Principal Component Analysis

import library

```
In [ ]: import numpy as np
  import matplotlib.pyplot as plt
  import matplotlib.colors as colors
  from matplotlib import cm
```

load data

```
In []: fname_data = 'assignment_12_data.txt'
    feature0 = np.genfromtxt(fname_data, delimiter=',')

    number_data = np.size(feature0, 0)
    number_feature = np.size(feature0, 1)

    print('number of data : {}'.format(number_data))
    print('number of feature : {}'.format(number_feature))

number of data : 50
    number of feature : 2
```

plot the input data

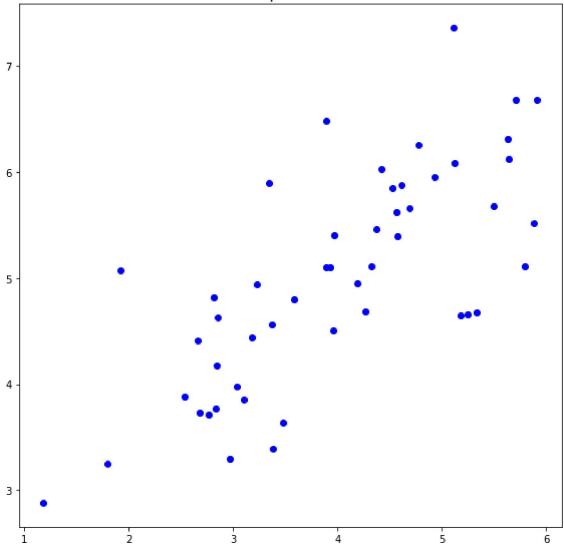
```
In []: plt.figure(figsize=(8,8))
    plt.title('input data')

x0 = feature0[:,0]
    y0 = feature0[:,1]

plt.scatter(x0, y0, color='blue')

plt.tight_layout()
    plt.show()
```





Normalization (Z-scoring)

• shape of feature = $n \times m$ where n is the number of data and m is the dimension of features

```
max_x = np.max(x)
max_y = np.max(y)
```

compute covariance matrix

• shape of feature = $n \times m$ where n is the number of data and m is the dimension of features

compute principal components

- np.linalg.eig
- argsort()
- return the eigenvalues and the eigenvectors in a decreasing order according to the eigenvalues

compute the projection of point onto the axis

- np.matmul
- np.dot
- shape of feature = $n \times m$ where n is the number of data and m is the dimension of features
- shape of vector = $m \times 1$ where m is the dimension of features

```
In [ ]: def compute_projection_onto_line(feature, vector):
```

compute the principal components and the projection of feature

```
In [ ]: (principal_component_1, principal_component_2) = compute_principal_component(feature
    projection1 = compute_projection_onto_line(feature, principal_component_1)
    projection2 = compute_projection_onto_line(feature, principal_component_2)
```

functions for presenting the results

```
In [ ]: def function_result_01():
           plt.figure(figsize=(8,8))
           plt.title('data normalized by z-scoring')
           plt.scatter(x, y, color='blue')
           plt.xlim(min_x - 0.5, max_x + 0.5)
           plt.ylim(min_y - 0.5, max_y + 0.5)
           plt.tight_layout()
           plt.show()
In [ ]: def function_result_02():
           plt.figure(figsize=(8,8))
           plt.title('principal components')
           # complete the blanks
           plt.quiver(*np.array([0, 0]), principal_component_1[0], principal_component_1[1]
           plt.quiver(*np.array([0, 0]), principal_component_2[0], principal_component_2[1]
           plt.scatter(x, y, color='blue')
           plt.xlim(min_x - 0.5, max_x + 0.5)
           plt.ylim(min_y - 0.5, max_y + 0.5)
```

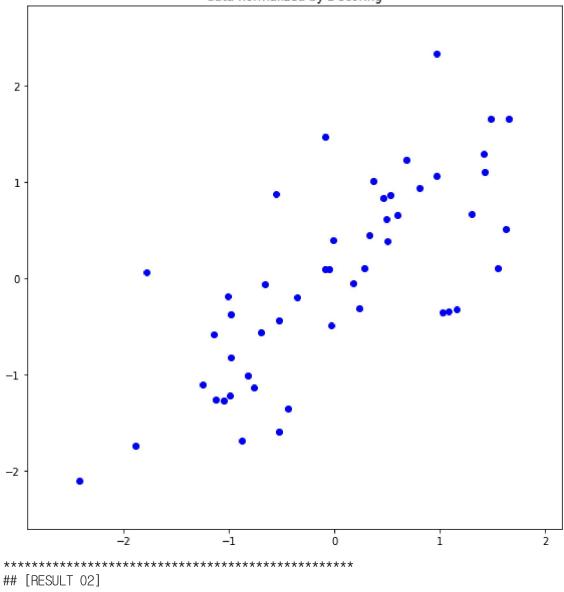
```
plt.tight_layout()
          plt.show()
In [ ]: def function_result_03():
          plt.figure(figsize=(8,8))
          plt.title('first principle axis')
          # complete the blanks
          plt.axline((0,0), slope=principal_component_1[1]/principal_component_1[0], color
          plt.scatter(x, y, color='blue')
          plt.xlim(min_x - 0.5, max_x + 0.5)
          plt.ylim(min_y - 0.5, max_y + 0.5)
          plt.tight_layout()
          plt.show()
In [ ]: def function_result_04():
          plt.figure(figsize=(8,8))
         plt.title('second principle axis')
         # complete the blanks
         #
          plt.axline((0,0), slope=principal_component_2[1]/principal_component_2[0], color
          plt.scatter(x, y, color='blue')
          plt.xlim(min_x - 0.5, max_x + 0.5)
          plt.ylim(min_y - 0.5, max_y + 0.5)
          plt.tight_layout()
          plt.show()
In [ ]: def function_result_05():
          plt.figure(figsize=(8,8))
          plt.title('projection onto the first principle axis')
         # complete the blanks
         #
          plt.axline((0,0), slope=principal_component_1[1]/principal_component_1[0], color
          plt.scatter(x, y, color='blue')
          plt.scatter(projection1[:, 0], projection1[:, 1], color='g')
          plt.xlim(min_x - 0.5, max_x + 0.5)
```

```
plt.ylim(min_y - 0.5, max_y + 0.5)
          plt.tight_layout()
          plt.show()
In [ ]: def function_result_06():
          plt.figure(figsize=(8,8))
          plt.title('projection onto the second principle axis')
          # complete the blanks
          #
          plt.axline((0,0), slope=principal_component_2[1]/principal_component_2[0], color
          plt.scatter(x, y, color='blue')
          plt.scatter(projection2[:, 0], projection2[:, 1], color='g')
          plt.xlim(min_x - 0.5, max_x + 0.5)
          plt.ylim(min_y - 0.5, max_y + 0.5)
          plt.tight_layout()
          plt.show()
In [ ]: def function_result_07():
          plt.figure(figsize=(8,8))
          plt.title('projection onto the first principle axis')
          # complete the blanks
          plt.axline((0,0), slope=principal_component_1[1]/principal_component_1[0], color
          plt.scatter(x, y, color='blue')
          plt.scatter(projection1[:, 0], projection1[:, 1], color='g')
          plt.plot(np.array([x, projection1[:, 0]]), np.array([y, projection1[:, 1]]), '-'
          plt.xlim(min_x - 0.5, max_x + 0.5)
          plt.ylim(min_y - 0.5, max_y + 0.5)
          plt.tight_layout()
          plt.show()
In [ ]: | def function_result_08():
          plt.figure(figsize=(8,8))
          plt.title('projection to the second principle axis')
          # complete the blanks
          #
          plt.axline((0,0), slope=principal_component_2[1]/principal_component_2[0], color
          plt.scatter(x, y, color='blue')
          plt.scatter(projection2[:, 0], projection2[:, 1], color='g')
          plt.plot(np.array([x, projection2[:, 0]]), np.array([y, projection2[:, 1]]), '-
```

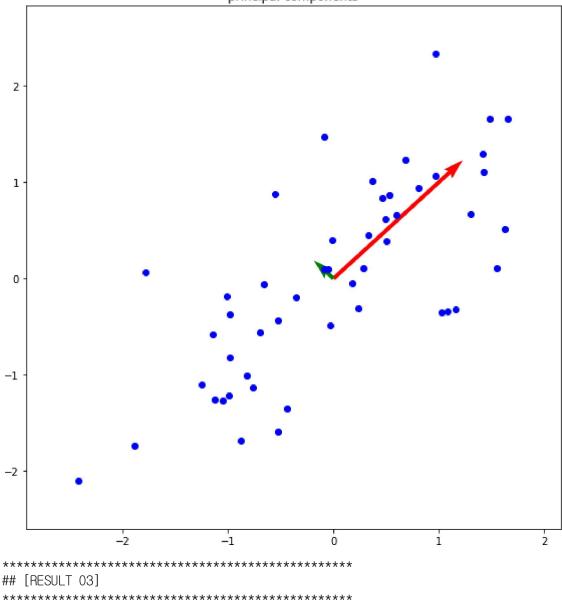
results

[RESULT 01]

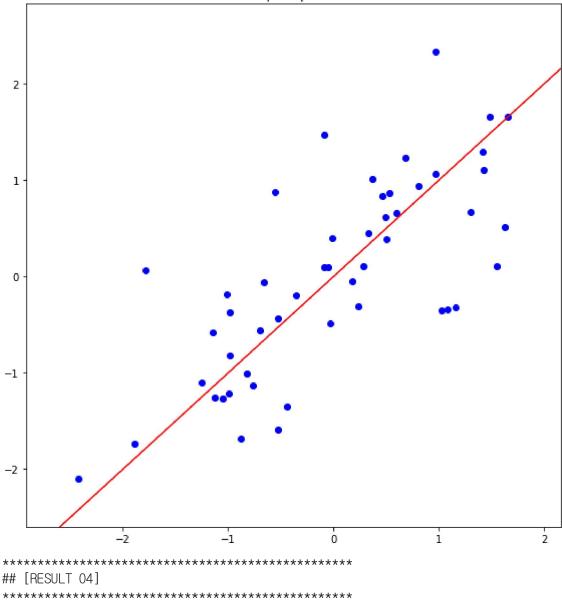
data normalized by z-scoring



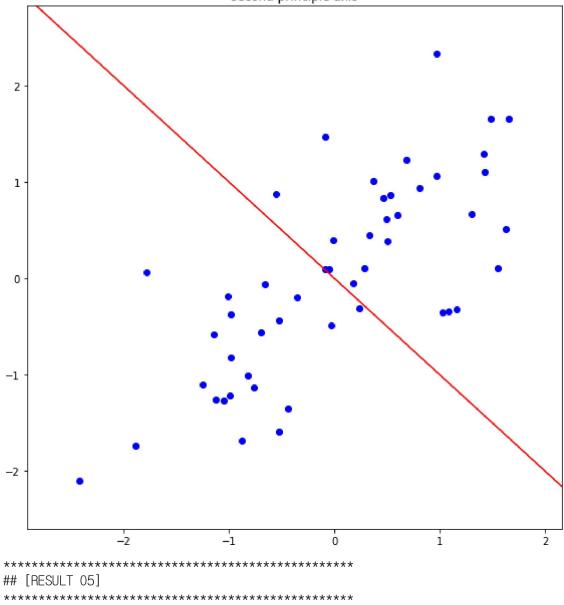
principal components



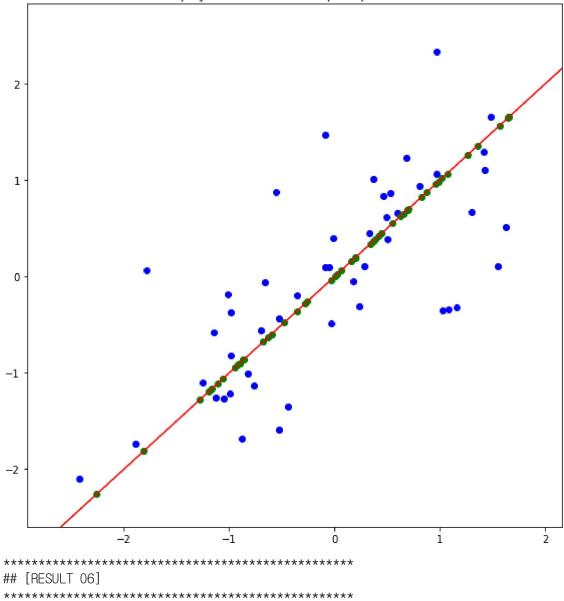


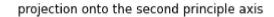


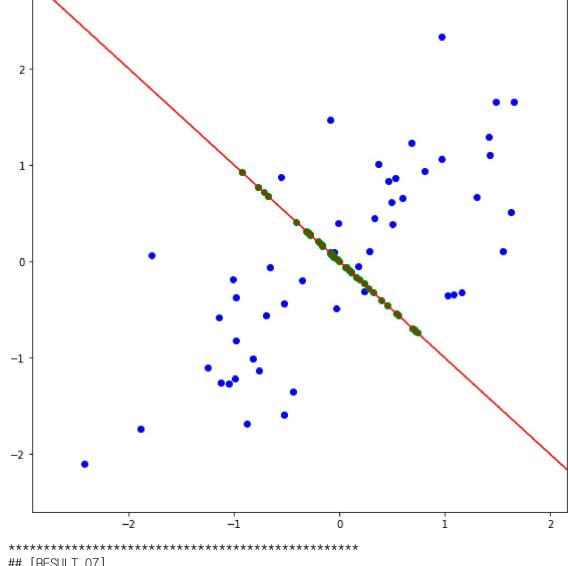
second principle axis



projection onto the first principle axis

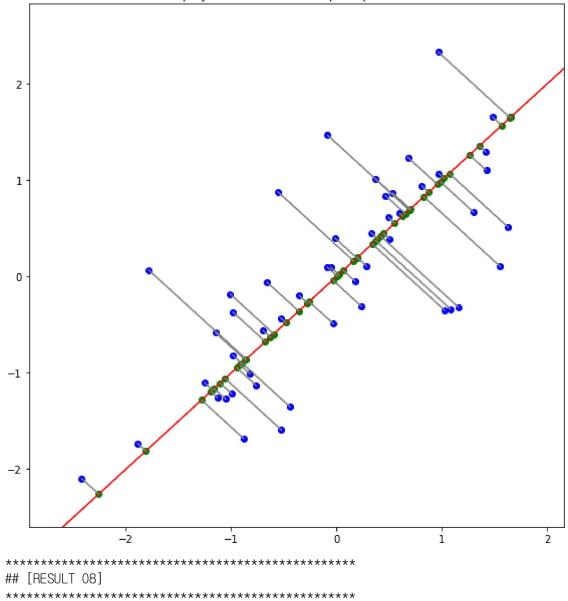






[RESULT 07]

projection onto the first principle axis



file:///C:/Users/주영석/Desktop/cd/machine-learning-2022-1/12/assignment_12.html



