AutoEncoderBySize(alpha=3)

December 10, 2021

1 Autoencoder Performance by Size

In this notebook, we investigate the performance of a basic autoencoder model iwhen neighbors become random in the high-dimensional space according to the data size. We start by loading the necessary libraries.

```
[1]: # Handling arrays
import numpy as np

# Handling data frames
import pandas as pd

# neural networks in Python
import torch
from torch import nn

# plotting
import matplotlib.pyplot as plt

%matplotlib inline
```

We define our experiment parameters.

```
[2]: ntimes = 100 # number of noise replicates to investigate dimred performance
npoints = [25, 50, 100] # number of points in our ground truth data set to be
investigated
maxdim = 10000 # maximal dimension of the data set to be investigated
dims = np.round(np.exp(np.linspace(np.log(2), np.log(maxdim), num=10))).

⇒astype("int") # dimensions to study
a = 1.25 # magnitude of noise: per dimension we sample noise uniformly from
⇒[-a, a]
alpha = 3 # factor controling the growth rate of the ground truth diamete
```

We construct the ground truth data sets according to the various growth rates.

```
[3]: datasets = []
for idx, points in enumerate(npoints):
    t = np.linspace(0, 1, num=points)
```

We define an autoencoder model.

```
[4]: class autoencoder(nn.Module):
         def init_weights(self, m):
             if isinstance(m, nn.Linear):
                 nn.init.xavier_uniform_(m.weight, gain=1.0)
                 nn.init.zeros (m.bias)
         def __init__(self, input_dim, encoding_dim):
             super(autoencoder, self).__init__()
             self.input_dim = input_dim
             self.encoding_dim = encoding_dim
             self.encoder = nn.Sequential(
                 nn.Linear(self.input_dim, 24),
                 nn.Tanh(),
                 nn.Linear(24, 6),
                 nn.Tanh(),
                 nn.Linear(6, self.encoding_dim),
                 nn.Tanh())
             self.decoder = nn.Sequential(
                 nn.Linear(self.encoding_dim, 6),
                 nn.Tanh(),
                 nn.Tanh(),
                 nn.Linear(6, 24),
                 nn.Linear(24, self.input_dim))
             self.encoder.apply(self.init_weights)
             self.decoder.apply(self.init_weights)
         def forward(self, x):
             x = self.encoder(x)
             x = self.decoder(x)
             return x
     def autoencode(X, encoding_dim, num_epochs=2000, learning_rate=1e-3, eps=1e-07):
         X = torch.tensor(X).type(torch.float)
         model = autoencoder(input_dim=X.shape[1], encoding_dim=encoding_dim)
         criterion = nn.MSELoss()
         optimizer = torch.optim.Adam(model.parameters(), lr=learning_rate, eps=eps)
```

```
for epoch in range(num_epochs):
    output = model(X)
    loss = criterion(output, X)
    loss.backward()
    optimizer.step()
    optimizer.zero_grad()

Y = model.encoder(X).detach().numpy()

return(Y)
```

We measure the autoencoder performance by dimensionality and data size.

```
[5]: cor_auto = np.zeros([len(dims), len(npoints)])
     for idx in range(ntimes):
         print("progress: " + str(round(100 * idx / ntimes, 2)).ljust(5, "0") + "%", __
      \rightarrowend="\r")
         N = a * (2 * np.random.rand(max(npoints), maxdim) - 1)
         for np_idx, points in enumerate(npoints):
                 XN = datasets[np_idx] + a * N[:datasets[np_idx].shape[0],]
                 for dim idx, dim in enumerate(dims):
                     Y = autoencode(XN[:,:dim], 1)
                      cor = np.max([np.corrcoef(Y[:,0], datasets[np_idx][:,0])[0, 1],
                                    np.corrcoef(np.flip(Y[:,0], axis=0),__
      \rightarrowdatasets[np_idx][:,0])[0, 1]])
                      cor_auto[dim_idx, np_idx] += cor
     cor_auto /= ntimes
     print("progress: 100.0%", end="\r")
     fig, ax = plt.subplots(figsize=(5, 5))
     ax.set_xlabel("dim")
     ax.set_ylabel("correlation")
     ax.set_xscale("log")
     for idx, points in enumerate(npoints):
         ax.plot(dims, cor_auto[:,idx], label=points)
```

```
ax.scatter(dims, cor_auto[:,idx])

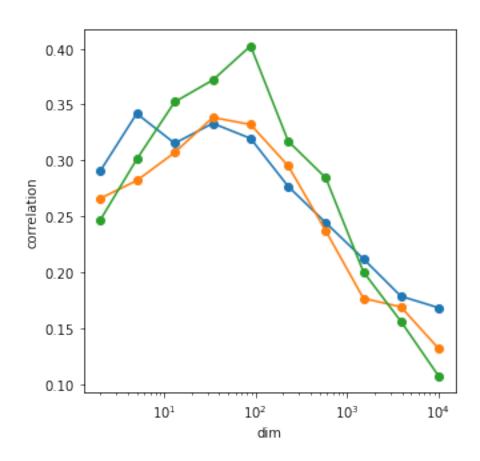
ax.legend(title="data size", loc="upper center", ncol=3, bbox_to_anchor=(0.5, 1.

→25))
```

progress: 100.0%

[5]: <matplotlib.legend.Legend at 0x7f3c84338160>





We modify the style of the results and save as csv for plotting in R.

```
[6]: cor_auto_df = np.zeros([cor_auto.shape[0] * cor_auto.shape[1], 3])
   idx = 0
   for idx1, points in enumerate(npoints):
        for idx2, dim in enumerate(dims):
            cor_auto_df[idx,:] = [points, dim, cor_auto[idx2, idx1]]
```

```
idx += 1

cor_auto_df = pd.DataFrame(cor_auto_df)

cor_auto_df.columns = ["size", "dim", "cor"]

cor_auto_df.to_csv("../Results/Size/AUTO_alpha3.csv")
```

[]: