Appendix - Practical 1, 2, & 3

Practical 1

Figures

Figure 1: Bitcoin Prices and Negative Log Returns Over Time on Common Scale

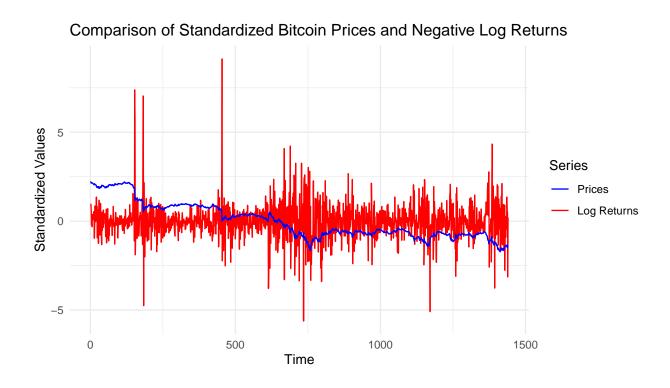


Figure 2: Bitcoin Prices Over Time

Bitcoin Prices

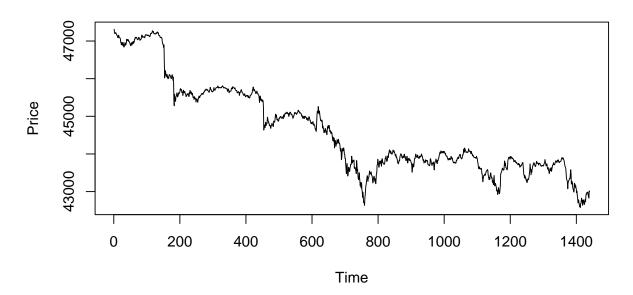


Figure 3: Negative Log Returns of Bitcoin Over Time

Negative Log Returns of Bitcoin

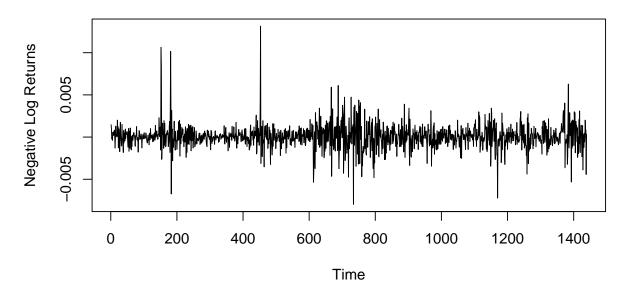


Figure 4: Histogram of Negative Log Returns

Histogram of Negative Log Returns

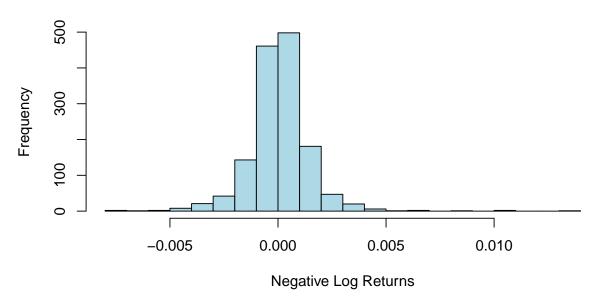


Figure 5: QQ-Plot of Negative Log Returns

QQ-Plot of Negative Log Returns vs. Normal Distribution

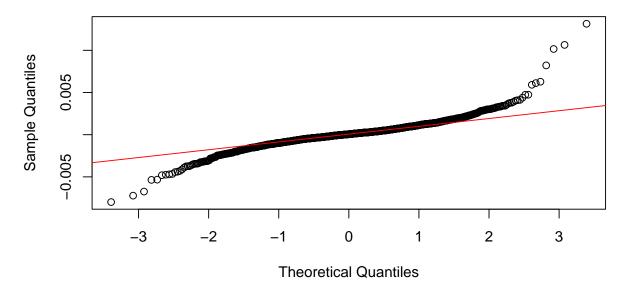


Figure 6: QQ-Plot of Negative Log Returns with t-Distribution

QQ-Plot of Negative Log Returns vs t-Distribution

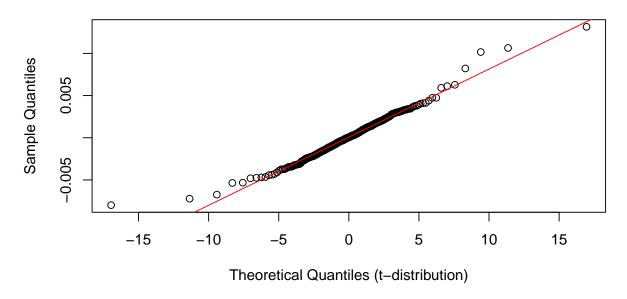


Figure 7: Histogram of Bitcoin Negative Log Returns with Fitted t and Normal Distribution

Histogram of Bitcoin Neg. Log Ret. with Fitted t and Normal Distribution

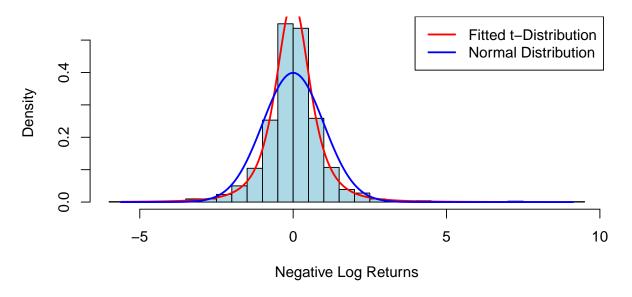


Figure 8: Density Comparison: Normal vs t-Distribution

Figure 8: Density Comparison: Normal vs t-Distribution

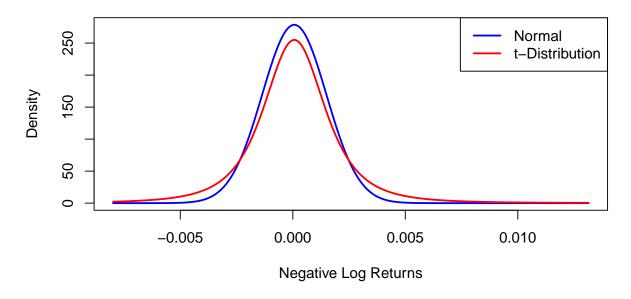


Figure 9: ACF of Bitcoin Prices

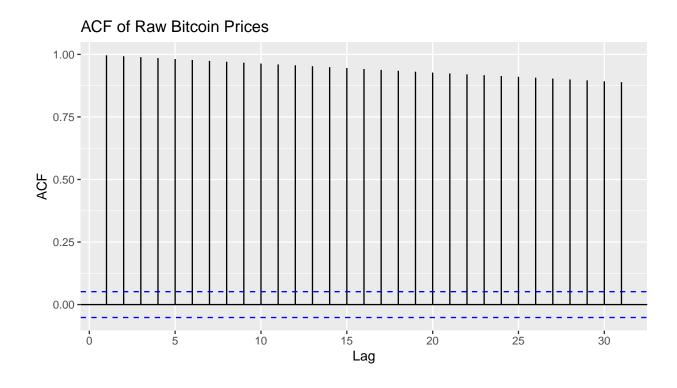


Figure 10: ACF of Negative Log Returns

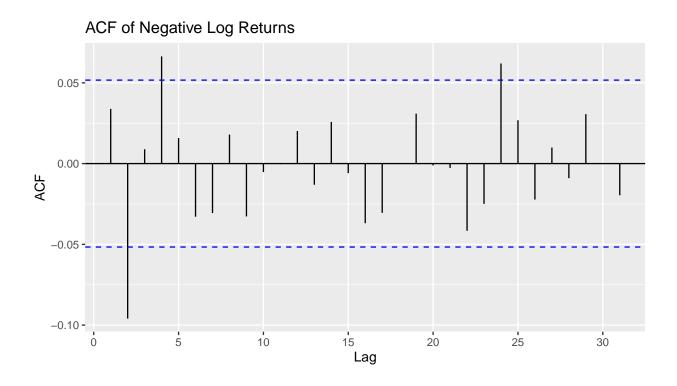


Figure 11: PACF of Negative Log Returns

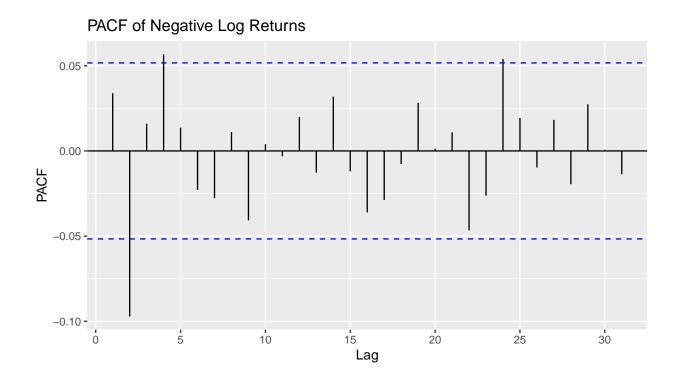


Figure 12: ACF of ARIMA(2, 0, 2) Residuals

```
##
## Call:
## arima(x = bitcoin_negative_log_returns, order = c(2, 0, 2))
##
## Coefficients:
##
                                      ma2
                                           intercept
             ar1
                     ar2
                             ma1
                                               1e-04
##
         -0.0520
                 -0.5415 0.0853
                                  0.4479
## s.e.
         0.1717
                  0.1664 0.1824 0.1773
                                               0e+00
##
## sigma^2 estimated as 2.022e-06: log likelihood = 7391.82, aic = -14771.65
```

ACF of ARIMA Model Residuals

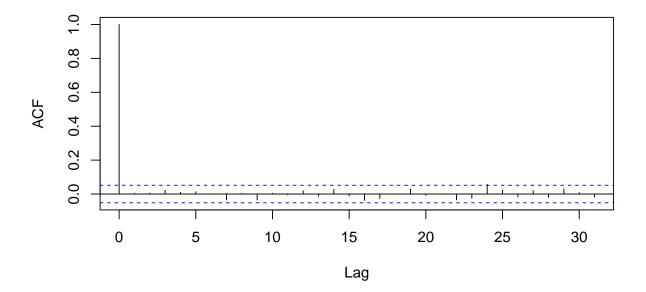


Figure 13: QQ-Plot of ARIMA(2, 0, 2) Residuals

Normal Q-Q Plot

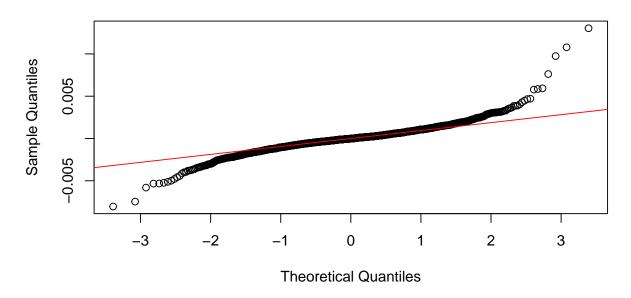


Figure 14: Residuals of ARIMA(2, 0, 2) Over Time

Residuals of ARIMA Model

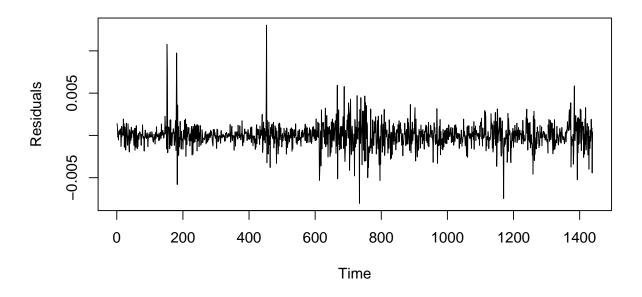


Figure 15: ACF of GARCH Normal(1, 1)

ACF of Residuals (GARCH Normal)

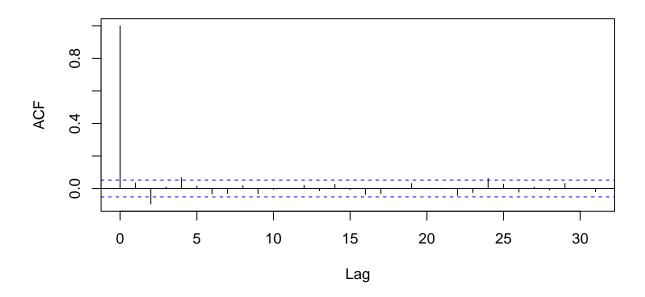


Figure 16: ACF of GARCH t-Distribution(1, 1)

ACF of Residuals (GARCH t-Distribution)

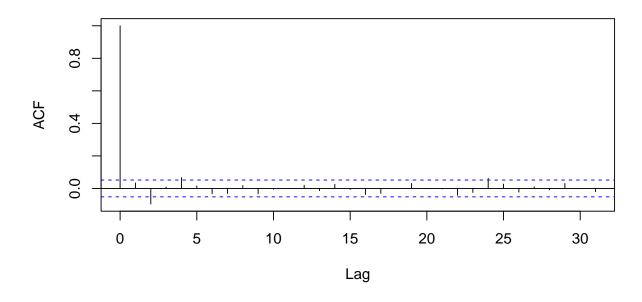


Figure 17: QQ-Plot of GARCH Normal(1, 1) Residuals

QQ-Plot of Residuals (GARCH Normal)

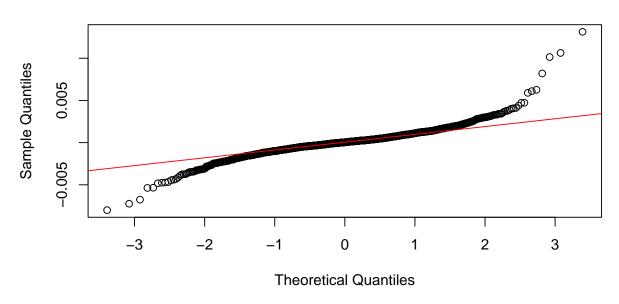


Figure 18: QQ-Plot of GARCH t-Distribution(1, 1) Residuals

QQ-Plot of Residuals (GARCH t-Distribution vs t-Quantiles)

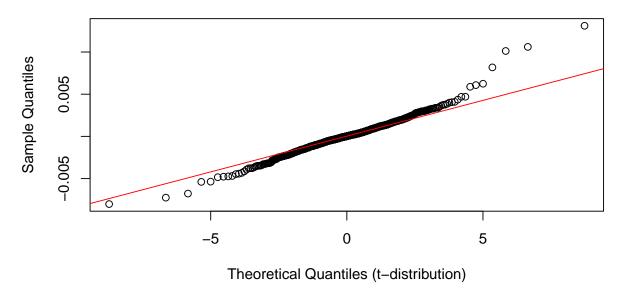
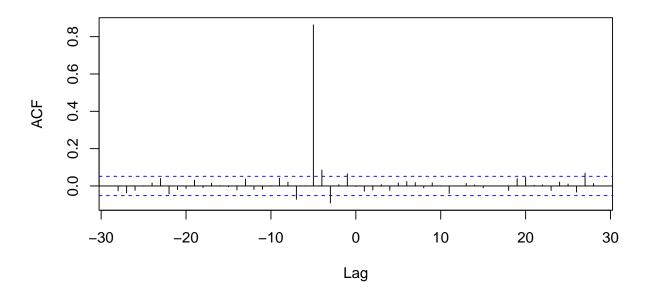


Figure 19: Cross-Correlation Function (CCF) between Bitcoin and Ethereum

bitcoin_negative_log_returns & eth_negative_log_returns



Results tables

Table 1: Augmented Dickey-Fuller Test for Bitcoin Prices

```
##
## Augmented Dickey-Fuller Test
##
## data: bitcoin_prices
## Dickey-Fuller = -2.4484, Lag order = 11, p-value = 0.3885
## alternative hypothesis: stationary
```

Table 2: Augmented Dickey-Fuller Test for Negative Log Returns

```
##
## Augmented Dickey-Fuller Test
##
## data: bitcoin_negative_log_returns
## Dickey-Fuller = -11.035, Lag order = 11, p-value = 0.01
## alternative hypothesis: stationary
```

Table 3: Anderson-Darling Test for Normality of Negative Log Returns

```
##
## Anderson-Darling normality test
##
## data: bitcoin_negative_log_returns
## A = 26.277, p-value < 2.2e-16</pre>
```

Table 4: Ljung-Box Test for Autocorrelation in Bitcoin Prices

```
##
## Box-Ljung test
##
## data: bitcoin_prices
## X-squared = 26873, df = 20, p-value < 2.2e-16</pre>
```

Table 5: Ljung-Box Test for Autocorrelation in Negative Log Returns

```
##
## Box-Ljung test
##
## data: bitcoin_negative_log_returns
## X-squared = 33.356, df = 20, p-value = 0.03082
```

Table 6: Ljung-Box Test for ARIMA(2, 0, 2) Residuals

```
##
## Box-Ljung test
##
## data: residuals_arima
## X-squared = 11.355, df = 20, p-value = 0.9365
```

Table 7: Shapiro-Wilk Test for Normality of ARIMA(2, 0, 2) Residuals

```
##
## Shapiro-Wilk normality test
##
## data: residuals_arima
## W = 0.89619, p-value < 2.2e-16</pre>
```

Table 8: Ljung-Box Test for GARCH Normal(1, 1) Residuals

```
##
## Box-Ljung test
##
## data: garch_normal_residuals
## X-squared = 33.356, df = 20, p-value = 0.03082
```

Table 9: Ljung-Box Test for GARCH t-Distribution(1, 1) Residuals

```
##
## Box-Ljung test
##
## data: garch_t_residuals
## X-squared = 33.356, df = 20, p-value = 0.03082
```

Table 10: Shapiro-Wilk Test for Normality of GARCH Normal(1, 1) Residuals

```
##
## Shapiro-Wilk normality test
##
## data: garch_normal_residuals
## W = 0.89321, p-value < 2.2e-16</pre>
```

Table 11: Ljung-Box Test for ARIMA-GARCH Residuals

```
##
## Box-Ljung test
##
## data: garch_residuals
## X-squared = 11.355, df = 20, p-value = 0.9365
```

Table 12: Correlation Test for Bitcoin and Ethereum Negative Log Returns

```
##
## Pearson's product-moment correlation
##
## data: bitcoin_negative_log_returns and eth_negative_log_returns
## t = -0.11935, df = 1437, p-value = 0.905
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## -0.05481486    0.04853492
## sample estimates:
## cor
## -0.00314838
```

Table 13: Granger Causality Test: Bitcoin Predicting Ethereum

```
## $selection
## AIC(n) HQ(n)
                  SC(n) FPE(n)
##
               6
                      6
        6
## $criteria
##
                                   2
                                                                            5
                     1
                                                 3
                                                              4
## AIC(n)
              11.74758
                            11.74842
                                         11.73190
                                                       11.70473
                                                                     11.70439
## HQ(n)
              11.75588
                            11.76226
                                         11.75127
                                                       11.72963
                                                                     11.73482
## SC(n)
              11.76980
                            11.78545
                                         11.78374
                                                       11.77138
                                                                     11.78585
## FPE(n) 126447.48020 126553.88745 124480.02097 121143.07359 121101.78267
##
                    6
                                 7
                                              8
                                                          9
                                                                      10
                                                                                   11
## AIC(n)
             10.33822
                          10.34235
                                      10.34261
                                                   10.34300
                                                                10.34724
                                                                            10.34978
## HQ(n)
             10.37418
                          10.38385
                                      10.38964
                                                   10.39557
                                                               10.40534
                                                                            10.41341
## SC(n)
             10.43450
                          10.45344
                                      10.46852
                                                   10.48372
                                                               10.50277
                                                                            10.52012
## FPE(n) 30890.87400 31018.93079 31026.98120 31039.12344 31171.09002 31250.37386
                                            14
##
                    12
                                13
                                                         15
                                                                      16
                                                                                   17
## AIC(n)
             10.35202
                          10.35351
                                      10.35204
                                                   10.35342
                                                               10.35812
                                                                            10.36156
## HQ(n)
             10.42119
                          10.42821
                                      10.43227
                                                   10.43919
                                                               10.44942
                                                                            10.45839
## SC(n)
             10.53718
                          10.55348
                                      10.56682
                                                   10.58302
                                                               10.60253
                                                                            10.62078
## FPE(n) 31320.59749 31367.26535 31321.09895 31364.65641 31512.45178 31621.09687
```

```
##
                   18
                               19
## AIC(n)
             10.36068
                         10.35837
                                     10.36011
## HQ(n)
             10.46304
                         10.46627
                                     10.47354
## SC(n)
             10.63471
                         10.64722
                                     10.66376
## FPE(n) 31593.29845 31520.72453 31575.63915
## Granger causality test
## Model 1: eth_negative_log_returns ~ Lags(eth_negative_log_returns, 1:6) + Lags(bitcoin_negative_log_returns)
## Model 2: eth_negative_log_returns ~ Lags(eth_negative_log_returns, 1:6)
    Res.Df Df
                    F
       1420
## 1
## 2
     1426 -6 811.12 < 2.2e-16 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

Table 14: Granger Causality Test: Ethereum Predicting Bitcoin

```
## Granger causality test
##
## Model 1: bitcoin_negative_log_returns ~ Lags(bitcoin_negative_log_returns, 1:6) + Lags(eth_negative_
## Model 2: bitcoin_negative_log_returns ~ Lags(bitcoin_negative_log_returns, 1:6)
## Res.Df Df F Pr(>F)
## 1 1420
## 2 1426 -6 0.4948 0.8126
```

Code

Practical 1

Practical 2

Practical 3

Cleaning

EDA

Risk Analysis