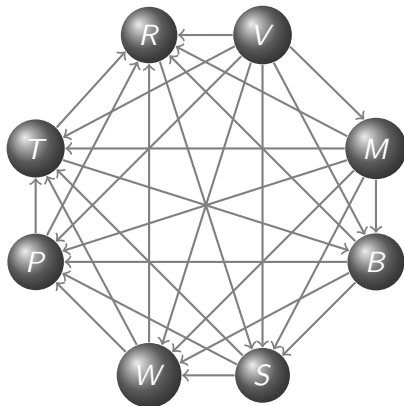
Cycle of length 3

Year 1998



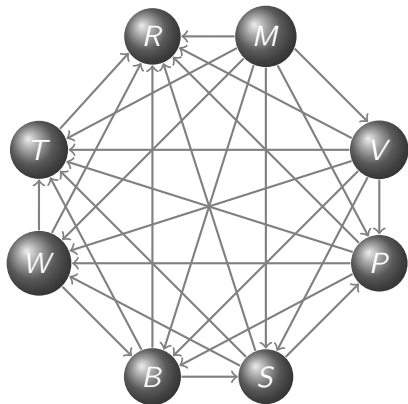
Cycle of length 3

Year 1999



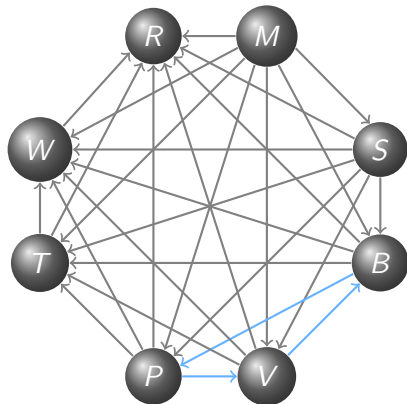
Cycle of length 3

Year 2000



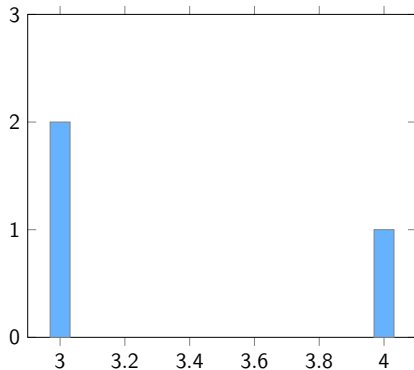
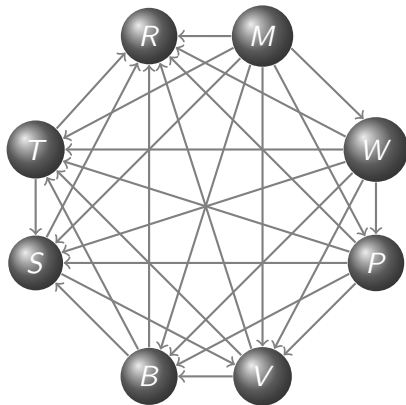
Cycle of length 3

Year 2001

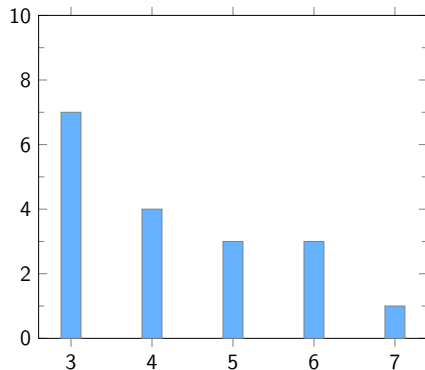
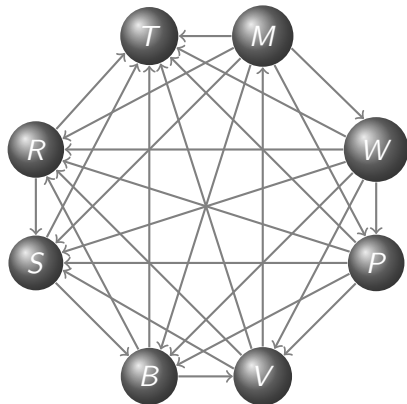


Cycle of length 3

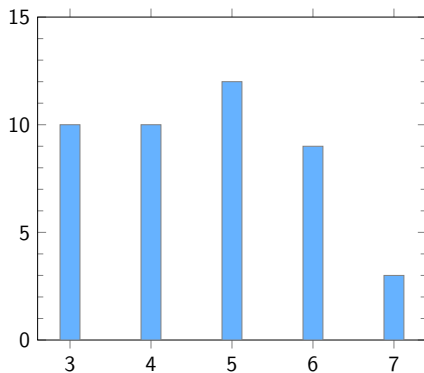
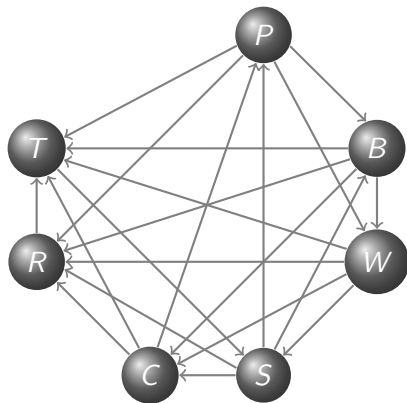
Year 2002



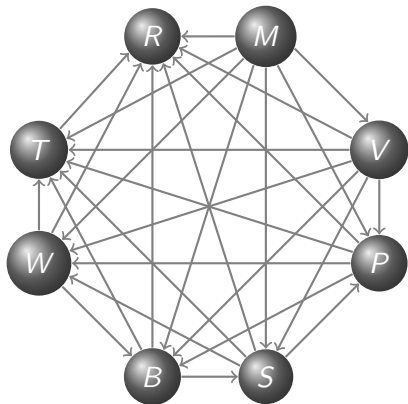
Year 2003



Year 2004

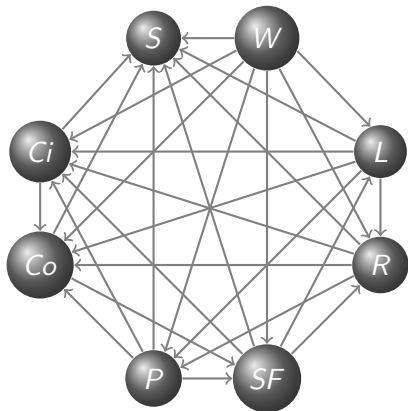


Year 2000

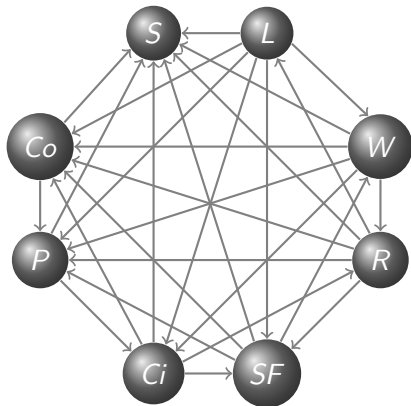


Cycle of length 3

Year 2005



Year 2006



Year 2007

