

# MA-236: Homework 11

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I pledge my honor that I have abided by the Stevens Honor System.

"Prove that  $ss0$  is not equal to  $sss0$  in Robinson arithmetic."

Pruned Tree where  $Q_1 \dots Q_7$  are the axioms of Robinson's arithmetic:

1.  $ss0 = sss0 \quad \neg\text{Conclusion}$   
|
2.  $0 \neq s0 \quad Q_2$   
|
3.  $s0 \neq ss0 \quad Q_{1,2}$   
|
4.  $ss0 \neq sss0 \quad Q_{1,3}$   
×

Since the pruned refutation tree closes, the sentences are **inconsistent**. Therefore, the argument is **valid**.