Topic Modeling



```
"I love my pet rabbit."

"That dish yesterday was amazing."

"She cooked the best rabbit dish ever."

"I gave leftovers of that dish to my pet, mr. rabbit"

"Rabbits make messy pets."

"My rabbit growls when I pet her."

"He has five rabbits."

"I had this weird dish with fried rabbit."

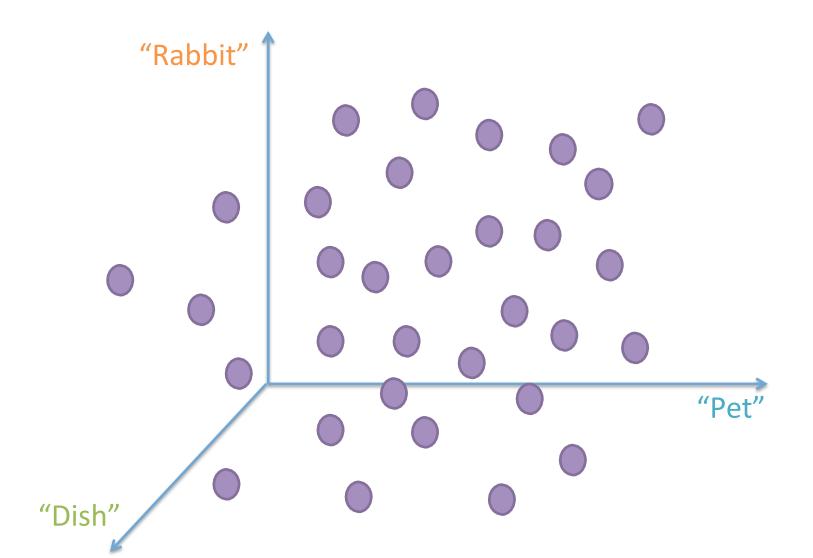
"That's my pet rabbit's favorite dish."
```

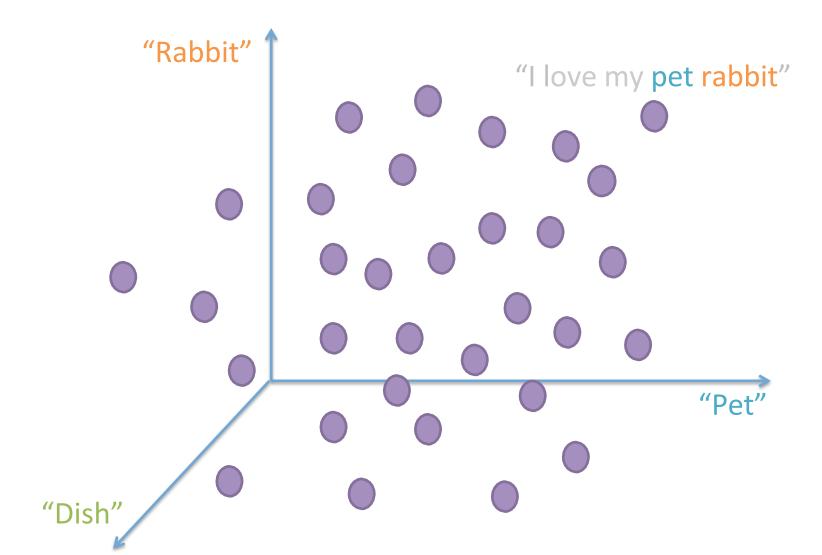
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"My rabbit growls when I pet her."
"He has five rabbits."
"I had this weird dish with fried rabbit."
"That's my pet rabbit's favorite dish."
```

Remove stop words, only keep nouns, end up with 3 features: "rabbit", "pet", "dish"

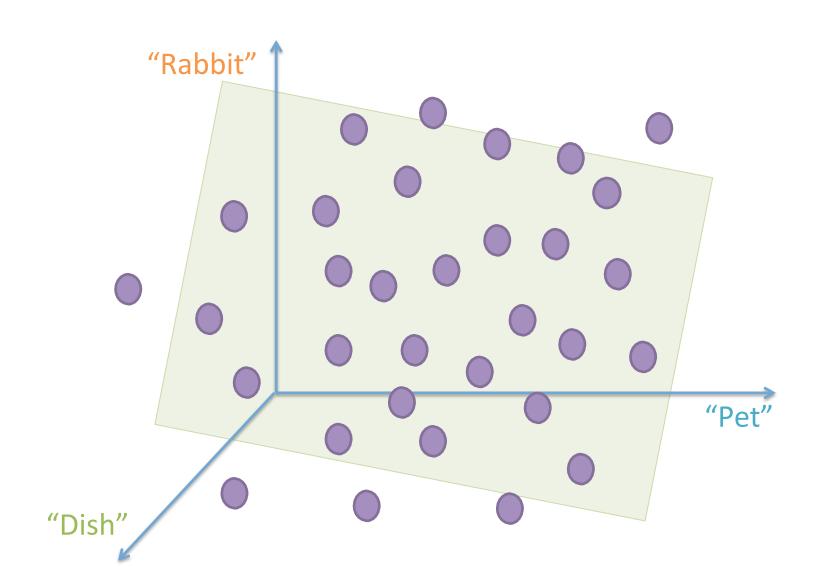
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Remove stop words, only keep nouns, end up with
```

3 features: "rabbit", "pet", "dish"

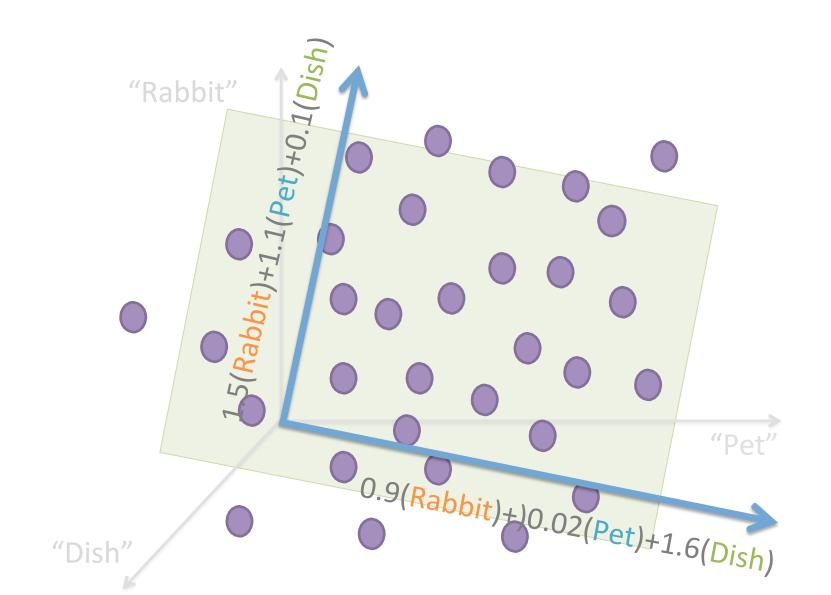




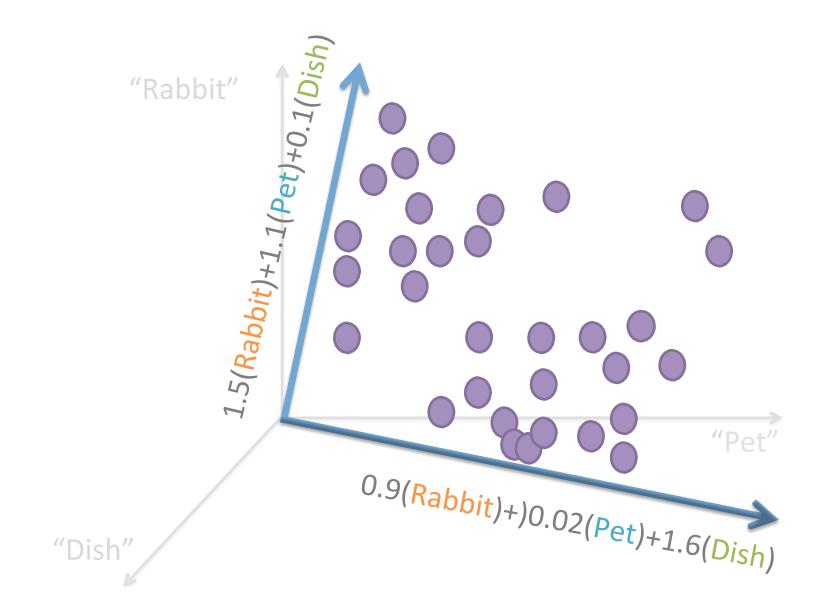
3D → 2D Feature Extraction



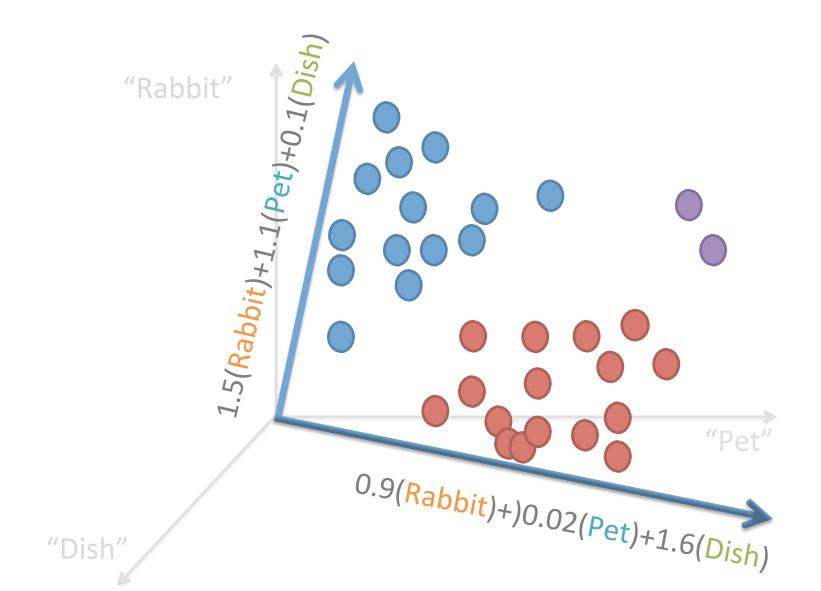
3D → 2D Feature Extraction



3D → 2D Feature Extraction



Clustering is easier on this space



What are the clusters?

```
"I love my pet rabbit."

"Rabbits make messy pets."

"My rabbit growls when I pet her."

"He has five rabbits."
```

```
"That dish yesterday was amazing."

"She cooked the best rabbit dish ever."

"I had this weird dish with fried rabbit."
```

"I gave leftovers of that dish to my pet, Mr. Rabbit" "That's my pet rabbit's favorite dish."

```
Axis 1: 1.5(Rabbit) + 1.1(Pet) + 0.1(Dish)
Axis 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish)
```

```
"I love my pet rabbit."

"Rabbits make messy pets."

"My rabbit growls when I pet her."

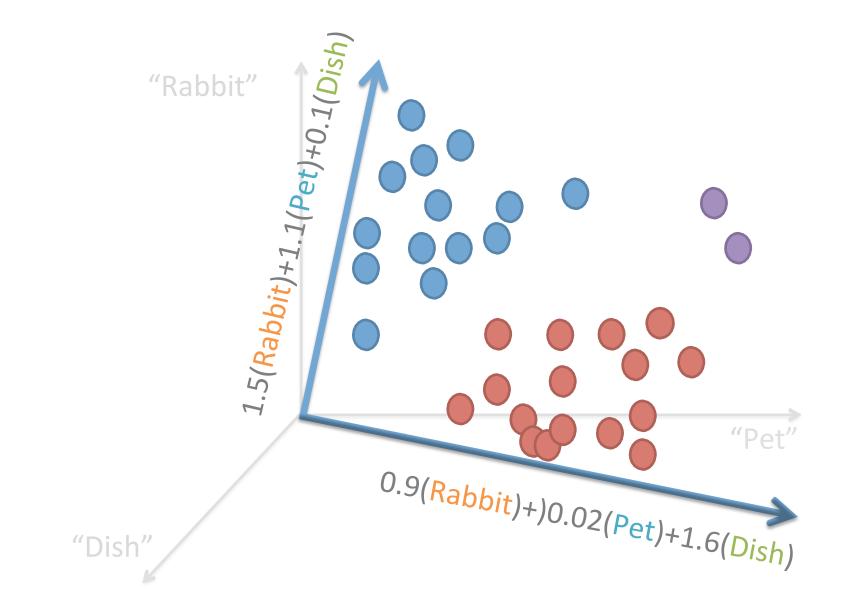
"He has five rabbits."
```

"That dish yesterday was amazing."

"She cooked the best rabbit dish ever."

"I had this weird dish with fried rabbit."

"I gave leftovers of that dish to my pet, Mr. Rabbit" "That's my pet rabbit's favorite dish."



```
Axis 1: 1.5(Rabbit) + 1.1(Pet) + 0.1(Dish)
Axis 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish)
```

```
"I love my pet rabbit."

"Rabbits make messy pets."

"My rabbit growls when I pet her."

"He has five rabbits."
```

"That dish yesterday was amazing."

"She cooked the best rabbit dish ever."

"I had this weird dish with fried rabbit."

"I gave leftovers of that dish to my pet, mr. rabbit" "That's my pet rabbit's favorite dish."

```
Axis 1: 1.5(Rabbit) + 1.1(Pet) + 0.1(Dish)
Axis 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish)
```

"I love my pet rabbit."

Axis1: High

"Rabbits make messy pets."

"My rabbit growls when I pet her."

"He has five rabbits."

"That dish yesterday was amazing."

"She cooked the best rabbit dish ever."

"I had this weird dish with fried rabbit."

"I gave leftovers of that dish to my pet, mr. rabbit" "That's my pet rabbit's favorite dish."

Axis 1:
$$1.5(Rabbit) + 1.1(Pet) + 0.1(Dish)$$

Axis 2: $0.9(Rabbit) + 0.02(Pet) + 1.6(Dish)$

"I love my pet rabbit."

Axis1: High

"Rabbits make messy pets."

"My rabbit growls when I pet her."

"He has five rabbits."

Axis1: Low
Axis2: High

"That dish yesterday was amazing."

"She cooked the best rabbit dish ever."

"I had this weird dish with fried rabbit."

"I gave leftovers of that dish to my pet, mr. rabbit" "That's my pet rabbit's favorite dish."

Axis 1:
$$1.5(Rabbit) + 1.1(Pet) + 0.1(Dish)$$

Axis 2: $0.9(Rabbit) + 0.02(Pet) + 1.6(Dish)$

"I love my pet rabbit."

Axis1: High

"Rabbits make messy pets."

"My rabbit growls when I pet her."

"He has five rabbits."

Axis1: Low
Axis2: High

"That dish yesterday was amazing."

"She cooked the best rabbit dish ever."

"I had this weird dish with fried rabbit."

Axis1: High "I gave leftovers of that dish to my pet, mr. rabbit" Axis2: High "That's my pet rabbit's favorite dish."

TOPIC 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish) \leftarrow Food, rabbit dishes

"I love my pet rabbit."

Topic1: High "Rabbits make messy pets."

Topic2: High

Topic2: Low "My rabbit growls when I pet her."

"He has five rabbits."

Topic1: Low "That dish yesterday was amazing."

"She cooked the best rabbit dish ever."

"I had this weird dish with fried rabbit."

Topic1: High "I gave leftovers of that dish to my pet, mr. rabbit"

Topic2: High "That's my pet rabbit's favorite dish."

```
TOPIC 1: 1.5(Rabbit) + 1.1(Pet) + 0.1(Dish) \leftarrow Pet rabbits, pets
```

TOPIC 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish) \leftarrow Food, rabbit dishes

```
T1
     T2
             "I love my pet rabbit."
87%
      13%
             "Rabbits make messy pets."
88%
      12%
             "My rabbit growls when I pet her."
80%
     20%
66% 34%
             "He has five rabbits."
             "That dish yesterday was amazing."
 2%
      98%
             "She cooked the best rabbit dish ever."
16%
     84%
15%
      85%
             "I had this weird dish with fried rabbit."
             "I gave leftovers of that dish to my pet, mr. rabbit"
47%
      53%
             "That's my pet rabbit's favorite dish."
42%
      58%
```

Topics are not (hard) clusters. A document does not belong to a single topic. Each topic is present in the document up to a certain degree. For each doc, we have a distribution over topics.

```
T1
     T2
             "I love my pet rabbit."
87%
      13%
             "Rabbits make messy pets."
88%
      12%
80% 20%
             "My rabbit growls when I pet her."
66% 34%
            "He has five rabbits."
             "That dish yesterday was amazing."
 2%
     98%
             "She cooked the best rabbit dish ever."
16%
     84%
15% 85%
             "I had this weird dish with fried rabbit."
             "I gave leftovers of that dish to my pet, mr. rabbit"
47%
     53%
             "That's my pet rabbit's favorite dish."
42%
      58%
```

TOPIC 2: $0.9(Rabbit) + 0.02(Pet) + 1.6(Dish) \leftarrow$ Food, rabbit dishes

What is a topic?

TOPIC 2: $0.9(Rabbit) + 0.02(Pet) + 1.6(Dish) \leftarrow$ Food, rabbit dishes

What is a topic?

When writing about a specific topic (like pet rabbits), we use some words more often than others.

Words like "pet", "rabbit", "lettuce", "cage", "fluffy", etc. are more likely to appear, words like "dish", "transmission", "opaque", "affair" are less likely to appear.

A topic can be thought as a Probability distribution over all possible words

TOPIC 2: $0.9(Rabbit) + 0.02(Pet) + 1.6(Dish) \leftarrow$ Food, rabbit dishes

What is a topic?

Probability distribution over all possible words

Word	Prob in [Pet Rabbits]	Prob in [Food]
pet	2.3x107	1.2x1010
rabbit	7.9x10 ⁷	3.4x10 ⁸
dish	6.8x1011	4.5x10 ⁷
car	3.1x1012	1.8x1012
hello	8.3x10 ⁹	1.4x109
the	7.4x104	7.3x104
love	5.4x108	3.9x10 ⁸
affair	3.0x1013	2.1x1013
delicious	9.1x10 ⁹	9.8x10 ⁸

TOPIC 2: $0.9(Rabbit) + 0.02(Pet) + 1.6(Dish) \leftarrow$ Food, rabbit dishes

What is a topic?

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TOPIC 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish) \leftarrow Food, rabbit dishes

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dish	6.8x10 ¹¹	4.5x10 ⁷
car	3.1x10 ¹²	1.8x1012
hello	8.3x109	1.4x109
the	7.4x104	7.3x104
love	5.4x108	3.9x10 ⁸
affair	3.0x10 ¹³	2.1x1013
delicious	9.1x10 ⁹	9.8x10 ⁸

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Topic Modeling

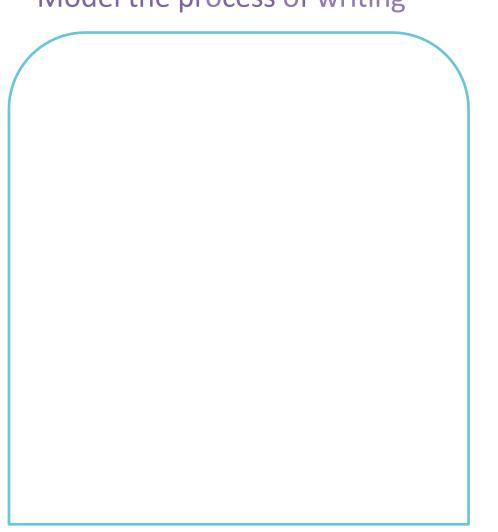
Let's use an algorithm specifically developed to find topics.

Let's use an algorithm specifically developed to find topics.

Model the process of writing

Let's use an algorithm specifically developed to find topics.

Model the process of writing



Empty page: I'll write a document.

Let's use an algorithm specifically developed to find topics.

Model the process of writing

Empty page: I'll write a document.

First, I'll decide what topics to write on. Choose the topic distribution.

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Model the process of writing

Empty page: I'll write a document.

First, I'll decide what topics to write on. Choose the topic distribution. Sex:2%, Drugs:33%, Rock'n Roll:65%

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First, I'll decide what topics to write on. Choose the topic distribution. Sex:2%, Drugs:33%, Rock'n Roll:65%

Ok. I'll write the document word by word (bag of words). First word!

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A Rock'n Roll word. Randomly pick a word according to the prob. distribution of the Rock'n Roll topic.

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Guitar

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Guitar

riff

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Guitar

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Guitar riff cocaine

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Model the process of writing

Guitar riff cocaine

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Model the process of writing

Guitar riff cocaine chord

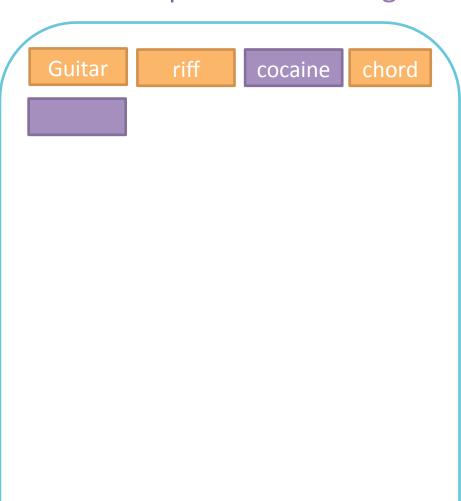
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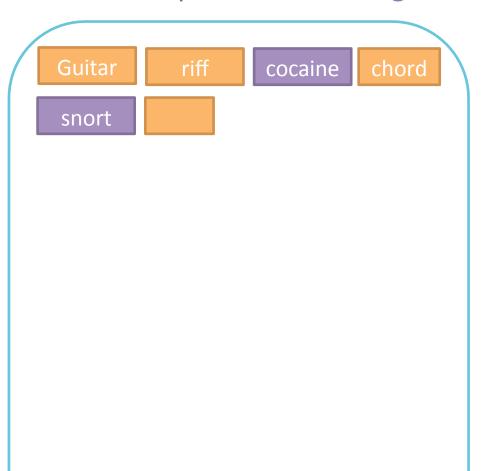
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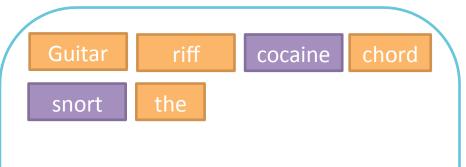


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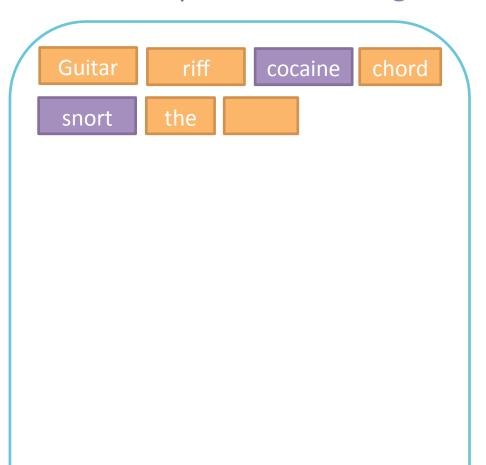
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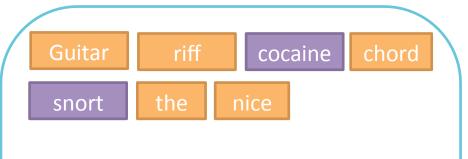


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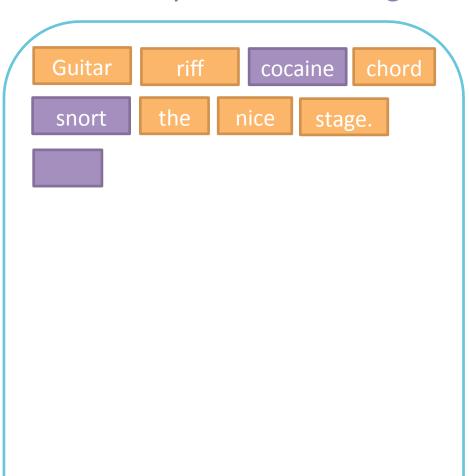
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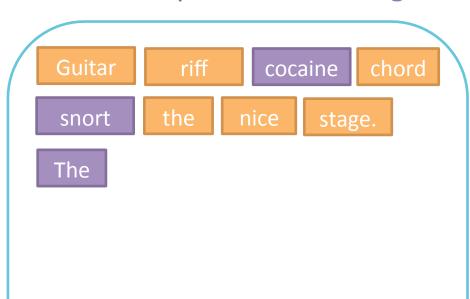


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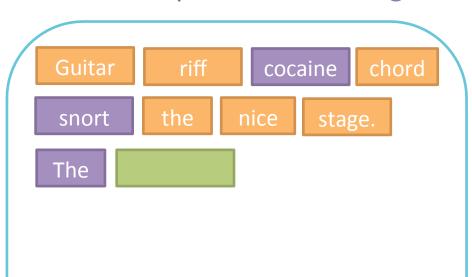
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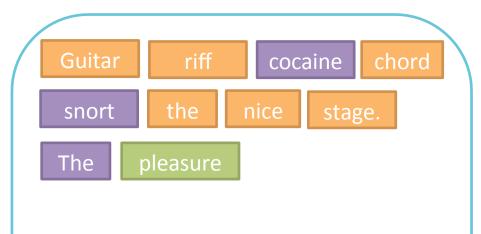


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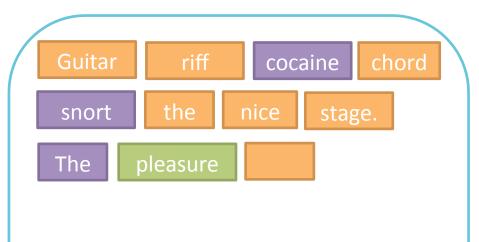
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Model the process of writing

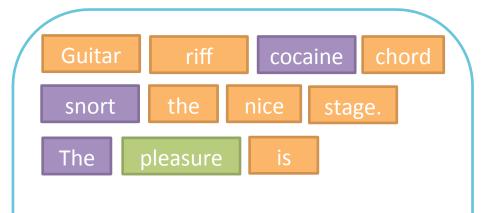


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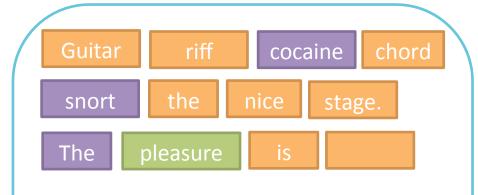
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Choose next word's topic. Roll the dice.

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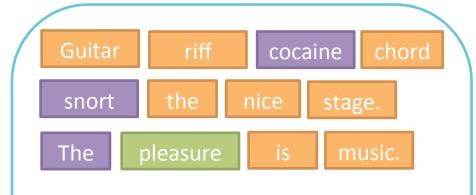


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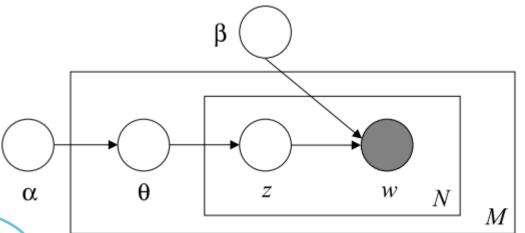
Model the process of writing



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First, I'll decide what topics to write on. Choose the topic distribution. Sex:2%, Drugs:33%, Rock'n Roll:65%

Choose next word's topic.
Roll the dice.



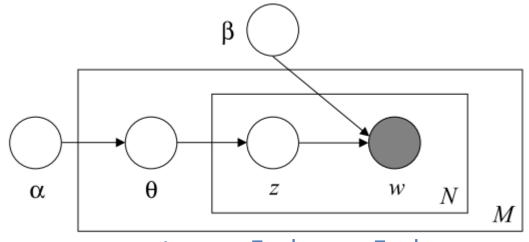


First, I'll decide what topics to write on. Choose the topic distribution. Sex:2%, Drugs:33%, Rock'n Roll:65%

Choose next word's topic. Roll the dice.

Choosing word for a topic:

topic's prob dist. over words



Corpus:

possible topic

distributions

for documents

Each

doc:

Topic

dist.

for doc

Each

word:

which

topic

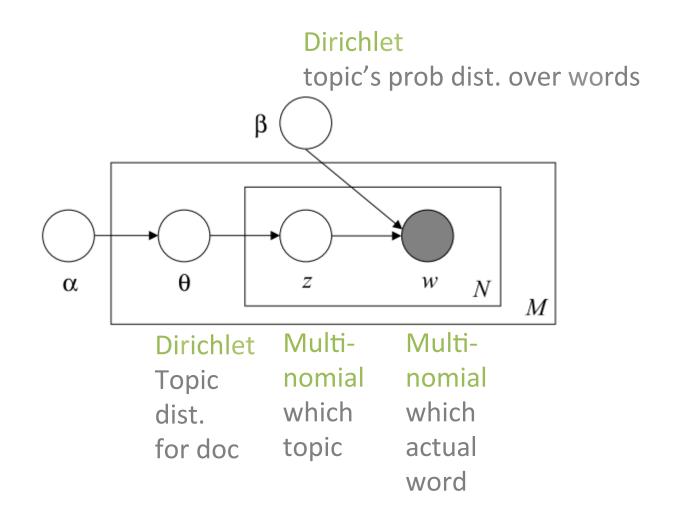
Each

word:

which

actual

word



$$p(\beta_{1:K}, \theta_{1:D}, z_{1:D} | w_{1:D}) = \frac{p(\beta_{1:K}, \theta_{1:D}, z_{1:D}, w_{1:D})}{p(w_{1:D})}$$

Topic Modeling

What and why

Rotating the coordinate space

We regard documents as made of different portions of topics Instead of different proportions of words.

Word space → Topic space

Similarity of docs

Searching for similar documents may be more meaningful in topic space

Dimensionality reduction

Clustering/classifying in topic space can be easier/meaningful

Intuition, Understanding

Look at prob. Dist. For topics, and how they are distributed over docs.