MA-236: Homework 8

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I pledge my honor that I have abided by the Stevens Honor System.

Use the tree test to check if the following set of three sentences is consistent. If yes, find an interpretation in which the sentences are all true.

$$Fa \qquad \forall x(\neg Fx \to Gx) \qquad \forall xGx$$

$$1. \qquad Fa \quad \text{Input}$$

$$2. \quad \forall x(\neg Fx \to Gx) \quad \text{Input}$$

$$3. \qquad \forall xGx \quad \text{Input}$$

$$4. \qquad Ga \quad 3. \forall$$

$$5. \qquad \neg Fa \to Ga \quad 2. \forall$$

$$6. \qquad Fa \quad 5. \to Ga \quad 5. \to$$

Since the tree is open, the sentences are **consistent**.

Interpretation

Domain:
$$\{p_1\}$$
 $Fa \Rightarrow \text{true}$ $a \text{ names } p_1$ $\forall x (\neg Fx \to Gx) \Rightarrow \neg Fa \to Ga \Rightarrow \text{true}$ $Fa = \text{true}$ $Ga = \text{true}$ $\forall x Gx \Rightarrow Ga \Rightarrow \text{true}$