# **Linear Regression**

## import library

```
In [ ]:
    import numpy as np
    import matplotlib.image as img
    import matplotlib.pyplot as plt
    import matplotlib.colors as colors
    from mpl_toolkits.mplot3d import Axes3D
```

## load point data for training and testing

```
In [ ]: filename_data = 'assignment_07_data.csv'
                        = np.genfromtxt(filename_data, delimiter=',')
        data
        number_data
                        = data.shape[0]
        x = data[:, 0]
        y = data[:, 1]
        z = data[:, 2]
        print('number of data = ', number_data)
        print('data\ type\ of\ x=',\ x.dtype)
        print('data type of y =', y.dtype)
        print('data type of z =', z.dtype)
        number of data = 2500
        data type of x = float64
        data type of y = float64
        data type of z = float64
```

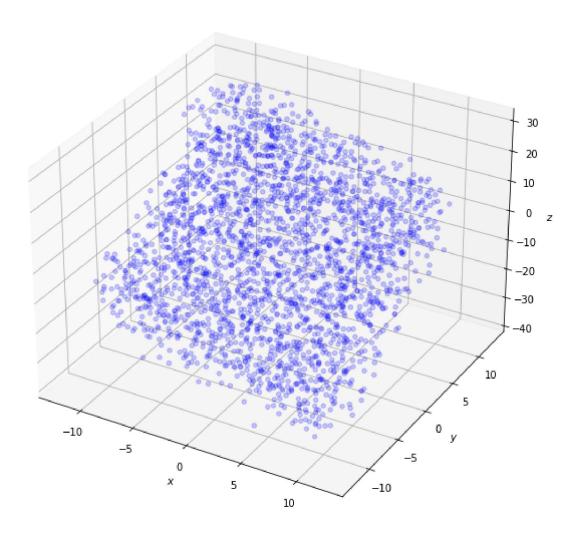
#### plot the data in the three dimensional space

```
In []: fig = plt.figure(figsize=(12, 8))
    ax1 = plt.subplot(111, projection='3d')

ax1.set_xlabel('$x$')
    ax1.set_ylabel('$y$')
    ax1.set_zlabel('$z$')
    ax1.scatter(x, y, z, marker='o', color='blue', alpha=0.2)

plt.title('data points')
    plt.tight_layout()
    plt.show()
```

#### data points



## compute the prediction function

- ullet  $heta=( heta_0, heta_1, heta_2)\in\mathbb{R}^3$
- $x, y \in \mathbb{R}$

## compute the loss function

- $heta = ( heta_0, heta_1, heta_2) \in \mathbb{R}^3$
- $x,y,z\in\mathbb{R}$

```
In [ ]: def compute_residual(theta, x, y, z):
```

• useful functions: np.inner

## compute the gradient for the model parameters heta

• useful functions: np.matmul

#### gradient descent for the optimization

#### functions for presenting the results

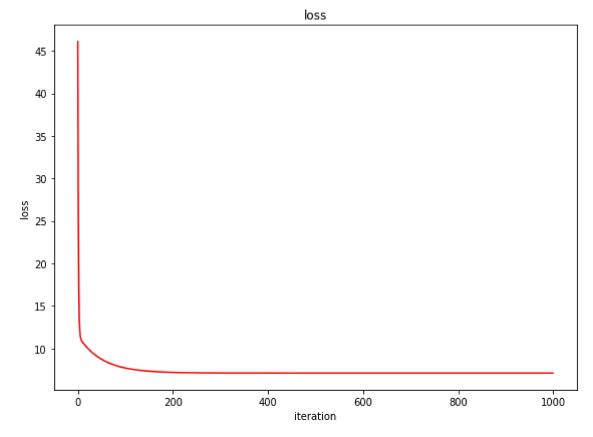
```
In [ ]: def function_result_01():
           plt.figure(figsize=(8,6))
           plt.title('loss')
           plt.plot(loss_iteration, '-', color='red')
           plt.xlabel('iteration')
           plt.ylabel('loss')
           plt.tight_layout()
           plt.show()
In [ ]: def function_result_02():
           plt.figure(figsize=(8,6))
           plt.title('model parameters')
           plt.plot(theta_iteration[:, 2], '-', color='blue', label=r'$\text{\psi}theta_2$')
           plt.xlabel('iteration')
           plt.ylabel('model parameter')
           plt.legend()
           plt.tight_layout()
           plt.show()
In [ ]: def function_result_03():
```

```
ax.set_xlabel(r'$x$')
ax.set_ylabel(r'$y$')
ax.set_zlabel(r'$z$')

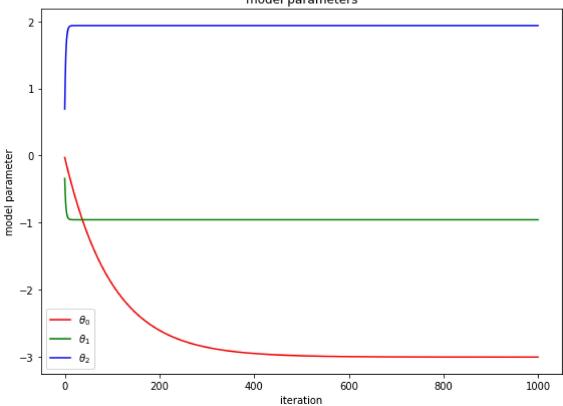
ax.plot_surface(grid_x, grid_y, zz, rstride=1, cstride=1, cmap='viridis', edgecdax.scatter(x, y, z, marker='o', color='blue', alpha=0.5)

plt.tight_layout()
plt.show()
```

## results

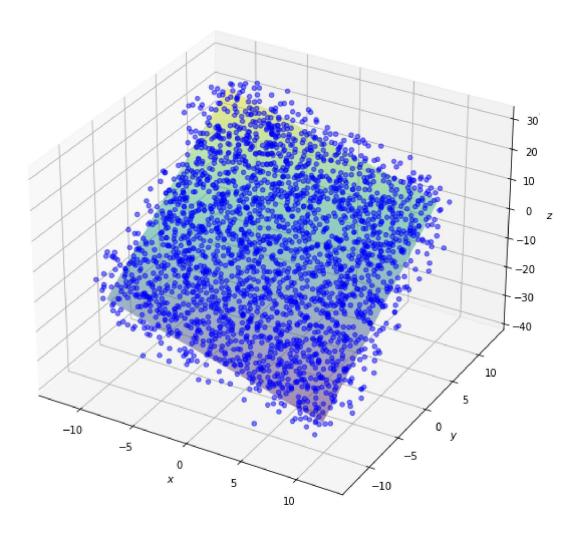


model parameters



## [RESULT 03]

#### regression surface



In [ ]: