MA-236: Homework 2

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I pledge my honor that I have abided by the Stevens Honor System.

1.18 Problems

(3) Show that the following argument is valid:

$$A \vee B, A \rightarrow C, B \rightarrow C, \text{ so } C$$

To compute this efficiently, we find try to find a counter example such that all the premises are true and the conclusion is false. We can cut the table down to premises we know that can possibly produce counter examples:

A	B	C	$A \lor B$	$A \to C$	$B \to C$	$\mid C \mid$
t	t	f	t	f	f	f
\mathbf{t}	\mathbf{f}	f	t	f	\mathbf{t}	f
f	\mathbf{t}	\mathbf{f}	t	\mathbf{t}	\mathbf{f}	f
f	\mathbf{f}	f	f	\mathbf{t}	\mathbf{t}	f

Full computation:

A	B	C	$A \lor B$	$A \to C$	$B \to C$	C
t	\mathbf{t}	t	t	t	t	t
\mathbf{t}	\mathbf{t}	f	t	\mathbf{f}	f	f
\mathbf{t}	f	\mathbf{t}	t	\mathbf{t}	\mathbf{t}	t
\mathbf{t}	\mathbf{f}	\mathbf{f}	t	\mathbf{f}	\mathbf{t}	f
f	\mathbf{t}	\mathbf{t}	t	\mathbf{t}	\mathbf{t}	t
f	\mathbf{t}	\mathbf{f}	t	\mathbf{t}	f	f
\mathbf{f}	f	\mathbf{t}	f	\mathbf{t}	\mathbf{t}	t
\mathbf{f}	f	f	f	\mathbf{t}	\mathbf{t}	f

Since we cannot find a counter example, the argument is valid.