ClusterByAlpha

Load libraries

```
library("ggplot2") # general plotting
library("ggpubr") # combining plots
library("ggpubr") # combining plots
library("Spectrum") # spectral clustering
library("hitandrun") # sampling from hypersphere
```

Specify the experiment parameters

```
set.seed(17) # seed for reproducibility
ntimes <- 100 # number of noise replicates to investigate cluster performance
npoints <- 25 # number of points per ground truth cluster to be investigated
maxdim <- 10000 # maximal dimension of the data set to be investigated
dims <- round(exp(seq(log(10), log(maxdim), length.out=4))) # dimensions to study from log-scale
sigma <- 1 # magnitude of noise: per dimension we sample from gaussian with std sigma
alphas <- c(3, 4, 5) # factors controling the growth rate of the ground truth diameters</pre>
```

Construct the ground data sets according to the growth rates

```
group <- factor(c(rep(1, npoints), rep(2, npoints)))
datasets <- lapply(alphas, function(alpha){
   if(alpha==Inf) center <- rep(1, maxdim) else center <- (1:maxdim)**(-1 / alpha)
   center[1:2] <- 5 * center[1:2]
   S1 <- (norm(center, type="2") / 4) * runif(npoints) * hypersphere.sample(maxdim, npoints)
   S2 <- t(replicate(npoints, center)) +
        (norm(center, type="2") / 4) * runif(npoints) * hypersphere.sample(maxdim, npoints)
        data.frame(rbind(S1, S2))
})</pre>
```

We view the magnitude of noise and spectral clustering result for various data sets

```
PlotList <- list() # empty list for storing plots</pre>
N <- matrix(rnorm(2 * maxdim * npoints, sd=sigma), ncol=maxdim) # noise matrix identical for all data
for(alpha idx in 1:length(alphas)){
  # compute clustering and visualizations for this growth rate determined by alpha (noise-free)
  thisX <- datasets[[alpha idx]]</pre>
  thisX$pred <- factor(Spectrum(data.frame(t(thisX)), maxk=2, # compute spectral clustering
                                silent=TRUE, showres=FALSE)$assignments)
  PlotList[[length(PlotList) + 1]] <- ggplot(data=thisX, # compute and store plot
                                             aes(x=X1, y=X2, fill=pred)) +
    geom_point(size=3, aes(shape=group)) +
    ggtitle(paste0("without noise \n alpha = ", alphas[alpha_idx], ", dim = ", maxdim)) +
   theme bw() +
   theme(text=element_text(size=10), plot.title=element_text(hjust=0.5, size=12)) +
    scale_fill_manual(values=c("#F8766D", "#00BFC4")) +
    scale_shape_manual(values=c(21, 24)) +
   labs(fill="predicted cluster", shape="true cluster") +
    guides(fill=guide legend(override.aes=list(colour=c("#F8766D", "#00BFC4"))))
```

```
# add noise to data
  XN <- datasets[[alpha_idx]] + N</pre>
  for(dim in dims){
     thisX <- XN[,1:dim]</pre>
     # compute clustering and visualization for this growth rate and dimension (noisy)
     thisX$pred <- factor(Spectrum(data.frame(t(thisX)), maxk=2, # compute spectral clustering
                                          silent=TRUE, showres=FALSE)$assignments)
     PlotList[[length(PlotList) + 1]] <- ggplot(data=thisX, # compute and store plot
                                                            aes(x=X1, y=X2, fill=pred)) +
        geom_point(size=3, aes(shape=group)) +
       ggtitle(paste0("with noise \n alpha = ", alphas[alpha_idx], ", dim = ", dim)) +
        theme_bw() +
       theme(text=element_text(size=10), plot.title=element_text(hjust=0.5, size=12)) +
        scale_fill_manual(values=c("#F8766D", "#00BFC4")) +
        scale_shape_manual(values=c(21, 24)) +
       labs(fill="predicted cluster", shape="true cluster") +
       guides(fill=guide_legend(override.aes=list(colour=c("#F8766D", "#00BFC4"))))
  }
}
do.call("ggarrange", c(PlotList, nrow=length(alphas), ncol=length(dims) + 1, common.legend=TRUE))
                                        predicted cluster
                                                            true cluster O 1 \triangle 2
    without noise alpha = 3, dim = 10000
                                                                                                      with noise
                                with noise
                                                        with noise
                                                                               with noise
                              alpha = 3, dim = 10
                                                                                                  alpha = 3, dim = 10000
                                                    alpha = 3, dim = 100
                                                                           alpha = 3, dim = 1000
                         5.0
X 2
                       X 2.5
                                              X
                                                                      X
                         0.0
       without noise
                                with noise
                                                        with noise
                                                                               with noise
                                                                                                      with noise
                              alpha = 4, dim = 10
    alpha = 4. dim = 10000
                                                    alpha = 4, dim = 100
                                                                           alpha = 4 dim = 1000
                                                                                                  alpha = 4 dim = 10000
                         5.0
                                                                        5.0
                                                                                               5.0
X 2
                       X 2.5
                                                                                               2.5
                                                                       2.5
                         0.0
                                   2
X1
           X1
                                                          х<sub>1</sub>
                                                                                  X1
                                                                                                         X1
    without noise
alpha = 5, dim = 10000
                                with noise
                                                                               with noise
                                                                                                      with noise
                                                                           alpha = 5, dim = 1000
                                                                                                  alpha = 5, dim = 10000
                              alpha = 5, dim = 10
                                                    alpha = 5, dim = 100
                         5.0
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                         0.0
```