

ENCYCLOPEDIA OF MATHEMATICS AND ITS APPLICATIONS

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Volume 39

## Combinatorial Matrix Theory

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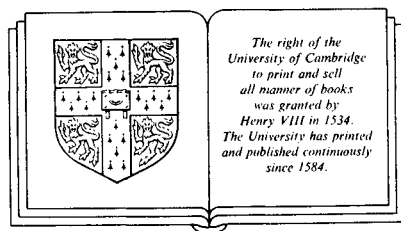
# *Combinatorial Matrix Theory*

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CAMBRIDGE UNIVERSITY PRESS

*Cambridge*

*New York Port Chester Melbourne Sydney*

Published by the Press Syndicate of the University of Cambridge  
The Pitt Building, Trumpington Street, Cambridge CB2 1RP  
40 West 20th Street, New York, NY 10011, USA  
10 Stamford Road, Oakleigh, Melbourne 3166, Australia

© Cambridge University Press 1991

First published 1991

*Library of Congress Cataloging-in-Publication Data*

Brualdi, Richard A.

Combinatorial matrix theory / Richard A. Brualdi, Herbert J. Ryser

p. cm. – (Encyclopedia of mathematics and its applications ; 39.)

Includes bibliographical references and index.

ISBN 0-521-32265-0

1. Matrices. 2. Combinatorial analysis. I. Ryser, Herbert John.

II. Title. III. Series.

QA188.B78 1991

512.9'434 – dc20

90-20210

CIP

*British Library Cataloguing in Publication Data*

Brualdi, Richard A.

Combinatorial matrix theory.

1. Algebra. Matrices

I. Title II. Ryser, Herbert J. III. Series

512.9434

ISBN 0-521-32265-0

Transferred to digital printing 2003