## Linear programming

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## Part I

**Zad. 1.** Manufacturer produces two goods  $W_I$  i  $W_{II}$ , profit from selling them is respectively 4 and 1. There are three resources used in the production process  $S_1$ ,  $S_2$  and  $S_3$ , reserves are respectively 12, 6 and 1. For production of  $W_I$  2 units of  $S_1$  are required, 3 units of  $S_2$  and 1 of  $S_3$ . Resource  $S_3$  is a waste in production process of good  $W_{II}$  (2 units pre product), additionally unit of  $W_{II}$  needs 3 units of  $S_1$  and one unit of  $S_2$ . Manufacturer is obliged to give away to its contractor 3 units of  $S_3$  at the end of production process. Construct linear programming model. How to maximize profit?

**Zad. 2.** Two distinct goods  $G_1$  and  $G_2$  are produced. Production process needs three resources consumption, limits and profits are given in the table.

Resource	$G_1$	$G_2$	Limits
$R_1$	1	1	7
$R_2$	4	10	40
$R_3$	0	1	3
Profit	1	4	

Determine the optimal solution assuming that products are indivisible.

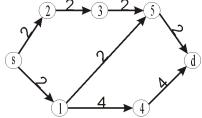
**Zad. 3.** There are four machines and three employees. Each machine can be operated by each worker, the costs are given in the table. Using Hungarian algorithm find the minimal matching, if we allow that one machine wont be operated.

	Machines				
Worker	$M_1$	$M_2$	$M_3$	$M_4$	
$W_1$	5	1	6	4	
$W_2$	4	8	5	3	
$W_3$	7	2	5	6	

Zad. 4. There are five workers and four tasks each cost of executing each task by each worker is given in the table. Using Hungarian algorithm find the minimal assignment.

	$W_1$	$W_2$	$W_3$	$W_4$	$W_5$		
$T_1$	12	3	4	3	7		
$T_2$	7	4	6	5	21		
$T_3$	4	1	2	12	5		
$T_4$	6	7	5	4	3		

**Zad. 5.** Determine the maximal flow. 2 3 3 5



Determine the maximal flow.

