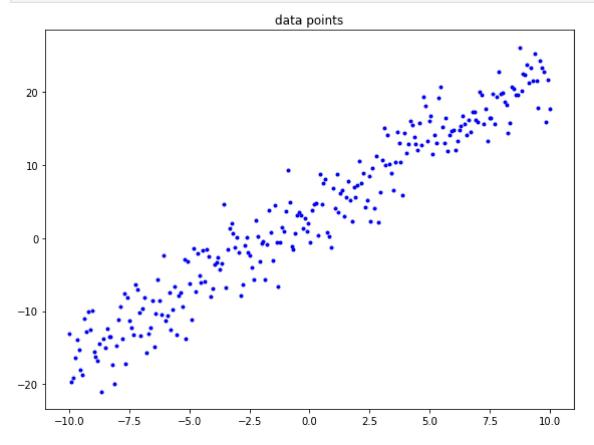
# Linear regression

## import library

```
In [ ]: import numpy as np
   import matplotlib.image as img
   import matplotlib.pyplot as plt
   import matplotlib.colors as colors
   from mpl_toolkits.mplot3d import Axes3D
```

### load data points

•  $\{(x_i, y_i)\}_{i=1}^n$ 



#### compute the residual

# compute the loss

• useful functions: np.inner

# compute the gradient with respect to $\theta_0$

• useful functions: np.inner

# compute the gradient with respect to $heta_1$

• useful functions: np.inner

#### gradient descent for the optimization

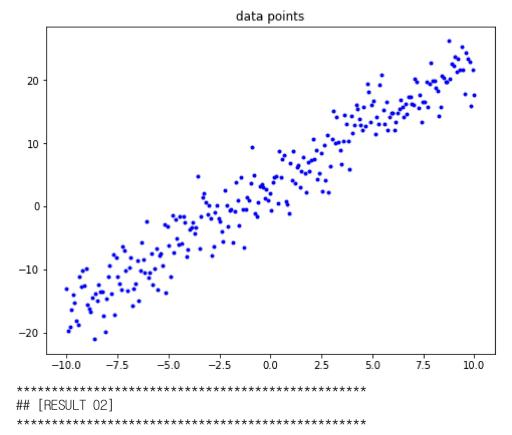
```
number iteration = 500
In [ ]:
       learning_rate
                      = 0.01
                       = 0
       theta0
       theta1
       list_theta0
                      = np.zeros(number_iteration)
       list_theta1
                      = np.zeros(number_iteration)
       list_loss
                      = np.zeros(number_iteration)
       for i in range(number_iteration):
          # complete the blanks
          theta0 = theta0 - learning_rate * compute_gradient_theta0(x, y, theta0, theta1)
          theta1 = theta1 - learning_rate * compute_gradient_theta1(x, y, theta0, theta1)
               = compute_loss(x, y, theta0, theta1)
          list\_theta0[i] = theta0
          list_theta1[i] = theta1
          list_loss[i] = loss
```

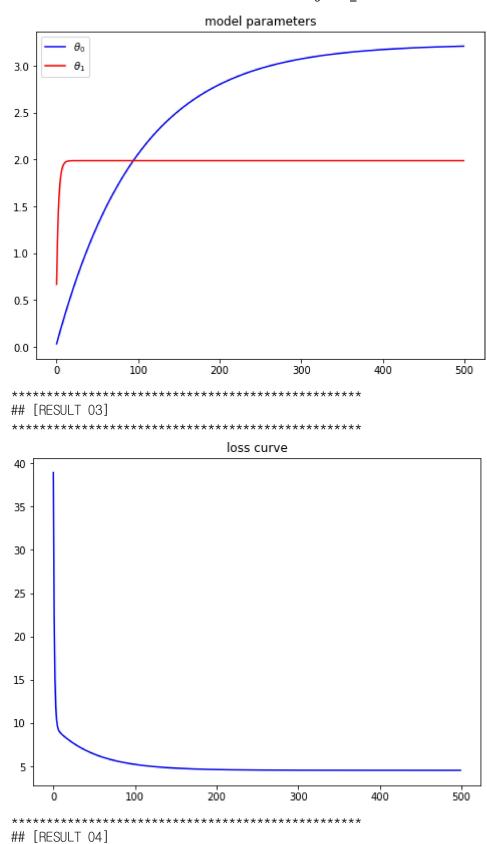
# functions for presenting the results

```
In [ ]: def function_result_01():
            plt.figure(figsize=(8,6))
            plt.plot(x, y, '.', color='blue')
            plt.title('data points')
            plt.show()
In [ ]: def function_result_02():
            plt.figure(figsize=(8,6))
            ax = plt.gca()
            plt.title('model parameters')
            ax.legend()
            plt.show()
In [ ]: def function_result_03():
            plt.figure(figsize=(8,6))
            plt.plot(list_loss, '-', color='blue')
            plt.title('loss curve')
            plt.show()
In [ ]: def function_result_04():
            f = theta0 + theta1 * x
            plt.figure(figsize=(8.6))
            ax = plt.gca()
            plt.plot(x, y, '.', color='blue', label='data point')
plt.plot(x, f, '-', color='red', label='regression')
            plt.title('regression')
            ax.legend()
            plt.show()
In [ ]: def function_result_05():
            X0 = np.arange(-10, 10, 0.1)
            X1 = np.arange(-10, 10, 0.1)
            grid_theta0, grid_theta1 = np.meshgrid(X0, X1)
            grid_loss = np.zeros(grid_theta0.shape)
            for i, t0 in enumerate(X0):
                for j, t1 in enumerate(X1):
                    grid_loss[j, i] = compute_loss(x, y, t0, t1)
            fig = plt.figure(figsize=(8,6))
            ax = fig.add_subplot(111, projection='3d')
            plt.title('loss surface')
            ax = plt.axes(projection='3d')
            ax.set_xlabel(r'$\theta_0$')
            ax.set_ylabel(r'$\theta_1\$')
            ax.set_zlabel('loss')
            ax.plot_surface(grid_theta0, grid_theta1, grid_loss, rstride=1, cstride=1, cmap=
```

```
plt.tight_layout()
plt.show()
```

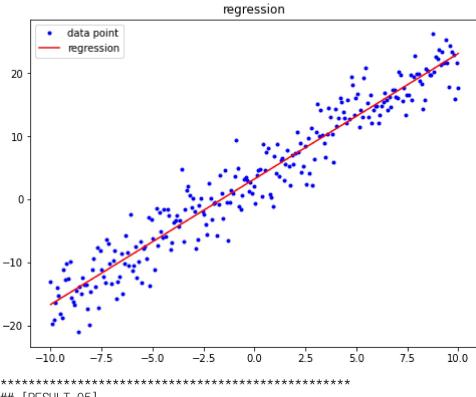
### results

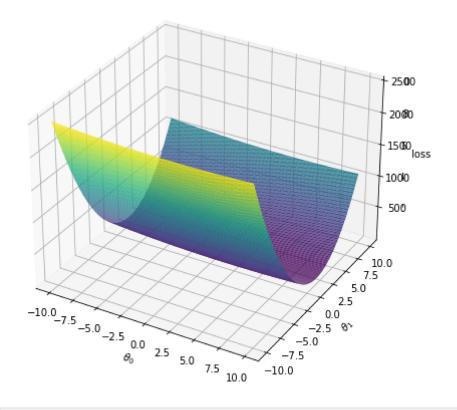




file:///C:/Users/주영석/Desktop/cd/machine-learning-2022-1/06/assignment\_06.html

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